

Phenomenology of LNV in SMEFT at dimension 7

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University of Ioannina



Evidence of New Physics

The Standard Model (SM) is a very successful theory, but it is known to be incomplete by several different observations.

Baryon asymmetry



Evidence from CMB, BBN.

Neutrino masses



Evidence from neutrino oscillations.

Neutrino masses and LNV

One possibility: **Dirac** mass $\nu_L \neq \nu_R^c$

Very small neutrino masses imply very small Yukawa couplings: $y_\nu \sim 10^{-12}$

Well motivated scenario: **Majorana** mass $\nu_L = \nu_R^c$

Neutrino Majorana mass implies **Lepton Number Violation (LNV)**

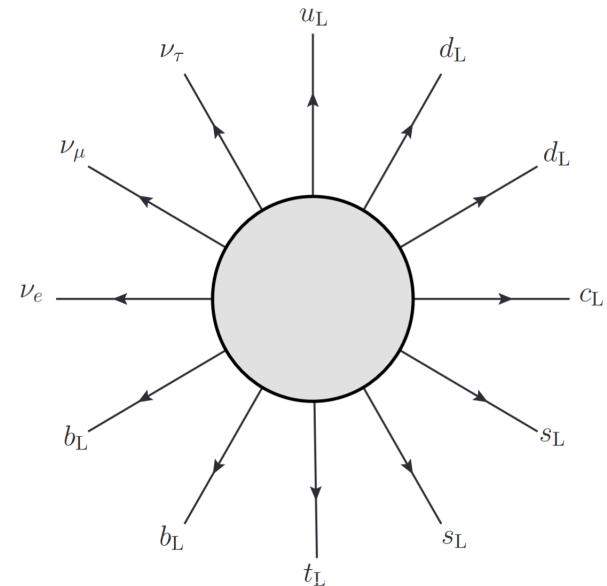
LNV is related to the matter/antimatter asymmetry:

A lepton asymmetry can be converted into a baryon asymmetry via sphaleron transitions (part of the SM)

Majorana neutrino mass: $\Delta L = 2$

Sphalerons: $\Delta L = -\Delta B = 3$

Can LNV be studied in a model-independent way?



SM Effective field theory

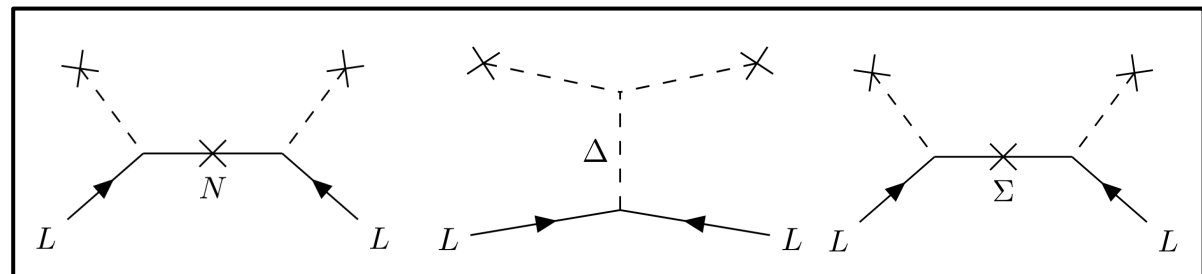
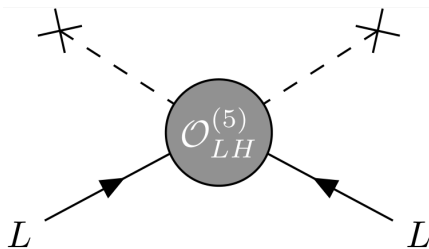
$$\mathcal{L}_{\text{EFT}} = \sum_i C_i \mathcal{O}_i + \text{h.c.} \quad \text{Wilson coefficient: } C_i \propto \frac{1}{\Lambda^{(D-4)}}, \Lambda = \text{New Physics (NP) scale}$$

LVN only occurs at odd mass dimension

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda_1} \mathcal{O}_1^{(5)} + \sum_i \frac{1}{\Lambda_i^3} \mathcal{O}_i^{(7)} + \sum_i \frac{1}{\Lambda_i^5} \mathcal{O}_i^{(9)} + \dots$$

All SMEFT operators up to mass dimension 11 have been classified (excluding derivatives) Babu, Leung (2001), de Gouvêa, Jenkins (2007), Deppisch et. al. (2018)

Lowest dimension for $\Delta L = 2$ LVN: The dimension-5 operator $\mathcal{O}_{LH}^{(5)} = L^\alpha L^\beta H^\rho H^\sigma \epsilon_{\alpha\rho} \epsilon_{\beta\sigma}$

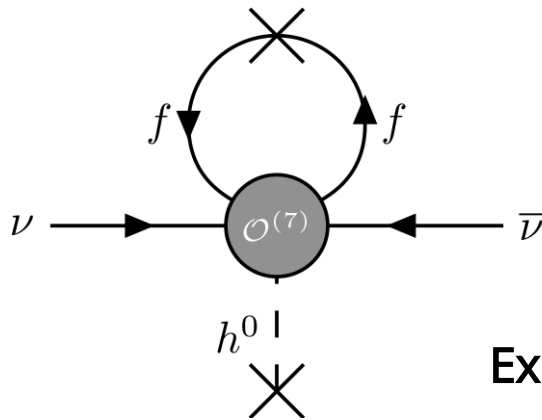


LVN at dimension-7

Second-most simple realization: LVN at dimension-7

e.g. Lehman (2014), Liao, Ma (2019)

