

# GRAVITATIONAL WAVES: observational forays into fundamental physics

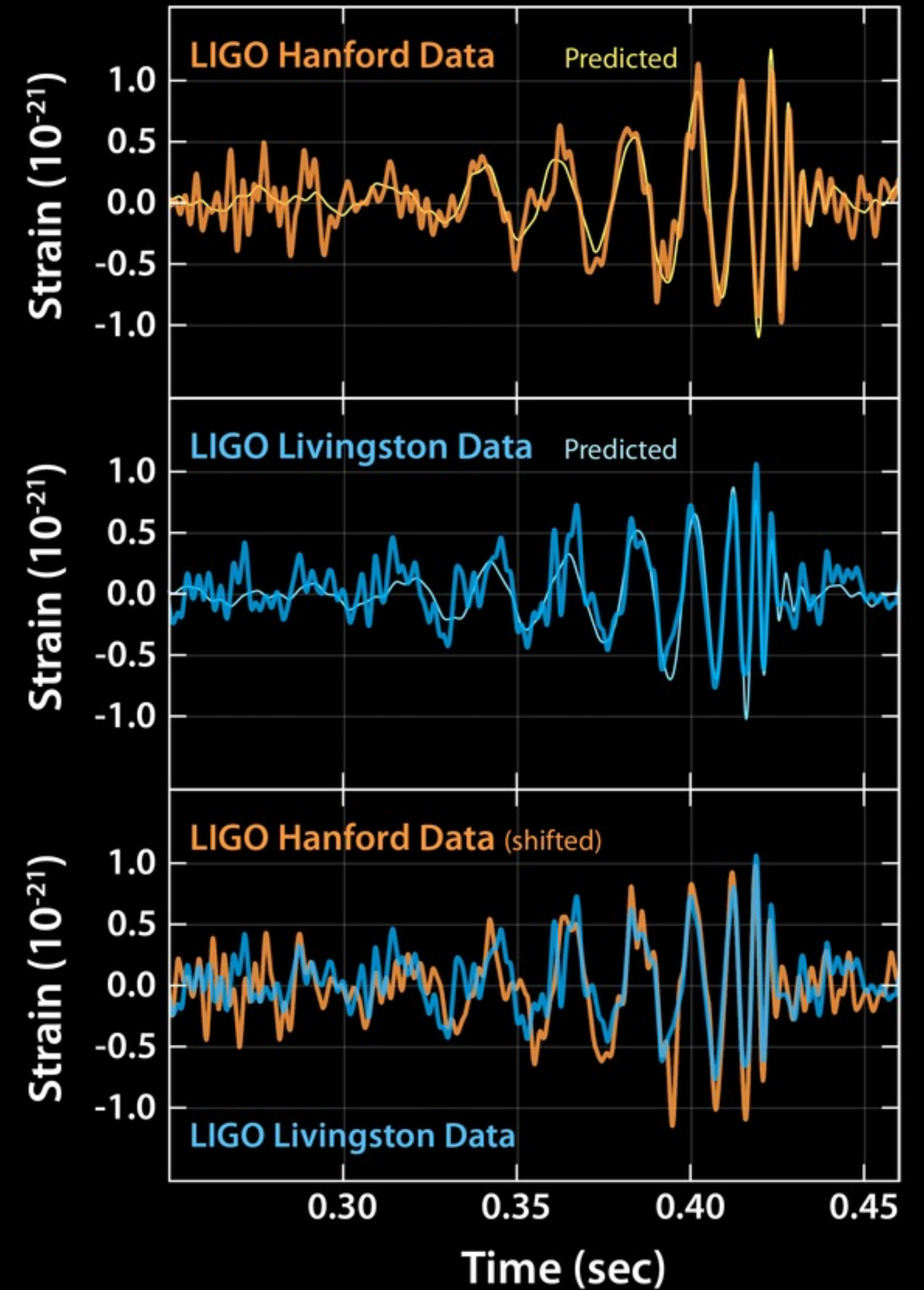
Michalis Agathos



# Outline

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- GW detections
- Tests of GR
- Fundamental fields
- Peculiar observations
- Stochastic GW Background
- Next generation





LIGO Hanford



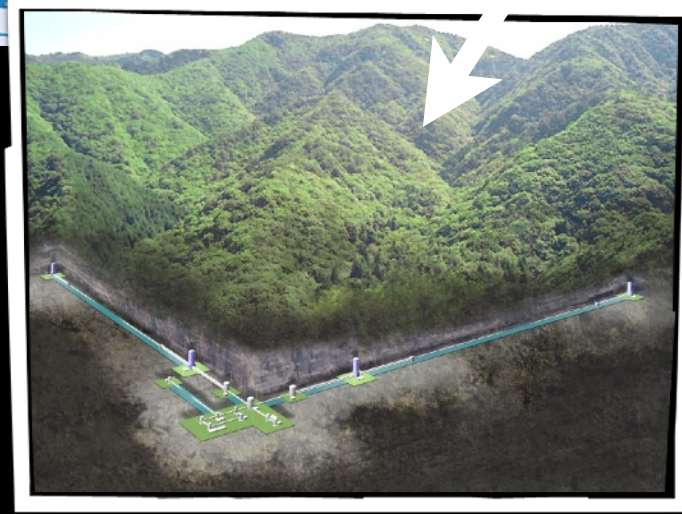
LIGO Livingston



VIRGO



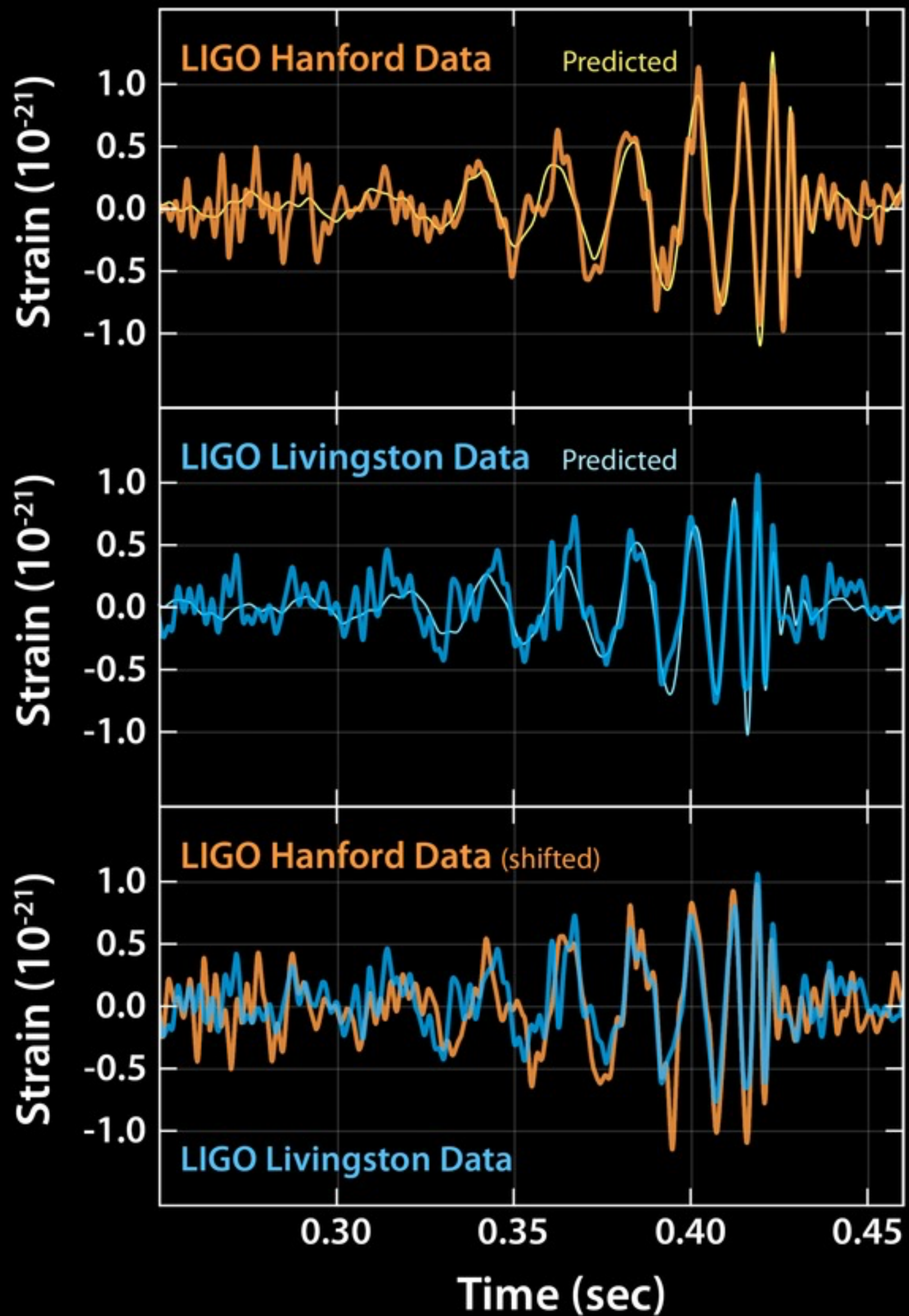
KAGRA



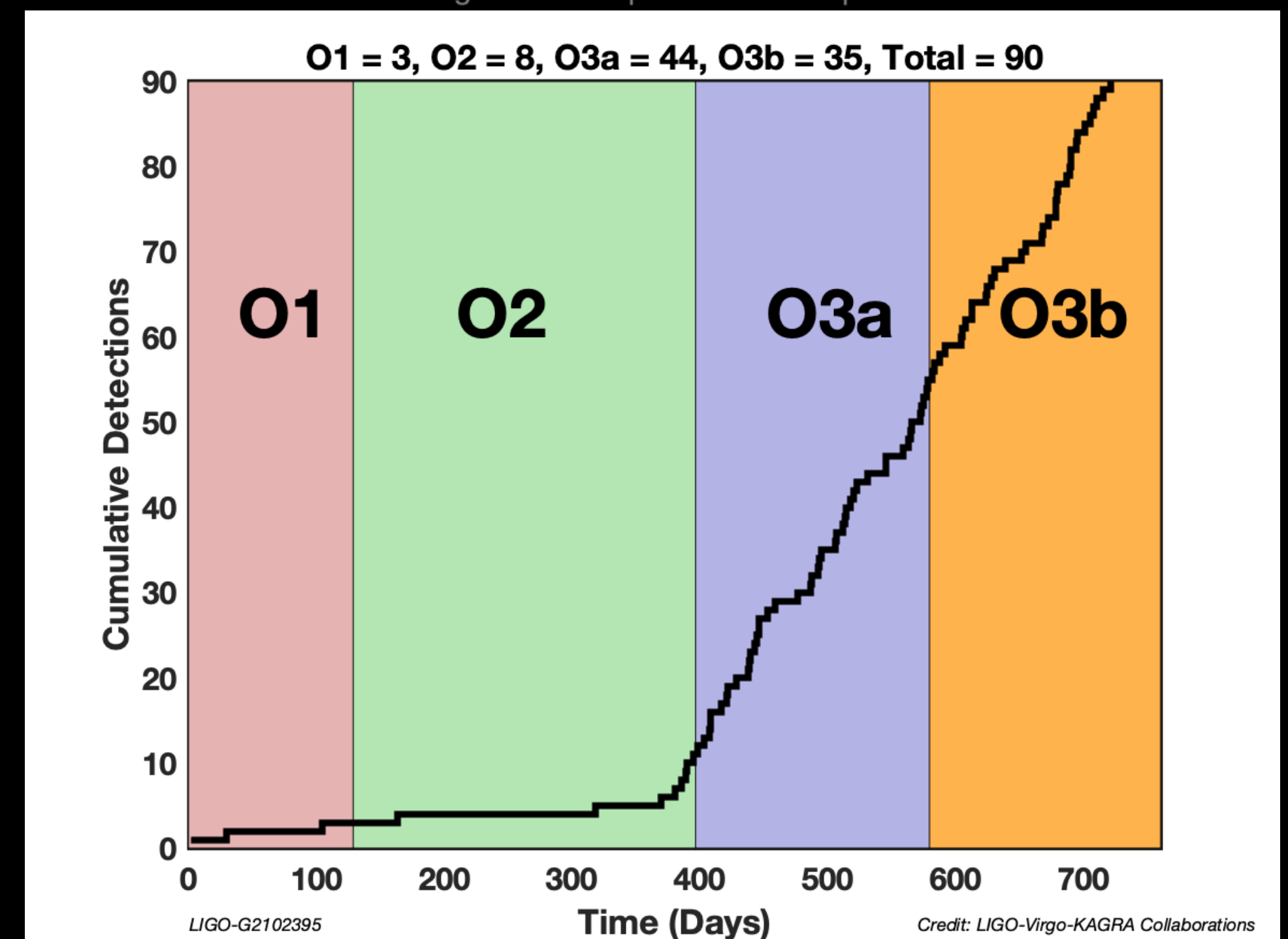
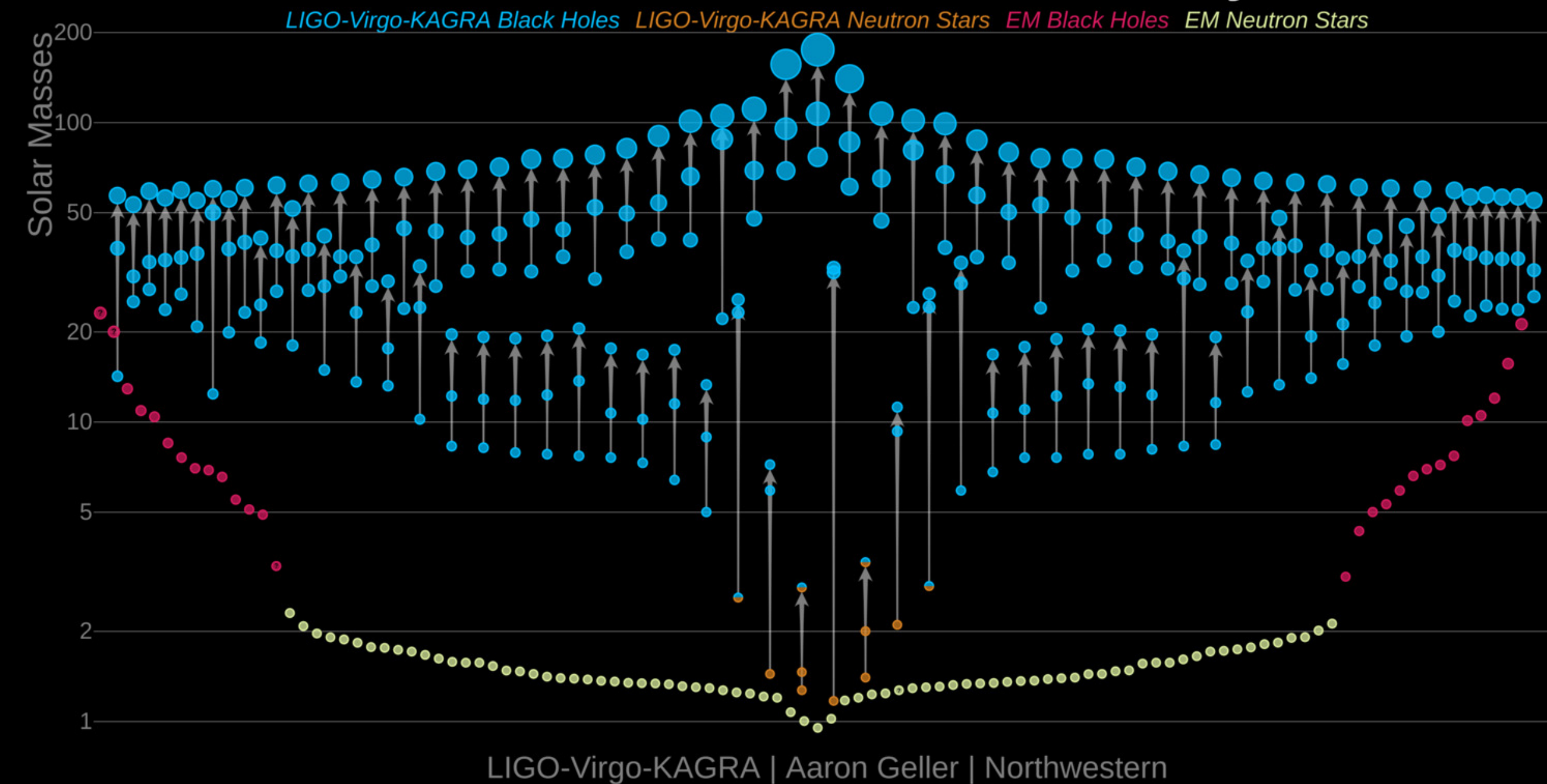




