

Sensitivity to dark matter production at future e^+e^- colliders

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Research supported by  NATIONAL SCIENCE CENTRE
POLAND

Workshop on Standard Model and Beyond, Corfu'2021
September 4, 2021

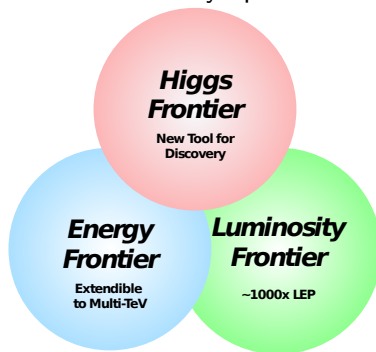
Introduction

An aerial photograph of a coastal city, likely Thessaloniki, Greece. The city is built on a hillside, with a prominent rocky hill in the center. The sea is visible in the background, and mountains are visible in the distance. The sky is clear and blue.

Dark Matter

Many hints for existence of Dark Matter (DM), but its nature is unknown.
Many possible scenarios, wide range of masses and couplings to consider.

High energy e^+e^- machines offer many options for DM searches:

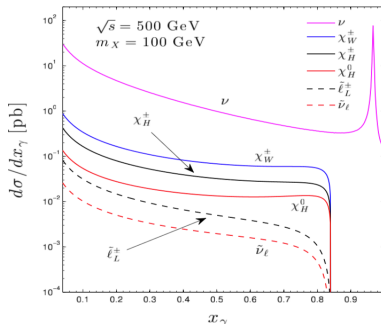
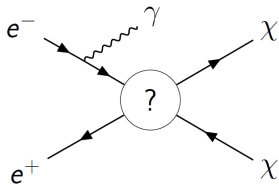


Tomohiko Tanabe @ LCWS'2021

For more general picture see my presentation at [SUSY'2021](#)

Mono-photon signature

The mono-photon signature is considered to be the most general way to look for **DM particle production** in future e^+e^- colliders.



DM can be pair produced in the e^+e^- collisions via exchange of a new **mediator particle**, which couples to both electrons (SM) and DM states

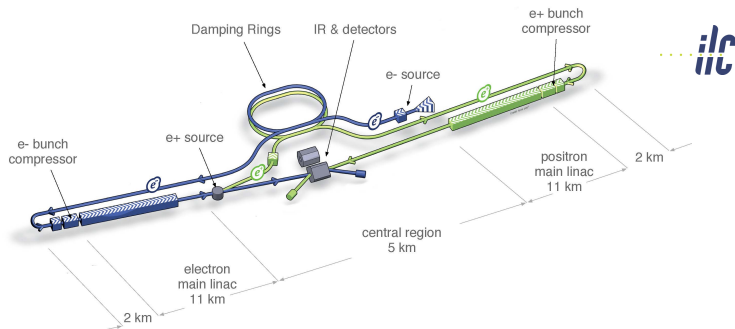
This process can be detected, if **additional hard photon radiation** from the initial state is observed in the detector...

Outline

- 1 Introduction
- 2 Colliders and Experiments
- 3 Simulating mono-photon events
- 4 Mono-photon results
 - Heavy mediator approximation (ILD and CLICdp studies)
 - Light mediator exchange
- 5 Conclusions

Colliders and Experiments

International Linear Collider



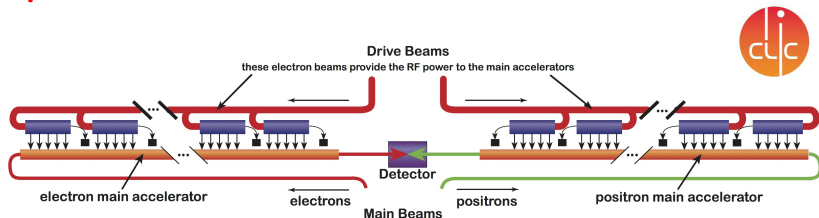
ILC Scheme | © www.fzj.de

Technical Design (TDR) completed in 2013

[arXiv:1306.6328](https://arxiv.org/abs/1306.6328)

- superconducting accelerating cavities
- 250 – 500 GeV c.m.s. energy (baseline), 1 TeV upgrade possible
- footprint 31 km
- polarisation for both e^- and e^+ (80%/30%)

Compact Linear Collider



Conceptual Design (CDR) presented in 2012

CERN-2012-007

- high gradient, two-beam acceleration scheme
- staged implementation plan with energy from 380 GeV to 3 TeV
- footprint of 11 to 50 km
- e^- polarisation (80%)

For details refer to [arXiv:1812.07987](https://arxiv.org/abs/1812.07987)

Running scenarios

Staged construction assumed for both ILC and CLIC.

