

PHYSTAT2011

Unfolding: Introduction

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The problem

Given a one-dimensional histogram for a particular variable, obtained in a detector with known experimental resolution, can we estimate the distribution that would have been obtained if the detector did not introduce any smearing? And we need to provide a covariance matrix for our unsmearred distribution.

(Some obvious generalisations of this)

Programme

- 9.10 Victor Panaretos "A statistician's view"
 - 10.00 Volker Blobel "Unfolding methods for particle physics"
 - 10.40 Coffee, and Poster Session
 - 11.10 Guenter Zech "Regularization and error assignment in unfolding"
 - 11.40 Vato Kartvelishvili "Unfolding with SVD"
 - 12.10 Katharina Bierwagen 'Bayesian Unfolding'
 - 12.25 Comparison on HEP methods
 - 12.45 Lunch
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- 2.00 Bogdan Malaescu 'Iterative dynamically stabilized method of data unfolding'
 - 2.25 Kerstin Tackmann 'SVD-based unfolding: implementation and experience'
 - 2.45 Michael Schmelling 'Regularization by control of resolution function'
 - 3.05 Hans Dembinski 'ARU - towards optimal unfolding of data distributions'
 - 3.30 Tim Adye 'Unfolding algorithms and tests using RooUnfold'
 - 3.55 Coffee
 - 4.25 Matthias Weber 'CMS unfolding'
 - 4.55 Georgios Choudalakis 'ATLAS unfolding'
 - 5.25 Jan Fiete Grosse-Oetringhaus 'ALICE unfolding'
 - 5.45 Summary (Victor Panaretos) + Discussion

Non-expert comments on Unfolding

- Why unfold?
- Correction factors
- Choice of bin-size
- How good is your method?
- Error estimates

Why Unfold?

If possible, **don't Unfold data**, but smear theory

When not possible?

- a) Compare data with data from different experiment
- b) Tune MC by fitting QCD parameters to data
- c) Future theories

Also provides more useful result (but complicated correlated errors)

Why Unfold?

If possible, **don't Unfold data**, but smear theory

When not possible?

a) Compare data with data from different experiment

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~~c) Future theories~~

Provide smearing matrix,
so that future theorists can smear
their theories

Also provides nicer picture to look at (but complicated correlated errors)

Matrix method

$$d_i = \sum M_{ij} t_j$$

Assume M_{ij} known with small statistical error from MC {Estimate effect of M_{ij} bias from incorrect resolution}

Max likelihood solution can have large bin-to-bin oscillations. Effect not serious for wide enough bins

Bin-by-bin correction factors

Use MC to find how exptl resolution makes:

'Truth' \rightarrow Observed data Beware MC statistical and systematic errors

$$t_i = C_i * d_i \quad (\text{Contrast} \quad t_i = \sum M^{-1}_{ij} * d_j \text{ for matrix method})$$

Problems:

- 1) $C_i = 0.1$, $d_i = 100 \pm 10 \rightarrow t_i = 10 \pm 1$??
i.e. Error too small. But this error estimate is incorrect
- 2) C_i depends on assumed distribution of t , which we are trying to find.
(For small bin-size, matrix method is less sensitive to distribution of t)
- 3) No bin-to-bin estimates of correlations
- 4) Sum of estimated truth \neq Sum of observed data (Matrix method O.K.)

CONCLUSION: Do not use (Cf Cousins)

Problems with Correction Factors

	Bin 1	Bin 2	Smearing matrix		True	
Truth (not known)	800	200			1	2
Mean observed	760	240	Observed	1	0.9	0.2
				2	0.1	0.8

As t_1	As t_2	Re d_1	Re d_2	CF ₁	CF ₂	Est t_1	Est t_2	Sum
1000	0	900	100	1.11	0	844	0	844
800	200	760	240	1.05	0.83	800	200	1000
760	240	732	268	1.04	0.90	789	215	1004
667	333	667	333	1.00	1.00	760	240	1000
500	500	550	450	0.91	1.11	691	267	958
200	800	340	660	0.59	1.21	447	291	738
0	1000	200	800	0	1.25	0	300	300

As t_i Assumed # in bin i

De d_i Resulting expected # in bin i

CF _{i} Correction factor for bin $i = (As\ t) / (De\ d)$

Est t_i Estimated true # in bin i

Sum Est $t_1 + Est\ t_2$

$$Est\ t_1 = 760 * CF_1 \quad (\text{truth} = 800)$$

$$Est\ t_2 = 240 * CF_2 \quad (\text{truth} = 200)$$

Bin size?

Not too small

M_{ij} has large off-diagonal elements

Not too large

Lose sensitivity

M_{ij} begins to depend on true distribution

Bin width for unfolded distribution also depends on that for data, and on exptl resolution.

Recommendation for optimum?

Regularisation

Damps out oscillations at price of (small?) bias

Recipe for optimal regularisation? (Depends on....)

How to judge which method is 'best'? Challenge?

Bob Cousins' "bottom line test":

Compare 2 theories with data via χ^2 (χ^2_1 and χ^2_2)

a) by smearing theories (well-defined)

b) by unsmearing data (use your favourite method)

Do $\Delta\chi^2 = \chi^2_1 - \chi^2_2$ for a) and for b) agree?

Can unfolded dist have $\sigma < \sqrt{n}$?

Regularisation can produce this.

Cf Straight line fitting to data \rightarrow fitted uncertainties smaller than measured ones

Estimate errors by MC or by bootstrap replications of data

Looking forward to all the talks, and to hearing what Statisticians (especially **Victor Panaretos**) can tell us about the subject.

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Maybe even consensus on 'best approach'?