

Outline of the four lectures

- 1 {
- Introduction to flavour; concept of lepton flavour universality (LFU) and theory description of rare transitions of the type $b \rightarrow s\ell^+\ell^-$ (Gim. Isidori)

- 2 {
- Why b physics and why it is interesting
 - The CKM Matrix
 - Neutral meson oscillations
 - The main experiments in the field (discussing their benefits and possible shortcomings)
 - Selected results on rare decays:
 - Leptonic ($B_{(s)} \rightarrow \mu^+\mu^-$)
 - Semileptonic ($b \rightarrow s\ell^+\ell^-$) (branching fractions and angular distributions)
- "Anomalies"

- 3 {
- Tests of LFU
 - in neutral-current mediated $b \rightarrow s\ell^+\ell^-$ transitions
 - in charged current mediated $b \rightarrow c\tau\nu$ transitions
 - Search for LFV processes

- 4 {
- Theoretical interpretation of the recent anomalies in semileptonic B decays in terms of physics beyond the Standard Model (Gim. Isidori)

Latest $B_{(s)} \rightarrow \mu^+ \mu^-$ combination

LHCb-CONF-2020-002
CMS PAS BPH-20-003
ATLAS-CONF-2020-049

- **LHCb**, PRL 118 (2017) 191801

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6_{-0.2}^{+0.3}) \times 10^{-9} \quad 7.8\sigma$$

$$B(B^0 \rightarrow \mu^+ \mu^-) < 3.4 \times 10^{-10} \text{ @ 95 \% CL}$$

- **CMS**, JHEP 04 (2020) 188

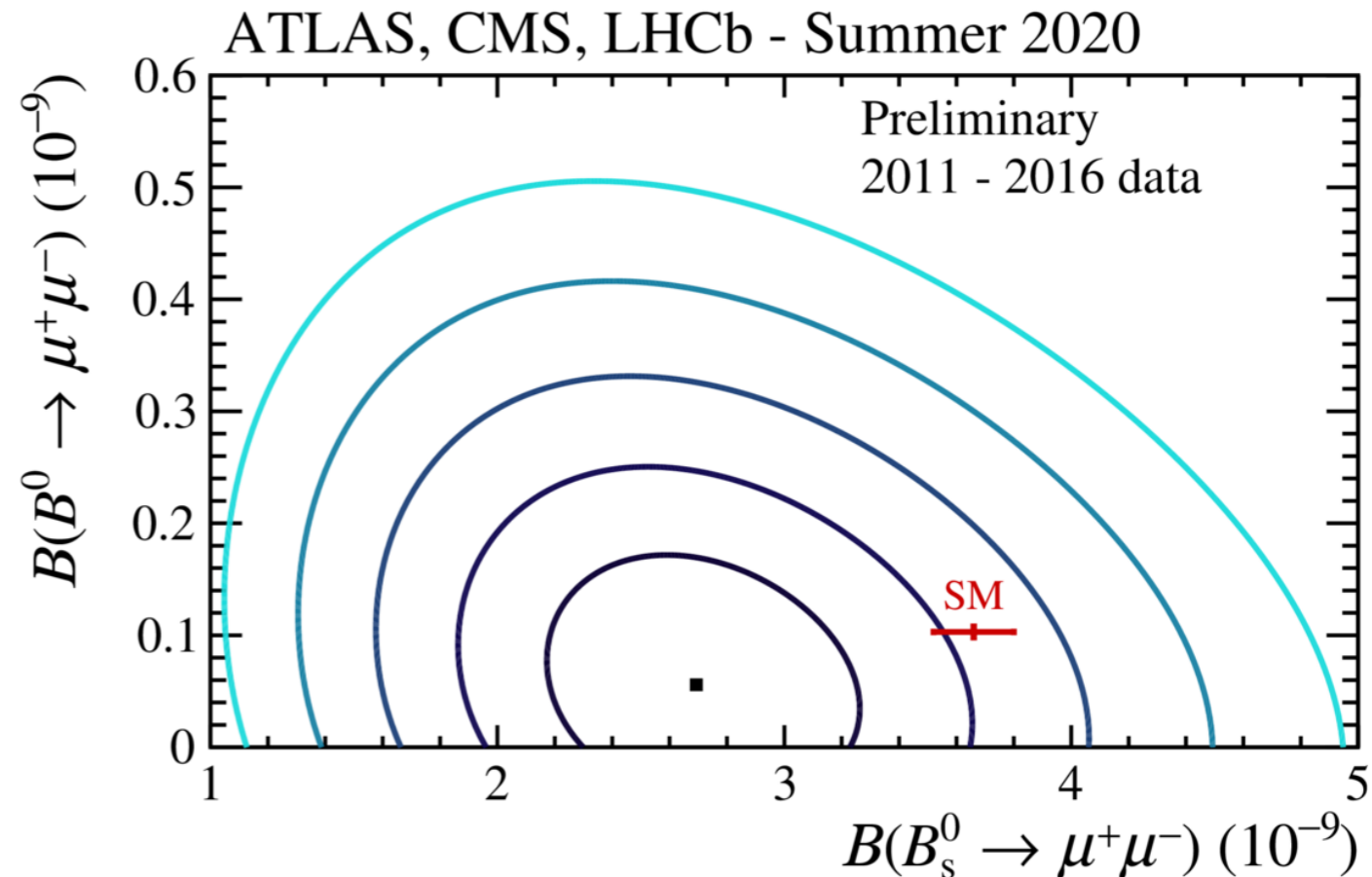
$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.9 \pm 0.7 (\text{exp}) \pm 0.2 (\text{frag})) \times 10^{-9} \quad 5.6\sigma$$

$$B(B^0 \rightarrow \mu^+ \mu^-) < 3.6 \times 10^{-10} \text{ @ 95 \% CL}$$

- **ATLAS**, JHEP 04 (2019) 098

$$B(B_s^0 \rightarrow \mu^+ \mu^-) = (2.8_{-0.7}^{+0.8}) \times 10^{-9} \quad 4.6\sigma$$

$$B(B^0 \rightarrow \mu^+ \mu^-) < 2.1 \times 10^{-10} \text{ @ 95 \% CL}$$



Era of precision measurements of $B_{(s)} \rightarrow \mu^+ \mu^-$ has started

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (2.69_{-0.35}^{+0.37}) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 1.9 \times 10^{-10} \text{ @ 95 \% CL}$$

2.1 σ below SM
prediction (2D
compatibility)

Question on $B_{(s)}^0 \rightarrow \tau^+ \tau^-$

- Interesting for NP coupled dominantly to third generation
- In the SM, larger BF due to larger τ mass (less helicity suppressed : m_τ^2/m_B^2)

$$\mathcal{B}(B_s^0 \rightarrow \tau^+ \tau^-) = (7.73 \pm 0.49) \times 10^{-7}$$

Bobeth et al.

$$\mathcal{B}(B^0 \rightarrow \tau^+ \tau^-) = (2.22 \pm 0.19) \times 10^{-8}$$

PRL 112 (2014) 101801

- Experimentally challenging due to undetected neutrinos in final state
- Searched by LHCb through the decay $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau$
- $B_{s,d}$ unresolvable in mass \rightarrow analysis optimised for B_s
- Limits set (Run1 data):

PRL 118 (2017) 251802

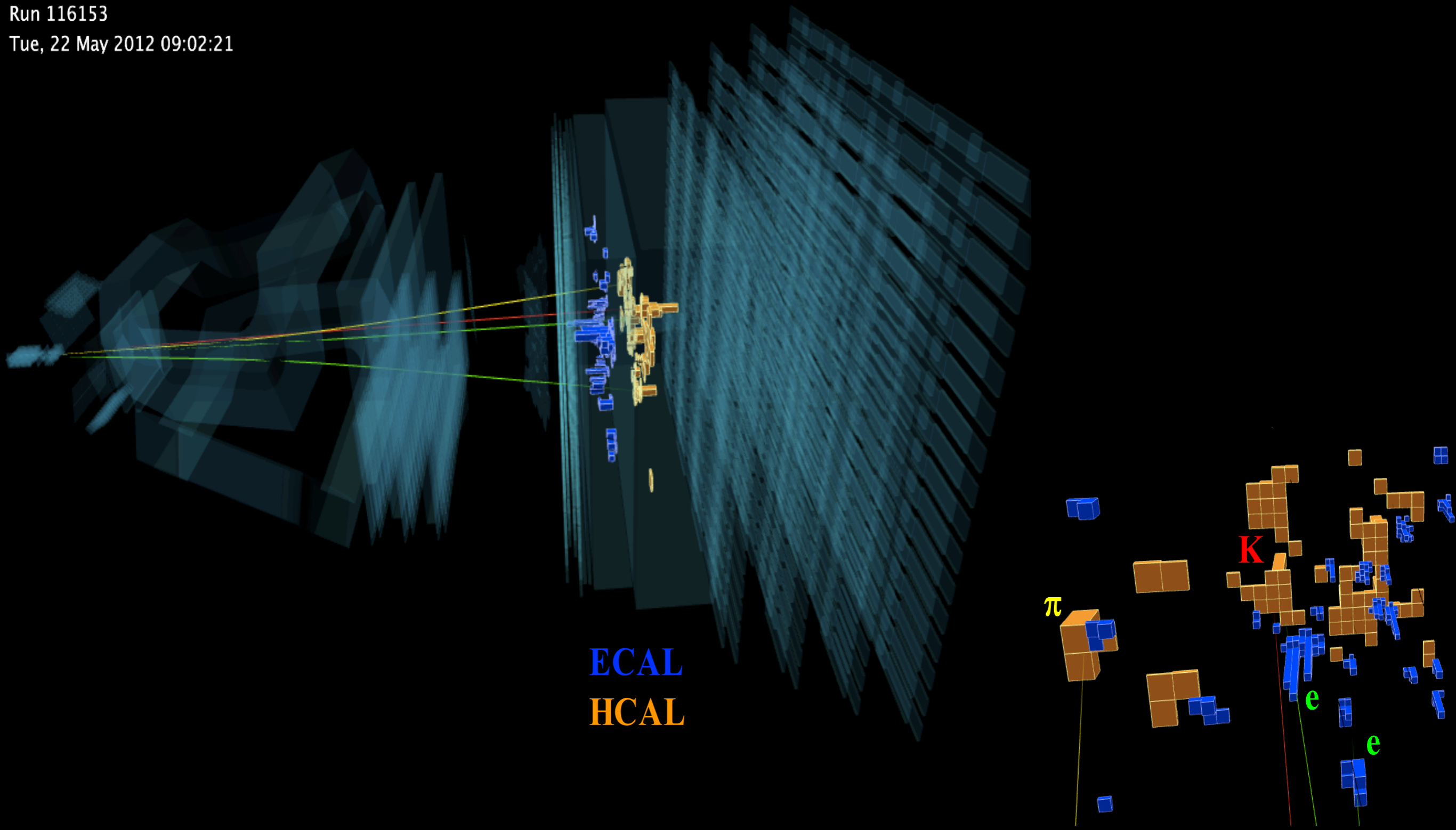
$$\mathcal{B}(B_s \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3} \text{ at 95\% C.L.} \quad \rightarrow \text{first direct limit}$$

$$\mathcal{B}(B_d \rightarrow \tau^+ \tau^-) < 2.1 \times 10^{-3} \text{ at 95\% C.L.} \quad \rightarrow \text{best limit}$$



$b \rightarrow s \ell^+ \ell^-$ decays

Event 27196644
Run 116153
Tue, 22 May 2012 09:02:21



Other interesting rare decays:

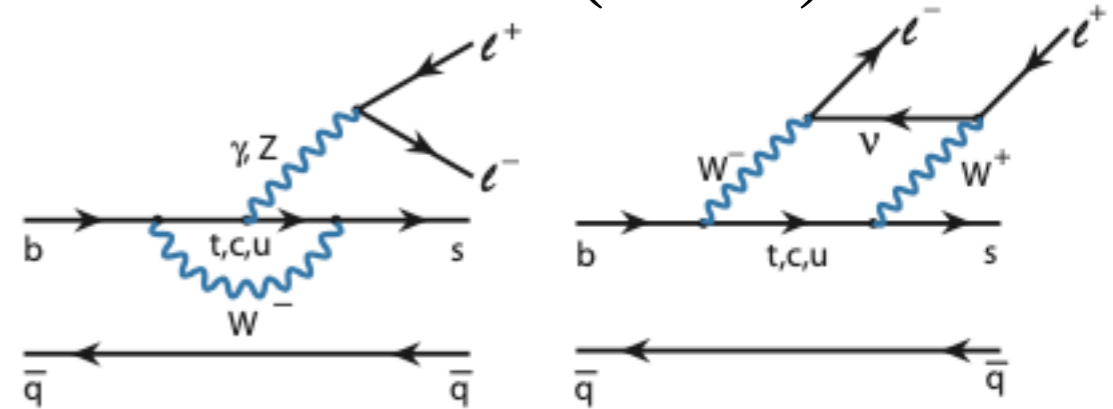
$$B \rightarrow H_s \mu^+ \mu^- \text{ with } H_s = K, K^*, \phi \dots$$

- Same loop diagrams, different spectator quarks
- Branching fractions (BFs) and angular distributions sensitive to NP
- A lot of phenomenological work invested in defining “clean” observables with reduced theoretical uncertainties
 - Form-factors cancel at leading order
 - E.g: are we estimating correctly contributions from charm loops that produce a $\ell^+ \ell^-$ pair via a virtual photon?

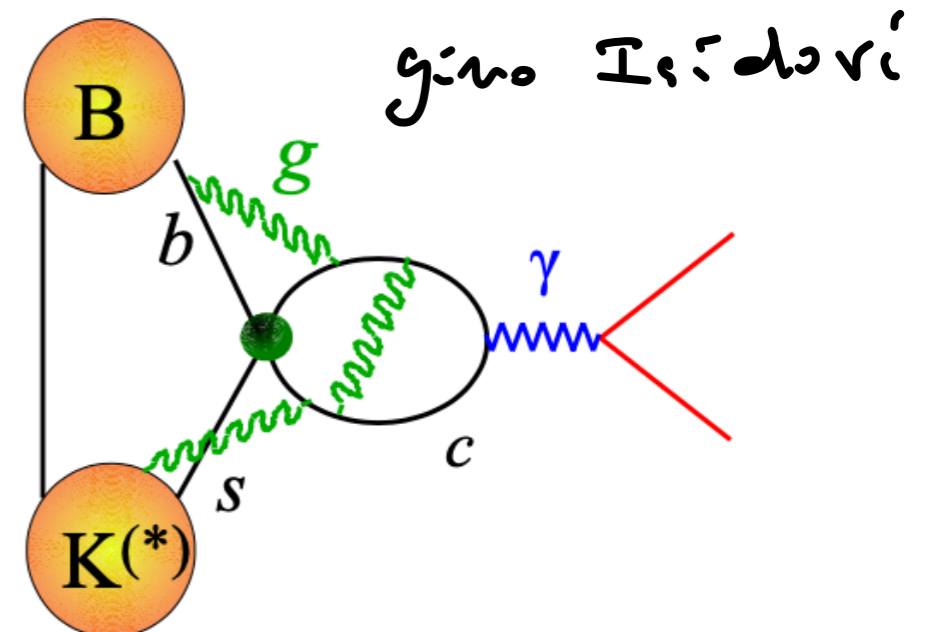
• Question: how clean?

