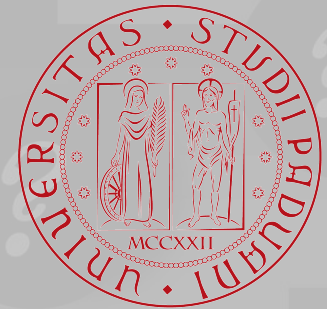


# Higgs couplings and naturalness

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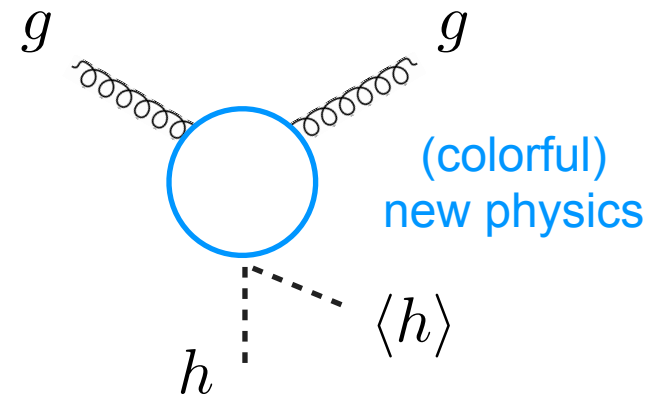
5th FCC Physics Workshop  
February 7, 2022

# Higgs naturalness solved by symmetry?

- New states near the weak scale that contribute to Higgs **mass**...

$$m_h^2 \sim \text{---} h \text{---} \text{---} \text{SM} \text{---} h \text{---} + \text{---} h \text{---} \text{---} \text{new physics} \text{---} h \text{---} \Lambda$$

... should modify Higgs **couplings** too: for instance



- Higgs coupling measurements as probe of naturalness

# Higgs couplings as probe of naturalness

- Connection is robust, but with important quantitative variations

correction to  
on-shell couplings

$$\frac{\delta g_h}{g_{h,\text{SM}}} \sim \frac{g_*^2}{\Lambda^2} v^2$$

$g_*$  new physics coupling

$\Lambda$  new physics mass scale

For fixed BSM mass, effects are enhanced at strong coupling

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$g_*$  new physics coupling

$\Lambda$  new physics mass scale

## Weakly coupled solutions (supersymmetry)

$$g_* \sim g_{\text{SM}}$$



$$c_{hff} = 1 \pm O\left(\frac{m_Z^2}{m_A^2}\right)$$

mass of second  
Higgs doublet

$$c_{hVV} = 1 - O\left(\frac{m_Z^4}{m_A^4}\right)$$

very small



# Higgs couplings as probe of naturalness

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$$\frac{\delta g_h}{g_{h,\text{SM}}} \sim \frac{g_*^2}{\Lambda^2} v^2$$

$g_*$  new physics coupling

$\Lambda$  new physics mass scale

## Strongly coupled solutions (Higgs as composite pseudo-Goldstone boson)

$$g_* \gg g_{\text{SM}}$$

$$\Lambda \sim g_* f$$



$$c_{hVV} = 1 - \frac{v^2}{2f^2}$$

Higgs “decay constant”  
(think of  $f_\pi$  in chiral Lagrangian)

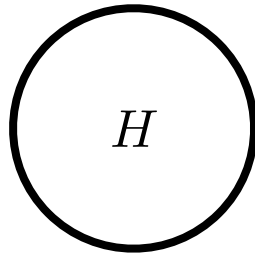
$$c_{hff} = 1 - O\left(\frac{v^2}{f^2}\right) \quad \text{more model-dependent}$$



