

# Strong-phase inputs for CPV measurements at LHCb and Belle II

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HQL2021, Warwick, 14/09/2021

BESIII



## Strong-phase inputs for $\gamma$ measurement

### Strong-phase measurements at BESIII

$$D \rightarrow K\pi\pi\pi / K\pi\pi^0 \quad [\text{JHEP 05 (2021) 164}]$$

$$D \rightarrow K\pi \quad [\text{PLB 05, 071 (2014)}]$$

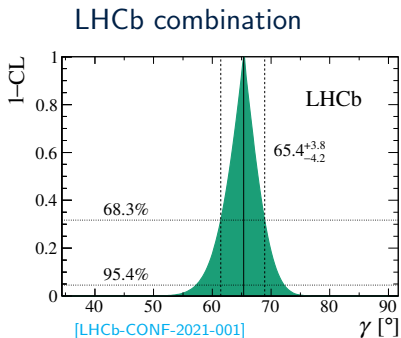
$$D \rightarrow K_S^0 h^+ h^- \quad [\text{PRD 101 (2020) 112002; PRD 102 (2020) 052008}]$$

## Strong-phase inputs for indirect charm CPV

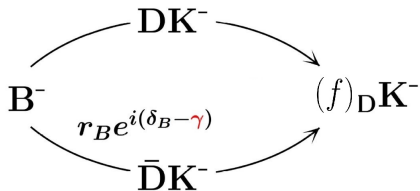
## Future prospects at BESIII

## Summary

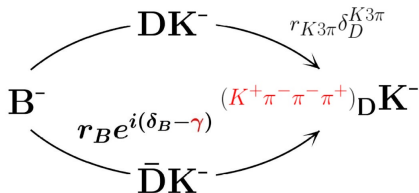
- CKM matrix, only source of  $CP$  violation in the SM
- CKM angles are large ( $\mathcal{O}(1)$ ) in the  $b$  sector  $\Rightarrow$  direct  $CP$  violation



- Determined in tree-level  $B$  decays, eg.  $B \rightarrow DK$
- No interference from NP effects
- Large experimental uncertainties
  - Statistics, systematics
  - External inputs



- Measurement of the interference between the two paths depends on the  $B$  and  $D$  decay parameters  $\Rightarrow$  External inputs of strong phase and associated parameters in  $D$  decays
- Allow extracting  $\gamma$  using different  $D$  decays:
  - DCS decays (eg.  $K\pi$ ,  $K\pi\pi^0$ ,  $K\pi\pi\pi$ ): "ADS" [PRL 78 (1997) 3257; PRD 63 (2001) 036005]  $\Rightarrow \delta_D, R_f$
  - Self-conjugate decays (eg.  $K_S^0 h^+ h^-$ ): "BPGGSZ" [PRD 68 (2003) 054018; PRD 67 (2003) 071301; A. Bondar]  $\Rightarrow c_i, s_i$
  - (Quasi-)CP eigenstates (eg.  $h^+ h^-$ ): "GLW" [PLB 265 (1991) 172; PLB 253 (1991) 483]  $\Rightarrow$  CP fraction  $F^+$ ; Others...



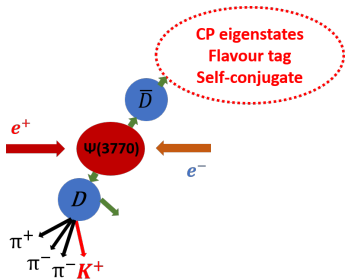
- Both DCS and CF processes contribute to  $B^\mp \rightarrow (K^\pm 3\pi)_D K^\mp$
- Phase-space integrated decay rate

$$\Gamma(B^\mp \rightarrow (K^\pm 3\pi)_D K^\mp) \propto r_{K3\pi}^2 + r_B^2 + 2r_B R_{K3\pi} r_{K3\pi} \cos(\delta_B \pm \gamma - \delta_D^{K3\pi})$$

- $R_S e^{-i\delta_D^S} = \frac{\int \mathcal{A}_S^*(\mathbf{x}) \mathcal{A}_{\bar{S}}(\mathbf{x}) d\mathbf{x}}{A_S A_{\bar{S}}}$ , coherence factor and strong phase
- $R$  indicates the intermediate resonances,  $0 < R < 1$  for  $K3\pi$  and  $K\pi\pi^0$ ,  $R = 1$  for  $K\pi$

