

NPointFunctions: a calculator of amplitudes and observables in FlexibleSUSY

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KERN- UND
TEILCHENPHYSIK



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UNIVERSITÄT
DRESDEN

Overview

- Motivation
- What is FlexibleSUSY?
- What is NPointFunctions?
- Some applications

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- now → Workflow of a phenomenologist:
- 1) define/get \mathcal{L}
 - 2) get vertices, masses, RGE
 - 3) calculate observables
 - 4) make parameter scans

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SARAH

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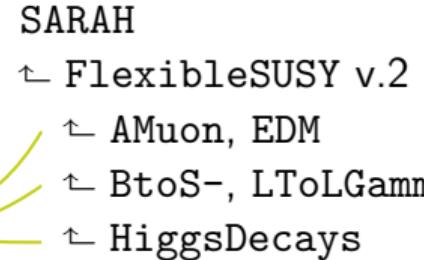
SARAH
↑ FlexibleSUSY

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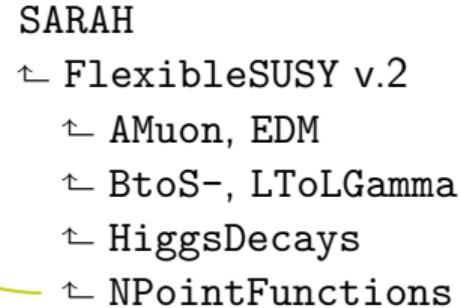


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- Motivation

- What is FlexibleSUSY?  A spectrum generator - generator

- What is NPointFunctions?

- Some applications

Workflow of a phenomenologist:

- 1) define/get \mathcal{L}_i
- 2) get vertices, masses, RGE
- 3) calculate observables i
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SARAH

- ↑ FlexibleSUSY v.2
- ↑ AMuon, EDM
- ↑ BtoS-, LToLGamma
- ↑ HiggsDecays
- ↑ NPointFunctions

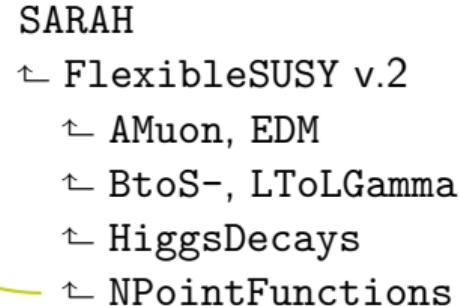
Overview

- Motivation

- What is FlexibleSUSY?

Workflow of a phenomenologist:

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A spectrum generator - generator

- What is NPointFunctions? later

A calculator of amplitudes and observables

- Some applications

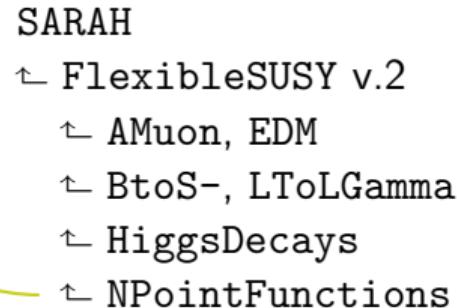
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A spectrum generator - generator

- What is NPointFunctions?

A calculator of amplitudes and observables **BRIEFLY**

- Some applications

Overview

- Motivation

- What is FlexibleSUSY?

A spectrum generator - generator

- What is NPointFunctions?

A calculator of amplitudes and observables **BRIEFLY**

- Some applications

later

MRSSM, leptoquarks*, Grimus-Neufeld model*

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i

| #1 | #2 | #3 | Mathematica code: |
|-----------------------------|--|---------------------------------------|--|
| MODEL.m model definition | parameters.m additional information | particles.m additional information | vertices masses 2-loop RGE EWSB |

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i  **1) create**
 - #1 MODEL.m model definition
 - #2 parameters.m additional information
 - #3 particles.m additional information
- Mathematica code:
- | |
|------------|
| vertices |
| masses |
| 2-loop RGE |
| EWSB |

