

# The search for «missing links» of nuclear quadrupole moments – A status report

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for the IS640, IS673, and IS703 teams

Nuclear moments are determined by measuring their interaction energy/frequency with  
an external field:

For magnetic moments  $\mu$  the  
Larmor frequency  
$$\nu_L = B \cdot \mu / (I \cdot h)$$
with  $B$  the external magnetic  
field, generally well known,  
it requires  $I > 0$

For quadrupole moments  $Q$  the  
quadrupole coupling constant  
$$\nu_Q = V_{zz} \cdot Q \cdot e / h$$
with  $V_{zz}$  the electric field gradient (efg)  
at the nucleus, to be obtained by theory,  
it requires  $I > 1/2$

# Methods for quadrupole moment determination

For long-lived states  $>10$  ms

Atomic spectroscopy

For stable isotopes also:

Molecular spectroscopy

in

atoms or simple molecules

Accuracy of efg theory

1% in most cases



For short-lived states  $< 1$  ms

Mössbauer spectroscopy ME

Perturbed angular correlation PAC

Perturbed angular distribution PAD

in

condensed matter, generally metals

Accuracy of efg theory

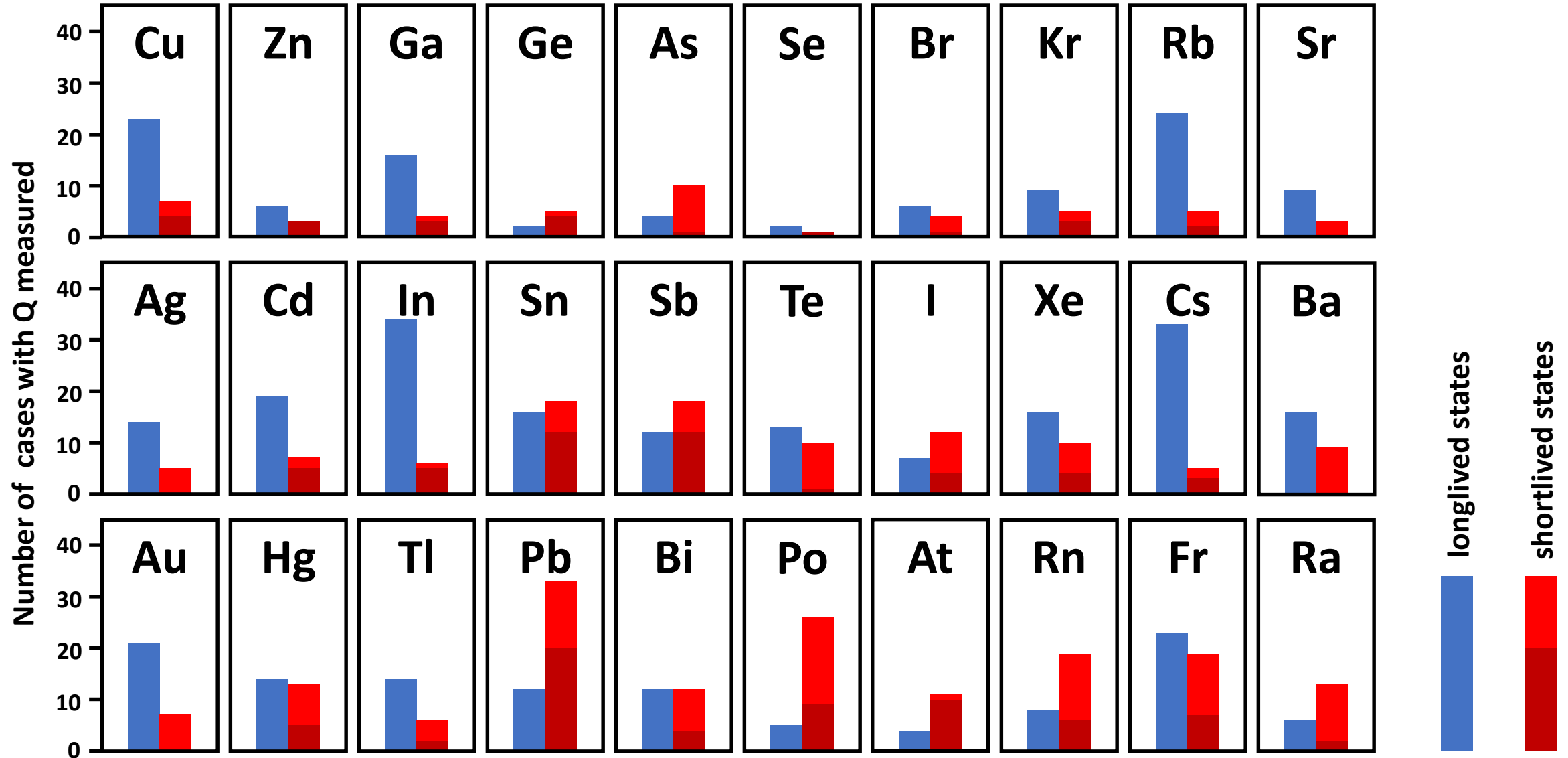
10-20%















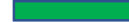

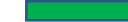

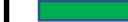
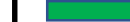












Linking the two areas by  
Nuclear magnetic resonance NMR  
Nuclear quadrupole resonance NQR  
Mössbauer spectroscopy ME

Only possible for stable isotopes !!































## The extend of the problem



# Elements **with** / **without** stable $I > 1/2$ isotopes

Cu	Zn	Ga	Ge	As	Se	Br	Kr	Rb	Sr
									
Ag	Cd	In	Sn	Sb	Te	I	Xe	Cs	Ba
									
Au	Hg	Tl	Pb	Bi	Po	At	Rn	Fr	Ra
									

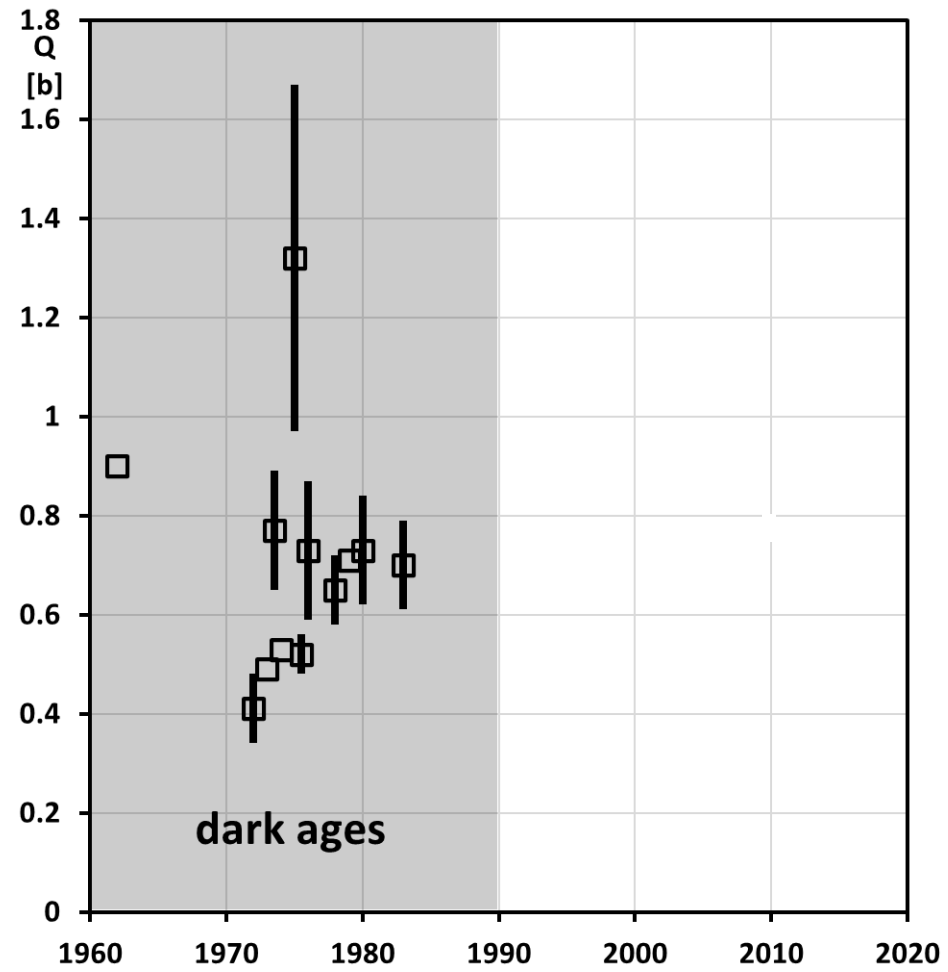
## The «easy» cases

<b>Cu</b> NQR 	<b>Zn</b> ME 	<b>Ga</b> NQR 	<b>Ge</b> ? 	<b>As</b> NQR 	<b>Se</b> 	<b>Br</b> NQR 	<b>Kr</b> ME 	<b>Rb</b> NMR 	<b>Sr</b> ? 
<b>Ag</b> 	<b>Cd</b> 	<b>In</b> NQR 	<b>Sn</b> 	<b>Sb</b> NQR 	<b>Te</b> 	<b>I</b> NQR 	<b>Xe</b> ? 	<b>Cs</b> NMR 	<b>Ba</b> ? 
<b>Au</b> ME 	<b>Hg</b> NQR 	<b>Tl</b> 	<b>Pb</b> 	<b>Bi</b> NQR 	<b>Po</b> 	<b>At</b> 	<b>Rn</b> 	<b>Fr</b> 	<b>Ra</b> 

