



Higgs 2022 | PISA

Higgs and flavour anomalies

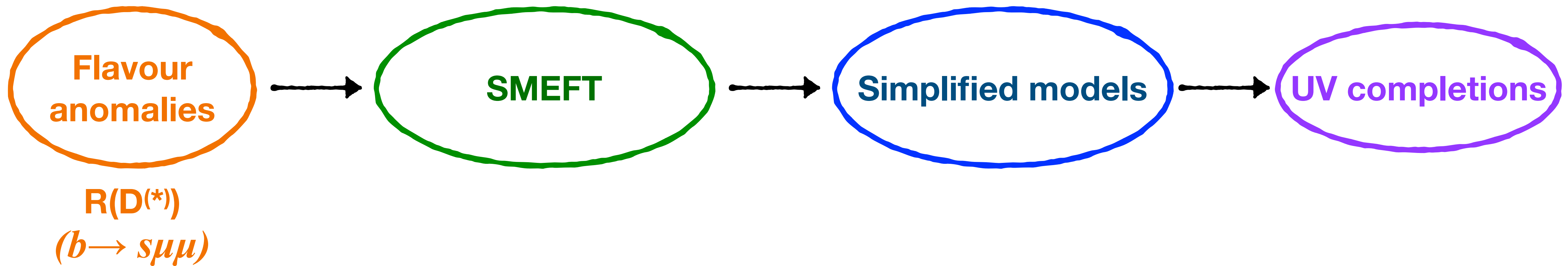
David Marzocca



11 - 11 - 2022

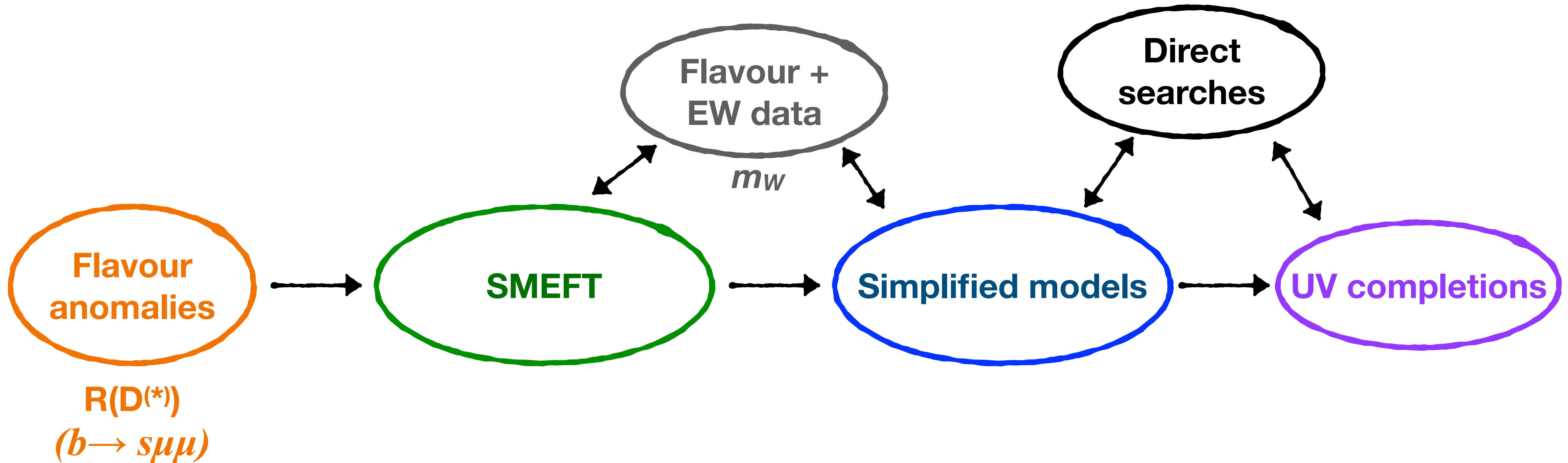
Higgs and the Flavour Anomalies

What are the possible connections?



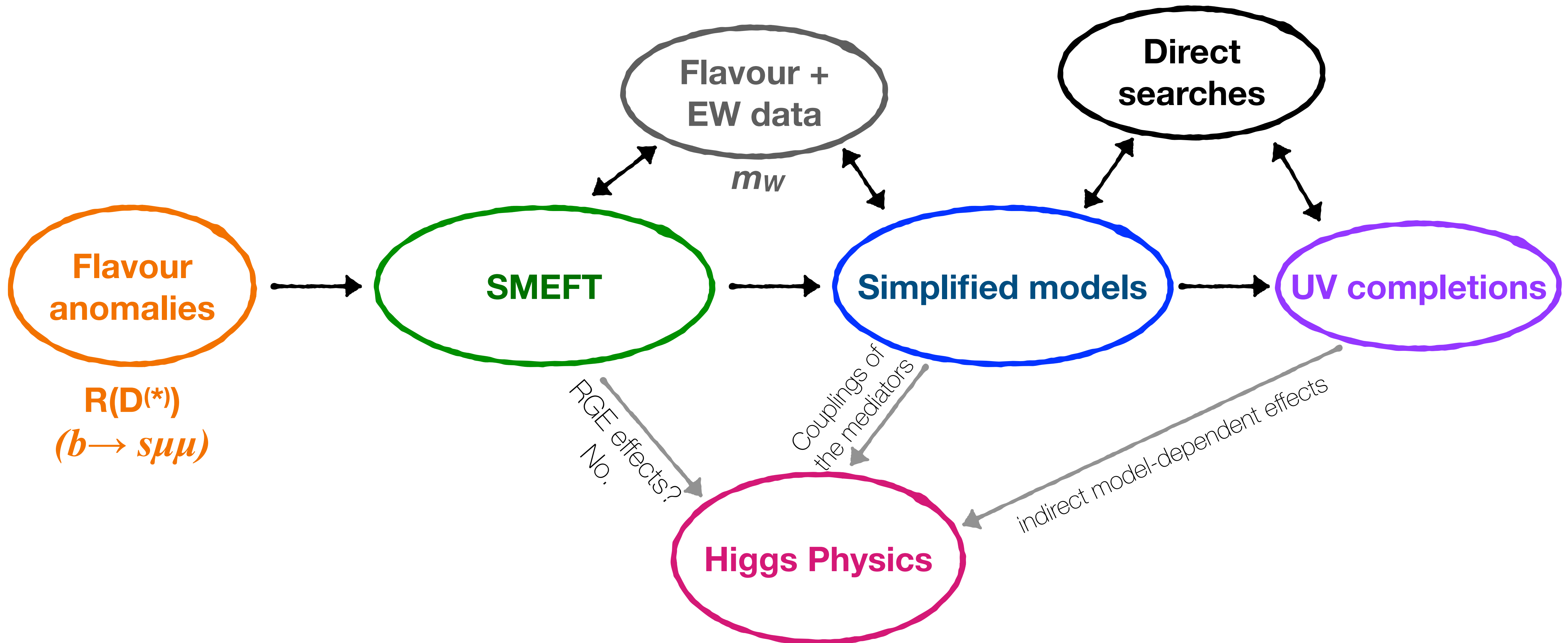
Higgs and the Flavour Anomalies

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Higgs and the Flavour Anomalies

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B-anomalies

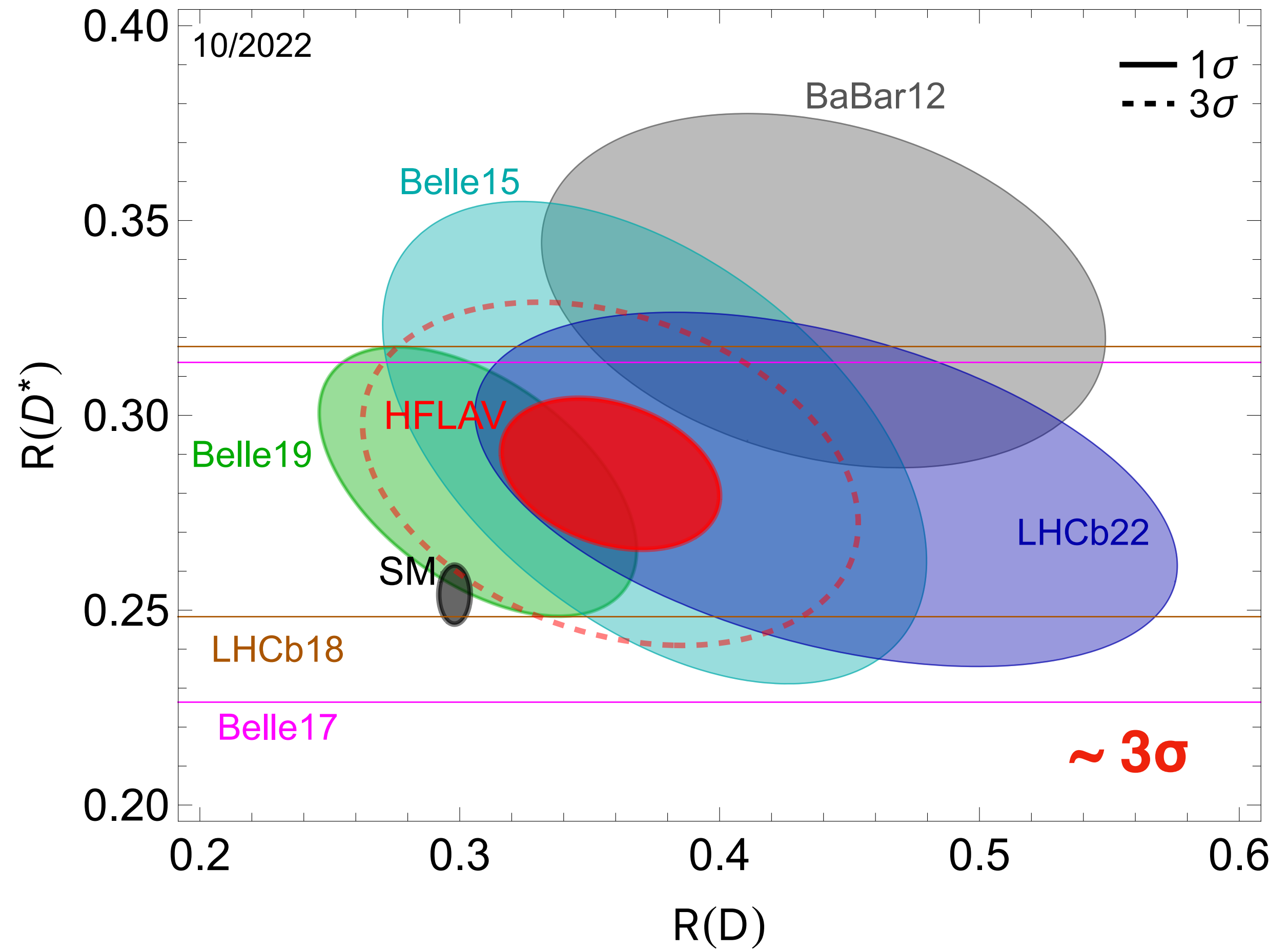
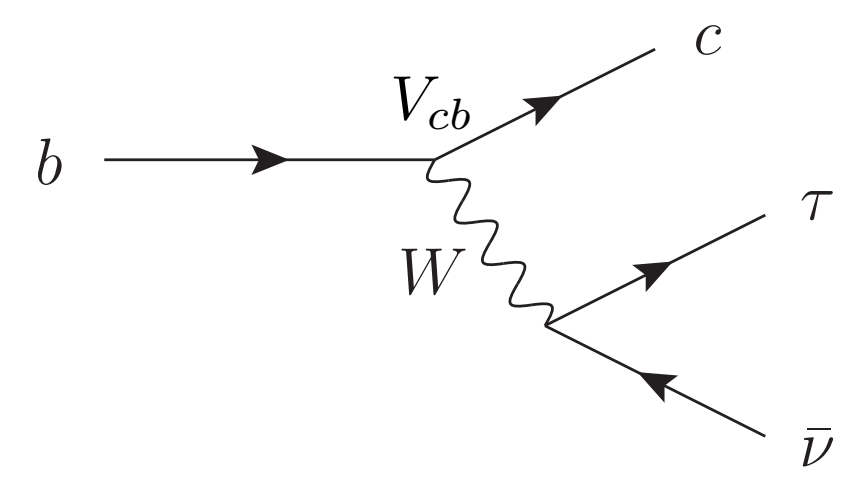
$$b \rightarrow c \tau \bar{\nu}_\tau$$

Lepton Flavour Universality

$$R(D^{(*)}) \equiv \frac{\mathcal{B}(B^0 \rightarrow D^{(*)+} \tau \nu)}{\mathcal{B}(B^0 \rightarrow D^{(*)+} \ell \nu)},$$

$\ell = \mu, e$

Tree-level SM process with V_{cb} suppression.



Latest LHCb'22 $R(D^{(*)})$ result still based on Run-1 data. Waiting for Run-2 results.. Also waiting for the first Belle-II results!

B-anomalies

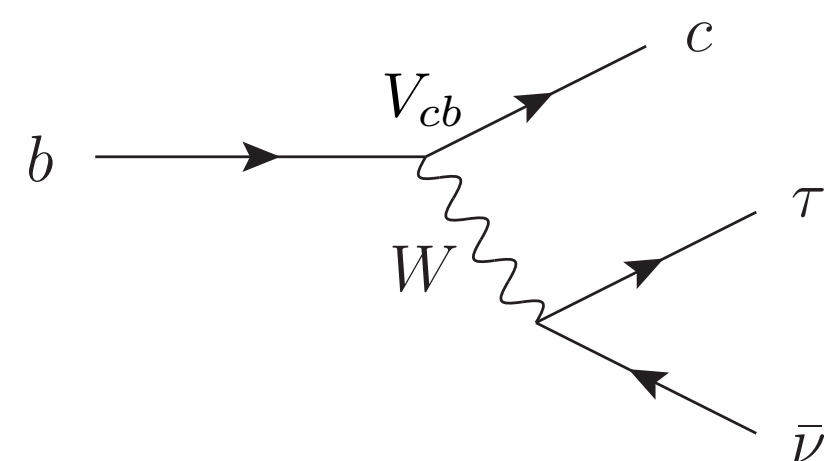
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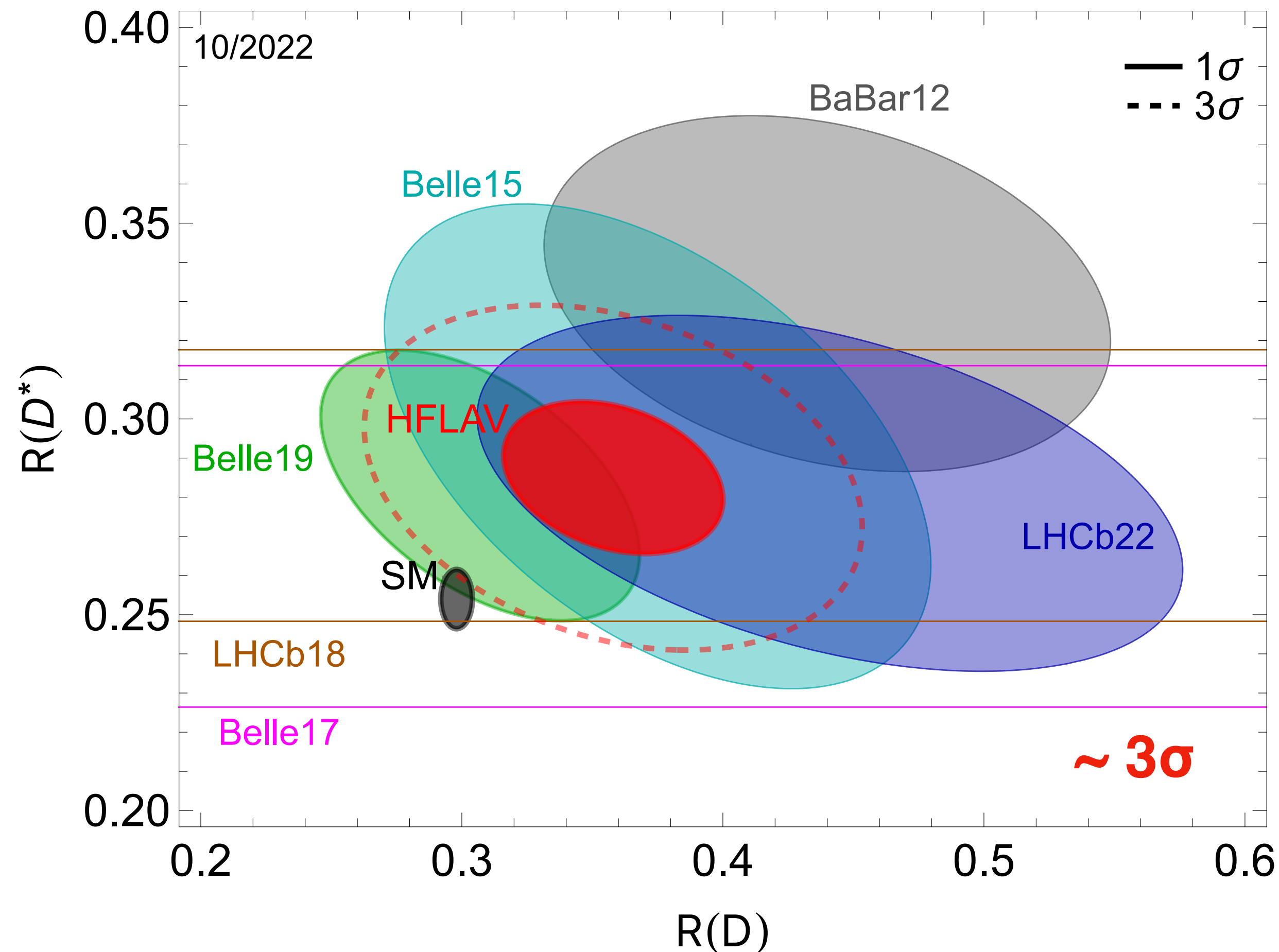
Tree-level SM process
with V_{cb} suppression.



~13% enhancement from the SM amplitude

Requires a **New Physics scale** of

$$C_{cb\tau\nu}^{R(D^{(*)})} \sim (4 \text{ TeV})^{-2}$$



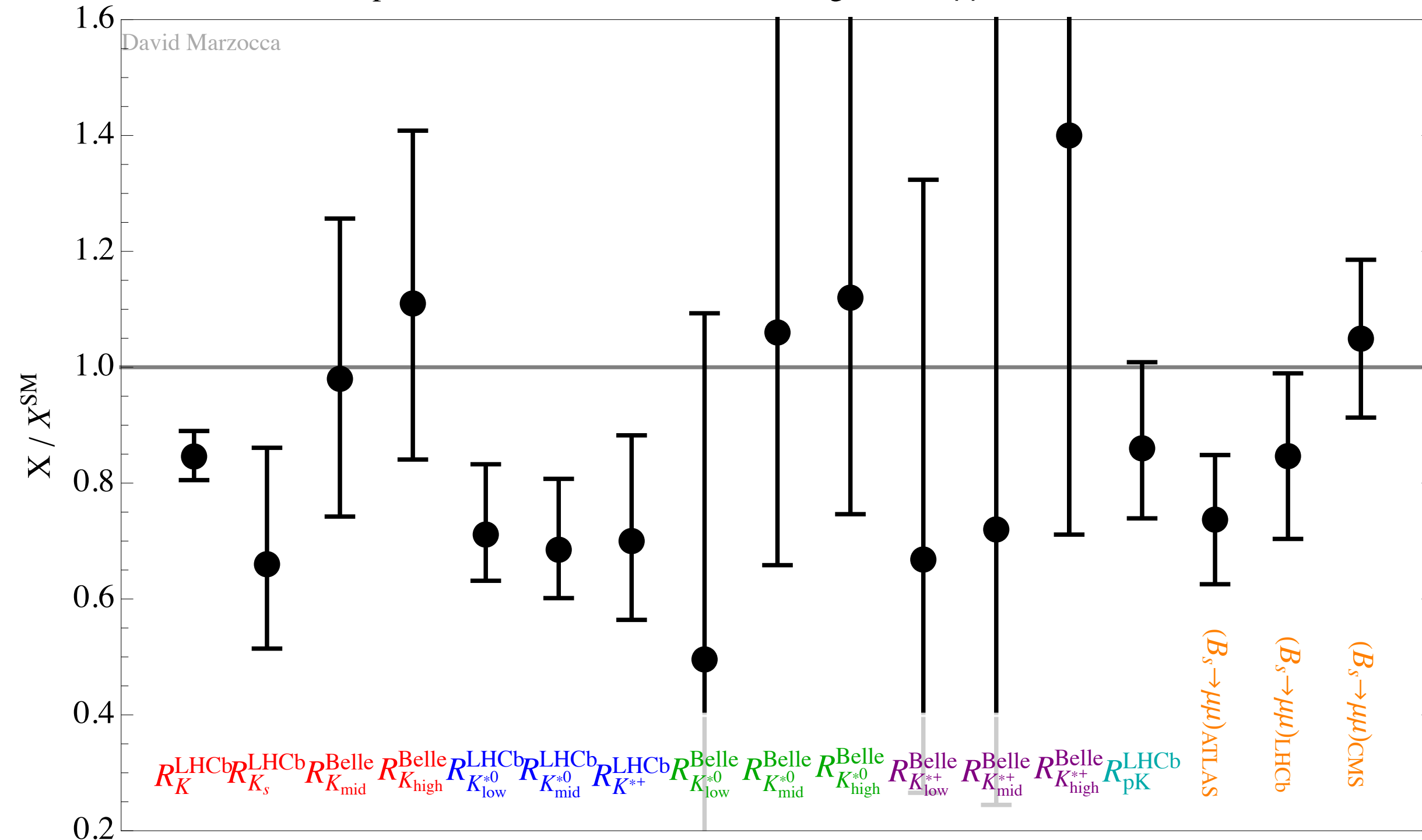
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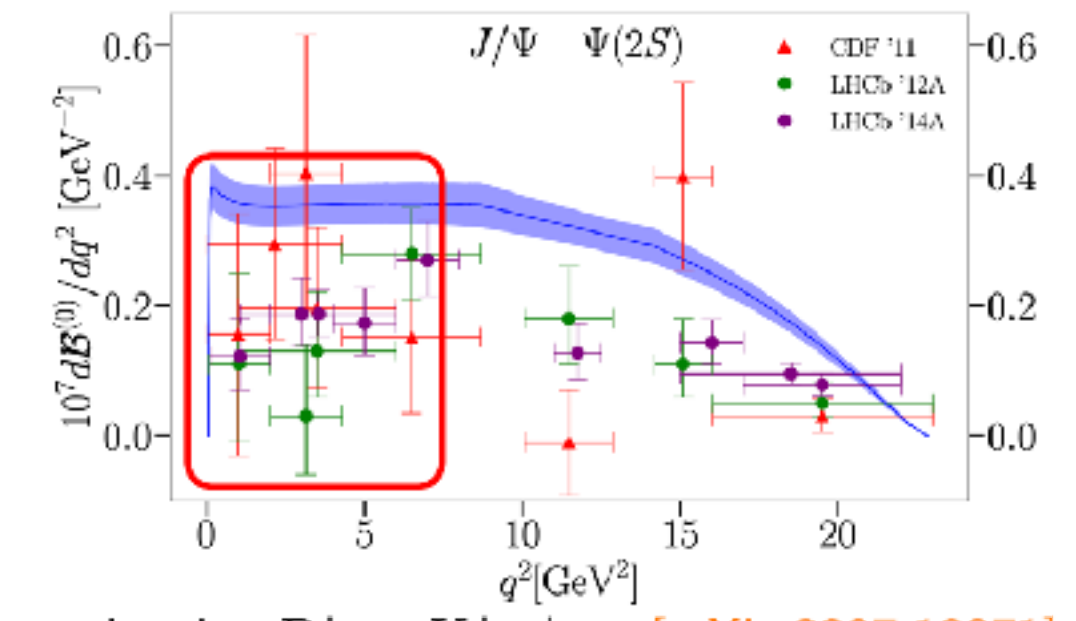
"Clean" observables

Compilation of clean observables testing the $b \rightarrow s \mu \mu$ transition. 08/2022

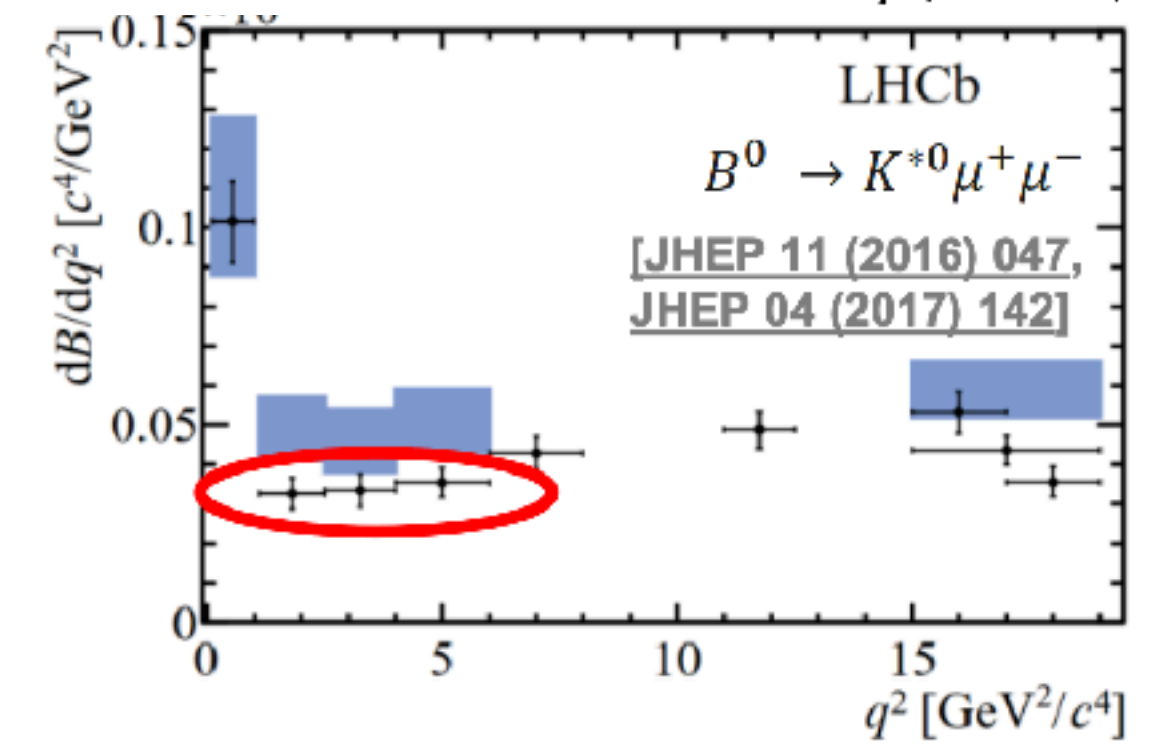
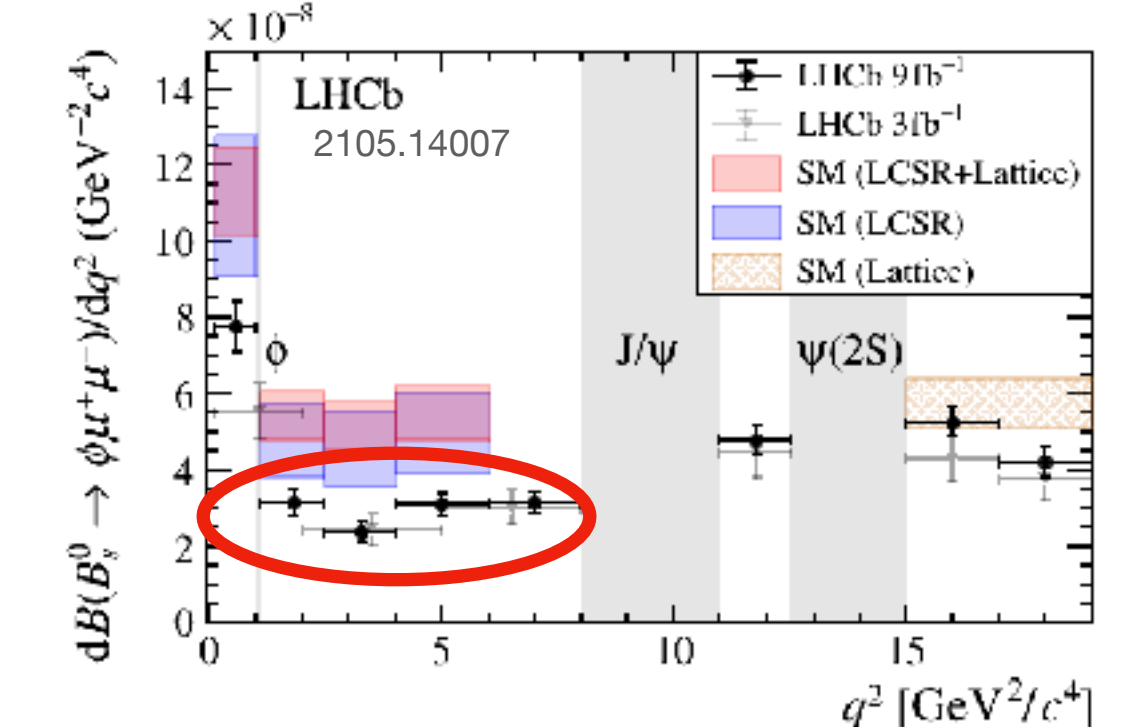
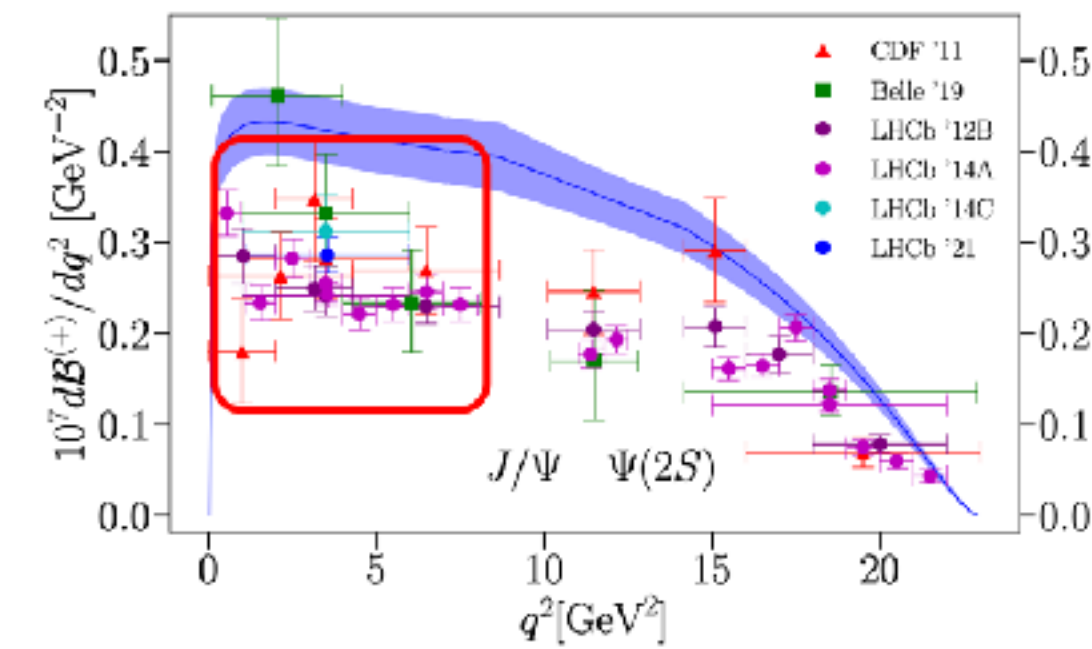


Branching ratios

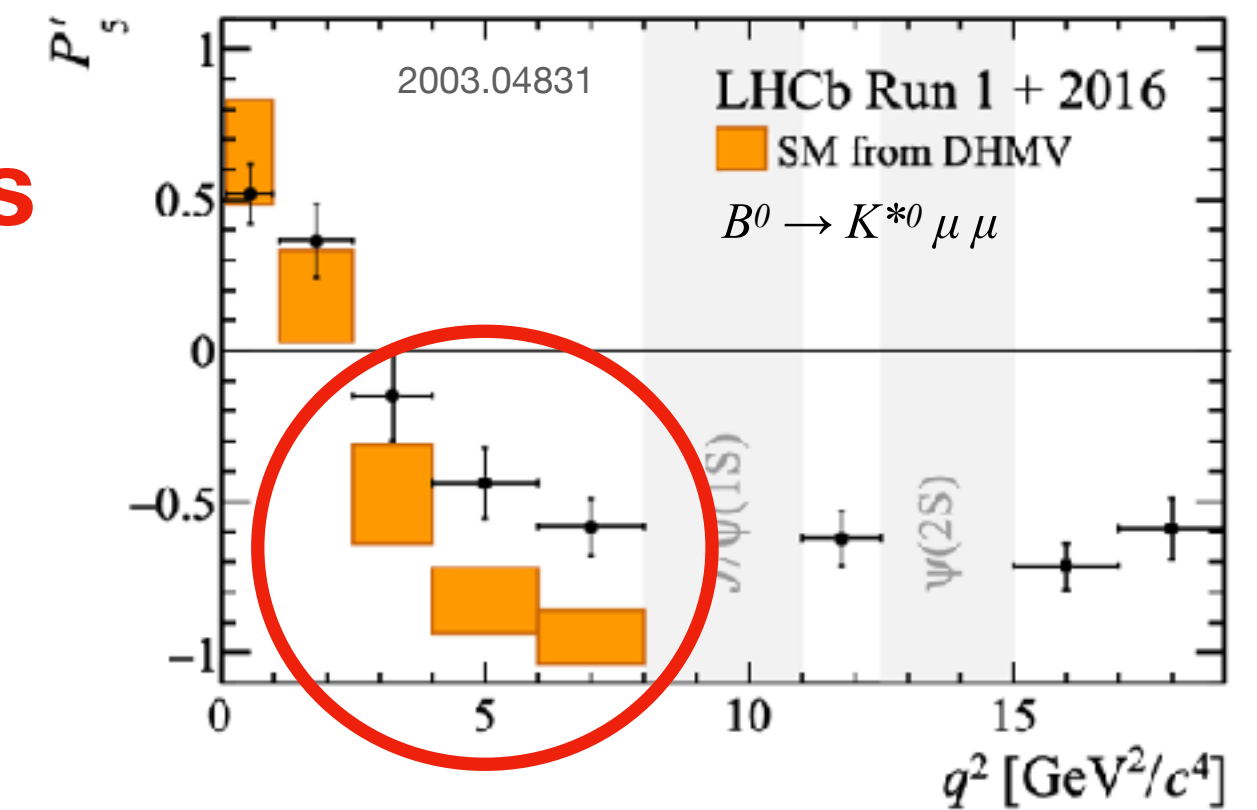
Lattice $B^0 \rightarrow K^0 \mu^+ \mu^-$ [arXiv:2207.13371]



Lattice $B^+ \rightarrow K^+ \mu^+ \mu^-$ [arXiv:2207.13371]