- Quantum correlated  $C$ -odd  $D\bar{D}$  produced at BESIII

$$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$$



- $\int dt\mathcal{L} = 2.93 \text{ fb}^{-1}$
- 10597,000 neutral  $D\bar{D}$   
[CPC 42 (2018) 083001]
- "Double-tag" method:  
reconstruct both  $D$  &  $\bar{D}$
- $M_{\text{BC}} = \sqrt{E_{\text{beam}}^2/c^4 - |\mathbf{p}_D^2|/c^2}$
- $\Delta E = E_D - E_{\text{beam}}$

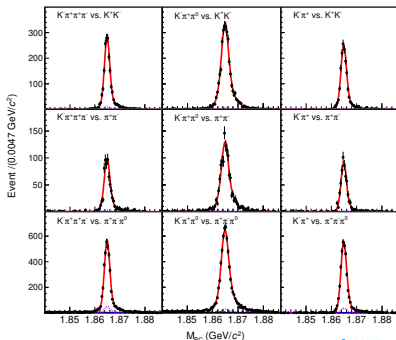
- Compare the double tag yields w/w.o. quantum correlation

$$\Gamma_{\text{QC}}(S|T) = \Gamma_0 A_S^2 A_T^2 [(r_D^S)^2 + (r_D^T)^2 - 2R_S R_T r_D^S r_D^T \cos(\delta_D^T - \delta_D^S)]$$

$$\Gamma(ST) = \Gamma_0 A_S^2 A_T^2 [(r_D^S)^2 + (r_D^T)^2]$$

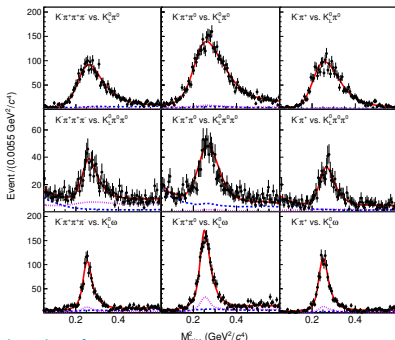
- Example fits to double tag events

Fully reconstructed  $CP$  modes

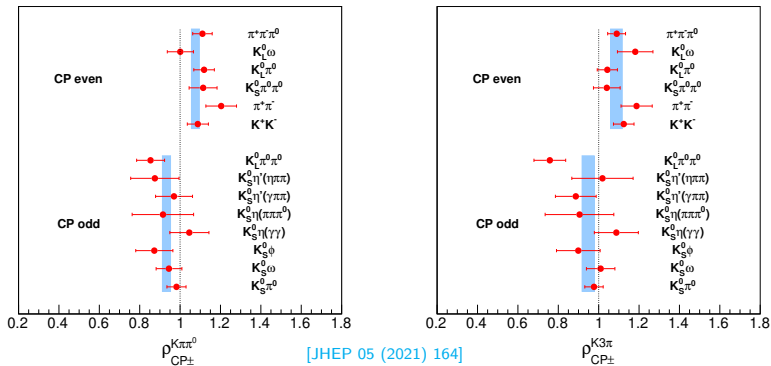


[JHEP 05 (2021) 164]

$K_L^0$  modes



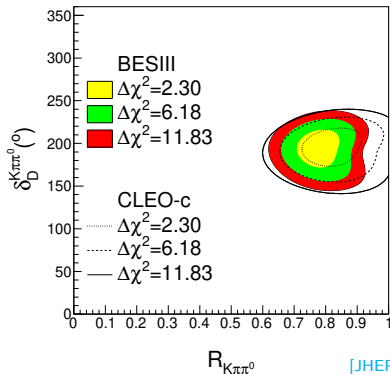
- Clean background in fully reconstructed events
- $K_L^0$  can be reconstructed with the missing mass  $M_{miss}^2$  recoiled against the tagged  $D$  and particles in the signal side



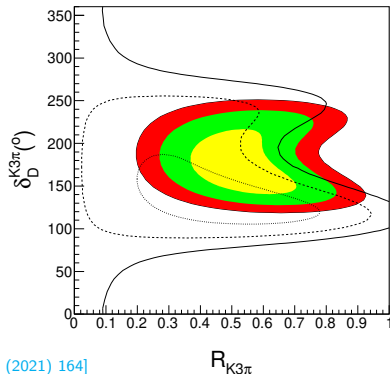
- $\rho_{CP}$ , the ratio of background-subtracted and efficiency-corrected yields and expectations w.o. QC, differ from 1
- Other tags also contribute: Like-sign flavour tags (eg.  $K^+3\pi$  vs  $K^+3\pi$ );  $K_S^0\pi^+\pi^-$  tag (phase variations over Dalitz plane)