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i  $\xrightarrow{1) \text{ create}}$ #1 #2 #3  $\xrightarrow{2) \text{ SARAH}}$ Mathematica code:

| | | |
|------------------|------------------------|------------------------|
| MODEL.m | parameters.m | particles.m |
| model definition | additional information | additional information |

vertices
masses
2-loop RGE
EWSB

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i  #1 #2 #3 

| MODEL.m | parameters.m | particles.m |
|------------------|------------------------|------------------------|
| model definition | additional information | additional information |

Mathematica code:
vertices
masses
2-loop RGE
EWSB

- Setup model  #1 #2
- | | |
|---------------------------------|---|
| FlexibleSUSY.m | LesHouches.in.MODEL |
| restrictions*, extra*, settings | numerical values for the input parameters |
- C++* code, which:
solves BVP*
finds mixings
finds masses
finds observables*

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i #1 #2 #3 Mathematica code:

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FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i $\xrightarrow{1) \text{ create}}$ #1 #2 #3 $\xrightarrow{2) \text{ SARAH}}$ Mathematica code:

| | | |
|------------------|------------------------|------------------------|
| MODEL.m | parameters.m | particles.m |
| model definition | additional information | additional information |

vertices
masses
2-loop RGE
EWSB
- Setup model $\xrightarrow{3) \text{ create}}$ #1 #2 $\xrightarrow{4) \text{ FlexibleSUSY}}$ C++* code, which:

| | |
|---------------------------------|---|
| FlexibleSUSY.m | LesHouches.in.MODEL |
| restrictions*, extra*, settings | numerical values for the input parameters |

solves BVP*
finds mixings
finds masses
finds observables*

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i #1 #2 #3 Mathematica code:

| | | |
|------------------|------------------------|------------------------|
| MODEL.m | parameters.m | particles.m |
| model definition | additional information | additional information |

vertices
masses
2-loop RGE
EWSB
 - Setup model #1 #2 C++* code, which:

| | |
|---------------------------------|---|
| FlexibleSUSY.m | LesHouches.in.MODEL |
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solves BVP*
finds mixings
finds masses
finds observables*
-
- The diagram illustrates the evolution of the scale Λ [GeV] along the horizontal axis. It is divided into three regions: SM (Standard Model), SUSYScale, and BSM (Beyond Standard Model). Three vertical tick marks on the axis are labeled LowScale, SUSYScale, and HighScale*. A double-headed red arrow labeled "RGE" spans from the LowScale mark to the HighScale* mark, indicating the range of the Renormalization Group Evolution. Brackets below the axis group these regions: "SM" covers the range from the origin to the LowScale mark; "RGE" covers the range from LowScale to HighScale*; and "BSM" covers the range from HighScale* to the end of the axis.

FlexibleSUSY? [1406.2319], [1710.03760] The end-user side.

- Define \mathcal{L}_i #1 #2 #3 Mathematica code:

| MODEL.m | parameters.m | particles.m |
|------------------|------------------------|------------------------|
| model definition | additional information | additional information |

- Setup model #1 #2 C++* code, which:

| FlexibleSUSY.m | LesHouches.in.MODEL |
|---------------------------------|---|
| restrictions*, extra*, settings | numerical values for the input parameters |

A nice place
for something
new!

5) ...

solves BVP*
finds mixings
finds masses
finds observables*

```
FlexibleSUSYObservable`BrLTo3L[Fe@2 -> {Fe@1, Fe@1, bar@Fe@1}, Scalars, 1]
```

NPointFunctions? [soon] The end-user side.

- Setup observable_i

#1

settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

- 1) Mathematica* code,
- 2) C++ code, which:
 - adds*, new input blocks
 - evaluates observable_i
 - evaluates Wilson coefficients

NPointFunctions? [soon] The end-user side.