- These theory uncertainties affect BFs and angular distributions in $B \rightarrow H_s \ell^+ \ell^-$, but *NOT* LFU ratios (clean) or $B_{(s)} \rightarrow \mu^+ \mu^-$ (clean)

$$\text{BF} \sim \mathcal{O}(10^{-7})$$



Irreducible theory error due to long distance effects, particularly large close to $c\bar{c}$ resonances

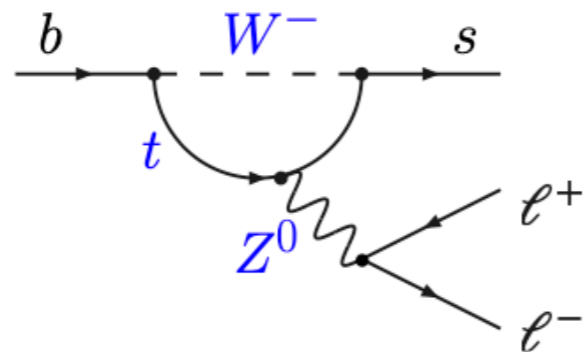


Effective Lagrangian for $b \rightarrow s \ell^+ \ell^-$ transitions

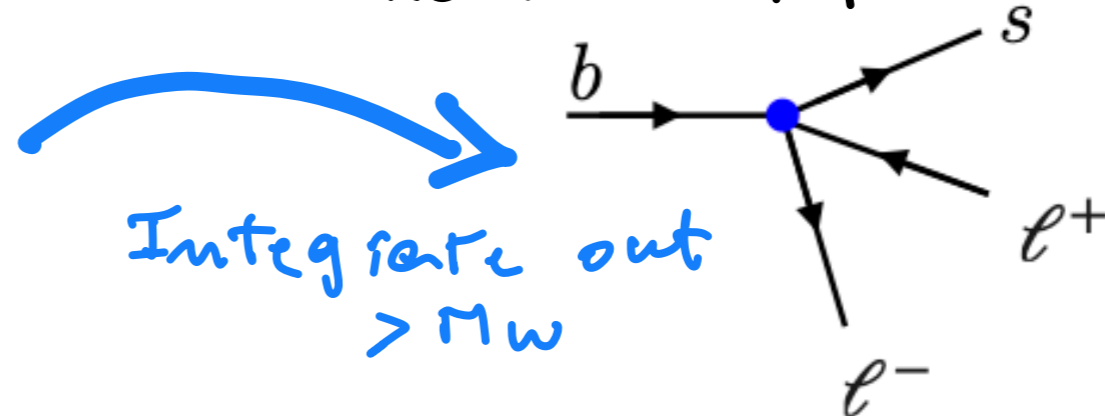
gino Isidori

- To describe these processes within the SM and beyond, construct an effective Lagrangian at the EW scale integrating out all the heavy fields (W, Z, top)

Full theory (SM)



Effective Fermi 4-fermion interaction



- $\mathcal{L}_{\text{eff}} \sim \sum_i C_i(M_W) O_i$
 \uparrow Wilson coefficients
- Four-fermion interaction described by effective couplings $C_i = C_i^{\text{SM}} + C_i^{\text{NP}}$
- The interesting short-distance information (sensitive to NP) is encoded in the Wilson coefficients C_i (especially C_9 and C_{10})

FCNC OPERATORS

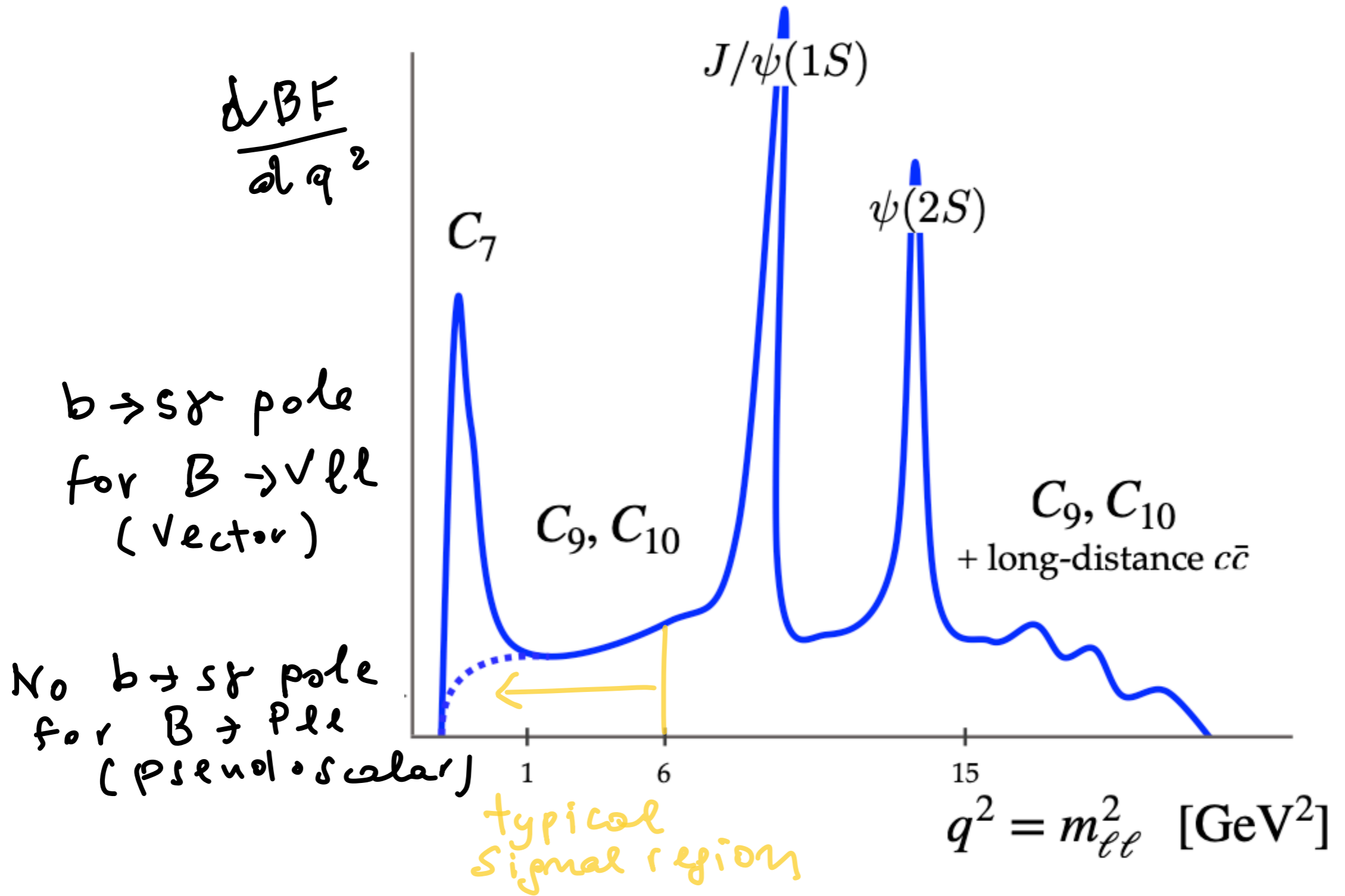
$$O_{10}^{\ell} = (\bar{s}_L \gamma_{\mu} b_L) (\bar{\ell} \gamma^{\mu} \gamma_5 \ell)$$

$$O_9^{\ell} = (\bar{s}_L \gamma_{\mu} b_L) (\bar{\ell} \gamma^{\mu} \ell)$$

$$Q_7 = m_b (\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu}$$

Z penguin & box
 γ and Z penguin
 γ penguin

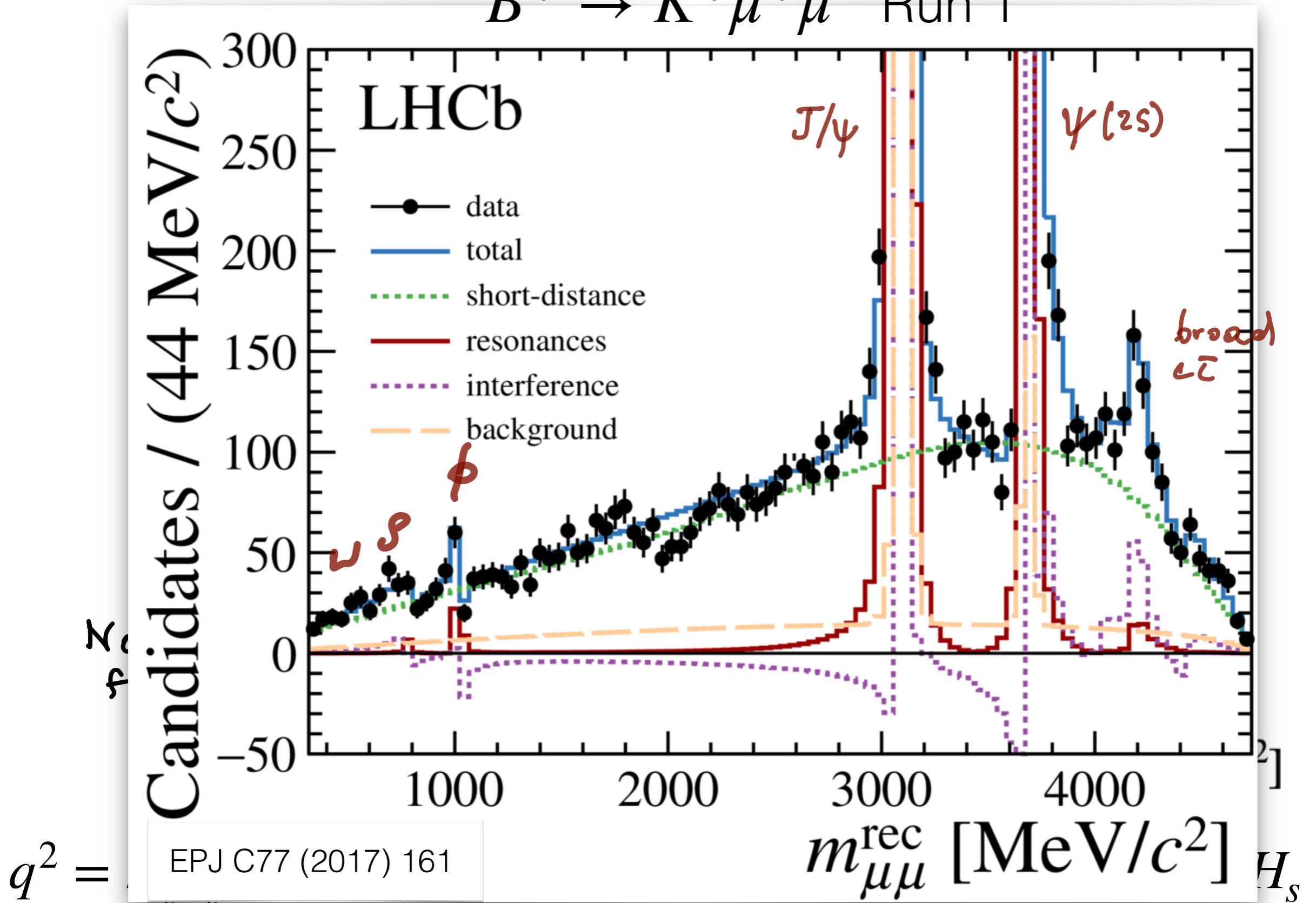
q^2 spectrum of $b \rightarrow s \ell^+ \ell^-$ decays



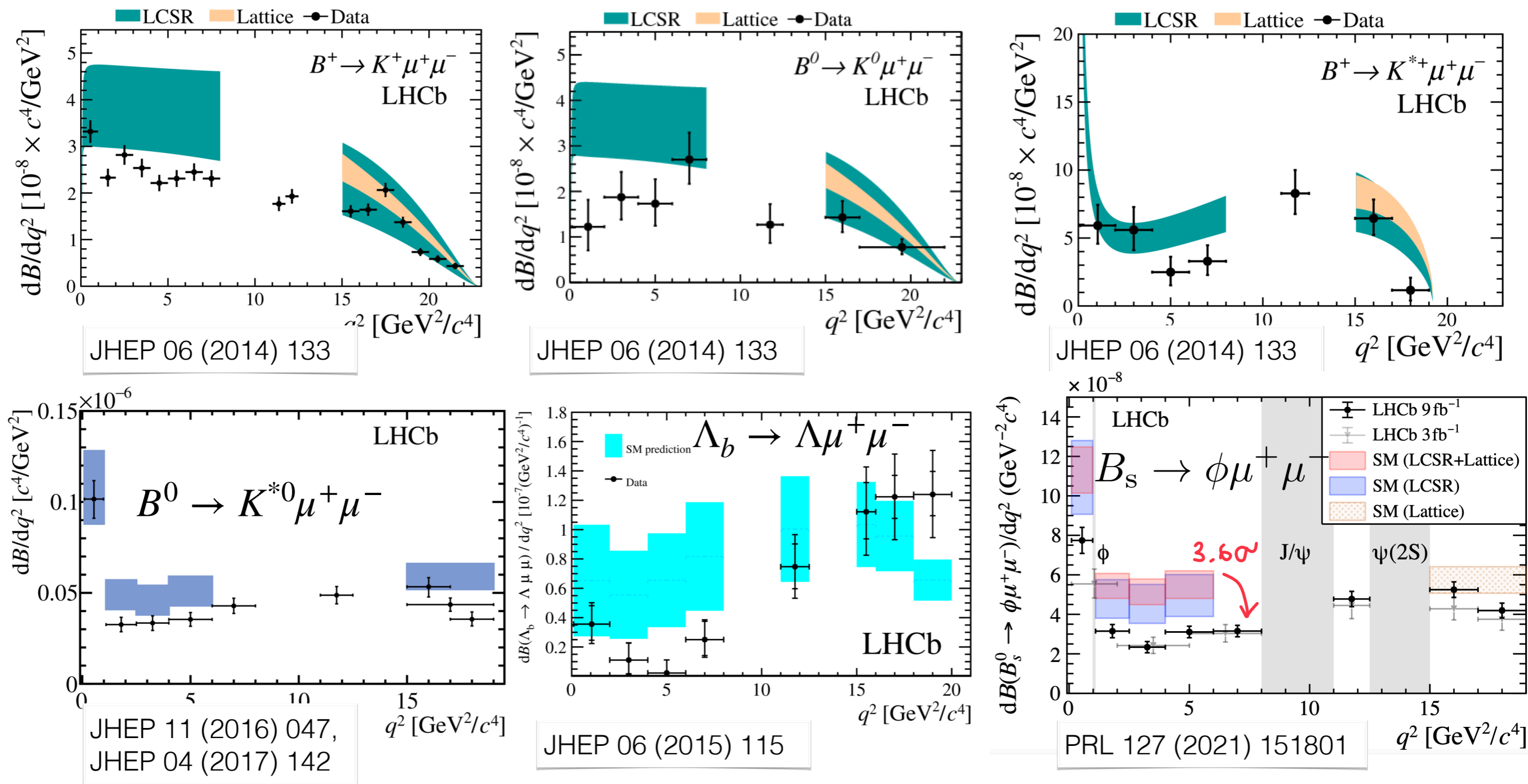
$q^2 = m_{\ell^+ \ell^-}^2$ four-momentum transfer squared between B and H_s

