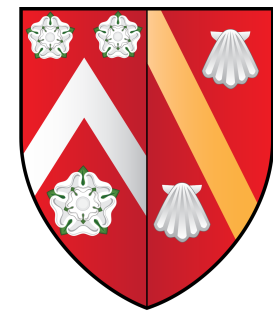


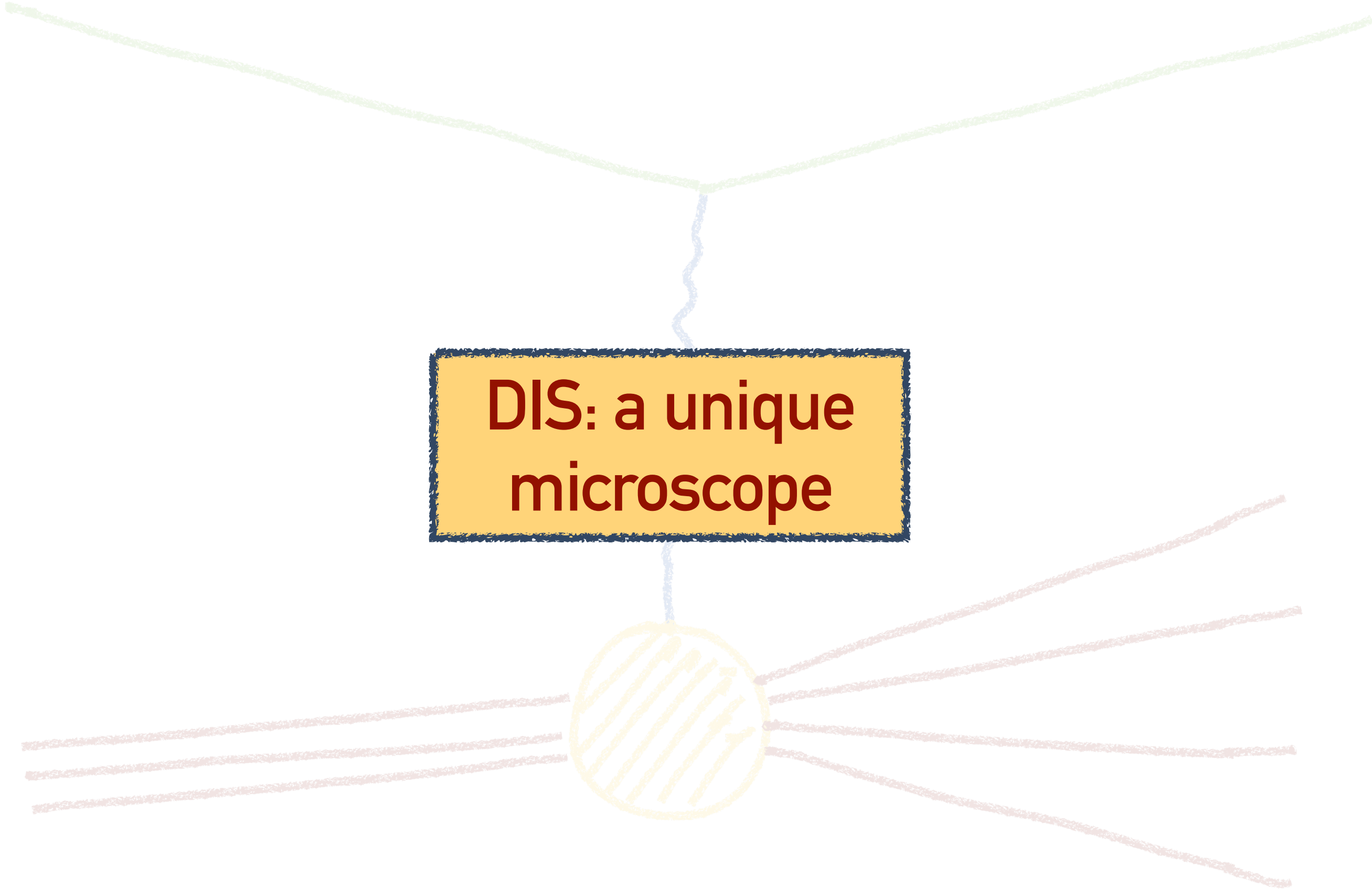
# DIS in the big picture of HEP

Fabrizio Caola

Rudolf Peierls Centre for Theoretical Physics & Wadham College

DIS2022, Santiago de Compostela, May 6th 2022



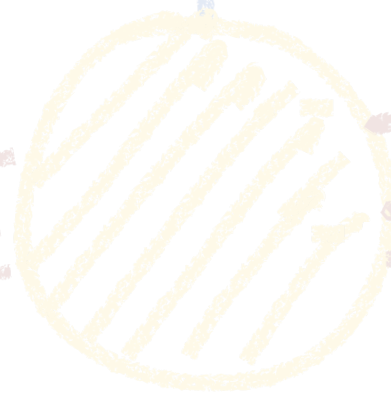


**DLS: a unique  
microscope**

## Fundamentals of QCD in a clean environment

- Bjorken scaling
- QCD evolution & the rise of the gluon at HERA
- New regimes of QCD: saturation, CGC...
- Nuclear Theory: from models to first principles

**DIS: a unique  
microscope**



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## **DIS: a unique microscope**

## A precise mapping of the proton/nuclei

- PDFs at high precision → crucial for hadron colliders
- HERA: high-precision at hadron colliders is possible
- Beyond PDFs: TMDs, 3D tomography...
- Mass/spin of the proton



## Fundamentals of QCD in a clean environment

- Bjorken scaling
- QCD evolution & the rise of the gluon at HERA
- New regimes of QCD: saturation, CGC...
- Nuclear Theory: from models to first principles

## **DIS: a unique microscope**

## A high-energy probe

- EW physics in DIS
- Precision SM parameters
- Higgs couplings
- BSM models

## A precise mapping of the proton/nuclei

- PDFs at high precision → crucial for hadron colliders
- HERA: high-precision at hadron colliders is possible
- Beyond PDFs: TMDs, 3D tomography...
- Mass/spin of the proton

# This talk:

Some illustrative examples of the richness of the DIS program, emphasising their connection to a broader HE picture

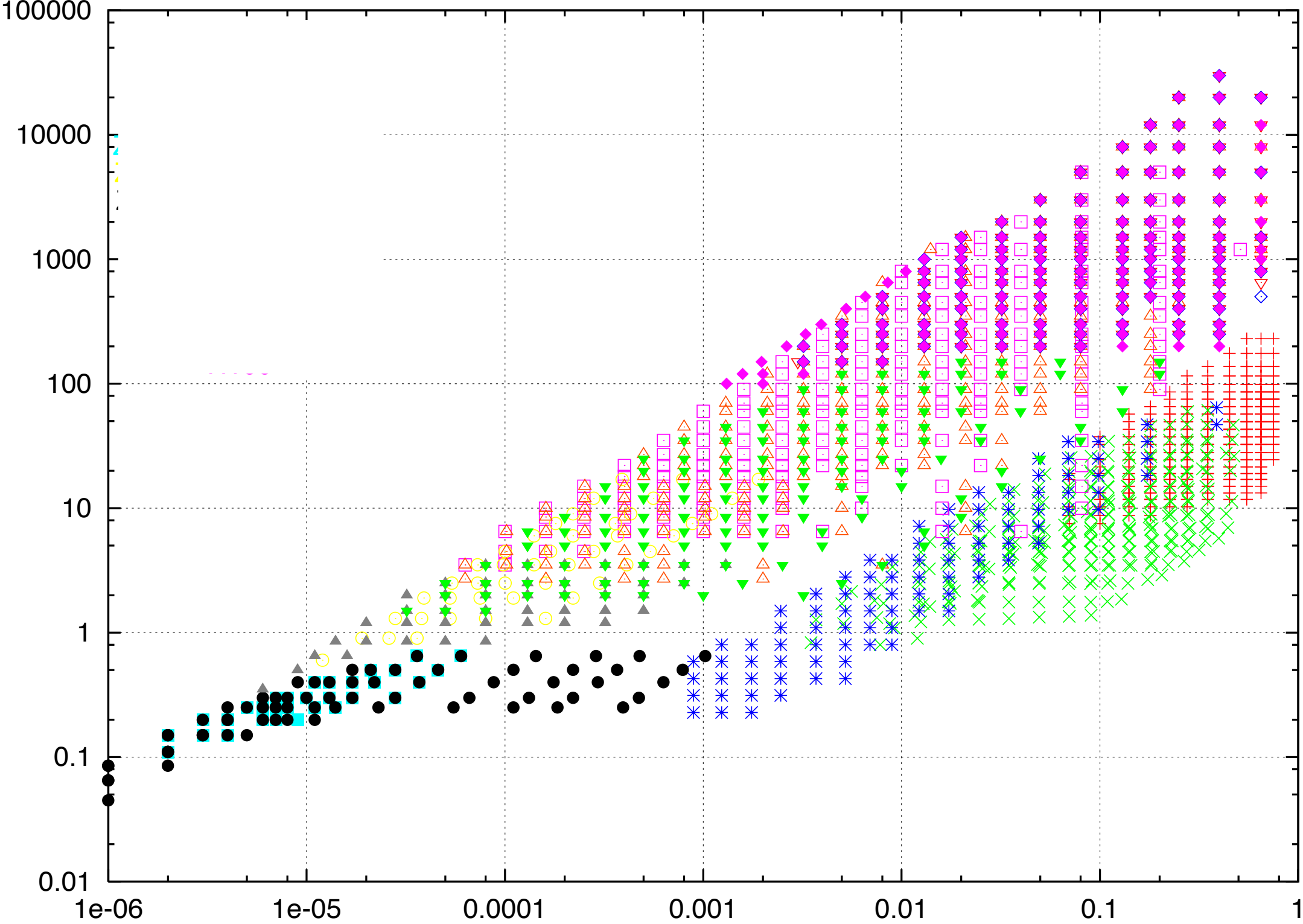
## Caveats

- Examples drawn mostly from topics I am familiar with. Apologies if your favourite subject is not here!
- Mostly focus on DIS now, but with an eye on the future.

