

Seeing $H, A \rightarrow$ SUSY in natural SUSY at FCC-hh

H. Baer, V. Barger, R. Jain, C. Kao, D. Sengupta and X. Tata
arXiv:2112.02232

Why FCC-hh is the right machine for future of HEP and CERN

- Regarding colliders, energy (almost) always wins for discovery
- Expanding tunnel from 27km \rightarrow 100 km is most conservative option
- If magnet development 8 T \rightarrow 16 T fails (magnet reliability over 5-30 years), can still place reliable 8T magnets in new tunnel and get a 50 TeV collider :)
- If magnet development succeeds, then get 75-100 TeV!
- To discover gluinos, stops: need $\sqrt{s} > \sim 30$ TeV in natural SUSY (DEW < 30)

HB, Barger, Gainer, Sengupta, Serce, Tata, arXiv:1808.04844

Status of SUSY in the 21st century

- 20th century: expect $m(\text{sparticles}) \sim m(W) \sim 100$ GeV (naturalness)
- computed finetuning in models like mSUGRA/CMSSM: BUT EFT parameters correlated in more UV-complete models e.g. strings: finetuning overestimated by large factors 10–100

HB, Barger, Mickelson, arXiv:1309.2984

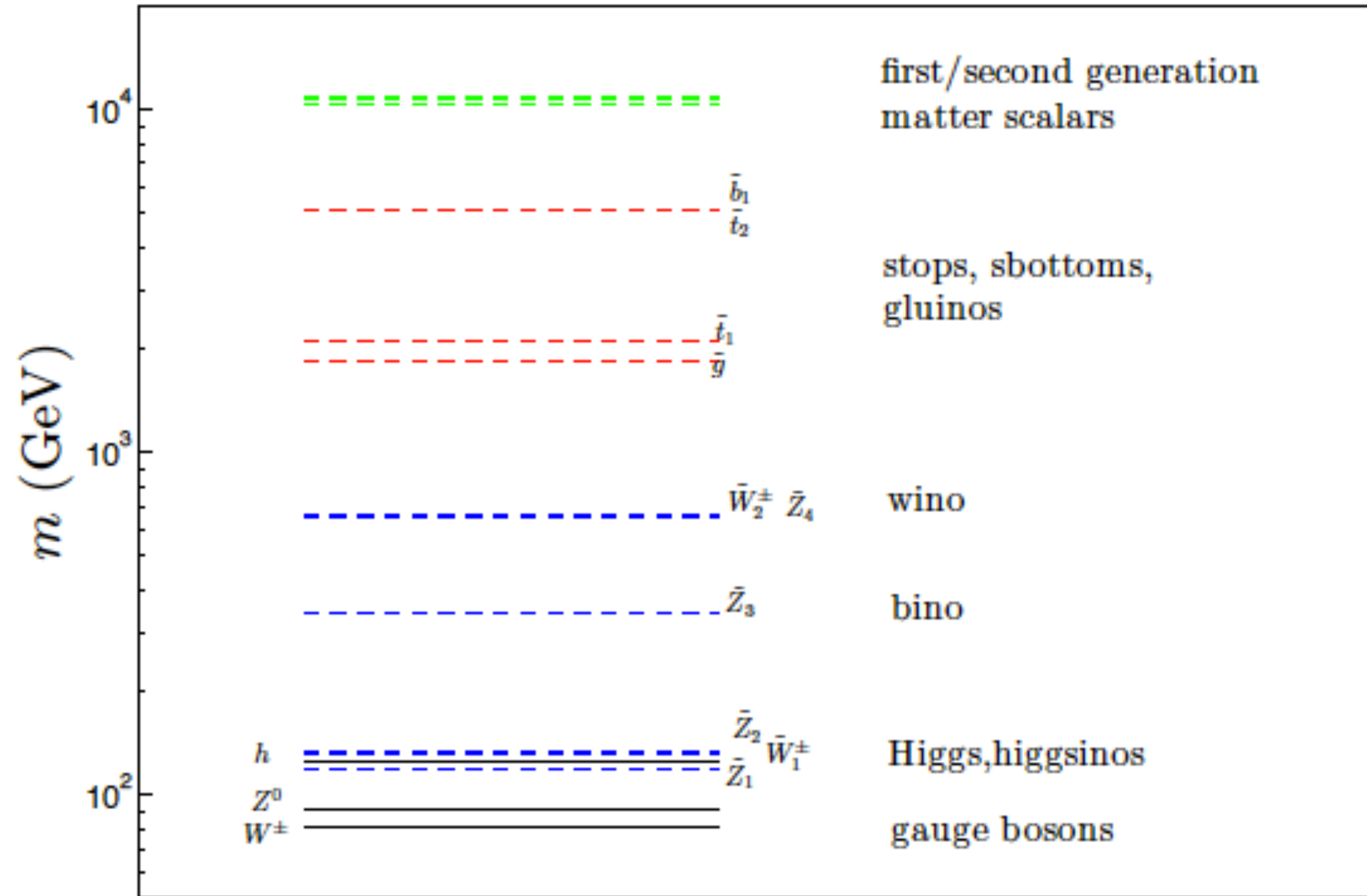
- EW naturalness measure: parameter free, depends only on spectra

HB, Barger, Huang, Mustafayev, Tata, PRL109 (2012) 161802

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

- μ is SUSY conserving: 100–350 GeV \Rightarrow light higgsinos! ; $m(\text{gluino}) < \sim 6$ TeV
- understand Cosm. Constant (Weinberg 1987); emergence of string landscape as manifest in eternally inflating multiverse (Bousso&Polchinski 2000, Susskind, Douglas et al, KKLT, 2000–2005)
- In landscape, statistical draw to large soft terms (Douglas; Susskind; Arkani-Hamed, Dimop, Kachru)
- Tempered by need for pocket universe weak scale \sim our weak scale 100–350 GeV (Agrawal, Barr, Donoghue, Seckel, 1997)

Typical spectrum for low Δ_{EW} models



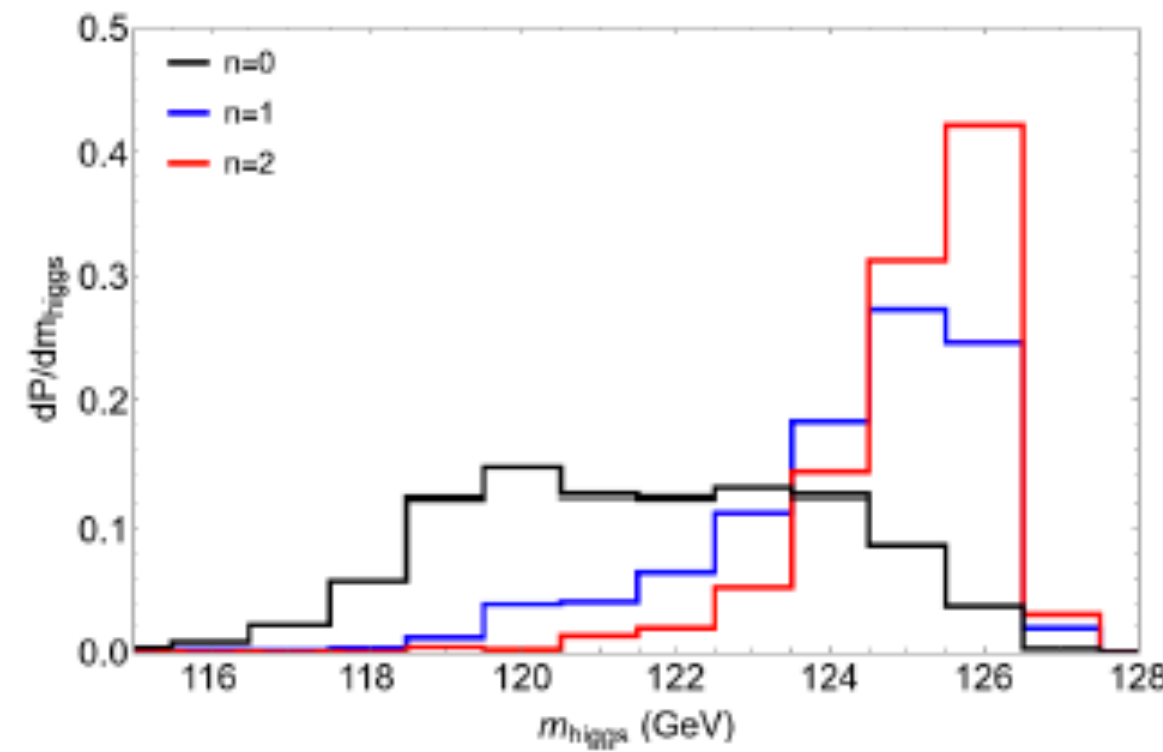
There is a Little Hierarchy, but it is **no problem**

$$\mu \ll m_{3/2}$$

higgsinos likely the lightest superparticles!

