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Probing hadronization and jet substructure with leading particles in jet at H1<br>Mriganka Mouli Mondal ${ }^{1}$<br>CFNS, Stony Brook University


#### Abstract

We measure the charge and momentum correlations $\left(r_{c}\right)$ of the two leading momentum particles in a jet. The observable, $r_{c}$ used is expected to be very sensitive to fragmentation dynamics. The measurement is made with various kinematic variables and in particular the formation time ( $t_{\text {form }}$ ) brings the information of when the di-hadron fragmentation occurred separating the regions dominated by perturbative or non-pertubative dynamics. The associated structure in jet in terms of partonic branching is studied via jet substructure and recursive soft drop using recursive soft drop technique. An association of subjets to the leading particles and the related correlations is framed to extaract $r_{c}$ which is more resembles as partonic branching. It is revealing that soft and core part of the fragmentation significantly differ in building $r_{c}$ correlations in large formation time region.


## 1 Introduction: Observable

In the process of fragmentation the two-particle correlation of the leading charged hadron $h_{1}$ and next-to-leading charged hadron $h_{2}$ is studied with charge correlations [1,2]. The charge correlation ratio, $r_{c}$, is defined from the differential cross sections $\mathrm{d} \sigma_{h_{1} h_{2}} / \mathrm{d} X$ to quantify flavor and kinematic dependence of hadronization in the production of $h_{1}$ and $h_{2}$ or $\bar{h}_{2}$ (the anti-particle of $h_{2}$ ),

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\begin{equation*}
r_{c}(X)=\frac{\mathrm{d} \sigma_{h_{1} h_{2}} / \mathrm{d} X-\mathrm{d} \sigma_{h_{1} \bar{h}_{2}} / \mathrm{d} X}{\mathrm{~d} \sigma_{h_{1} h_{2}} / \mathrm{d} X+\mathrm{d} \sigma_{h_{1} \bar{h}_{2}} / \mathrm{d} X} . \tag{1}
\end{equation*}
$$

We will explore the dependence of $r_{c}$ on a variety of kinematic variables, $X$. In the definition, Eq. (1), $h_{1}$ and $h_{2}$ can in principle be arbitrary hadron species, including charged and neutral hadrons. We will select the events only in the case where both of them are charged particles. The $r_{c}$ is negative for the cases where $h_{1} \bar{h}_{2}$ cases dominate over $h_{1} h_{2}$ and in the string breaking picture opposite pair production dominates that leads to $r_{c}$ value be between 0 and -1 .

Formation time, $t_{\text {form }}=\frac{[2 z(1-z) P]}{k_{\perp}^{2}}$, is calculated from leading $\left(h_{1}\right)$ and next-to-leading $\left(h_{2}\right)$ hadron's kinematics. Leading and next-to-leading hadrons in jets are selected in terms of the momentum fraction along the jet axis. In formulating the formation time, $z$ and $P$ are defined as follows $z=$ $P_{h_{2}} /\left(P_{h_{2}}+P_{h_{1}}\right), P_{h_{1}}=(1-z) P$ and $P_{h_{2}}=z P$. Formation time can be related to time scale of hadronization where Small formation time corresponds small $z$ or large $k_{\perp}$. For a specific $z$ (specific $P_{h_{2}}$ and $P_{h_{1}}$ magnitudes), a large $\theta$ or large $k_{\perp}$ corresponds to a small $t_{\text {form }}$ resulting in early decorrelations and the region is dominated by wide angle gluon radiations. On the contrary a small $\theta$ corresponds to small $k_{\perp}$ and this is the region for large $t_{\text {form }}$.

Building $r_{c}$ correlations with partonic branches is made with angular ordered clusters and this fits with the picture where the struck parton undergoes pertubative shower evolution. The charges of a prong is assigned as the charge of the leading particle within.

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## 2 Data and MC samples and event selection

The data were taken by the H1 experiment during 2003-2007 using 27.6 GeV electron/positron scatters off 920 GeV proton at HERA, which corresponds to a center-of-mass energy $\sqrt{s}=319 \mathrm{GeV}$. The data are selected requiring functional central trackers (CJC1, CJC2) and calorimeters (LAr, SpaCal). The MC samples are reconstructed using the same detector condition of the corresponding years with Djangoh 1.4 and Rapgap 3.1 event generator. Subtrigger ST67 is used and it is sufficient for our interest in getting relatively high $Q^{2}\left(>150 \mathrm{GeV}^{2}\right)$ events and with good tracking using central detectors. The $z$-vertex distribution spreads widely mostly due to the 107 colliding bunch size in the accelerator while the transverse spread is narrow. The interaction region in the $z$ direction in this analysis is required to be less than $\pm 30 \mathrm{~cm}$. The longitudinal momentum of Hadronic Final State (HFS) and the scattered electron $\left(E-p_{z}\right)$ is expected to be two times the incident electron energy, i.e., 55.2 GeV . The spread in the variable $\left(E-p_{z}\right)$ appears due to experimental resolution effects in determination of HFS and photon radiations from colliding beam. We have taken events with $45<E-p_{z}<65 \mathrm{GeV}$ and this reduces events with initial state photon radiations and photoproduction events. To have a well defined kinematics the events are selected with $Q^{2}>150 \mathrm{GeV}^{2}$ and $0.2<y<0.7$, where $y \simeq Q^{2} / x s$ and x is the Bjorken scaling variable.