q^2 spectrum of $b \rightarrow s \ell^+ \ell^-$ decays

$$B^+ \rightarrow K^+ \mu^+ \mu^- \text{ Run 1}$$



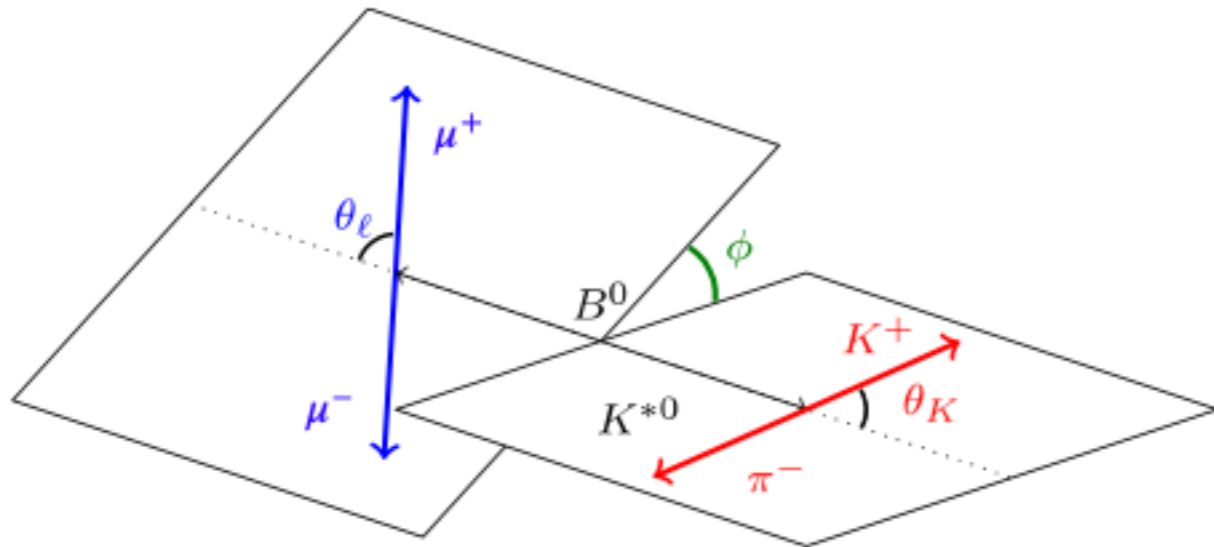
BF of semileptonic $b \rightarrow s \mu^+ \mu^-$



- In general, data tend to be lower than theory predictions at low q^2 (but uncertainties on the theory could be correlated among different modes)

Angular distributions in $B \rightarrow K^* \mu^+ \mu^-$

- $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ with $K^{*0} \rightarrow K^+ \pi^-$
- Decay rate fully described in terms of $\Omega = (\cos \theta_\ell, \cos \theta_K, \phi)$, $q^2 = m_{\mu^+ \mu^-}^2$



$$\frac{d^4\Gamma[\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_i I_i(q^2) f_i(\vec{\Omega})$$

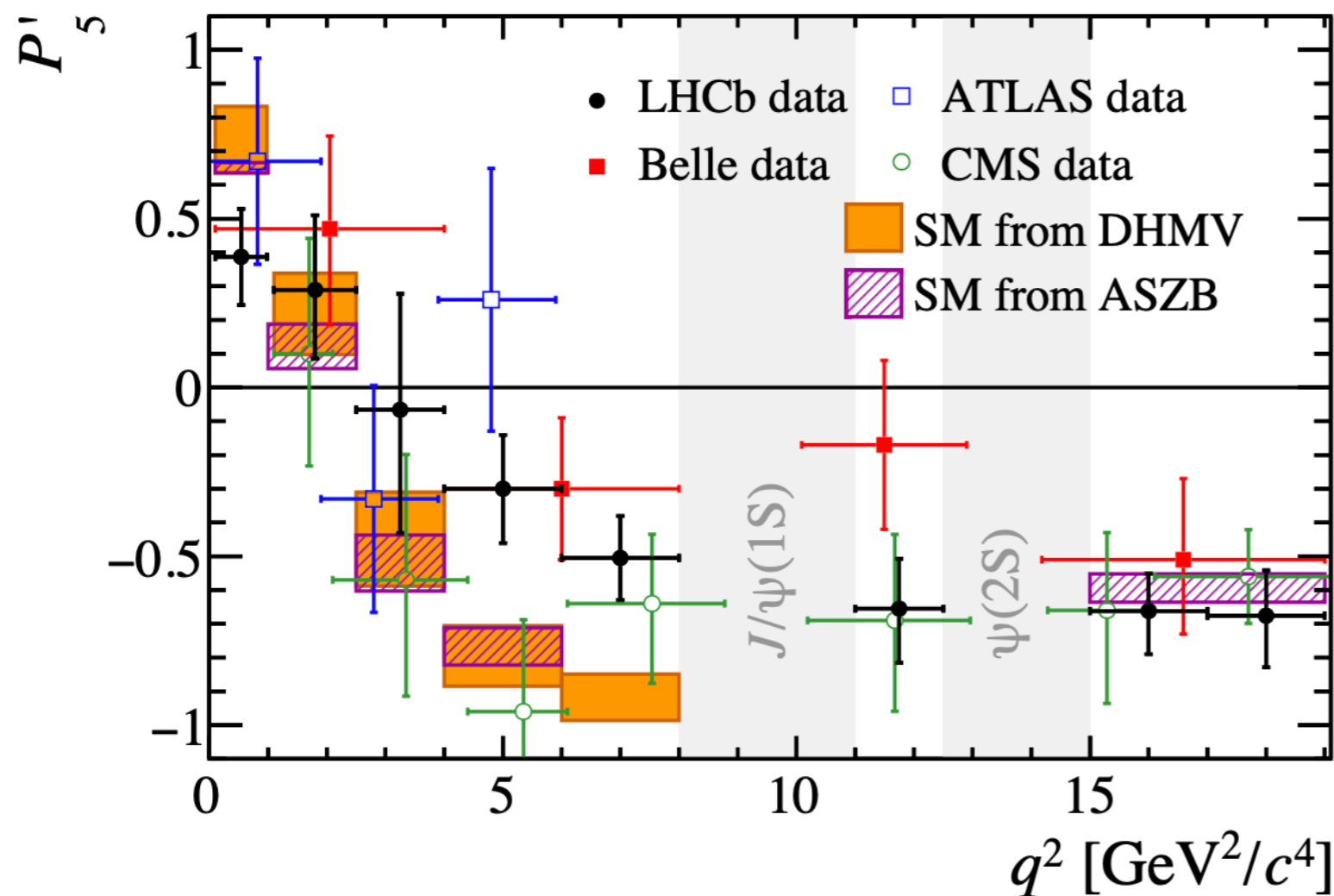
angular coefficients

angular functions

combination of different K^{*0} amplitudes that depend on Wilson coefficients and form factors

$B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ angular analysis (old LHCb result with 3/fb)

- LHCb observed a tension in the “optimised variable” P'_5 , not exactly intuitive, but constructed from ratios of angular observables to be robust from ‘form-factor uncertainties’
- However, inconclusive when adding ATLAS, CMS and Belle



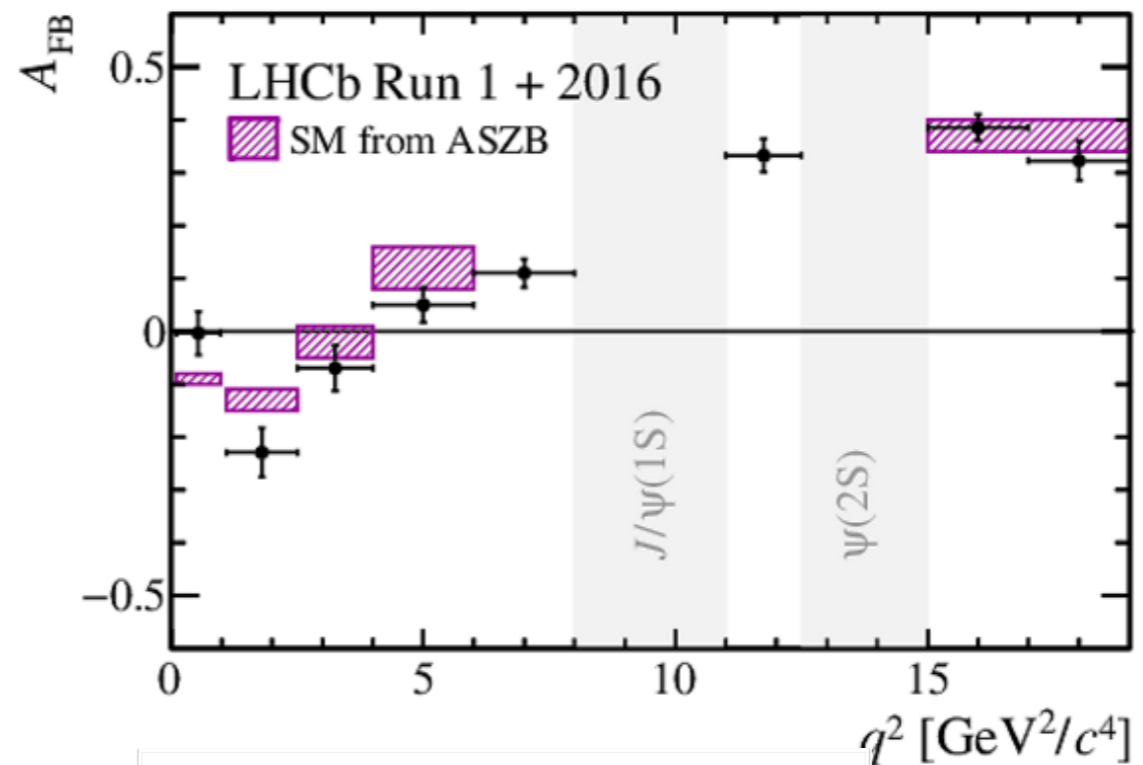
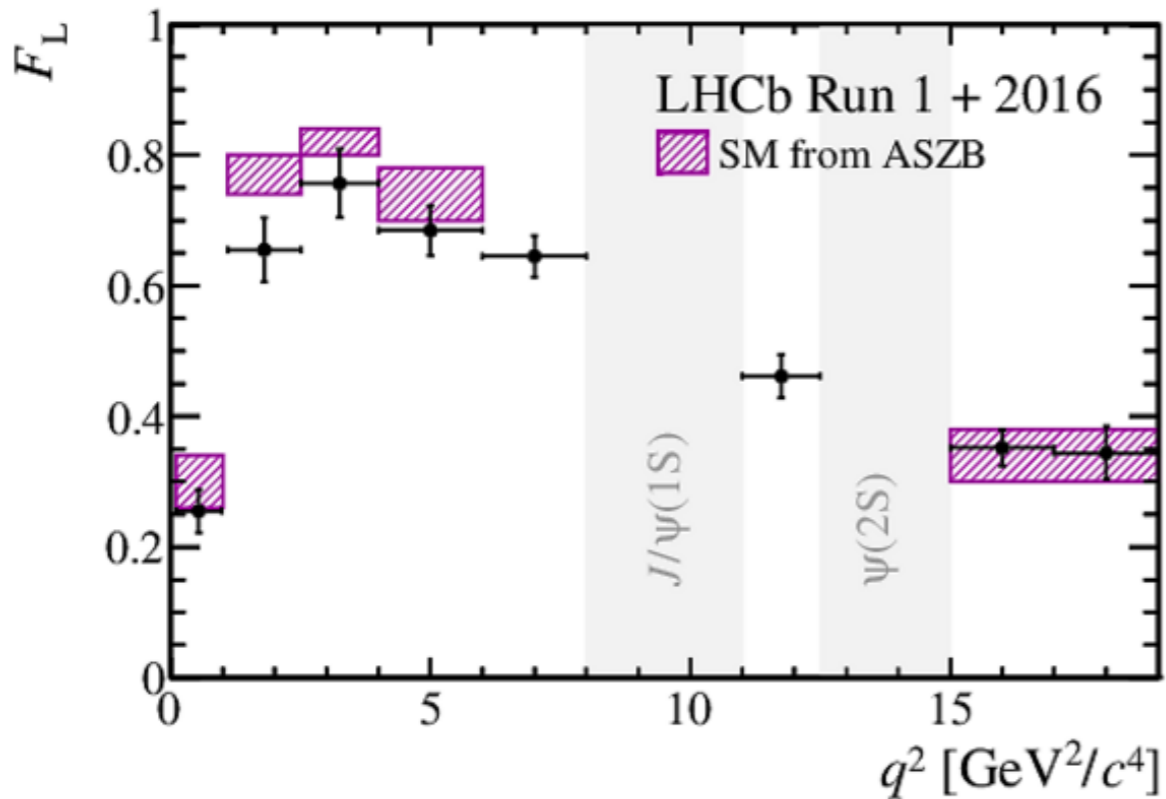
LHCb: JHEP 02 (2016) 104
 Belle: PRL 118 (2017) 111801
 ATLAS: JHEP 10 (2018) 047
 CMS: PLB 781 (2018) 517541

$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}, \text{ with } F_L \text{ and } S_5$$