- 12 operators instead of one
- Phenomenologically rich: can be UV-completed by 26 different fields in 56 different combinations
- Can lead to radiative neutrino mass



Type	\mathcal{O}	Operator
$\Psi^2 H^4$	\mathcal{O}_{LH}^{pr}	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci}L_r^m)H^jH^n(H^\dagger H)$
$\Psi^2 H^3 D$	\mathcal{O}_{LeHD}^{pr}	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci}\gamma_\mu e_r)H^j(H^m iD^\mu H^n)$
$\Psi^2 H^2 D^2$	\mathcal{O}_{LHD1}^{pr}	$\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci}D_\mu L_r^j)(H^m D^\mu H^n)$
	\mathcal{O}_{LHD2}^{pr}	$\epsilon_{im}\epsilon_{jn}(\overline{L}_p^{ci}D_\mu L_r^j)(H^m D^\mu H^n)$
$\Psi^2 H^2 X$	\mathcal{O}_{LHB}^{pr}	$g\epsilon_{ij}\epsilon_{mn}(\overline{L}_p^{ci}\sigma_{\mu\nu}L_r^m)H^jH^n B^{\mu\nu}$
	\mathcal{O}_{LHW}^{pr}	$g'\epsilon_{ij}(\epsilon\tau^I)_{mn}(\overline{L}_p^{ci}\sigma_{\mu\nu}L_r^m)H^jH^n W^{I\mu\nu}$
$\Psi^4 D$	$\mathcal{O}_{duLLD}^{prst}$	$\epsilon_{ij}(\overline{d}_p\gamma_\mu u_r)(\overline{L}_s^{ci}iD^\mu L_t^j)$
$\Psi^4 H$	$\mathcal{O}_{eLLLH}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\overline{e}_p L_r^i)(\overline{L}_s^{cj}L_t^m)H^n$
	$\mathcal{O}_{dLueH}^{prst}$	$\epsilon_{ij}(\overline{d}_p L_r^i)(\overline{u}_s^c e_t)H^j$
	$\mathcal{O}_{dLQLH1}^{prst}$	$\epsilon_{ij}\epsilon_{mn}(\overline{d}_p L_r^i)(\overline{Q}_s^{cj}L_t^m)H^n$
	$\mathcal{O}_{dLQLH2}^{prst}$	$\epsilon_{im}\epsilon_{jn}(\overline{d}_p L_r^i)(\overline{Q}_s^{cj}L_t^m)H^n$
	$\mathcal{O}_{QuLLH}^{prst}$	$\epsilon_{ij}(\overline{Q}_p u_r)(\overline{L}_s^{ci}L_t^j)H^j$

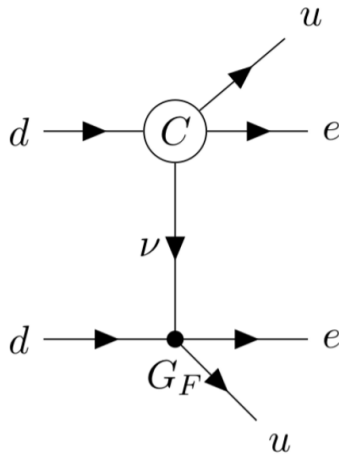
Experimental probes of dimension-7 LVN?

Neutrinoless double beta decay

Neutrinoless double beta decay ($0\nu\beta\beta$):

+Most sensitive probe of LNV

-Only sensitive to electron flavour

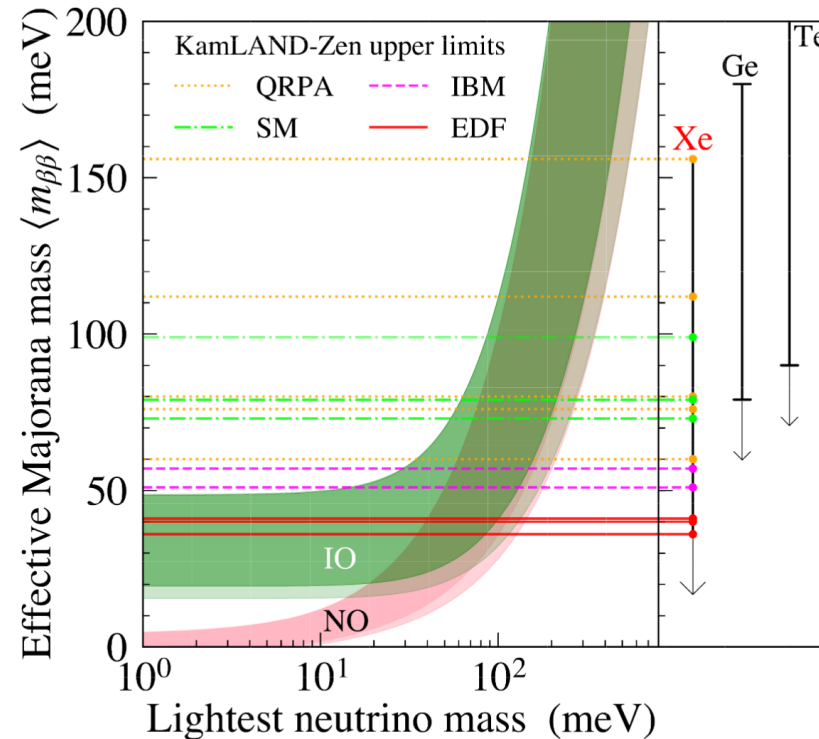


e.g. Cirigliano et. al. (2017)

Dimension-7 LNV operators
give rise to long-range
contributions to $0\nu\beta\beta$ decay