# Strong-phase difference and coherence factor **BESIII**

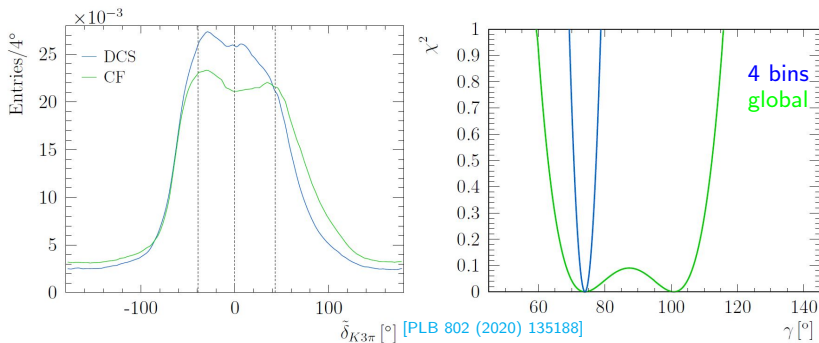


[JHEP 05 (2021) 164]



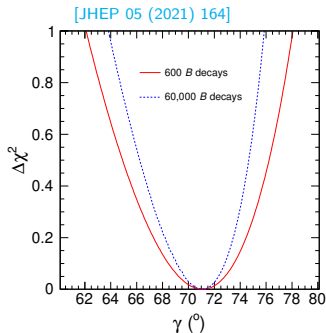
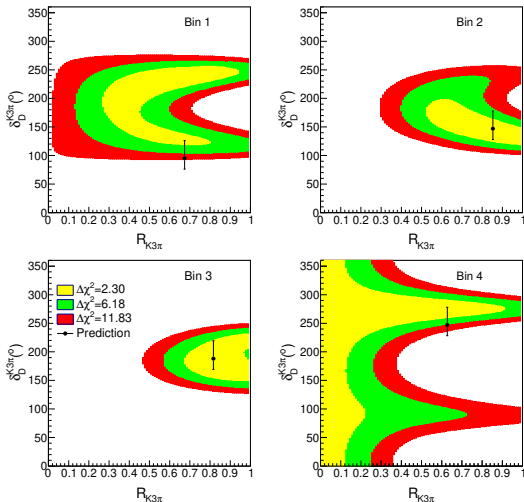
- Average  $\delta_D$  and  $R$  in the whole phase space in  $K3\pi$  and  $K\pi\pi^0$
- Significant improvement compared to CLEO-c results [PLB 757 (2016) 520]

- $D \rightarrow K3\pi$  is rich of resonances,  $\delta_D^{K3\pi}$  varies in phase space regions
- Sensitivity on  $\gamma$  can be improved measuring it in  $D \rightarrow K3\pi$  bins



- Model-independent measurement, only binning method depends on the DCS and CF model of  $D \rightarrow K3\pi$  [EPJC 78 (2018) 443]

# Results of binned $\delta_D^{K3\pi}$ and $R_{K3\pi}$



- $\delta_{\text{LHCb}}^{\text{Run1\&2}} = \begin{pmatrix} +7 \\ -9 \end{pmatrix}^\circ$
- $\begin{pmatrix} +5 \\ -7 \end{pmatrix}^\circ$  comes from BESIII
- $\delta_{\text{LHCb}}^{K_S^0 \pi \pi} \sim 5^\circ$  [JHEP 02 (2021) 169]

- Significant improvement compared to CLEO-c results [PLB 802 (2020) 135188]

# Determination of $\cos \delta_D^{K\pi}$ at BESIII

$$\bullet \mathcal{A}_{K\pi}^{CP} = \frac{2r_D^{K\pi} \cos \delta_{K\pi} + y}{1 + R_{WS}} = \frac{\mathcal{B}_{D^0 S^- \rightarrow K^- \pi^+} - \mathcal{B}_{D^0 S^+ \rightarrow K^- \pi^+}}{\mathcal{B}_{D^0 S^- \rightarrow K^- \pi^+} + \mathcal{B}_{D^0 S^+ \rightarrow K^- \pi^+}}$$

