

# Test of Fundamental Physics with Neutrinos

## outline

1. Test of Fundamental Physics
2. High-Energy Astrophysical Neutrinos
3. Search of Lorentz violation in IceCube
4. Conclusions

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King's College London

Corfu 2021 Workshop on the Standard Model and Beyond, Greece, Sep. 3, 2021

# 1. Test of Fundamental Physics

## 2. Astrophysical High-Energy Neutrinos

## 3. Search of Lorentz violation in IceCube

## 4. Conclusions

# 1. Effective violation of fundamental physics

All fundamental physics phenomena must be experimentally tested

- Spin statistics (Fermion and Boson)
  - Lorentz symmetry (rotation and Lorentz boost)
  - Poincare symmetry (energy and momentum conservation)
  - CPT symmetry (combination of above)
- etc.

Fundamental physics laws are basis of all science, so the violation, if it exists, must be **very small**

Often people assume fundamental physics can be violated **effectively**, not intrinsic violation

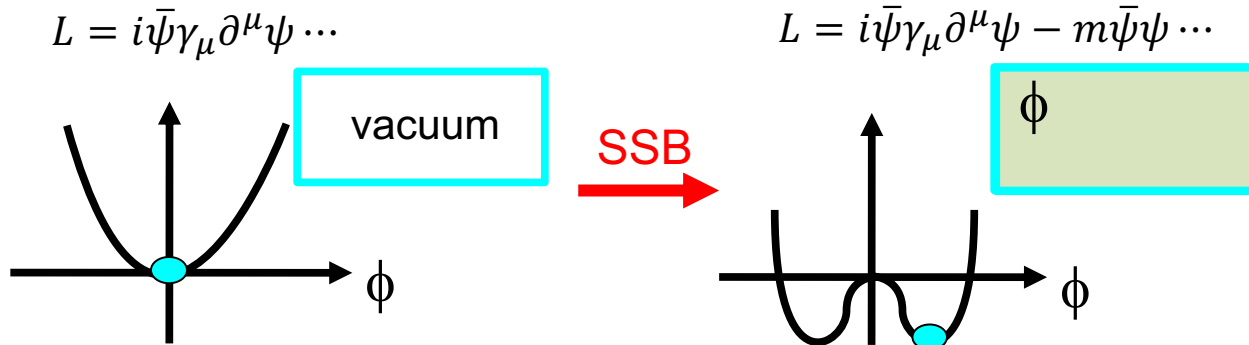
Many Beyond-the-Standard-Model theories show it is possible to violate these fundamental physics laws

- string theory
  - noncommutative field theory
  - Horava-Lifshitz gravity
- etc.

# 1. Spontaneous Lorentz symmetry breaking (SLSB)

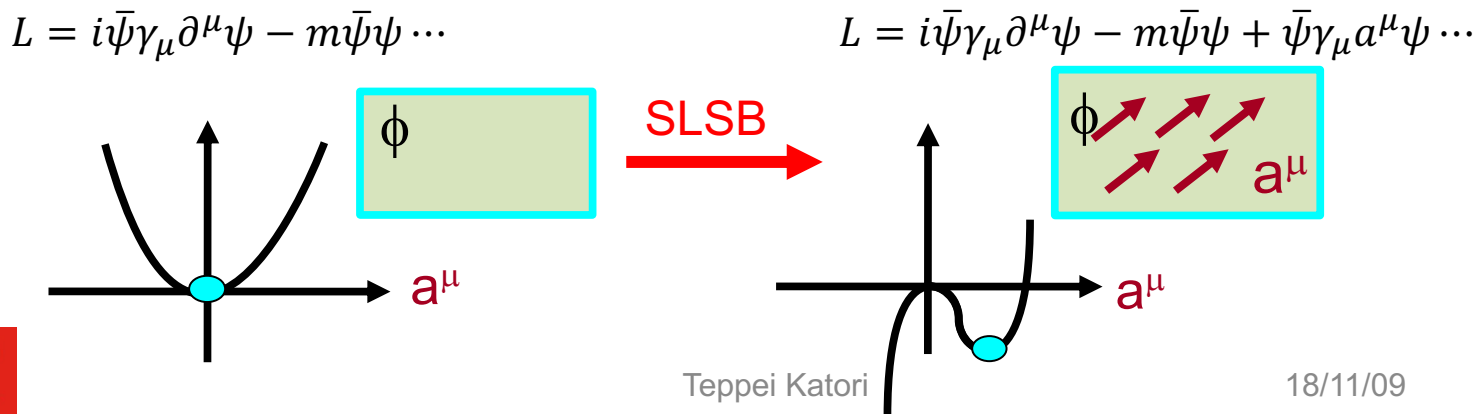
## SSB of scalar field in Standard Model (SM)

- A scalar field generates vacuum expectation value (VEV), reason unknown
- Particle acquires mass term, spontaneously violating gauge invariance



## SLSB in string field theory

- Vector fields can generate VEVs
- Lorentz symmetry is spontaneously broken



# 1. Violation of fundamental physics

Coupling of SM particles and new physics might modify behaviour of SM physics in vacuum

- matter-antimatter asymmetry
  - Direction dependent physics
  - Modified dispersion
- etc.

Expected effect is small. We need **high-precision measurements** to find such new physics

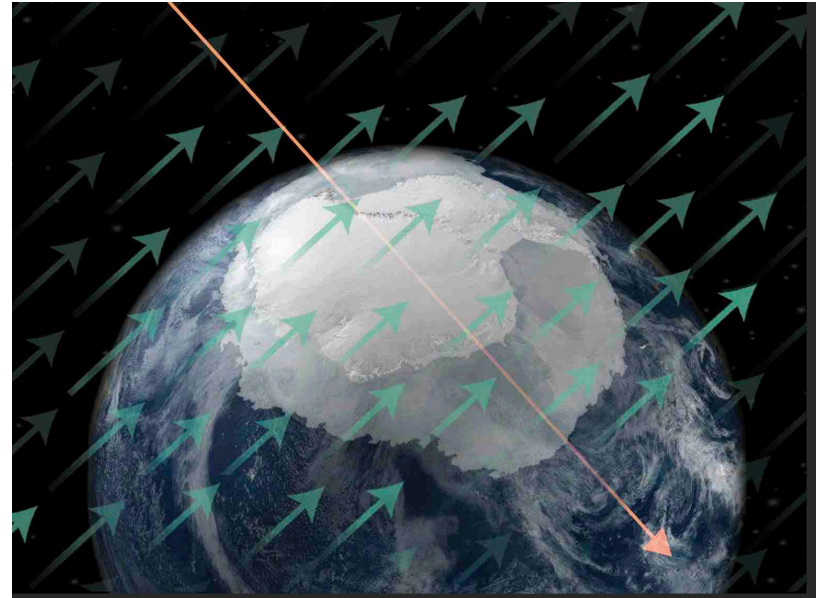
## quantum foam

- quantum fluctuation of space time

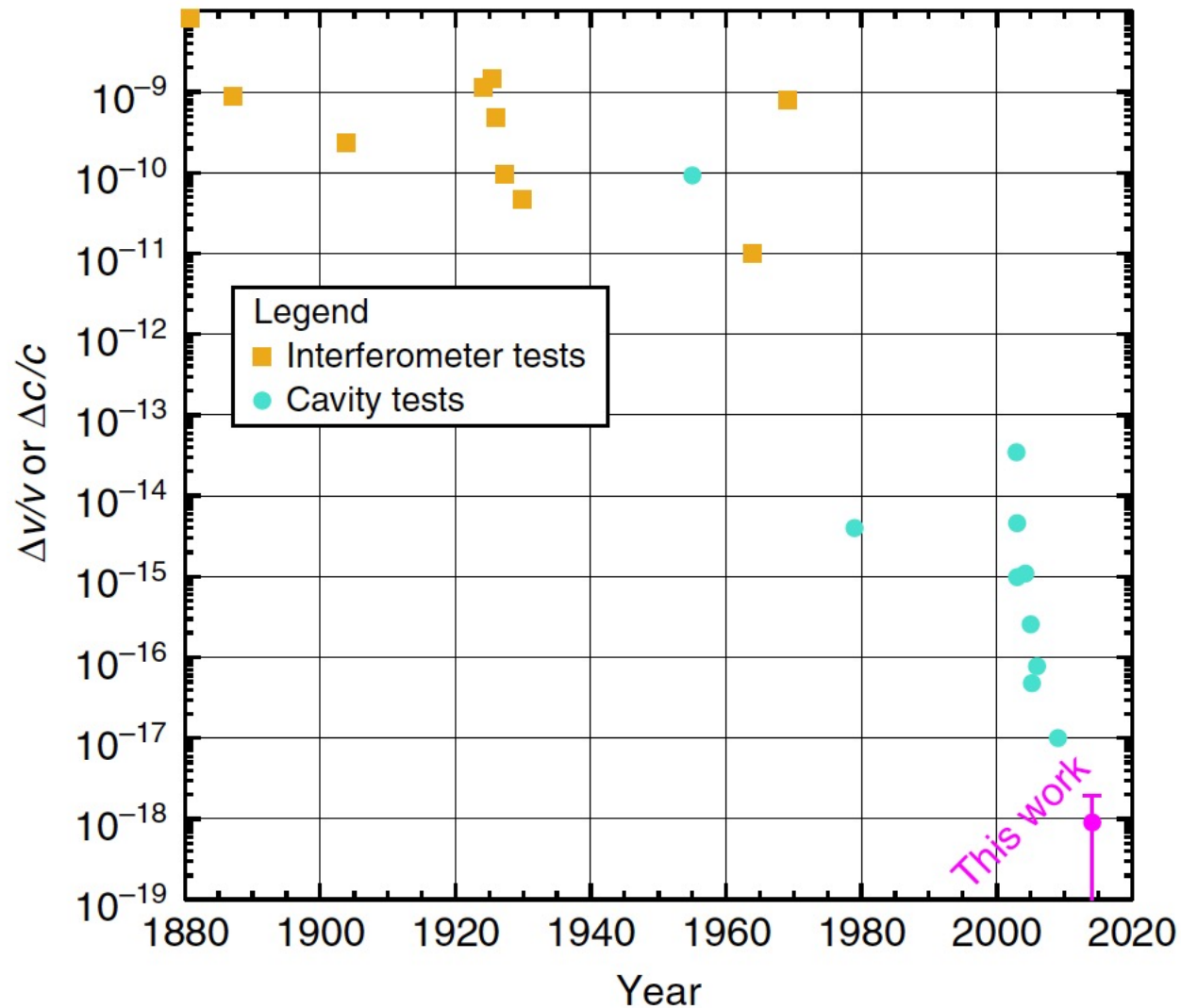


## Lorentz violating field

- new field saturating the universe (æther)



# 1. History of Michelson-Morley experiment (2015)



1. Test of Fundamental Physics

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## 2. High-energy astrophysical neutrinos

High-energy particles ( $>100$  TeV) propagating a long distance ( $>100$  Mpc)  
- Neutrinos can probe new physics in the universe



astrophysical  
neutrino





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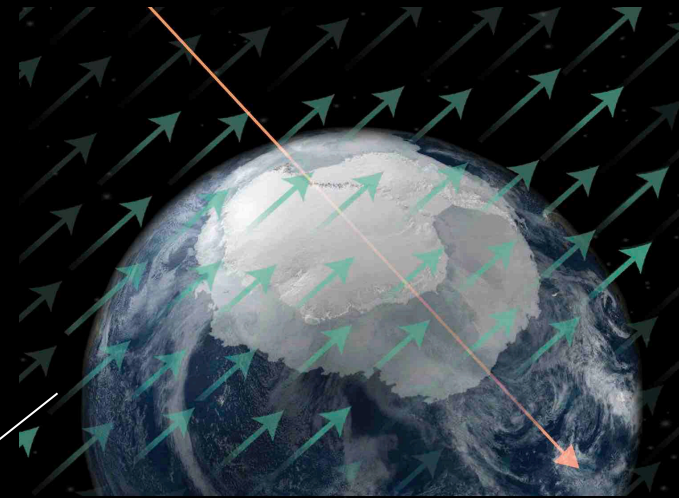
### Quantum foam