Angular observables

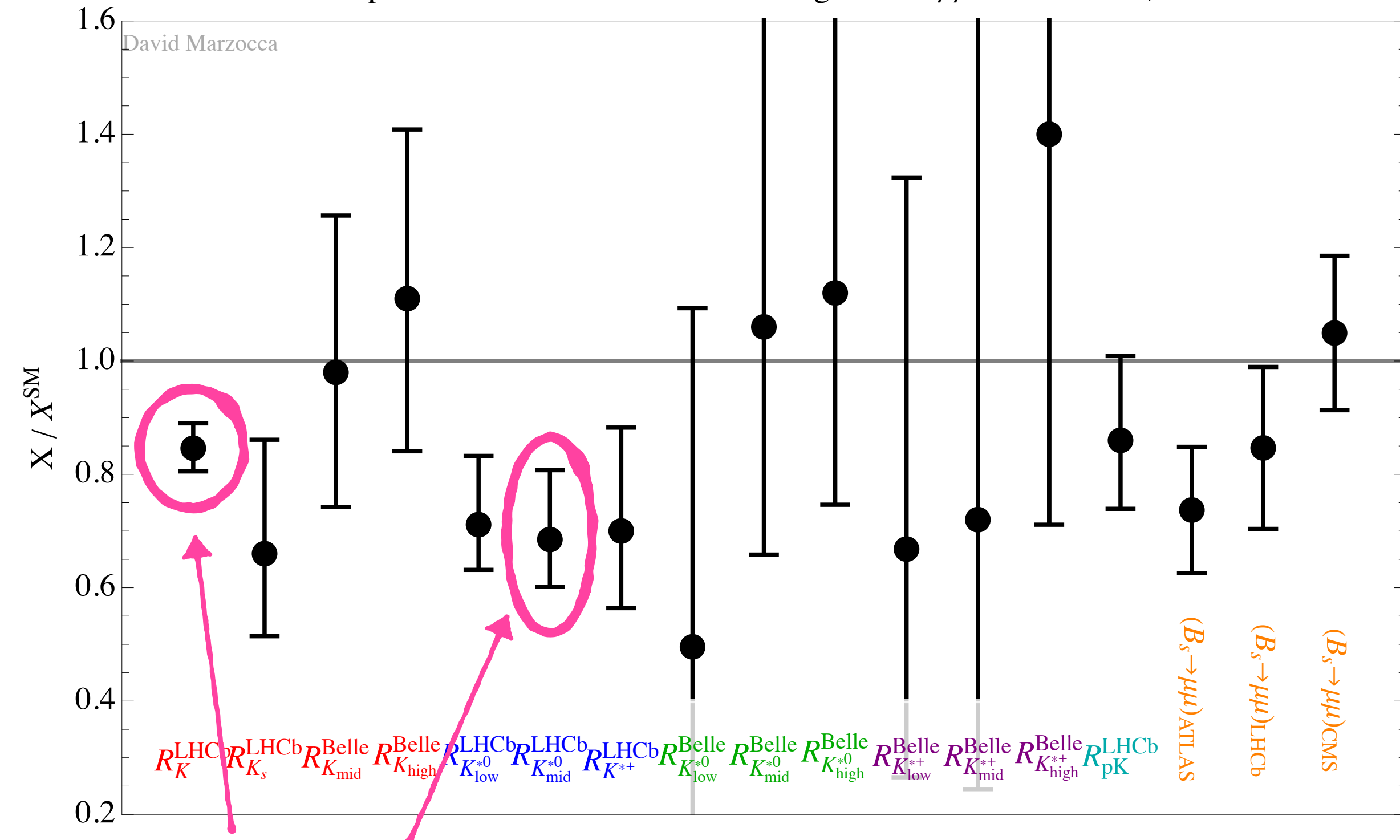


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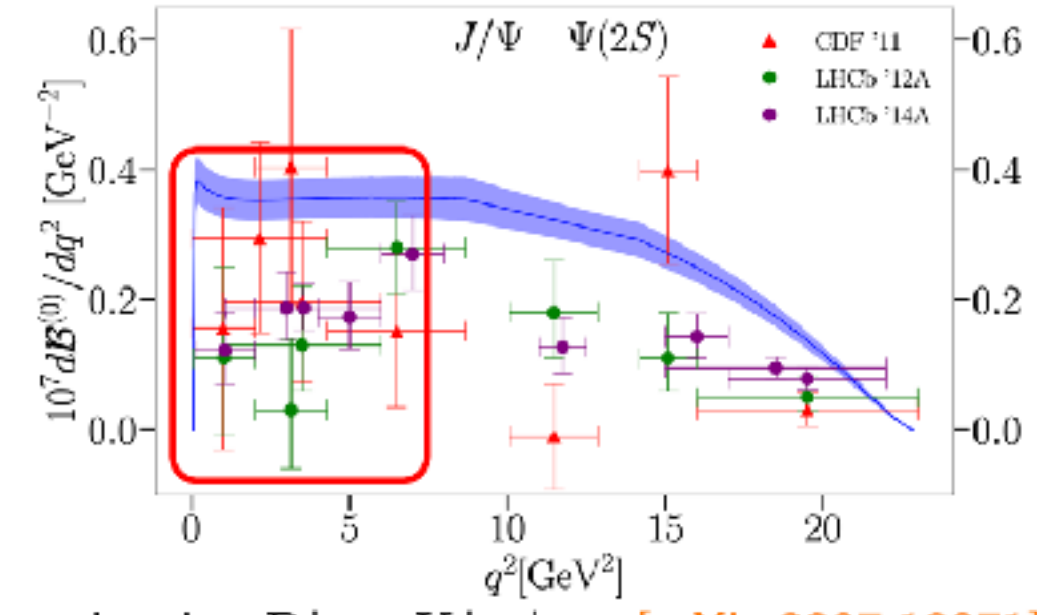
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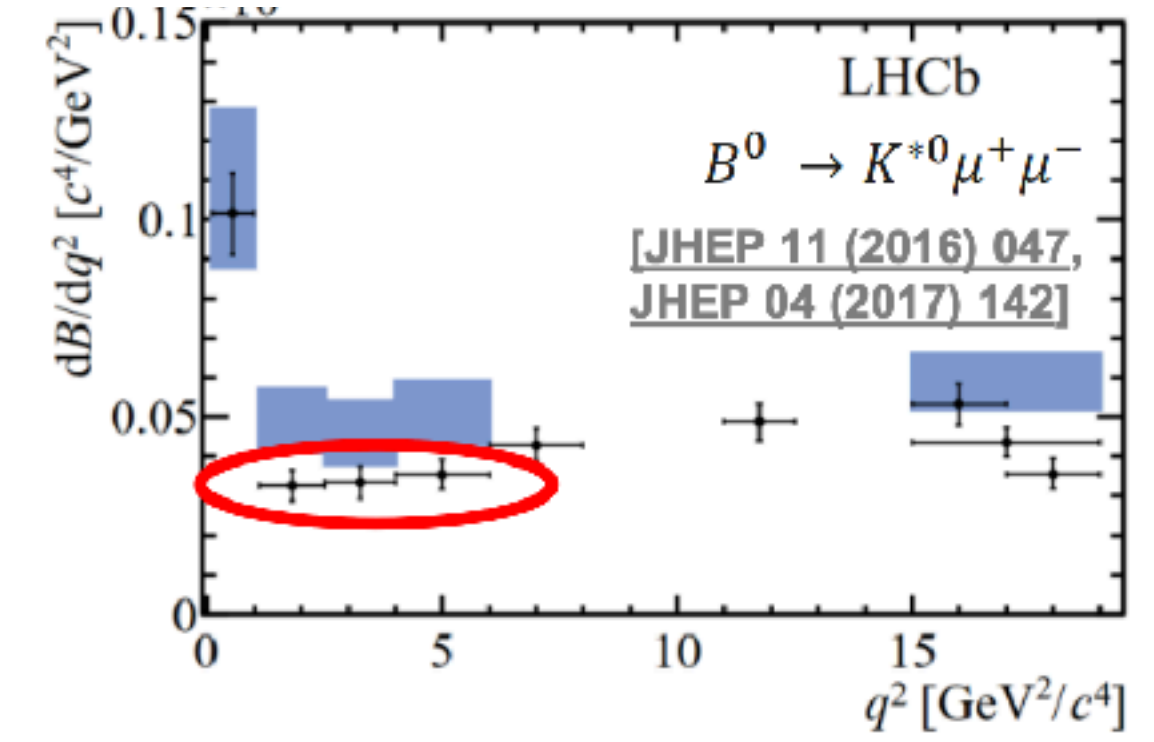
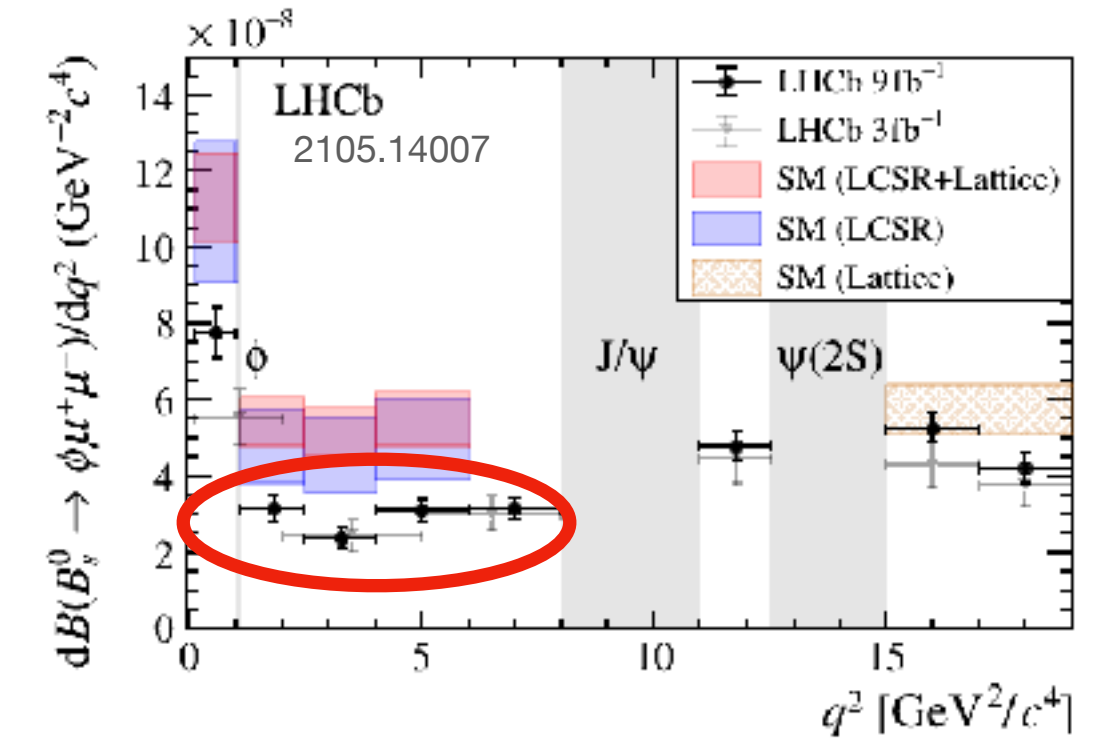
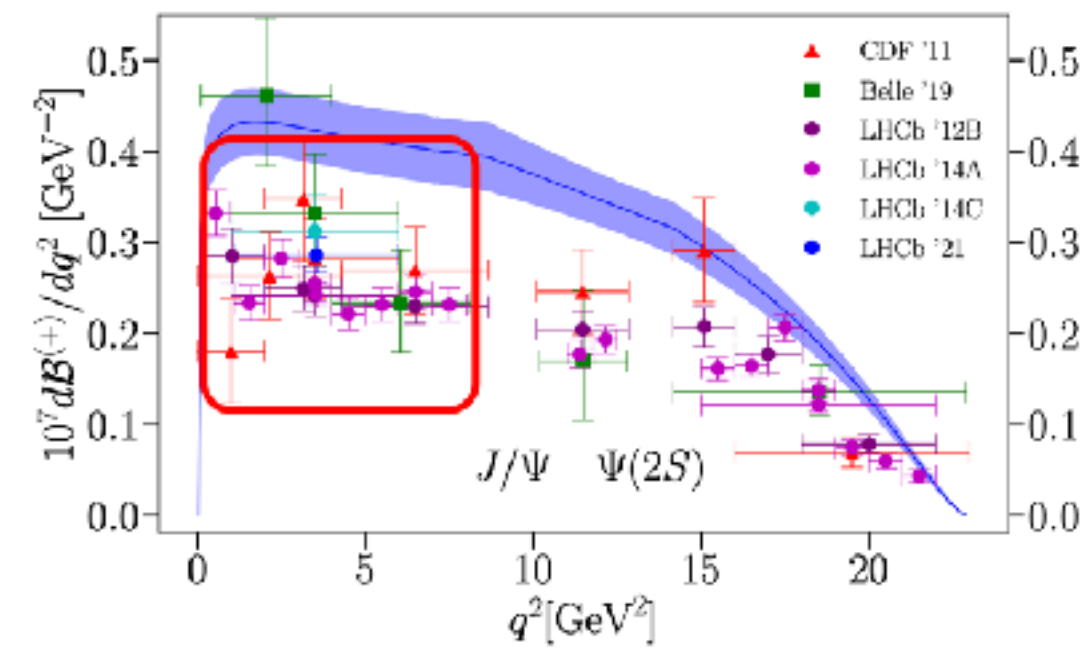
Waiting for the LHCb re-analysis of the Run-2 data for the joint R_K - R_{K^*} measurement.

Branching ratios

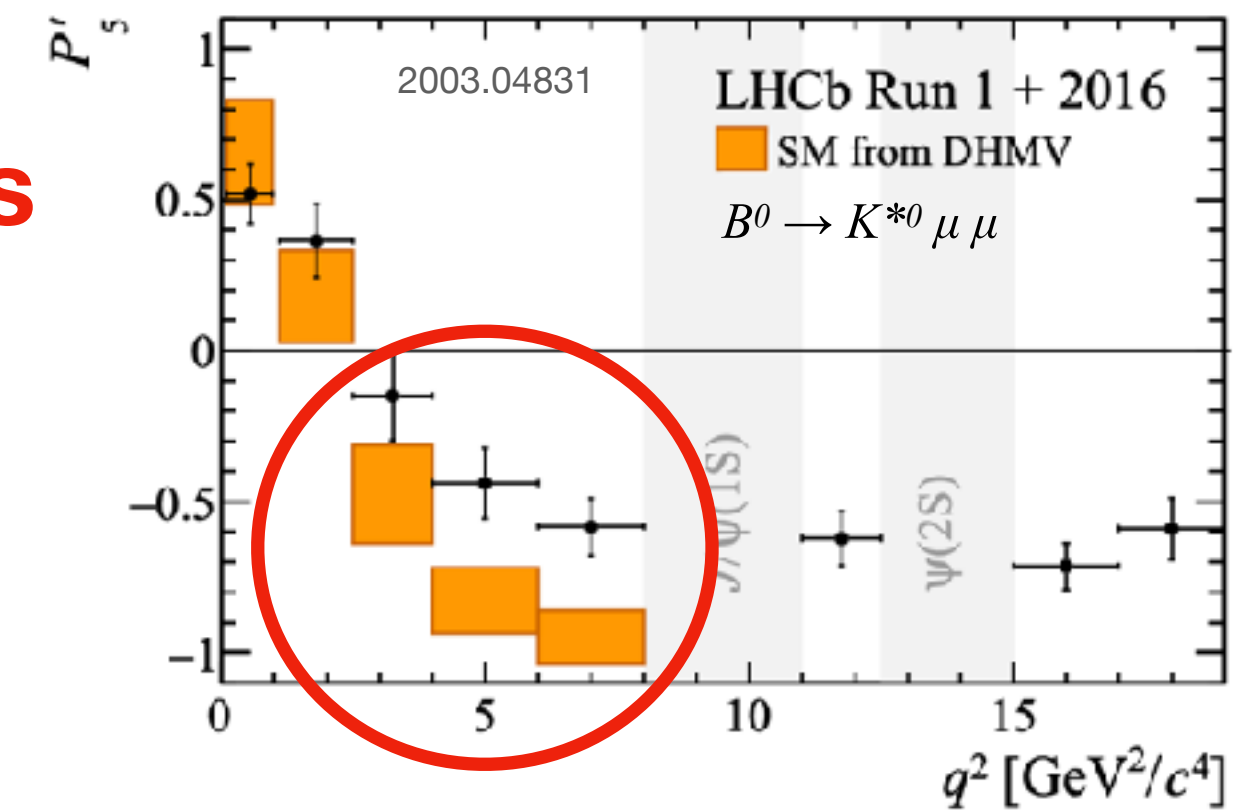
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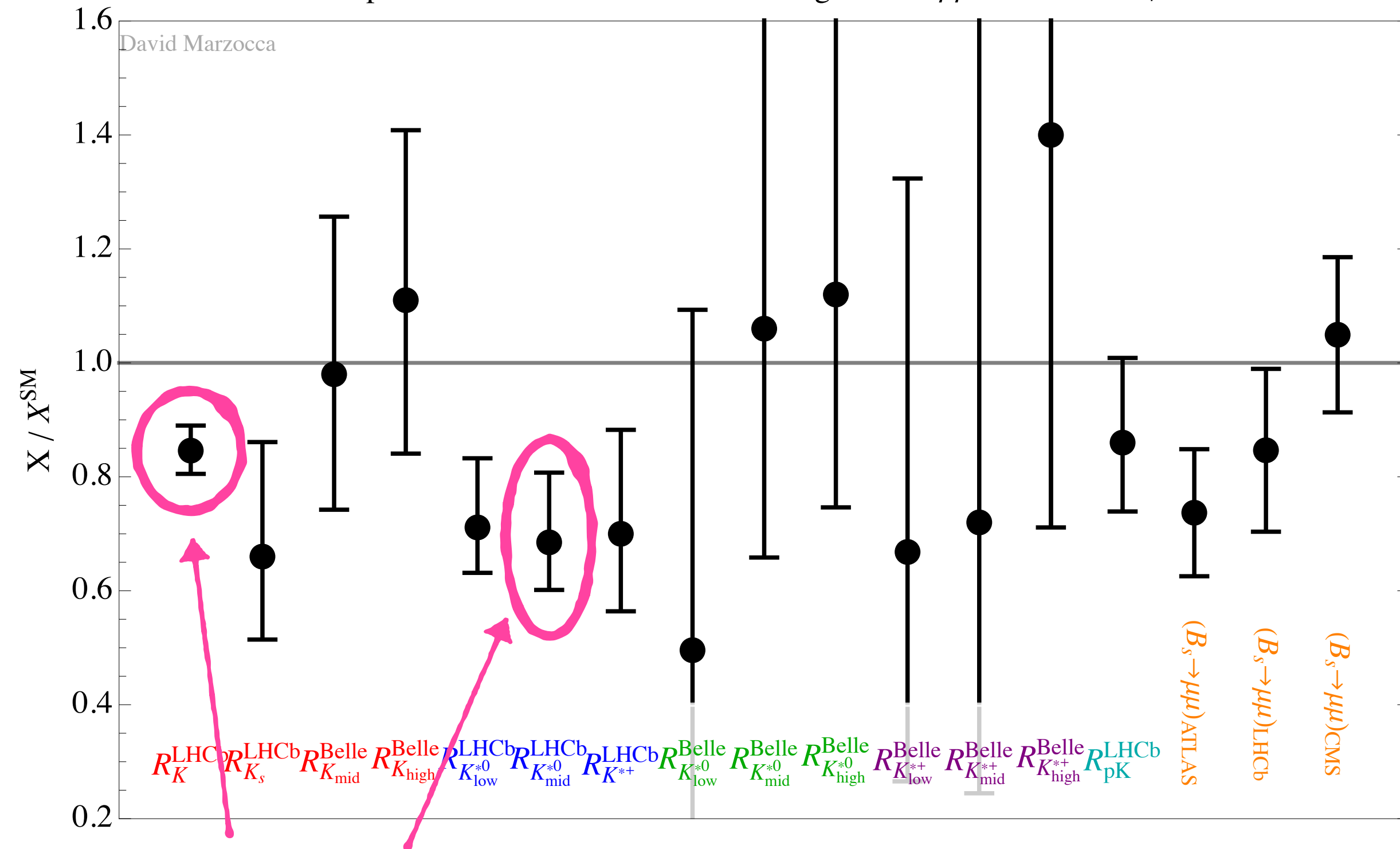


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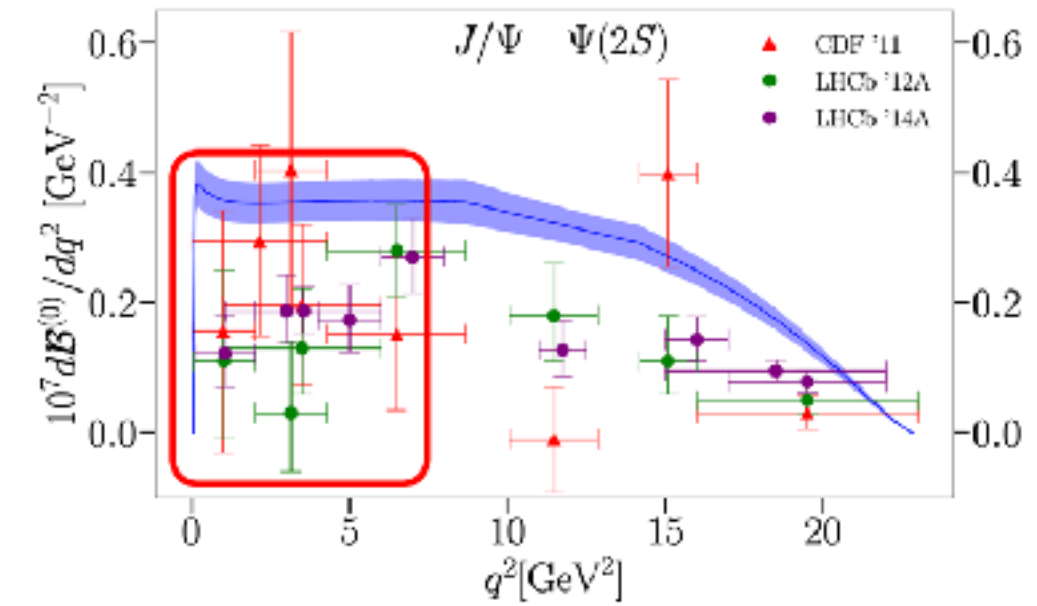
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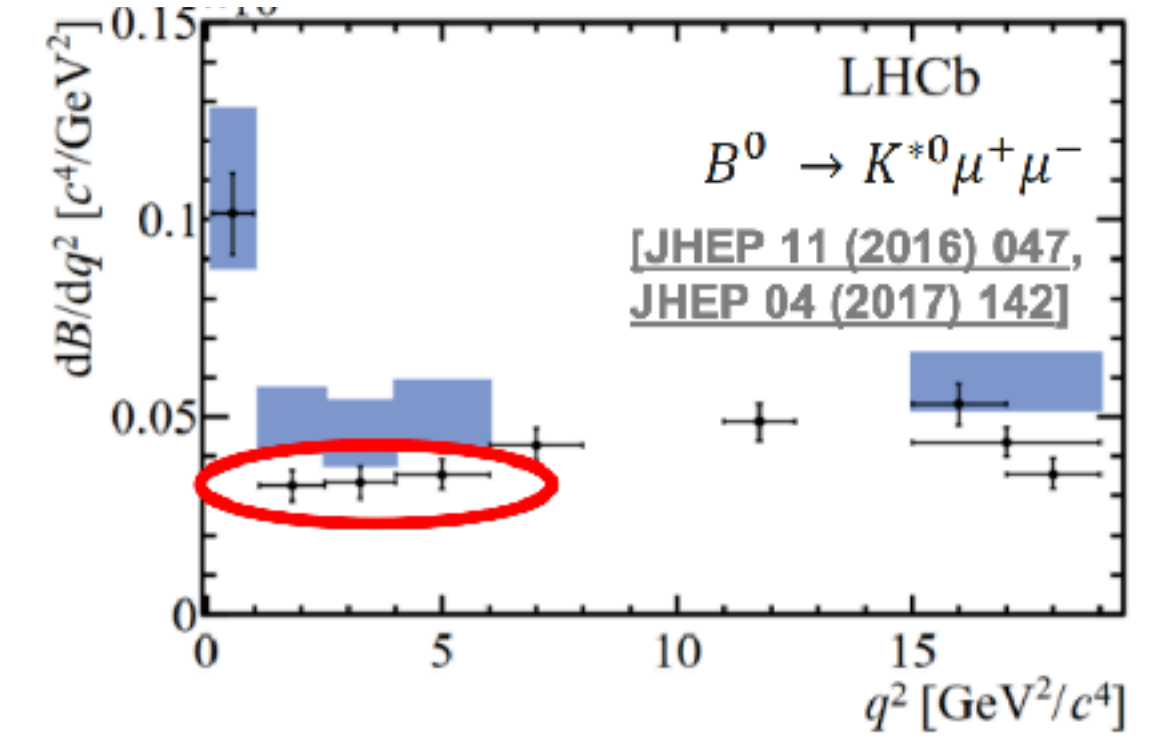
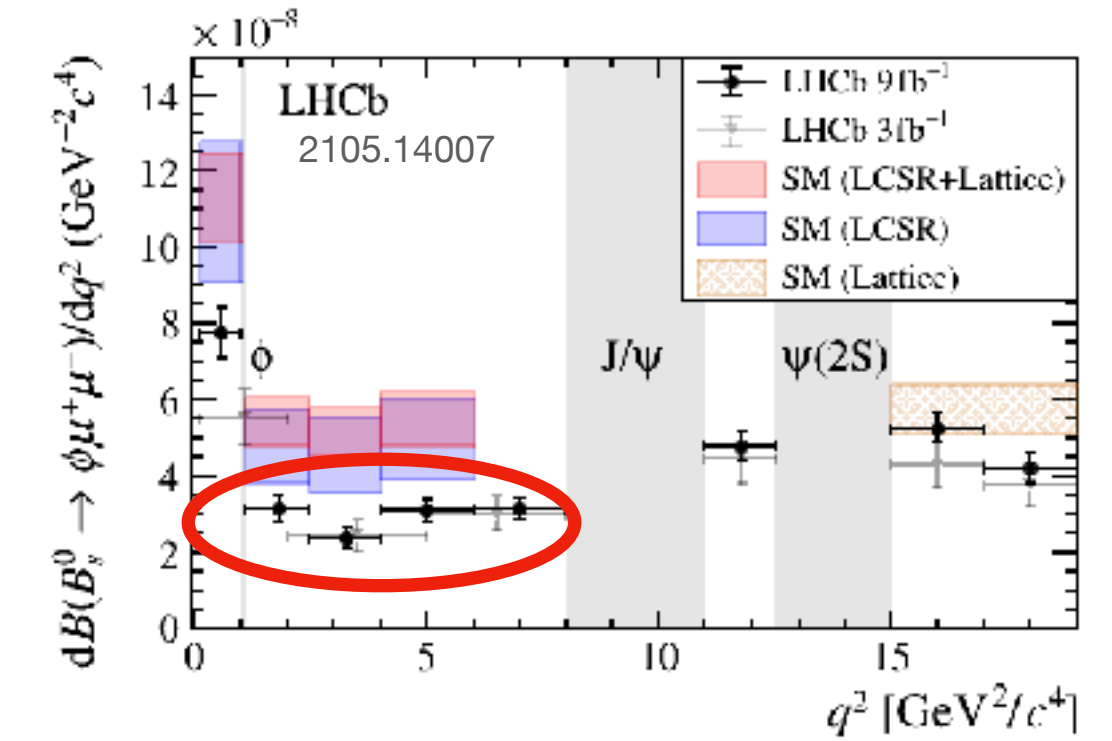
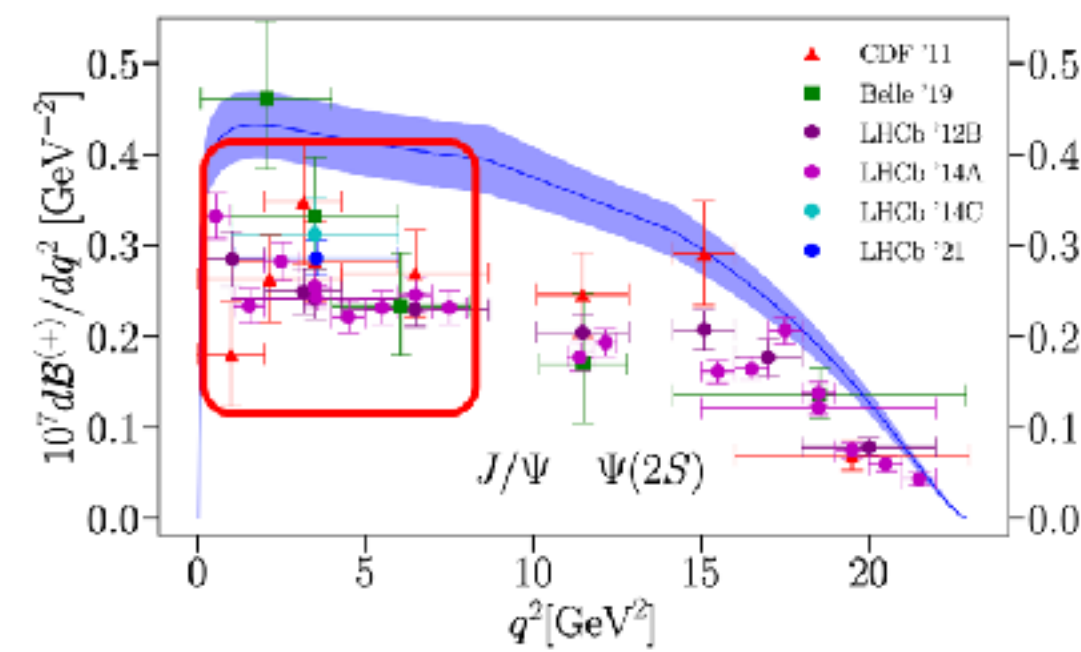


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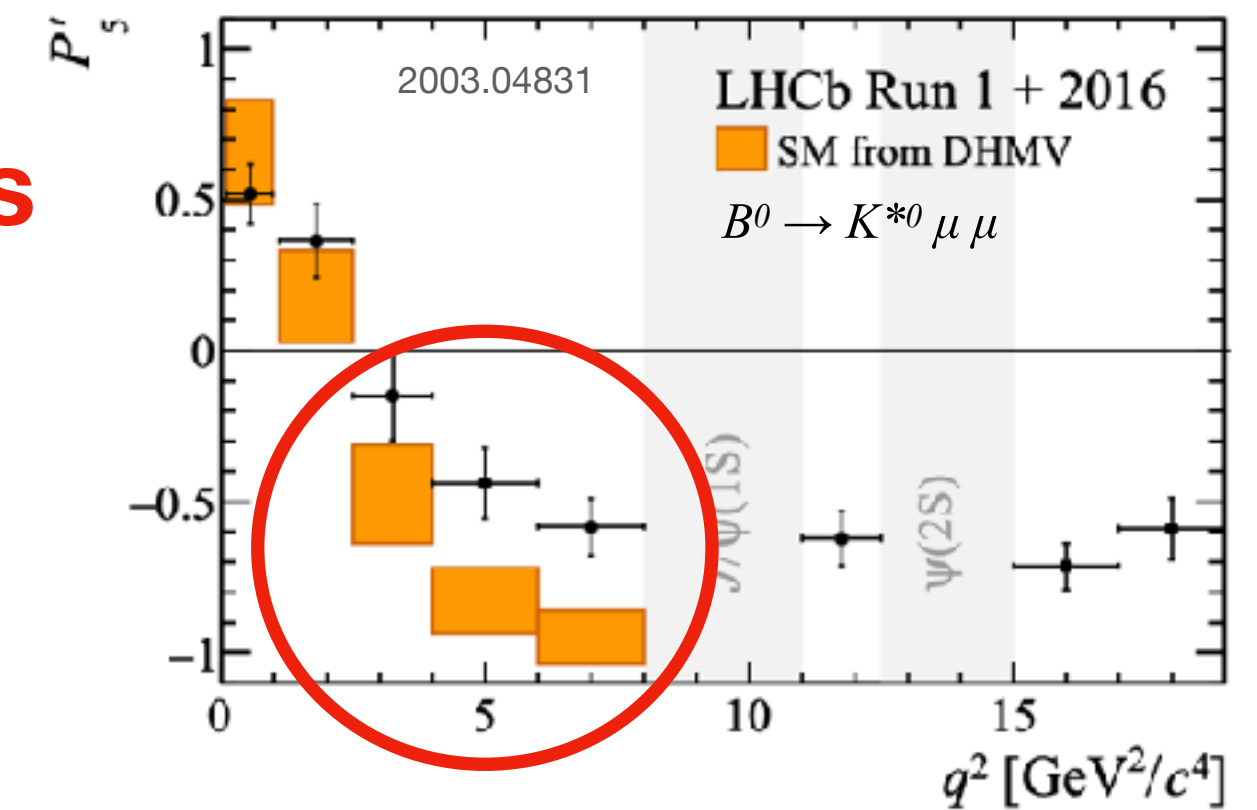
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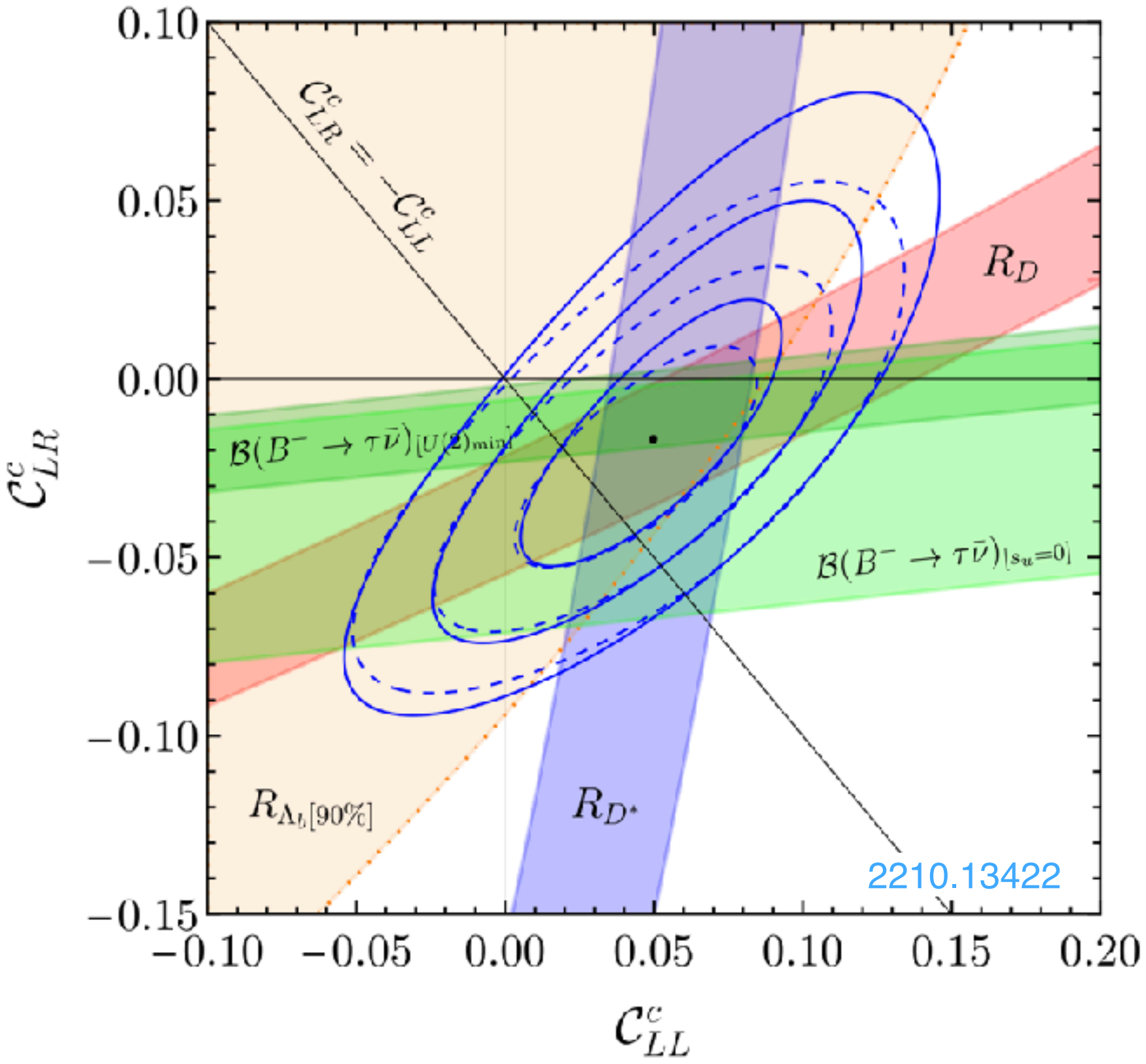


$$\mathcal{L}_{\text{LEFT}} = C_{S,bc\mu\mu} (\bar{s}_L \gamma_\mu b_L) (\bar{\mu}_L \gamma^\mu \mu_L)$$

$$C_{S,bc\mu\mu} \approx (37 \text{ TeV})^{-2}$$

Coherent EFT interpretation

$b \rightarrow c \tau \bar{\nu}_\tau$



$$[O_{lq}^{(1)}]_{\alpha\beta ij} = (\bar{l}_L^\alpha \gamma_\mu l_L^\beta) (\bar{q}_L^i \gamma^\mu q_L^j),$$

$$[O_{lq}^{(3)}]_{\alpha\beta ij} = (\bar{l}_L^\alpha \sigma^I \gamma_\mu l_L^\beta) (\bar{q}_L^i \sigma^I \gamma^\mu q_L^j)$$