Results presented in [this talk](#) focus on the **highest energy stages**.

ILC

Total of 4000 fb^{-1} assumed at 500 GeV (H-20 scenario)

- $2 \times 1600 \text{ fb}^{-1}$ for LR and RL beam polarisation combinations
- $2 \times 400 \text{ fb}^{-1}$ for RR and LL beam polarisation combinations

assuming **polarisation of $\pm 80\%$ for electrons** and **$\pm 30\%$ for positrons**

[arXiv:1903.01629](#)

CLIC

Total of 5000 fb^{-1} assumed at 3 TeV

- 4000 fb^{-1} for negative electron beam polarisation
- 1000 fb^{-1} for positive electron beam polarisation

assuming **polarisation of $\pm 80\%$ for electrons**

[arXiv:1812.06018](#)

Detector Requirement

“Particle Flow” concept:

High calorimeter granularity

⇒ single particle reconstruction/ID

Precise momentum measurement

⇒ best energy for charged particles

⇒ dominates jet energy resolution

High precision vertex detector

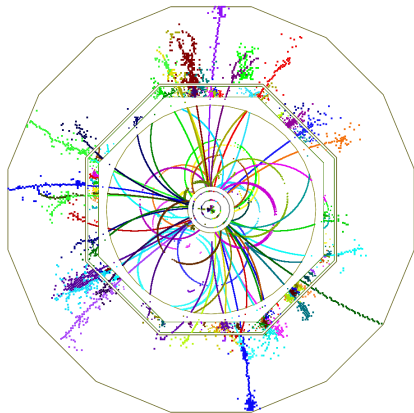
⇒ very efficient flavour tagging

Instrumentation down to smallest angles

⇒ hermeticity, missing energy tagging

Example event

$$e^+e^- \rightarrow t\bar{t} \rightarrow 6j$$

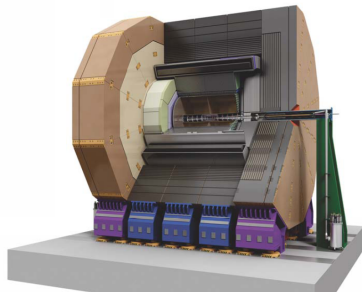


Detector Requirements same for ILC and CLIC

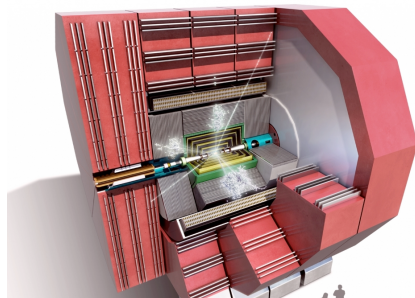
- Track momentum resolution: $\sigma_{1/p} < 5 \cdot 10^{-5} \text{ GeV}^{-1}$
- Impact parameter resolution: $\sigma_d < 5 \mu\text{m} \oplus 10 \mu\text{m} \frac{1 \text{ GeV}}{p \sin^{3/2} \Theta}$
- Jet energy resolution: $\sigma_E/E = 3 - 4\%$ (for highest jet energies)
- Hermeticity: $\Theta_{min} = 5 \text{ mrad}$

Detailed detector concepts for ILC and CLIC:

ILD



CLICdet

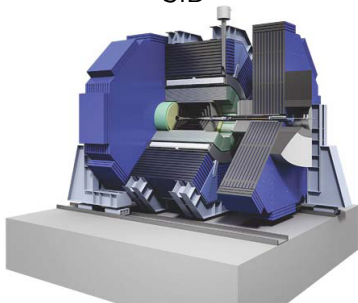


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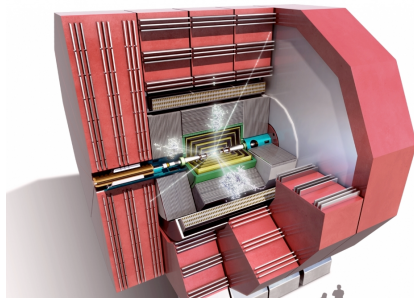
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Detailed detector concepts for ILC and CLIC:

SiD



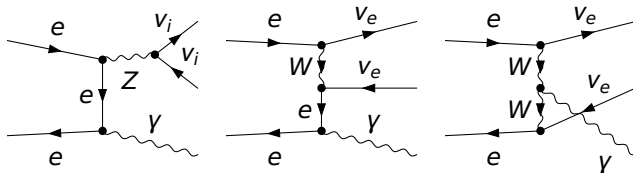
CLICdet



Simulating mono-photon events

For proper estimate of the mono-photon signature sensitivity **consistent simulation** of BSM processes and of the SM backgrounds is crucial.