Ellis, Mavromatos, Nanopoulos PRL 293 (1992) 37



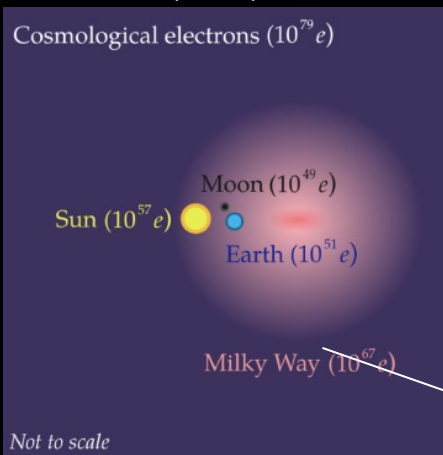
### Lorentz violating field

Argüelles, TK, Salvado, PRL 115 (2015) 161303

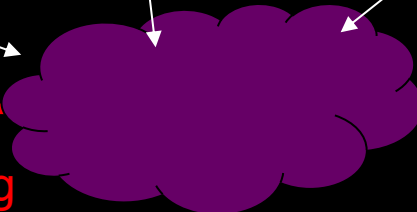


### new long-range force

Bustamante, Agarwalla  
PRL 122 (2019) 061103



neutrino mixing

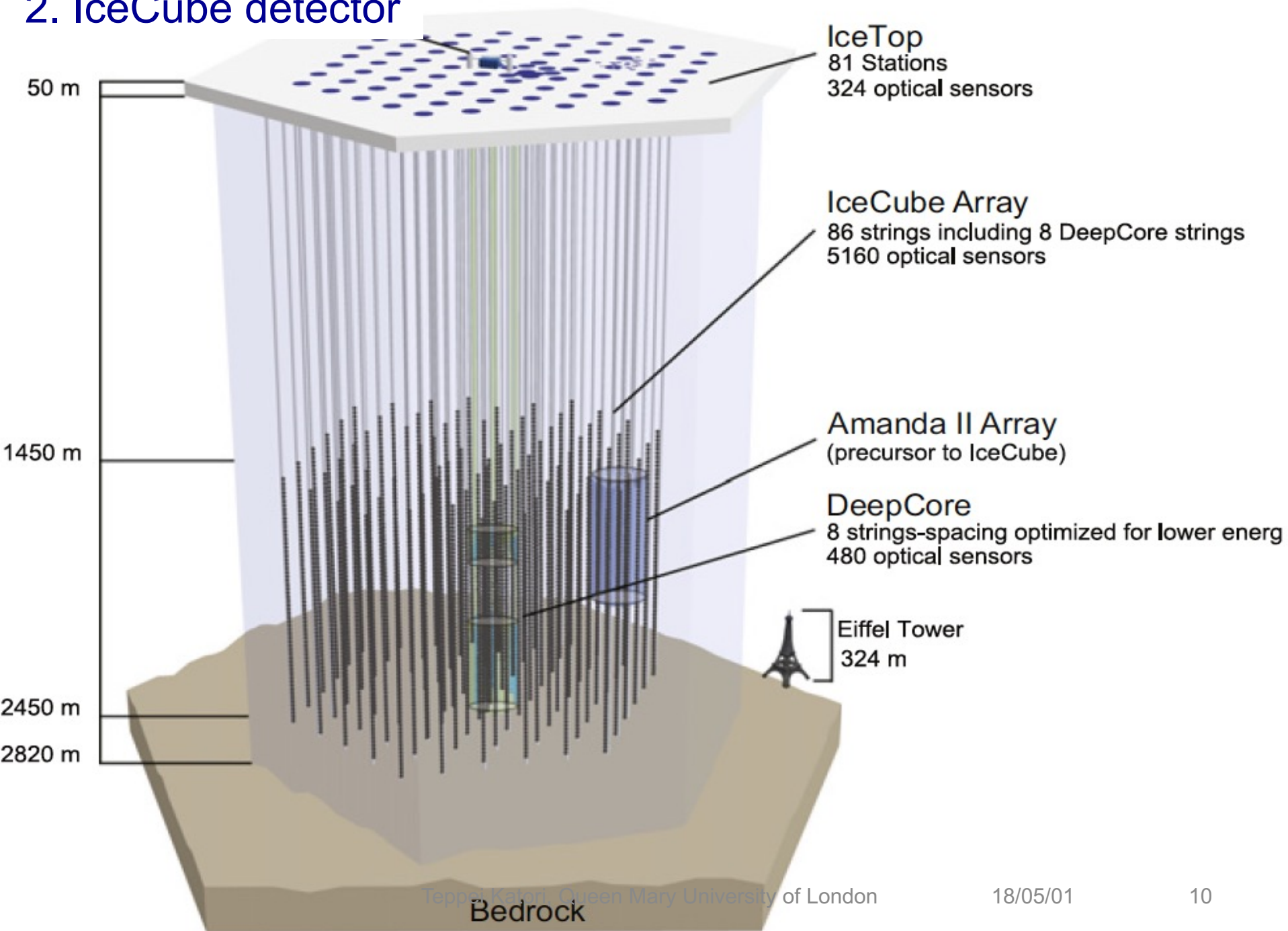


New physics

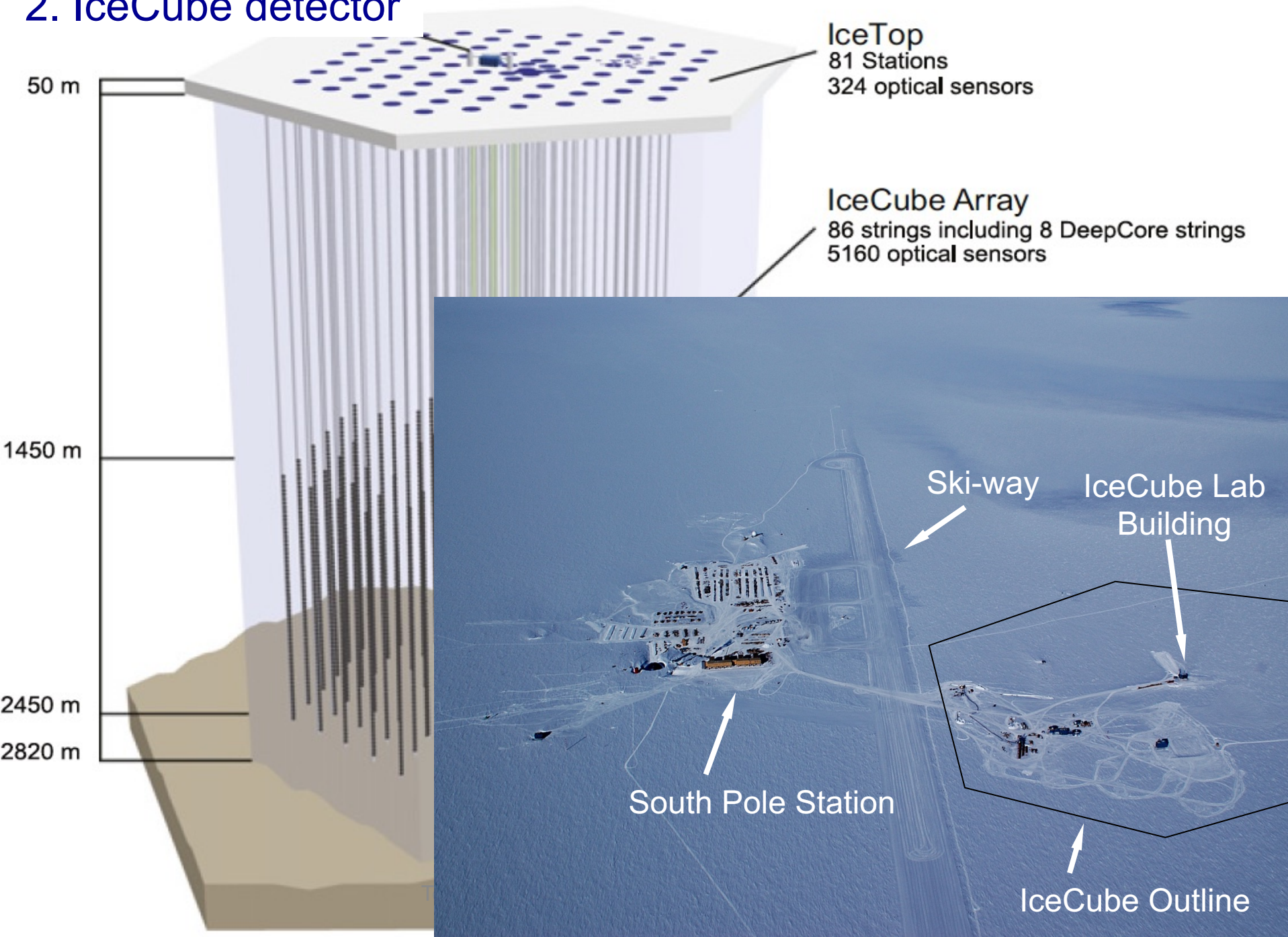
astrophysical neutrino



## 2. IceCube detector

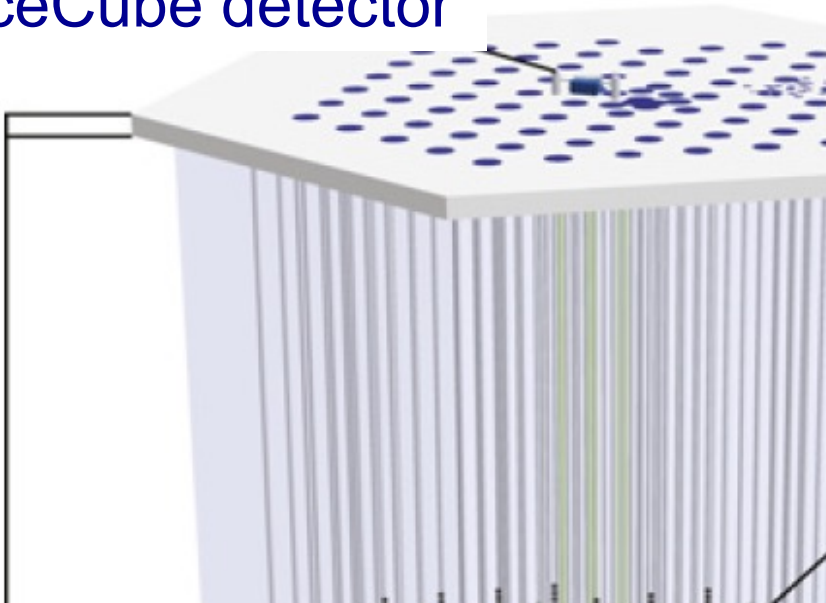


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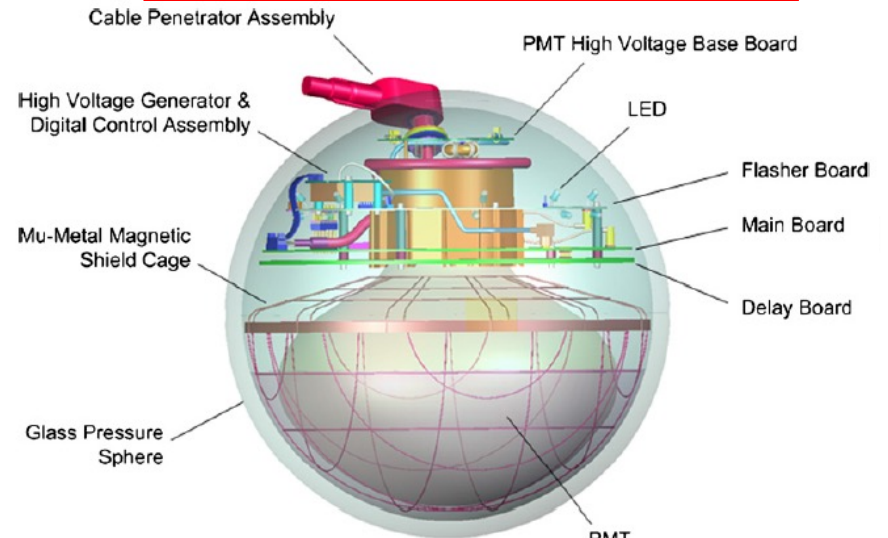


# 2. IceCube detector

50 m



## digital optical module (DOM)



(precursor to IceCube)

### DeepCore

8 strings-spacing optimized for lower energy  
480 optical sensors

Eiffel Tower  
324 m

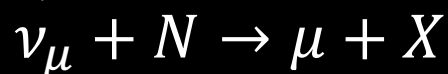


optical sensor deployment

## 2. IceCube event morphology

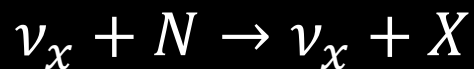
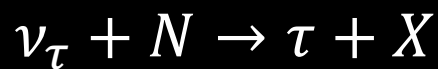
Track

$\nu_\mu$ CC



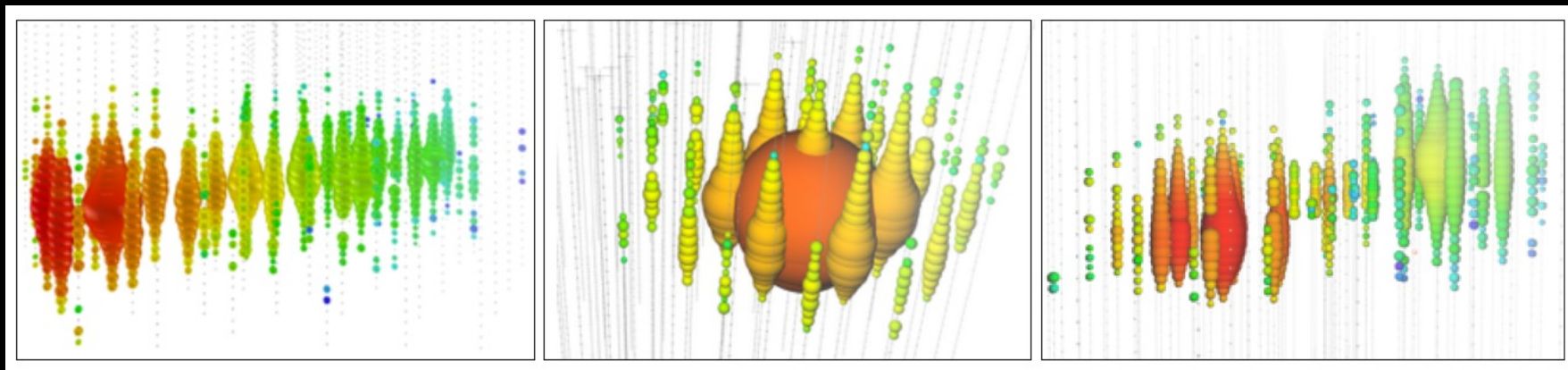
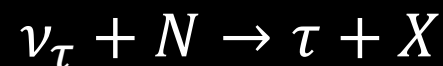
Cascade

$\nu_e$ CC,  $\nu_\tau$ CC, NC



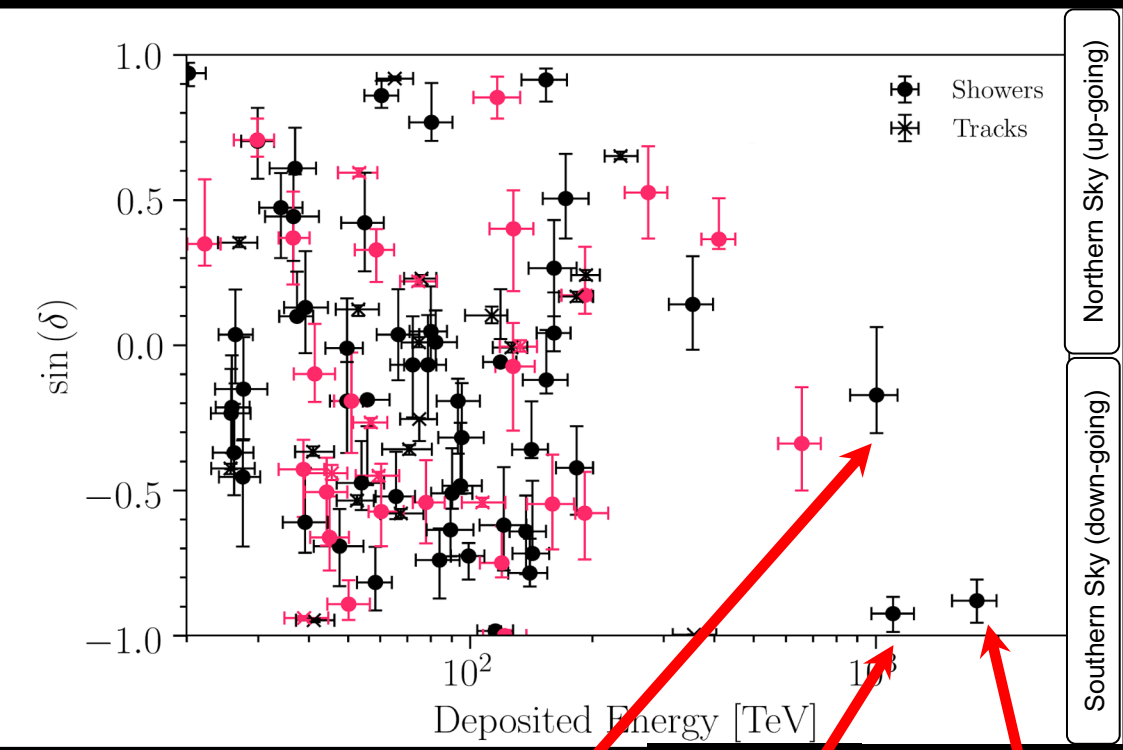
Double cascade

$\nu_\tau$ CC ( $L \sim 50 \text{m} \cdot E/\text{PeV}$ )

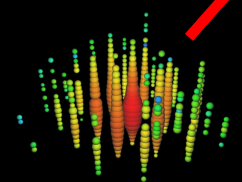


# 2. Astrophysical Very-High-Energy Neutrinos

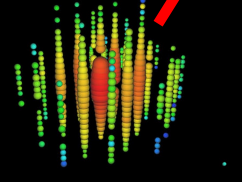
First observation (2013) by IceCube Neutrino Observatory  
- 60-2000 TeV neutrinos



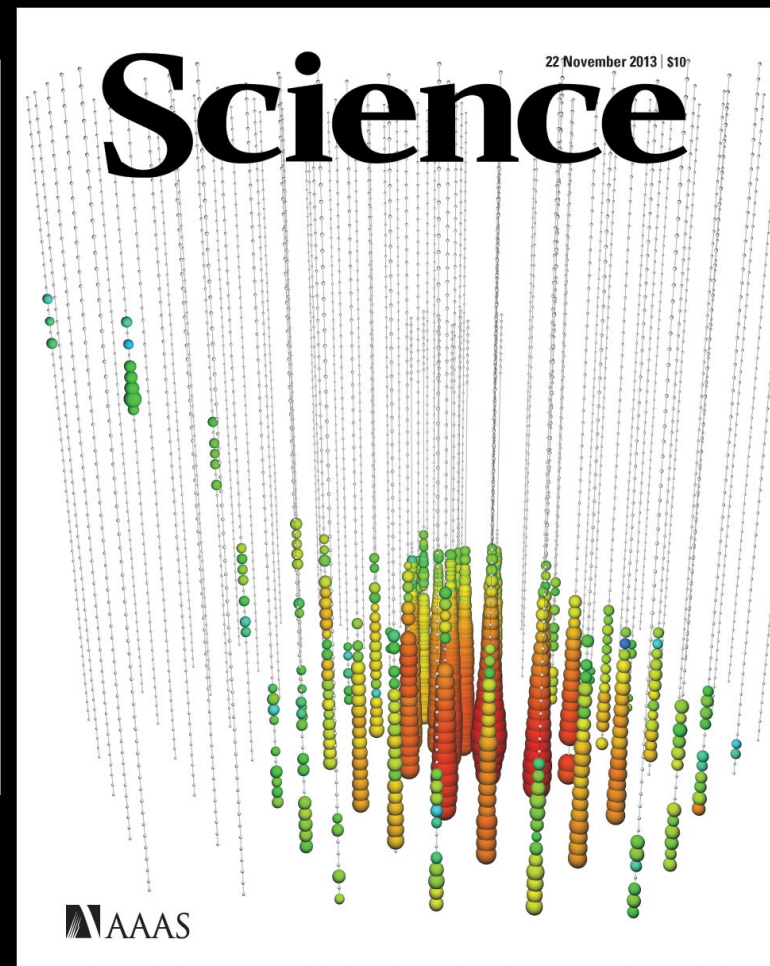
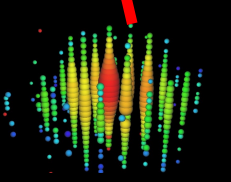
“Bert”  
1.1 PeV



“Ernie”  
1.0 PeV



“Big Bird”  
2.0 PeV



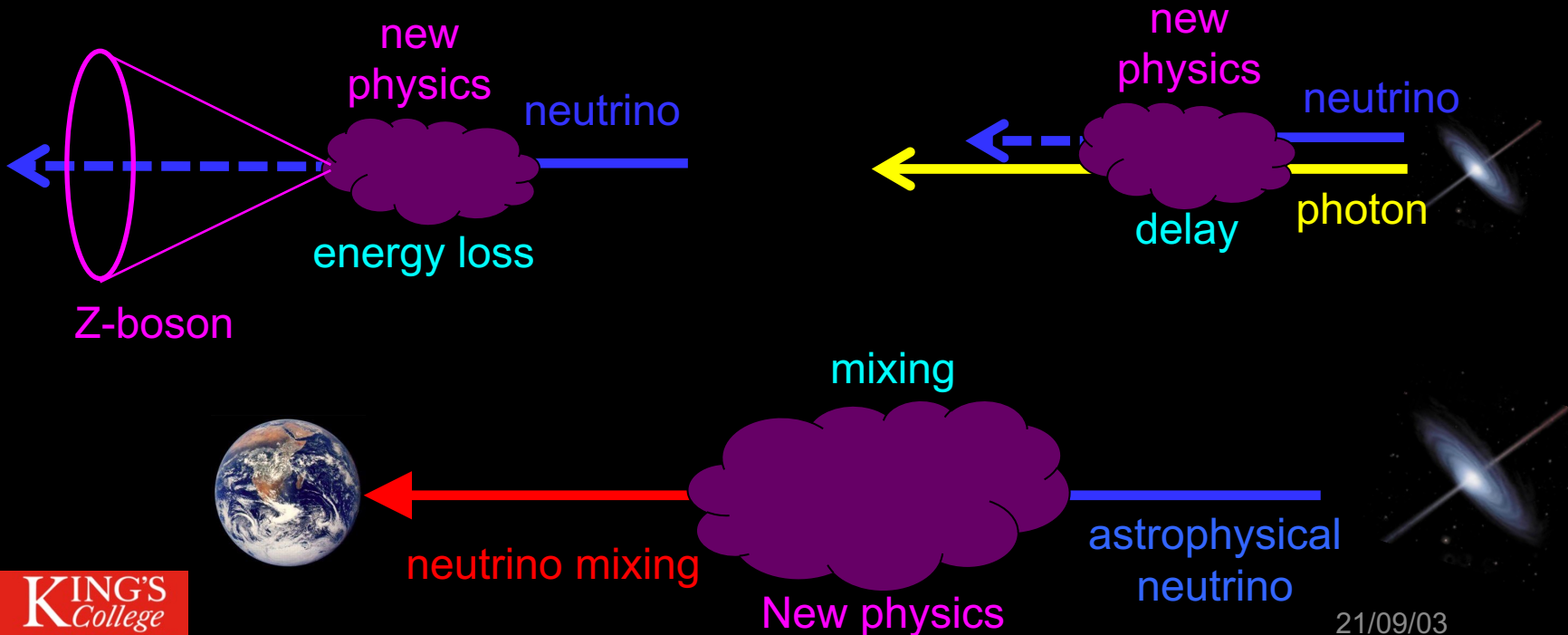
1. Test of Fundamental Physics
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- 3. Search of Lorentz violation in IceCube**
4. Conclusions

### 3. Search for Lorentz violation with astrophysical neutrinos

High-energy particles ( $>100$  TeV) propagating a long distance ( $>100$  Mpc)  
- Neutrinos can probe new physics in the universe

New physics search

- Spectrum distortion (vacuum Cherenkov radiation)
- Time of Flight (modified dispersion)
- New flavour structure (new vacuum effect)