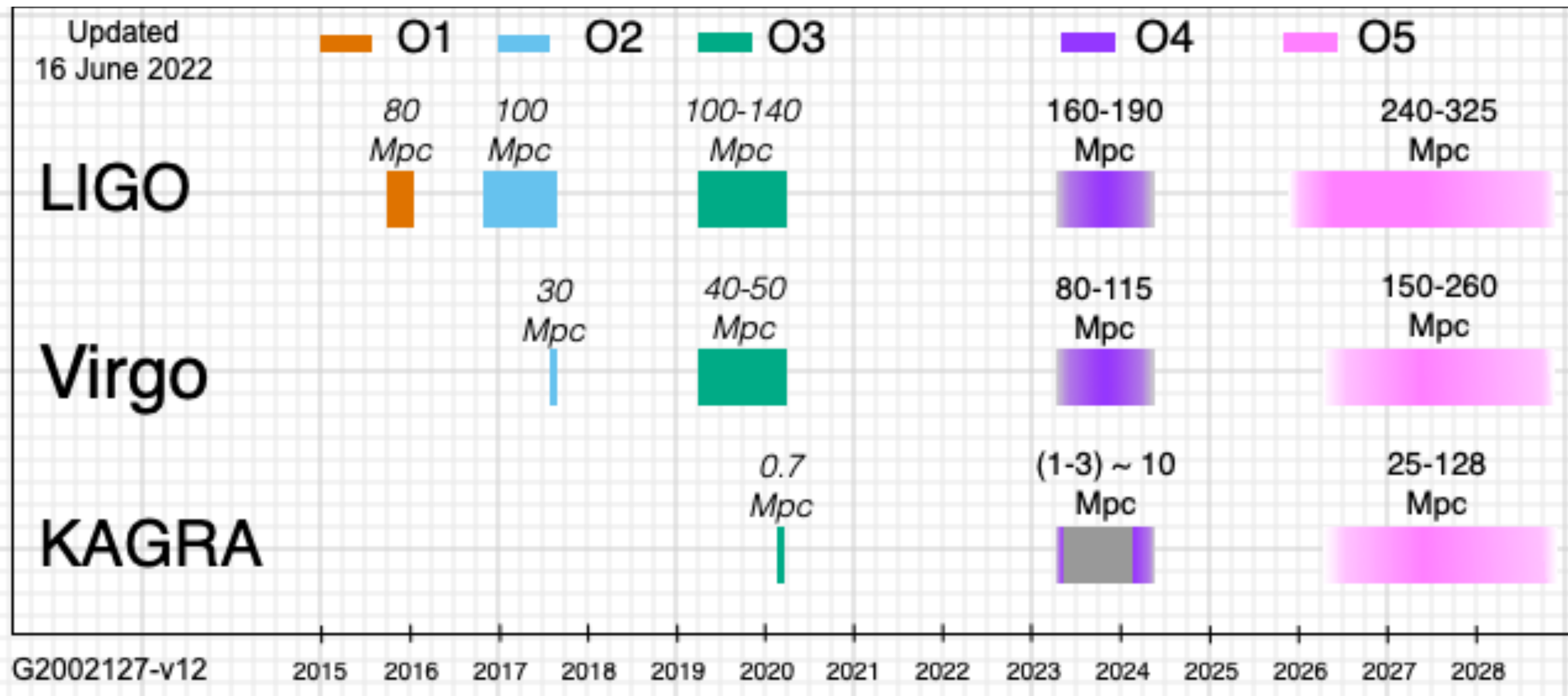




# Masses in the Stellar Graveyard







LIGO | Virgo | KAGRA Observing  
Plan

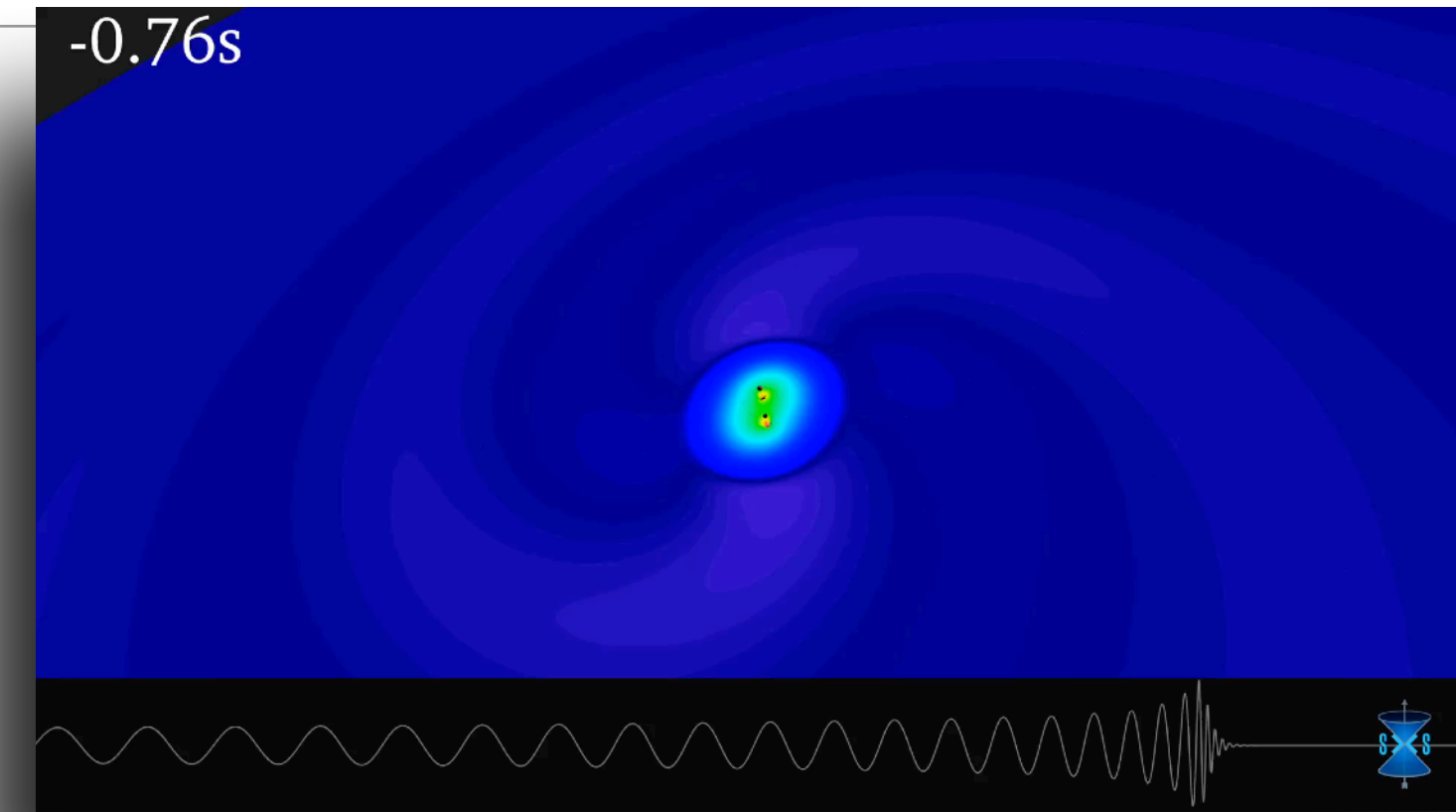
Coming up



# Gravitational wave Data analysis

- I) Direct problem (source modelling):

*“Given a GW source of known properties (e.g. BBH of known masses, spins, etc), what is the emitted gravitational wave signal?”*

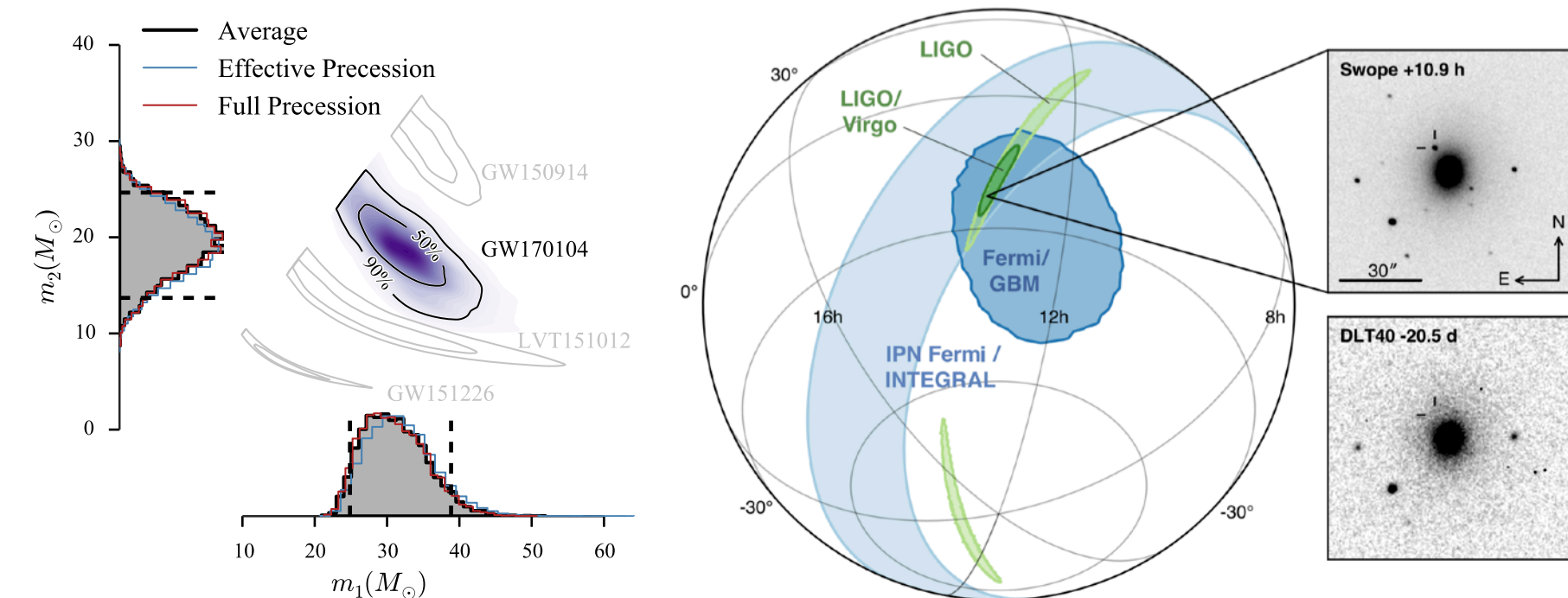


<https://www.ligo.caltech.edu/video/ligo20160211v10>

- II) Inverse problem (data analysis):

*“Given a stretch of noisy data and the stochastic properties of noise, can you reconstruct a signal and estimate the properties of the source?”*

$$\vec{\theta}_{CBC} = (m_1, m_2, \vec{S}_1, \vec{S}_2, D, \alpha, \delta, \iota, \psi, t_c, \varphi_c)$$



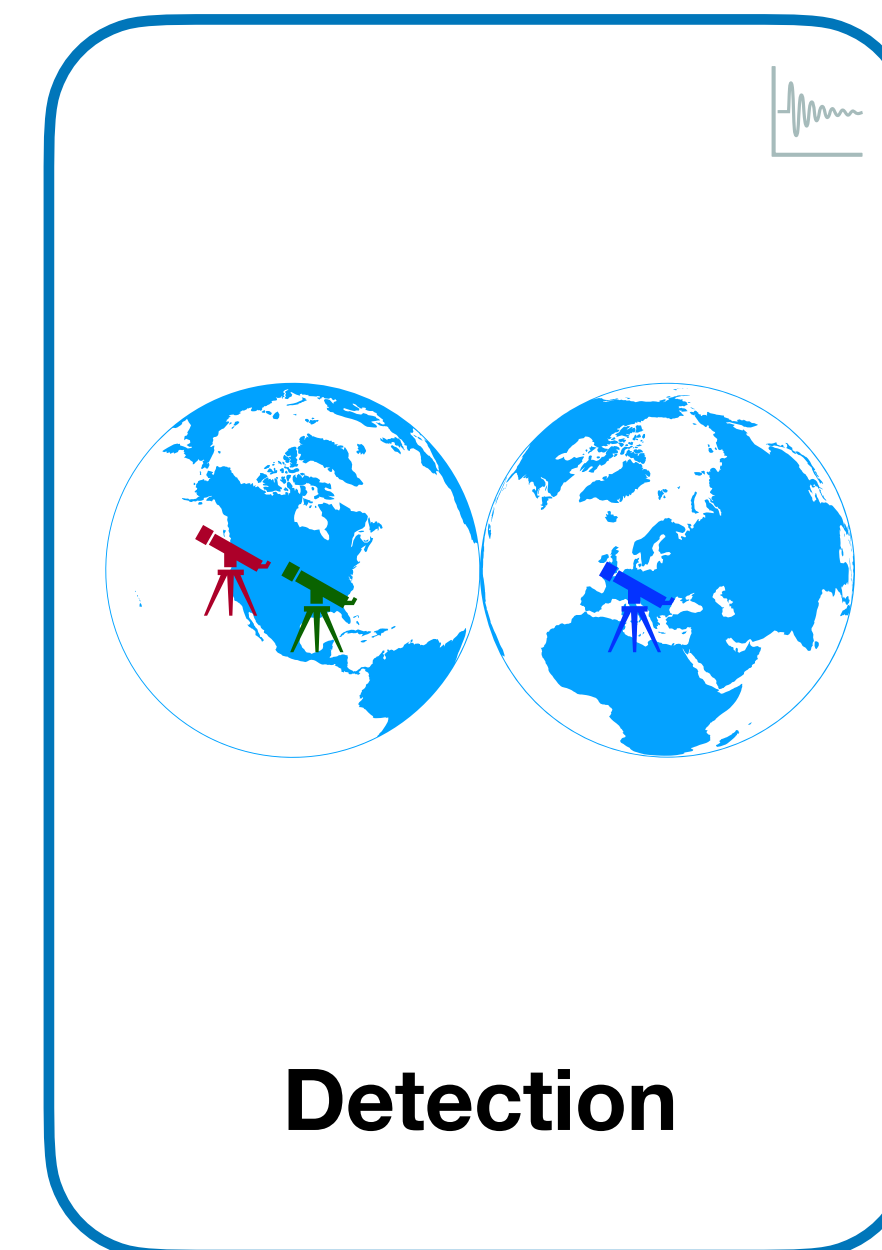
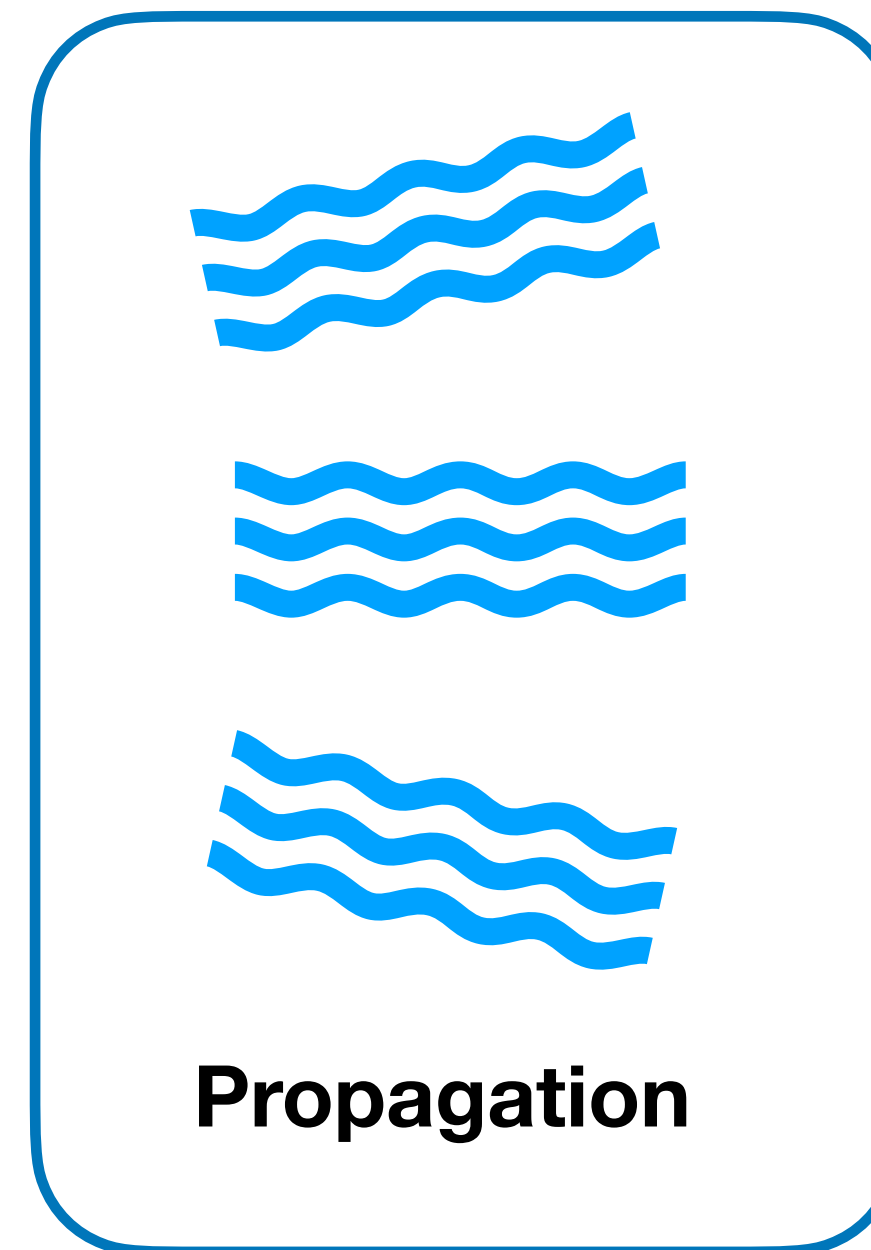
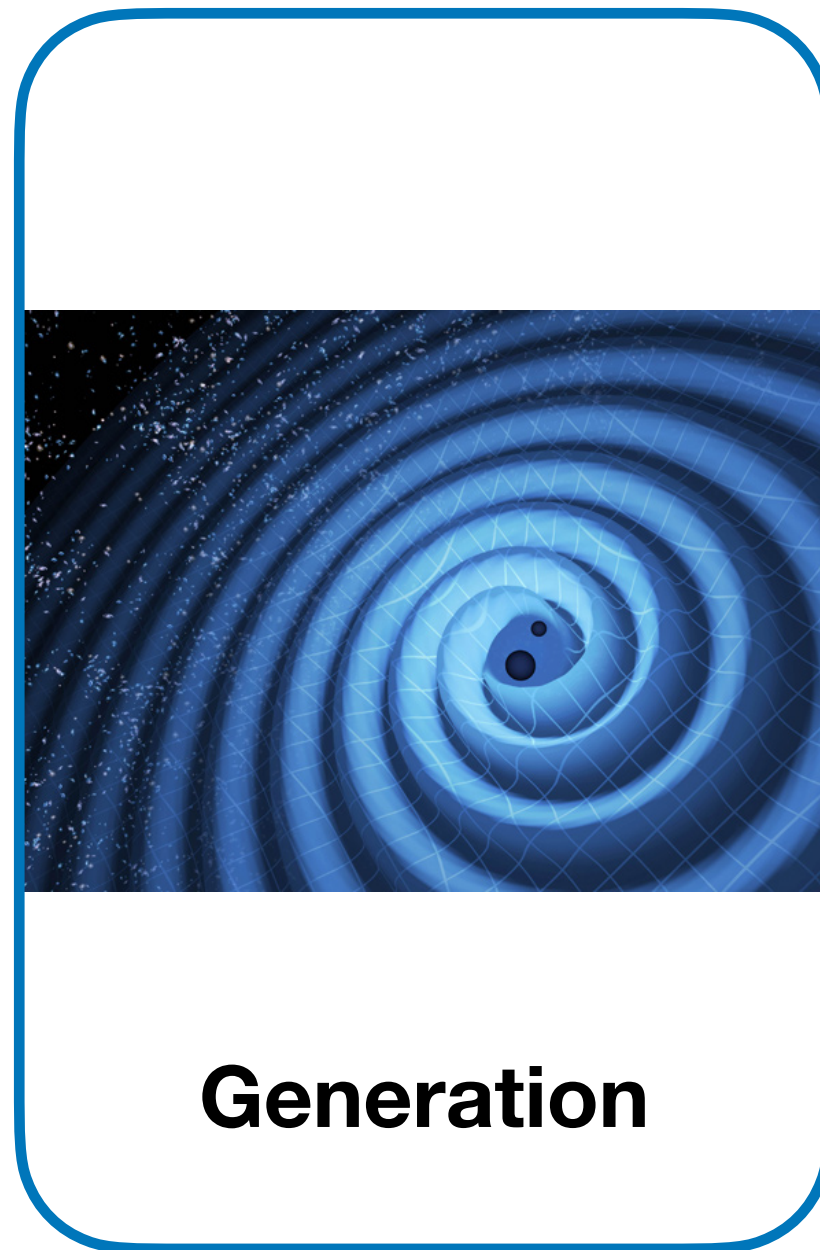
[LVC PRL 119, 161101 (2017)]



