



## Neutrino interactions in FLUKA: NUNDIS

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# Neutrinos in FLUKA

- Generators of neutrino-nucleon interactions:
  - QuasiElastic Acta Phys.Polon. B40 (2009) 2491-2505
  - Resonance CERN-Proceedings-2010-001 pp.387-394.
  - DIS
- Embedded in FLUKA nuclear models for Initial State and Final State effects
- Only for Argon: absorption of few-MeV (solar) neutrinos on whole nucleus
- Elastic scattering on electrons - to be refreshed
- Products of the neutrino interactions can be directly transported in the detector (or other) materials
- Used for all ICARUS simulations/publications

**Web Site:** <http://www.fluka.org>

# Quasi Elastic and Resonant

## QE

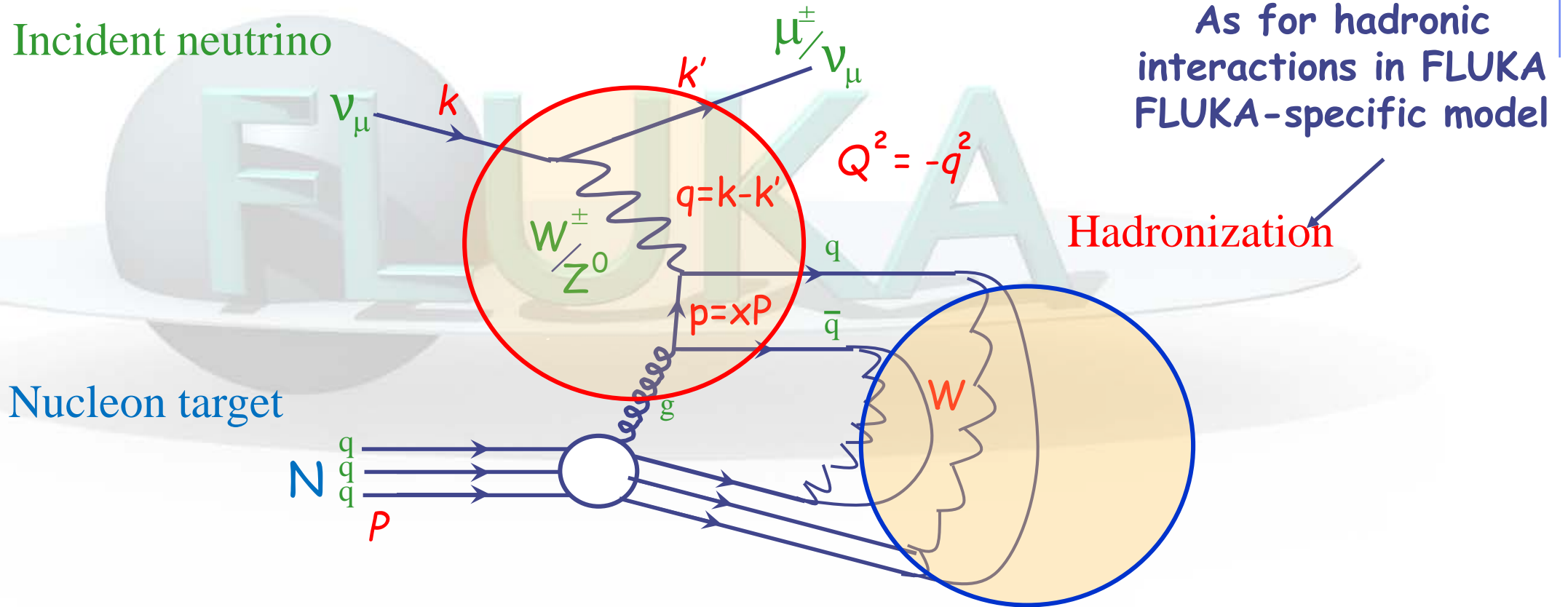
- Following Llewellyn Smith formulation
- $M_A = 1.03$ ,  $M_V = 0.84$
- Lepton masses accounted for

## Resonance production

- From Rein-Sehgal formulation
- Keep only  $\Delta$  production
- No non-resonant background term, assuming that the non-resonant contribution comes from NunDIS
- **TRANSITION** from RES to DIS: linear decrease of both  $\sigma$  as a function of  $W$

# DIS (NUNDIS)

FLUKA hadronization and nuclear interactions work well independently of primary interaction vertex



# Sample $x$ and $Q^2$ from double differential cross sections

$$\frac{d^2\sigma}{dx dQ^2} = \frac{d^2\sigma}{dx dy} \cdot \frac{dy}{dQ^2} = \frac{d^2\sigma}{dx dy} \cdot \frac{1}{2ME_\nu x}$$

$$\frac{d^2\sigma}{dx dy} = \frac{G_F^2 M E_\nu}{\pi(1 + Q^2/M_{W/Z}^2)^2} \sum_{i=1}^5 A_i(x, y, E_\nu) F_i(Q^2, x)$$

## Structure functions $F_i(Q^2, x)$

$$F_2^{\nu p}(Q^2, x) = 2x[d + \bar{u} + s + \bar{c}]$$

$$xF_3^{\nu p}(Q^2, x) = 2x[d - \bar{u} + s - \bar{c}]$$

**Callan-Gross relation:**  $F_1 = \frac{F_2}{2x}$

To be updated to

$$2xF_1(Q^2, x) = F_2(Q^2, x) \frac{1 + 4M^2 x^2 / Q^2}{1 + R(Q^2, x)}$$

**Albright-Jarlskog relations:**

$$F_4 = 0,$$

$$F_5 = \frac{F_2}{x}.$$

$$A_1 = y \left( xy + \frac{m_\ell^2}{2ME_\nu} \right)$$

$$A_2 = 1 - y \left( 1 + \frac{Mx}{2E_\nu} \right) - \frac{m_\ell^2}{4E_\nu^2}$$

$$A_3 = \pm y \left[ x \left( 1 - \frac{y}{2} \right) - \frac{m_\ell^2}{4ME_\nu} \right]$$

$$A_4 = \frac{m_\ell^2}{2ME_\nu} \left( y + \frac{m_\ell^2}{2ME_\nu x} \right)$$

$$A_5 = -\frac{m_\ell^2}{ME_\nu}$$

# Quark dependence $q_i(Q^2, x)$ determined from Parton Distribution Functions (PDFs)

GRV94	Glück et al., Z. Phys. C67 (1995) 433.
<b>GRV98</b>	<b>Glück et al., Eur. Phys. J. C5 (1998) 461.</b>
BBS	Bourelly et al., Eur. Phys. J. C23 (2003) 487.
CTEQ	J. High Energy Phys. 0207 (2002) 012.
MRST	arXiv:hep-ph/0211080.
Alekhin	Phys. Rev. D68 (2003) 014002.
...	

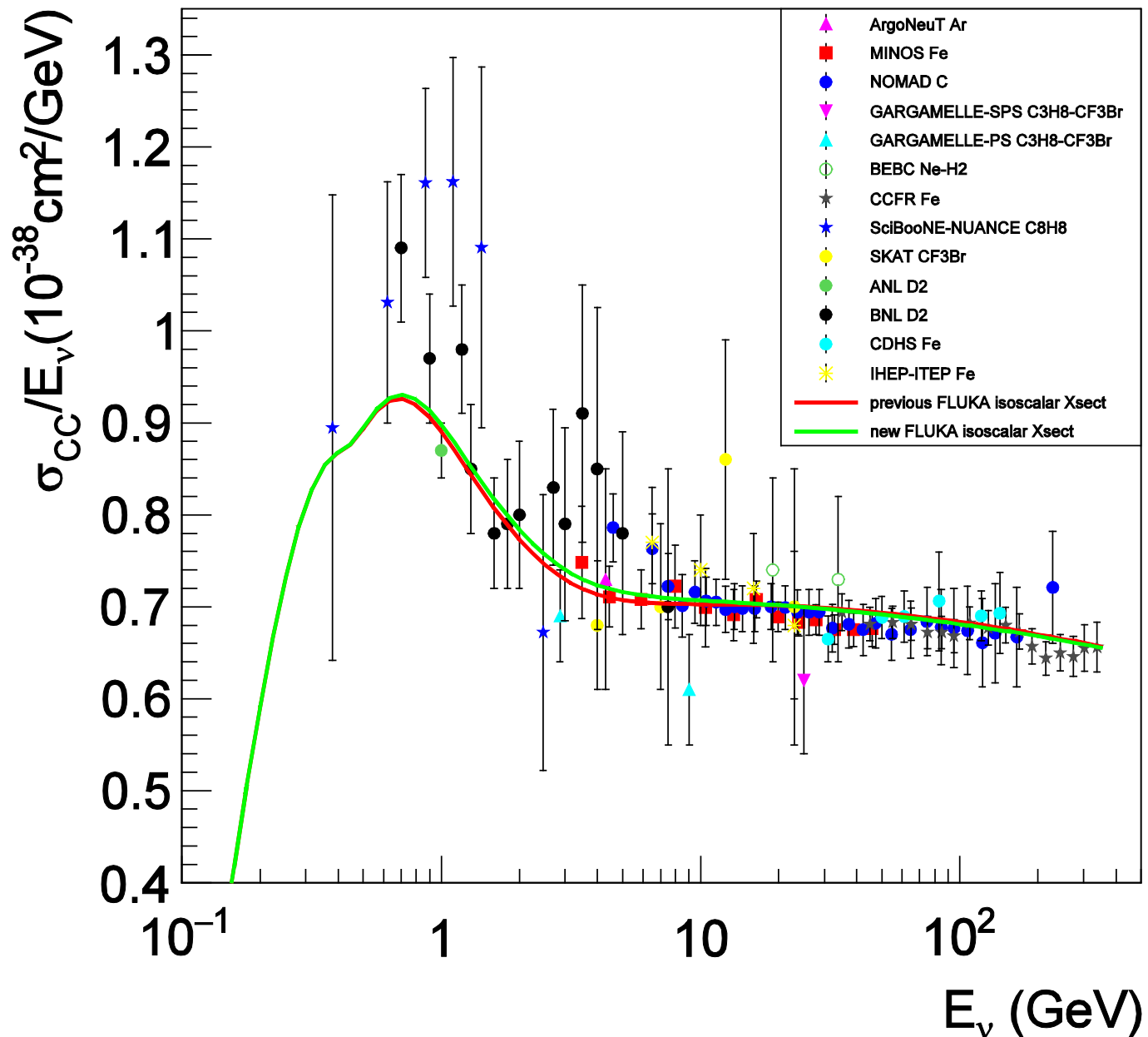
**NUNDIS WORKS WITH THESE PDFs**

**DEFAULT OPTION**

In the NLO (DIS) version  
M. Glück, E. Reya and A. Vogt, Eur. Phys. J. C5 (1998) 461  
With extrapolation to  $Q^2=0$  as in  
M. Bertini et al. 1996

# Comparison with data on total cross section

Isoscalar  
 $\nu_\mu$  - Nucleon total  
CC cross section  
Fluka (lines) with  
two pdf options  
Vs  
Experimental data