# Higgs as composite Goldstone boson

[Kaplan, Georgi 1984]  
[Kaplan 1992]  
[Agashe, Contino, Pomarol 2004]

strongly-interacting  
sector



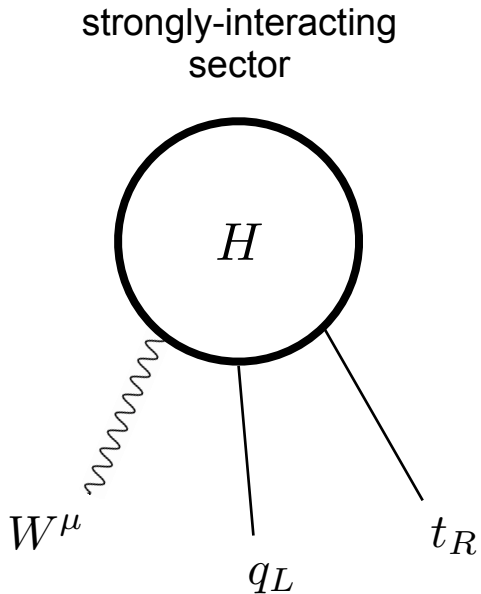
Tree level: Goldstone shift symmetry

$$H \rightarrow H + \epsilon \quad \longrightarrow \quad V(H) = 0$$

$m_h \ll \Lambda$  is natural

# Higgs as composite Goldstone boson

[Kaplan, Georgi 1984]  
[Kaplan 1992]  
[Agashe, Contino, Pomarol 2004]



One loop: potential is generated by SM fields

$$V \sim -\alpha f^2 \sin^2 \frac{h}{f} + \beta f^2 \sin^4 \frac{h}{f}$$



realistic vacuum needs some residual fine-tuning

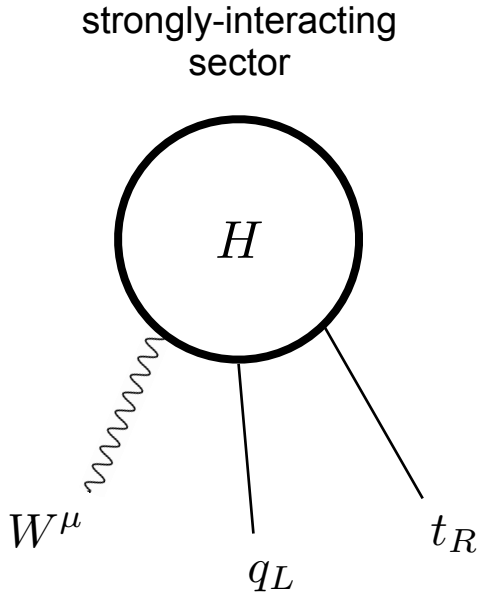
$$\Delta = \frac{(\alpha/\beta)_{\text{required}}}{(\alpha/\beta)_{\text{expected}}} = \frac{2v^2/f^2}{1} \ll 1$$

(also called “minimal tuning”; some models need stronger cancellations)

[e.g. Panico, Wulzer 2015]

# Higgs as composite Goldstone boson

[Kaplan, Georgi 1984]  
 [Kaplan 1992]  
 [Agashe, Contino, Pomarol 2004]



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$$\Delta = \frac{(\alpha/\beta)_{\text{required}}}{(\alpha/\beta)_{\text{expected}}} = \frac{2v^2/f^2}{1} \ll 1$$

• Therefore  $c_{hVV} = 1 - \frac{v^2}{2f^2} = 1 - \frac{\Delta}{4}$

“sharp” sense in which Higgs coupling measurements probe fine tuning



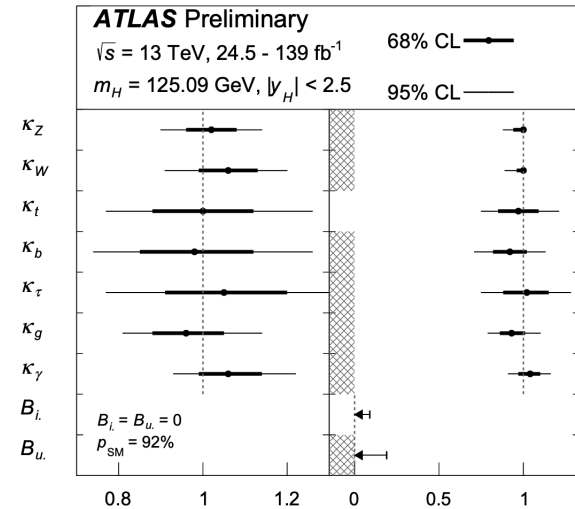
# LHC: present and future

[ATLAS-CONF-2020-027]  
[CMS-PAS-HIG-19-005]