## 3 Jet reconstructions

Jets are reconstructed in the lab frame using fastjet anti-kt algorithm with $R=1.0$ with energy weighted scheme where as inputs HFS objects are taken with $p_{\mathrm{T}}>0.2 \mathrm{GeV}$. The selected jets are with jet $p_{\mathrm{T}}>5 \mathrm{GeV}$ within the fiducial region, $-1.5<\eta<1.5$, where the pseudo-rapidity variable $\eta=-\ln (\tan (\theta / 2))$.


Figure 1: (left) number of jets in an event, (middle) leading jet pseudo-rapidity distributions, (right) leading jet transverse momentum distributions. The jet transverse momentum and pseudorapidity regions are indicated. Only the leading jet is considered for the subsequent analysis, corresponding to more than $90 \%$ of all jets. The jet rapidity is restricted in order to match the central tracker acceptance for the jet's leading particle selection. The peak near transverse jet momenta of 10 GeV is a reflection of the $Q^{2}>150 \mathrm{GeV}$ selection cut.

For the simplicity we are currently using only leading $p_{\mathrm{T}}$ jet which. Two-jet events might be interesting in terms of their origin from higher order processes and in such a case the analysis would be
interesting in predicting $r_{c}$ which might be dominated by jets of gluonic origin. It is to be mentioned that it requires the leading momentum objects (subjets) within jets to have well defined charge either +1 or -1 . The charge of the subjets are currently picked from the charge of the leading constituents. Figure 1 shows number of jets, psuodorapidity and transverse momentum distributions. Figure 2 shows some number of constituents in the jet and the momentum sharing for the two leading particles.


Figure 2: (left) Number of constituents in jets. These contain neutral and charge objects in reconstructed data and MC. Fraction of momentum carried by the leading particle (middle) and next to leading particle (right) along the jet axis.

### 3.1 Recursive soft drop

In the Soft Drop (SD) [5, 6] procedure the constituents of an initial jet with radius $R_{0}$ are re-clustered with the Cambridge/Aachen (C/A) algorithm. The soft wide angle emissions are removed that do not satisfy the SD condition. This is a powerful probe of the QCD splitting function. We will use a recursive extension [7] of the SD algorithm, Recursive Soft Drop (RSD), where SD is reapplied along the C/A clustering history until a specified number $n$ of SD conditions are satisfied. The number $n=1$ corresponds to first split while $n=2$ would correspond to the second split. The SD conditions we implied is that the leading and next-to leading particles in original jet are found in two separate branches. At the matching we called them as resolved prongs $n_{R}$ and this senses nonoperative aspects of splitting. Defining $z_{g}$ and $R_{g}$ as

$$
\begin{gather*}
z_{g}=\frac{\min \left(p_{t, 1}, p_{t, 2}\right)}{p_{t, 1}+p_{t, 2}}>z_{\mathrm{cut}}\left(\frac{R_{g}}{R_{0}}\right)^{\beta}  \tag{2}\\
R_{g}=\Delta R_{12}=\sqrt{\Delta \eta_{1,2}^{2}+\Delta \phi_{1,2}^{2}} \tag{3}
\end{gather*}
$$

the values for the $\beta=1$ and $z_{\mathrm{cut}}=0.2$ is used in the main analysis. $\beta=1$ means that grooming using the dynamic radius in reaching successive steps and higher $z_{\text {cut }}$ means more harsher cuts on soft particles.
In general it is very informative to see the $n_{R}$ distributions to check where the correlation of the prongs and leading particles happens. Specifically $z_{\text {cut }}$ has much to do in transforming $n_{R}$ distributions. Larger $z_{\text {cut }}$ eliminates soft wide angle radiations and the matching probability of the leading hadron gets enhanced in the first node. Nevertheless, a modest $z_{\text {cut }}$ cut would still keep a soft wide angle component in the first split. The consecutive splits are narrower and thus for the current analysis we will split the data into $1^{\text {st }}$ prong and $2^{\text {nd+ }}$ prongs.