5) configure

- Setup observable $_i$ → #1

```
settings.m*
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

- 1) Mathematica* code,
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NPointFunctions?^[soon] The end-user side.

- Setup observable_i → #1 → 6) NPointFunctions

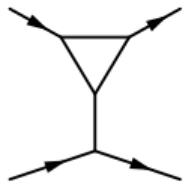
settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

- 1) Mathematica* code,
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NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → 5) configure → #1 → 6) NPointFunctions



settings.m*

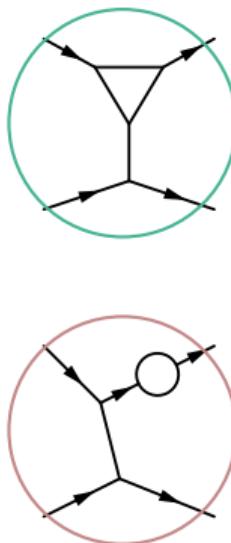
```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

- 1) Mathematica* code,
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 - evaluates Wilson coefficients

Example: PRELIMINARY

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → #1 → 6) NPointFunctions



settings.m*

include

exclude

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

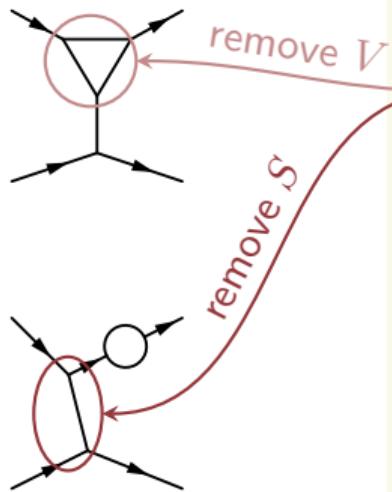
- 1) Mathematica* code,
- 2) C++ code, which:
 - adds*, new input blocks
 - evaluates observable $_i$
 - evaluates Wilson coefficients

Example: PRELIMINARY

```
topologies[1] = {
Scalars -> triangleT,
Vectors -> outSelfT, ...}
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → 5) configure → #1 → 6) NPointFunctions



settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

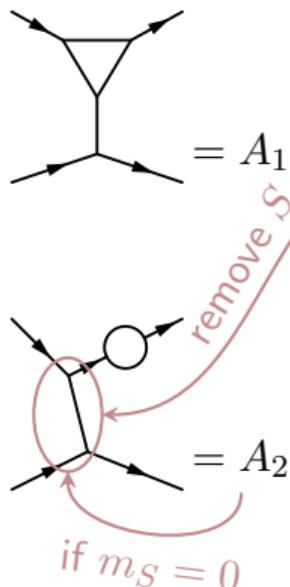
- 1) Mathematica* code,
- 2) C++ code, which:
 - adds*, new input blocks
 - evaluates observable $_i$
 - evaluates Wilson coefficients

Example: PRELIMINARY

```
diagrams[1, Plus] = {
  Scalars -> {
    triangleT -> {"No V",
      FreeQ[LoopFields@##,
      FeynArts`V]&}, ...}
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → #1 → 6) NPointFunctions



settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

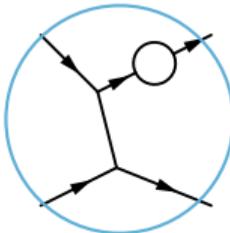
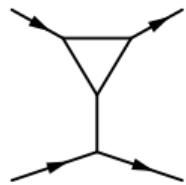
- 1) Mathematica* code,
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 - evaluates Wilson coefficients

Example: PRELIMINARY

```
diagrams[1, Minus] = {
  Vectors -> {
    outSelfT -> {"No S",
      FreeQ[#, InternalMass[
        FeynArts`S, 5] -> 0]&}, ...}
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → 5) configure → #1 → 6) NPointFunctions



use MS

settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

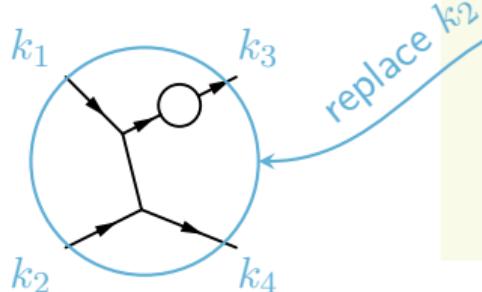
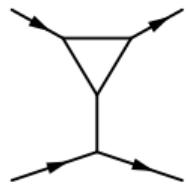
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 - evaluates Wilson coefficients

Example: PRELIMINARY