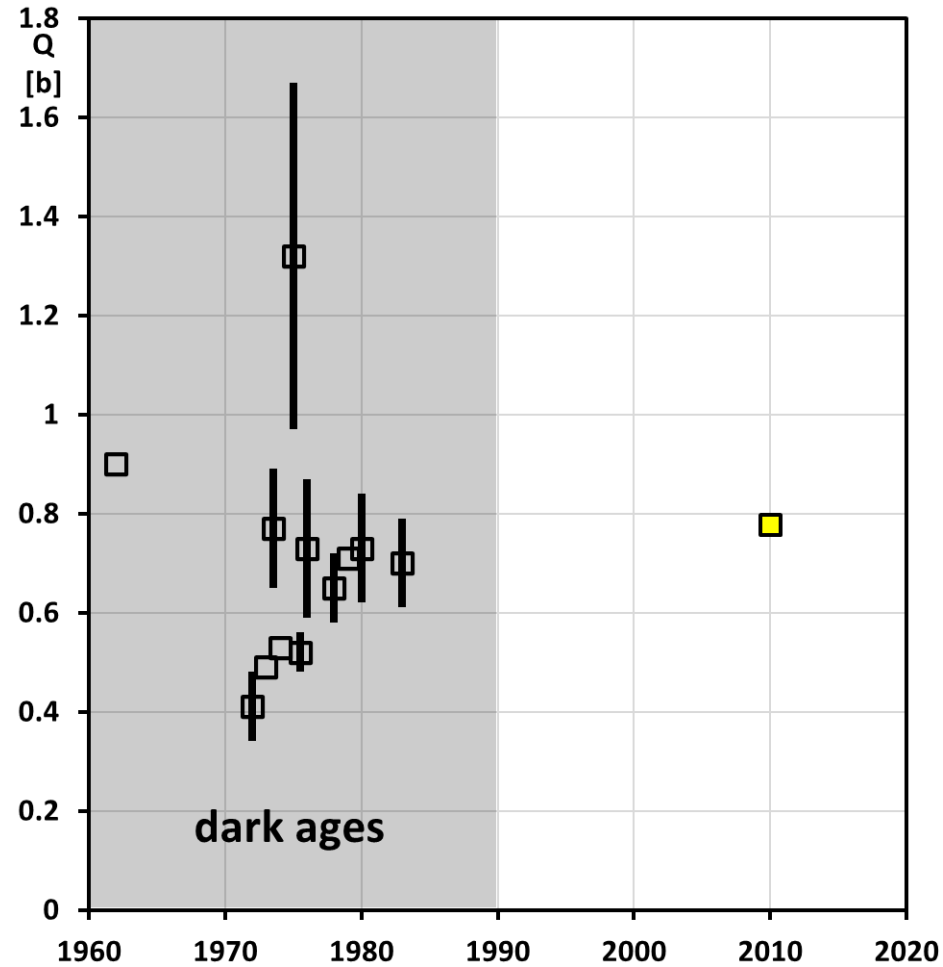
## The problem cases

Cu	Zn IS640	Ga	Ge	As	Se	Br	Kr	Rb	Sr
Ag	Cd IS640	In	Sn IS673	Sb	Te	I	Xe	Cs	Ba
Au	Hg IS640	Tl	Pb IS703	Bi	Po	At	Rn	Fr	Ra

## History of Q for $^{111}\text{Cd } 5/2^+$



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Hyperfine Interact (2010) 198:133–137

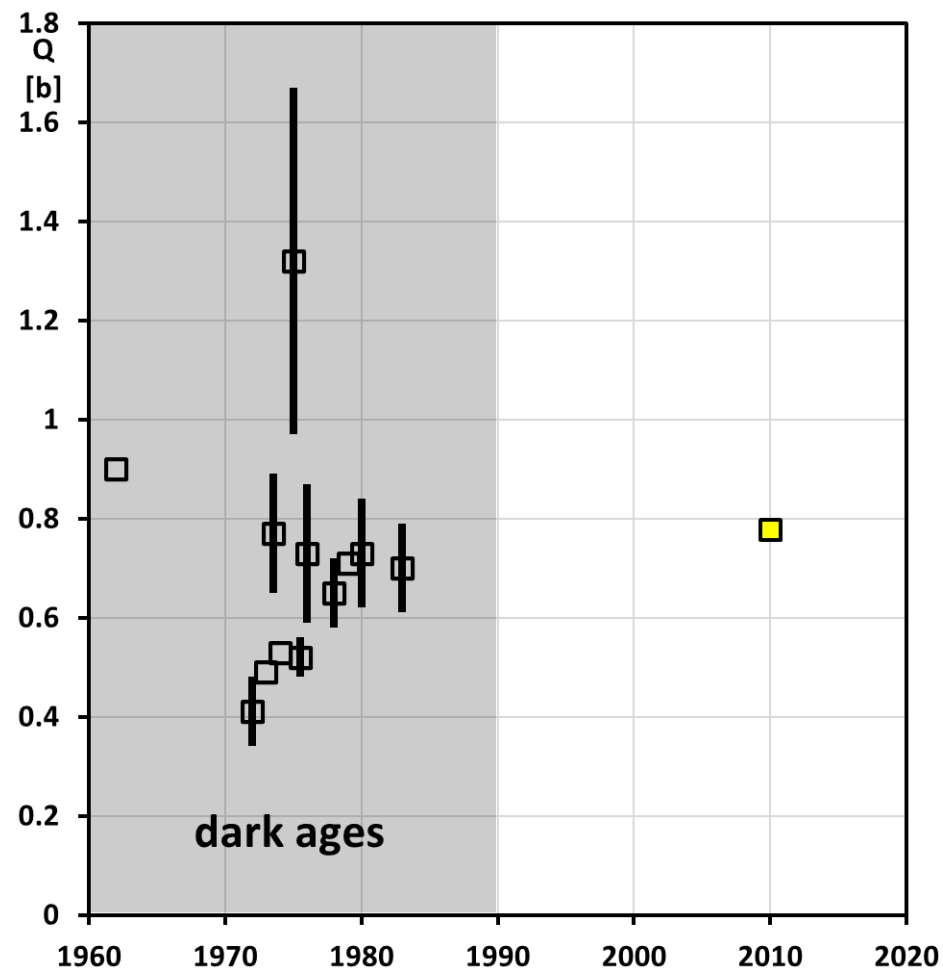
### The quadrupole moments of Zn and Cd isotopes—an update

H. Haas · J. G. Correia

Standard DFT



## History of Q for $^{111}\text{Cd } 5/2^+$



Hyperfine Interact (2010) 198:133–137

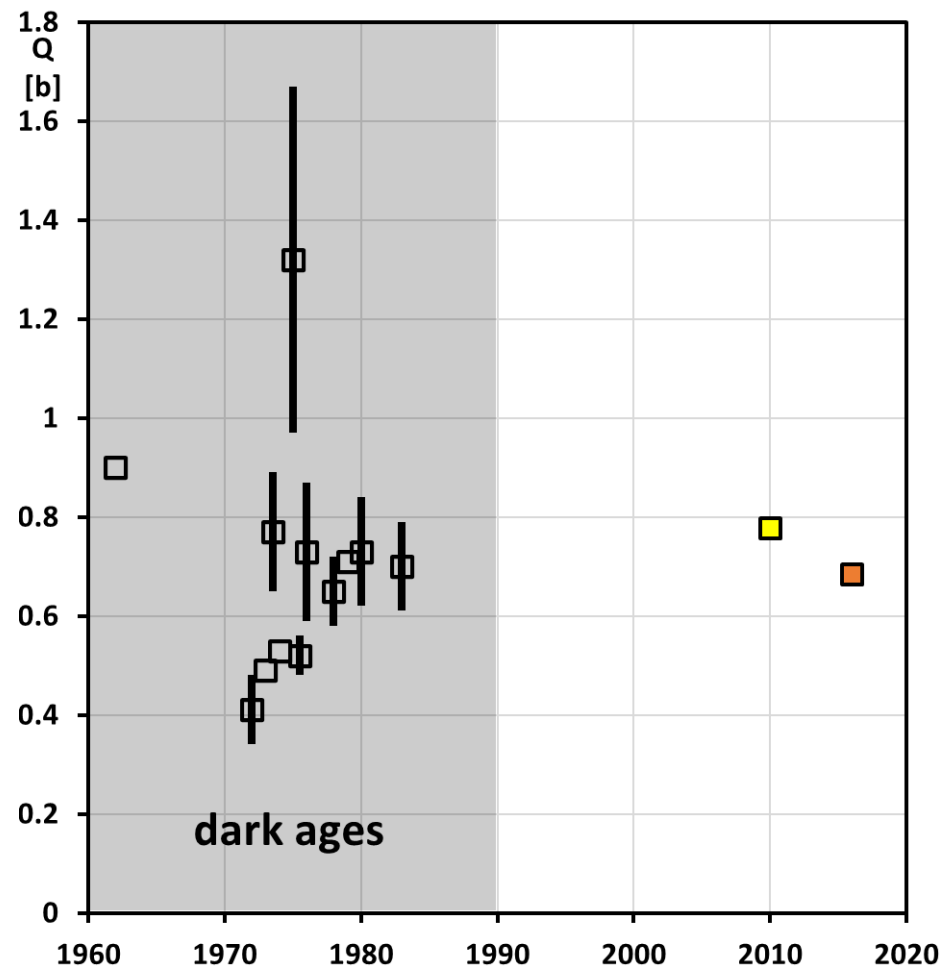
### The quadrupole moments of Zn and Cd isotopes—an update