$$3_q \rightarrow 2_q 3_l 3_l$$

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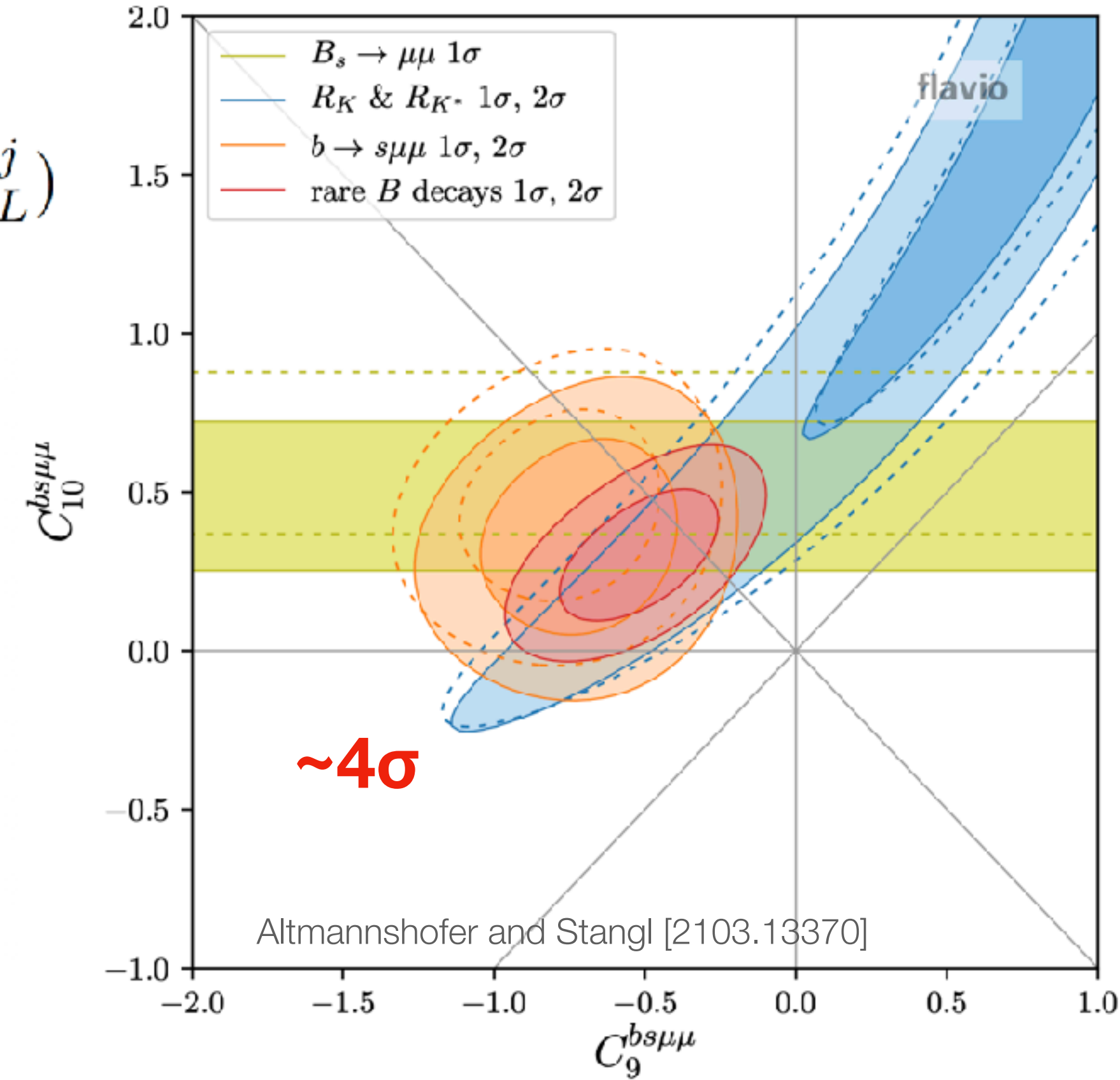
$$\sim \frac{1}{(4 \text{ TeV})^2}$$

$$\sim \frac{1}{(40 \text{ TeV})^2}$$

$$\sim c_q \frac{V_{cb} (\Lambda_q)^2}{\Lambda^2}$$

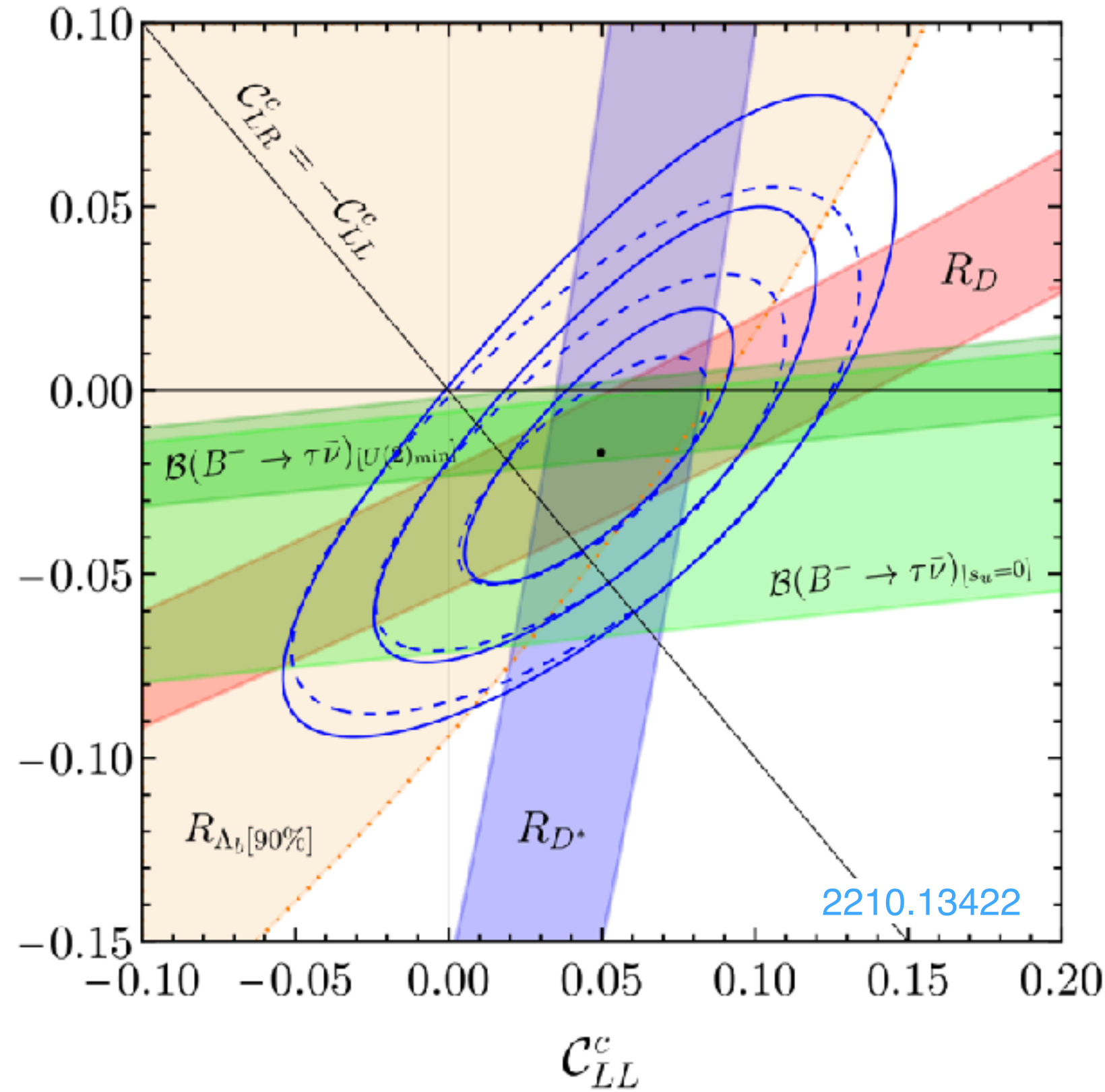
$$\sim c_\mu \frac{V_{ts} (\Lambda_\mu)^2}{\Lambda^2}$$

$b \rightarrow s \mu^+ \mu^-$

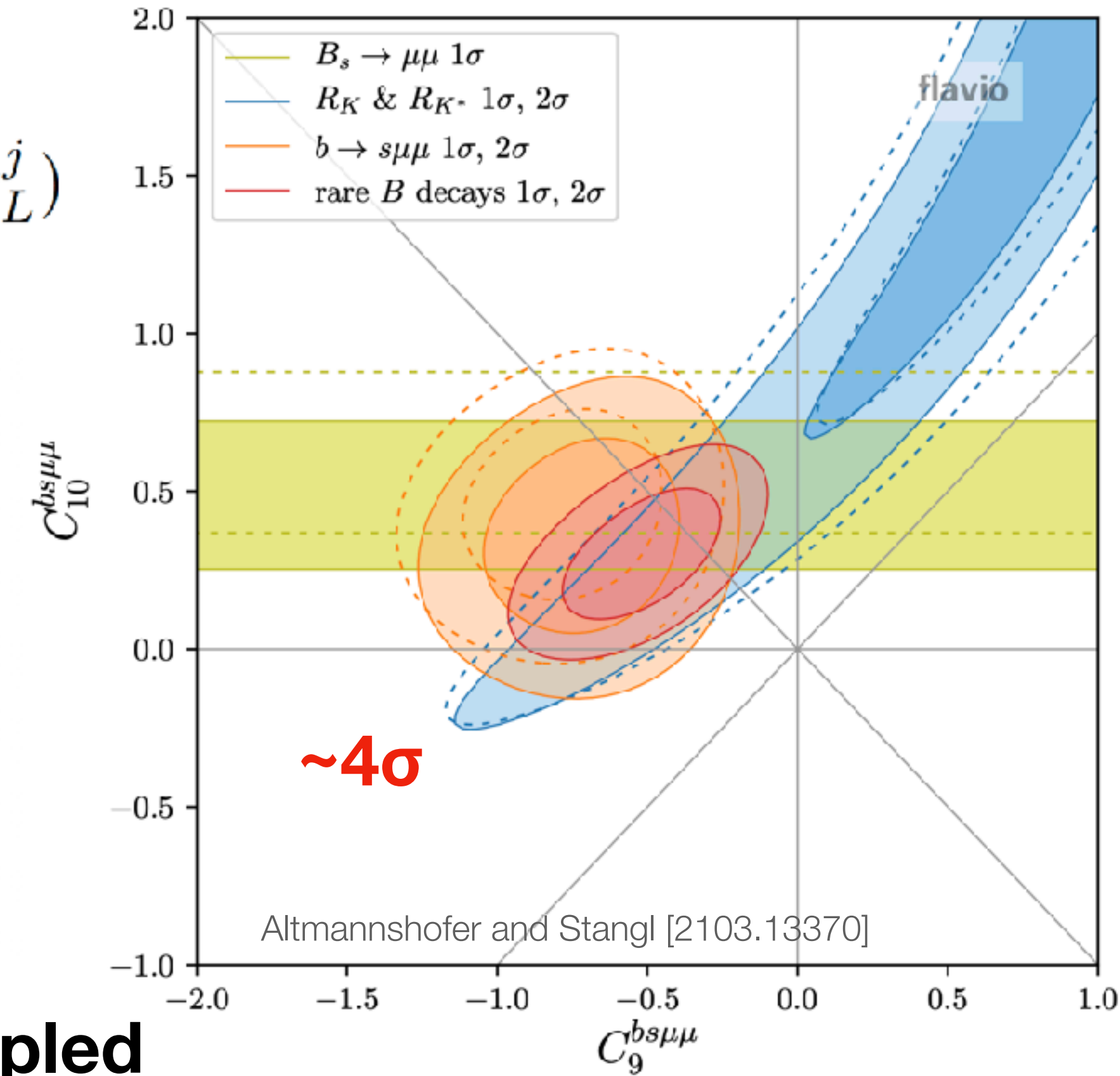


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$$3_q \rightarrow 2_q 3_l 3_l \qquad 3_q \rightarrow 2_q 2_l 2_l$$

$$\sim \frac{1}{(4 \text{ TeV})^2} \gg \sim \frac{1}{(40 \text{ TeV})^2}$$

$$\sim c_q \frac{V_{cb} (\lambda_\tau)^2}{\Lambda^2} \qquad \sim c_\mu \frac{V_{ts} (\lambda_\mu)^2}{\Lambda^2}$$

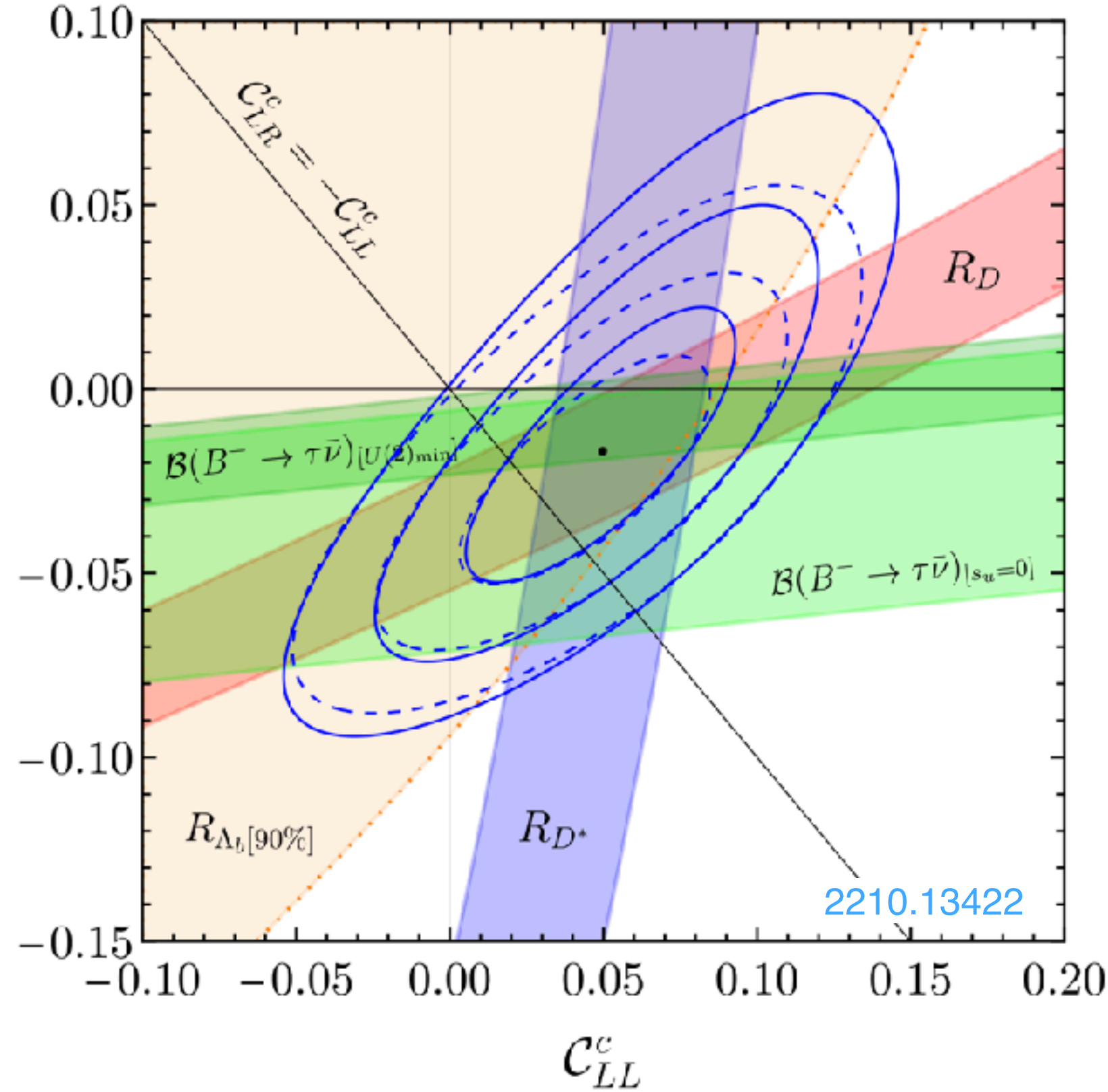
$$\Rightarrow \begin{cases} \lambda_\tau = 1, \lambda_\mu \sim 0.1 \Leftrightarrow \frac{\lambda_\mu}{\lambda_\tau} \sim \frac{m_\mu}{m_\tau} \\ \Lambda \sim 1 \text{ TeV} \\ c_{\mu,\tau} \gtrsim \mathcal{O}(1) \end{cases}$$

New Physics mainly coupled to the 3rd generation.

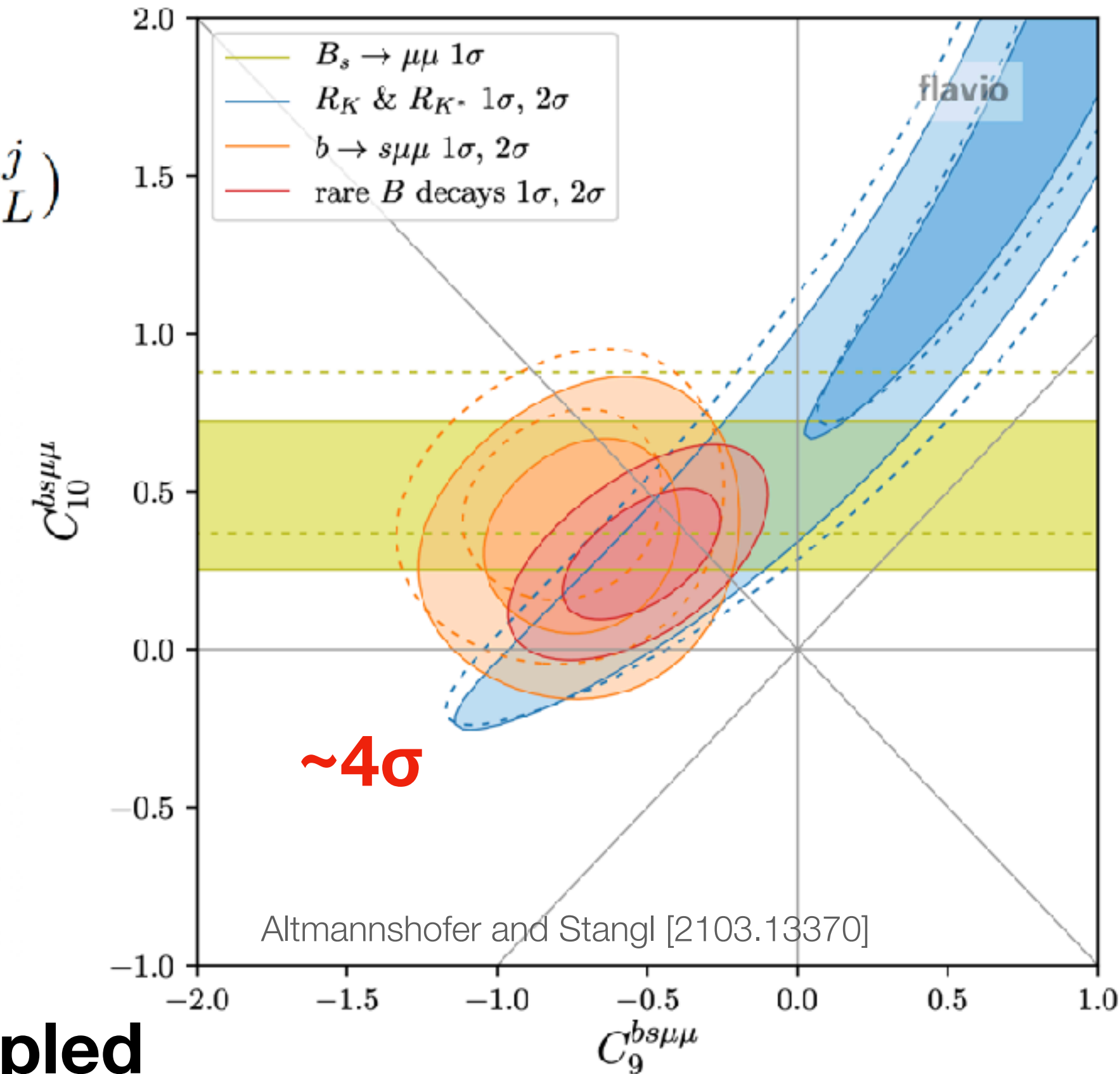
R(D^(*)) anomalies drive most new physics requirements

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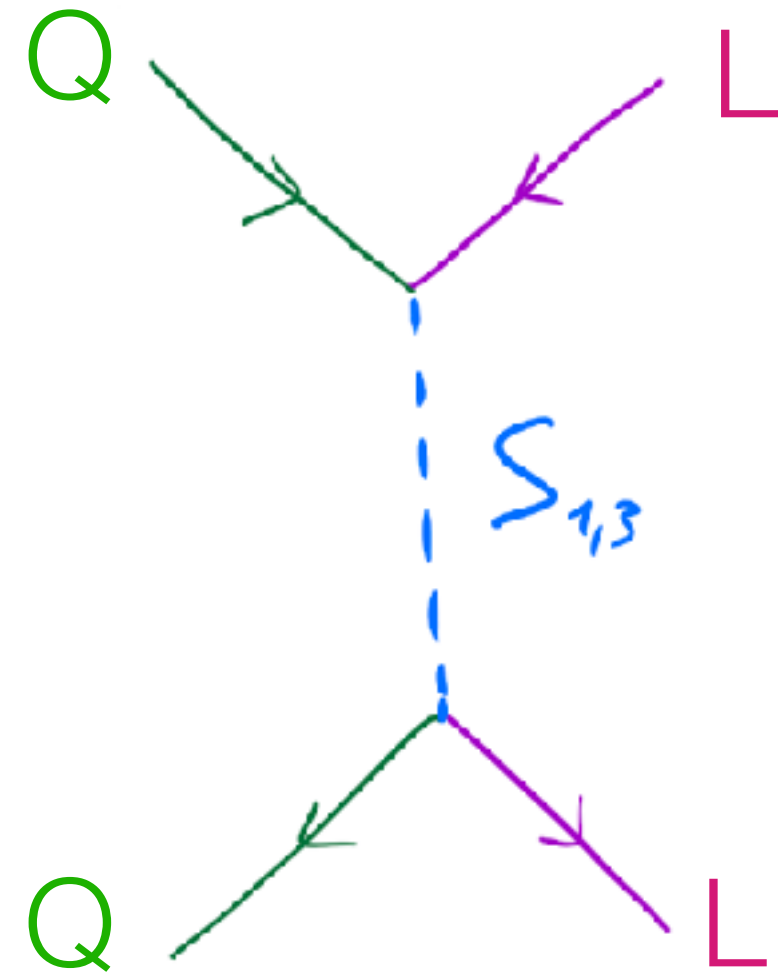
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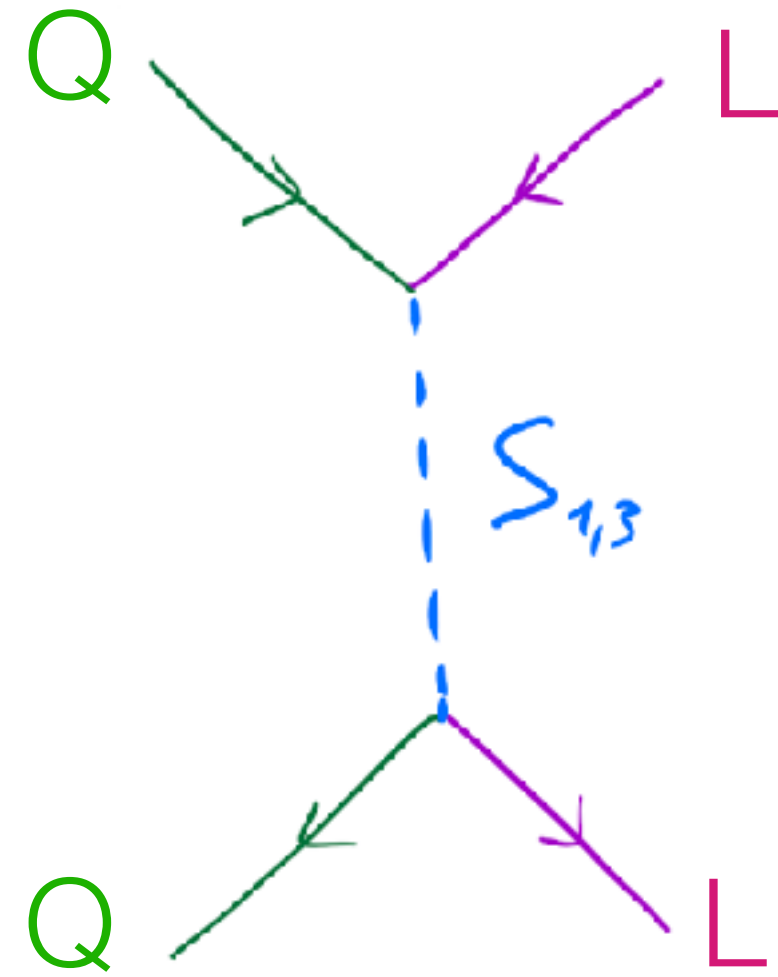
No sizeable effect in Higgs physics from these operators.

Leptoquarks and B-anomalies



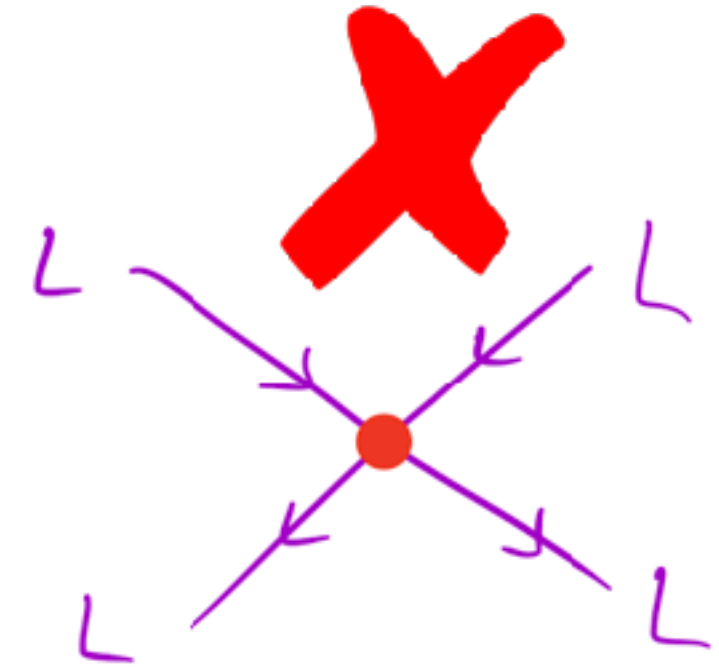
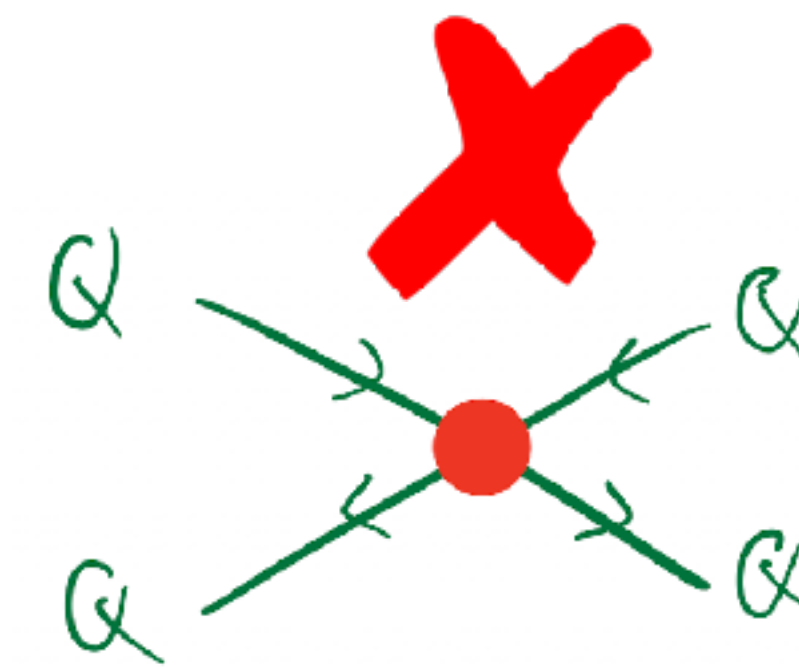
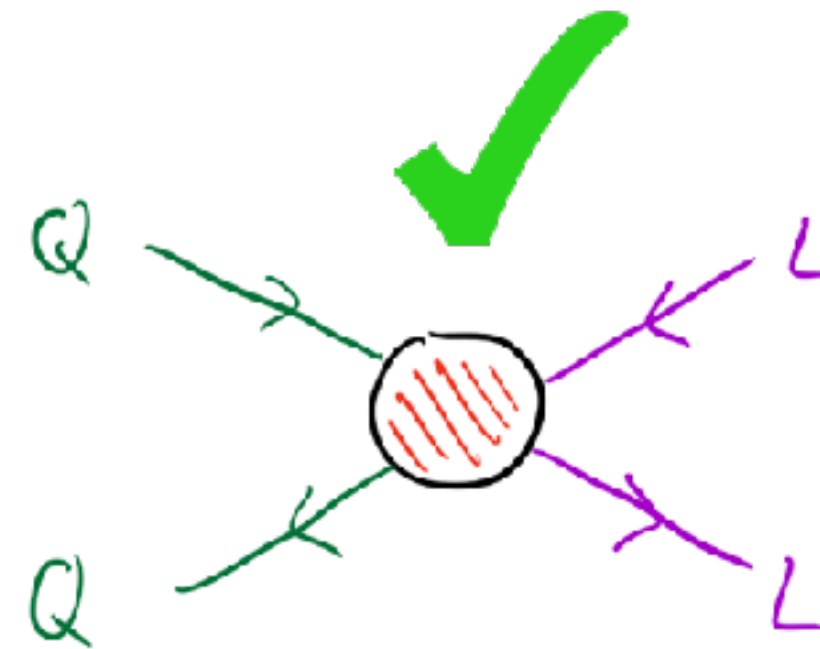
LQ induce semileptonic @ tree level,
4-quark & 4-lepton only at loop level.

Leptoquarks and B-anomalies

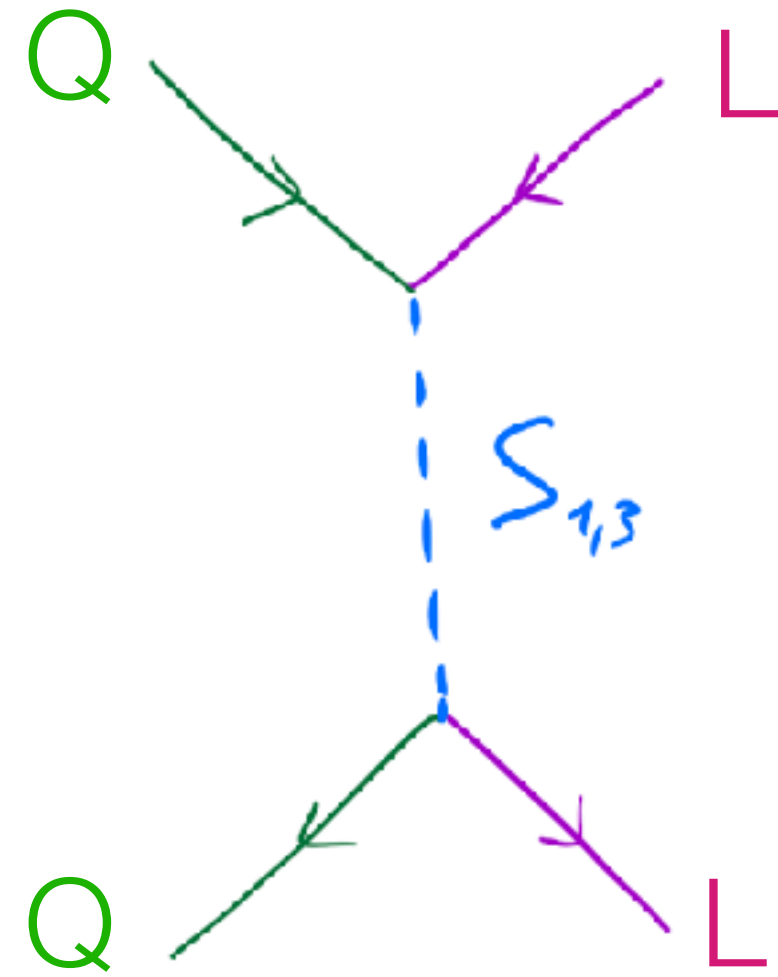


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Deviations in **semileptonic** processes,
strong bounds from $\Delta F=2$ & **CLFV** processes.