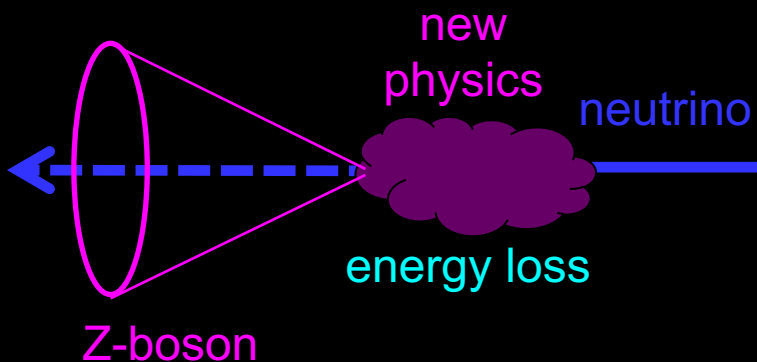
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Lorentz violating field cause  
Cherenkov radiation in vacuum

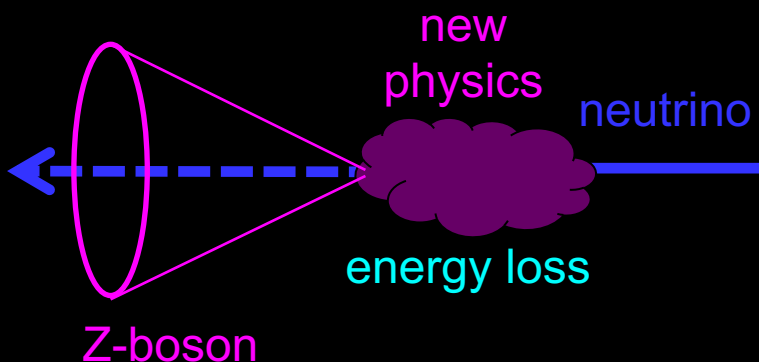
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Lorentz violating field cause  
Cherenkov radiation in vacuum

CMB polarization data  
may indicate nonzero  
vacuum birefringence  
 $k^{(3)}_{00} \sim 10^{-43}$  GeV

PHYSICAL REVIEW LETTERS **125**, 221301 (2020)

Editors' Suggestion    Featured in Physics

**New Extraction of the Cosmic Birefringence from the Planck 2018 Polarization Data**

Yuto Minami<sup>\*</sup>  
High Energy Accelerator Research Organization, 1-1 Oho, Tsukuba, Ibaraki 305-0801, Japan

Eiichiro Komatsu<sup>†</sup>

### 3. Search for Lorentz violation with astrophysical neutrinos

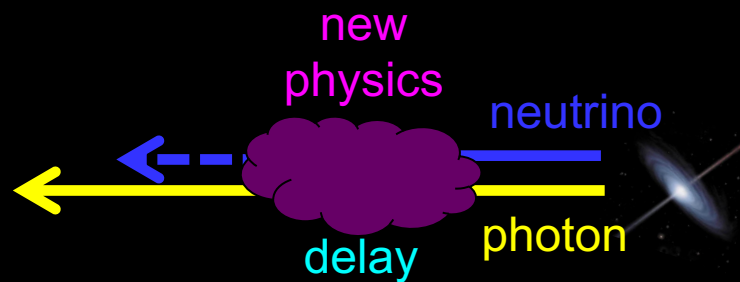
High-energy particles ( $>100$  TeV) propagating a long distance ( $>100$  Mpc)

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Modified dispersion due to quantum foam cause unexpected delay/advance for neutrinos



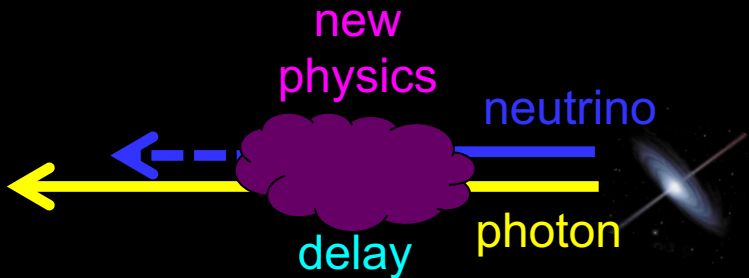
# 3. Search for Lorentz violation with astrophysical neutrinos

High-energy particles (>100 TeV) propagating a long distance (>100 Mpc)  
 - Neutrinos can probe new physics in the universe

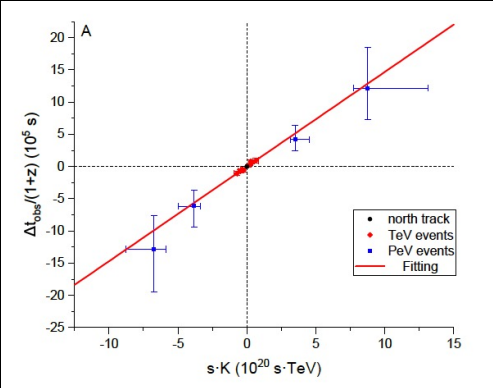
## New physics search

- Spectrum distortion (vacuum Cherenkov radiation)
- Time of Flight (modified dispersion)
- New flavour structure (new vacuum effect)

Modified dispersion due to quantum foam cause unexpected delay/advance for neutrinos



nonzero LV  
 $E_{LV} \sim 10^{17}$  GeV



$$\frac{\Delta t_{obs}}{1+z} = \Delta t_{in} + s \cdot \frac{K}{E_{LV}}$$

### 3. Search for Lorentz violation with astrophysical neutrinos

High-energy particles ( $>100$  TeV) propagating a long distance ( $>100$  Mpc)

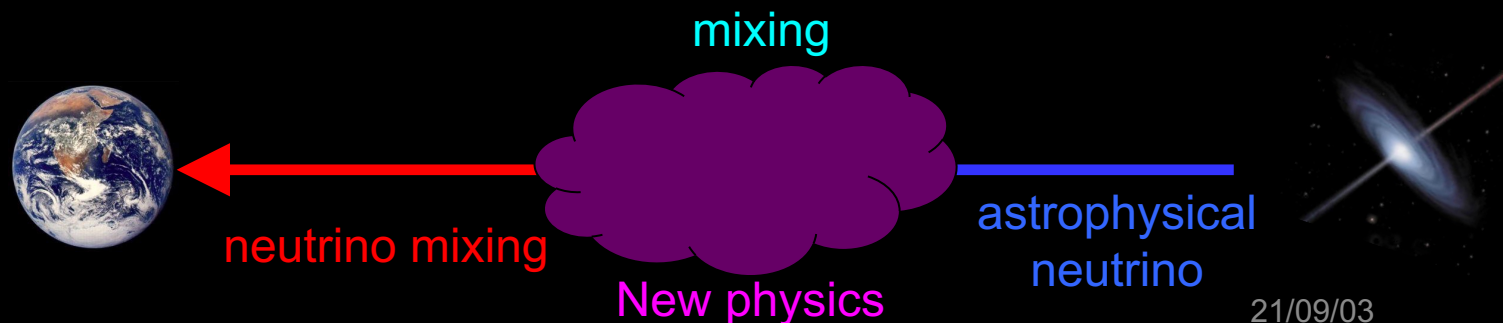
- Neutrinos can probe new physics in the universe

New physics search

- Spectrum distortion (vacuum Cherenkov radiation)
- Time of Flight (modified dispersion)
- **New flavour structure (new vacuum effect)**

Flavour effect

- Macroscopic quantum effect and sensitive to small effects
- **Today's topic**



### 3. Flavor new physics search with effective operators

Standard Model Extension (SME) is an effective field theory to look for Lorentz violation

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu\psi + \bar{\psi}\gamma^\mu c_{\mu\nu}\partial^\nu\psi \dots$$

Standard Model      New physics

Effective Hamiltonian can be written from here

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} \dots$$

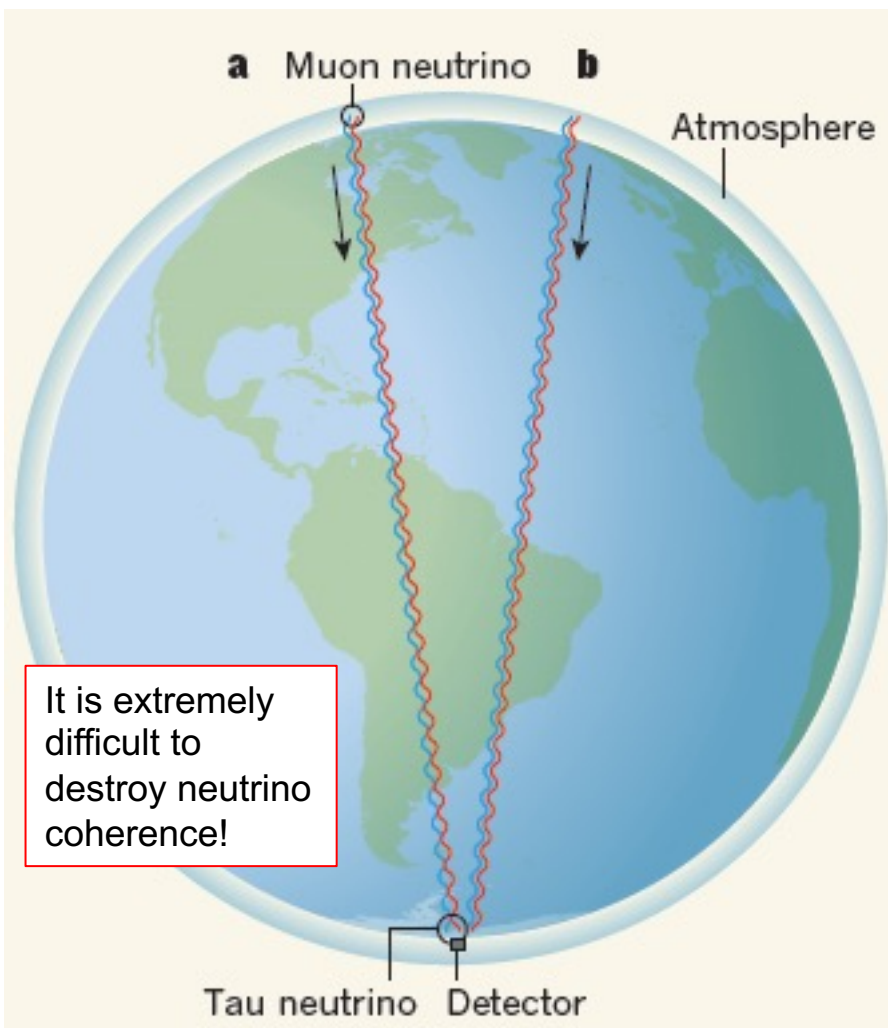
Standard Model      New physics (renormalizable)      higher dimension operator (non-renormalizable)

$E^3 c_{\alpha\beta}^{(6)} = E^3 \begin{pmatrix} c_{ee}^{(6)} & c_{e\mu}^{(6)} & c_{\tau e}^{(6)} \\ c_{e\mu}^{(6)*} & c_{\mu\mu}^{(6)} & c_{\mu\tau}^{(6)} \\ c_{\tau e}^{(6)*} & c_{\mu\tau}^{(6)*} & c_{\tau\tau}^{(6)} \end{pmatrix}$

IceCube is sensitive to higher dimension operators

dimension-6 operator natural scale:  $c^{(6)} \sim \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$

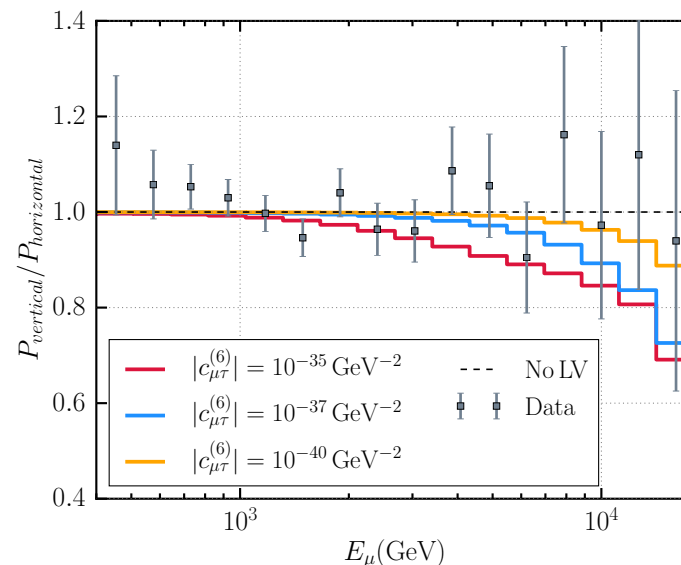
### 3. Neutrino interferometry – Atmospheric neutrinos



Neutrino oscillation is a nature interferometer. Any extra interactions in the Lagrangian contribute the phase shift

The highest energy - 20 TeV  
The longest baseline - 12700km

If anomalous coupling with neutrinos in vacuum cause a phase shift in similar order, we can see it from **spectrum distortion of atmospheric neutrinos**



IceCube atmospheric neutrino limit,  $c^{(6)} < 10^{-36} GeV^{-2}$   
This is close to the target signal region,  $c^{(6)} \sim 10^{-38} GeV^{-2}$

### 3. Neutrino interferometry – Atmospheric neutrinos

| dim.                 | method                            | type          | sector  | limits   | ref.      |
|----------------------|-----------------------------------|---------------|---|--|-----------|
| 3                    | CMB polarization                  | astrophysical | photon  | $\sim 10^{-43}$ GeV  | [6]       |
|                      | He-Xe comagnetometer              | tabletop      | neutron   | $\sim 10^{-34}$ GeV  | [10]      |
|                      | torsion pendulum                  | tabletop      | electron  | $\sim 10^{-31}$ GeV  | [12]      |
|                      | muon g-2                          | accelerator   | muon  | $\sim 10^{-24}$ GeV  | [13]      |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $ \text{Re}(\hat{a}_{\mu\tau}^{(3)}) ,  \text{Im}(\hat{a}_{\mu\tau}^{(3)})  < 2.9 \times 10^{-24}$ GeV (99% C.L.)<br>$< 2.0 \times 10^{-24}$ GeV (90% C.L.)                | this work |
| 4                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-38}$  | [7]       |
|                      | Laser interferometer              | LIGO          | photon  | $\sim 10^{-22}$  | [8]       |
|                      | Sapphire cavity oscillator        | tabletop      | photon  | $\sim 10^{-18}$  | [5]       |
|                      | Ne-Rb-K comagnetometer            | tabletop      | neutron   | $\sim 10^{-29}$  | [11]      |
|                      | trapped $\text{Ca}^+$ ion         | tabletop      | electron  | $\sim 10^{-19}$  | [14]      |
| neutrino oscillation | atmospheric                       | neutrino      | $ \text{Re}(\hat{c}_{\mu\tau}^{(4)}) ,  \text{Im}(\hat{c}_{\mu\tau}^{(4)})  < 3.9 \times 10^{-28}$ (99% C.L.)<br>$< 2.7 \times 10^{-28}$ (90% C.L.) | this work  |           |
| 5                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-34}$ GeV $^{-1}$  | [7]       |
|                      | ultra-high-energy cosmic ray      | astrophysical | proton  | $\sim 10^{-22}$ to $10^{-18}$ GeV $^{-1}$  | [9]       |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{a}_{\mu\tau}^{(5)}) ,  \text{Im}(\hat{a}_{\mu\tau}^{(5)})  < 2.3 \times 10^{-32}$ GeV $^{-1}$ (99% C.L.)<br>$< 1.5 \times 10^{-32}$ GeV $^{-1}$ (90% C.L.) | this work |
| 6                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-31}$ GeV $^{-2}$  | [7]       |
|                      | ultra-high-energy cosmic ray      | astrophysical | proton  | $\sim 10^{-42}$ to $10^{-35}$ GeV $^{-2}$  | [9]       |
|                      | gravitational Cherenkov radiation | astrophysical | gravity   | $\sim 10^{-31}$ GeV $^{-2}$  | [15]      |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{c}_{\mu\tau}^{(6)}) ,  \text{Im}(\hat{c}_{\mu\tau}^{(6)})  < 1.5 \times 10^{-36}$ GeV $^{-2}$ (99% C.L.)<br>$< 9.1 \times 10^{-37}$ GeV $^{-2}$ (90% C.L.) | this work |
| 7                    | GRB vacuum birefringence          | astrophysical | photon  | $\sim 10^{-28}$ GeV $^{-3}$  | [7]       |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{a}_{\mu\tau}^{(7)}) ,  \text{Im}(\hat{a}_{\mu\tau}^{(7)})  < 8.3 \times 10^{-41}$ GeV $^{-3}$ (99% C.L.)<br>$< 3.6 \times 10^{-41}$ GeV $^{-3}$ (90% C.L.) | this work |
| 8                    | gravitational Cherenkov radiation | astrophysical | gravity   | $\sim 10^{-46}$ GeV $^{-4}$  | [15]      |
|                      | neutrino oscillation              | atmospheric   | neutrino  | $\text{Re}(\hat{c}_{\mu\tau}^{(8)}) ,  \text{Im}(\hat{c}_{\mu\tau}^{(8)})  < 5.2 \times 10^{-45}$ GeV $^{-4}$ (99% C.L.)<br>$< 1.4 \times 10^{-45}$ GeV $^{-4}$ (90% C.L.) | this work |

TABLE I: Comparison of attainable best limits of SME coefficients in various fields.