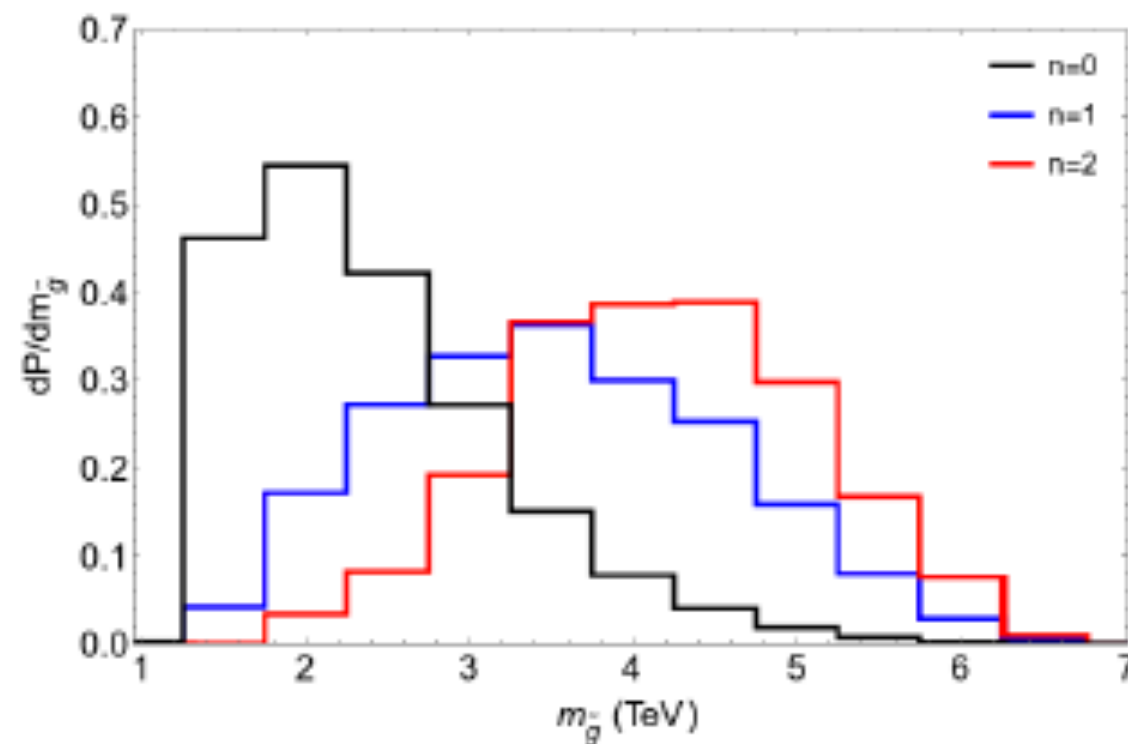
SUSY predictions from string landscape

$$dN_{\text{vac}} \sim m_{\text{soft}}^n * f_{\text{EWSB}}$$



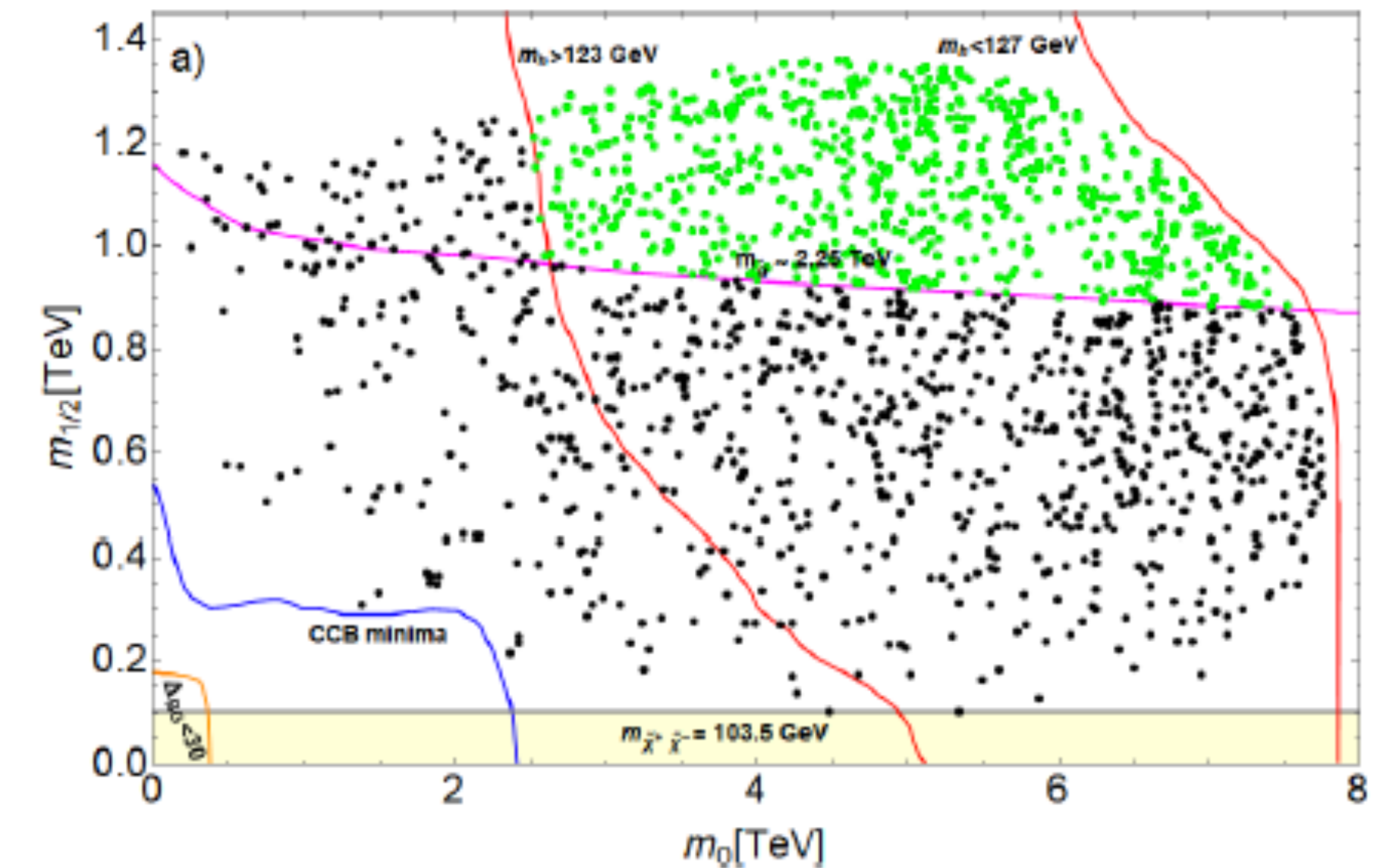
pull A_0 to maximal mixing
 $m(h) \sim 125$ GeV

FIG. 18: Distribution in m_h after requiring the anthropic selection of $m_{\text{weak}} < 350$ GeV.



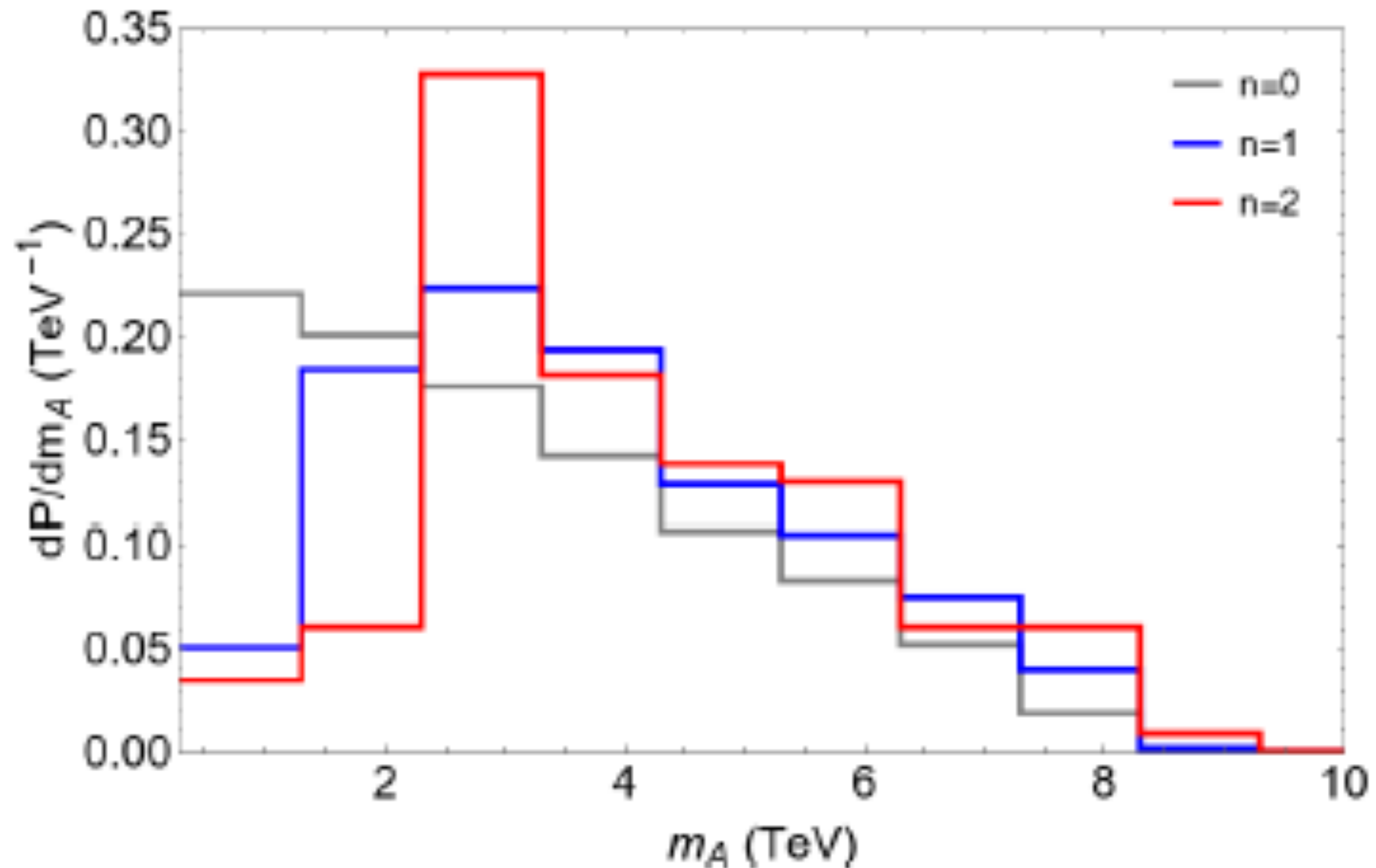
$m(\tilde{g}) > 2$ TeV

FIG. 19: Distribution in $m_{\tilde{g}}$ after requiring the anthropic selection of $m_{\text{weak}} < 350$ GeV.



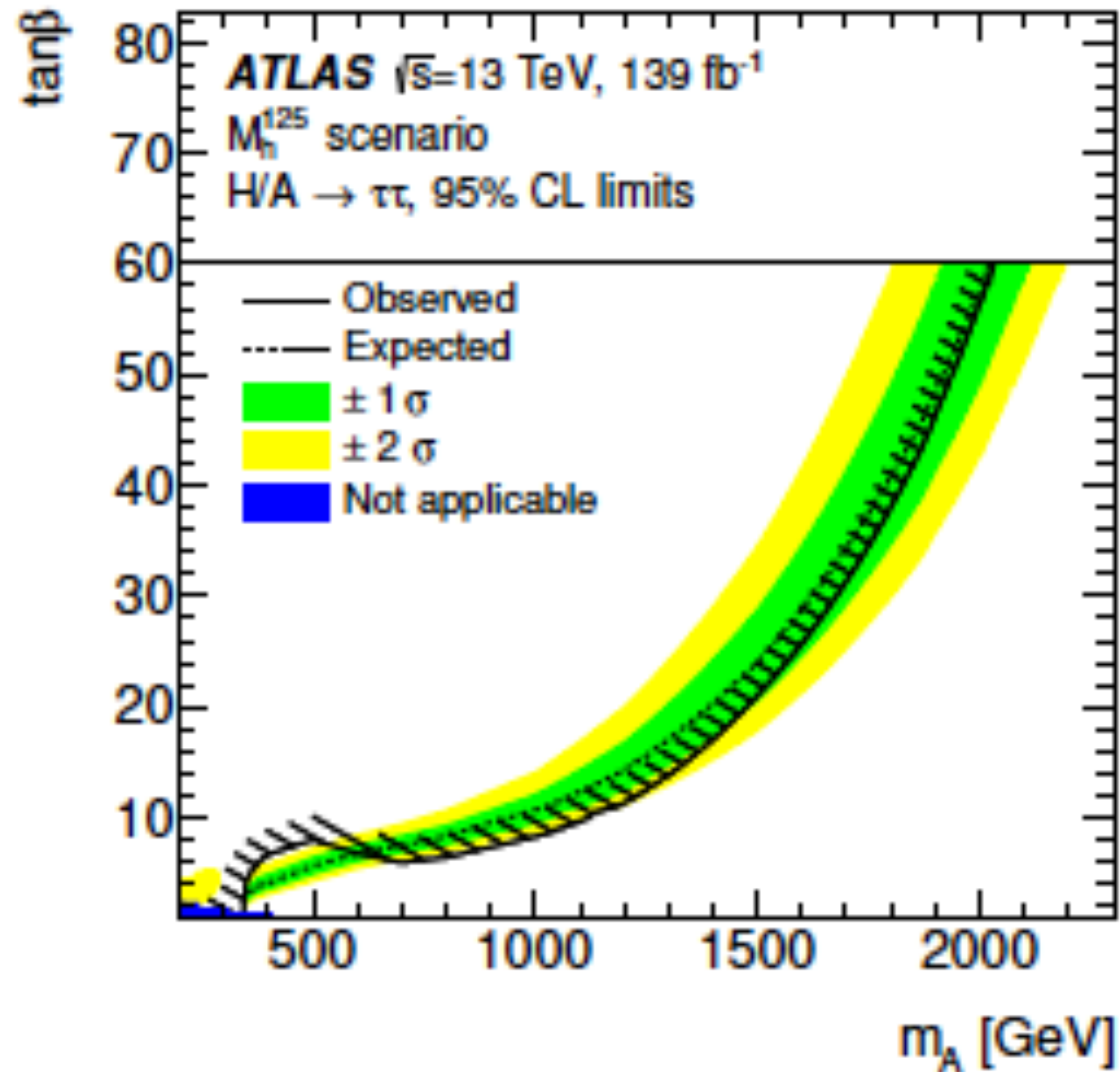
more stringy natural-
 greater density of points:
 heavy sparticles favored so long as $m_{Z^{\text{PU}}} < \sim 4 * m_{Z^{\text{OU}}}$

What about SUSY Higgs bosons?