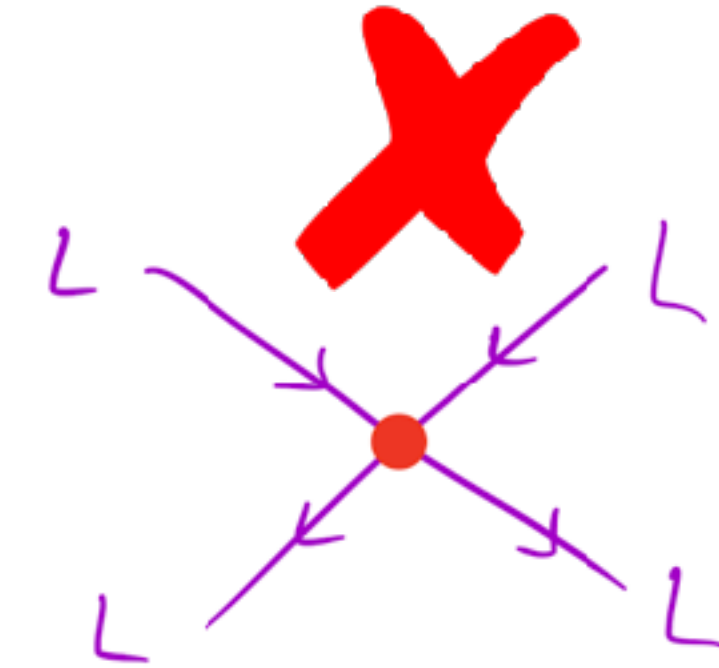
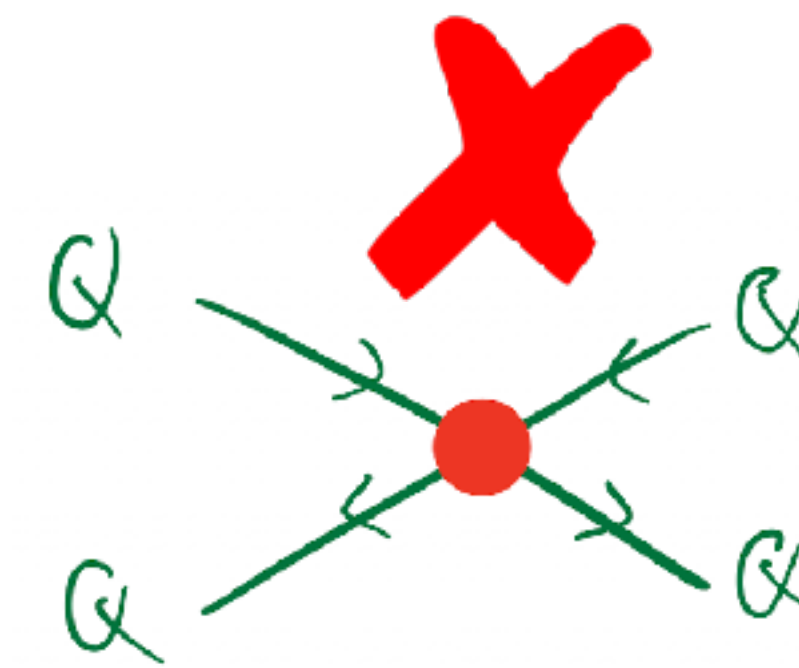
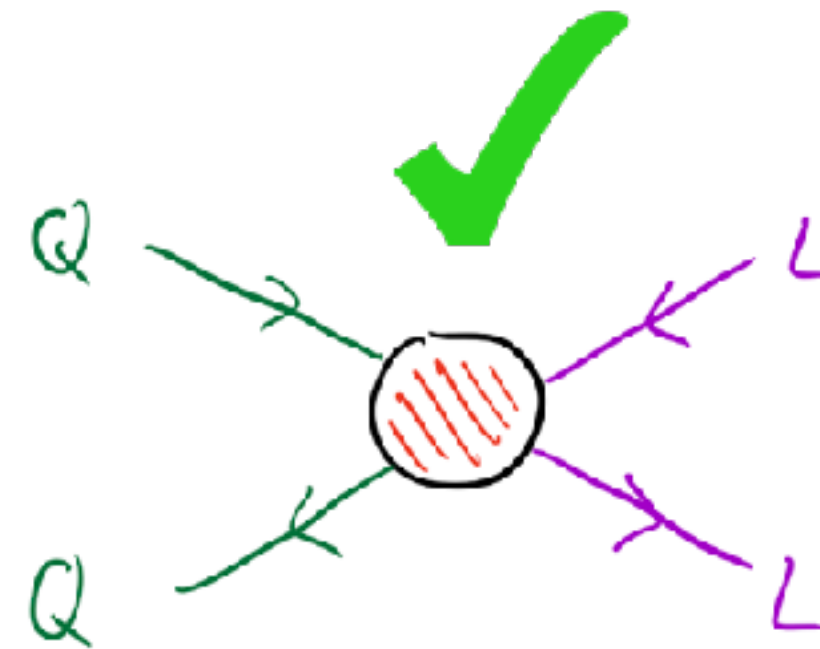


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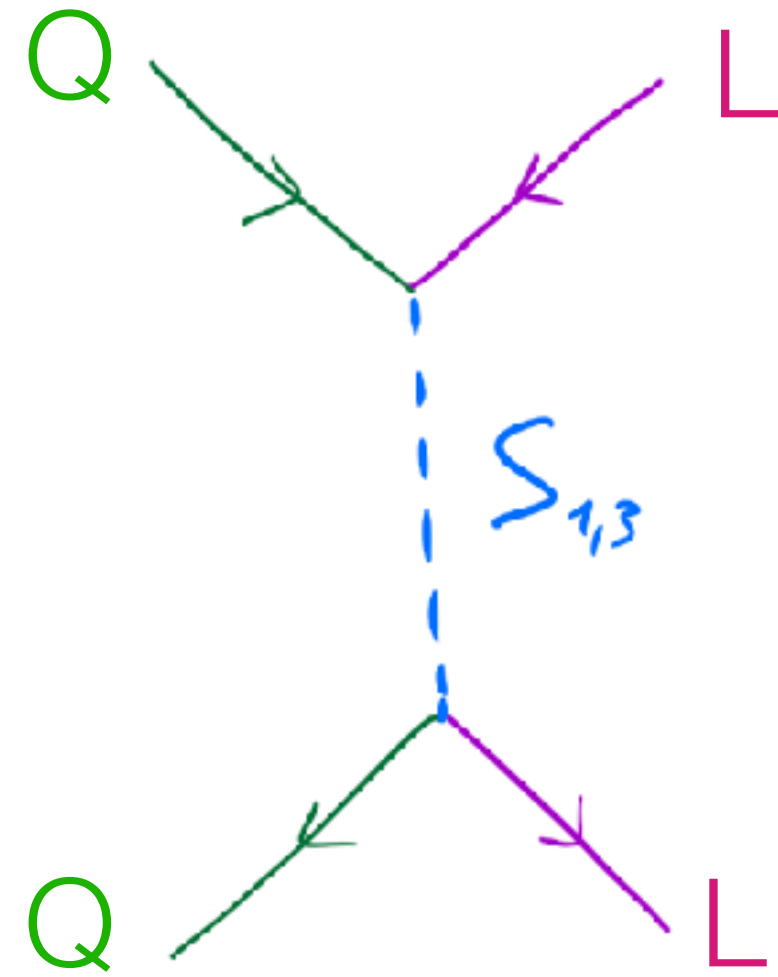
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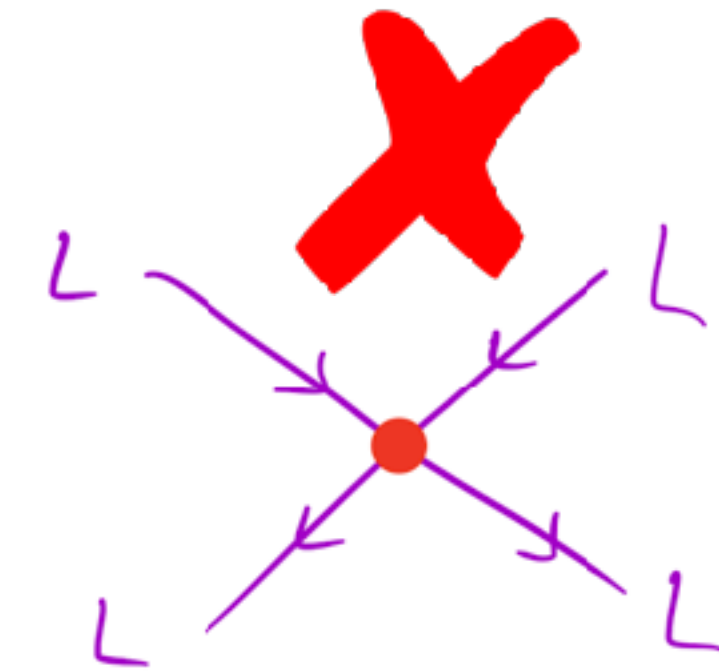
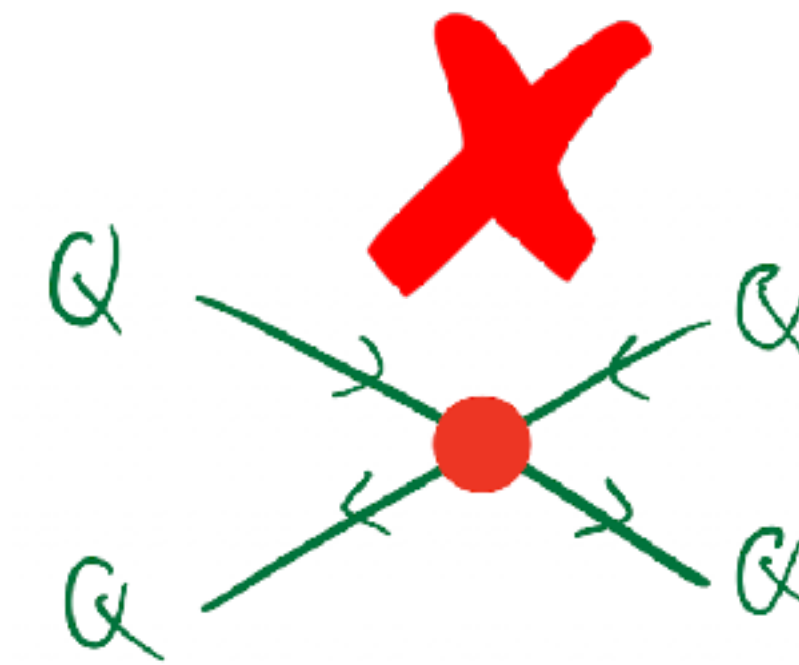
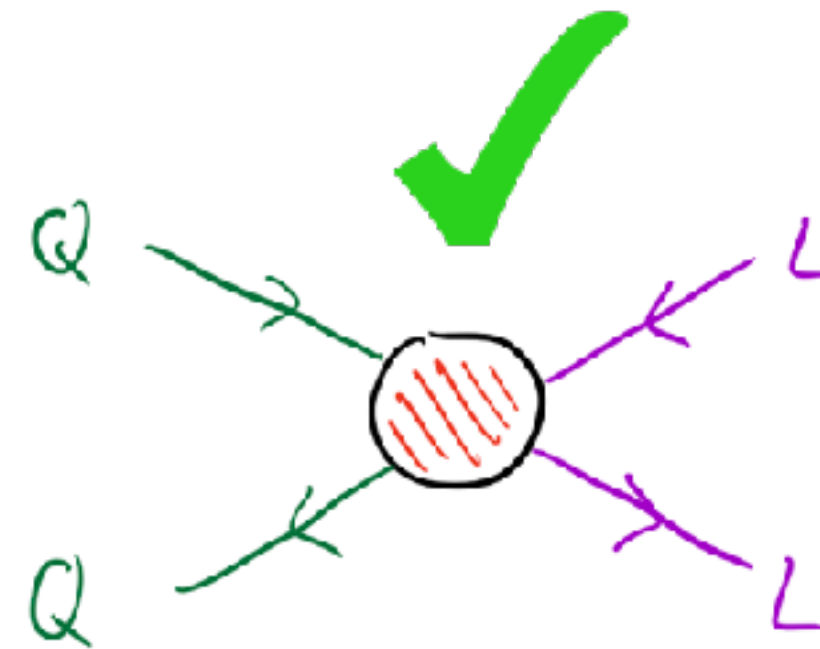
>> Very strong bounds on LQ couplings to 1st generation fermions, e.g. $K_L \rightarrow \mu e$, etc..

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To address both B-anomalies:

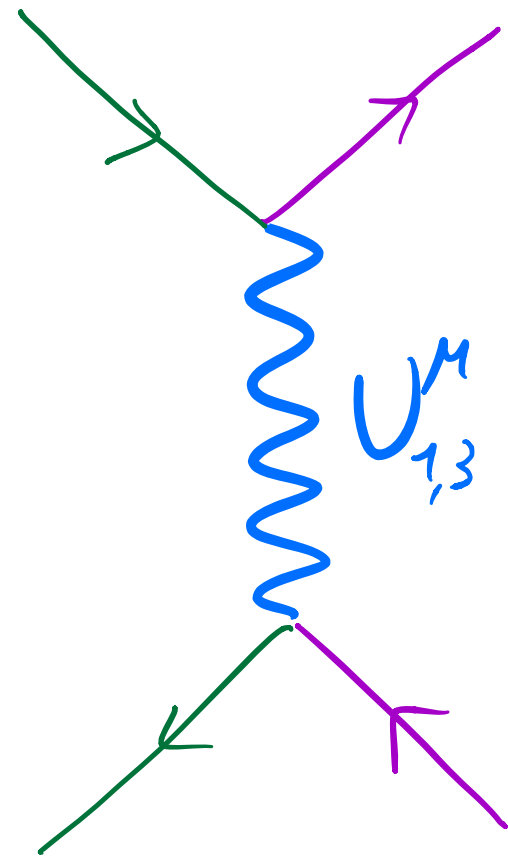
TeV-scale leptoquark coupled to **3rd** and **2nd** generation
 $g(\mathbf{3rd}) > g(\mathbf{2nd}) > g(\mathbf{1st})$

$$\lambda \sim \begin{pmatrix} e & \mu & \tau \\ \cdot & \odot & \odot \\ \odot & \odot & \odot \\ \odot & \odot & \odot \end{pmatrix} \begin{matrix} d, u \\ s, c \\ b, t \end{matrix}$$

Leptoquarks and B-anomalies

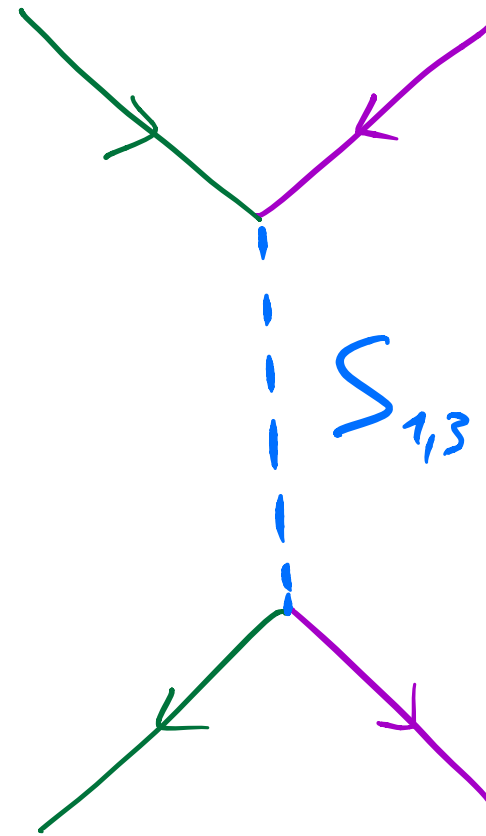
Vector Leptoquark

$$U_1 = (\mathbf{3}, \mathbf{1}, 2/3),$$



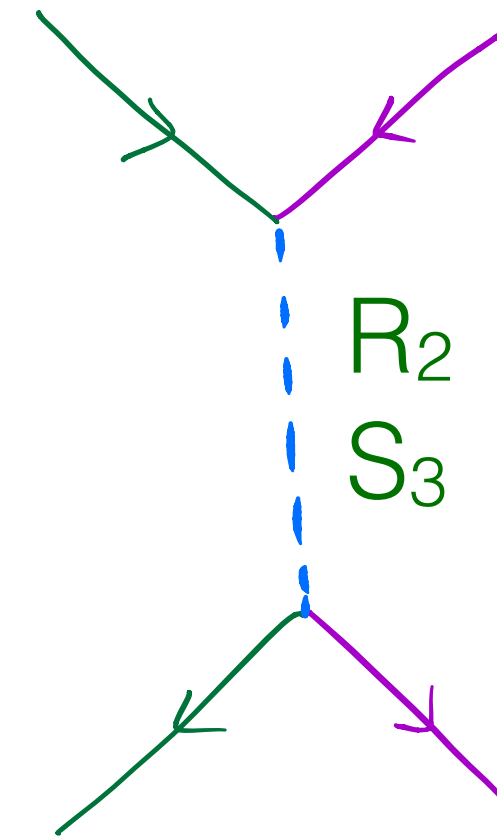
Scalar Leptoquarks

$$S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3),$$
$$S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3),$$

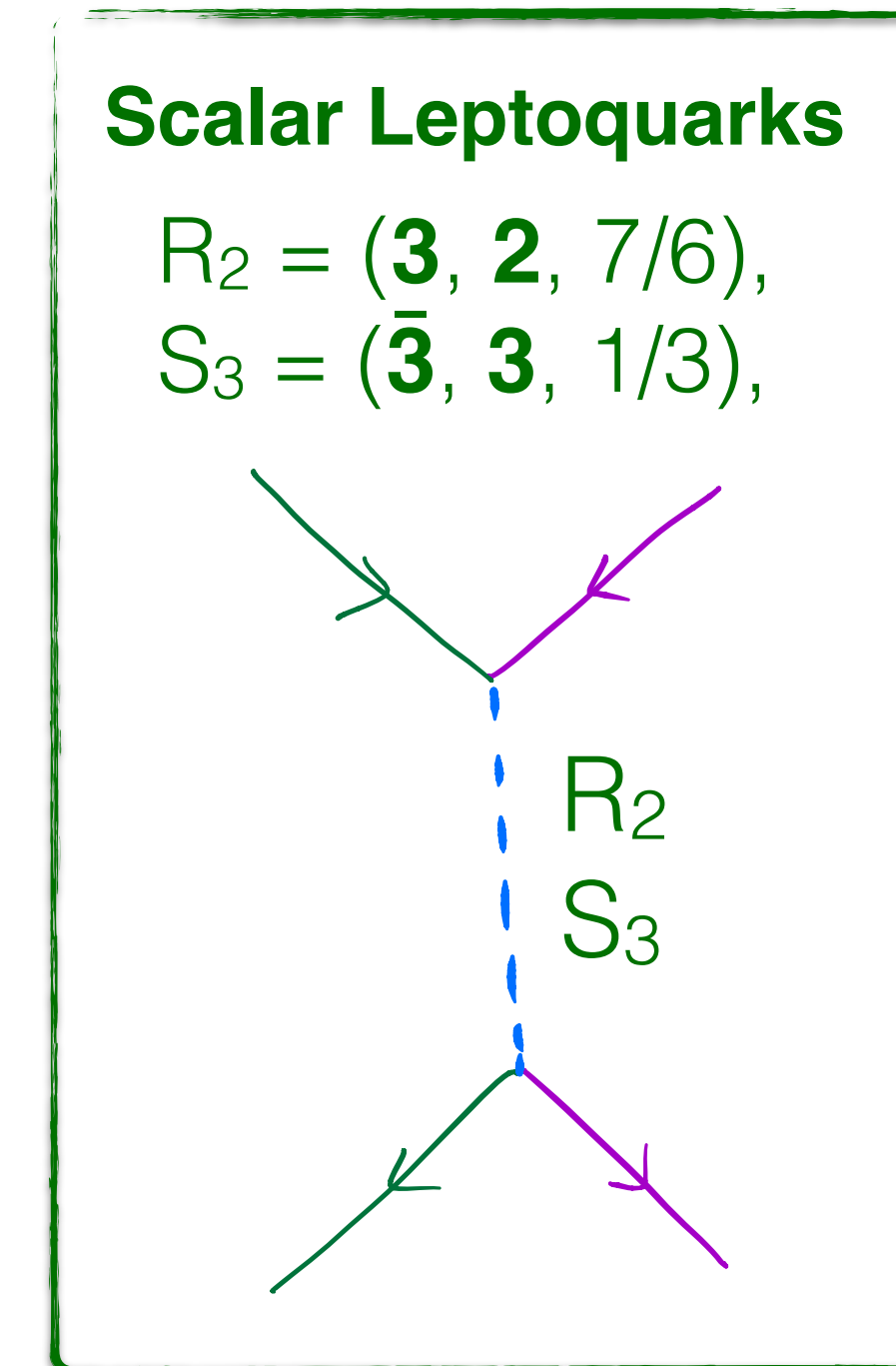
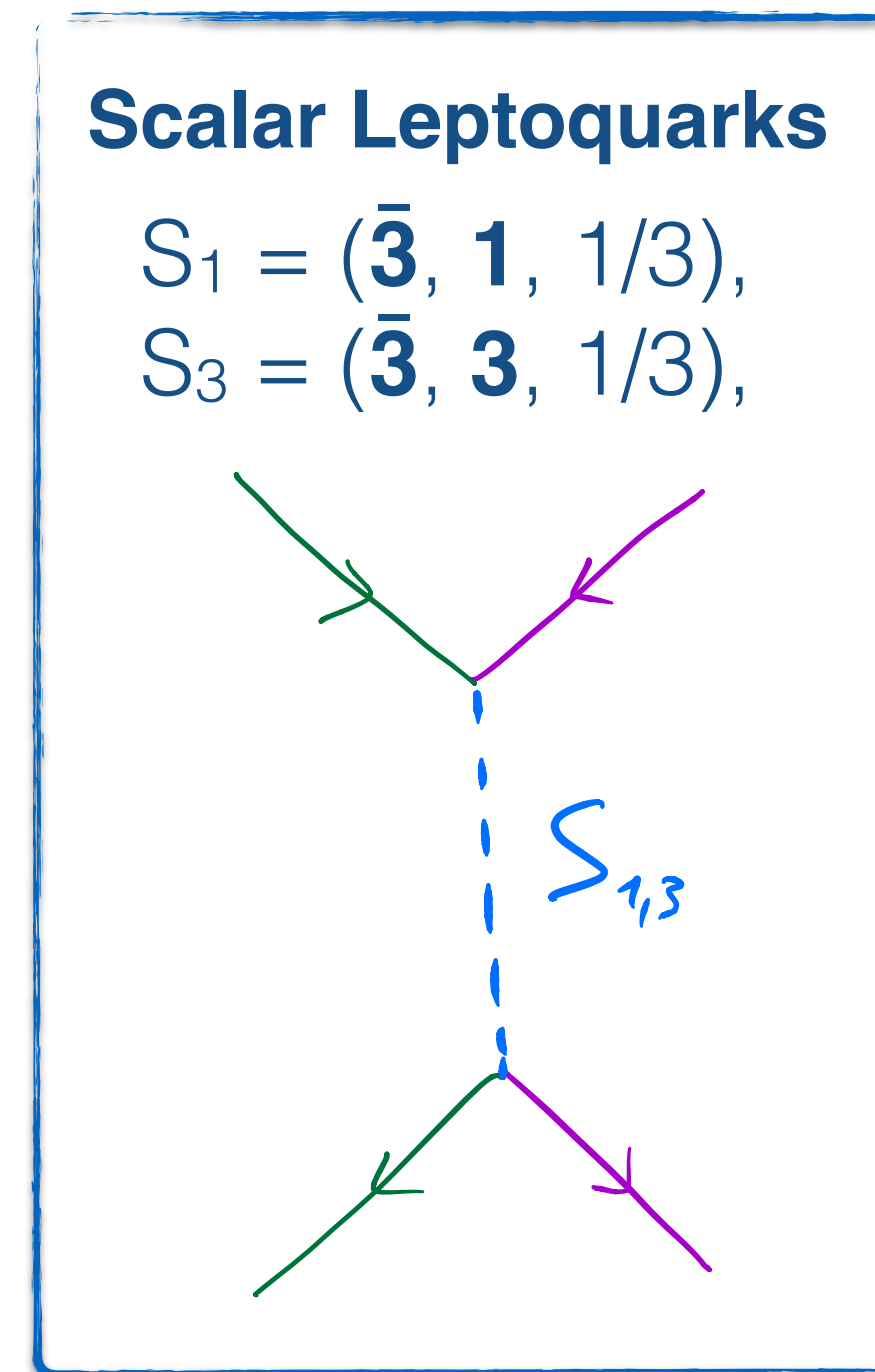
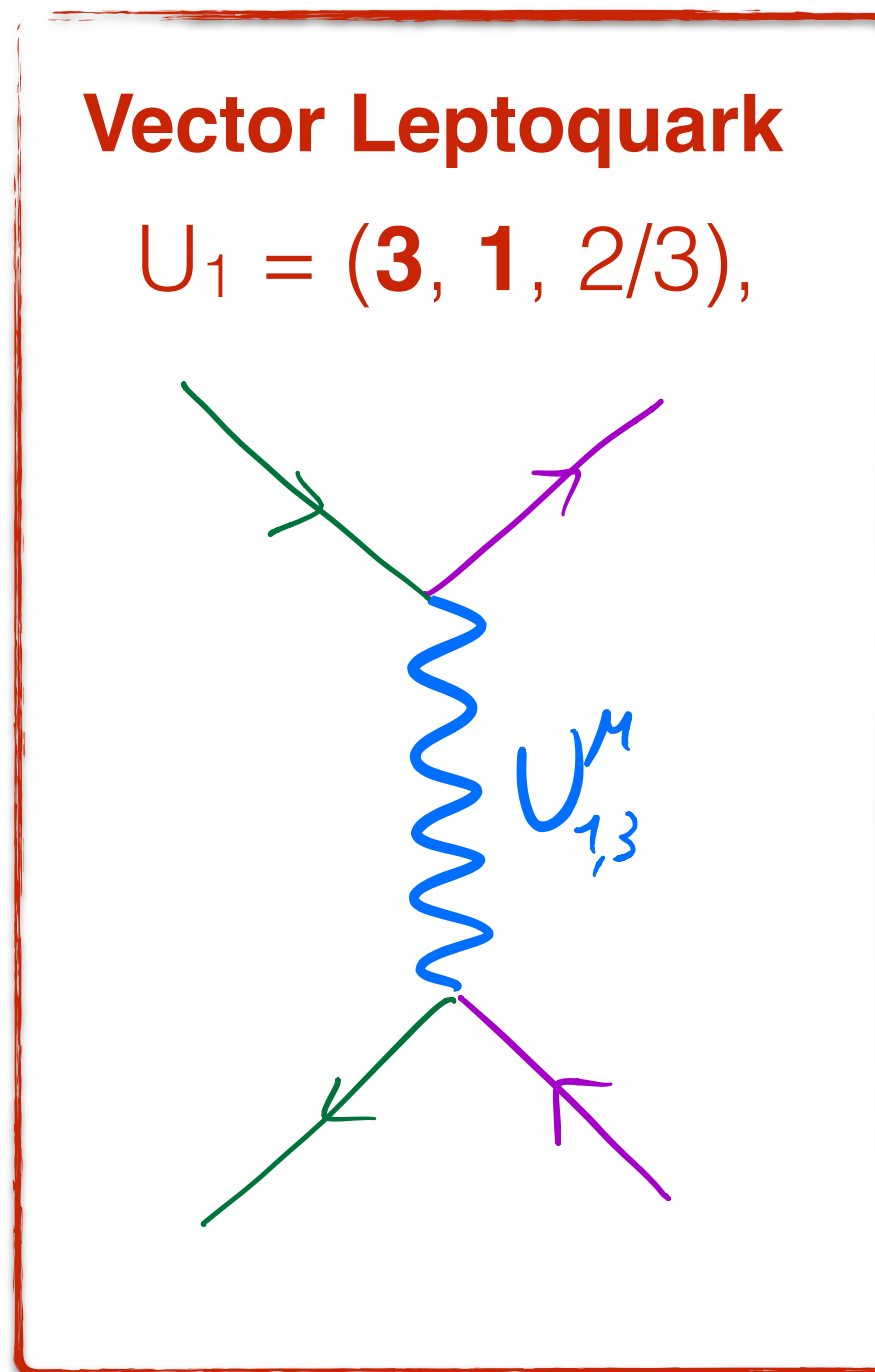


Scalar Leptoquarks

$$R_2 = (\mathbf{3}, \mathbf{2}, 7/6),$$
$$S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3),$$



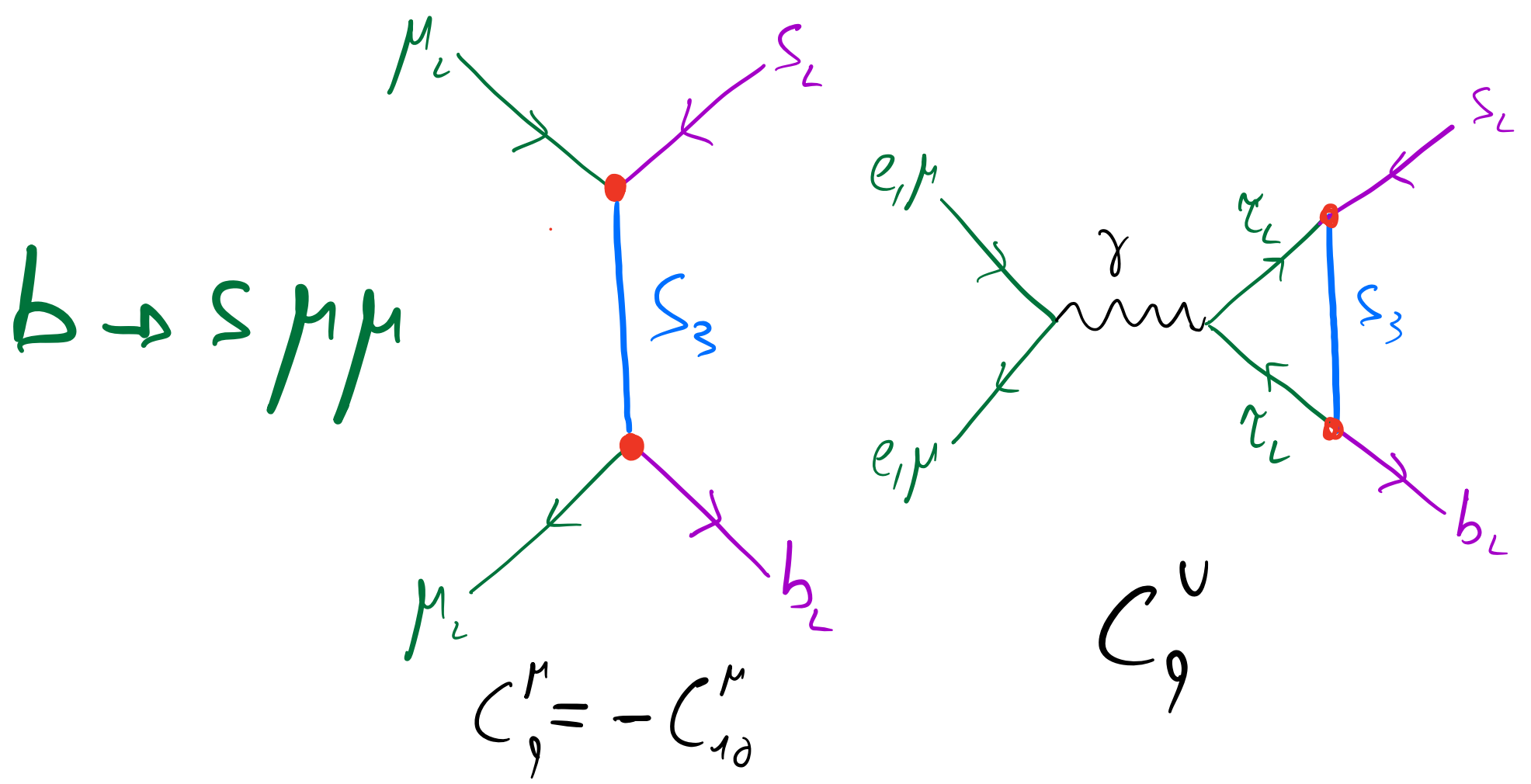
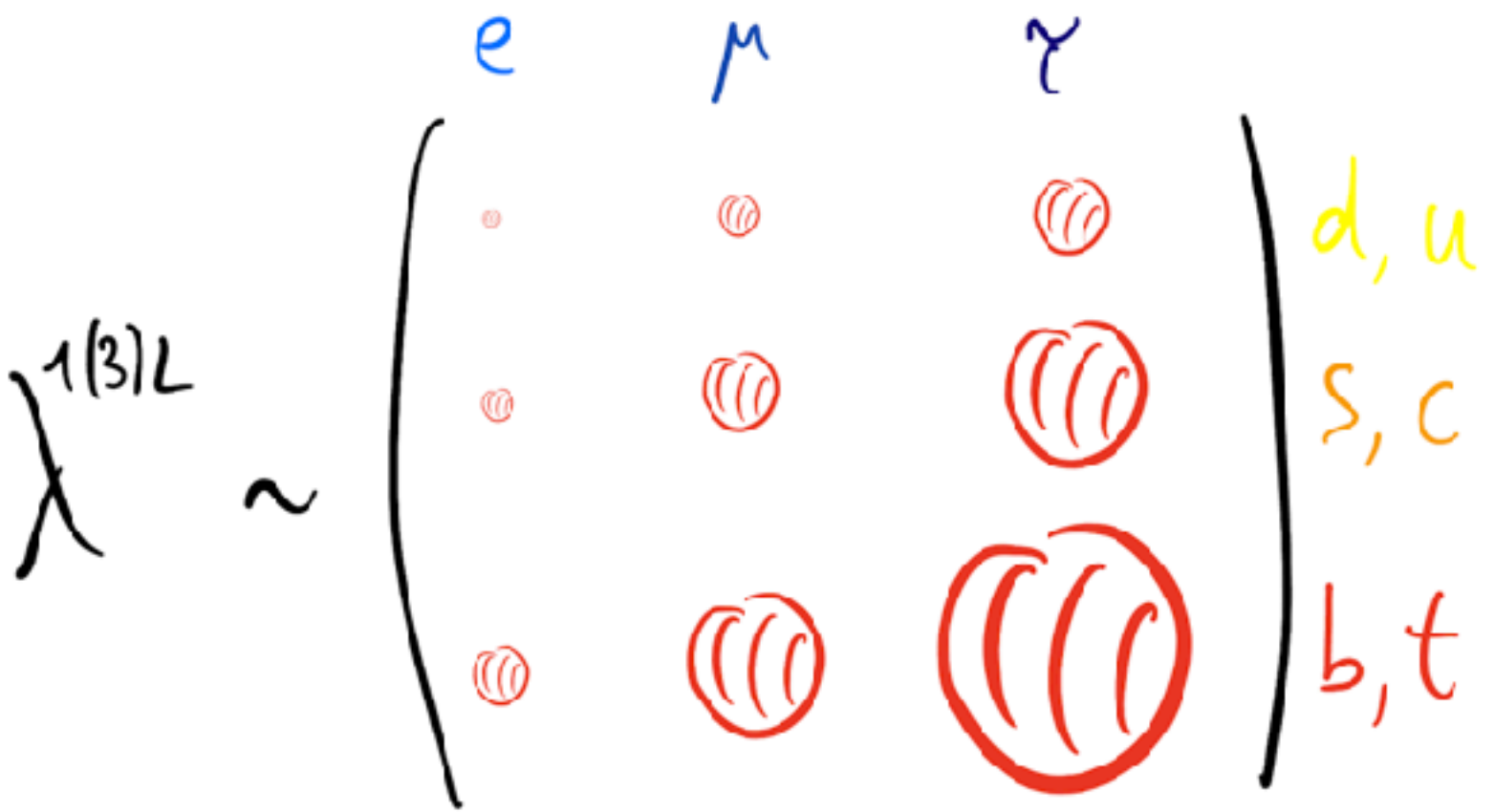
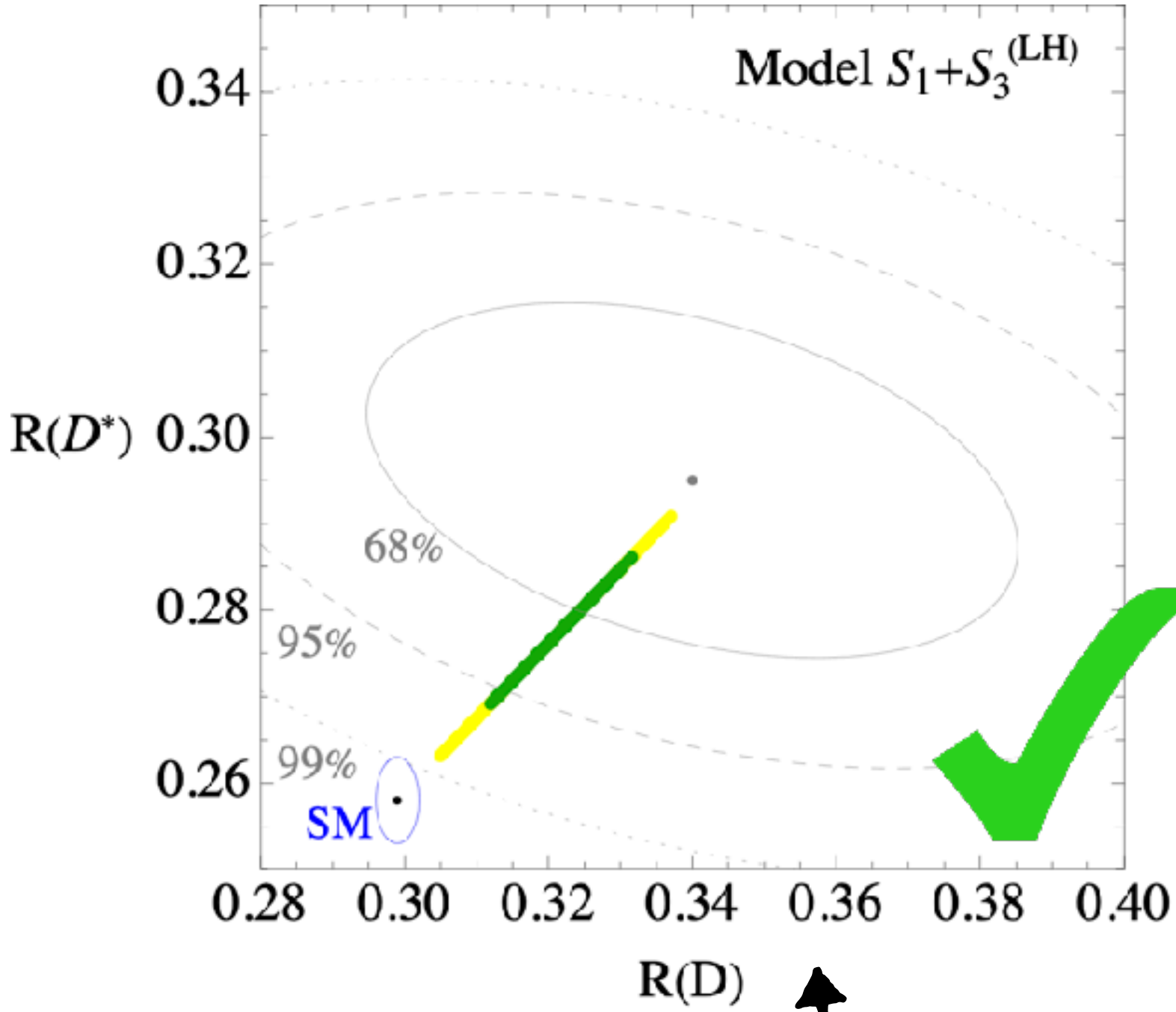
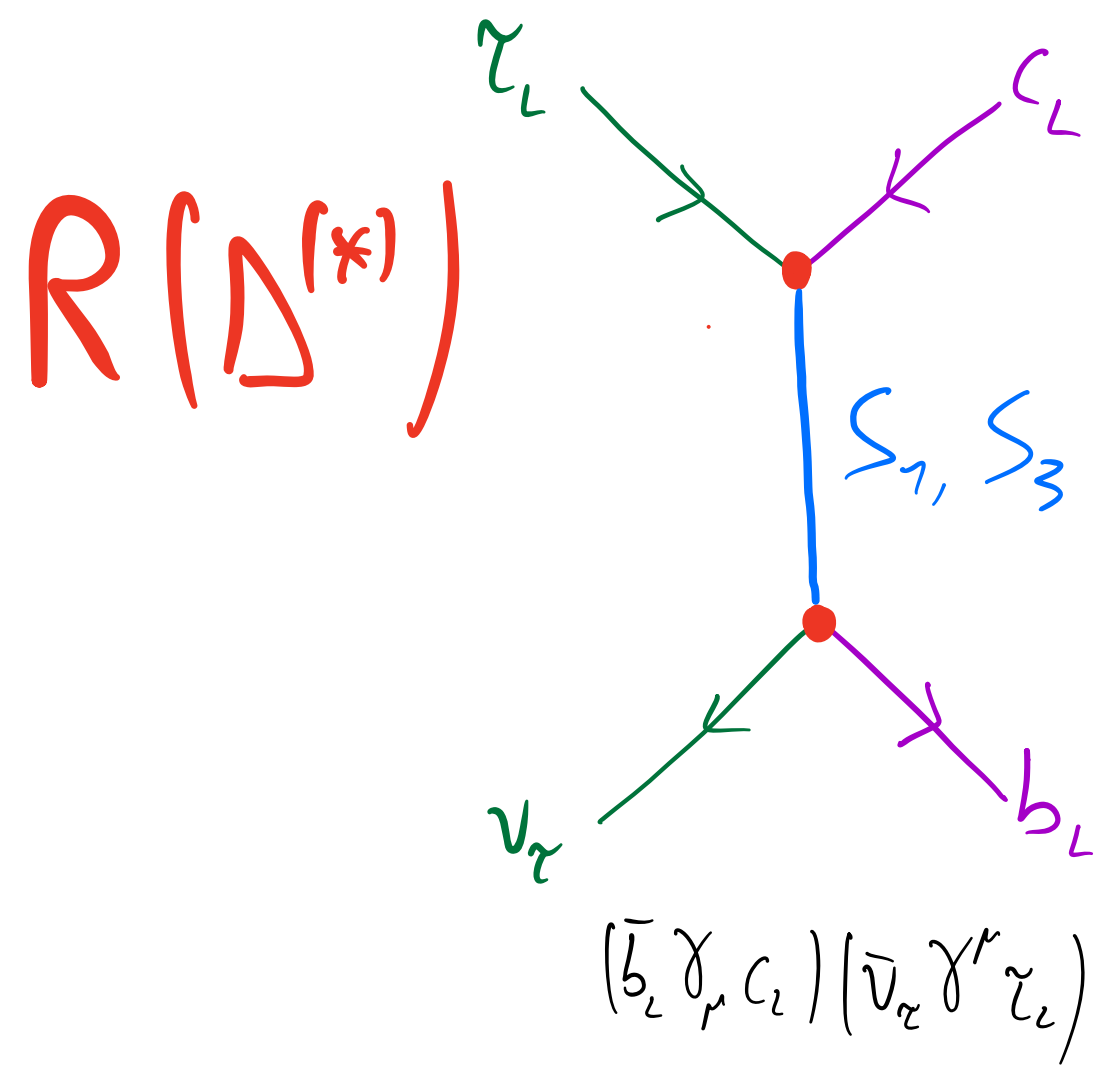
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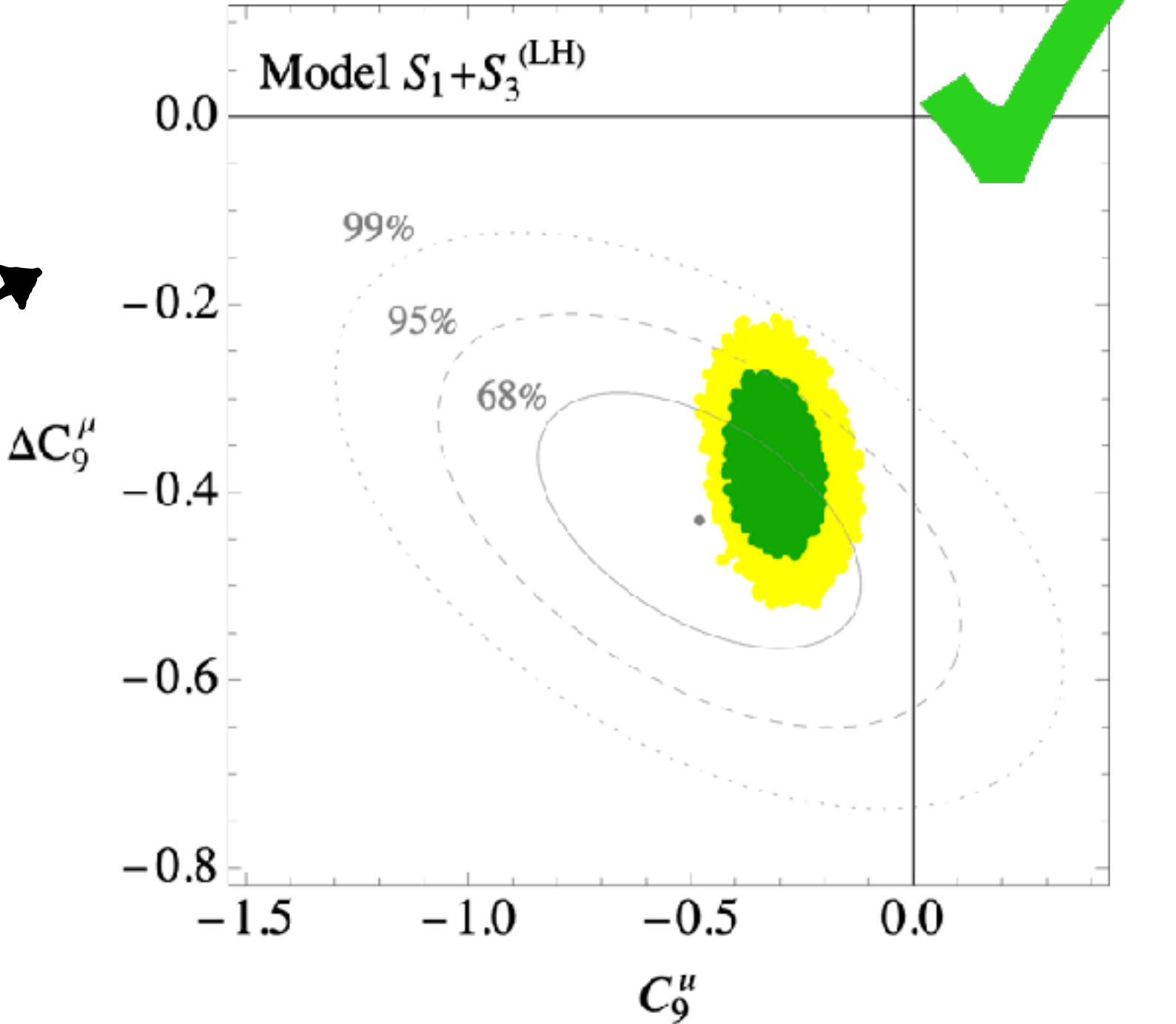
TeV-scale leptoquark coupled to **3rd** and **2nd** generation

