

Drell-Yan cross-sections with fiducial cuts

-

Impact of linear power corrections and  
 $q_T$ -resummation in PDF determinations

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di Genova**

DIS 2022

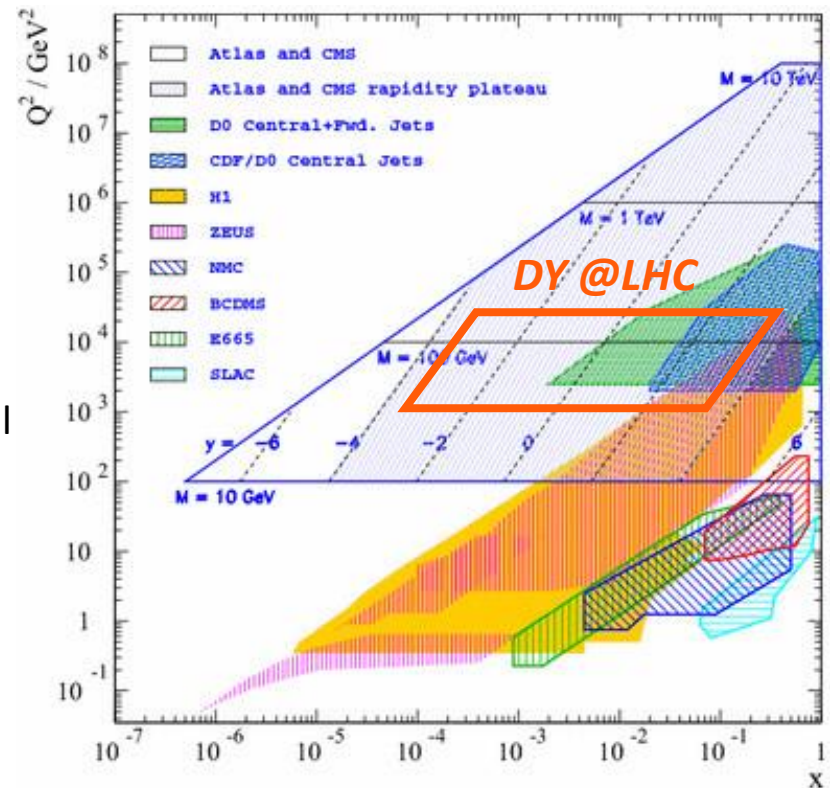
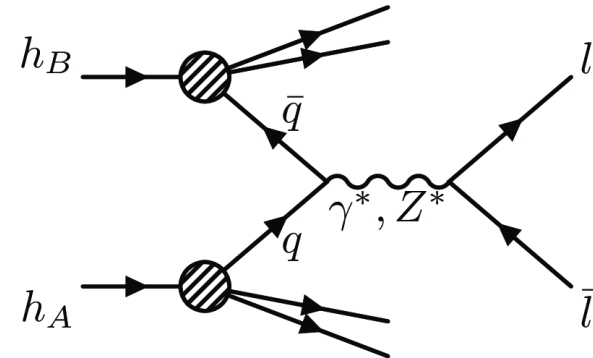
Santiago de Compostela

May22



# Drell-Yan process and PDF

- Vector boson creation in hadron collisions
- Drell-Yan is the prime process for precision benchmark
- DY is predicted with high precision
  - NNLO fully differential result
  - N3LO [e.g. arXiv 2007.13313, arXiv 2107.09085, arXiv 2111.10379]
  - NLO EW
  - NNLO mixed QCDxEW
    - (E.g. in arXiv:2106.11953, arXiv:2201.01754, arXiv:2203.11237)
- DY contribute to PDF knowledge
  - Accurate knowledge of PDF is fundamental part of LHC program
- Important for PDF evaluation
  - $u$ -  $d$ - valence quark PDFs
  - $R_s = (s + \bar{s})/(\bar{u} + \bar{d})$



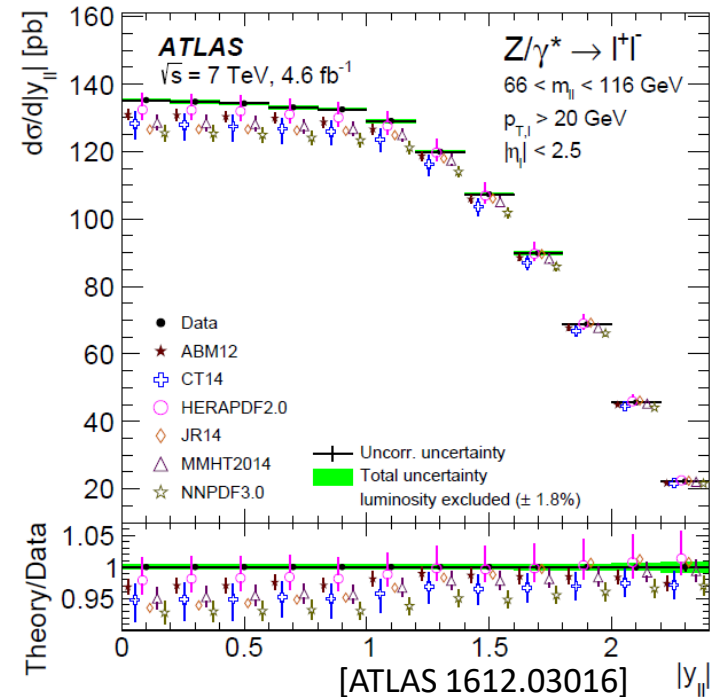
# DY measurements at the LHC

- **High precision ATLAS 7TeV  $W/Z$  cross section**
  - Challenges the accuracy of theoretical predictions
  - Z peak accuracy at 0.5% (excluding luminosity)
  - high experimental precision requires equally high theory accuracy for inclusion in QCD fits
  - Difficult to describe in modern PDF fit

Ultimate goal – understand the effects of the mismatch:

- PDF fit at fixed order
- But PDF used in parton shower MC e.g. [arXiv:1406.7693]

Effort for ATLAS 7TeV started in [ATL-PHYS-PUB-2018-004]



# ATLAS 7TeV $W/Z$ measurement

- Fiducial volume for  $Z$  cross section

- Central Channel
  - $p_T^\ell > 20\text{GeV}$
  - $|\eta| < 2.5$

- Forward Channel
  - $p_T^\ell > 20\text{GeV}$
  - $|\eta^1| < 2.5, 2.5 < |\eta_2| < 4.9$

- Symmetric  $p_T^\ell$  cuts

- $|y_{\ell\ell}|$  differential measurement in each mass bin
- Cross section extracted at Born level (prior final state QED radiation)

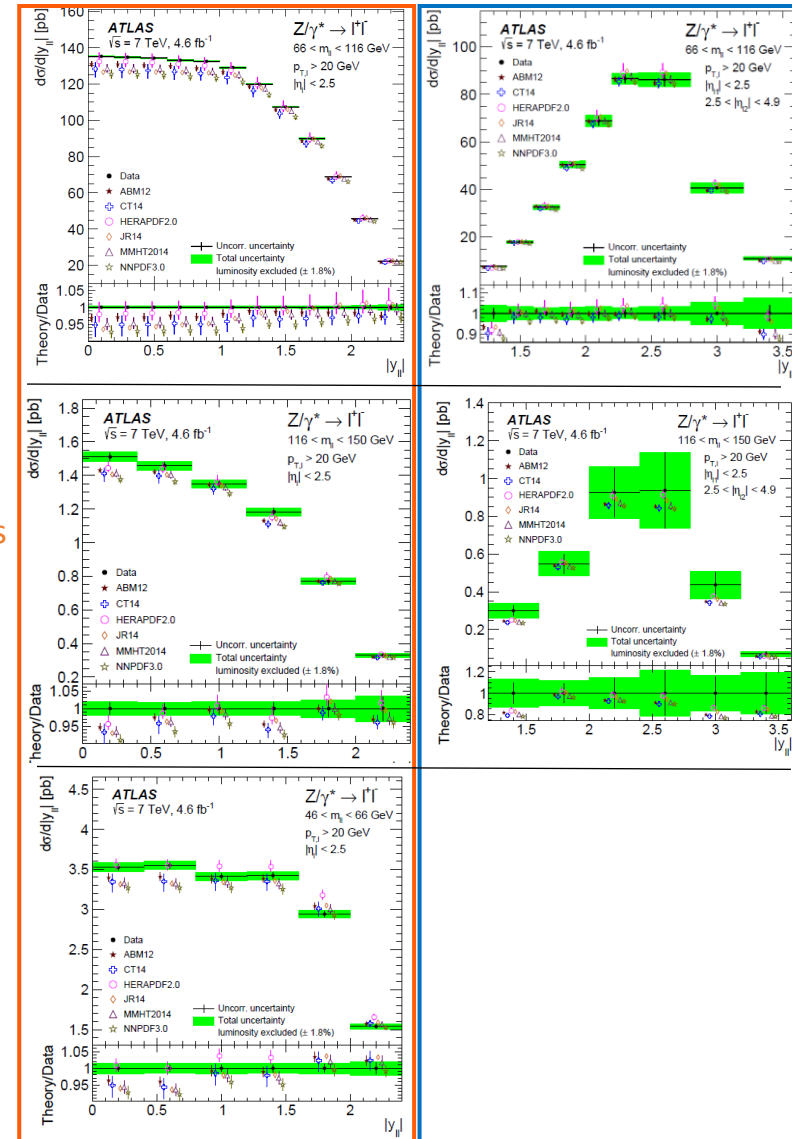
High  
Mass

$Z$ -Mass  
Peak

Low  
Mass

Central Channel

Forward Channel



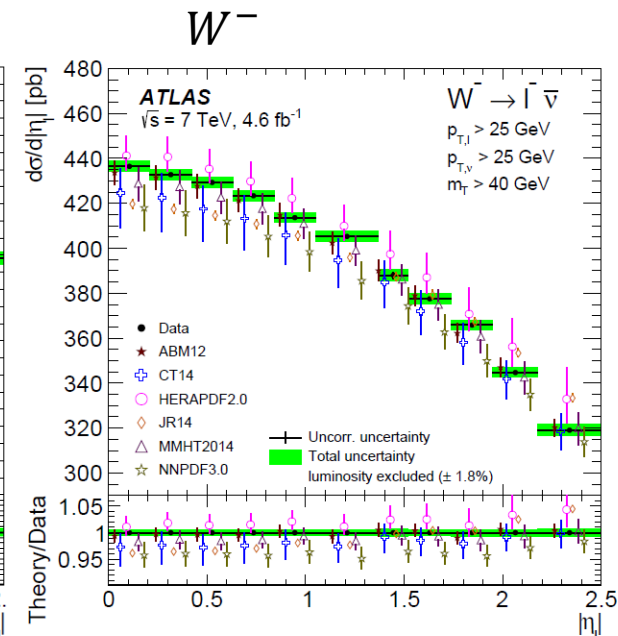
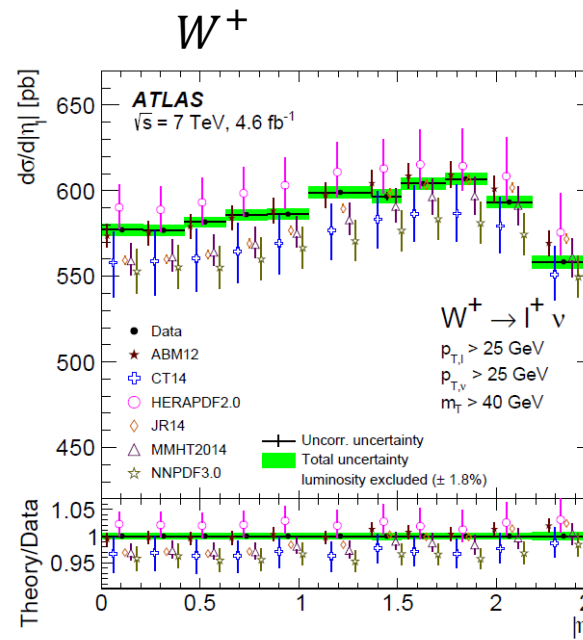
[ATLAS 1612.03016]