“Future of DIS//new facilities” → J. d’Hondt, M. d’Onofrio’s talks

# DIS kinematics

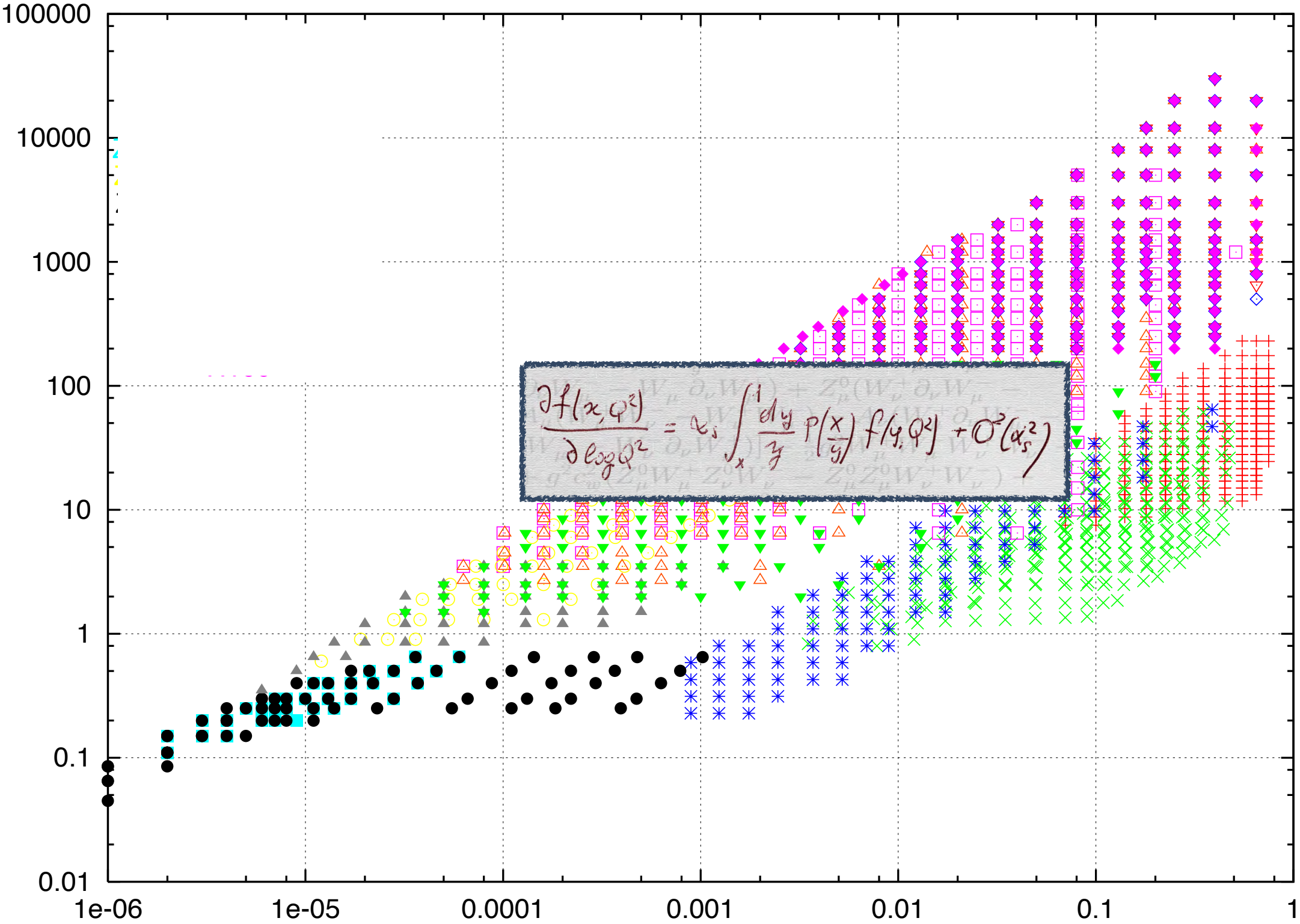
$Q^2$



$x$

# DIS kinematics

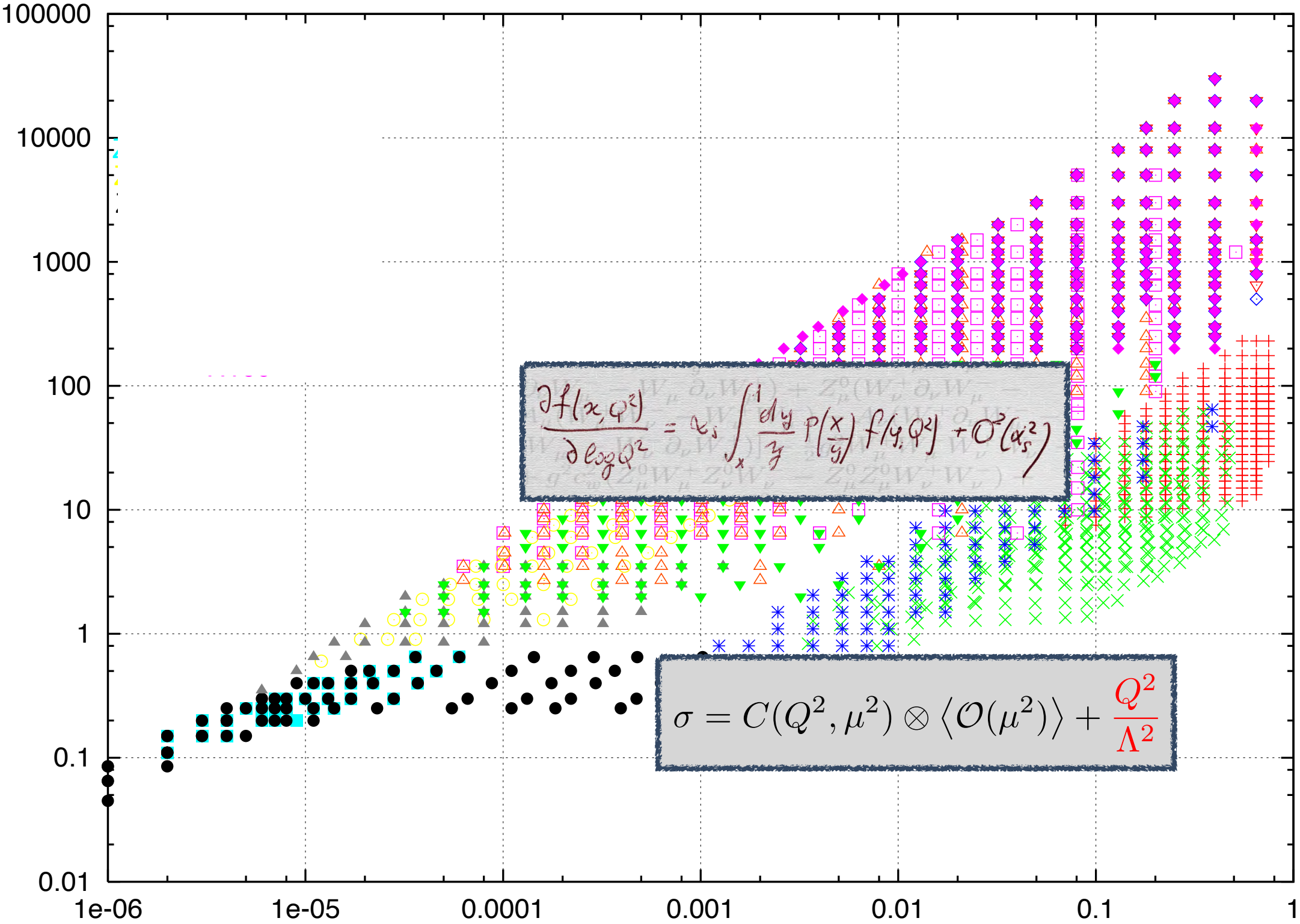
$Q^2$



$x$

# DIS kinematics

$Q^2$

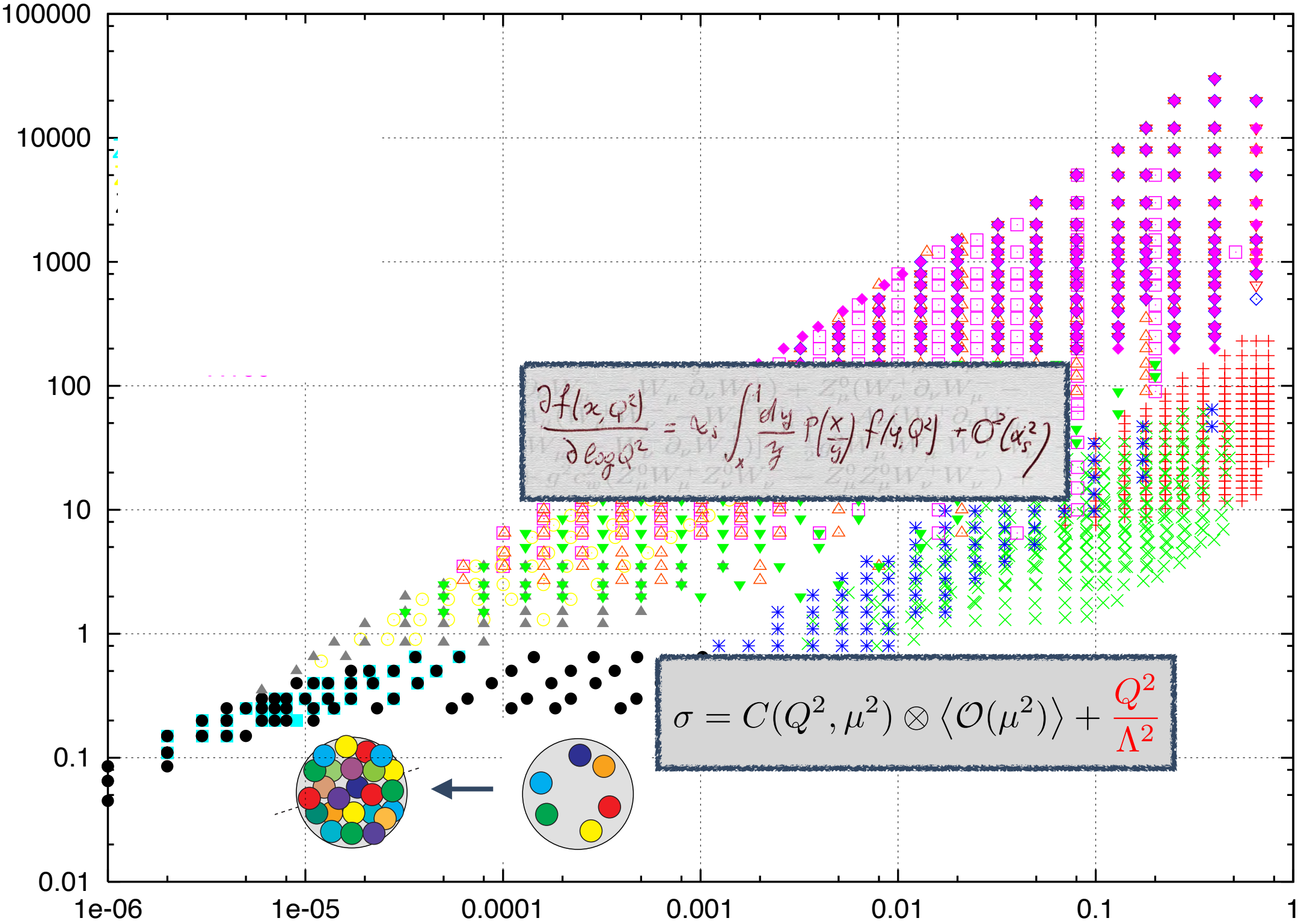


$x$



# DIS kinematics

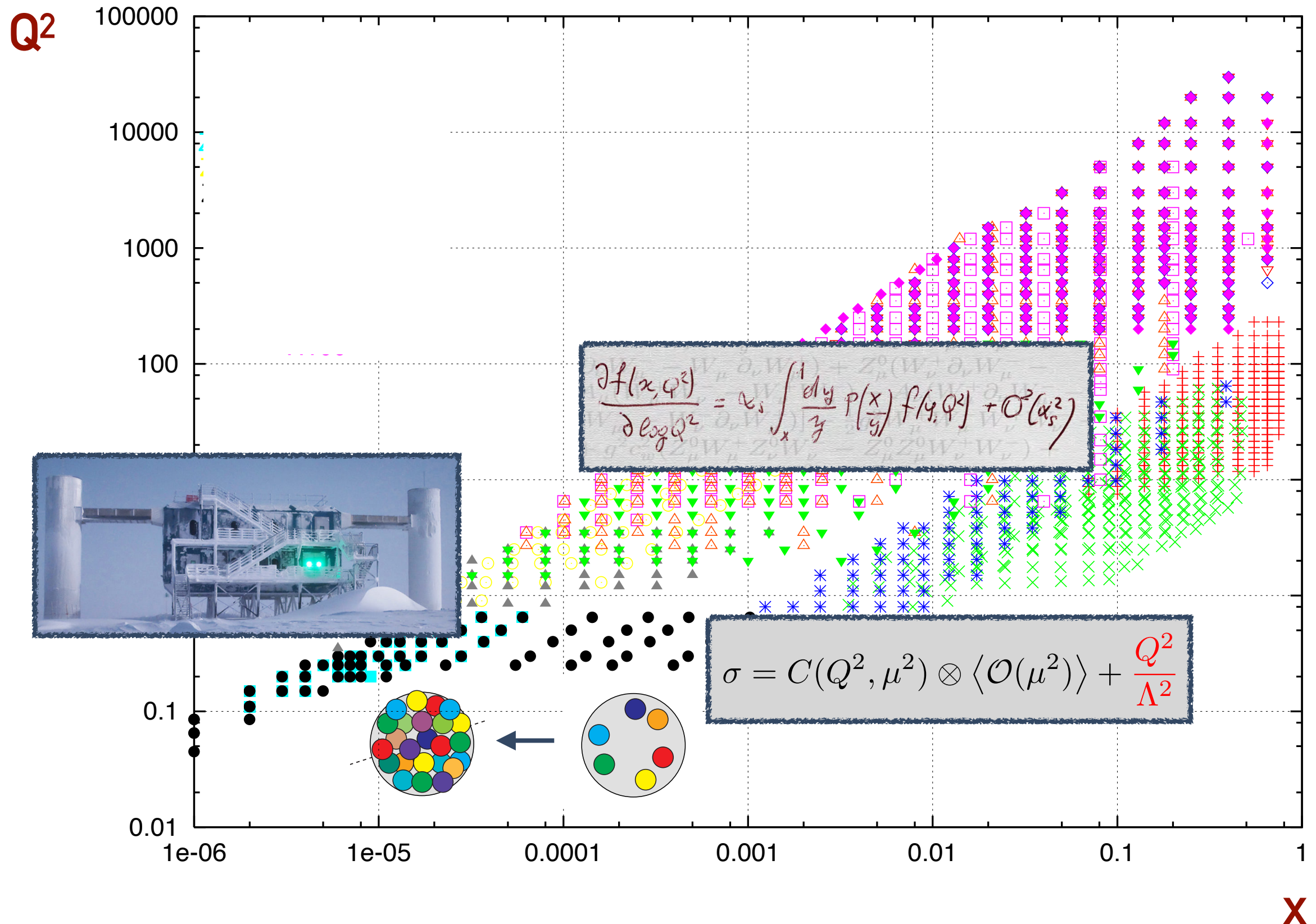
$Q^2$



$x$

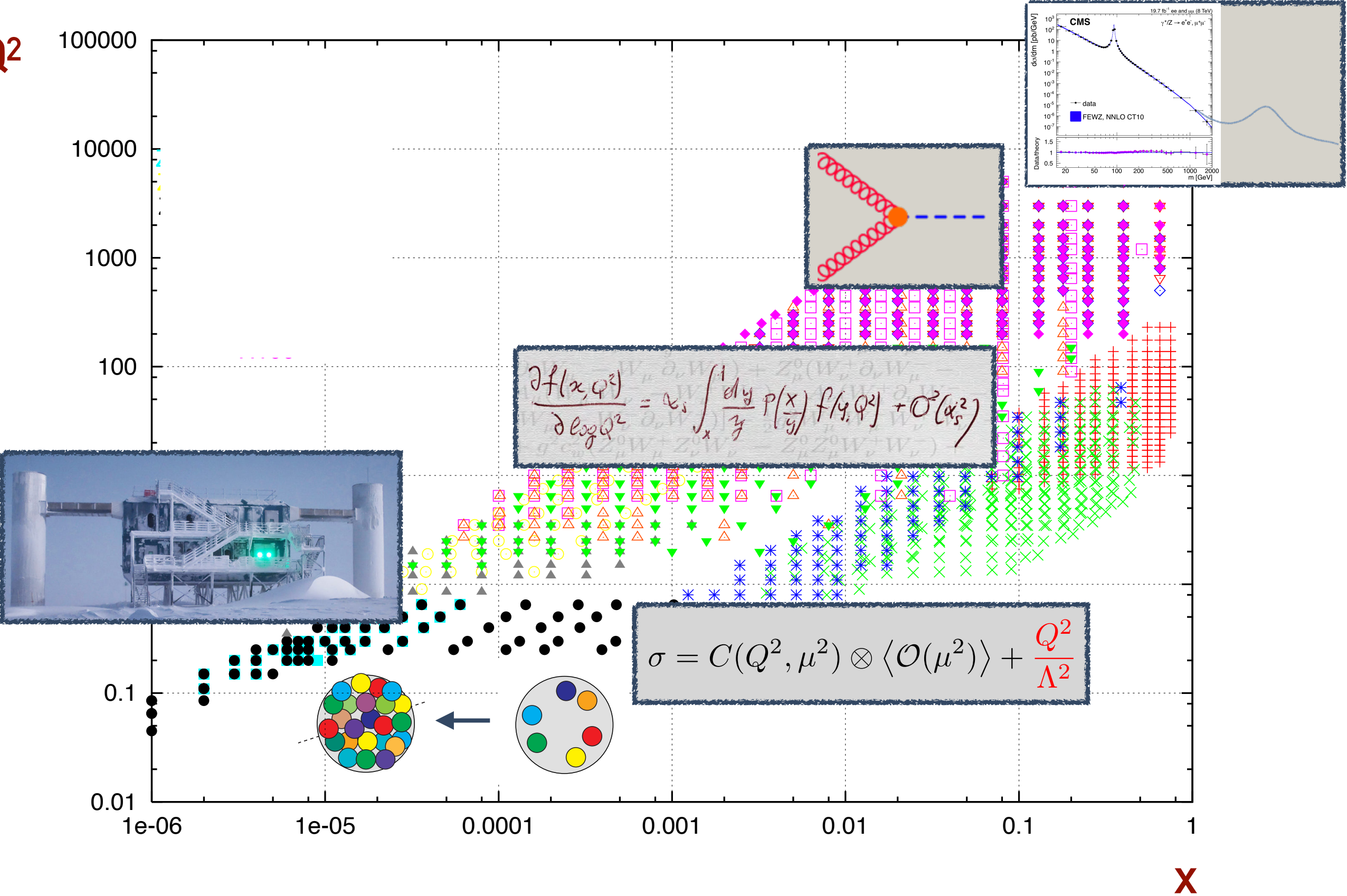


# DIS kinematics

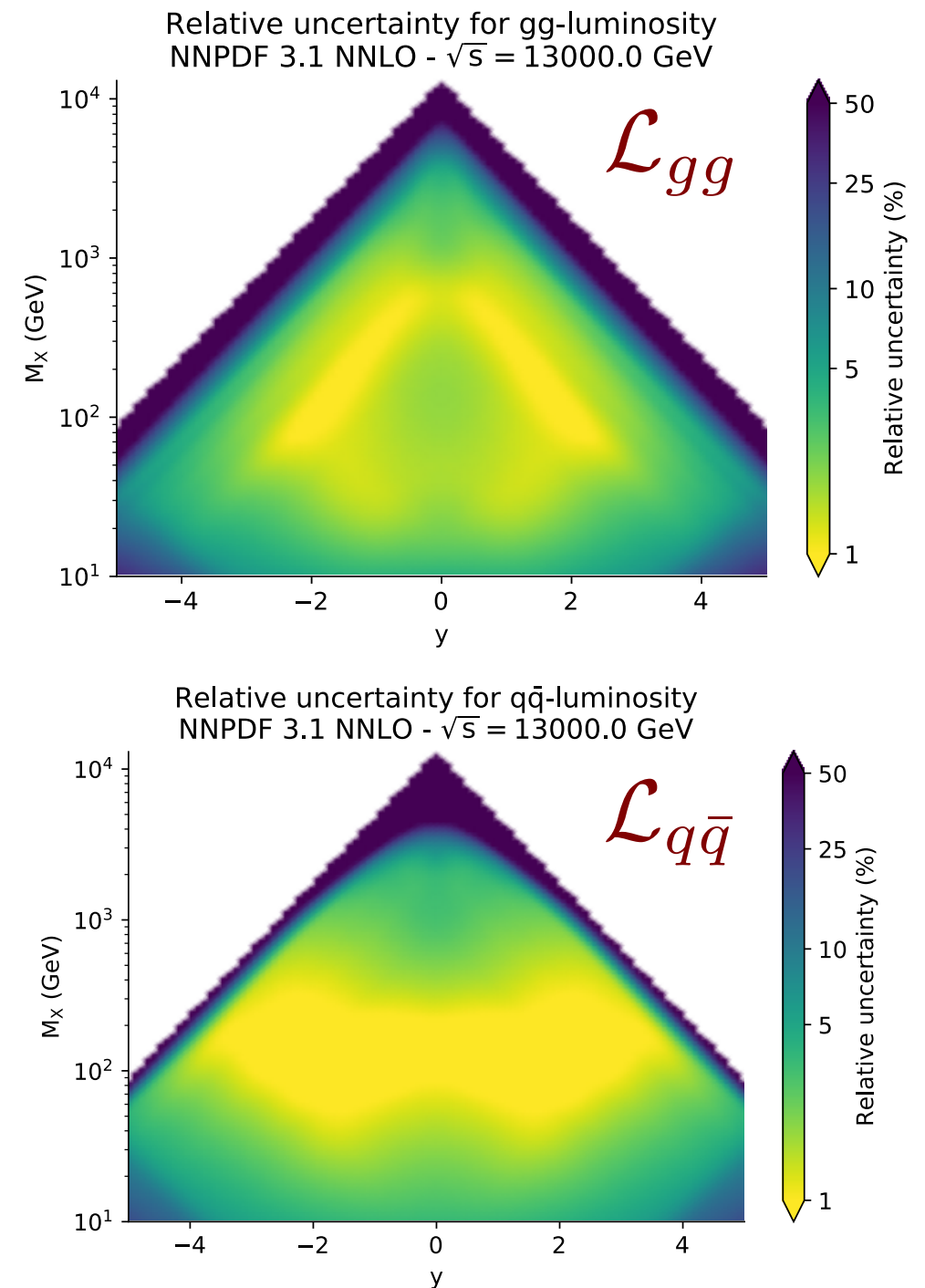
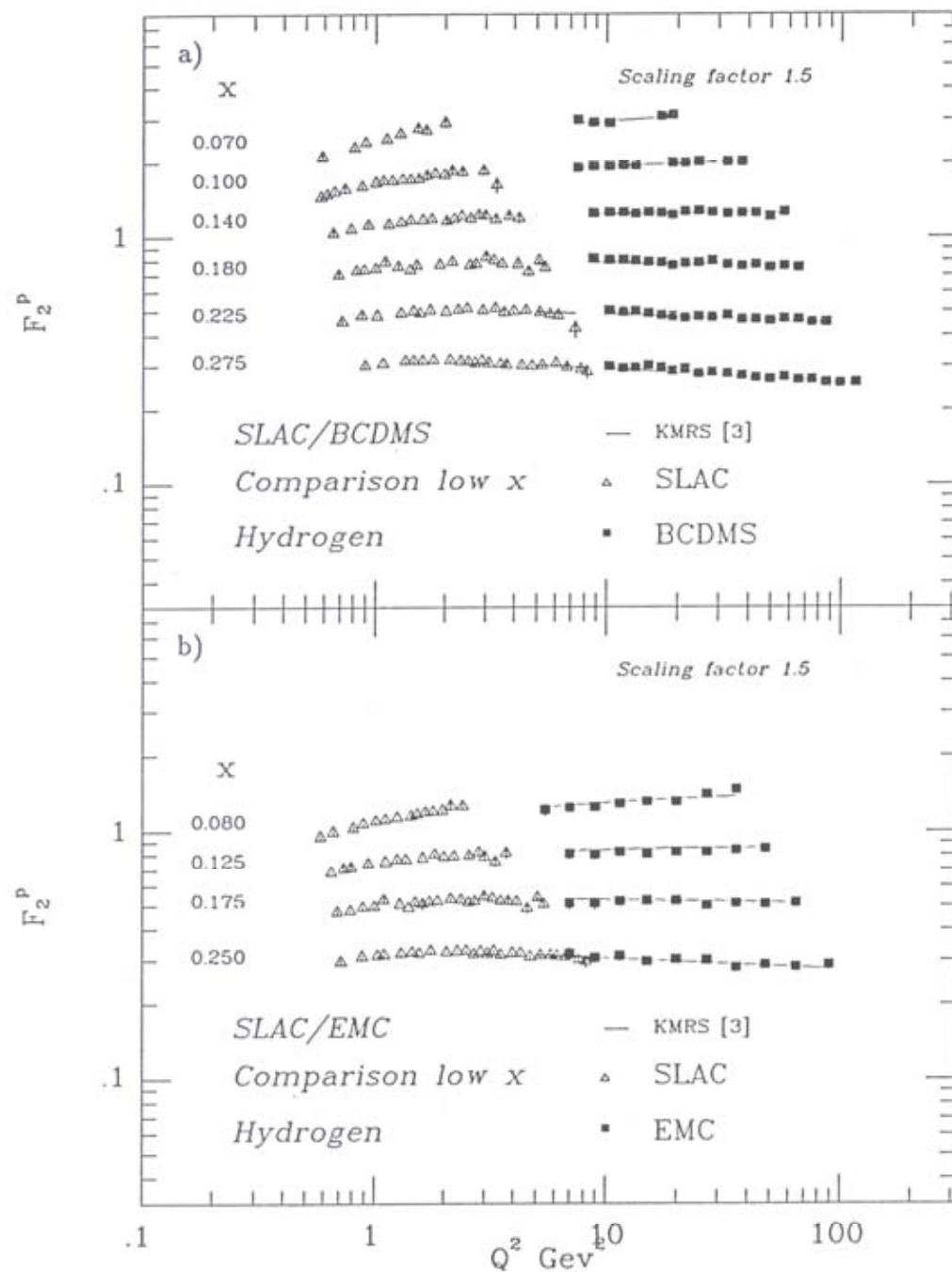


# DIS kinematics

$Q^2$



# PDFs: at the core of any hadron collider

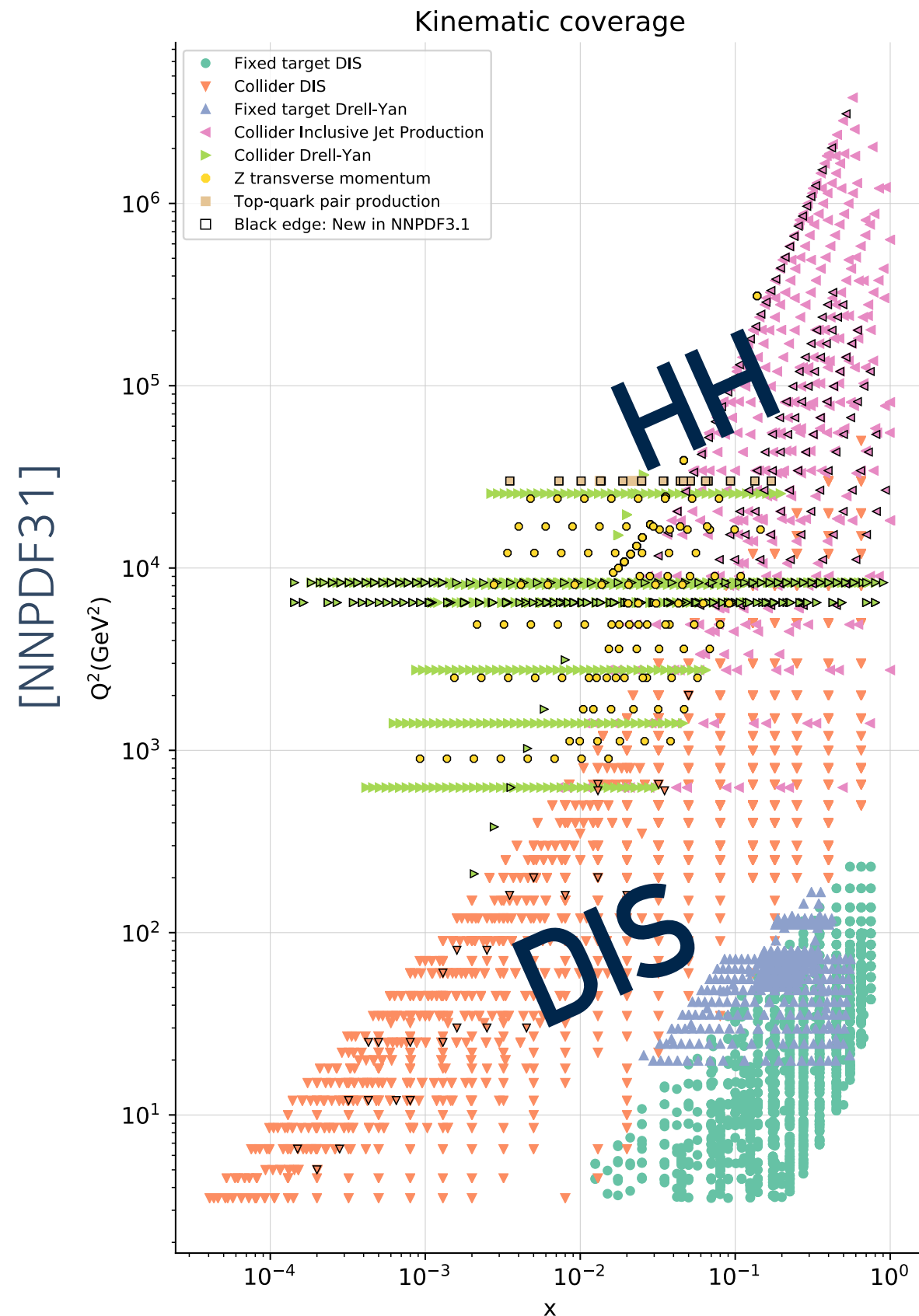


[NNPDF31]

From scaling violations to physics at the few percent



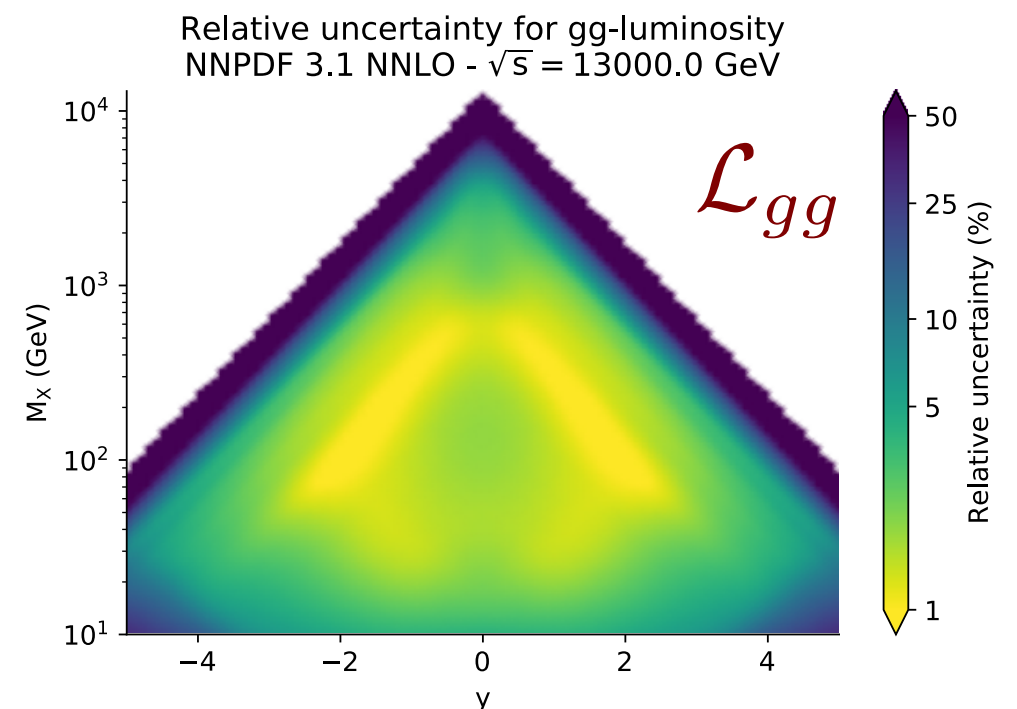
# PDFs: at the core of any hadron collider



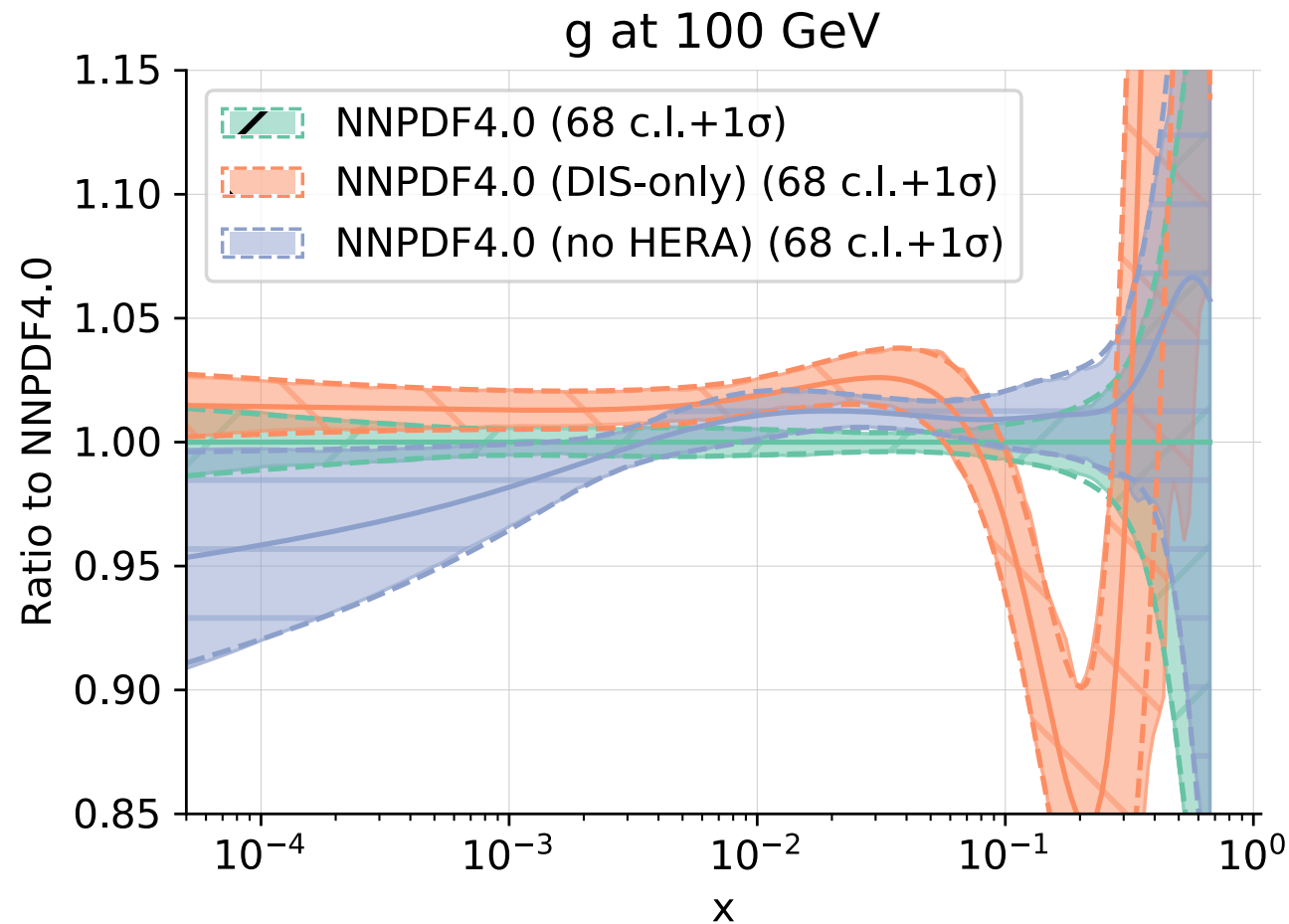
An incredible synergy between DIS and HH