# Testing GR with Gravitational Waves

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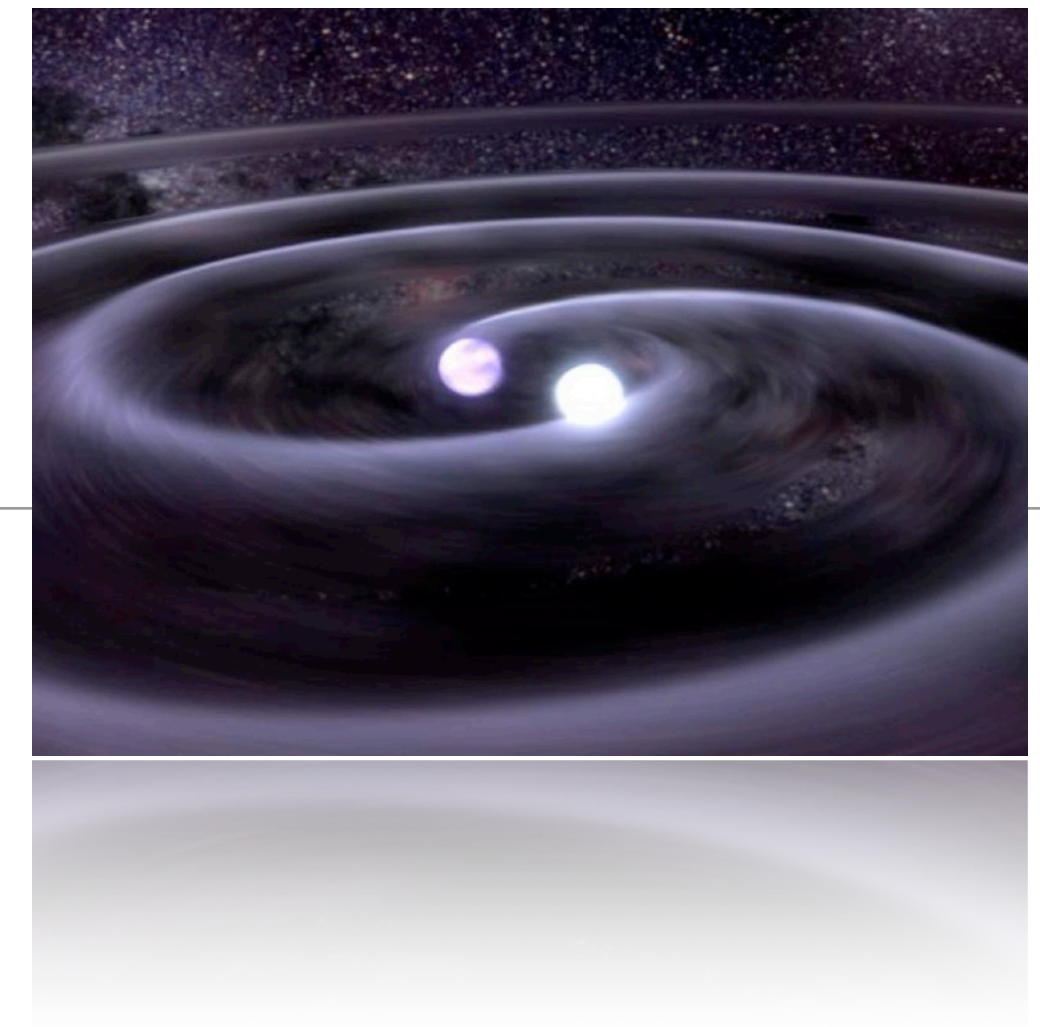
*What are we testing?*



- + *waveform systematics*
- + *noise model & calibration*



# GW Source modelling



- A **post-Newtonian** (PN) expansion gives approximate solutions to the 2-body problem in GR

- Accurate analytic solution for the best part of the **quasicircular Inspiral**

- Simple frequency-domain waveform:  $\tilde{h}(f) = \mathcal{A} f^{-7/6} \cos(2\Phi(f; m_1, m_2) + \phi_0) \quad v = (\pi M f)^{1/3}$

$$\Phi = \left(\frac{v}{c}\right)^{-5} \sum_{i=0}^N \left[ \psi_i + \psi_i^{(l)} \ln \frac{v}{c} \right] \left(\frac{v}{c}\right)^i$$

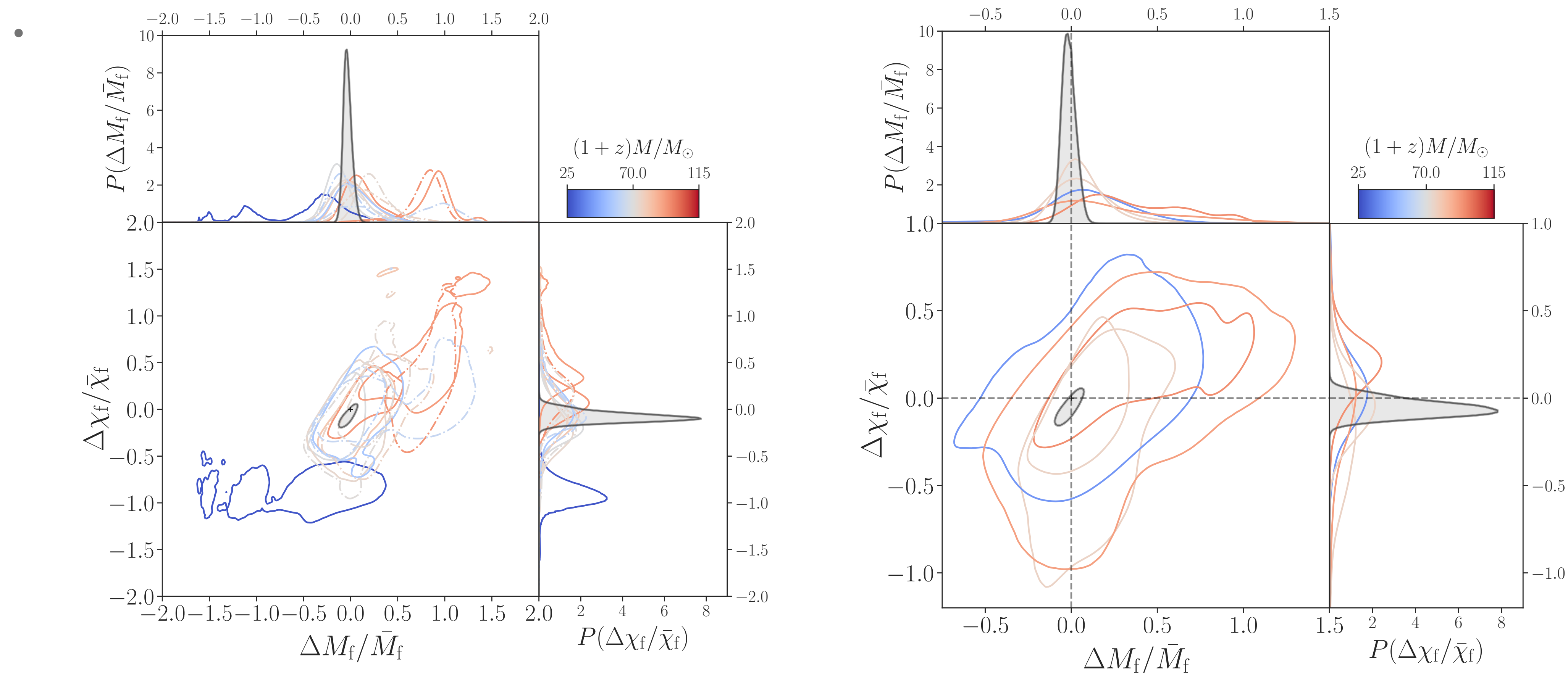
- Calculations in GR give PN phase coefficients  $\psi_i(m_1, m_2, \mathbf{S}_1, \mathbf{S}_2)$ ,  $\psi_i^{(l)}(m_1, m_2, \mathbf{S}_1, \mathbf{S}_2)$
- **Numerical Relativity** simulations complete the model close to/during **Merger**, where perturbative expansions fail
- **BH perturbation** theory informed by NR gives model for the **Ringdown**
- **IMR** models are used in full LVK analyses



# Inspiral - Merger-Ringdown consistency

LVC PRD **103**, 122002 (2021)  
LVK [arXiv:2112.06861]

- Posteriors show consistency with GR predictions

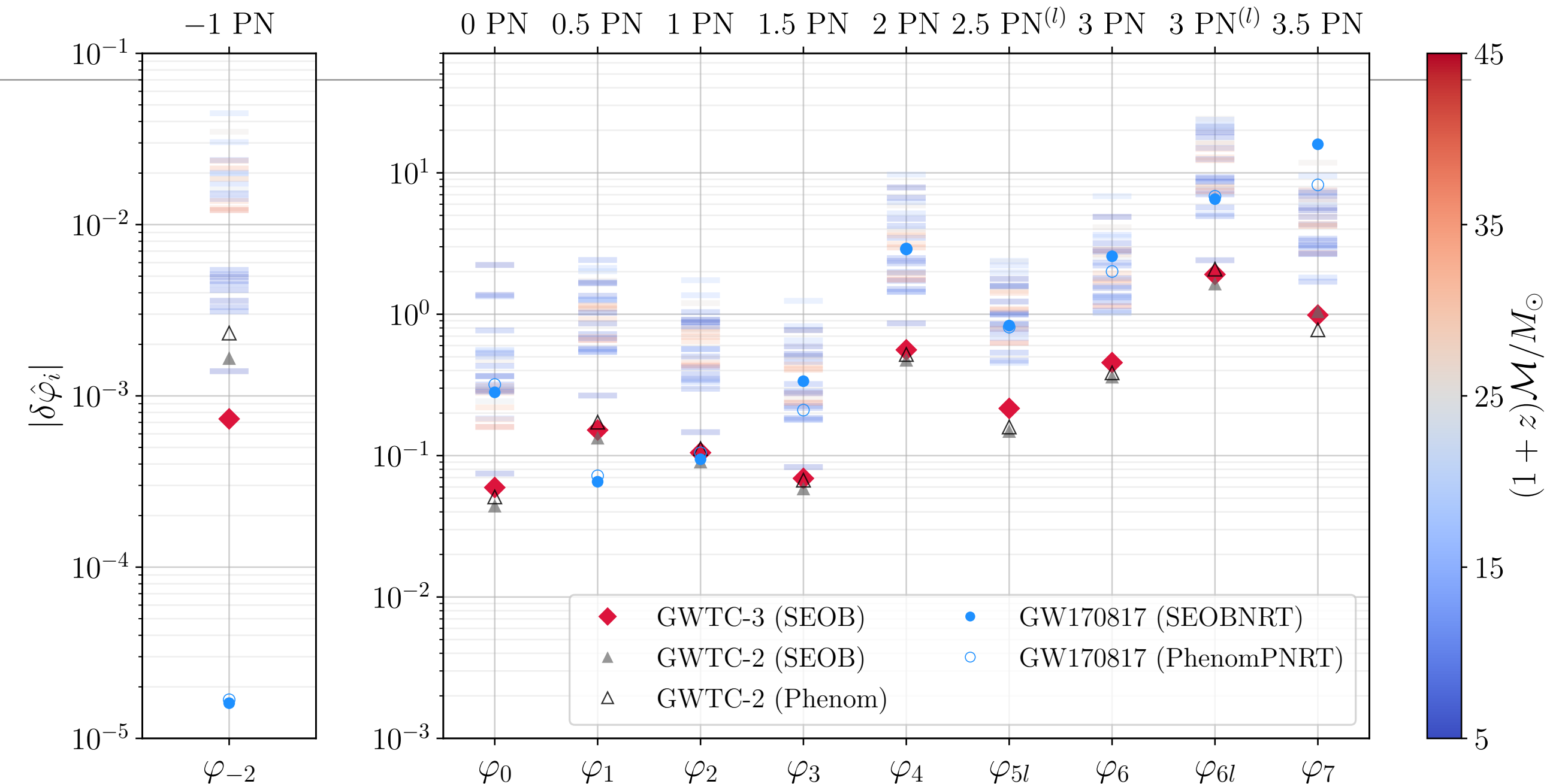




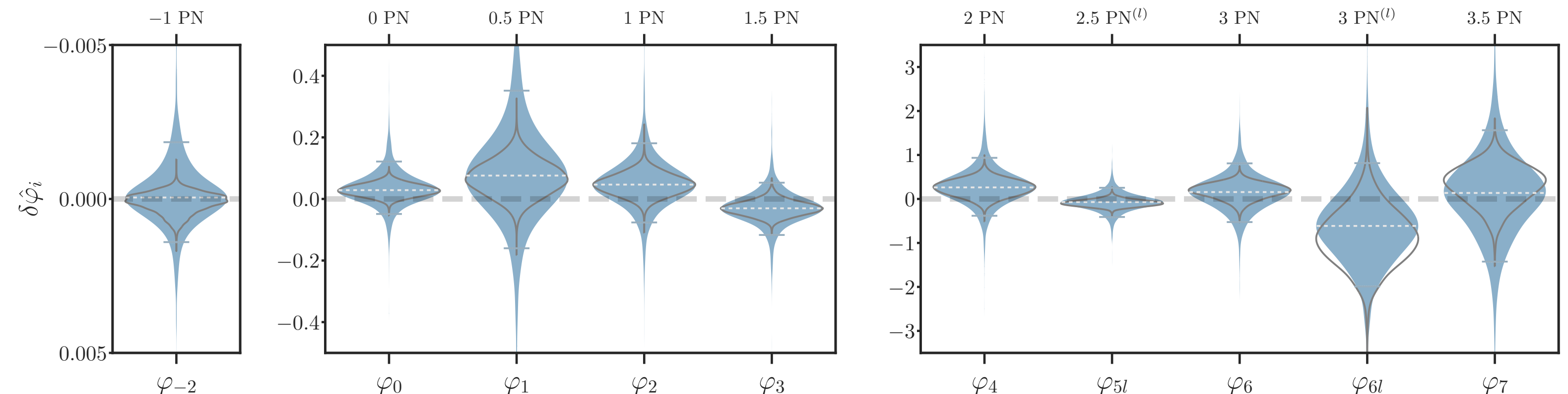
# Parameterized tests of GR

- Phase evolution of the binary is dictated by GR
- Violation of GR would modify **inspiral** dynamics
- Allow for parameterized violations of GR in post-Newtonian phase coefficients and measure them:

$$\varphi_i \rightarrow \varphi_i(1 + \delta\hat{\varphi}_i)$$



Arun+ [PRD 74, 024006 (2006)]  
Yunes+ [PRD 80, 122003 (2009)]  
Li, MA+ [PRD 85, 082003 (2012)]  
MA+ [PRD 89, 082001 (2014)]  
Meidam, MA+ [PRD 97, 044033 (2018)]

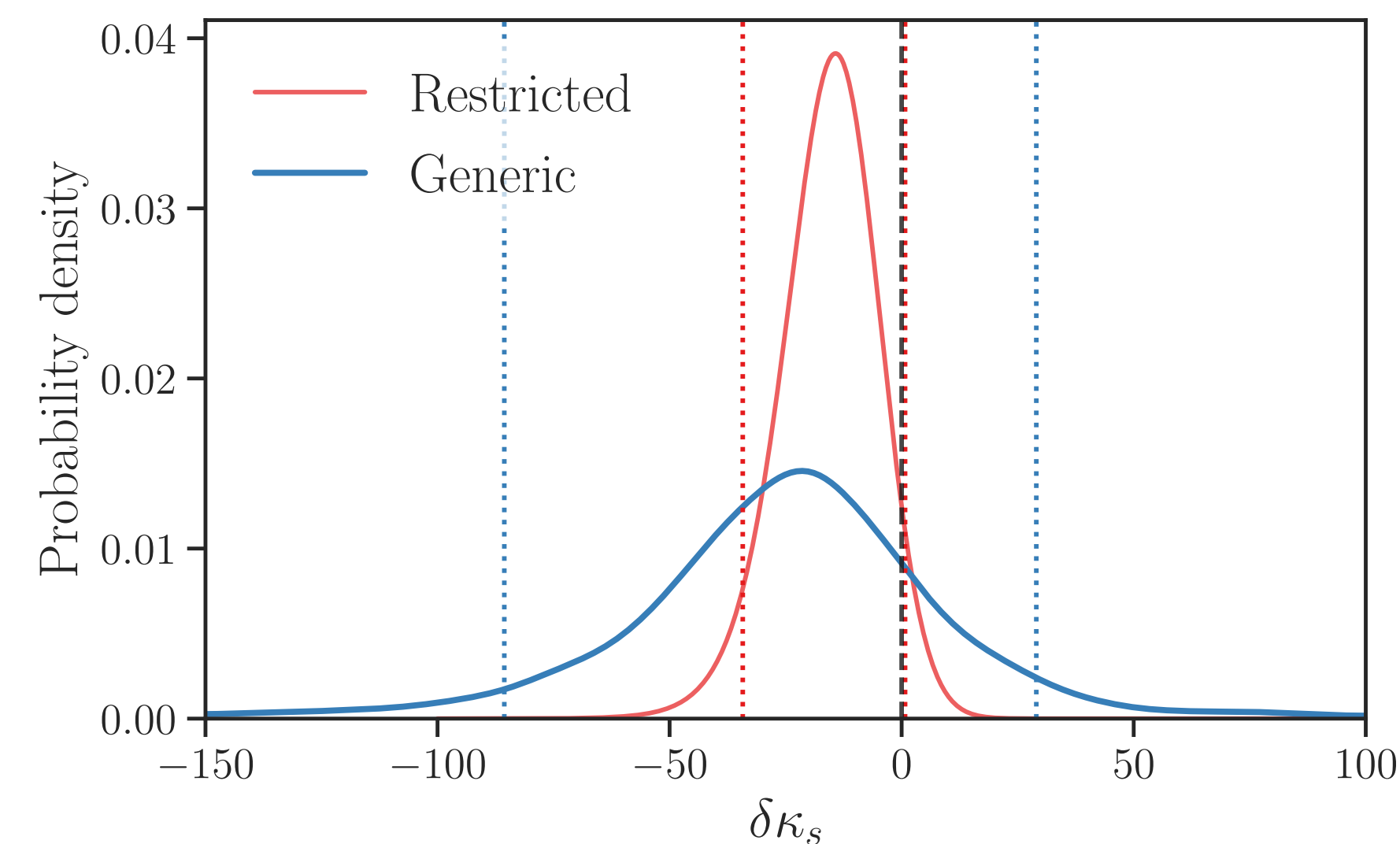
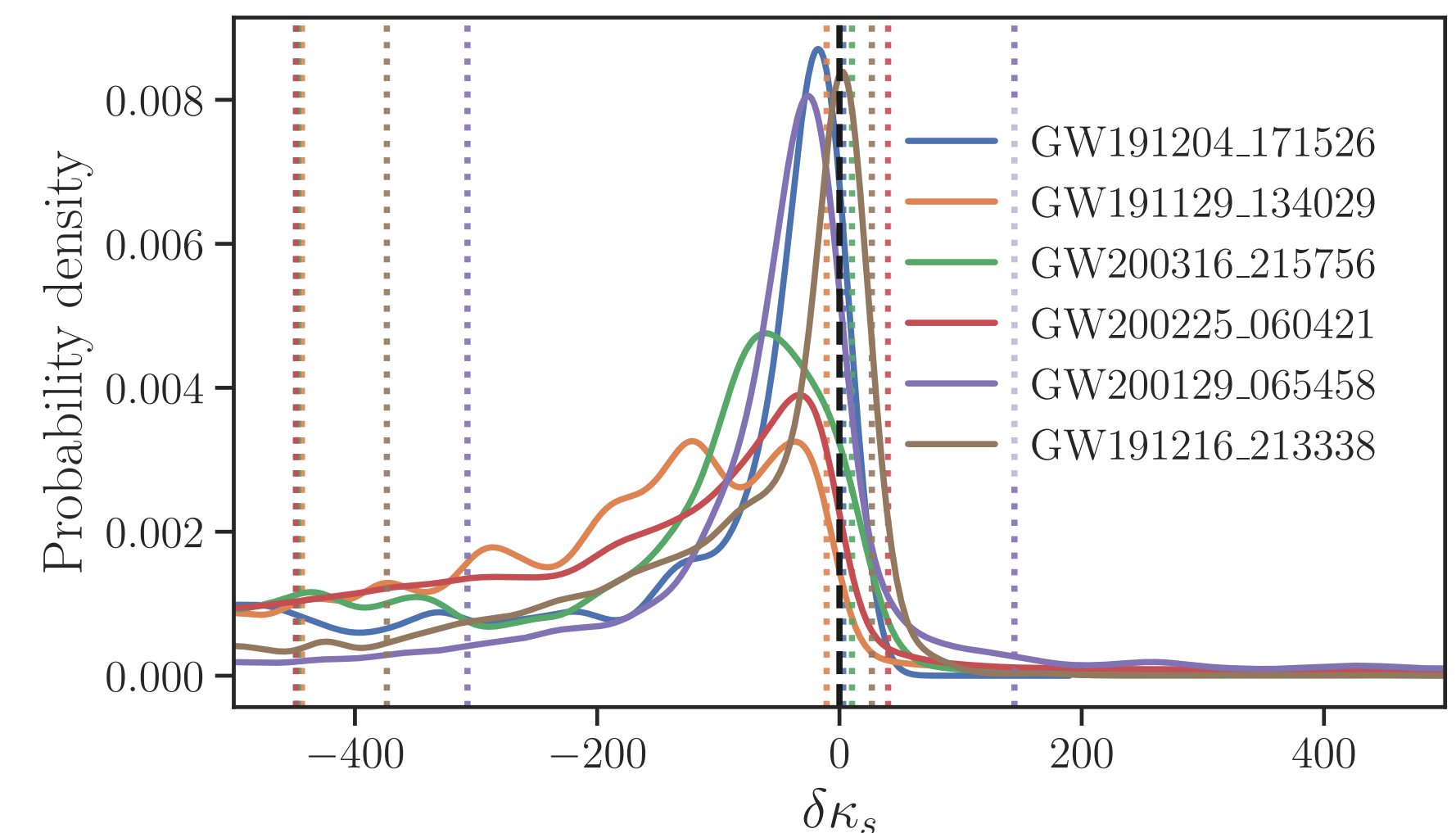