# ATLAS 7TeV $W/Z$ measurement

- Fiducial volume for  $W^{+/-}$  cross section

- $p_{T,\ell} > 25\text{GeV}$
- $|\eta_\ell| < 2.5$
- $p_{T,\nu} > 25\text{ GeV}$
- $m_T > 40\text{ GeV}$

- Symmetric  $p_T^\ell$  cut
- $|\eta_\ell|$  differential cross section
- Cross section extracted at Born level (prior final state QED radiation)



[ATLAS 1612.03016]

# Drell-Yan at NNLO (QCD) - Fiducial Power Correction

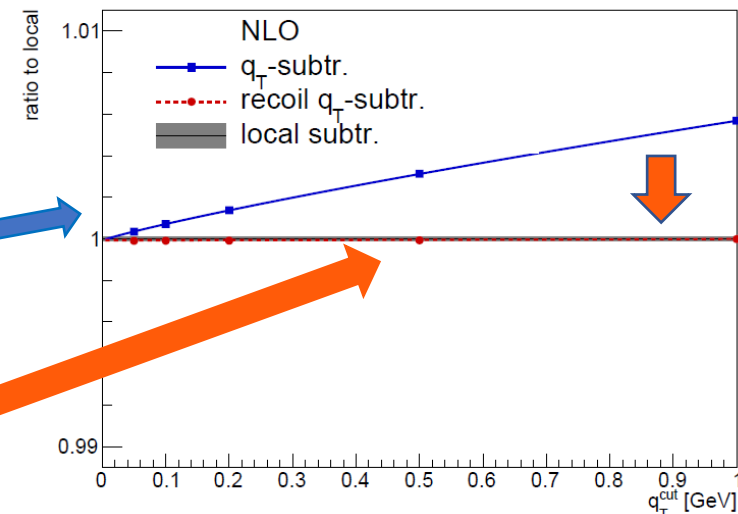
NNLO (QCD) calculations (from different programs) differ at % level [arXiv 2104.02400]

→ this spoils the nominal accuracy of the calculations

- The difference is shown to be connected to the **subtraction scheme...**
  - Local subtraction scheme
  - Non-local subtraction scheme (e.g.  $q_T$ -subtraction)
- ...and due to the **symmetric lepton fiducial cuts** [arXiv:2006.11382]
  - These induce a **Linear  $q_T$**  dependence of the **acceptance**
  - $\Phi(q_T) - \Phi^{\text{BORN}} \sim q_T$
  - → **linear bias** in  $q_T$  sub. Scheme

Including boson  $q_T$  recoil prescription the **nominal accuracy is recovered** [arXiv:2102.08039]

- Recoil prescription from resummation results
- Implemented in codes SCETlib, MATRIX [arXiv2111.1366], DYTurbo [arXiv2111.14509]



*Non-local/local sub. Scheme.  
 $q_T$  recoil allows us to recover  
 $O(q_T^2)$  accuracy*

# Drell-Yan at NNLO (QCD) - $q_T$ Resummation

Acceptance depend on small  $q_T$  values

➔ Enhanced  $q_T/Q$  *logarithms* affect the calculation regardless of the subtraction scheme used

- Need to resum fiducial power correction to obtain a meaningful prediction
  - We explore the differences in the predictions using DYTurbo

Other approaches to the problem

- Asymmetric or Staggered cut [2106.08329] (avoid the linear power corrections)
- Defiducialization [2001.02933]

# DYTurbo

- Fast Drell-Yan predictions with  $q_T$  subtraction [arXiv 1910.07049]
  - Improved reimplementation of DYNNLO + DYqT + DYRes
  - Fully differential up to N3LL' QCD [2103.0497]
  - **Implements  $q_T$  recoil prescription in Fixed order prediction**

We produce NNLO DY prediction with DYTurbo for the ATLAS measurement

Our setup:

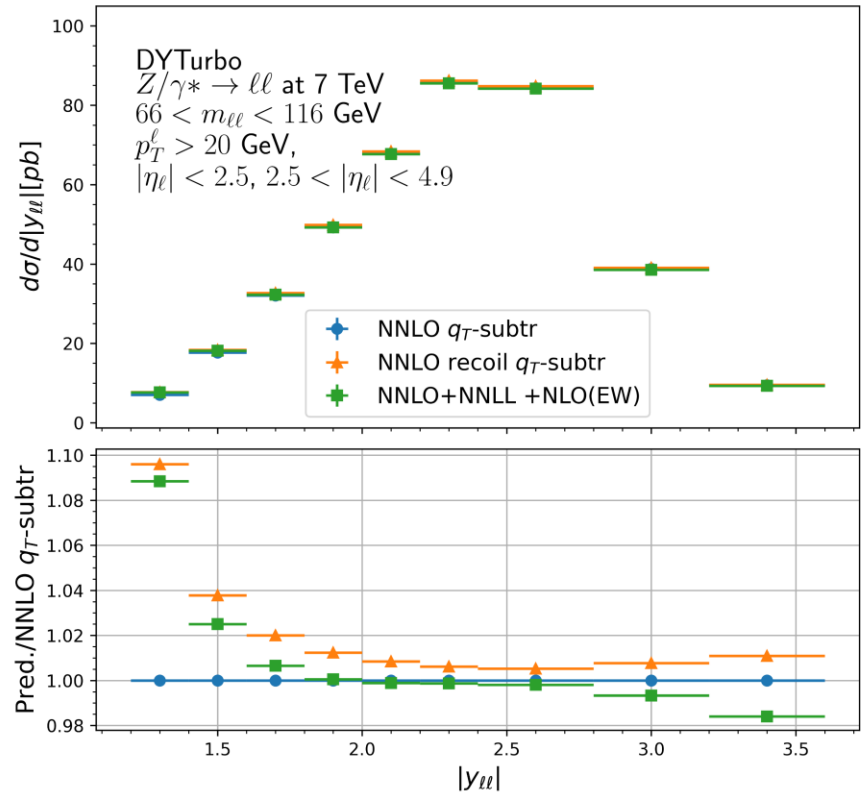
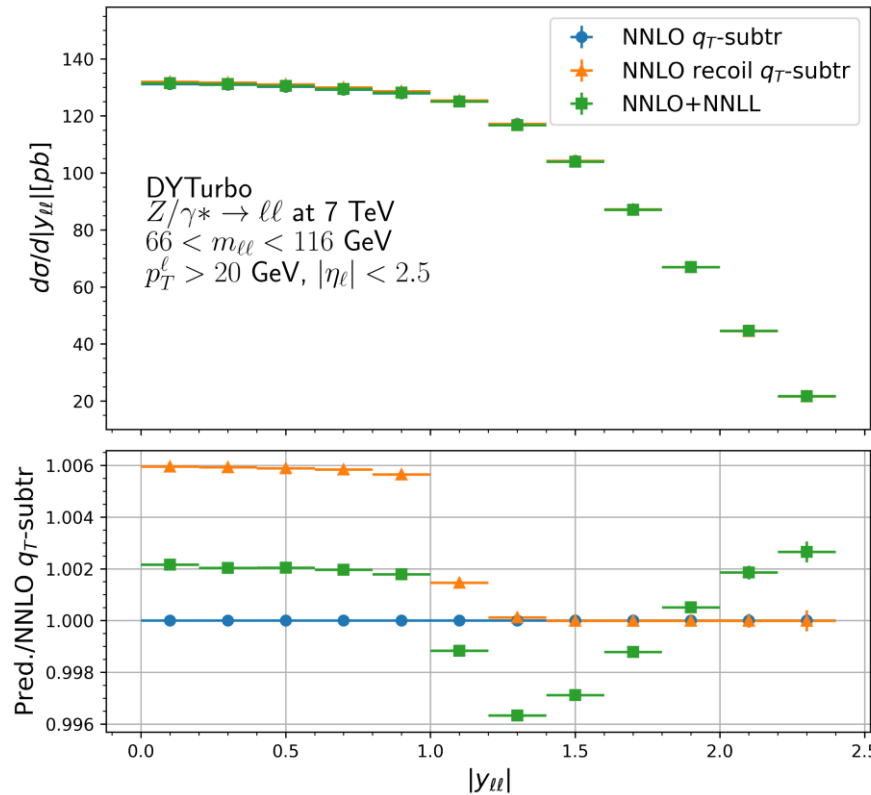
$q_T$ subtr	
$q_T^{cut}/Q$	0.008
$EW$	
$G_\mu$ scheme	
$m_W$	80.385 GeV
$m_Z$	91.187 GeV
$G_F$	$1.167 \cdot 10^{-5} \text{ GeV}^{-2}$

QCD	
PDF set	NNPDF31nnlo
$\mu_R$	$m_{\ell\ell}$
$\mu_F$	$m_{\ell\ell}$

Resummation	
$\mu_{Res}$	$m_{\ell\ell}$
Sudakov form factor	$\exp(-g_1 b^2), g_1 = 0.8$
Resummation damping	$\exp(-(k \cdot m_{\ell\ell} - q_T)^2 / (\delta \cdot m_{\ell\ell}^2)), k = 0.75, \delta = 0.5$



# NNLO QCD Predictions with DYTurbo

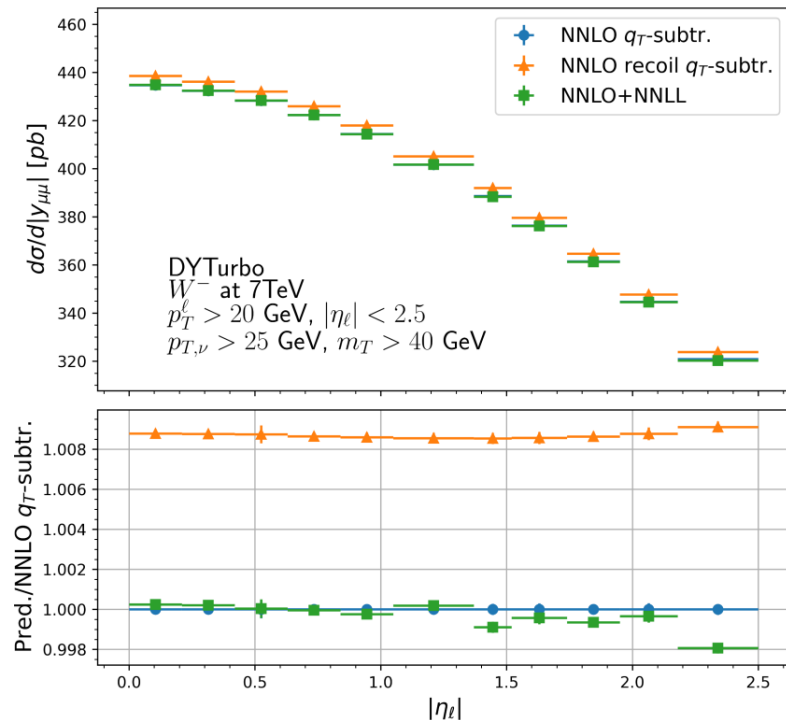
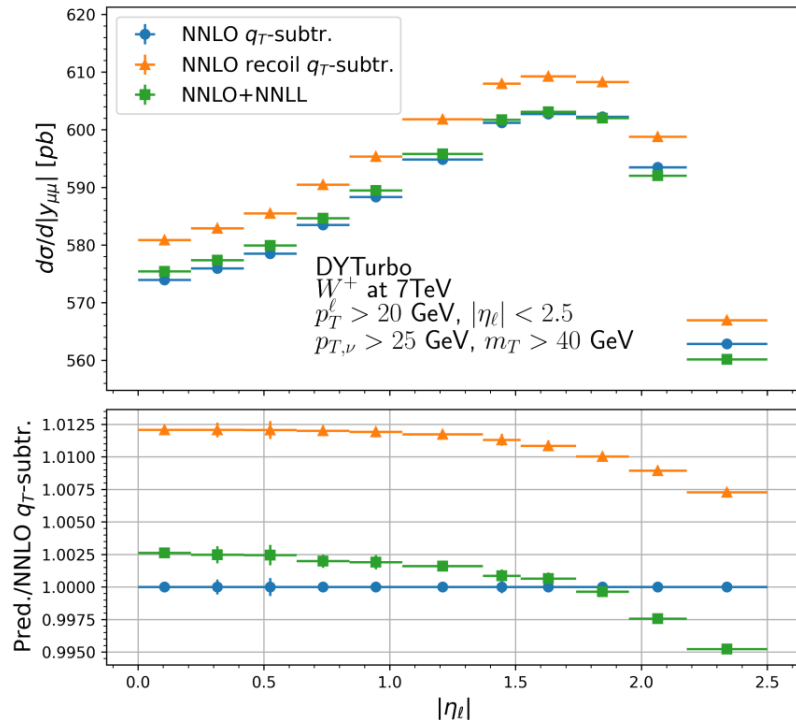