$$g(\mathbf{3rd}) > g(\mathbf{2nd}) > g(\mathbf{1st})$$

S₁ and S₃ - contributions to anomalies



Global fit
with all relevant
flavour,
EW, and **collider**
constraints.
(details in backup)



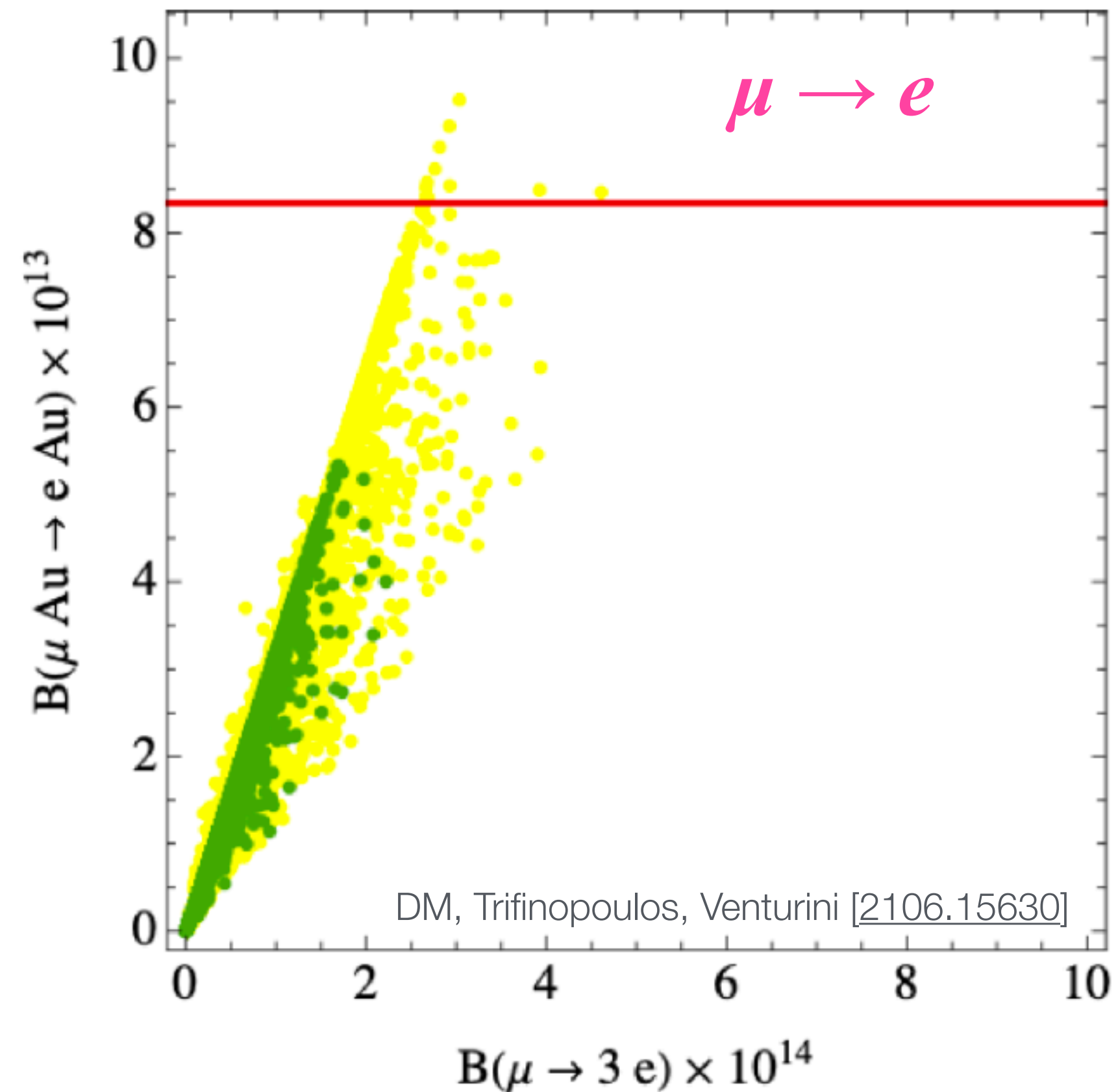
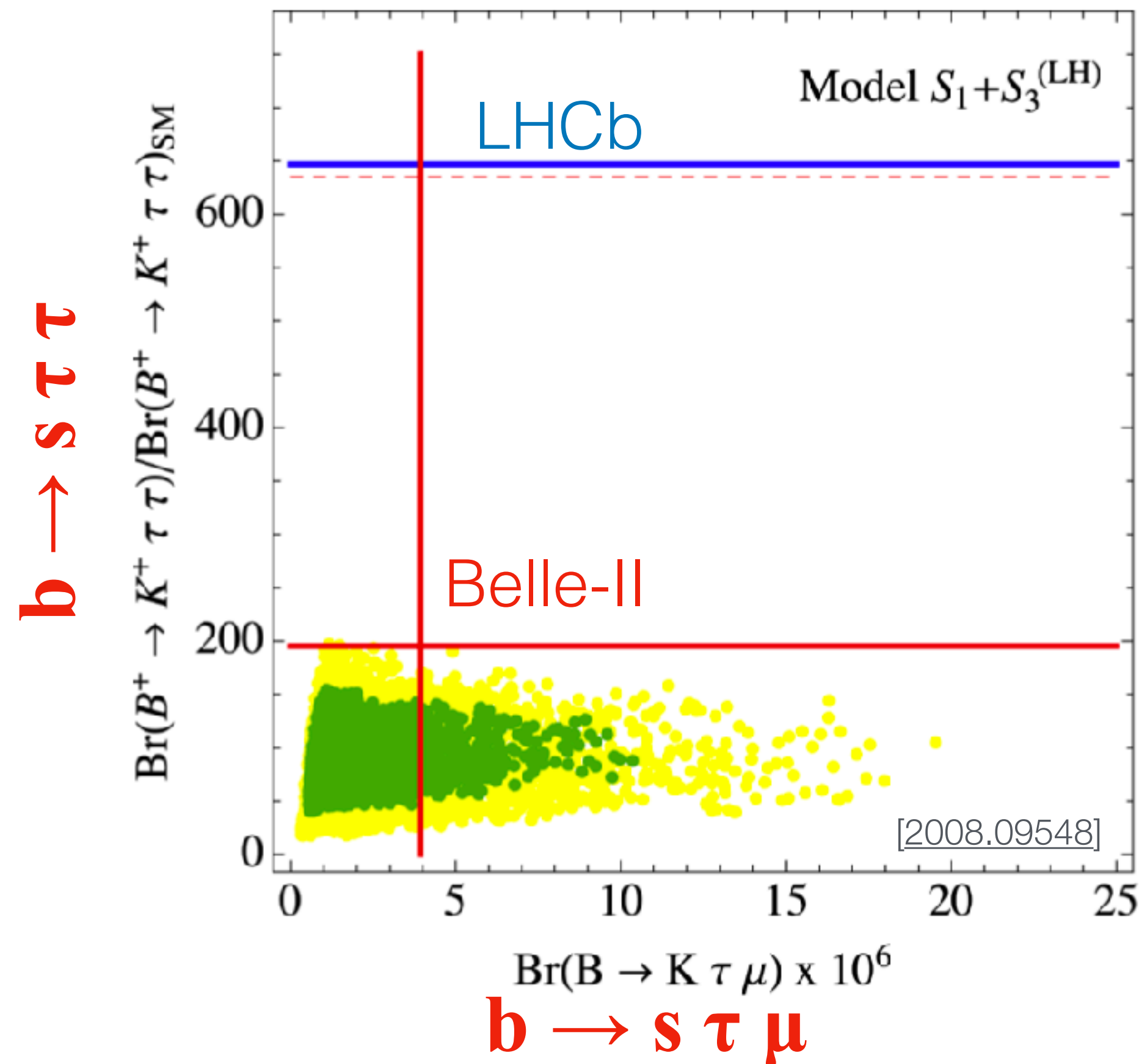
V. Gherardi, E. Venturini, D.M. [2008.09548]

Predictions

Typical for all models addressing $R(D^{(*)})$

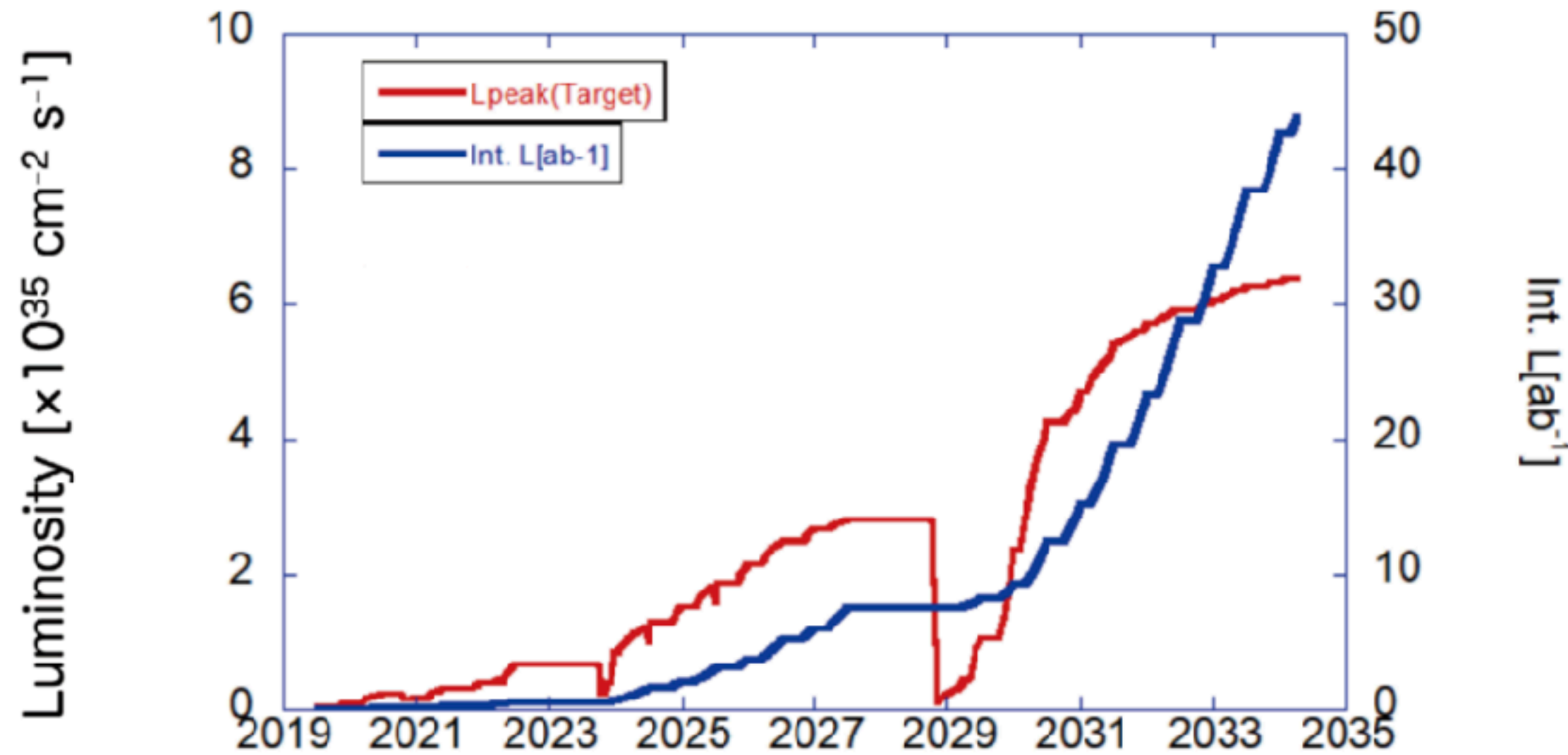
→ The large couplings to τ imply signatures in DY tails of $pp \rightarrow \tau\tau$, deviations in τ LFU tests and $\tau \rightarrow \mu$ LFV tests (Belle-II). Also B_s -mixing and $B \rightarrow K^* \nu \bar{\nu}$ are close to present bounds.

Large effects are also expected in $b \rightarrow s \tau \tau$ and $b \rightarrow s \tau \mu$ transitions, as well as in $\mu \rightarrow e$:



Near Future Prospects in Flavour

Belle-II



$\mu \rightarrow e$ LFV

today:

$\mathcal{B}(\mu \rightarrow e\gamma)$	$< 5.0 \times 10^{-13}$
$\mathcal{B}(\mu \rightarrow 3e)$	$< 1.2 \times 10^{-12}$
$\mathcal{B}_{\mu e}^{(\text{Ti})}$	$< 5.1 \times 10^{-12}$
$\mathcal{B}_{\mu e}^{(\text{Au})}$	$< 8.3 \times 10^{-13}$

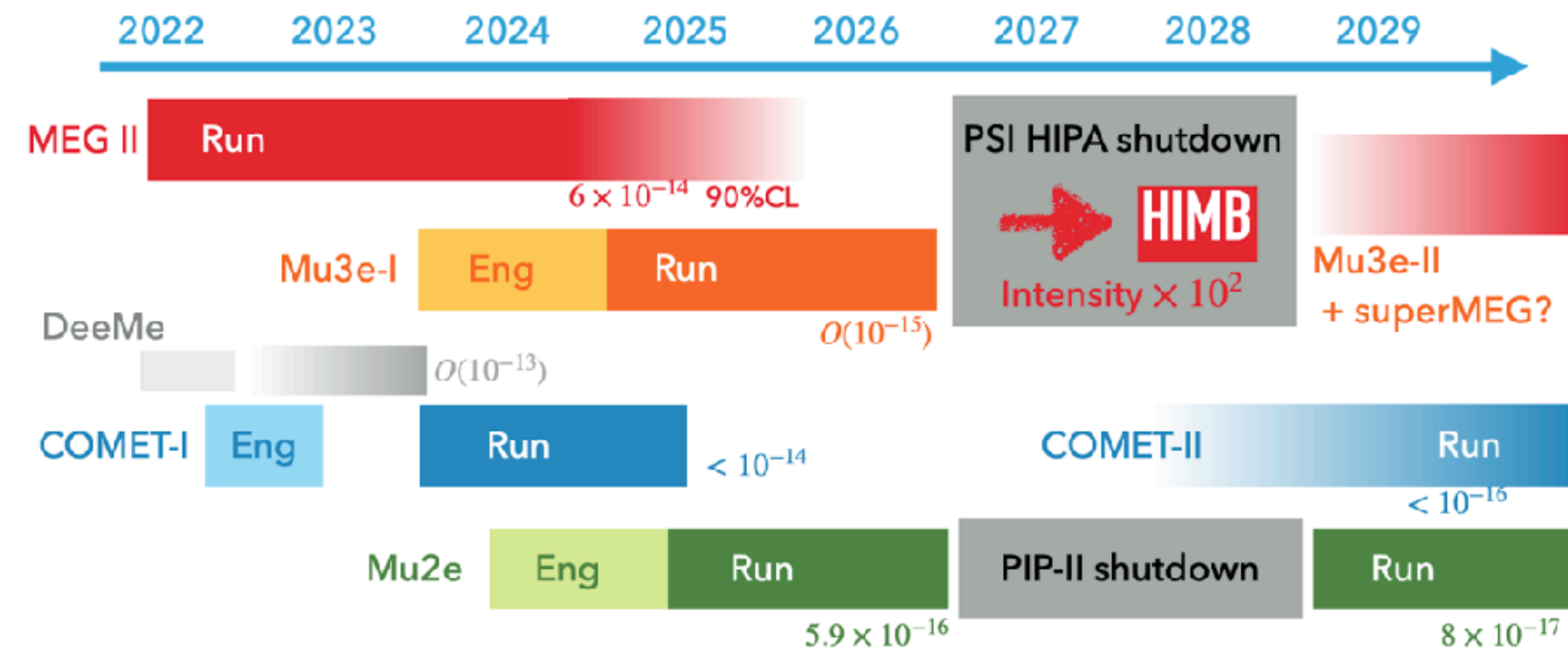
CHARGED LEPTON FLAVOUR EXPERIMENTS / T. MORI

[T. Mori ICHEP 2022]

13

TIMELINE OF MUON CLFV EXPERIMENTS

"My Rough Sketch"



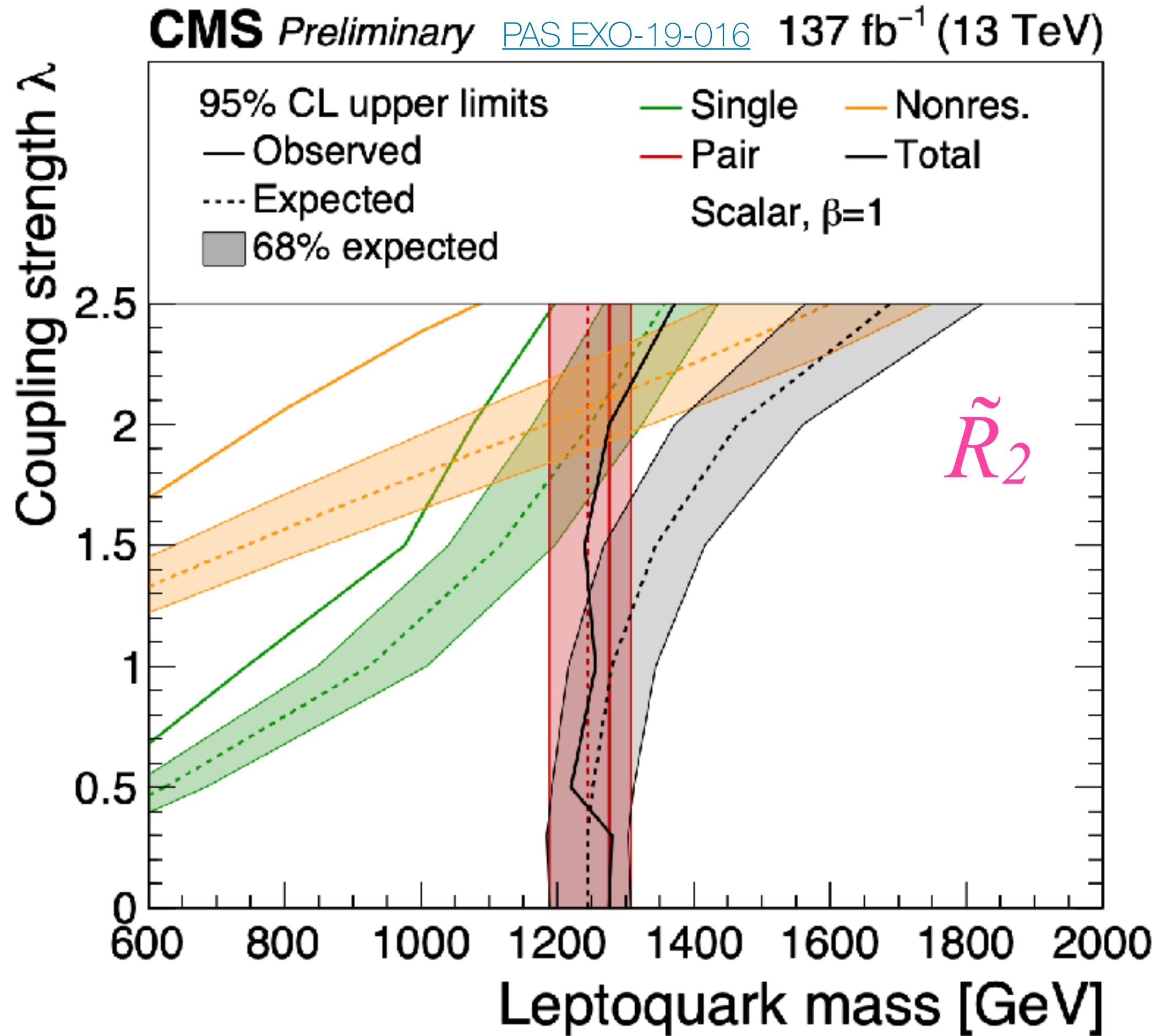
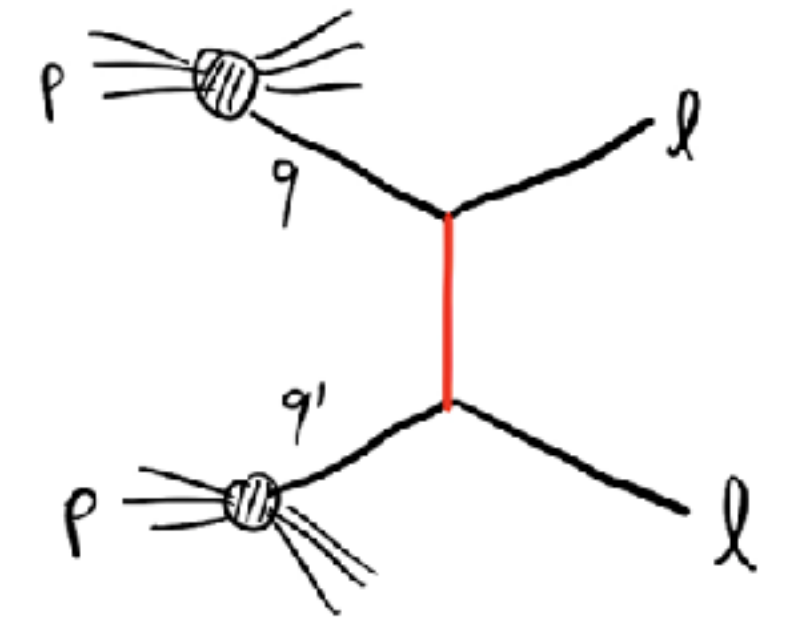
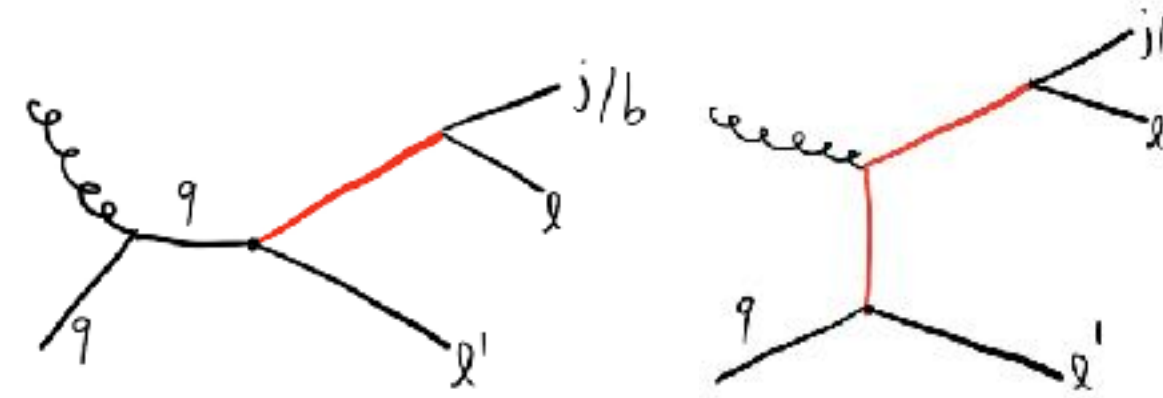
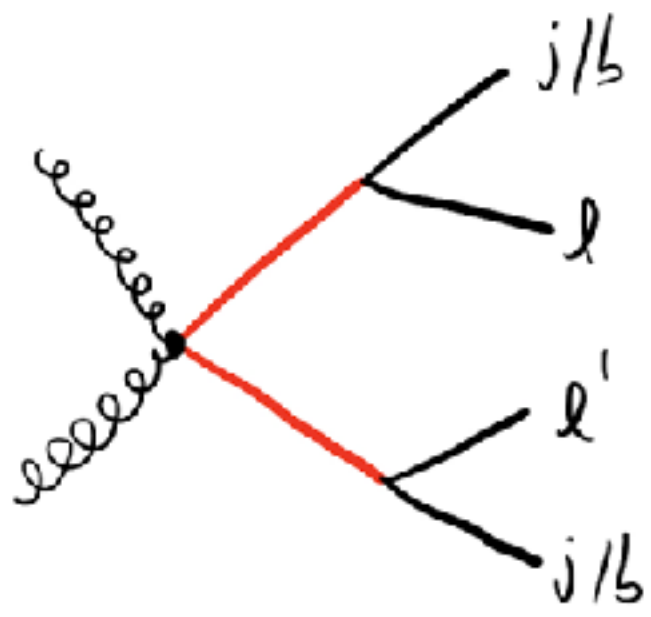
Belle-II will be able to **completely test $R(D^{(*)})$ with $5ab^{-1}$** .

Measuring $R(K^{(*)})$ with 3% precision requires $50ab^{-1}$.

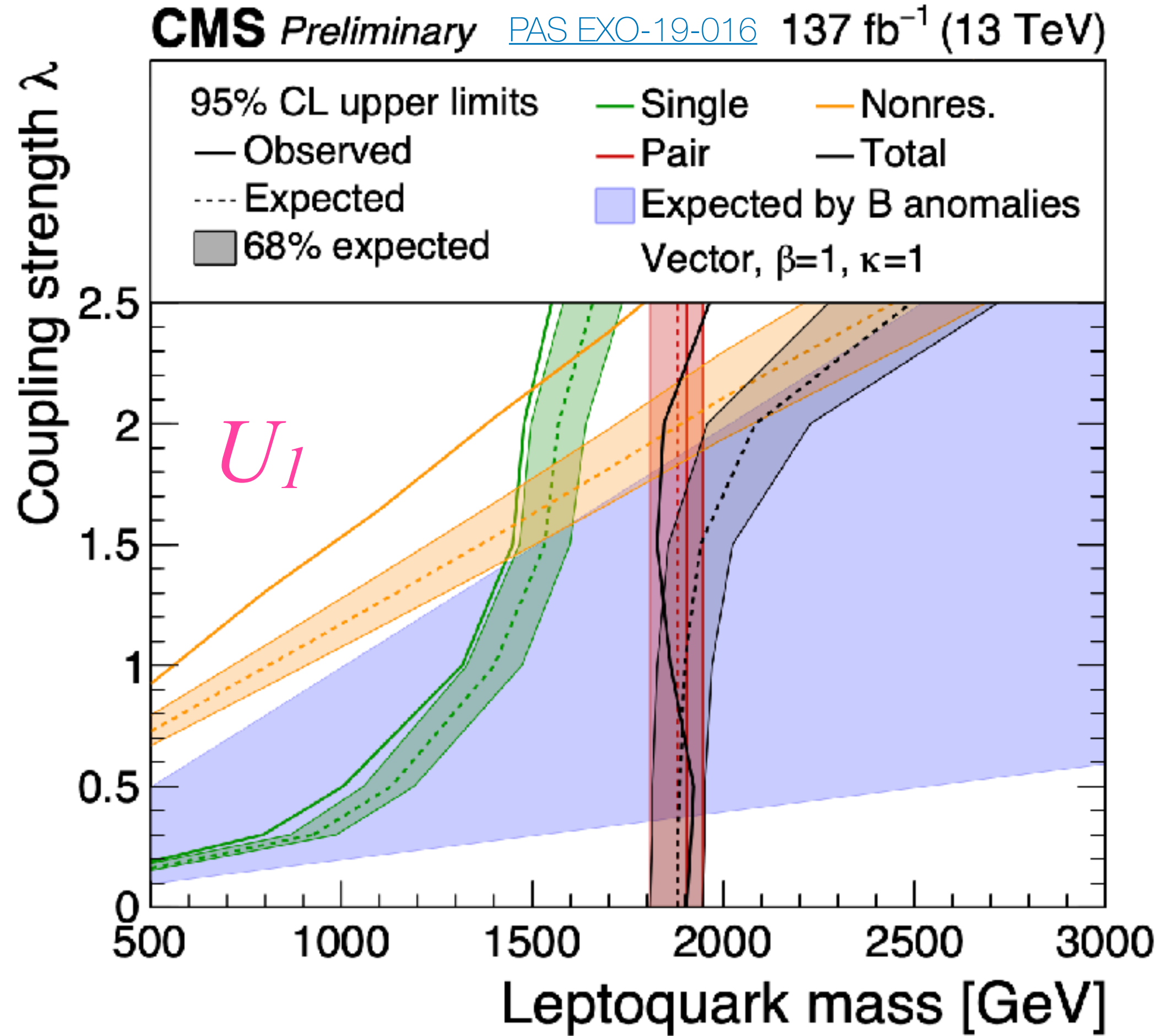
Discover SM value of $B^0 \rightarrow K^{*0} \nu \bar{\nu}$ with $\sim 5ab^{-1}$.

Bound on $Br(\tau \rightarrow \mu \gamma (3 \mu))$ will **improve by a factor of 6 (60)**.