# Black Hole Quadrupole

LVC PRD **103**, 122002 (2021)  
LVK [arXiv:2112.06861]

- All properties of a Kerr BH are uniquely determined by knowing its mass and spin
- Simple formula for mass and current multipoles
- Spin-induced mass quadrupole:  
$$Q = -\kappa\chi^2 M^3, \quad \kappa_{\text{BH}} = 1$$
- Introduces modification in the GW phase that enters @2PN
- Non-Kerr compact objects will in general have  $\kappa \neq 1$ , e.g. neutron-/boson-/grava- stars, etc.
- We measure a combination of  $\kappa$  to be consistent with the Kerr BH value





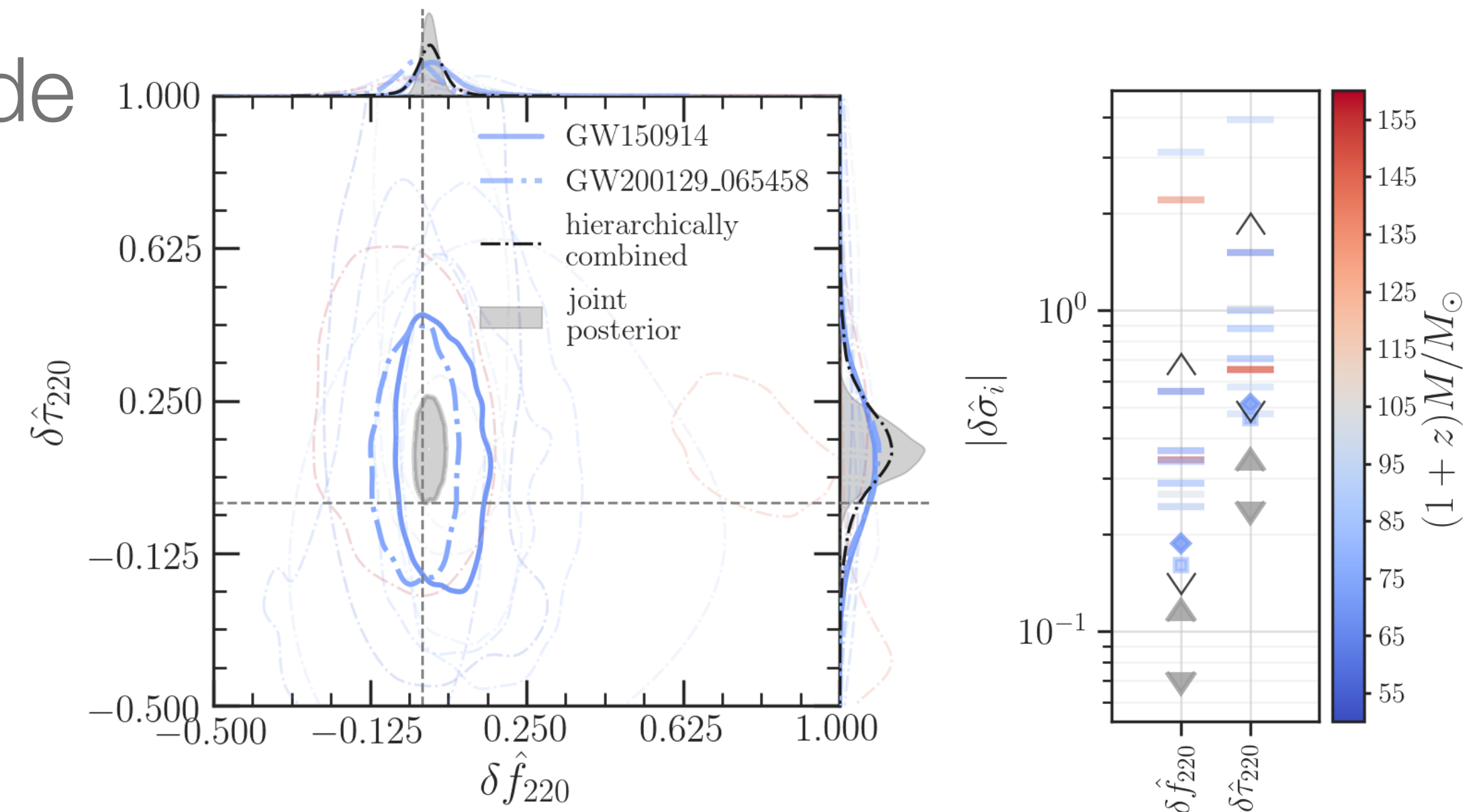
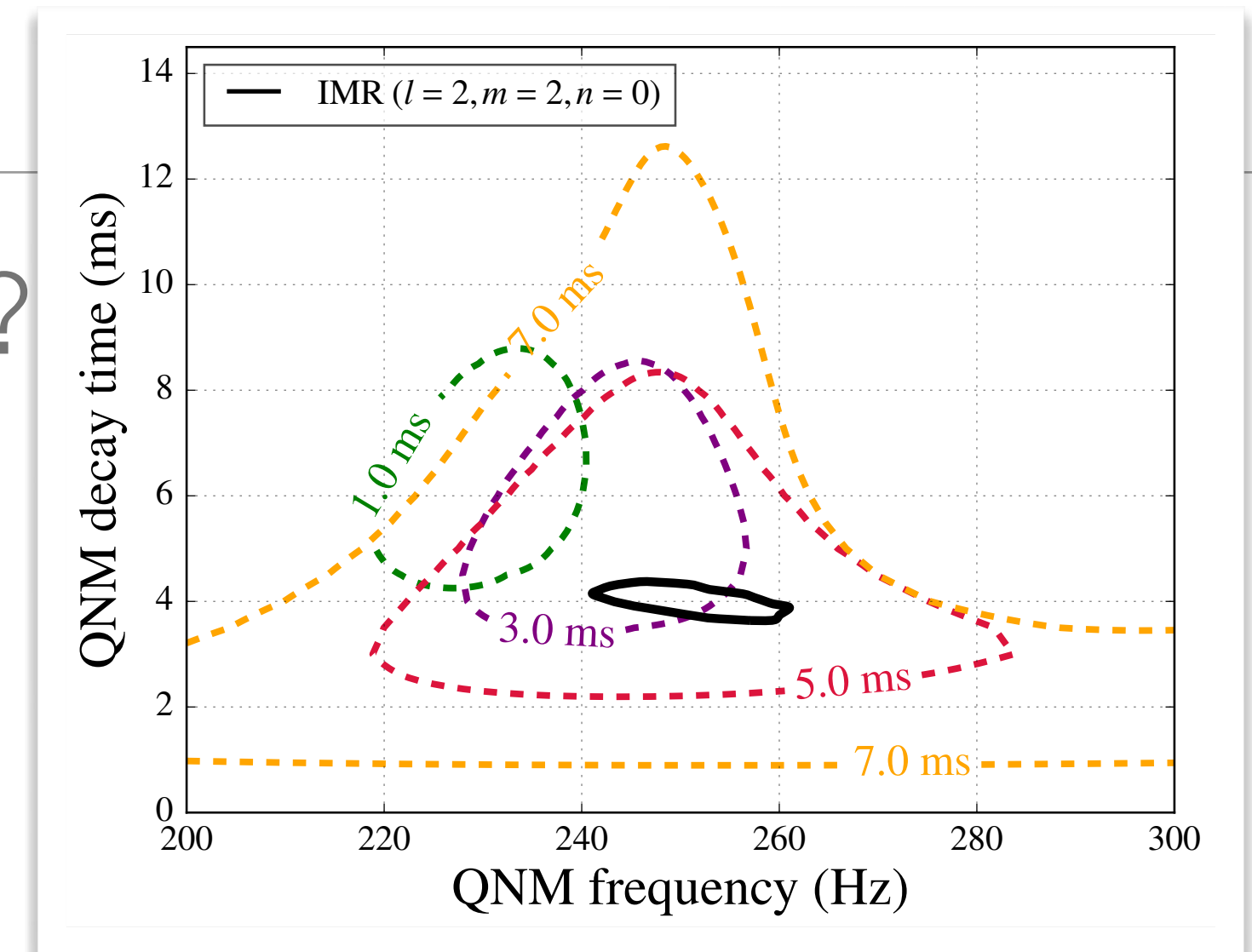
# Ringdown analysis

- “Is there clear evidence of a quasi-normal ringdown?”
- Final BH radiates damped sinusoids

$$h_+(t) - ih_\times(t) = \sum_{\ell=2}^{+\infty} \sum_{m=-\ell}^{\ell} \sum_{n=0}^{+\infty} \mathcal{A}_{\ell mn} \exp\left[-\frac{t-t_0}{(1+z)\tau_{\ell mn}}\right] \exp\left[-\frac{2\pi i f_{\ell mn}(t-t_0)}{1+z}\right] {}_{-2}S_{\ell mn}(\theta, \phi, \chi_f),$$

- Estimate  $f$  &  $\tau$  of **dominant** ( $\ell=2$   $m=2$ ) mode

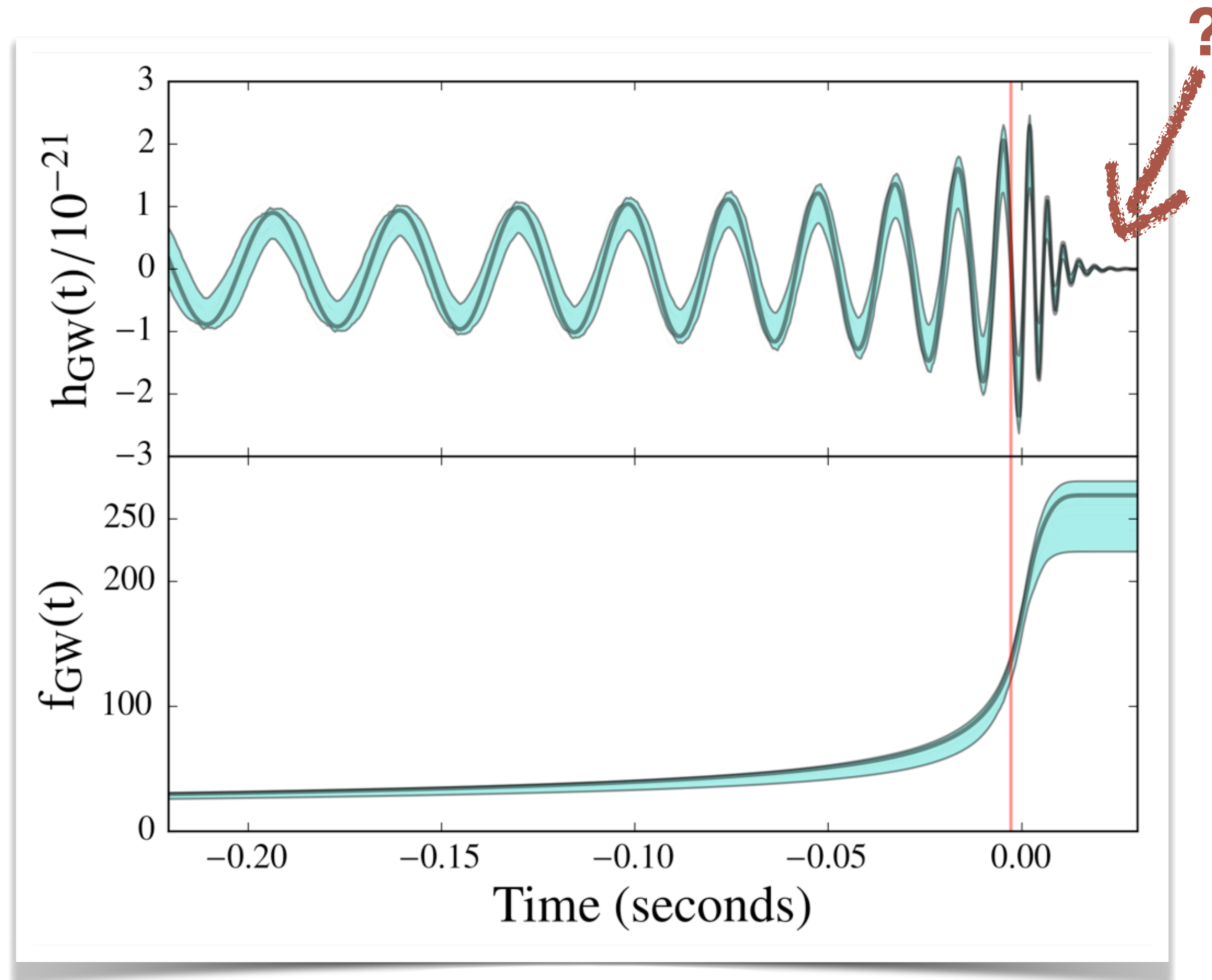
[LVC PRL 116, 221101 (2016)]



LVC PRD **103**, 122002 (2021)  
LVK [arXiv:2112.06861]



Is there anything beyond ringdown?





# Echoes from Exotic Compact Objects

📌 Are we still sure these are BHs?

📌 Alternative: objects that

- are compact enough
- have the same light-ring structure as a BH **but** no horizon

📌 Candidates: Wormholes, thin-shell Gravastars, other?

📌 GW signature: echoes at fixed time intervals  $\Delta t$

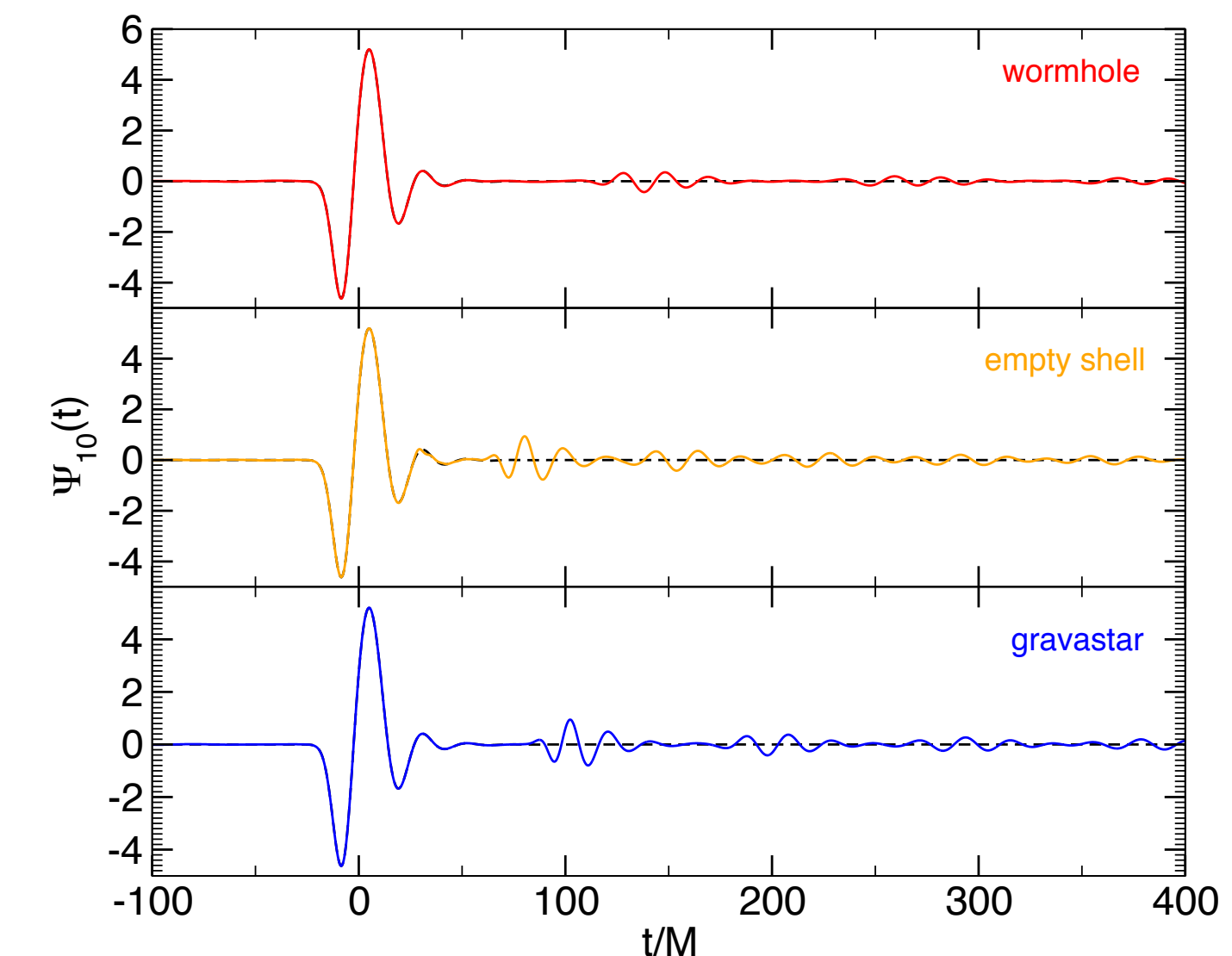
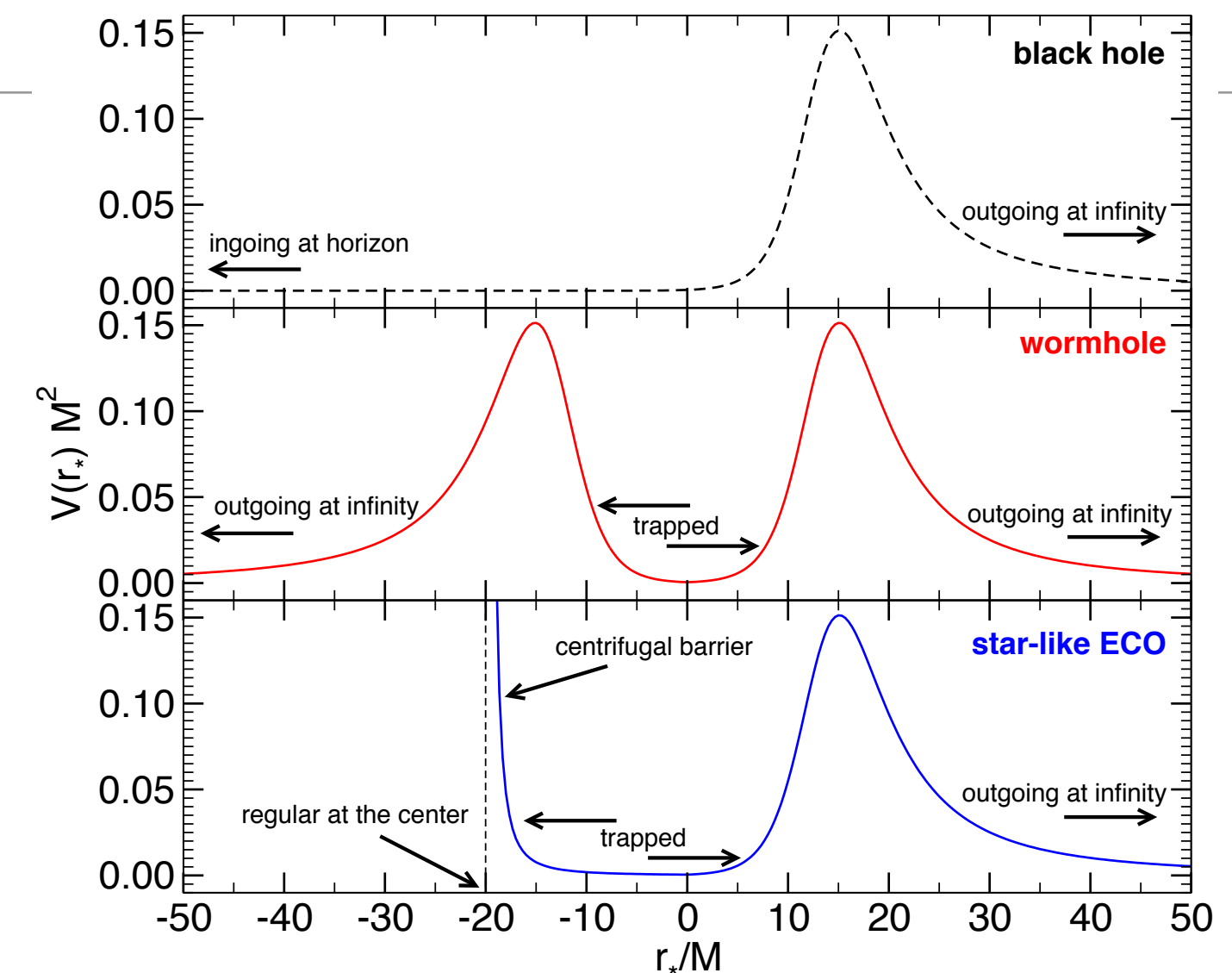
$$\Delta t \sim -nM \log \left( \frac{\ell}{M} \right), \quad \ell \ll M$$