Prediction for **Z mass peak** (other bins in backup) cross section

- $q_T$  subtraction result
- Include linear power corrections with  $q_T$  recoil
- Include  $q_T$  resummation

Negligible statistical uncertainty, 0.1 – 0.5per mille

# NNLO QCD Predictions with DYTurbo



Prediction for  $W^{+/-}$  cross section

- $q_T$  subtraction result
- Include linear power corrections with  $q_T$  recoil
- Include  $q_T$  resummation

Negligible statistical uncertainty at 0.1 – 0.5 per mille

# Comparison with data

Include NLO EW corrections from  
*ReneSANCe* [[arXiv:1310.3644](https://arxiv.org/abs/1310.3644)]

NLO QED

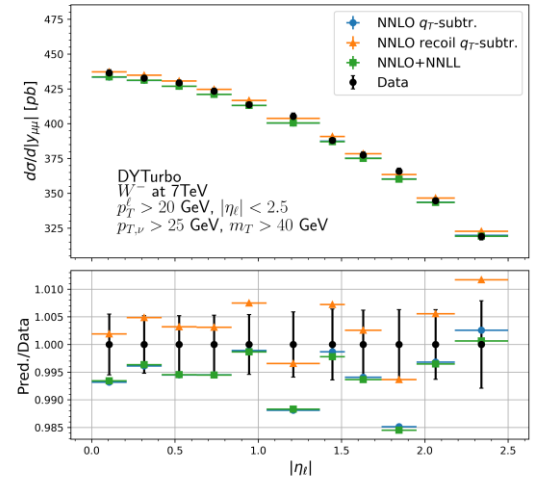
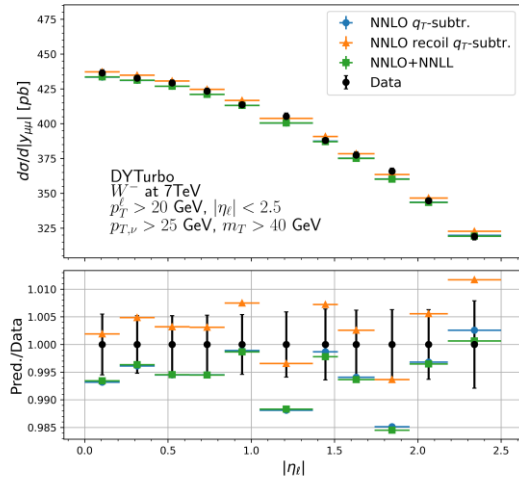
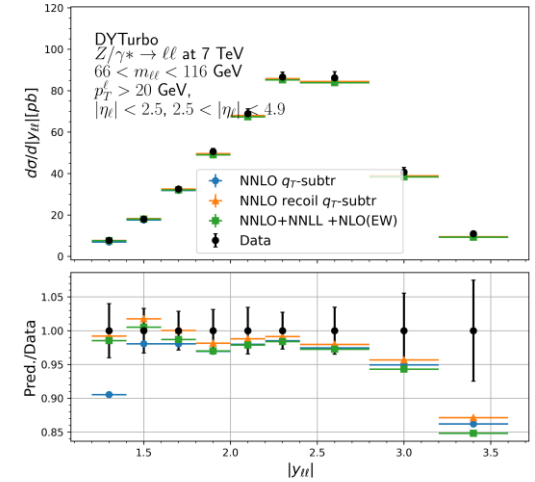
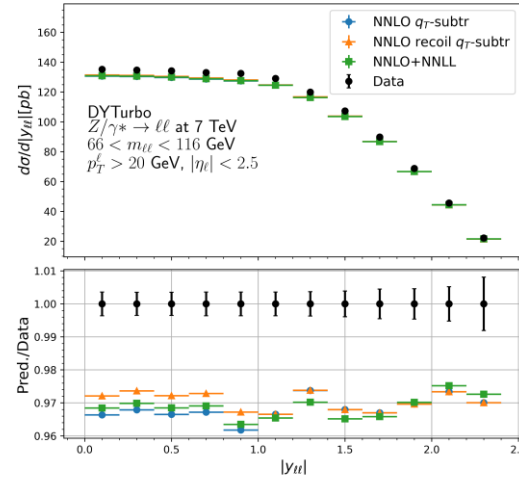
- pure Weak
- Initial State Radiation
- Initial Final Interference

Use Kfactor applied multiplicatively

$$kF_{NLO(EW)} = \sigma_{NLO(EW)}^{LO(QCD)} / \sigma_{LO(EW)}^{LO(QCD)}$$

EW correction important to describe the data

- We observe:  $\Delta\chi_{NLO(EW)}^2 \simeq 20$



# Quantitative comparison with data

$\chi^2$  data theory comparison

- Study performed with **xFitter** framework
- Include PDF uncertainties
- Theo. & exp. correlated uncertainty accounted with nuisance parameters  $\mathbf{b}^{th}, \mathbf{b}^{data}$

$$\chi^2(\mathbf{b}^{data}, \mathbf{b}^{th}) = \sum_i \frac{[D_i - T_i(1 - \sum_j \gamma_{ij}^{th} b_j^{th} - \sum_j \gamma_{ij}^{data} b_j^{data})]^2}{\Delta_i^2} + \sum_j b_{j,data}^2 + \sum_k b_{k,th}^2$$

Data set  $\chi^2$

Correlated  $\chi^2$

We test different PDFs

- Theory points  $T_i$  obtained with PDF and NLO APPLgrid (generated with MCFM)
- NNLO QCD + NLO EW accuracy reached with *kFactors*
- NNLO QCD from DYTurbo

$$kF = \frac{\sigma_i^{NNLO(QCD)+NLO\ EW}}{\sigma_i^{NLO(QCD)}}$$

*Reproduce ATLAS paper results*

*Slightly better result  $\rightarrow$  better stat of new predictions*

CT14nnlo 68%CL

Dataset	DYNNLO ATL. paper	DYTurbo $q_T$ -subtr.
ATLAS W+ $ \eta_\ell $	10 / 11	9.4 / 11
ATLAS W- $ \eta_\ell $	9.0 / 11	8.2 / 11
ATLAS low mass Z $ y_{\ell\ell} $	11 / 6	11 / 6
ATLAS peak CC Z $ y_{\ell\ell} $	15 / 12	15 / 12
ATLAS peak CF Z $ y_{\ell\ell} $	10 / 9	9.6 / 9
ATLAS high mass CC Z $ y_{\ell\ell} $	6.3 / 6	6.0 / 6
ATLAS high mass CF Z $ y_{\ell\ell} $	5.1 / 6	5.2 / 6
Correlated $\chi^2$	39	39
Log penalty $\chi^2$	-4.09	-4.33
Total $\chi^2$ / dof	102 / 61	99 / 61
$\chi^2$ p-value	0.00	0.00

# Quantitative comparison with data

Use CT14 NNLO PDF rescaled at 68%CL

- Used in the ATLAS paper
- Does not include these data set

Dataset	CT14nnlo 68%CL		
	NNLO $q_T$ -subtr.	NNLO recoil $q_T$ -subtr.	NNLO+ NNLL
ATLAS W+ lepton rapidity	9.4 / 11	8.8 / 11	8.8 / 11
ATLAS W- lepton rapidity	8.2 / 11	8.7 / 11	8.2 / 11
ATLAS low mass Z rapidity	11 / 6 →	7.2 / 6 →	7.5 / 6
ATLAS peak CC Z rapidity	15 / 12 →	10 / 12 →	7.7 / 12
ATLAS peak CF Z rapidity	9.6 / 9	5.3 / 9	6.4 / 9
ATLAS high mass CC Z rapidity	6.0 / 6	6.5 / 6	5.8 / 6
ATLAS high mass CF Z rapidity	5.2 / 6	5.6 / 6	5.3 / 6
Correlated $\chi^2$	39 →	40 →	32
Log penalty $\chi^2$	-4.33	-3.39	-4.20
Total $\chi^2$ / dof	99 / 61 →	88 / 61 →	77 / 61
$\chi^2$ p-value	0.00	0.01	0.08

Improvement of single data set  $\chi^2$

Including resummation effects reduce the total  $\chi^2$  of 10(20) points

# Compare to other PDF sets

PDFs NOT include  
ATLAS 7TeV data  
sets



PDF	Total $\chi^2$ (ndf=61)		
	NNLO $q_T$ subtr.	NNLO recoil $q_T$ -subtr	NNLO+NLL
CT10nnlo68%CL	100	85	76
CT14nnlo68%CL	99	88	77
CT18NNLO68%CL	102	90	79
MMHT14nnlo68%CL	124	99	94
NNPDF30nnlo	139	133	111
ABMP16_5_NNLO	124	106	92
HERAII PDF	199	201	160

PDFs include ATLAS  
7TeV data sets



PDF	Total $\chi^2$ (ndf=61)		
	NNLO $q_T$ subtr.	NNLO recoil $q_T$ -subtr	NNLO+NLL
CT18ANNLO68	96	84	74
MSHT20nnlo	111	87	79
NNPDF31	91	84	71
NNPDF40nnlo	89	83	69

We always observe a reduction of the  $\chi^2$  when  
including  $q_T$  resummation  $\rightarrow \Delta\chi^2 \sim 20(10)$