3rd gen LQ searches



scalar $M_{LQ} \gtrsim 1.3$ TeV



vector $M_{LQ} \gtrsim 1.9$ TeV

S_1, S_3 : Higgs, EW and m_W

The two leptoquarks have potential couplings to the Higgs:

$$\begin{aligned} \mathcal{L}_{LQ} \supset & - \left(\lambda_{H13} (H^\dagger \sigma^I H) S_3^{I\dagger} S_1 + \text{h.c.} \right) - \lambda_{\epsilon H3} i \epsilon^{IJK} (H^\dagger \sigma^I H) S_3^{J\dagger} S_3^K \\ & - \lambda_{H1} |H|^2 |S_1|^2 - \lambda_{H3} |H|^2 |S_3^I|^2 \end{aligned}$$

At one loop they **contribute to Higgs couplings**
and **S, T parameters**:

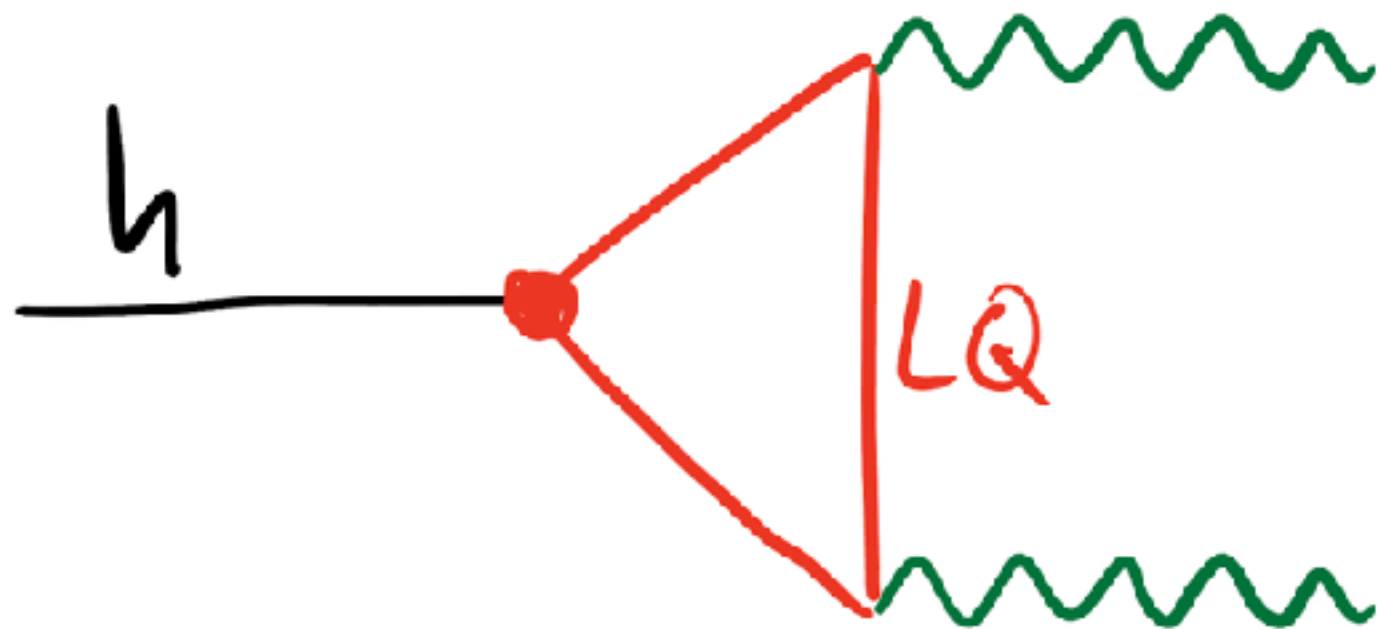
S₁, S₃: Higgs, EW and m_w

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$$\mathcal{L}_{\text{LQ}} \supset - \left(\lambda_{H13} (H^\dagger \sigma^I H) S_3^{I\dagger} S_1 + \text{h.c.} \right) - \lambda_{\epsilon H3} i \epsilon^{IJK} (H^\dagger \sigma^I H) S_3^{J\dagger} S_3^K$$

$$- \lambda_{H1} |H|^2 |S_1|^2 - \lambda_{H3} |H|^2 |S_3^I|^2$$

At one loop they **contribute to Higgs couplings** and **S, T parameters**:



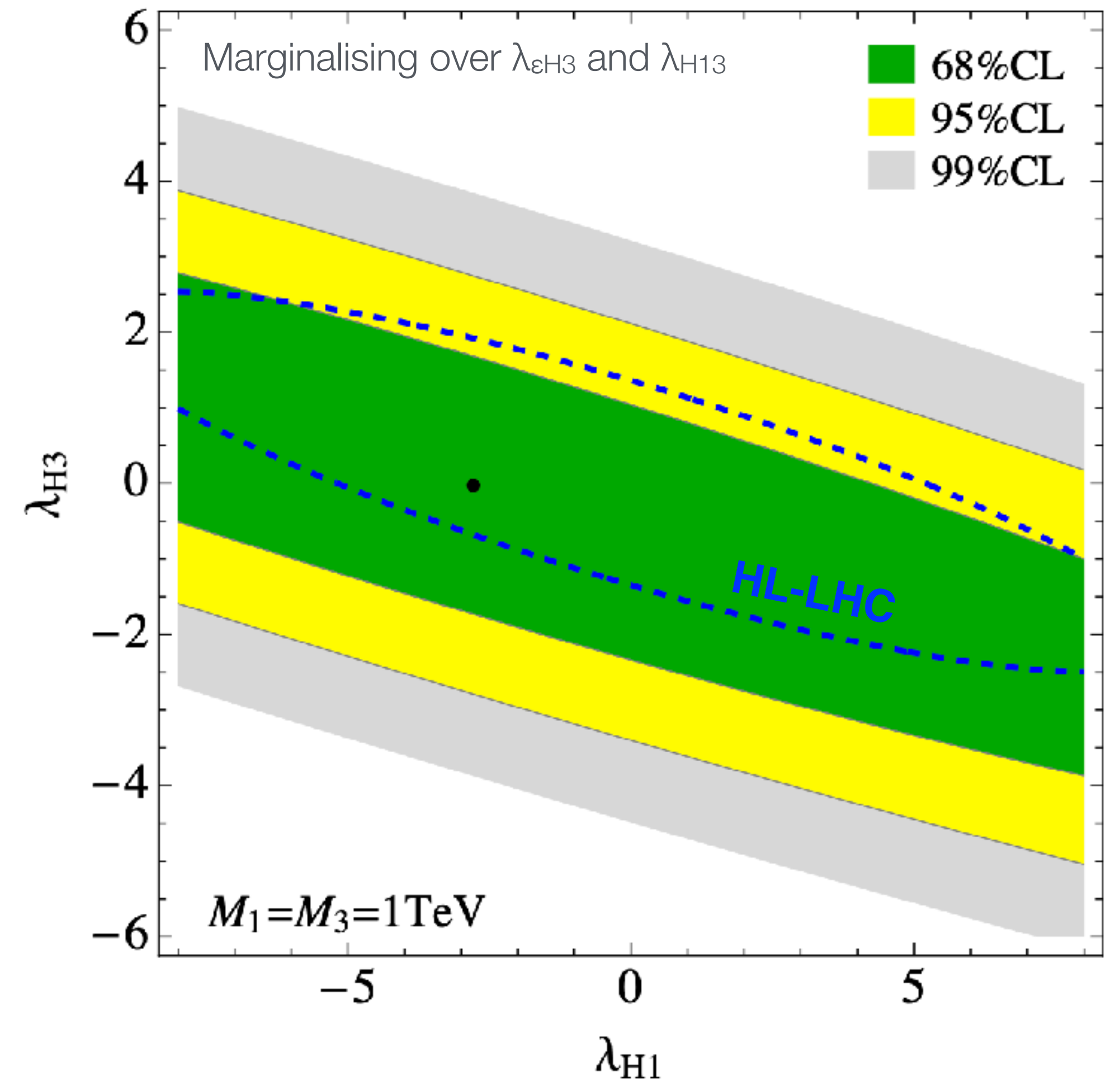
$$\kappa_g - 1 = -(3.51\lambda_{H3} + 1.17\lambda_{H1}) \times 10^{-2}/m^2,$$

$$\kappa_\gamma - 1 = -(2.32\lambda_{H3} + 0.66\lambda_{\epsilon H3} - 0.11\lambda_{H1}) \times 10^{-2}/m^2,$$

$$\kappa_{Z\gamma} - 1 = -(1.89\lambda_{H3} + 0.23\lambda_{\epsilon H3} - 0.033\lambda_{H1}) \times 10^{-2}/m^2.$$

$$m = M_{\text{LQ}} / \text{TeV}$$

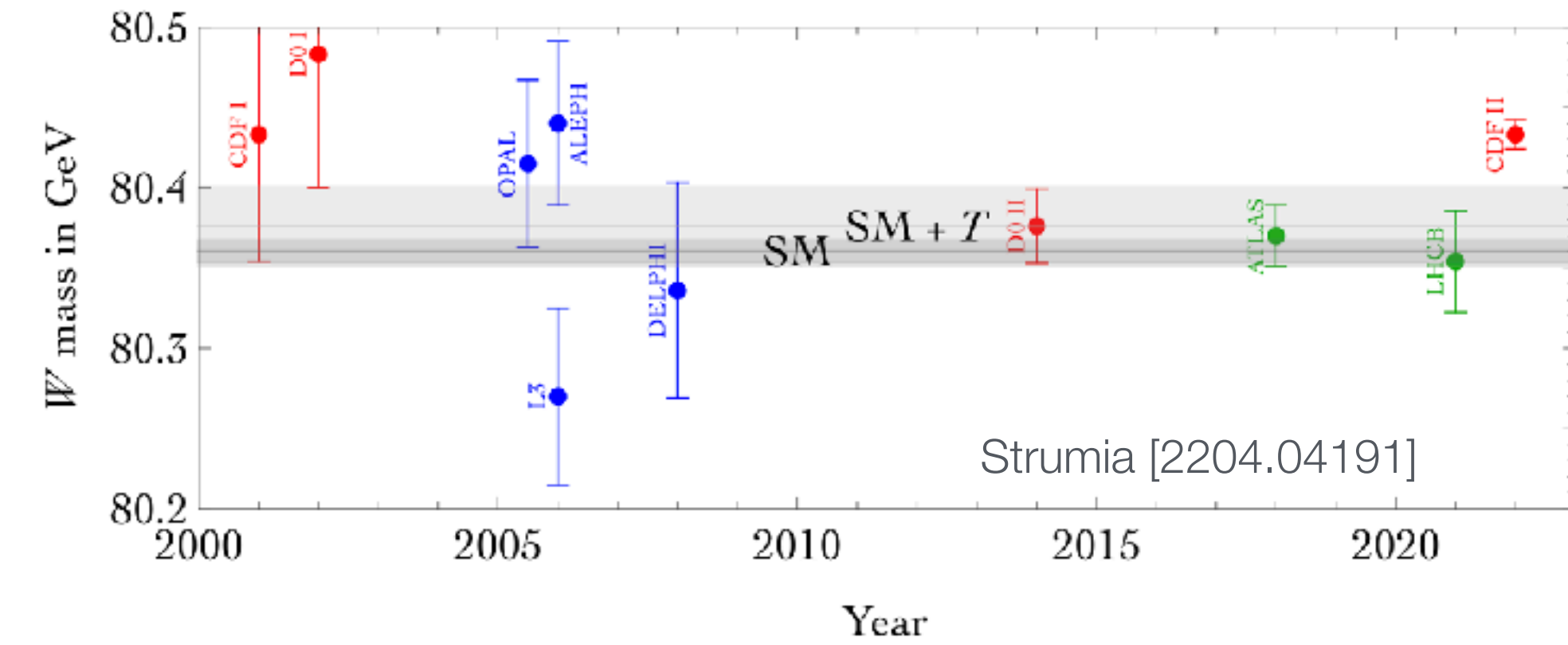
V. Gherardi, E. Venturini, D.M. [2008.09548]
See also 1910.03877, 2006.10758 and 2204.03996



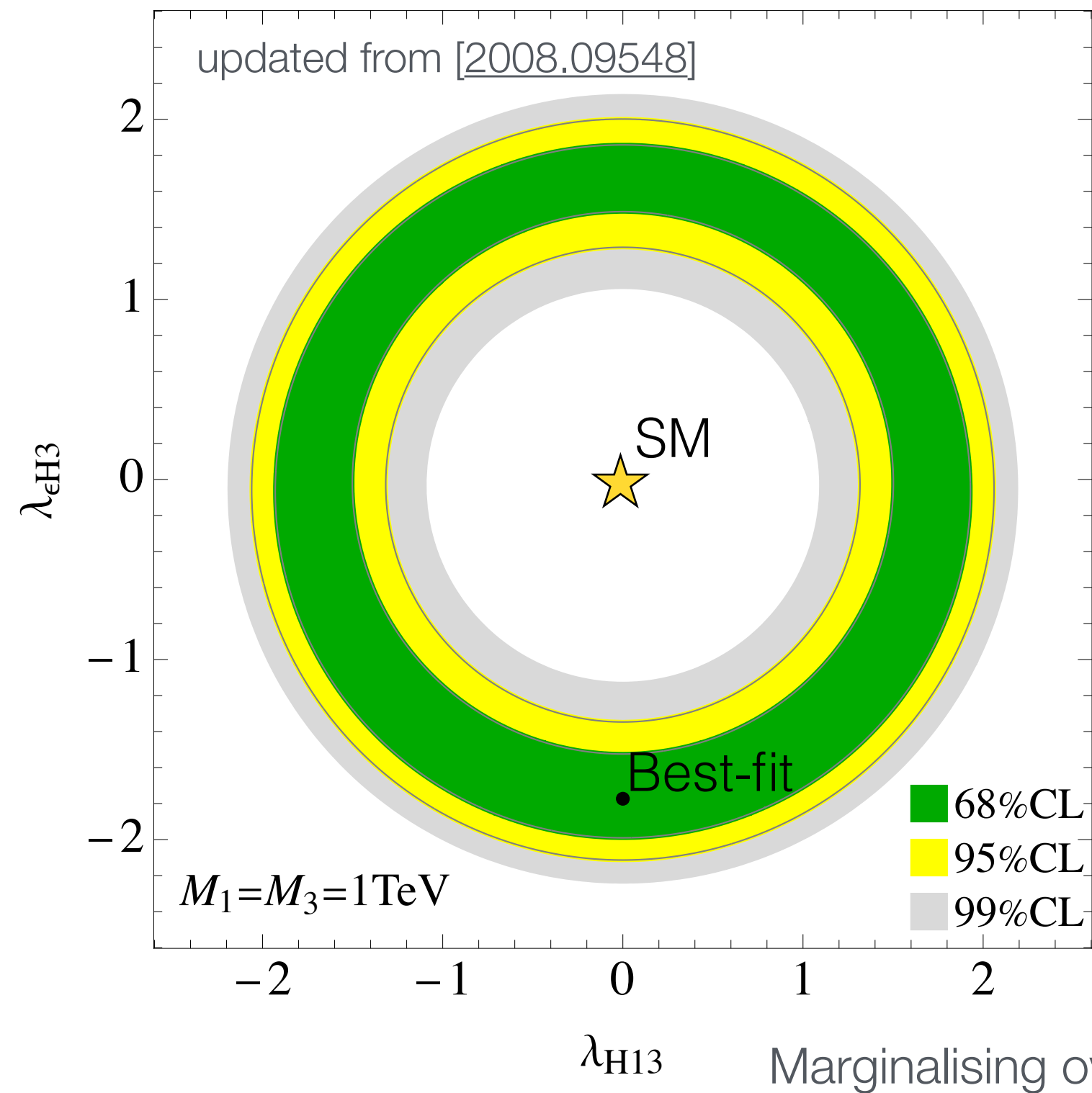
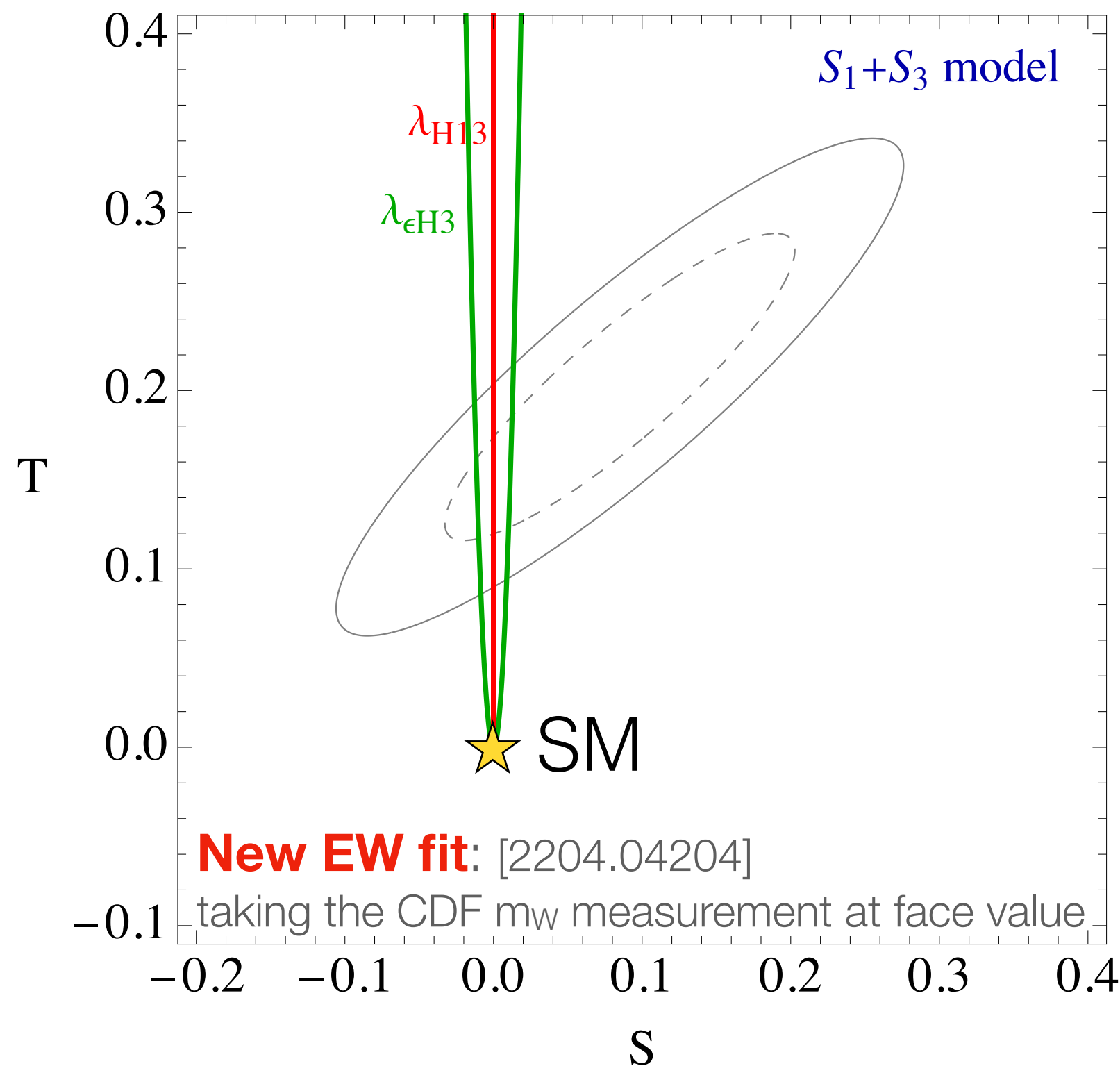
S₁, S₃: Higgs, EW and m_w

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Could these LQ address the m_w discrepancy recently claimed by CDF? Yes!



They can fit the anomaly with $\sim 1\text{TeV}$ masses and $O(1)$ couplings

Intriguing experimental hints for New Physics.

We should wait and see what more data will bring...

meanwhile, they spawned some interesting model building

(a partial selection in what follows)

From Leptoquarks to the Higgs, and back

From B-anomalies

$$M_{LQ} \sim \text{TeV}$$

Hierarchical couplings to SM fermions

$$g(\mathbf{3rd}) > g(\mathbf{2nd}) > g(\mathbf{1st})$$

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Higgs & EW hierarchy

$$M_{BSM} \approx \text{TeV}$$

Hierarchical Yukawa couplings

$$y(\mathbf{3rd}) > y(\mathbf{2nd}) > y(\mathbf{1st})$$

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$$y(\mathbf{3rd}) > y(\mathbf{2nd}) > y(\mathbf{1st})$$

LQ from same UV responsible for the EW scale,
connection between LQ couplings and Yukawa couplings.

Model building for LQs and Higgs

Scalar Leptoquarks + Higgs as pNGB

or

**U_1 Vector Leptoquark as TC Pati Salam
+ Higgs as pNGB**

[2004.11376]

[0910.1789, 1412.1791, 1803.10972]

> extensions of Composite Higgs models <

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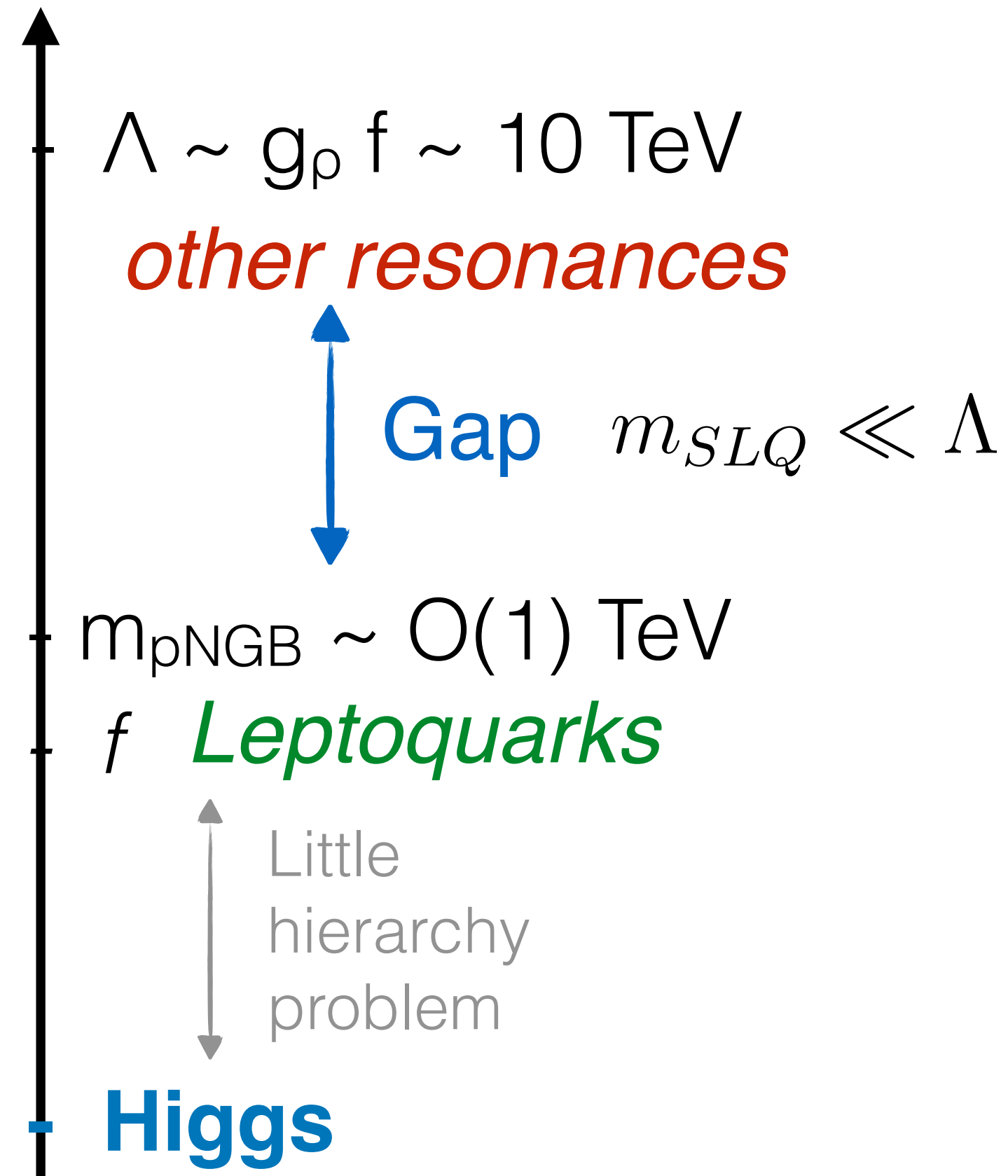
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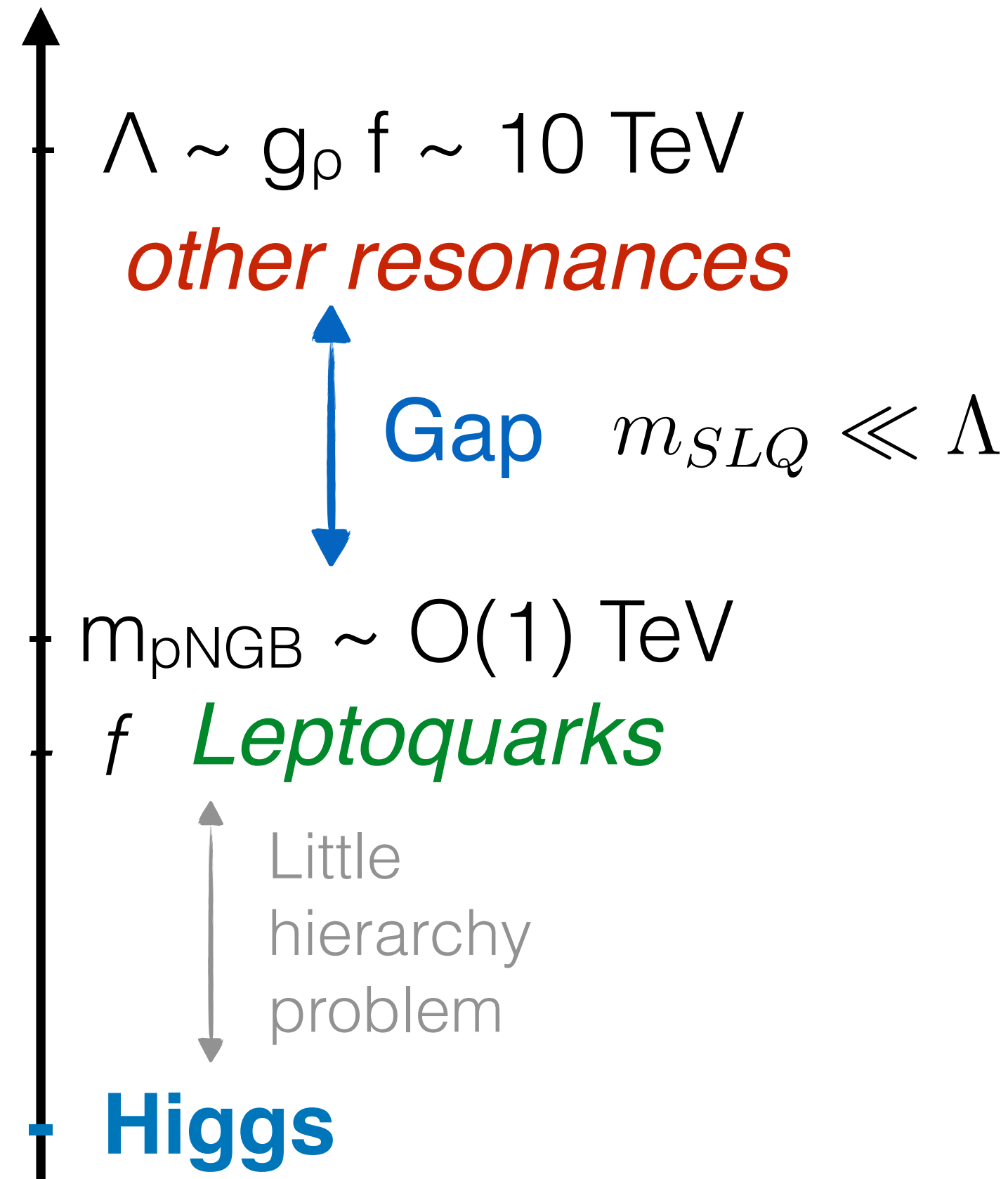
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Higgs Yukawas and LQ couplings can arise from same dynamics.



$$\langle \bar{\Psi}_i \Psi_j \rangle = -B_0 f^2 \delta_{ij}$$

The condensate of the strong sector, that gives the Higgs as pNGB, also breaks spontaneously an extra $SU(4)$ gauge symmetry. The NGBs are eaten by the U_1 LQ.

$$M_U \sim g_4 f$$

Model building for LQs and Higgs

Scalar Leptoquarks + Higgs as pNGB

or

U₁ Vector Leptoquark as TC Pati Salam + Higgs as pNGB

[2004.11376]

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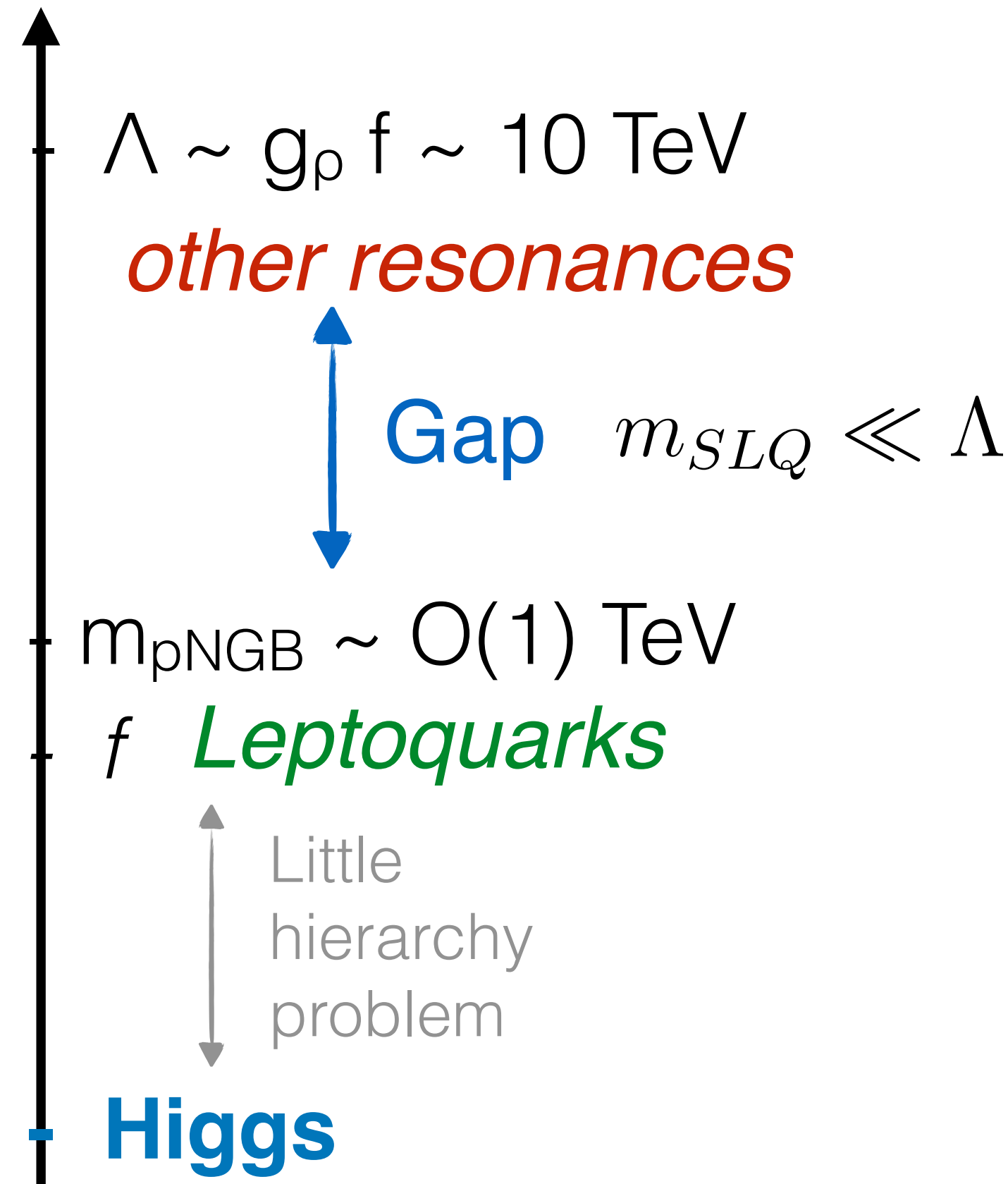
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The condensate of the strong sector, that gives the Higgs as pNGB, also breaks spontaneously an extra SU(4) gauge symmetry. The NGBs are eaten by the U₁ LQ.

$$M_U \sim g_4 f$$



Deviations in Higgs couplings as in typical Composite Higgs models:

$$\delta\kappa_{Vf} \sim v^2 / f^2 \sim (\text{few}) \%$$

Conclusions

Several interesting anomalies in B decays, pointing to New Physics at the TeV scale.

Waiting for updates from LHCb and Belle-2.

Correlated signals are expected ($p p \rightarrow \tau \tau$, $b \rightarrow s \nu \nu$, lepton LFV, ...).

Connections to Higgs physics are not direct, but the mediators responsible for the anomalies could leave an impact on Higgs couplings.

Flavour anomalies + EW hierarchy problem point both to New Physics at TeV.

A combined solution seems natural. For example:

extensions of Composite Higgs models with scalar or vector leptoquarks.

Deviations in Higgs couplings due to its composite nature are then expected.

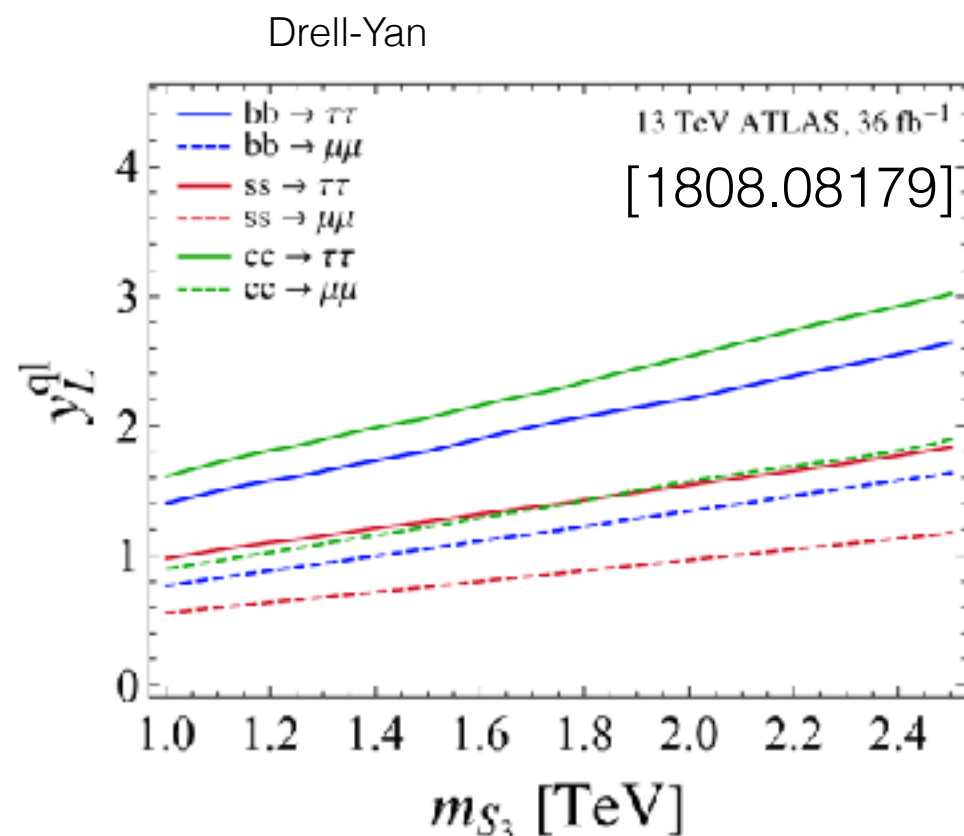
S₁ and S₃ - global analysis

Using the complete one-loop matching to SMEFT, we include in our analysis the following observables.