## • $CP$ tagged $K\pi$ events

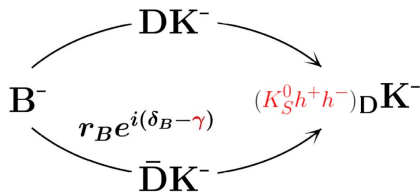
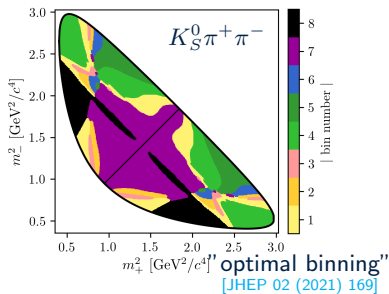
DT mode	$n_{K\pi, S^\pm}$
$K\pi, K^+K^-$	$1671 \pm 41$
$K\pi, \pi^+\pi^-$	$610 \pm 25$
$K\pi, K_S^0 \pi^0 \pi^0$	$806 \pm 29$
$K\pi, \pi^0 \pi^0$	$213 \pm 14$
$K\pi, \rho \pi^0$	$1240 \pm 35$
$K\pi, K_S^0 \pi^0$	$1689 \pm 41$
$K\pi, K_S^0 \eta$	$230 \pm 15$
$K\pi, K_S^0 \omega$	$747 \pm 27$

[PLB 05, 071 (2014)]

- $\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$
- $\cos \delta_{K\pi} = 0.81_{-0.18-0.05}^{+0.22+0.07}$  [CLEO-c, PRD 86 (2012) 112001]
- $\delta_{K\pi} = (187.2_{-9.2}^{+7.9})^\circ$  [HFLAV, summer2021]

- Future prospects: explore how much could be gained for  $\delta_{K\pi}$  by including other  $CP$  tags and  $K_S^0 h^+ h^-$  tags with binned method

# Phase-difference parameters in $D \rightarrow K_S^0 h^+ h^-$ BESIII



- Divide  $D \rightarrow K_S^0 \pi^+ \pi^-$  Dalitz plot into bins  $\Rightarrow$  full potential to  $\gamma$  measurement

- Binned  $B \rightarrow DK$  yields:

$$N_{\pm i}^{\pm} = h_{B\pm} [F_{\mp i} + ((x_{\pm}^{DK})^2 + (y_{\pm}^{DK})^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_{\pm}^{DK} c_i \mp y_{\pm}^{DK} s_i)]$$

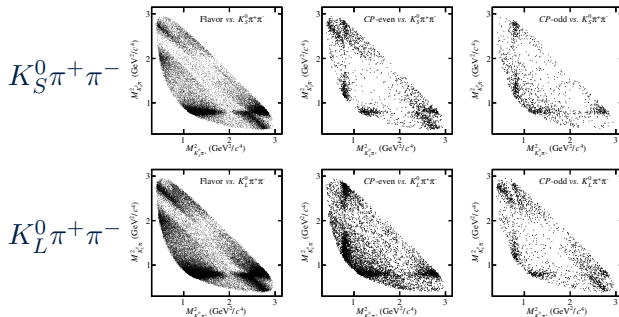
$$(x_{\pm} = r_B \cos(\delta_B \pm \gamma), y_{\pm} = r_B \sin(\delta_B \pm \gamma))$$

- Require input of the bin-averaged strong-phase parameters

$$c_i = \cos(\Delta\delta_D), s_i = \sin(\Delta\delta_D)$$

# Measurement of $c_i$ and $s_i$ in $D \rightarrow K_S^0 h^+ h^-$

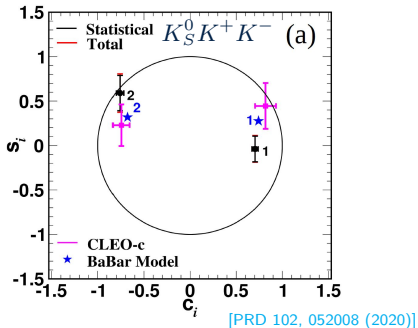
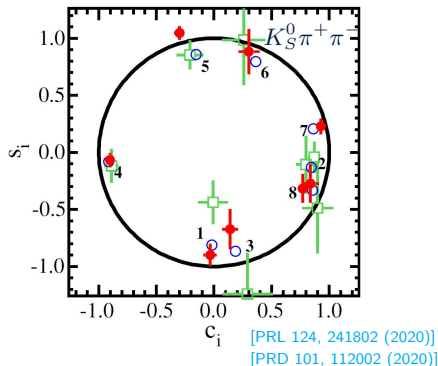
- $CP$  tags (eg.  $\pi\pi\pi^0$ ,  $K_S^0\pi^0$ ): different behaviour in Dalitz plot for  $CP$ -even/odd events  $\Rightarrow c_i$
- Self tags (tagged by itself)  $\Rightarrow c_i, s_i$
- $K_S^0 h'^+ h'^- / K_L^0 h^{(\prime)+} h^{(\prime)-}$  tags  $\Rightarrow c_i, s_i$  and  $c'_i, s'_i$