# PDF profiling

Quantify the impact of new data in PDF determination

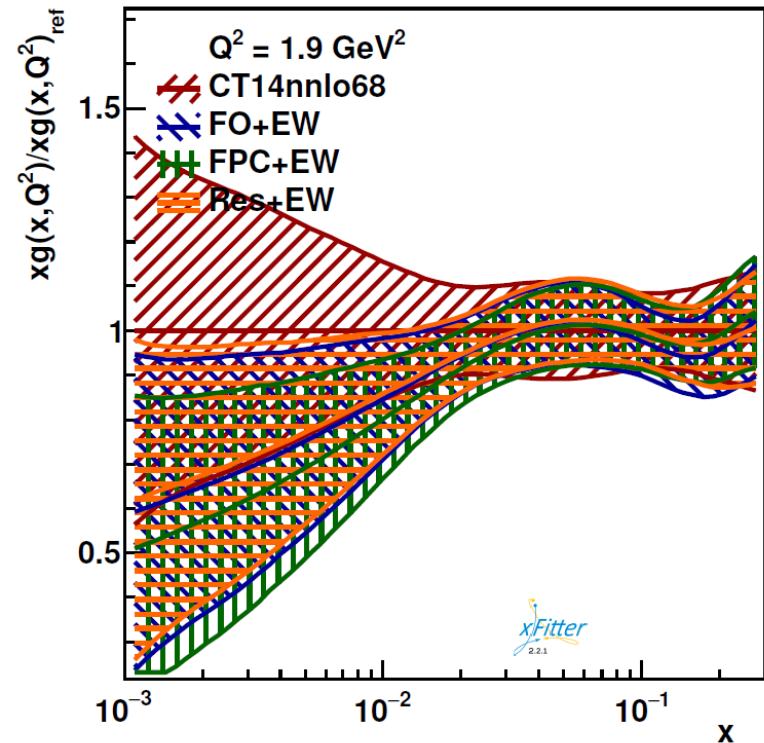
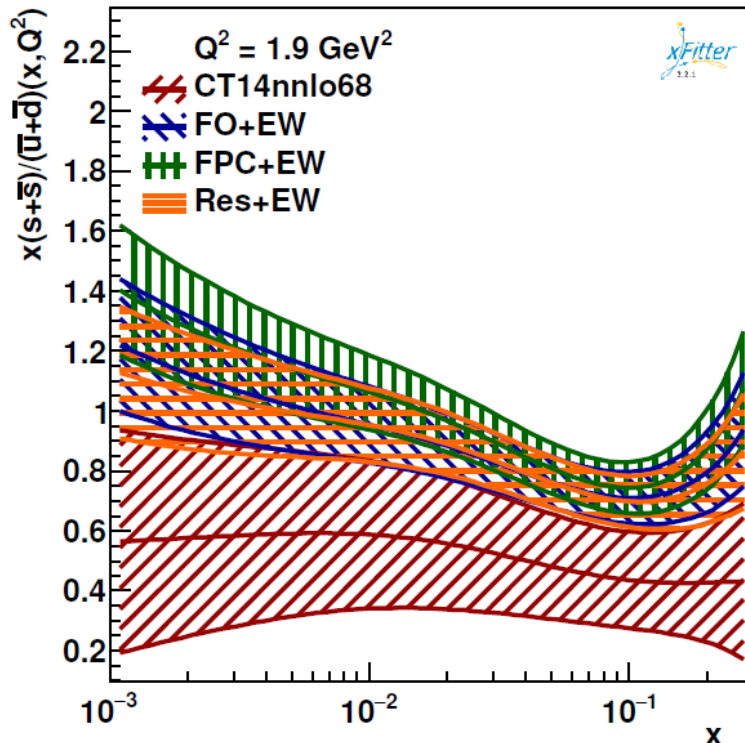
Use the shift  $b_{th}$  to update the PDF

- Uncertainty reduction
- Shift of the central value

Profiled PDF

$$f'_0 = f_0 + \sum_k \beta_{k,th}^{\min} \left( \frac{f_k^+ - f_k^-}{2} - \beta_{k,th}^{\min} \frac{f_k^+ + f_k^- - 2f_0}{2} \right)$$

- ATLAS data give strong constrain on strange PDF
  - What changes with new predictions?



# Conclusion and Outlook

- We looked at the effects of linear power corrections and resummation in the ATLAS 7TeV data set
  - Resummation improves the data-MC agreement
  - Improvement in  $\chi^2$  with all the PDF sets
  - The impact of ATLAS data don't change much when using different theories
- It is interesting to check the effect of fiducial cuts in other measurement phase space, (LHCb)
- Perform a PDF fit to wide DY datasets with coherent theory predictions
  - NNLO + EW Corrections fit
  - NNLO+NNLL + EW Corrections fit
- The paper with these results is in preparation
  - All of our kFactor will be public available for PDF fitters



Thanks for the attention!

# BACKUP

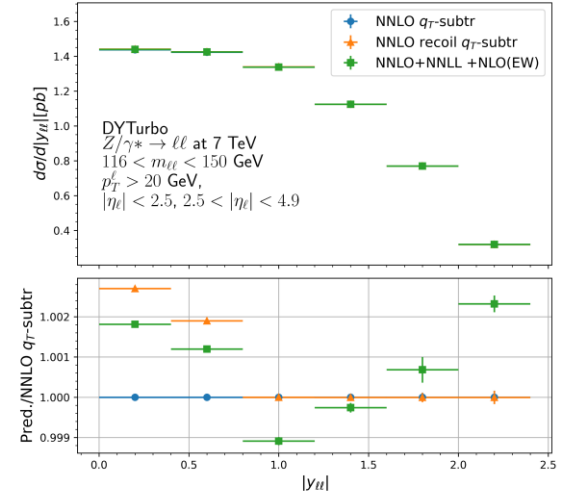
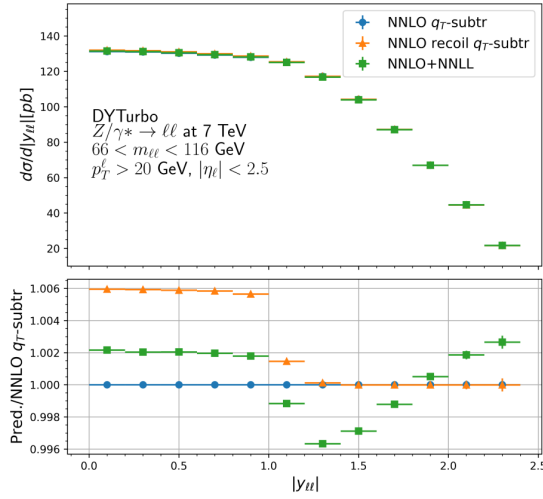
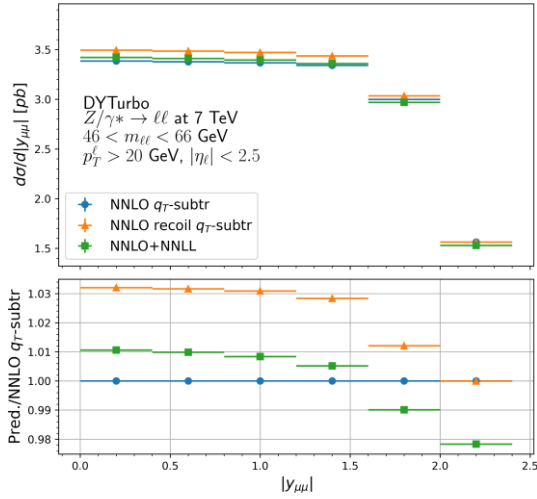
# All Z cross sections

Low  
Mass

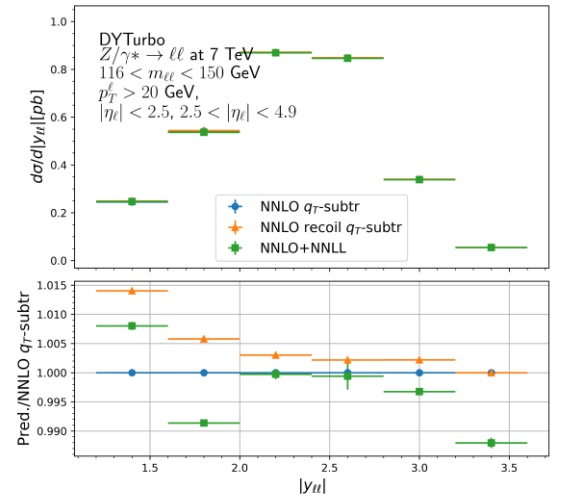
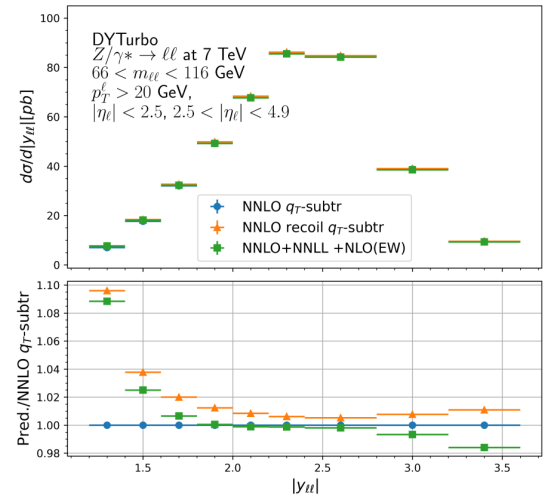
Z-Mass  
Peak

High  
Mass

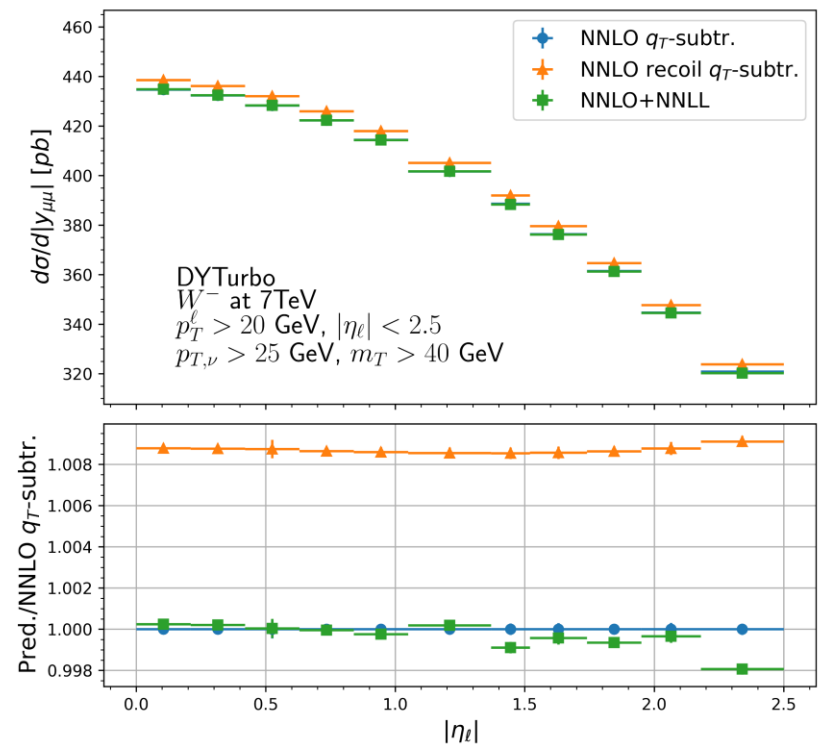
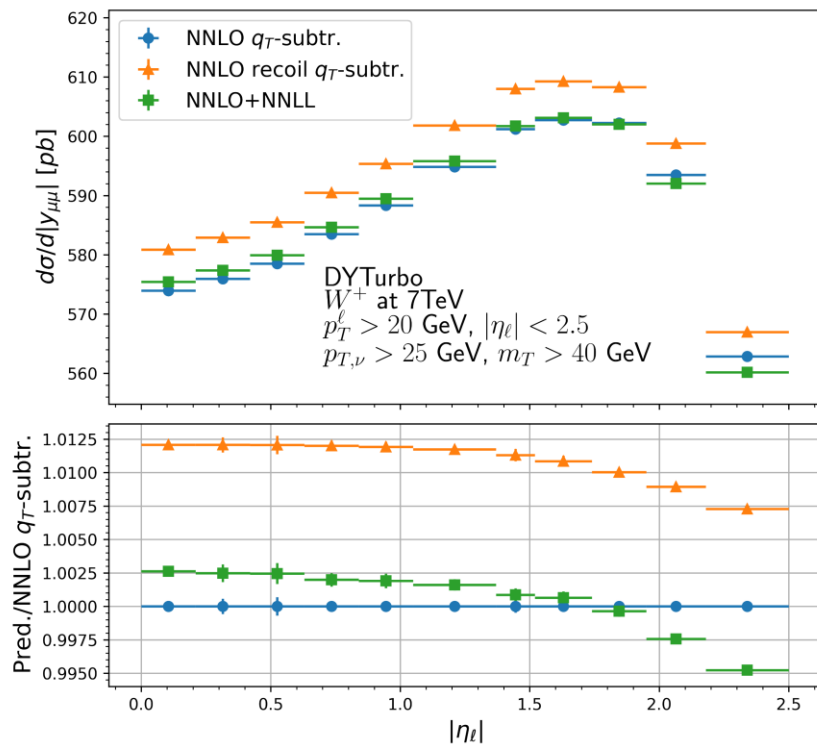
Central Channel