- Run 2:

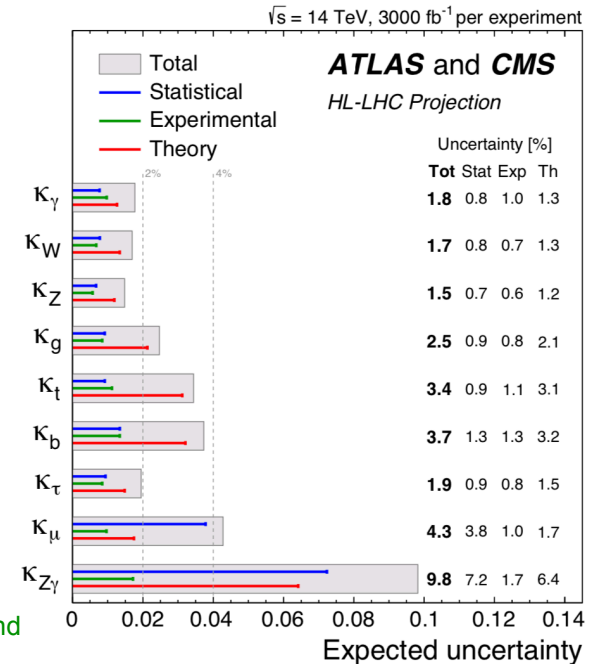
$$c_{hVV} \gtrsim 0.9 \quad \rightarrow \quad \Delta \lesssim 30\%$$

(approx 95% CL)



- High Luminosity: uncertainties in 1.5 - 4% range

$$f > 1 \text{ TeV} \quad \rightarrow \quad \Delta \lesssim 10\%$$



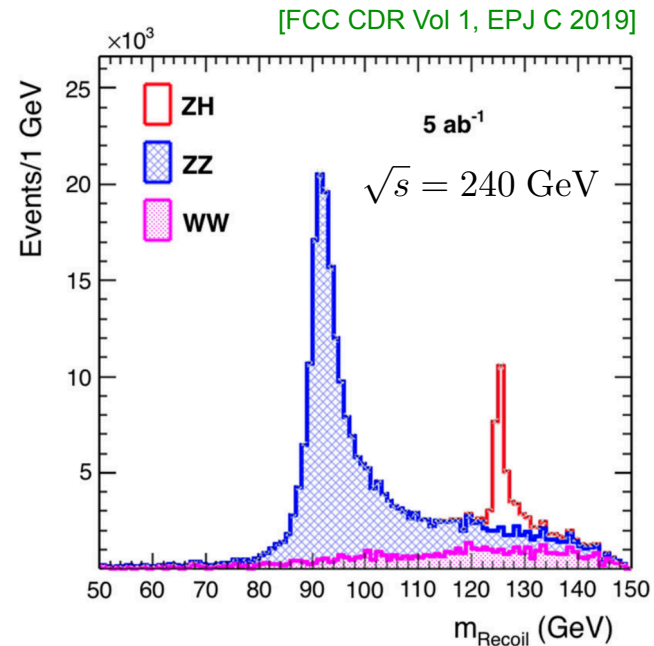
[Higgs physics @ HL- and HE-LHC, 1902.00134]

