



S. Di Noi

The SMEFT

4t operators in
 $h + j$

Preliminary
results

Outlook

RGESolver

Backup

Constraining SMEFT four-quark operators via Higgs+jet production at NLO

Higgs2022, Pisa

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Introduction

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- The Standard Model (SM) leaves several phenomena unexplained.
- None of the proposed theories beyond the SM (BSM) has empirical support (to date).
- The Standard Model Effective Field Theory (SMEFT) provides a powerful and pragmatic approach to the search for heavy new physics.





The Standard Model Effective Field Theory (SMEFT)

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- BSM effects are encoded in the coefficients of Lorentz and gauge-invariant higher-dimensional operators \mathcal{O}_i :

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{\mathcal{D}_i > 4} C_i \mathcal{O}_i = \mathcal{L}_{\text{SM}} + \sum_{\mathcal{D}_i > 4} \frac{C_i}{\Lambda^{\mathcal{D}_i - 4}} \mathcal{O}_i.$$

- The operators \mathcal{O}_i are built using only SM fields.
- The gauge group and the transformation properties of the fields are the same of the SM:

$$\text{SU}(3)_C \otimes \text{SU}(2)_W \otimes \text{U}(1)_Y.$$





The SMEFT at dimension-six level

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- At $\mathcal{D} = 6$ a complete basis of independent and gauge invariant operators (that preserve baryon and lepton number) is given by the **Warsaw basis** [Grzadkowski, Iskrzynski, Misiak, Rosiek, '10].
- 59 independent operators, 2499 when the flavour structure is considered.





Impact of SMEFT operators

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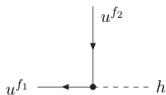
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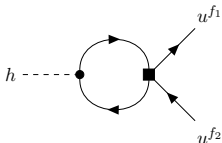
- Insertions of SMEFT operators change the interaction vertices with $\mathcal{O}(1/\Lambda^2)$ corrections

[Dedes, Materkowska, Paraskevas, Rosiek, Suxho, '17] .



$$-\frac{i}{v} \delta_{f_1 f_2} m_{u_{f_1}} - i v \delta_{f_1 f_2} C^{\varphi \square} m_{u_{f_1}} + \frac{i v}{4} \delta_{f_1 f_2} C^{\varphi D} m_{u_{f_1}} + \frac{i v^2}{\sqrt{2}} \left(P_L C_{f_2 f_1}^{u \varphi *} + P_R C_{f_1 f_2}^{u \varphi} \right)$$

- They also modify the running of SM parameters via loop effects [Jenkins, Manohar, Trott, '13].





Framework

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- We focus on 4 top operators.
- The Lagrangian at the heavy new physics scale Λ is:

$$\begin{aligned}\mathcal{L}_{\mathcal{D}=6} = & C_{tt}(\bar{t}_R\gamma^\mu t_R)(\bar{t}_R\gamma_\mu t_R) \\ & + C_{QQ1}(\bar{Q}_L\gamma^\mu Q_L)(\bar{Q}_L\gamma_\mu Q_L) \\ & + C_{QQ3}(\bar{Q}_L\gamma^\mu\tau^I Q_L)(\bar{Q}_L\gamma_\mu\tau^I Q_L) \\ & + C_{Qt1}(\bar{Q}_L\gamma^\mu Q_L)(\bar{t}_R\gamma_\mu t_R) \\ & + C_{Qt8}(\bar{Q}_L\gamma^\mu T^A Q_L)(\bar{t}_R\gamma_\mu T^A t_R).\end{aligned}$$

- We want to test their impact in the p_T distribution of the Higgs+jet production in a pp collider.





State-of-the-art

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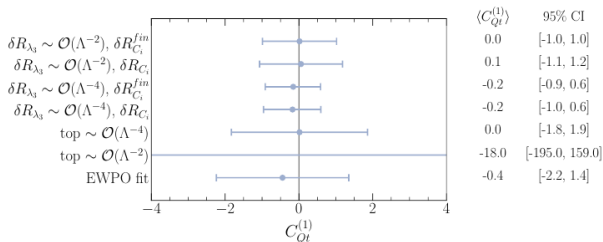
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- Indirect bounds from single Higgs production ([Alasfar,de Blas,Gröber,'22]) are competitive with the ones from top quark data ([Ethier et. al.,'21]) and from EWPO ([Dawson,Giardino,'22]).



[Alasfar,de Blas,Gröber,'22]

- Some operators can also be constrained from flavour observables ([Silvestrini,Valli,'18]).