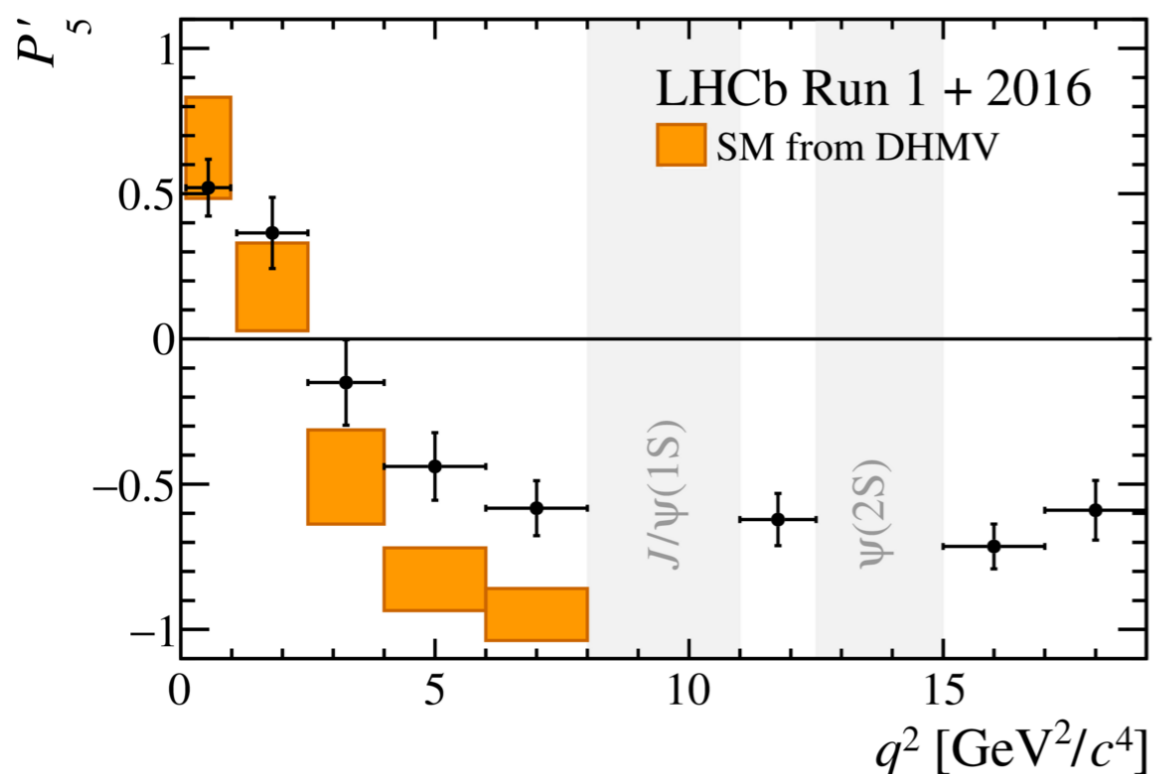
combinations of K^{*0} spin amplitudes dependent on Wilson coefficients and form factors

$B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$ angular analysis

- LHCb update based on 4.7/fb (~doubling the number of B^0 to ~4600 events)



PRL 125 (2020) 011802



- P'_5 : local tension of 2.5σ and 2.9σ in q^2 bins of $[4.0, 6.0]$ and $[6.0, 8.0]$ GeV^2
- Global fit to angular observables finds a deviation of 3.3σ (shift wrt SM value of C_9)
- Consistent with previous result

TESTS OF LEPTON

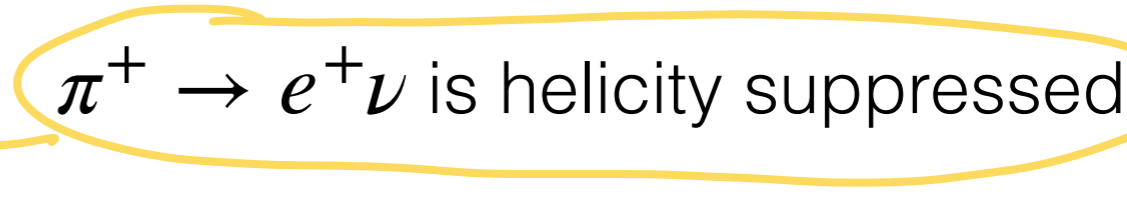
FLAVOUR

UNIVERSALITY

Lepton Flavour Universality

- The property that the three charged leptons (e , μ , τ) couple in a universal way to the SM gauge bosons
- In the SM the only flavour non-universal terms are the three lepton masses:
 $m_\tau, m_\mu, m_e \leftrightarrow 3477 / 207 / 1$ (boring!)
- Turn this “boring” property into a powerful tool to discover physics beyond the SM
- The SM quantum numbers of the three families could be an “accidental” low-energy property: the different families may well have a very different behaviour at high energies, as signalled by their different masses
- If NP couples in a non-universal way to the three lepton families, then we can discover it by comparing classes of rare decays involving different lepton pairs (e.g. e/μ or μ/τ)
- Test LFU in $b \rightarrow s \ell^+ \ell^-$ transitions, i.e. flavour-changing neutral currents with amplitudes involving loop diagrams

Precise tests of LFU in π decays

- Ratio of BFs $R_{e/\mu} = \frac{\Gamma(\pi^+ \rightarrow e^+\nu(\gamma))}{\Gamma(\pi^+ \rightarrow \mu^+\nu(\gamma))}$ provides the best test of electron–muon universality in charged-current weak interactions


$\pi^+ \rightarrow e^+\nu$ is helicity suppressed
- $R_{e/\mu}(\text{SM}) = 1.23524(15) \times 10^{-4}$, one of the most precisely calculated weak interaction observable involving quarks
- $R_{e/\mu}(\text{exp}) = 1.2327(23) \times 10^{-4}$ Very accurate test!
(New experiment PIONEER at PSI approved to improve the experimental accuracy by factor 15)

The family of R ratios

- Comparing the rates of $B \rightarrow H e^+ e^-$ and $B \rightarrow H \mu^+ \mu^-$ allows precise testing of lepton flavour universality

$$R_H [q_{\min}^2, q_{\max}^2] = \frac{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\Gamma(B \rightarrow H \mu^+ \mu^-)}{dq^2}}{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\Gamma(B \rightarrow H e^+ e^-)}{dq^2}}, \quad q^2 = m^2(\ell\ell)$$

$B: B^+, B^0, B_s^0, \Lambda_b^0$

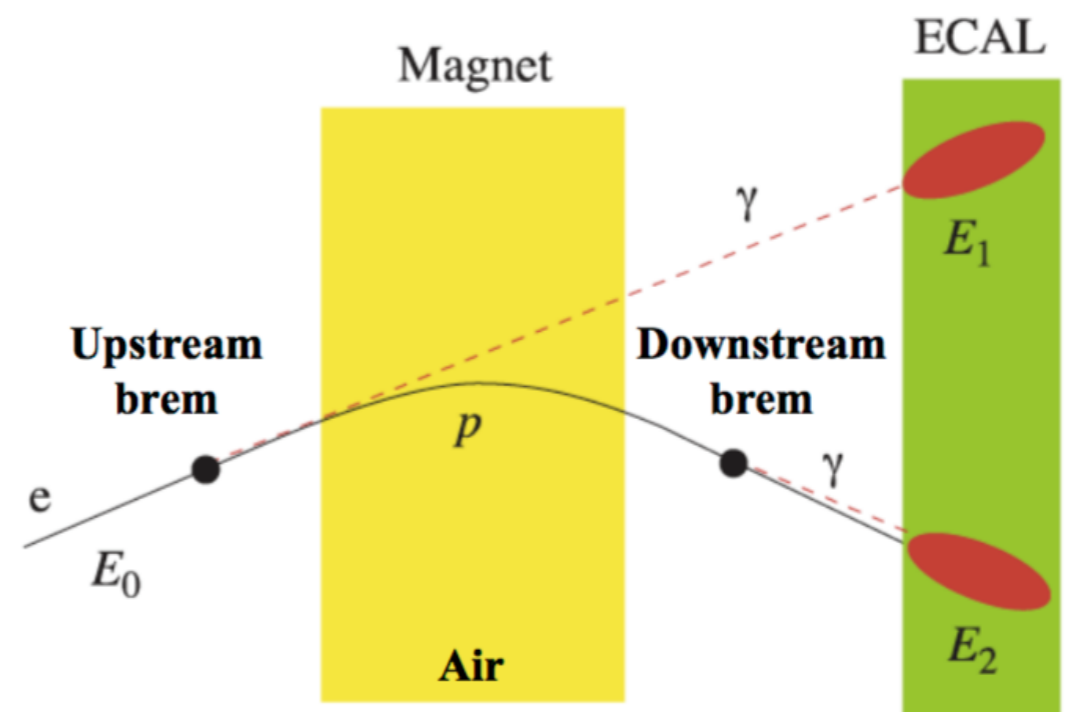
- These ratios are clean probes of NP : $H: K^+, K^{*0}, pK, \phi \dots$
 - Sensitive to possible new interactions that couple in a non-universal way to electrons and muons
 - Small theoretical uncertainties because hadronic uncertainties cancel : $R_H = 1$ in SM, neglecting lepton masses, with QED corrections at $\sim\%$ level (when physical observables defined with LHCb choice of cuts on q^2 and on the reconstructed B mass, see Bordone, Isidori, Pattori)

Lepton identification is anything but universal!

- High occupancy in calorimeters → trigger thresholds are higher for electrons (~ 2.5 to 3.0 GeV) than for muons (~ 1.5 to 1.8 GeV)
- Electrons emit a large amount of bremsstrahlung, degrading momentum and mass resolution. Two situations :

- **Downstream brem** (wrt dipole bending magnet) Photon energy in the same calorimeter cell as the electron and momentum correctly measured
- **Upstream of the magnet** Photon energy in different calorimeter cells than electron and momentum evaluated after bremsstrahlung

JHEP 08 (2017) 055



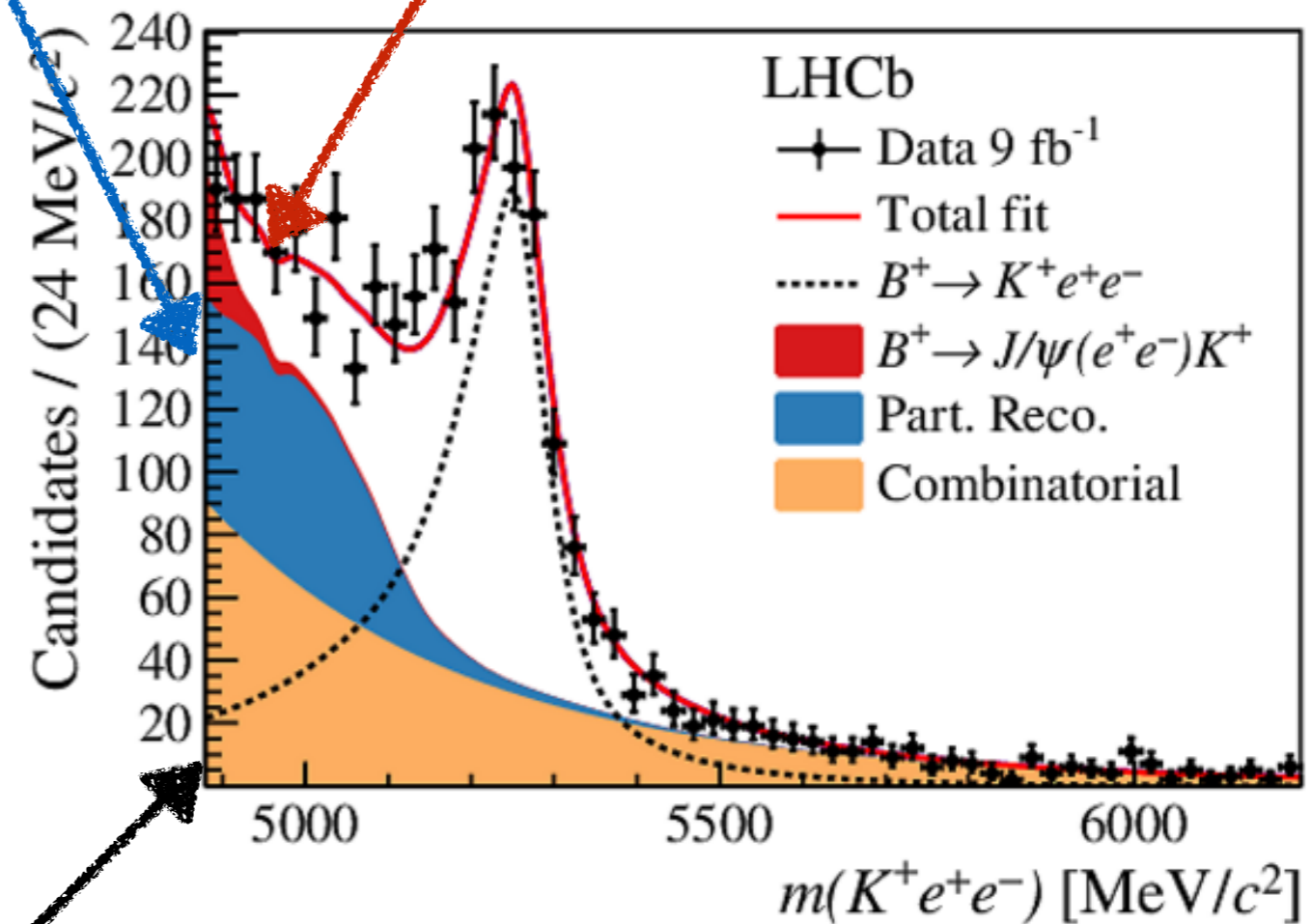
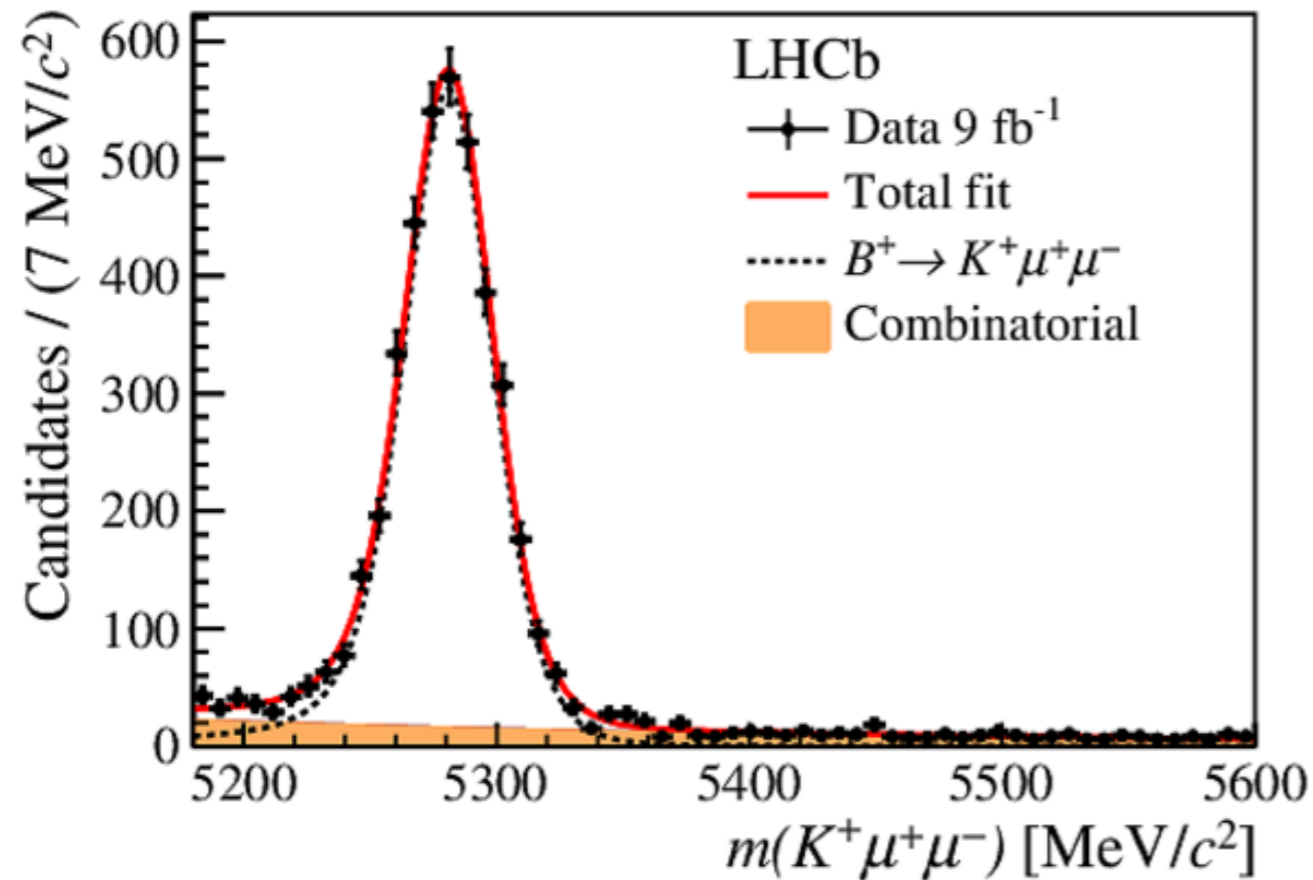
→ Look for photon clusters compatible with electron direction before magnet and “add” the cluster energy back to the electron momentum (if $E_T > 75\text{MeV}$)

