

# A taste of cosmology

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# OUTLINE

- The standard cosmological model
- The successes of cosmology over the past 10 years
- Cosmic Microwave Background
- Large-scale structure
- Inflation and outlook for the future

*Lectures and additional material will appear at*

<http://icc.ub.edu/~liciaverde/CLASHEP.html>

# Cosmology

Cosmos= Universe, Order, beauty  
-logy= study

Greek!

Study of the Universe as a whole

Aim at getting an understanding of:

- its origin

- its structure and composition

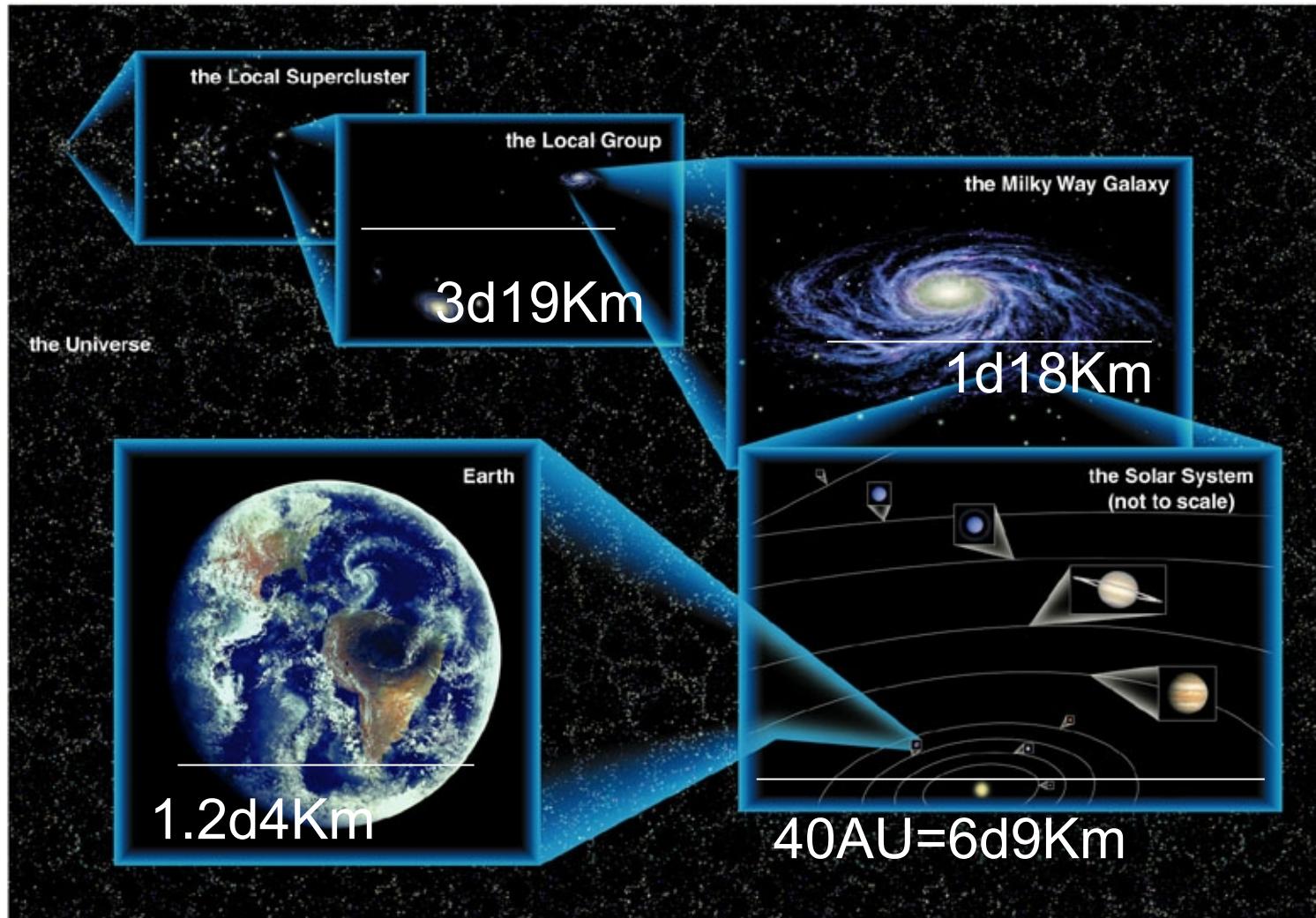
(where do galaxies, stars, planets, people come from?)

- its evolution

- its fate

In general for cosmologists galaxies are points....

# Scales involved!



# New units of measure

For distance, we use pc, Kpc & Mpc

$$1 \text{ pc} = 3.086 \times 10^{16} \text{ m}$$
$$1 \text{ Mpc} = 3.086 \times 10^{22} \text{ m}$$

For comparison, mean Earth-Sun distance (Astronomical Unit):

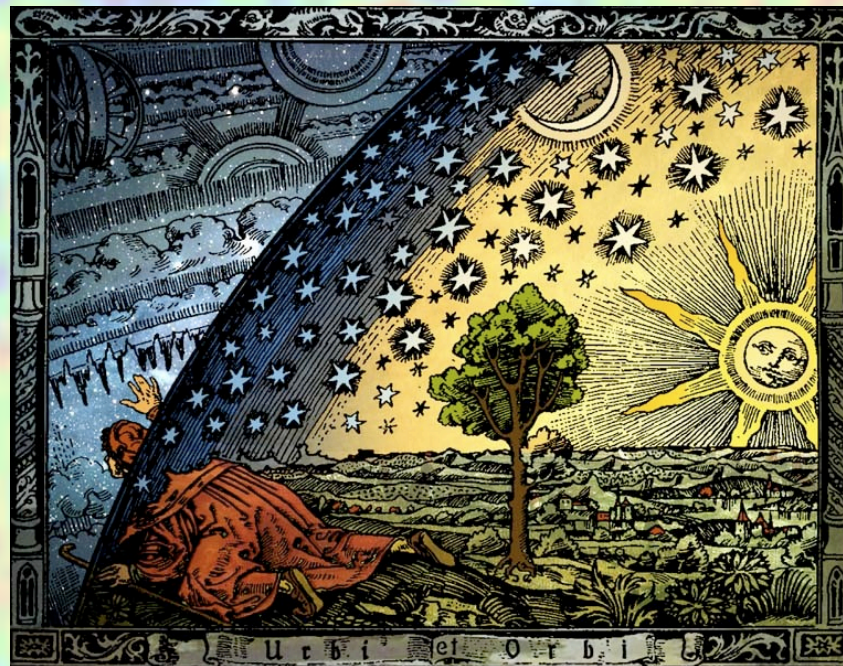
$$1 \text{ AU} = 1.496 \times 10^{11} \text{ m}$$
$$1 \text{ pc} = 2.1 \times 10^5 \text{ AU}$$

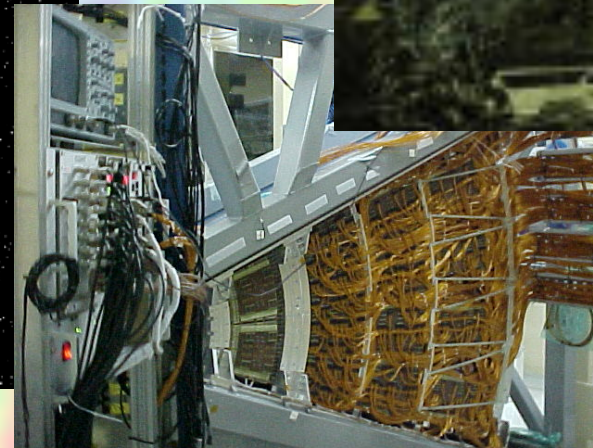
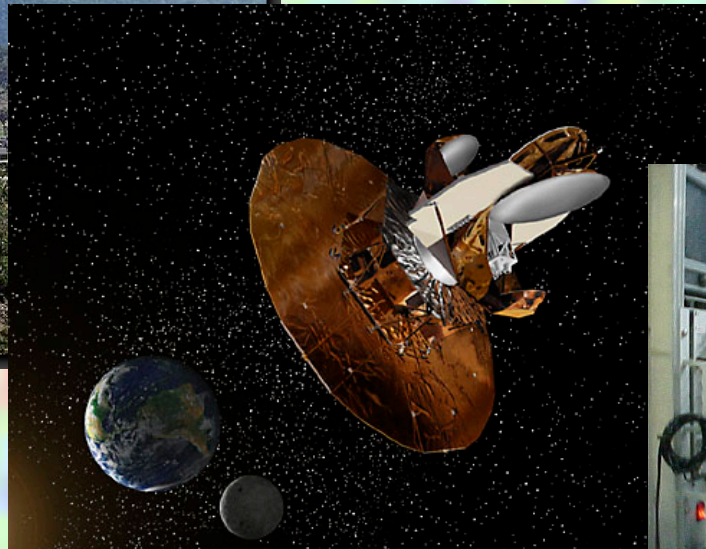
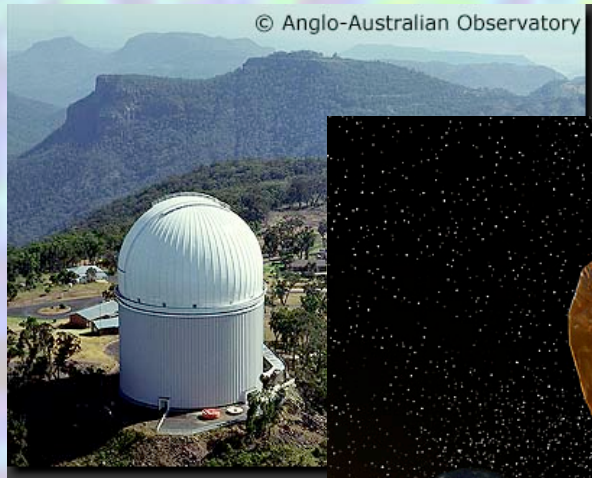
- Cosmologists often express masses
  - in units of the solar mass:
- $$1 M_{\odot} = 1.99 \times 10^{30} \text{ kg}$$

# MOTIVATION

- Cosmology over the past 15 years has made the transition to *precision cosmology*
- Cosmology has moved from a *data-starved science* to a *data-driven science*
- Cosmology has now a *standard model*. The *standard cosmological model* only needs few parameters to describe origin composition and evolution of the Universe
- Big difference between modeling and understanding

**Motivation: Why should you care about observational cosmology?**





Deep connections  
between cosmology and fundamental physics



## Testing fundamental physics by looking up at the sky is not new

The interplay between astrophysics and fundamental physics has already produced spectacular findings (e.g. the solar neutrino problem)

Cosmology has entered the precision era very recently

**Cosmological data can be used to  
test fundamental physics**

4 Areas

Dark matter

Neutrinos

**Inflation**

**Dark energy**

## Fundamental assumptions

Physics as we know it can describe the Universe

On the largest scales the driving force is gravity  
(forget about “gastrophysics”)

General Relativity rules!  
(for many applications you can be Newtonian)

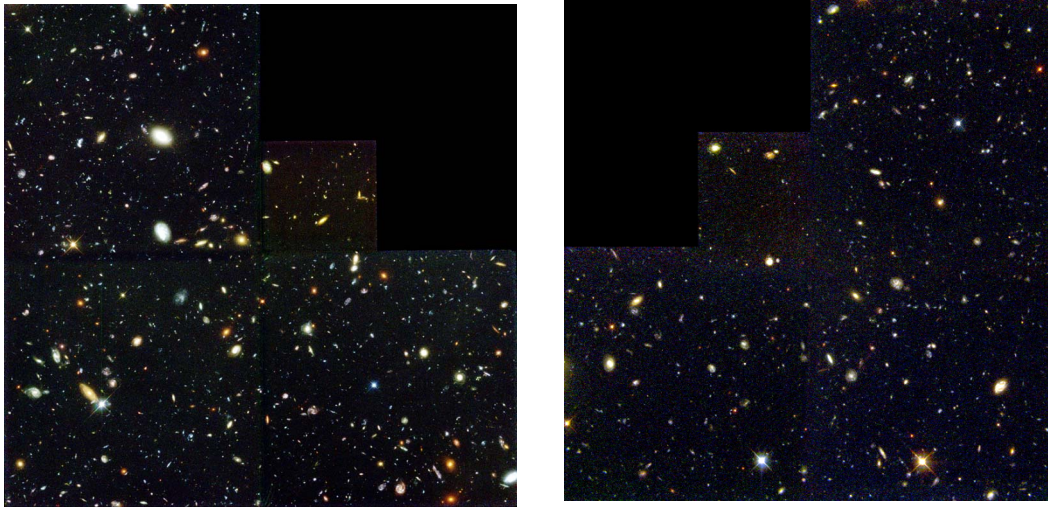
**Homogeneity and isotropy**

FLRW metric

Three possible global geometries only

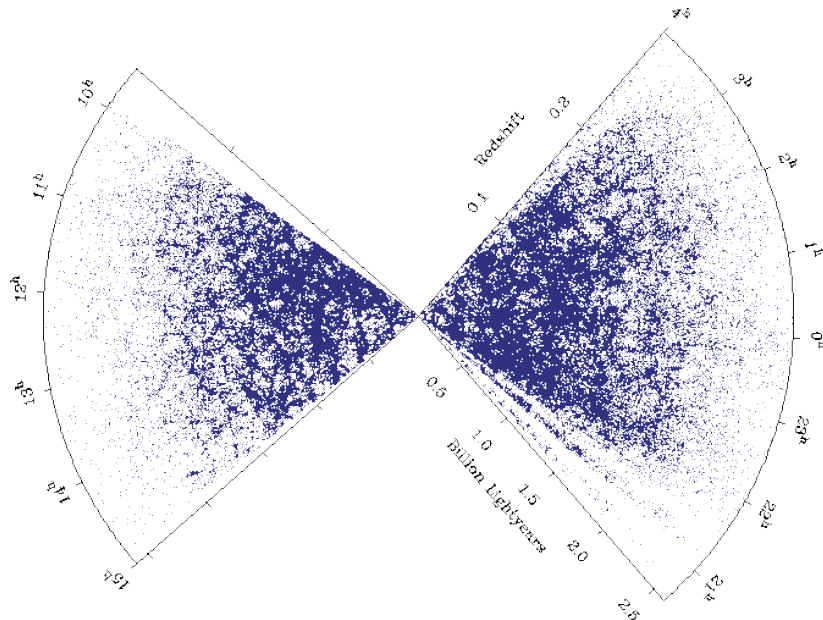
# Some assumptions

The Universe is homogeneous and isotropic on large scales



This is supported  
by observations

HDF north  
and south



2dF GRS

Large volumes of the sky in  
different directions, 100's of  
Mpc in size, look about the  
same.

# The standard cosmological model: parameters

## Different type of parameters

The smooth Universe

{ Parameters that govern the global geometry of space-time

{ Parameters that govern the expansion rate

GR geometry, fate of Universe, content (but not much details)

Inhomogeneous Universe

{ Parameters that characterize inhomogeneities

Statistically speaking: clustering, galaxies etc...

Parameterizing our ignorance

{ Derived parameters

Beyond the minimal model: “extra” parameters

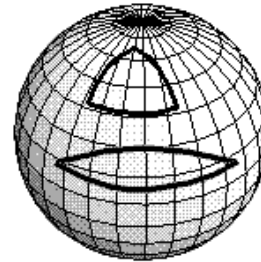
test: which is which?

# The smooth Universe: content

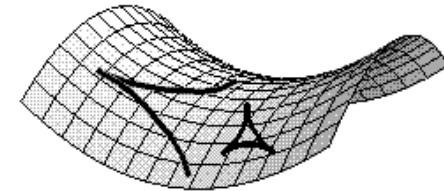
$$\Omega = \frac{\rho}{\rho_{crit}}$$

Gives the global geometry/curvature

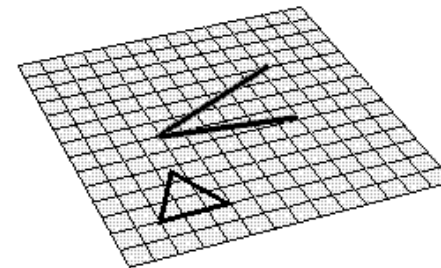
$$\Omega = \Omega_m + ???$$



Universe with *positive* curvature. Diverging line converge at great distances. Triangle angles add to more than  $180^\circ$ .

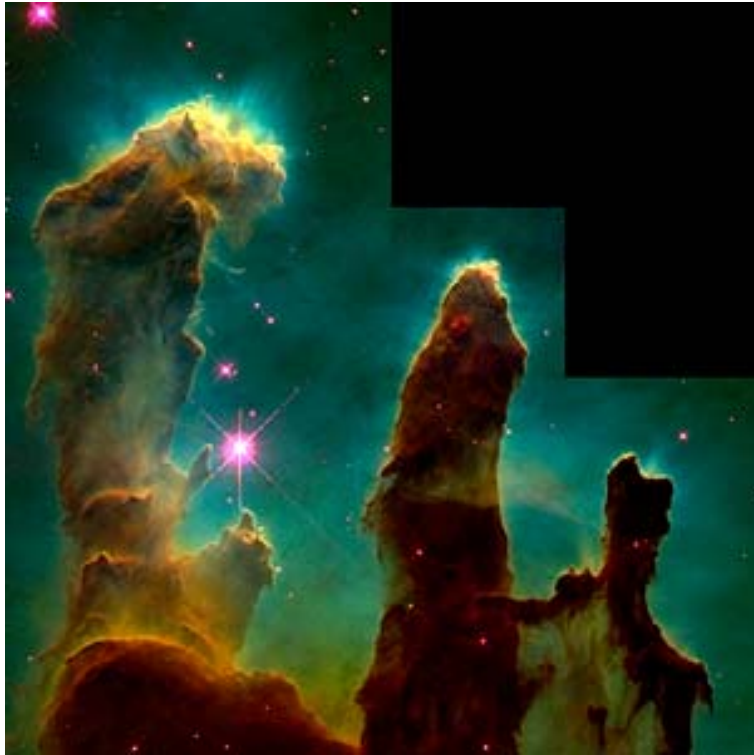


Universe with *negative* curvature. Lines diverge at ever increasing angles. Triangle angles add to less than  $180^\circ$ .



Universe with no curvature. Lines diverge at constant angle. Triangle angles add to  $180^\circ$ .

