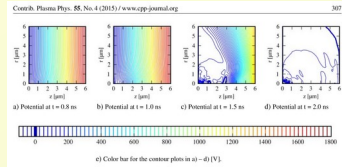
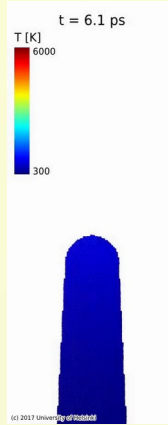
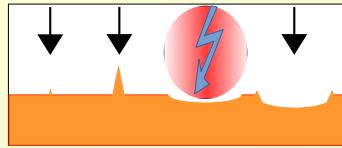




Field enhancer sharpening mechanism via biased surface diffusion

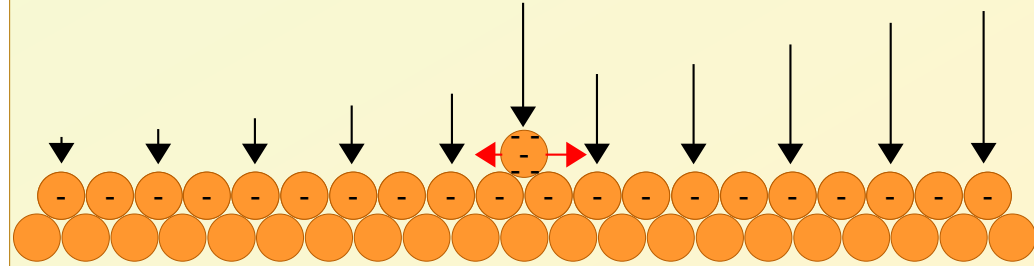
Breakdown mechanism on Cu surface.
Sharpening of initial protrusions lead to runaway?



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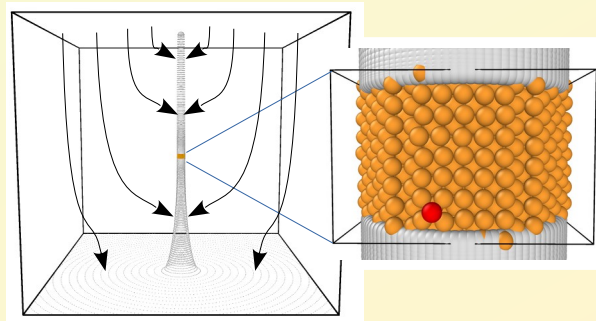
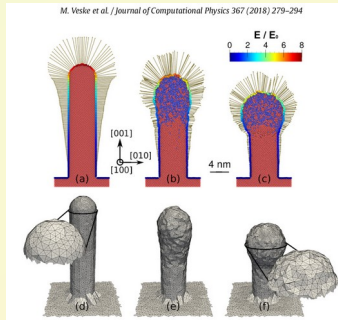


Theory: electric field gradient biases diffusion



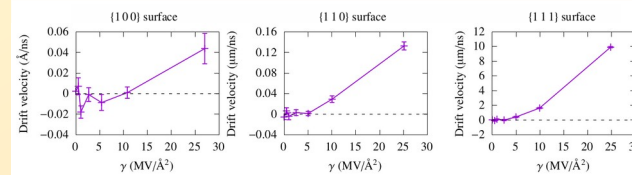
$$\Delta E_m \propto \mathcal{M} \gamma + \mathcal{A} \gamma F$$