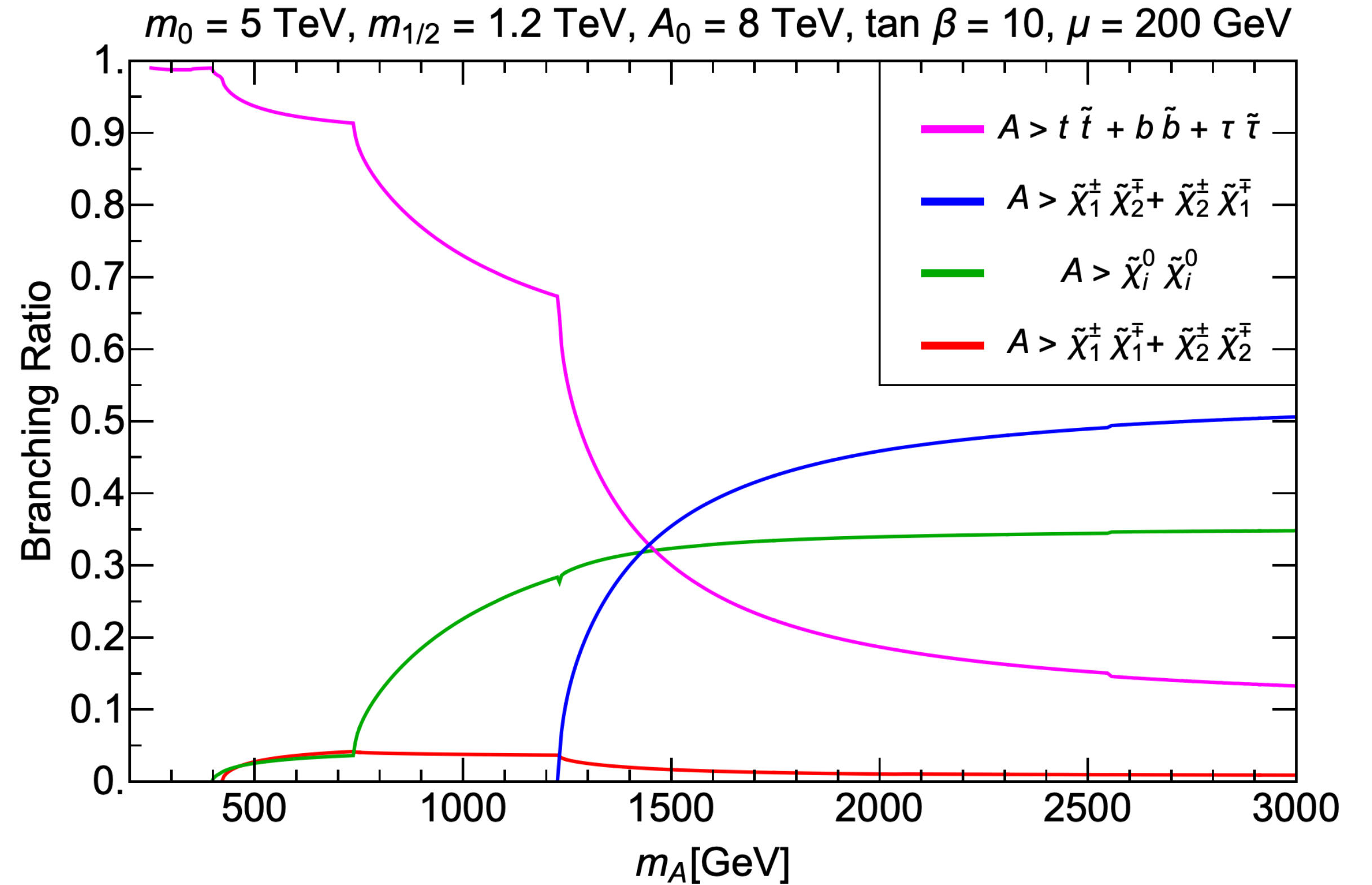
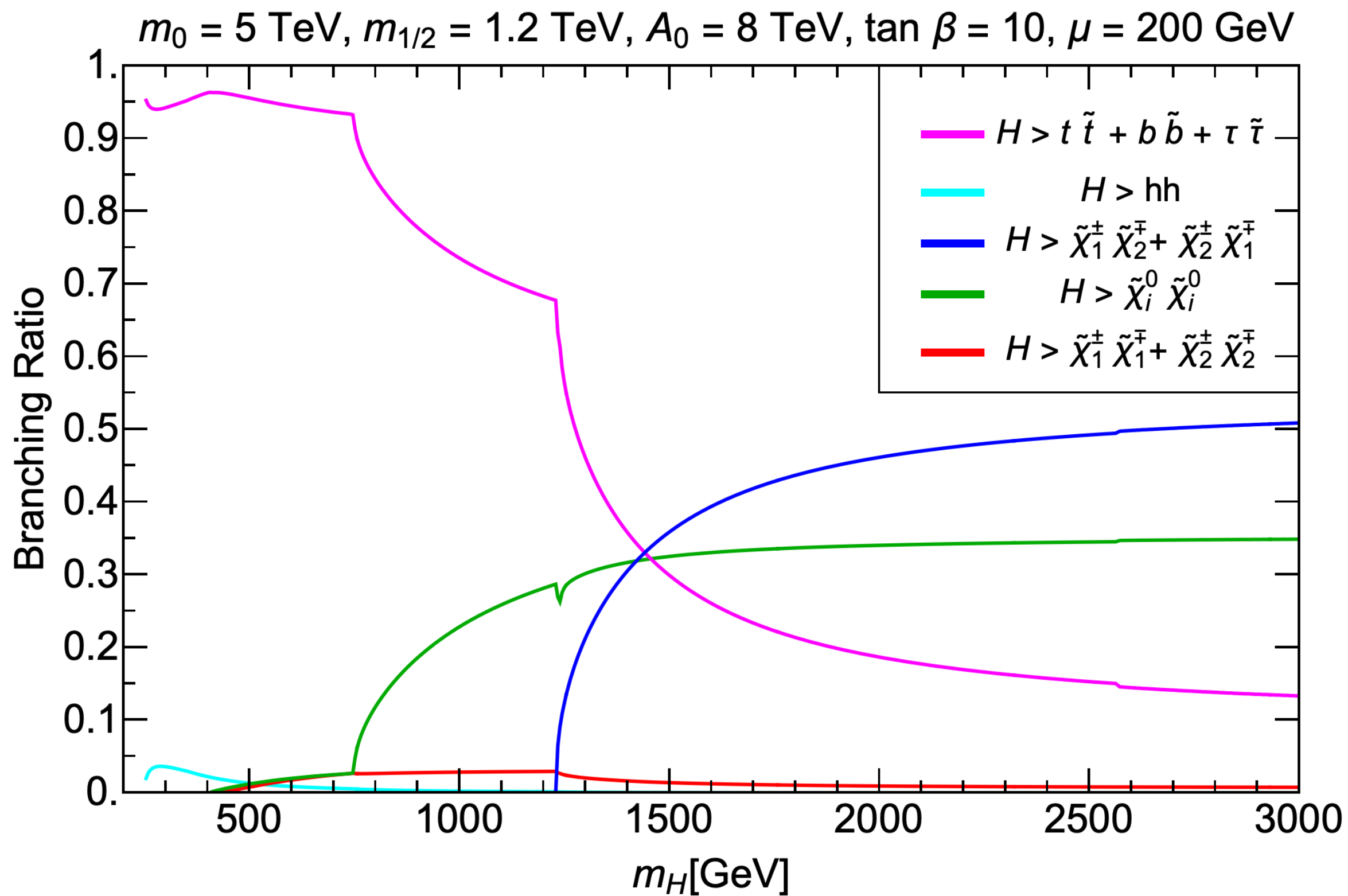
$m(A,H) \sim 1-8$ TeV so decays to SUSY should be open

Best heavy Higgs discovery mode -> tau+taubar



ATLAS: $m(H,A) > \sim 1$ TeV for $\tan\beta \sim 10$

H, A -> natSUSY BFs



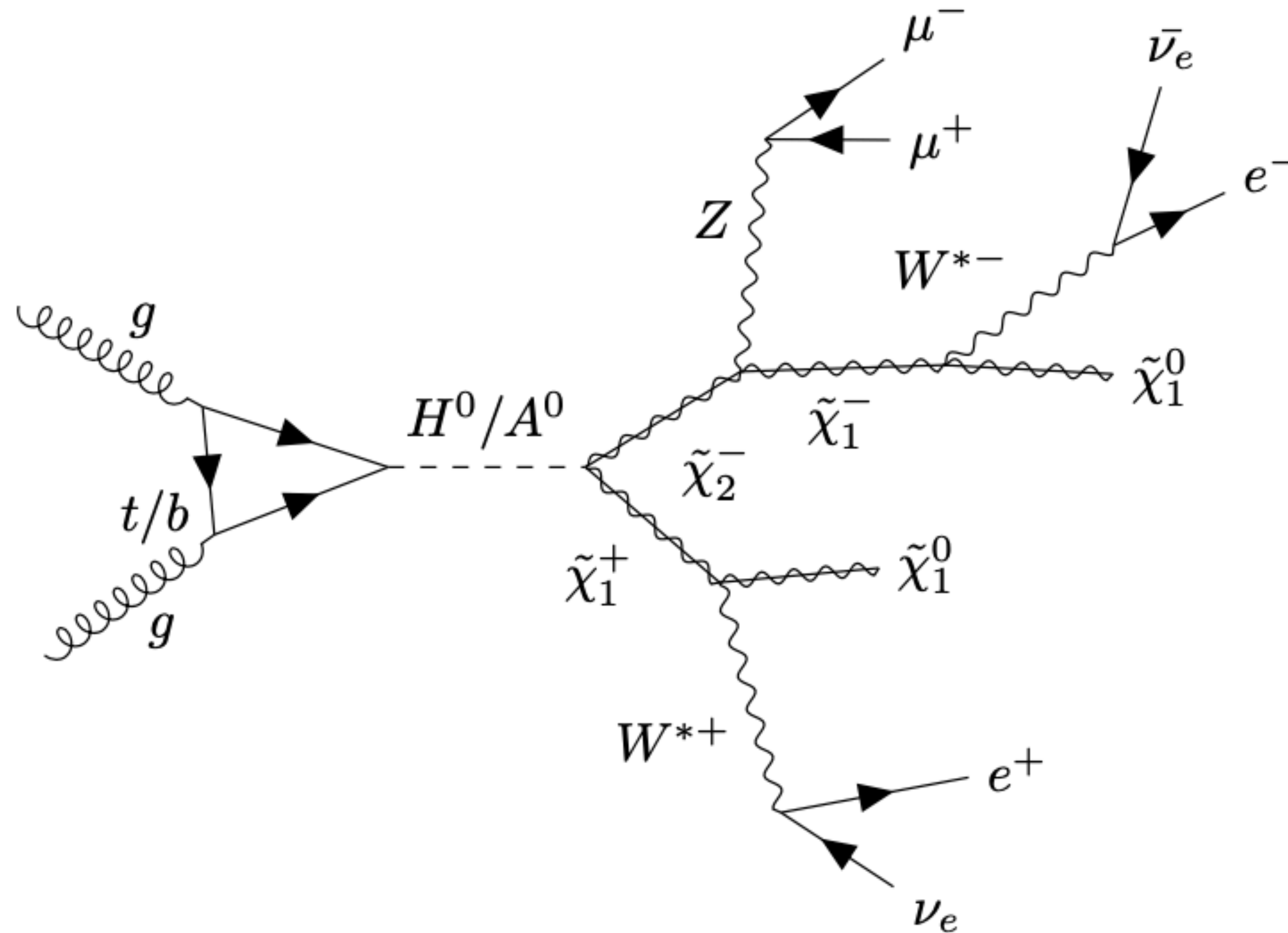
$$\mathcal{L} \ni -\sqrt{2} \sum_{i,A} S_i^\dagger g t_A \bar{\lambda}_A \frac{1-\gamma_5}{2} \psi_i + h.c.$$