# Content: Baryons: stars



HST image of stars being born,  
but it has no direct use  
for Cosmology;  
exploding stars (supernovae)  
are very useful  
(you'll see later on)

By the way, we are star-dust


# galaxies

Collections of  $\sim 10^{11} \sim 10^{12}$  Stars



# galaxies



The Tadpole Galaxy — UGC 10214  HUBBLESITE.org



# galaxies

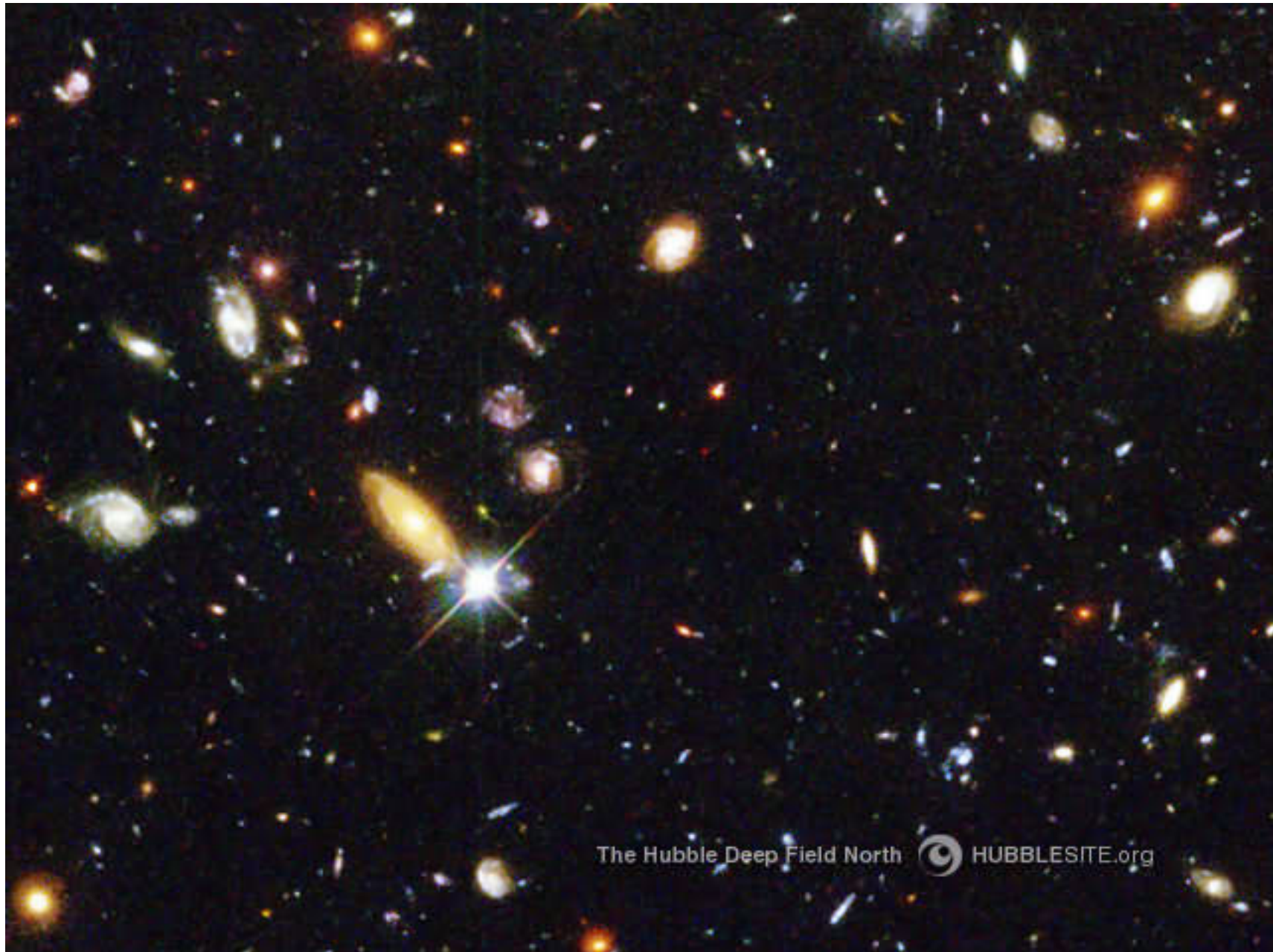


The Sombrero Galaxy — M104  HUBBLESITE.org

groups



# Hubble deep field

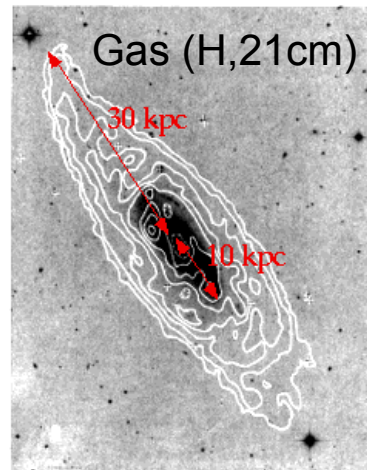
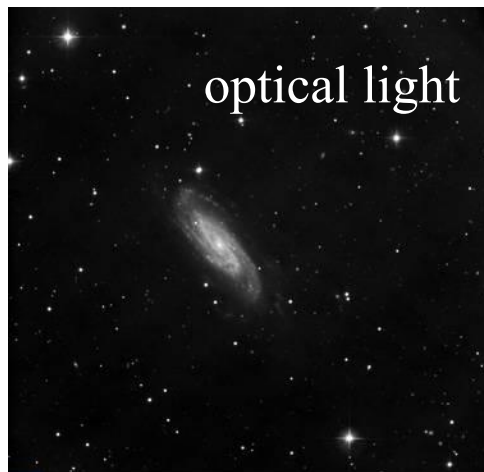


# There is more than meets the eye

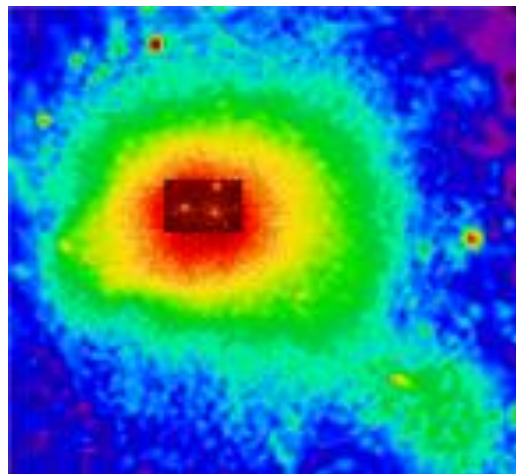
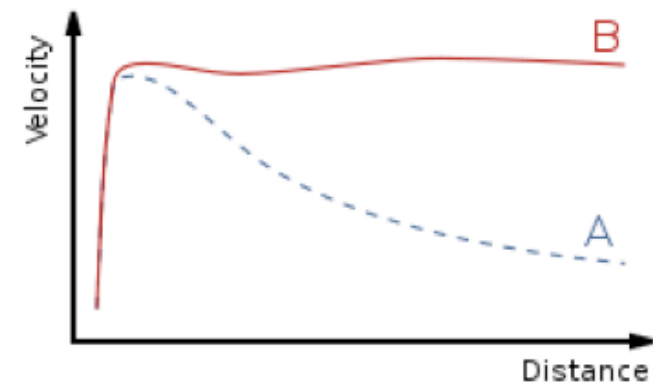
In the solar system sun + planets

Mass-to-light ratio

Let's consider galaxies



rotating



And clusters: Xrays

$$K.E. \sim \frac{3}{2}kT = \frac{3}{2}m_H\sigma_v^2$$

$$T \sim 6 \times 10^7 K; \lambda \sim \frac{c}{\nu} = \frac{ch}{KT}$$

# Content: Dark matter



**Fritz Zwicky**

# Dark matter

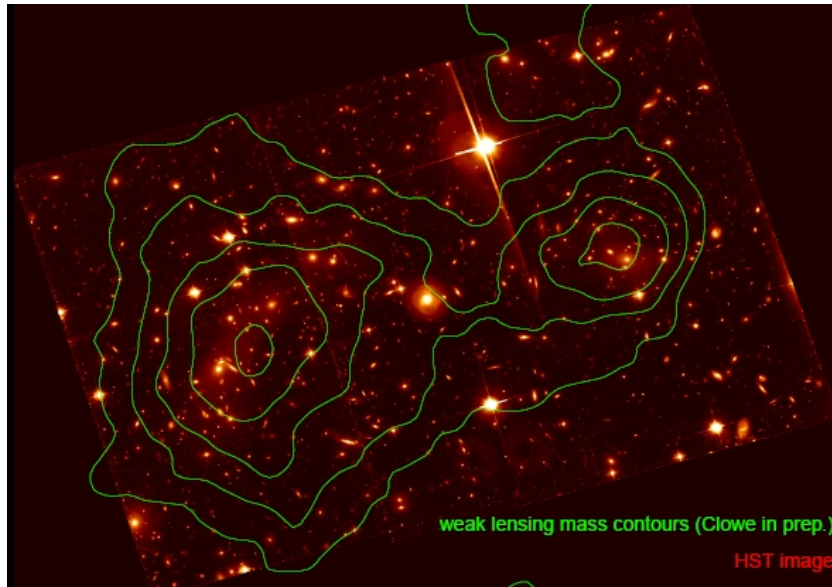


Gravitational lensing

# New evidence

REAL DATA!

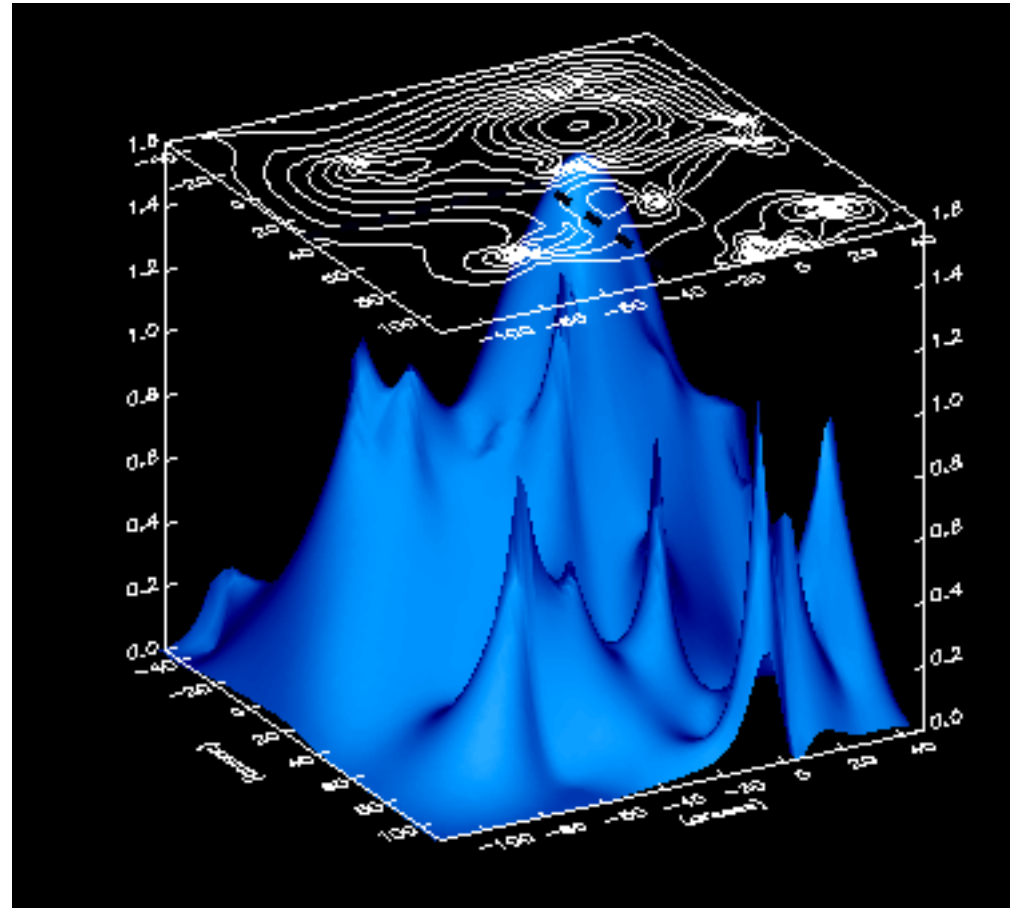
Bullet cluster



1E 0657-56



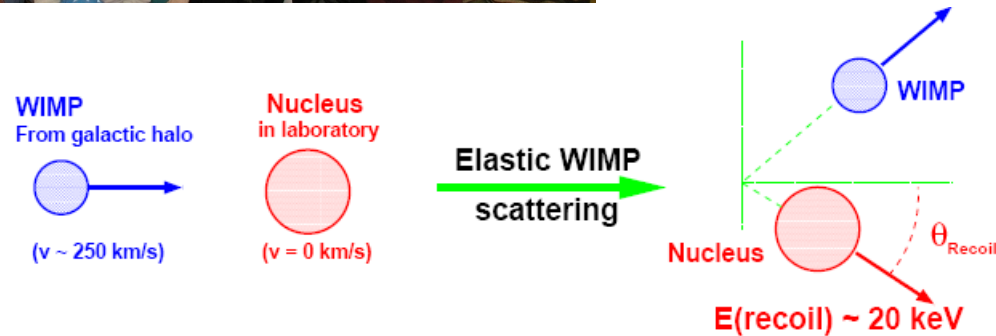
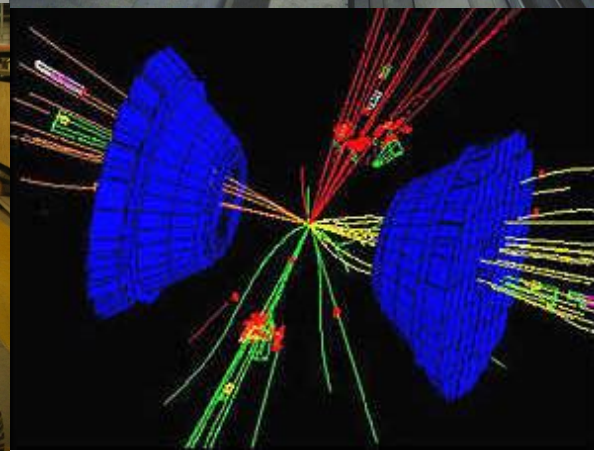
# Reconstructed dark matter distribution of cluster Abell 2218



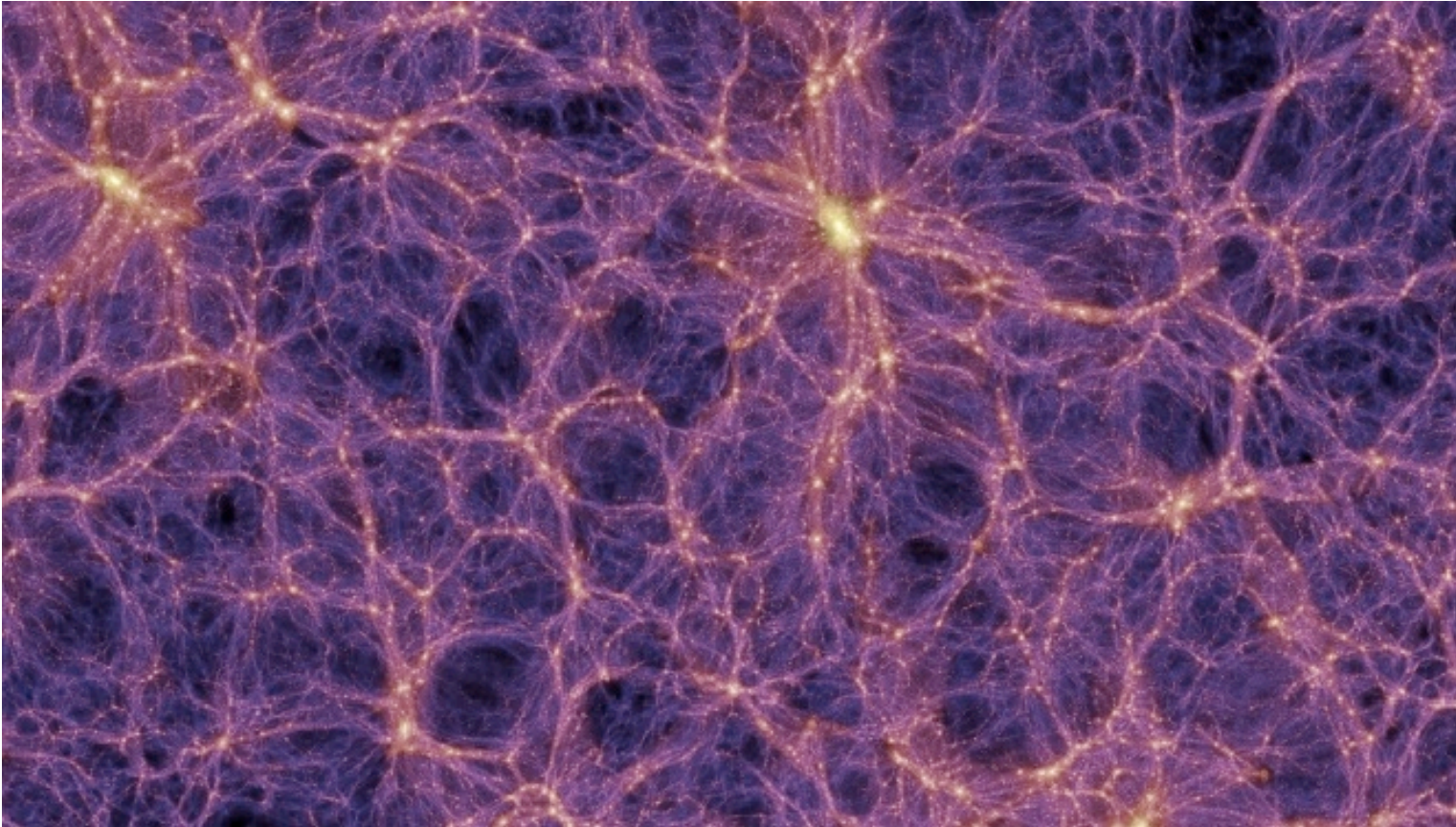
Abell 2218



# DIY dark matter

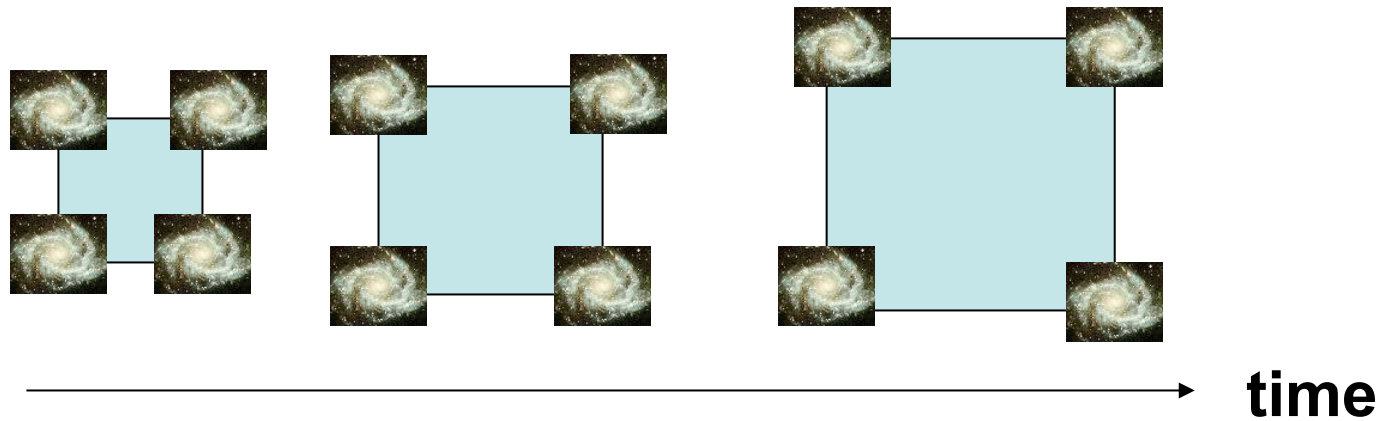


# Computer simulation of dark matter distribution



# Expanding Universe

# The scale factor $a$



$$\mathbf{r}(t) = \mathbf{r}(t_0) a(t)$$

**Comoving coordinates!**

$$\mathbf{v}_{12} = d\mathbf{r}_{12}/dt = \dot{a} \mathbf{r}_{12}(t_0) = \dot{a}/a \mathbf{r}_{12}(t)$$