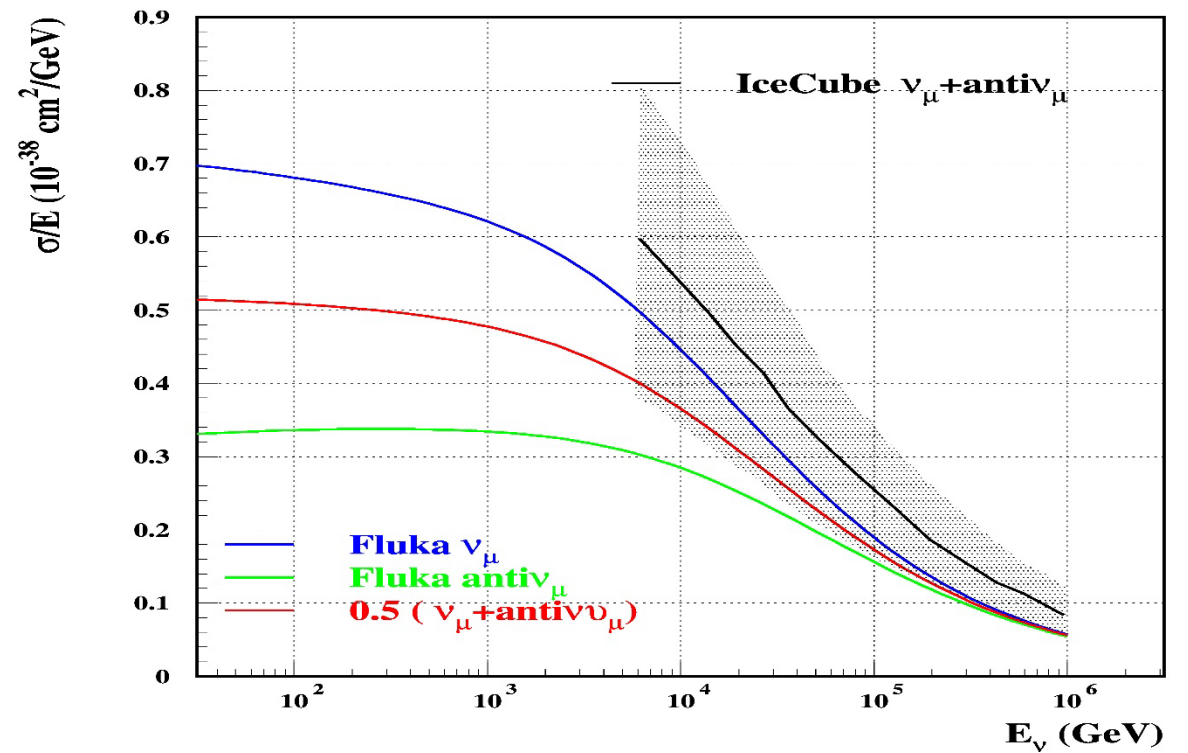
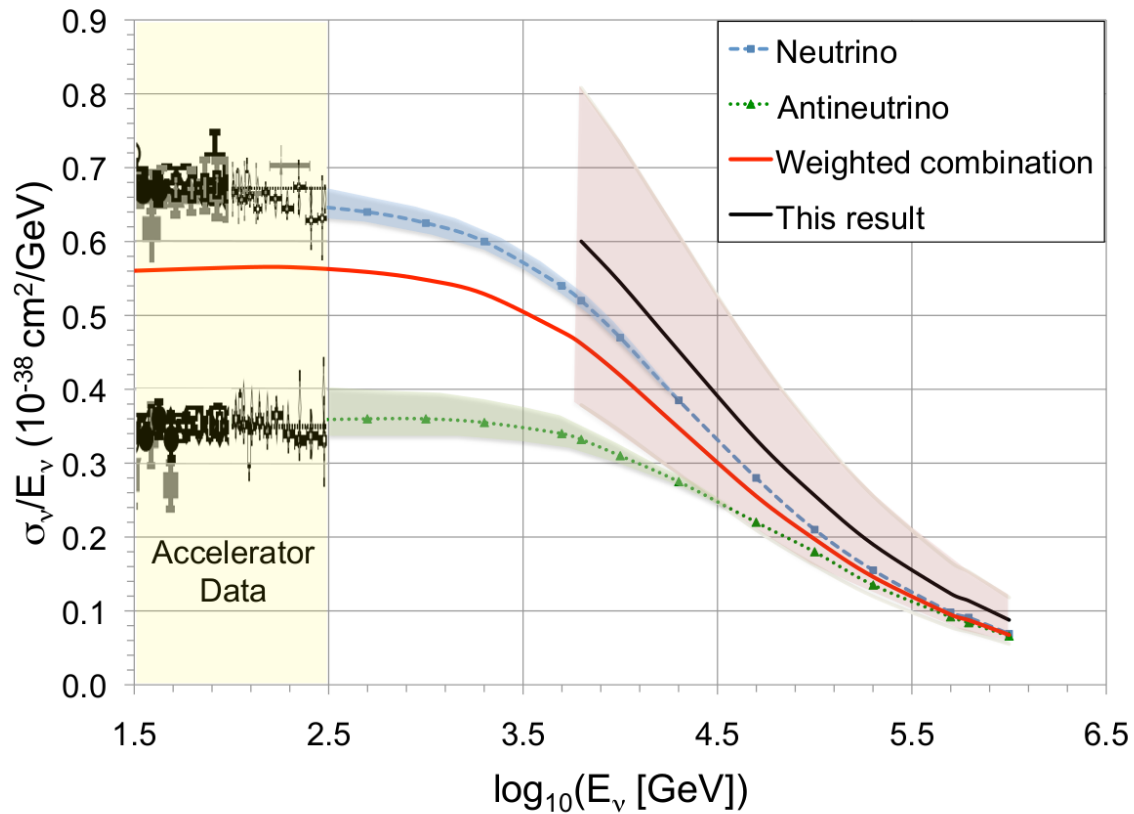
# At higher energies

IceCube cross section data, Muon neutrino and antineutrino ,  
"weighted combination" ?

[arXiv:1711.08119](https://arxiv.org/abs/1711.08119) , *Nature* 51,596 (2017)

Blue and green: "standard model predictions"

FLUKA results





# Hadronization

Implementation FLUKA-native  
(evolution of old BAMJET )

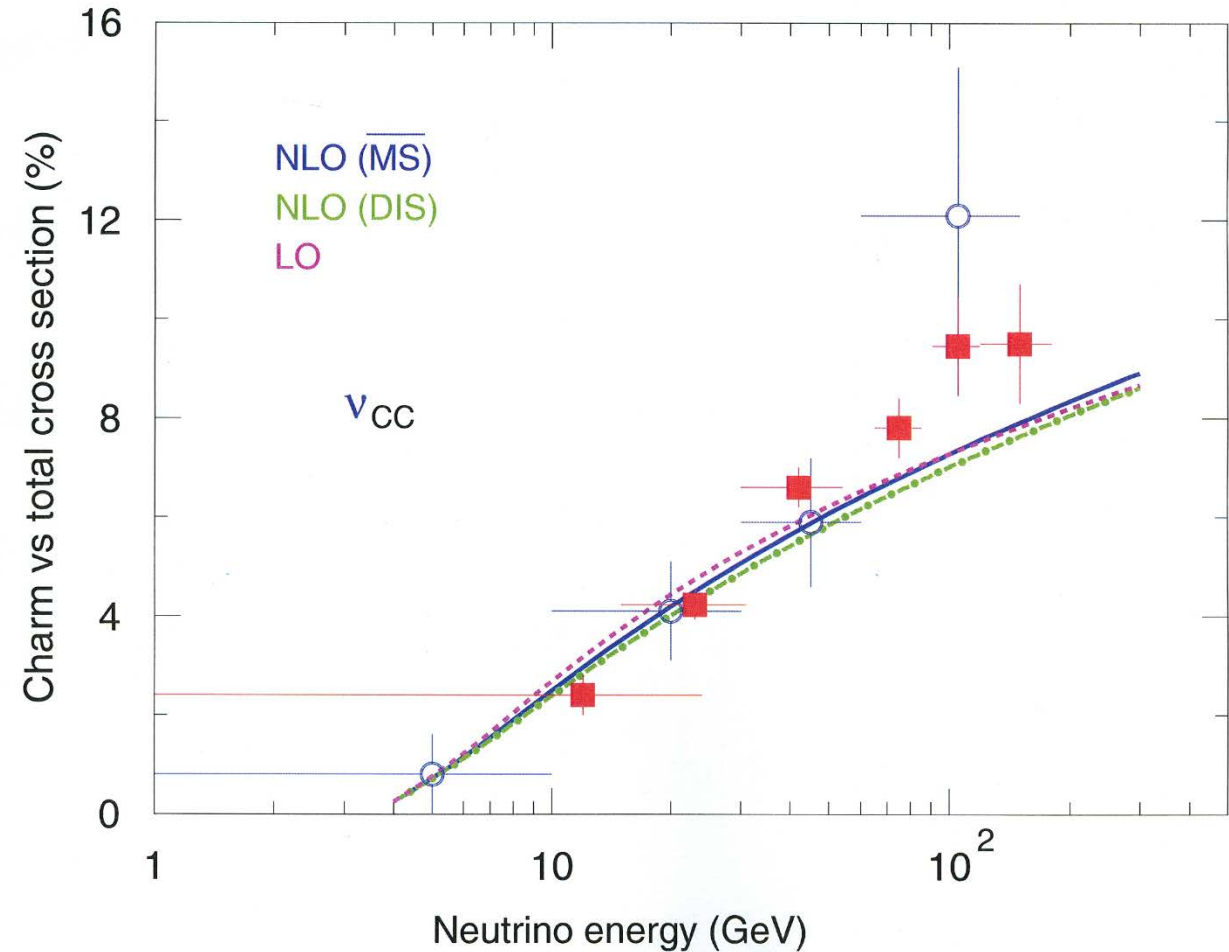
- Assumes chain universality
- Fragmentation functions from hard processes and  $e+e^-$  scattering
- Transverse momentum from uncertainty considerations
- Mass effects at low energies ( change fragmentation function to account for the need to create real hadrons)
- Chains generated at very low energy  $\rightarrow$  create single/few resonances
- Chains generated at low energy  $\rightarrow$  “phase space explosion” constrained in  $p_T$  , including baryons, mesons, resonances.

The same functions and parameters for all reactions and energies

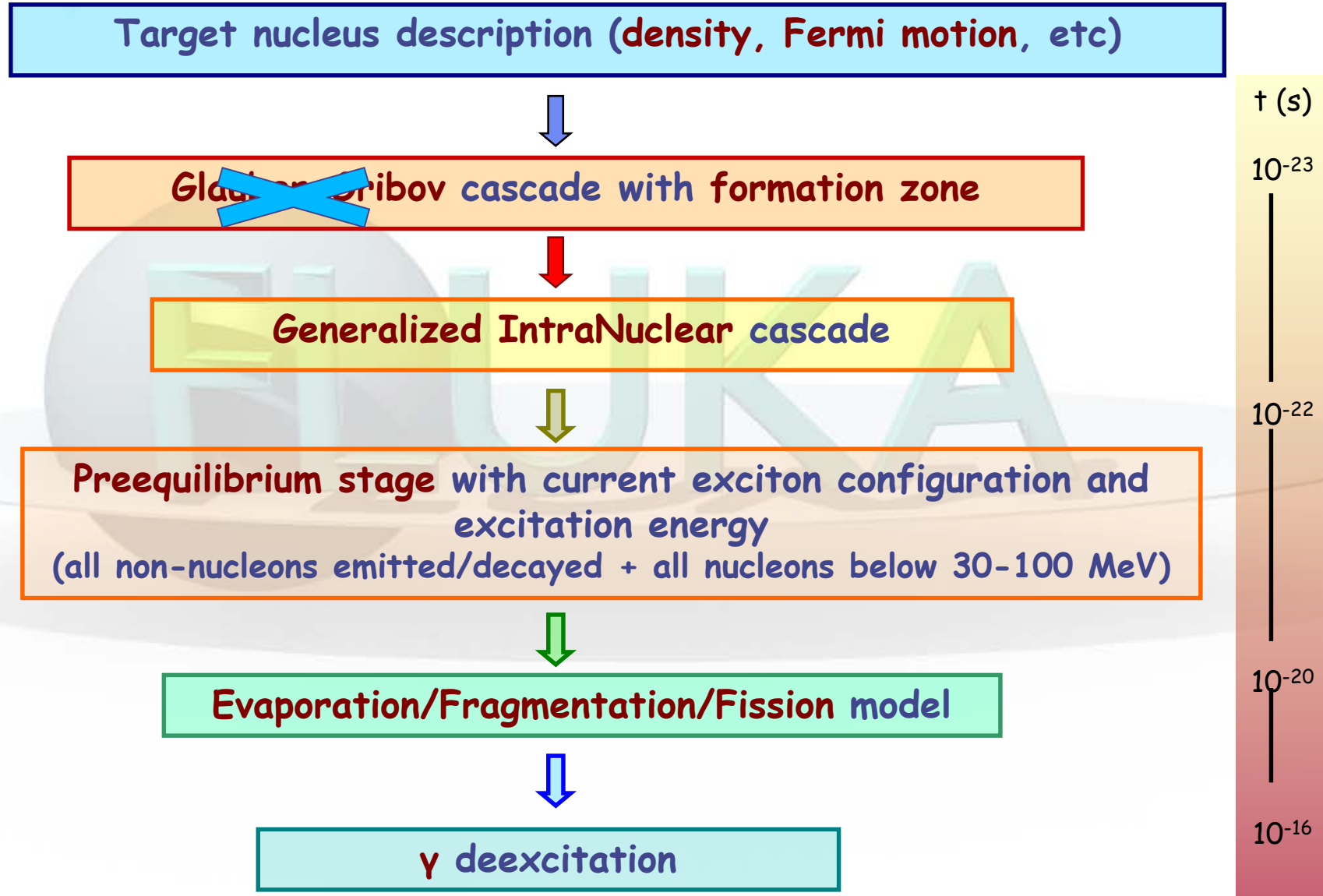
- Chains from  $\nu$  DIS :
  - One quark-diquark chain if interaction on valence quark
  - One quark-diquark plus one  $q$ - $q$ bar chain if int on sea quark

# Charm production in neutrino interactions

- Ratio of the charm to total cross sections
- Results of NUNDIS simulation with  $M_c = 1.35$  GeV (curves) and experimental data: E531 (open circles) and CHORUS-2011 (filled squares).