“Irreducible” background comes from **radiative neutrino pair-production**



Detector acceptance & reconstruction efficiency

⇒ significant contribution from **radiative Bhabha scattering**

WHIZARD provides the ISR structure function option that includes all orders of soft and soft-collinear photons as well as up to the third order in high-energy collinear photons.

However, WHIZARD ISR photons are not ordinary final state photons: they represent all photons radiated in the event from a given lepton line.

ISR structure function can not account for hard non-collinear photons
 \Rightarrow all “detectable” photons generated on Matrix Element level

Dedicated procedure developed to avoid double-counting of ISR and ME

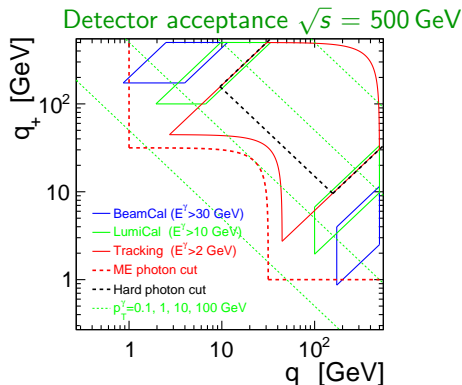
For details: J. Kalinowski et al., Eur. Phys. J. C 80 (2020) 634, arXiv:2004.14486

Two variables, calculated separately for each emitted photon:

$$q_- = \sqrt{4E_0 E_\gamma} \cdot \sin \frac{\theta_\gamma}{2},$$

$$q_+ = \sqrt{4E_0 E_\gamma} \cdot \cos \frac{\theta_\gamma}{2},$$

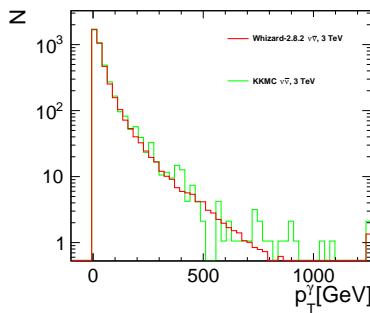
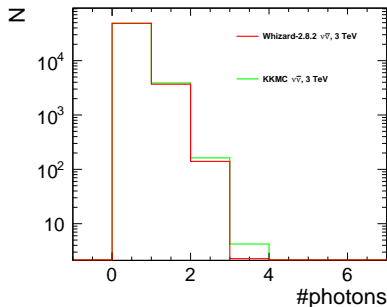
are used to separate “soft ISR” emission region from the region described by ME calculations.



Validation of the procedure

WHIZARD predictions were compared to the results from the KKMC code for $e^+e^- \rightarrow \nu\bar{\nu} + N\gamma$

3 TeV CLIC



⇒ very good agreement observed (both for shape and normalisation)

For more details:

J. Kalinowski et al., *Eur. Phys. J. C* 80 (2020) 634, arXiv:2004.14486

Simplified DM model

UFO model covering most popular scenarios of DM pair-production

⇒ Feynrules

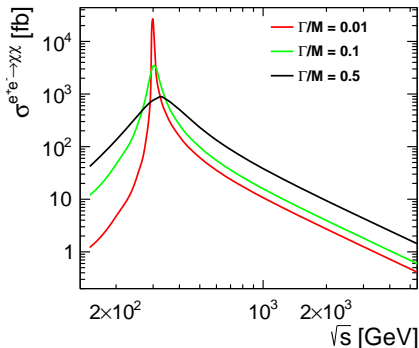
Possible mediators:

- scalar
- pseudo-scalar
- **vector**
- pseudo-vector
- V−A coupling
- V+A coupling

Possible DM candidates:

- real or complex scalar
- Majorana or **Dirac fermion**
- real vector

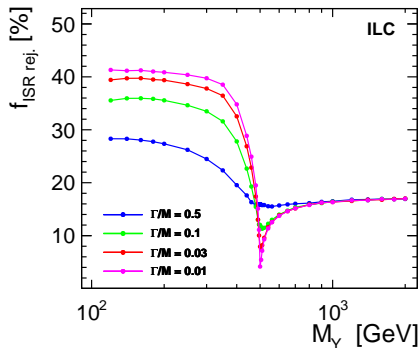
Cross section for $e^+e^- \rightarrow \chi\chi$ for
 $M_\chi = 50 \text{ GeV}$ and $M_\gamma = 300 \text{ GeV}$