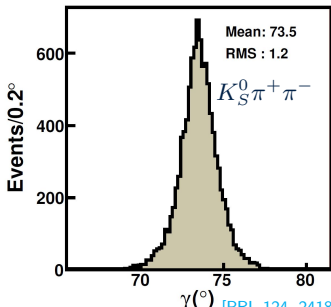
[PRD 101, 112002 (2020)]

# Results of $c_i$ and $s_i$ at BESIII

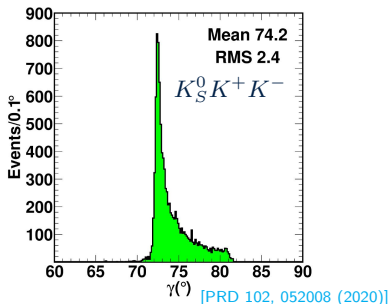
- Global analysis of the flavour,  $CP$  and self-tagged  $K_S^0 h^+ h^-$  events
- $K_S^0 K^+ K^-$  is similarly studied with 2 bins due to low statistics



- Significant improvement compared to CLEO-c measurements
- Results with more binning methods can be found in the publications



[PRL 124, 241802 (2020)]  
[PRD 101, 112002 (2020)]

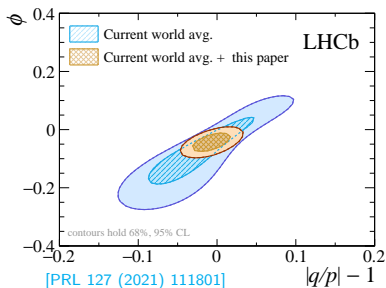


- Improvement of the  $\gamma$  sensitivity with only CLEO-c inputs  $\sim 3^{\circ}$   
[PRD 82, 112006 (2010)]
- BESIII uncertainty of  $K_S^0 \pi^+ \pi^-$  contributes around  $1^{\circ}$  to the latest LHCb measurement, leading to the best single measurement of  $\gamma$  ( $5^{\circ}$ ) [JHEP 02 (2021) 169]



# Strong-phase inputs for CPV in charm decays **BESIII**

- Indirect  $CP$  violation due to charm mixing and interference of mixing and decay
- Non-vanishing  $\phi$  and  $|q/p| - 1$  leads to observation



- $D \rightarrow K_S^0 \pi^+ \pi^-$
- **Not observed yet but significantly constrained**
- $c_i, s_i$  input from BESIII contributes to non-negligible systematics
- Other strong-phase measurements could contribute as inputs to charm mixing and  $CPV$  studies

[PRD 99 (2019) 012007; PRD 91 (2015) 094032]

[PLB 701 (2011) 353]

## Strong-phase inputs for $\gamma$ measurement

### Strong-phase measurements at BESIII

$$D \rightarrow K\pi\pi\pi / K\pi\pi^0 \text{ [JHEP 05 (2021) 164]}$$

$$D \rightarrow K\pi \text{ [PLB 05, 071 (2014)]}$$

$$D \rightarrow K_S^0 h^+ h^- \text{ [PRD 101 (2020) 112002; PRD 102 (2020) 052008]}$$

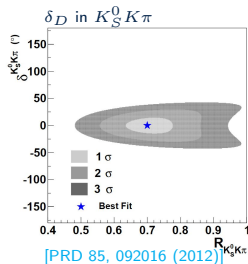
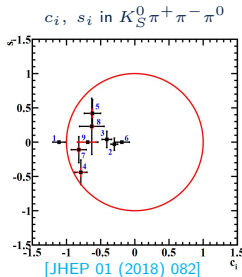
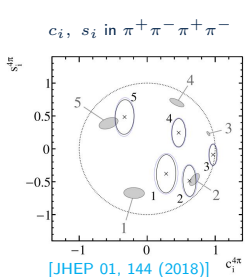
## Strong-phase inputs for indirect charm CPV

### Future prospects at BESIII

### Summary

# Other decays measured by CLEO-c

- $0.818 \text{ fb}^{-1}$   $\psi(3770)$  CLEO-c data, BESIII can provide improved measurements with about 3.5 times data



- Improvement in  $K_S^0\pi^+\pi^-\pi^0$  shall be of interest for Belle II as its  $\mathcal{B}$  reaches  $(5.2 \pm 0.6)\%$  and it's challenging in LHCb