$n=8$

$n=4$

$n=6$

Cardoso et al. 2016



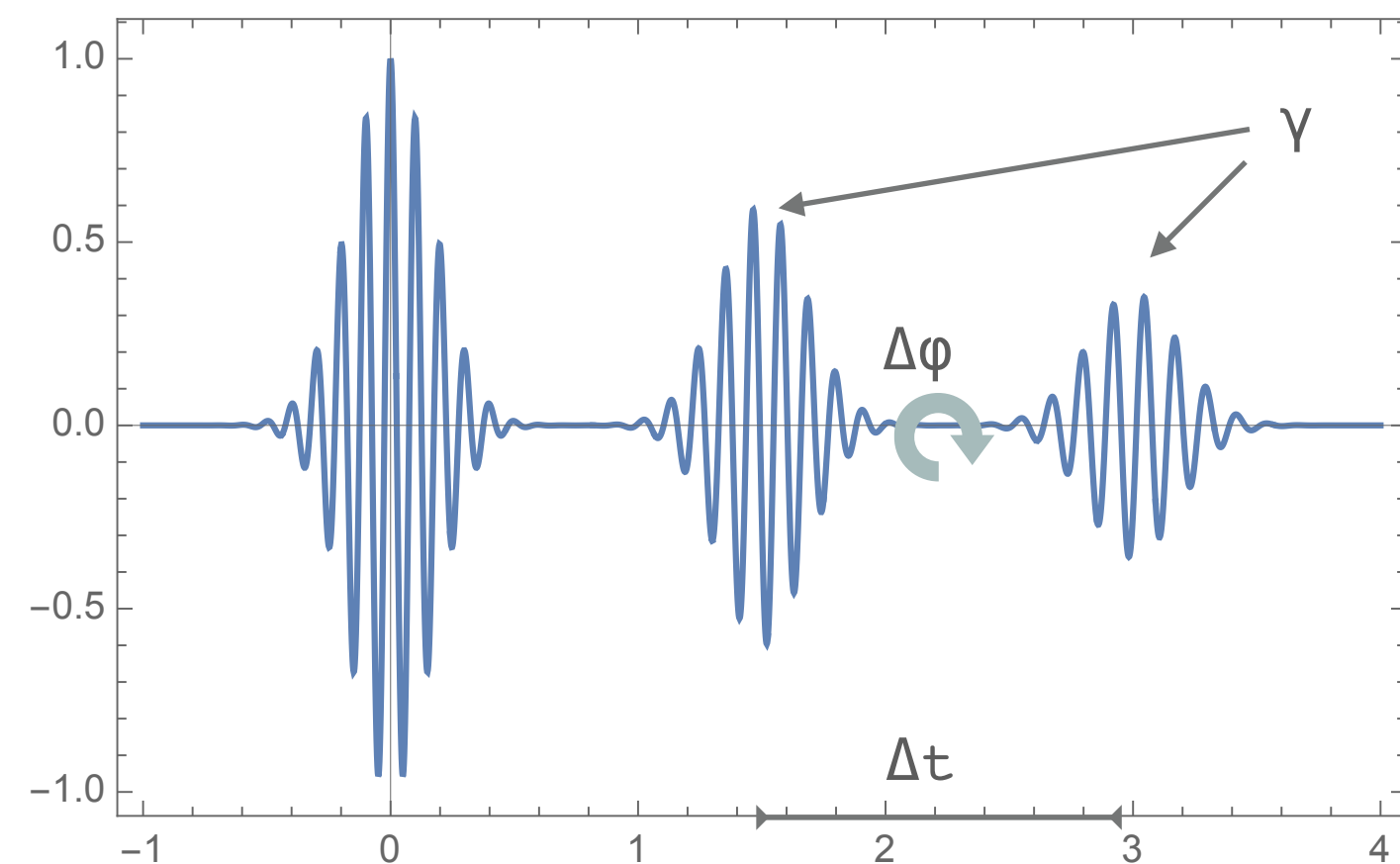


# GWTC-2 searches for echoes

LVC PRD **103**, 122002 (2021)  
LVK [arXiv:2112.06861]

- Look for quasi-periodic bursts of GWs after the ringdown
- Template-based analysis using ringdown signal as basis that is modulated and repeated in echoes [Lb+ arXiv:1811.07431]

- No support for echoes in data

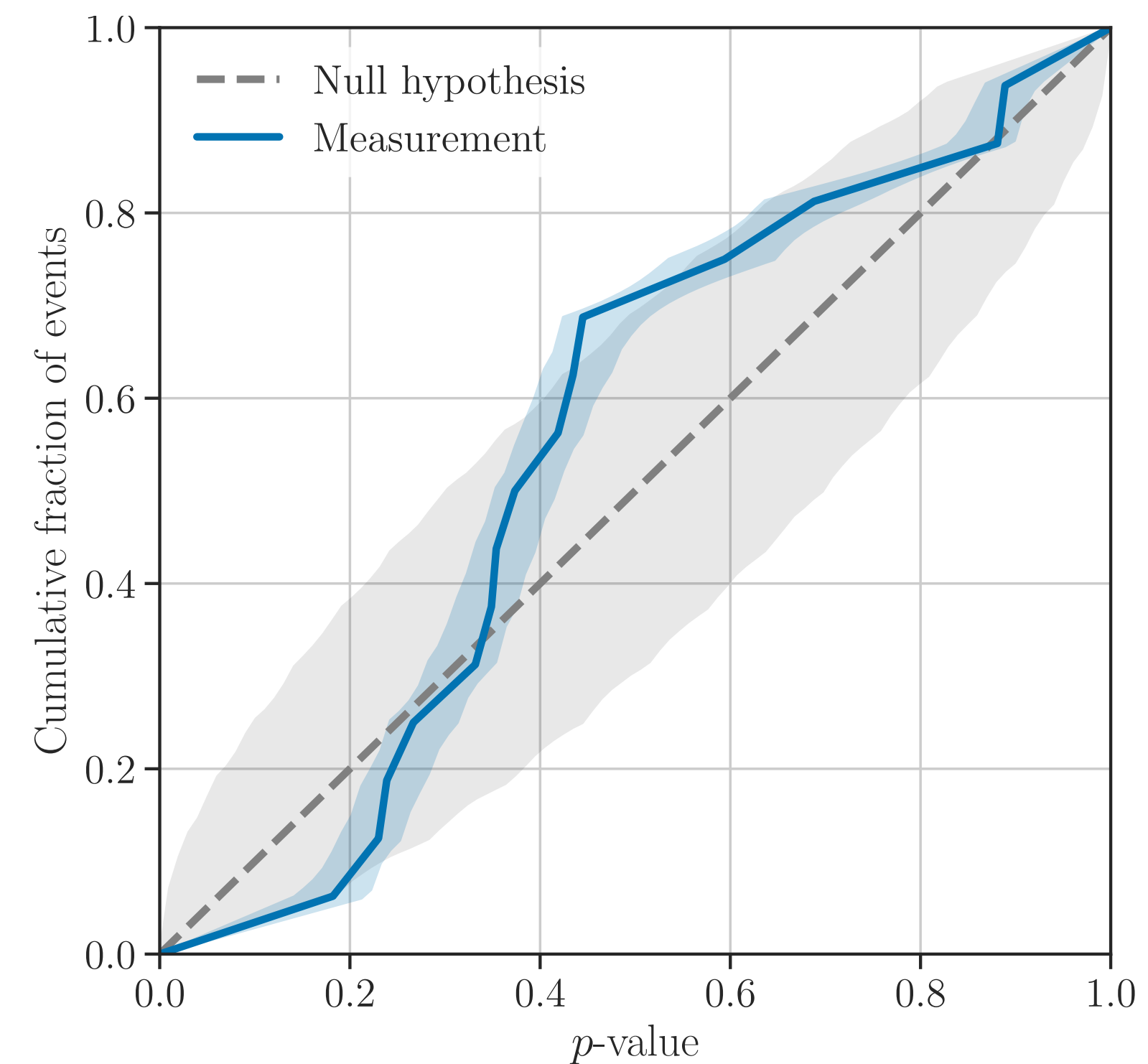


- Earlier model-independent searches also gave null results in O1 and O2

[Cornish & Littenberg arXiv:1410.3835]

[Tsang,...,MA+ arXiv:1804.04877]

[Tsang,...,MA+ arXiv:1906.11168]





# Massive graviton effect on propagation

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- “Massive graviton”: GWs propagate along timelike geodesics under the dispersion relation

$$E^2 = p^2 c^2 + m_g^2 c^4$$

$$\lambda_g = \frac{h}{m_g c}$$

- Waveform undergoes dispersion:

- (early) low-f waves get delayed w.r.t. (late) high-f waves

$$\left(\frac{v_g}{c}\right)^2 = 1 - \frac{h^2 c^2}{\lambda_g^2 E^2}$$

- “Chirp”-like signals get squeezed together

$$\Delta t_a = (1 + Z) \left[ \Delta t_e + \frac{D}{2\lambda_g^2} \left( \frac{1}{f_e^2} - \frac{1}{f_e'^2} \right) \right]$$

- Phase modification in the frequency domain:

$$\delta\Phi_{\text{MG}}(f) = -\frac{\pi D c}{\lambda_g^2 (1 + z) f}$$



# Lorentz-Invariance-Violating dispersion

LVC PRD **103**, 122002 (2021)  
LVK [arXiv:2112.06861]

- More general form of modified dispersion relation:

[Mirshekari, Yunes, Will 2011]

- $\alpha=0$  : massive graviton [de Rham LRR-2014-7]

$$E^2 = p^2 c^2 + \Lambda p^\alpha c^\alpha$$

- $\alpha=2$  : no dispersion, non-LIV

$$\lambda_\Lambda = h \Lambda^{\frac{1}{\alpha-2}}$$

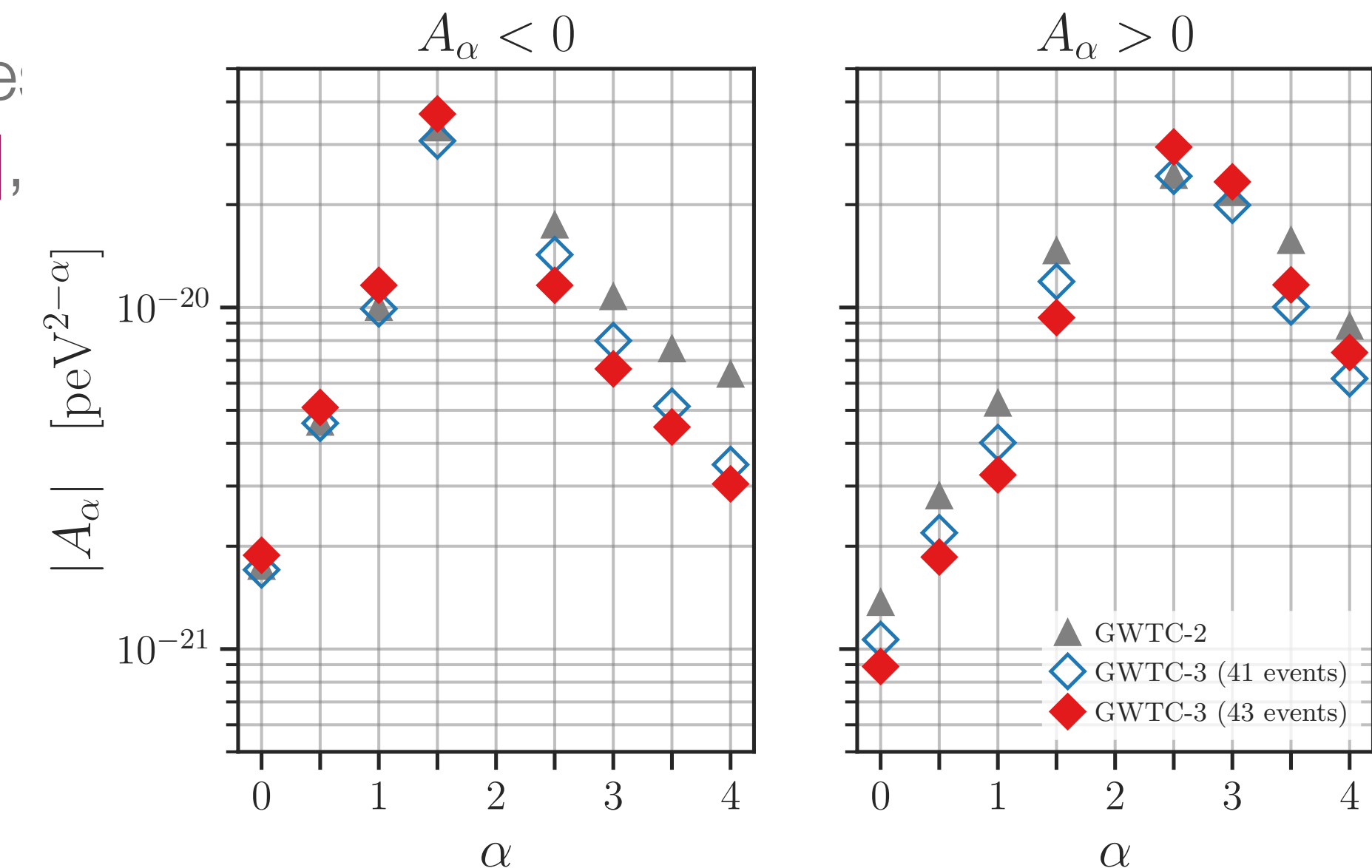
	$m_g$ [ $10^{-23}$ eV/ $c^2$ ]
GWTC-2	1.76
<b>GWTC-3</b>	<b>1.27</b>

- other: Lorentz invariance violating, some motivated by approaches to quantum gravity, e.g. dSR ( $\alpha=3$ ) [Amelino-Camelia 2002,2010], extra dims & Horava-Lifshitz ( $\alpha=4$ ) [Blas&Sanctuary 2011]

- More general forms include vector/tensor contractions with  $p^\mu$

- GW phase modification:

$$\delta\Psi_\alpha(f) = -\cancel{\beta(\pi M f)} - \frac{\pi D_\alpha}{(1-\alpha)\lambda_\Lambda^{2-\alpha}(1+z)^{1-\alpha}} f^{\alpha-1} \quad \alpha \neq 1$$





# Gravitational Wave Detection

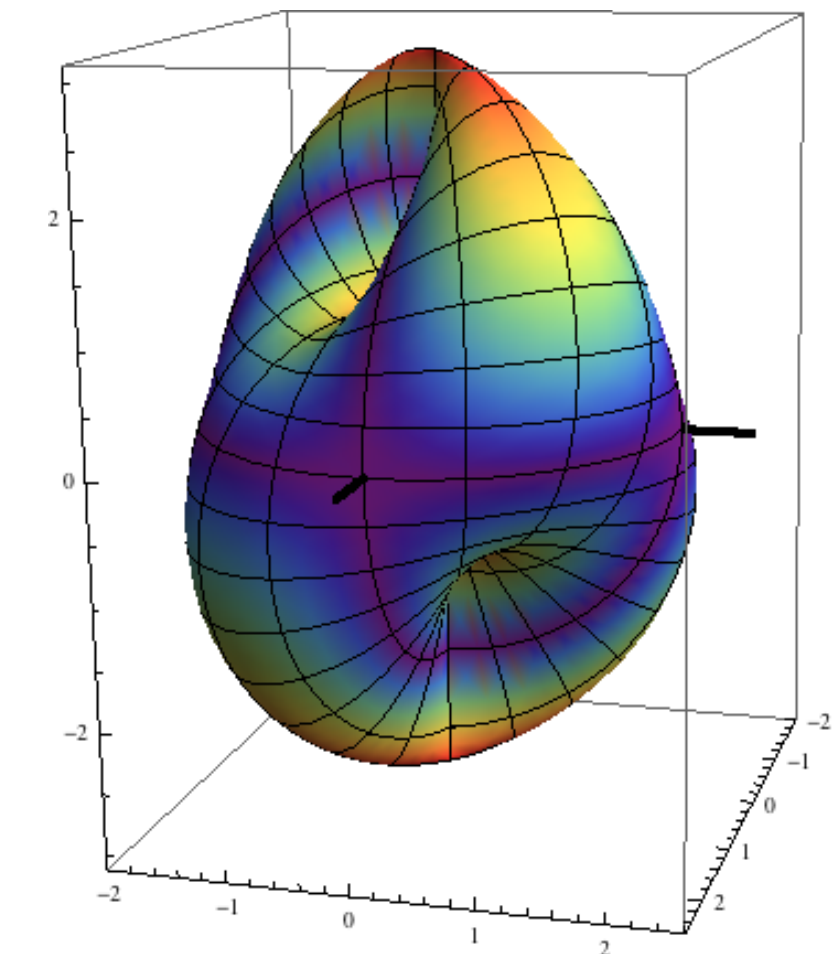
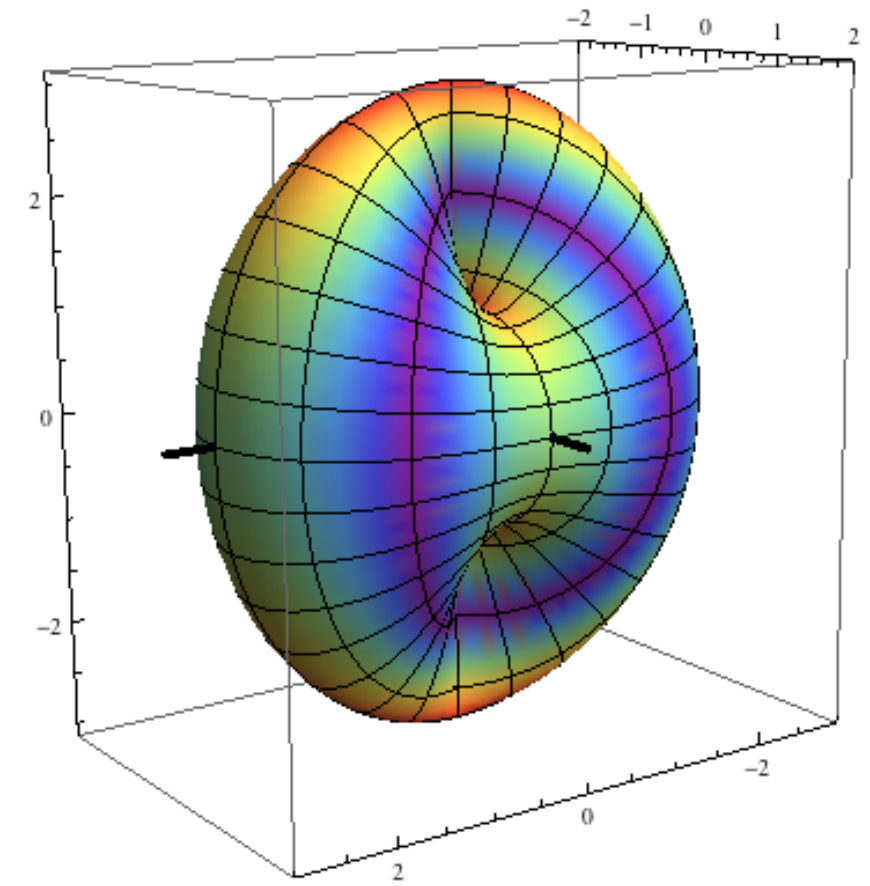
- Detector arms stretch and squeeze in a different way
- Antenna pattern gives detector response that depends on direction of propagation

$$h(t) = F_+(\hat{n}) h_+(t) + F_\times(\hat{n}) h_\times(t),$$
$$F_P(\hat{n}) = D^{ij} \epsilon_{ij}^P(\hat{n}) \quad , \quad P = +, \times$$