Molecular dynamics simulations with E field

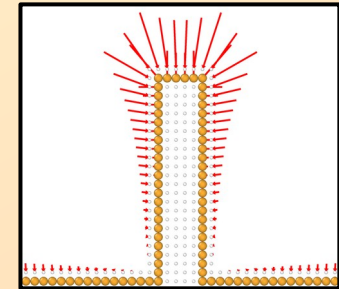


MD coupled with finite elements method Laplace equation solver

Result: Diffusion bias agrees with theory & DFT



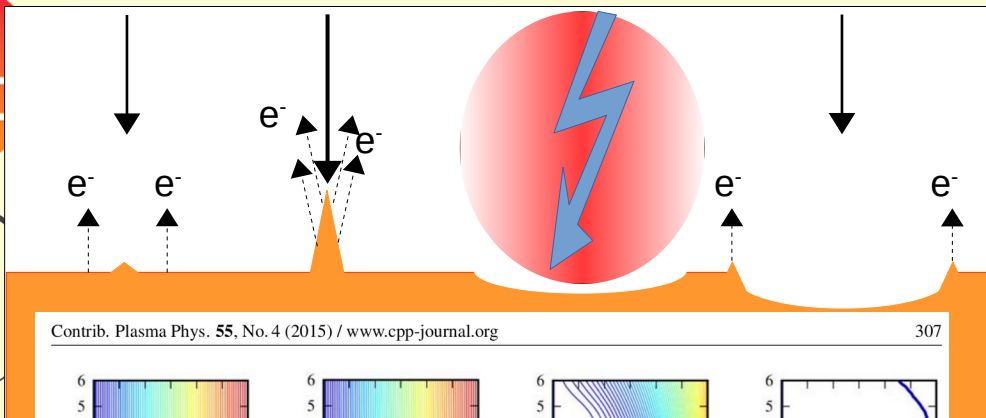
Surface	\mathcal{M} (eÅ)		\mathcal{A} (eÅ ² /V)	
	MD	DFT	MD	DFT
Cu {100}	2 ± 1	0.106 ± 0.003	0.0 ± 0.5	0.27 ± 0.02
Cu {110}	0.7 ± 0.1	0.094 ± 0.006	0.24 ± 0.08	0.30 ± 0.04
Cu {111}	0.61 ± 0.06	0.162 ± 0.003	0.27 ± 0.05	0.23 ± 0.02



Field enhancers facet and sharpen

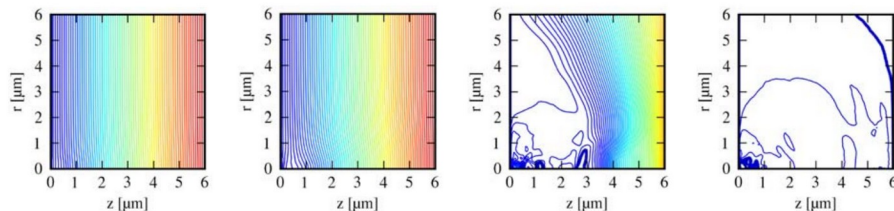
Field enhancer sharpening mechanism via biased surface diffusion

Breakdown mechanism on Cu surface.
Sharpening of initial protrusions lead to runaway?



Contrib. Plasma Phys. 55, No. 4 (2015) / www.cpp-journal.org

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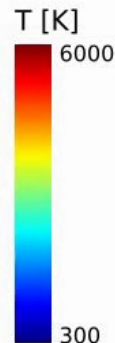


a) Potential at t = 0.8 ns b) Potential at t = 1.0 ns c) Potential at t = 1.5 ns d) Potential at t = 2.0 ns



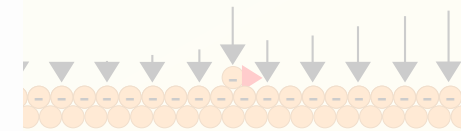
e) Color bar for the contour plots in a) – d) [V].

t = 6.1 ps



A. Kyritsakis et al. *Journal of Physics D: Applied Physics* 51.22 (2018):225203.

Theory

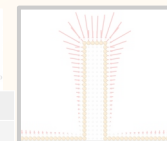


$$\Delta E_m \propto \mathcal{M} \gamma + \mathcal{A} \gamma F$$

Results

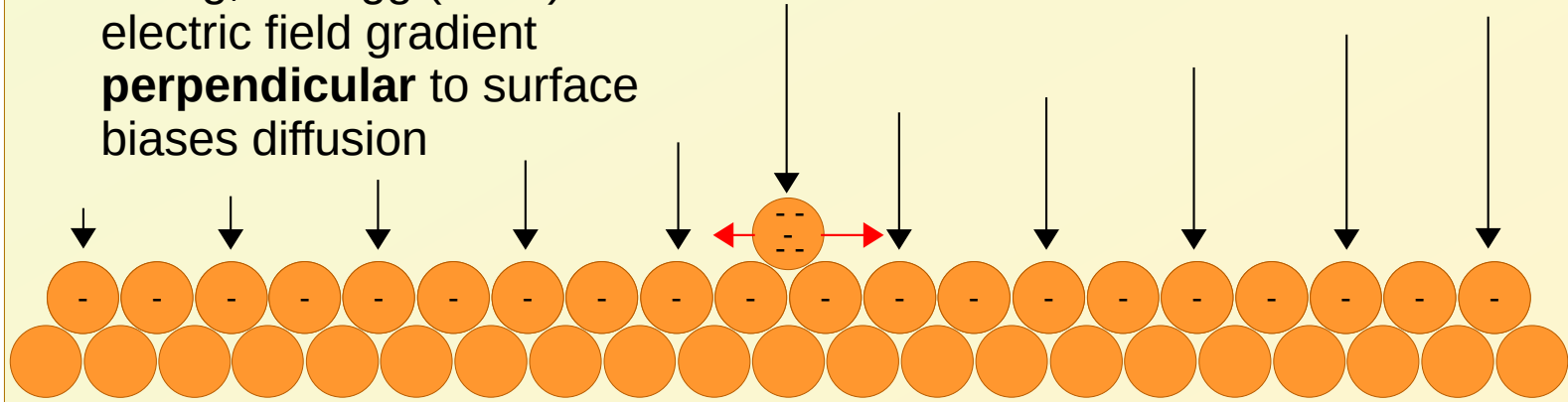


Method	r (nm)		z (nm)	
	MD	DFT	MD	DFT
Δr (nm)	2 ± 1	0.106 ± 0.003	0.0 ± 0.5	0.27 ± 0.02