Decay mode	Quantity of interest
✓ $D \rightarrow K_S^0 \pi^+ \pi^-$	$c_i$ and $s_i$
✓ $D \rightarrow K_S^0 K^+ K^-$	$c_i$ and $s_i$
✓ $D \rightarrow K^\pm \pi^\mp \pi^+ \pi^-$	$R, \delta$
$D \rightarrow K^+ K^- \pi^+ \pi^-$	$c_i$ and $s_i$
$D \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	$F_+$ or $c_i$ and $s_i$
✓ $D \rightarrow K^\pm \pi^\mp \pi^0$	$R, \delta$
$D \rightarrow K_S^0 K^\pm \pi^\mp$	$R, \delta$
$D \rightarrow \pi^+ \pi^- \pi^0$	$F_+$
$D \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	$F_+$ or $c_i$ and $s_i$
$D \rightarrow K^+ K^- \pi^0$	$F_+$
✓ $D \rightarrow K^\pm \pi^\mp$	$\delta$

- Limited by statistics:

- $\pi^+ \pi^- \pi^+ \pi^-$
- $K^+ K^- \pi^+ \pi^-$

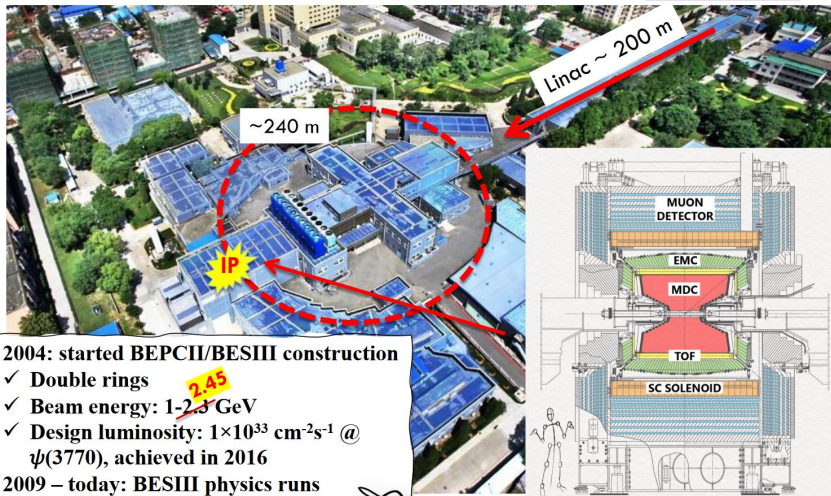
- Inputs for Belle II (challenging for LHCb):

- $K_S^0 \pi^+ \pi^- \pi^0$
- $K \pi \pi^0$
- $\pi^+ \pi^- \pi^0, K^+ K^- \pi^0$

- BESIII provides unique quantum correlated  $D\bar{D}$  data to measure the strong-phase parameters in  $D$  decays as inputs to LHCb and Belle II for
  - CKM angle  $\gamma$  measurement in the  $b$  sector
  - Indirect  $CP$  violation and mixing in neutral  $D$  meson decays
- Decays have been studied at BESIII:
  - $K_S^0 h^+ h^-$ ,  $K3\pi$ ,  $K\pi\pi^0$ ,  $K\pi$
- $20 \text{ fb}^{-1}$   $\psi(3770)$  data at BESIII in the near future [CPC 44, 040001 (2020)]
  - Improve the current measurement, eg.  $c_i$ ,  $s_i$  and  $\delta_D^{K3\pi}$  and  $R_{K3\pi}$
  - Low statistics decays, eg.  $\pi^+\pi^-\pi^+\pi^+$ ,  $K^+K^-\pi^+\pi^+$

Thanks!

# Back-up: BEPCII



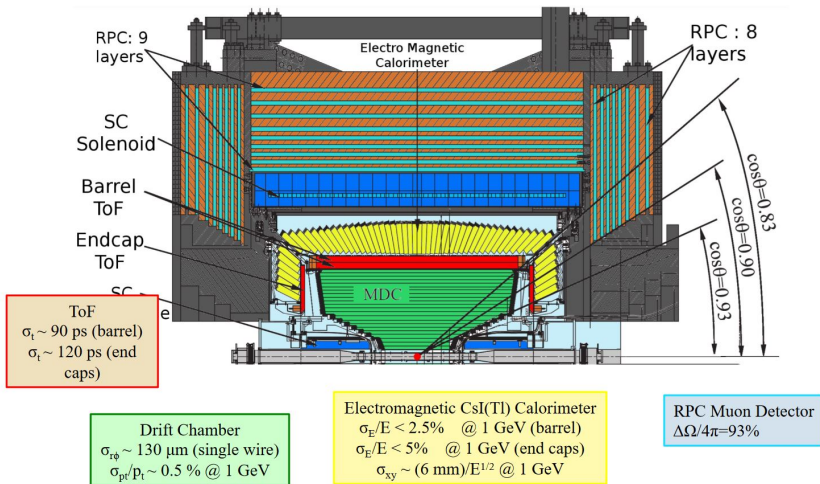
2004: started BEPCII/BESIII construction