- Detector output (strain) is the differential deformation of arms

$$D^{ij} = \frac{1}{2}(\hat{x}_i \hat{x}_j - \hat{y}_i \hat{y}_j)$$

- With many IFOs we can resolve polarizations

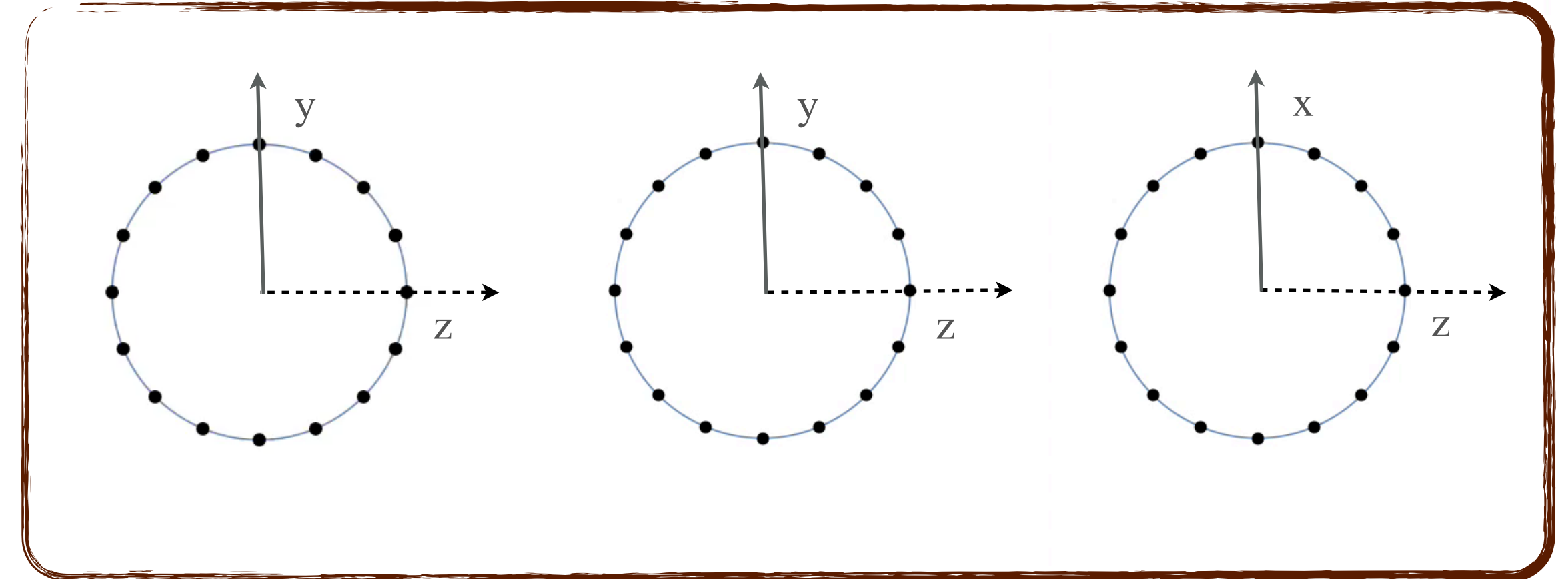
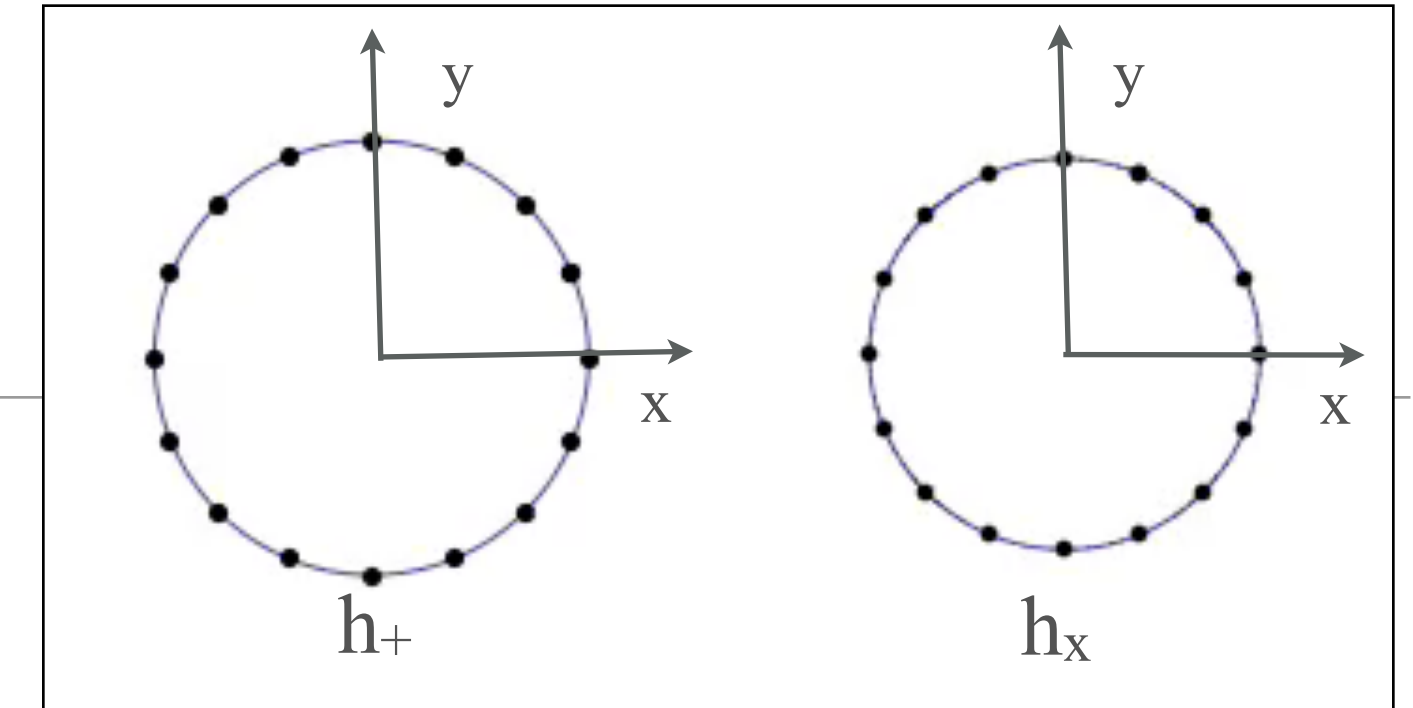




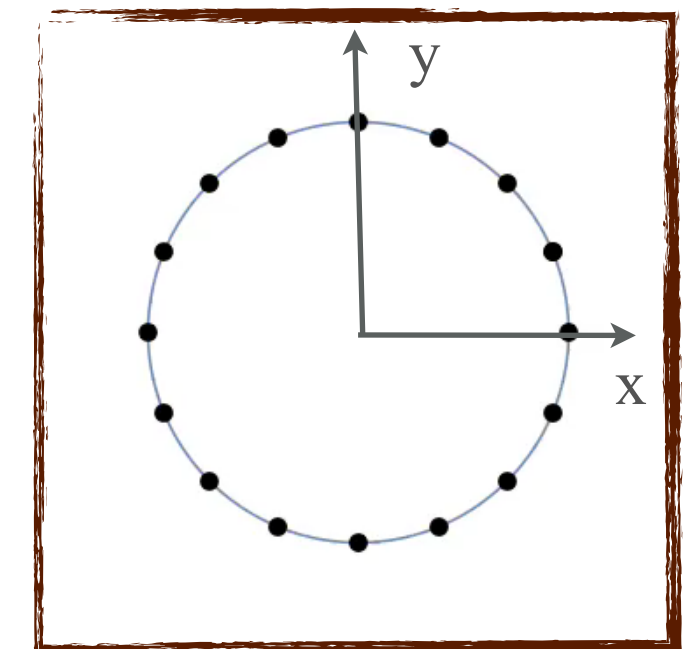
# Anomalous polarizations

- GR predicts 2 transverse GW polarizations (+,x)
- Alternative metric theories allow for additional:

- longitudinal modes
- breathing mode



- With the 2 LIGO detectors: cannot tell the difference!
- Virgo, KAGRA (2019) and IndIGO will help resolve degeneracies between polarizations



[LVC PRL 119, 141101 (2017)]  
[LVC arXiv:1811.00364 ]  
[Isi, Weinstein arXiv:1710.03794]



# Testing presence of nontensorial polarizations

LVC PRD **103**, 122002 (2021)  
LVK [arXiv:2112.06861]

- Null-stream test without modelling the actual signal
- Any residual signal must be non-tensorial
- No evidence for nontensorial signal in data; scalar is more disfavoured

Events	$\log_{10} \mathcal{B}_T^S$	$\log_{10} \mathcal{B}_T^V$	$\log_{10} \mathcal{B}_T^{TS}$	$\log_{10} \mathcal{B}_T^{TV}$	$\log_{10} \mathcal{B}_T^{VS}$	$\log_{10} \mathcal{B}_T^{TVS}$
O1	$-0.04 \pm 0.07$	$0.09 \pm 0.07$	$0.04 \pm 0.07$	$0.09 \pm 0.07$	$0.09 \pm 0.07$	$0.07 \pm 0.07$
O2	$-0.42 \pm 0.12$	$0.04 \pm 0.12$	$0.08 \pm 0.12$	$0.22 \pm 0.12$	$0.09 \pm 0.12$	$0.35 \pm 0.12$
O3a	$-1.85 \pm 0.21$	$-1.04 \pm 0.20$	$0.25 \pm 0.20$	$0.07 \pm 0.20$	$-1.05 \pm 0.20$	$-0.18 \pm 0.20$
O3b	$-1.93 \pm 0.17$	$-0.79 \pm 0.17$	$-0.17 \pm 0.17$	$-0.07 \pm 0.17$	$-0.86 \pm 0.17$	$-0.32 \pm 0.17$
Combined	$-4.24 \pm 0.30$	$-1.70 \pm 0.30$	$0.20 \pm 0.30$	$0.31 \pm 0.30$	$-1.73 \pm 0.30$	$-0.08 \pm 0.30$



# Tests of Gravity with GW170817

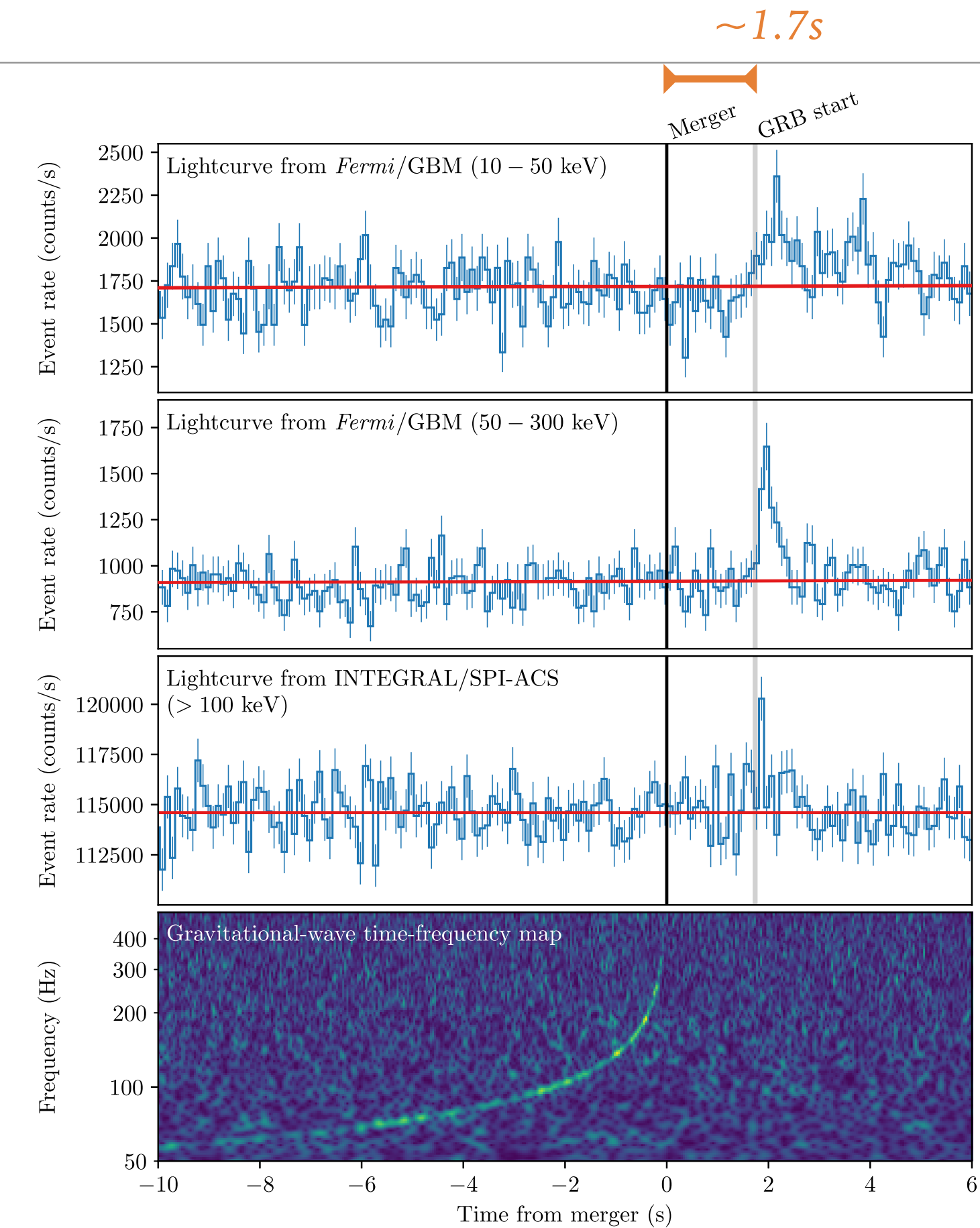
- Coincident GWs and  $\gamma$ -ray detections
- Distance travelled  $\sim 40$  Mpc
- GW  $\rightarrow$  GRB time delay (+ reasonable astrophysical priors)  $\Rightarrow$

$$-3 \times 10^{-15} \leq \frac{\Delta v}{v_{\text{EM}}} \leq +7 \times 10^{-16}$$

- Test of the equivalence principle (Shapiro time delay):

$$\delta t_S = -\frac{1 + \gamma}{c^3} \int_{r_e}^{r_o} U(\mathbf{r}(l)) dl,$$

$$-2.6 \times 10^{-7} \leq \gamma_{\text{GW}} - \gamma_{\text{EM}} \leq 1.2 \times 10^{-6}$$