Relevant partonic processes

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- An Higgs boson and a jet are produced via different partonic channels: $\bar{q}q \rightarrow gh$, $qg \rightarrow qh$, $\bar{q}g \rightarrow \bar{q}h$, $gg \rightarrow gh$.
- In this talk I will focus on quark-initiated channels.
- $qg \rightarrow qh$ and $\bar{q}g \rightarrow \bar{q}h$ can be obtained by crossing from $\bar{q}q \rightarrow gh$.
- The hadronic cross section is then obtained with:

$$\sigma_{\text{Had}}(pp \rightarrow hj) = \sum_X \int dx_1 dx_2 f(x_1) f(x_2) \sigma_{\text{Par}}(X \rightarrow hj).$$





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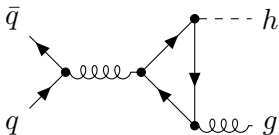
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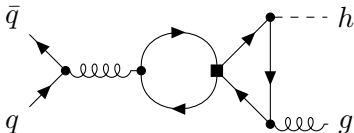
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- One of the diagrams contributing to the LO amplitude (2 in total).



- One of the diagrams contributing to the NLO amplitude (12 in total).

- We consider only the contribution of the top quark in the loops.





Computation of NLO matrix element

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- The computation is performed via a computer program, using:
 - `qgraf-3.4.2` to generate the amplitudes,
 - `FORM` to carry on the color and Dirac algebra,
 - `kira 1.2` to perform the IBP reduction.
- The result is cross-checked using `FeynArts` and `FIRE`.
- Currently, the cross-check has been performed for the operators \mathcal{O}_{tt} , \mathcal{O}_{QQ1} , \mathcal{O}_{QQ3} .





Renormalization

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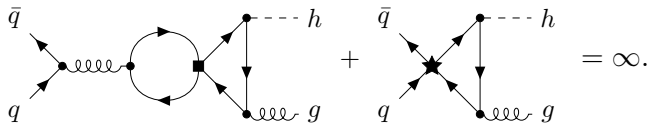
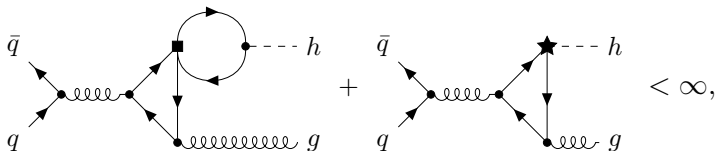
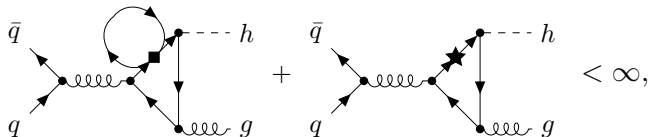
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- The 12 diagrams can be divided in 3 categories:





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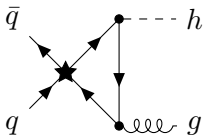
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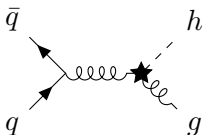
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- The counterterms from $(\bar{q}q\bar{t}t)$ operators don't remove all the divergencies.



- We found a 2 loop counterterm for the operator \mathcal{O}_{HG} :

$$\delta_{HG} = (C_{Qt8} - 6C_{Qt1}) \frac{g_s^2 m_t^2}{3(16\pi^2)^2 \epsilon v^2}.$$

- The same counterterm was found by J. Lang, G. Heinrich (see J.L.'s talk on Wednesday).





Phenomenological consequences of the 4 top operators

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- 4 top operators modify the Higgs + jet production via the NLO amplitude.
- $\neq 0$ 4 top operators at $\mu = \Lambda$ generate via operator mixing $\bar{q}q\bar{t}t$, ggh vertices at $\mu = \mu_{\text{Low}} = \frac{\sqrt{p_T^2 + m_h^2}}{2}$.
- Operator mixing generates also $C_{uH}^{3,3}(\mu_{\text{Low}}) \neq 0$, leading to a modification of the $h\bar{t}t$ vertex.

$$\mathcal{M}_{\text{TOT}} = \mathcal{M}_{\text{LO}} \left(1 + \underbrace{\Delta_{\mathcal{M}}}_{\mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)} \right) + \underbrace{\mathcal{M}_{\text{NLO}}}_{\mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)} + \underbrace{\mathcal{M}_{\bar{q}q\bar{t}t}}_{\mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)} + \underbrace{\mathcal{M}_{HG}}_{\mathcal{O}\left(\frac{v^2}{\Lambda^2}\right)}.$$

$$\mathcal{M}_{\bar{q}q\bar{t}t} =$$

$$i\mathcal{M}_{HG} =$$





Results

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- We implemented a FORTRAN program to perform the integration on the partonic momenta, using:
 - VEGAS to perform the Monte Carlo integration,
 - NNPDF30_1o_as_0118 set (accessed via LHAPDF-6.5.1).
- The running effects of the Wilson coefficients in SMEFT have been computed with a C++ program that uses RGESolver [S.D.N., Silvestrini,'22].
- The following plots have been obtained with:

$$C_X(\Lambda) = \frac{1}{\Lambda^2}, \quad \Lambda = 1 \text{ TeV} \quad (X = tt, QQ1, QQ3, Qt1, Qt8),$$

$$E_{\text{C.M.}} = 13 \text{ TeV.}$$





Transverse momentum distribution (preliminary)