QCD works over many order of magnitudes, in a very precise way.  
No obvious signs of breakdown

Combining DIS + HH: luminosities with few percent error possible in the bulk of the EW region



# PDFs: DIS vs hadron-hadron

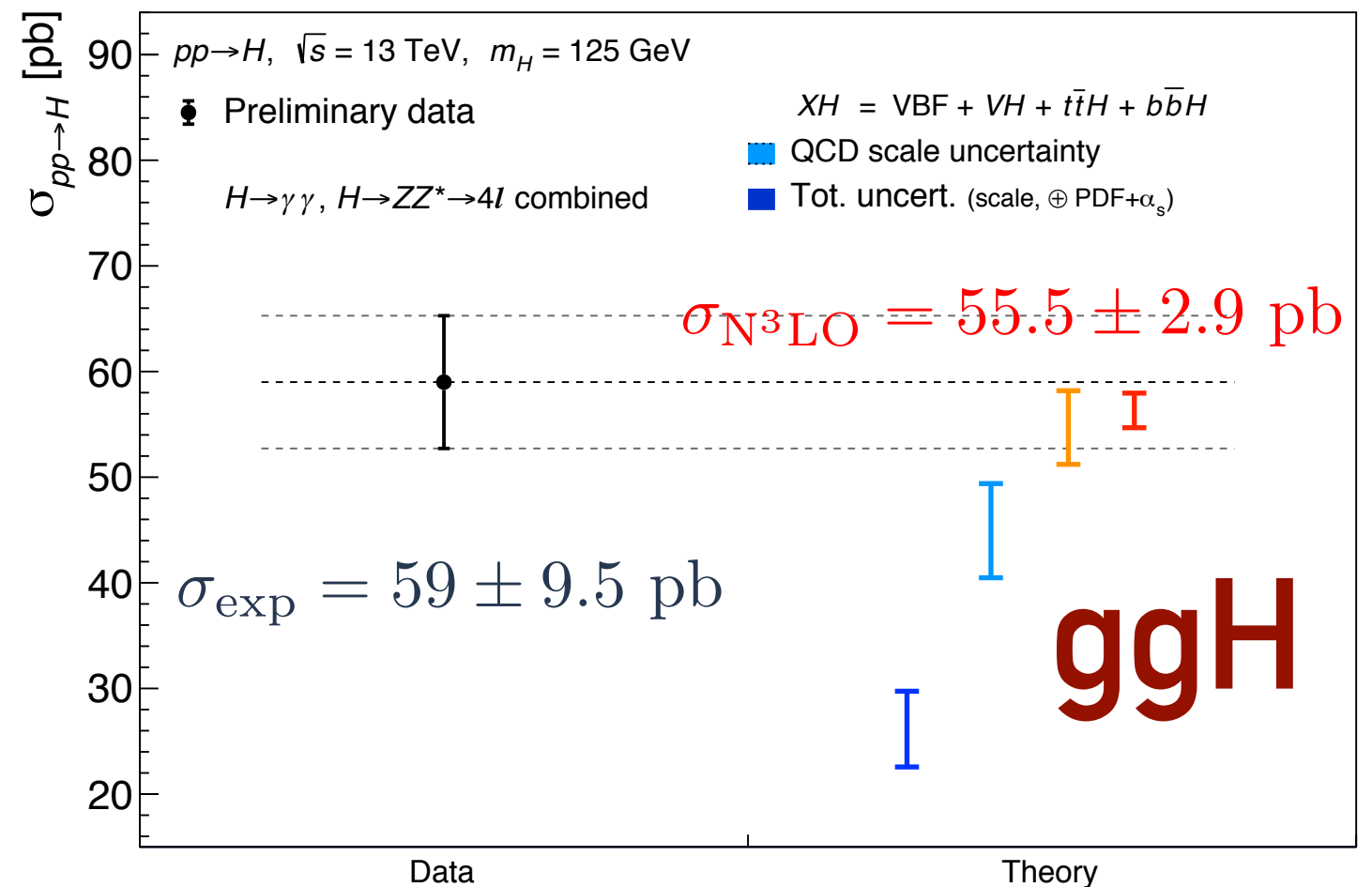
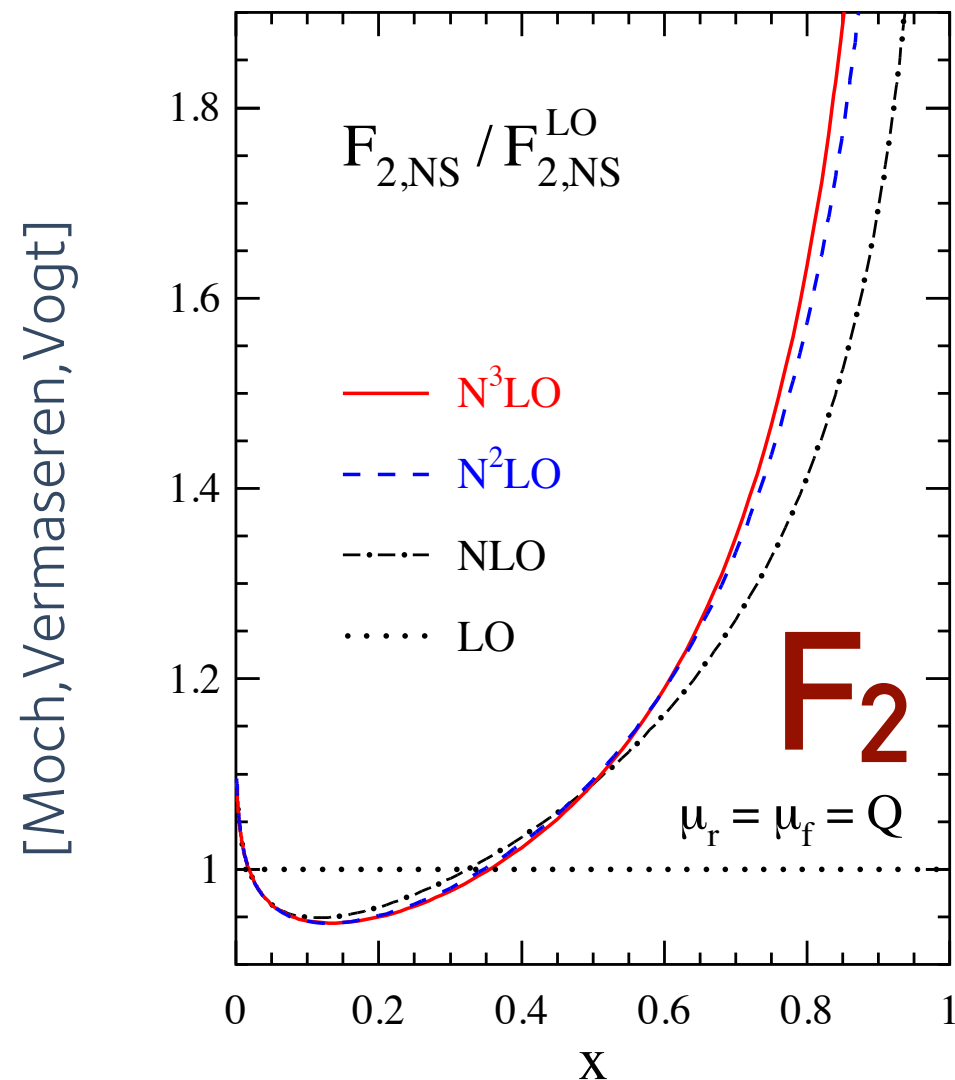


LHC bringing in more and more constraining power, but DIS here to stay

HERA legacy dataset:

- very robust, extremely well-understood dataset. Solid backbone
- LHC: often more complex observables/analysis, tensions (Z  $p_t$ , jets...)
- DIS: QCD theory under better control...

# The perturbative expansion in DIS and @LHC



[Anastasiou et al; Mistlberger]

- In general, perturbative expansion much better behaved in DIS
- ggH is an extreme case, but larger K-factors at the LHC [ $\rightarrow$  M. Bonvini's talk]
- LHC: more differential, complex observables, often quite delicate
- Understanding of source of large K-factors not yet fully-satisfactory



# The perturbative expansion in DIS and @LHC

## Consequences for PDFs

[MSHT2020]

Data set	Points	NLO $\chi^2/N_{pts}$	NNLO $\chi^2/N_{pts}$
DØ $W$ asymmetry	14	0.94 (2.53)	0.86 (14.7)
$\sigma_{t\bar{t}}$ [93]- [94]	17	1.34 (1.39)	0.85 (0.87)
LHCb 7+8 TeV $W + Z$ [95, 96]	67	1.71 (2.35)	1.48 (1.55)
LHCb 8 TeV $Z \rightarrow ee$ [97]	17	2.29 (2.89)	1.54 (1.78)
CMS 8 TeV $W$ [98]	22	1.05 (1.79)	0.58 (1.30)
CMS 7 TeV $W + c$ [99]	10	0.82 (0.85)	0.86 (0.84)
ATLAS 7 TeV jets $R = 0.6$ [18]	140	1.62 (1.59)	1.59 (1.68)
ATLAS 7 TeV $W + Z$ [20]	61	5.00 (7.62)	1.91 (5.58)
CMS 7 TeV jets $R = 0.7$ [100]	158	1.27 (1.32)	1.11 (1.17)
ATLAS 8 TeV $Z p_T$ [75]	104	2.26 (2.31)	1.81 (1.59)
CMS 8 TeV jets $R = 0.7$ [101]	174	1.64 (1.73)	1.50 (1.59)
ATLAS 8 TeV $t\bar{t} \rightarrow l + j$ sd [102]	25	1.56 (1.50)	1.02 (1.15)
ATLAS 8 TeV $t\bar{t} \rightarrow l^+ l^-$ sd [103]	5	0.94 (0.82)	0.68 (1.11)
ATLAS 8 TeV high-mass DY [73]s	48	1.79 (1.99)	1.18 (1.26)
ATLAS 8 TeV $W^+ W^- + \text{jets}$ [104]	30	1.13 (1.13)	0.60 (0.57)
CMS 8 TeV $(d\sigma_{t\bar{t}}/dp_{T,t} dy_t)/\sigma_{t\bar{t}}$ [105]	15	2.19 (2.20)	1.50 (1.48)
ATLAS 8 TeV $W^+ W^-$ [106]	22	3.85 (13.9)	2.61 (5.25)
CMS 2.76 TeV jets [107]	81	1.53 (1.59)	1.27 (1.39)
CMS 8 TeV $\sigma_{t\bar{t}}/dy_t$ [108]	9	1.43 (1.02)	1.47 (2.14)
ATLAS 8 TeV double differential $Z$ [74]	59	2.67 (3.26)	1.45 (5.16)
Total, LHC data in MSHT20	1328	1.79 (2.18)	1.33 (1.77)
Total, non-LHC data in MSHT20	3035	1.13 (1.18)	1.10 (1.18)
Total, all data	4363	1.33 (1.48)	1.17 (1.36)

... but more in general, QCD “cleaner” in DIS

# Example of subtleties: CMS jets and NNLO

[Chen, Gehrmann, Glover, Huss, Mo (2022)]

- CMS 8 TeV dijet data, differential in  $p_{t,\text{avg}}$ ,  $y^* = |\Delta y|/2$  and  $y_b = |y_1 + y_2|/2$
- Strongest constraining power among jets, but strong pull for gluon at  $x \sim 0.3$
- Tension with legacy DIS/DY  $\rightarrow$  discarded

- NNPDF4.0: single-differential CMS 8TeV. Underlying TH: best prediction available at the time of fitting  $\rightarrow$  NNLOQCD+NP, only leading-colour contributions

$$\delta\sigma_{\text{NNLO}} = A N_c^2 + B n_f N_c + C n_f^2 + \cancel{D N_c^0} + \cancel{E \frac{n_f}{N_c}} + \cancel{\frac{G}{N_c^2}}$$

- Recently: full-colour calculations available [Czakon, van Hameren, Mitov, Poncelet (2019); Chen, Gehrmann, Glover, Huss, Mo (2022)]

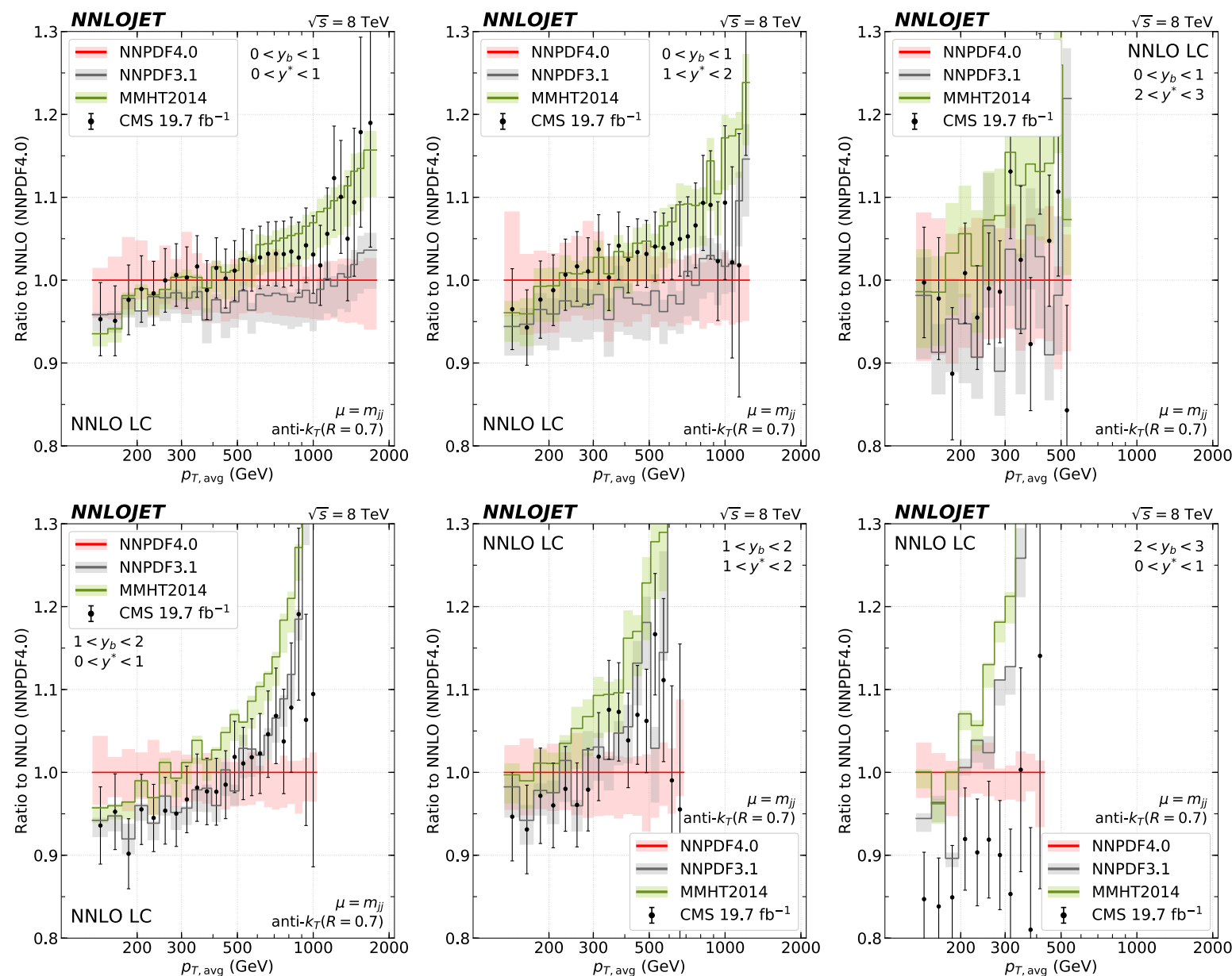
[ $\rightarrow$  see talk by J. Mo]

# Example of subtleties: CMS jets and NNLO

- Full-colour analysis

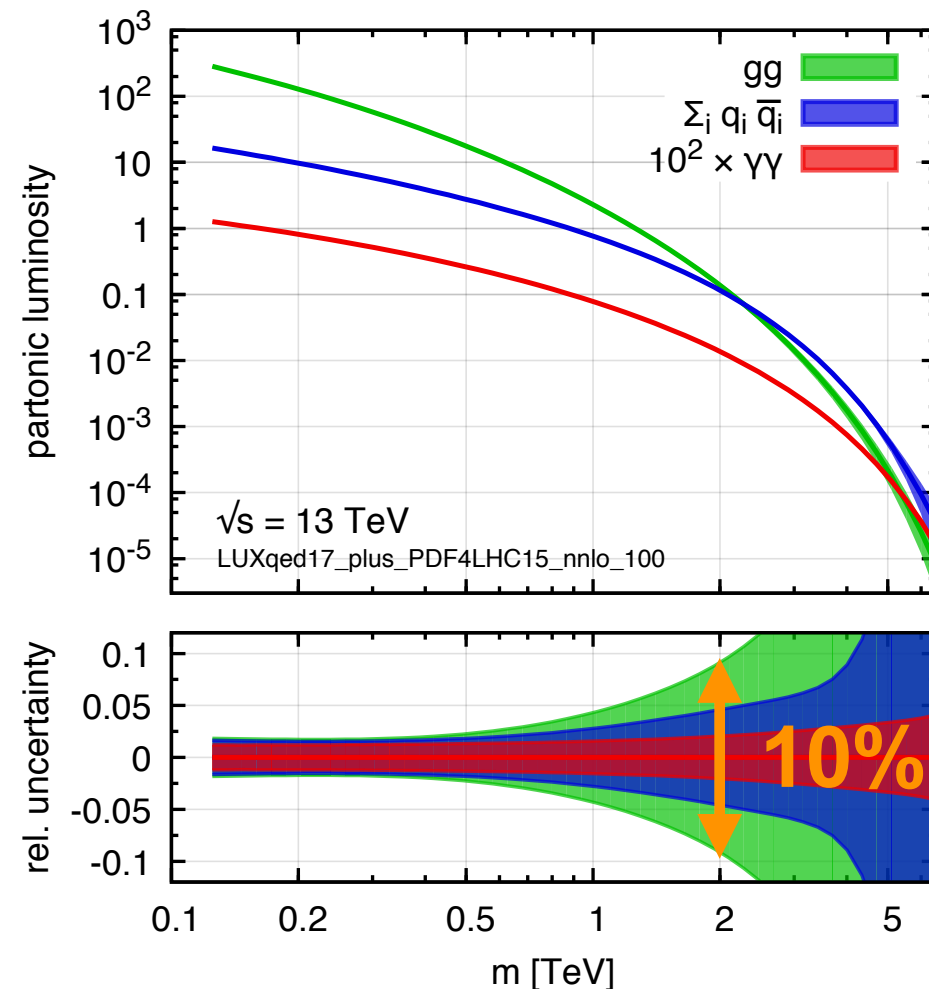
$$\delta\sigma_{\text{NNLO}} = A N_c^2 + B n_f N_c + C n_f^2 + D N_c^0 + E \frac{n_f}{N_c} + \frac{G}{N_c^2}$$

- Sets without CMS8 jet data seem to fit better
- Jury still out, but this example shows that the LHC can be tricky...
- General comment: robust TH uncertainty in the PDFs most welcome [→ talks by Z. Kassabov, J. McGowan, M. Bonvini]

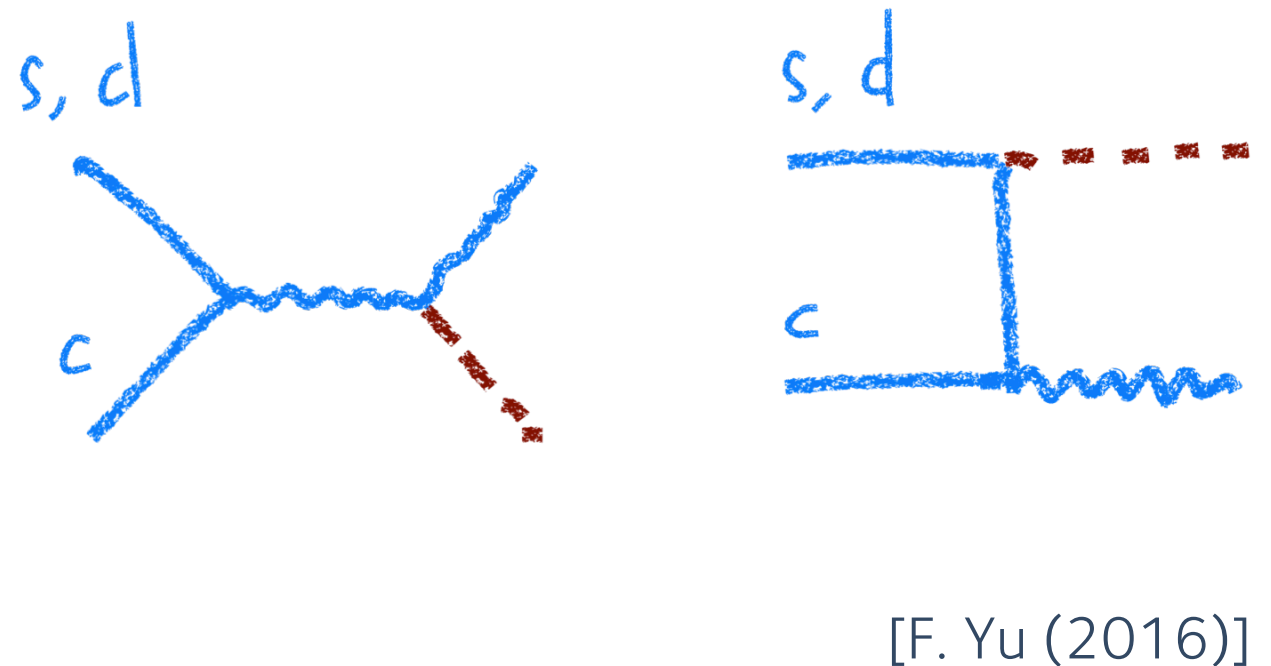


# PDFs: important information still missing

High-mass searches require  
large- $x$  PDFs



Interesting ideas for constraining  
2<sup>nd</sup> generation Yukawa require  
good  $s$ ,  $c$  and  $\bar{d}/d$  control