Looks like Hubble law

$$H = \frac{\dot{a}}{a}$$

**Important!**

Distances are difficult:  
velocities are “easy”  
Thank you Edwin Hubble



# REDSHIFT

$$z = \frac{\lambda_{\text{obsv}} - \lambda_{\text{emit}}}{\lambda_{\text{emit}}} \quad \text{or} \quad 1 + z = \frac{\lambda_{\text{obsv}}}{\lambda_{\text{emit}}}$$

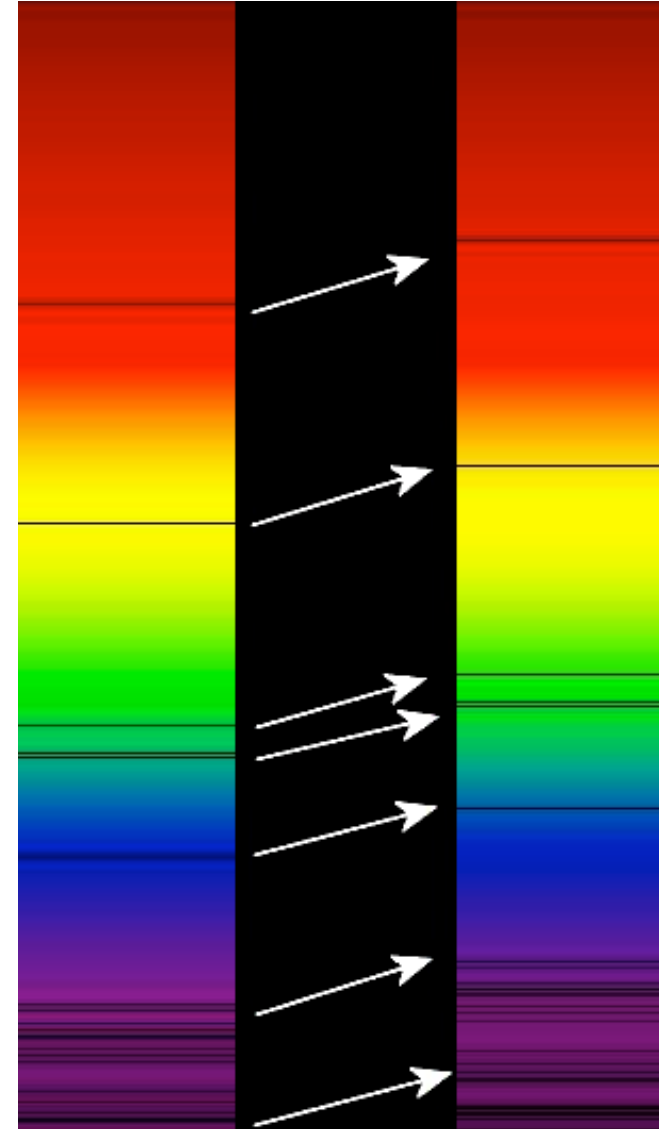
**In relativity:**

$$1 + z = \gamma \left( 1 + \frac{v_{\parallel}}{c} \right)$$

$$z \approx \frac{v_{\parallel}}{c} \quad \text{For small velocity}$$

or

$$1 + z = \frac{1 + v \cos(\theta)/c}{\sqrt{1 - v^2/c^2}}$$

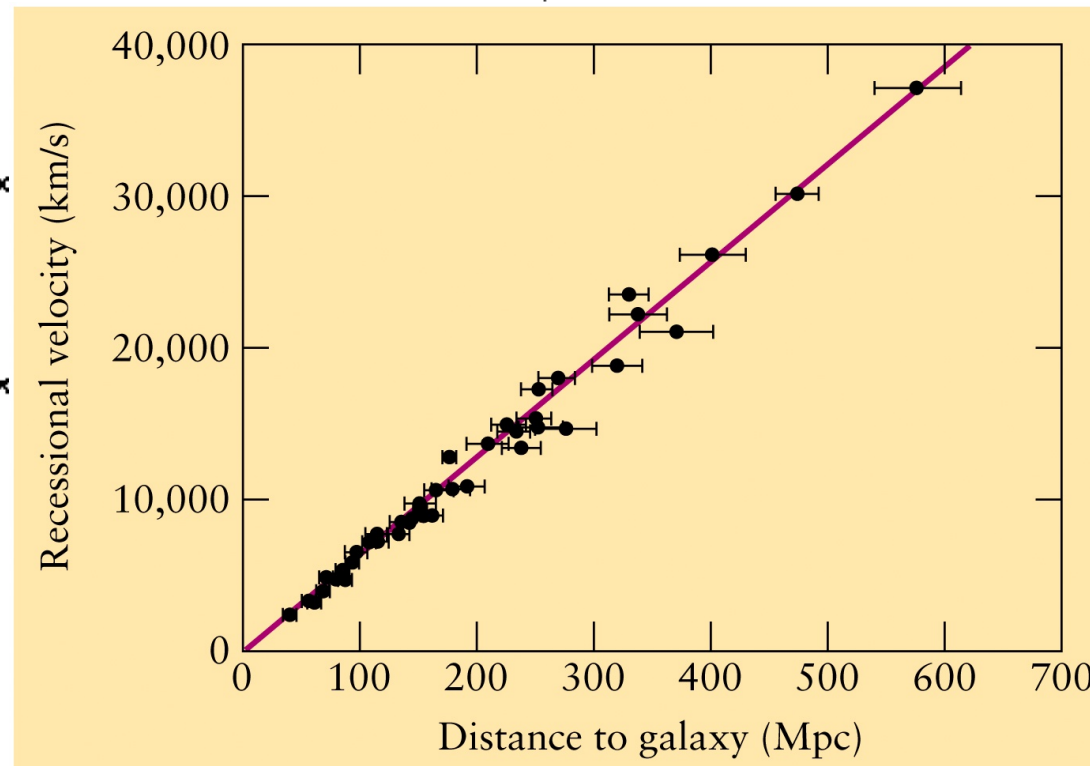


# Hubble's Law

$$cz = v = H_0 d$$

$$H_0 = 74.2 \pm 3.8 \text{ km/s/Mpc}$$

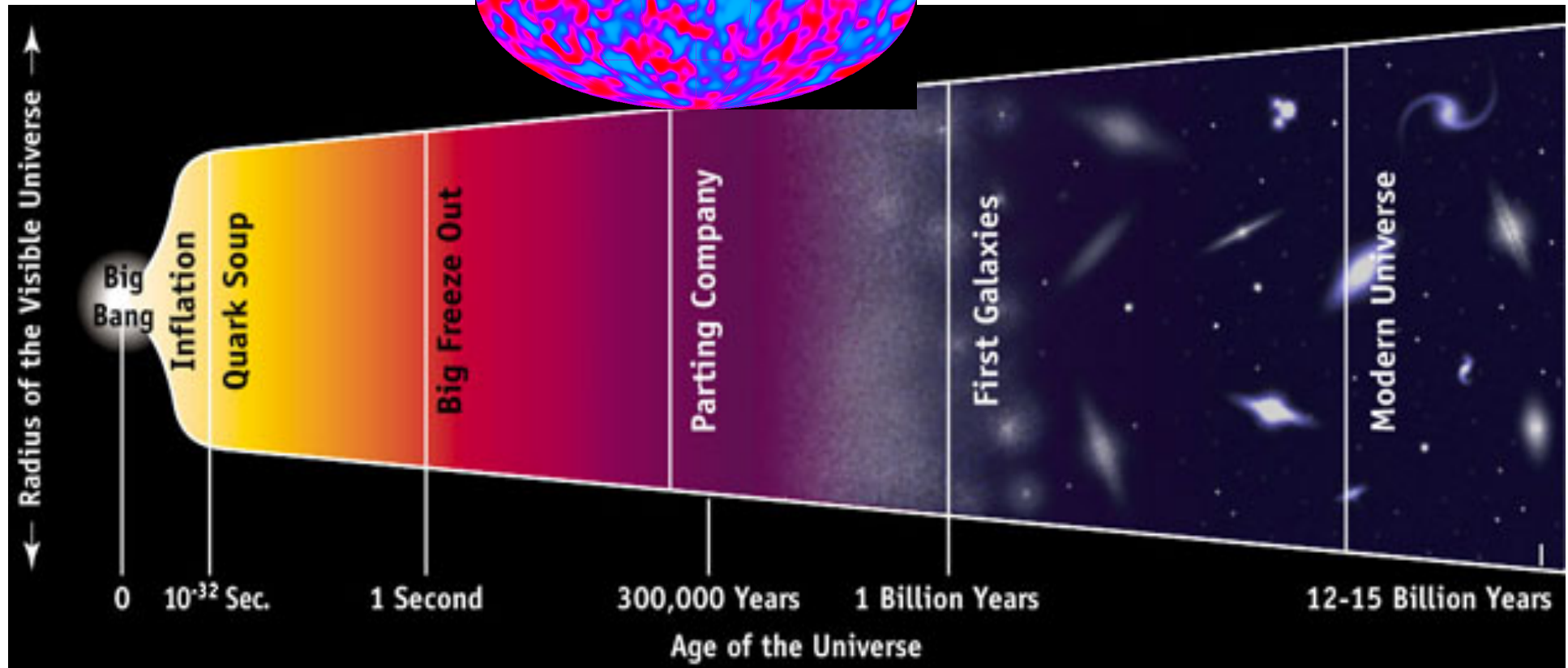
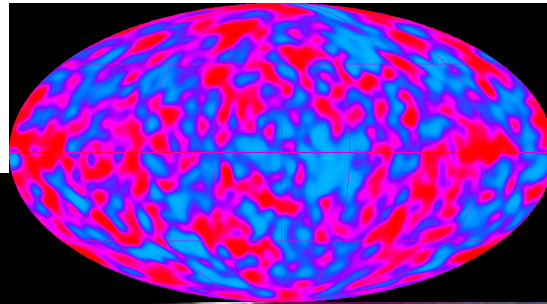
Hubble 1929  
(PNAS vol 15)



The universe is expanding!

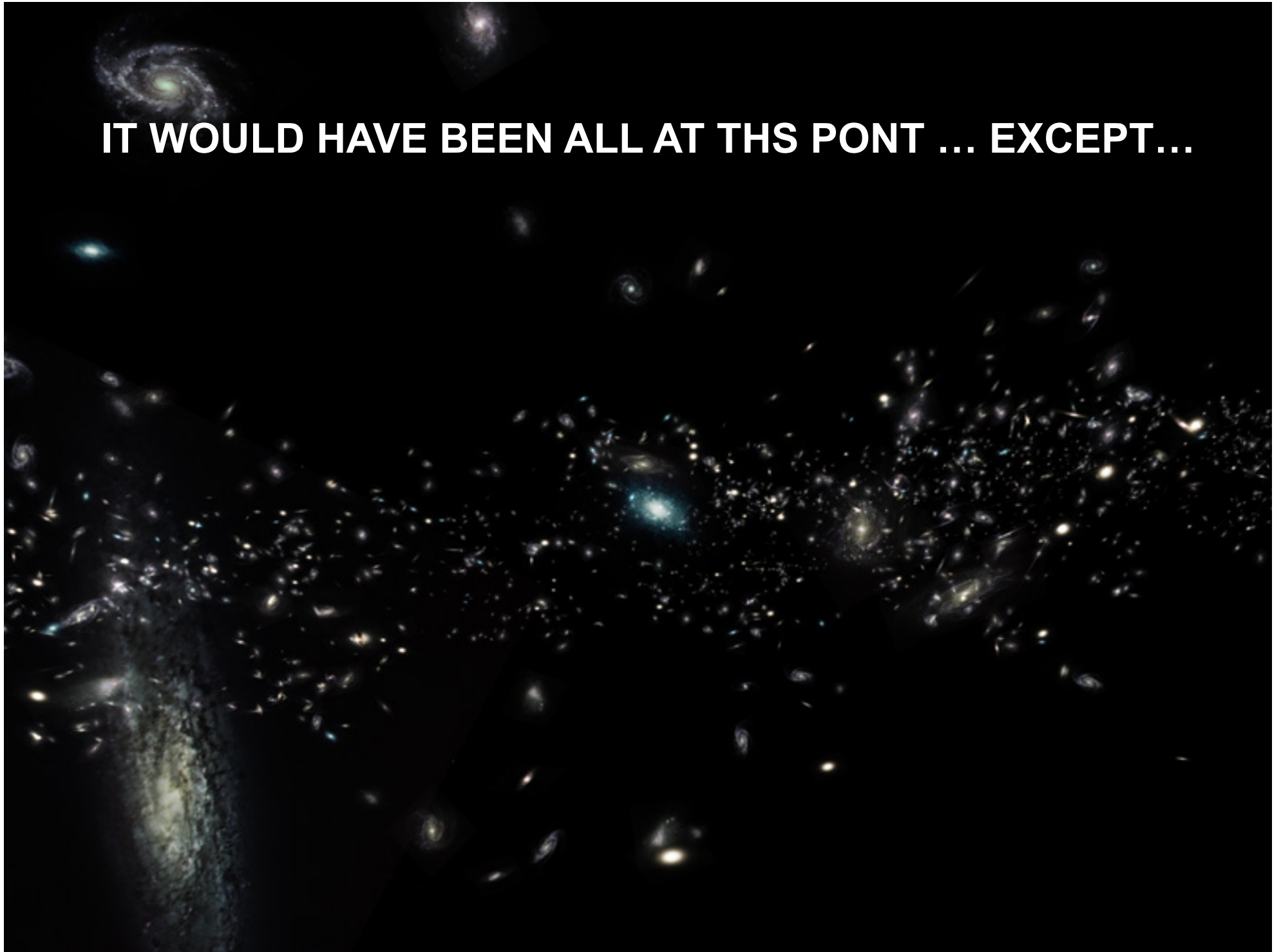
The universe had a beginning!

The extremely successful BIG BANG theory!



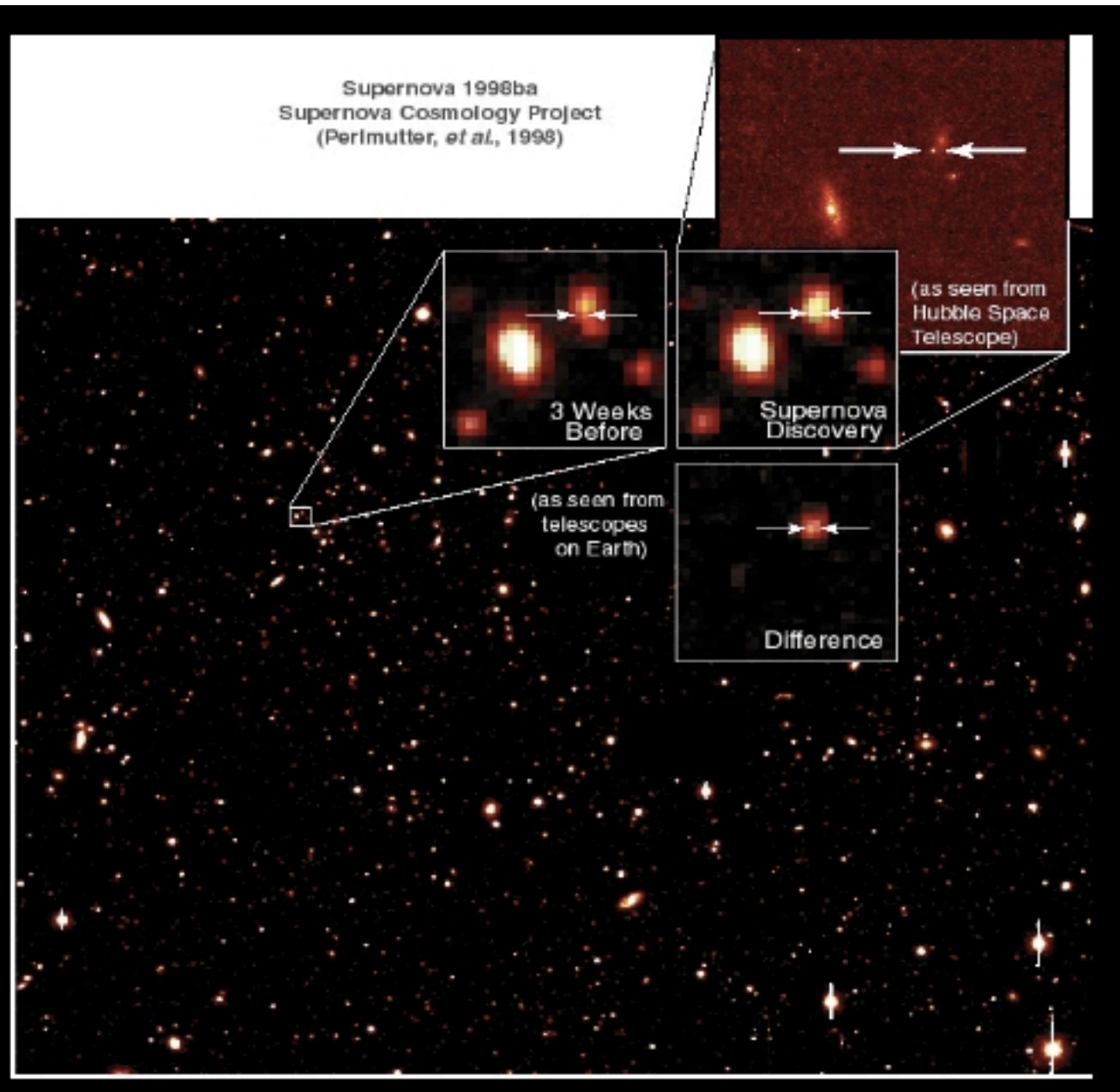


**IT WOULD HAVE BEEN ALL AT THIS POINT ... EXCEPT...**



# Standard candles

Strategy:  
stare at one  
patch of  
the sky for a  
long time,  
waiting for  
a star to  
blow up.





1998!

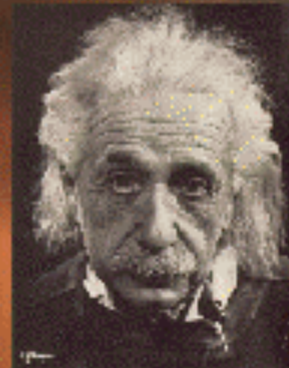


Humm the expansion seems to accelerate...