Figure 3: Event distribution in $1 / R_{g}$ vs. $R_{g} Z_{g}$ for the first split (left) and for the second split (right).

### 3.1. Recursive soft drop: resolved prongs

The kinematics of leading and next-to-leading particles are replaced to that of subjets; i.e, the jet with $R=1.0$ is subdivided into smaller jets mimicking the angular ordering of the shower from the final state particles in jets. Angular order of the branches in the clustering tree is followed through the hardest branch till the leading hadrons are found in two separate subjets. We call at that point that the leading next to leading hadrons are get resolved. Soft drop is used with $z_{\text {cut }}=0.2$ and $\beta=1$ in order to remove very soft particles activities surrounding the core hadronization region around the leading particles. In that way we classify the events with $n_{R}=1$ (resolved first prong) and $n_{R} \geq 2$ (resolved $2 \mathrm{nd}+$ prongs). The first split ( $n_{R}=1$ ) is relatively wider angle soft splitting and the $2 \mathrm{nd}+\left(n_{R} \geq 2\right)$ prongs are relatively narrower and harder splitting Figure 3.


## 4 Results: $r_{c}$ with formation time, $k_{\perp}$ and $p_{T}$

Figure 4 shows $r_{c}$ as a function of $t_{\text {form }}$ (left), $\mathrm{k}_{\perp}$ (middle) and jet- $p_{T}$ (right) for different splits and $h_{1} h_{2}$. The $r_{c}$ at small formation time ( $\sim 1 \mathrm{fm}$ ) is large $k_{\perp}$ or small $z$ origin, and this is the region where leading and next to leading particles originate from early decorrelations. This region appears to be purely perturbative in nature. Large formation time ( $\sim 10 \mathrm{fm}$ or more) corresponds to nonperturbative in nature where $k_{\perp}<200 \mathrm{MeV}$. The striking difference is that at large formation time $r_{c}$ for the first split is stronger compared to that of the subsequent splits. Djangoh [3] and Rapgap [4] compare with data fairly well in most of the region. The systematic bands are the errors appearing from bin-by-bin corrections using Rapgap and Djangoh event generators. Small $k_{\perp}$ shows strong correlations and this is the nonperturbative region. Large $k_{\perp}$ appears from wide angle early gluon radiations and this might trigger independent hadronization which de-correlates the $r_{c}$ correlations in charge. The $r_{c}$ for $h_{1} h_{2^{-}}$ case depends weakly on $p_{\mathrm{T}, \mathrm{jet}}$. The first split seems to have stronger dependency with jet transverse momentum compared to that of the later splits.


Figure 4: The $r_{c}$ are shown with (left) formation time, (middle) $k_{\perp}$ and (right) $p_{\mathrm{T}}$.

## 5 Summary

The charge correlations $r_{c}$ is measured at HERA DIS collisions using jets reconstructed using H1 detector. The correlations are negative as expected and the values are compared with Rapgap and Djangoh event generators. The $r_{c}$ extracted for subjets at first split and later splits shows different values at large formation time. The behavior needs to be studied in details to find out origin of the differences and if this indicates a transition between perturbative and nonpertubative region in formation time scale. Such measurements at H1 in addition to LEP, BELLE, and hadronic $p p$ collisions at the RHIC and the LHC need to be made to understand the dynamics of fragmentation and jet substructure. In particular before EIC these measurements would be very important to understand hadronization and EIC will bring measurement of $r_{c}$ for different flavor with very high precision.

## References

[1] Y. T. Chien, A. Deshpande, M. M. Mondal and G. Sterman, Phys. Rev. D 105, no.5, L051502 (2022)
[2] A. Accardi, Y. T. Chien, D. d’Enterria, A. Deshpande, C. Dilks, P. A. G. Garcia, W. W. Jacobs, F. Krauss, S. L. Gomez and M. M. Mondal, et al. [arXiv:2204.02280 [hep-ex]].
[3] K. Charchula, G. A. Schuler and H. Spiesberger, Comput. Phys. Commun. 81, 381-402 (1994) doi:10.1016/0010-4655(94)90086-8
[4] H. Jung, Comput. Phys. Commun. 86, 147-161 (1995) doi:10.1016/0010-4655(94)00150-Z
[5] R. Aaij et al. [LHCb], JHEP 09, 006 (2013)
[6] A. J. Larkoski, S. Marzani, G. Soyez and J. Thaler, JHEP 05, 146 (2014)
[7] F. A. Dreyer, L. Necib, G. Soyez and J. Thaler, JHEP 06, 093 (2018)


[^0]:    ${ }^{1}$ (for the H1 Collaboration) [H1prelim-22-032]