dominant decay modes once kinematically allowed: H,A -> gaugino+higgsino,

*SUSY modes reduce H,A-> SM modes

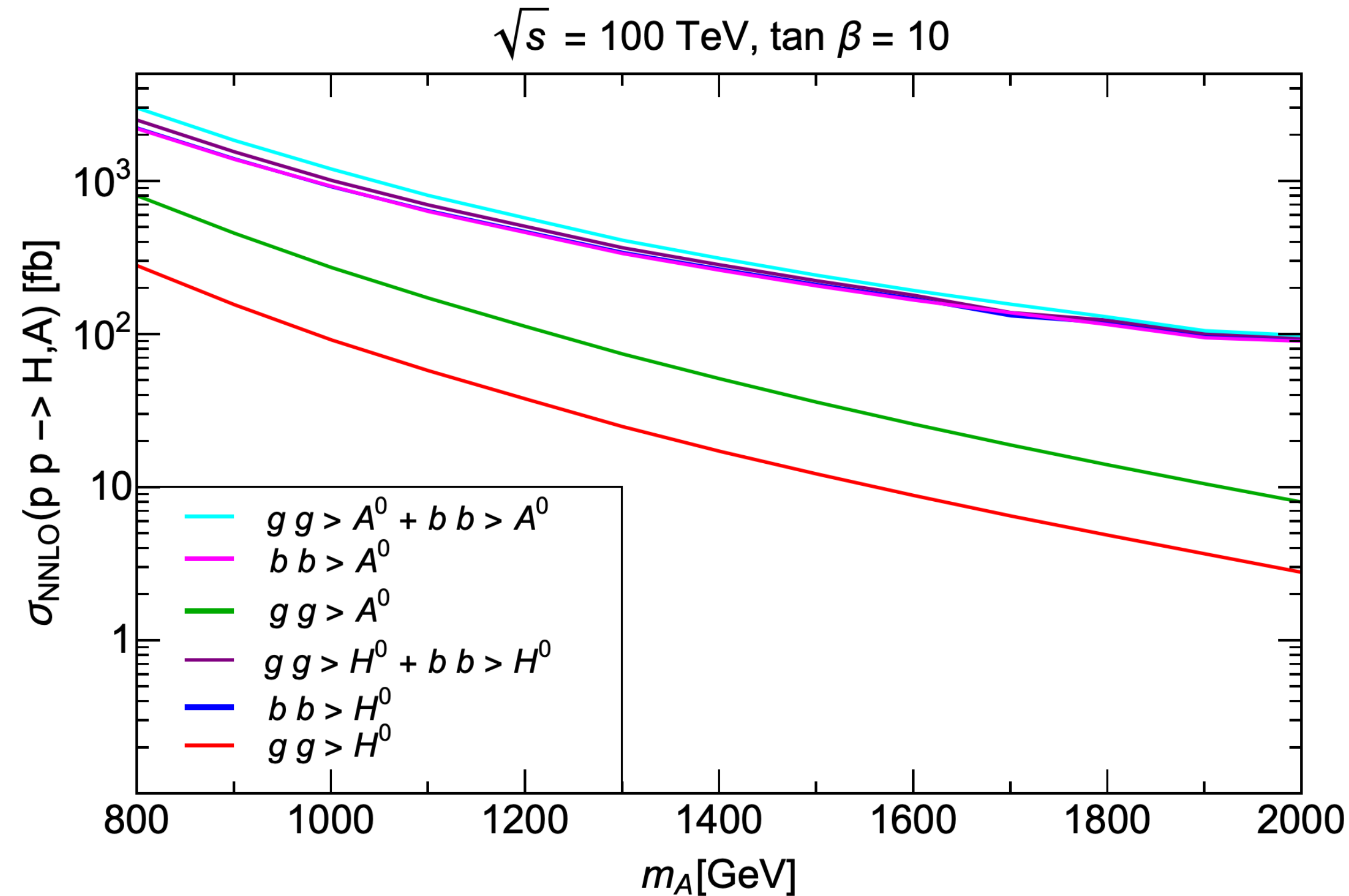
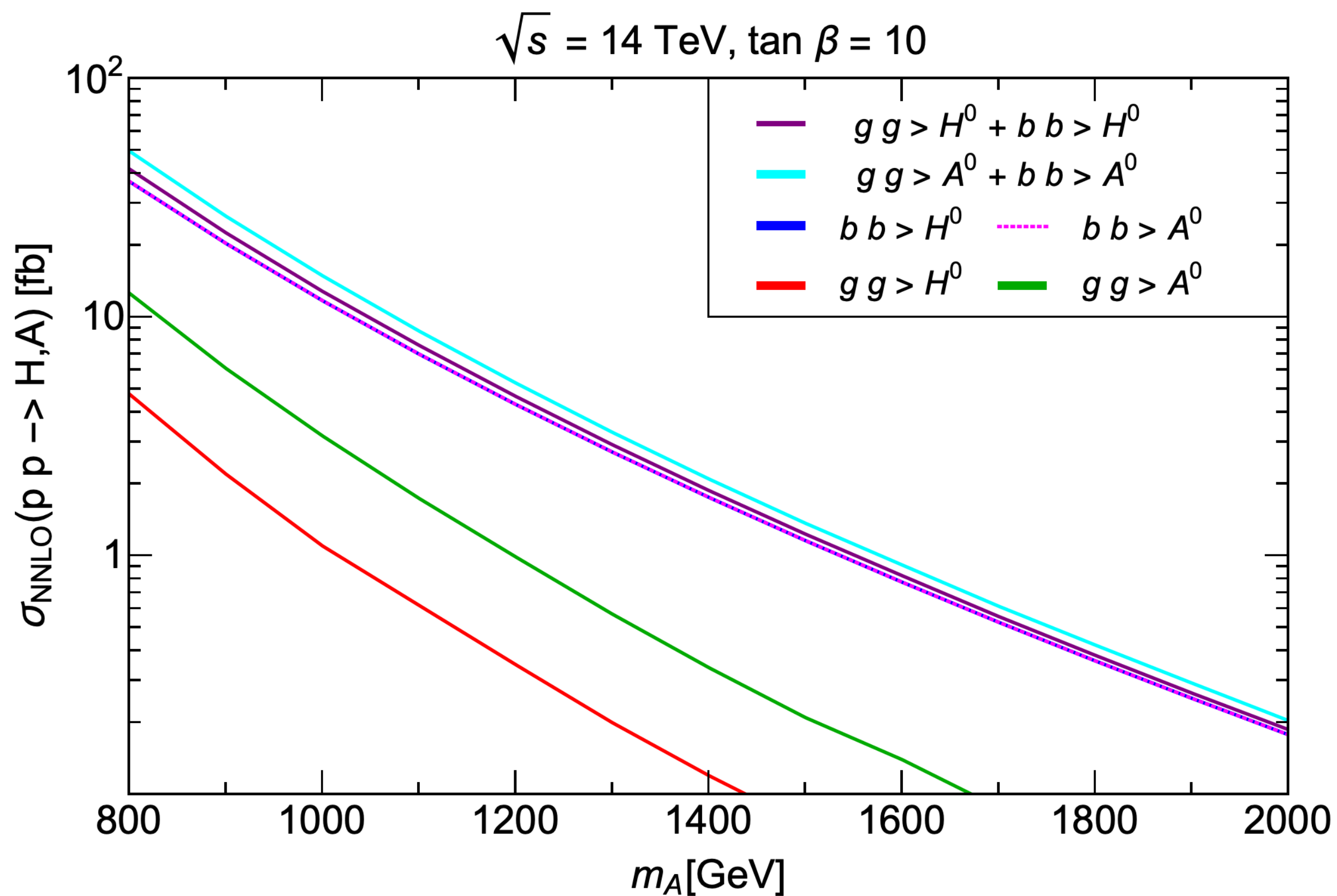
*but new discovery possibilities arise

Can we see $H, A \rightarrow$ SUSY at hadron colliders?