```
regularization[1] = {
triangleT -> 4,
outSelfT -> D,...
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → #1 → 6) NPointFunctions



settings.m*

topologies [LOOPS]
diagrams [LOOPS, TYPE]
amplitudes [LOOPS, TYPE]
regularization [LOOPS]

momenta [LOOPS] →
order []
sum [LOOPS]
chains [LOOPS]
mass [LOOPS]

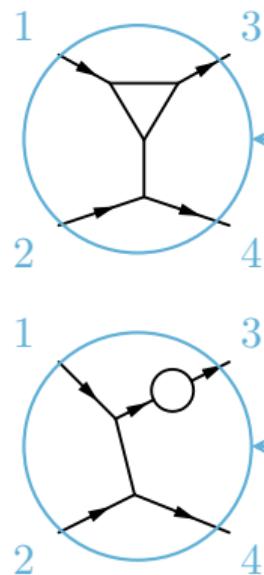
- 1) Mathematica* code,
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Example: PRELIMINARY

```
momenta[1] = {  
    triangleT -> 4,  
    outSelfT -> 2,...
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → 5) configure → #1 → 6) NPointFunctions



settings.m*

topologies [LOOPS]
diagrams [LOOPS, TYPE]
amplitudes [LOOPS, TYPE]
regularization [LOOPS]
momenta [LOOPS]
order [] ←
sum [LOOPS]
chains [LOOPS]
mass [LOOPS]

use order
like 1243

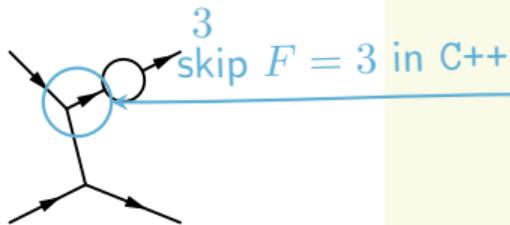
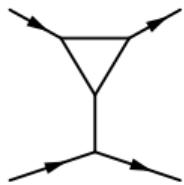
- 1) Mathematica* code,
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 - evaluates Wilson coefficients

Example: PRELIMINARY

```
order [] = {1, 2, 4, 3};
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → 5) configure → #1 → 6) NPointFunctions



settings.m*

topologies [LOOPS]
diagrams [LOOPS, TYPE]
amplitudes [LOOPS, TYPE]
regularization [LOOPS]
momenta [LOOPS]
order []
sum [LOOPS]
chains [LOOPS]
mass [LOOPS]

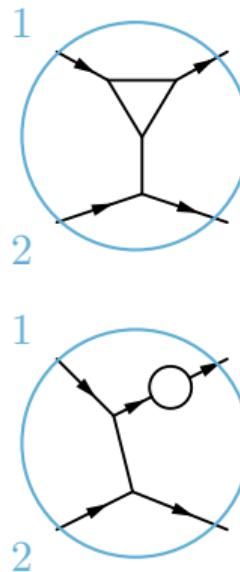
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 - evaluates Wilson coefficients

Example: PRELIMINARY

```
sum[1] = {  
  outSelfT -> {"Unsame"  
  {6, Field[#3, 3]&}}},...
```