Forward Channel



# All $W$ cross section



# Impact of EW corrections

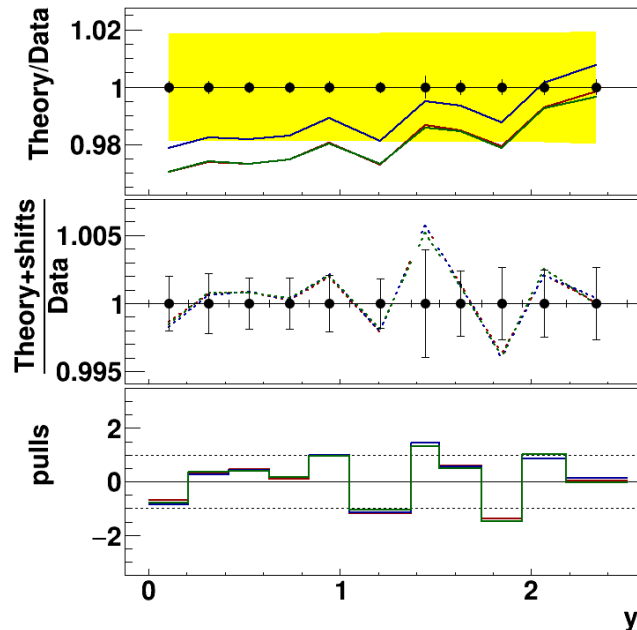
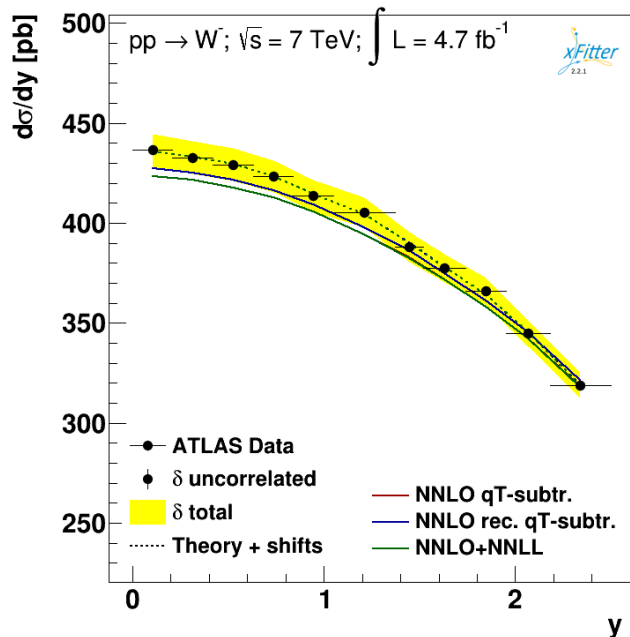
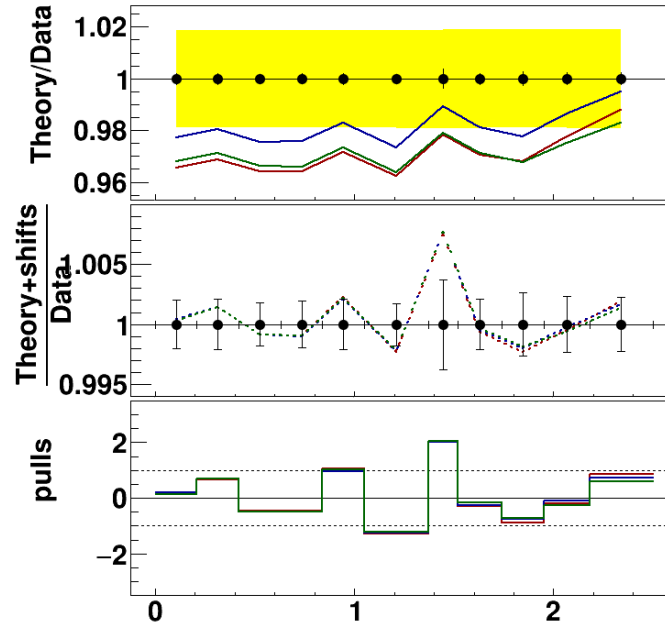
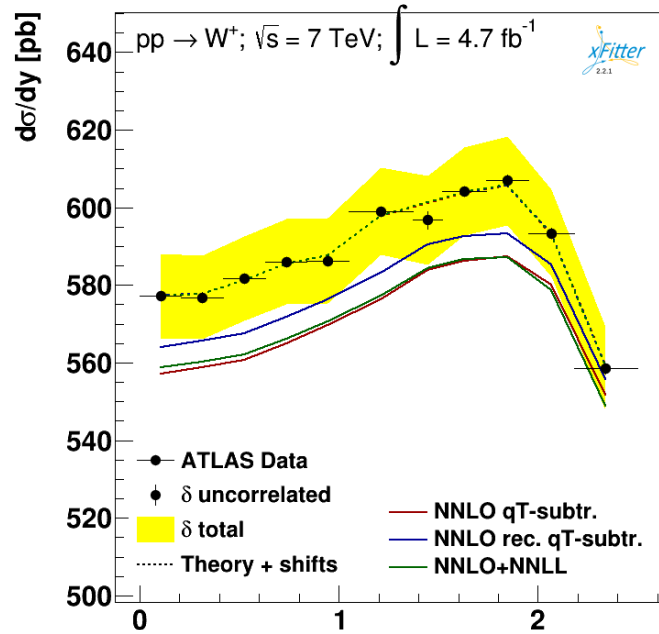
## NO EW Corrections

Dataset	FO	FPC	Res
ATLAS W- lepton rapidity 2011	9.4 / 11	9.8 / 11	9.2 / 11
ATLAS W+ lepton rapidity 2011	9.3 / 11	8.7 / 11	8.8 / 11
ATLAS peak CC Z rapidity 2011	15 / 12	11 / 12	8.2 / 12
ATLAS high mass CF Z rapidity 2011	4.4 / 6	4.7 / 6	4.5 / 6
ATLAS peak CF Z rapidity 2011	8.9 / 9	4.7 / 9	5.6 / 9
ATLAS high mass CC Z rapidity 2011	6.1 / 6	5.8 / 6	6.0 / 6
ATLAS low mass Z rapidity 2011	15 / 6	9.4 / 6	11 / 6
Correlated $\chi^2$	52	46	44
Log penalty $\chi^2$	-4.23	-3.28	-4.09
Total $\chi^2$ / dof	116 / 61	96 / 61	93 / 61
$\chi^2$ p-value	0.00	0.00	0.00

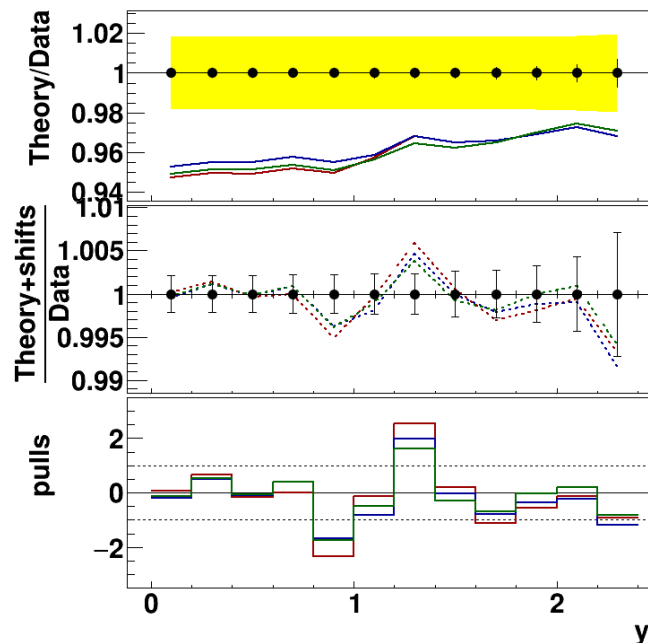
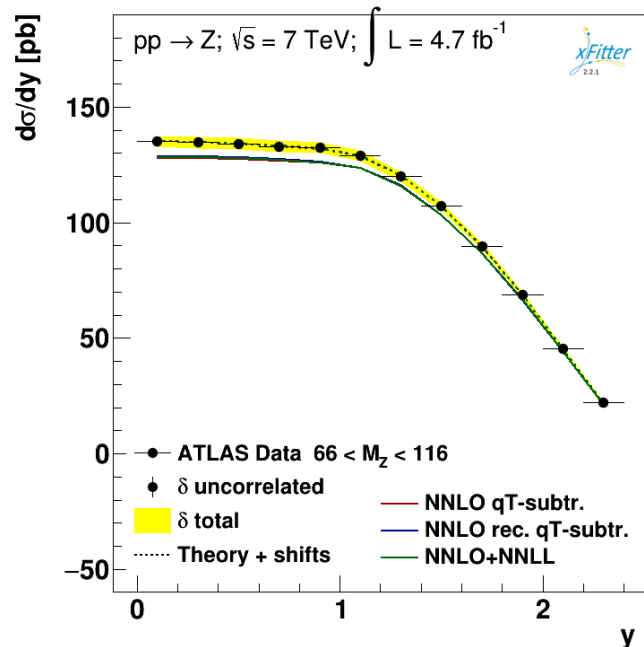
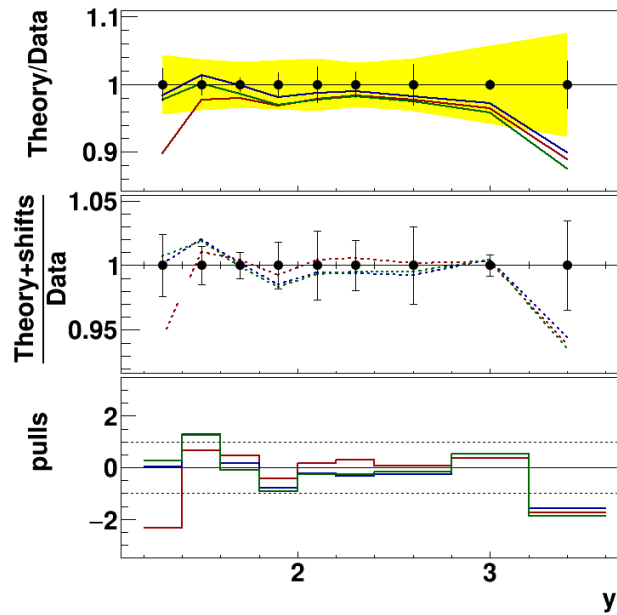
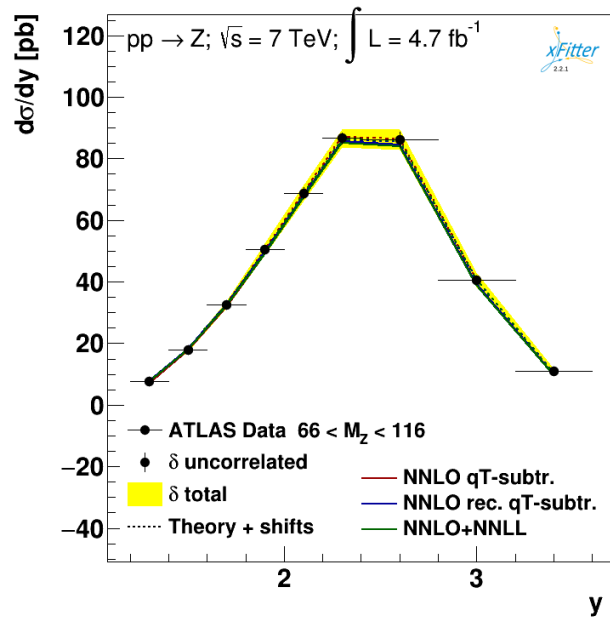
## With EW Corrections