All these are used to build a **global likelihood**.

$$-2\log \mathcal{L} \equiv \chi^2(\lambda_x, M_x) = \sum_i \frac{(\mathcal{O}_i(\lambda_x, M_x) - \mu_i)^2}{\sigma_i^2}$$

Observable	Experimental bounds
Z boson couplings	App. A.12
$\delta g_{\mu L}^Z$	$(0.3 \pm 1.1)10^{-3}$ [99]
$\delta g_{\mu R}^Z$	$(0.2 \pm 1.3)10^{-3}$ [99]
$\delta g_{\tau L}^Z$	$(-0.11 \pm 0.61)10^{-3}$ [99]
$\delta g_{\tau R}^Z$	$(0.66 \pm 0.65)10^{-3}$ [99]
δg_{bL}^Z	$(2.9 \pm 1.6)10^{-3}$ [99]
δg_{cR}^Z	$(-3.3 \pm 5.1)10^{-3}$ [99]
N_ν	2.9963 ± 0.0074 [100]



Observable	SM prediction	Experimental bounds
<i>b</i> → <i>s</i> ℓℓ observables		[37]
$\Delta C_9^{sb\mu\mu}$	0	-0.43 ± 0.09 [79]
C_9^{univ}	0	-0.48 ± 0.24 [79]
<i>b</i> → <i>c</i> τ(ℓ)ν observables		[37]
R_D	0.299 ± 0.003 [12]	$0.34 \pm 0.027 \pm 0.013$ [12]
R_D^*	0.258 ± 0.005 [12]	$0.295 \pm 0.011 \pm 0.008$ [12]
$P_\tau^{D^*}$	-0.488 ± 0.018 [80]	$-0.38 \pm 0.51 \pm 0.2 \pm 0.018$ [7]
F_L	0.470 ± 0.012 [80]	$0.60 \pm 0.08 \pm 0.038 \pm 0.012$ [81]
$\mathcal{B}(B_c^+ \rightarrow \tau^+ \nu)$	2.3%	< 10% (95% CL) [82]
$R_D^{\mu/e}$	1	0.978 ± 0.035 [83, 84]
<i>b</i> → <i>s</i> νν and <i>s</i> → <i>d</i> νν		[37]
R_K^ν	1 [85]	< 4.7 [86]
$R_{K^*}^\nu$	1 [85]	< 3.2 [86]
<i>b</i> → <i>d</i> μμ and <i>b</i> → <i>d</i> ee		App. A.5
$\mathcal{B}(B^0 \rightarrow \mu\mu)$	$(1.06 \pm 0.09) \times 10^{-10}$ [87, 88]	$(1.1 \pm 1.4) \times 10^{-10}$ [89, 90]
$\mathcal{B}(B^+ \rightarrow \pi^+ \mu\mu)$	$(2.04 \pm 0.21) \times 10^{-8}$ [87, 88]	$(1.83 \pm 0.24) \times 10^{-8}$ [89, 90]
$\mathcal{B}(B^0 \rightarrow ee)$	$(2.48 \pm 0.21) \times 10^{-15}$ [87, 88]	< 8.3×10^{-8} [51]
$\mathcal{B}(B^+ \rightarrow \pi^+ ee)$	$(2.04 \pm 0.24) \times 10^{-8}$ [87, 88]	< 8×10^{-8} [51]
<i>B</i> LFV decays		[37]
$\mathcal{B}(B_d \rightarrow \tau^\pm \mu^\mp)$	0	< 1.4×10^{-5} [91]
$\mathcal{B}(B_s \rightarrow \tau^\pm \mu^\mp)$	0	< 4.2×10^{-5} [91]
$\mathcal{B}(B^+ \rightarrow K^+ \tau^- \mu^+)$	0	< 5.4×10^{-5} [92]
$\mathcal{B}(B^+ \rightarrow K^+ \tau^+ \mu^-)$	0	< 3.3×10^{-5} [92] < 4.5×10^{-5} [93]

Observable	SM prediction	Experimental bounds
<i>D</i> leptonic decay		[37] and App. A.4
$\mathcal{B}(D_s \rightarrow \tau\nu)$	$(5.169 \pm 0.004) \times 10^{-2}$ [94]	$(5.48 \pm 0.23) \times 10^{-2}$ [51]
$\mathcal{B}(D^0 \rightarrow \mu\mu)$	$\approx 10^{-11}$ [95]	< 7.6×10^{-9} [96]
$\mathcal{B}(D^+ \rightarrow \pi^+ \mu\mu)$	$\mathcal{O}(10^{-12})$ [97]	< 7.4×10^{-8} [98]
Rare Kaon decays (νν)		App. A.1
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu\nu)$	8.64×10^{-11} [99]	$(11.0 \pm 4.0) \times 10^{-11}$ [100]
$\mathcal{B}(K_L \rightarrow \pi^0 \nu\nu)$	3.4×10^{-11} [99]	< 3.6×10^{-9} [101]
Rare Kaon decays (ℓℓ)		App. A.3 and A.2
$\mathcal{B}(K_L \rightarrow \mu\mu)_{SD}$	8.4×10^{-10} [102]	< 2.5×10^{-9} [76]
$\mathcal{B}(K_S \rightarrow \mu\mu)$	$(5.18 \pm 1.5) \times 10^{-12}$ [76, 103, 104]	< 2.5×10^{-10} [105]
$\mathcal{B}(K_L \rightarrow \pi^0 \mu\mu)$	$(1.5 \pm 0.3) \times 10^{-11}$ [106]	< 4.5×10^{-10} [107]
$\mathcal{B}(K_L \rightarrow \pi^0 ee)$	$(3.2_{-0.8}^{+1.2}) \times 10^{-11}$ [108]	< 2.8×10^{-10} [109]
LFV in Kaon decays		App. A.3 and A.2
$\mathcal{B}(K_L \rightarrow \mu e)$	0	< 4.7×10^{-12} [110]
$\mathcal{B}(K^+ \rightarrow \pi^+ \mu^- e^+)$	0	< 7.9×10^{-11} [111]
$\mathcal{B}(K^+ \rightarrow \pi^+ e^- \mu^+)$	0	< 1.5×10^{-11} [112]
CP-violation		App. A.8
ϵ'_K/ϵ_K	$(15 \pm 7) \times 10^{-4}$ [113]	$(16.6 \pm 2.3) \times 10^{-4}$ [51]

Observable	SM prediction	Experimental bounds
$\Delta F = 2$ processes		[37]
$B^0 - \bar{B}^0: C_{B_d}^1 $	0	< 9.1×10^{-7} TeV ⁻² [114, 115]
$B_s^0 - \bar{B}_s^0: C_{B_s}^1 $	0	< 2.0×10^{-5} TeV ⁻² [114, 115]
$K^0 - \bar{K}^0: \text{Re}[C_K^1]$	0	< 8.0×10^{-7} TeV ⁻² [114, 115]
$K^0 - \bar{K}^0: \text{Im}[C_K^1]$	0	< 3.0×10^{-9} TeV ⁻² [114, 115]
$D^0 - \bar{D}^0: \text{Re}[C_D^1]$	0	< 3.6×10^{-7} TeV ⁻² [114, 115]
$D^0 - \bar{D}^0: \text{Im}[C_D^1]$	0	< 2.2×10^{-8} TeV ⁻² [114, 115]
$D^0 - \bar{D}^0: \text{Re}[C_D^4]$	0	< 3.2×10^{-8} TeV ⁻² [114, 115]
$D^0 - \bar{D}^0: \text{Im}[C_D^4]$	0	< 1.2×10^{-9} TeV ⁻² [114, 115]
$D^0 - \bar{D}^0: \text{Re}[C_D^5]$	0	< 2.7×10^{-7} TeV ⁻² [114, 115]
$D^0 - \bar{D}^0: \text{Im}[C_D^5]$	0	< 1.1×10^{-8} TeV ⁻² [114, 115]
LFU in τ decays		[37]
$ g_\mu/g_e ^2$	1	1.0036 ± 0.0028 [116]
$ g_\tau/g_\mu ^2$	1	1.0022 ± 0.0030 [116]
$ g_\tau/g_e ^2$	1	1.0058 ± 0.0030 [116]
LFV observables		[37]
$\mathcal{B}(\tau \rightarrow \mu\phi)$	0	< 1.00×10^{-7} [117]
$\mathcal{B}(\tau \rightarrow 3\mu)$	0	< 2.5×10^{-8} [118]
$\mathcal{B}(\tau \rightarrow \mu\gamma)$	0	< 5.2×10^{-8} [119]
$\mathcal{B}(\tau \rightarrow e\gamma)$	0	< 3.9×10^{-8} [119]
$\mathcal{B}(\mu \rightarrow e\gamma)$	0	< 5.0×10^{-13} [120]
$\mathcal{B}(\mu \rightarrow 3e)$	0	< 1.2×10^{-12} [121]
$\mathcal{B}_{\mu e}^{(\text{Ti})}$	0	< 5.1×10^{-12} [122]
$\mathcal{B}_{\mu e}^{(\text{Au})}$	0	< 8.3×10^{-13} [123]
EDMs		[37]
$ d_e $	< 10^{-44} e · cm [124, 125]	< 1.3×10^{-29} e · cm [126]
$ d_\mu $	< 10^{-42} e · cm [125]	< 1.9×10^{-19} e · cm [127]
d_τ	< 10^{-41} e · cm [125]	$(1.15 \pm 1.70) \times 10^{-17}$ e · cm [37]
d_n	< 10^{-33} e · cm [128]	< 2.1×10^{-26} e · cm [129]
Anomalous Magnetic Moments		[37]
$a_e - a_e^{SM}$	$\pm 2.3 \times 10^{-13}$ [130, 131]	$(-8.9 \pm 3.6) \times 10^{-13}$ [132]
$a_\mu - a_\mu^{SM}$	$\pm 43 \times 10^{-11}$ [42]	$(279 \pm 76) \times 10^{-11}$ [40, 42]
$a_\tau - a_\tau^{SM}$	$\pm 3.9 \times 10^{-8}$ [130]	$(-2.1 \pm 1.7) \times 10^{-7}$ [133]

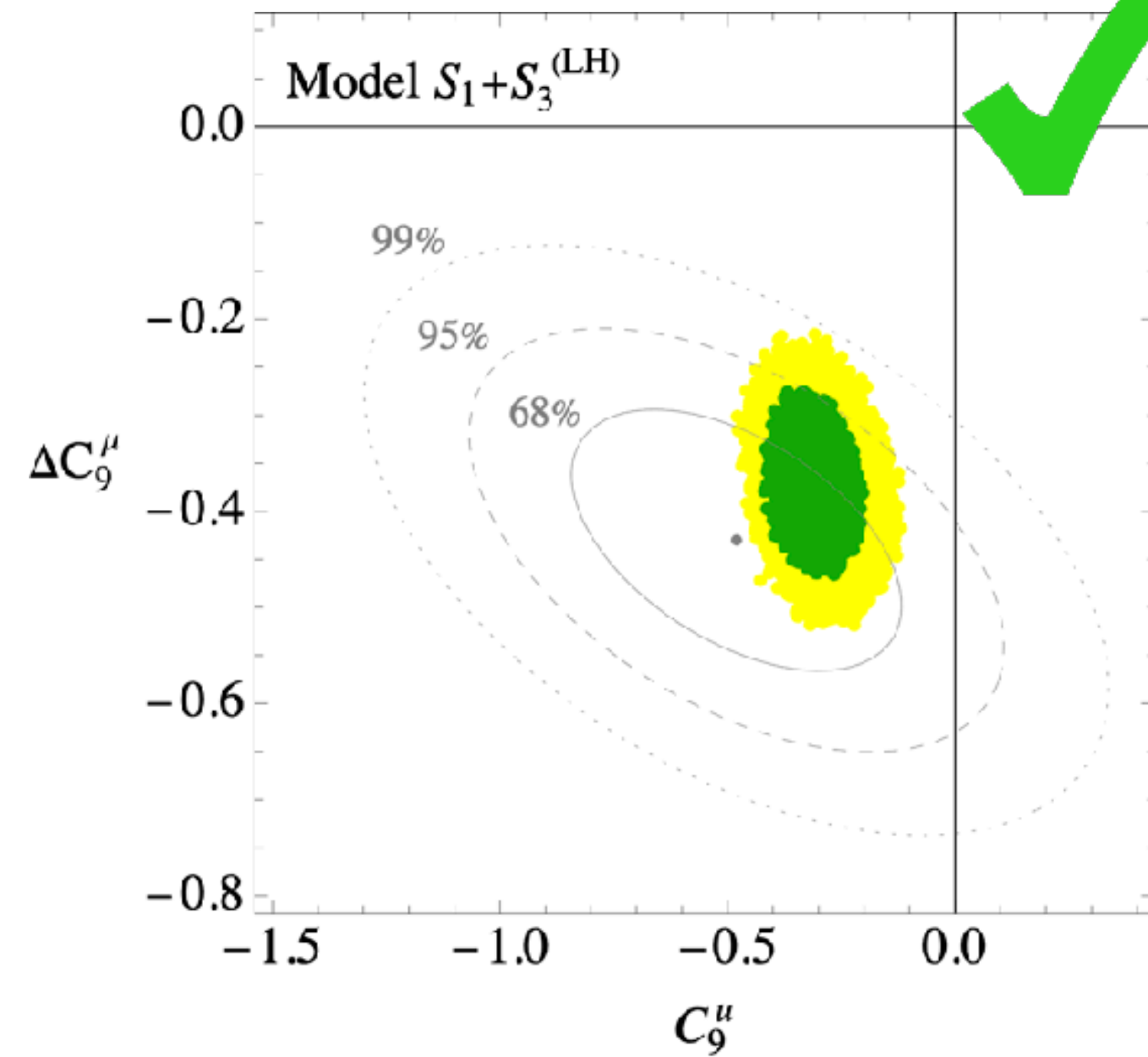
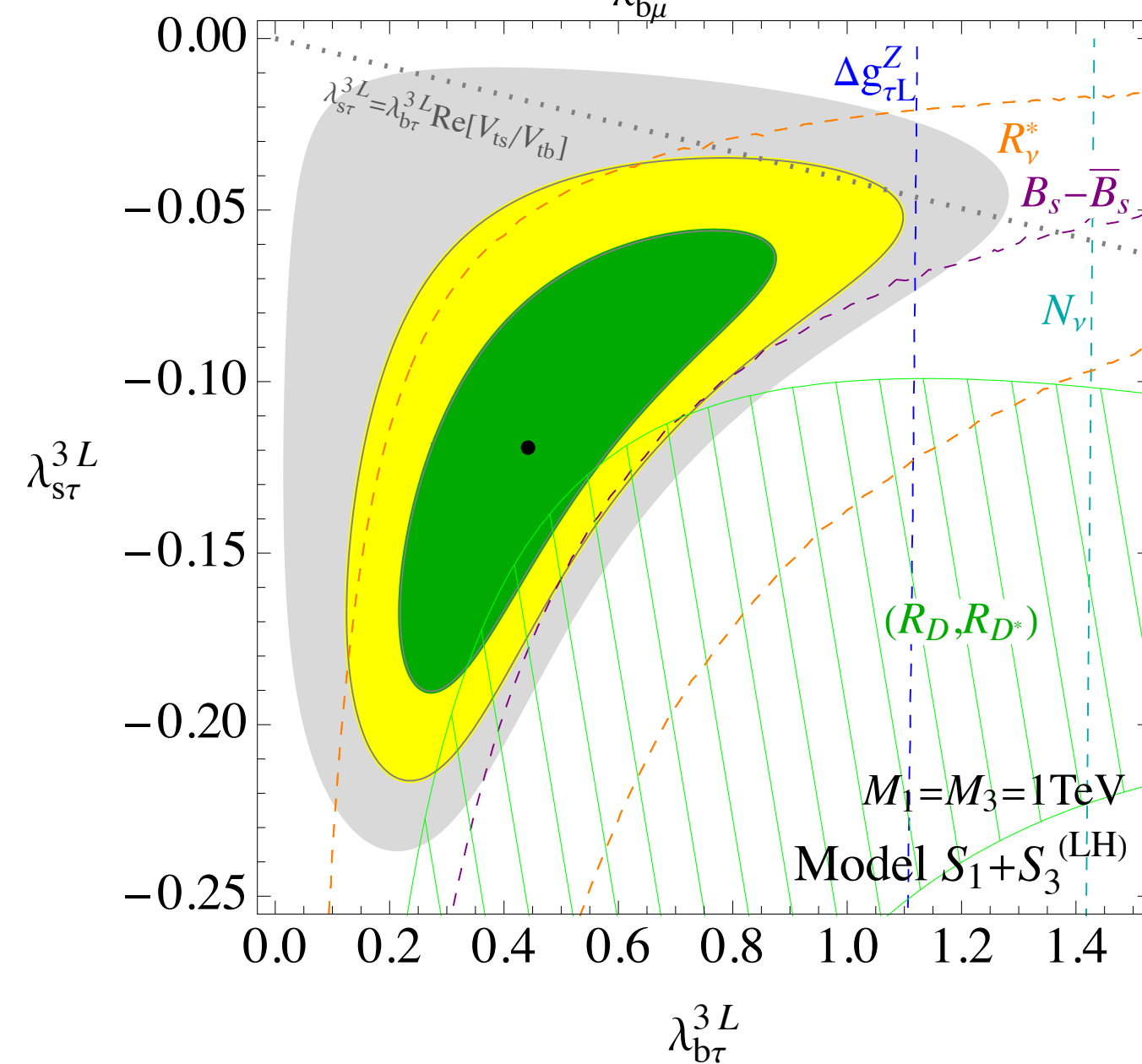
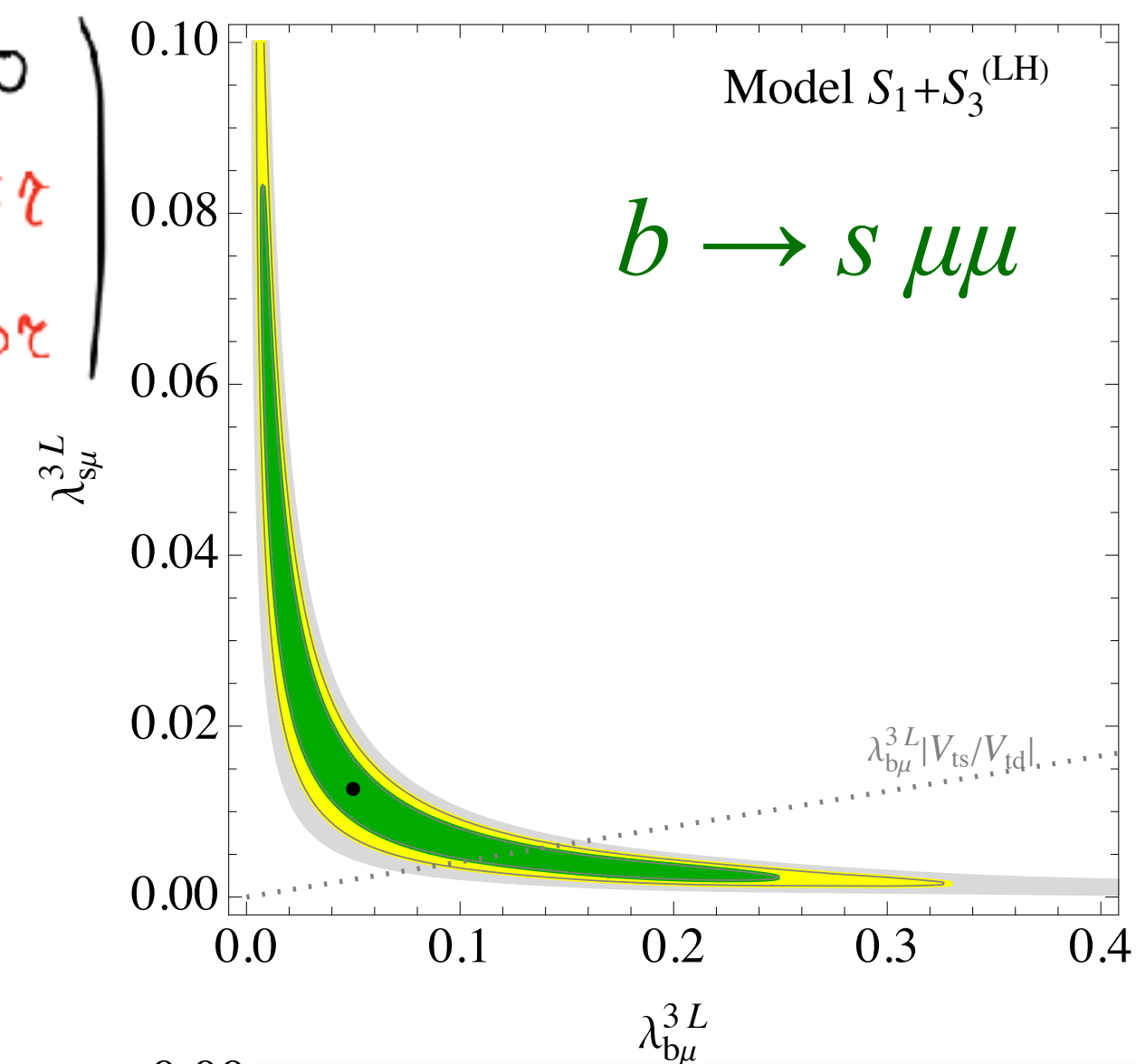
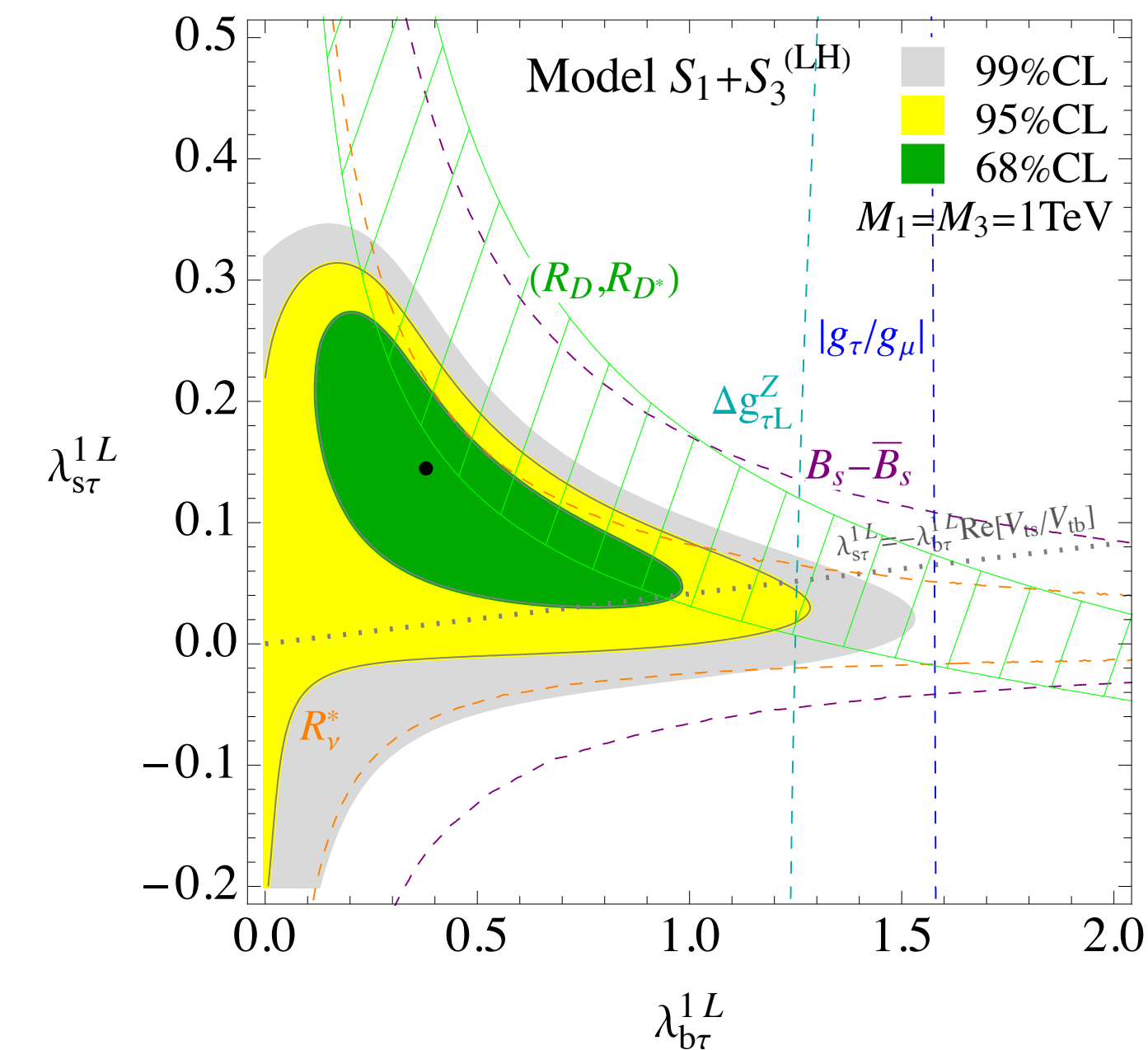
S_1 and S_3 — only LH couplings

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s\tau \\ 0 & 0 & b\tau \end{pmatrix} \quad \lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s\mu & s\tau \\ 0 & b\mu & b\tau \end{pmatrix}$$

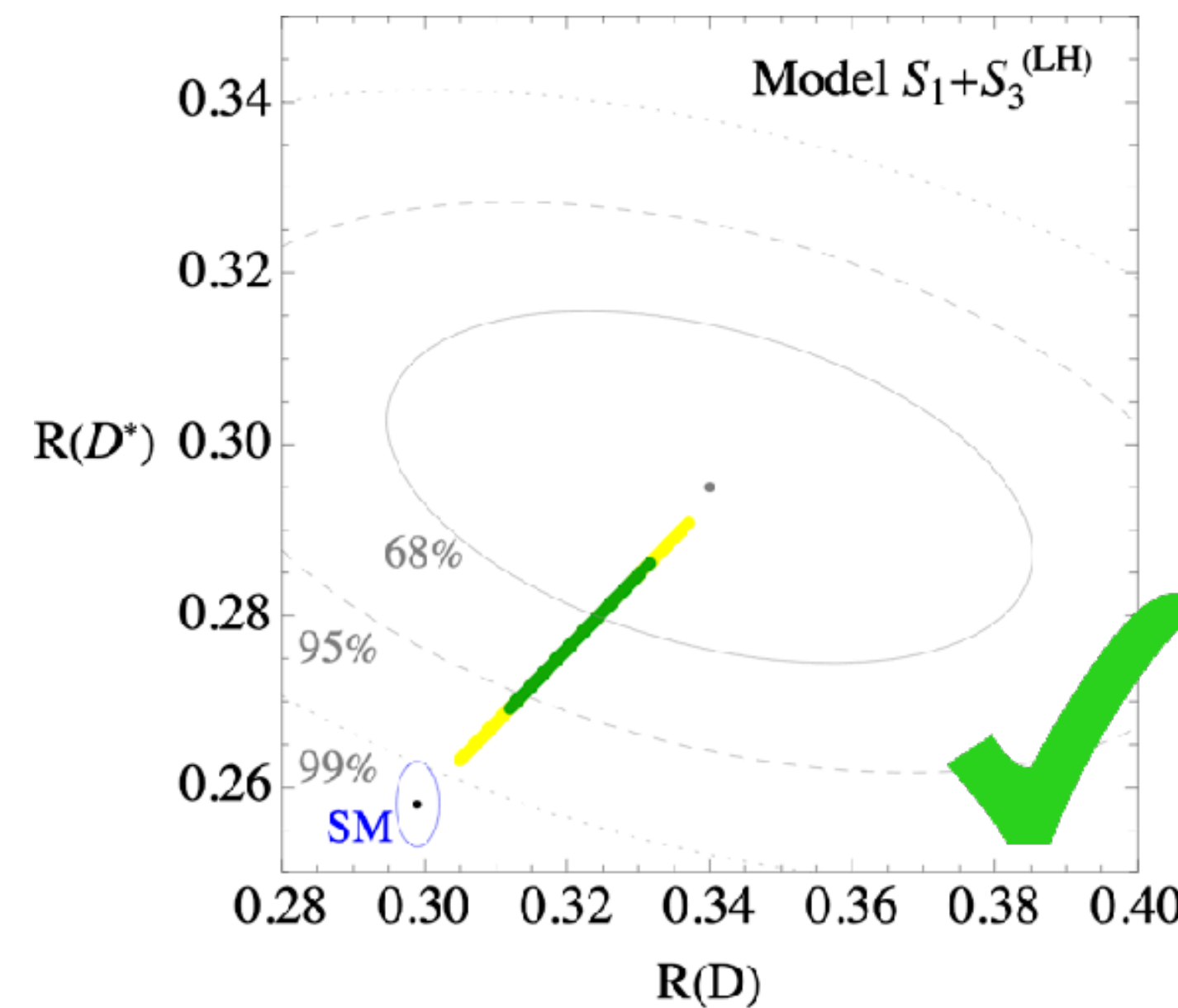
$\lambda^{1R} = \mathbf{0} \rightarrow$ Cannot fit $(g-2)_\mu$

(see backup slides for a S_1+S_3 scenario that addresses also the muon magnetic moment)

$R(D^*)$



very good fit of B-anomalies



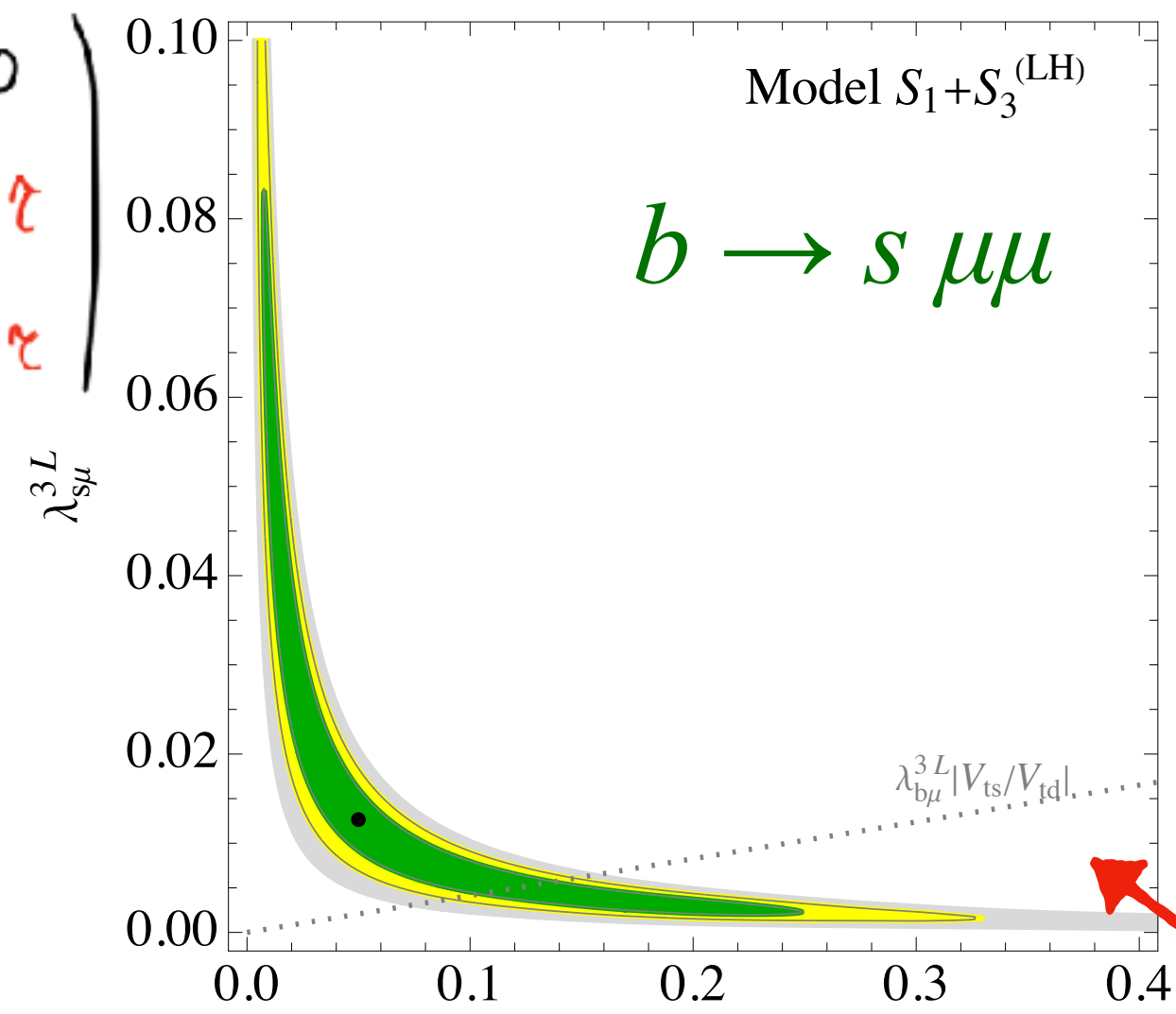
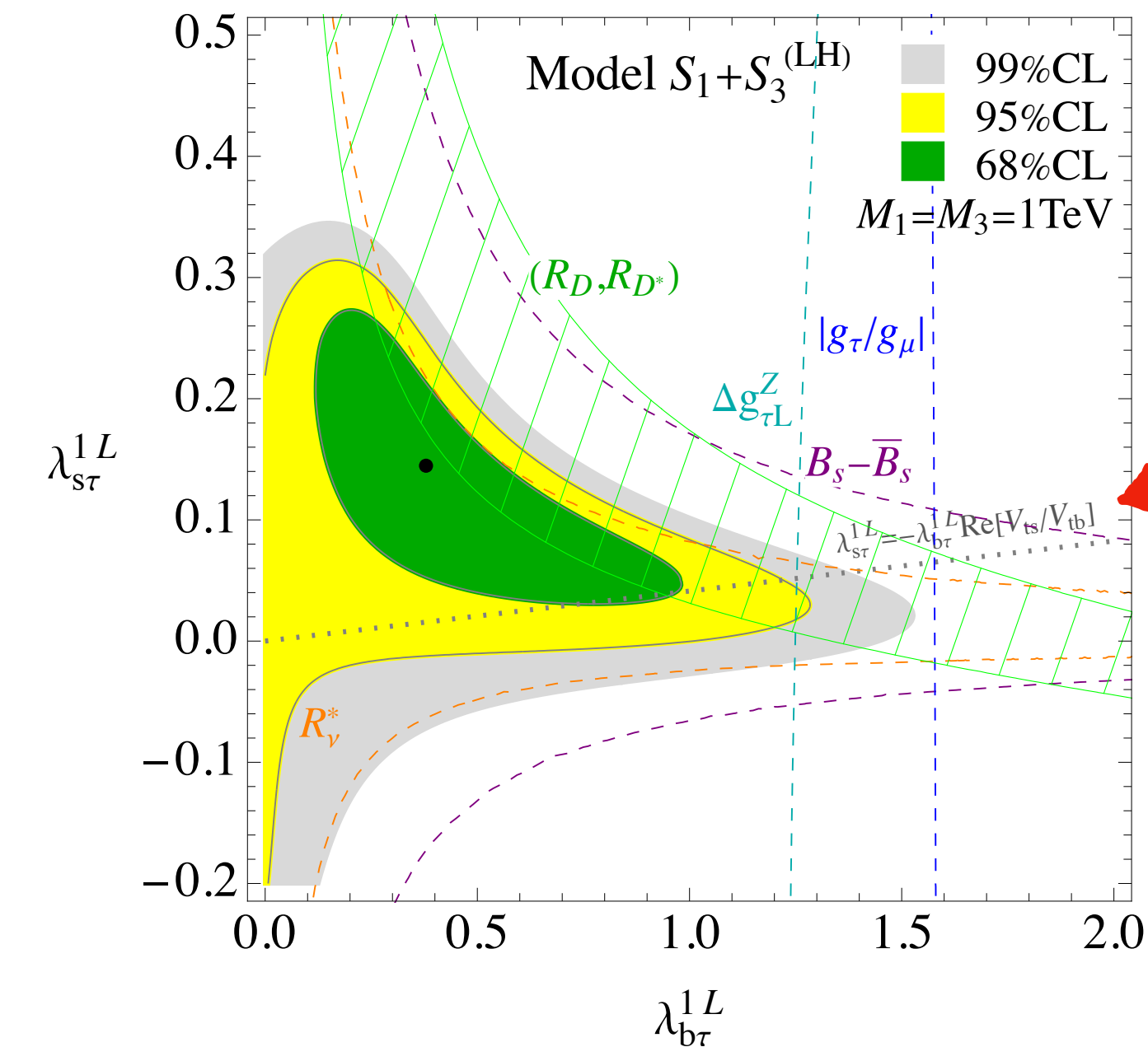
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$R(D^{(*)})$