## Einstein's Greatest Blunder

1909: Einstein's general theory of relativity  
*predicts the expansion of the universe!*

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

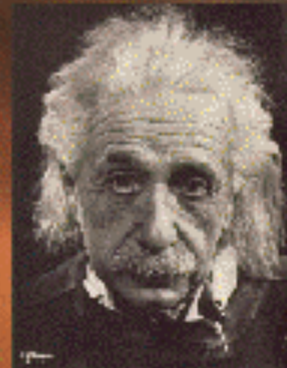


Dis iss clearly  
wrong!

## Einstein's Greatest Blunder

1909: Einstein's general theory of relativity  
*predicts the expansion of the universe!*

$$G_{\mu\nu} = 8\pi T_{\mu\nu} + \Lambda\delta_{\mu\nu}$$

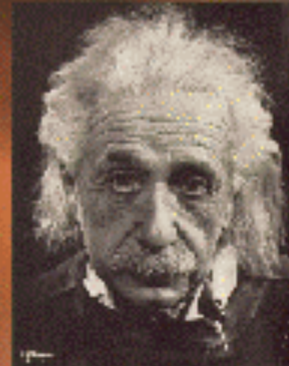
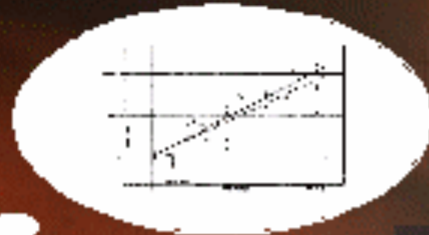


Better!

Einstein introduced a fudge factor to make the  
universe static: the *cosmological constant*,  
 $\Lambda$  = the energy of empty space.

# Einstein's Greatest Blunder

1929: Hubble discovers the cosmological expansion.

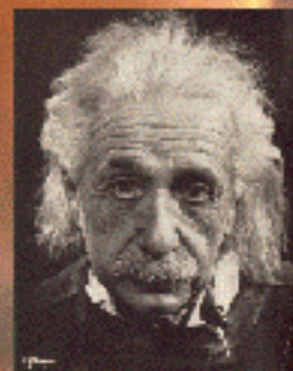
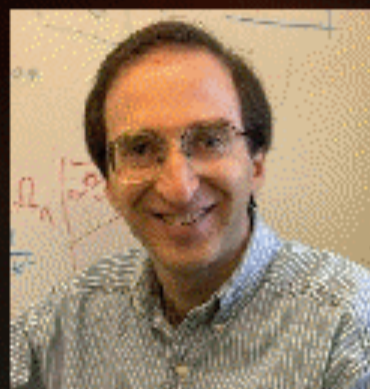


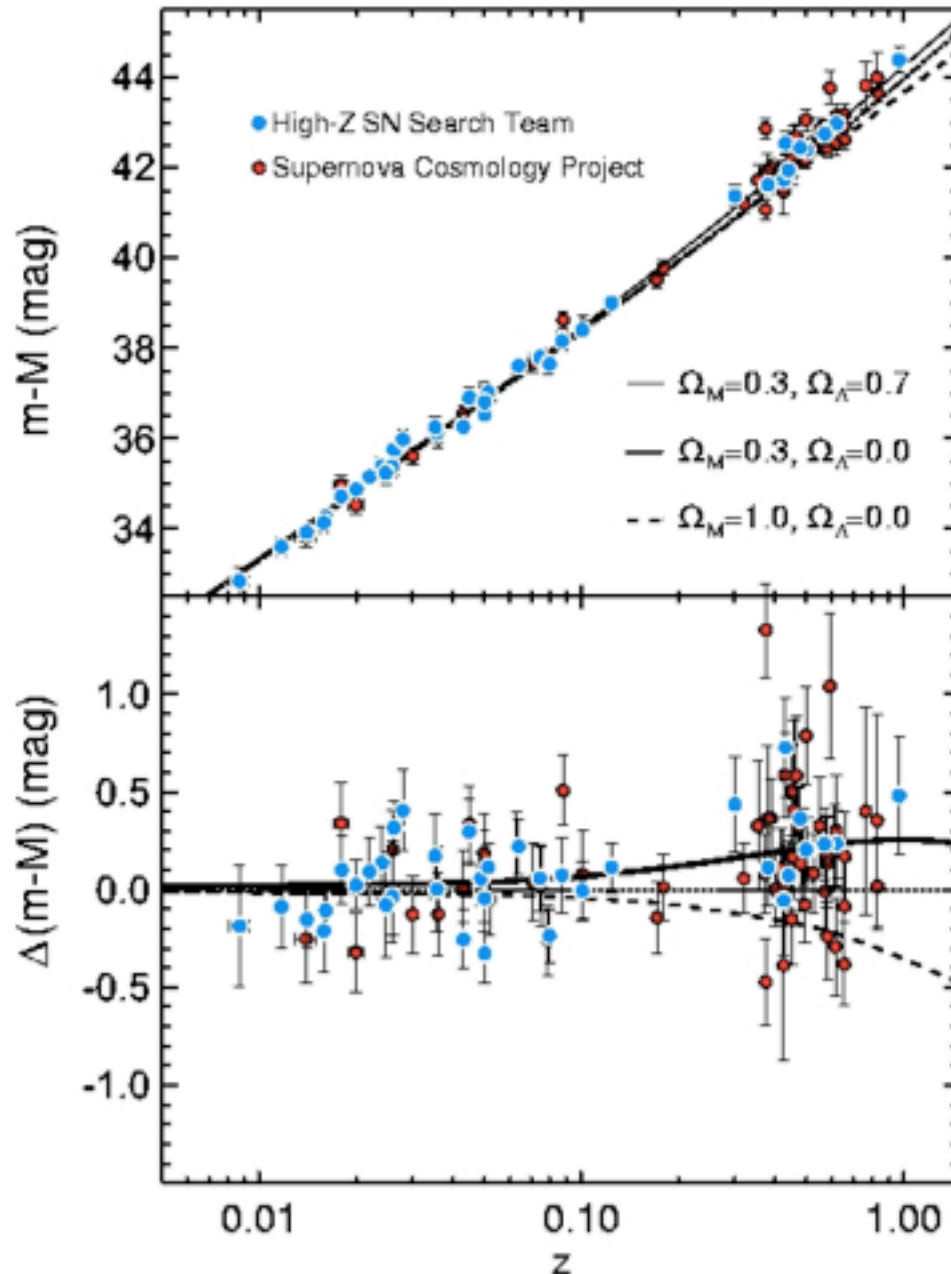
D'oh!

Courtesy of W. Kinney

# Einstein's Greatest Blunder

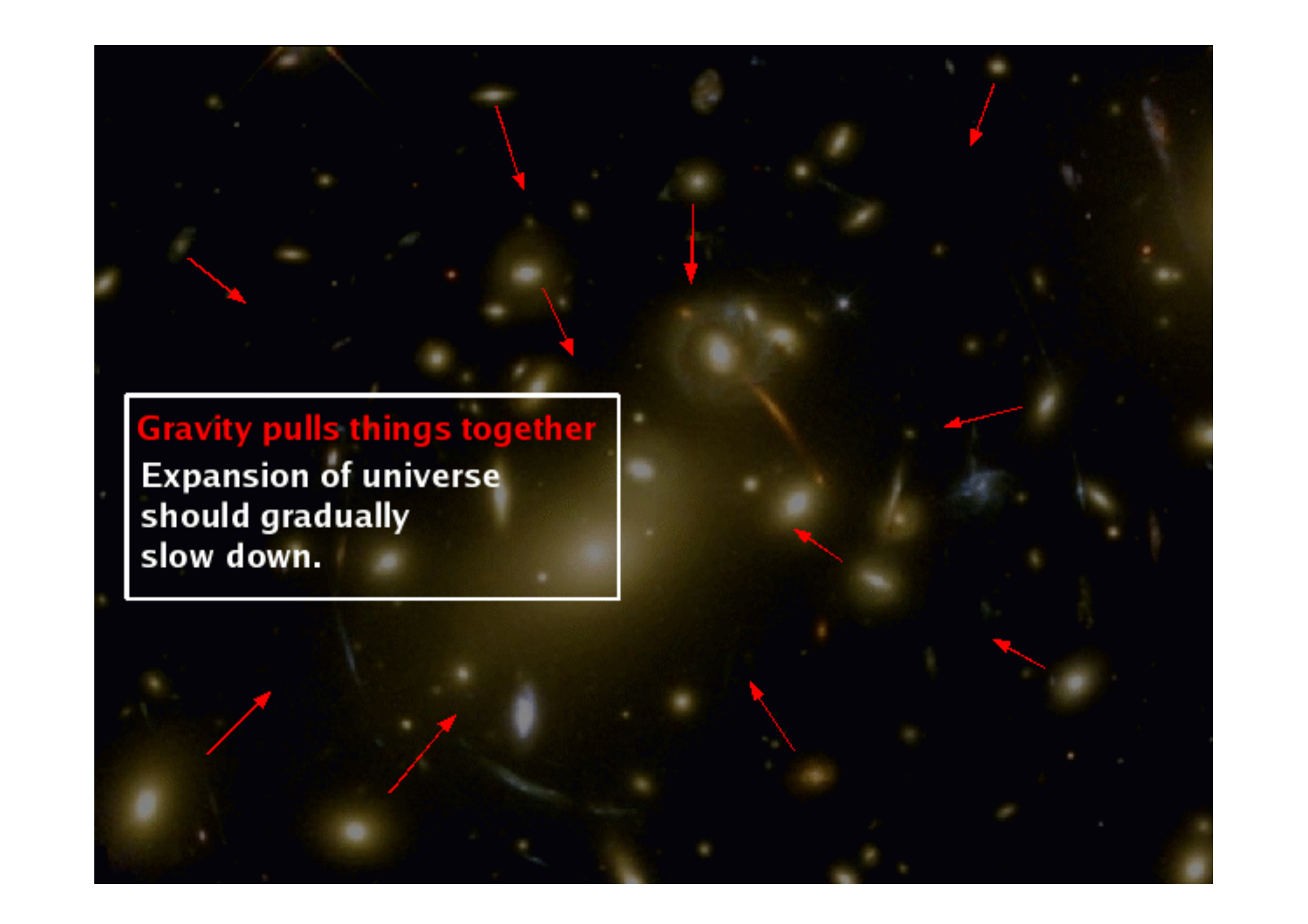
1998: Accelerating expansion





- This program gives most accurate value for Hubble's constant
  - $H=74.2 \text{ km/s/Mpc}$ , error  $<4\%$
- Find acceleration, not deceleration!
  - Very subtle, but really is there in the data!
  - Profound result!



The image shows a dark space filled with numerous galaxies of various shapes and colors, including yellow, white, and blue. Red arrows are scattered throughout the field, all pointing towards a central area, which visually represents the concept of gravity pulling objects together. A white-bordered box with red and white text is overlaid on the left side of the image.

**Gravity pulls things together**  
Expansion of universe  
should gradually  
slow down.

**Something** is pushing the galaxies apart

**DARK ENERGY**



# Friedmann equations

NOT independent!

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho(t) - \frac{kc^2}{R_0^2 a^2}$$

$$\dot{\epsilon} + 3\frac{\dot{a}}{a}(\epsilon + P) = 0$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3c^2}(\epsilon + 3P)$$

$$\rho(t)c^2 = \epsilon(t)$$

If you want to solve for

$$a(t), \epsilon(t), P(t)$$

need more info...

$$P = P(\epsilon)$$

$$P = w\epsilon$$

Interesting cases:

Non-relativistic matter  $w \simeq 0$

R adiation  $w = 1/3$

Accelerating fluid  $w < -1/3$

Cosmological constant  $w = -1$

This is weird.....

but looks like we are stuck with it

# Parameters: the smooth Universe

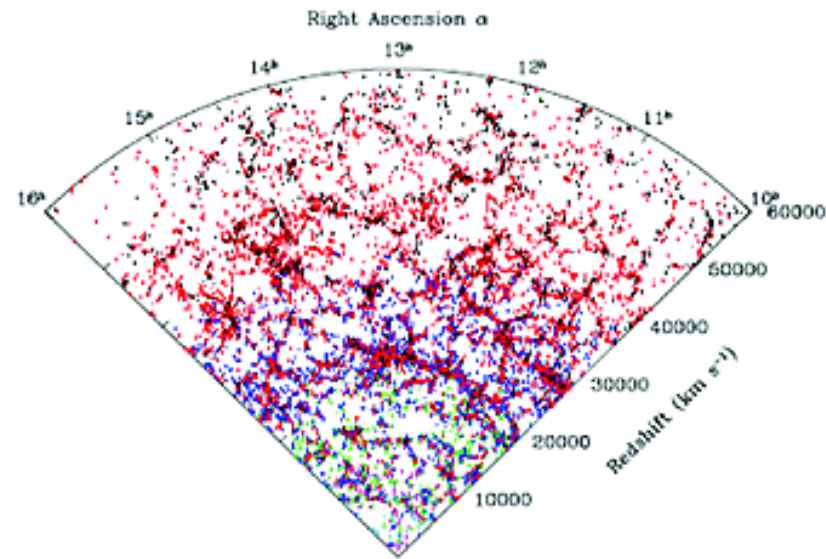
$$\Omega = \Omega_c + \Omega_b + \Omega_\Lambda \quad \Omega_m = \Omega_c + \Omega_b$$

+radiation

During the Universe expansion different components scale Differently (eq. of state parameter)

Next: the perturbations

# Parameters describing structure



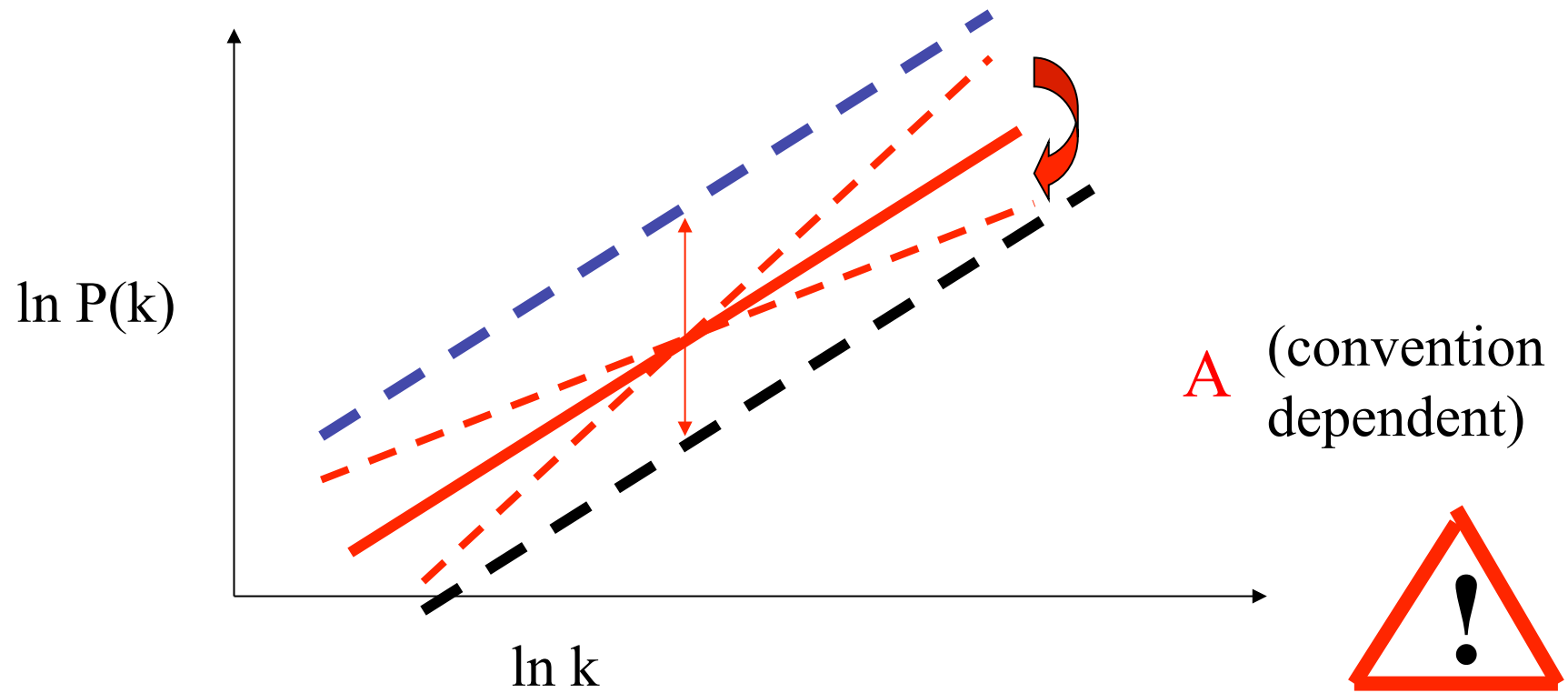
These fluctuations grew under gravity

THE POWER SPECTRUM

Primordial power spectrum =  $A k^n$

slope

Amplitude of the power law



# The standard cosmological model (LCDM)

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Only 6 parameters, fits observations of the Universe from  $z=1100$  to today.