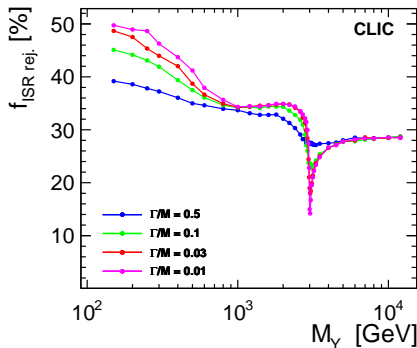
ISR rejection probability

Fraction of events generated by WHIZARD **removed** in merging procedure (ISR photons emitted in the phase-space region covered by ME)

ILC @ 500 GeV



CLIC @ 3 TeV



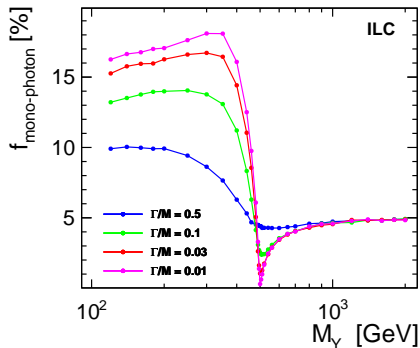
Tagging efficiency

based on DELPHES simulation

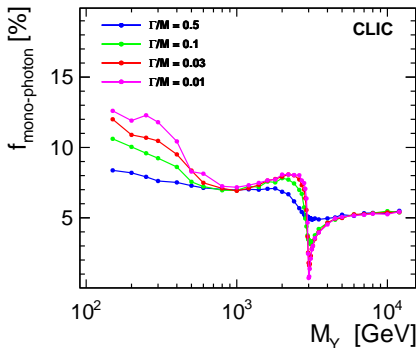
Mono-photons reconstructed only in a fraction of generated signal event

$$\sigma(e^+e^- \rightarrow \chi\chi\gamma_{\text{tag}}) = f_{\text{mono-photon}} \cdot \sigma(e^+e^- \rightarrow \chi\chi(\gamma))$$

ILC @ 500 GeV



CLIC @ 3 TeV



Emission strongly suppressed for narrow mediator with $M_\gamma \sim \sqrt{s}$

Mono-photon results



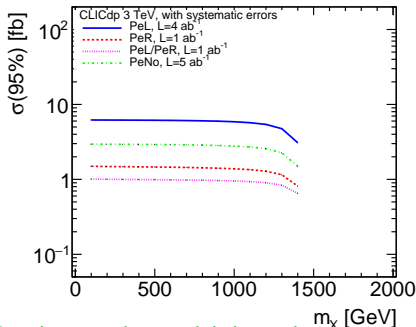
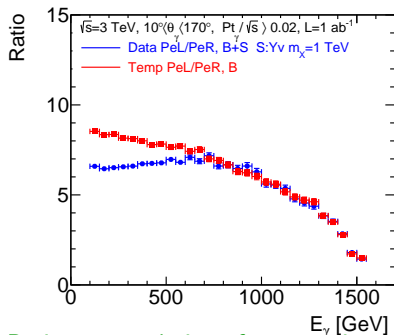
Heavy mediator approximation, generator level

arXiv:2103.06006

Signature:

high energy, isolated photon no other “hard” activity in the detector

Highest sensitivity to DM production from the ratio of the photon energy distributions measured for the two electron beam polarisations



Ratio \Rightarrow cancelation of systematic uncertainties, but results model-dependent

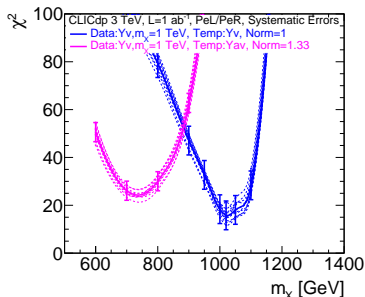
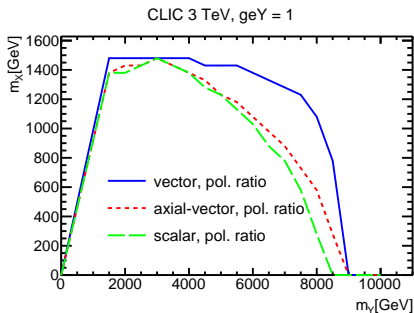
Heavy mediator approximation, generator level

arXiv:2103.06006

Limits on the mono-photon cross section can be translated to the expected **exclusion range** in the DM-mediator **mass space**.

For a light WIMP mass the exclusion range extends up to 9 TeV

If **significant excess** of mono-photon events is observed, WIMP mass in a TeV range can be extracted with a **1% accuracy**.