Currently most stringent limit:

$$T_{1/2}^{136\text{Xe}} \leq 2.3 \times 10^{26} \text{ yrs, 90\% C.L.}$$



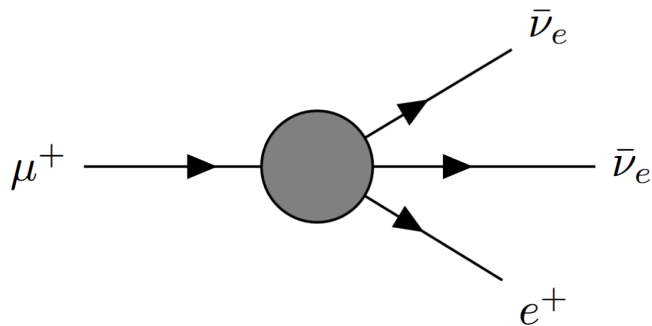
KamLAND-Zen collaboration (2022)

The muon sector

LNV μ decay: $\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu$

+ Includes the μ flavour

- Probes only a single operator



e.g. Cirigliano et. al. (2017)

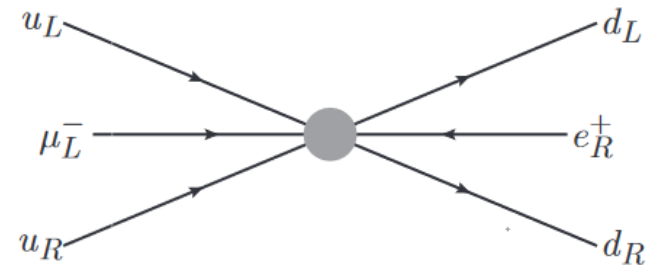
$$\text{BR}(\mu^+ \rightarrow e^+ \bar{\nu}_e \bar{\nu}_\mu) \lesssim 0.9 \times 10^{-3}$$

KARMEN collaboration (2003)

μ^- to e^+ conversion

+ Includes the μ flavour

- Dimension-9



e.g. Berryman, de Gouvêa, Kelly, Kobach (2017)

$$R_{\mu^- e^+}^{\text{Ti}} \equiv \frac{\Gamma(\mu^- + \text{Ti} \rightarrow e^+ + \text{Ca})}{\Gamma(\mu^- + \text{Ti} \rightarrow \nu_\mu + \text{Sc})} < 1.7 \times 10^{-12}$$

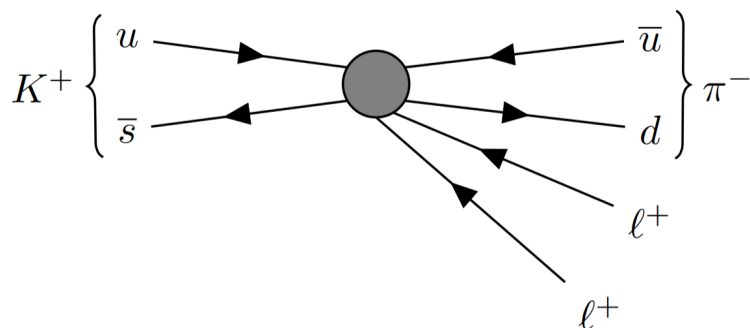
SINDRUM II collaboration (1998)

LVN in meson decays (e.g. kaons)

Double charged lepton final state

+Guaranteed LVN
-Dimension-9

e.g. Chun, Das, Mandal,
Mitra, Sinha (2019)



Muons or electrons in the final state

$$\text{BR}(K^+ \rightarrow \pi^- \mu^+ \mu^+) \leq 4.2 \times 10^{-11}, 90\% \text{ C.L.}$$

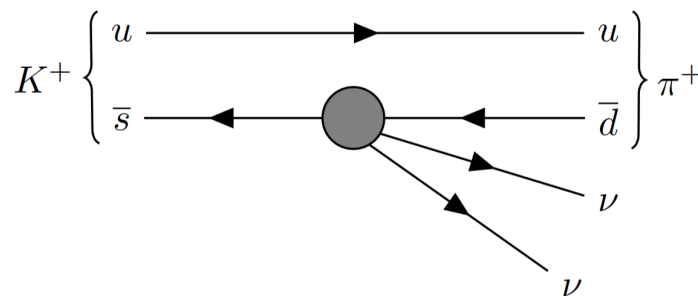
NA62 collaboration (2019)

Two-neutrino final state (rare)

+Dimension-7

-LVN not guaranteed

e.g. Li, Ma, Schmidt (2019)
Deppisch, KF, Harz (2020)



Cannot determine flavour of neutrinos

Experiment:

$$\text{BR}(K^+ \rightarrow \pi^- \nu \bar{\nu}) = (10.6^{+4.9}_{-4.3}) \times 10^{-11}, 68\% \text{ C.L.}$$

NA62 collaboration (2021)

SM expectation:

$$\text{BR}(K^+ \rightarrow \pi^- \nu \bar{\nu}) = (8.4 \pm 1.0) \times 10^{-11}$$

Buras et. al. (2015)