Theory: electric field gradient biases diffusion

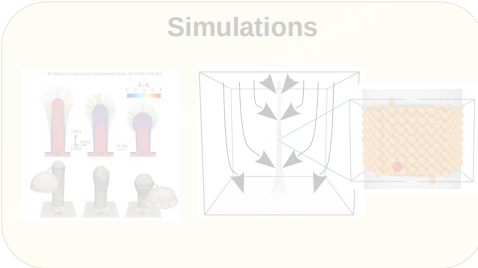
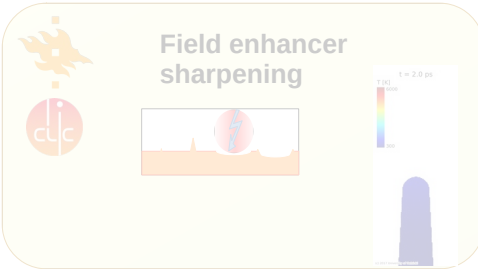
Tsong, Kellogg (1975):
electric field gradient
perpendicular to surface
biases diffusion



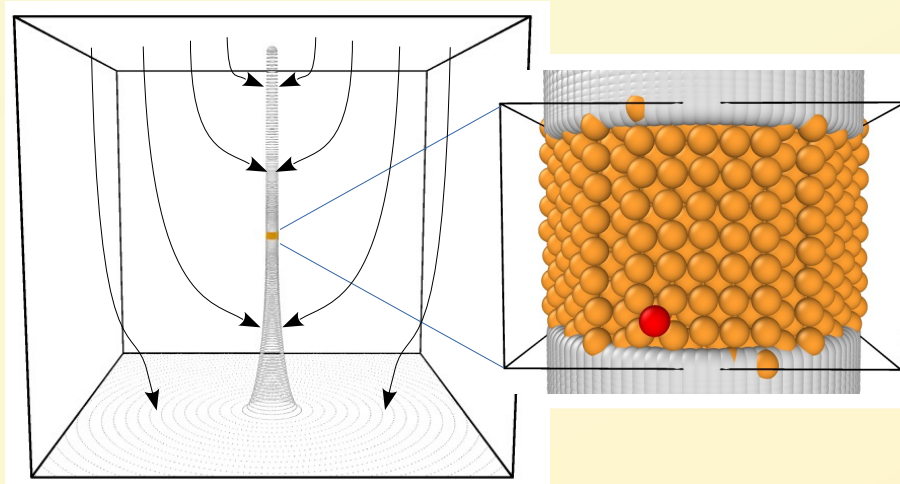
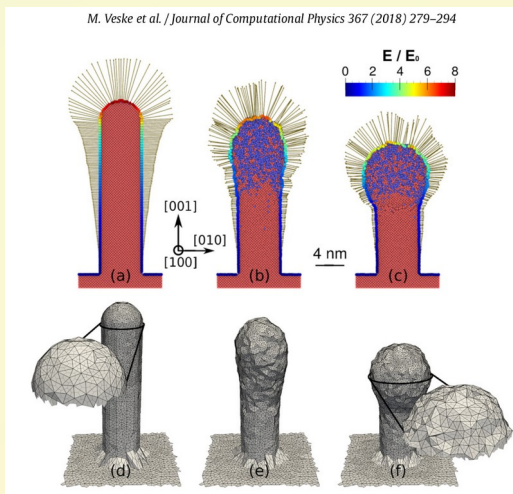
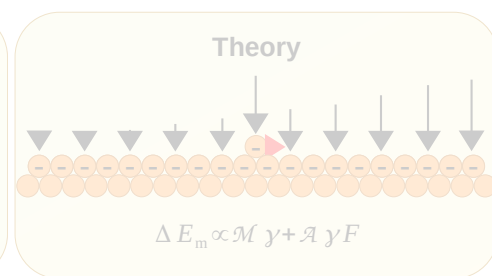
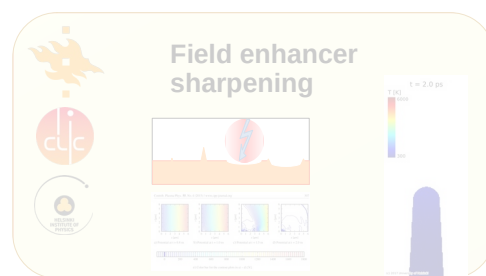
Change in migration energy barrier: $\Delta E_m \propto \mathcal{M} \gamma + \mathcal{A} \gamma F$