# FCC-ee

- Explore **one order of magnitude** in fine tuning:

$$f > 3 \text{ TeV} \quad \rightarrow \quad \Delta \lesssim 1 \%$$

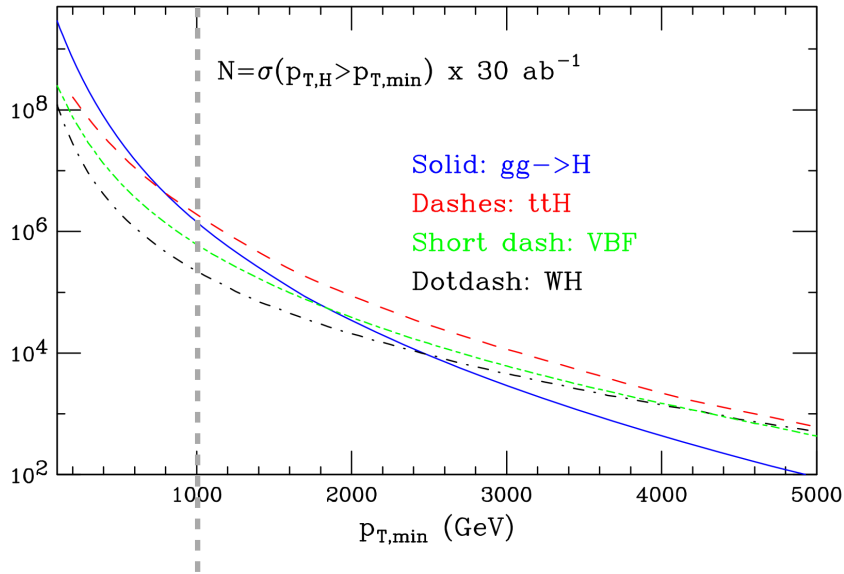
(95% CL)



Collider	HL-LHC	ILC <sub>250</sub>	CLIC <sub>380</sub>	LEP <sub>3240</sub>	CEPC <sub>250</sub>	FCC-ee <sub>240+365</sub>	(68% CL)	
Lumi ( $\text{ab}^{-1}$ )	3	2	1	3	5	5 <sub>240</sub> + 1.5 <sub>365</sub>	+ HL-LHC	
Years	25	15	8	6	7	3 + 4		
$\delta\Gamma_{\text{H}}/\Gamma_{\text{H}}$ (%)	SM	3.6	4.7	3.6	2.8	2.7	<b>1.3</b>	1.1
$\delta g_{\text{HZZ}}/g_{\text{HZZ}}$ (%)	1.5	0.3	0.60	0.32	0.25	0.2	<b>0.17</b>	0.16

# FCC-hh

[FCC CDR Vol 1, EPJ C 2019]

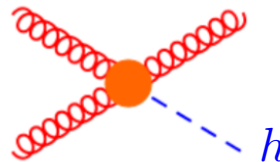


- Program is fully complementary to FCC-ee
- Probes high -  $q^2$  region with unprecedented sensitivity



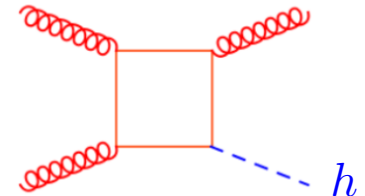
~ FCC-ee statistics,  
but above 1 TeV!

$$H^\dagger H G_{\mu\nu}^a G^{\mu\nu a}$$



$$\mathcal{M} \sim s$$

$$H^\dagger H \bar{q}_L \tilde{H} t_R$$



tell apart  
from

$$\mathcal{M} \sim \log^2 \frac{s}{m_t^2}$$

[Grojean, Salvioni, Schlaffer, Weiler 2013]

[Banfi, Martin, Sanz 2013]

[Azatov, Paul 2013]

...