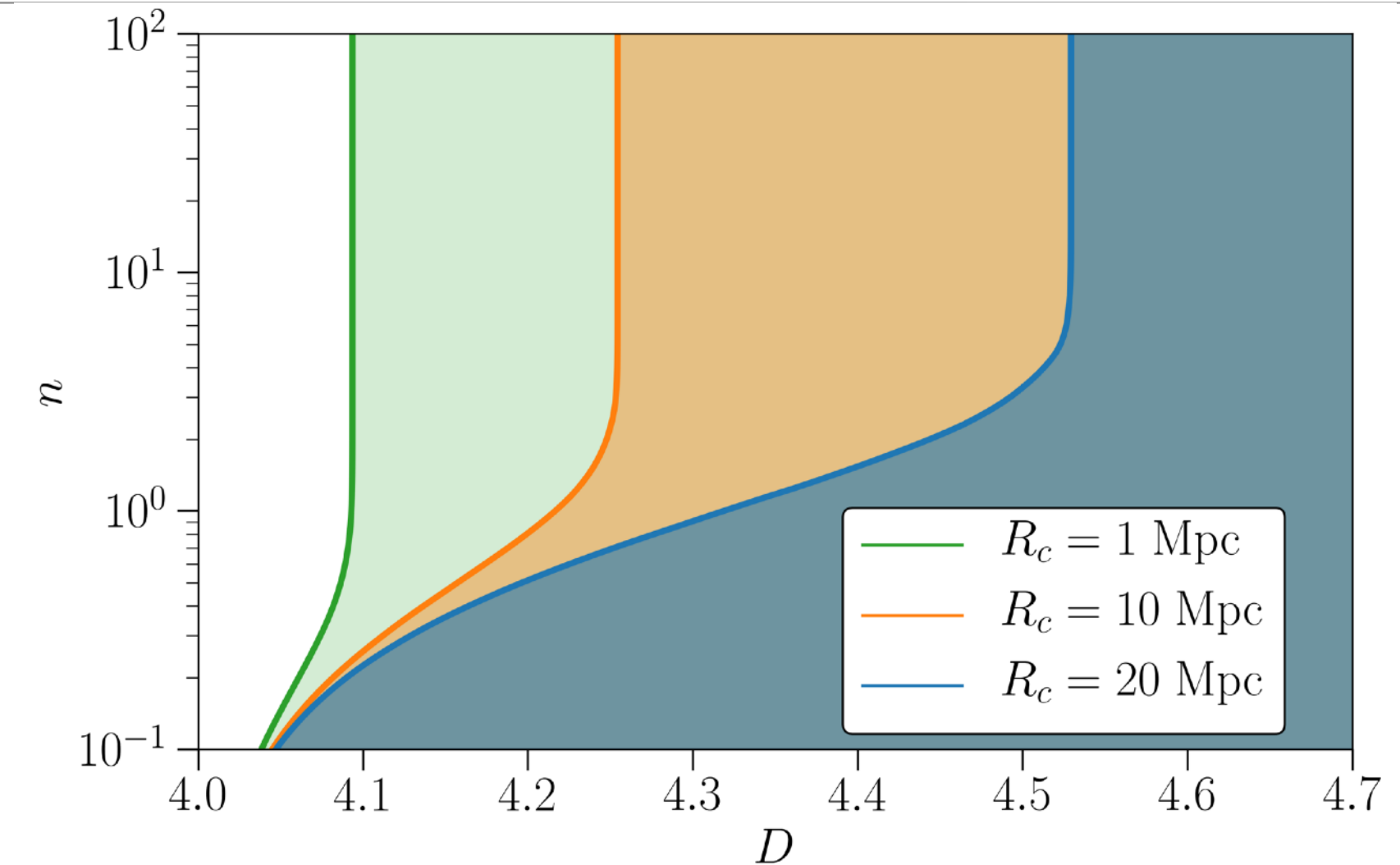
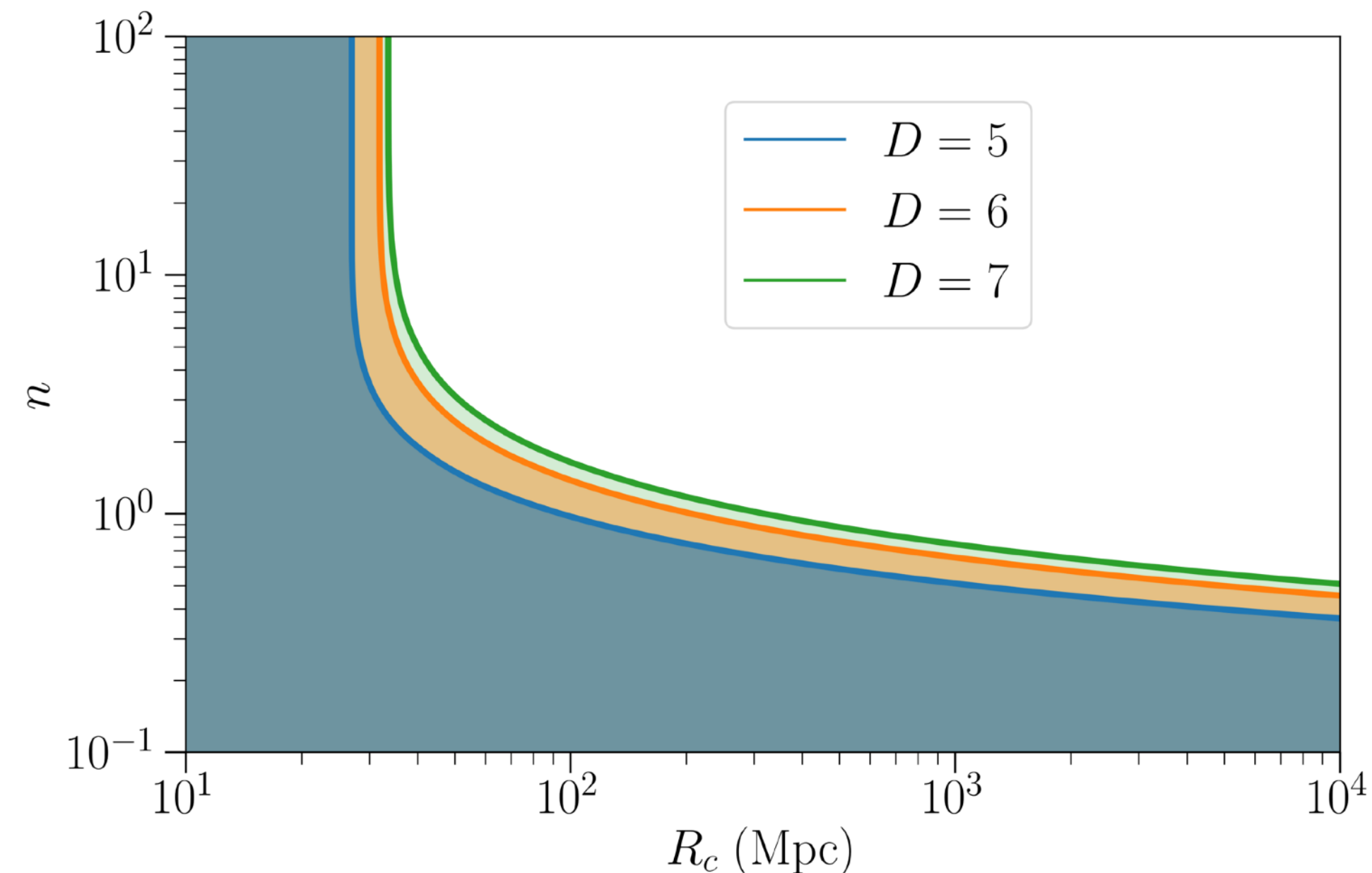


# GW170817: Test of extra dimensions

LVC 2018 [arXiv:1811.00364]

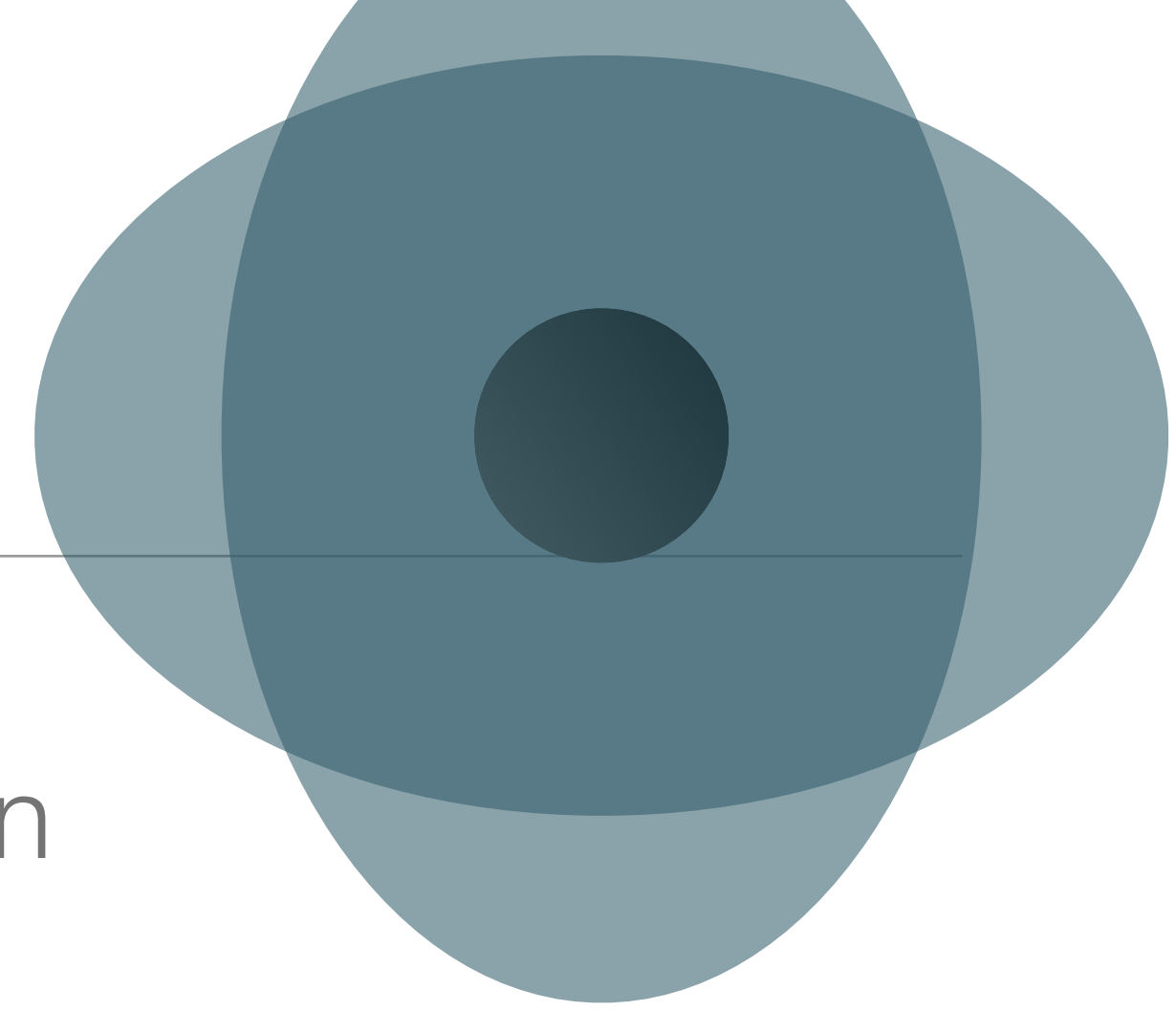
- GW detection + EM identification of host galaxy -> independent measurements of distance to source
- In higher-dim gravity, GWs may “leak” into extra dimensions (larger effective distance)

$$h \propto \frac{1}{d_L^{\text{GW}}} = \frac{1}{d_L^{\text{EM}}} \left[ 1 + \left( \frac{d_L^{\text{EM}}}{R_c} \right)^n \right]^{-(D-4)/(2n)}$$

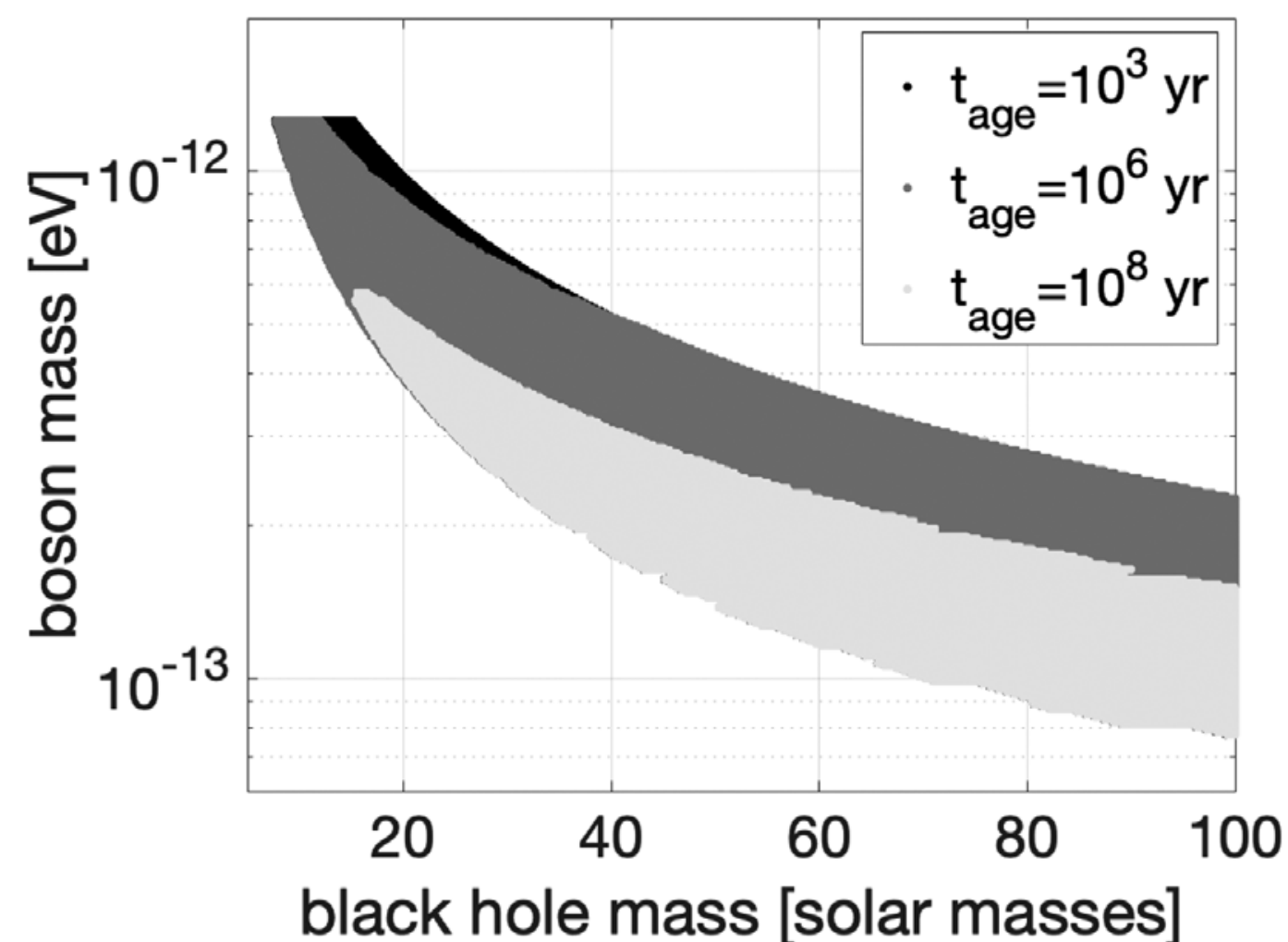


- screening out to “activation radius”  $R_c$
- $n$ : transition steepness
- Astrophysical length scales ->  $D=4$
- Cosmological length scales ( $R_c \sim R_H$ ):
  - slow transition ( $n \sim 0.1$ ):  $D=4$
  - steep transition: unconstrained

# Light bosons & BH Superradiance



- Growth of bosonic field with  $\frac{\hbar c}{m_b} \simeq \frac{GM_{BH}}{c^2}$ , stimulated by BH spin
  - Direct detection via CW emission
  - Indirect detection in population statistics (mass-spin plane)



- LVK sets bounds on long-duration signals from UL scalars [\[PRD 105, 102001\]](#)
- Continuous wave emission during cloud decay phase
- Axionic case fits with mass  $\sim 10^{-13} - 10^{-12}$  eV



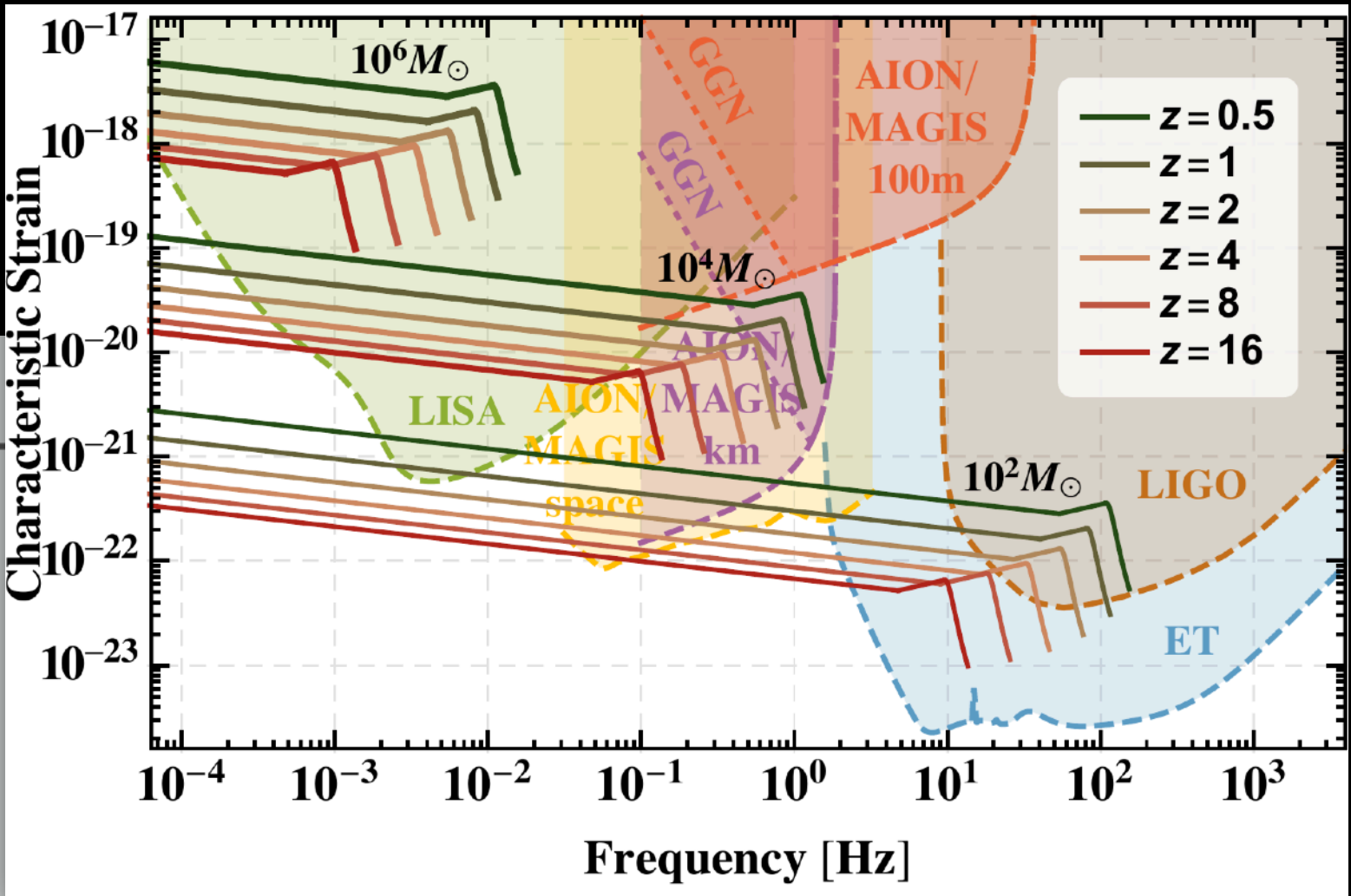
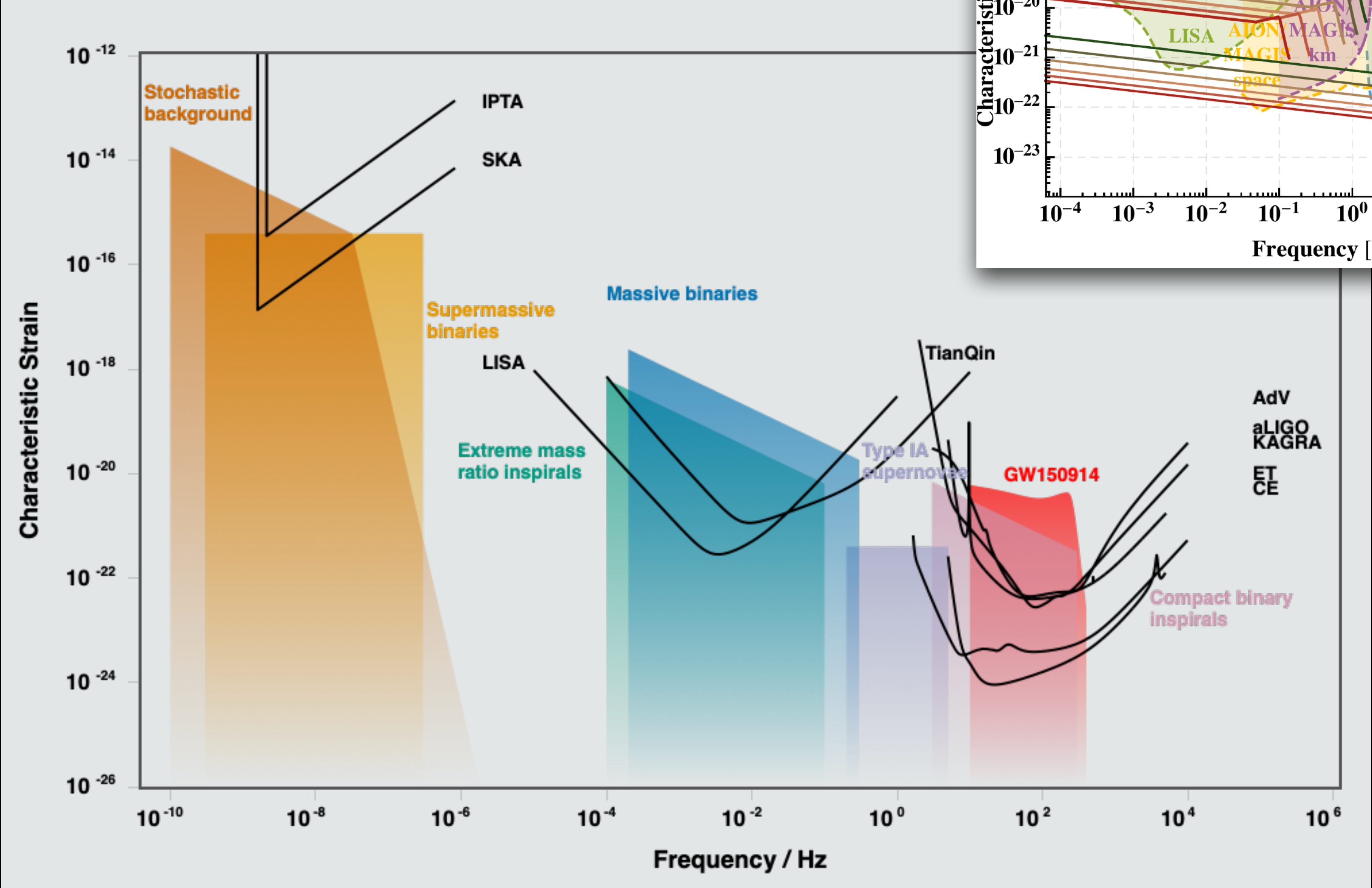
# GW Phenomenology of New Physics