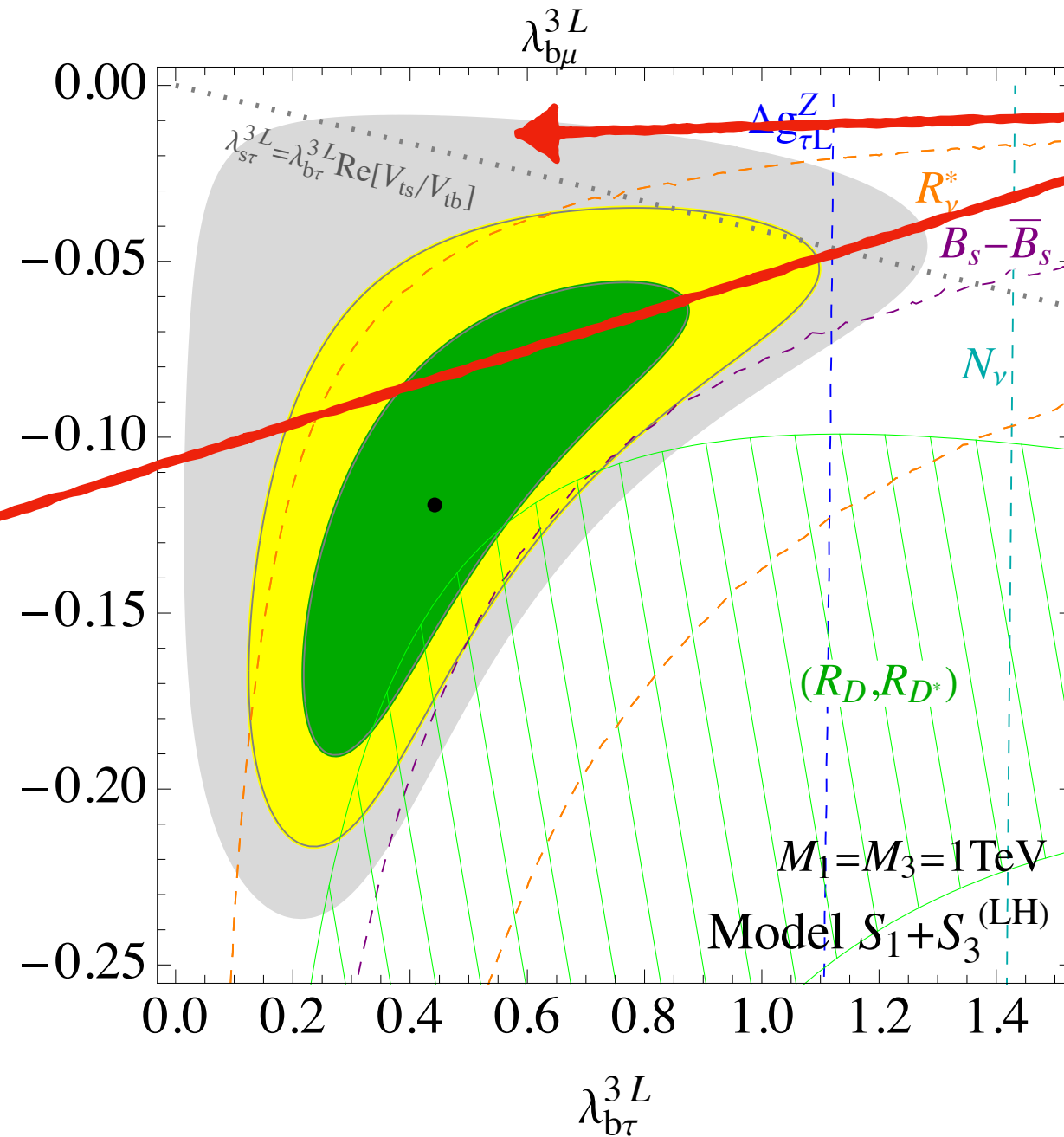
The relation between couplings to s -quark and b -quark is compatible with a $U(2)^5$ flavour symmetry, that would predict:

$$\lambda_{s\alpha} = c_{U(2)} V_{ts} \lambda_{b\alpha}$$

$c_{U(2)} = 1$

$$c_{U(2)} \sim \mathcal{O}(1) \text{ e.g. } 3 - 5$$

See also Buttazzo, Greljo, Isidori, D.M. 1706.07808



S₁ and S₃ : R(K^(*)) + R(D^(*)) + (g-2)_μ

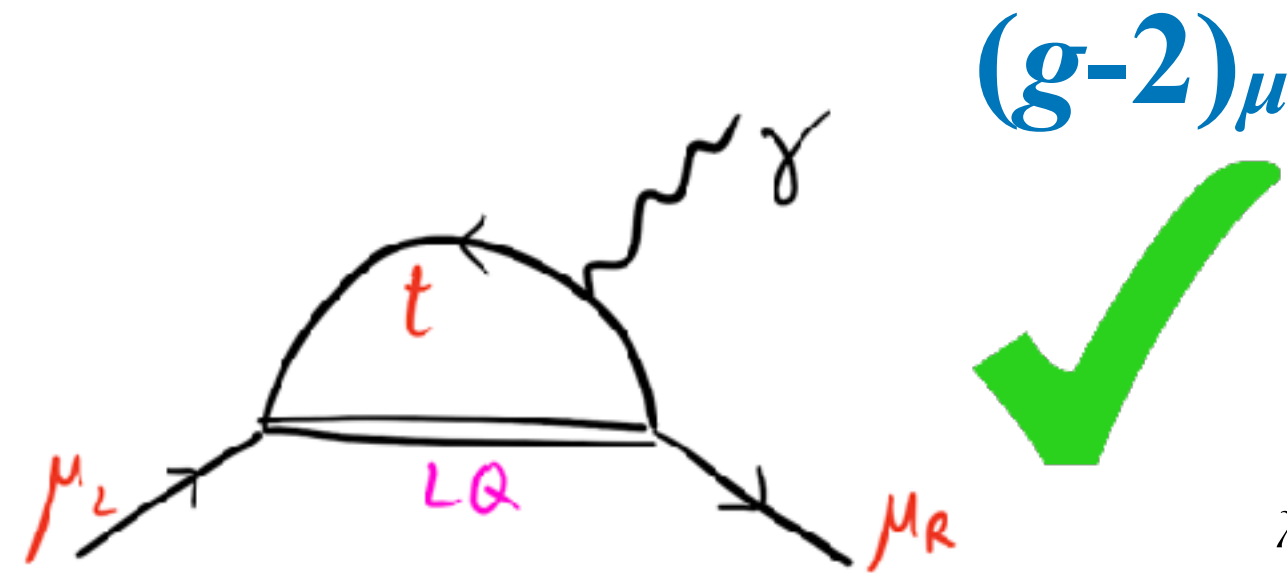
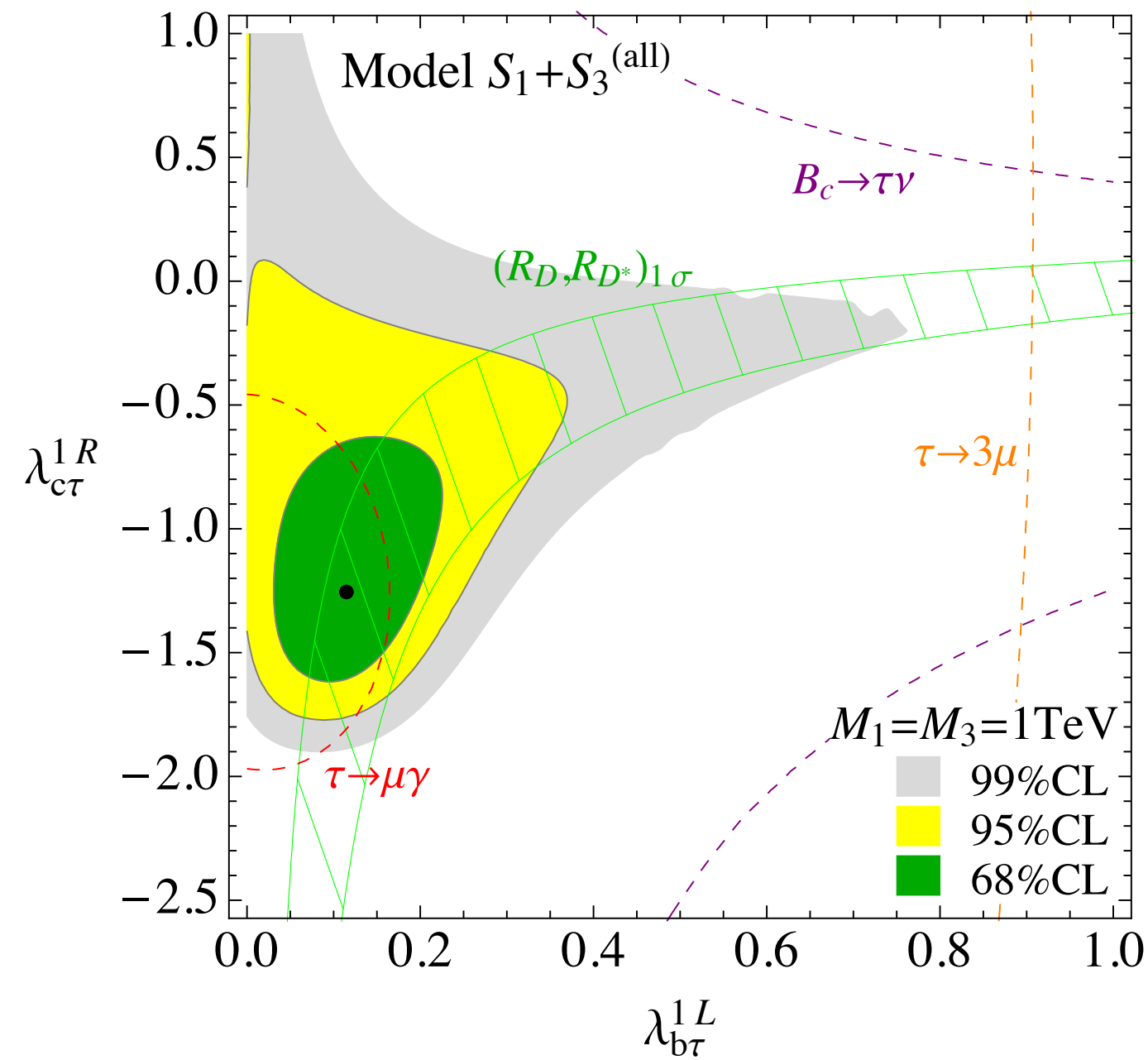
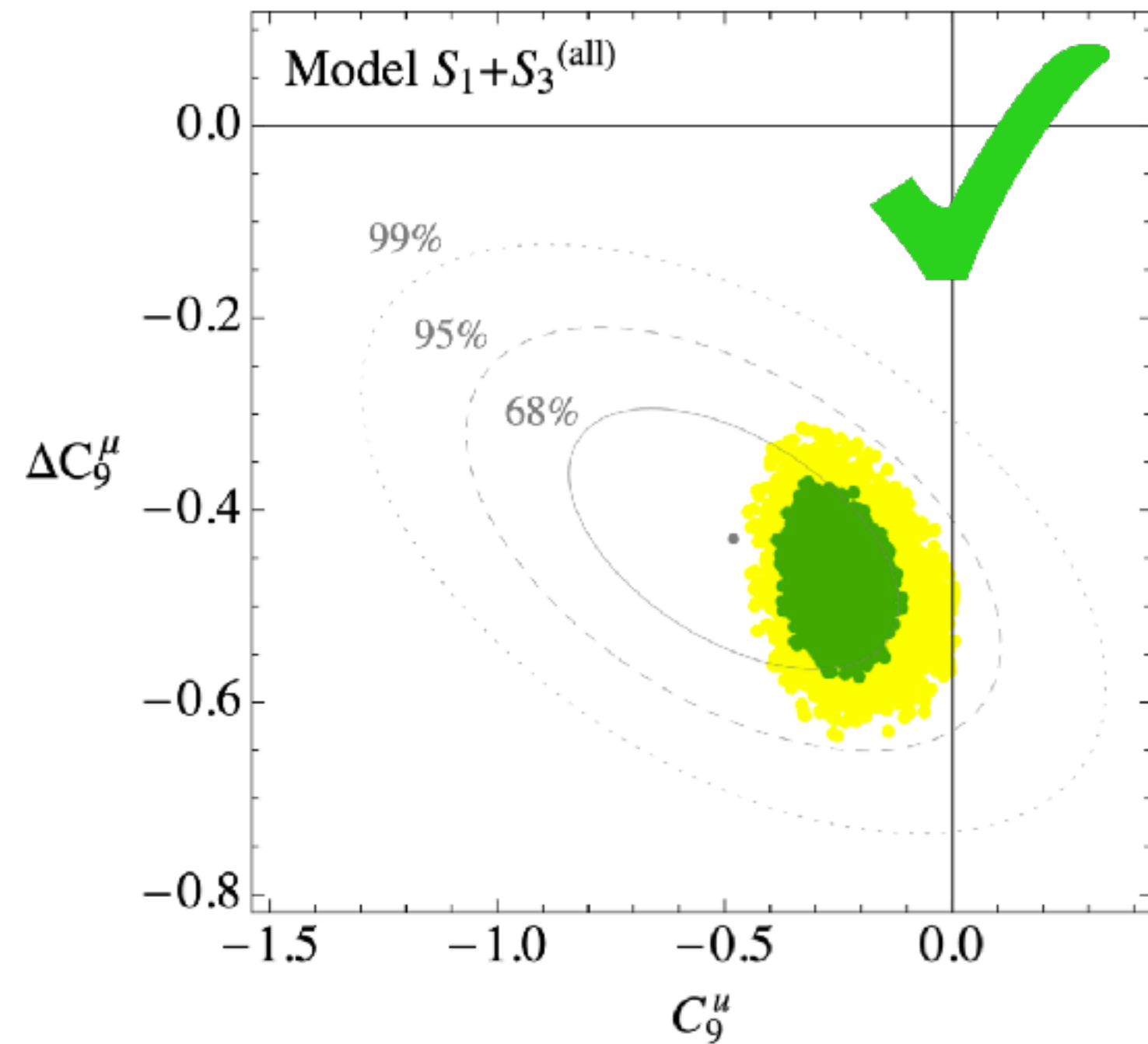
No a-priori flavour structure imposed

$$\lambda^{1L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & s^e \\ 0 & b_\mu & b_e \end{pmatrix}$$

$$\lambda^{3L} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & s_\mu & s_e \\ 0 & b_\mu & b_e \end{pmatrix}$$

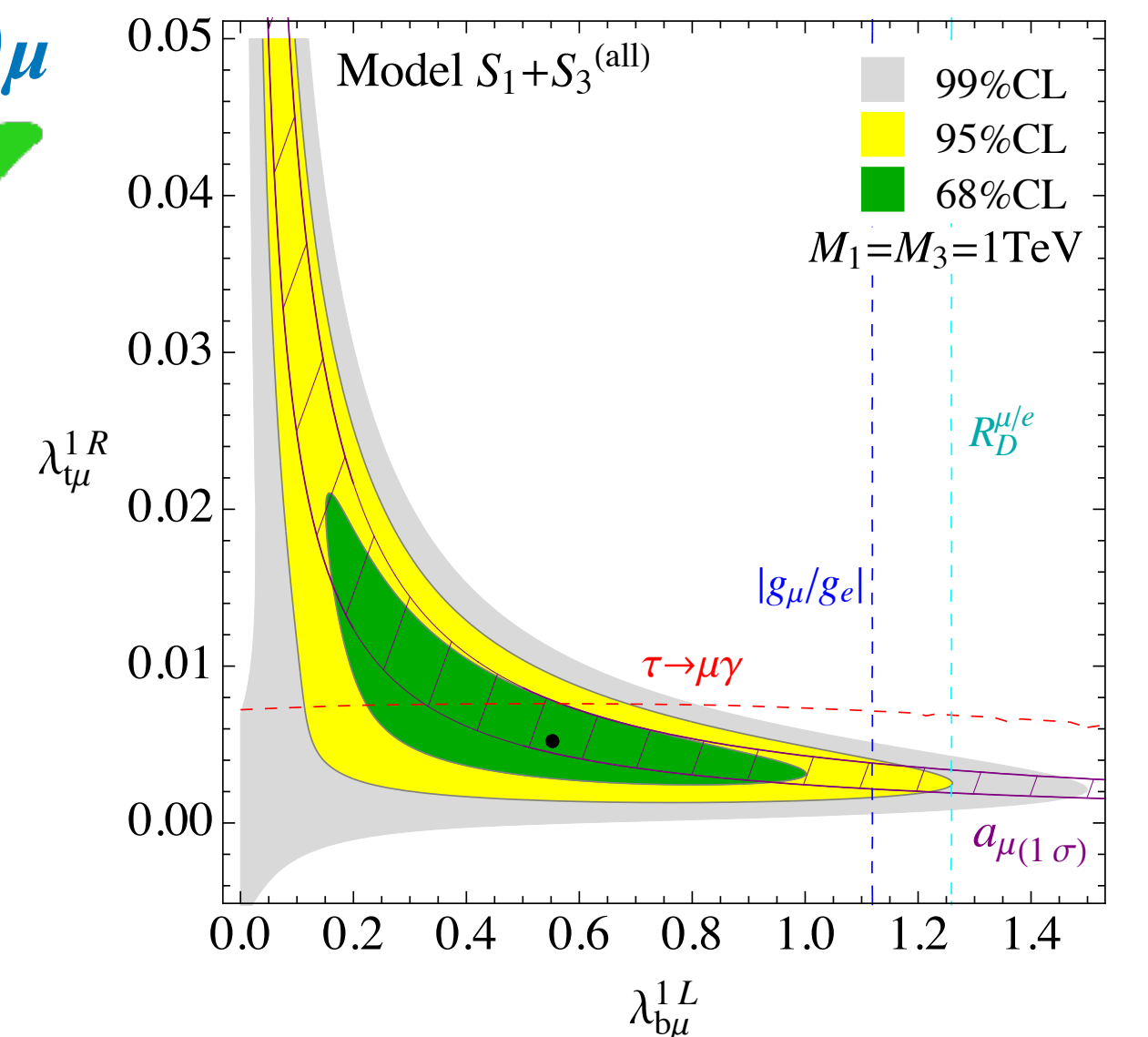
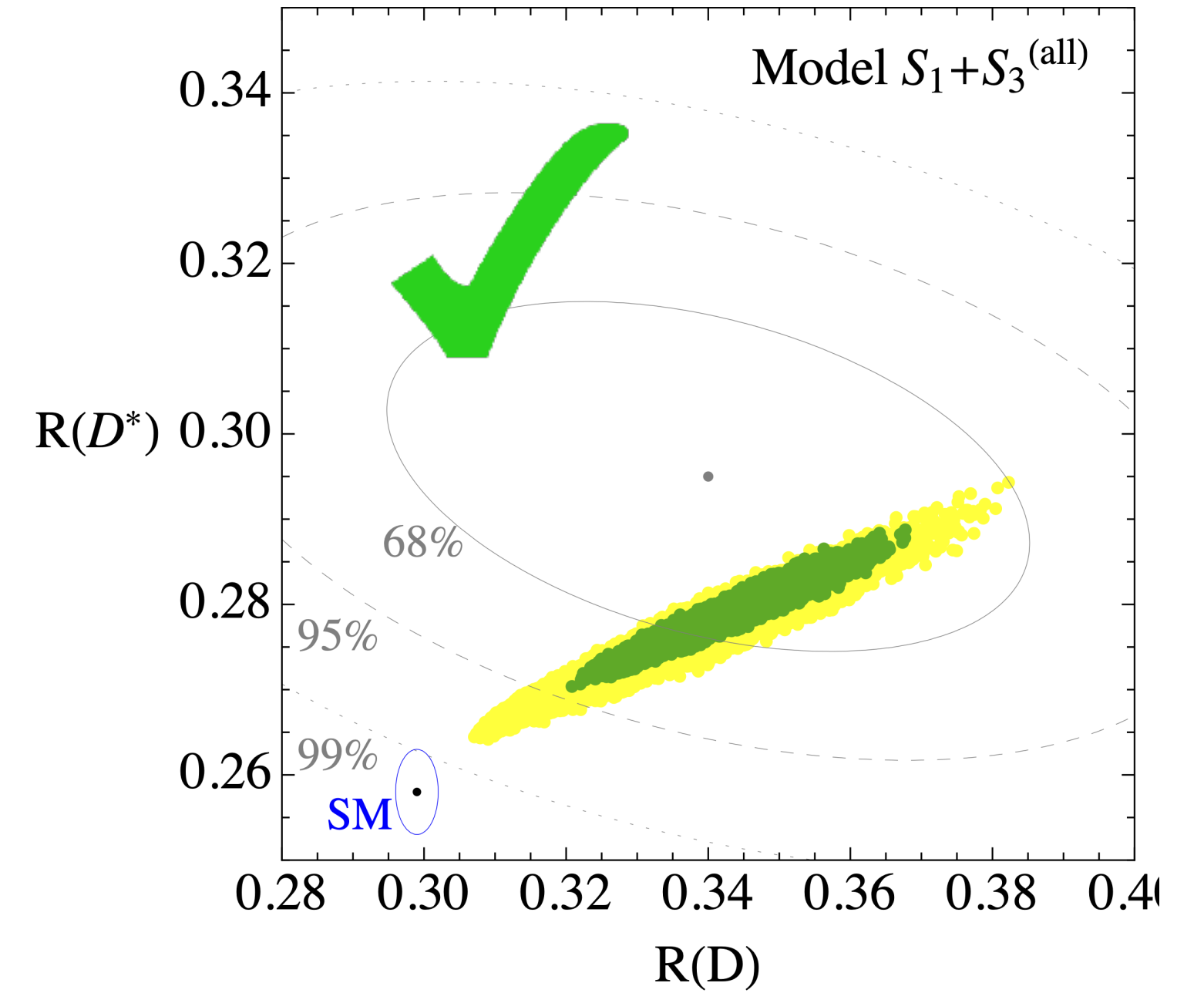
$$\lambda^{1R} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & c_e \\ 0 & t_\mu & t_e \end{pmatrix}$$

b → **s l l**



Very good fit of all anomalies!

R(D^(*))



A Fundamental Composite Higgs + LQ Model

Gauge group:

$$SU(N_{HC}) \times SU(3)_c \times SU(2)_w \times U(1)_Y$$

"HyperColor"

	$SU(N_{HC})$	$SU(3)_c$	$SU(2)_w$	$U(1)_Y$
Ψ_L	\mathbf{N}_{HC}	$\mathbf{1}$	$\mathbf{2}$	Y_L
Ψ_N	\mathbf{N}_{HC}	$\mathbf{1}$	$\mathbf{1}$	$Y_L + 1/2$
Ψ_E	\mathbf{N}_{HC}	$\mathbf{1}$	$\mathbf{1}$	$Y_L - 1/2$
Ψ_Q	\mathbf{N}_{HC}	$\mathbf{3}$	$\mathbf{2}$	$Y_L - 1/3$

[D.M. 1803.10972]

$SU(N_{HC})$ confines at $\Lambda_{HC} \sim 10 \text{ TeV}$ $\langle \bar{\Psi}_i \Psi_j \rangle = -B_0 f^2 \delta_{ij}$

$$G = SU(10)_L \times SU(10)_R \times U(1)_V \xrightarrow{f \sim 1 \text{ TeV}} H = SU(10)_V \times U(1)_V$$

H and LQ are close partners!!

Several states are present at the **TeV scale** as pNGB, including

Two Higgs doublets: $H_{SM}, \tilde{H}_2 \sim (\mathbf{1}, \mathbf{2})_{1/2}$

Singlet and Triplet LQ: $S_1 \sim (\mathbf{3}, \mathbf{1})_{-1/3} + S_1 \sim (\mathbf{3}, \mathbf{3})_{-1/3}$

$$H_1 \sim i\sigma^2 (\bar{\Psi}_L \Psi_N)$$

$$H_2 \sim (\bar{\Psi}_E \Psi_L)$$

$$S_1 \sim (\bar{\Psi}_Q \Psi_L)$$

$$S_3 \sim (\bar{\Psi}_Q \sigma^a \Psi_L)$$

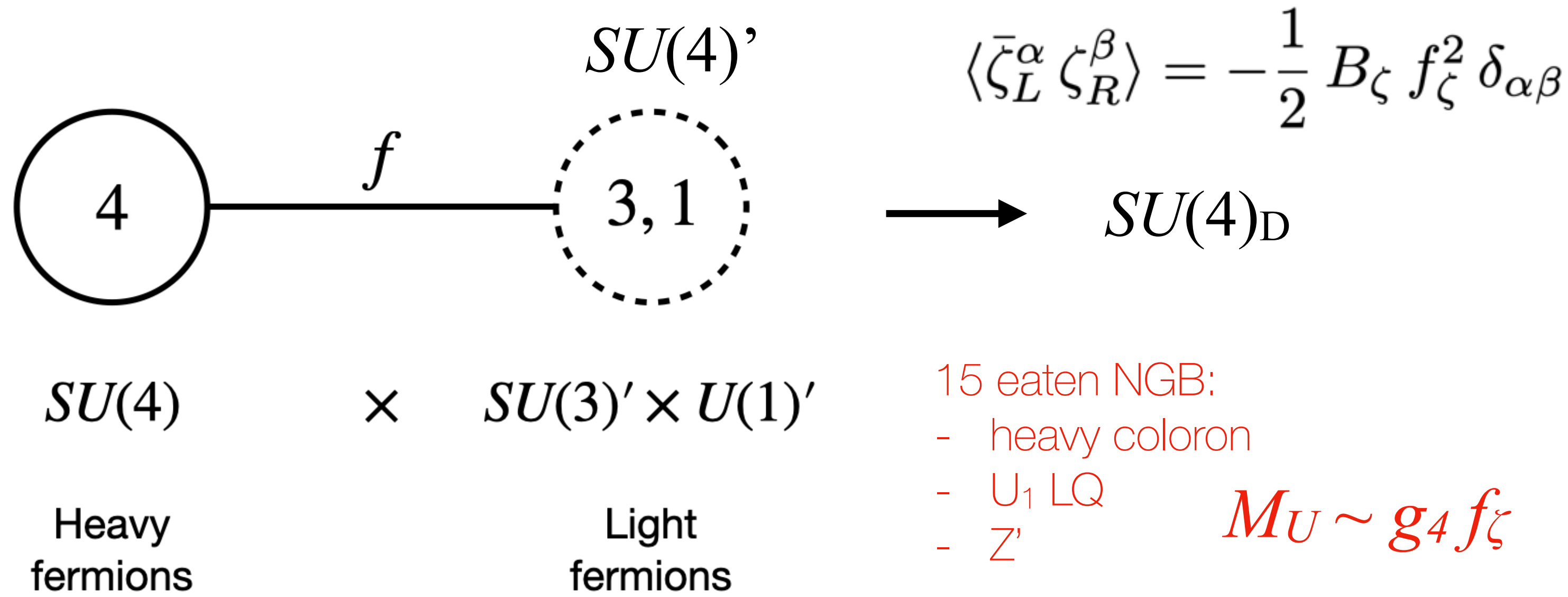
$$\mathcal{L}_{4\text{-Fermi}} \sim \frac{c_{\psi\Psi}}{\Lambda_t^2} \bar{\psi}_{SM} \psi_{SM} \bar{\Psi} \Psi \xrightarrow{E \lesssim \Lambda_{HC}} \sim y_{\psi\phi} \bar{\psi}_{SM} \psi_{SM} \phi + \dots$$

Yukawas &
LQ couplings

+ impose approximate $U(2)^5$ flavor symmetry

Composite Higgs + Vector LQ

[2004.11376]



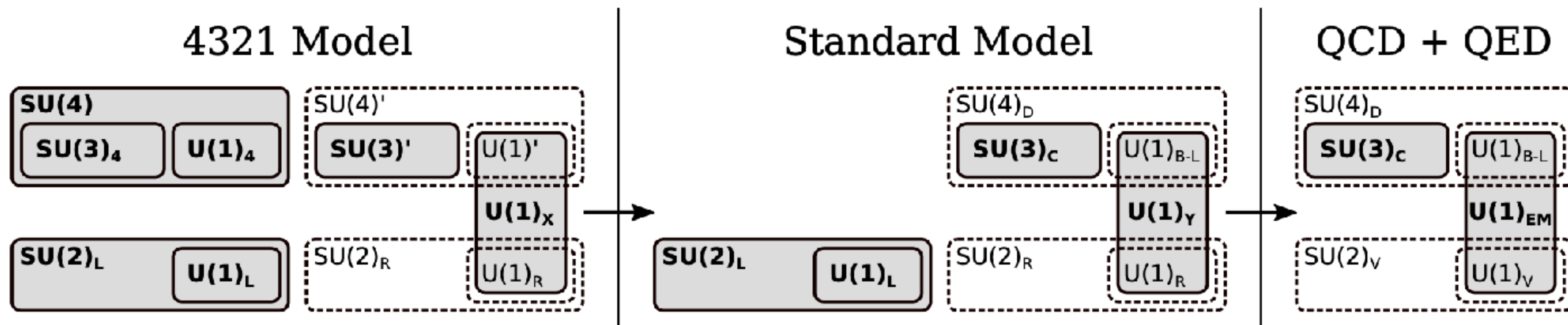
For the Composite Higgs part:

$$\langle \bar{\xi}_L^{ic} \xi_L^j \rangle = \langle \bar{\xi}_R^{ic} \xi_R^j \rangle = -\frac{1}{2} B_\xi f_\xi^2 \epsilon_{ij}$$

$$SU(4)_{EW} \times U(1)_A \rightarrow Sp(4)_{EW}$$

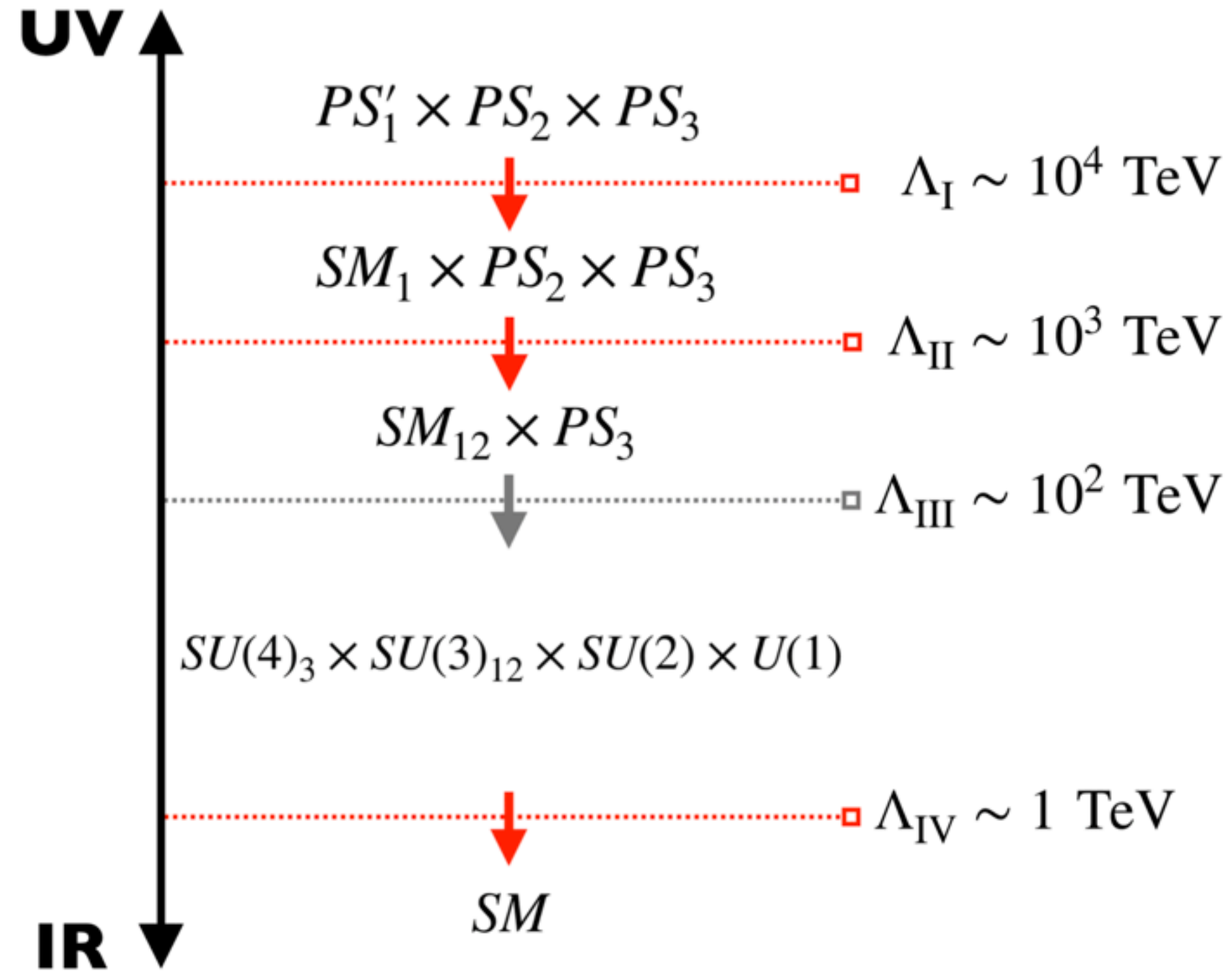
6 pNGB:

- Higgs doublet
- 2 singlets

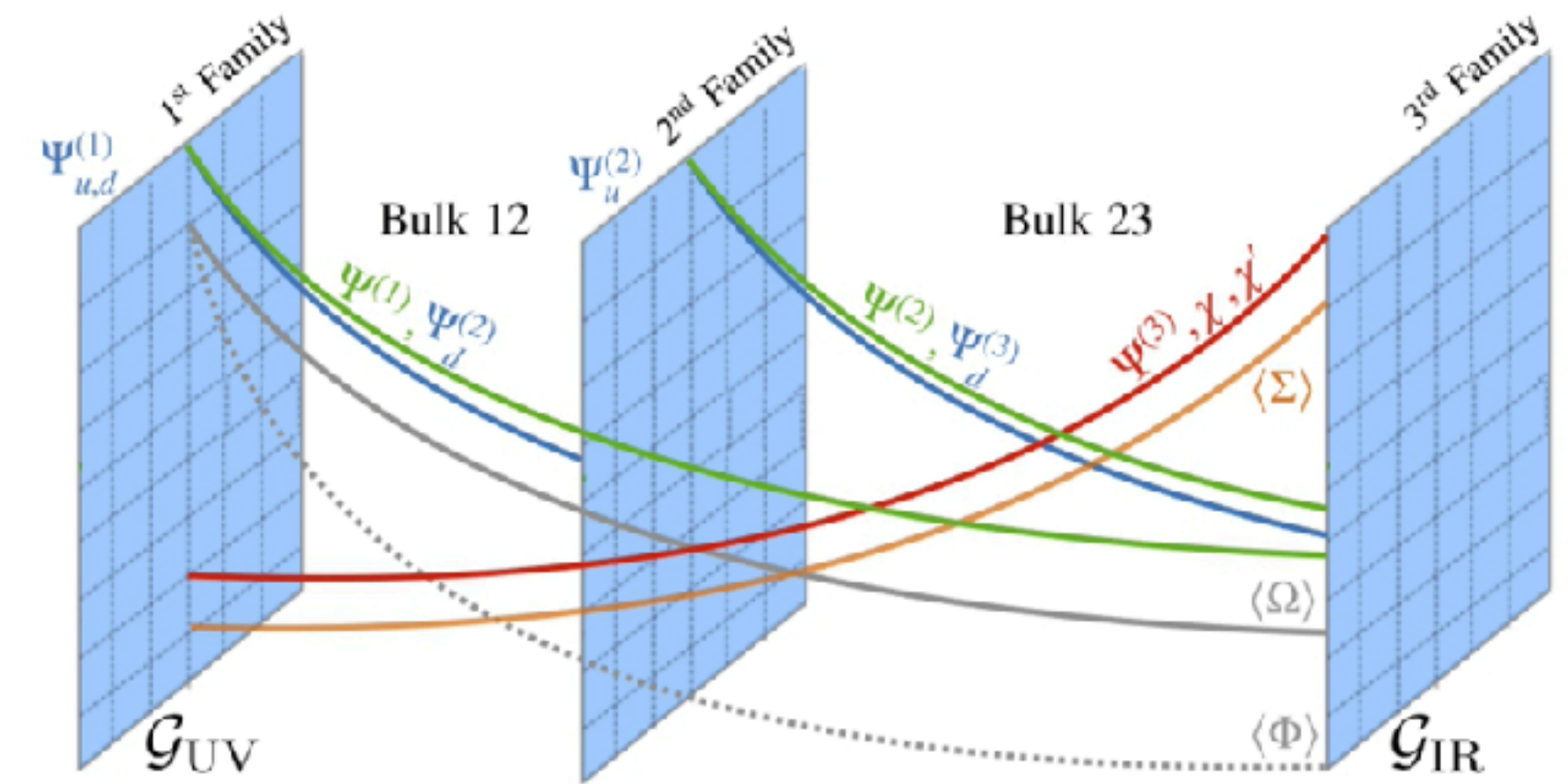


Vector leptoquark UV models

Bordone, Cornella, Fuentes-Martin, Isidori; 1712.01368



This picture can be embedded in a warped 5D compactification



Fuentes-Martin et al; 2203.01952

EW hierarchy problem can be addressed by adding a further Planck brane.

Flavour hierarchy \leftrightarrow Hierarchy of scales (RG stable)

Accidental approximate $U(2)^5$ at low energy!