IceCube atmospheric neutrino limit,  $c^{(6)} < 10^{-36} \text{GeV}^{-2}$   
 This is close to the target signal region,  $c^{(6)} \sim 10^{-38} \text{GeV}^{-2}$



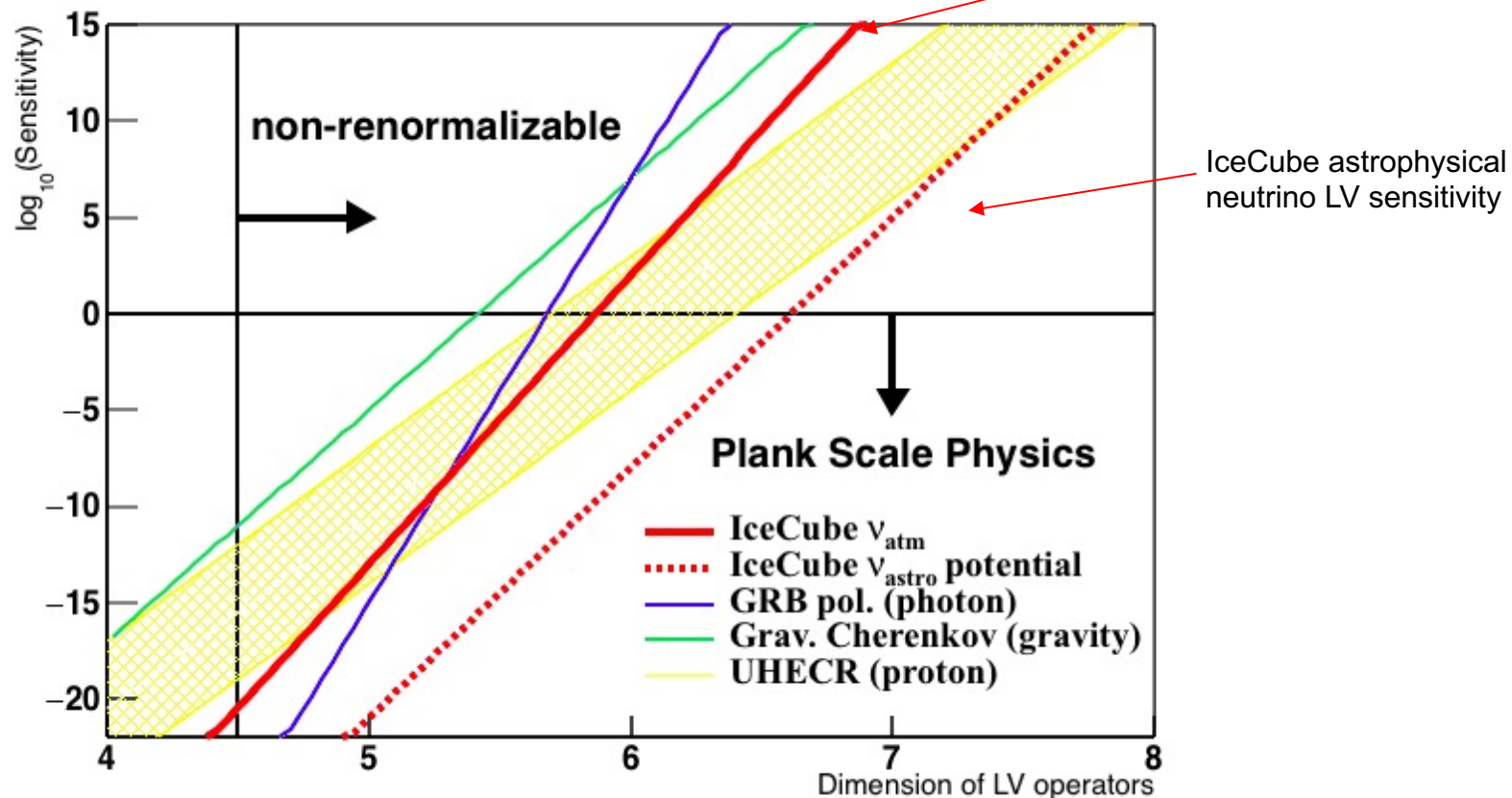
### 3. Neutrino interferometry – Astrophysical neutrinos

Higher-dimension operators may be related to new physics

- Dimension-5 operator (unit:  $\text{GeV}^{-1}$ ), example: Majorana mass
- Dimension-6 operator (unit:  $\text{GeV}^{-2}$ ), example: Fermi constant ( $G_F$ )

IceCube atmospheric  
neutrino LV sensitivity  
[Nature Physics 14\(2018\)961](#)

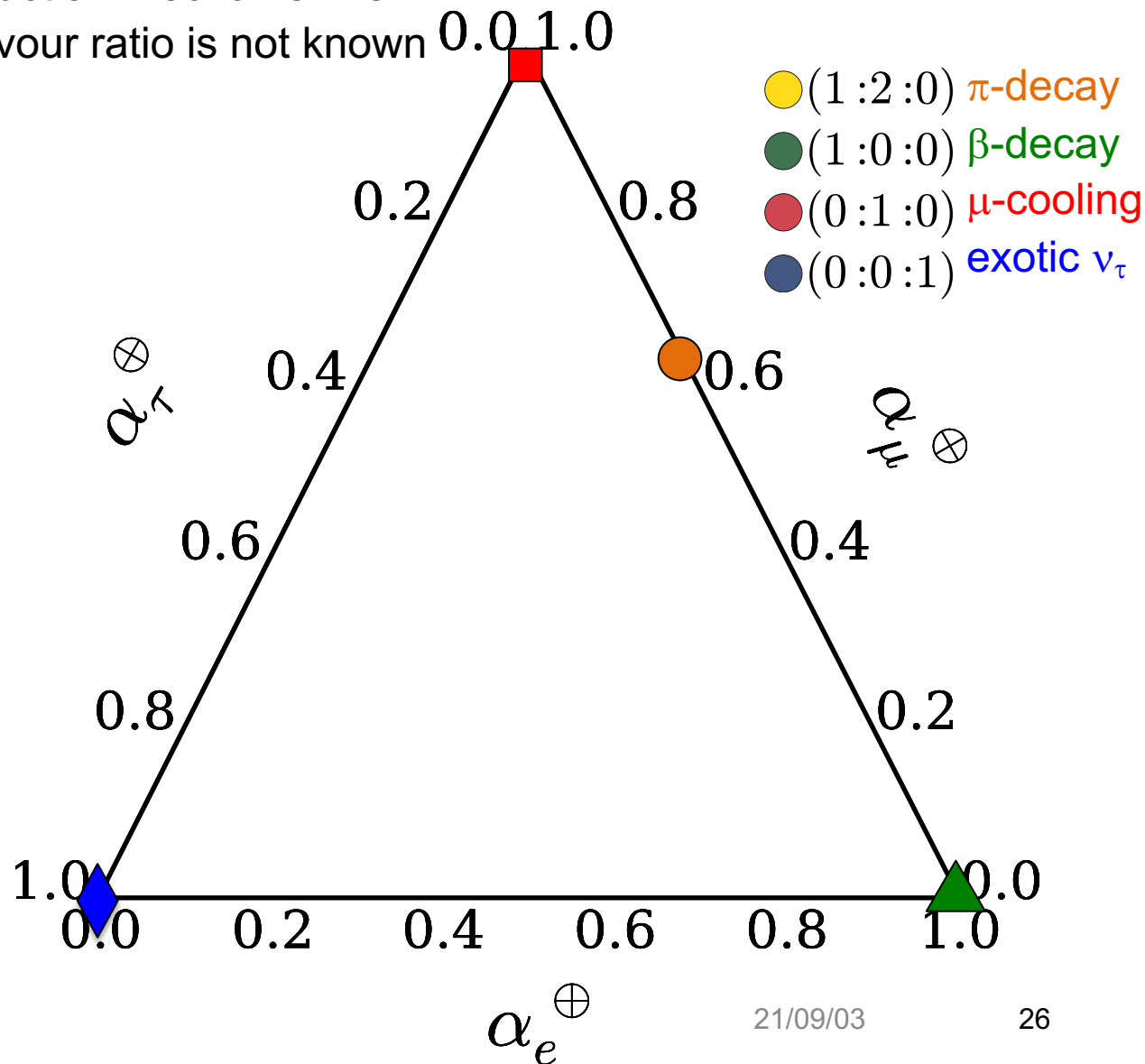
New physics limits and projected sensitivity



Astrophysical neutrino dim-6 LV operator search can reach quantum gravity motivated region ( $\sim 1/M_{\text{Planck}}^2 \sim 10^{-38} \text{ GeV}^{-2}$ )

### 3. Neutrino flavor ratio ( $\nu_e : \nu_\mu : \nu_\tau$ )

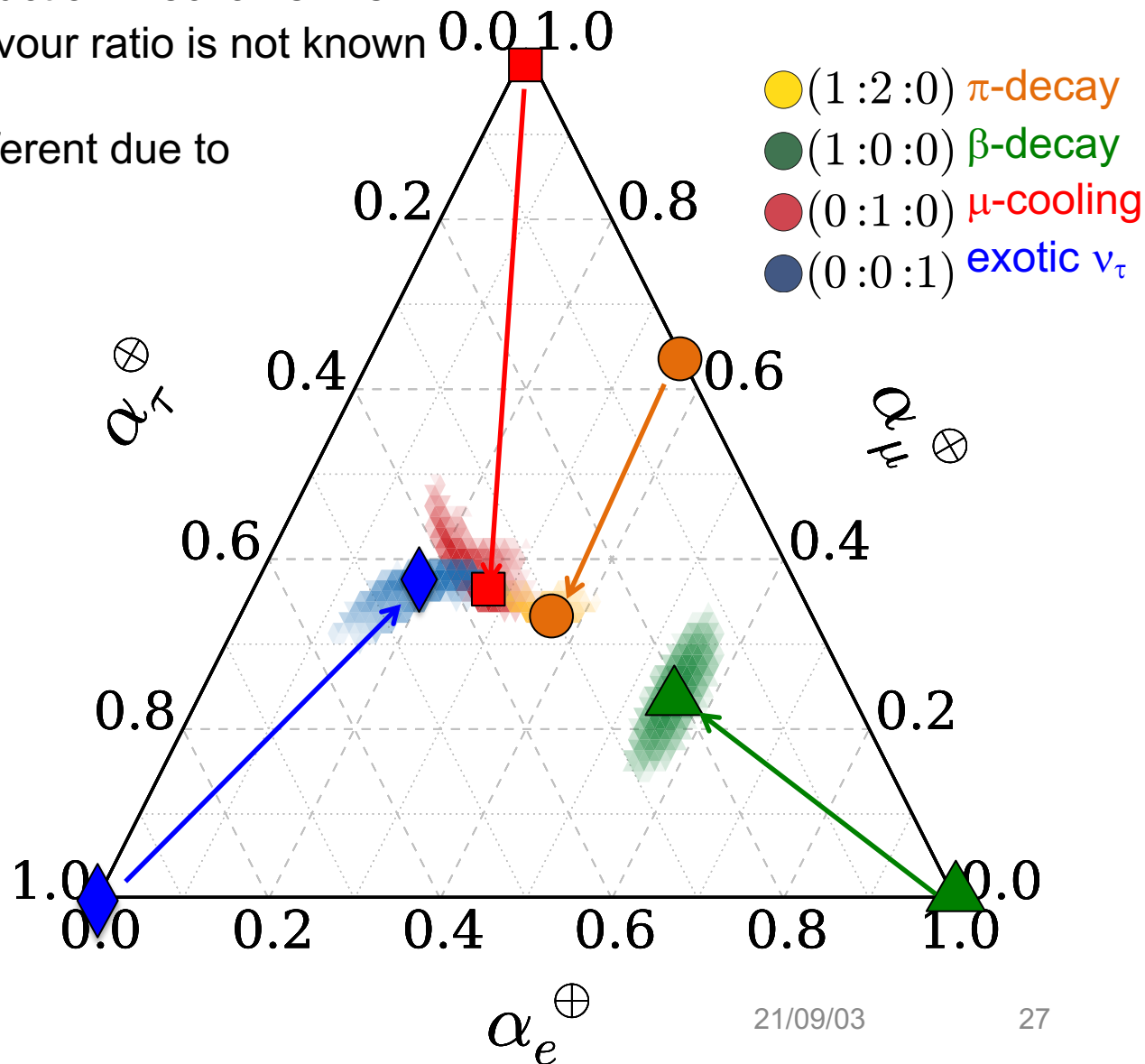
Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known



### 3. Neutrino flavor ratio ( $\nu_e : \nu_\mu : \nu_\tau$ )

Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known

Flavour ratio on Earth is different due to mixing by neutrino masses

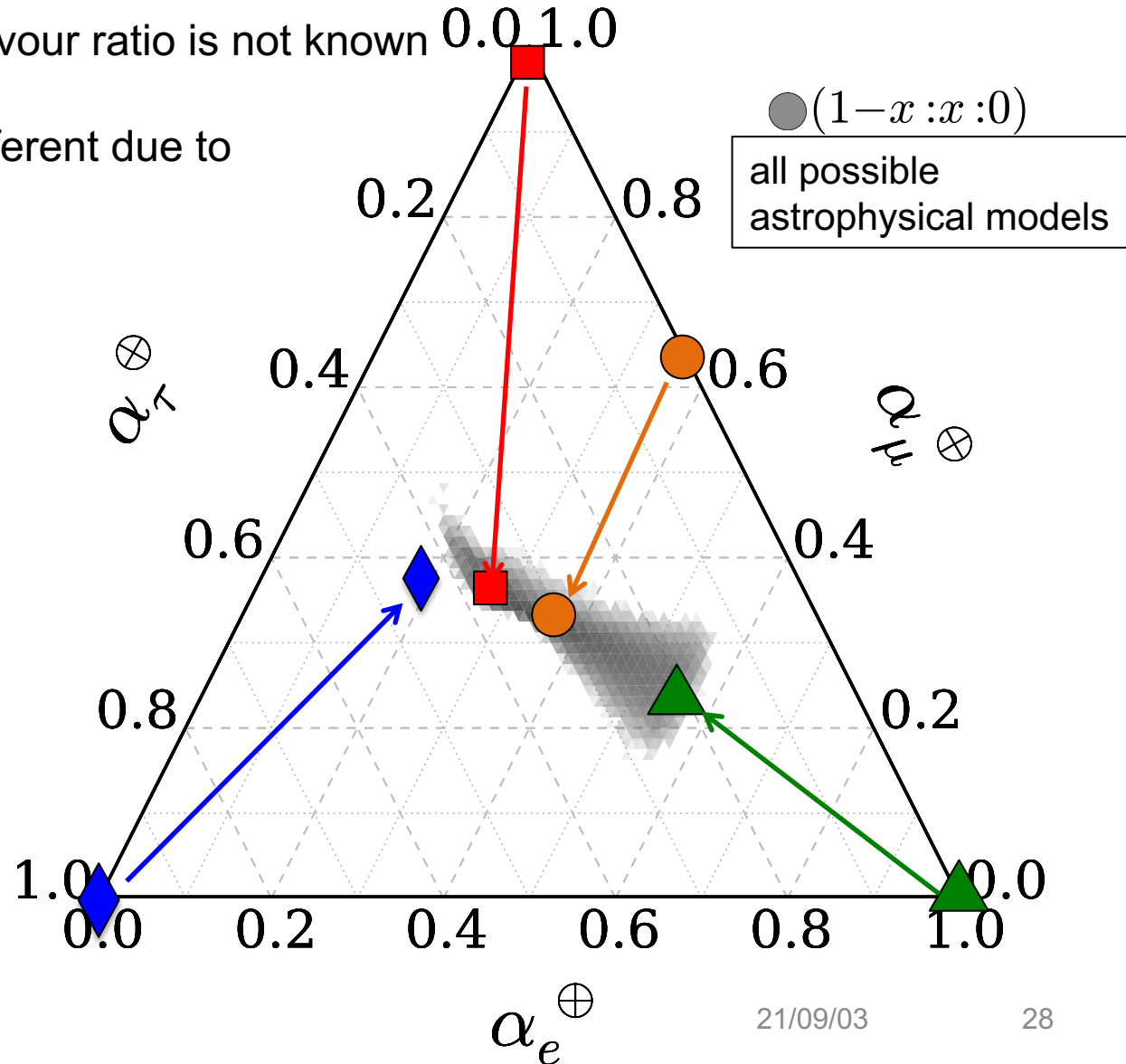


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Astrophysical neutrino production mechanism is not known  $\rightarrow$  production flavour ratio is not known

Flavour ratio on Earth is different due to mixing by neutrino masses

All possible flavour ratio is confined in a small space



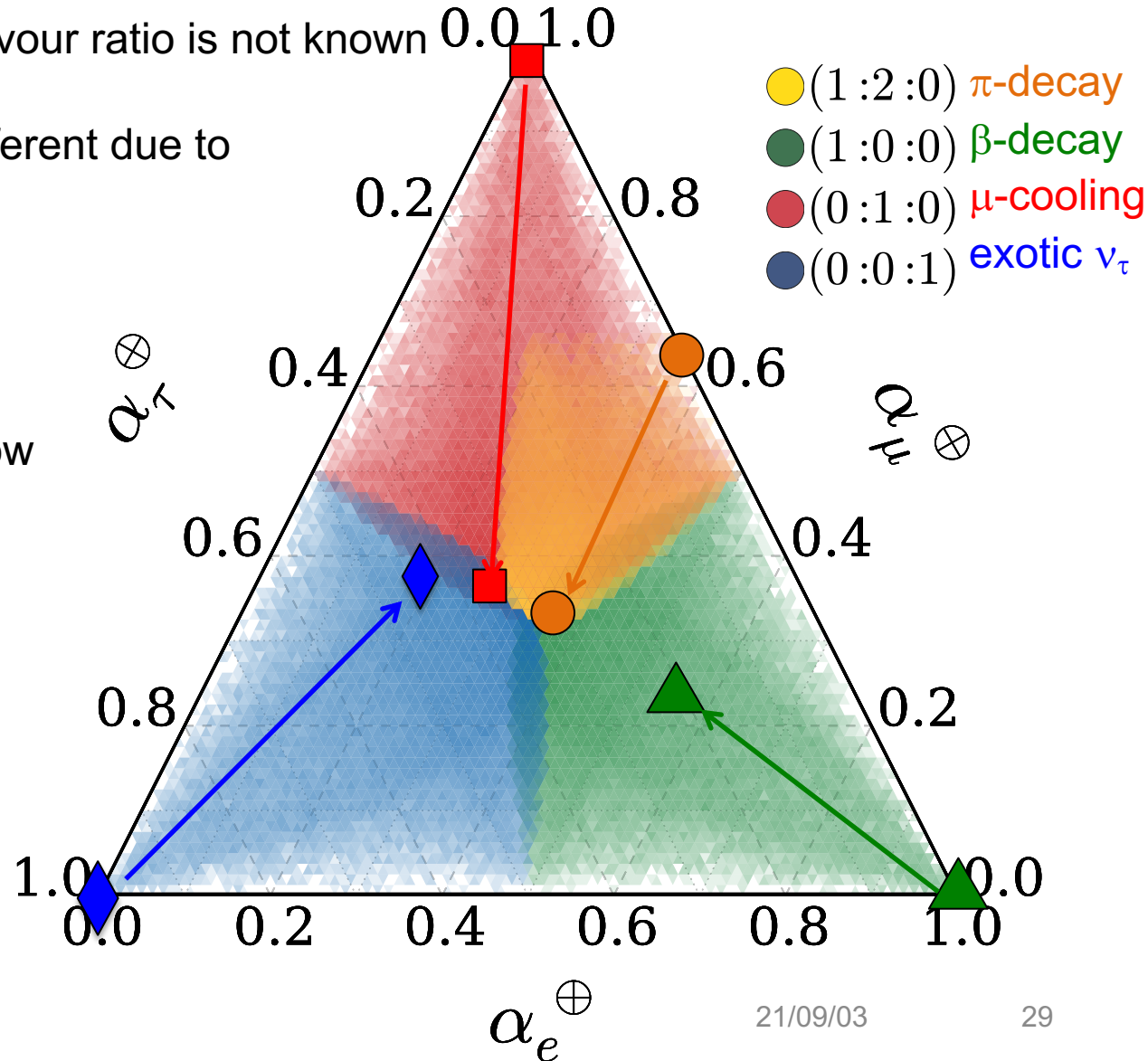
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All possible flavour ratio is confined in a small space

