

## Comparison of codes

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Five codes, which differ only in details:

Method	ARU	GURU	RUN	ResCon	TUnfold
input: matrix $n$ -tuple	?	✓	✓	✓	✓
discretization	B-spl	hist	B-spl	hist	hist
dimension: true	1	1	1	1	$\leq 3$
meas	1	1	$\leq 3$	1	$\leq 3$
Kernel	fcn	MC	MC	MC	MC
statistical meth	ML-Pois	LS	ML-Pois	LS	LS
lin. algebra	diag	SVD	diag	SVD	solution
regularization parameter	entropy $n_{\text{eff}}$	derivative $n_{1/2}$	derivativ. $n_{\text{eff}}$	trunc/Max Ent $n$	derivatives L-curve
covar. matrix automat. binning MC reweighting	propag.	propag.	propag./MC ✓ ✓	propag.	propag.

RUN (Fortran), converted to C++ TRUUEE by Natalie Milke (Uni Dortmund) [natalie.milke\(at\)tu-dortmund.de](mailto:natalie.milke(at)tu-dortmund.de)

# Types of unfolding problems

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## Parametrized unfolding:

parameterized expression with few parameters: no regularization necessary – using normal fit program.

## Parameter-free unfolding: bins (or classes)

- Classification problems, small number: no reduction of number possible;
- Correction of distributions with small migration effects;
- Structureless distributions (small number of Fourier coefficients):
  - Smooth distribution: regularization with possibility to reduce number of bins;
  - Steeply falling: try transformation to remove steepness, evtl. use parametrization
- Unfolding with transformation, evtl.  $> 1$  measured distribution;
- Distributions with narrow structures, peaks: try to use parametrization e.g. Gaussian peaks – using normal fit program.

## Open questions

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- discretization: continuous B-splines of higher order (necessary for re-weighting of MC – RUN) instead of simple discontinuous bins
- input of  $n$ -tuples instead of vectors/matrices
- strategies for steeply falling distributions and for class data (e.g. 2-, 3- ... jet events)
- alternative low-pass filter strategies
- data presentation with small or large number of data points
- projection methods (DCT) in one- and two-dimensions
- case of limited acceptance regions (e.g. low  $p_T$  – using constraints (Lagrange multiplier – RUN)) in one- and two-dimensions
- using general fit program (like `aplcon`) for unfolding? (flexible: e.g. fit may include uncertainty of  $\mathbf{A}$  or background fit)
- uncertainties of response matrix elements
- algorithm for automatic variable bin definition (RUN)
- statistical comparison of information content for different number of degrees of freedom
- use of detailed estimates of the unfolding result (multiplicative, additive)