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → #1 → 5) configure → 6) NPointFunctions



settings.m*

topologies [LOOPS]
diagrams [LOOPS, TYPE]
amplitudes [LOOPS, TYPE]
regularization [LOOPS]
momenta [LOOPS]
order []
sum [LOOPS]
chains [LOOPS]
mass [LOOPS]

modify spinor
chains

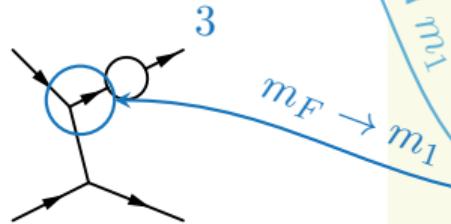
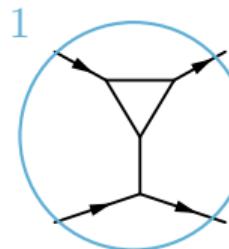
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Example: PRELIMINARY

```
chains[1] = {  
    ExceptLoops -> {  
        1[k[4|2], __] -> 0, ...
```

NPointFunctions? [soon] The end-user side.

- Setup observable i → #1 → 5) configure → 6) NPointFunctions



settings.m*

```
topologies [LOOPS]
diagrams [LOOPS, TYPE]
amplitudes [LOOPS, TYPE]
regularization [LOOPS]
momenta [LOOPS]
order []
sum [LOOPS]
chains [LOOPS]
mass [LOOPS]
```

- 1) Mathematica* code,
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 - adds*, new input blocks
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 - evaluates Wilson coefficients

Example: PRELIMINARY

```
mass [1] = {
triangleT -> {"Hold it"
{Hold, ExternalMass [1]}},
...}
```

NPointFunctions?^[soon] The end-user side.

- Setup observable_i → #1 → 6) NPointFunctions

settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

- 1) Mathematica* code,
- 2) C++ code, which:
 - adds*, new input blocks
 - evaluates observable_i
 - evaluates Wilson coefficients

- Main* dependencies

FeynArts
FormCalc
ColorMath

NPointFunctions? [soon] The end-user side.

- Setup observable $_i$ → #1 → 6) NPointFunctions

settings.m*

```
topologies[LOOPS]
diagrams[LOOPS, TYPE]
amplitudes[LOOPS, TYPE]
regularization[LOOPS]
momenta[LOOPS]
order[]
sum[LOOPS]
chains[LOOPS]
mass[LOOPS]
```

- 1) Mathematica* code,
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- Main* dependencies

FeynArts

- Implemented*

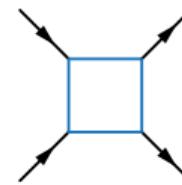
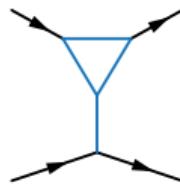
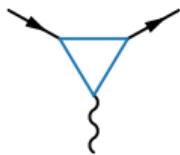
$$l_i \rightarrow l_j l_k l_k^C$$
$$l_i \rightarrow l_j \text{ conversion}$$

connected to $l_i \rightarrow l_j \gamma$

FormCalc

ColorMath

LFV processes



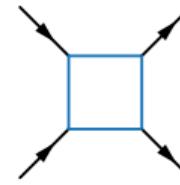
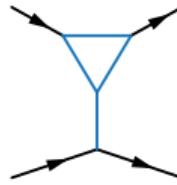
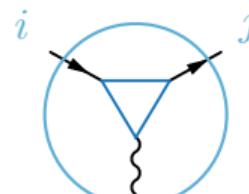
$$\mathcal{L}_{\text{LEFT}} \ni m_\mu C_X^{\mathcal{D}} [\bar{e} \sigma^{\mu\nu} P_X \mu] F_{\mu\nu} + C_{XY,f}^{\mathcal{F}} [\bar{e} \Gamma_X \mu] [\bar{f} \Gamma_Y f]$$

$$\Gamma_{\mu \rightarrow e\gamma}^{[\text{any}]} \propto \sum |C^{\mathcal{D}}|^2$$

$$\Gamma_{\mu \rightarrow 3e}^{[\text{hep-ph/9510309}]} \propto 0.006 \cdot \Gamma_{\mu \rightarrow e\gamma} + \sum (\text{Re } C_e^{\mathcal{V}} C^{\mathcal{D}*} + |C_e^{\mathcal{S},\mathcal{V}}|^2)$$

$$\omega_{\mu-e}^{[\text{hep-ph/0203110}]} \propto \sum |DC_X^{\mathcal{D}} - \sum (S^{(N)} g^{\mathcal{S}} + V^{(N)} g^{\mathcal{V}})|^2$$