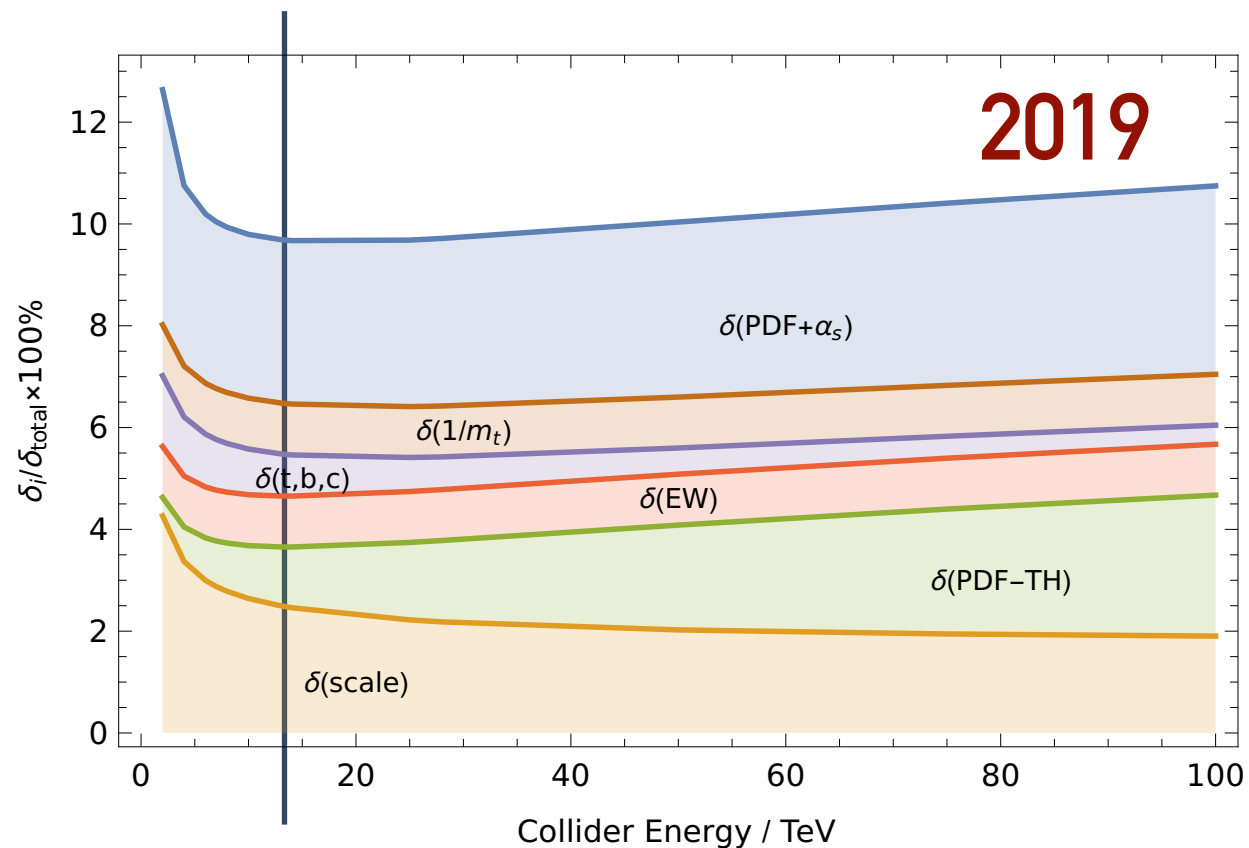
UHE neutrinos, prompt  $\nu$   
flux  $\rightarrow$  small- $x$ , charm

Any progress in these  
directions welcome

# PDFs: also a theory problem...

N<sup>3</sup>LO PDFs not available → order mismatch

## ggH theory error budget

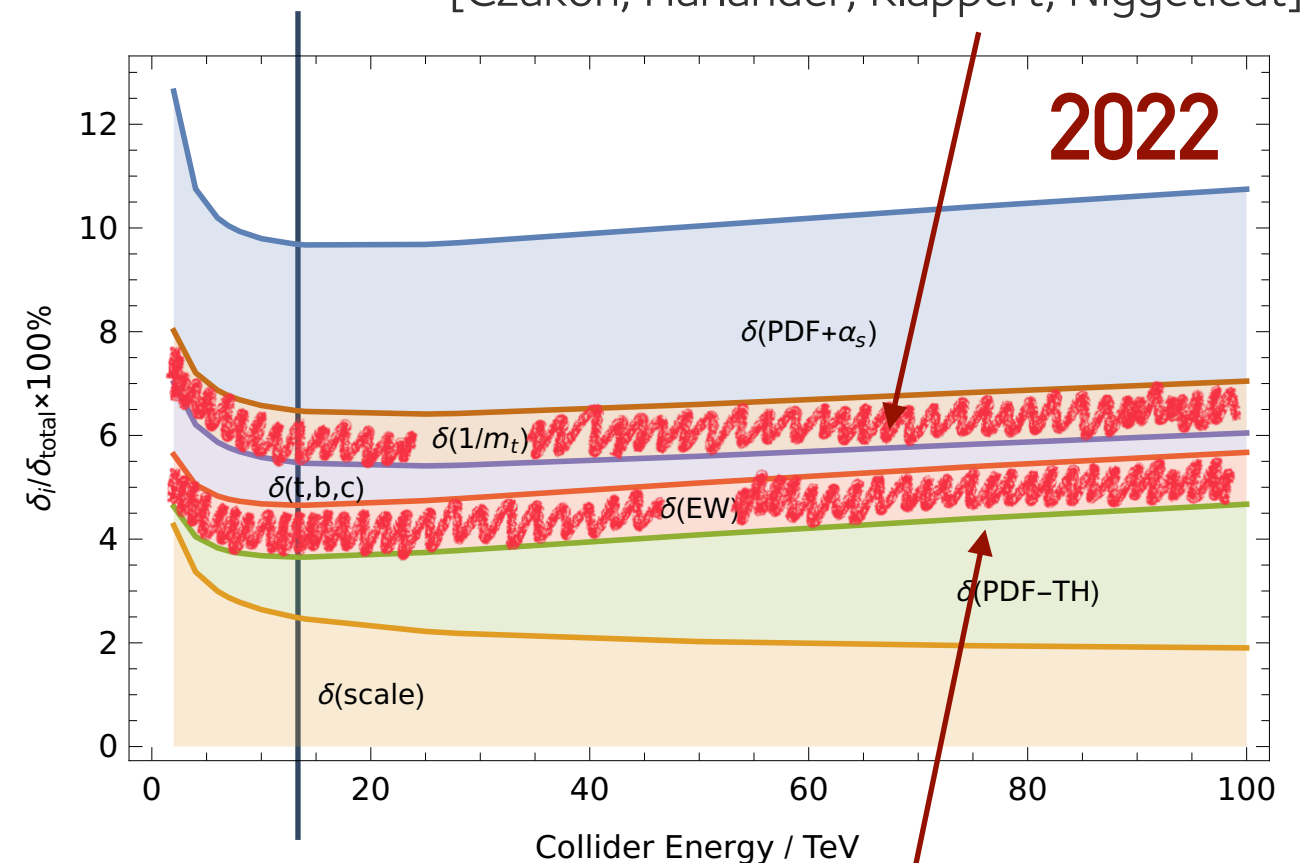
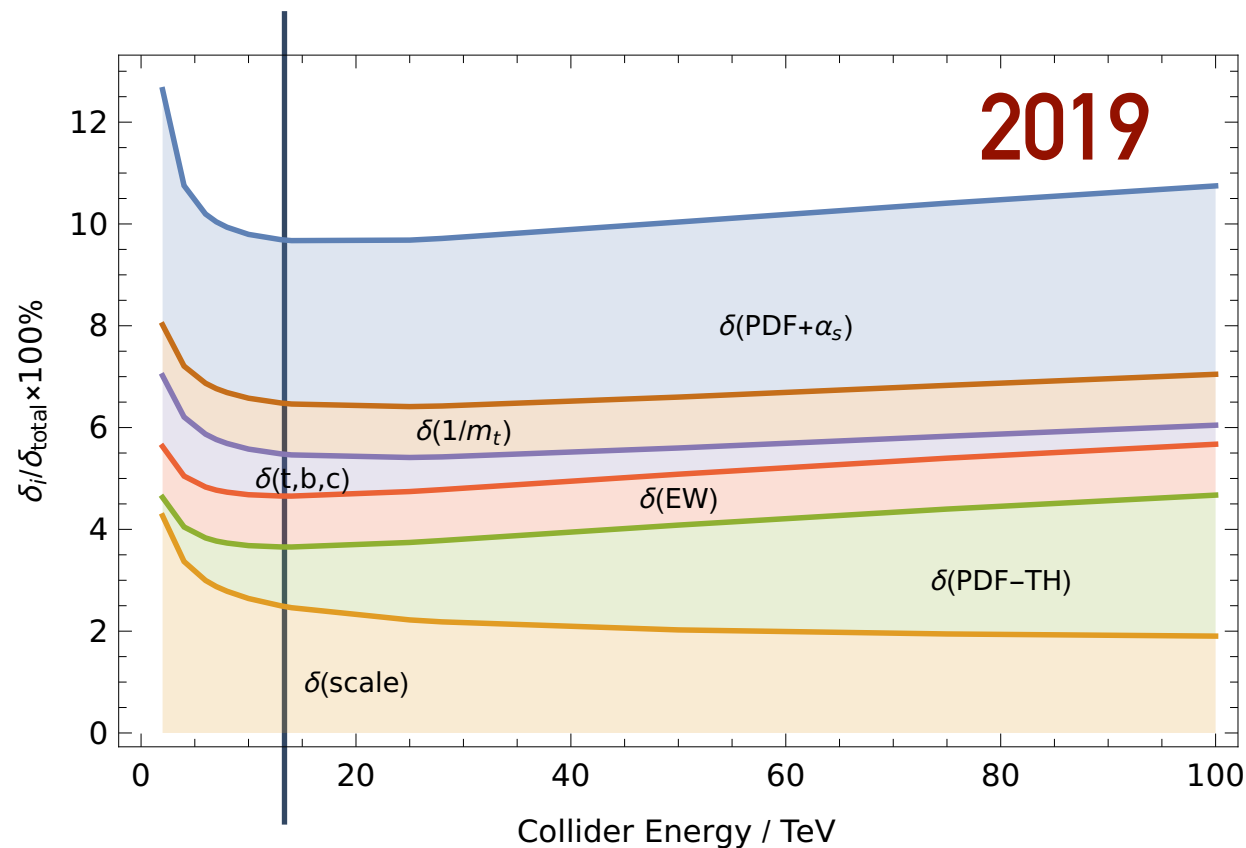


# PDFs: also a theory problem...

N<sup>3</sup>LO PDFs not available → order mismatch

## ggH theory error budget

[Czakon, Harlander, Klappert, Niggetiedt]



[Becchetti, Bonciani, del Duca, Hirschi, Moriello, Schweitzer; Bonetti, Panzer, Smirnov, Tancredi, Melnikov]

Missing N<sup>3</sup>LO PDFs, as well as  $\alpha_s$ +PDFs uncertainty: significant

[Recent progress towards N<sup>3</sup>LO → talks by J. McGowan, K. Schönwald]

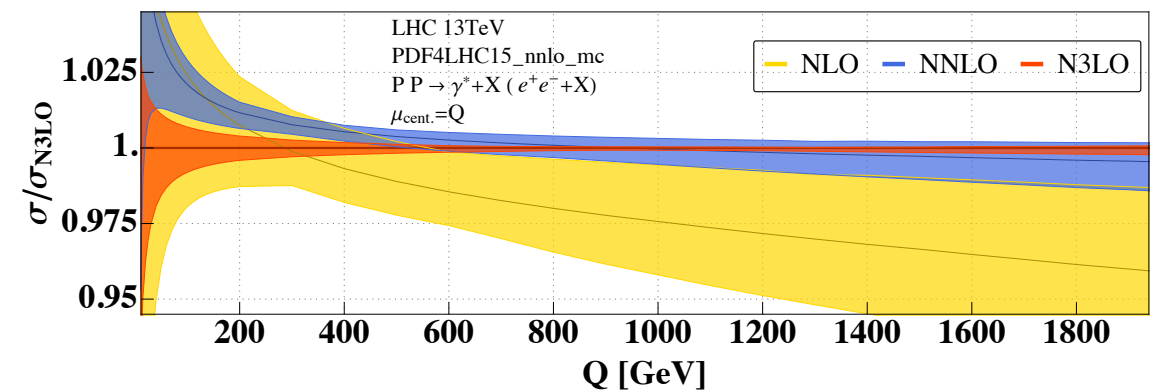
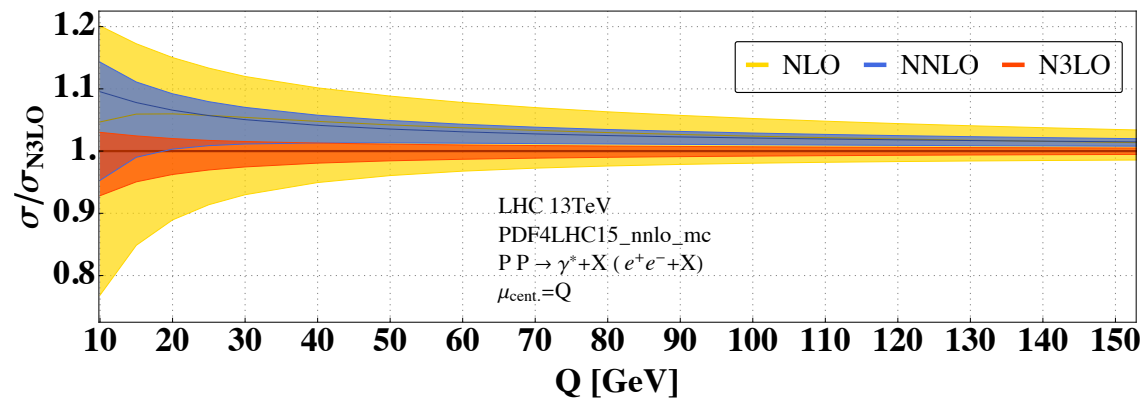


# Inclusive Drell-Yan at N<sup>3</sup>LO

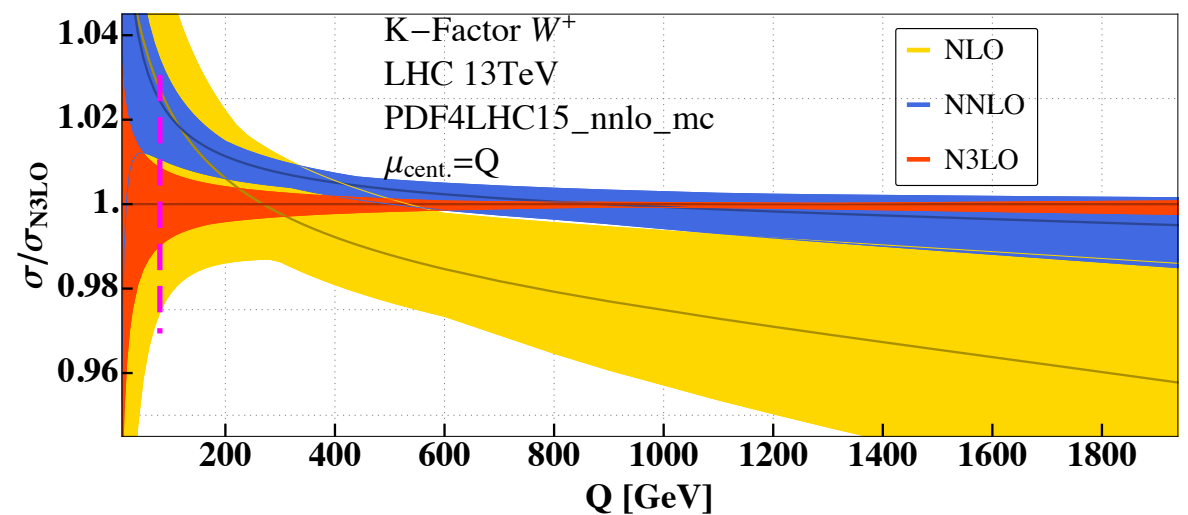
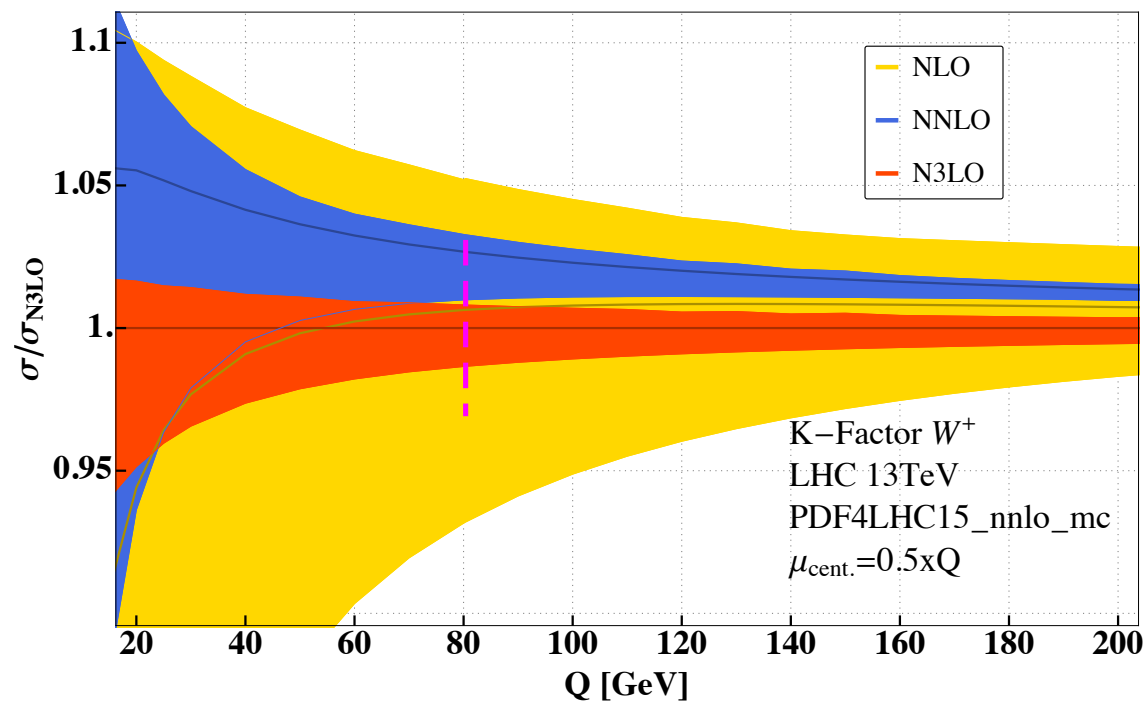
In the EW region  $Q \sim 100$  GeV:  $\sim 2-3\%$  N<sup>3</sup>LO vs per-mill NNLO

[Duhr, Dulat, Mistlberger (2020-21)]