muons vs electrons

- Even after Bremsstrahlung recovery di-electron pair and B meson still have degraded mass resolution

Partially reconstructed background, mainly from $B^{0,+} \rightarrow K^{*0,+} e^+ e^-$ where a pion is lost

$B^+ \rightarrow K^+ J/\psi(e^+ e^-)$ events where a photon is not reconstructed



Longer radiative tail due to bremsstrahlung

arXiv:2103.11769
 Nature Physics

Measure as a double ratio

- To mitigate muon and electron differences, measurement performed as a double ratio with “resonant” control modes $B^0 \rightarrow J/\psi H$, which are not expected to be affected by NP:

$$R_H = \frac{\mathcal{B}(B^0 \rightarrow H \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow H J/\psi(\rightarrow \mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^0 \rightarrow H e^+ e^-)}{\mathcal{B}(B^0 \rightarrow H J/\psi(\rightarrow e^+ e^-))}$$

$$R_H = \frac{N(B \rightarrow H \mu^+ \mu^-)}{\epsilon(B \rightarrow H \mu^+ \mu^-)} \times \frac{\epsilon(B \rightarrow H e^+ e^-)}{N(B \rightarrow H e^+ e^-)} \times \frac{N(B \rightarrow H J/\psi(e^+ e^-))}{\epsilon(B \rightarrow H J/\psi(e^+ e^-))} \times \frac{\epsilon(B \rightarrow H J/\psi(\mu^+ \mu^-))}{N(B \rightarrow H J/\psi(\mu^+ \mu^-))}$$

→ Relevant experimental quantities: yields & (trigger, reconstruction and selection) and efficiencies for the four decay modes

- Similarities between the experimental efficiencies of the non resonant and resonant modes ensure a substantial reduction of systematic uncertainties in the double ratio. Note, however, that the cancellation does not apply to background.

- $r_{J/\psi} = \frac{B(B \rightarrow H J/\psi(\mu^+ \mu^-))}{B(B \rightarrow H J/\psi(e^+ e^-))}$ known to be compatible with unity within 0.4%

- Analyses performed blind

R_K measurement (9 fb^{-1})

- Performed in q^2 interval $1.1 < q^2 < 6.0 \text{ GeV}^2$

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(\rightarrow \mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(\rightarrow e^+ e^-))}$$

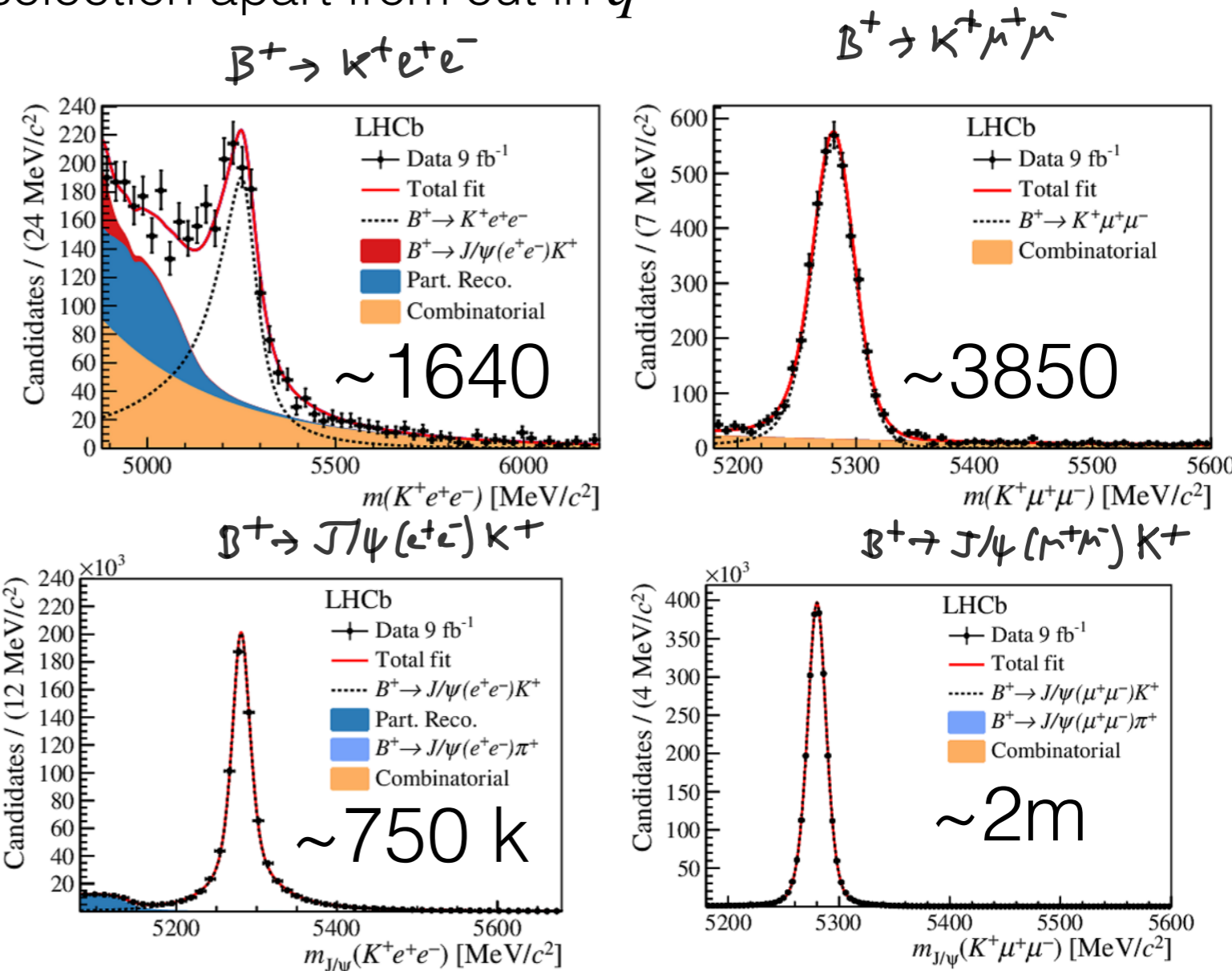
- Rare and J/ψ mode share identical selection apart from cut in q^2

$$R_K = \frac{N_{\mu^+ \mu^-}^{\text{rare}} \epsilon_{\mu^+ \mu^-}^{J/\psi}}{N_{\mu^+ \mu^-}^{J/\psi} \epsilon_{\mu^+ \mu^-}^{\text{rare}}} \times \frac{N_{e^+ e^-}^{J/\psi} \epsilon_{e^+ e^-}^{\text{rare}}}{N_{e^+ e^-}^{\text{rare}} \epsilon_{e^+ e^-}^{J/\psi}}$$

- Yields determined from fits to the invariant mass distributions

- Efficiencies computed using simulation calibrated with control channels in data

arXiv:2103.11769
Nature Physics



R_K cross-checks

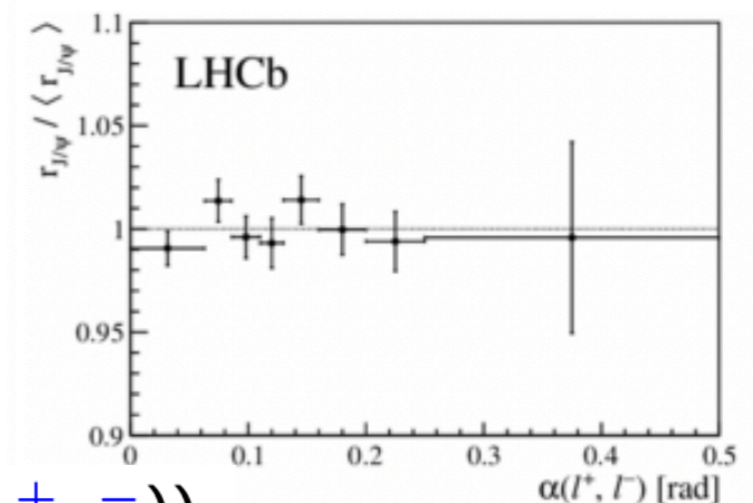
- Large number of crosschecks performed before unblinding the results
- To ensure that the efficiencies are under control, measure

$$r_{J/\psi} = \frac{B(B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-))}{B(B^+ \rightarrow K^+ J/\psi(e^+ e^-))}$$

arXiv:2103.11769
Nature Physics

- Very stringent test, which does not benefit from the cancellation of the experimental systematics provided by the double ratio

- $r_{J/\psi} = 0.981 \pm 0.020$ - checked across datasets, samples and as a function of kinematics



$$R_{\psi(2S)} = \frac{B(B^+ \rightarrow K^+ \psi(2S)(\mu^+ \mu^-))}{B(B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-))} \bigg/ \frac{B(B^+ \rightarrow K^+ \psi(2S)(e^+ e^-))}{B(B^+ \rightarrow K^+ J/\psi(e^+ e^-))} = 0.997 \pm 0.011$$

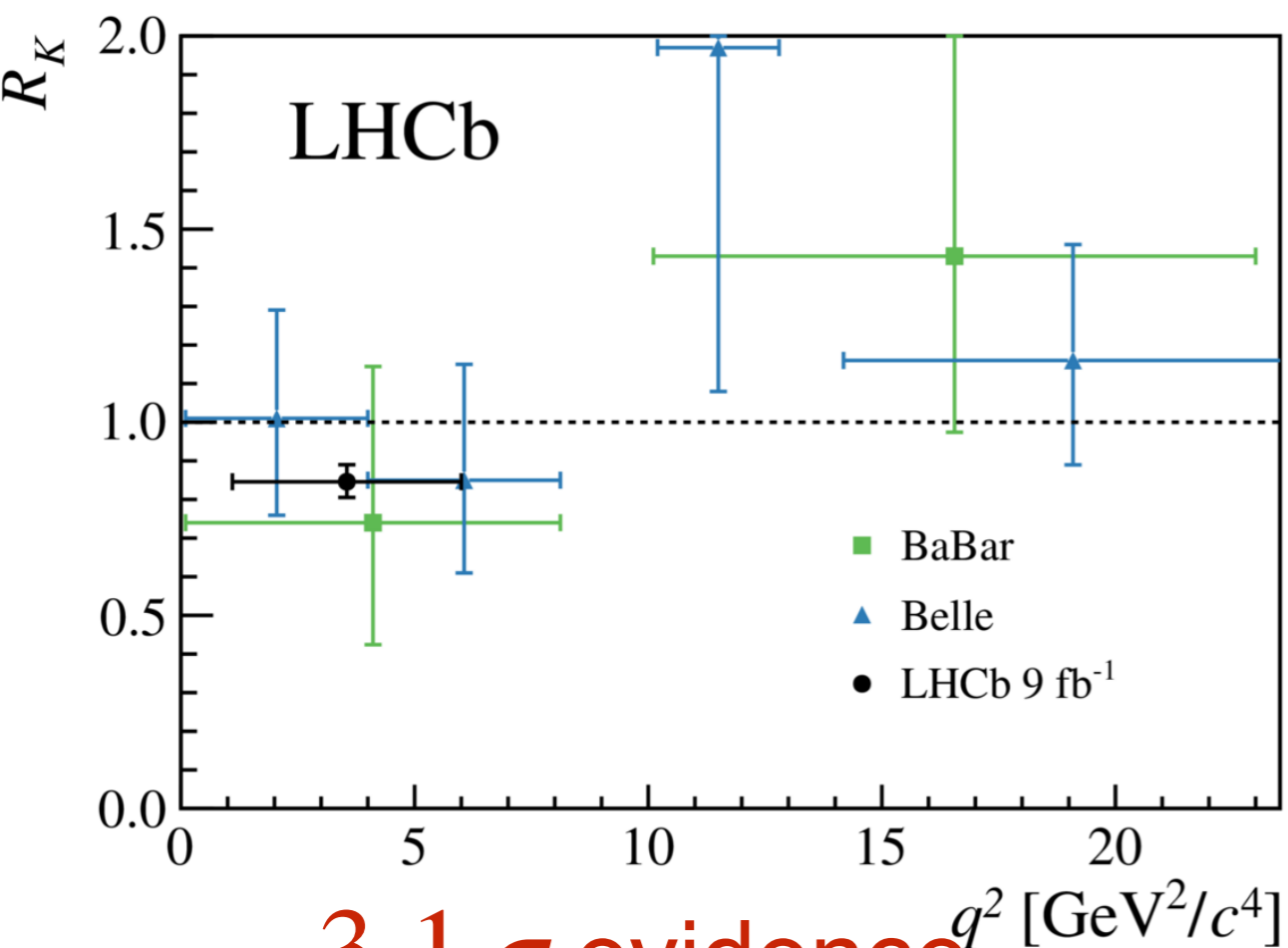
validation of the double-ratio procedure at q^2 away from J/ψ