# More FCC-hh

- 1% measurement of  $g_{htt}$  coupling, exploiting ratio  $\sigma(t\bar{t}h)/\sigma(t\bar{t}Z)$  to reduce systematics

[Mangano, Plehn, Reimitz, Schell, Shao 2015]

- Very important for composite Higgs framework, where most promising models (tuning, EW precision) single out with **maximal size** the operators

$$\frac{1}{f^2} \partial_\mu |H|^2 \partial^\mu |H|^2$$



$$c_{hVV} = 1 - \frac{v^2}{2f^2}$$



$$\frac{1}{f^2} y_t H^\dagger H \bar{q}_L \tilde{H} t_R$$



$$c_{htt} = 1 - O\left(\frac{v^2}{f^2}\right)$$

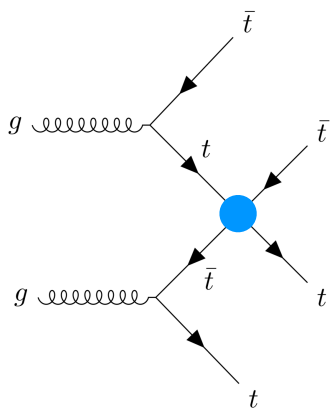
$$\frac{1}{f^2} (\bar{t}_R \gamma^\mu t_R)^2$$

# More FCC-hh

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[Mangano, Plehn, Reimitz, Schell, Shao 2015]

- Very important for composite Higgs framework, where most promising models (tuning, EW precision) single out with **maximal size** the operators



$$\mathcal{M} \sim \frac{s}{f^2}$$

grows with energy

$$\frac{1}{f^2} (\bar{t}_R \gamma^\mu t_R)^2$$

Expected sensitivity from 4-top production @ FCC-hh:

$$f > 6.5 \text{ TeV}$$



key complementary observable

[Banelli, Salvioni, Serra, Theil, Weiler 2020]

# Where are the top partners?

- Top partners not too far above weak scale are essential for naturalness
- In “classic” scenarios, direct searches for **color-charged particles** are important tests (top squarks, vector-like quarks)

[Matsedonskyi, Panico, Wulzer 2012]  
[Pomarol, Riva 2012]

- Concretely: in composite Higgs, observed Higgs mass requires  $M_T \lesssim 1.5 f$

$$M_T \approx 2 \text{ TeV}$$

HL-LHC direct reach



$$f \gtrsim 1.2 \text{ TeV}$$

“equivalent” reach,  
comparable to Higgs couplings

# Where are the top partners?

- Top partners not too far above weak scale are essential for naturalness
- In “classic” scenarios, direct searches for **color-charged particles** are important tests (top squarks, vector-like quarks)
- In **neutral naturalness models**, top partners are color-less

[Chacko, Goh, Harnik 2005]  
and many more

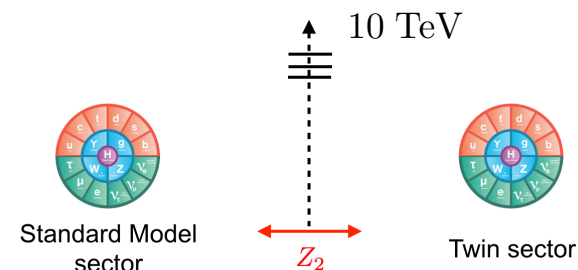
Twin Higgs:

➔ “Twin top” is light, but fully neutral under Standard Model

➔ new color-charged states can be close to  $4\pi f \gtrsim 10 \text{ TeV}$

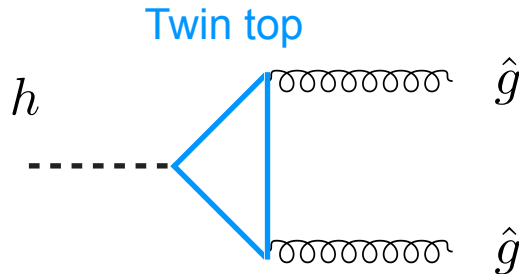
➔ direct discovery may need to wait for FCC-hh

$$m_{\hat{t}} = \frac{y_t f}{\sqrt{2}}$$



# Higgs $\rightarrow$ invisible decays

- In Twin Higgs there is an “irreducible” contribution from  $h \rightarrow$  Twin gluons



$$\text{BR}(h \rightarrow \hat{g}\hat{g}) \approx \left(\frac{v}{f}\right)^4 \text{BR}(h \rightarrow gg)$$