# Nuclear interactions in FLUKA: the PEANUT model



# a special FSI : Formation zone

Naively: "materialization" time (originally proposed by Stodolski).

Qualitative estimate:

In the frame where  $p_{||} = 0$

$$\bar{t} = \Delta t \approx \frac{\hbar}{E_T} = \frac{\hbar}{\sqrt{p_T^2 + M^2}}$$

Particle proper time

$$\tau = \frac{M}{E_T} \bar{t} = \frac{\hbar M}{p_T^2 + M^2}$$

Going to the nucleus system

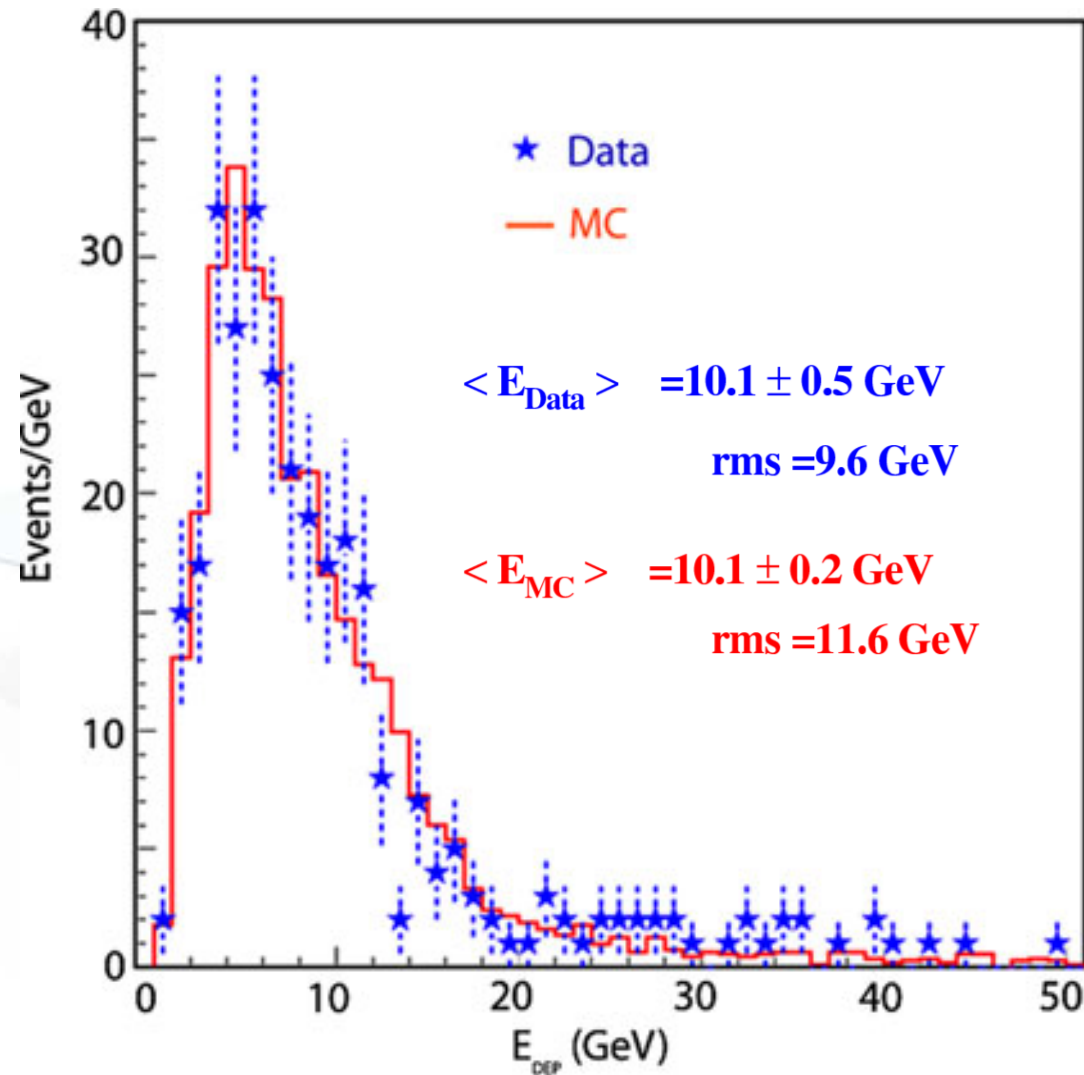
$$\Delta x_{for} \equiv \beta c \cdot t_{lab} \approx \frac{p_{lab}}{E_T} \bar{t} \approx \frac{p_{lab}}{M} \tau = k_{for} \frac{\hbar p_{lab}}{p_T^2 + M^2}$$

Condition for possible reinteraction inside a nucleus:  $\Delta x_{for} \leq R_A \approx r_0 A^{\frac{1}{3}}$

Decrease of the reinteraction probability

Applied also to DIS neutrino interactions and, in an analogue way, to QE neutrino interactions

# CNGS data

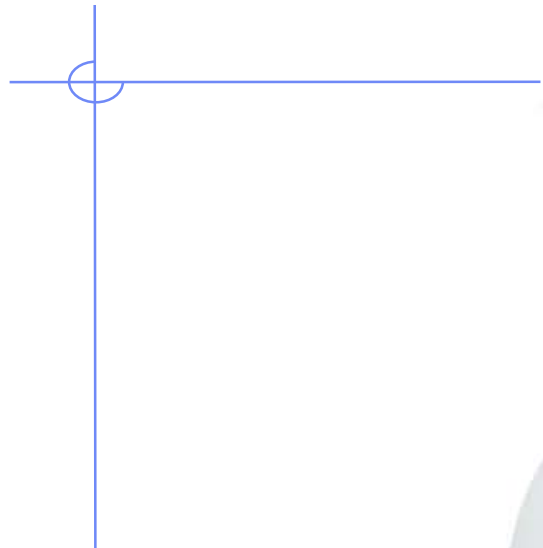


Distribution of total deposited energy in the T600 detector  
CNGS numuCC events (~20 GeV  $E_{\nu}$  peak)

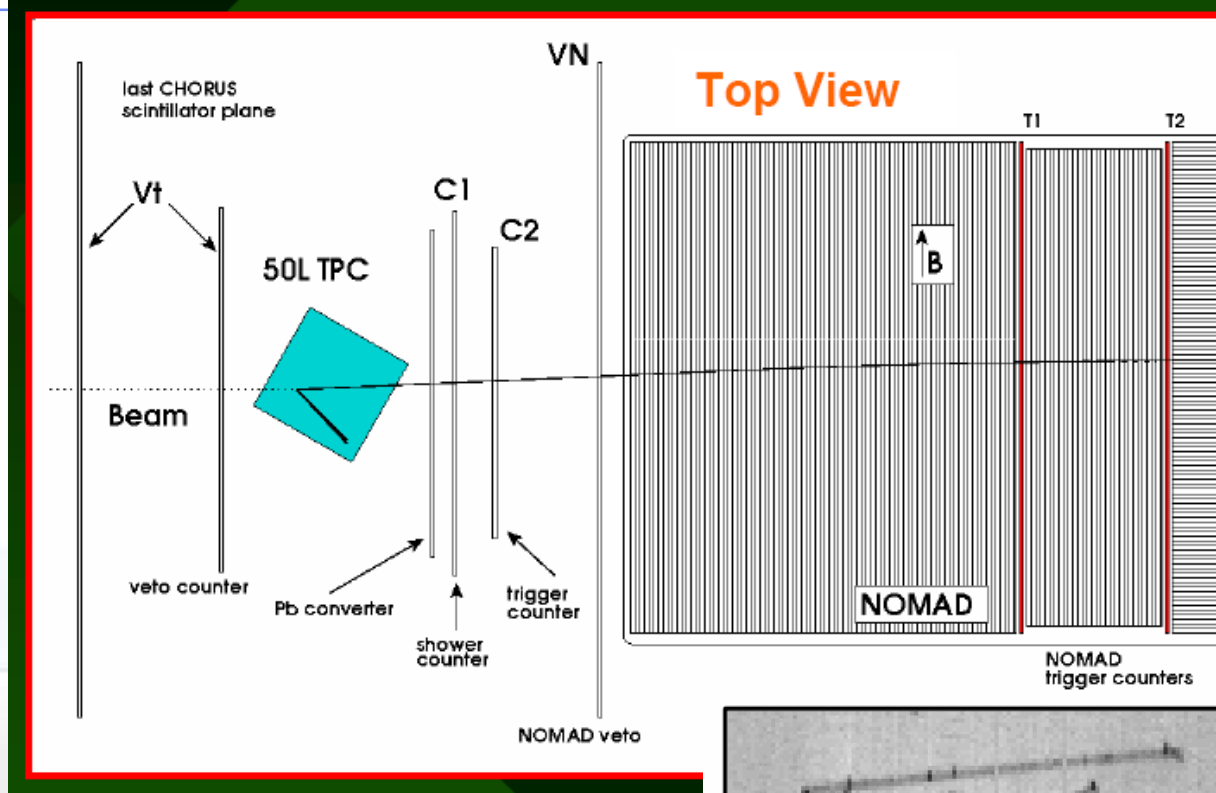
Same reconstruction in MC and Data  
Neutrino fluxes from FLUKA cngs simulations

Absolute agreement on neutrino rate within 6%

Eur. Phys. J. C (2013) 73:2345  
Phys. Lett. B (2014)



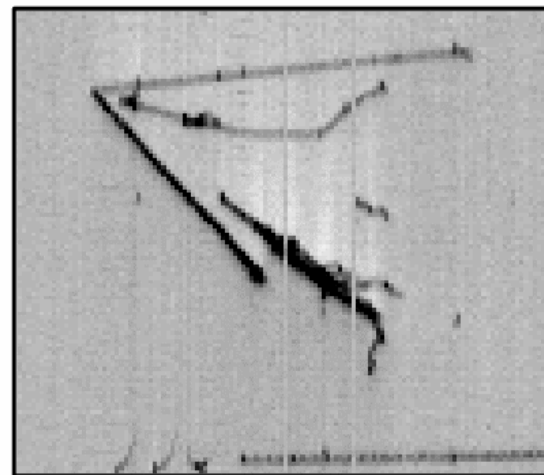
# The 50L LAr TPC in the WANF neutrino beam(1997)



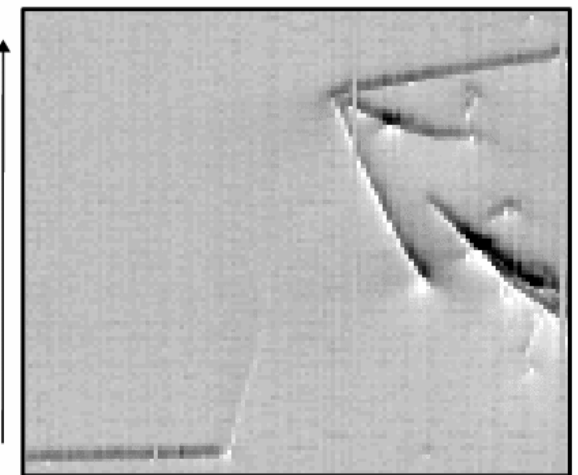
Trigger and  $\mu$   
reconstruction: NOMAD