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Standard DFT

**But: DFT is not really a theory,  
just a technique, so try another one!**

## History of Q for $^{111}\text{Cd } 5/2^+$



Hyperfine Interact (2010) 198:133–137

### The quadrupole moments of Zn and Cd isotopes—an update

H. Haas · J. G. Correia

Standard DFT

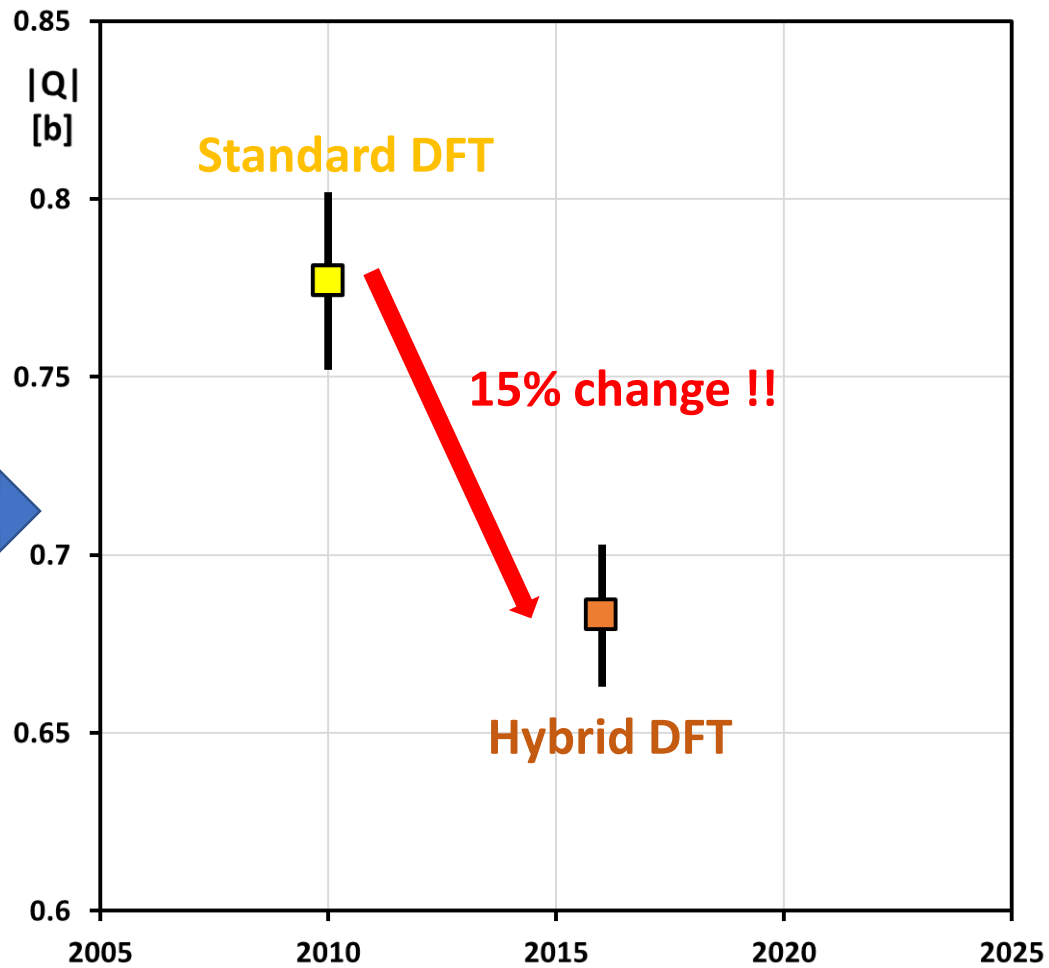
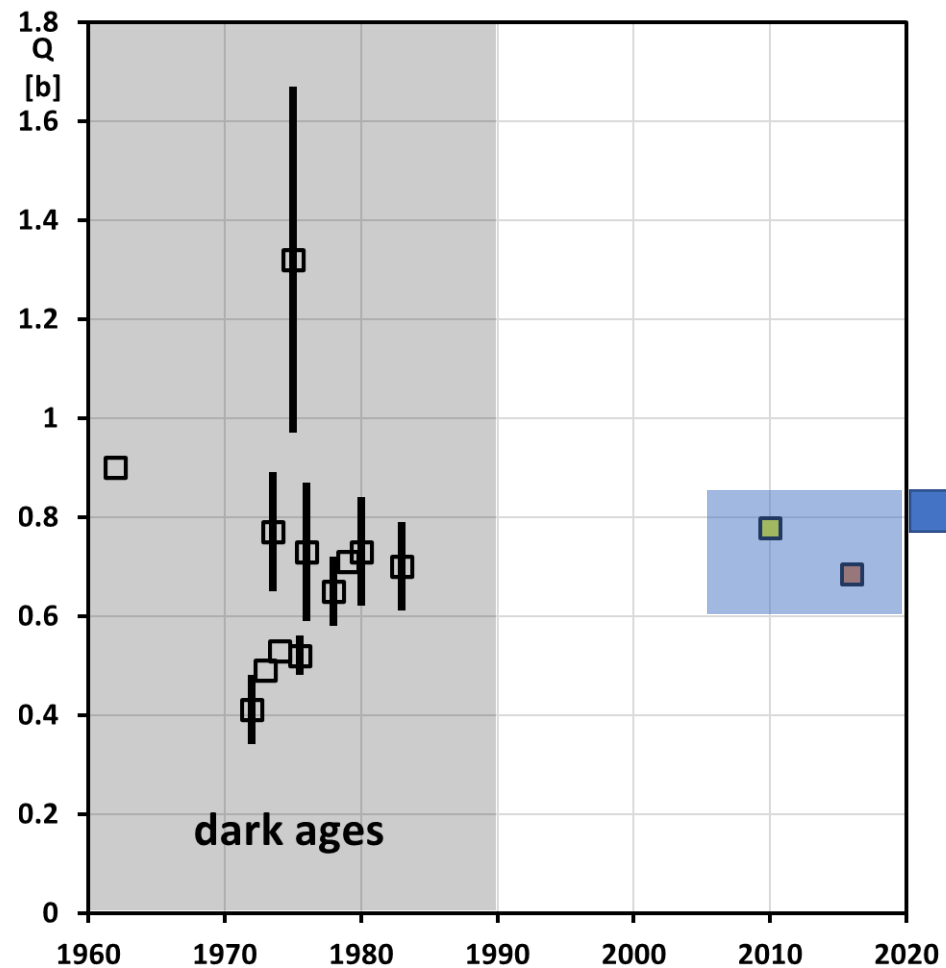
Hyperfine Interact (2016) 237:115

### The quadrupole moments of Cd and Zn isotopes - an apology

H. Haas<sup>1,4</sup>  · M. B. Barbosa<sup>2</sup> · J. G. Correia<sup>3,4</sup>

Hybrid DFT

## Detail of Q for $^{111}\text{Cd } 5/2^+$



## What can we do better?

Calculate the efg in a simple molecule  $\text{Cd}(\text{CH}_3)_2$  with quantum chemistry techniques and extract Q for  $^{111}\text{Cd } 5/2^+$ , using a 50 years old PAC result (in molecular solid)

EPL, 117 (2017) 62001

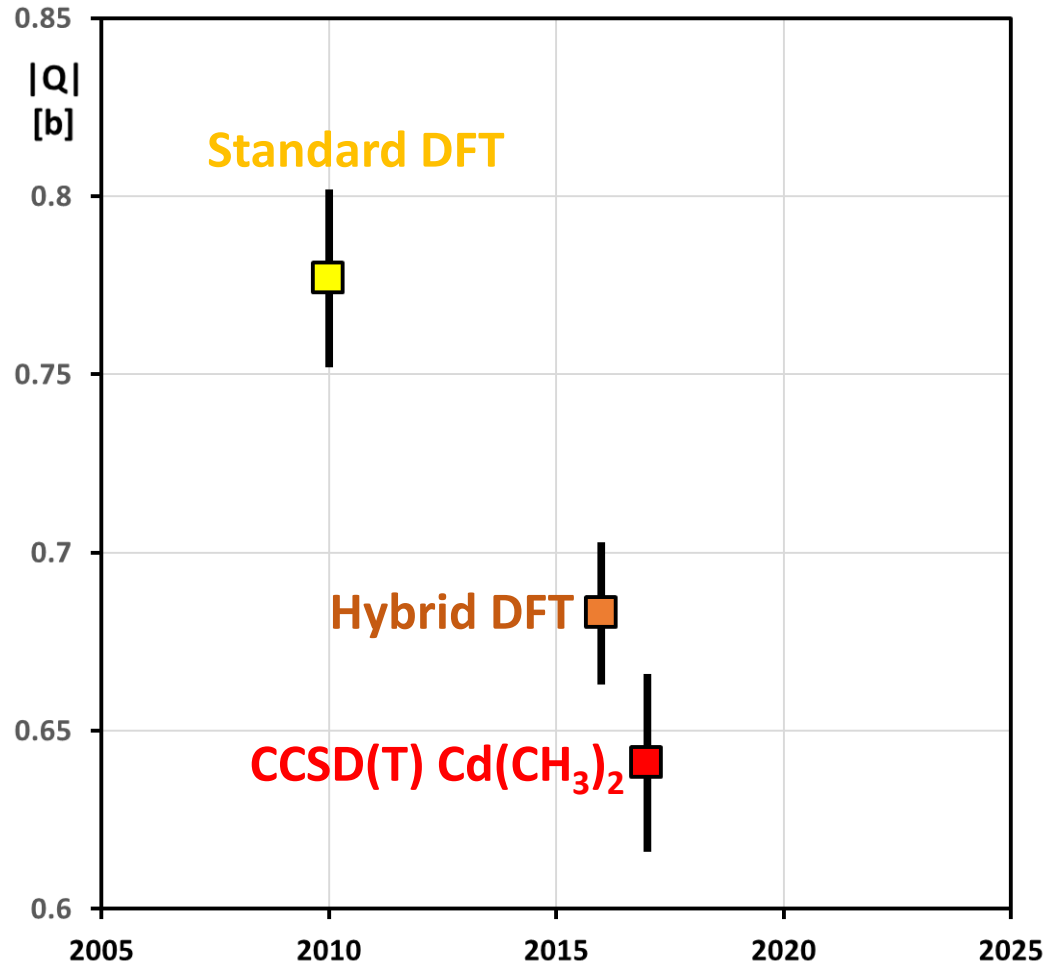
**Quadrupole moments of Cd and Zn nuclei: When solid-state, molecular, atomic, and nuclear theory meet**