real $Z \rightarrow l\bar{l}$ plus 2 softer leptons+MET

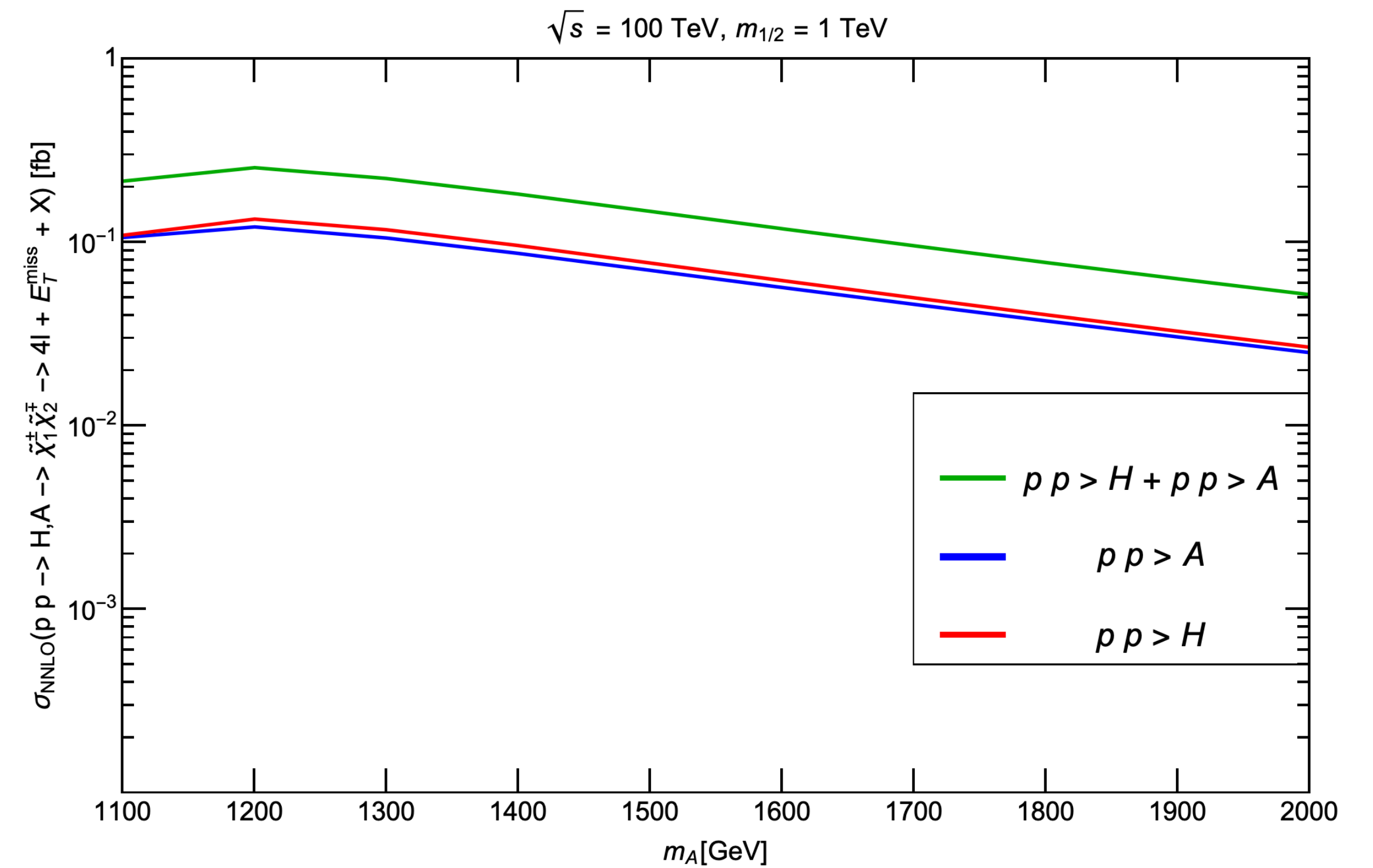
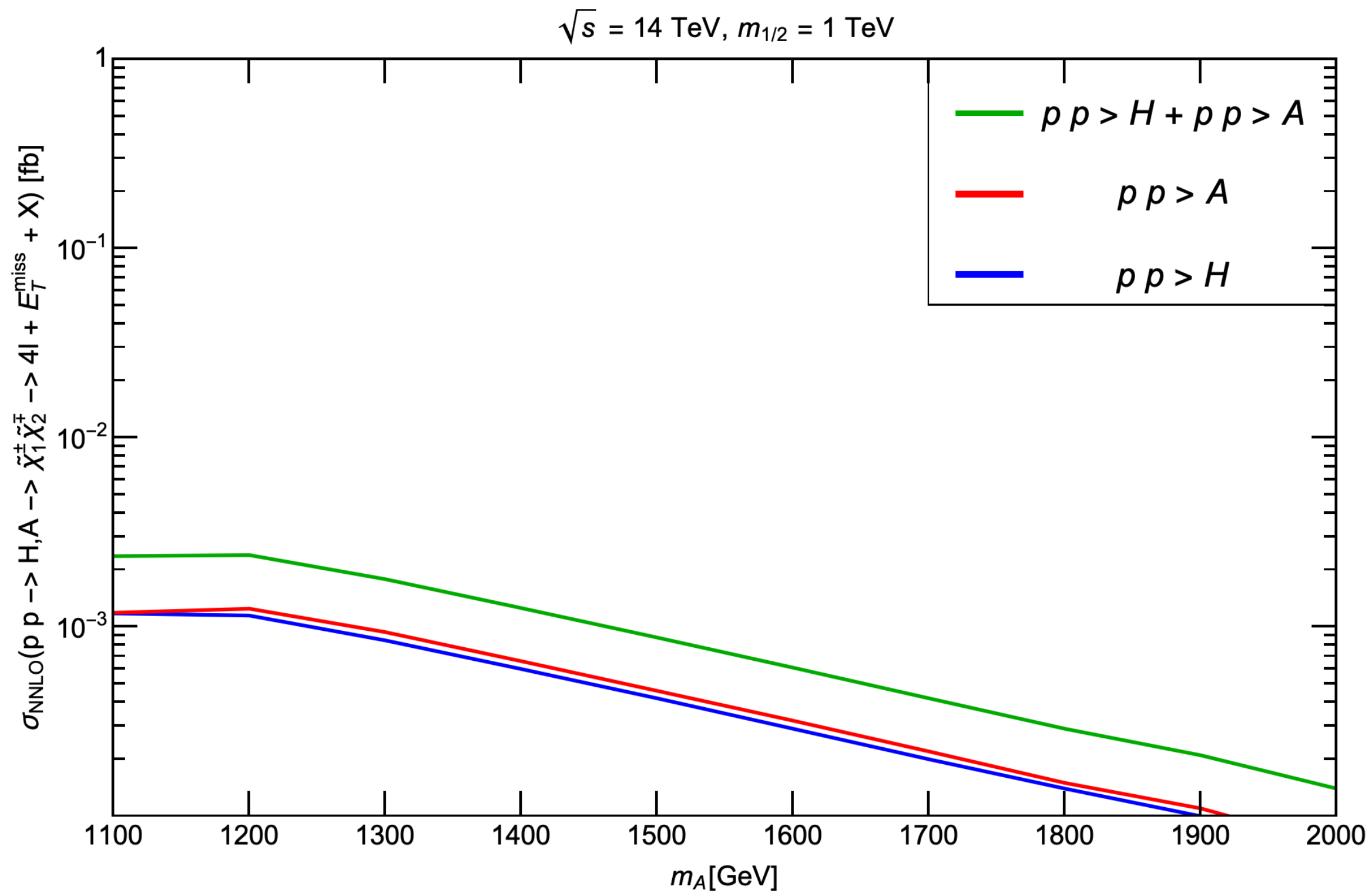
gg,bbbar fusion cross sections



probably need FCC-hh to do the job; rates too low at HL-LHC

total cross sections jump by $\sim 75\text{--}200$ in moving from 14 \rightarrow 100 TeV

fold in BFs to 4-lepton final states (but no cuts yet)

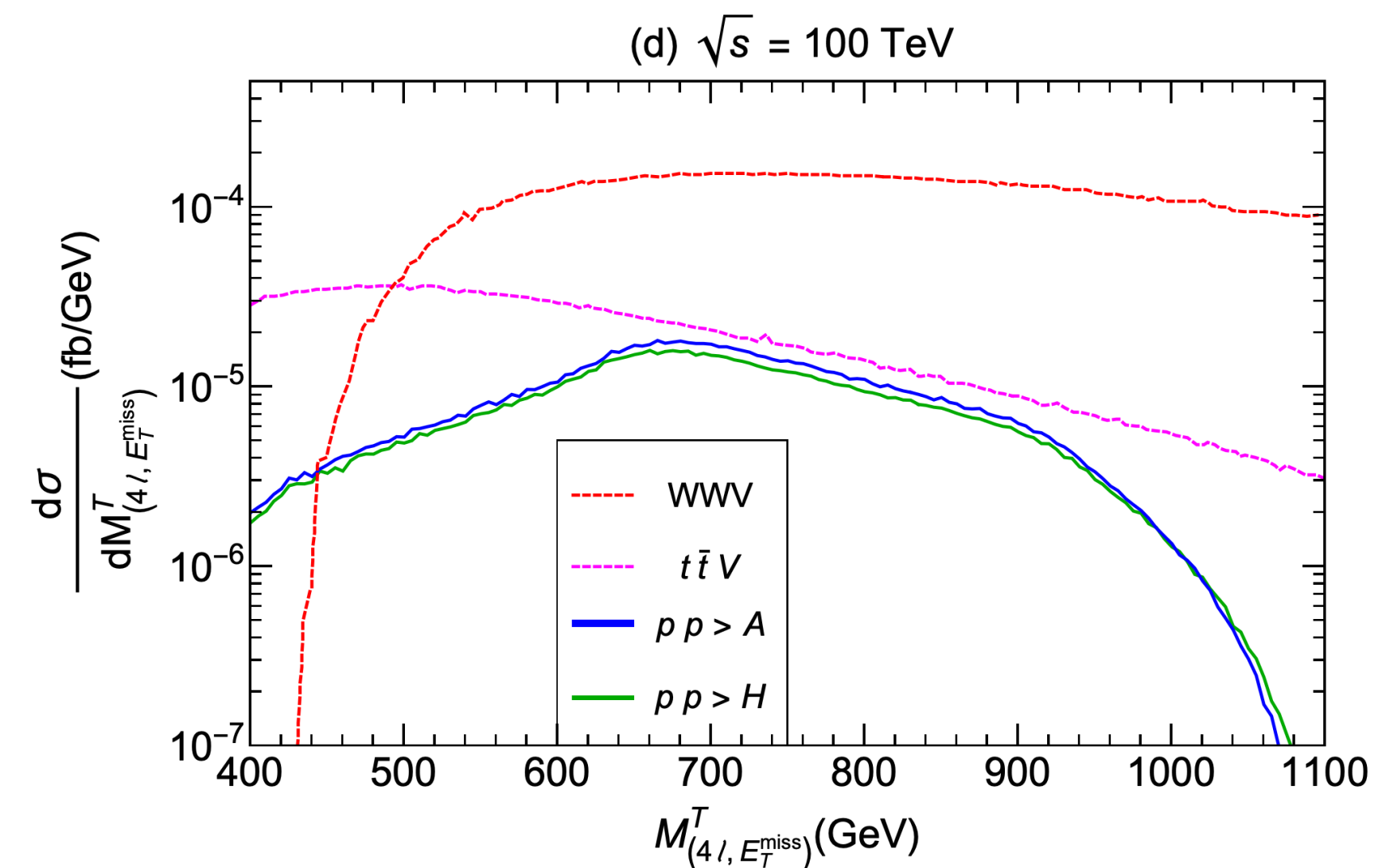
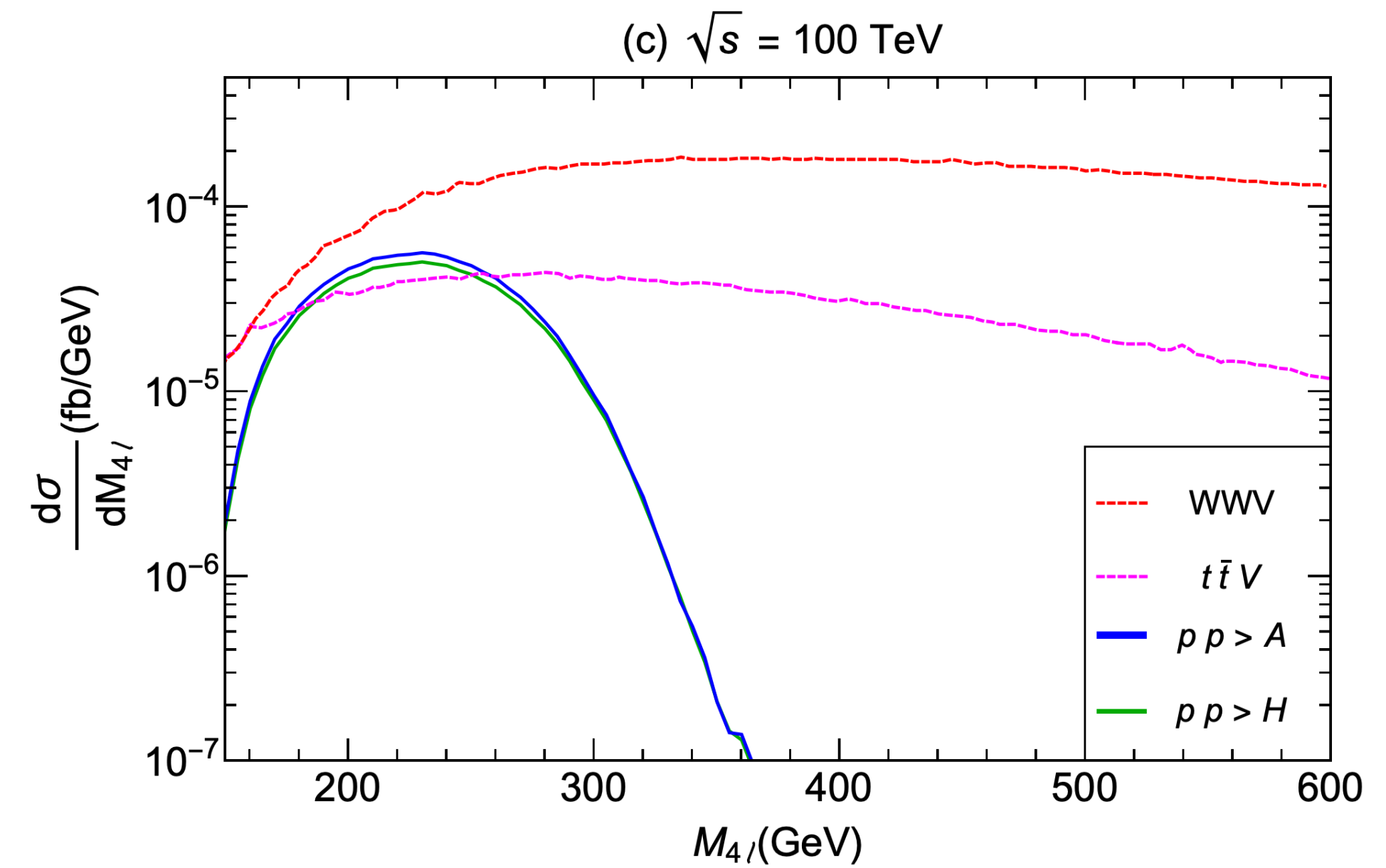
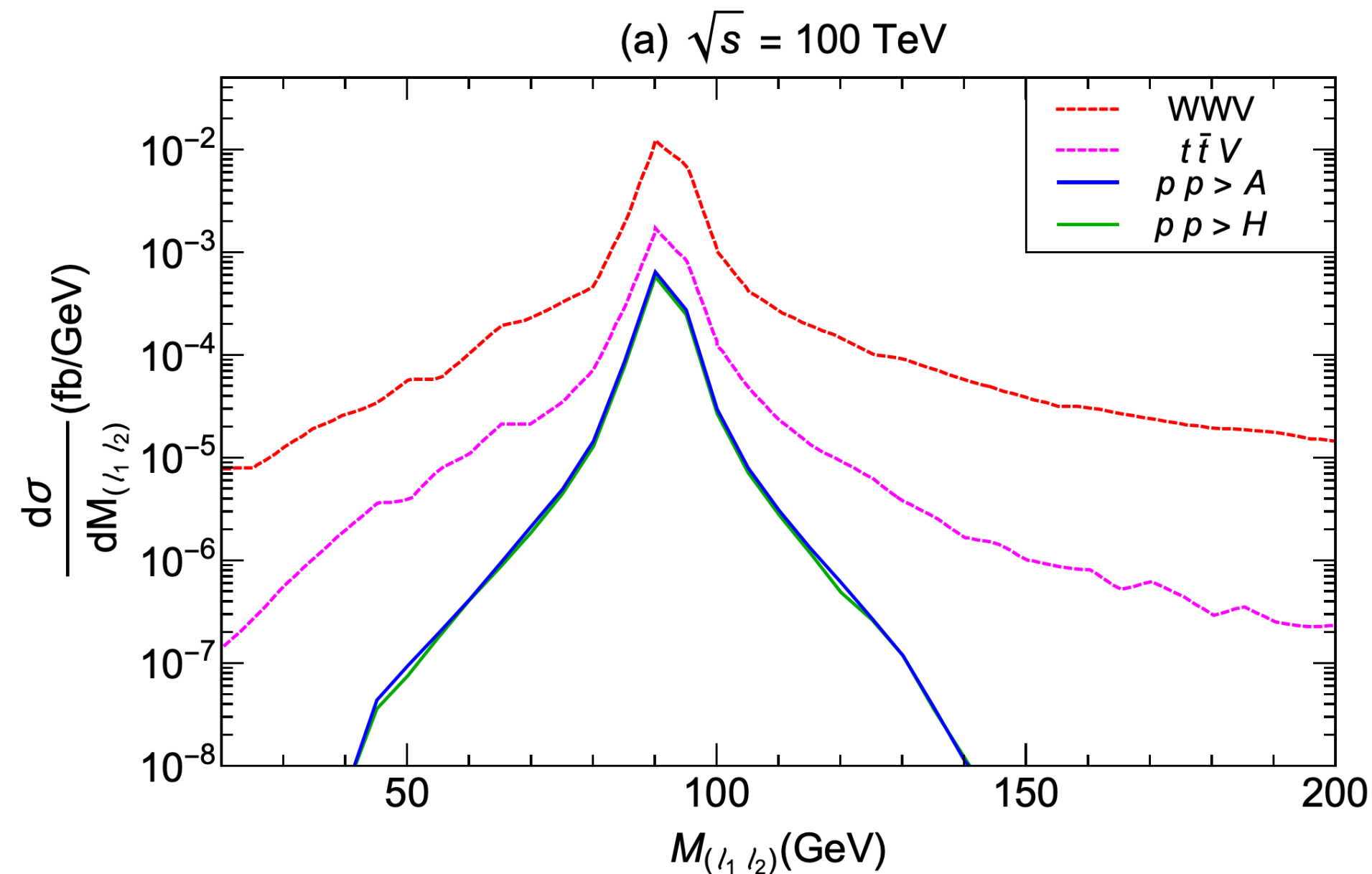