(invisible width can be larger, depending on twin fermion masses)

[Borgonovi et al.  
CERN-ACC-2018-0045]

$$\text{BR}(h \rightarrow \text{inv}) < 2.5 \times 10^{-4}$$

FCC-hh



$$f \gtrsim 1.1 \text{ TeV}$$

- Many striking **visible** signals are possible (and model-dependent):

Higgs exotic decays probe neutral naturalness

[Craig, Katz, Strassler, Sundrum 2015]



# Higgs cubic coupling

- HL-LHC has first sensitivity (50% on  $c_{hhh}$ , at 68% CL)
- FCC-ee will improve via loop effects (20%)
- FCC-hh will truly pin it down (7%)
- **Models of Higgs naturalness** usually do not predict parametrically larger deviations in  $c_{hhh}$  than in single Higgs couplings

[de Blas et al. 1905.03764]

# Higgs cubic coupling

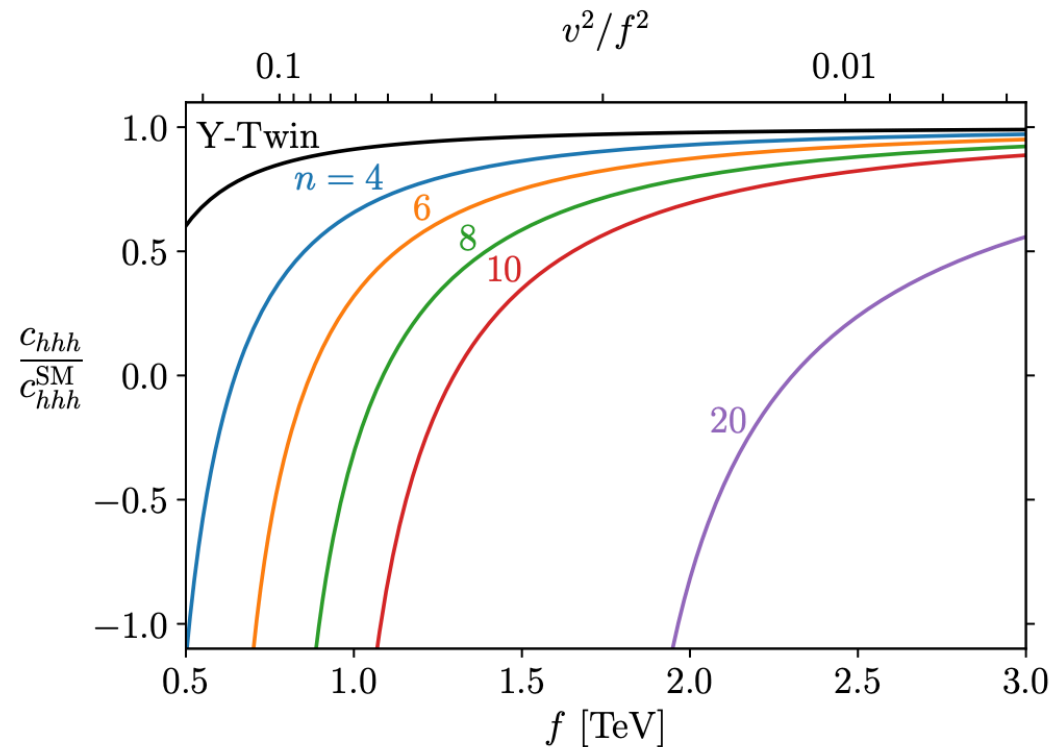
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- **Models of Higgs naturalness** usually do not predict parametrically larger deviations in  $c_{hhh}$  than in single Higgs couplings
  
- There are exceptions: “Gegenbauer’s Twin” [Durieux, McCullough, Salvioni 2202.01228]
  
- Twin Higgs model where explicit  $SO(8)$  breaking arises from higher-dimensional irreps  
➔ (part of) Higgs potential is Gegenbauer polynomial,  $v \ll f$  natural

# Higgs cubic coupling

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- FCC-ee will improve via loop effects (20%)
- FCC-hh will truly pin it down (7%)

[de Blas et al. 1905.03764]

- Parametrically enhanced deviations in cubic self-coupling



[Durieux, McCullough, Salvioni 2202.01228]

# Conclusion

- HL-LHC + FCC program will be **extraordinary probe of Higgs naturalness**.