H. HAAS<sup>1,5</sup>, S. P. A. SAUER<sup>2</sup>, L. HEMMINGSEN<sup>2</sup>, V. KELLÖ<sup>3</sup> and P. W. ZHAO<sup>4</sup>

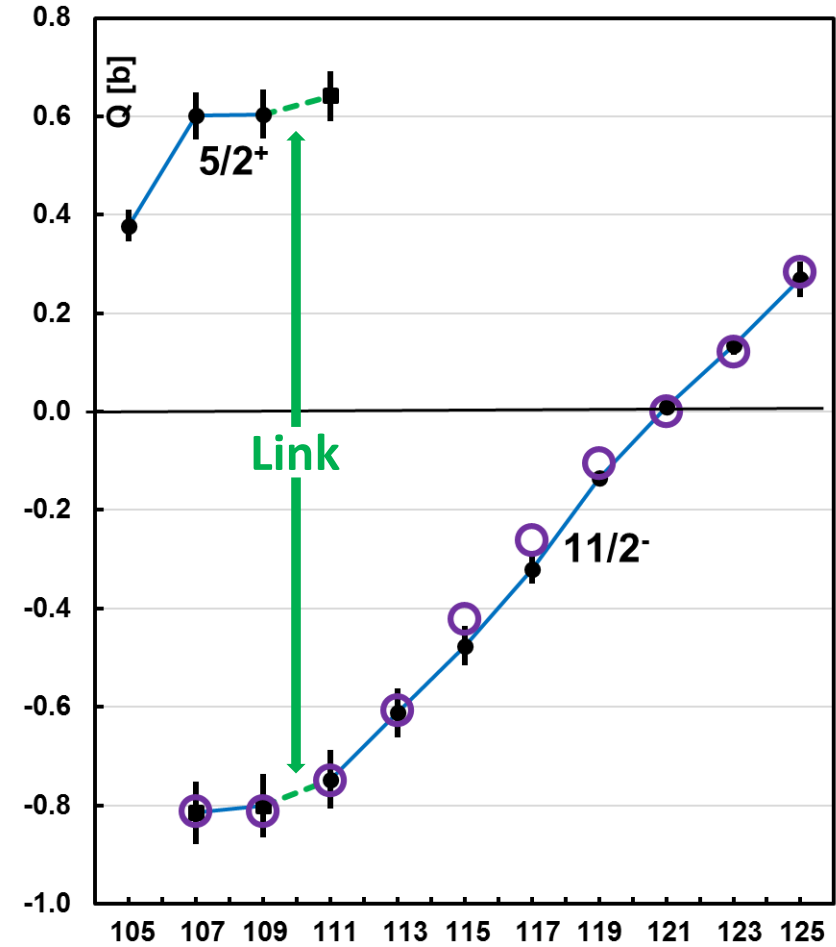
Extended the series of Q for  $11/2^-$  states in Cd by combining ISOLDE laser spectroscopy results with old PAC and PAD data

Confirmed the saturation of Q at  $^{109}\text{Cd}$  predicted by nuclear covariant density functional calculations

## Result: $Q$ for $^{111}\text{Cd } 5/2^+$



## Nuclear theory comparison



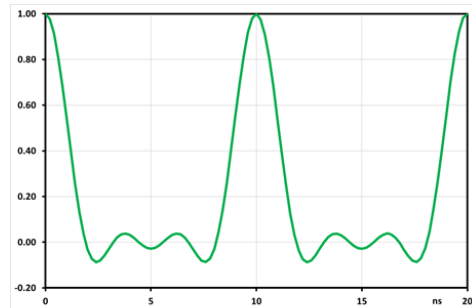
## Can we do better yet? Project IS640

- Measure the quadrupole interaction in some free Cd (and Hg) molecules in the gas state by PAC
- Basic concept: In a linear molecule the efg ( $V_{zz}^{\text{mol}}$ ) is along the molecular axis
- The rotation axis J is always perpendicular to the molecular axis
- The efg component along J is then, independent of J:
- $$V_{zz}^{\text{rot}} = -1/2 V_{zz}^{\text{mol}}$$
- For large J the quantization should be fully along J, leading to a splitting frequency independent of J !
- Our 50 years old idea, but early experiments (Berkeley, Bonn) in the 1970s have failed

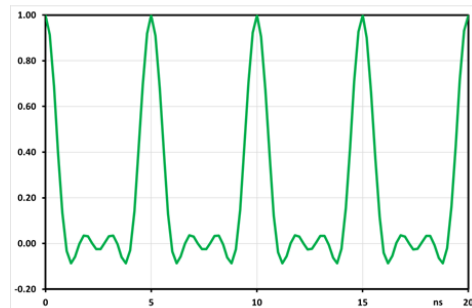
# Test of concept with $^{199}\text{Hg } 5/2^-$

What  $R(t)$  could we get ?

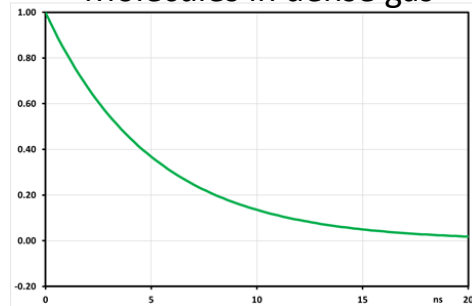
Free molecules in gas



Molecules in solid



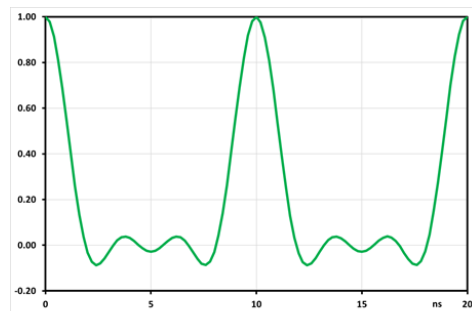
Molecules in dense gas



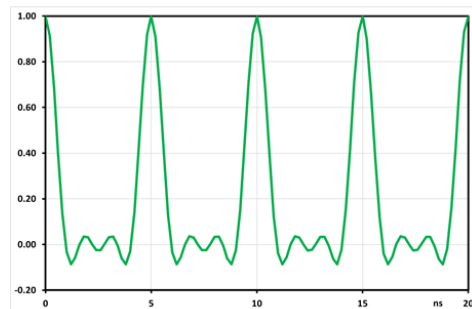
# Test of concept with $^{199}\text{Hg } 5/2^-$

What  $R(t)$  could we get ?

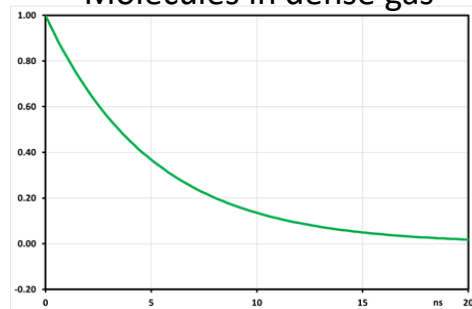
Free molecules in gas



Molecules in solid

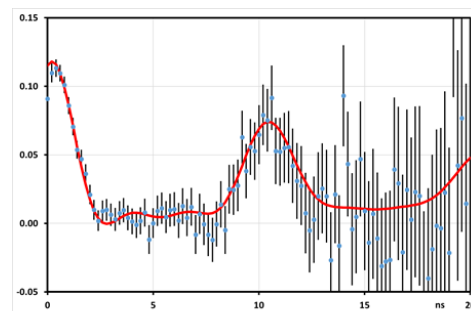


Molecules in dense gas

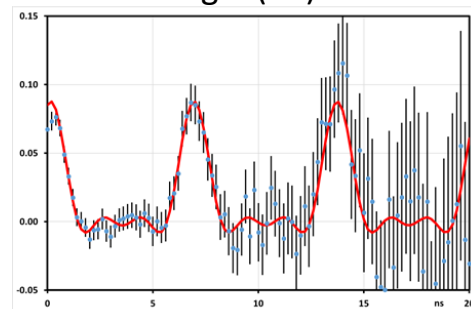


What  $R(t)$  did we see ?