$Y^*$



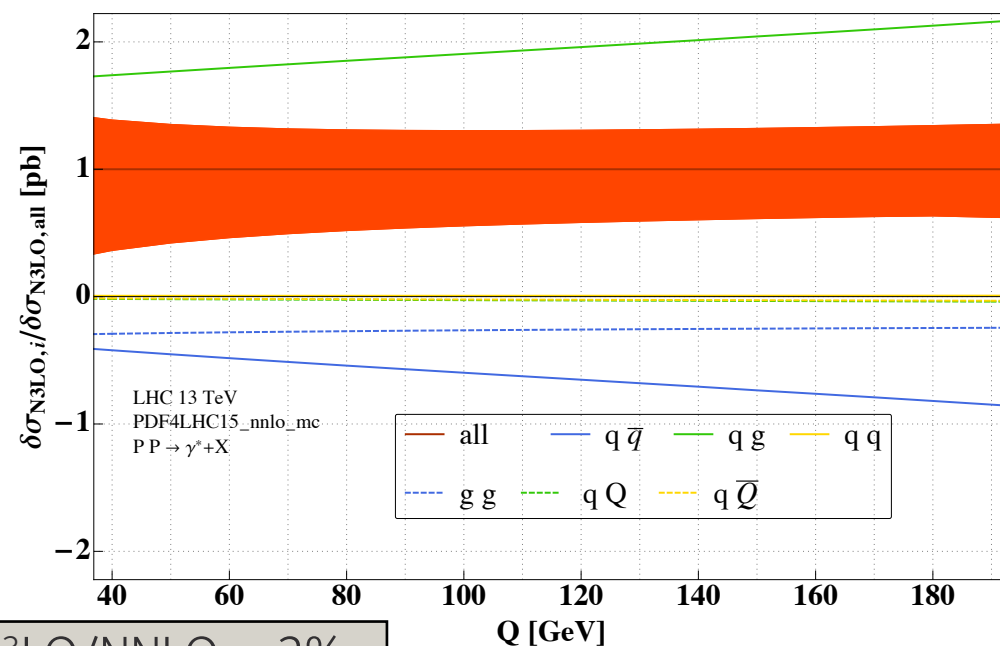
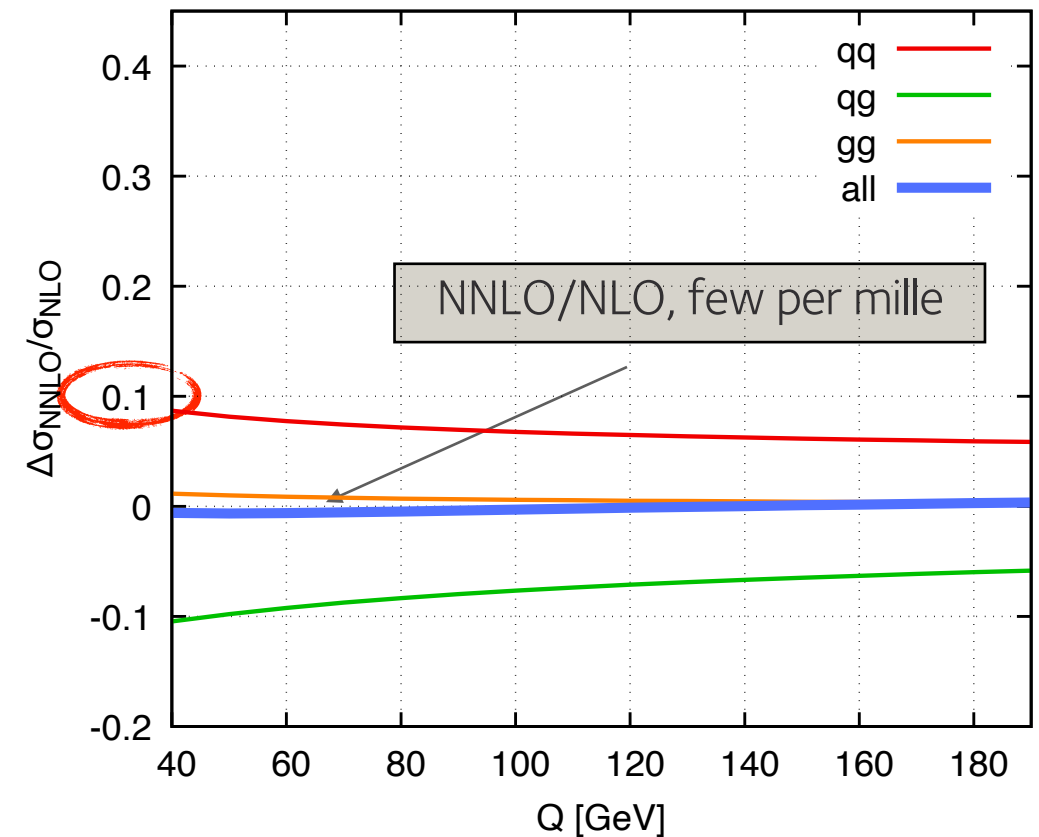
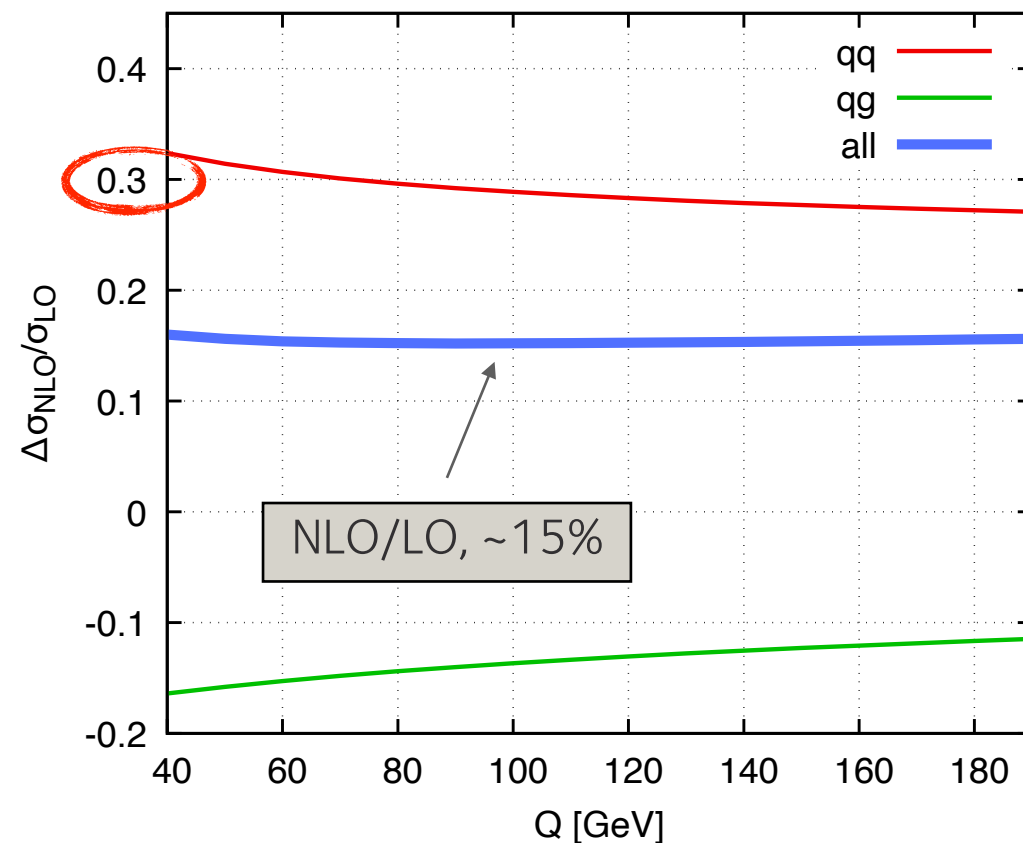
$W^+$



Band only overlap at large  $Q^2 \rightarrow$  trouble in the high-precision region?

# Neutral-current DY: flavour decomposition

Per-mille NNLO: unnaturally small. Very large cancellations



- Individual channels ( $\mu=Q$ ) much larger than final result, delicate cancellation pattern
- Individual channels: perturbative convergence
- N<sup>3</sup>LO “natural”, tiny PDFs changes can significantly affect this picture

# N<sup>3</sup>LO PDFs issues: evolution

N<sup>3</sup>LO: evolution and the problems of small-x

NNLO: an issue at low-mass, not quite so at the EW scale. N<sup>3</sup>LO?

$$\chi_0(M) = \frac{C_A}{\pi} [2\psi(1) - \psi(M) - \psi(1 - M)] \rightarrow$$

$$\gamma_{LL}(N) = \frac{\bar{\alpha}_s}{N} + 0 \cdot \alpha_s^2 + 0 \cdot \alpha_s^3 + 2\zeta_3 \frac{\bar{\alpha}_s^4}{N^4}, \quad \bar{\alpha}_s = \alpha_s C_A / \pi$$

Spurious leading pole in 0, starting at N<sup>3</sup>LO (vs pole at N~0.3).

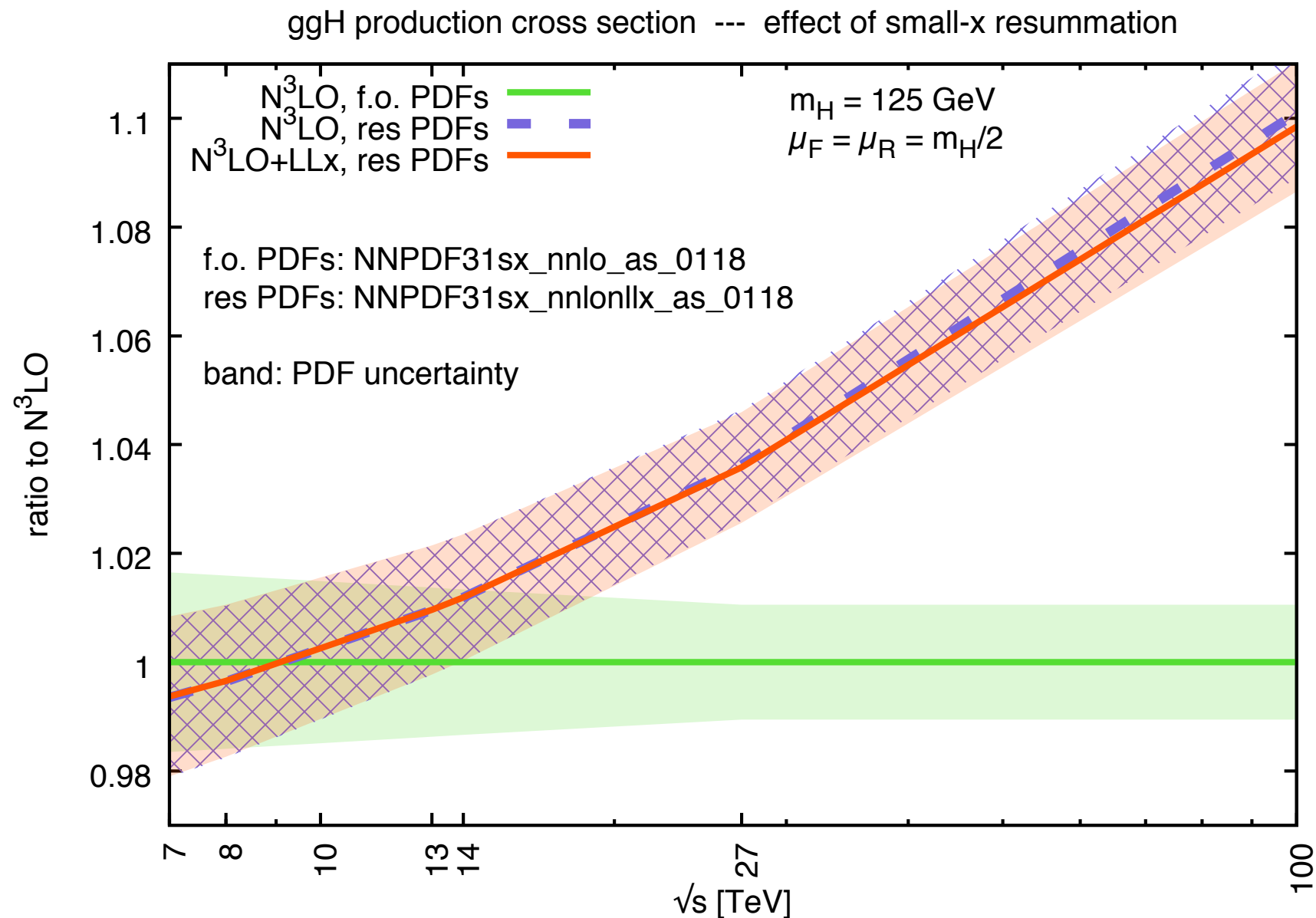
Is this an issue for precision physics (at the EW scale and beyond)?

- How dangerous is the spurious N<sup>3</sup>LO growth?
- Are subleading terms under control?
- To which extent DGLAP evolution washes out small-x effects?
- Control-sample with effectively no evolution (i.e. DIS vs LHC-only fits)?

[Resummed evolution → talk by A. Stasto]

# Small-x physics and high-energy colliders

Proper understanding of small-x crucial for precision  
EW physics at future hadron colliders



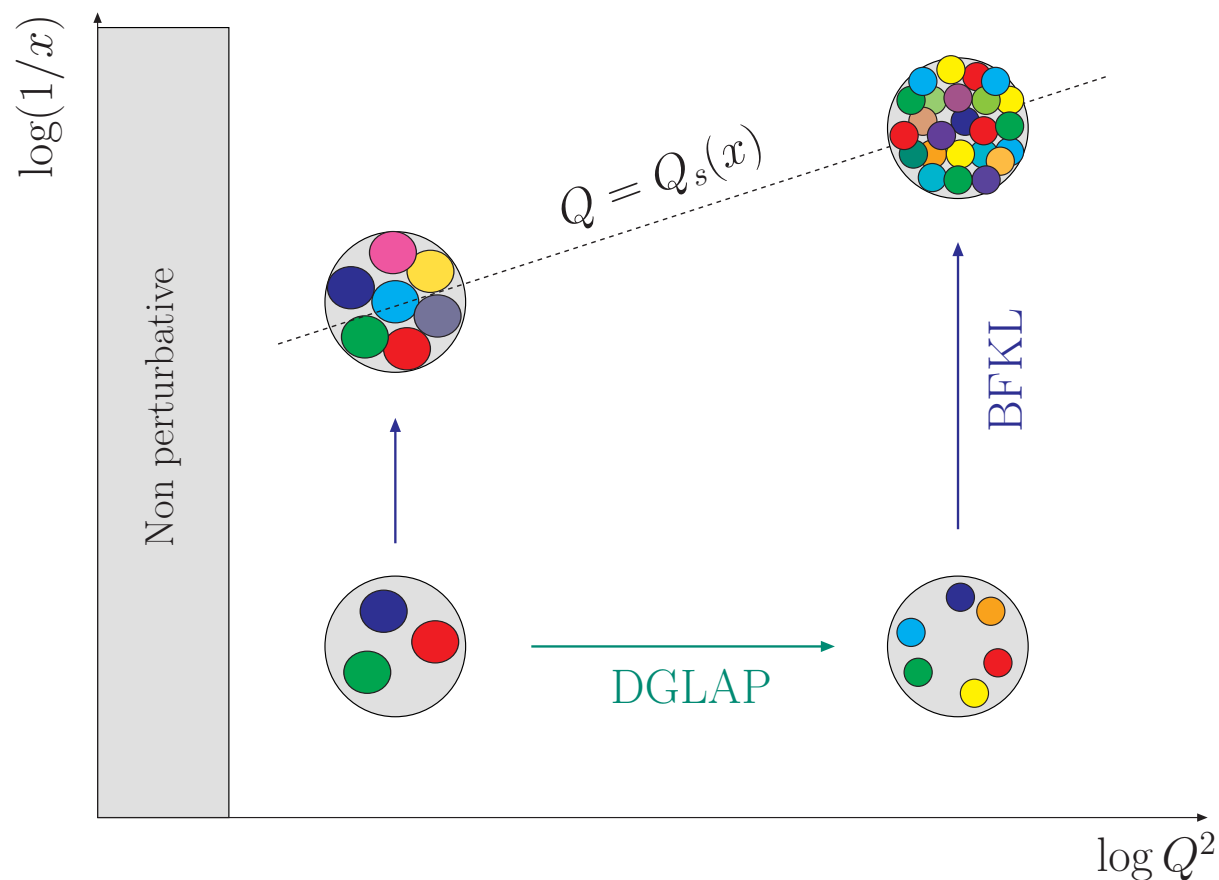
What is the impact of  
sub-leading terms?  
How robust is this  
picture?

[Bonvini, Marzani (2018)]

# Small-x physics: beyond standard evolution

Small-x physics extremely interesting in its own merit.

QCD in a new regime



- A lot of recent progress towards making predictions more precise and accurate → see B. Xiao's talk
- Effects larger in pA,  $A^{1/3}$  enhancement of the saturation scale
- Also can be studied from diffraction, in a relative clean fashion [see E. Iancu's talk]

Can we study the onset of saturation and its connection to (resummed) DGLAP with as little modelling as possible, in a clean (=protons, perturbative) setting?

# Beyond PDFs: TMDs

The screenshot shows the website for DIS2022: XXIX International Workshop on Deep-Inelastic Scattering and Related Subjects. The header is blue with white text. Below the header, the dates '2-6 May 2022' and 'Europe/Madrid timezone' are displayed. A left sidebar contains navigation links: Overview, Scientific Programme, Call for Abstracts, Timetable, Contribution List, and Registration. The main content area has a 'Search' section with a search bar containing 'TMD'. Below the search bar, there are two tabs: 'Contributions (33)' which is selected and highlighted in red, and 'Materials (6)'. At the bottom right of the main content area, there is a 'Sort by: Most relevant' dropdown menu.

A lot of progress... In a nutshell

- better determinations
- better theoretical understanding (from phenomenological models to first principles)

Understanding the intrinsic transverse momentum of partons plays an important role for highest-precision LHC studies...



# Beyond PDFs: TMDs and the W mass

Legacy LHC measurement: W mass.

- Best handle at the LHC: W transverse momentum distribution
- Require (sub) per-mill control over  $p_t$  spectra  $\rightarrow$  impossible theoretically
- Idea: calibrate Z using data, only **need to control differences between Z and W**  $\rightarrow$  PDFs, EW
- Few per-mill distortion of spectra  $\leftrightarrow$  O(10 MeV) shift in  $m_W$
- Right now:  $\Delta m_{W,ATLAS} = \sim 19$  MeV [CDF:  $\sim 10$  MeV, EW precision:  $\sim 8$  MeV]

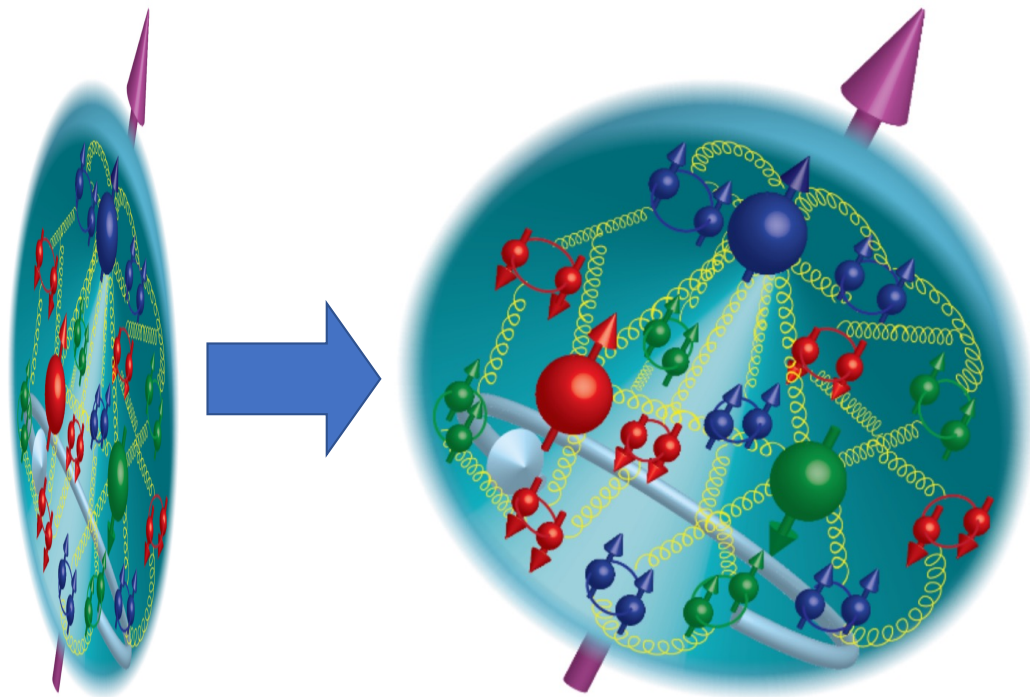
Good control of flavour-dependence of intrinsic  $k_t$  crucial  $\rightarrow$  TMD

	$\Delta M_{W^+}$			$\Delta M_{W^-}$		
Set	$m_T$	$p_{T\ell}$	$p_{T\nu}$	$m_T$	$p_{T\ell}$	$p_{T\nu}$
1	0	-1	-2	-2	3	-3
2	0	-6	0	-2	0	-5
3	-1	9	0	-2	4	-10
4	0	0	-2	-2	-4	-10
5	0	4	1	-1	-3	-6
6	1	0	2	-1	4	-4
7	2	-1	2	-1	0	-8
8	0	2	8	1	7	8
9	0	4	-3	-1	0	7

- Shifts uncomfortably large...
- Better control would be very welcome
- ... especially after the CDF new measurement

# Towards a 3D image of the proton

[graphics by O. Hen]

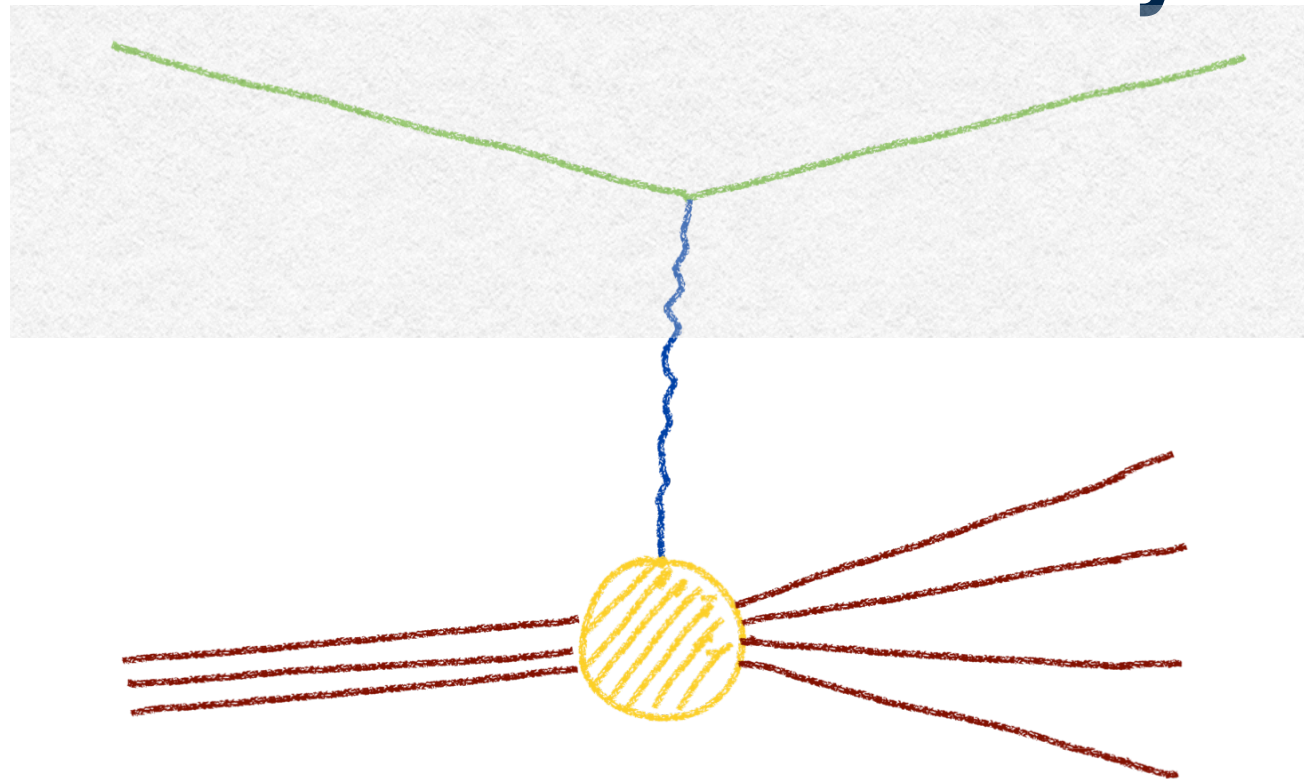


Eventually, we want to map the full 3D structure of the proton → Wigner's functions

Interesting in its own merit, but in the long run may be important for general studies at hadron colliders, beyond QCD

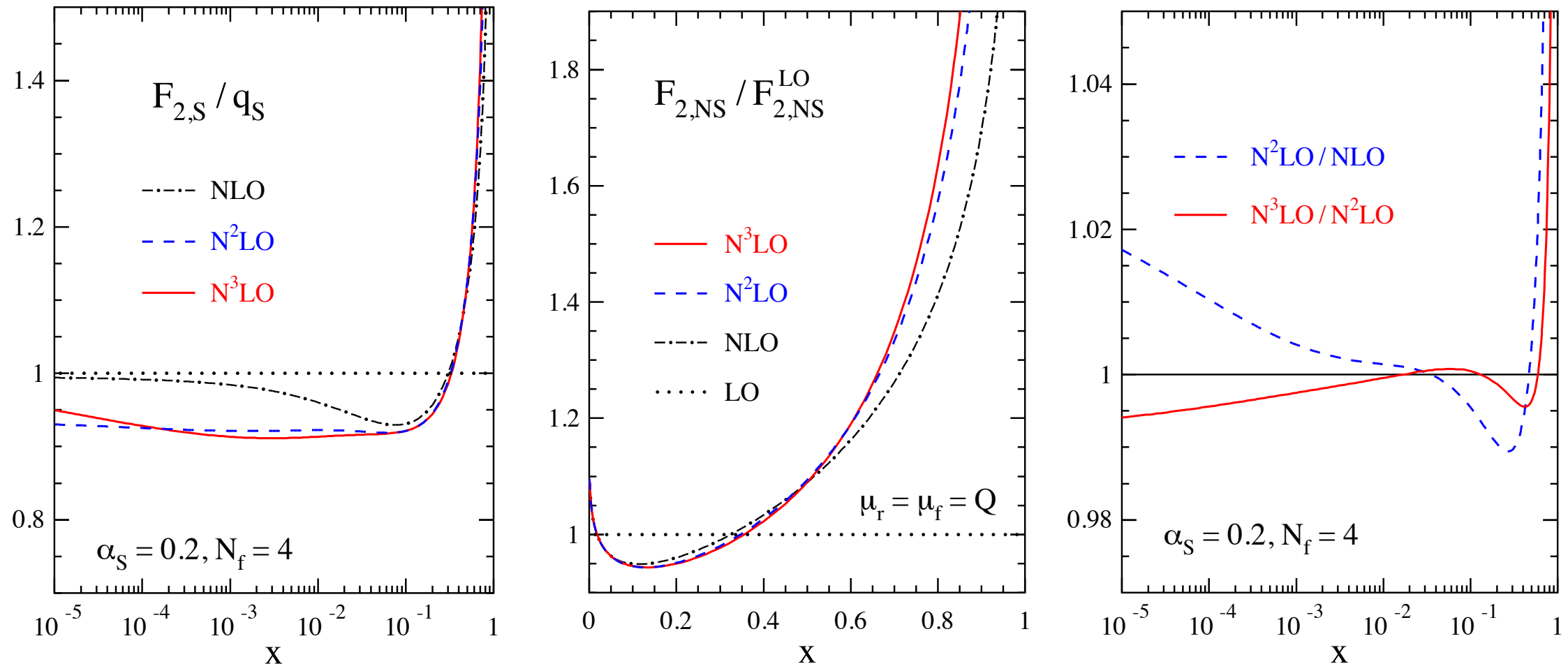
- PS, bread and butter of colliders, are getting better and better = under quantifiable theoretical control [→ see M. Dasgupta's talk]
- Non-perturbative bit still from phenomenological models. Ideally, rely less and less on models, and more and more on data
- Example: MPI. VBF Higgs: +5% at low  $p_t$  [NNLO QCD: 4–7%]
- Still very far from tomography-informed MPI, but a lot of progress on tomography expected from the EIC...