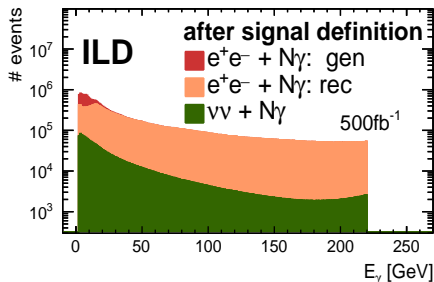
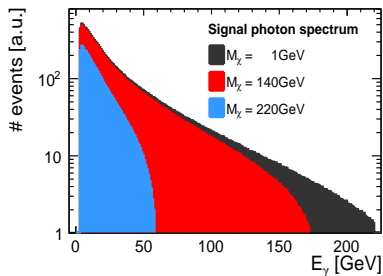


Heavy mediator (EFT limit), full simulation

arXiv:2001.03011

Signature:

- single photon in the central region (high tracking efficiency)

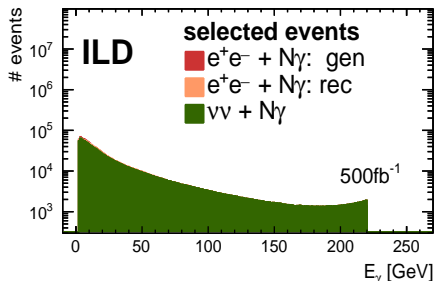
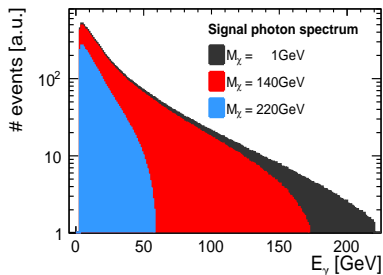


Heavy mediator (EFT limit), full simulation

arXiv:2001.03011

Signature:

- **single photon** in the central region (high tracking efficiency)
- **no other activity** in the detector
- **veto** in BeamCal (forward region)



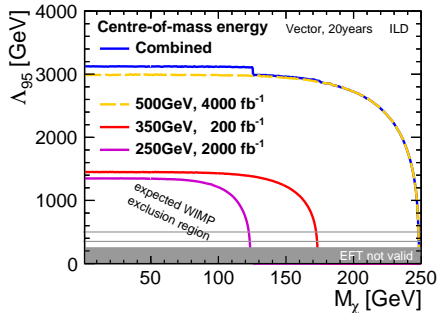
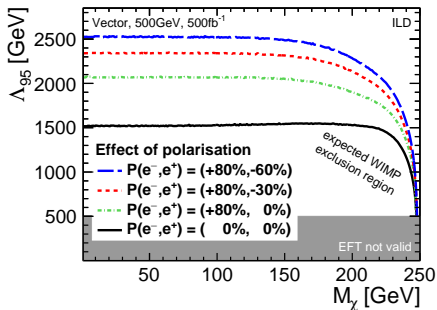
“Irreducible” background from radiative neutrino pair-production events $e^+e^- \rightarrow \nu\nu + N\gamma$ dominates after selection and bg suppression cuts

Heavy mediator (EFT limit), full simulation

arXiv:2001.03011

Different polarisation combinations help to reduce the systematics

⇒ significant improvement of mass scale limits

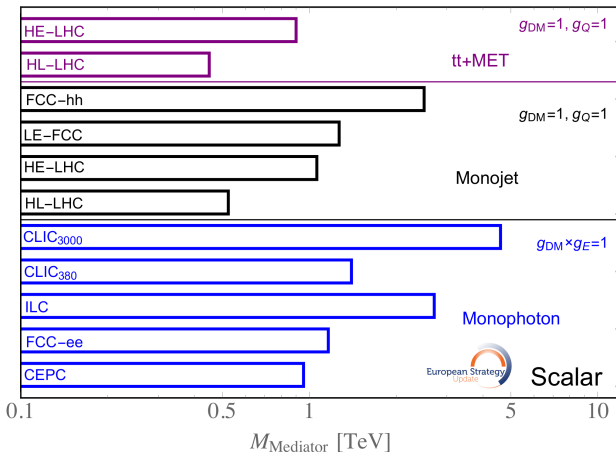


Sensitivity to the BSM mass scales up to $\Lambda \sim 3$ TeV

$$\Lambda^2 = \frac{M_Y^2}{|g_{eeY}g_{\chi\chi Y}|}$$

Comparison of mass scale limits

calculated in the EFT framework



e^+e^- mass reach comparable with that of FCC-hh !!!