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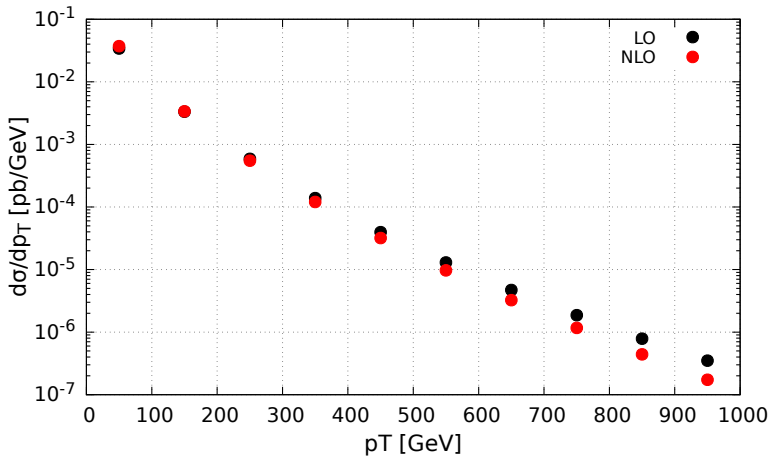
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Transverse momentum distribution (preliminary)

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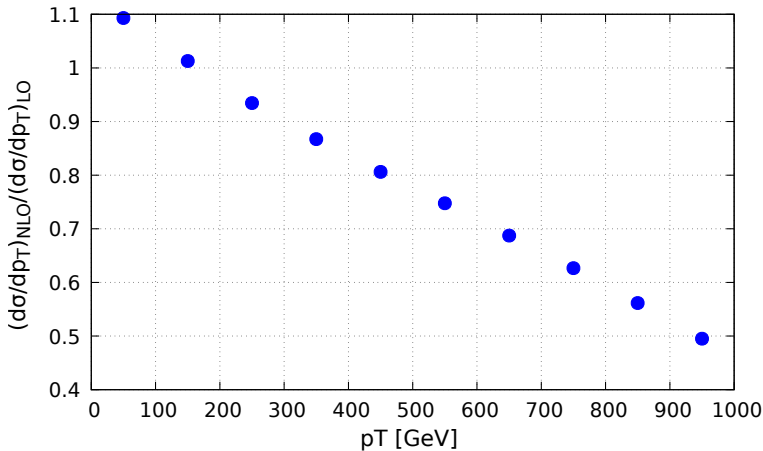
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Outlook

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- The next step will be completing the computation for the gluon fusion channel $gg \rightarrow gh$ (work in progress).
- Our plans are to perform a fit to put bounds on 4 top operators.





RGESolver

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- A C++ library that performs renormalization group evolution of SMEFT coefficients.
- General flavour structure (assuming lepton and baryon number conservation).
- Numerical and approximate (first leading log) solutions of the RGEs are available.
- Back-rotation effects can be included ([[Aebischer, Kumar, '20](#)]).
- High time efficiency.



- Authors:
 - Stefano Di Noi,
 - Luca Silvestrini.





Transformation properties of the SM fields

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Field	$(\mathbf{R}_C, \mathbf{R}_W)_y$	Field	$(\mathbf{R}_C, \mathbf{R}_W)_y$
q^p	$(\mathbf{3}, \mathbf{2})_{+\frac{1}{6}}$	H	$(\mathbf{1}, \mathbf{2})_{+\frac{1}{2}}$
l^p	$(\mathbf{1}, \mathbf{2})_{-\frac{1}{2}}$	G_μ^a	$(\mathbf{8}, \mathbf{1})_0$
u^p	$(\mathbf{3}, \mathbf{1})_{+\frac{2}{3}}$	W_μ^I	$(\mathbf{1}, \mathbf{3})_0$
d^p	$(\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}$	B_μ	$(\mathbf{1}, \mathbf{1})_0$
e^p	$(\mathbf{1}, \mathbf{1})_{-1}$		





The Warsaw Basis

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X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_{φ^6}	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\varphi^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$





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$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{tu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{td}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^j)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	Q_{qqq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^m)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