rates for $pp \rightarrow H, A \rightarrow 4l + \text{MET}$ pretty low at 14 TeV; need FCC-hh

various cuts for $m(H,A) \sim 1$ TeV

BGs: WWV, $t\bar{t}V$, Zh, ZZV ($V=W,Z,\gamma^*$)

- $p_T(\ell_1, \ell_2, \ell_3, \ell_4) > 20$ GeV, 10 GeV, 10 GeV, 10 GeV;
- $|\eta|(\ell_1, \ell_2, \ell_3, \ell_4) < 2.5$. cut set A
- Veto events with b -jets $p_T(\text{jet}) > 20$ GeV and $|\eta|(\text{jet}) < 2.5$ as already mentioned;
- $\Delta_R(j, \ell) > 0.4$, where j denotes a b -quark with $p_T < 20$ GeV or with $|\eta_b| > 0.4$, to mimic lepton isolation;
- Invariant mass for two opposite sign same flavor leptons $m_{\ell^+\ell^-} > 10$ GeV, to reduce the background from $\gamma^* \rightarrow \ell\bar{\ell}$;
- $\cancel{E}_T > 125$ GeV.



cuts motivated by distributions

- We define ℓ_1 and ℓ_2 as the two leptons whose invariant mass is closest to M_Z and require $|M(\ell_1, \ell_2) - M_Z| < 10$ GeV since the signal includes one Z boson;⁶

cut set B

- $10 < M(\ell_3, \ell_4) < 75$ GeV, where ℓ_3 and ℓ_4 denotes the remaining leptons.

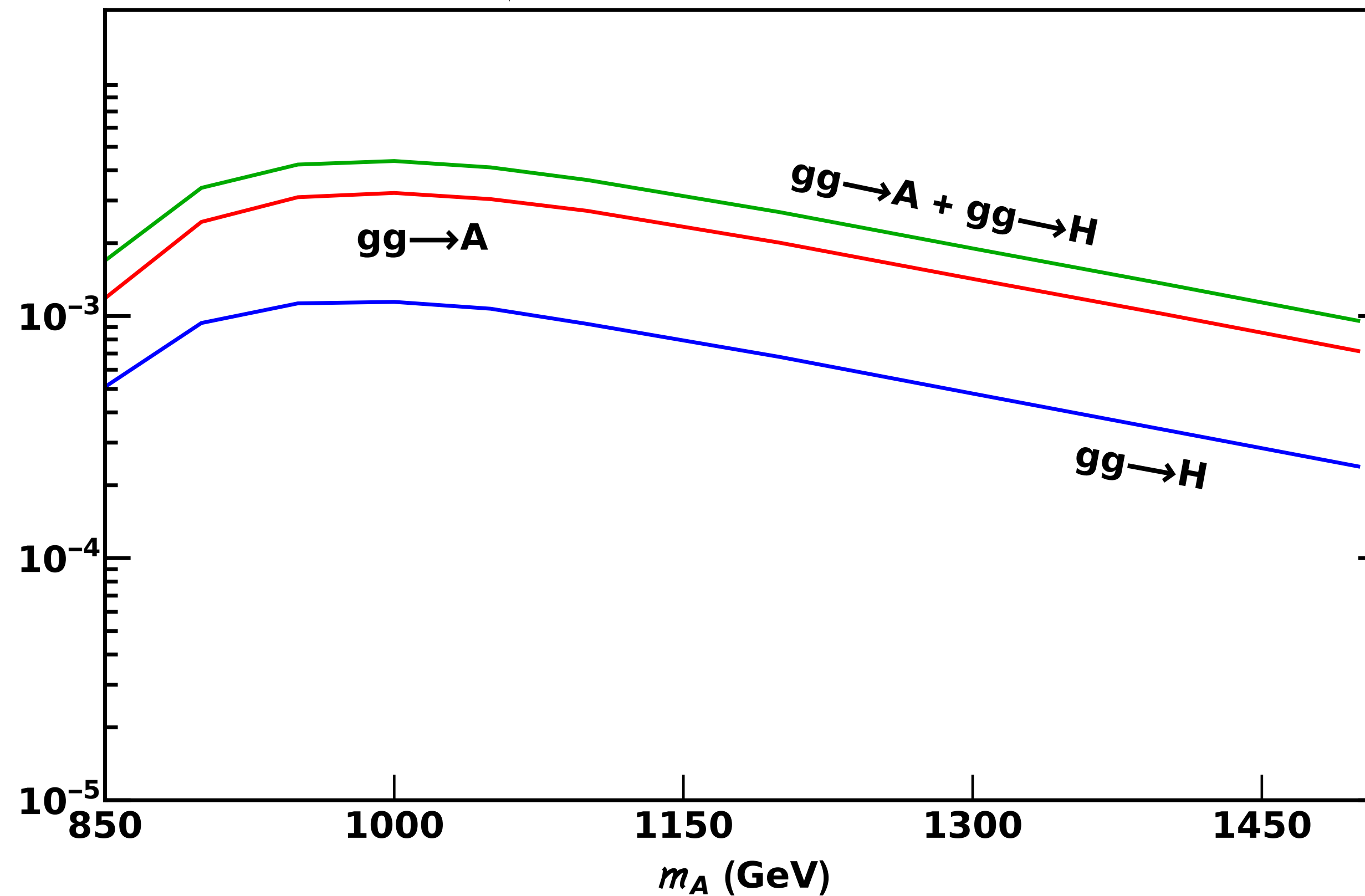
- $0.14m_A < M(4\ell) < 0.34m_A$

(get m_A from e.g. $H, A \rightarrow \tau\tau$)

- $\cancel{E}_T > 200$ GeV.