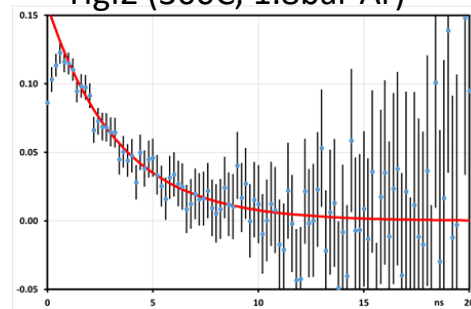
HgI2 (300C)



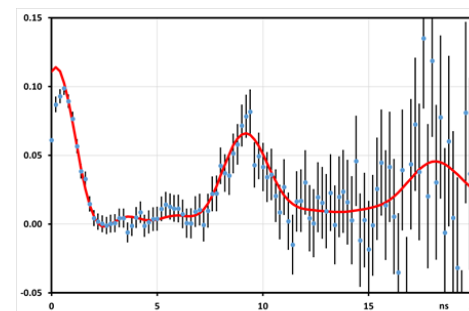
HgI2 (RT)



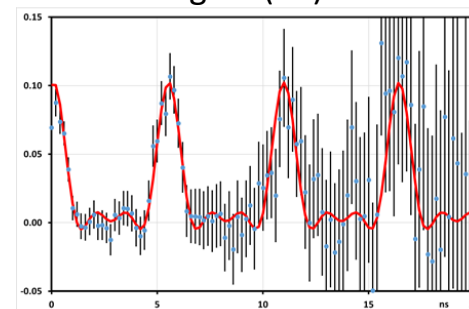
HgI2 (300C, 1.8bar Ar)



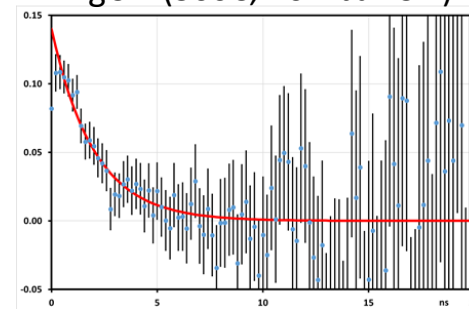
HgCl2 (300C, 2mbar Cl2)



HgCl2 (RT)



HgCl2 (300C, 40mbar Cl2)

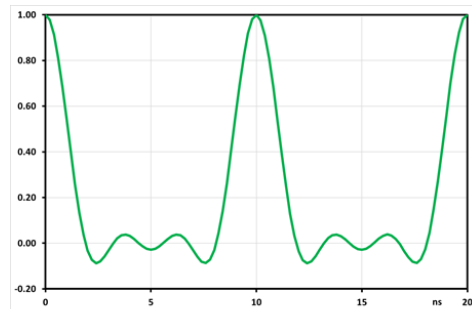




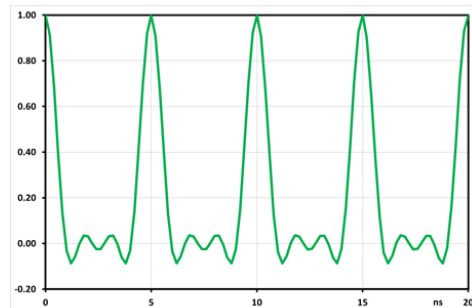
# Test of concept with $^{199}\text{Hg } 5/2^-$

What  $R(t)$  could we get ?

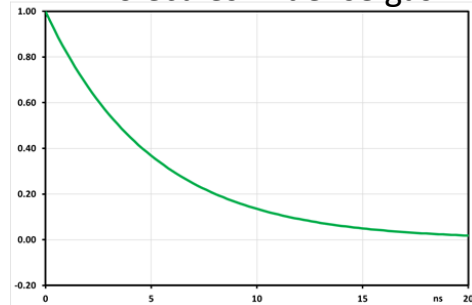
Free molecules in gas



Molecules in solid

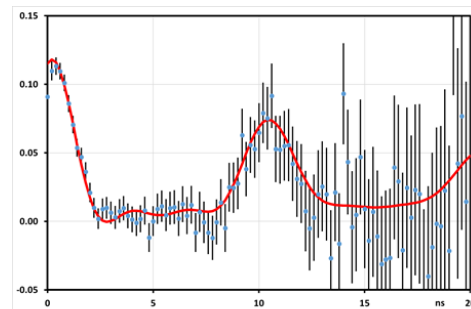


Molecules in dense gas

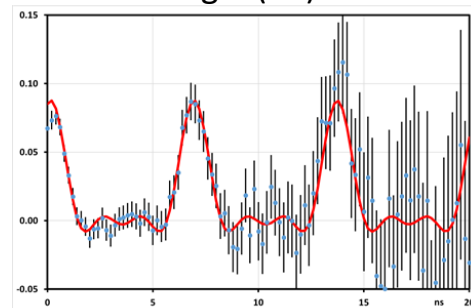


What  $R(t)$  did we see ?

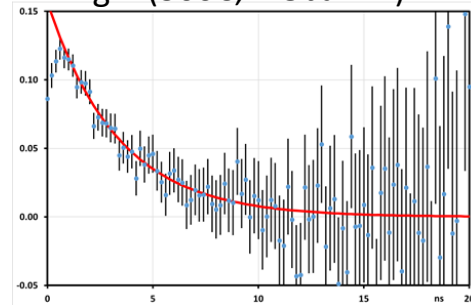
HgI2 (300C)



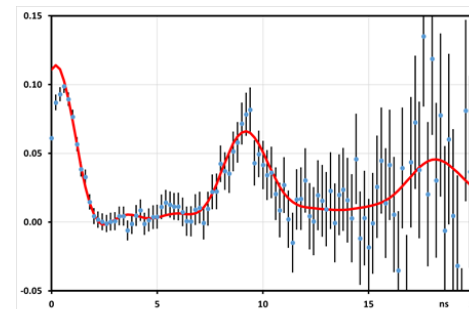
HgI2 (RT)



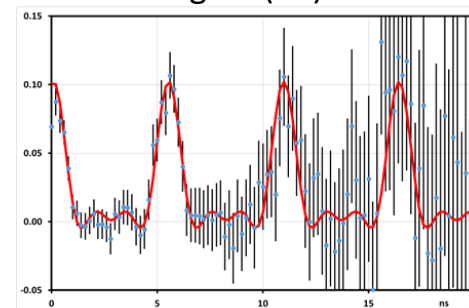
HgI2 (300C, 1.8bar Ar)



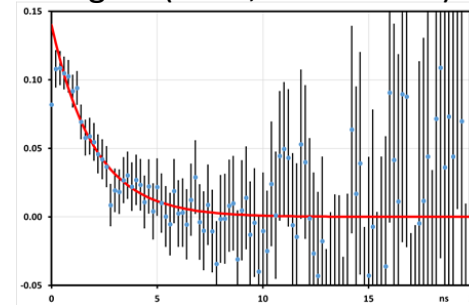
HgCl2 (300C, 2mbar Cl2)



HgCl2 (RT)



HgCl2 (300C, 40mbar Cl2)