New analysis approach

arXiv:2107.11194

DM production via light mediator exchange **still not excluded**
for scenarios with very small mediator couplings to SM, $\Gamma_{SM} \ll \Gamma_{tot}$

“Experimental-like” approach

⇒ focus on cross section limits as a function of mediator mass and width

Detector response simulated in the DELPHES framework (fast simulation).

WHIZARD level selection:

- 1, 2 or 3 ME photons
- at least one ME photon with
 $p_T^\gamma > 2 \text{ GeV} \ \& \ 5^\circ < \theta^\gamma < 175^\circ$
(ILC 500 GeV)
- $p_T^\gamma > 5 \text{ GeV} \ \& \ 7^\circ < \theta^\gamma < 173^\circ$
(CLIC 3 TeV)

DELPHES level selection:

- single photon with
 $p_T^\gamma > 3 \text{ GeV} \ \& \ |\eta^\gamma| < 2.8$ (ILC)
- $p_T^\gamma > 10 \text{ GeV} \ \& \ |\eta^\gamma| < 2.6$ (CLIC)
- no other activity in the detector
other reconstructed objects

Background vs Signal distributions

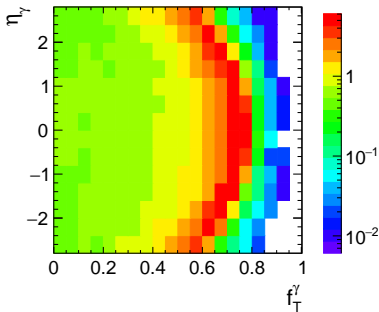
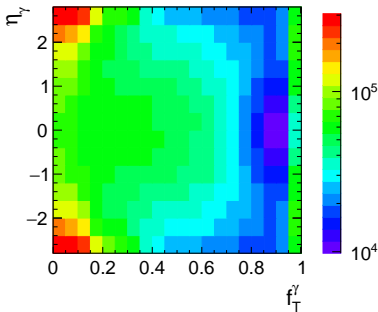
arXiv:2107.11194

For mono-photon events, two variables fully describe event kinematics

⇒ use 2D distribution of (p_T^γ, η) to constrain DM production

Background

Signal



ILC 500 GeV (-80%/+30%) 1600 fb^{-1} $M_\gamma = 400 \text{ GeV}$, $\Gamma/M = 0.03$

Signal normalised to unpolarised DM pair-production cross section of 1 fb

Cross section limits for radiative events (with tagged photon)

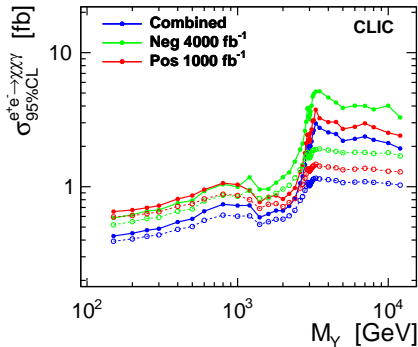
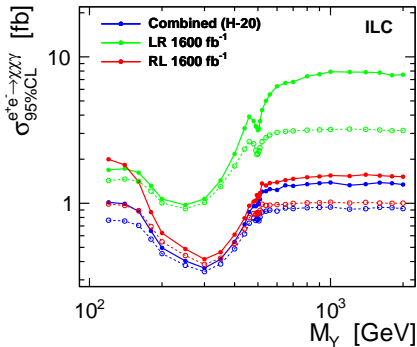
Vector Mediator

$\Gamma/M = 0.03$

with and without systematics

ILC @ 500 GeV

CLIC @ 3 TeV



Systematic effects reduced for on-shell production of narrow mediator

Cross section limits for radiative events (with tagged photon)

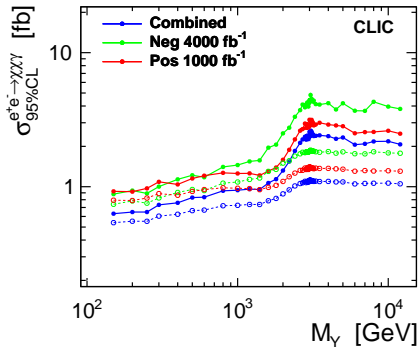
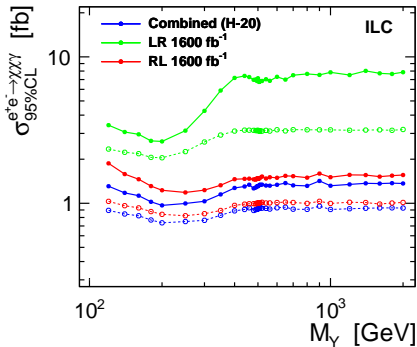
Vector Mediator