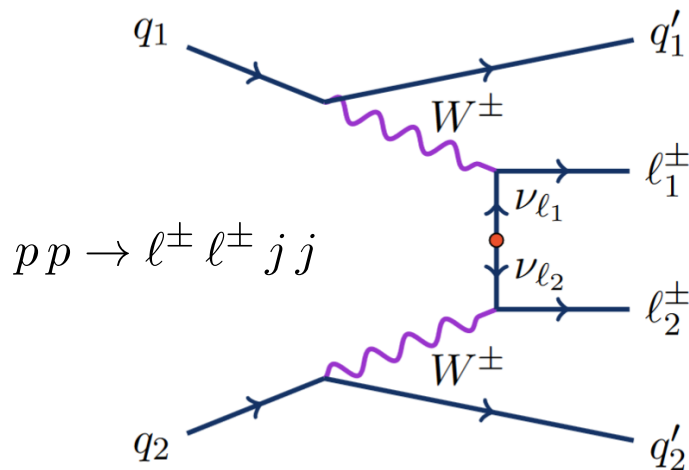
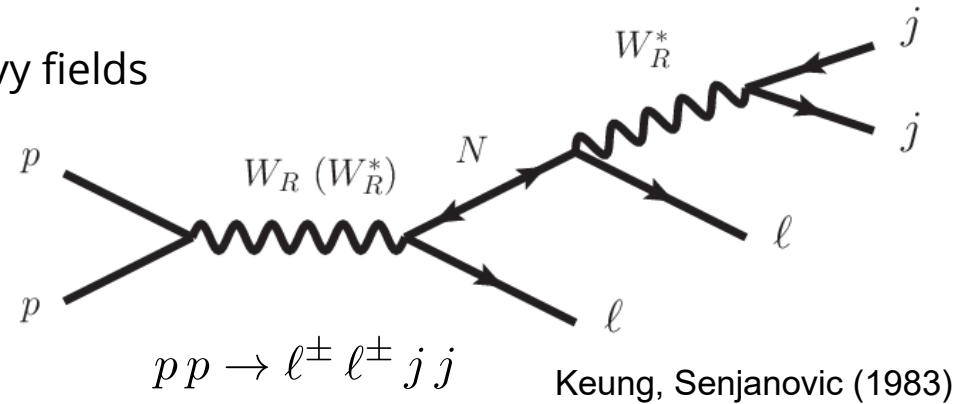
LVN at the LHC

Keung-Senjanović process: leads to LVN at **dimension-9** when integrating out the heavy fields

Probes $5 \text{ GeV} \gtrsim m_N \gtrsim 50 \text{ GeV}$

for couplings $|U_{e/\mu}| \gtrsim 10^{-5}$

ATLAS collaboration (2019) + ...



Fuks et. al. (2021)

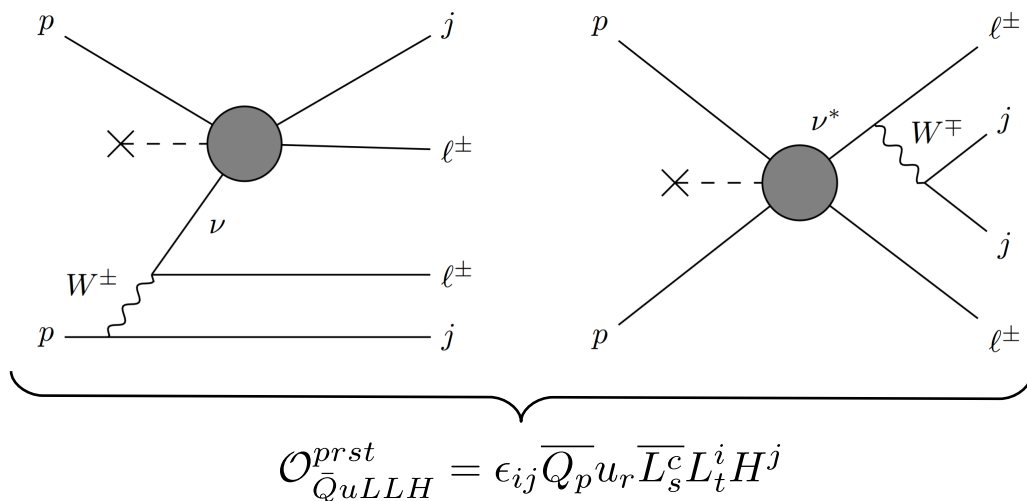
Possible to probe the **dimension-5** Weinberg operator at colliders in vector boson fusion

$$m_{\mu\mu} < 10.8 \text{ GeV at 95\% C.L.}$$

$$m_{\ell\ell'} = \frac{C_{\ell\ell'} v^2}{\Lambda} \quad \text{CMS collaboration (2022)}$$

Dimension-7 LNV at the LHC

Nine out of the twelve dimension-7 $\Delta L=2$ LNV operators lead to $pp \rightarrow \ell^\pm \ell^\pm jj$



$$\mathcal{O}_{\bar{d}uLLD}^{prst} = \epsilon_{ij} \bar{d}_p \gamma_\mu u_r \bar{L}_s^c i D^\mu L_t^j$$

Leads to the same signal as for dimension-9 processes: we can use existing LHC results and compare with EFT cross section obtained using `MADGRAPH5_AMC@NLO`

Alwall et. al. (2014)

J. High Energ. Phys. (2019) 2019: 16
DOI: [10.1007/JHEP01\(2019\)016](https://doi.org/10.1007/JHEP01(2019)016)

CERN-EP-2018-199
13th November 2019

Search for heavy Majorana or Dirac neutrinos and right-handed W gauge bosons in final states with two charged leptons and two jets at $\sqrt{s} = 13$ TeV with the ATLAS detector