Spatially flat, made of baryonic matter, cold dark matter, cosmological constant, radiation-unimportant today-, present-day expansion rate

inflationary scenario generated perturbations:  
amplitude and slope of the power spectrum of primordial perturbations

Optical depth (reionization)

*Extremely successful model*

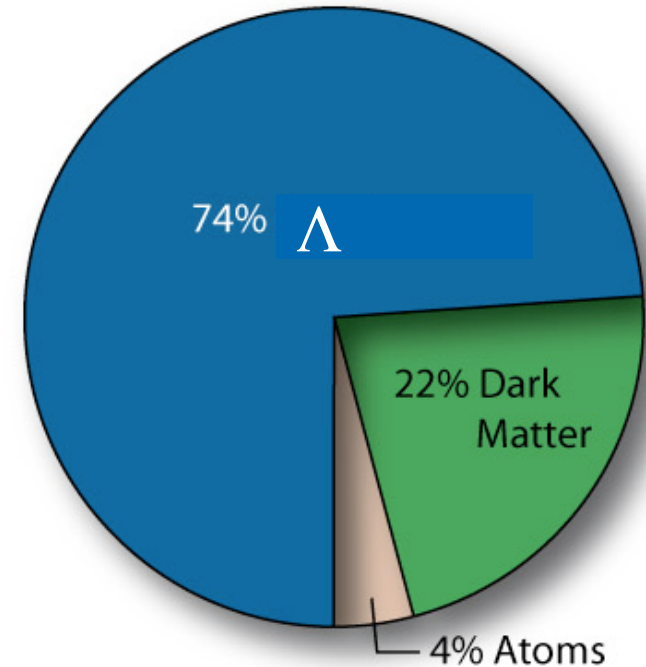
# The standard cosmological model

## $\Lambda$ CDM model

Spatially flat Universe

Power-law, primordial power spectrum

Only 6 parameters

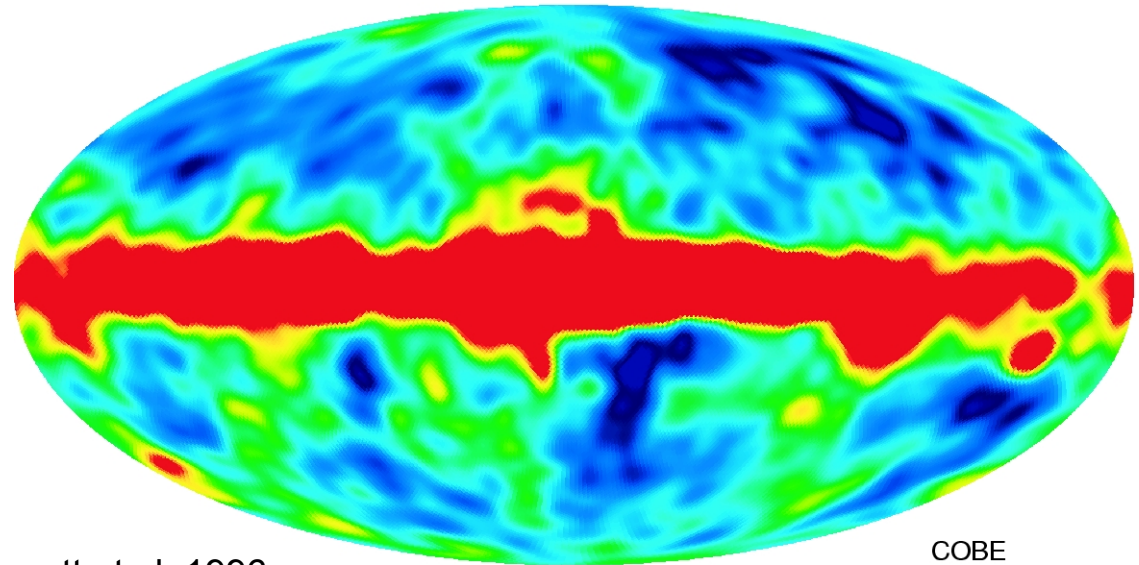


Parameter	WMAP Only	WMAP +CBI+VSA	WMAP+ACBAR +BOOMERanG	WMAP + 2dFGRS	WMAP+ SDSS	WMAP+ SNLS	WMAP + SN Gold
$100\Omega_b h^2$	$2.233^{+0.072}_{-0.091}$	$2.212^{+0.066}_{-0.084}$	$2.231^{+0.070}_{-0.088}$	$2.223^{+0.066}_{-0.083}$	$2.233^{+0.062}_{-0.086}$	$2.233^{+0.069}_{-0.088}$	$2.227^{+0.065}_{-0.082}$
$\Omega_m h^2$	$0.1268^{+0.0072}_{-0.0095}$	$0.1233^{+0.0070}_{-0.0086}$	$0.1259^{+0.0077}_{-0.0095}$	$0.1262^{+0.0045}_{-0.0062}$	$0.1329^{+0.0056}_{-0.0075}$	$0.1295^{+0.0056}_{-0.0072}$	$0.1349^{+0.0056}_{-0.0071}$
$h$	$0.734^{+0.028}_{-0.038}$	$0.743^{+0.027}_{-0.037}$	$0.739^{+0.028}_{-0.038}$	$0.732^{+0.018}_{-0.025}$	$0.709^{+0.024}_{-0.032}$	$0.723^{+0.021}_{-0.030}$	$0.701^{+0.020}_{-0.026}$
$A$	$0.801^{+0.043}_{-0.054}$	$0.796^{+0.042}_{-0.052}$	$0.798^{+0.046}_{-0.054}$	$0.799^{+0.042}_{-0.051}$	$0.813^{+0.042}_{-0.052}$	$0.808^{+0.044}_{-0.051}$	$0.827^{+0.045}_{-0.053}$
$\tau$	$0.088^{+0.028}_{-0.034}$	$0.088^{+0.027}_{-0.033}$	$0.088^{+0.030}_{-0.033}$	$0.083^{+0.027}_{-0.031}$	$0.079^{+0.029}_{-0.032}$	$0.085^{+0.028}_{-0.032}$	$0.079^{+0.028}_{-0.034}$
$n_s$	$0.951^{+0.015}_{-0.019}$	$0.947^{+0.014}_{-0.017}$	$0.951^{+0.015}_{-0.020}$	$0.948^{+0.014}_{-0.018}$	$0.948^{+0.015}_{-0.018}$	$0.950^{+0.015}_{-0.019}$	$0.946^{+0.015}_{-0.019}$
$\sigma_8$	$0.744^{+0.050}_{-0.060}$	$0.722^{+0.043}_{-0.053}$	$0.739^{+0.047}_{-0.059}$	$0.737^{+0.033}_{-0.045}$	$0.772^{+0.036}_{-0.048}$	$0.758^{+0.038}_{-0.052}$	$0.784^{+0.035}_{-0.049}$
$\Omega_m$	$0.238^{+0.030}_{-0.041}$	$0.226^{+0.026}_{-0.036}$	$0.233^{+0.029}_{-0.041}$	$0.236^{+0.016}_{-0.024}$	$0.266^{+0.026}_{-0.036}$	$0.249^{+0.024}_{-0.031}$	$0.276^{+0.023}_{-0.031}$



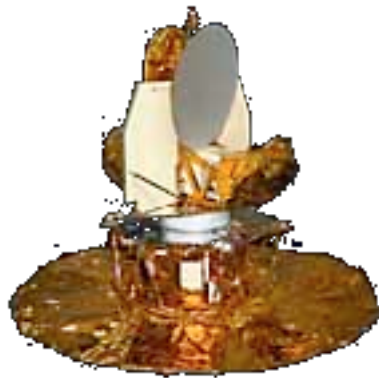
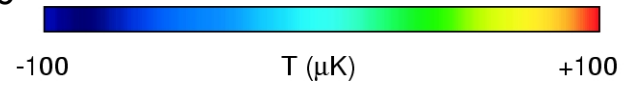