- ✓ Double rings **2.45**
- ✓ Beam energy: ~~1-2.3~~ GeV
- ✓ Design luminosity:  $1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  @  $\psi(3770)$ , achieved in 2016

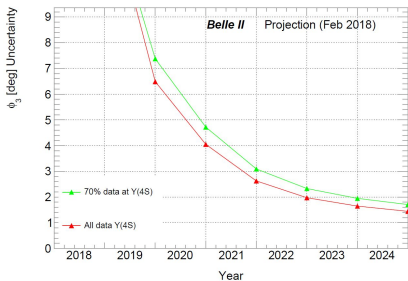
2009 – today: BESIII physics runs

# Back-up: BESIII

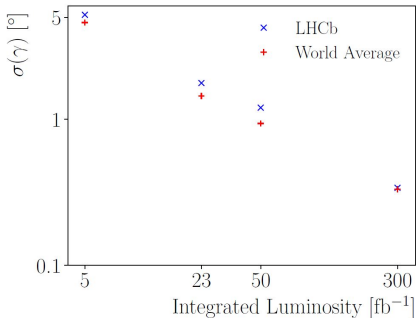
Nucl. Instr. Meth. A614, 345 (2010)



# Back-up: $\gamma$ sensitivity at LHCb and Belle II



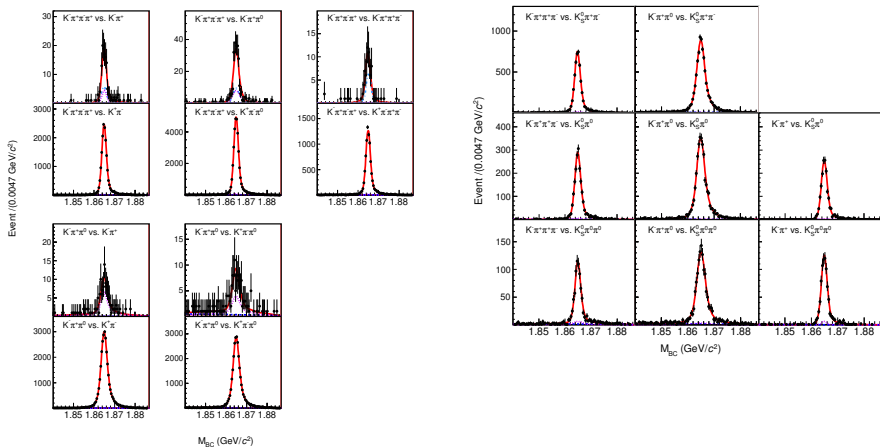
[arXiv: 1808.10567]



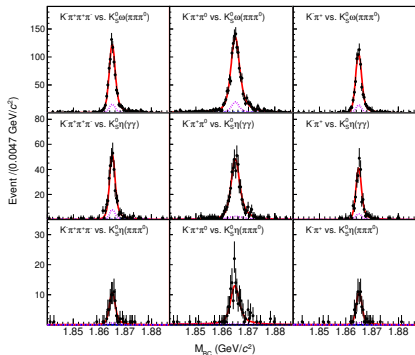
[arXiv:1808.08865]



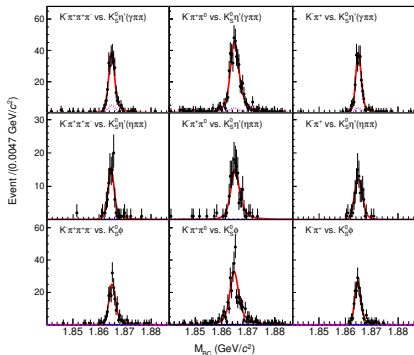
# Back-up: $K3\pi/K\pi\pi^0$ DT modes



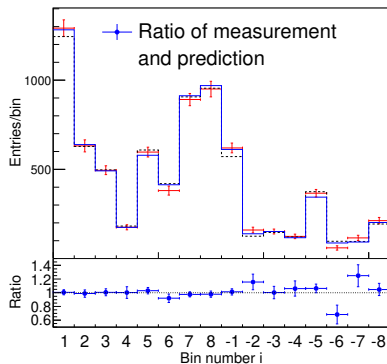
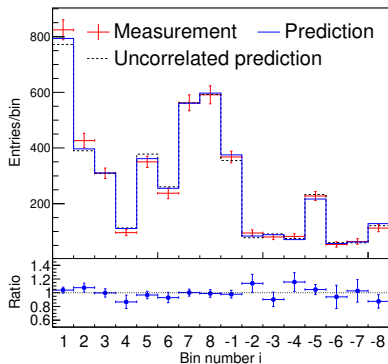
# Back-up: $K3\pi/K\pi\pi^0$ DT modes