- If corrections to simulation are not accounted for, the ratio of the efficiencies (and thus R_K) changes by $\sim 3\%$

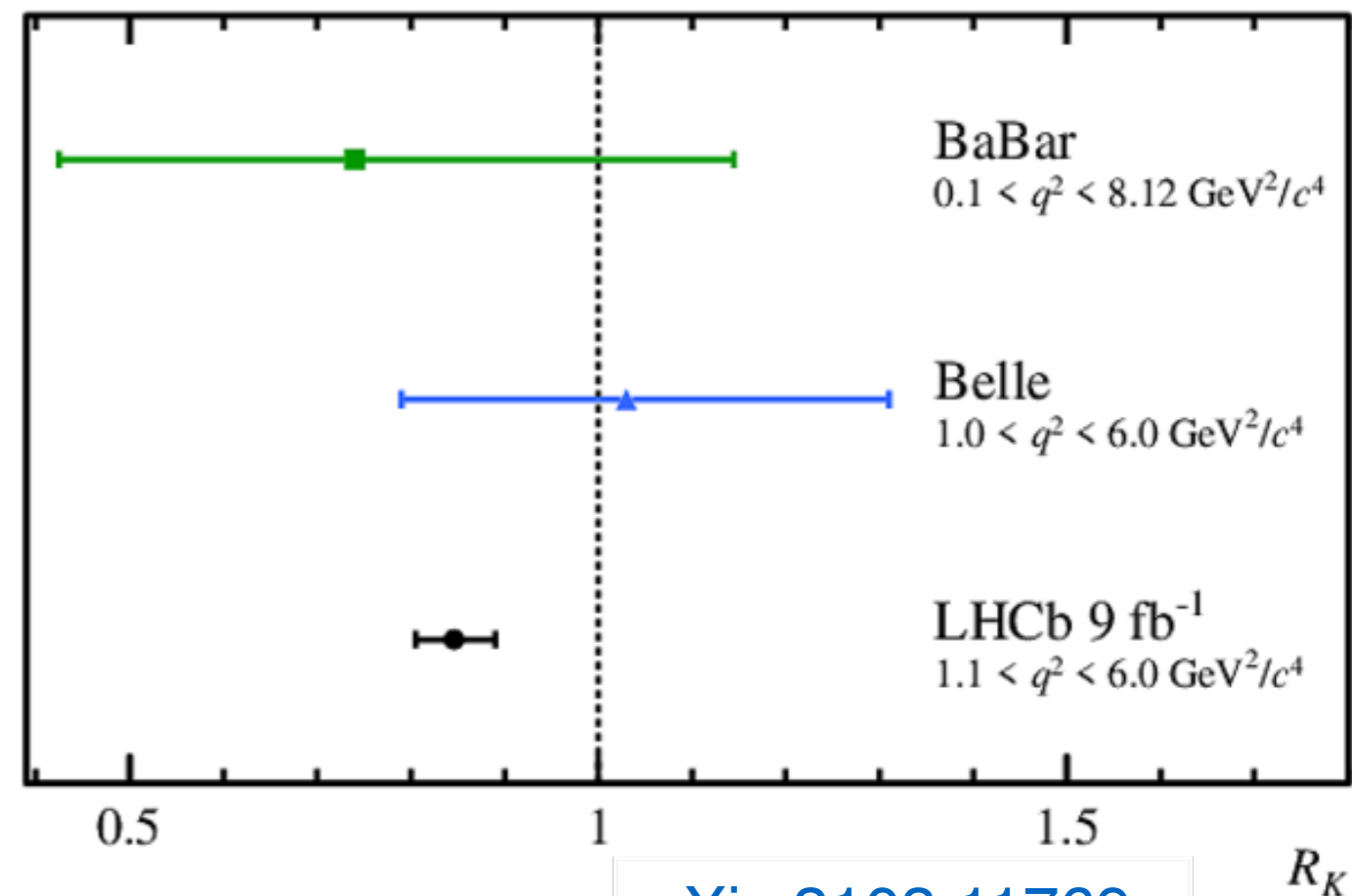
$$R_K (B^+ \rightarrow K^+ \ell^+ \ell^-)$$

- $R_K(1.1 < q^2 < 6.0 \text{ GeV}^2) = 0.846^{+0.042}_{-0.039} (\text{stat})^{+0.013}_{-0.012} (\text{syst})$

Dominant systematics ($\sim 1\%$) is due to modelling of signal and background components used in the fit



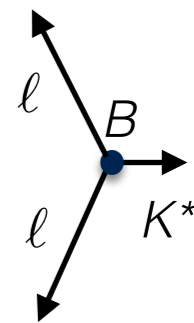
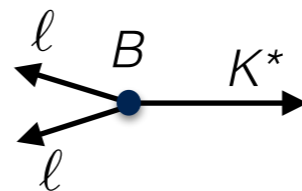
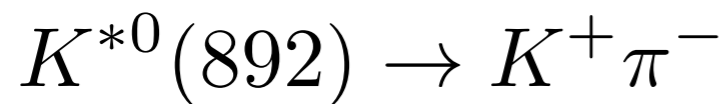
3.1 σ evidence



arXiv:2103.11769
Nature Physics

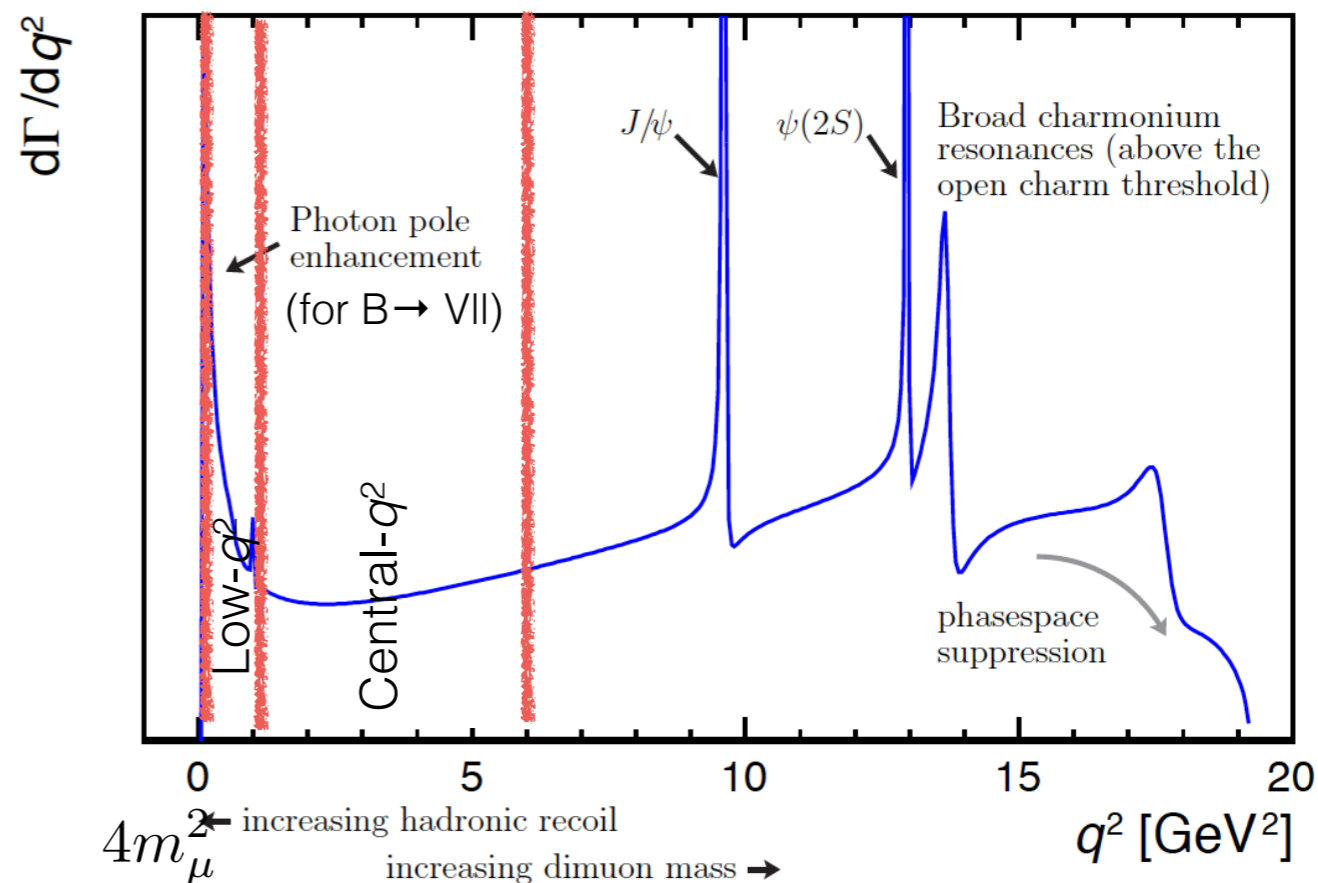
Another ratio: R_{K^*}

$$R_{K^*} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi(\rightarrow \mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi(\rightarrow e^+ e^-))}$$



- LHCb performed measurement in two q^2 bins that are sensitive to different NP contributions (Run 1 data, 3 fb^{-1}):

- Low- q^2 bin: $[0.045, 1.1] \text{ GeV}^2$
- Central- q^2 bin: $[1.1, 6.0] \text{ GeV}^2$



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Fit to the invariant masses

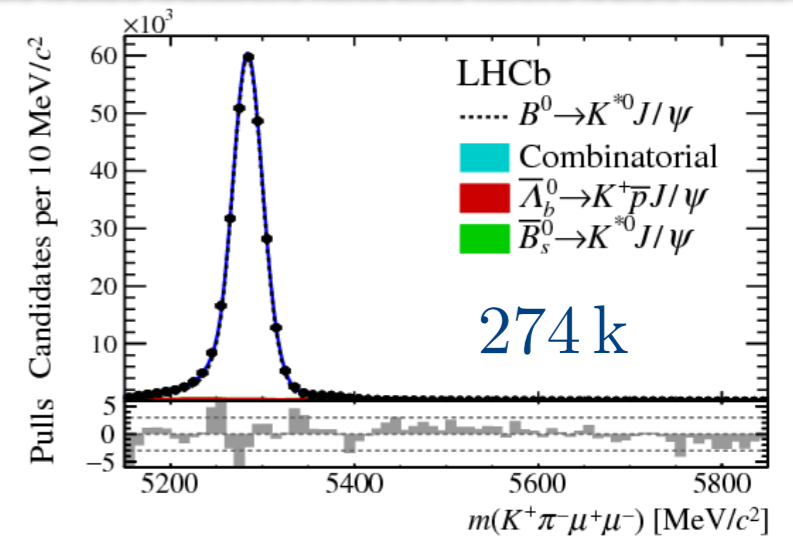
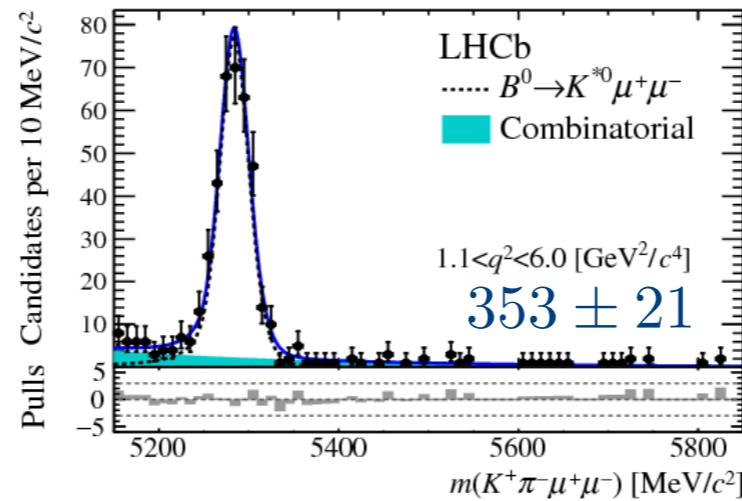
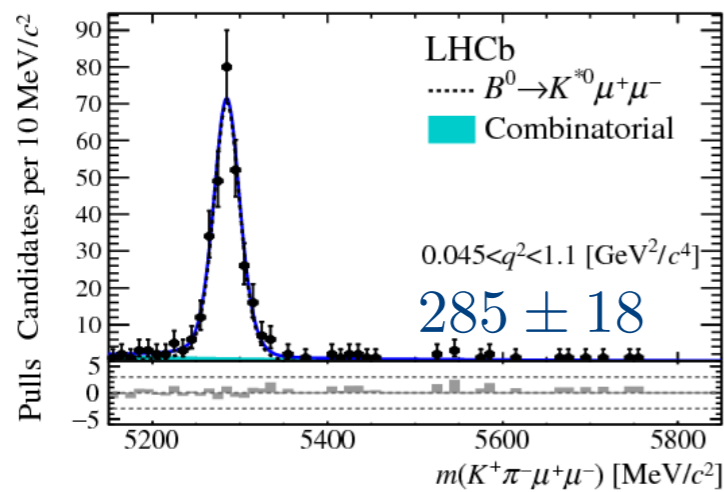
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Low- q^2