LFV processes



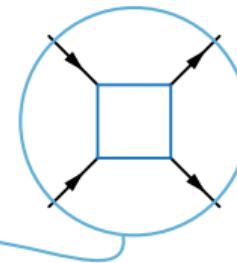
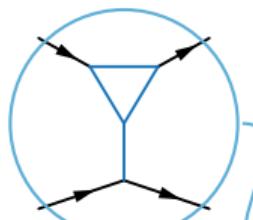
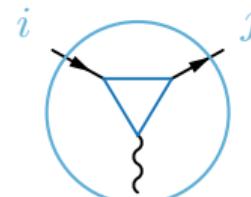
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$$\Gamma_{\mu \rightarrow e\gamma}^{[\text{any}]} \propto \sum |C^{\mathcal{D}}|^2$$

$$\Gamma_{\mu \rightarrow 3e}^{[\text{hep-ph/9510309}]} \propto 0.006 \cdot \Gamma_{\mu \rightarrow e\gamma} + \sum (\text{Re } C_e^{\mathcal{V}} C^{\mathcal{D}*} + |C_e^{\mathcal{S},\mathcal{V}}|^2)$$

$$\omega_{\mu-e}^{[\text{hep-ph/0203110}]} \propto \sum |DC_X^{\mathcal{D}} - \sum (S^{(N)} g^{\mathcal{S}} + V^{(N)} g^{\mathcal{V}})|^2$$

LFV processes



$$\mathcal{L}_{\text{LEFT}} \ni m_\mu C_X^{\mathcal{D}} [\bar{e} \sigma^{\mu\nu} P_X \mu] F_{\mu\nu} + C_{XY,f}^{\Gamma} [\bar{e} \Gamma_X \mu] [\bar{f} \Gamma_Y f]$$

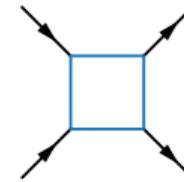
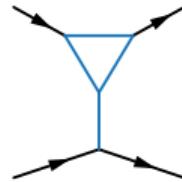
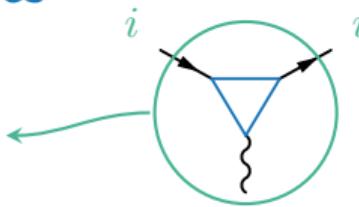
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LFV processes

What is
about
 $(g - 2)_i$?



$$\mathcal{L}_{\text{LEFT}} \ni m_\mu C_X^{\mathcal{D}} [\bar{e} \sigma^{\mu\nu} P_X \mu] F_{\mu\nu} + C_{XY,f}^{\mathcal{F}} [\bar{e} \Gamma_X \mu] [\bar{f} \Gamma_Y f]$$

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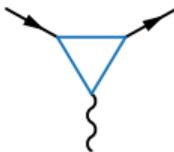
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Motivation by ...

- New bounds / results

$$(g - 2)_\mu \text{ BNL + FNAL: } (25.1 \pm 5.9) \cdot 10^{-10}$$



$\mu \rightarrow e$ conversion
 $\mu \rightarrow 3e$
 $\mu \rightarrow e\gamma$

COMETs: 3,4
Mu3es: 2,4
MEG-II: 1

They are connected! ... ?

Q: Do we need / How to use all of that?

- SUSY Extension of Poincaré algebra | No quadratic divergences | ...
- MRSSM Different SUSY realization | Absence of MSSM limit | R -symmetry
- Rich phenomenology^[2014...] Electroweak precision observables | Higgs boson mass | Dark matter relic density | Coloured sector
- Other models? Leptoquarks S_1 and R_2 | Grimus-Neufeld model

Well motivated!

Q: What's the model contribution / parameter dependence?