e.g.) New physics just below the limit can produce any flavour ratio



### 3. HESE 7.5-yr flavor ratio

60 HESE events in 60 TeV – 2 PeV  
First identification of tau neutrinos

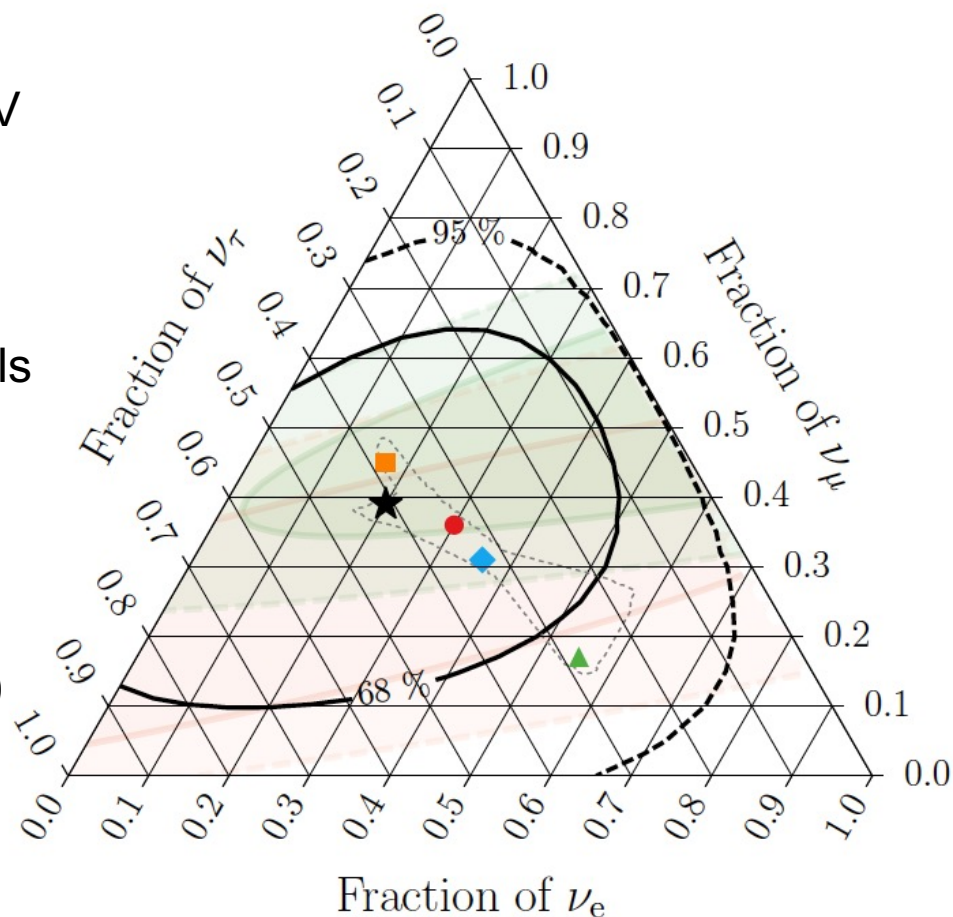
New flavour ratio measurement

- contour is too big, most of models are accepted by data

We will not find new physics

We need;

- higher statistics (IceCube-Gen2)
- better PID (software)



— HESE with ternary topology ID  
★ Best fit: 0.20 : 0.39 : 0.42  
■ Global Fit (IceCube, APJ 2015)  
■ Inelasticity (IceCube, PRD 2019)  
⋯⋯⋯ 3ν-mixing 3σ allowed region

$\nu_e : \nu_\mu : \nu_\tau$  at source  $\rightarrow$  on Earth:  
■ 0:1:0  $\rightarrow$  0.17 : 0.45 : 0.37  
● 1:2:0  $\rightarrow$  0.30 : 0.36 : 0.34  
▲ 1:0:0  $\rightarrow$  0.55 : 0.17 : 0.28  
◆ 1:1:0  $\rightarrow$  0.36 : 0.31 : 0.33

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60 HESE events in 60 TeV – 2 PeV

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New flavour ratio measurement

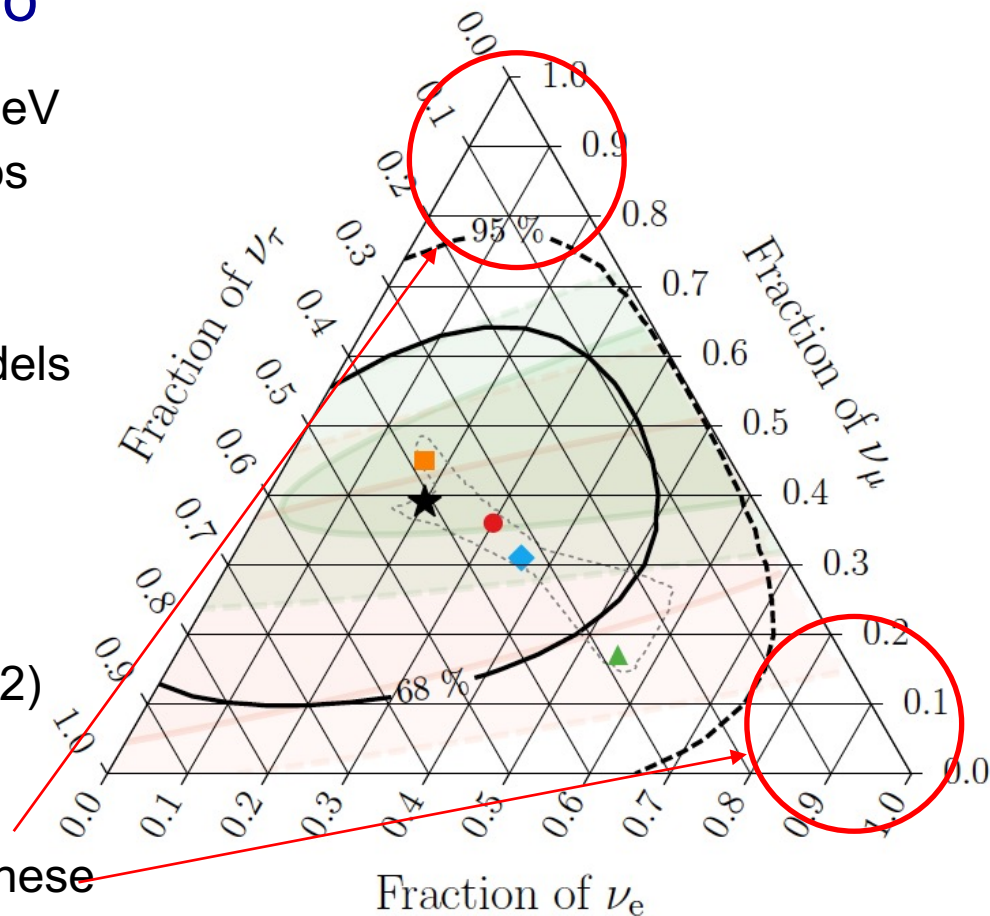
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We need;

- higher statistics (IceCube-Gen2)
- better PID (software)

Models predict flavour ratios at these corners would be rejected



|  |   |  |
|--|---|--|
|  | HESE with ternary topology ID           | $\nu_e : \nu_\mu : \nu_\tau$ at source $\rightarrow$ on Earth: |
|  | Best fit: 0.20 : 0.39 : 0.42            | 0:1:0 $\rightarrow$ 0.17 : 0.45 : 0.37                         |
|  | Global Fit (IceCube, APJ 2015)          | 1:2:0 $\rightarrow$ 0.30 : 0.36 : 0.34                         |
|  | Inelasticity (IceCube, PRD 2019)        | 1:0:0 $\rightarrow$ 0.55 : 0.17 : 0.28                         |
|  | $3\nu$ -mixing $3\sigma$ allowed region | 1:1:0 $\rightarrow$ 0.36 : 0.31 : 0.33                         |

### 3. HESE 7.5-yr flavor new physics search

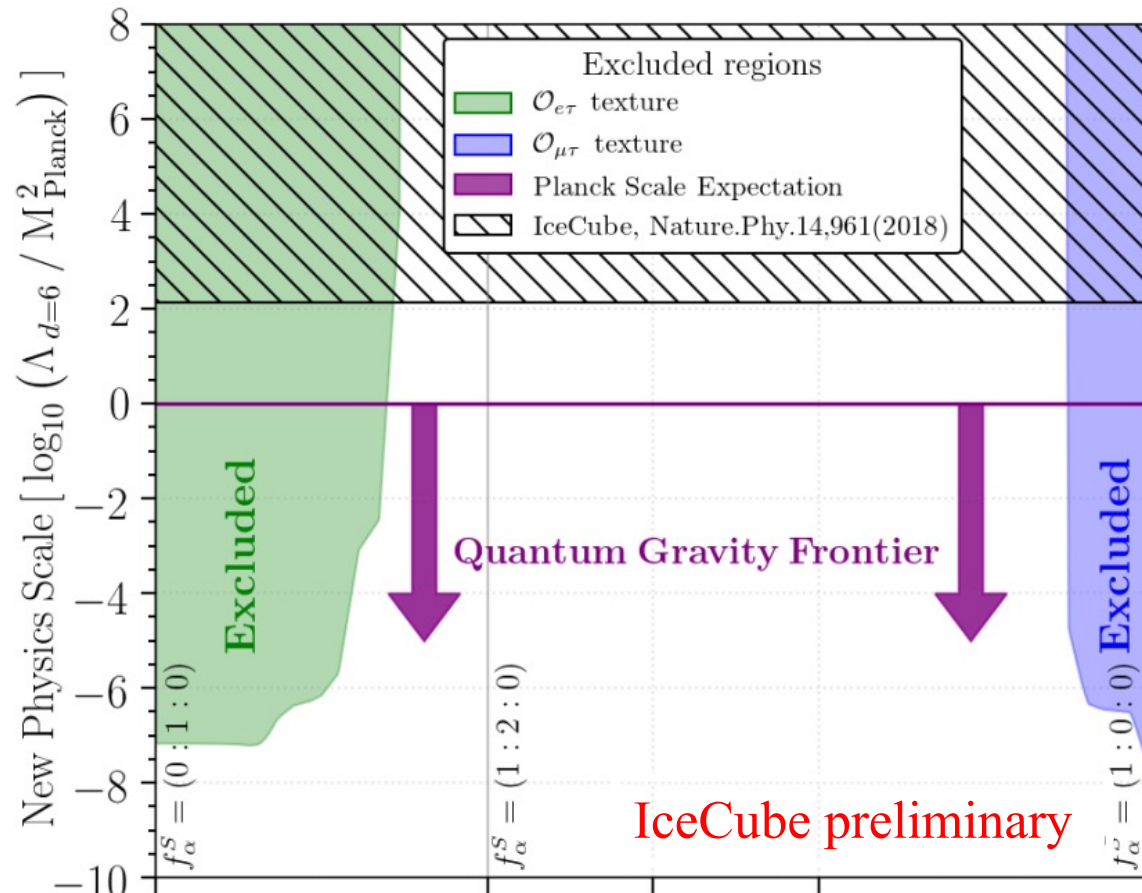
60 HESE events in 60 TeV – 2 PeV

First identification of tau neutrinos

Strong limits for many parameters depending on assumed initial flavour ratio

- $10^{-26}$  GeV  $\sim$  dim-3 LV limit
- $10^{-32}$   $\sim$  dim-4 LV limit
- $10^{-40}$  GeV $^{-1}$   $\sim$  dim-5 LV limit
- $10^{-46}$  GeV $^{-2}$   $\sim$  dim-6 LV limit
- $10^{-51}$  GeV $^{-3}$   $\sim$  dim-7 LV limit
- $10^{-58}$  GeV $^{-4}$   $\sim$  dim-8 LV limit

Paper in preparation (2021)



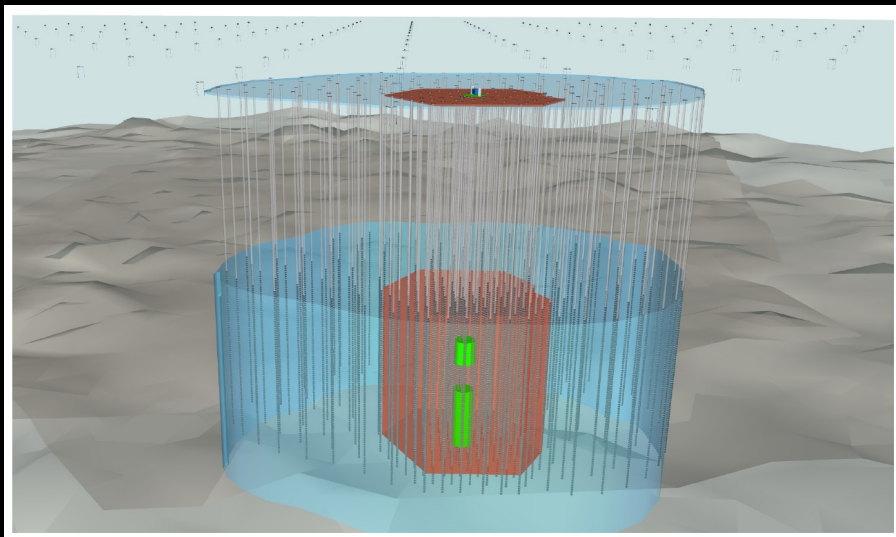




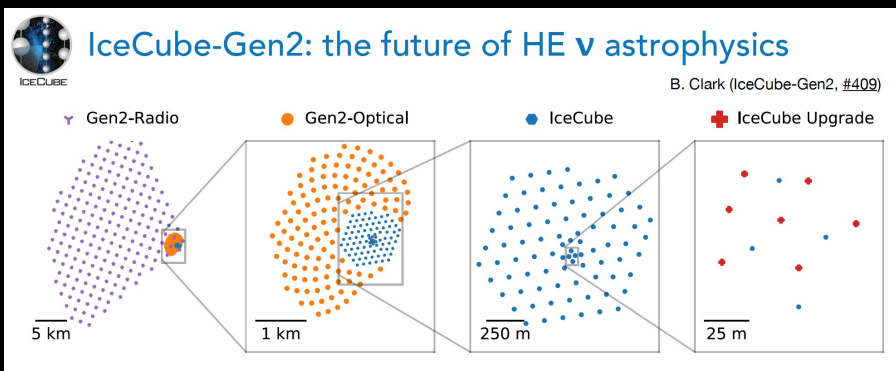
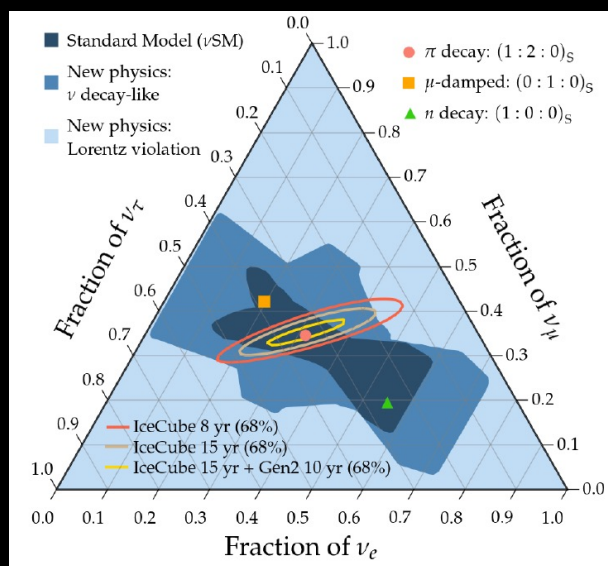
ICECUBE  
 GEN2

# 3. IceCube-Gen2

Larger separation (125m  $\rightarrow$   $\sim$ 200-300m) to cover larger volume  
 - 120 new strings with 100 sensors, 240 m separation, x10 coverage



IceCube-Gen2 flavour ratio sensitivity



The first stage of Gen2 (IceCube upgrade) is approved and ongoing



# Conclusion

Quantum gravity may create a new structure in vacuum.

Neutrino interferometry is a powerful technique to look for new physics.

Astrophysical neutrino mixing sensitivity reaches to naïve expectation of Planck scale physics. We need more statistics and better particle identification algorithm to find quantum gravity motivated physics.