Push minimal fine tuning from few  $10^{-1}$   $\rightarrow$  few  $10^{-3}$ , if no discovery


- If top partners are color-less, as in neutral naturalness models, resonance detection could be possible only at FCC-hh.

Until then (and after), **measuring Higgs properties is key to progress**


- Could not do justice to many more interesting theory ideas and their tests, nor characterization in presence of deviations from Standard Model

# **Supplementary material**

# Higgs $\rightarrow$ invisible, above threshold

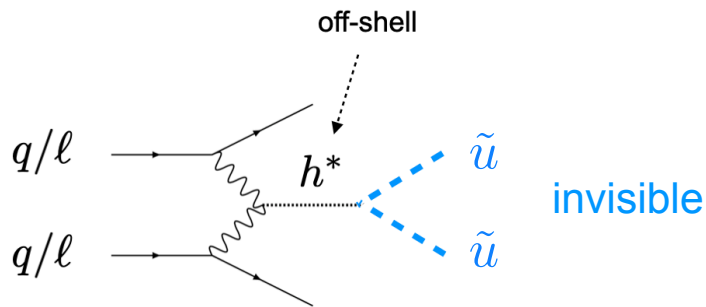
- Neutral naturalness models where Higgs is pseudo-Goldstone boson predict coupling corrections  $\sim v^2/(2f^2)$   allows for robust test
- In models where this is absent, may need to probe naturalness cancellation directly:

$$\mathcal{L} = -y_t^2 |\tilde{u}_1|^2 |H|^2 - y_t^2 |\tilde{u}_2|^2 |H|^2$$

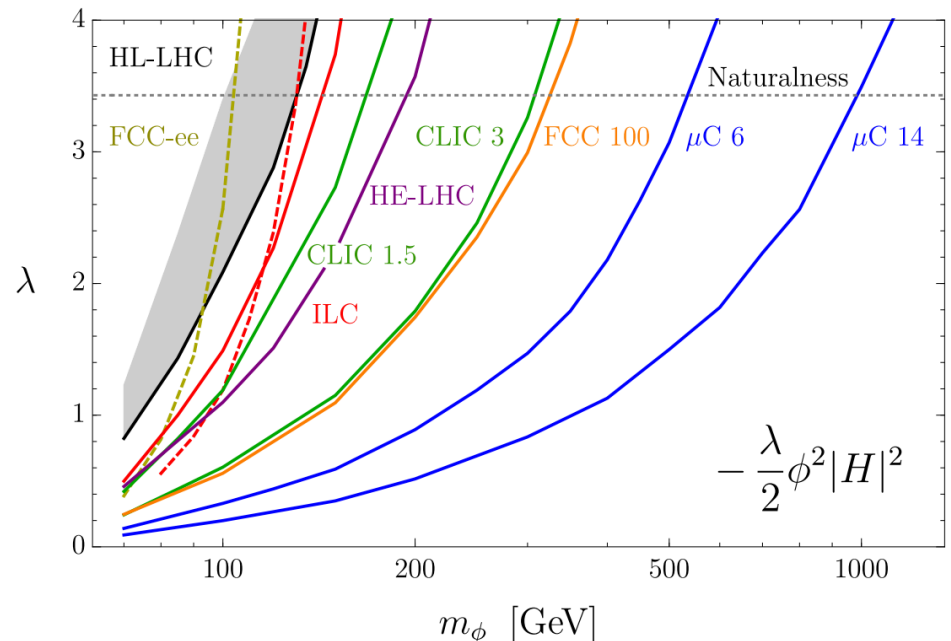
  
Standard Model-singlet  
scalar top partners

# Higgs $\rightarrow$ invisible, above threshold

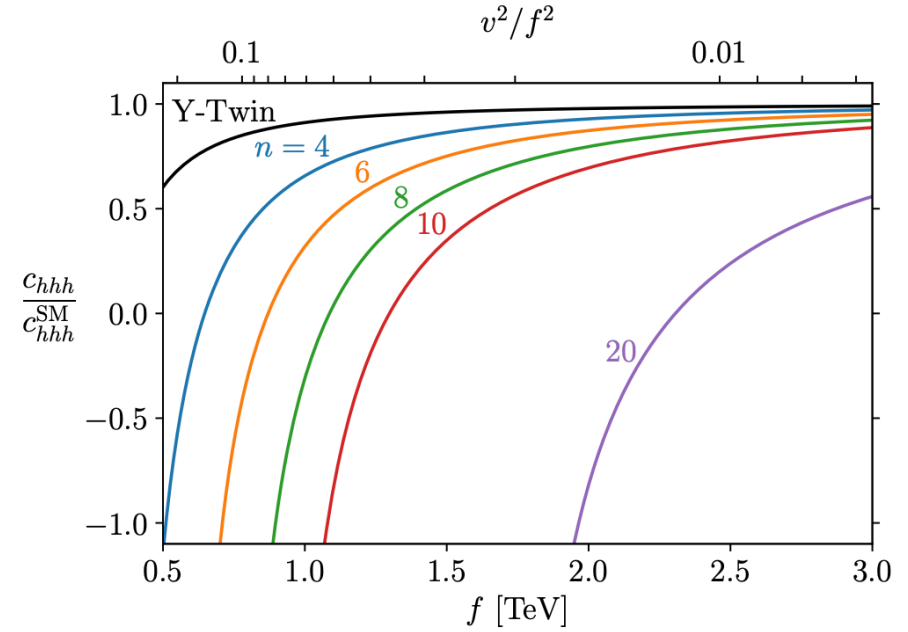
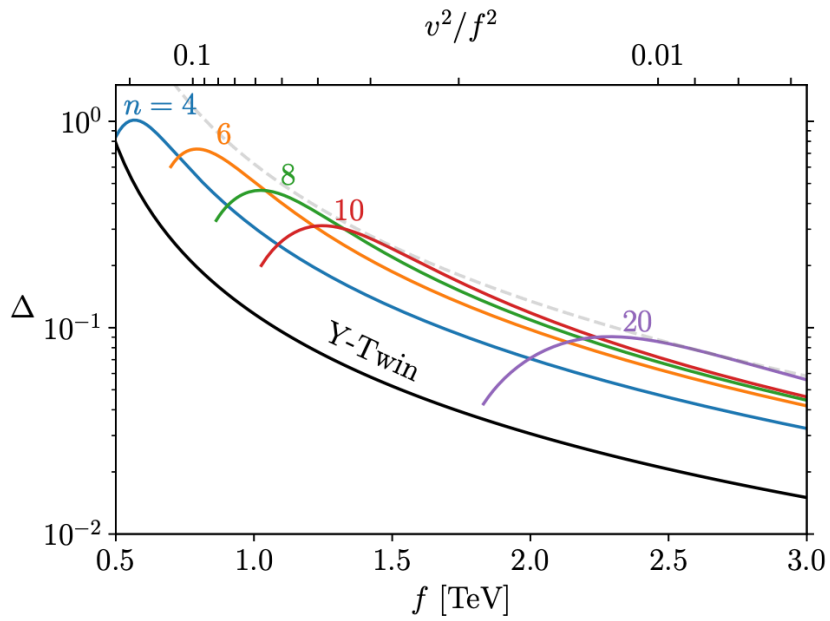
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- In models where this is absent, may need to probe naturalness cancellation directly:



**FCC-hh:**  $m_{\tilde{u}} > 330$  GeV



# Gegenbauer's Twin



[Durieux, McCullough, Salvioni 2202.01228]