dipole moment polarizability

F = electric field
 γ = electric field gradient



Molecular dynamics simulations with E field



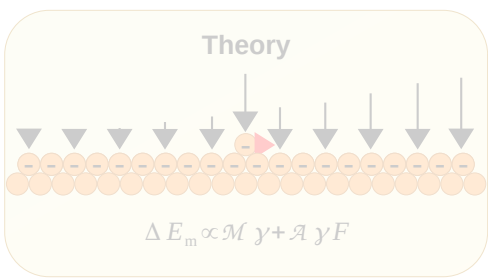
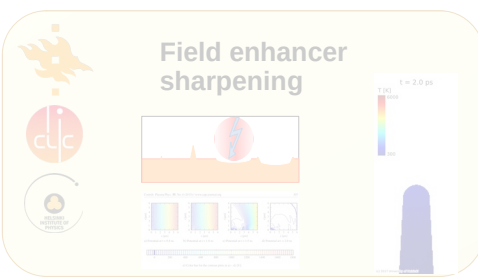
{100} surface accelerated with collective variable hyperdynamics (CVHD)

K. M. Bal and E. C. Neyts.
Journal of chemical theory and Computation **11.10** (2015): 4545–4554

MD coupled with finite elements method Laplace equation solver

Veske, Mihkel, et al. *Journal of Computational Physics* **367** (2018): 279-294.

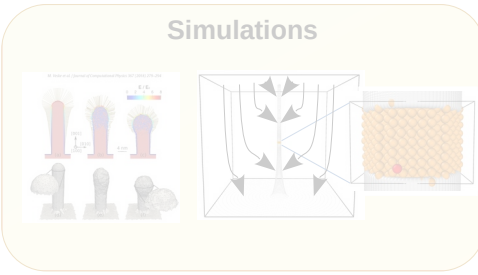
Kimari, Jyri, et al. In preparation.



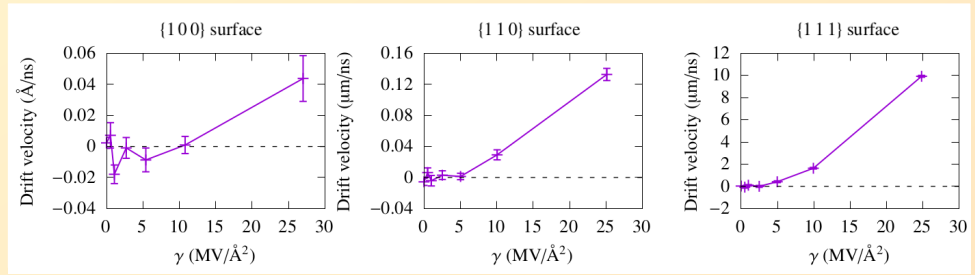
$$\Delta E_m \propto \mathcal{M} \gamma + \mathcal{A} \gamma F$$

dipole moment polarizability

F = electric field, γ = electric field gradient

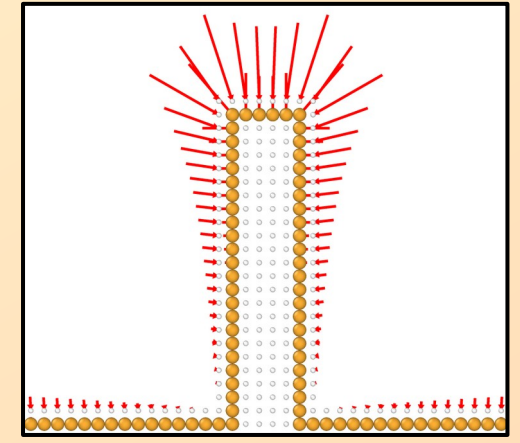


Result: Diffusion bias agrees with theory & DFT



“Drift velocity” ~ bias as function of gradient

Surface	\mathcal{M} ($\text{e}\text{\AA}$)		\mathcal{A} ($\text{e}\text{\AA}^2/\text{V}$)	
	MD	DFT	MD	DFT
Cu {100}	2 ± 1	0.106 ± 0.003	0.0 ± 0.5	0.27 ± 0.02
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Field enhancers facet and sharpen

Electric properties sanity check from DFT