**Results:**

**Idea confirmed**

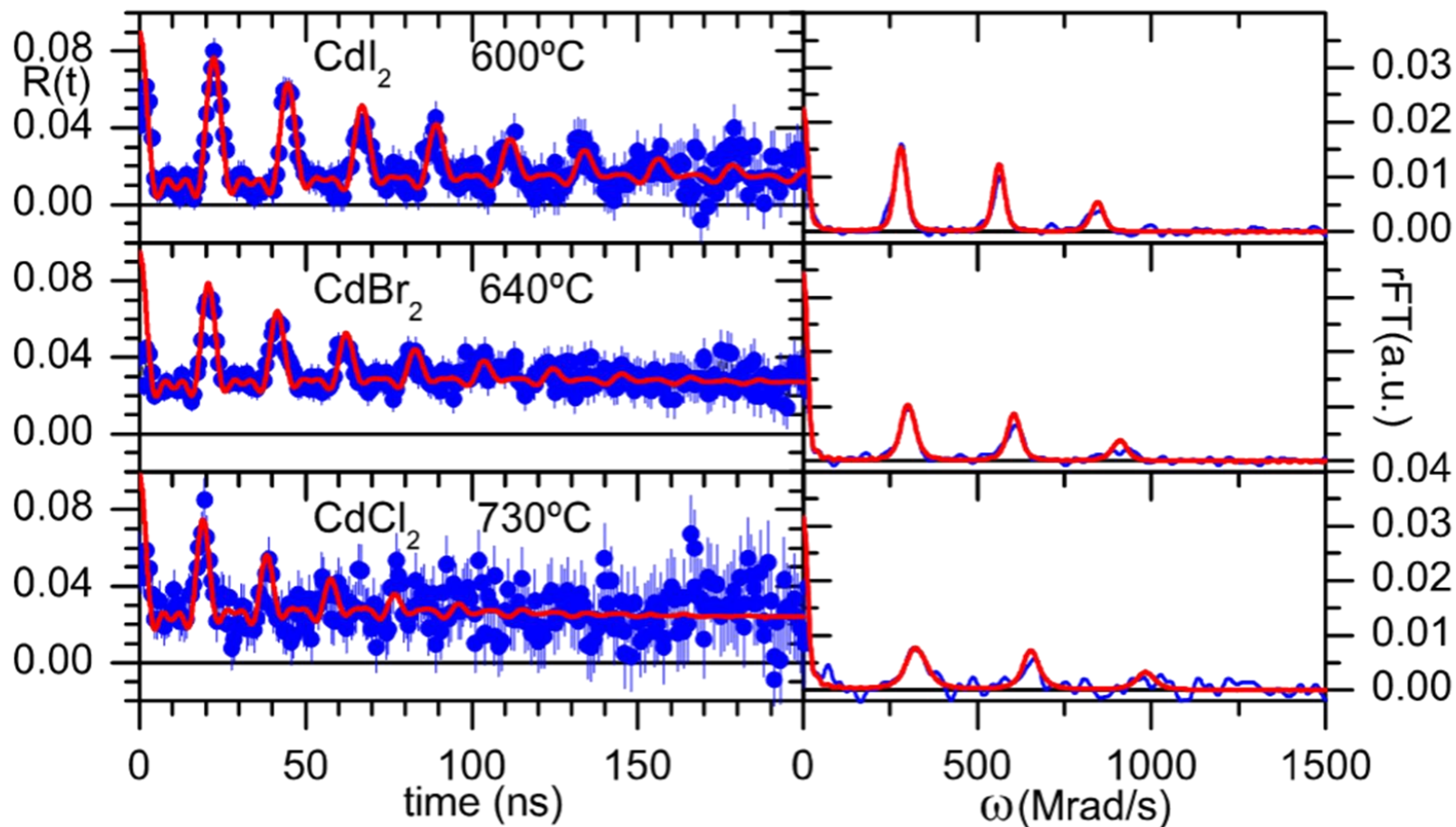
**Known Q  
redetermined**

**Effect of inter-  
molecular bond  
measured**

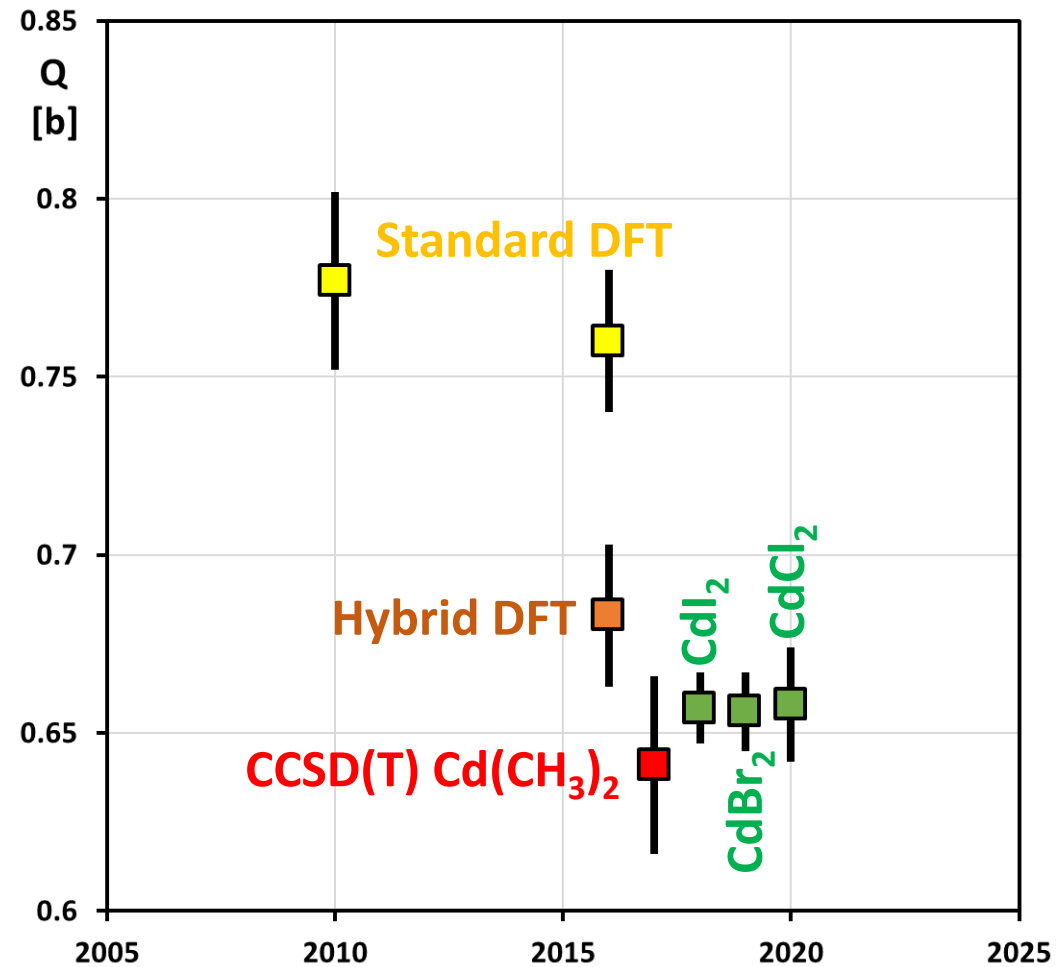
PHYSICAL REVIEW LETTERS **126**, 103001 (2021)

## Free Molecule Studies by Perturbed $\gamma$ - $\gamma$ Angular Correlation: A New Path to Accurate Nuclear Quadrupole Moments

Heinz Haas<sup>1,2</sup>, Jens Röder<sup>1,2</sup>, Joao G. Correia<sup>3,2</sup>, J. Schell<sup>4,2</sup>, Abel S. Fenta<sup>1</sup>, Reiner Vianden,<sup>5</sup>  
 Emil M. H. Larsen<sup>6</sup>, Patrick A. Aggelund,<sup>6</sup> Rasmus Fromsejer,<sup>6</sup> Lars B. S. Hemmingsen<sup>6</sup>,  
 Stephan P. A. Sauer<sup>6</sup>, Doru C. Lupascu,<sup>4</sup> and Vitor S. Amaral<sup>1</sup>