FO	FPC	Res
12 / 6	7.1 / 6	7.3 / 6
9.5 / 11	8.9 / 11	8.8 / 11
6.0 / 6	6.8 / 6	5.9 / 6
9.6 / 9	5.4 / 9	6.4 / 9
8.3 / 11	8.8 / 11	8.2 / 11
5.1 / 6	5.5 / 6	5.2 / 6
16 / 12	12 / 12	8.0 / 12
40	40	32
-4.33	-3.39	-4.20
102 / 61	91 / 61	78 / 61
0.00	0.01	0.07

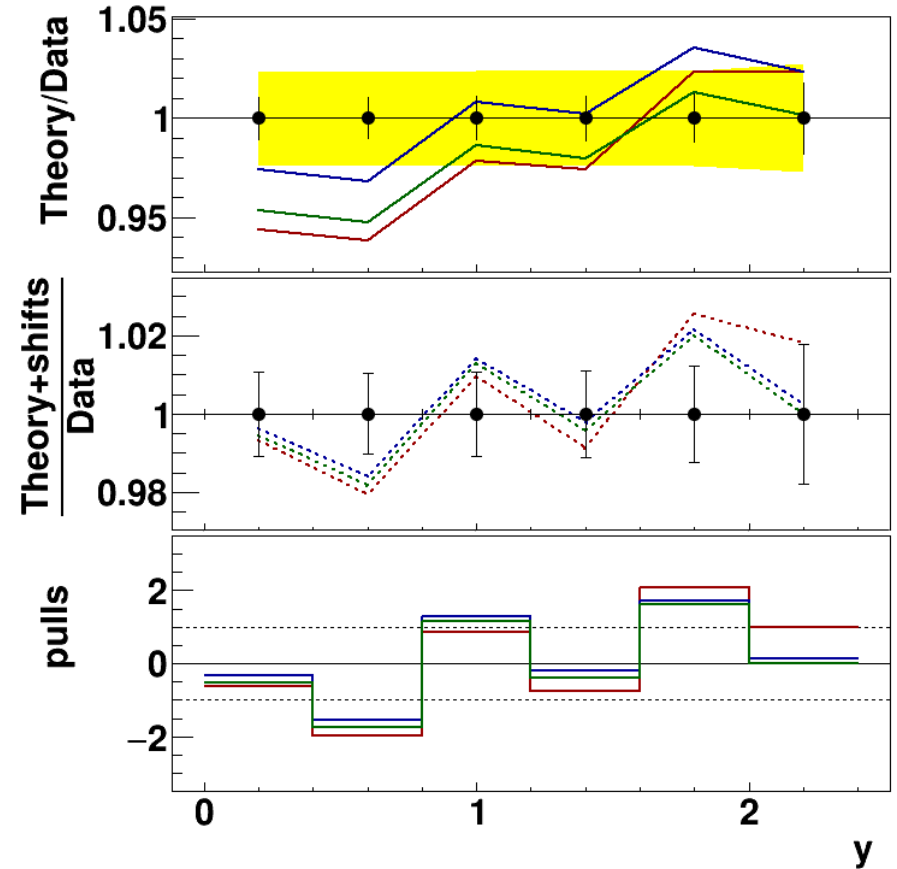
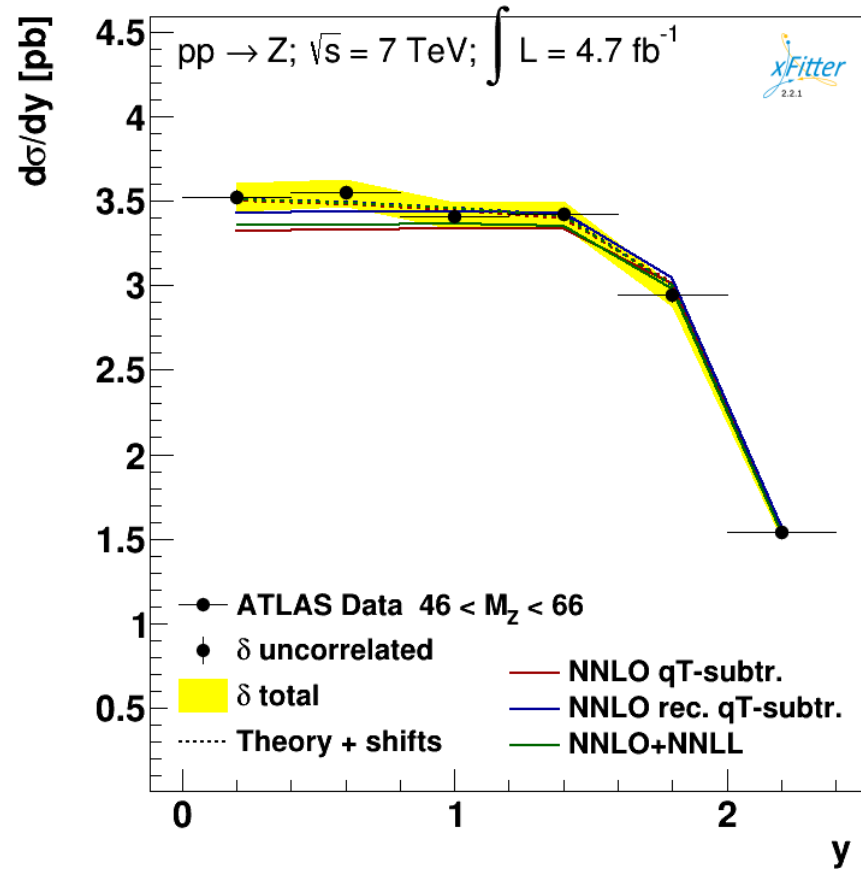
# CT14 data-theory



# CT14 data-theory

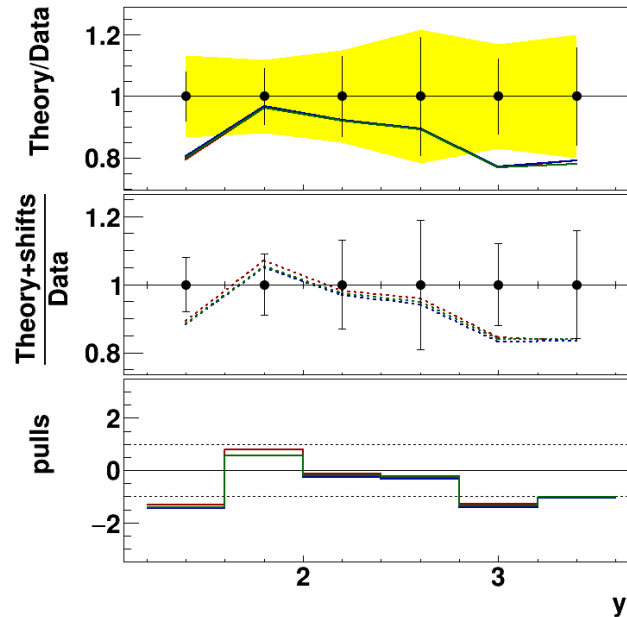
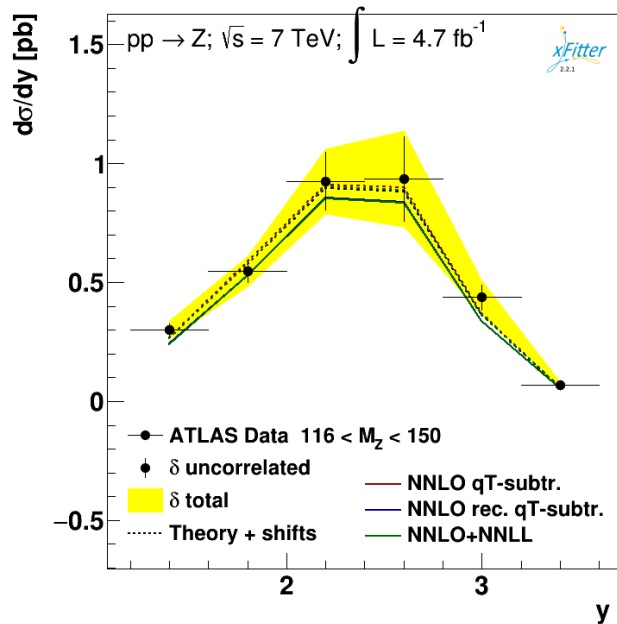
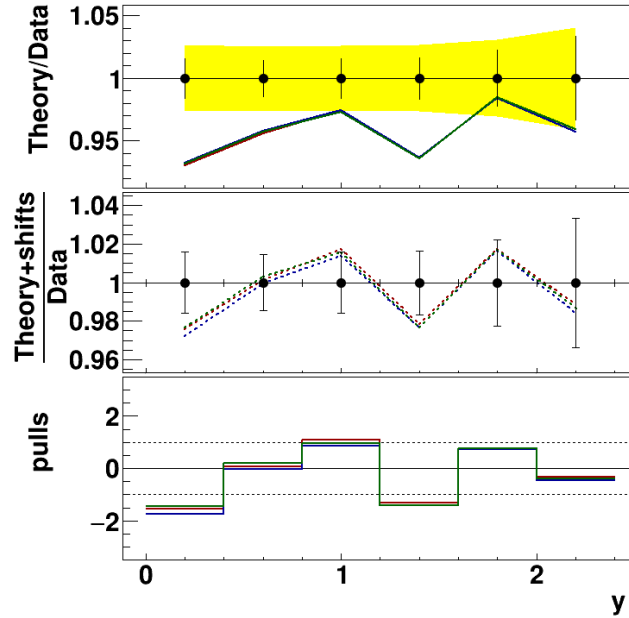
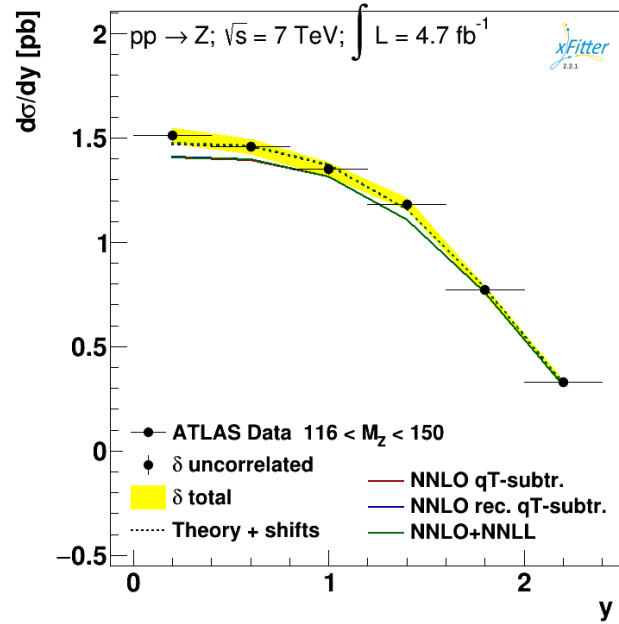