COBE 1992

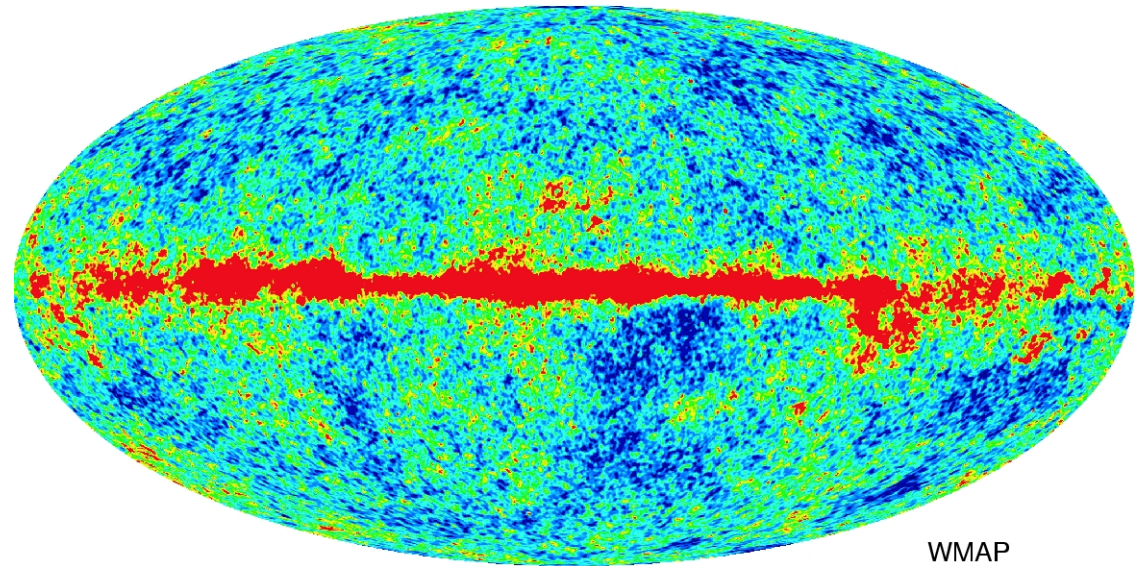


Bennett et al. 1996

COBE

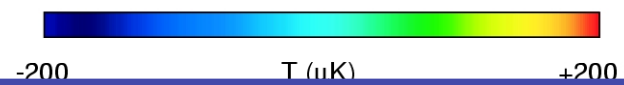


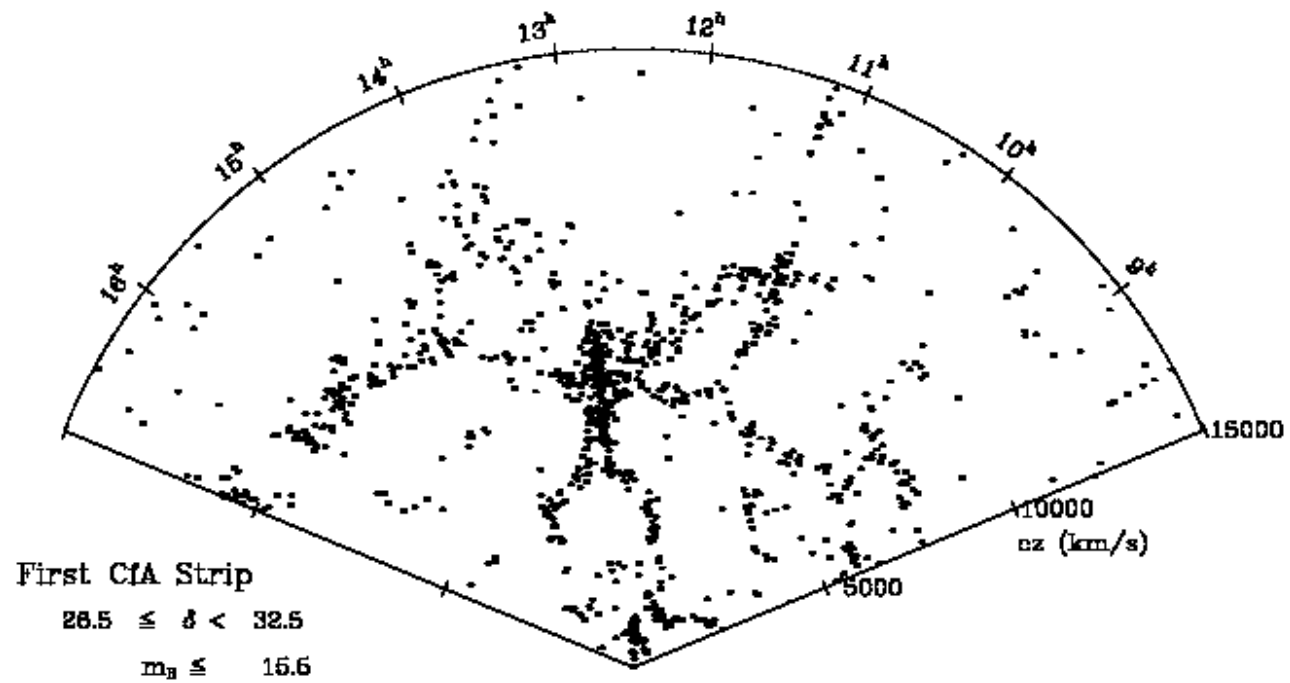
WMAP 2003



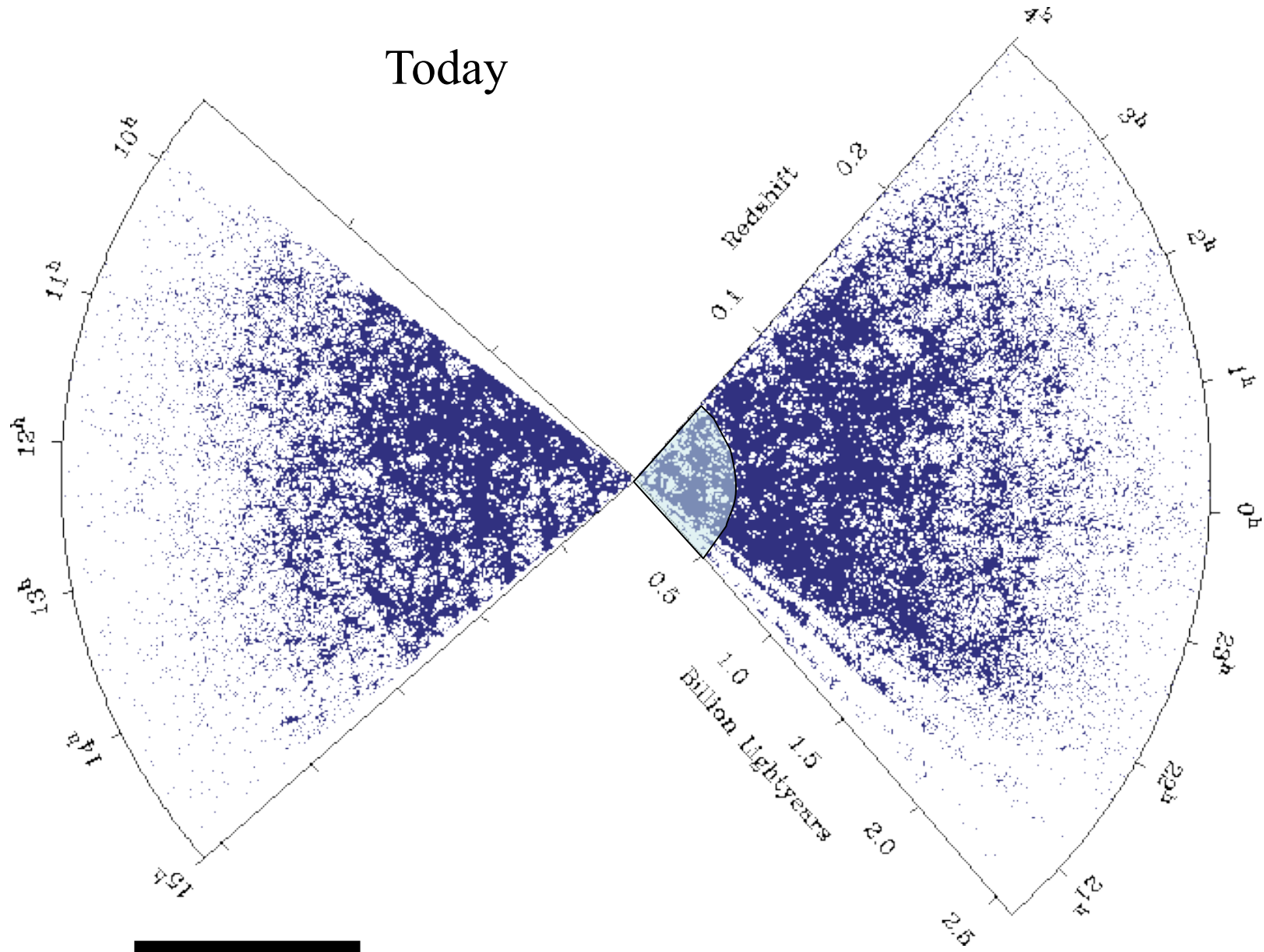
Bennett et al 2003

WMAP





Today

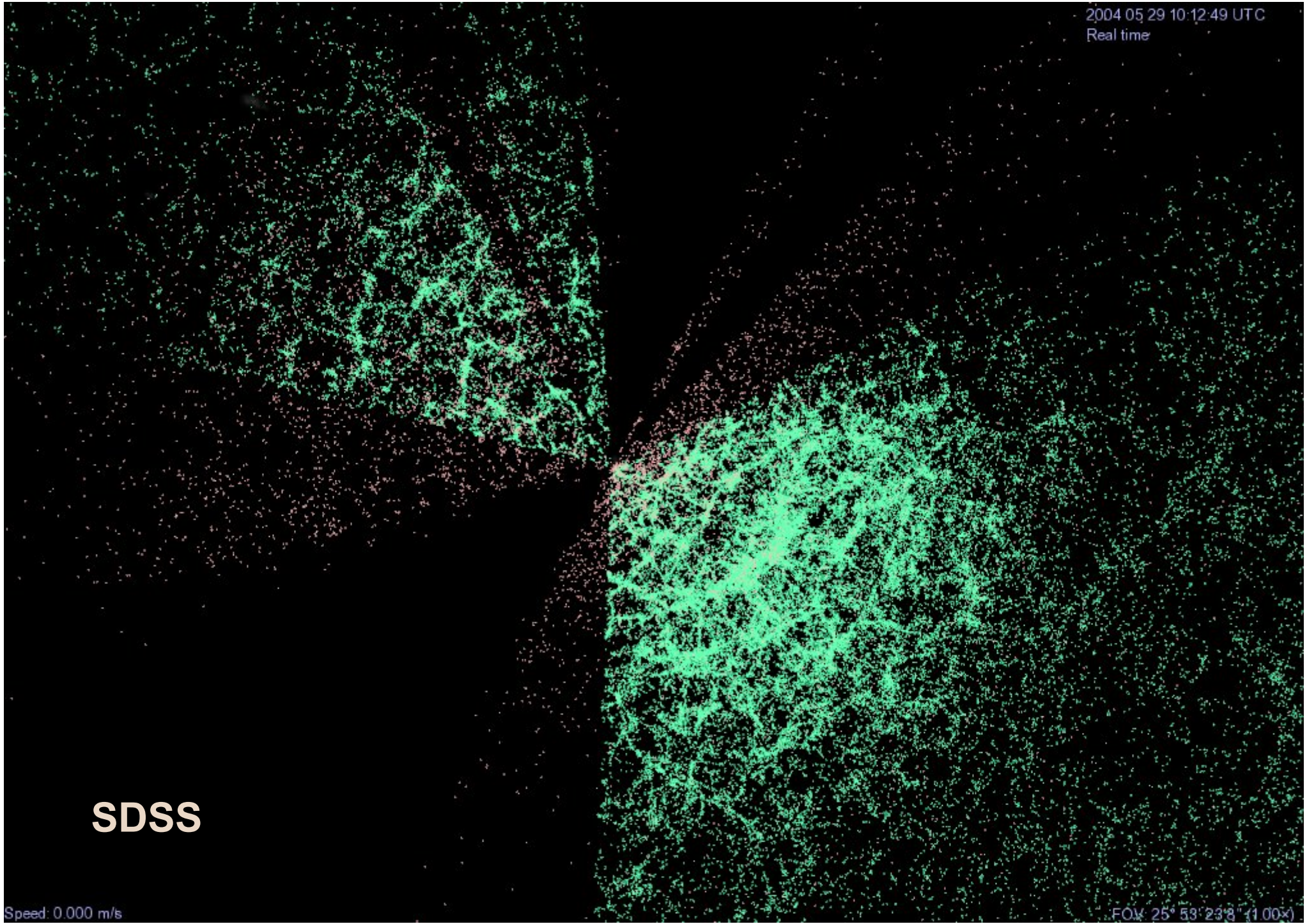


2004 05 29 10:12:49 UTC  
Real time

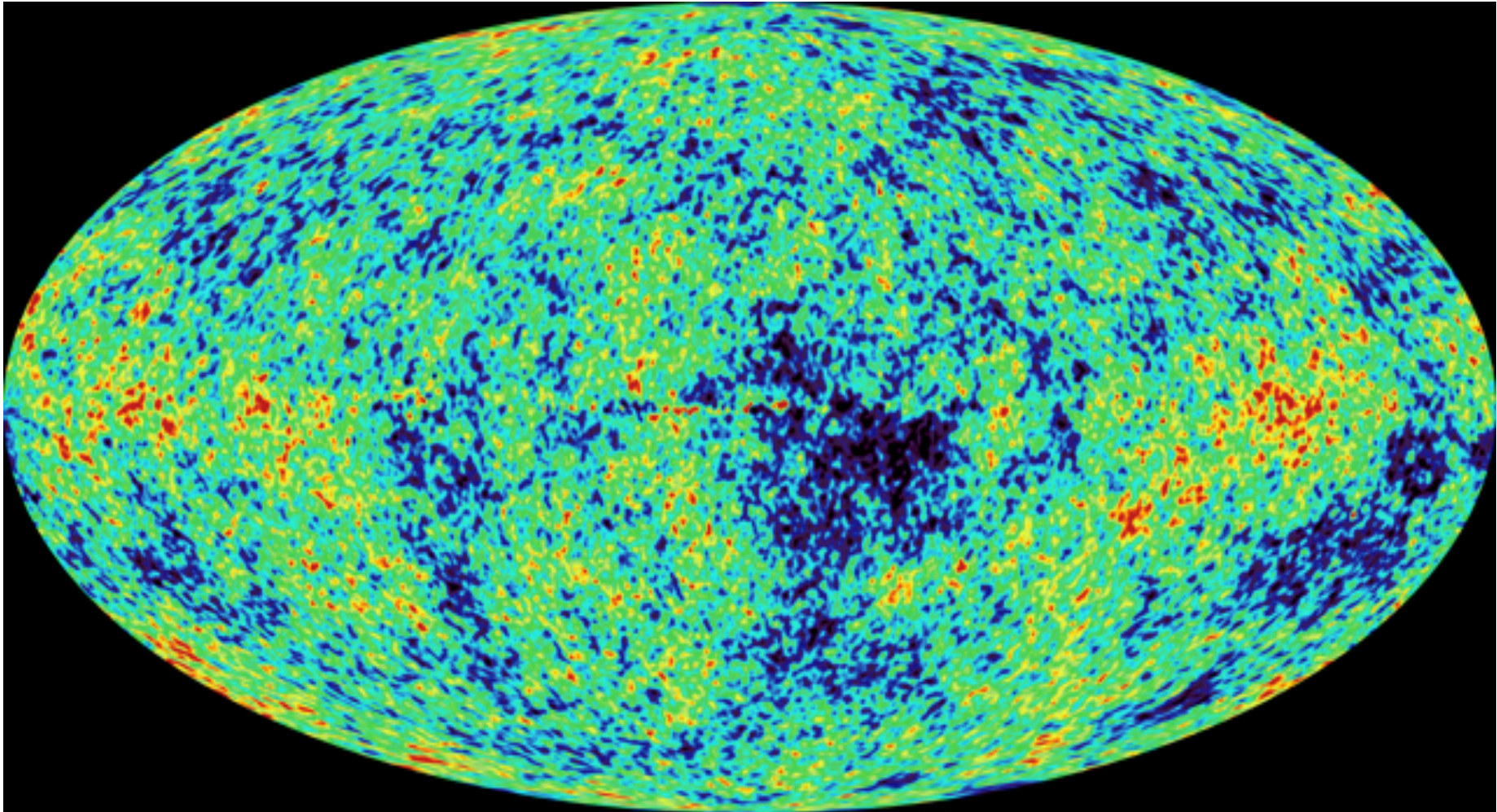
**SDSS**

Speed: 0.000 m/s

FOV: 25° 53' 23.8" (1.00x)



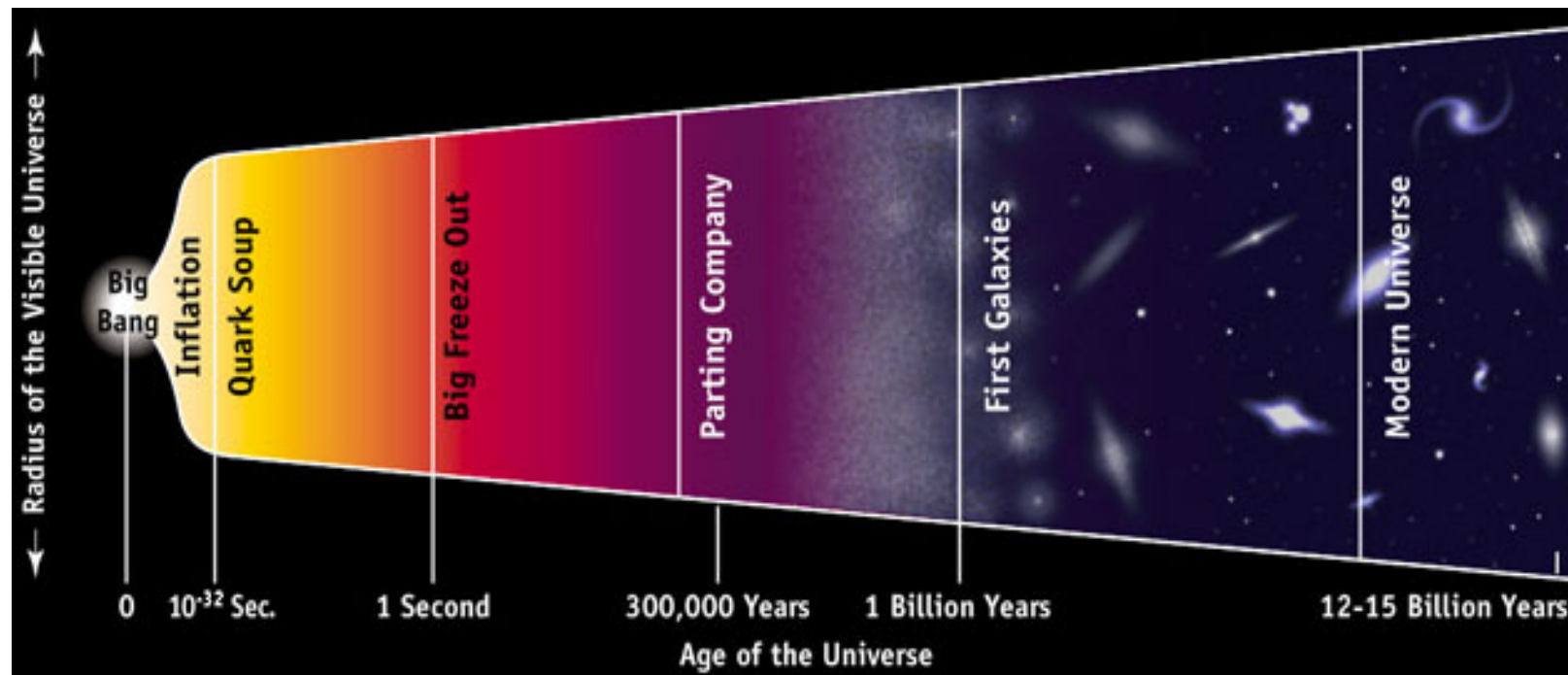
# The Cosmic Microwave background



The universe cools as it expands; the stretching of light results in a reduction of temperature (think Wien's Law).

*If the universe is large, cool, and expanding today, it must have been smaller, warmer, and expanding in the past.*

This leads to the cosmic microwave background.

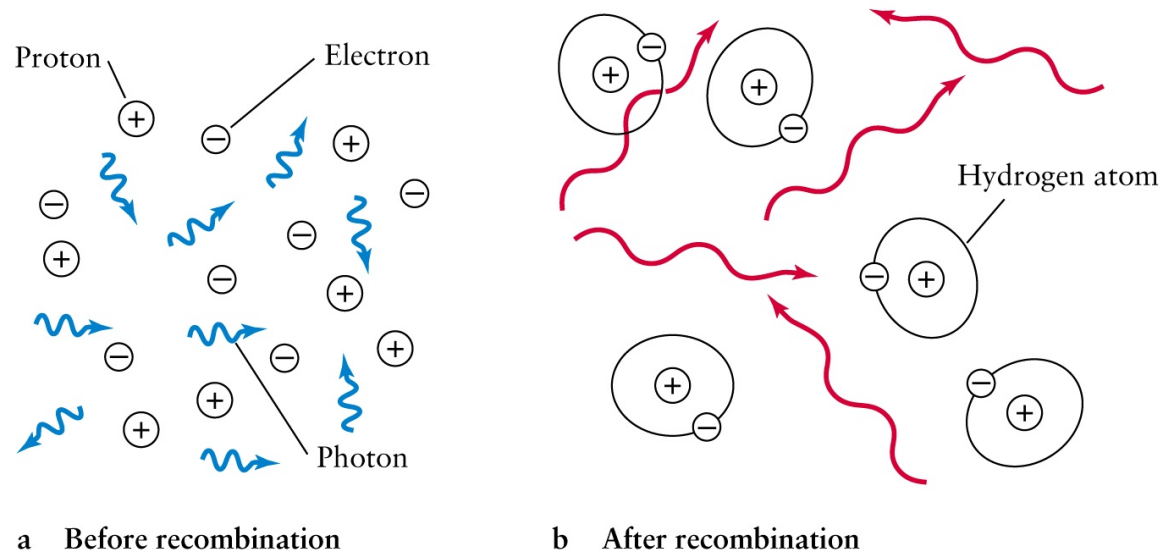


# The cosmic microwave background (CMB) radiation

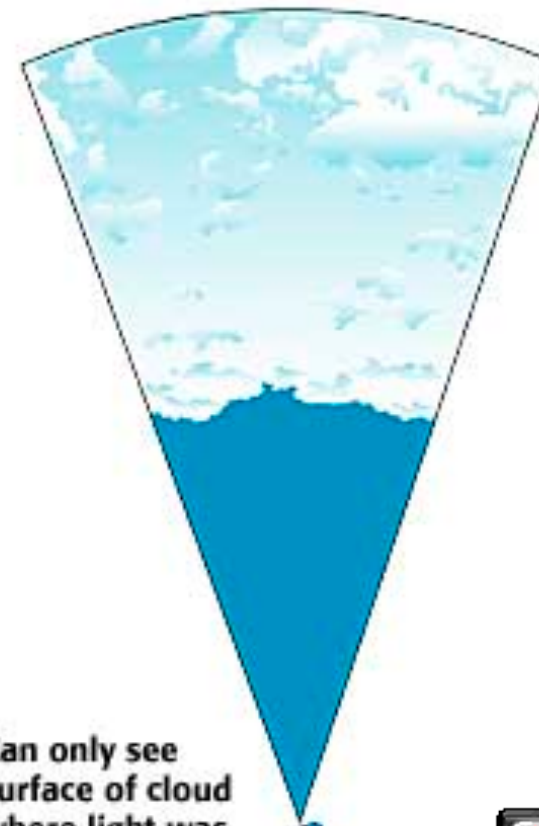
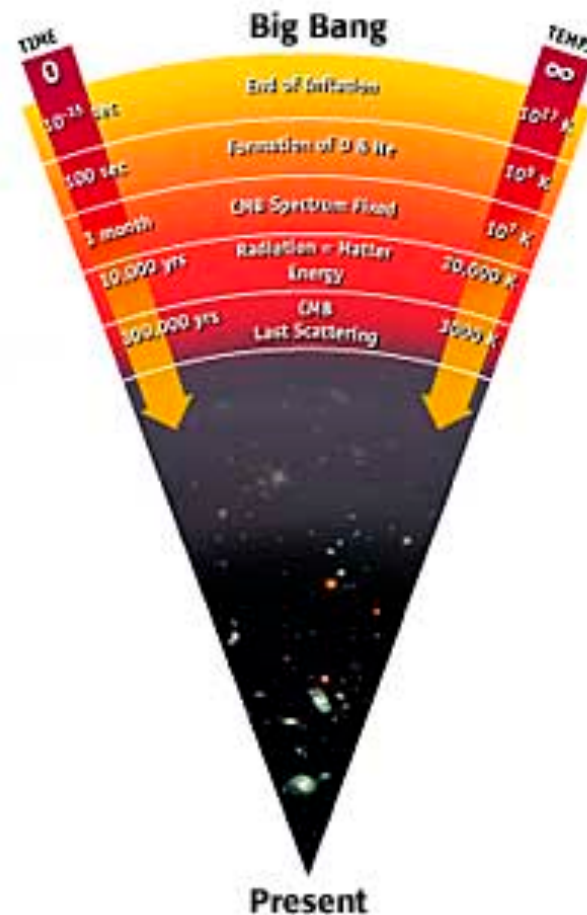
Regular hydrogen gas lets light pass through more or less unimpeded. This is the case today, where the hydrogen gas is either cold and atomic, or very thin, hot, and ionized.

But in the early universe, when it was much warmer, the gas would have been ionized, and the universe opaque to light—as if you were in a dense fog.

As the universe cooled, the electrons and protons “recombined” into normal hydrogen, and the universe suddenly became transparent.



# The last scattering surface: a snapshot of the early universe



Can only see surface of cloud where light was last scattered.



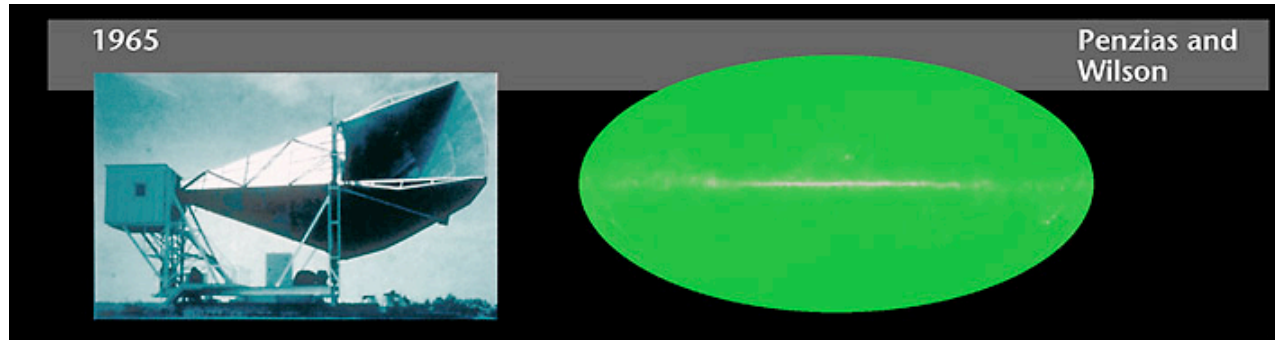
The Cosmic Microwave Background Radiation's "surface of last scatter" is analogous to the light coming through the clouds to our eye on a cloudy day.





# Some history

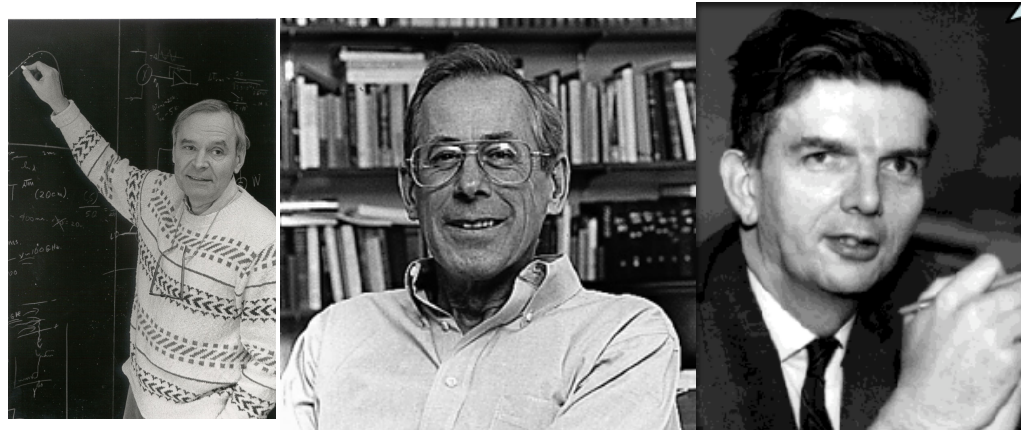
## Discovery



1978 Nobel

Two engineers for Bell Labs accidentally discovered the CMB radiation, as a uniform glow across the sky in the radio part of the spectrum, in 1965. It is the blackbody emission of hot, dense gas ( $T \sim 3000$  K,  $\lambda_{\text{max}} \sim 1000$  nm) red-shifted by a factor of 1000, to a peak wavelength of 1 mm and  $T \sim 3$  K.

“The primordial fireball”

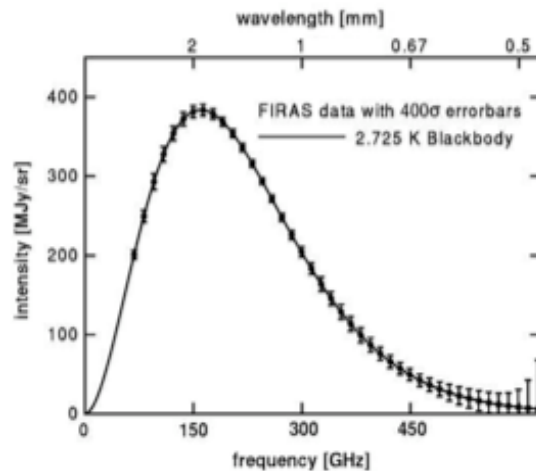


Support to the hot  
big bang theory

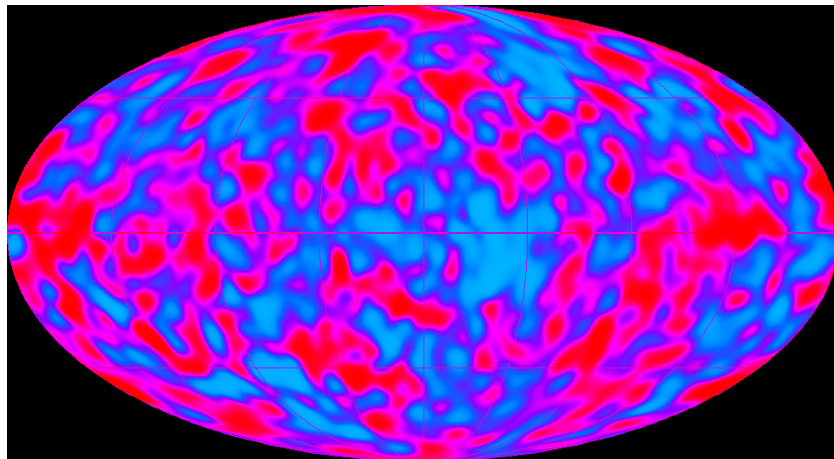
“Well boys, we have  
been scooped”

# Some history

COBE (1992): Nobel prize in Physics in 2006



Mather: for measuring the CMB to be a Blackbody



Smoot: for measuring the *tiny temperature variations*

Density fluctuations: seeds of cosmological structures

"These measurements... marked the inception of *cosmology as a precise science*"

# Clustering and gravitational instability

If the Universe is homogeneous and isotropic on large scales  $\bar{\rho} = \langle \rho \rangle = \frac{1}{V} \int_V \rho d^3r$   
Dark matter

$$\delta = \frac{\rho - \bar{\rho}}{\bar{\rho}}; \text{ where } \rho(r, t), \bar{\rho}(t)$$

$$\begin{aligned} \rho_0 &= 0.3\rho_{c,0} = 3 \times 10^{-27} \text{ kg/m}^3 \\ \delta_{you} &= 2 \times 10^{30} \end{aligned}$$

How did we get there from an almost uniform distribution?