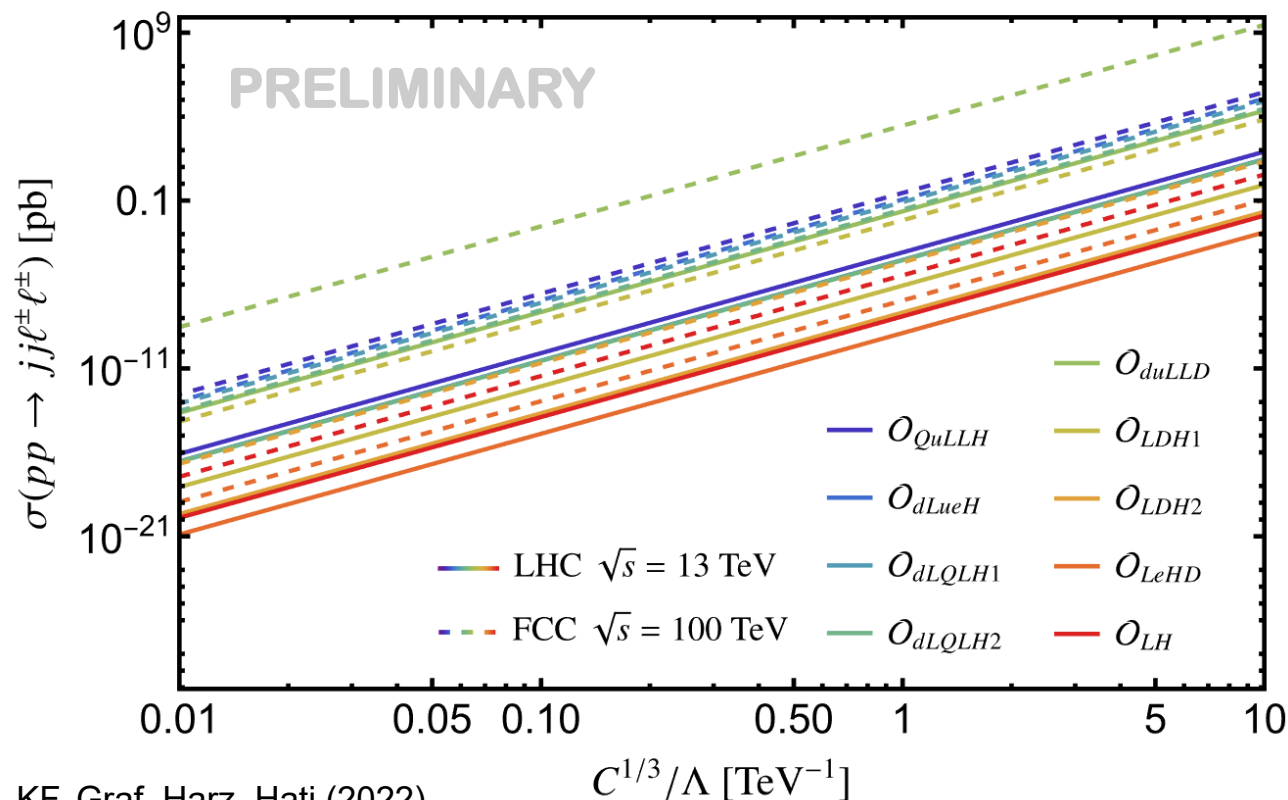


No events in 36.1 fb^{-1} of data.



Leads to constraints on Λ_{LNV}

LHC results for dimension-7



LVN scales in TeV

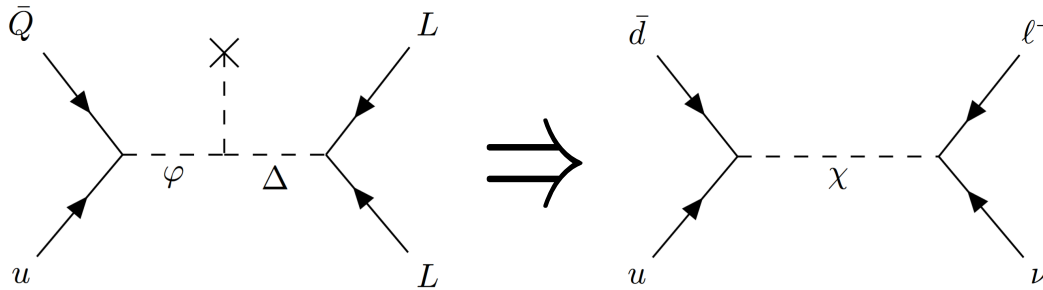
Operator	Λ_{LVN}	$\Lambda_{LVN}^{\text{future}}$
O_{dLueH}	0.72	5.1
O_{dLQLH1}	0.71	4.8
O_{dLQLH2}	0.71	4.1
$O_{\bar{Q}uLLH}$	0.85	6.0
O_{LDH1}	0.40	3.2
O_{LDH2}	0.22	1.2
O_{LeHD}	0.13	0.51
O_{duLLD}	2.2	28
O_{LH}	0.20	0.91

Constraints at 95% C.L.

LVN scales $\sim O(1 \text{ TeV})$ are constrained by same-sign dilepton plus dijet searches at the LHC

For FCC the constraints could reach $\sim O(\text{few TeV})$ up to $\sim 30 \text{ TeV}$