$U(1)_R$ symmetry: $\theta \rightarrow e^{i\alpha Q_\theta} \theta$, $Q_\theta := +1$

Same superfield \rightarrow related Q_*

| | | | | |
|--------------------|--|-----------------------|-------------------------------------|--|
| Assertion | $Q_V = 0$ | $Q(v_{d,u}) = 0$ | Yukawas form | All previous |
| Result | no Majorana gauginos | no μ -term | Q_{SM} are* fixed | no L/R mixing no A -terms |
| Consequence | Dirac masses | | | sfermion masses* |
| $-\mathcal{L} \ni$ | $M_B^D (\tilde{B} \tilde{S} - \sqrt{2} D_B S)$ | | | $(m_{\tilde{l}}^2)_{ij} \tilde{l}_i^* \tilde{l}_j$ |
| | | higgsino masses | usual Yukawas | new “Yukawas” |
| $W \ni$ | | $\mu_u R_u \cdot H_u$ | $-Y_{ij}^e \bar{E}_i L_j \cdot H_d$ | $\lambda_u S R_u \cdot H_u$ |

Parameters

Dirac masses

$$M_B^D(\tilde{B}\tilde{S} - \sqrt{2}D_BS)$$

M_B^D or M_W^D
should be light!

higgsino masses

$$\mu_u R_u \cdot H_u$$

μ_d – dipole

μ_u – restricted

sfermion masses*

$$(m_{\tilde{l}}^2)_{ij} \tilde{l}_i^* \tilde{l}_j$$

new “Yukawas”

$$\lambda_u S R_u \cdot H_u$$

$$\delta_L = \frac{(m_{\tilde{l}}^2)_{12}}{(m_{\tilde{l}}^2)_{11}(m_{\tilde{l}}^2)_{22}}$$

and / or

$$\delta_R = \frac{(m_{\tilde{e}}^2)_{12}}{(m_{\tilde{e}}^2)_{11}(m_{\tilde{e}}^2)_{22}}$$

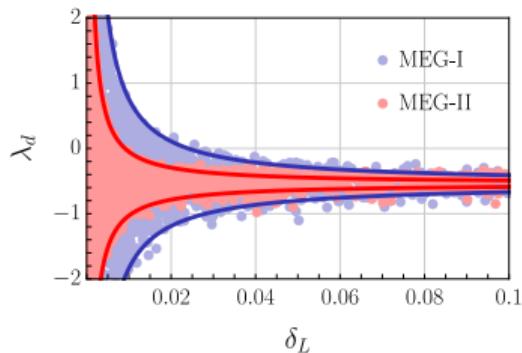
$\lambda_d, \lambda_u, \Lambda_d, \Lambda_u$ –
dependent

So many! **Q:** What to do?

Simplified scenarios: i.e. *BHL*

Scattering plots

BL: allowed regions for $\mu \rightarrow e\gamma$

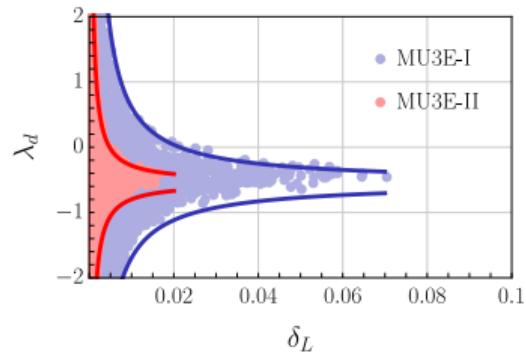


expectation:

$$\text{Br}_{\mu \rightarrow e\gamma} \propto \delta_L^2 (\lambda_d + \Delta)^2$$

check!