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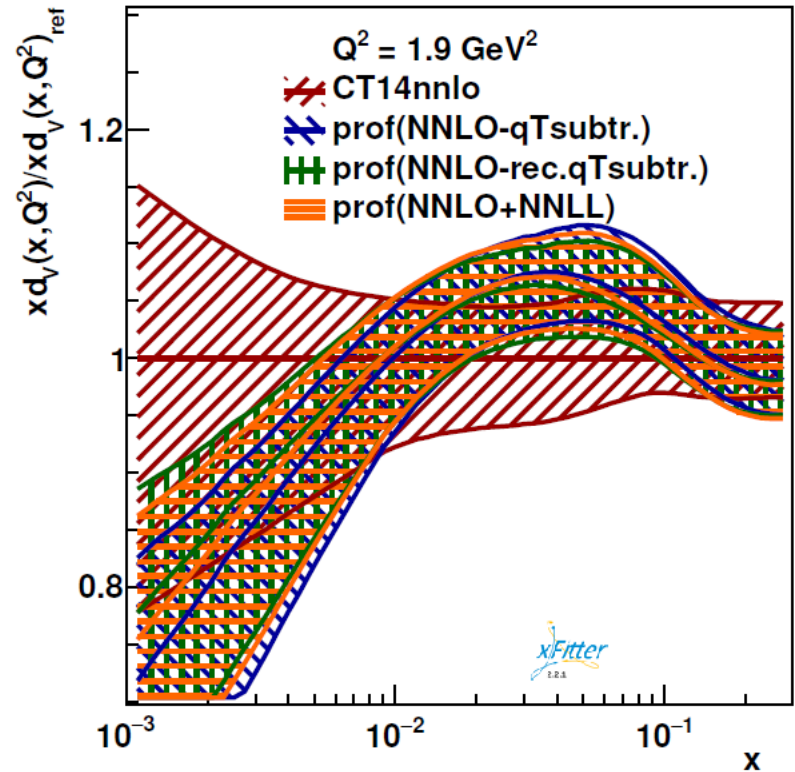
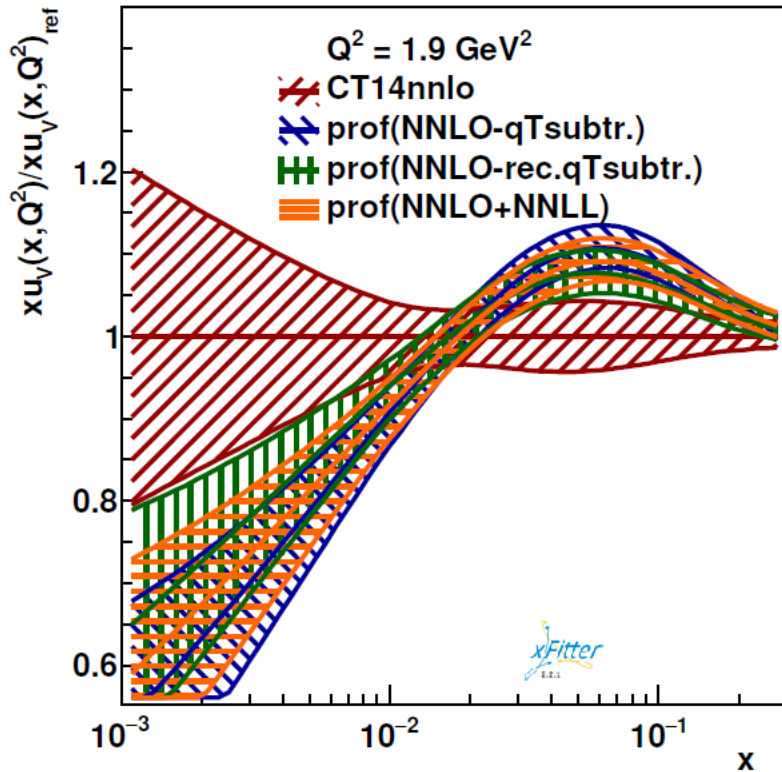




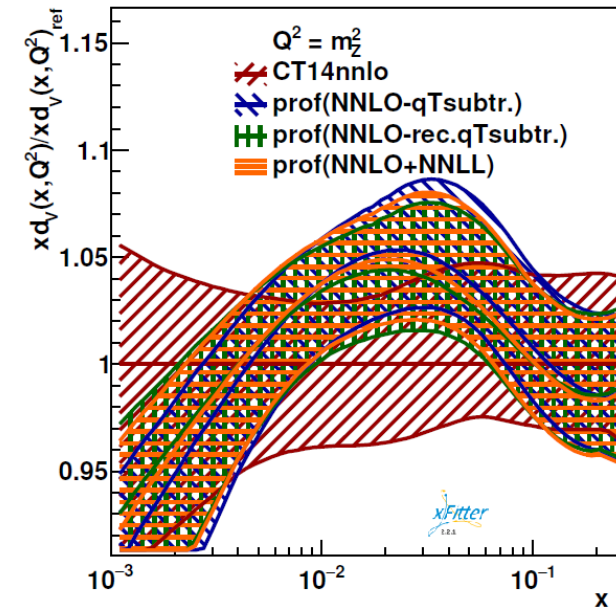
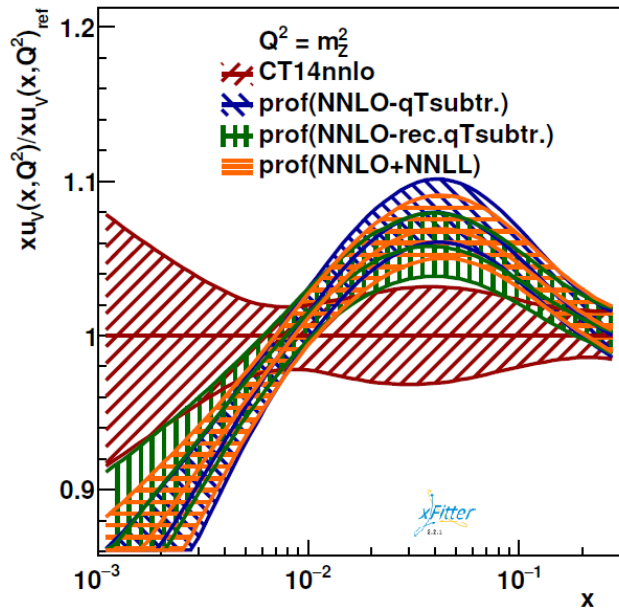
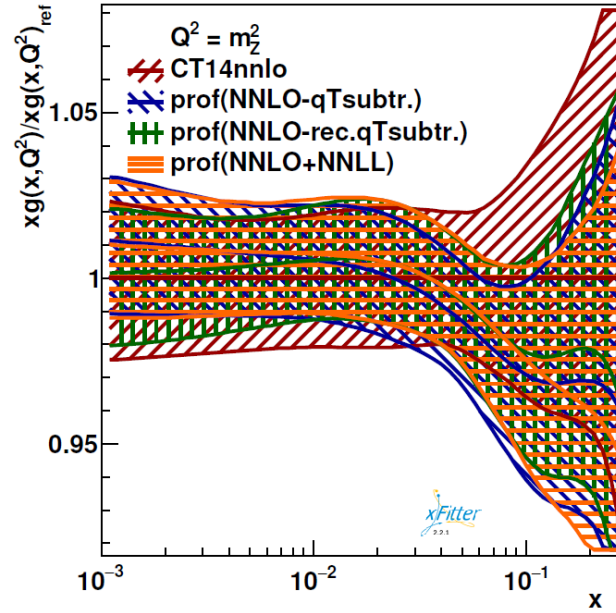
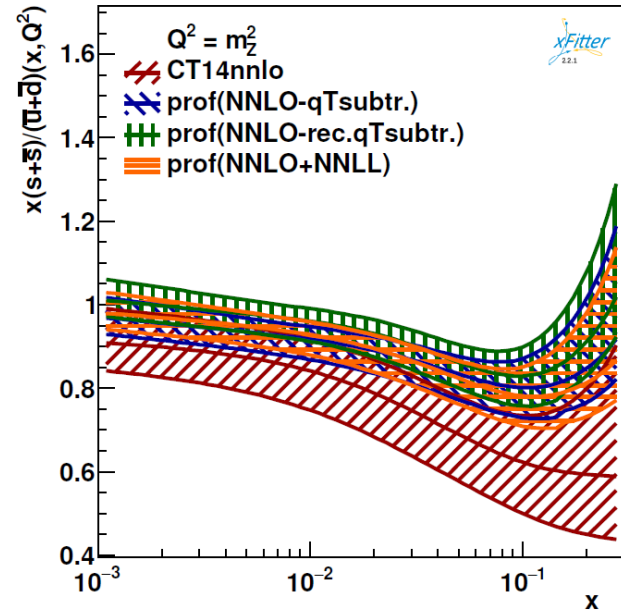
# CT14 data-theory



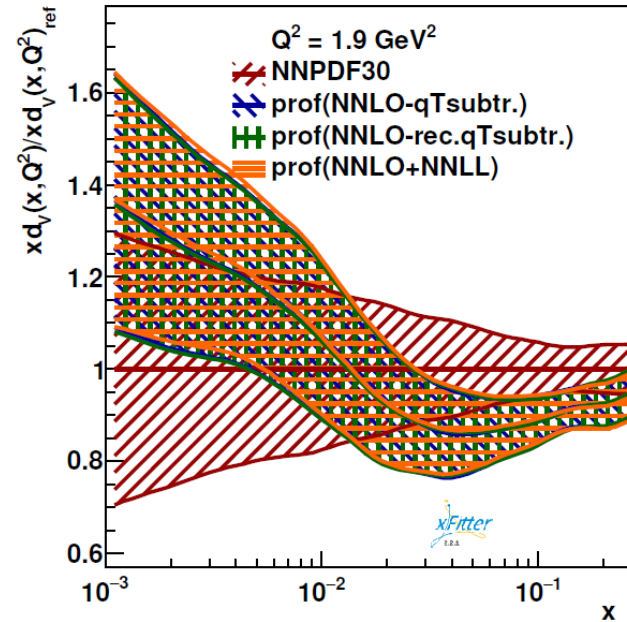
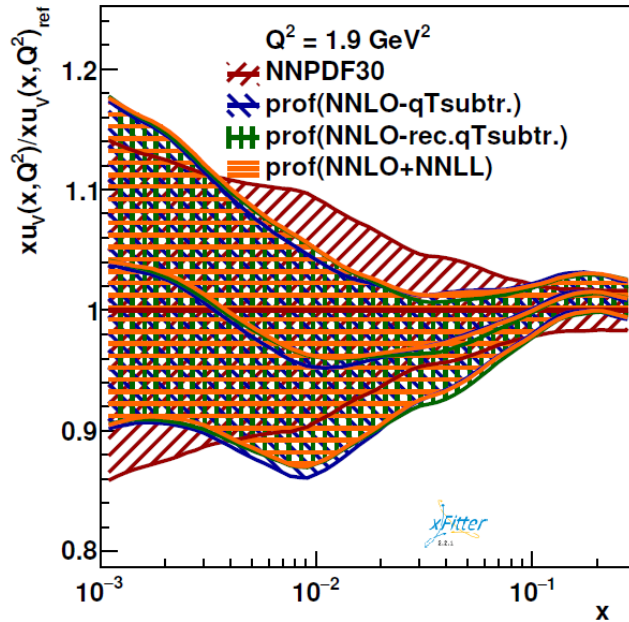
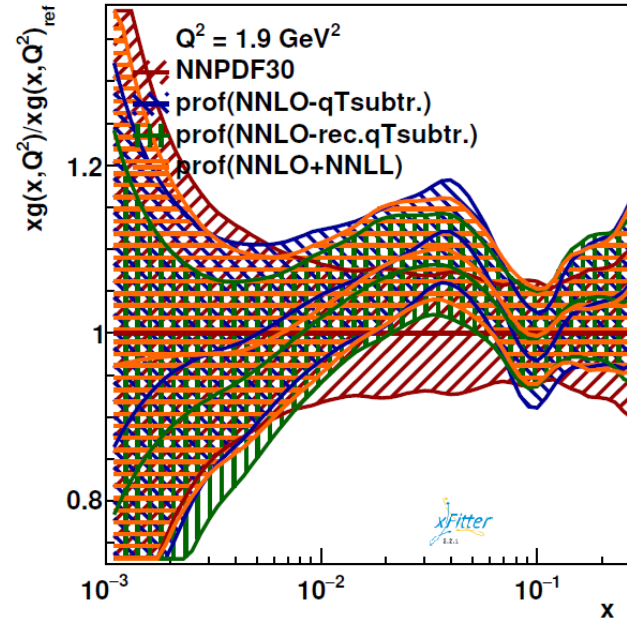
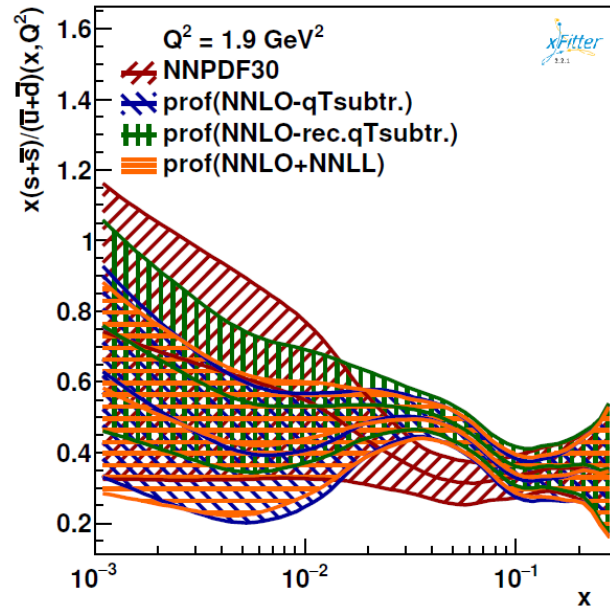
# CT14prof Q=Q0