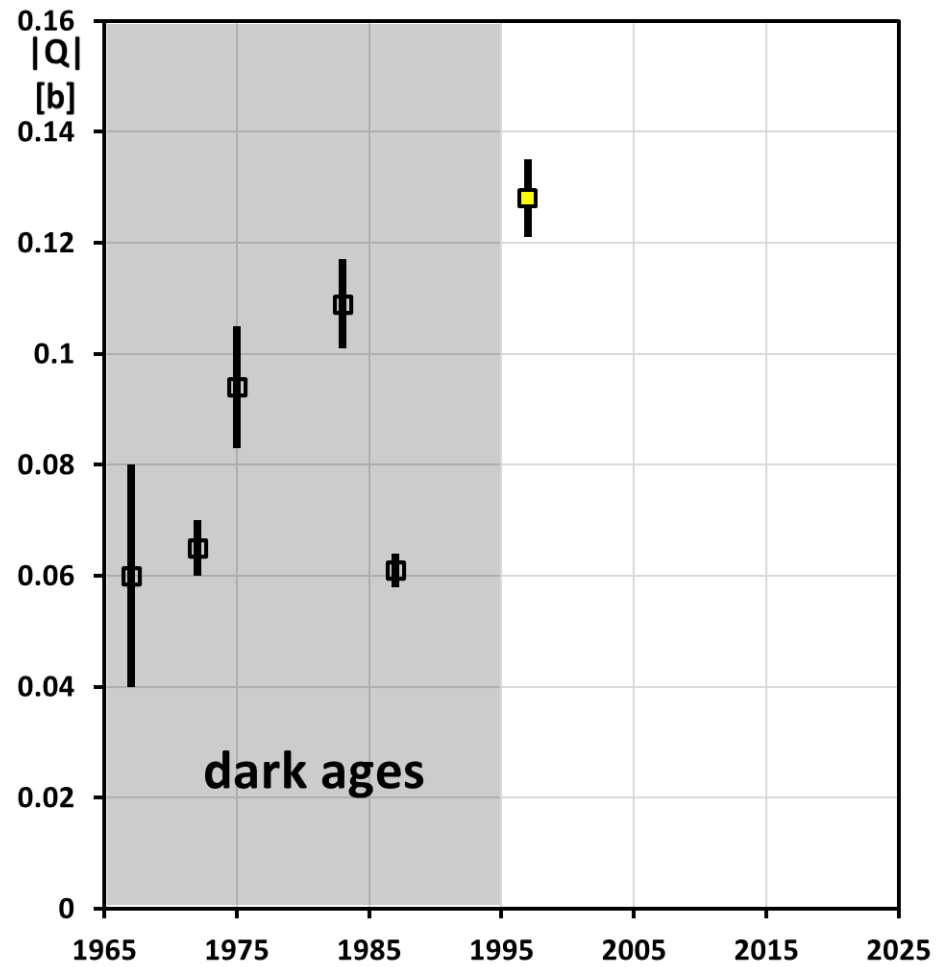


# IS640: Final results for Q of $^{111}\text{Cd } 5/2^+$

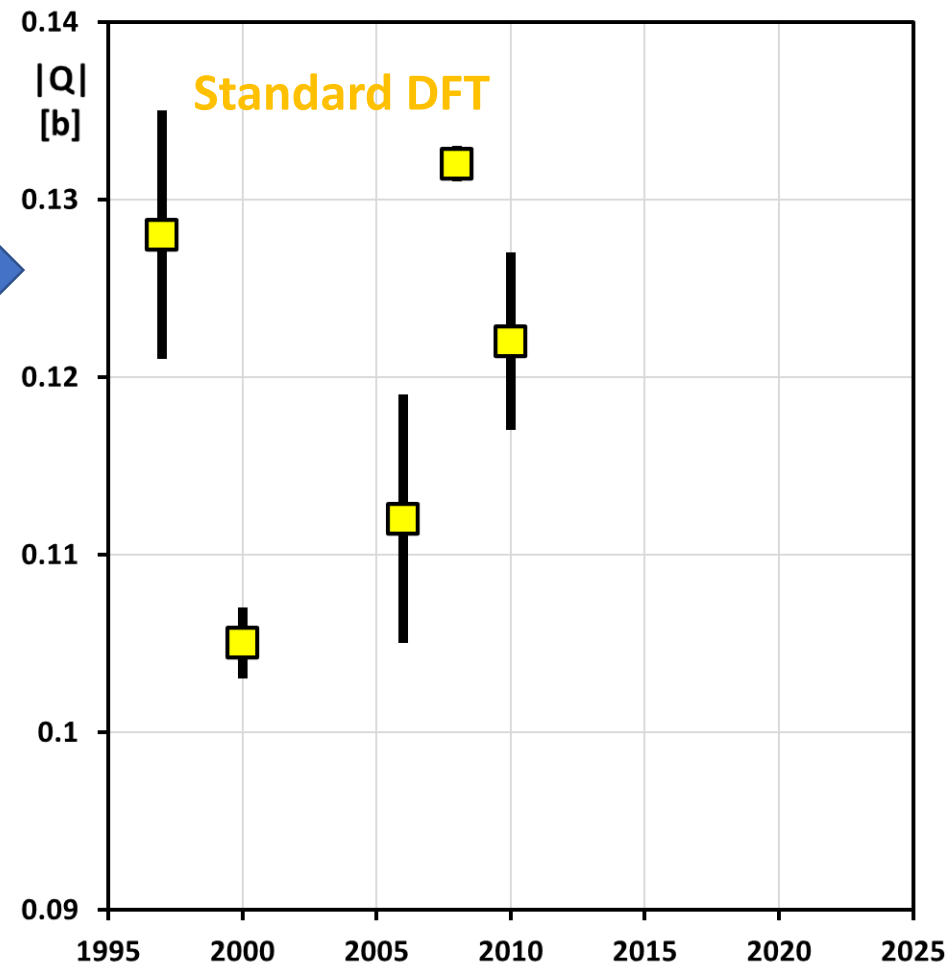
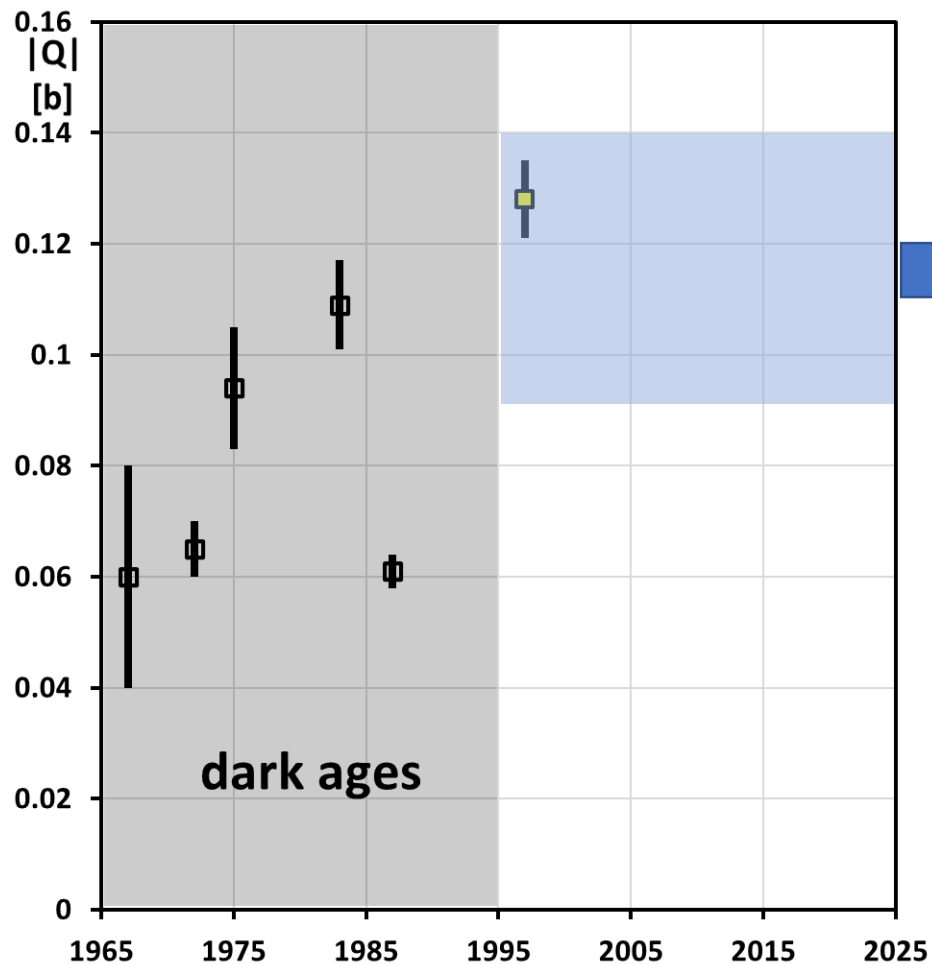


Accuracy  
achieved  
1.2%

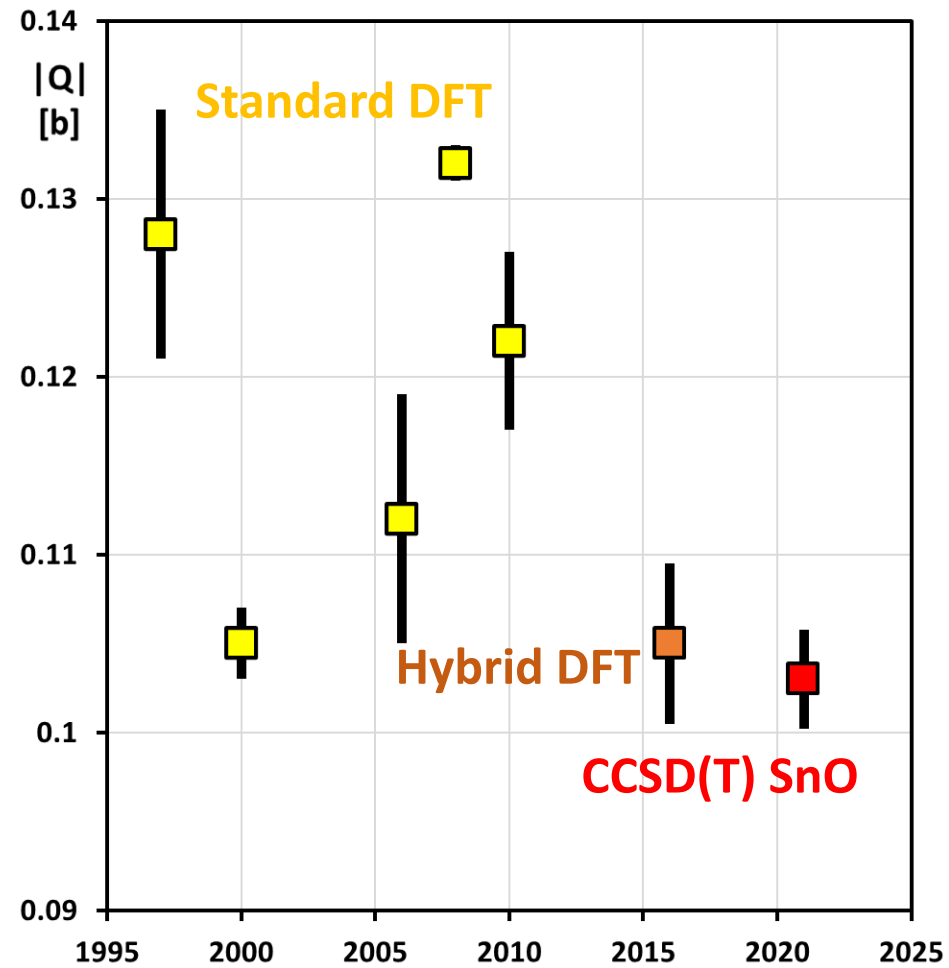
## History of Q for $^{119}\text{Sn } 3/2^+$