[JHEP 05 (2021) 164]

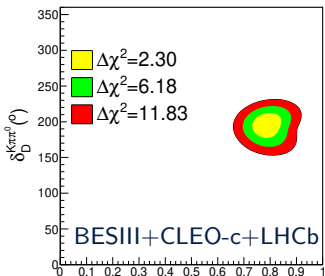
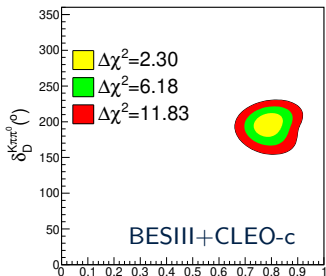
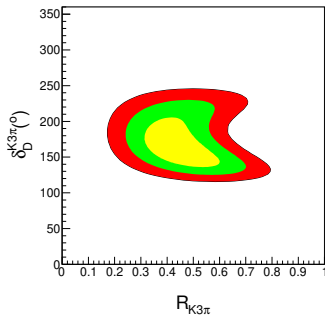
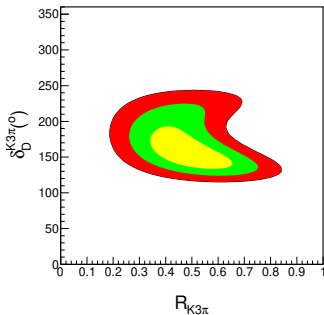


# Back-up: $K_S^0 \pi^+ \pi^-$ tag for $K3\pi/K\pi\pi^0$

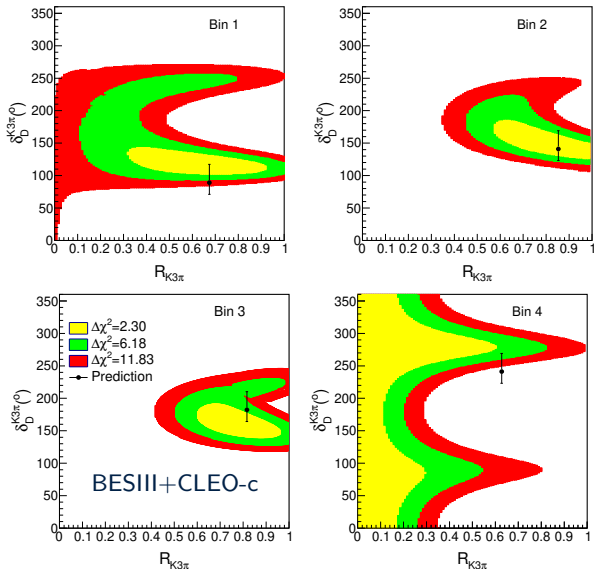


[JHEP 05 (2021) 164]

# Back-up: Combination of $\delta_D^{K3\pi}$ and $R_{K3\pi}$



# Back-up: Combination of binned $\delta_D^{K3\pi}$ and $R_{K3\pi}$



# Back-up: Determination of $CP$ fraction at CLEO-c

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- (Quasi) $CP$  tags:  $M(f|g) = \mathcal{Z}\mathcal{B}_f\mathcal{B}_g \left[ 1 - (2F_+^f - 1)(2F_+^g - 1) \right]$
- $K_{S,L}^0\pi^+\pi^-$  tags:  $M_i = h \left[ K_i + K_{-i} - (2F_+ - 1)2c_i\sqrt{K_iK_{-i}} \right]$
- [PLB 05, 043 (2015)]
- Input to  $\gamma$  measurement [PRD 91, 112014 (2015)]

Tag	$F_+^{\pi^+\pi^-\pi^0}$	$F_+^{K^+K^-\pi^0}$	$F_+^{\pi^+\pi^-\pi^+\pi^-}$
$CP$ eigenstates	0.968(17)(6)	0.731(58)(21)	0.754(31)(21)
$K_{S,L}^0\pi^+\pi^-$	1.014(45)(22)	0.734(106)(54)	0.737(49)(24)
$\pi^+\pi^-\pi^0$	-	-	0.695(50)(21)
Combined	$0.973 \pm 0.017$	$0.732 \pm 0.055$	$0.737 \pm 0.028$

- BESIII data can improve these measurements