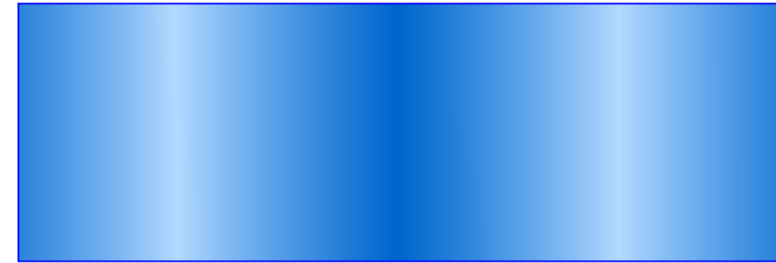
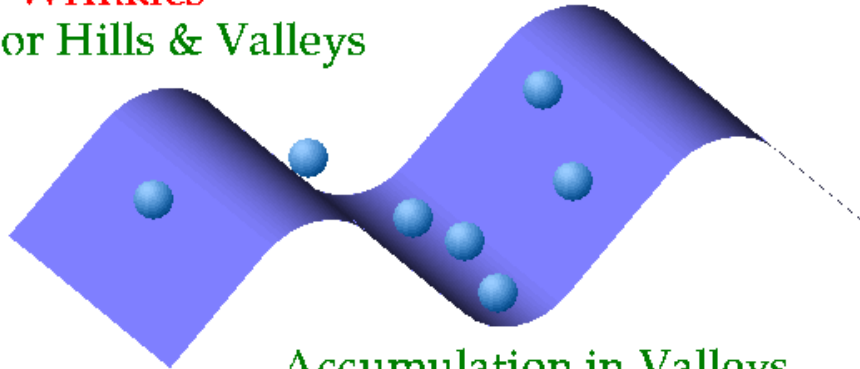
Recall Penzias and Wilson!!!!

This has puzzled cosmologists for decades and (with hindsight)  
Is one of the crucial evidences for DARK MATTER  
(and dark energy)

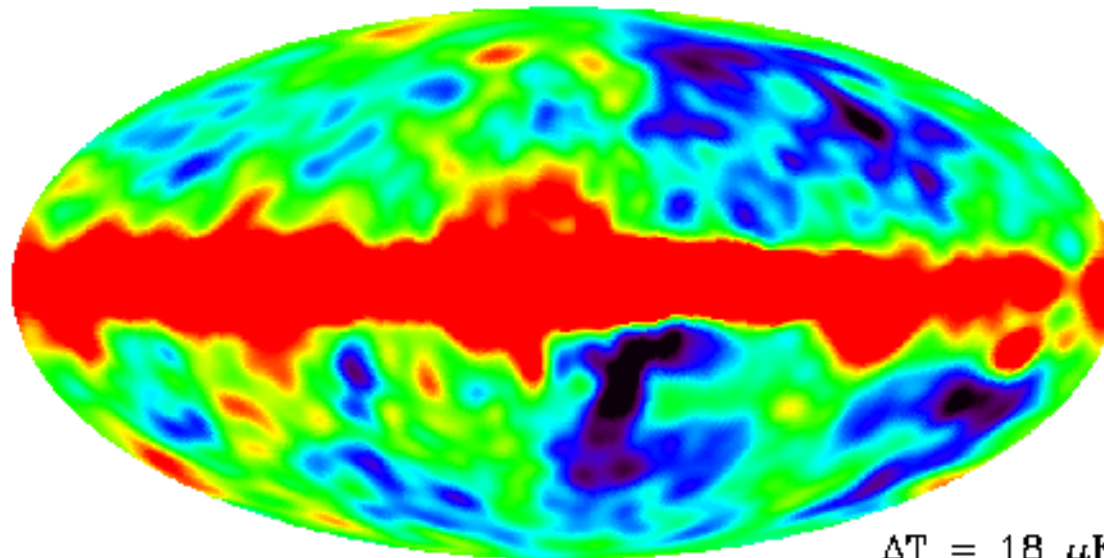
But first...

Where do the perturbations come from? Too difficult...  
How is that we see the perturbations?

"Wrinkles"  
or Hills & Valleys



"Top View"

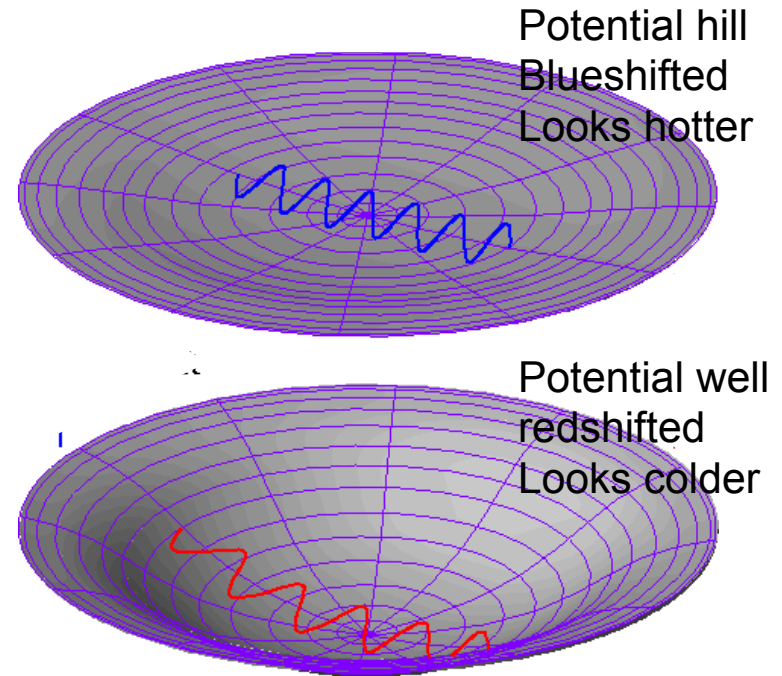


## We see them like temperature

On scales larger than a degree, fluctuations were outside the Hubble horizon at decoupling

Photons need to climb out of potential wells before they can travel to us (redshift or blueshift)  $h\nu/c^2\delta\phi$

$$\frac{\delta T}{T} = \frac{1}{3} \frac{\delta\phi}{c^2} \leftarrow \text{Given by } \delta\rho$$





# Perturbations: Some history

## SMALL-SCALE FLUCTUATIONS OF RELIC RADIATION\*

R. A. SUNYAEV and YA. B. ZELDOVICH

*Institute of Applied Mathematics, Academy of Sciences of the U.S.S.R., Moscow, U.S.S.R.*

(Received 11 September, 1969)

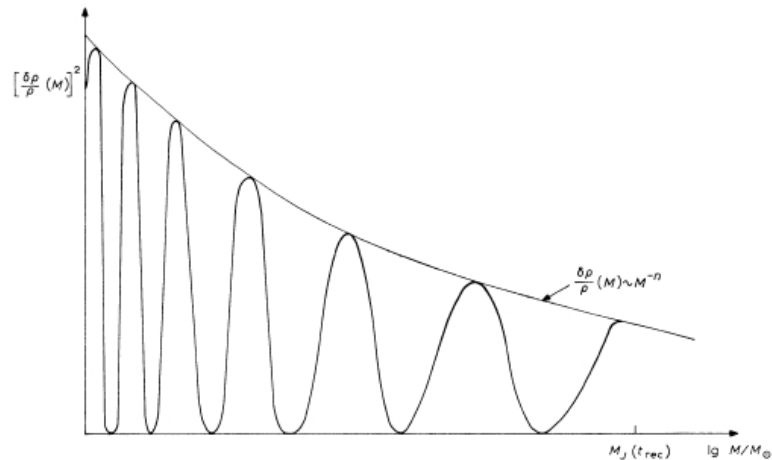


Fig. 1b. The dependence of the square of the amplitude of density perturbations of matter on scale. The fine line designates the usually assumed dependence  $(\delta\rho/\rho)_M \sim M^{-n}$ . It is apparent that fluctuations of relic radiation should depend on scale in a similar manner.

\* Translated from the Russian by D. F. Smith.

*Astrophysics and Space Science* 7 (1970) 3-19. All Rights Reserved  
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THE ASTROPHYSICAL JOURNAL, 162:815-836, December 1970  
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## PRIMEVAL ADIABATIC PERTURBATION IN AN EXPANDING UNIVERSE\*

P. J. E. PEEBLES†

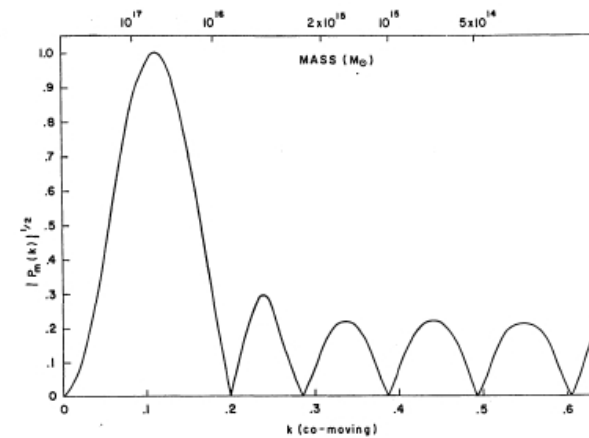
Joseph Henry Laboratories, Princeton University

AND

J. T. YU‡

Goddard Institute for Space Studies, NASA, New York

Received 1970 January 5; revised 1970 April 1



# Compress the CMB map to study cosmology

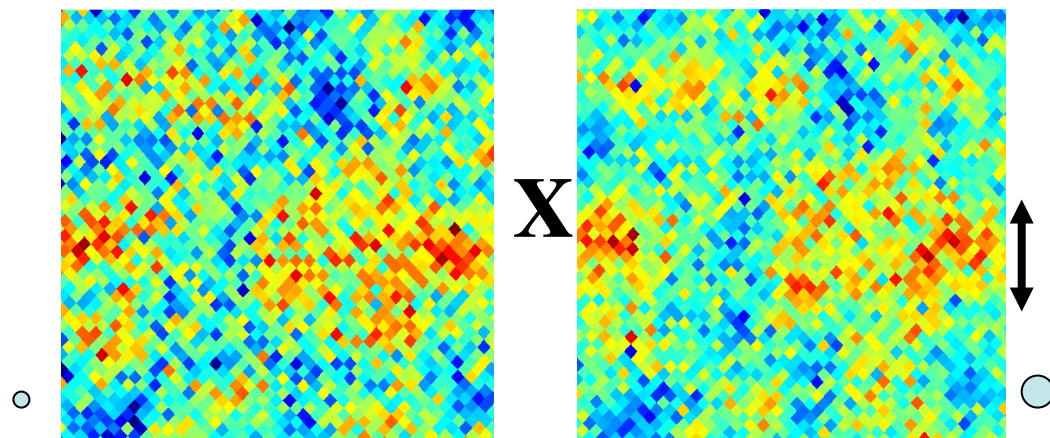
Express sky as: 
$$\delta T(\theta, \varphi) = \sum_{l,m} a_{lm} Y_{lm}(\theta, \varphi)$$

**If the anisotropy is a Gaussian random field**

(real and imaginary parts of each  $a_{lm}$  independent normal deviates, not correlated.)

***all the statistical information is contained in the angular power spectrum***

0.06% of map

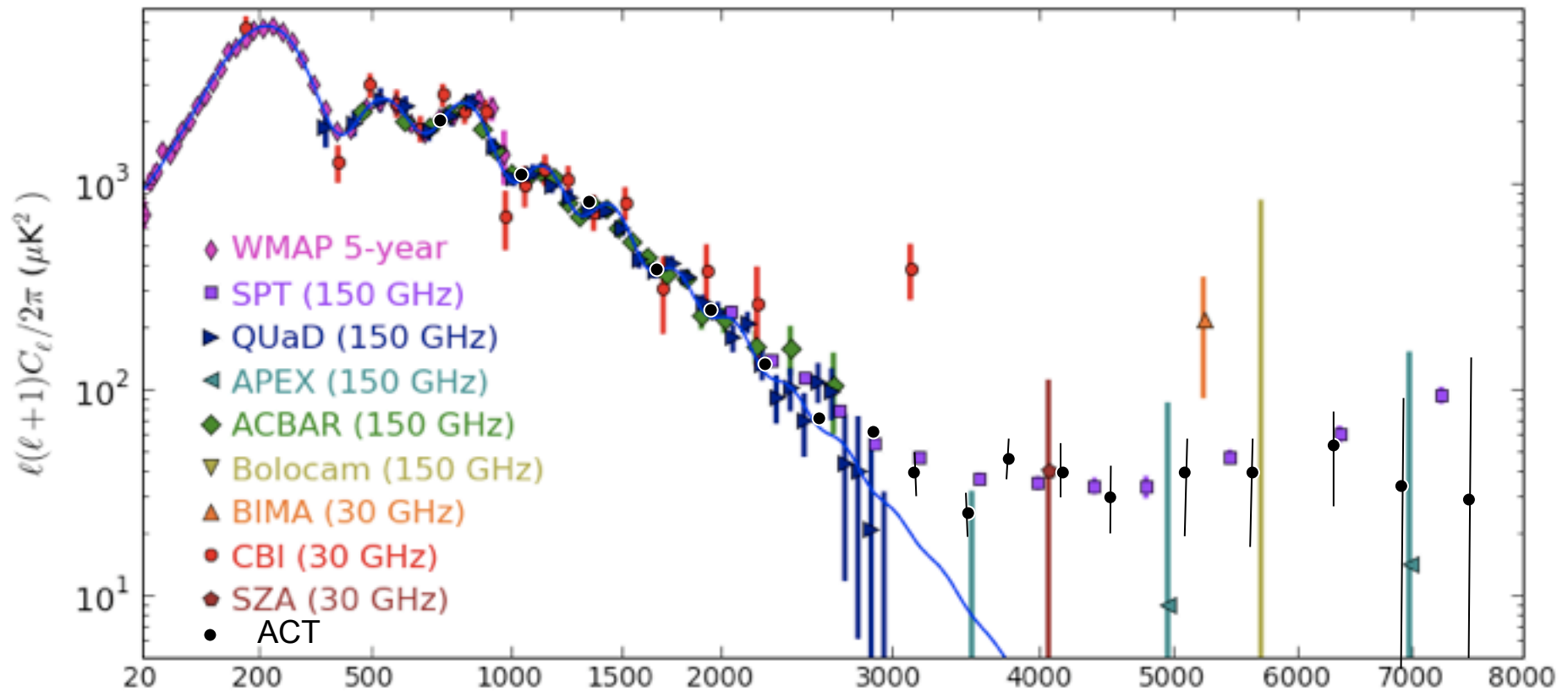


Raw 94 GHz near NEP    +/- 32 uK    Raw 61 GHz near NEP

$$C_l = \frac{1}{2l+1} \sum_m |a_{lm}|^2$$

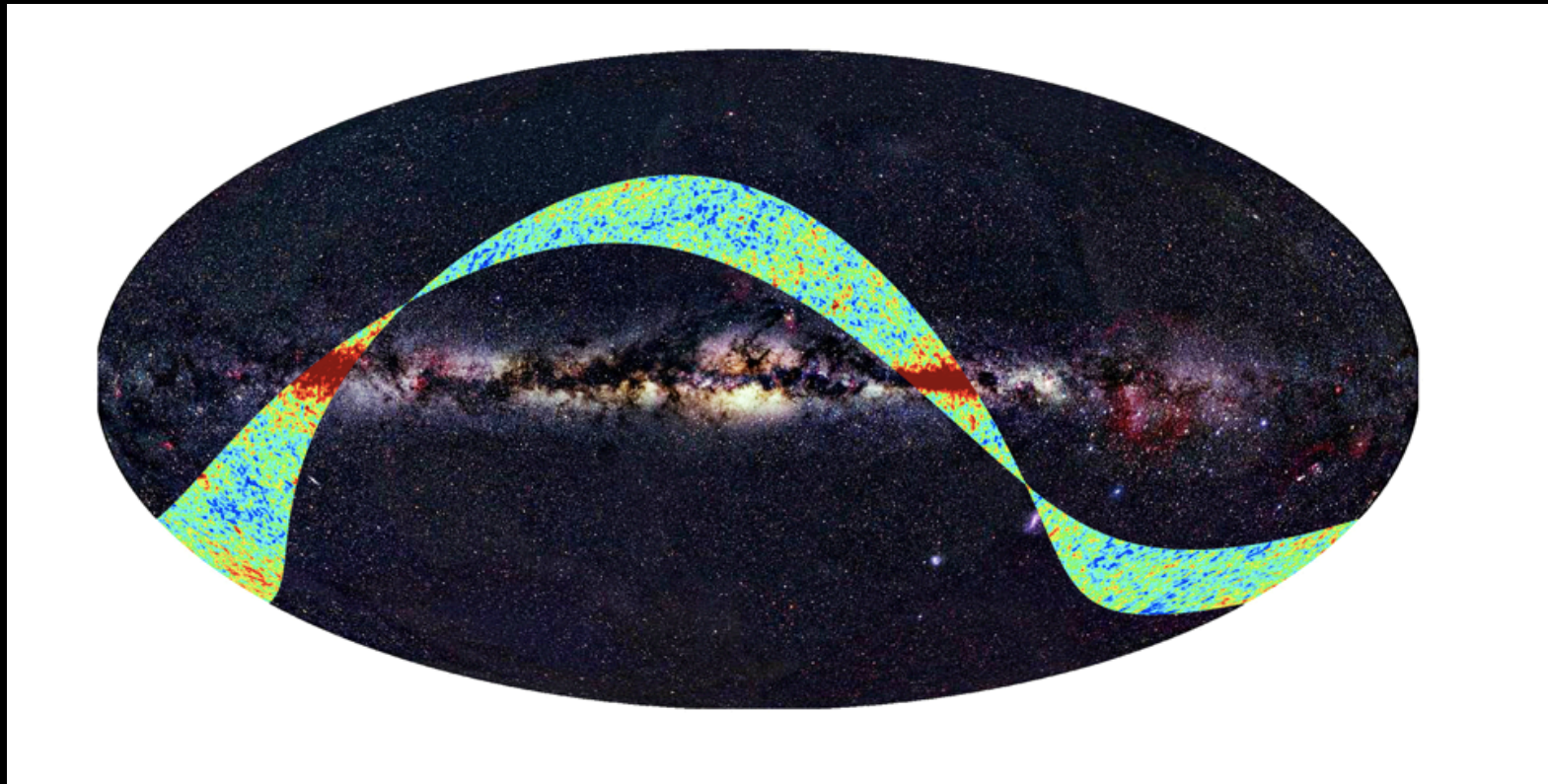


# State of the art: temperature



# The future is here

Planck satellite successfully launched in May!