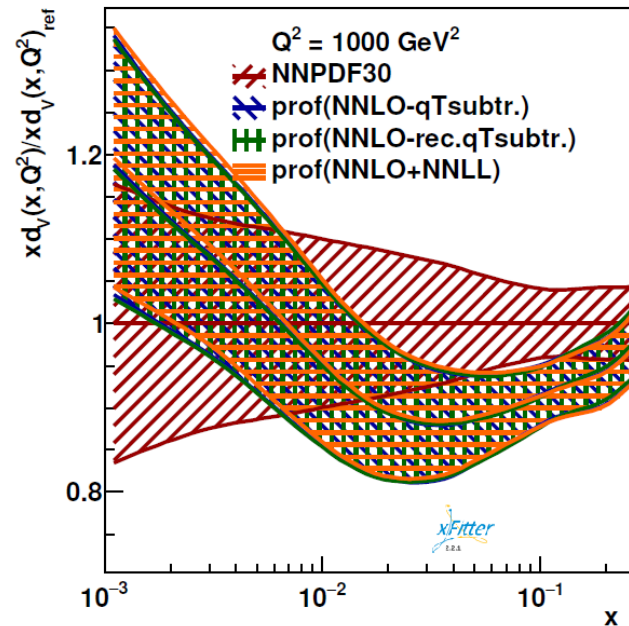
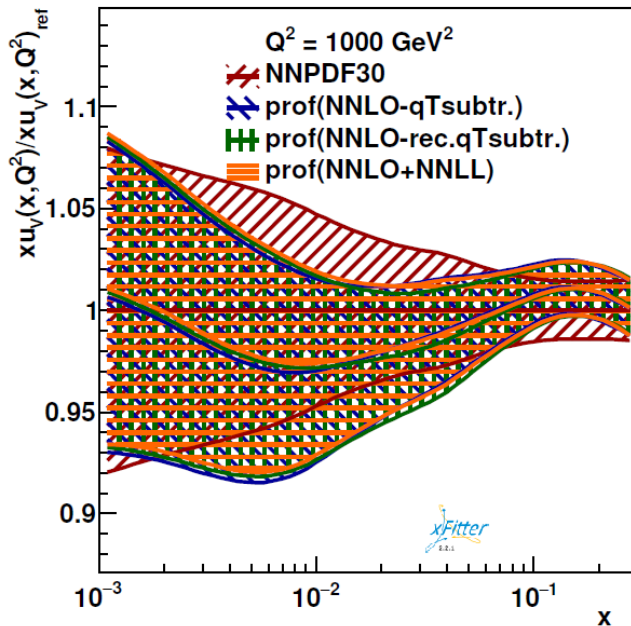
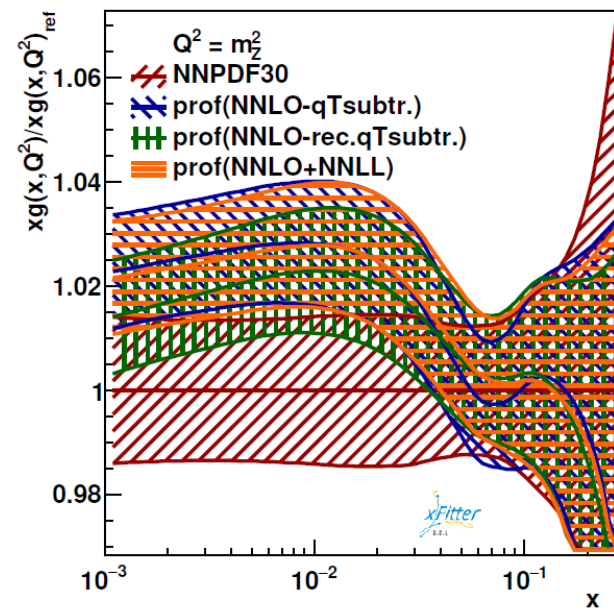
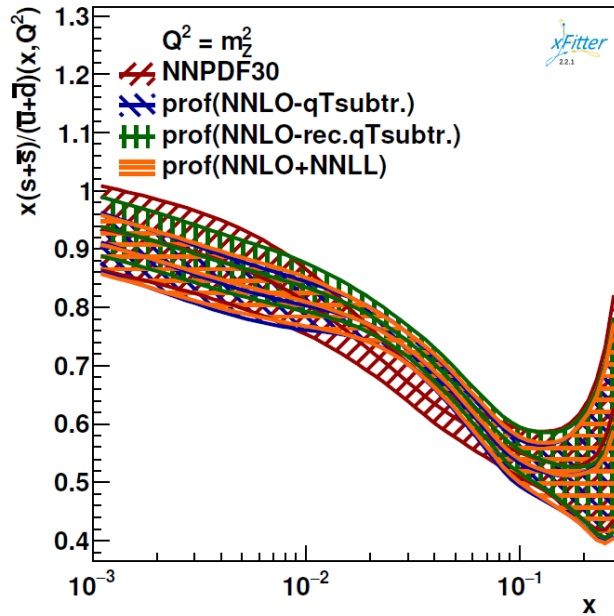
# CT14 Prof. $Q=m_Z$



# NNPDF30prof Q=Q0

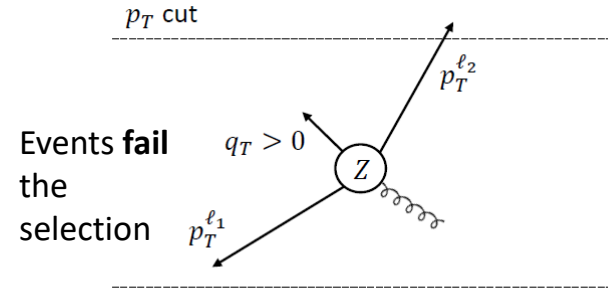
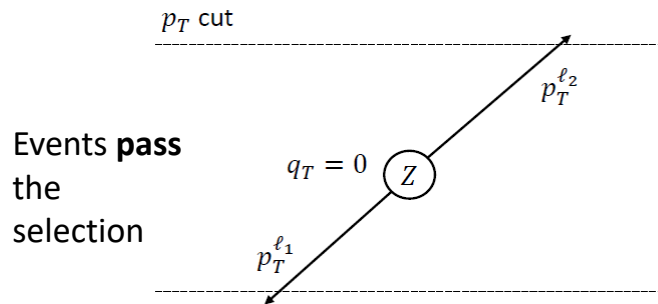


# NNPDF30prof Q=mZ



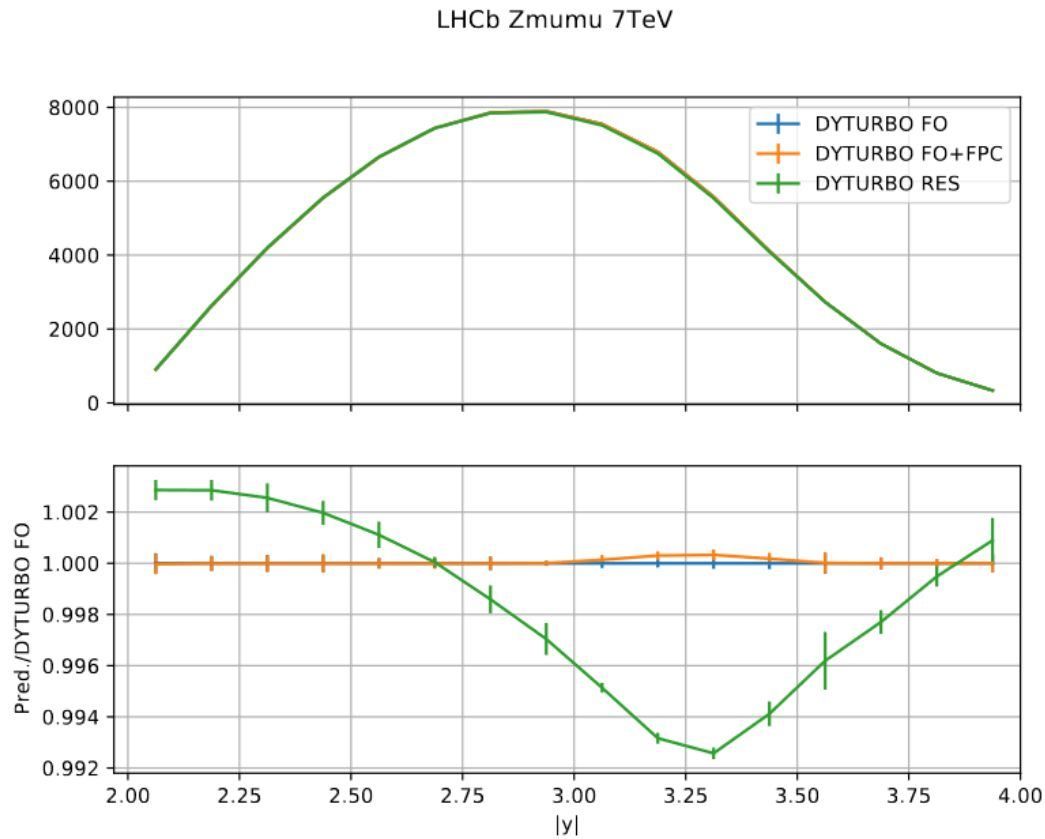
# Cuts & linear power correction

- Symmetric  $p_T$  cut configuration induces linear  $q_T$  on the acceptance  $f$ 
  - $p_T^{\ell_1}, p_T^{\ell_2} > p_T^{\text{cut}}$



- $\Phi^{\text{sym}}(q_T) = \Phi_0 + \Phi_1^{\text{sym}} \cdot \frac{q_T}{M} + O(q_T^2/M^2)$
- Great interest recently on this effect
- [Ebert, Tackmann,2019], [Ebert, Michel, Stewart, Tackmann,2020], [Alekhin, Kardos, Moch, Trocsanyi,2021],[Salam,Slade,2021],[Buonocore,Kallweit,Rottoli,Wiesemann,2021],[Camarda,Cieri,Ferrera,2021]

# LHCb Z



(a) NNLO comparison.