# DIS and HEP theory



- The simplest, yet non-trivial example of hadron collider
- Many techniques developed for DIS then successfully applied to the LHC
- Crucial results in pQCD [QCD evolution...]
- Tools [nested sums, iterated integrals...] widely used for state-of-the-art calculations
- Clean settings for NP studies, solid grounds in QFT (this is less the case for hadron-hadron colliders...)

# DIS: the first N<sup>3</sup>LO inclusive calculation...

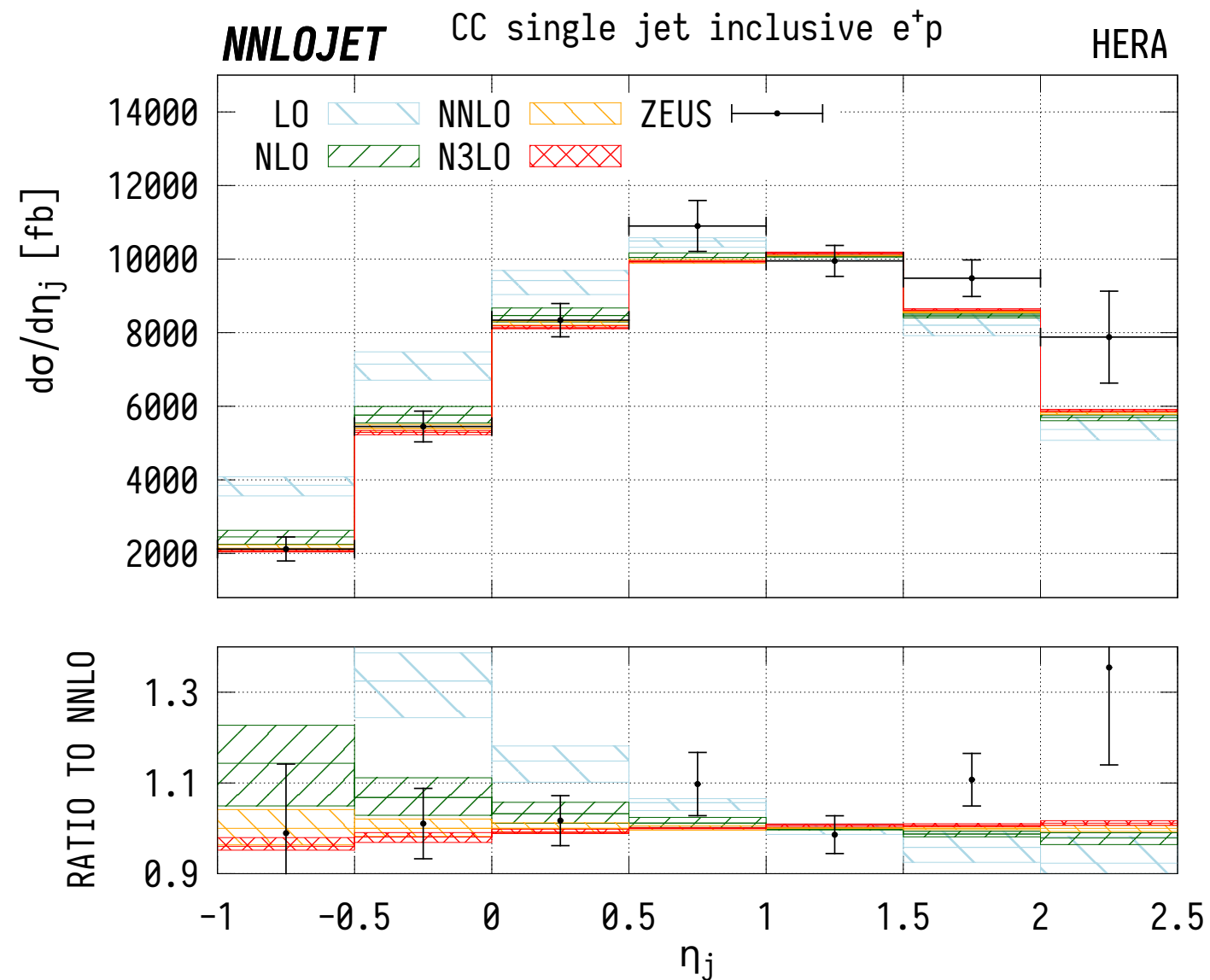


[Moch,Vermaseren,Vogt (2005)]

- Good perturbative convergence (away from small- $x$ )
- Naive  $\alpha_s$  power counting works well
- Crucial for high-precision fits

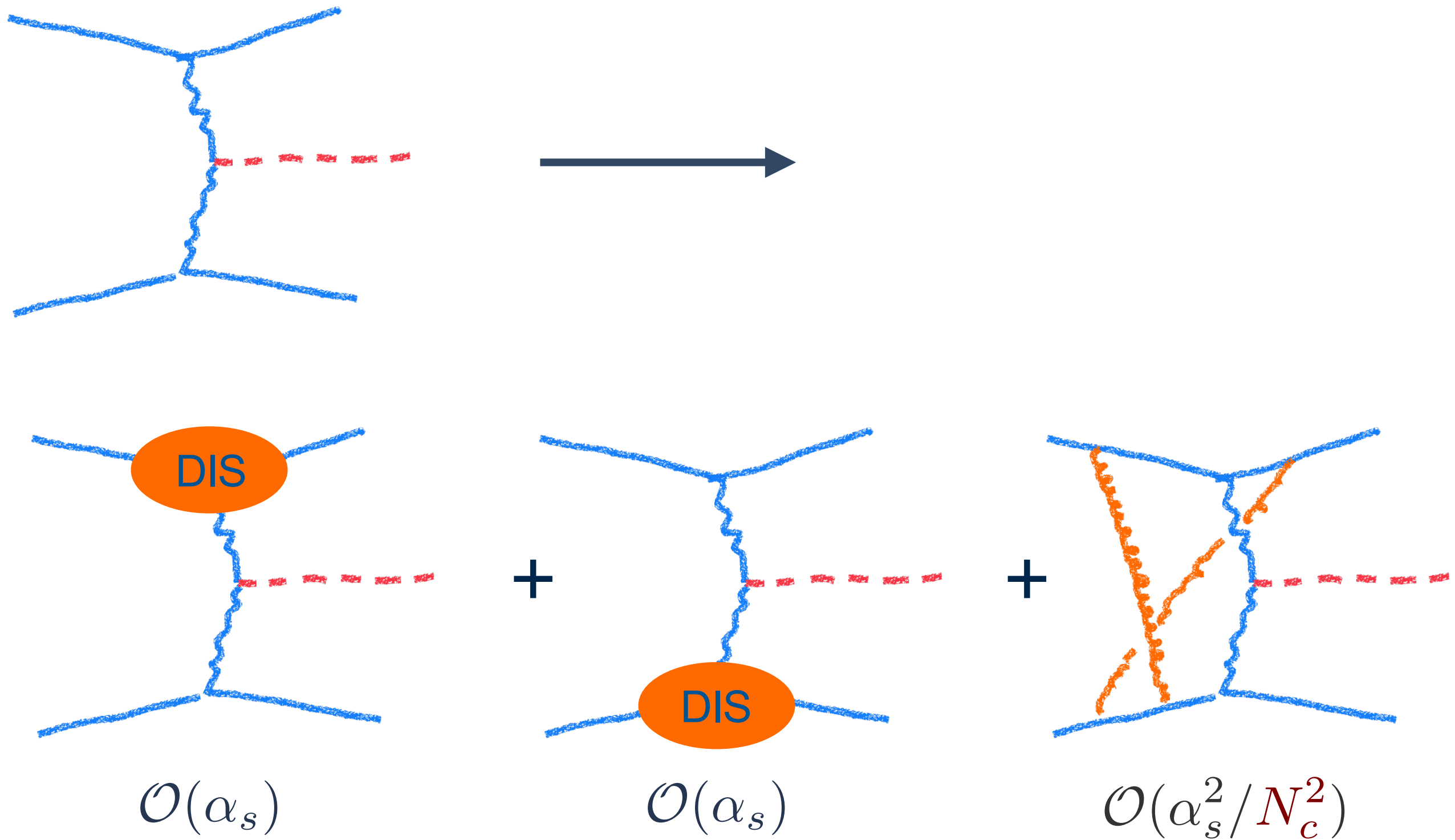
# DIS: ... and the first fully-exclusive one

[Gehrmann, Huss, Niehues,  
Vogt, Walker (2018)]



- Also in this case good convergence
- Testing grounds for similar calculations at hadron colliders

# DIS in disguise: VBF@LHC

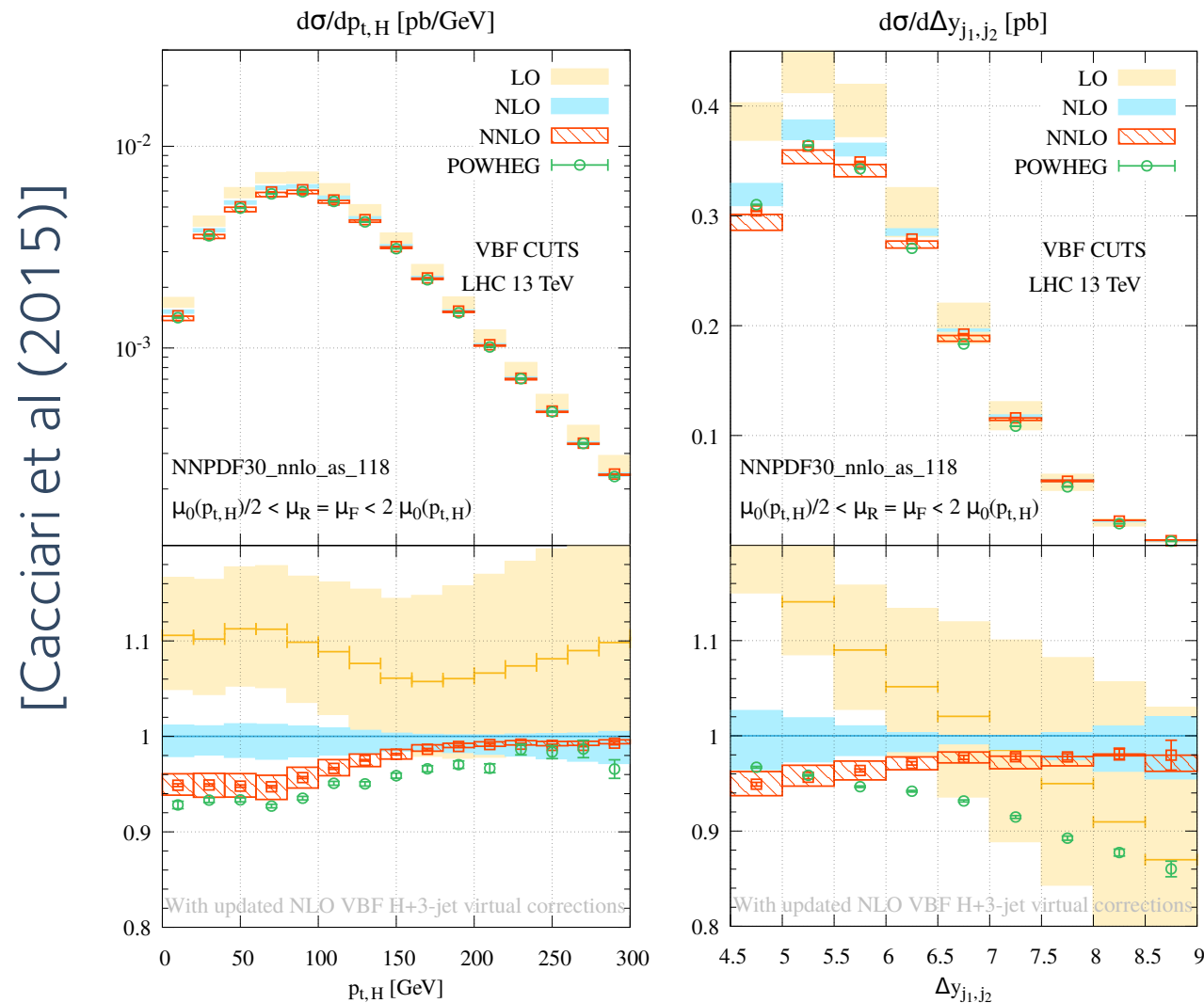


- Double-DIS approximation very good

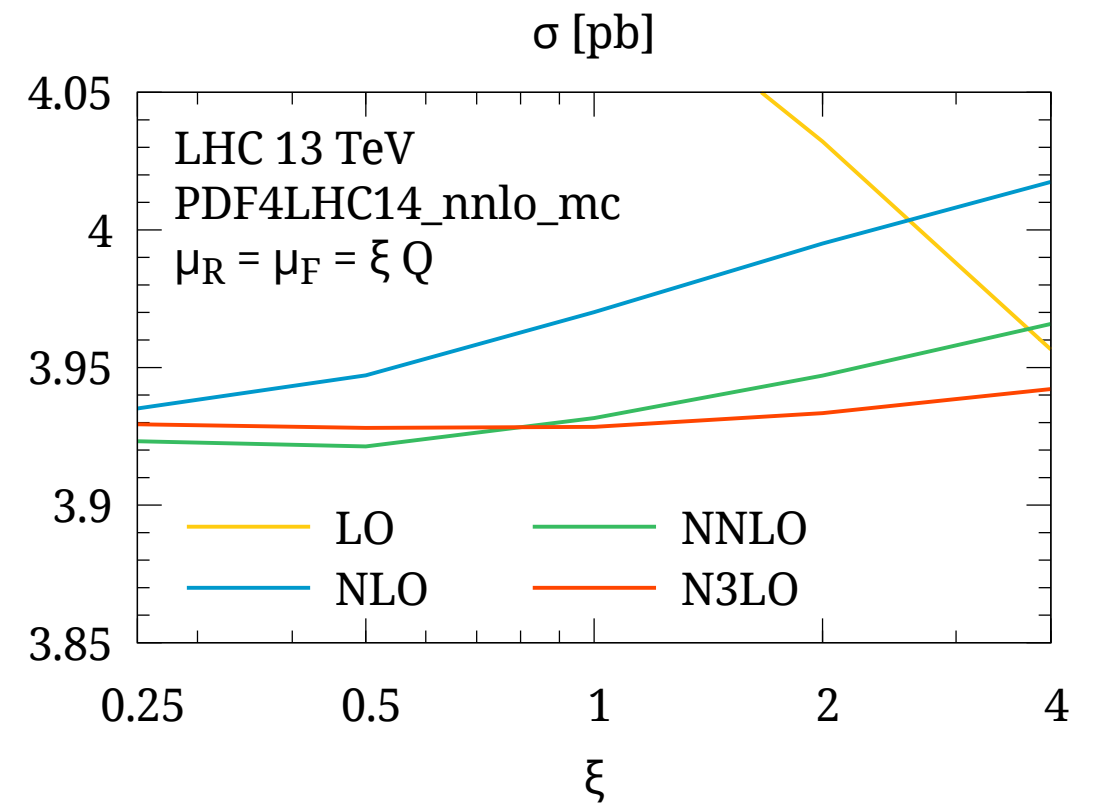
# DIS in disguise: VBF@LHC

Using DIS in a clever way:

## NNLO exclusive



## N<sup>3</sup>LO inclusive



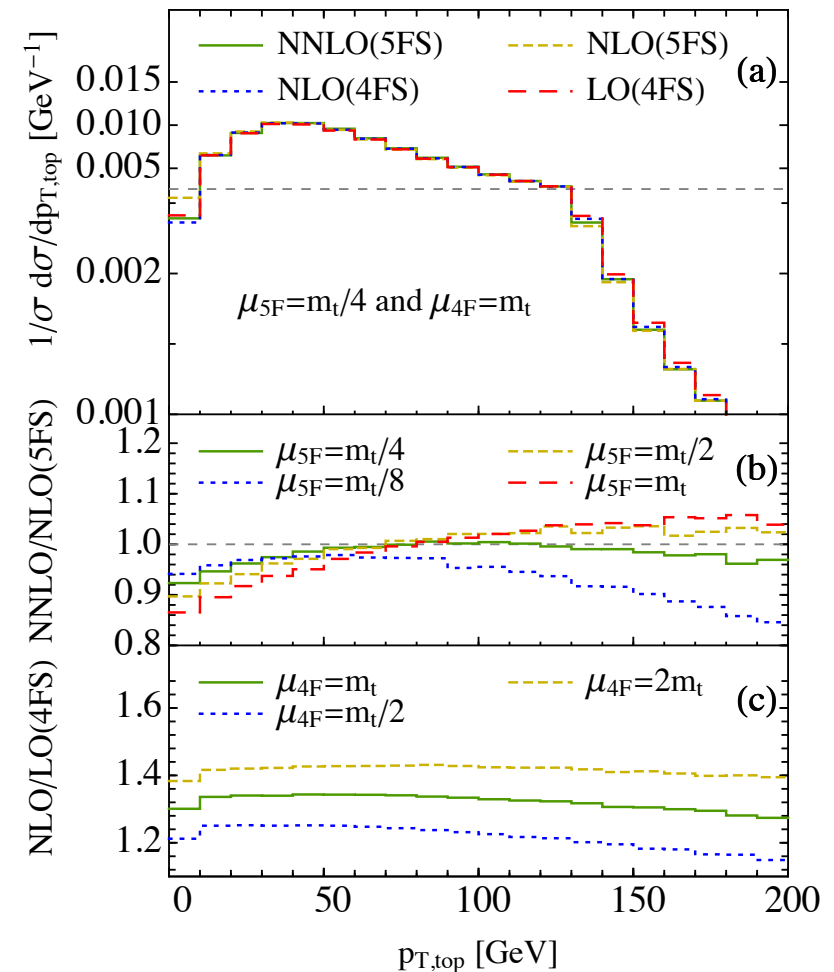
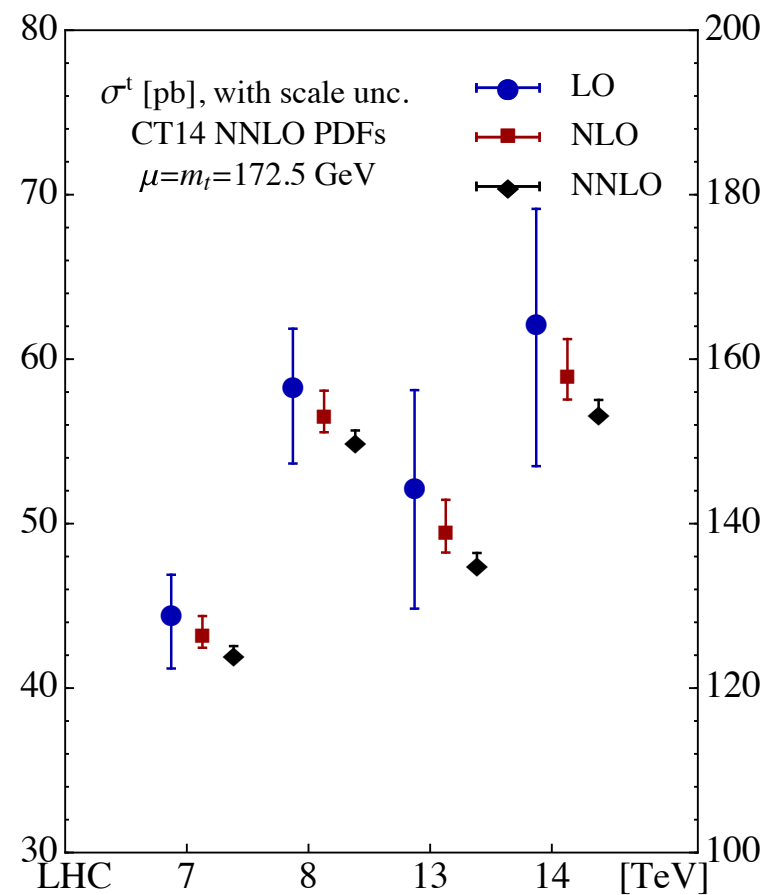
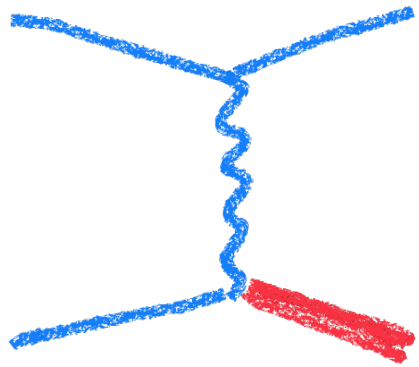
[Dreyer, Karlberg (2016)]