Event selection: "GOLDEN sample"  
= 1  $\mu$  and 1 proton  $>40\text{MeV}$  fully contained

Phys.Rev. D74 (2006) 112001



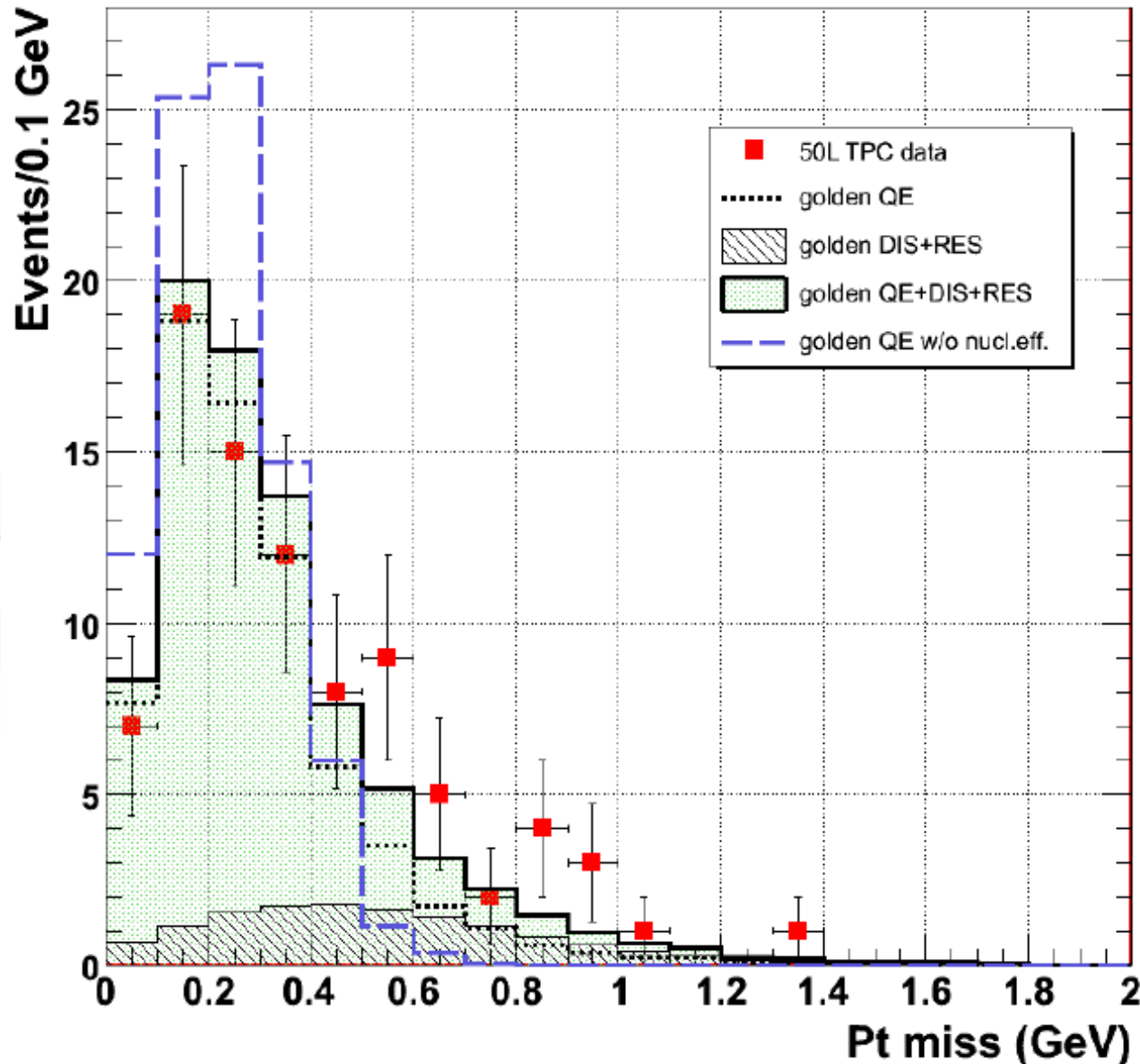
Collection wires. (128 wires: 32 cm.)



Induction wires. (128 wires: 32 cm.)

Time (1300 samples: 47 cm)

### Missing transverse momentum



- from 400 QE - golden fraction 16%
- background - additional 20% finally expected

$80 \pm 9(\text{stat.}) \pm 13(\text{syst.}) \rightarrow$  mainly QE fraction and beam simul)

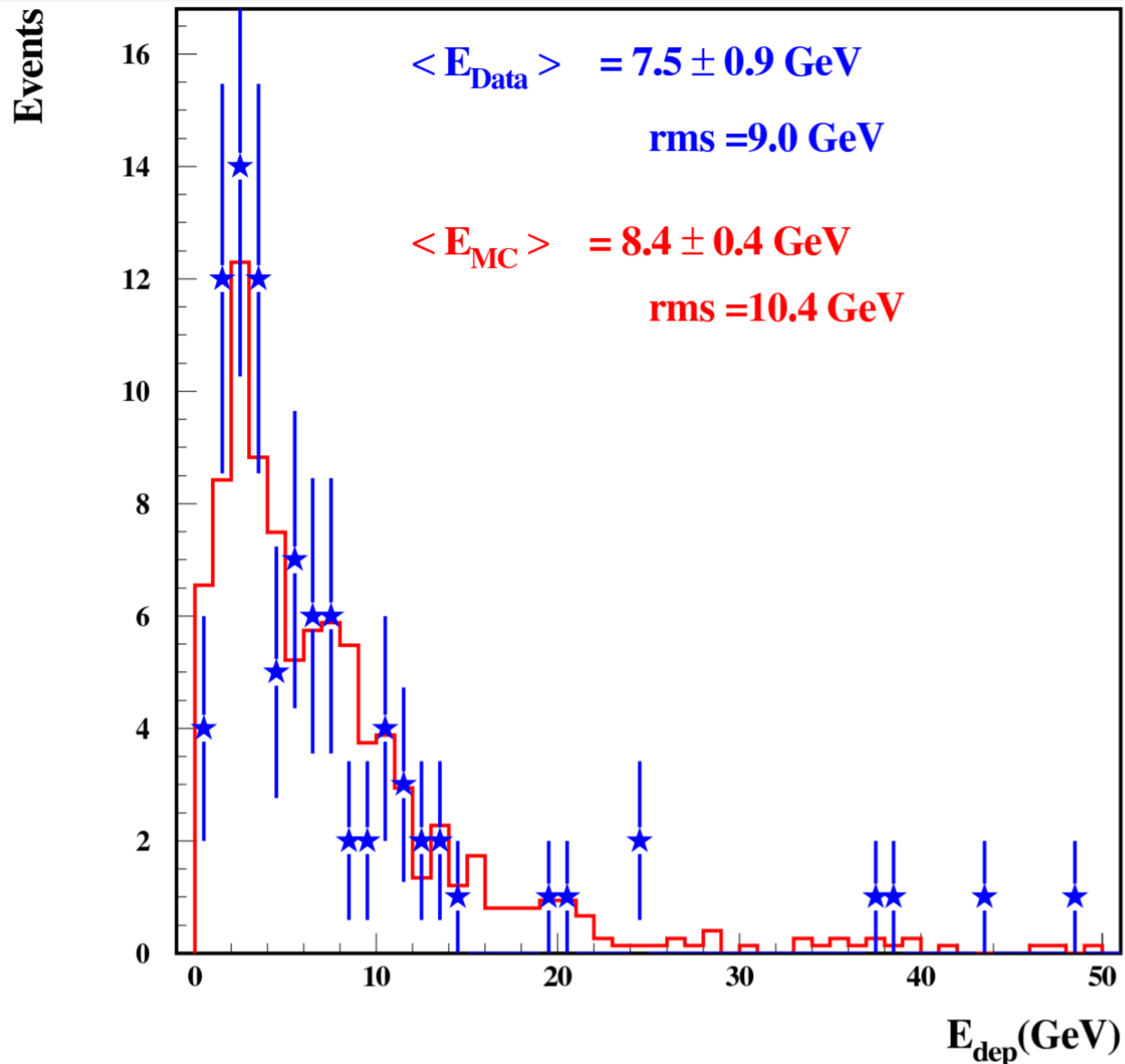
to be compared with **86** events observed

Very good consistency with expectations

Note: here DIS and RES from old coupling with the NUX code (A. Rubbia)



# CNGS data



Distribution of total deposited energy in the T600 detector  
CNGS nuNC

Same reconstruction in MC and Data  
Neutrino fluxes from FLUKA cngs simulations

Only events with  $E_{\text{dep}} > 500$  Mev

# NUNDIS 2015: kinematics

- Considered kinematical limits for the *PDF* available from GRV94, GRV98, and BBS analyses.

Variable	Required	GRV94		GRV98		BBS	
		Default	Tested	Default	Tested	Default	Tested
$E_{min}$ (GeV)	—	0.050					
$E_{max}$ (GeV)	$\geq 10^4$	$70 \cdot 10^3$			$10^5$		
$Q_{min}^2$ (GeV <sup>2</sup> )	$\leq 5.5 \cdot 10^{-12}$	0.4	0.4	0.8	0.8	2	0.8
$Q_{max}^2$ (GeV <sup>2</sup> )	$\geq 1.9 \cdot 10^4$	$10^6$	$10^9$	$10^6$	$10^9$	$10^4$	$2 \cdot 10^4$
$x_{min}$	$\leq 1.4 \cdot 10^{-11}$	$10^{-5}$	$10^{-30}$	$10^{-9}$	$10^{-30}$	$10^{-4}$	$10^{-30}$
$x_{max}$	1	0.99999	0.99999	1	1	1	1

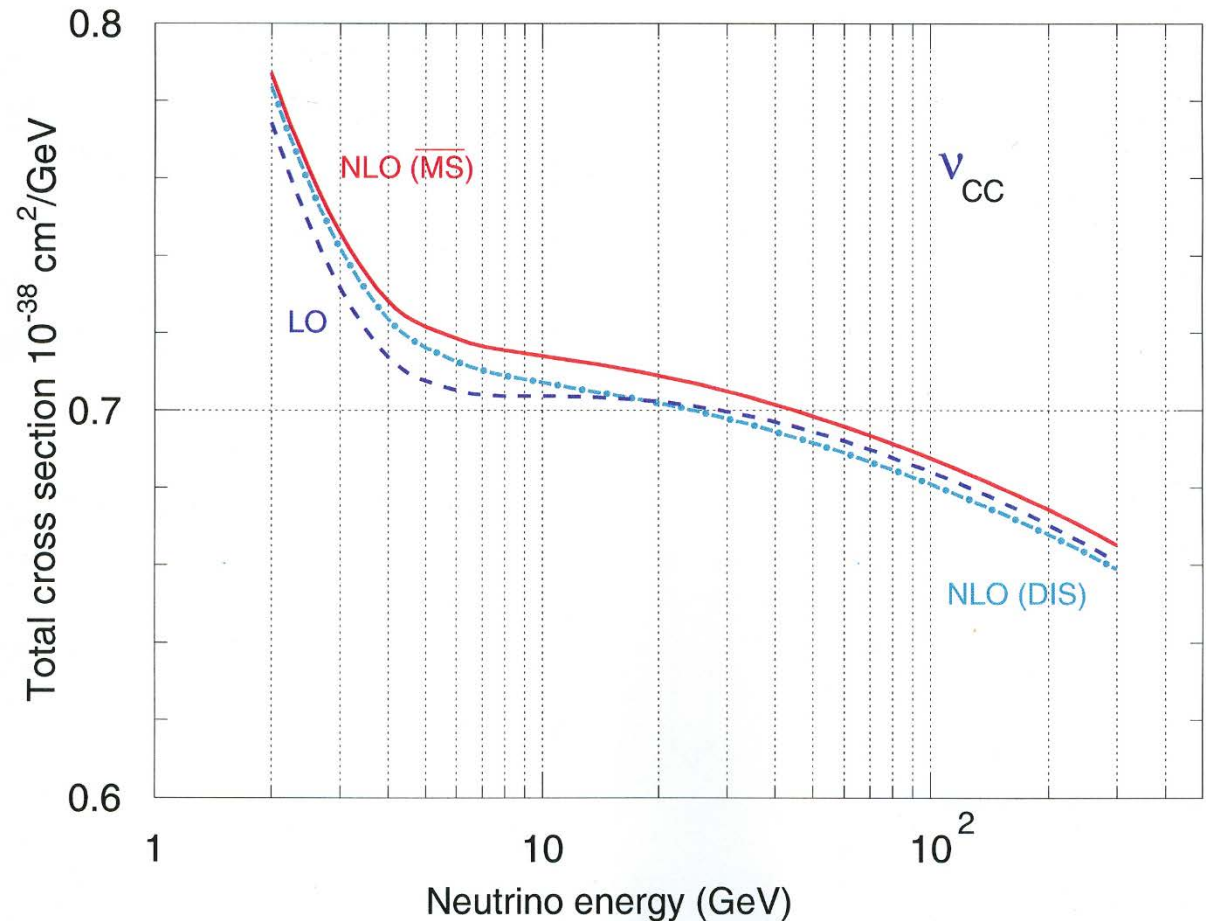
## More on pdfs

Three versions of pdf from the GRV98 analysis are included as options for evaluating nucleon structure functions