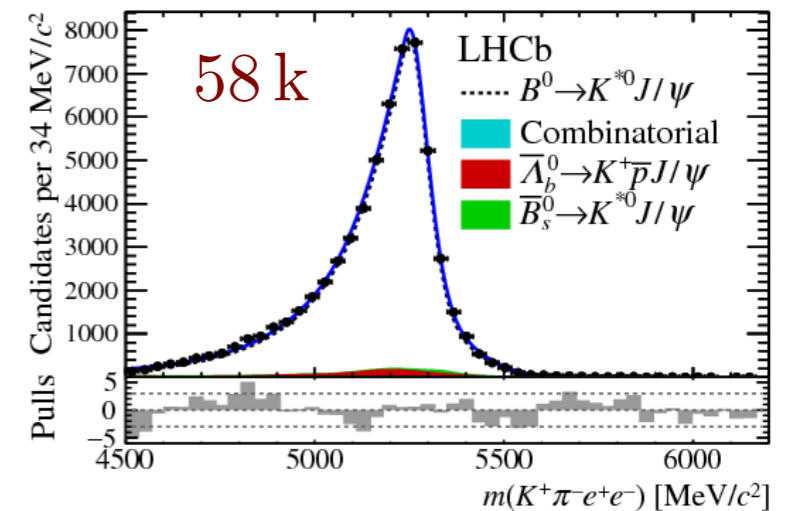
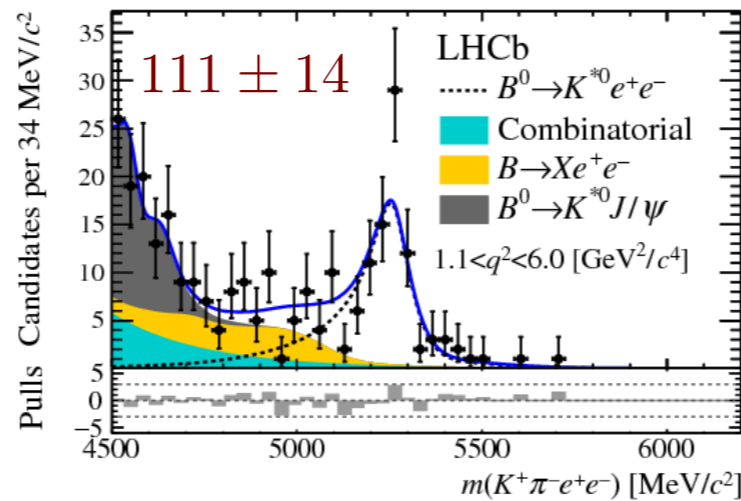
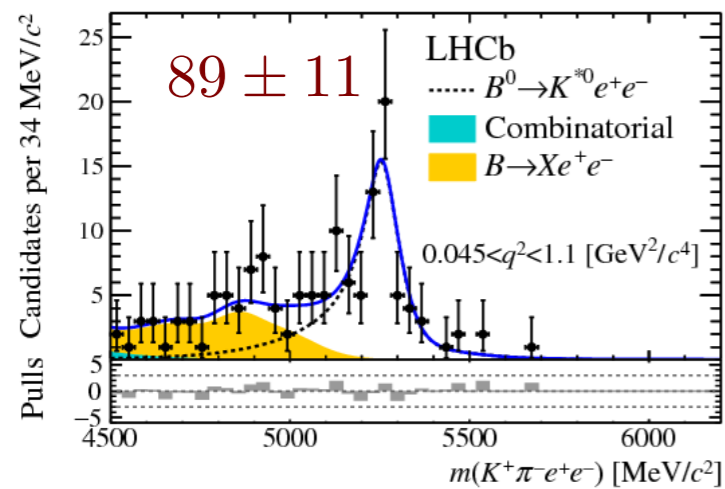
Central- q^2

$B^0 \rightarrow K^* J/\psi (\rightarrow \ell^+ \ell^-)$

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$



$B^0 \rightarrow K^{*0} e^+ e^-$



- Precision of measurement driven by statistics of electron sample : ~ 90 and 110 signal candidates in low- q^2 and central- q^2 , muon sample 3-5 times larger

Crosschecks

- Large number of crosschecks performed before unblinding the results

- $$r_{J/\psi} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi(\rightarrow \mu^+ \mu^-))}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi(\rightarrow e^+ e^-))} = 1.043 \pm 0.006 \pm 0.045$$

- test of absolute scale of the efficiencies

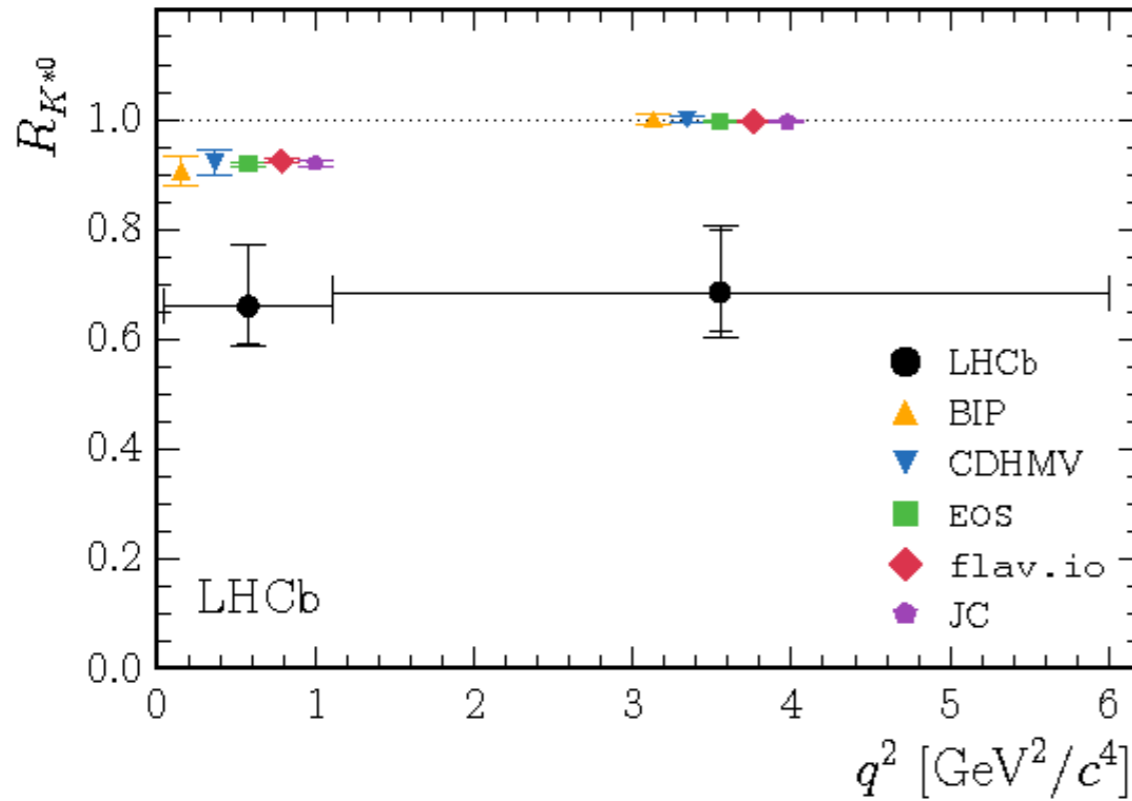
- $$R_{\psi(2S)} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \psi(2S)(\rightarrow \mu^+ \mu^-))}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi(\rightarrow \mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \psi(2S)(\rightarrow e^+ e^-))}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi(\rightarrow e^+ e^-))} \rightarrow 2\% \text{ measurement, within } 1\sigma \text{ from unity}$$

- $\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)$ in agreement with JHEP 04 (2017) 142

- If corrections to simulation are not accounted for, the ratio of the efficiencies (and thus R_{K^*}) changes by less than 5%

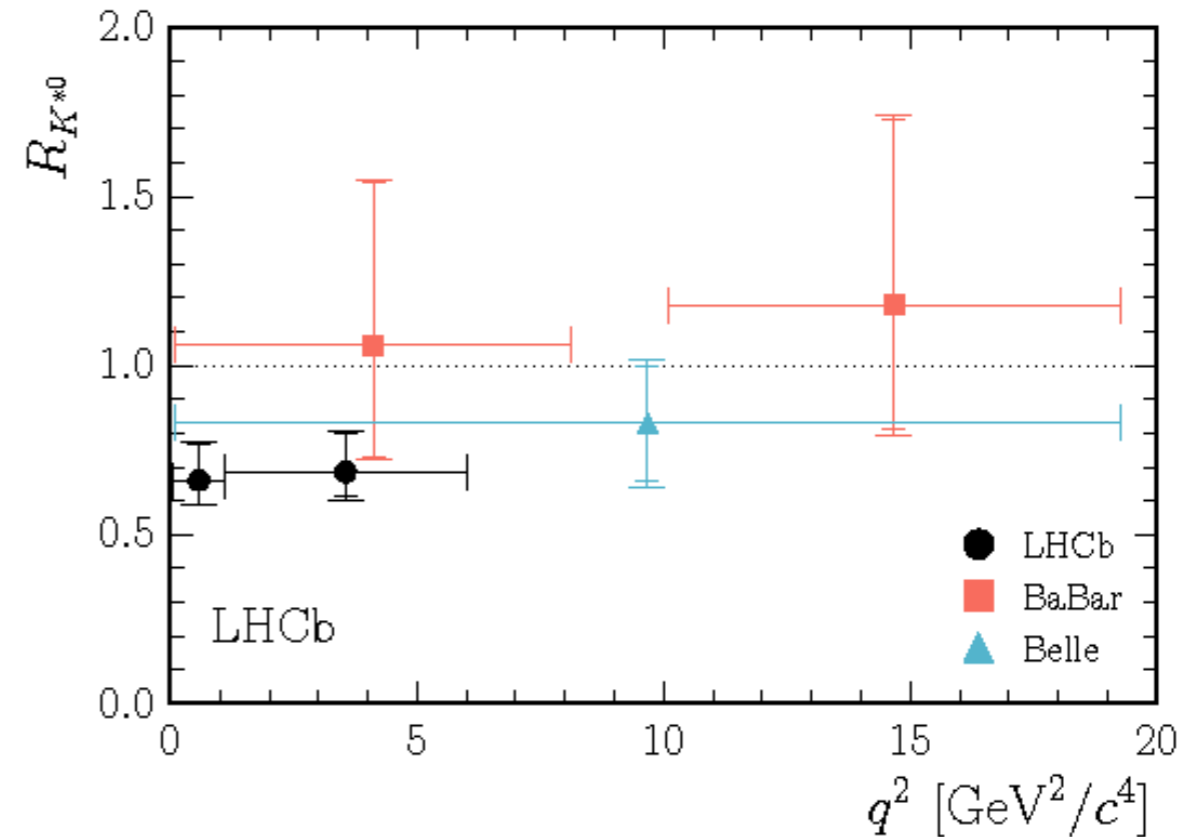
R_{K^*} results

Comparison with SM predictions



BIP: [arXiv:1605.07633](https://arxiv.org/abs/1605.07633)
 CDHMV: [arXiv:1510.04239](https://arxiv.org/abs/1510.04239), [1605.03156](https://arxiv.org/abs/1605.03156), [1701.08672](https://arxiv.org/abs/1701.08672)
 EOS: [arXiv:1610.08761](https://arxiv.org/abs/1610.08761), <https://eos.github.io>
 flav.io: [arXiv:1503.05534](https://arxiv.org/abs/1503.05534), [1703.09189](https://arxiv.org/abs/1703.09189), [flav-io/flavio](https://github.com/flav-io/flavio)
 JC: [arXiv:1412.3183](https://arxiv.org/abs/1412.3183)

Comparison with BaBar & Belle



BaBar: [PRD 86 \(2012\) 032012](https://arxiv.org/abs/1203.0321)
 Belle: [PRL 103 \(2009\) 171801](https://arxiv.org/abs/0903.1718)

LHCb: [JHEP 08 \(2017\) 055](https://arxiv.org/abs/1708.05506)

$$R_{K^*} = \begin{cases} 0.66_{-0.07}^{+0.11} \text{ (stat)} \pm 0.03 \text{ (syst)} & \text{for } 0.045 < q^2 < 1.1 \text{ GeV}^2 \\ 0.69_{-0.07}^{+0.11} \text{ (stat)} \pm 0.05 \text{ (syst)} & \text{for } 1.1 < q^2 < 6.0 \text{ GeV}^2 \end{cases}$$

2.1 - 2.3 σ
2.4 - 2.5 σ
below SM
expectations

Tests of LFU with $B^0 \rightarrow K_s^0 \ell^+ \ell^-$ and $B^+ \rightarrow K^{*+} \ell^+ \ell^-$

arXiv:2110.09501

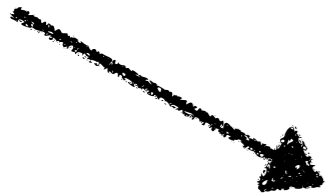
- Isospin partners of $B^+ \rightarrow K^+ \ell^+ \ell^-$, $B^0 \rightarrow K^{*0} \ell^+ \ell^-$, so potentially affected by the same NP
- Both channels involve long-lived $K_s^0 \rightarrow \pi^+ \pi^-$ ($K^{*+} \rightarrow K_s^0 \pi^+$) \rightarrow similar BF than their isospin partners, but lower efficiency because of the K_s^0 reconstruction
- $R_{K_s^0}$ and $B(B^0 \rightarrow K_s^0 \ell^+ \ell^-)$ measured in the region $1.1 < q^2 < 6 \text{ GeV}^2$
- For $R_{K^{*+}}$ and $B(B^+ \rightarrow K^{*+} \ell^+ \ell^-)$ q^2 range extended down to 0.045 GeV^2 to increase statistics
- Ratios and differential BFs normalised to control modes $B^0 \rightarrow J/\Psi(\ell^+ \ell^-) K_s^0$, $B^+ \rightarrow J/\Psi(\ell^+ \ell^-) K^{*+}$

Tests of LFU with $B^0 \rightarrow K_S^0 \ell^+ \ell^-$ and $B^+ \rightarrow K^{*+} \ell^+ \ell^-$

- $$R_{K^{(*)}}^{-1} = \frac{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}{\mathcal{B}(B \rightarrow J/\psi (e^+ e^-) K^{(*)})} / \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow J/\psi (\mu^+ \mu^-) K^{(*)})}$$

$$= \left(\frac{N_{\text{sig}}^{ee}}{\epsilon_{\text{sig}}^{ee}} \cdot \frac{\epsilon_{\text{con}}^{ee}}{N_{\text{con}}^{ee}} \right) / \left(\frac{N_{\text{sig}}^{\mu\mu}}{\epsilon_{\text{sig}}^{\mu\mu}} \cdot \frac{\epsilon_{\text{con}}^{\mu\mu}}{N_{\text{con}}^{\mu\mu}} \right) \quad \text{with } K^{(*)} = K_S^0, K^{*+}$$

- $$r_{J/\psi K^{(*)}}^{-1} \equiv \frac{\mathcal{B}(B \rightarrow J/\psi (e^+ e^-) K^{(*)})}{\mathcal{B}(B \rightarrow J/\psi (\mu^+ \mu^-) K^{(*)})} = \frac{N_{\text{con}}^{ee} \epsilon_{\text{con}}^{\mu\mu}}{N_{\text{con}}^{\mu\mu} \epsilon_{\text{con}}^{ee}}$$



$$r_{J/\psi K_S^0}^{-1} = 0.977 \pm 0.008 \pm 0.027$$

$$r_{J/\psi K^{*+}}^{-1} = 0.965 \pm 0.011 \pm 0.034$$

arXiv:2110.09501

- $$R_{\psi(2S)K_S^0}^{-1} = 1.014 \pm 0.030 \text{ (stat.)} \pm 0.020 \text{ (syst.)}$$

$$R_{\psi(2S)K^{*+}}^{-1} = 1.017 \pm 0.045 \text{ (stat.)} \pm 0.023 \text{ (syst.)}$$