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- Modified BH geometry (multipolar structure, QNMs)
- Modified binary dynamics
- Alternative polarizations (scalar, vector)
- Modified Dispersion Relation (massive, LIV)
- Speed of Gravity
- Superradiance (light boson)
- **Stochastics GW Background (cosmological/astrophysical)**
- **Phase transitions / topological defects**
- **Neutron star matter (composition, phase transitions)**
- **Stellar evolution**

FUTURE OF GW

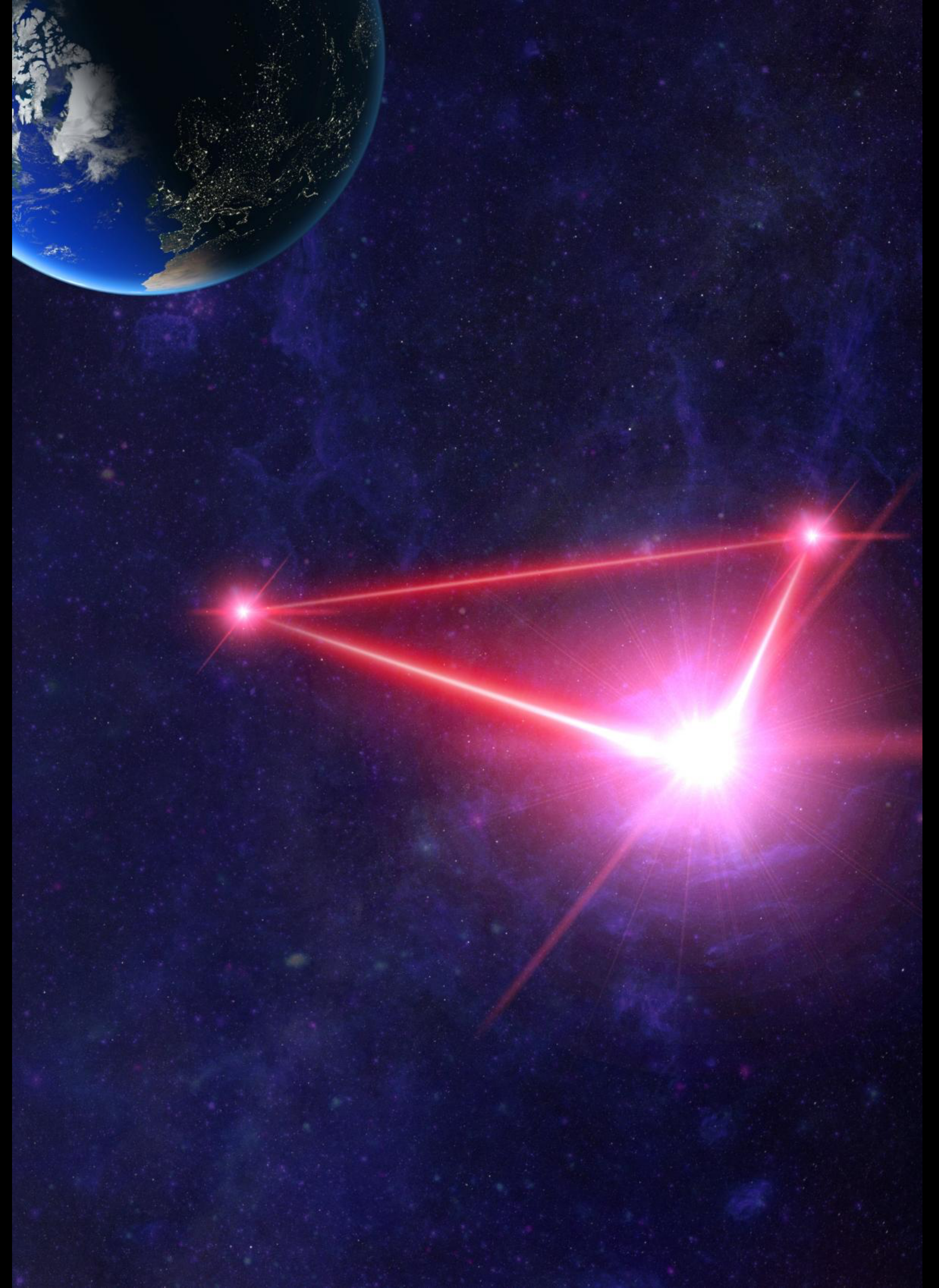
# Detectors & Sources





# LISA (2034+)

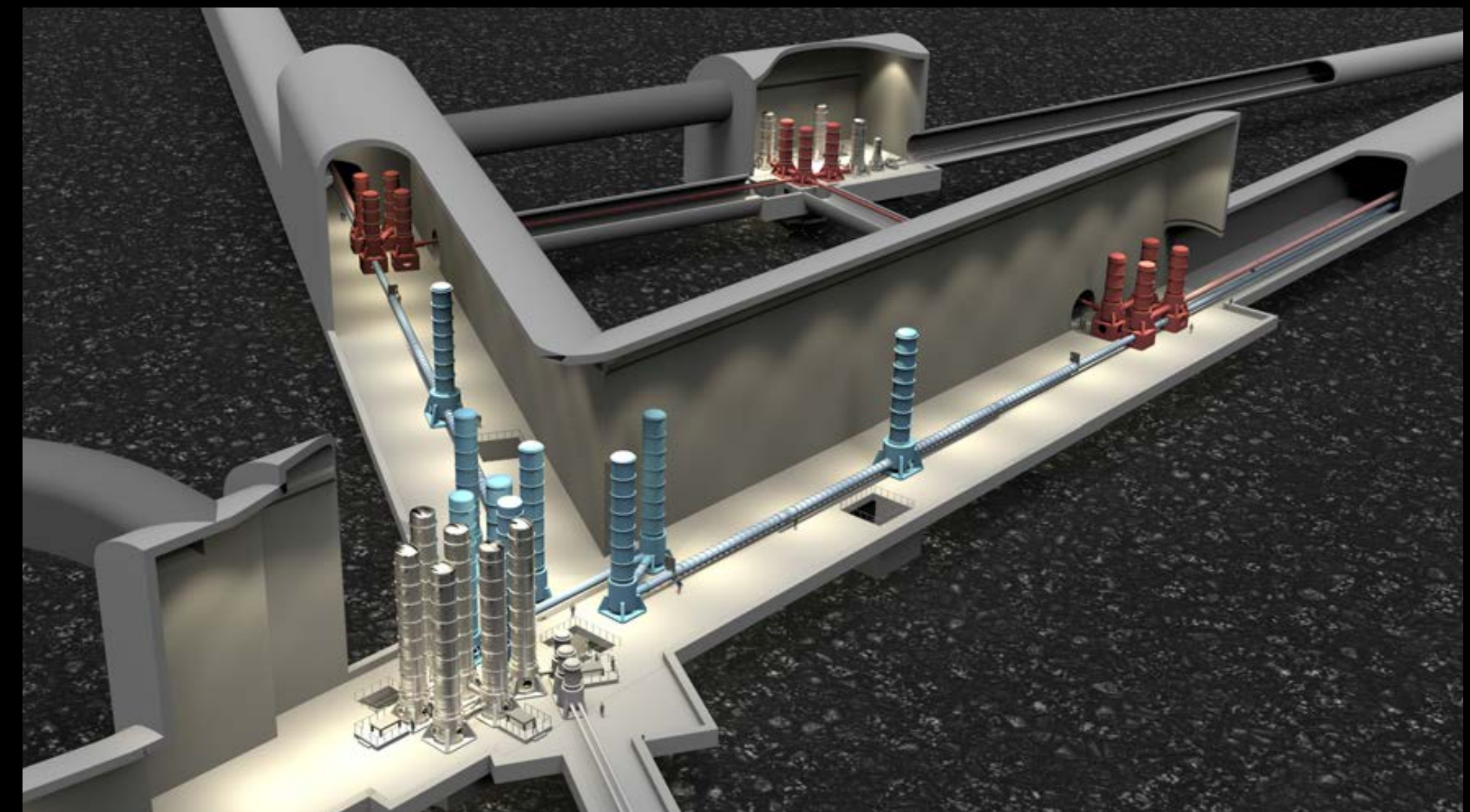
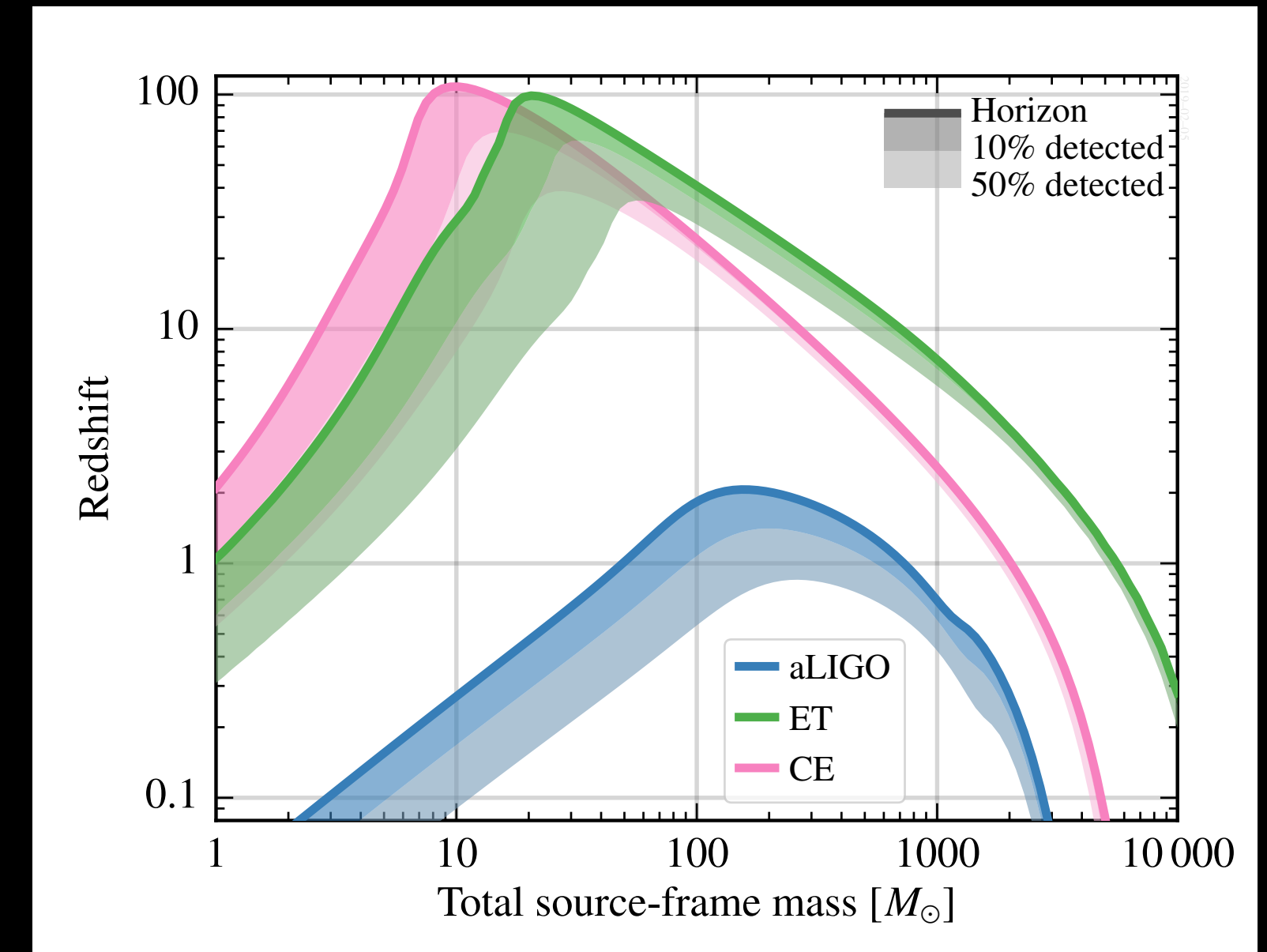
- Massive - Supermassive BBH mergers
- Horizon out to  $z \sim 10 - 20$
- MMA for transients
- Tests of GR
- Precision Black-Hole Spectroscopy
- Probe of MBH environment, DM halos, disks, etc
- Cosmology
- Physics in the Early Universe
  - Phase transitions
  - Cosmic string networks





# EINSTEIN TELESCOPE

- On the ESFRI Roadmap
- Candidate Sites:
  - i. Euregio Meuse-Rhine (NL) ii. Sardinia (IT)
- Scientific Consortium forming NOW!
- 10 km arm lengths
- Triangular shape
- Underground
- Cryogenic optics
- Improved sensitivity @ high- & low-freq
- Increase in sensitivity by  $O(10)$

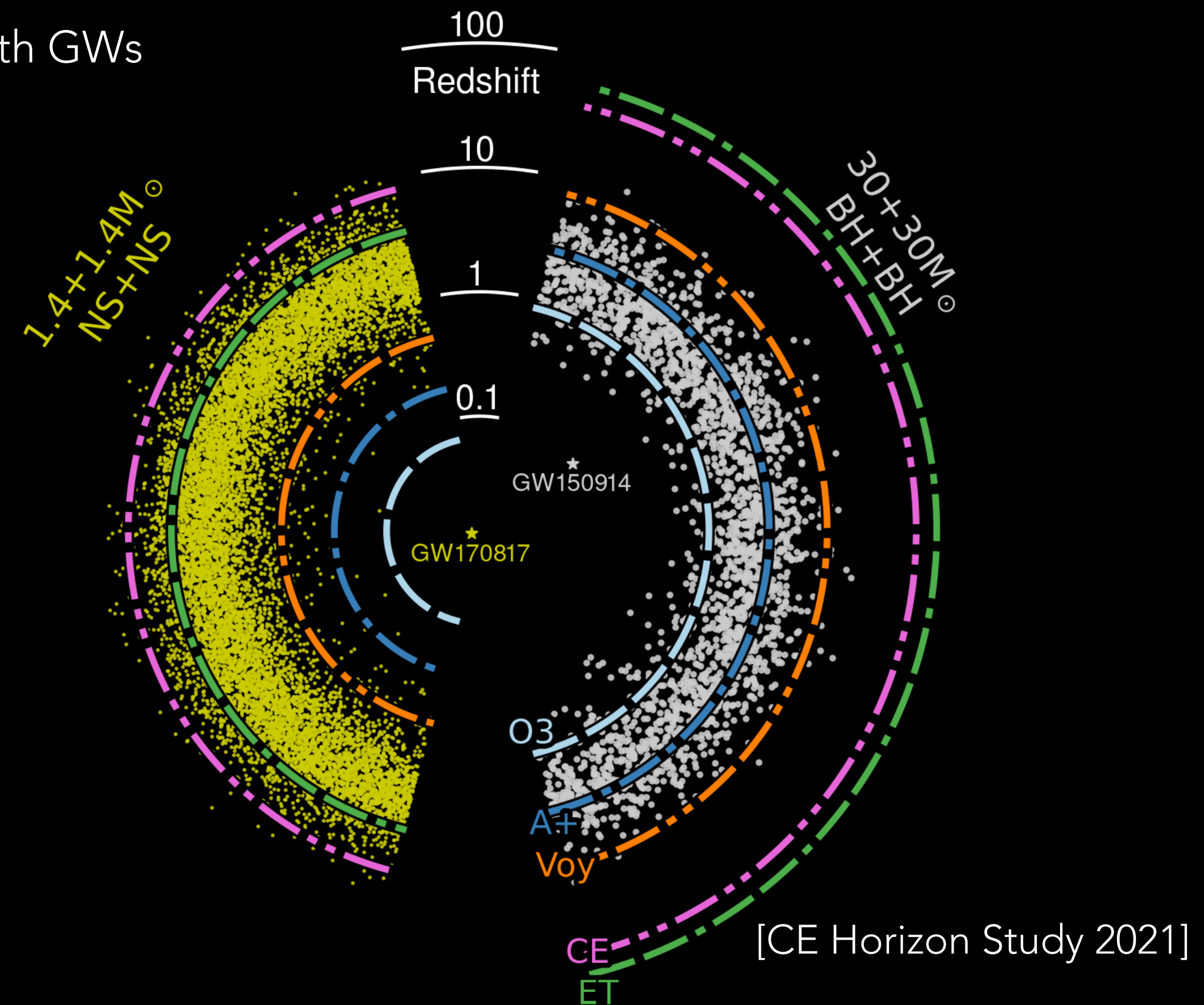




# THE SCIENCE OF 3G DETECTORS

- Multimessenger Astronomy with GWs
  - 100,000 - 1,000,000 CBC sources/yr
  - Improved Sky Localization for EM-bright transients
  - Early warning for transient events (e.g. BNS)
  - Multi-band detections (LISA -> AION -> ET/CE)
  - Supernova event detection
- Fundamental Physics
  - Tests of GR vs Modified Gravity
  - Precision BH Spectroscopy
  - Near-horizon physics & Exotic Compact Objects
  - Fundamental fields, DM, DE
  - Tight constraints on NS matter and EoS (pre- & post-merger)

- Cosmology
  - Cosmography with high-z population of sources
  - Stochastic backgrounds (cosmological/astrophysical)
  - Tests of  $\Lambda$ CDM with GWs
  - Cosmic strings
  - GW Lensing





## DATA AVAILABLE ONLINE!

- Detector strain data & more  
[www.gw-openscience.org](http://www.gw-openscience.org)
- Data release GWTC-2  
<https://dcc.ligo.org/LIGO-P2000438/public>
- Full posterior samples GWTC-2  
<https://zenodo.org/record/5172704#.YTOaSC1h2Zw>