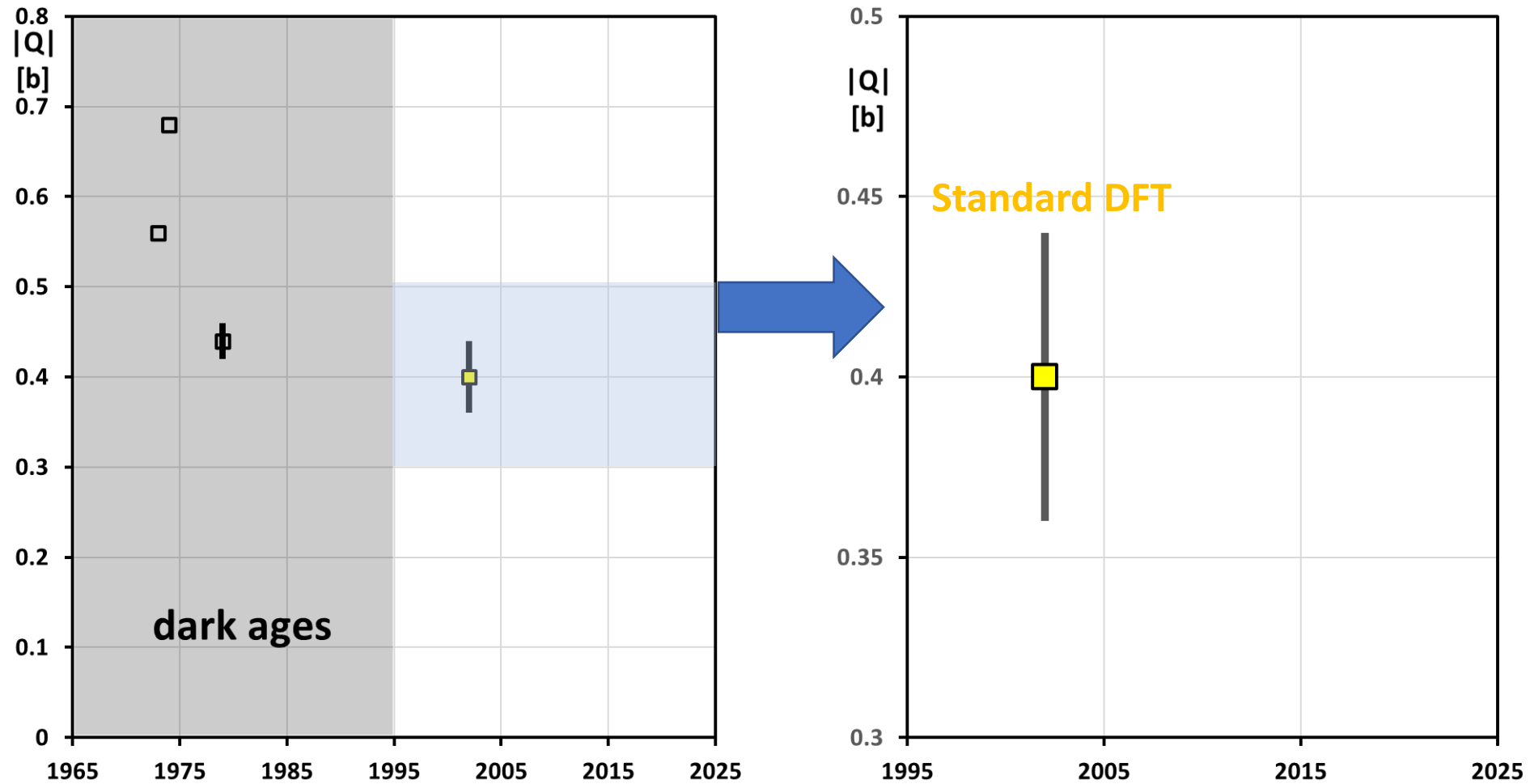
## Detail of Q for $^{119}\text{Sn } 3/2^+$



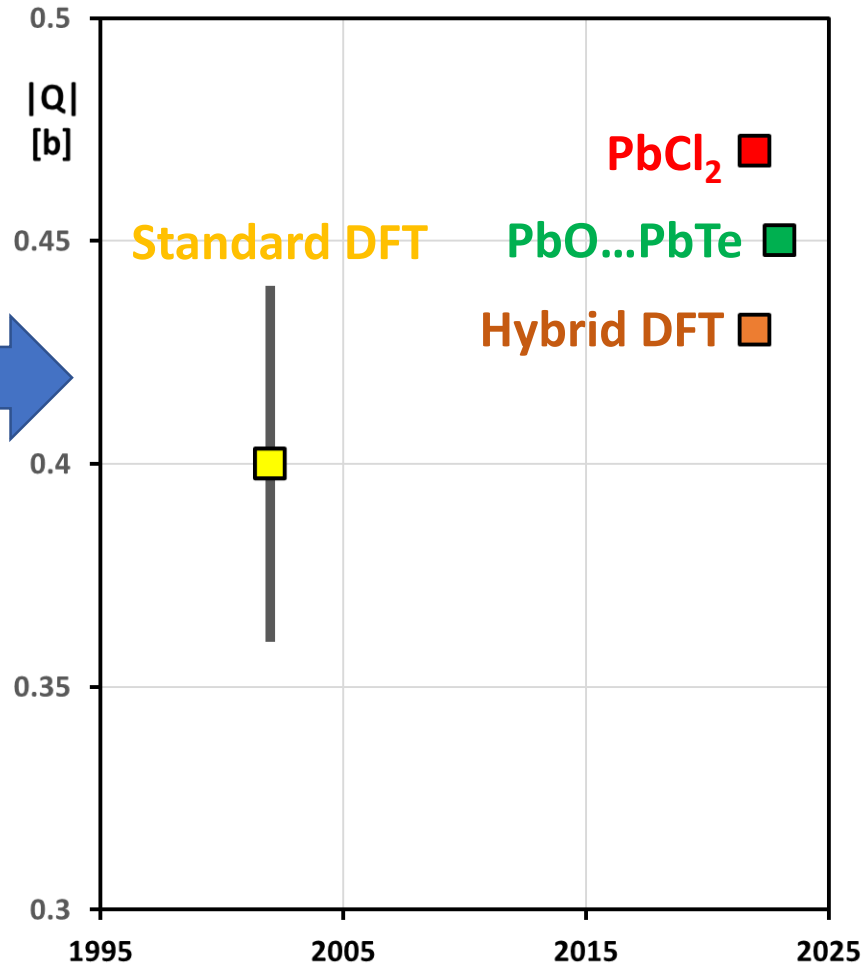
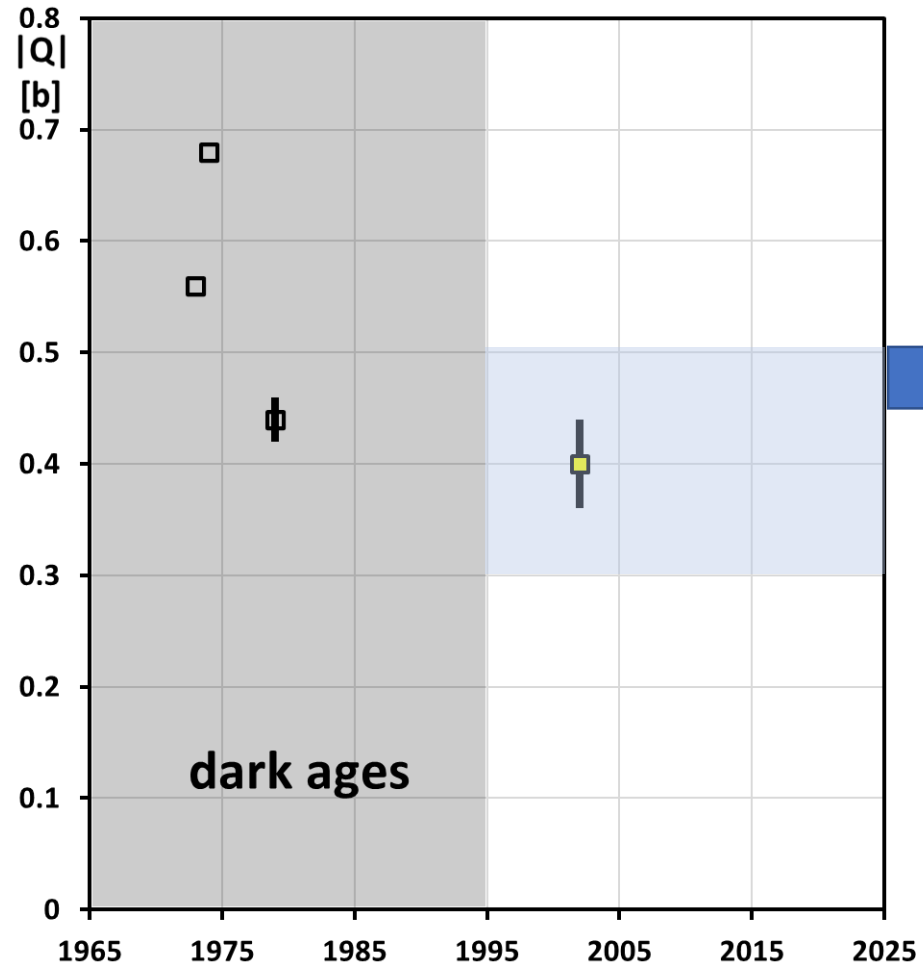
## IS673: Results for Q of $^{119}\text{Sn } 3/2^+$ (preliminary)



## History of Q for $^{204}\text{Pb } 4^+$



# Project IS703 for Q of $^{204}\text{Pb } 4^+$





# Project IS703 for Q of $^{204}\text{Pb } 4^+$