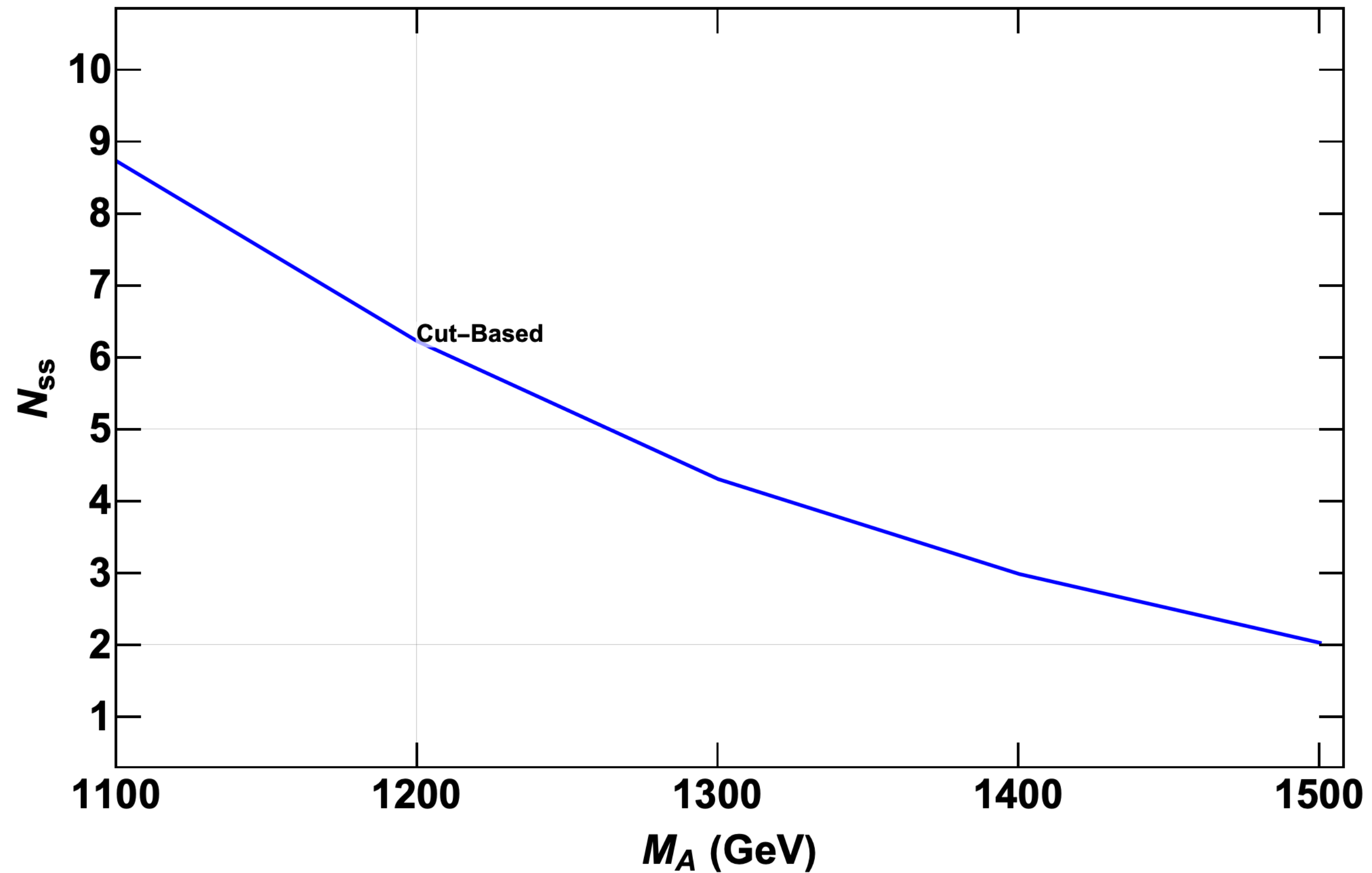
(b) $\sqrt{s} = 100$ TeV, $m_{1/2} = 800$ GeV

sigma after cut set B (fb)



cut based analysis

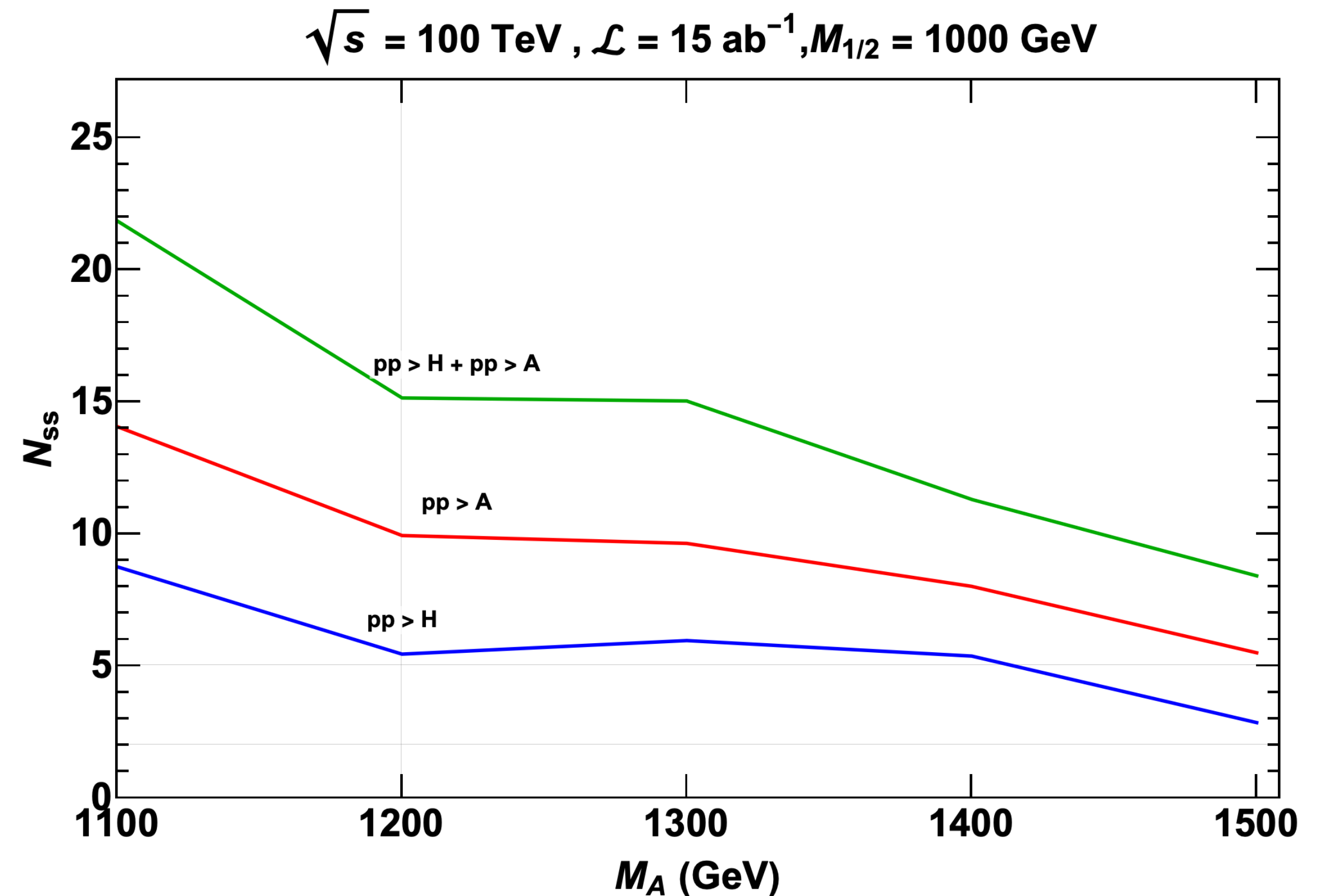
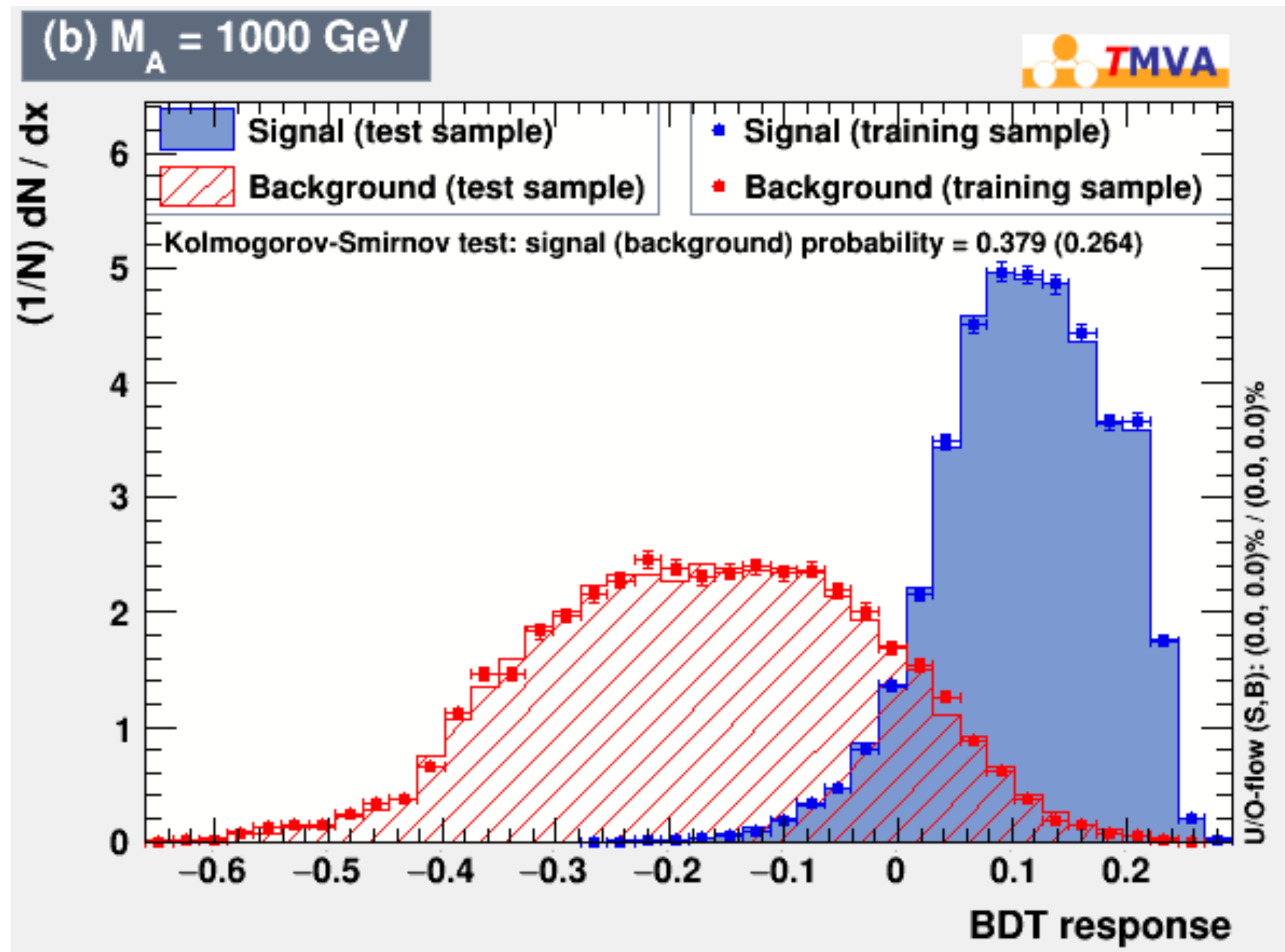
$$\sqrt{s} = 100 \text{ TeV}, \mathcal{L} = 15 \text{ ab}^{-1}, M_{1/2} = 1000 \text{ GeV}$$



5-sigma reach to $m(H,A) \sim 1250 \text{ GeV}$

(gg, bb \rightarrow H, A)

boosted decision tree analysis (BDT)