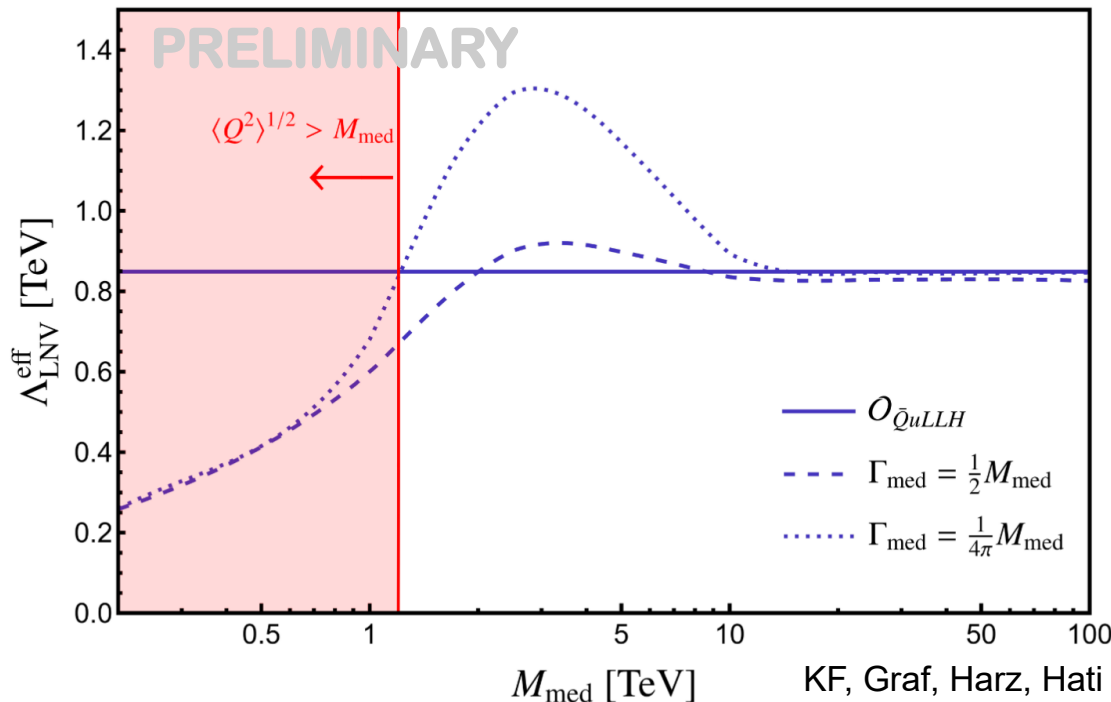
EFT vs simplified model



We can compare the EFT approach with a simplified model example to see how well it performs

$$\mathcal{O}_{\bar{Q}uLLH} = \epsilon_{ij} \bar{Q}u \bar{L}^c L^i H^j$$

$$\mathcal{L} \supset \lambda_1 \bar{d}_L u_{RH} \chi^* + \lambda_2 \bar{e}_L^c \nu_{LH} \chi + \text{h.c.}$$

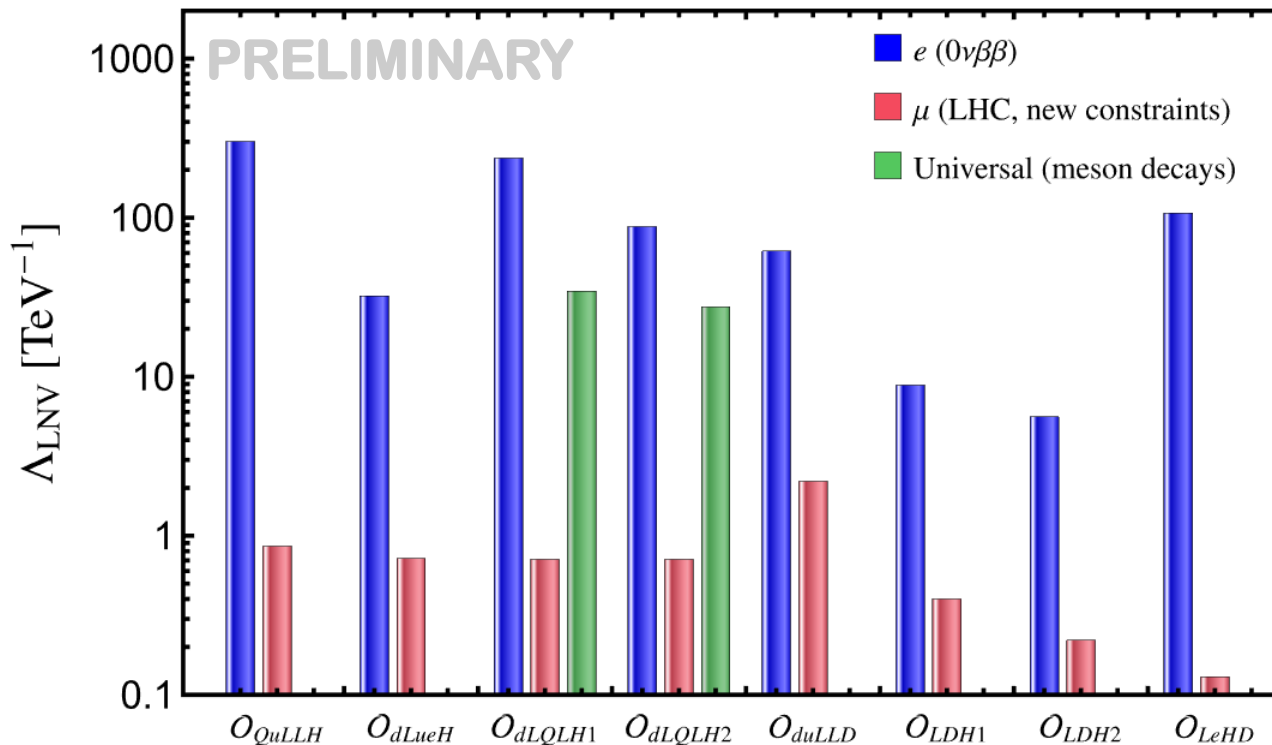


Using the relation

$$\frac{\lambda_1 \lambda_2}{M_{\text{med}}^2} = \frac{v}{(\Lambda_{\text{LNV}}^{\text{eff}})^3}$$

we naively expect the same cross section for the simplified model and EFT operator