$\Gamma/M = 0.5$

with and without systematics

ILC @ 500 GeV

CLIC @ 3 TeV

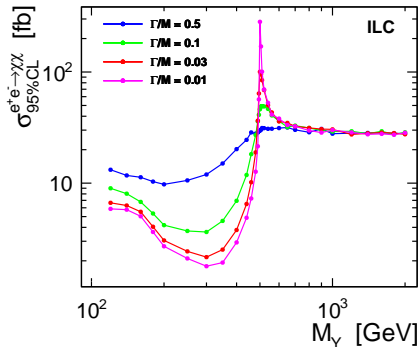


Systematic effects reduced for on-shell production of narrow mediator

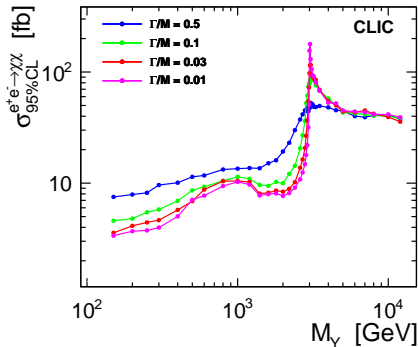
Cross section limits for total DM production cross section
 Corrected for probability of hard photon tagging!

Combined limits for **Vector mediator**

ILC @ 500 GeV



CLIC @ 3 TeV

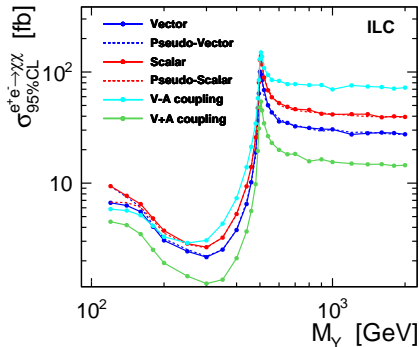


Radiation suppressed for narrow mediator with $M_Y \sim \sqrt{s} \Rightarrow$ weaker limits

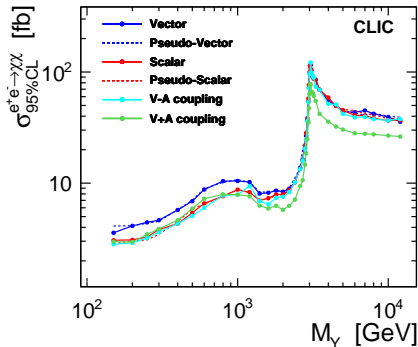
Cross section limits for total DM production cross section
 Corrected for probability of hard photon tagging!

Combined limits for mediators with $\Gamma/M = 0.03$

ILC @ 500 GeV



CLIC @ 3 TeV

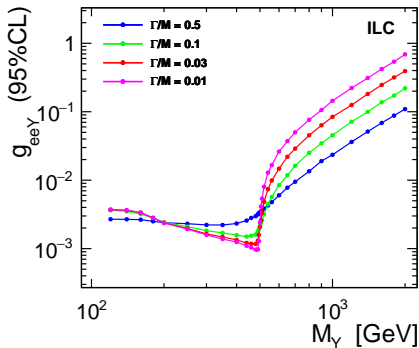


Radiation suppressed for narrow mediator with $M_Y \sim \sqrt{s} \Rightarrow$ weaker limits

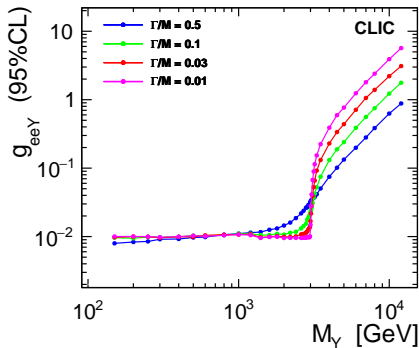
Coupling limits

Combined limits for Vector mediator

ILC @ 500 GeV



CLIC @ 3 TeV

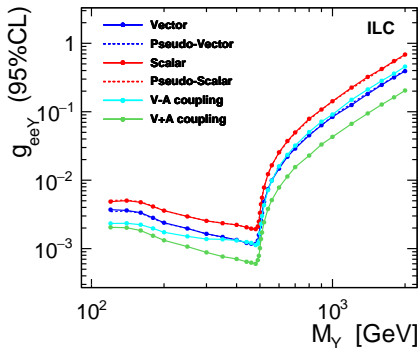


Almost uniform sensitivity to mediator coupling $g_{ee\gamma}$ up to kinematic limit.