($gg, b\bar{b} \rightarrow H, A$)

(works better than our conventional cuts)

conclusions

- natural SUSY from landscape: $m(h) \sim 125$ GeV and sparticles beyond LHC reach
- maybe discover SUSY at HL-LHC via light higgsinos: soft dilepton analysis
- otherwise, need hadron collider energy upgrade: $\sqrt{s} > 30$ TeV
- FCC-hh most conservative: $\sqrt{s} \sim 50-100$ TeV
- in addition to sparticle/heavy Higgs discovery, can see $H, A \rightarrow$ SUSY via $4l + \text{MET}$ cascade decays to gaugino+higgsino states
- can see $4l + \text{MET}$ signature over range $m(H, A) \sim 800-1200$ GeV; more using BDT

Backup slides

#1: Simplest SUSY measure: Δ_{EW}

No large uncorrelated cancellations in $m(Z)$ or $m(h)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

$$\Delta_{EW} \equiv \max_i |C_i| / (m_Z^2/2) \quad \text{with} \quad C_{H_u} = -m_{H_u}^2 \tan^2 \beta / (\tan^2 \beta - 1) \quad \text{etc.}$$

simple, direct, unambiguous interpretation:

- $|\mu| \sim m_Z \sim 100 - 200 \text{ GeV}$
- $m_{H_u}^2$ should be driven to small negative values such that $-m_{H_u}^2 \sim 100 - 200 \text{ GeV}$ at the weak scale and
- that the radiative corrections are not too large: $\Sigma_u^u \lesssim 100 - 200 \text{ GeV}$

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Radiative natural SUSY with a 125 GeV Higgs boson

Howard Baer,¹ Vernon Barger, Peisi Huang,² Azar Mustafayev,³ and Xerxes Tata⁴

¹Dept. of Physics and Astronomy, University of Oklahoma, Norman, OK, 73019, USA

²Dept. of Physics, University of Wisconsin, Madison, WI 53706, USA

³W. I. Fine Institute for Theoretical Physics, University of Minnesota, Minneapolis, MN 55455, USA

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High scale (HS, stop mass) measure

$$m_h^2 \simeq \mu^2 + m_{H_u}^2(\text{weak}) = \mu^2 + m_{H_u}^2(\Lambda) + \delta m_{H_u}^2$$

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2}(m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda^2/m_{SUSY}^2)$$

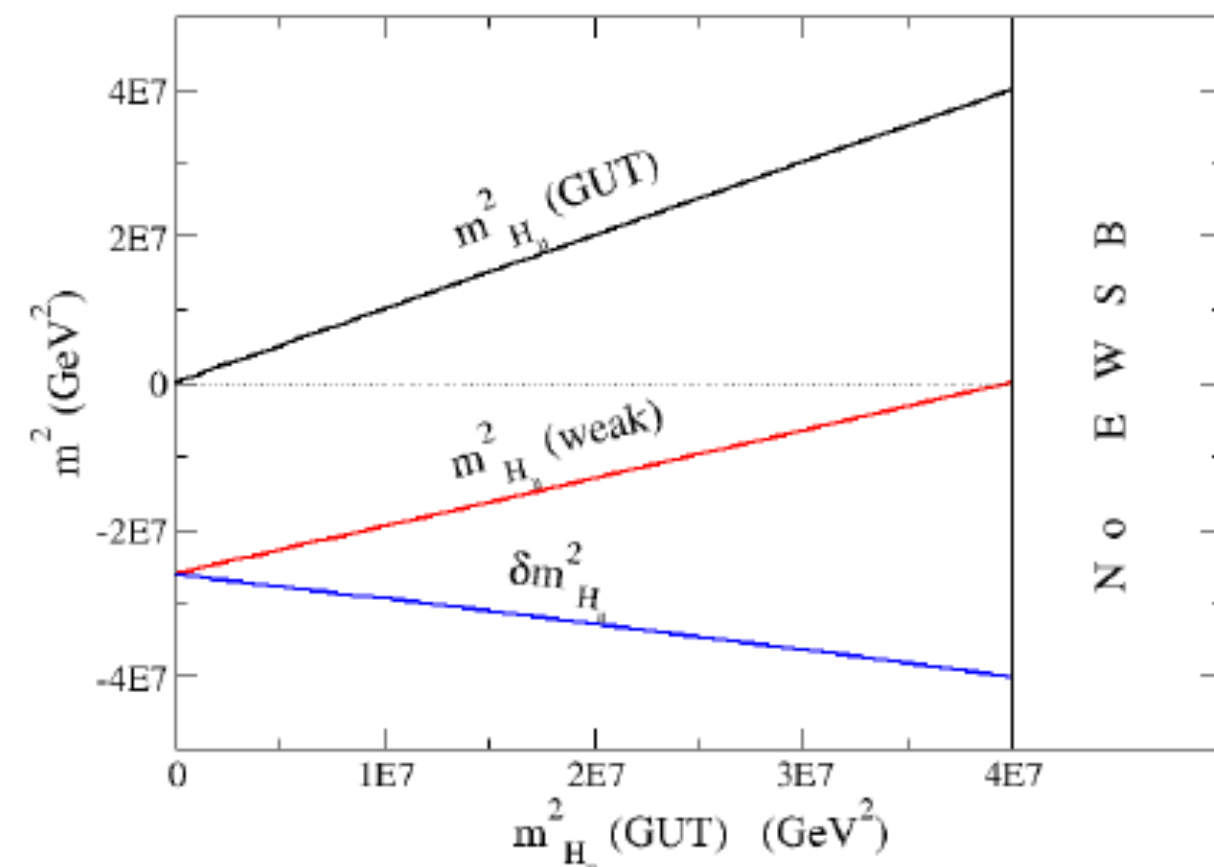
Implies 3 3rd generation squarks <500 GeV:

$$\text{SUSY ruled out under } \Delta_{HS} \equiv \frac{\delta m_{H_u}^2}{m_h^2}$$

BUT! too many terms ignored! **NOT VALID!**

$$\frac{dm_{H_u}^2}{dt} = \frac{1}{8\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right)$$

where $t = \ln(Q^2/Q_0^2)$, $S = m_{H_u}^2 - m_{H_d}^2 + \text{Tr}[m_Q^2 - m_L^2 - 2m_U^2 + m_D^2 + m_E^2]$ and $X_t = m_{Q_3}^2 + m_{U_3}^2 + m_{H_u}^2 + A_t^2$. By neglecting gauge terms and S ($S=0$)



The bigger $m_{H_u}^2(\Lambda)$ is, the bigger is the cancelling correction—these terms are *not independent*.

For big enough $m_{H_u}^2(\Lambda)$, then $m_{H_u}^2$ driven to natural value at weak scale: *radiatively driven naturalness (RNS)*

EENZ/BG naturalness

$$\Delta_{EENZ/BG} \equiv \max_i \left| \frac{\partial \log m_Z^2}{\partial \log p_i} \right|$$

- depends on input parameters of model
- different answers for same inputs assuming different models

model	c_{m_0}	$c_{m_{1/2}}$	c_{A_0}	c_μ	c_{H_u}	c_{H_d}	Δ_{BG}
mSUGRA	156	762	1540	-25.1	---	---	1540
NUHM2	16041	762	1540	-25.1	-15208	-643.6	16041

parameters introduced to parametrize our ignorance of SUSY breaking;
not expected to be fundamental

e.g. SUSY with dilaton-dominated breaking: $m_0^2 = m_{3/2}^2$ with $m_{1/2} = -A_0 = \sqrt{3}m_{3/2}$

(**doesn't make sense** to use independent m_0 , $m_{1/2}$, A_0)

while Δ_{BG} tells us about fine-tuning in our computer codes,
what we really want to know is: **is nature fine-tuned or natural?**

For correlated soft terms, then $\Delta_{BG} \rightarrow \Delta_{EW}$

Alternatively, only place independent soft terms makes sense
is in **multiverse**: but then selection effects in action

In fertile patch of vacua with MSSM as weak scale effective theory
but with no preferred SUSY breaking scale...

$$dP/d\mathcal{O} \sim f_{prior} \cdot f_{selection}$$

What is f_{prior} for SUSY breaking scale?

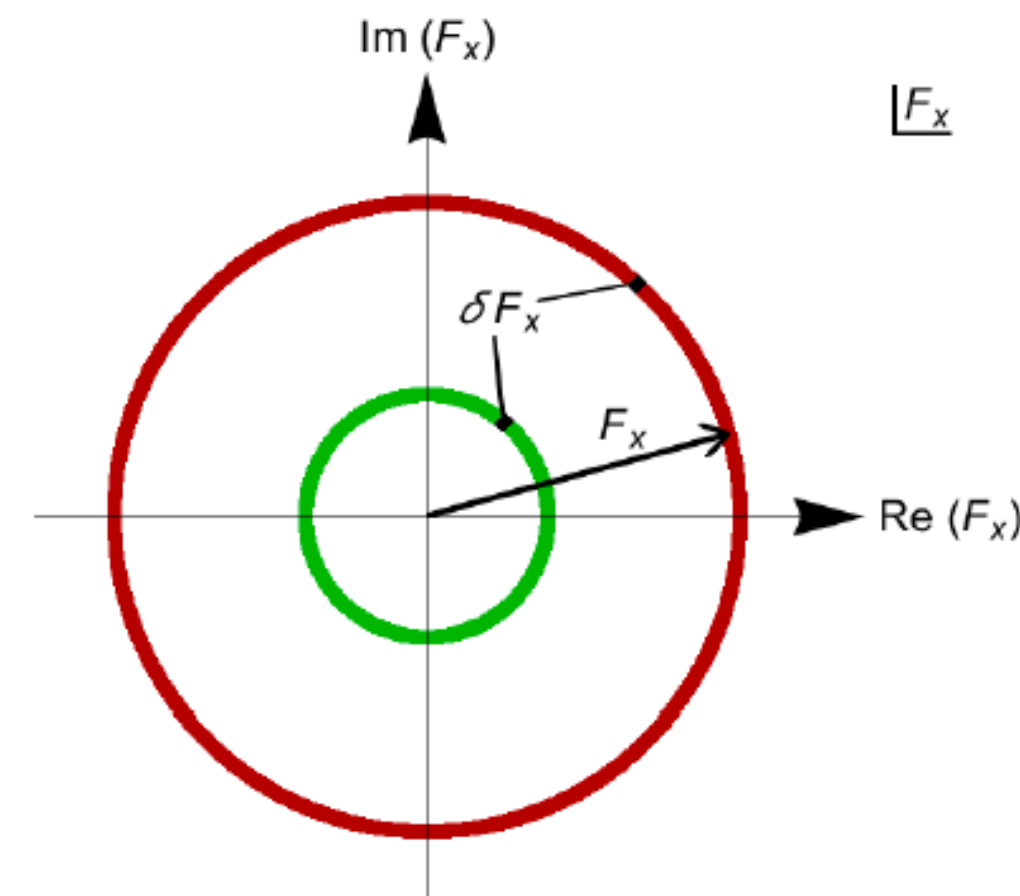
In string theory, usually multiple (~ 10) hidden sectors
containing a variety of F- and D- breaking fields

For comparable $\langle F_i \rangle$ and $\langle D_j \rangle$ values, then expect

$$f_{prior} \sim m_{soft}^{2n_F + n_D - 1}$$

Douglas ansatz

arXiv:0405279



Under single F-term
SUSY breaking,
expect **linear increasing
statistical selection
of soft terms**

Figure 1: Annuli of the complex F_X plane giving rise to linearly increasing selection of soft SUSY breaking terms.