IceCube-Gen2 collaboration



**Thank you for your attention!**

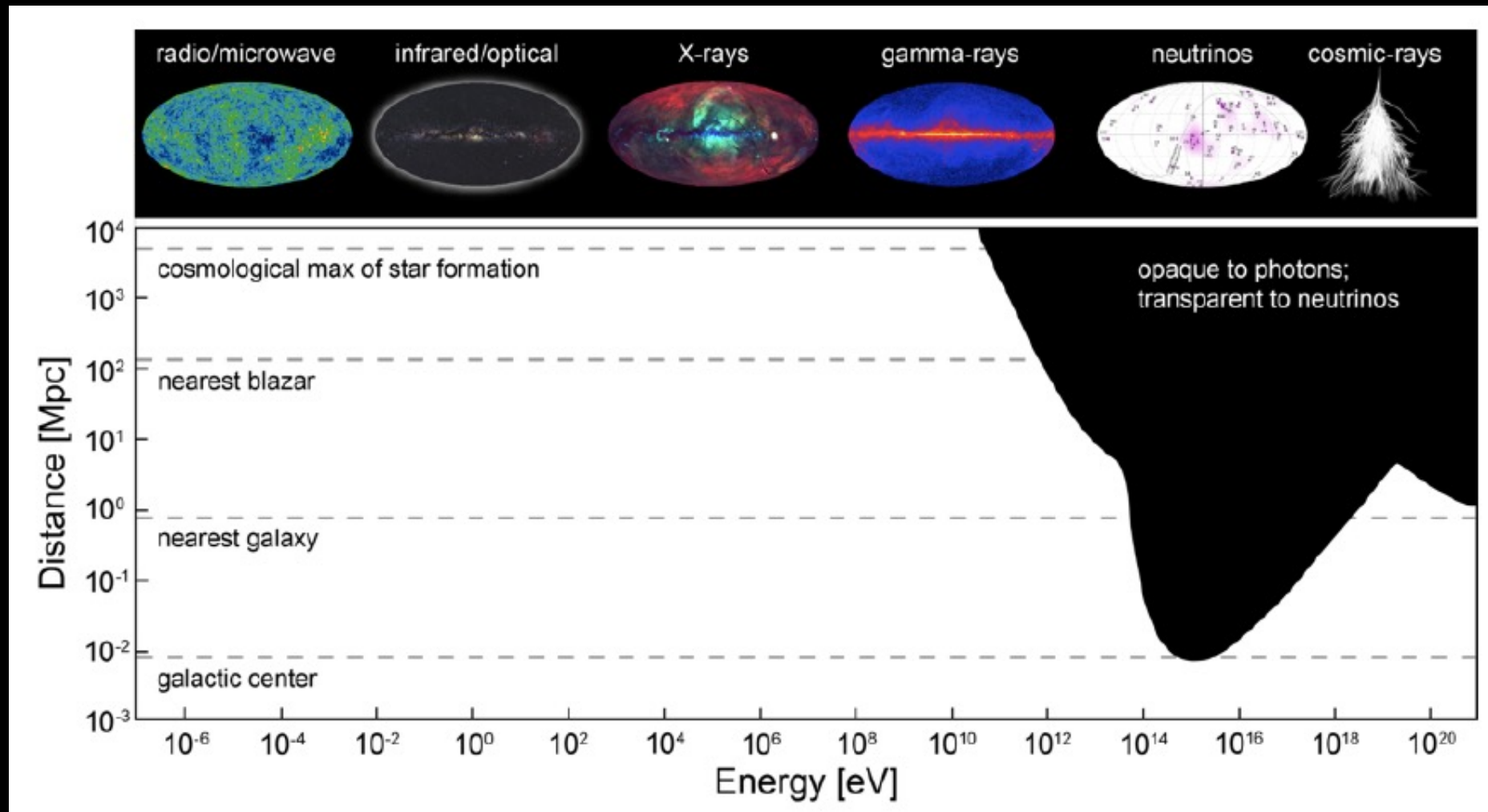
21/09/03



# Backup

## 2. High-energy astrophysical neutrinos

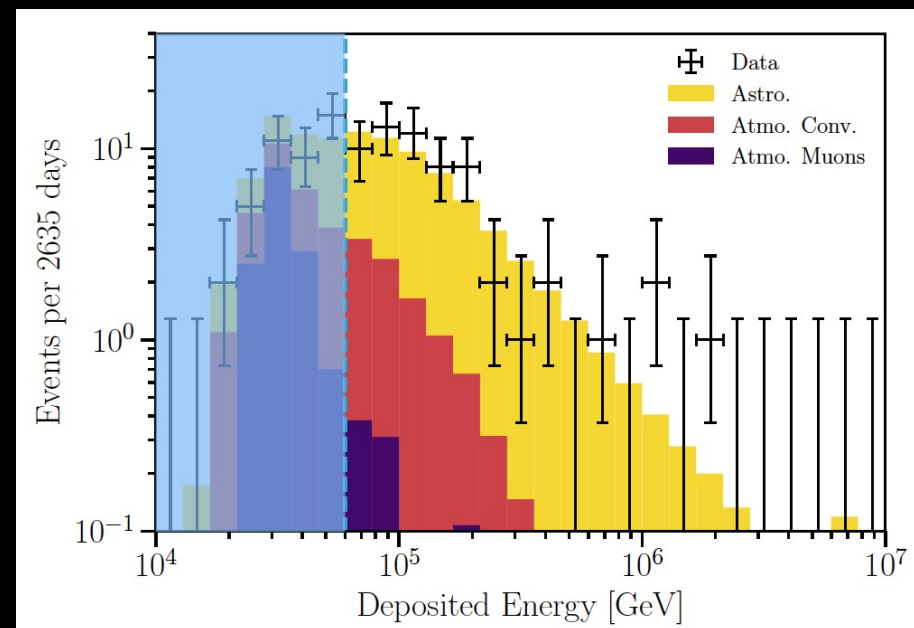
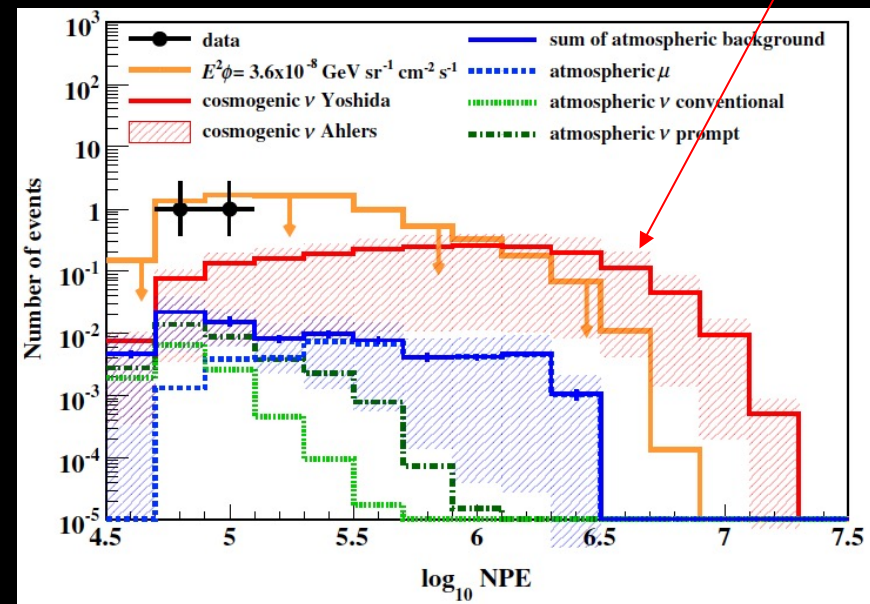
Above  $\sim 100$  TeV, neutrinos are only particles pointing to their high-energy sources



## 2. Astrophysical Very-High-Energy Neutrinos

First observation (2013) by IceCube Neutrino Observatory

- 60-2000 TeV neutrinos
- Too high-energy as atmospheric neutrinos
- Too low-energy as GZK neutrinos

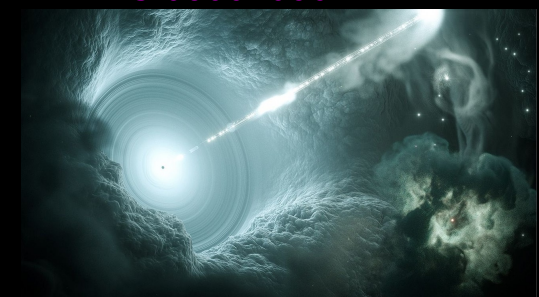


# 2. Astrophysical Very-High-Energy Neutrinos

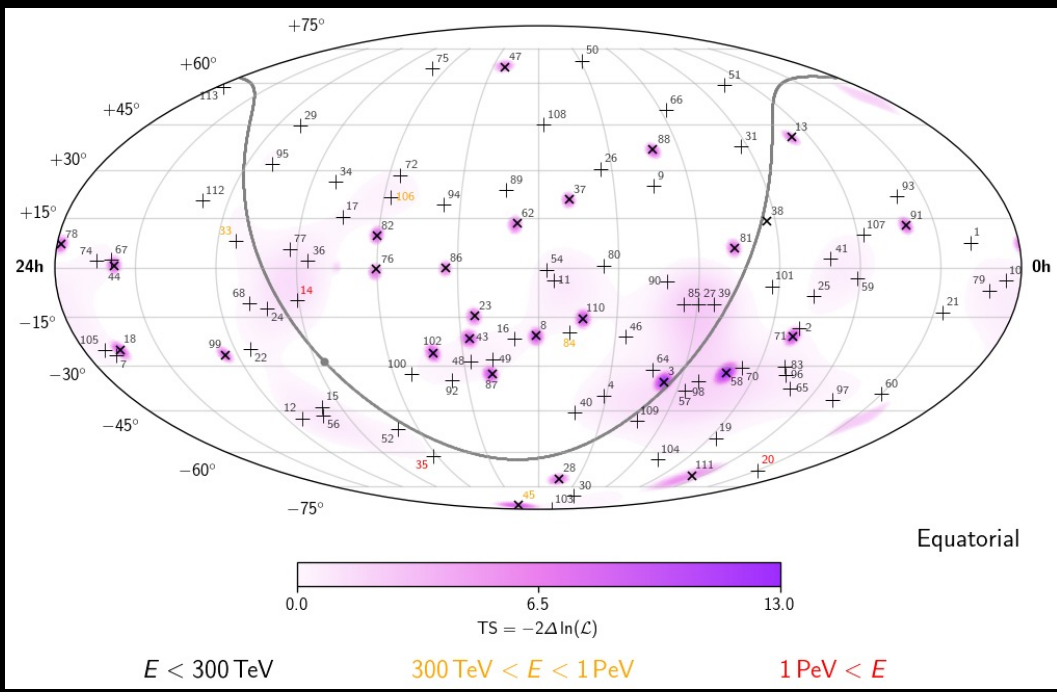
First observation (2013) by IceCube Neutrino Observatory

- 60-2000 TeV neutrinos
- Too high-energy as atmospheric neutrinos
- Too low-energy as GZK neutrinos
- Sources are mostly unknown (diffuse)

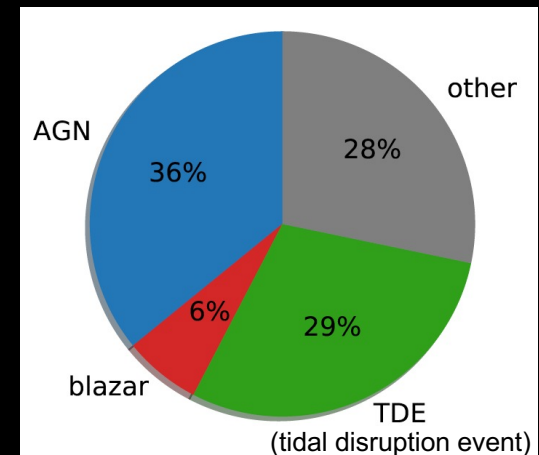
Evidence of Blazar Neutrino  
 - IC170922A  
 - TXS 0506+056



IceCube, Science361(2018)147  
 IceCube et al,(2018)eaat1378



IceCube astrophysical high-energy neutrino source contribution

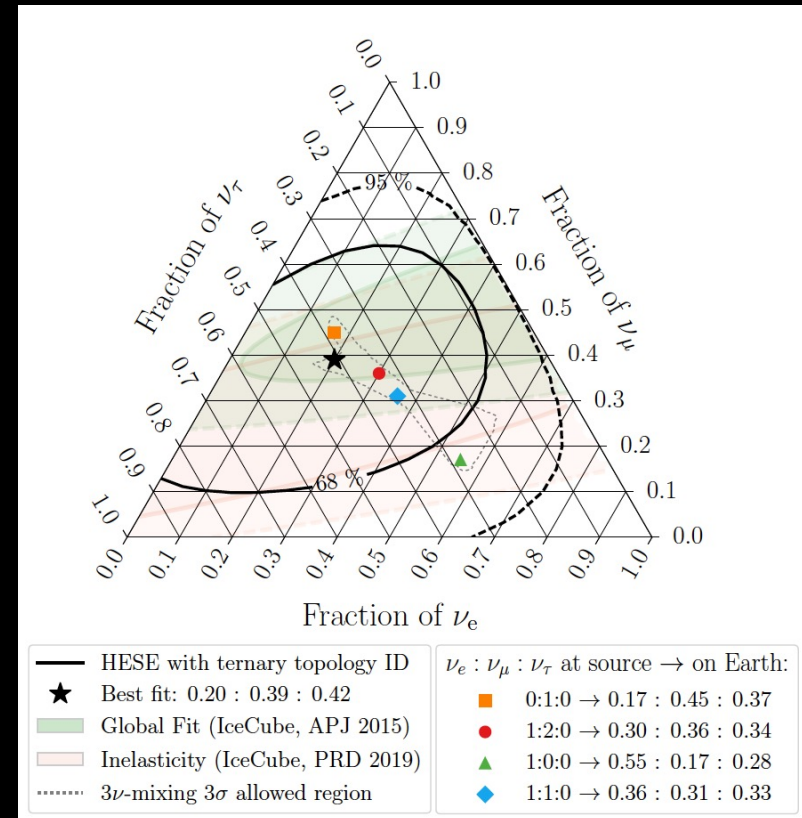
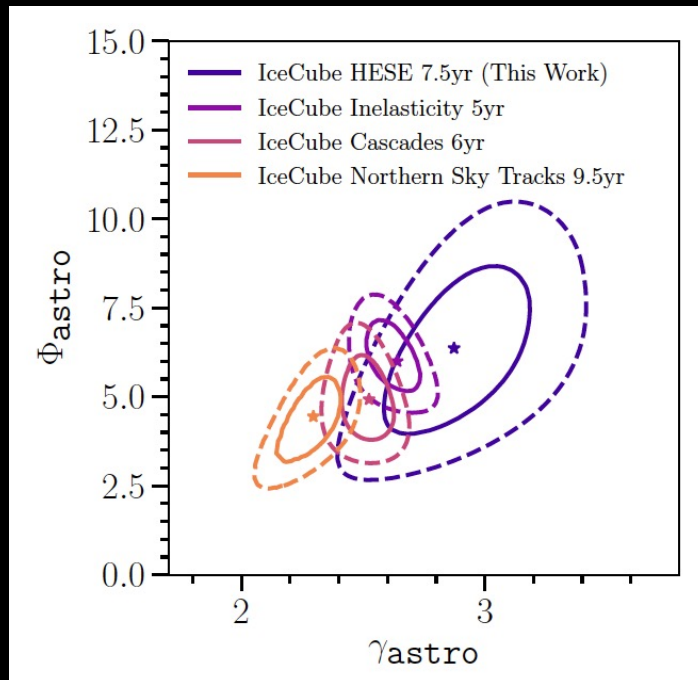


ArXiv:2105.03792

## 2. Astrophysical Very-High-Energy Neutrinos

First observation (2013) by IceCube Neutrino Observatory

- 60-2000 TeV neutrinos
- Too high-energy as atmospheric neutrinos
- Too low-energy as GZK neutrinos
- Sources are mostly unknown (diffuse)
- Large uncertainty on spectrum and flavor structure



# When do we find Lorentz violation???

Higher-dimension operators may be related to new physics

- Dimension-5 operator (unit:  $\text{GeV}^{-1}$ ), example: Majorana mass
- Dimension-6 operator (unit:  $\text{GeV}^{-2}$ ), example: Fermi constant ( $G_F$ )

nonrenormalizable  
 $\longrightarrow$

## SME Lagrangian

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu^{(3)}\psi + \bar{\psi}\gamma^\mu c_{\mu\nu}^{(4)}\partial^\nu\psi \dots$$

## SME motivated effective Hamiltonian for neutrinos

$$h_{eff} \sim \frac{1}{2E} M^2 + V_{CC} + a^{(3)} + E c^{(4)} + E^2 a^{(5)} + E^3 c^{(6)} \dots$$

$\longrightarrow$  nonrenormalizable

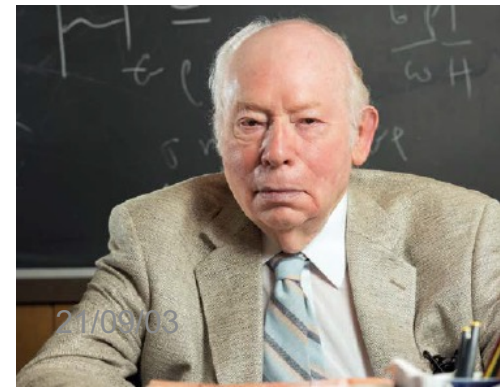
We focus on higher-dimension Lorentz violating operator search

If, Lorentz violation is related to Planck scale physics, it is suppressed inverse of Planck energy,  $1/E_{\text{Planck}}^2 \sim 10^{-38} \text{ GeV}^{-2}$   
 $\rightarrow$  natural scale of dimension-6 Lorentz violating operator

Limits from this operator by atmospheric neutrino is  $\sim 10^{-36} \text{ GeV}^{-1}$

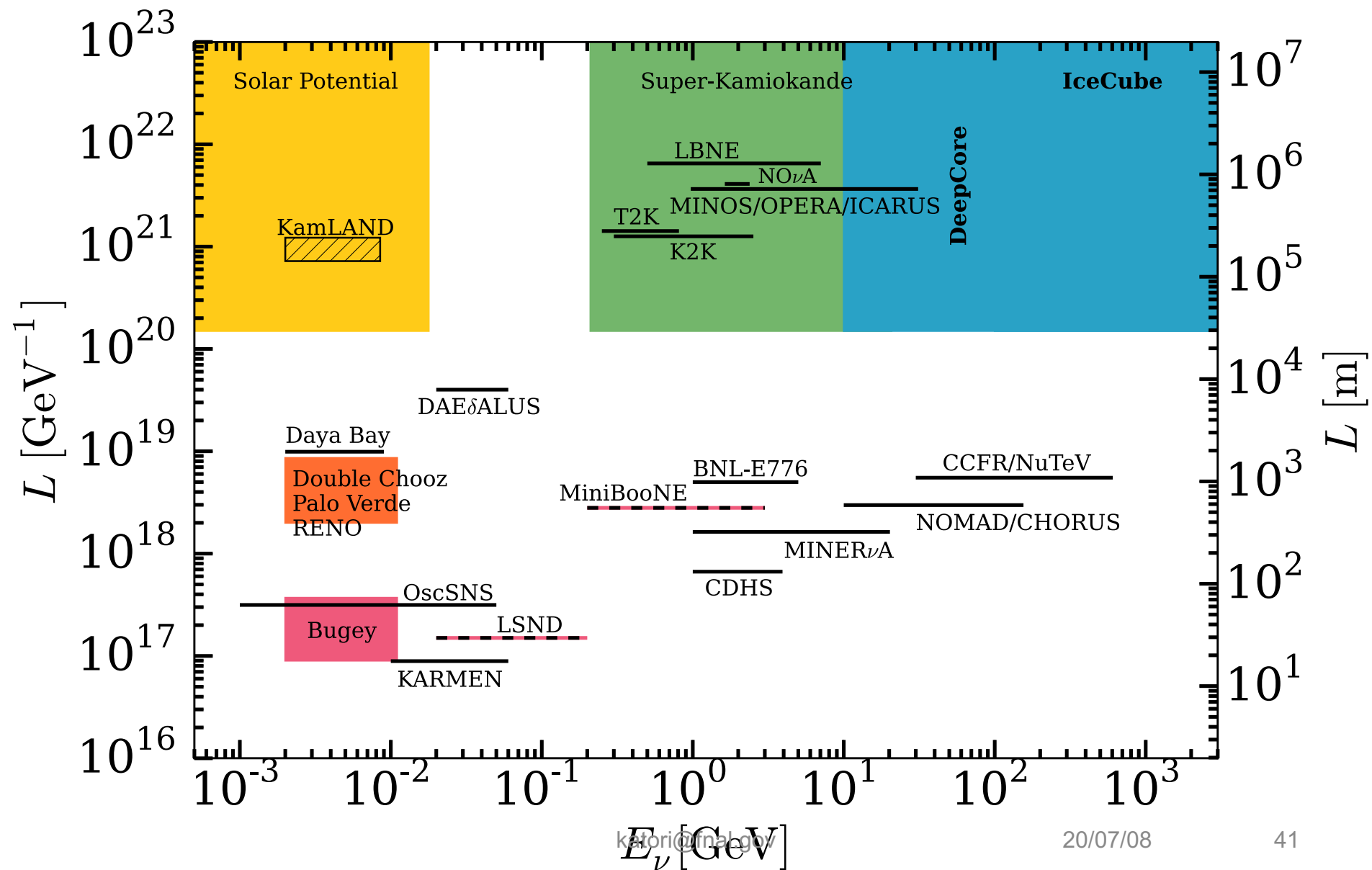
“In a sense it is beyond the SM, but I would rather say it is beyond the leading terms – the renormalizable, unsuppressed part of the SM,” says Weinberg. “But hell – so is gravity! The symmetries of general relativity don’t allow any renormalizable interactions of massless spin-2 particles called gravitons.”