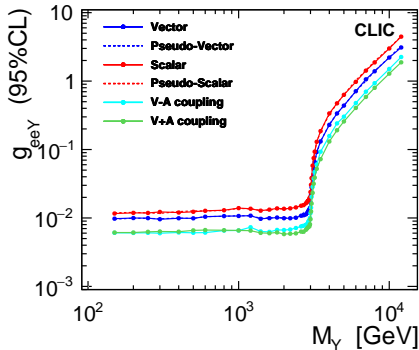
Coupling limits

Combined limits for mediators with $\Gamma/M = 0.03$

ILC @ 500 GeV



CLIC @ 3 TeV



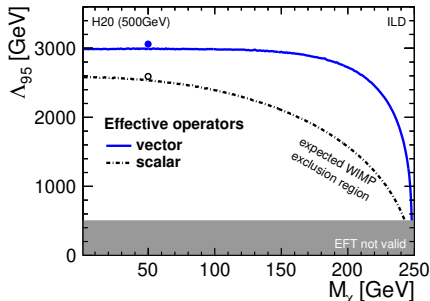
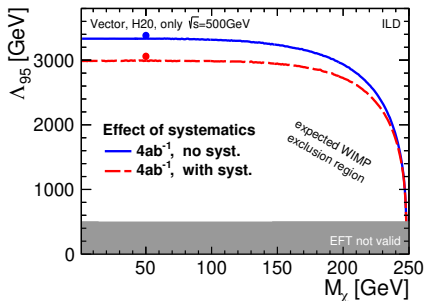
Almost uniform sensitivity to mediator coupling $g_{ee\gamma}$ up to kinematic limit.

Comparison with ILD study

arXiv:2001.03011
arXiv:2107.11194

Effective mass scale limits:
$$\Lambda^2 = \frac{M_Y^2}{|g_{eeY}g_{\chi\chi Y}|}$$

Limits from fast simulation (points) vs limits from full simulation (lines)



Very good agreement between full simulation and fast simulation results!
 \Rightarrow reliable extrapolation to low mediator mass domain...

Conclusions



Dark matter searches with mono-photon signature at future e^+e^- colliders

Future e^+e^- colliders: many complementary options for DM searches.

Mono-photon signature: the most general way to look for DM production, EFT sensitivity extending to the $\mathcal{O}(10)$ TeV mass scales

New framework for mono-photon analysis developed

focus on light mediator exchange and very small mediator couplings to SM

- $\mathcal{O}(1 \text{ fb})$ limits on the radiative production $e^+e^- \rightarrow \chi\chi\gamma_{\text{tag}}$
- $\mathcal{O}(10 \text{ fb})$ limits on the DM pair-production $e^+e^- \rightarrow \chi\chi(\gamma)$
except for the resonance region $M_\gamma \sim \sqrt{s}$
- $\mathcal{O}(10^{-3} - 10^{-2})$ limits on the mediator coupling to electrons
up to the kinematic limit $M_\gamma \leq \sqrt{s}$

For light mediators limits more stringent than those expected from direct resonance search in SM decay channels

Thank you!



Simplified DM model

Dark matter particles, X_i , couple to the SM particles via an mediator, Y_j .

Each simplified scenario is characterized by **one dark matter candidate** and **one mediator** from the set listed below:

	particle	mass	spin	charge	self-conjugate	type
DM	X_R	m_{X_R}	0	0	yes	real scalar
	X_C	m_{X_C}	0	0	no	complex scalar
	X_M	m_{X_M}	$\frac{1}{2}$	0	yes	Majorana fermion
	X_D	m_{X_D}	$\frac{1}{2}$	0	no	Dirac fermion
	X_V	m_{X_V}	1	0	yes	real vector
mediator	Y_R	m_{Y_R}	0	0	yes	real scalar
	Y_V	m_{Y_C}	1	0	yes	real vector
	T_C	m_{T_C}	0	1	no	charged scalar

Systematic uncertainties

following ILD study: Phys. Rev. D 101, 075053 (2020), [arXiv:2001.03011](https://arxiv.org/abs/2001.03011)

Considered sources of uncertainties:

- Integrated luminosity uncertainty of 0.26%
uncorrelated between polarisations
- Luminosity spectra shape uncertainty
correlated between polarisations
- Uncertainty in neutrino background normalisation of 0.2% (th+exp)
correlated between polarisations
- Uncertainty in Bhabha background normalisation of 1% (th+exp)
correlated between polarisations
- Uncertainty on beam polarisation of 0.02–0.08% (ILC)/0.2% (CLIC)
correlated for runs with same beam polarisation at ILC

⇒ nuisance parameters in the model fit (11 for ILC, 7 for CLIC)