- Double-DIS approximation very good... although careful at Glauber phases,  $\pi^2/N_c^2$  is not small [Melnikov, Penin (2019)]



# DIS in disguise: t-channel single top

A similar argument holds for t-channel single-top

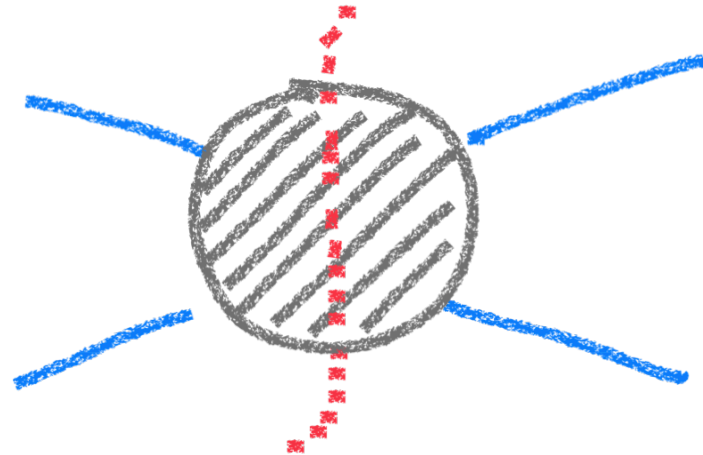


[Berger, Gao + Yuan, Zhu (2016-20)]

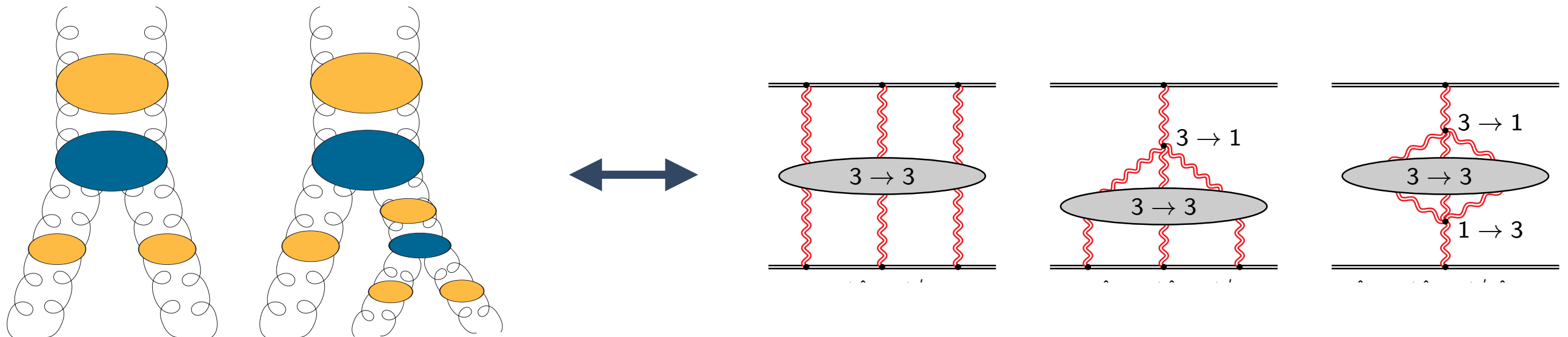
- Also requires massless  $\rightarrow$  massive DIS transitions [Berger, Gao, Li, Liu, Zhu (2016)]
- Double-DIS approximation very good... although careful at Glauber phases,  $\pi^2/N_c^2$  is not small [ $\rightarrow$  see C. Brønnum-Hansen's talk]

# Non-linear evolution in disguise

- Unitarity: parton evolution  $\leftrightarrow$  forward scattering of elastic amplitudes



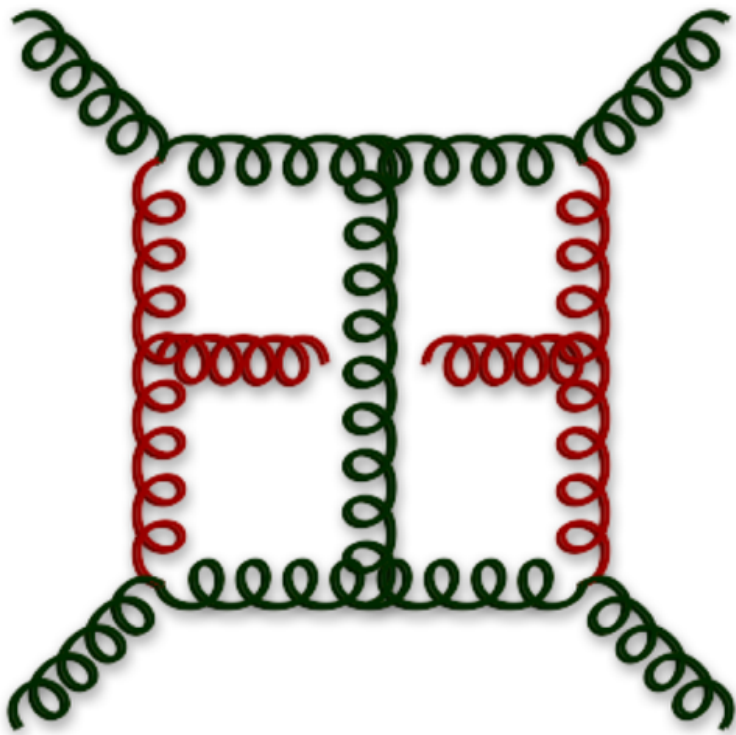
- High-enough logarithmic order: sensitive to full Balitsky-JIMWLK evolution



[formalism spelled out in Caron-Huot (2013) + del Duca, Falcioni, Gardi, Maher, Milloy, Vernazza (2013–2022); Fadin, Lipatov (2018)]

# Non-linear evolution in disguise

- $2 \rightarrow 2$  QCD scattering amplitudes@3L recently computed [Chakraborty, Gambuti, von Manteuffel, Tancredi, FC (2021)]



Everything as predicted!

Can test Regge factorisation at NNLL

$$\mathcal{H}_{\text{ren},\pm} = Z_g^2 e^{L \mathbf{T}_t^2 \tau_g} \sum_{n=0}^3 \bar{\alpha}_s^n \sum_{k=0}^n L^k \mathcal{O}_k^{\pm,(n)} \mathcal{H}_{\text{ren}}^{(0)},$$

Regge trajectory

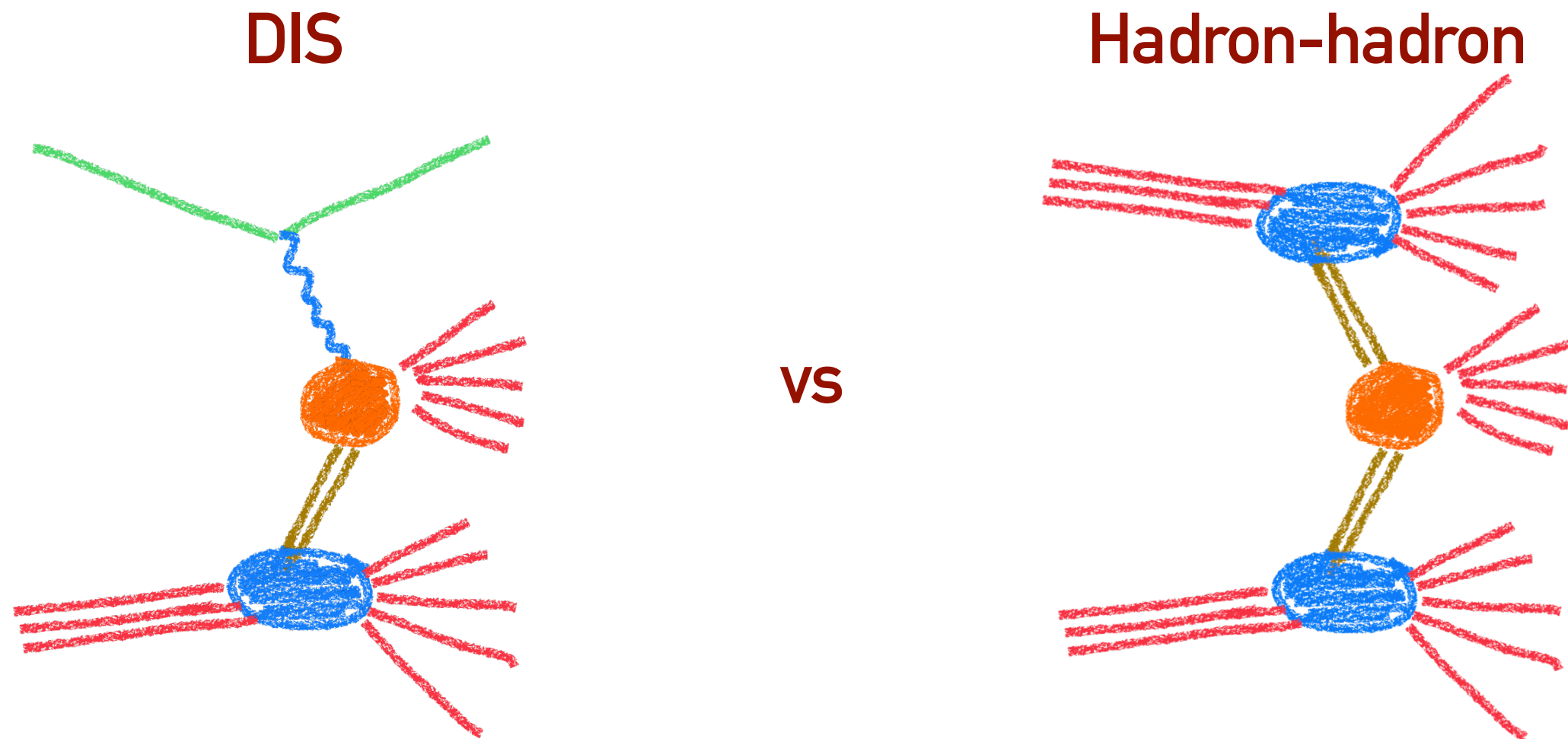
Multi-Reggeon interactions (SLC)

$$\mathcal{O}_0^{-,(0)} = 1, \quad \mathcal{O}_0^{-,(1)} = 2\mathcal{I}_1^g,$$

$$\mathcal{O}_0^{-,(2)} = \left[ 2\mathcal{I}_2^g + (\mathcal{I}_1^g)^2 \right] + \mathcal{C}^{-,(2)} \left[ (\mathbf{T}_{s-u}^2)^2 - \frac{N_c^2}{4} \right],$$

$$\mathcal{O}_1^{-,(3)} = \mathcal{C}_1^{-,(3)} \mathbf{T}_{s-u}^2 [\mathbf{T}_t^2, \mathbf{T}_{s-u}^2] + \mathcal{C}_2^{-,(3)} [\mathbf{T}_t^2, \mathbf{T}_{s-u}^2] \mathbf{T}_{s-u}^2,$$

# LHC: almost DIS2, but not always...

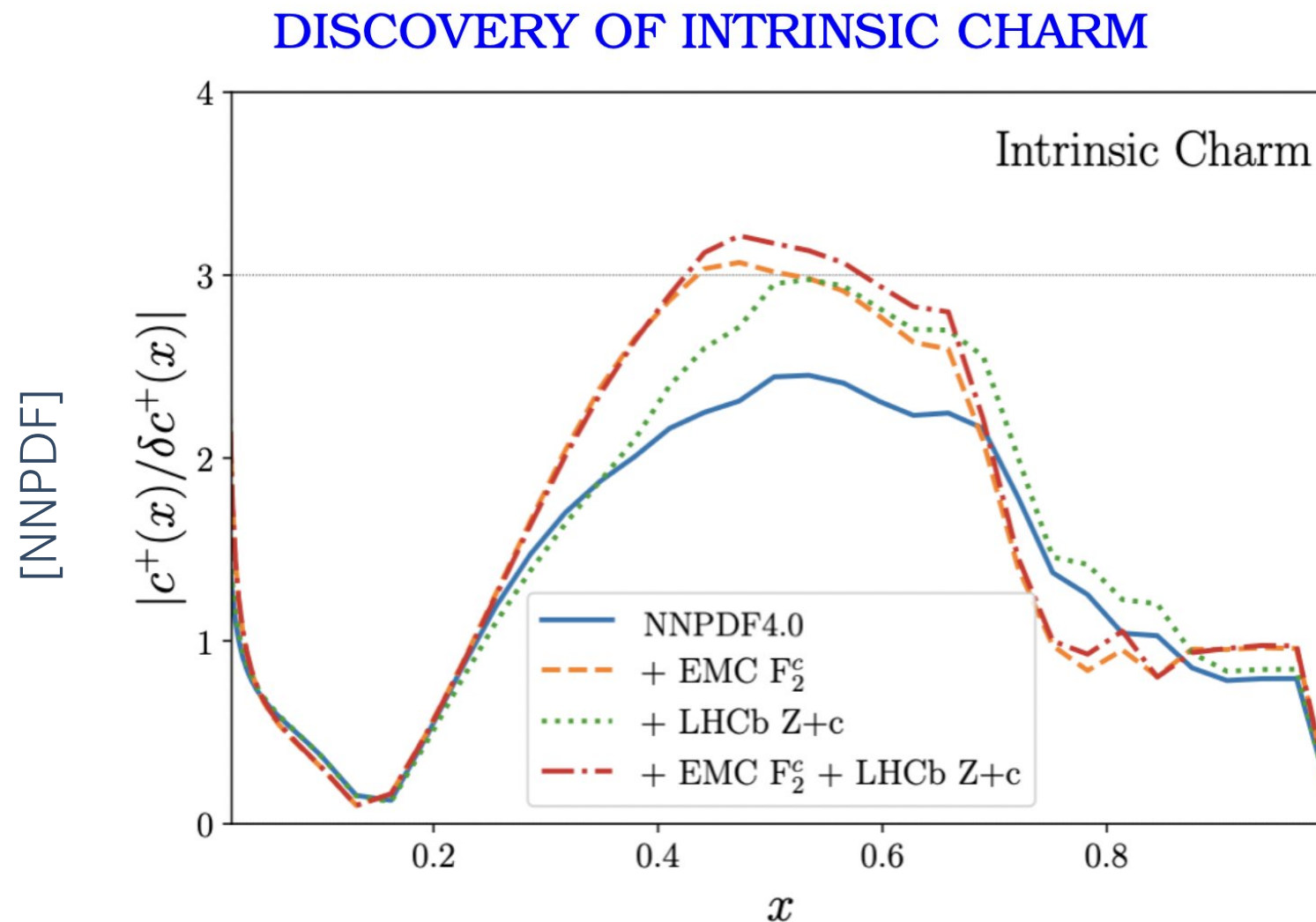


QCD with intrinsic heavy quarks:

- collinear factorisation violated at NNLO in hadron-hadron (i.e.  $R+V+\text{ren} = \infty$ )
- no problem in DIS

[Doria, Frenkel, Taylor (1980); many subsequent studies. See e.g. Melnikov, Napoletano, Tancredi, FC (2020) for a modern derivation and discussion]

# A new twist to an old story: intrinsic charm!



MORE THAN  $3\sigma$  EVIDENCE

Evidence for intrinsic charm in DIS + LHC data

- How to properly deal with it at NNLO at the LHC unclear
- DIS: solid foundation → guide and benchmark

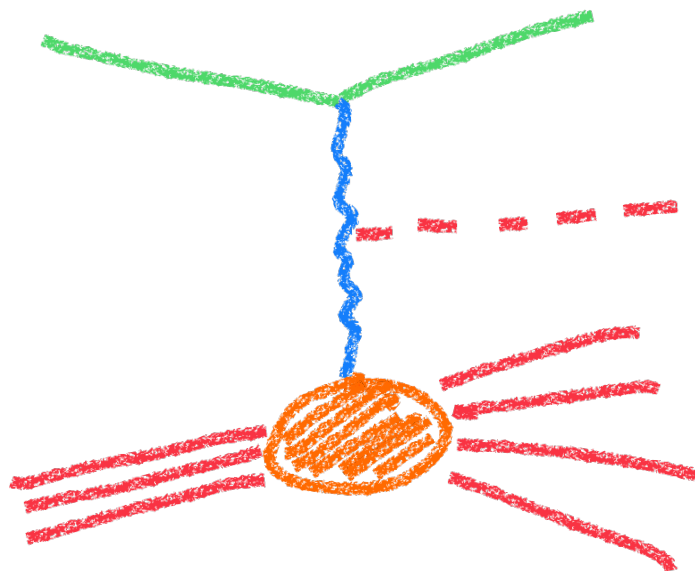
[→ see K. Kudashkin's talk and G. Magni's poster]

# DIS as a high-energy probe

DIS in the past did probe EW interactions (NC vs CC,  $\gamma/Z$  interference...)

Future DIS facilities: clean environment (low pile-up, controlled bkgd...) for precision EW studies

- A famous example: b/c Higgs Yukawa



- $S/B \sim 3!$
- Constrain signal strength to 0.8% (bb) and 7.4% (cc)

- Not the only one! W-mass in the t-channel, top polarisation, radiation zeros, hidden sectors, axions... rich program at future facilities

→ see J. d'Hondt & M. d'Onofrio's talks



# Conclusion I

“Interesting physics”  $\neq$  “BSM”

... as any physicist not working on particle physics would tell you

- If a collider can deliver new discoveries, that's of course great
- Looking at the future: the era of “guaranteed new physics deliveries” (like the Higgs for the LHC) may well be over
- But there is a rich set of unexplored areas in the SM that are worth pursuing

Many interesting open questions in QCD. For example

- Mass/spin proton/nuclei
- The structure of the proton [PDFs, TMDs, tomography...]
- Nuclear physics: from models to first principles
- QCD evolution and new phases of QCD (saturation, QGP...)
- ...

Future DIS facilities (EIC, LHeC, FCC-eh) would shed light on these issues



# Conclusion II

## DIS: the simplest hadron collider machine

- In this case: **simple**  $\leftrightarrow$  **powerful** (clean, well-understood)
- Hard to overstate the importance of accurate, precise and reliable determinations of the structure of the proton for the HE program at hadron colliders  $\rightarrow$  legacy DIS data augmented with LHC information, interesting cross-talks

Extreme regions (small/large- $x$ ) and individual quarks remain elusive  $\rightarrow$  limiting factor for different physics programs

- HE DIS: clean probe of EW scale and beyond
- Interesting synergies with other experiments
- Many interesting QCD questions
- Techniques developed for DIS have much broader applications