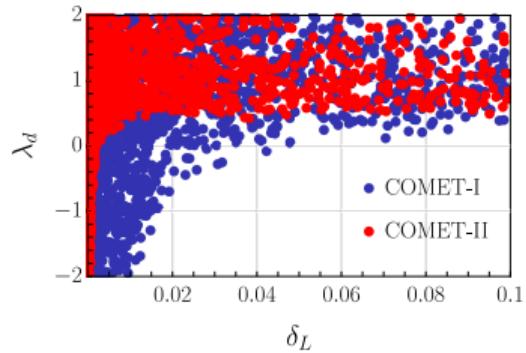
BL: allowed regions for $\mu \rightarrow 3e$



expectation:

dipole dominance if
 $\text{Br}_{\text{MEG}} \rightarrow \text{Br}_{\text{MU3E}} / 0.006$

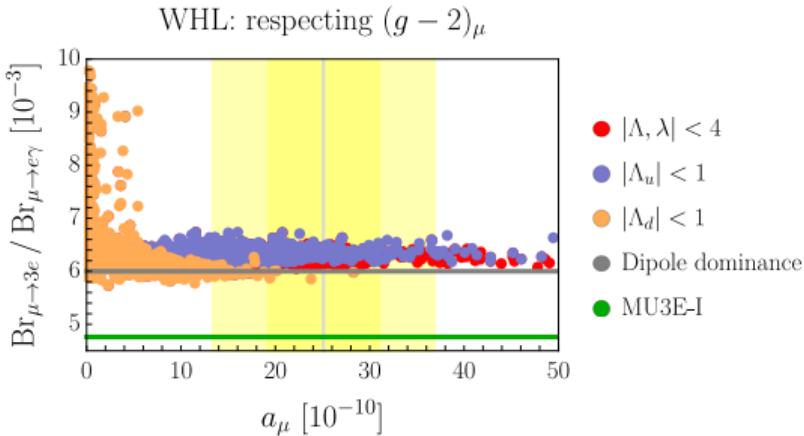
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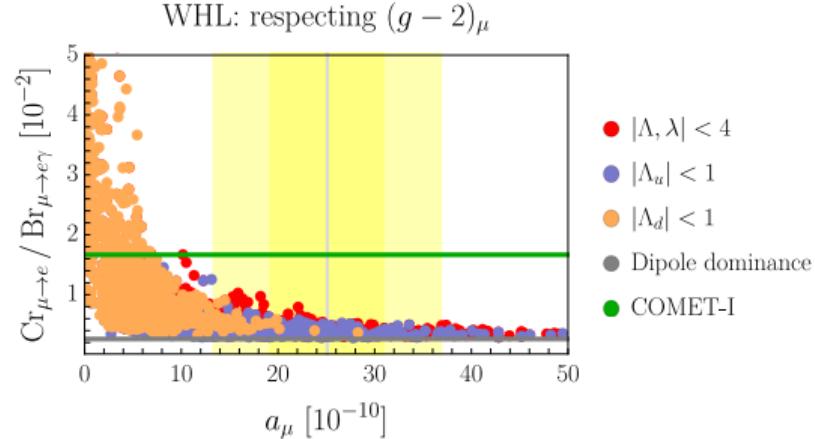
correlation?

cancellations,
non-correlation!

What if ... $(g - 2)_\mu$?



$$\frac{\text{Br}_{\mu \rightarrow 3e}}{\text{Br}_{\mu \rightarrow e\gamma}} \approx 0.006$$



$$\frac{\text{Cr}_{\mu \rightarrow e}}{\text{Br}_{\mu \rightarrow e\gamma}} \approx 0.0026$$

Chirality flip aka $\sigma_{\mu\nu}$, **no** μ -term $\rightarrow \Lambda_d, \lambda_d$ enhancement.

Conclusions

- **N**PointFunctions @ FlexibleSUSY

Fast (thanks to C++ and FORTRAN)
Customizable (on Mathematica and C++ levels)
Extendable (due to a modular structure)
Consistent checks / constraints from different scales

- **A**pplications

MRSSM [[U.Kh](#), [W.Kotlarski](#), [D.Stöckinger](#), [H.Stöckinger-Kim](#)]
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...

- **T**ODOs:

New observables
Some guide
Bug fixes / structure simplification
More options / loops / ...

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... WRITE ME :D

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