1. Leading order analyses (LO)
2. Next to leading order analyses (NLO  $\overline{\text{MS}}$ )
3. Next to leading order analyses (NLO DIS)

An interesting feature of the GRV98 analysis is a low threshold for the transferred, 4-momentum,  $Q^2 = 0.8 \text{ GeV}^2$

**NLO (DIS) is chosen as a default option**



# Nucleon correlation function:

Correlation function: it can be computed within the Fermi-gas model

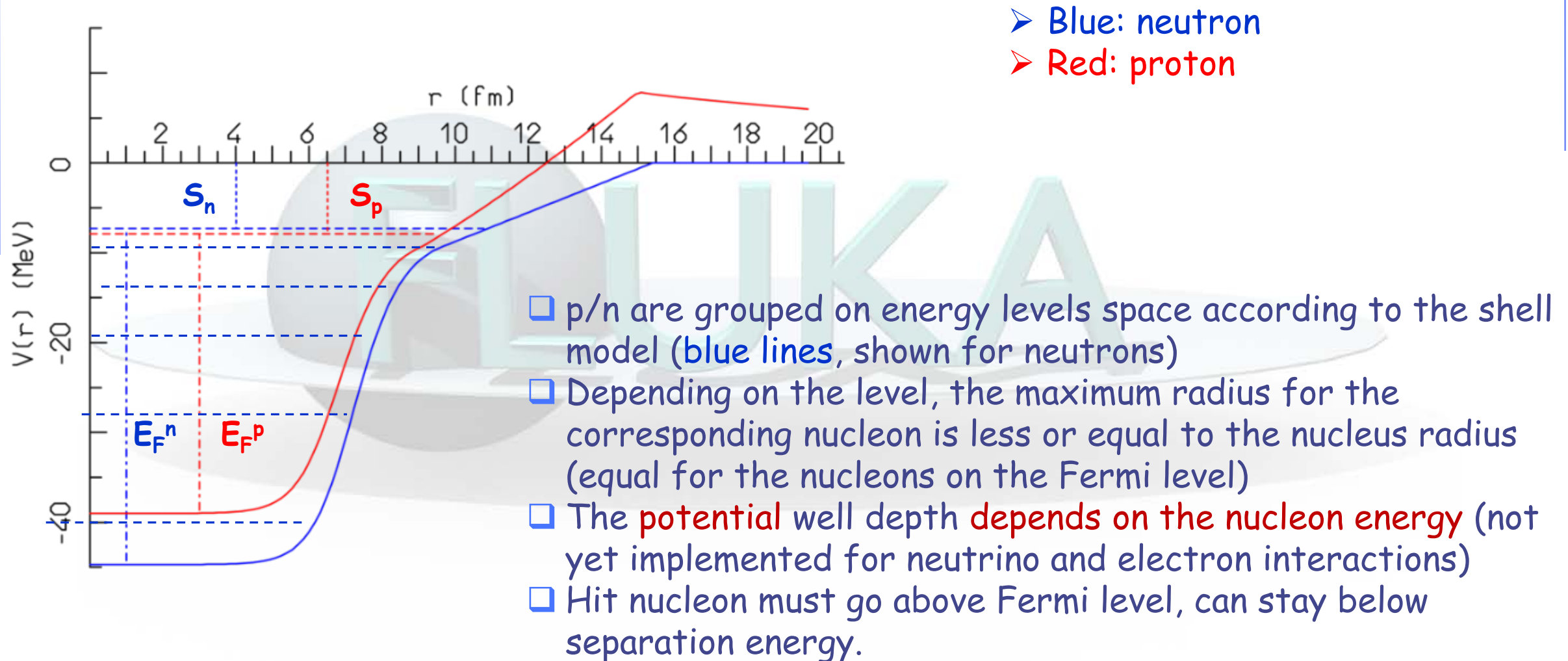
Due to the anti-symmetrization of the fermion's wave function, given a nucleon in a position  $\vec{r}$  in a nucleus with density  $\rho_0$ , the probability of finding another like nucleon in a position  $\vec{r}'$  is decreased for small values of the distance  $d = |\vec{r} - \vec{r}'|$  by a factor

$$g(x) = 1 - \frac{1}{2} \left[ \frac{3}{x^2} \left( \frac{\sin x}{x} - \cos x \right) \right]^2$$

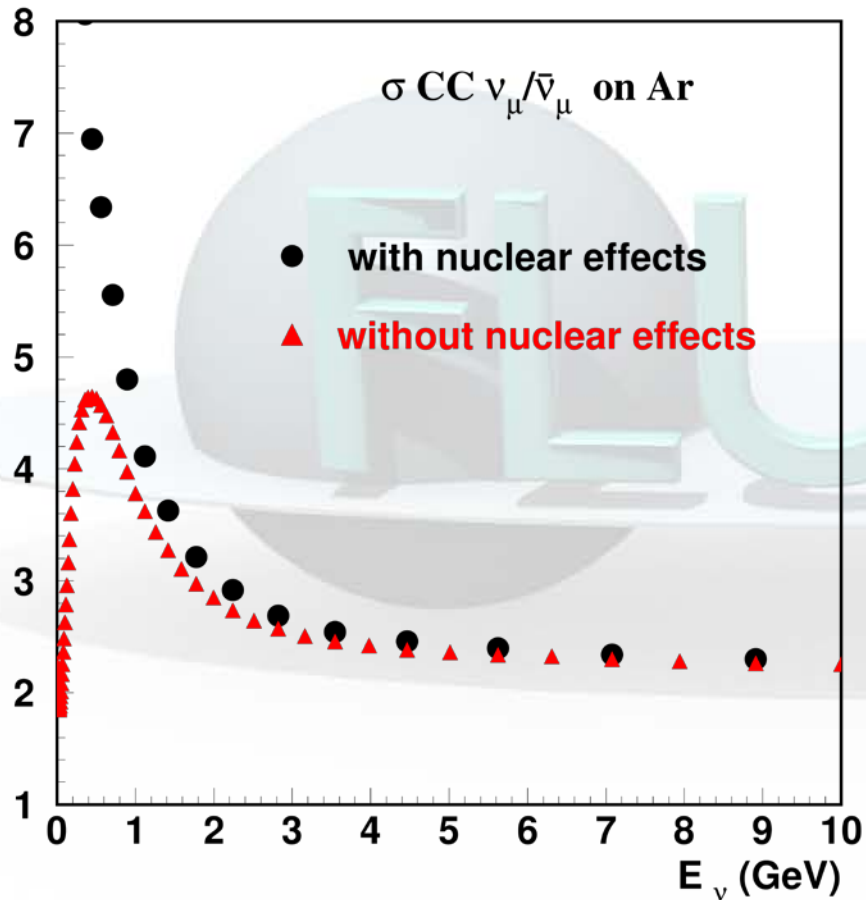
where  $x = K_F \cdot d$ , and the factor 1/2 in front of the parenthesis accounts for the two possible spin orientations.

Nucleon hard core effects are also taken into account, forbidding to "find" a nucleon of the same or different type at less than 1-1.5 fm distance. This check is applied at every possible re-interaction, checking against all nucleons already involved in previous interactions

# Nucleon levels inside the nuclear potential: schematic drawing



# Effect of Pauli Blocking: example



Ratio of Neutrino/antineutrino  $\sigma_{CC}$  vs  
(a) neutrino energy

For interactions in Ar nuclei,  $\nu_{\mu}$

As calculated with FLUKA


Black: full calculation

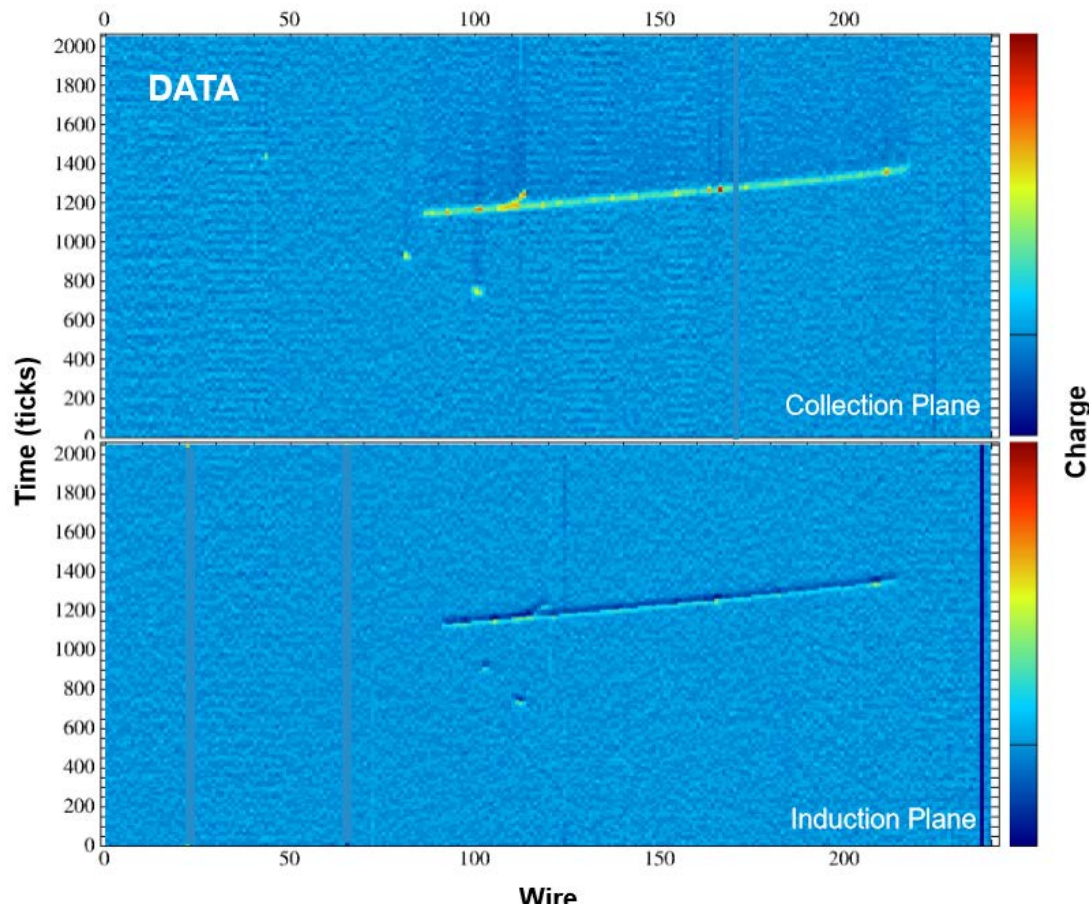
Red: simple sum of  $\nu$ -N cross section