Steve Weinberg  
 (CERN Courier, Nov 2017)



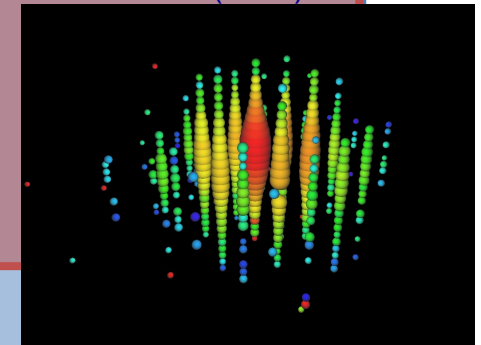


# Lorentz violation with neutrino oscillations

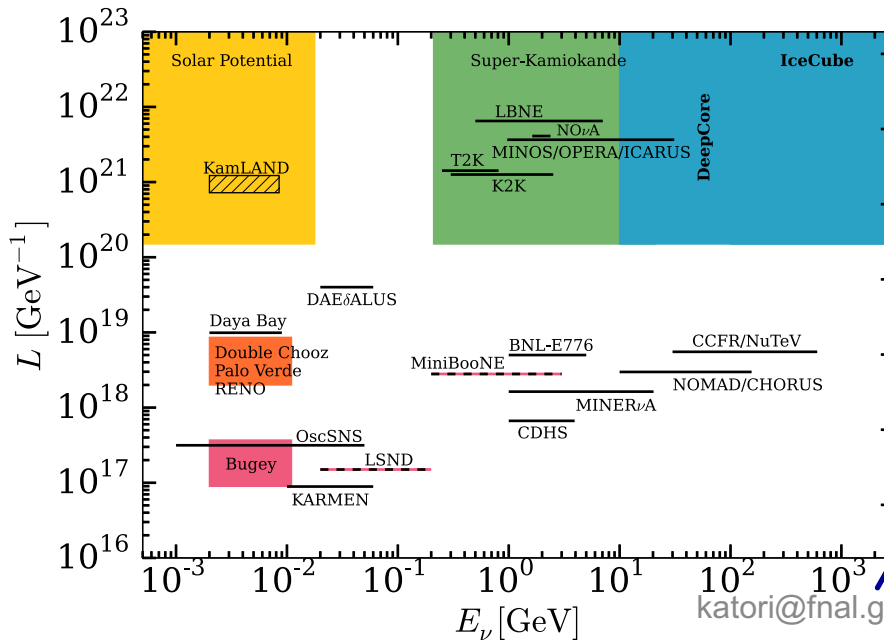


# Lorentz violation with neutrino oscillation

## extra galactic neutrino potential



→  
1Mpc(~Andromeda)



TeV neutrino  
potential

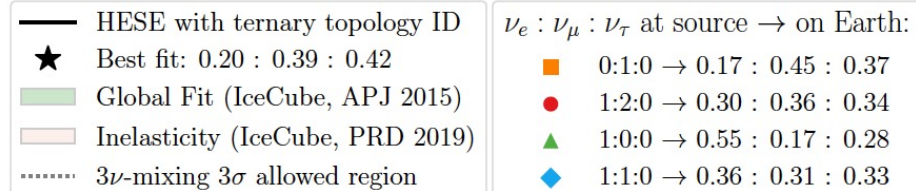
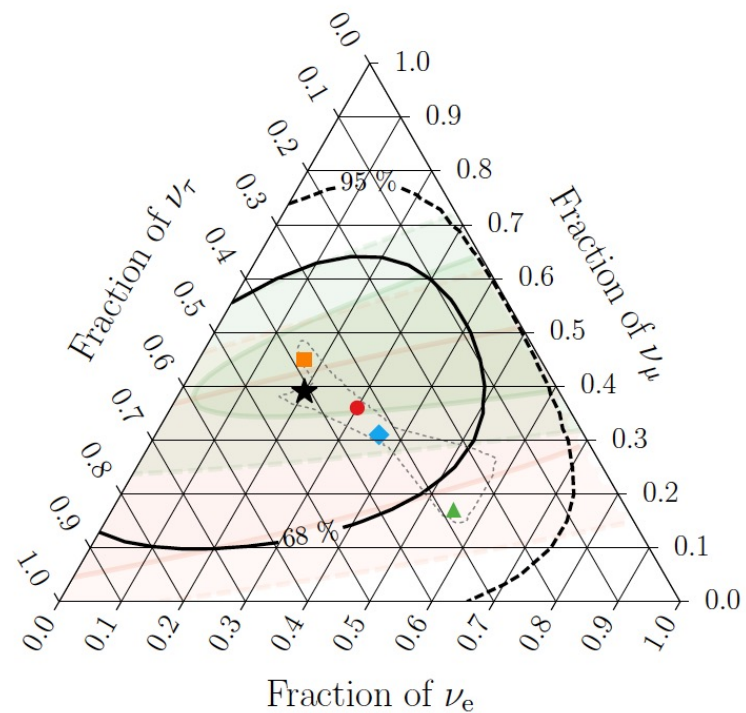
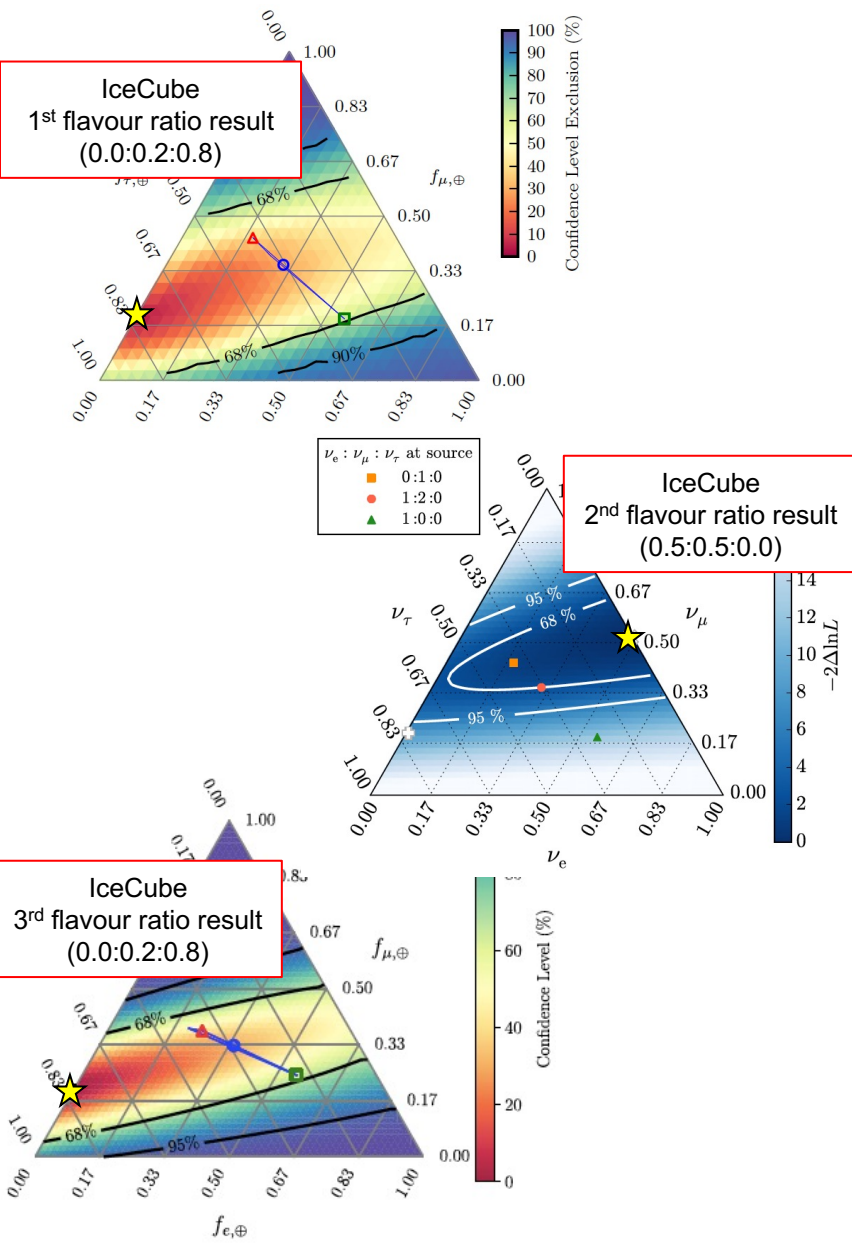
↑ 1TeV

katori@fnal.gov

20/07/08

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## HESE 7.5-yr data (2018)



## New flavour ratio measurement

- Likelihood is very shallow and fit often confuses between  $\nu_e$  and  $\nu_\tau$
- New flavour ratio result has some power to distinguish  $\nu_e$  and  $\nu_\tau$

# Astrophysical neutrino flavor with Lorentz violation

We start from isotropic model of nonminimal SME

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} + E^4 a_{\alpha\beta}^{(7)} - E^5 c_{\alpha\beta}^{(8)} \dots$$

dim-6 isotropic SME (d=6)

$$E^3 c_{\alpha\beta}^{(6)} = E^3 \frac{1}{\sqrt{4\pi}} \left( c_{\alpha\beta}^{(6)} \right)_{00} = E^3 \begin{pmatrix} c_{ee}^{(6)} & c_{e\mu}^{(6)} & c_{\tau e}^{(6)} \\ c_{e\mu}^{(6)*} & c_{\mu\mu}^{(6)} & c_{\mu\tau}^{(6)} \\ c_{\tau e}^{(6)*} & c_{\mu\tau}^{(6)*} & c_{\tau\tau}^{(6)} \end{pmatrix}$$

and so on...

We test dim-3 to dim-8 operators one by one to find nonzero scale (or set limit on scale)

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U - E^3 c_{\alpha\beta}^{(6)} = V^\dagger(E) \Delta V(E)$$

$$V(E) = \begin{pmatrix} V_{e1}(E) & V_{e2}(E) & V_{e3}(E) \\ V_{\mu1}(E) & V_{\mu2}(E) & V_{\mu3}(E) \\ V_{\tau1}(E) & V_{\tau2}(E) & V_{\tau3}(E) \end{pmatrix}, \quad \Delta = \begin{pmatrix} \lambda_1(E) & 0 & 0 \\ 0 & \lambda_2(E) & 0 \\ 0 & 0 & \lambda_3(E) \end{pmatrix}$$

# Astrophysical neutrino flavor with Lorentz violation

Neutrino oscillation formula is written with mixing matrix elements and eigenvalues

$$P_{\alpha \rightarrow \beta}(E, L) = 1 - 4 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin^2 \left( \frac{\lambda_i - \lambda_j}{2} L \right) + 2 \sum_{i>j} \text{Im}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin \left( (\lambda_i - \lambda_j) L \right)$$

However, astrophysical neutrinos propagate  $O(100\text{Mpc}) \rightarrow$  lost coherence

$$P_{\alpha \rightarrow \beta}(E, \infty) \sim 1 - 2 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) = \sum_i |V_{\alpha i}|^2 |V_{\beta i}|^2$$

Astrophysical neutrino flux of flavor  $\alpha$  at production is  $\phi_\alpha^p(E) \sim \phi_\alpha^p \cdot E^{-\gamma}$ . Since it's low statistics, we consider energy-averaged flavor composition  $\beta$  on Earth

$$\bar{\phi}_\beta^\oplus = \frac{1}{\Delta E} \int_{\Delta E} \sum_\alpha P_{\alpha \rightarrow \beta}(E, \infty) \phi_\alpha^p(E) dE$$

We take the fraction of this for each flavor.

$$f_\beta^\oplus = \frac{\bar{\phi}_\beta^\oplus}{\sum_{e,\mu,\tau} \bar{\phi}_\gamma^\oplus}$$

# HESE 7.5-yr Flavor new physics search

Data, 2635 days HESE sample [IceCube, ArXiv: 2011.03545](#)

- 17 track events, 20  $\log(E)$  bins [60 TeV, 10 PeV], 10  $\cos\theta$  bins [-1.0, +1.0 ]
- 41 cascade events, 20  $\log(E)$  bins [60 TeV, 10 PeV], 10  $\cos\theta$  bins [-1.0, +1.0 ]
- 2 double cascades, 20  $\log(E)$  bins [60 TeV, 10 PeV], 10  $\log(L)$  bins [10m, 100m]

## Simulation

[Bhattacharya et al., JHEP06\(2015\)110](#)

- Foregrounds, conventional (Honda flux), prompt (BERSS model), muon (CORSIKA)
- Astrophysical neutrinos, simple power law
- Interaction, NLO PDF DIS (CSMS model) [Cooper-Sarkar et al., JHEP08\(2011\)042](#)

## Systematics (15 nuisance parameters)

- oscillation parameters (6)
- normalization of flux : conventional (40%), prompt (free), muon (50%), astrophysical (free)
- spectrum index : primary cosmic ray (5%) astrophysical neutrinos (free)
- Ice model : (20%)
- DOM efficiency : overall (10%), angular dependence (50%)

## Limits

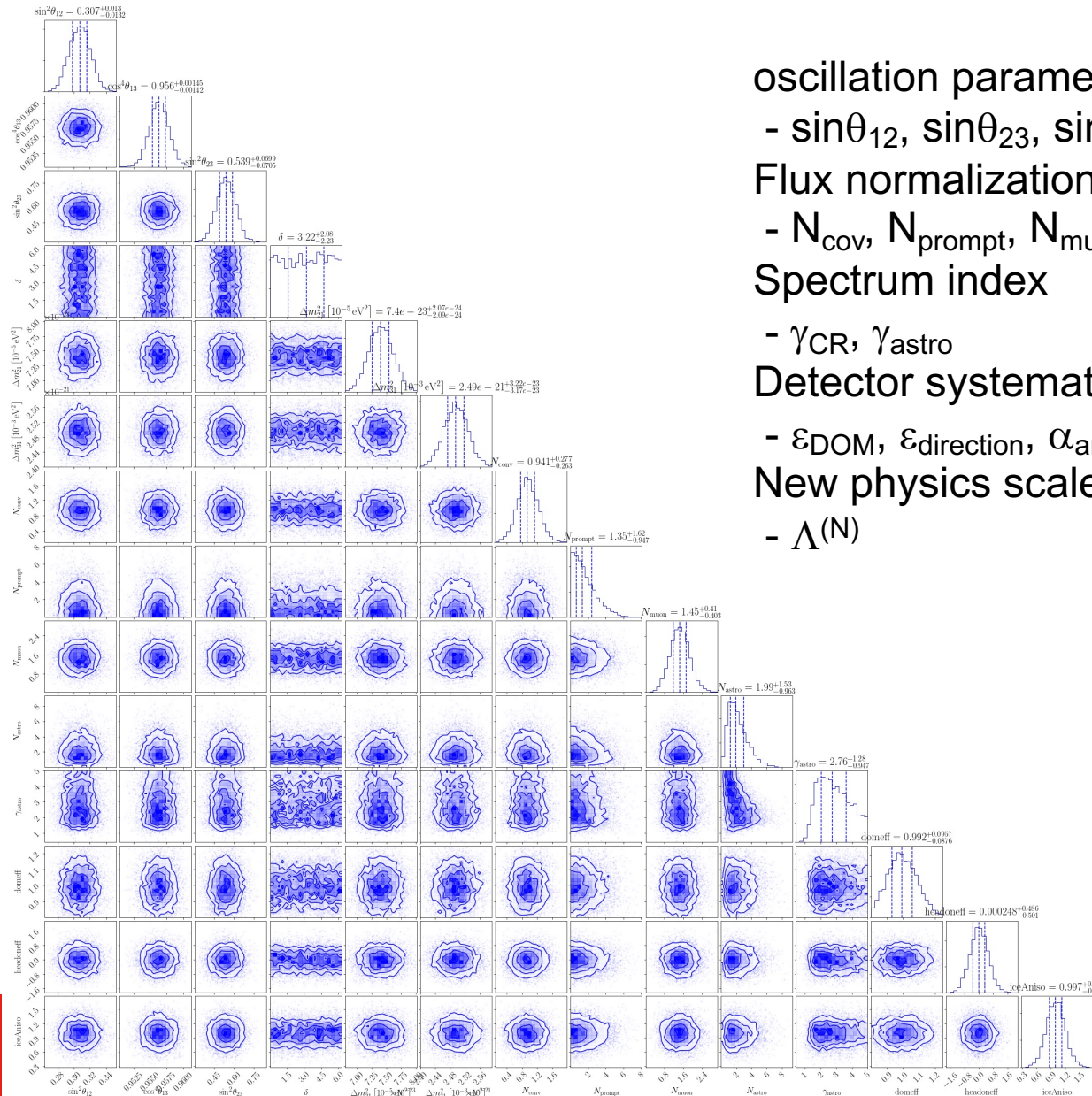
[Feroz et al., Mon. Not. Roy. Astron. Soc. 398,1601\(2009\)1601](#)