“PR” image

## **How's that?**

The Universe back then was made of a very hot and dense “gas”, so it was emitting radiation

This is the radiation we see when we look at the CMB

Uniform, but with tiny (contrast x 100000) density (and temperature) ripples

Ripples in a gas? **SOUND WAVES!**

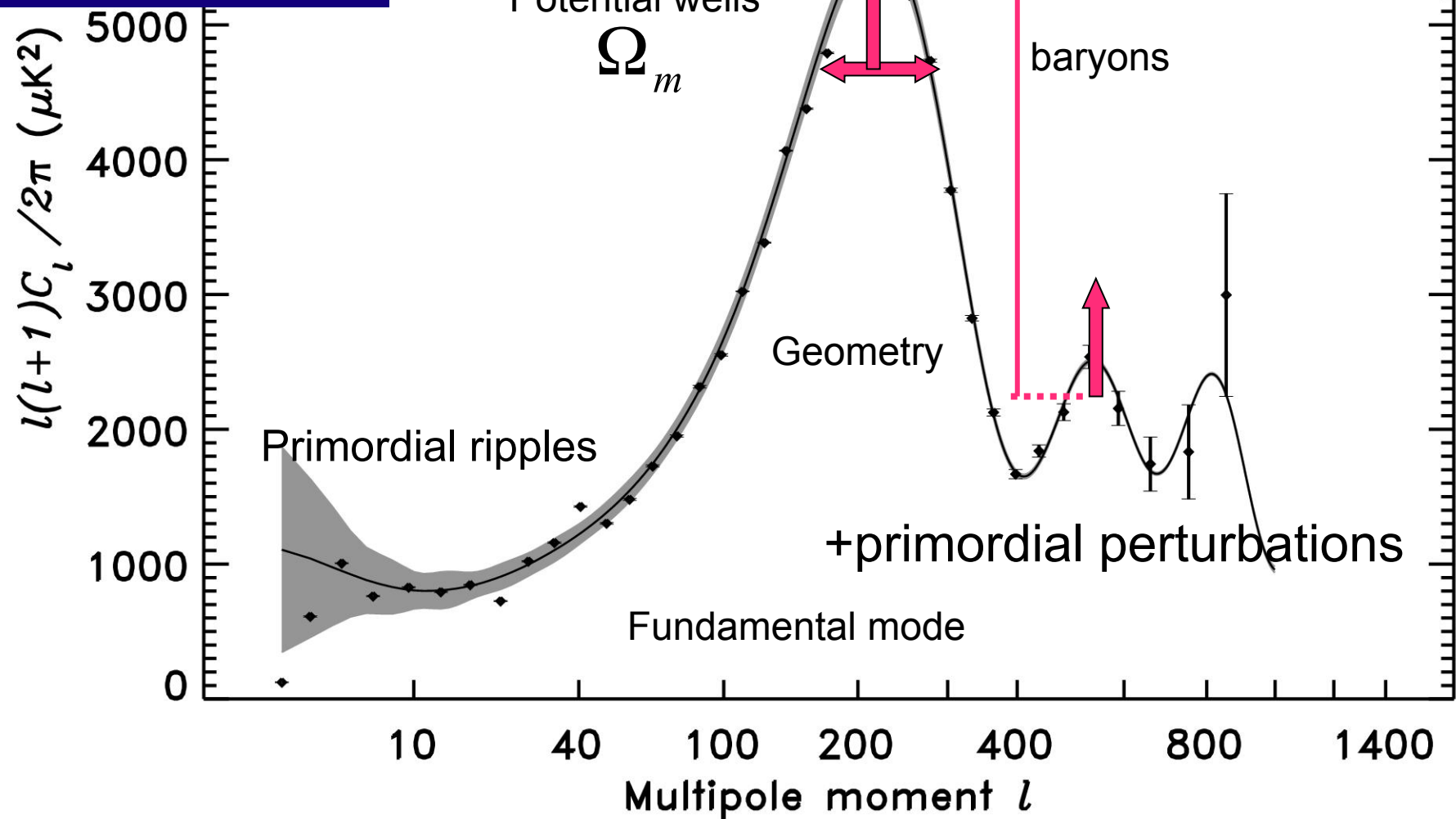
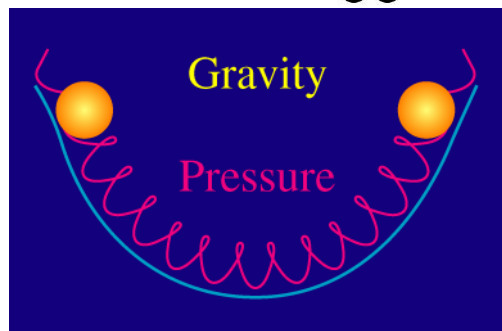
Truly a cosmic symphony... We are seeing sound!

These tiny fluctuations, quantitatively, give rise galaxies

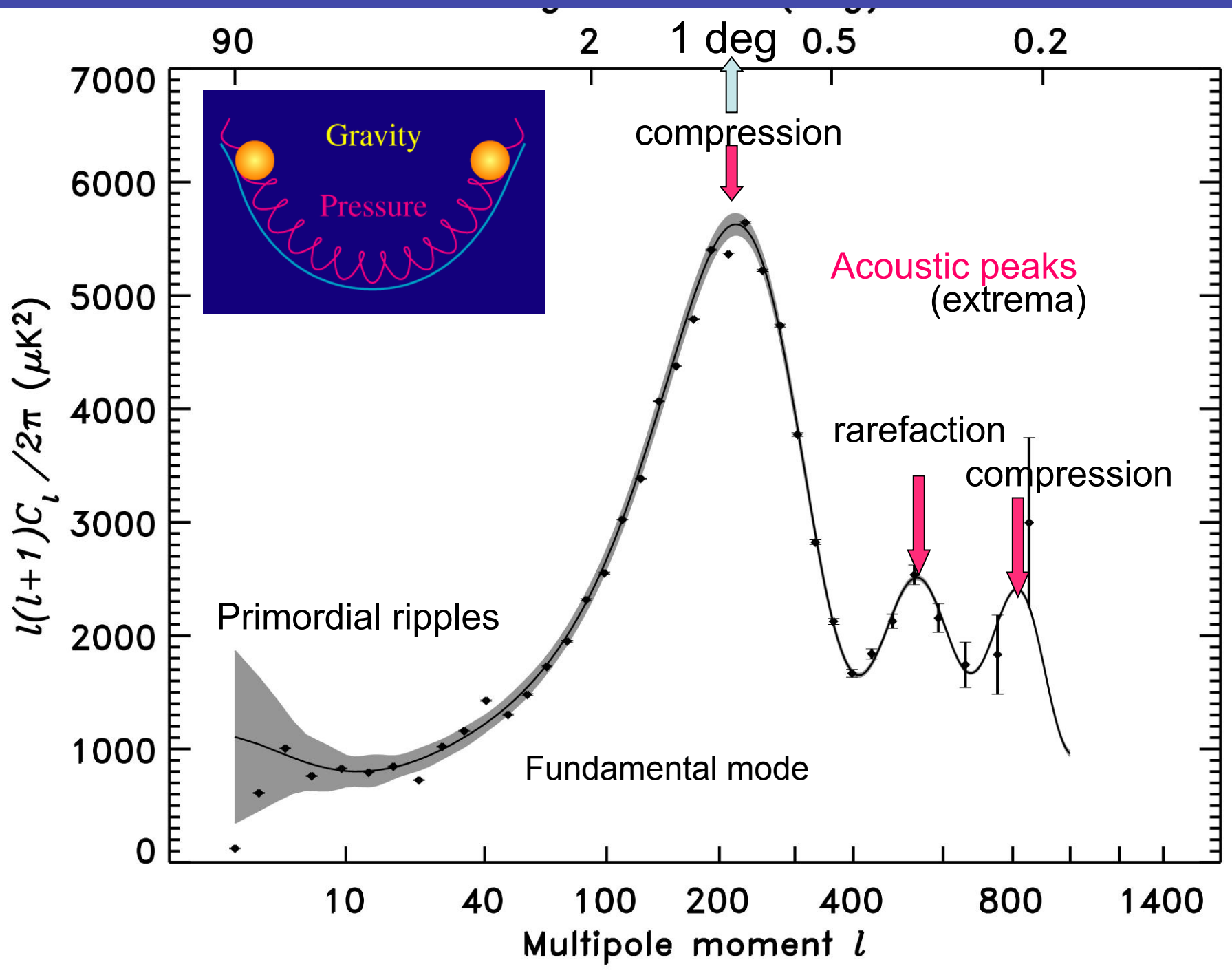
We try to listen to the sound and figure out how the instrument is made

Fundamental scale → Fundamental mode and overtones

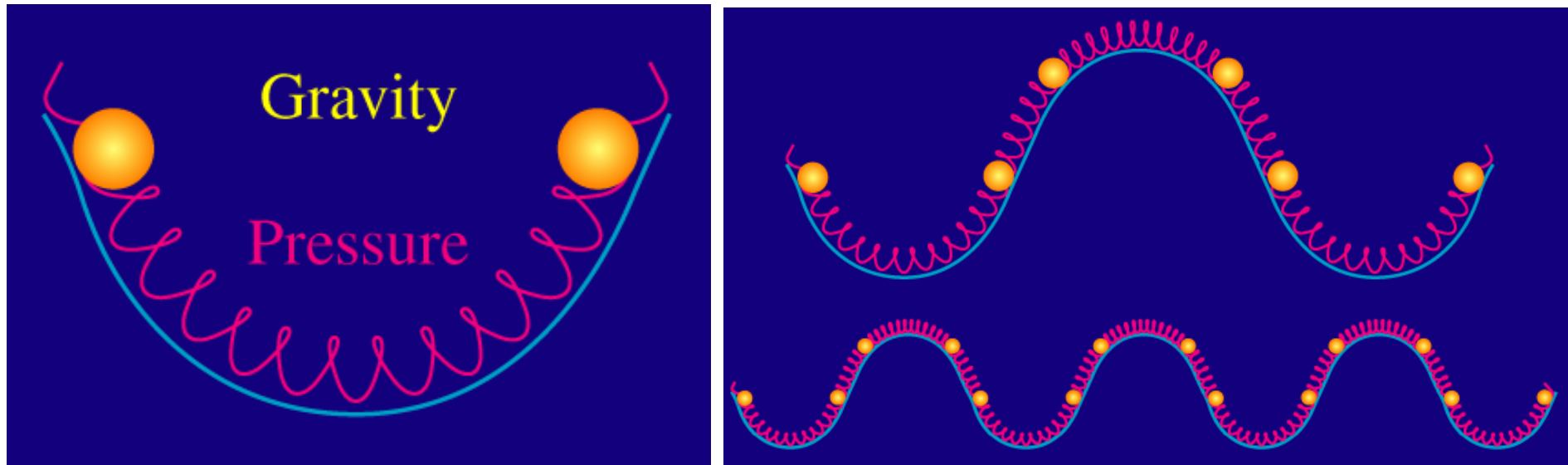
like blowing on a pipe....



Jungman, Kamionkowski, Kosowsky, Spergel, 1996



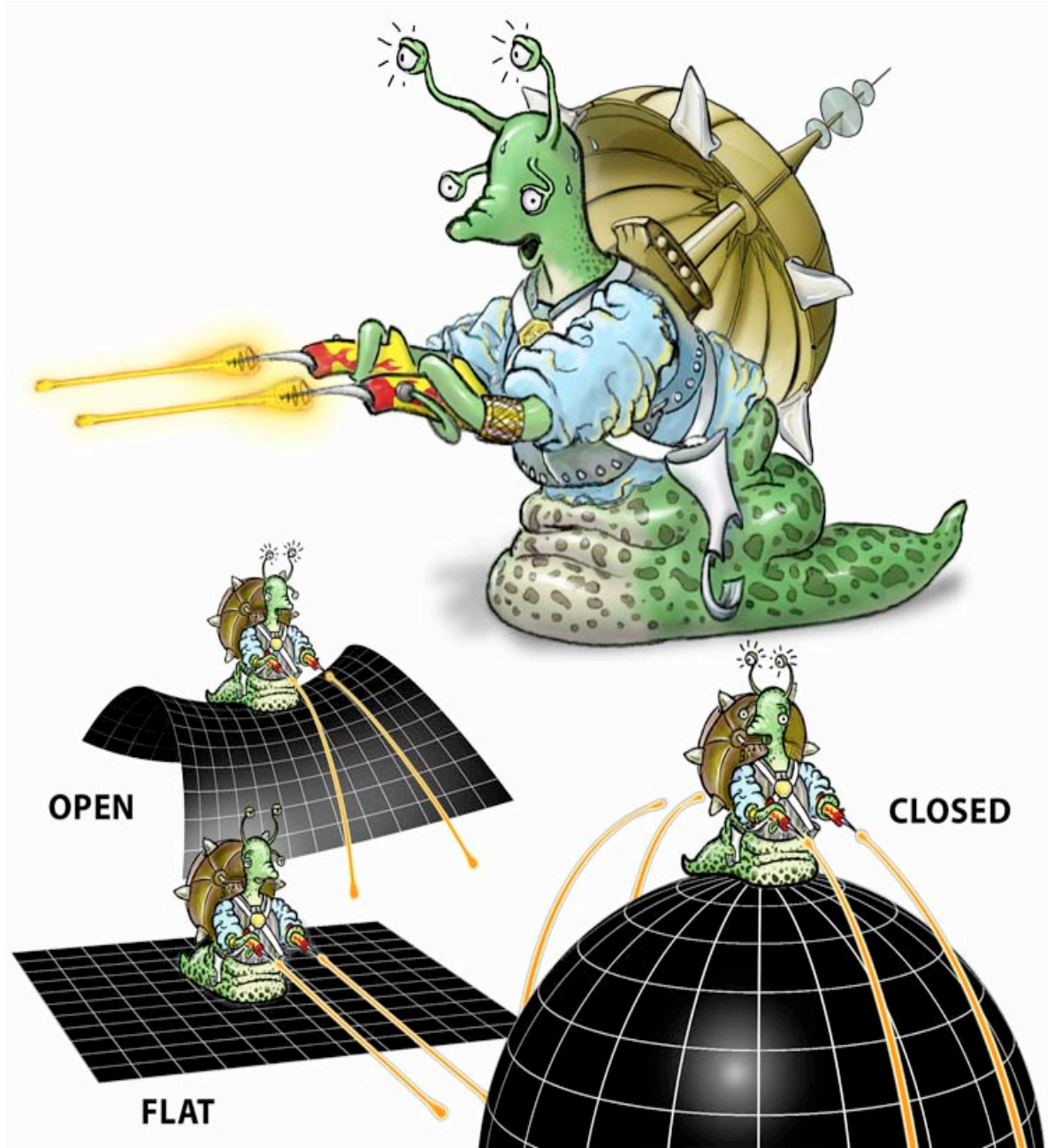
There is time between when a perturbation enters the horizon (and starts oscillate)  
And decoupling, when oscillations freeze.... And get imprinted in the CMB.



Longer wavelength modes oscillate slower  
The frequency of the oscillation is equal to the  
wavenumber times the speed of sound:  $\omega = kc_s$

The largest scales (sound horizon) can only go through a compression,  
Smaller scales can go through a compression and a rarefaction  
Etc...

Animations courtesy of W. Hu







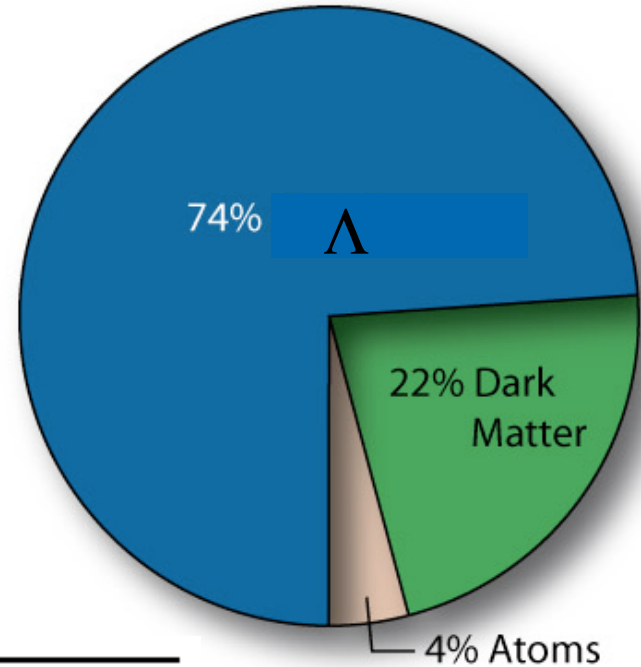


# The standard cosmological model $\Lambda$ CDM model

Spatially flat Universe

Power-law, primordial power spectrum

Only 6 parameters: WMAP5yr analysis



Class	Parameter	WMAP 5-year Mean <sup>b</sup>	WMAP+BAO+SN Mean
Primary	$100\Omega_b h^2$	$2.273 \pm 0.062$	$2.265 \pm 0.059$
	$\Omega_c h^2$	$0.1099 \pm 0.0062$	$0.1143 \pm 0.0034$
	$\Omega_\Lambda$	$0.742 \pm 0.030$	$0.721 \pm 0.015$
	$n_s$	$0.963^{+0.014}_{-0.015}$	$0.960^{+0.014}_{-0.013}$
	$\tau$	$0.087 \pm 0.017$	$0.084 \pm 0.016$
	$\Delta_{\mathcal{R}}^2 (k_0^e)$	$(2.41 \pm 0.11) \times 10^{-9}$	$(2.457^{+0.092}_{-0.093}) \times 10^{-9}$
Derived	$\sigma_8$	$0.796 \pm 0.036$	$0.817 \pm 0.026$
	$H_0$	$71.9^{+2.6}_{-2.7}$ km/s/Mpc	$70.1 \pm 1.3$ km/s/Mpc
	$\Omega_b$	$0.0441 \pm 0.0030$	$0.0462 \pm 0.0015$
	$\Omega_c$	$0.214 \pm 0.027$	$0.233 \pm 0.013$
	$\Omega_m h^2$	$0.1326 \pm 0.0063$	$0.1369 \pm 0.0037$
	$z_{\text{reion}}^f$	$11.0 \pm 1.4$	$10.8 \pm 1.4$
	$t_0^g$	$13.69 \pm 0.13$ Gyr	$13.73 \pm 0.12$ Gyr

Survived!

Next...