Smaller  $q^2$  in anti-neutrino results in  
higher Pauli-blocking probability

# First Demonstration of LArTPC MeV-Scale Physics in ArgoNeuT

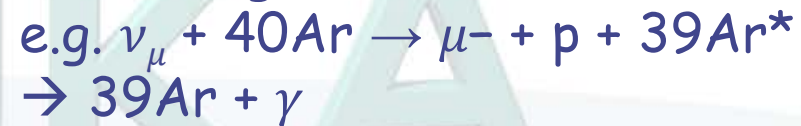
Ivan Lepetic *APS\_April2018*

 ILLINOIS INSTITUTE OF TECHNOLOGY  
For the ArgoNeuT Collaboration



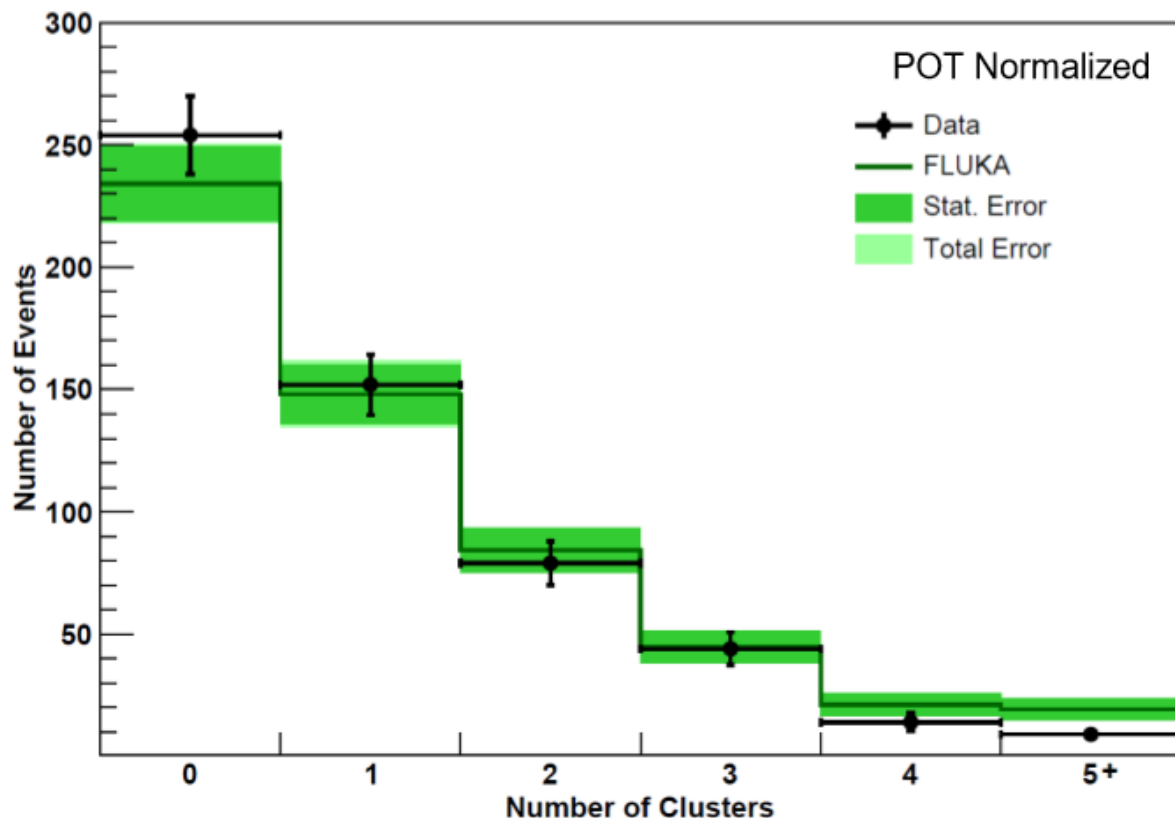
Low-energy gammas produced by neutrino-nucleus interactions in ArgoNeuT

Photons from **neutrino-produced nuclear de-excitation** and inelastic neutron scattering -



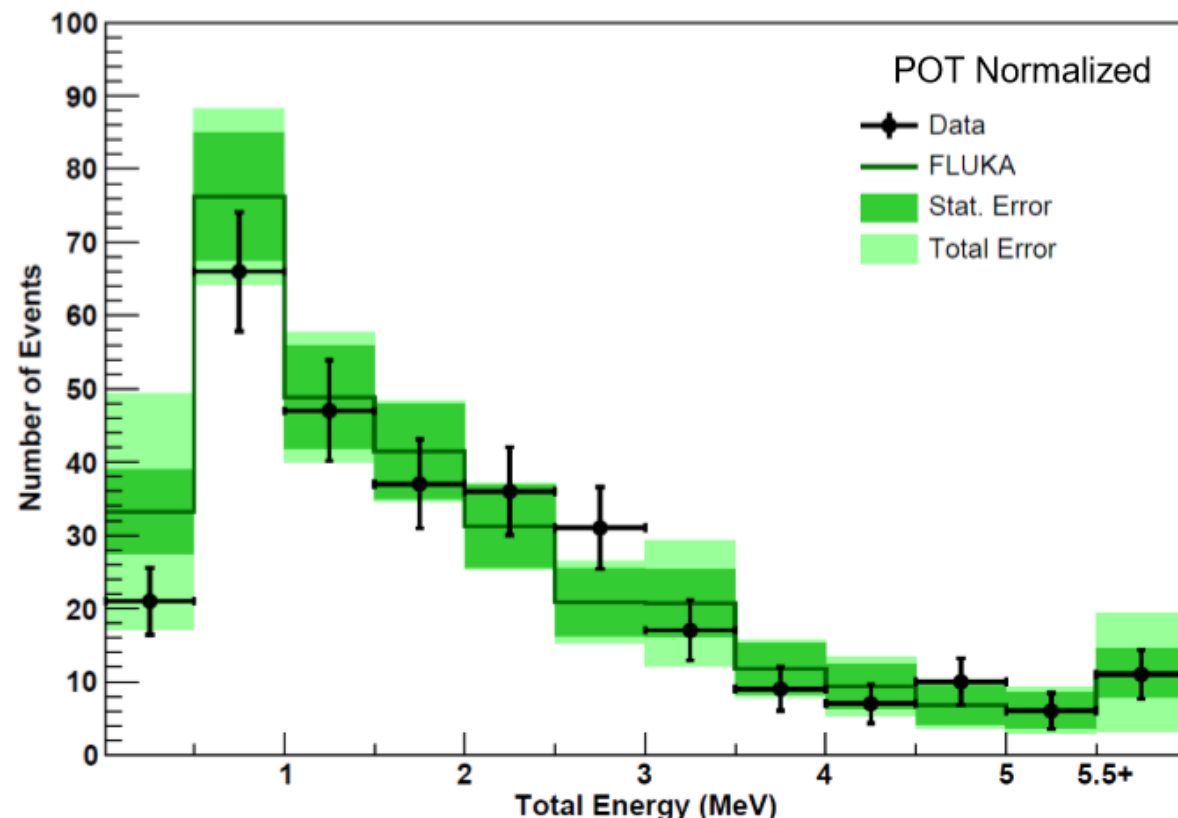
# Data and FLUKA

Number of Clusters in an Event



$\chi^2/\text{ndf} = 9.62/6$ . p-value = 0.14

Total Reconstructed Energy in an Event



$\chi^2/\text{ndf} = 7.74/12$ . p-value = 0.81

Agreement is far worse if either de-excitation or neutron produced gammas are removed.



# Effect of formation zone on residuals

Experimental and computed residual nuclei mass distribution

Ag(p,x)X at 300 GeV (top)

Au(p,x)X at 800 GeV (bottom)

Data from:

Phys. Rev. C19 2388 (1979) and

Nucl. Phys. A543, 703 (1992)

(The heavy fragment evaporation model is key for FLUKA predictions for  $A < 30$ )

Ag **with** and **without** form.zone:

$\langle \pi \rangle = 21.1$ ,  $\langle E_\pi \rangle = 7.3$  GeV

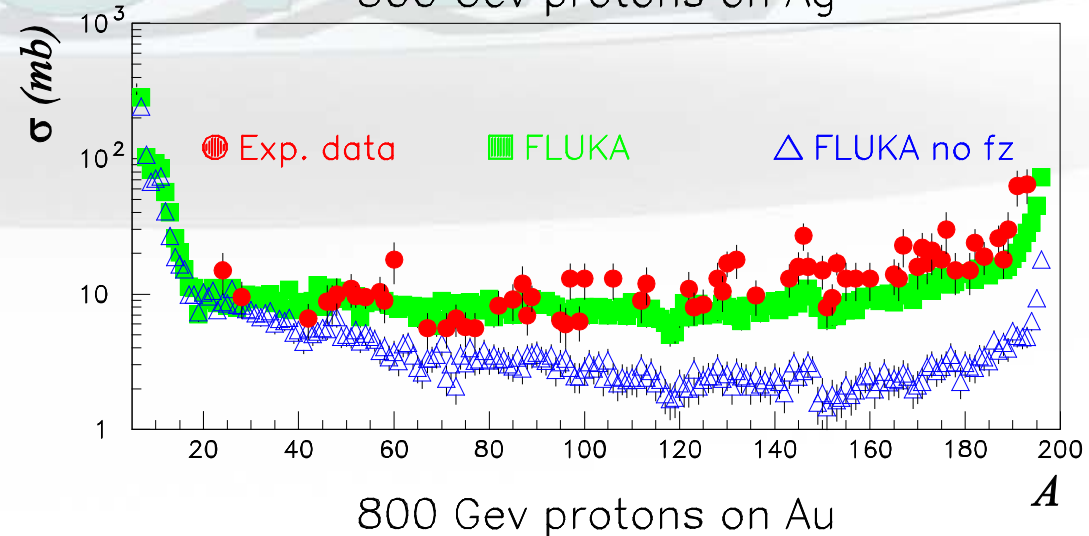
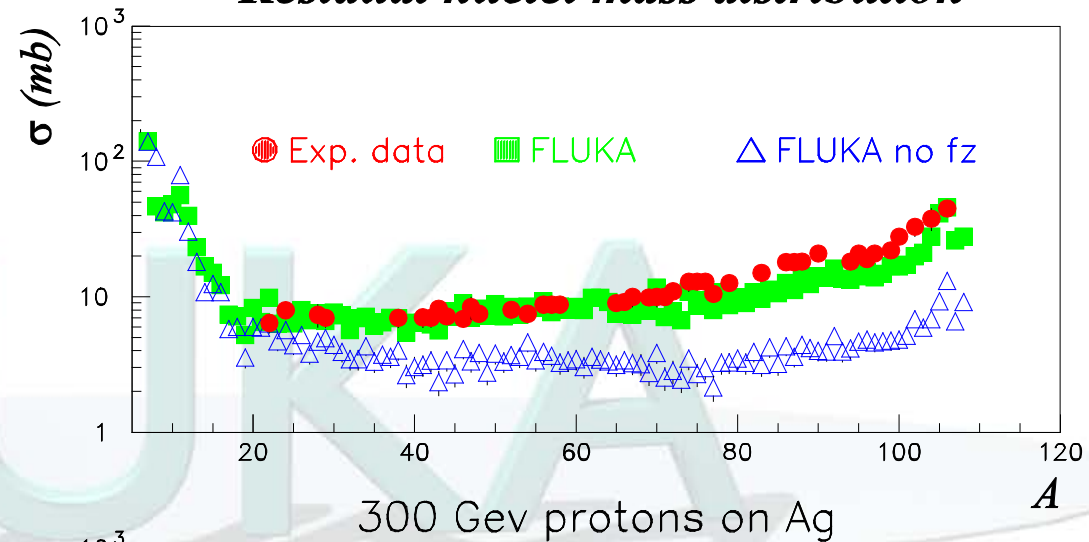
$\langle \pi \rangle = 49.7$ ,  $\langle E_\pi \rangle = 3.4$  GeV

Au **with** and **without** form.zone:

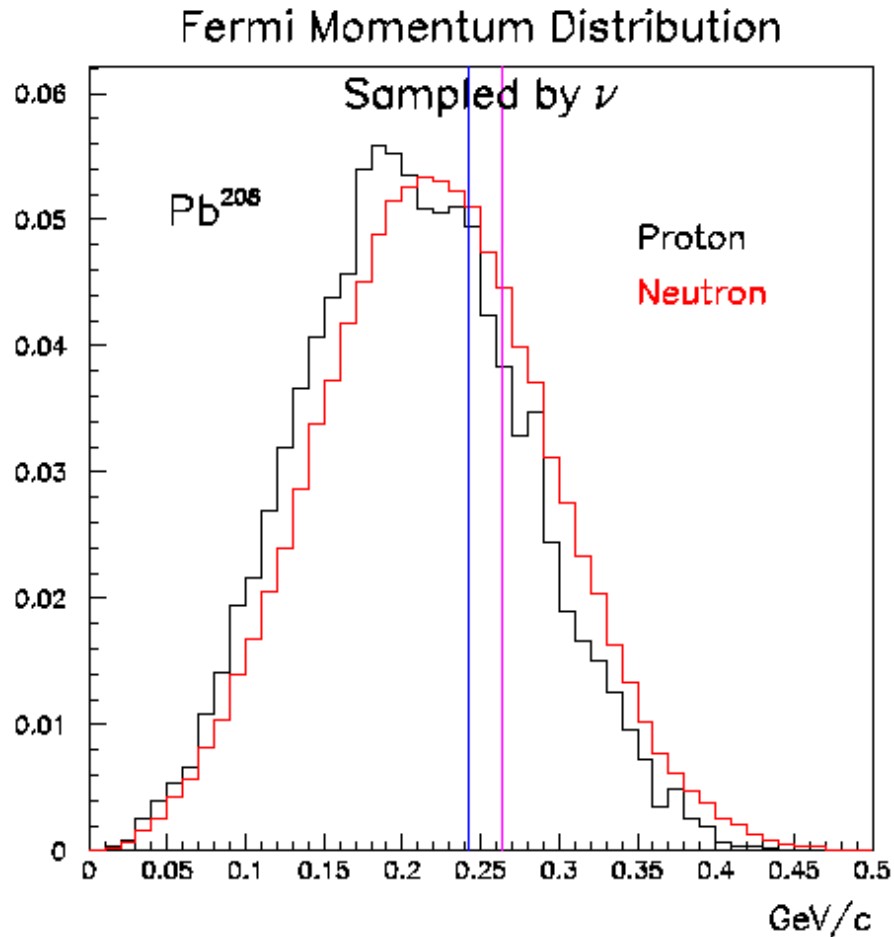
$\langle \pi \rangle = 30.1$ ,  $\langle E_\pi \rangle = 12.5$  GeV

$\langle \pi \rangle = 96.0$ ,  $\langle E_\pi \rangle = 4.6$  GeV

**Residual nuclei mass distribution**



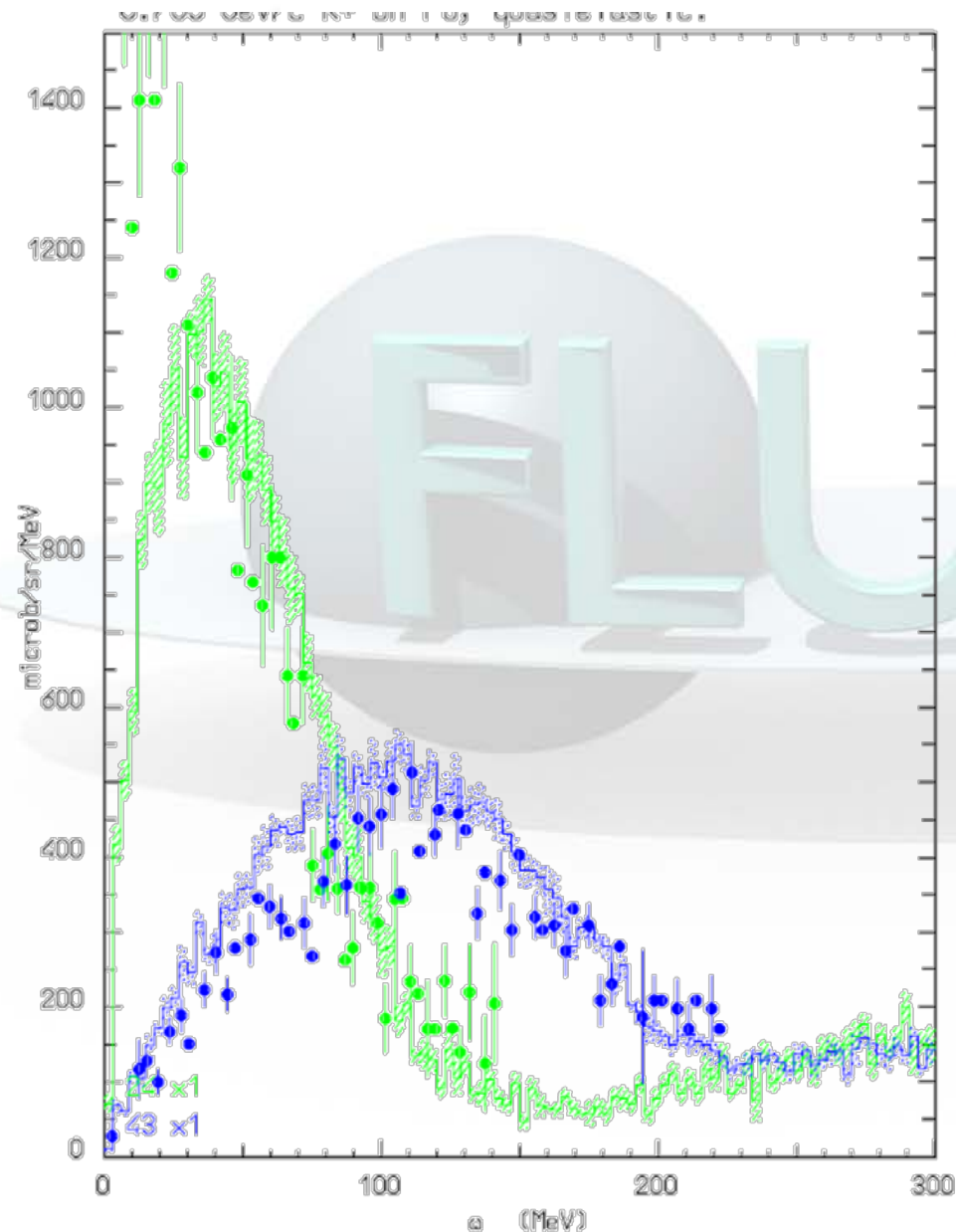
# Example of Fermi distribution



Fermi momentum distribution as "seen" by interacting neutrinos on lead.

Vertical lines: maximum Fermi momentum according to un-smearred distribution

# Positive kaons as a probe of Fermi motion



$K^+$  and  $K^0$

- No low mass  $S=1$  baryons
  - weak  $K^+N$  interaction
  - Only elastic and charge exchange up to  $\approx 800$  MeV/c

$K^+ Pb \rightarrow K^+ Pb$  705 MeV/c

Residual excitation spectrum

With  $K^+$  at  $24^\circ$  (green)

at  $43^\circ$  (blue)

Histogram : FLUKA

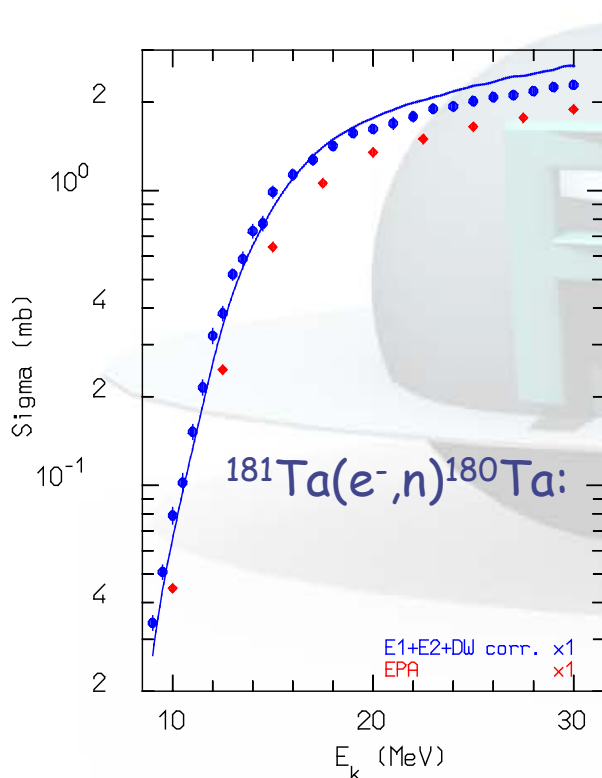
Dots : data (Phys. Rev. C51,669 (1995))

On free nucleon: recoil at 43 MeV or 117 MeV

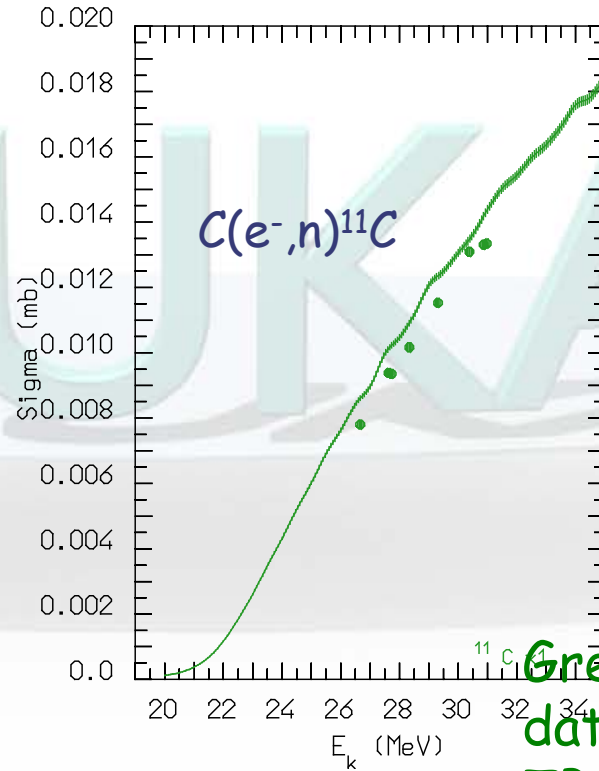
0-deg tail is elastic on nucleus, not included in sim

# Electron scattering

- Quasi-Elastic on nucleon (+ all nuclear)
- Inelastic via virtual photon exchange, recently improved (E1+E2 )



Blue symbols: data from JPG13,515  
Blue line: FLUKA new  
Red symbols: FLUKA with EPA



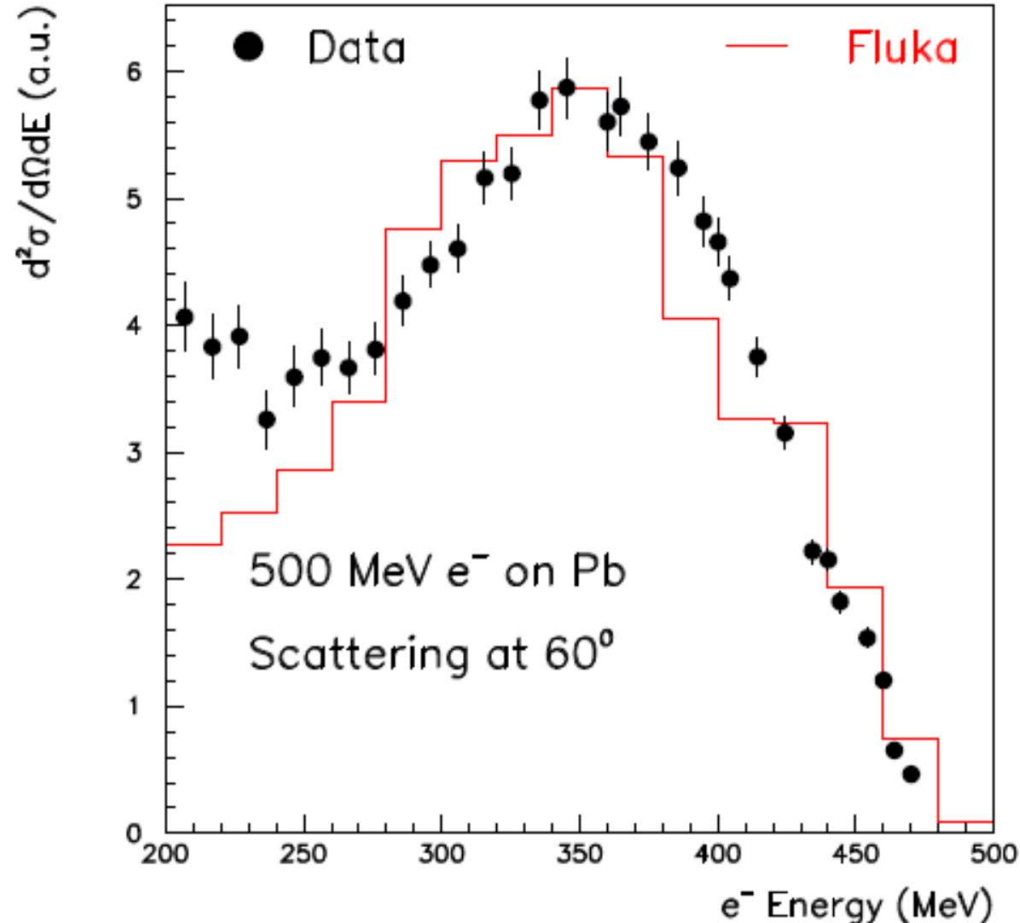
Green symbols:  
data from  
ZPA281,35  
Green curve:  
FLUKA