Comparison of different probes



KF, Graf, Harz, Hati (2022)

The red bars constitute new constraints on dimension-7 operators using LHC results

We see that LHC offers the most effective way to probe the μ flavour content of dimension-7 $\Delta L = 2$ SMEFT operators

Conclusion

- Neutrino masses may violate lepton number via a Majorana mass term, which in turn could be connected to the baryon asymmetry via leptogenesis.
- Dimension-7 LNV operators offer the second simplest solution to realize LNV mechanisms on an effective level.
- We find that the most stringent μ -sector constraints on the scale of LNV in many dimension-7 operators come from collider searches.

Thank you

Backup slides

Limitations on the EFT approach

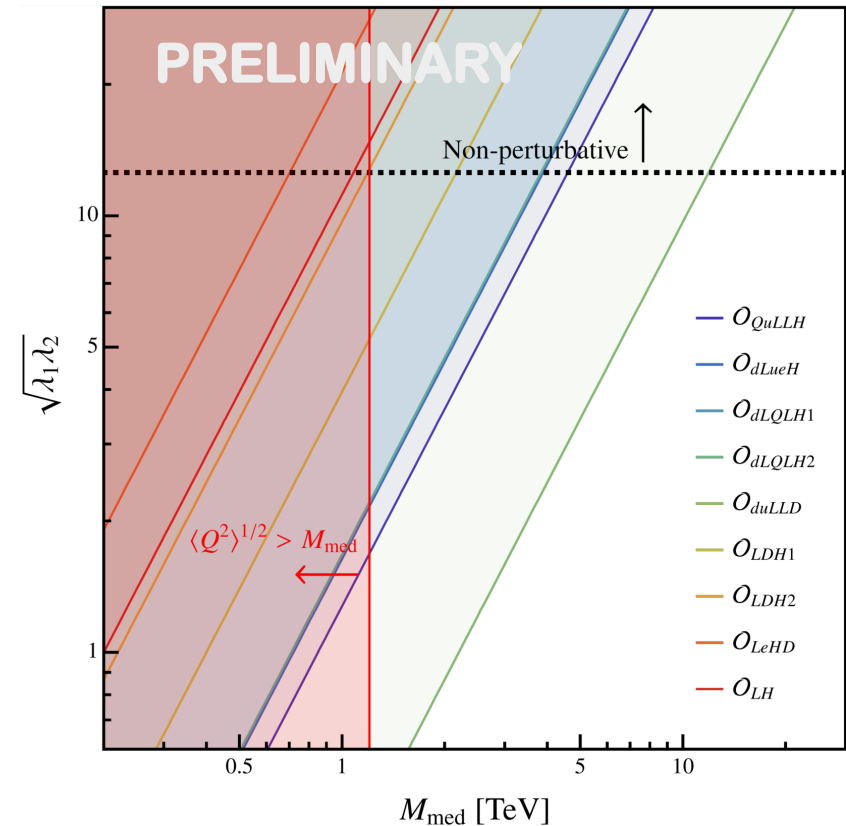
EFTs are only valid for $M_{\text{med}}^2 > Q^2$

$$\frac{1}{Q^2 - M_{\text{med}}^2} = -\frac{1}{M_{\text{med}}^2} \left[1 + \frac{Q^2}{M_{\text{med}}^2} + \mathcal{O}\left(\frac{Q^4}{M_{\text{med}}^4}\right) \right]$$

We can compare effective mediator mass with the average momentum transfer to get an idea of the validity range

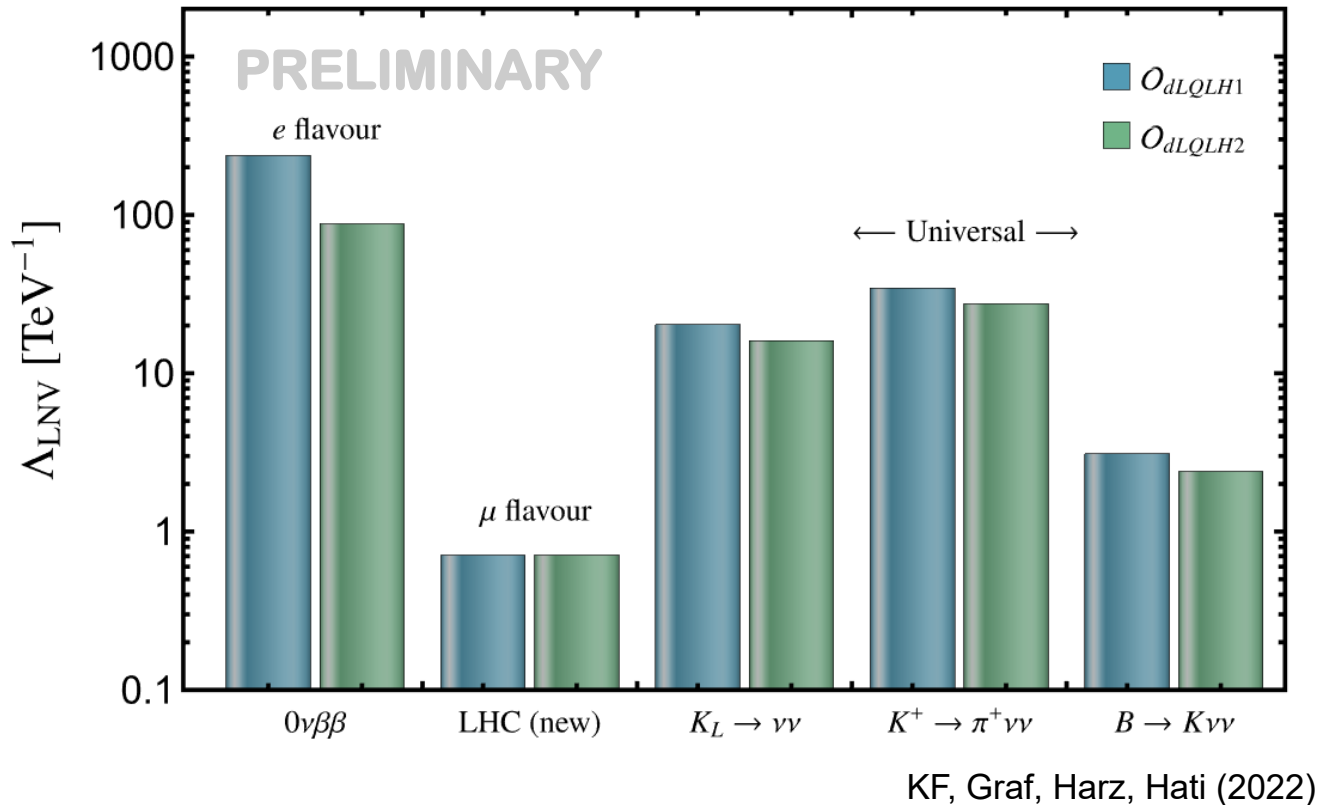
$$\Lambda_{\text{LNV}} = M_{\text{med}} / (\lambda_1 \lambda_2)^{1/3}$$