**DIS: very interesting and important  
role in the HEP landscape**

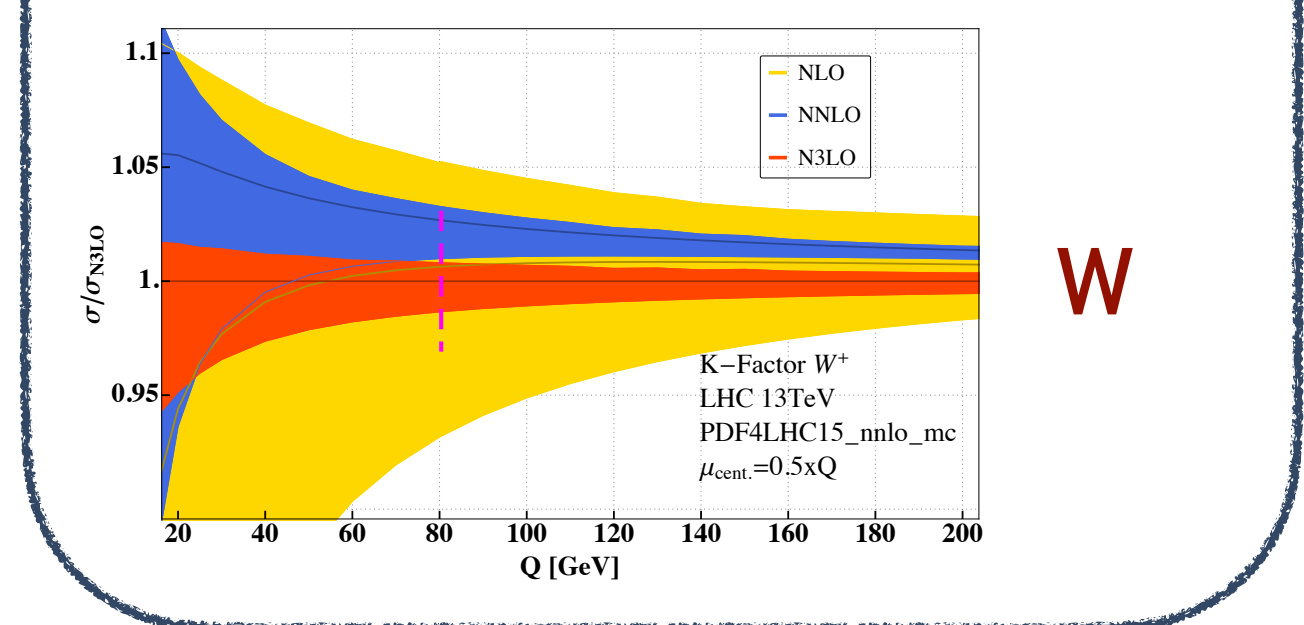
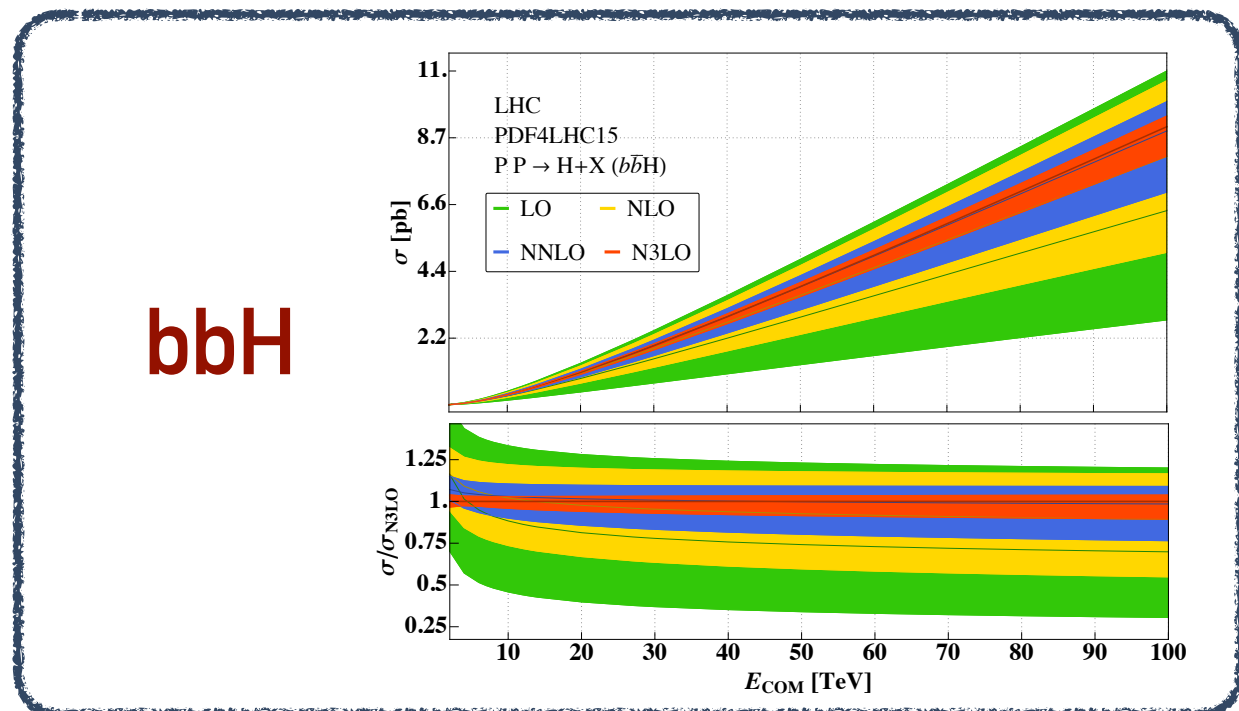
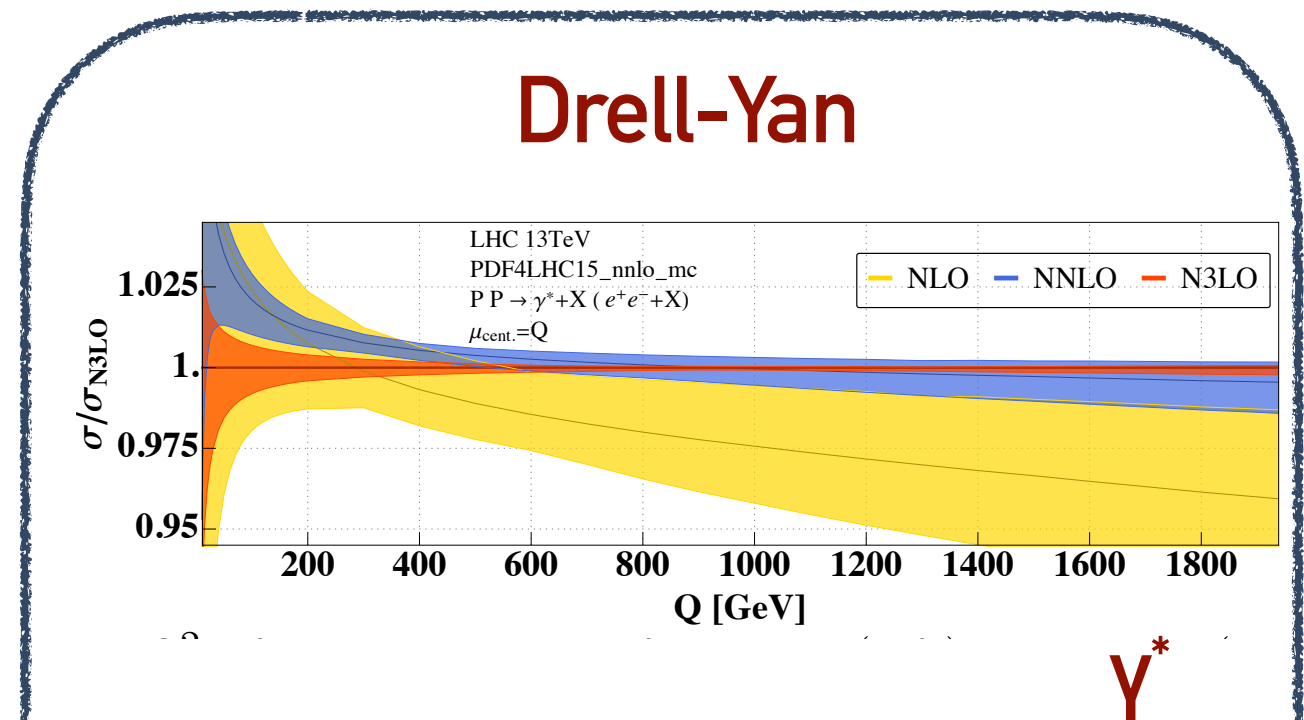
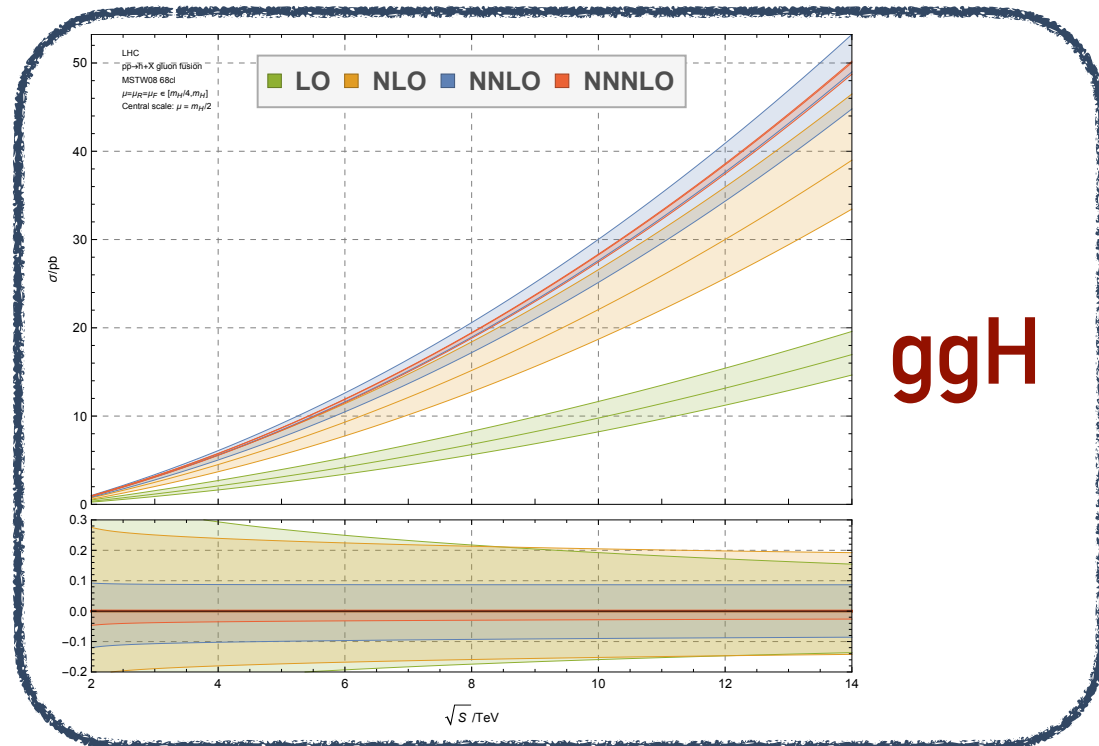
Thank you very much for your attention!

**Backup**

# N<sup>3</sup>LO: inclusive results

To a large extent, inclusive N<sup>3</sup>LO for 2 → 1 processes has been solved

[Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Lazopoulos, Mistlberger (2016-...);  
Duhr, Dulat, Mistlberger (2020-21)]



# N<sup>3</sup>LO: PDFs

N<sup>3</sup>LO PDFs not available → order mismatch

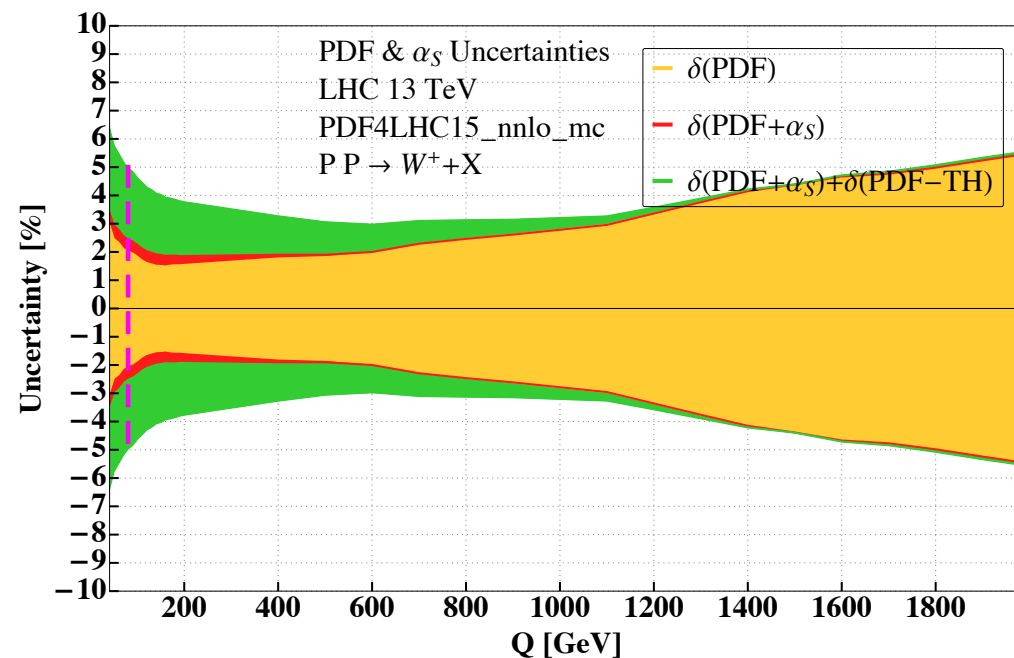
Y\*

Q/GeV	K <sub>QCD</sub> <sup>N<sup>3</sup>LO</sup>	δ(scale)	δ(PDF+α <sub>S</sub> )	δ(PDF-TH)
30	0.952	+1.5% -2.5%	±4.1%	±2.7%
50	0.966	+1.1% -1.6%	±3.2%	±2.5%
70	0.973	+0.89% -1.1%	±2.7%	±2.4%
90	0.978	+0.75% -0.89%	±2.5%	±2.4%
110	0.981	+0.65% -0.73%	±2.3%	±2.3%
130	0.983	+0.57% -0.63%	±2.2%	±2.2%
150	0.985	+0.50% -0.54%	±2.2%	±2.2%

Error: estimate from previous orders

$$\delta(\text{PDF-TH}) = \frac{1}{2} \left| \frac{\sigma_{W^\pm}^{(2), \text{NNLO-PDFs}} - \sigma_{W^\pm}^{(2), \text{NLO-PDFs}}}{\sigma_{W^\pm}^{(2), \text{NNLO-PDFs}}} \right|.$$

W<sub>+</sub>

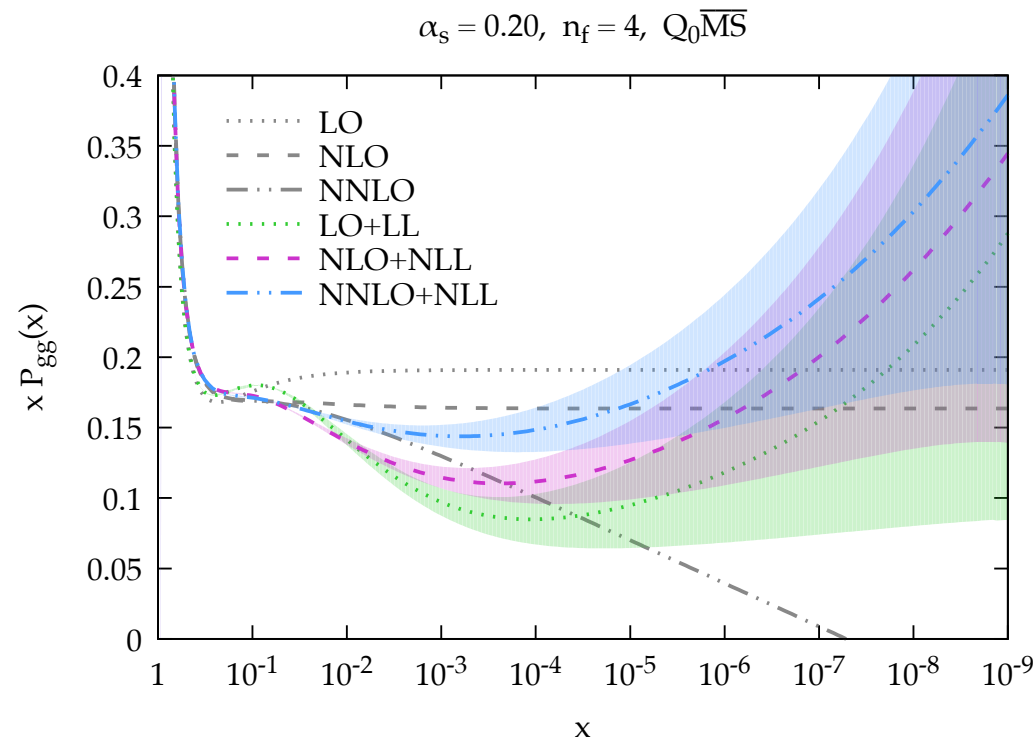


- ~ 2% PDF-TH error in the EW region
- significant fraction of the error budget
- same order of “standard” PDF+α<sub>S</sub>

# N<sup>3</sup>LO PDFs issues: evolution

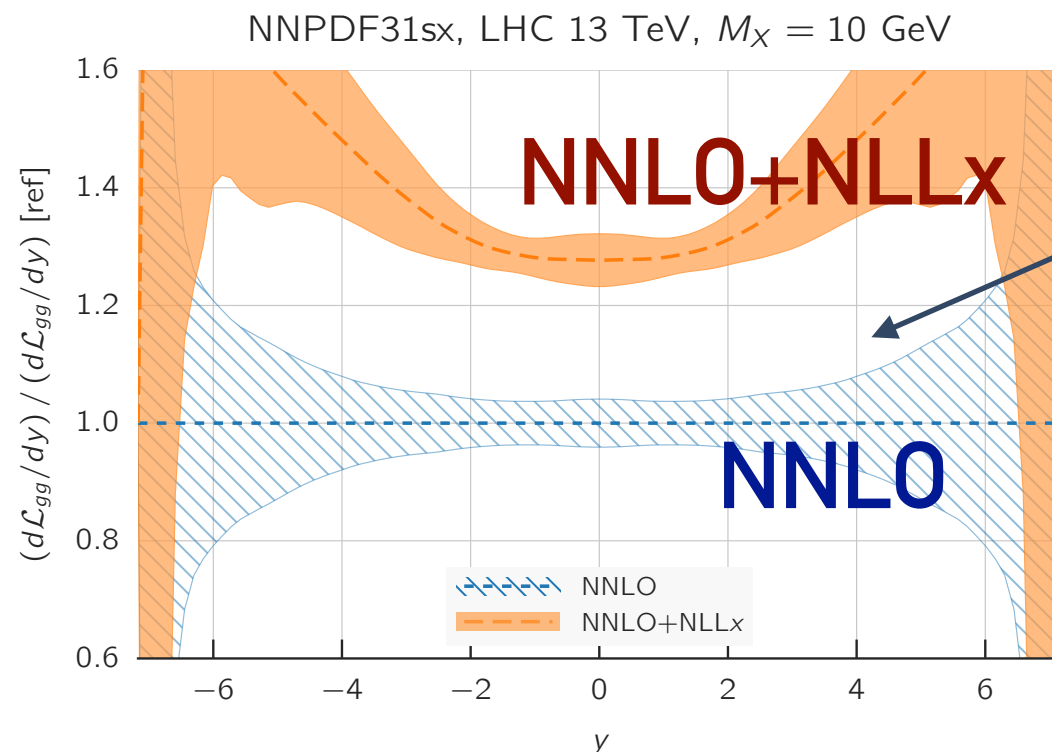
## N<sup>3</sup>LO: evolution and the problems of small-x

[Bonvini, Marzanni,  
Muselli (2017-18)]

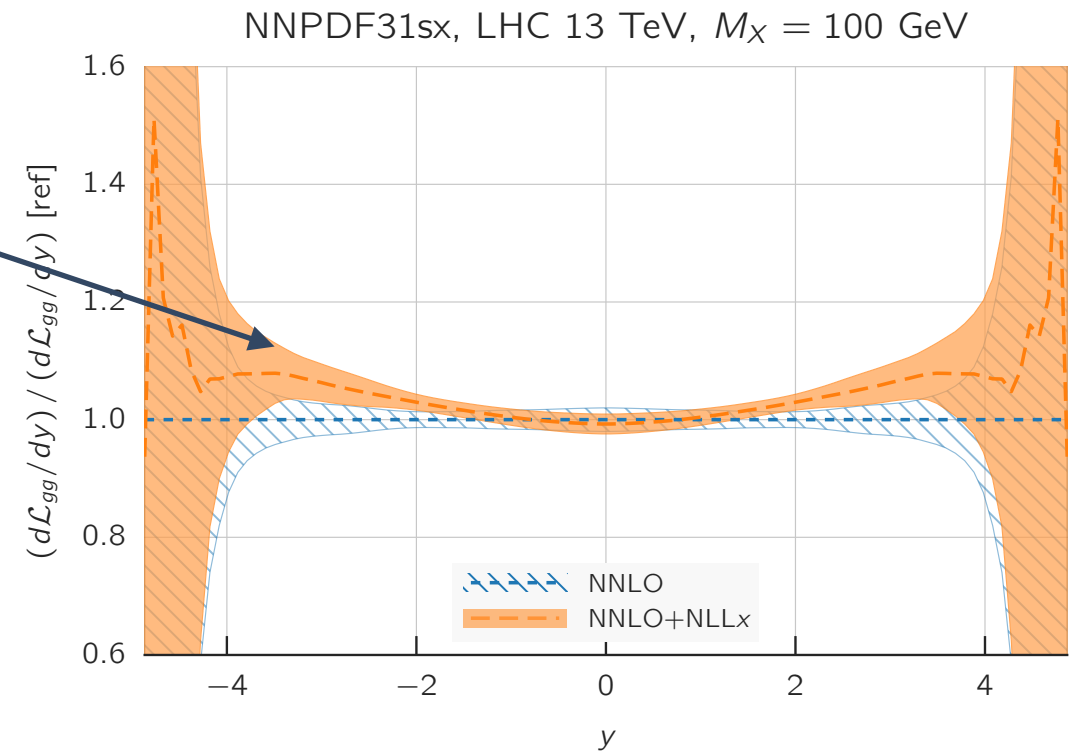


- N<sup>3</sup>LO calculation underway [Herzog, Moch, Ruijl, Ueda, Vermaseren, Vogt, in progress]
- N<sup>3</sup>LO: rapid small-x growth  $\rightarrow$  perturbative instabilities@N<sup>3</sup>LO
- NLL resummation known, but large subleading effects [Bonvini, Marzani (2018)]

[Ball, Bertone, Bonvini,  
Marzani, Rojo, Rottoli  
(2018)]



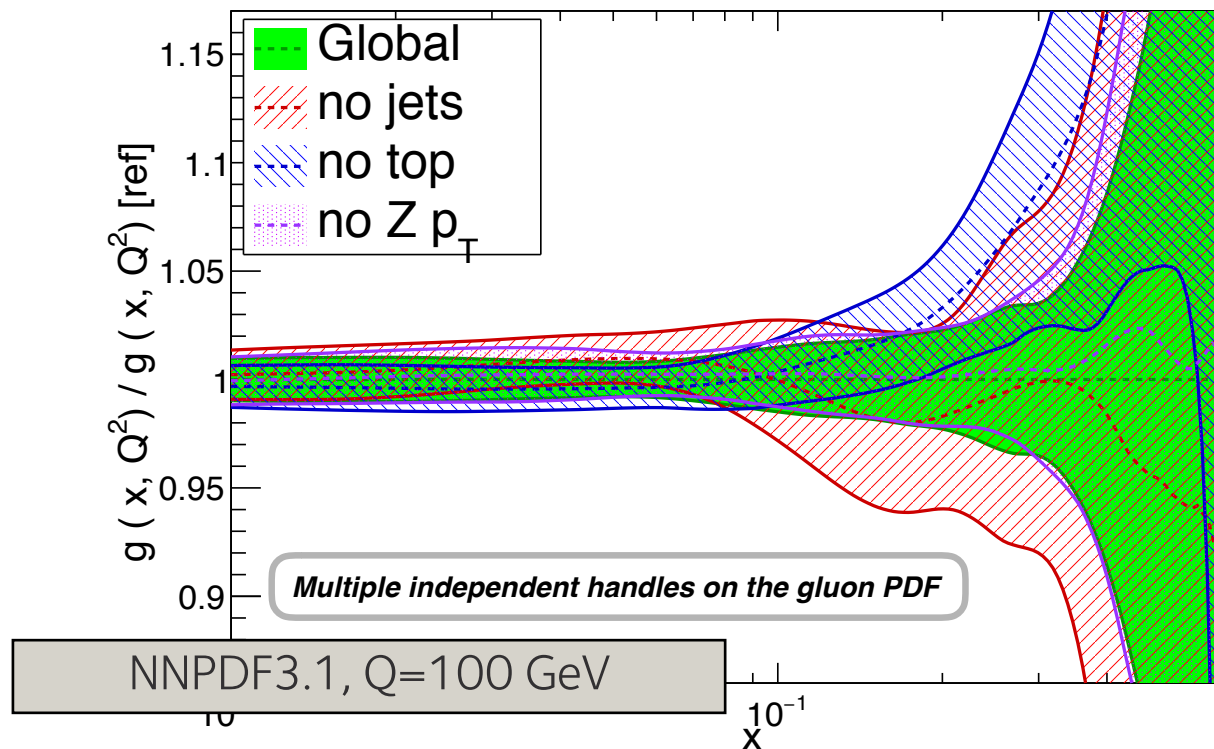
$\mathcal{L}_{gg}$



NNLO: an issue at low-mass, not quite so at the EW scale



# N<sup>3</sup>LO PDFs issues: data



- Collider data crucial to reduce perturbative uncertainty → fully-consistent N<sup>3</sup>LO fit would require top, Z p<sub>T</sub>, jets @ N<sup>3</sup>LO

## N<sup>3</sup>LO for PDFs: status and prospects

- DIS ✓
- DY ✓
- Z p<sub>T</sub>: ~ (unknown, but should be possible)
- Top: ~ (unknown, but should be possible given current understanding)
- Jets: ✗ (unknown, and there may be serious problems...)