- Bayesian: MCMC with Multinest, Bayes factor with Jefferey' scale “strong” limit
- Frequentist: Wilks' theorem

# Systematic errors

| Parameter                              | Prior (constraint) | Range               | Description                             |
|--|--------------------|---------------------|---|
| <b>Astrophysical neutrino flux:</b>    |                    |                     |   |
| $\Phi_{\text{astro}}$                  | -                  | $[0, \infty)$       | Normalization scale                     |
| $\gamma_{\text{astro}}$                | -                  | $(-\infty, \infty)$ | Spectral index                          |
| <b>Atmospheric neutrino flux:</b>      |                    |                     |   |
| $\Phi_{\text{conv}}$                   | $1.0 \pm 0.4$      | $[0, \infty)$       | Conventional normalization scale        |
| $\Phi_{\text{prompt}}$                 | -                  | $[0, \infty)$       | Prompt normalization scale              |
| $R_{K/\pi}$                            | $1.0 \pm 0.1$      | $[0, \infty)$       | Kaon-Pion ratio correction              |
| $2\nu/(\nu + \bar{\nu})_{\text{atmo}}$ | $1.0 \pm 0.1$      | $[0, 2]$            | Neutrino-anti-neutrino ratio correction |
| <b>Cosmic-ray flux:</b>                |                    |                     |   |
| $\Delta\gamma_{\text{CR}}$             | $0.0 \pm 0.05$     | $(-\infty, \infty)$ | Cosmic-ray spectral index modification  |
| $\Phi_{\mu}$                           | $1.0 \pm 0.5$      | $[0, \infty)$       | Muon normalization scale                |
| <b>Detector:</b>                       |                    |                     |   |
| $\epsilon_{\text{DOM}}$                | $0.99 \pm 0.1$     | $[0.80, 1.25]$      | Absolute energy scale                   |
| $\epsilon_{\text{head-on}}$            | $0.0 \pm 0.5$      | $[-3.82, 2.18]$     | DOM angular response                    |
| $a_{\text{s}}$                         | $1.0 \pm 0.2$      | $[0.0, 2.0]$        | Ice anisotropy scale                    |

# Fit example, large new physics in $c_{e\tau}$ (6)



oscillation parameters

- $\sin\theta_{12}$ ,  $\sin\theta_{23}$ ,  $\sin\theta_{13}$ ,  $\Delta m_{12}$ ,  $\Delta m_{23}$ ,  $\delta$

Flux normalization

- $N_{cov}$ ,  $N_{prompt}$ ,  $N_{muon}$ ,  $N_{astro}$

Spectrum index

- $\gamma_{CR}$ ,  $\gamma_{astro}$

Detector systematics

- $\epsilon_{DOM}$ ,  $\epsilon_{direction}$ ,  $\alpha_{anisotropy}$

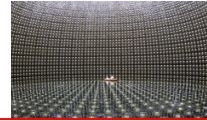
New physics scale

- $\Lambda(N)$



# Test of Lorentz violation with neutrinos

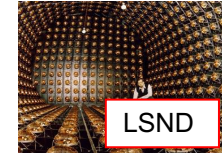
## Spectral distortion



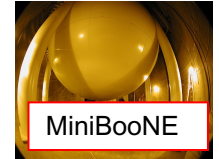
Super-Kamiokande  
PRD91(2015)052003



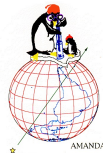
Daya Bay  
PRD98(2018)092013



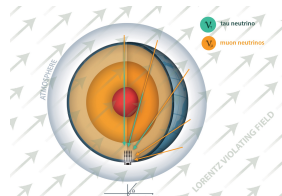
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PRD72(2005)076004



MiniBooNE  
PLB718(2013)1303



AMANDA  
PRD79(2009)102005



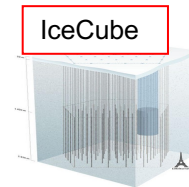
IceCube  
Nature Physics  
14(2018)961



MINOS ND  
PRL101(2008)151601



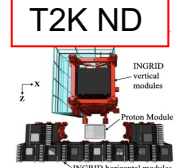
MINOS FD  
PRL105(2010)151601



IceCube  
PRD82(2010)112003

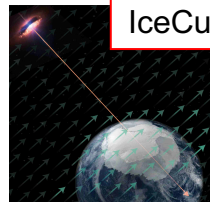


Double Chooz  
PRD86(2013)112009



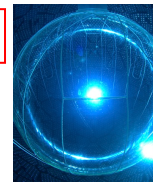
T2K ND  
PRD95(2017)111101

## Flavor ratio



IceCube  
To be published

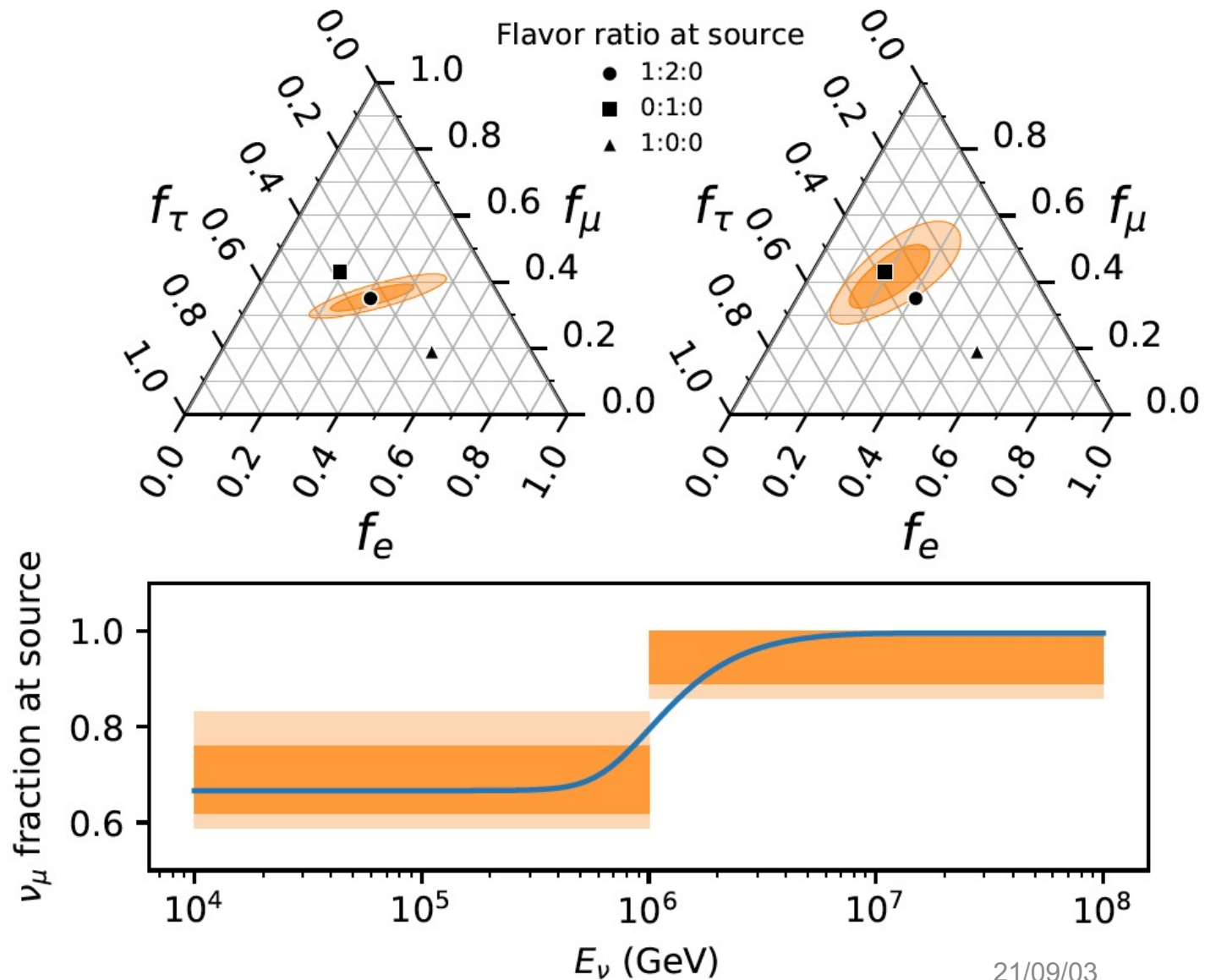
SNO



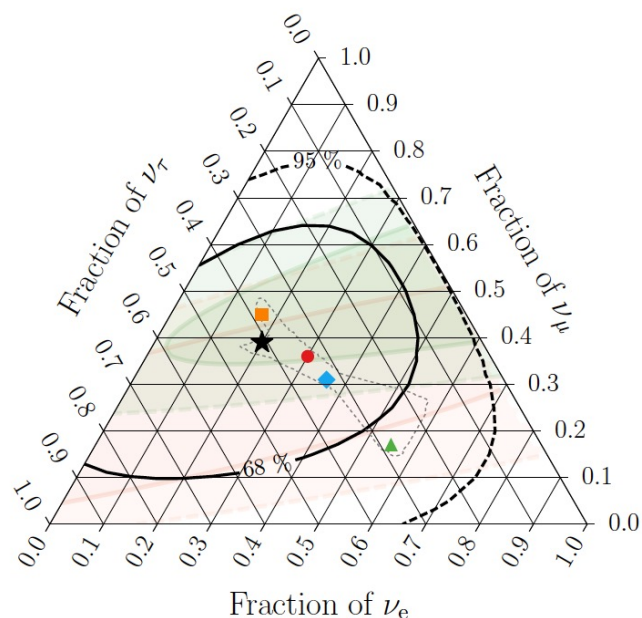
PRD98(2018)112013

## Seasonal variation

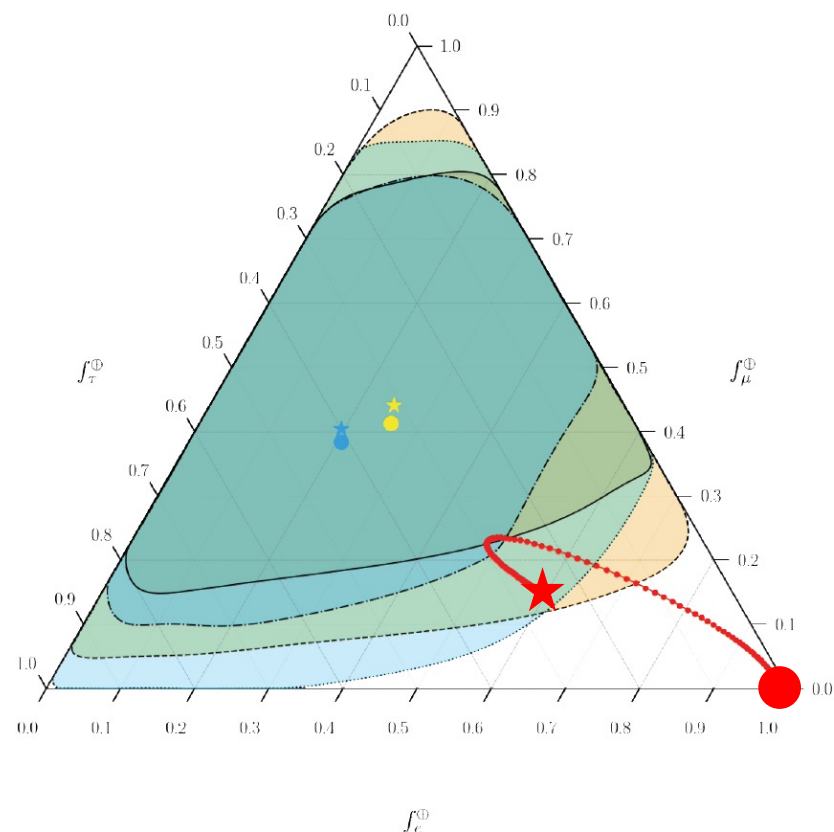
# Energy dependence of flavor ratio



# HESE 7.5-yr flavor new physics search



|   |  |
|---|--|
| — HESE with ternary topology ID           | $\nu_e : \nu_\mu : \nu_\tau$ at source $\rightarrow$ on Earth: |
| ★ Best fit: $0.20 : 0.39 : 0.42$          | ■ $0:1:0 \rightarrow 0.17 : 0.45 : 0.37$                       |
| ■ Global Fit (IceCube, APJ 2015)          | ● $1:2:0 \rightarrow 0.30 : 0.36 : 0.34$                       |
| ■ Inelasticity (IceCube, PRD 2019)        | ▲ $1:0:0 \rightarrow 0.55 : 0.17 : 0.28$                       |
| ⋯ $3\nu$ -mixing $3\sigma$ allowed region | ◆ $1:1:0 \rightarrow 0.36 : 0.31 : 0.33$                       |



e.g.) Initial flavour ratio ★ is  $(1:0:0)$ , and there is nonzero new physics  $c_{\mu\tau}^{(6)}$  term (exotic  $\nu_\mu$ - $\nu_\tau$  mixing). If the new physics term is big, the flavour ratio on Earth is ●

Such model is rejected by current data

# Neutrino Standard Model ( $\nu$ SM) - Unknowns

SM + 3 active massive neutrinos

Neutrinos are least known particles!

There are several unknowns and anomalies

→ Do they indicate new physics?

## Unknown parameters of $\nu$ SM

1. Dirac CP phase
2.  $\theta_{23}$  ( $\theta_{23}=40^\circ$  and  $50^\circ$  are same for  $\sin 2\theta_{23}$ , but not for  $\sin\theta_{23}$ )
3. normal mass ordering  $m_1 < m_2 < m_3$  or inverted mass ordering  $m_3 < m_1 < m_2$
4. Dirac or Majorana
5. Majorana phase
6. Absolute neutrino mass

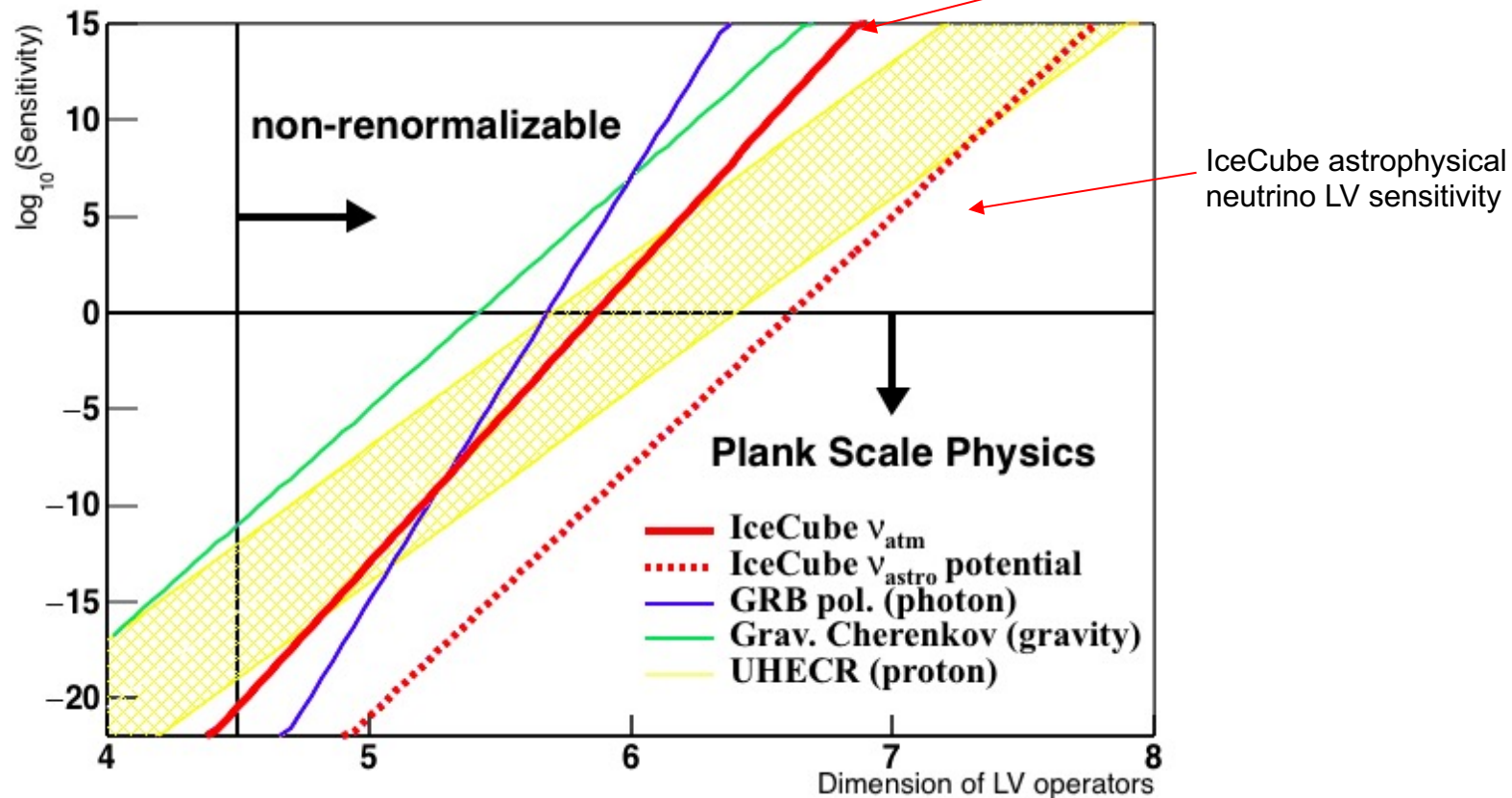
# When do we find Lorentz violation???

Higher-dimension operators may be related to new physics

- Dimension-5 operator (unit:  $\text{GeV}^{-1}$ ), example: Majorana mass
- Dimension-6 operator (unit:  $\text{GeV}^{-2}$ ), example: Fermi constant ( $G_F$ )

IceCube atmospheric  
neutrino LV sensitivity  
[Nature Physics 14\(2018\)961](#)

New physics limits and projected sensitivity



Astrophysical neutrino dim-6 LV operator search can reach quantum gravity motivated region ( $\sim 1/M_{\text{Planck}}^2 \sim 10^{-38} \text{ GeV}^{-2}$ ) 21/09/03