$$\langle Q^2 \rangle = \frac{\sum_{q\bar{q}} \int (\text{PDF} \times \text{PDF}) Q^2}{\sum_{q\bar{q}} \int (\text{PDF} \times \text{PDF})}$$



KF, Graf, Harz, Hati (2022)

Details of meson decay probes



Two operators are constrained by rare meson decays: no handle on flavour content since the final state neutrinos are not observed

Li, Ma, Schmidt (2019), Deppisch, KF, Harz (2020)

Operator explosion

“Explode” an operator to find all possible tree-level UV completions using combinatorics

$$\mathcal{O}_{\bar{Q}uLLH} = \epsilon_{ij}(\bar{Q}u)(\bar{L}^C L^i)H^j \rightarrow \epsilon_{ij} \bar{Q}^k u L^k L^i H^j$$

$$\mathcal{O}_{\bar{Q}uLLH} \rightarrow \epsilon_{ij} \chi_1^k L^k L^i H^j / \epsilon_{ij} \phi_1^k u L^i H^j / \epsilon_{ij} \psi_1^k u L^k H^j / \epsilon_{ij} \xi_1^k u L^k L^i$$

Leads to $4 \times 3 = 12$ models, but not all are unique.

$\chi_1 \sim S(1, 2, 1/2)$	$\psi_1 \sim V(\bar{3}, 1, -2/3)$	$\phi_1 \sim V(\bar{3}, 3, -2/3)$	$\xi_1 \sim F_L(\bar{3}, 3, 1/3)$
$\chi_2 \sim F_R(1, 1, 0)$	$\psi_2 \sim F_R(1, 1, 0)$	$\phi_2 \sim F_R(1, 3, 0)$	$\xi_2 \sim S(1, 3, 1)$
$\chi_3 \sim F_R(1, 3, 0)$	$\psi_3 \sim F_L(\bar{3}, 2, -7/6)$	$\phi_3 \sim F_L(\bar{3}, 2, -7/6)$	$\xi_3 \sim V(\bar{3}, 2, -1/6)$
$\chi_4 \sim S(1, 3, 1)$	$\psi_4 \sim V(\bar{3}, 2, -1/6)$	$\phi_4 \sim V(\bar{3}, 2, -1/6)$	$\xi_4 \sim V(\bar{3}, 2, -1/6)$

Here we find the simplified model that we used as an example earlier

Teaser: neutrino mass

Given all possible tree-level UV-completions of a dimension-7 operator, we can classify them in terms of the neutrino mass topology

We can then compare with the different EFT LNV constraints to see which mass mechanisms are excluded....
[Look to arXiv:2207:XXXXX](#)

○ = Generates the dimension-5 Weinberg operator

$$\mathcal{O}_{\overline{Q}uLLH} = \epsilon_{ij} (\overline{Q}_p u_r) (\overline{L}_s^c L_t^i) H^j$$

	Δ	φ	N	Σ	Q_7	T_1^\dagger	U_1	\bar{V}_2^\dagger	U_3
Δ		I			II	II			
φ			○	○					
N							○	○	
Σ								○	○
Q_7							II		II
T_1^\dagger								II	
U_1								I	
\bar{V}_2^\dagger									I
U_3									

KF, Graf, Harz, Hati (2022)

Field	Rep ($SU(3)_c, SU(2)_L, U(1)_Y$) (3B)
Δ	$S(1, 3, 1)(0)$
φ	$S(1, 2, 1/2)(0)$
N	$F(1, 1, 0)(0)$
Σ	$F(1, 3, 0)(0)$
Q_7	$F(3, 2, 7/6)(1)$
T_1	$F(3, 3, -1/3)(1)$
U_1	$V(3, 1, 2/3)(1)$
\bar{V}_2	$V(\bar{3}, 2, -1/6)(-1)$
U_3	$V(3, 3, 2/3)(1)$