# First checks with electrons

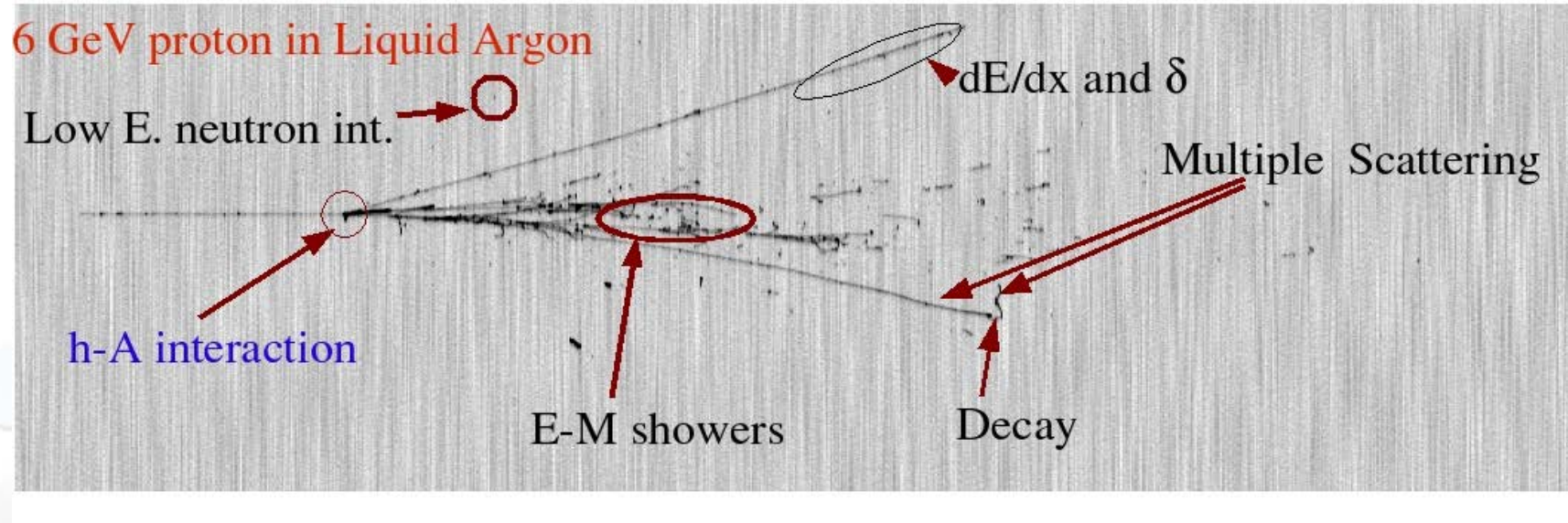
- **Quasi-Elastic scattering** of electrons on Lead, outgoing electron spectrum at  $60^\circ$
- Inelastic tail not included in simulation
- To be improved with the inclusion of **energy-dependent nuclear well**, as already there for nucleon-induced reactions
- **Much more tests needed**

Data:

R.R. Whitney et al., Phys Rev C9,2230 (1974)



# FLUKA : a multi-purpose Monte Carlo code



Web Site: <http://www.fluka.org>

# Extrapolation from $Q^2 = 1.0 \text{ GeV}^2$ to $Q^2 = 0$

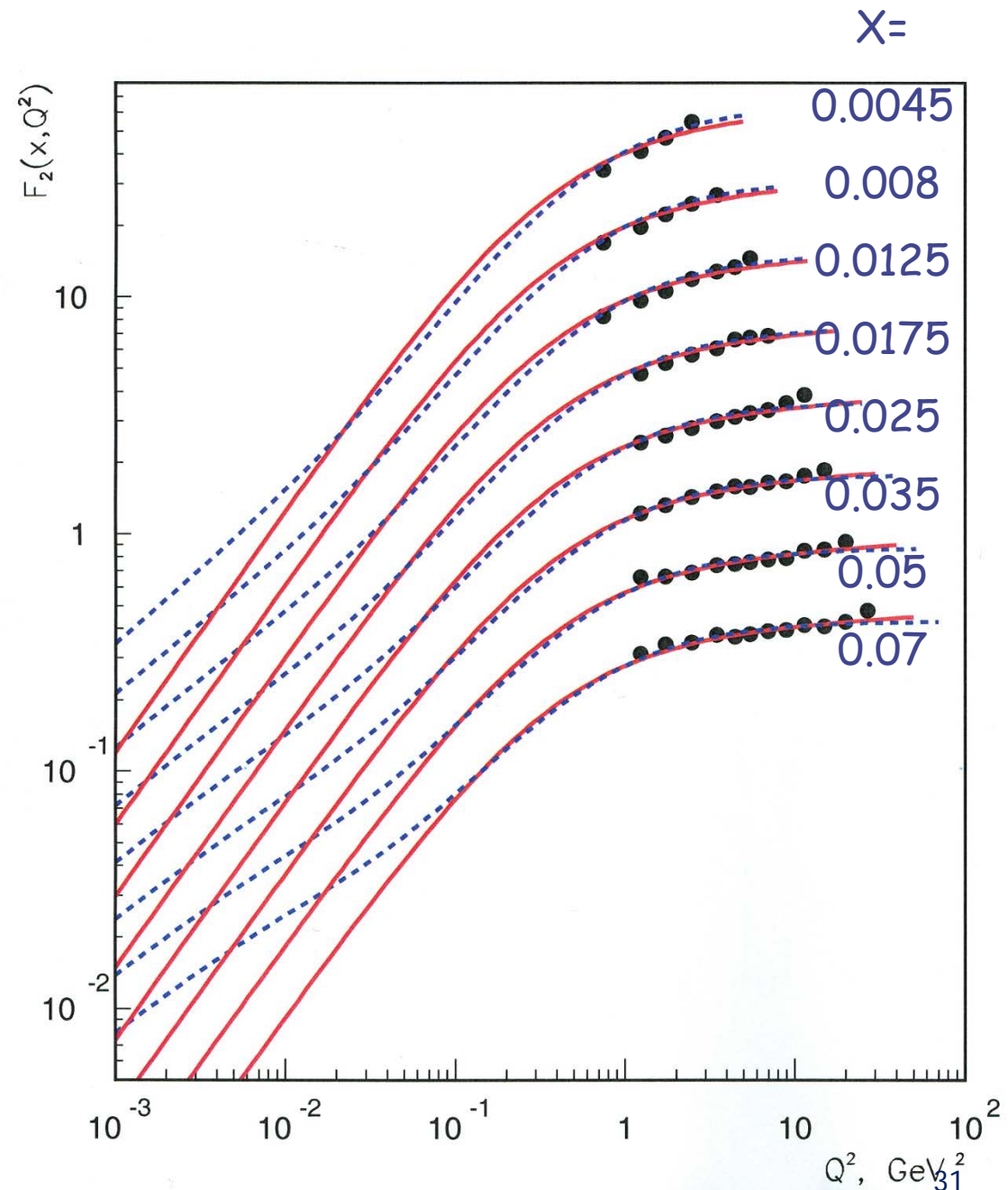
Solid lines: M. Bertini et al. 1996 (Default in NUNDIS)

$$F_2(x, Q^2) = A \left[ 1 + \epsilon \ln(Q^2(1/x - 1) + M^2) \right] \ln(1 + Q^2/(Q^2 + a^2)) .$$

Dashed lines: Donnachie-Landshoff 1994

$$F_2(x, Q^2) \sim Ax^{-0.0808} \left( \frac{Q^2}{Q^2 + a} \right)^{1.0808} + Bx^{0.4525} \left( \frac{Q^2}{Q^2 + b} \right)^{0.5475}$$

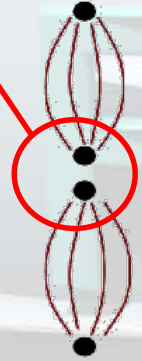
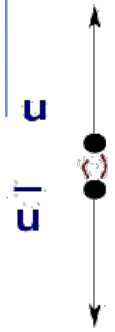
data points from NMC Collab., M. Arneodo et al., Nucl. Phys. B 483 (1997) 3-43  
Data/cuves scaled for clarity, factors from 1 to 128



# The "hadronization" of chains

An example:

Low mass chain: just 2-3 meson/(anti)baryon resonances



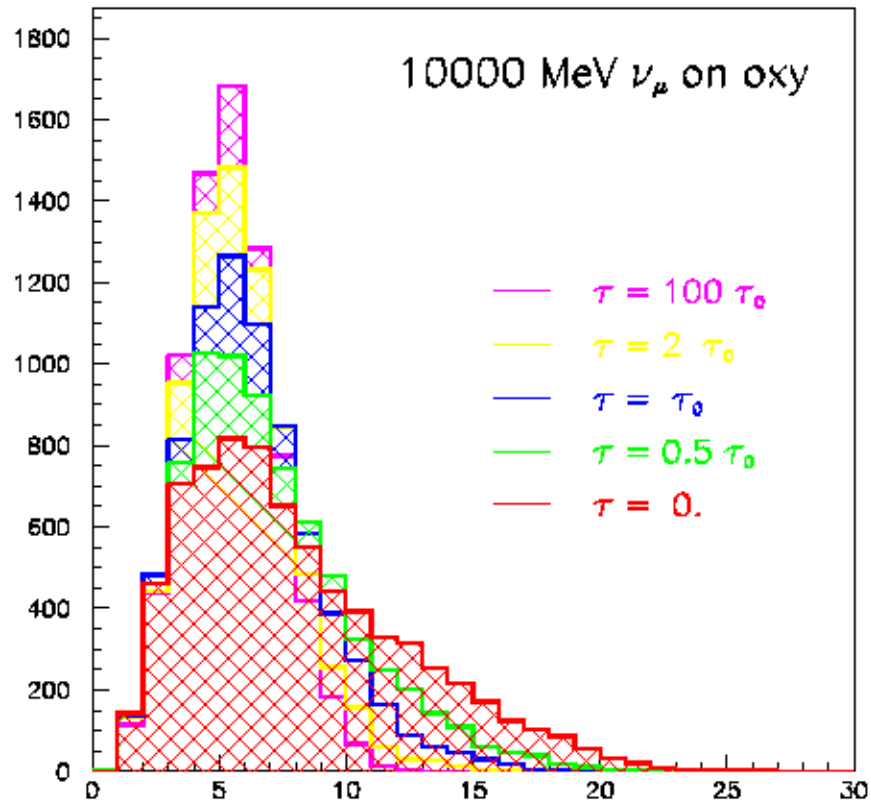
- $u\bar{d}$
- $d\bar{u}$
- $\bar{u}u\bar{d}$
- $udd$
- $u\bar{s}$
- $s\bar{d}$
- $u\bar{d}$
- $q\bar{q}$
- $q\bar{q}$
- $-$
- $\dots$
- $d\bar{u}$

Implementation FLUKA-native  
(evolution of old BAMJET)



# Effect of formation zone, neutrino int.

## Total hadron multiplicity



## Charged hadron spectra