Tests of LFU with $B^0 \rightarrow K_S^0 \ell^+ \ell^-$ and $B^+ \rightarrow K^{*+} \ell^+ \ell^-$

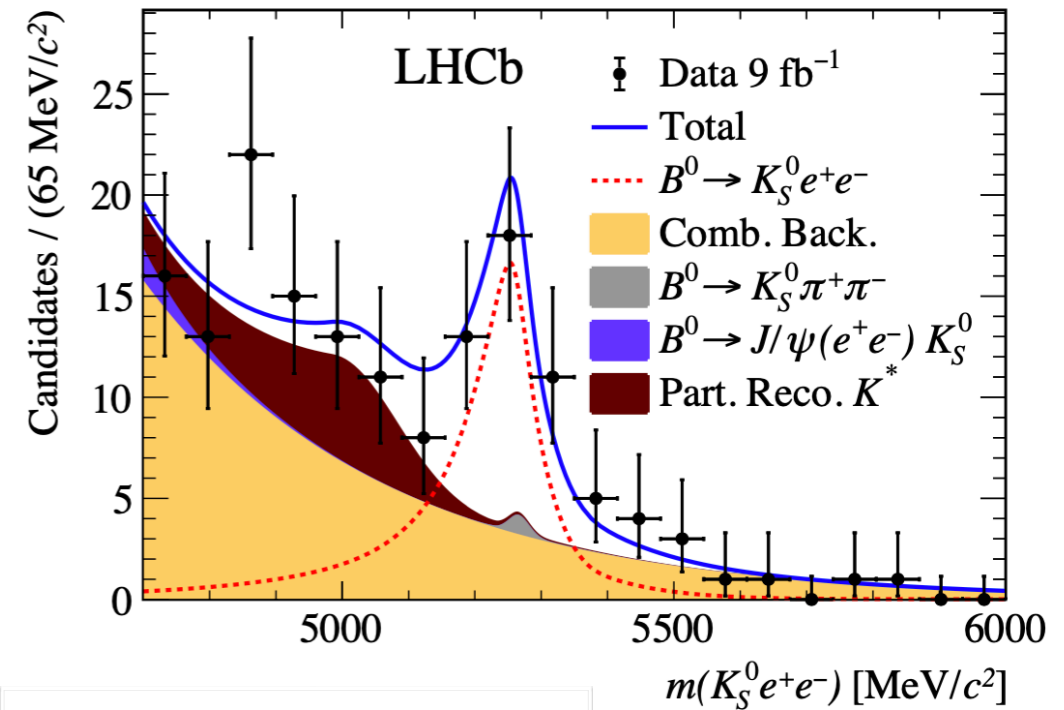
- e^+e^- modes observed for first time:

$$\frac{d\mathcal{B}(B^0 \rightarrow K^0 e^+ e^-)}{dq^2} = (2.6 \pm 0.6 \pm 0.1) \times 10^{-8} \text{ GeV}^{-2}$$

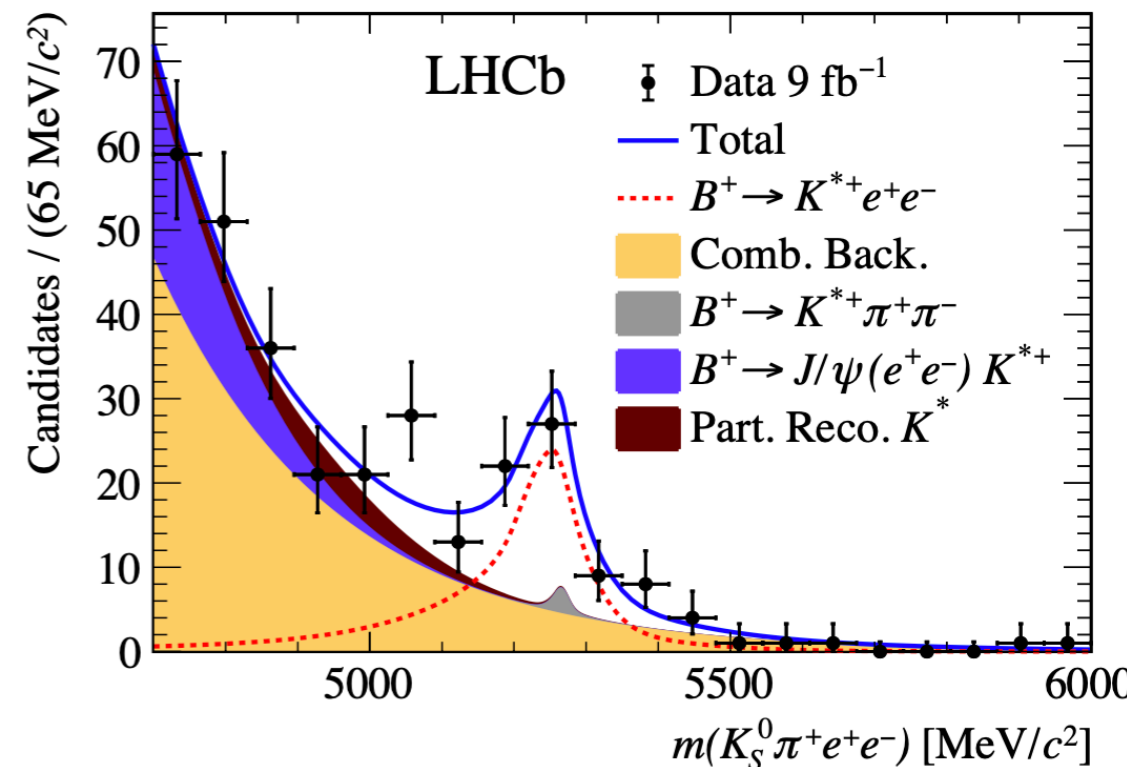
$$q^2 \in [1.1, 6.0] \text{ GeV}^2 \quad 5.3\sigma$$

$$\frac{d\mathcal{B}(B^+ \rightarrow K^{*+} e^+ e^-)}{dq^2} = (9.2_{-1.8-0.6}^{+1.9+0.8}) \times 10^{-8} \text{ GeV}^{-2}$$

$$q^2 \in [0.045, 6.0] \text{ GeV}^2 \quad 6.0\sigma$$



[arXiv:2110.09501](https://arxiv.org/abs/2110.09501)

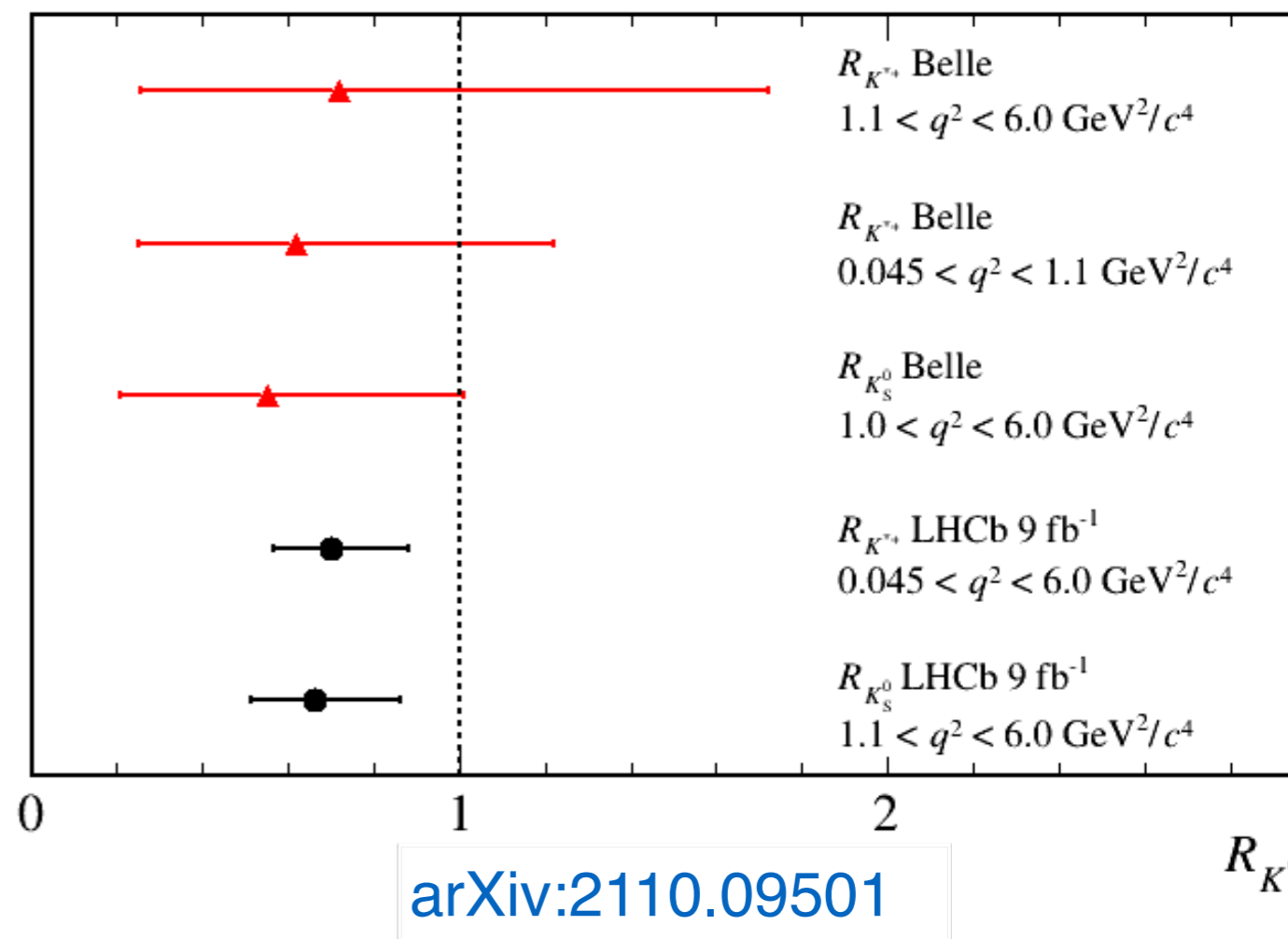


$R_{K_S^0}$ & $R_{K^{*+}}$

- Results are in agreement with SM and with previous results from Belle
- Central values exhibit same pattern of deviation of isospin partners R_{K^+} and $R_{K^{*0}}$
- Paper dedicated to the memory of Sheldon Stone [1946-2021]

$$R_{K_S^0} = 0.66_{-0.14}^{+0.20}(\text{stat.})_{-0.04}^{+0.02}(\text{syst})$$

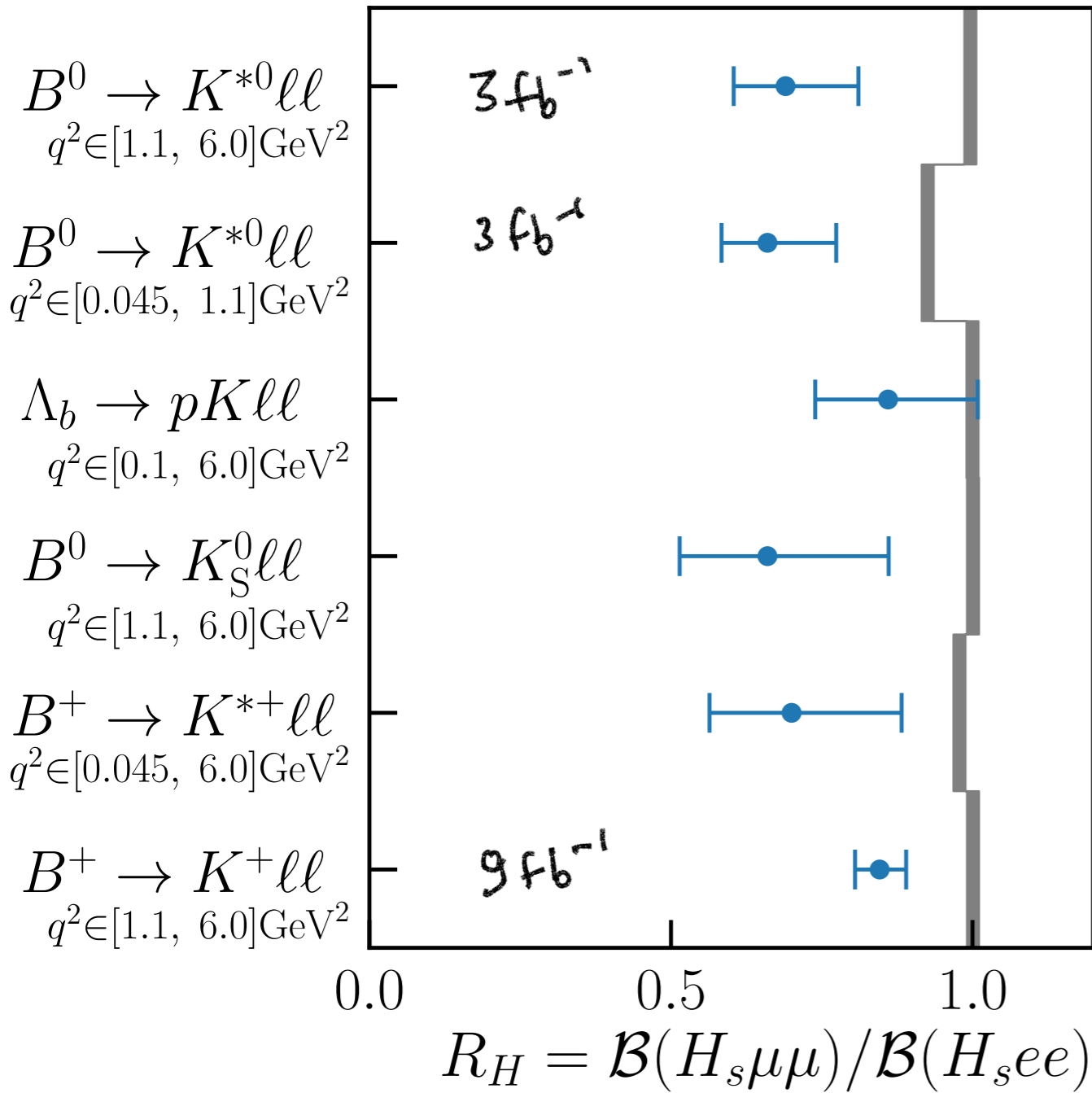
$$R_{K^{*+}} = 0.70_{-0.13}^{+0.18}(\text{stat.})_{-0.04}^{+0.03}(\text{syst})$$



A very intriguing pattern

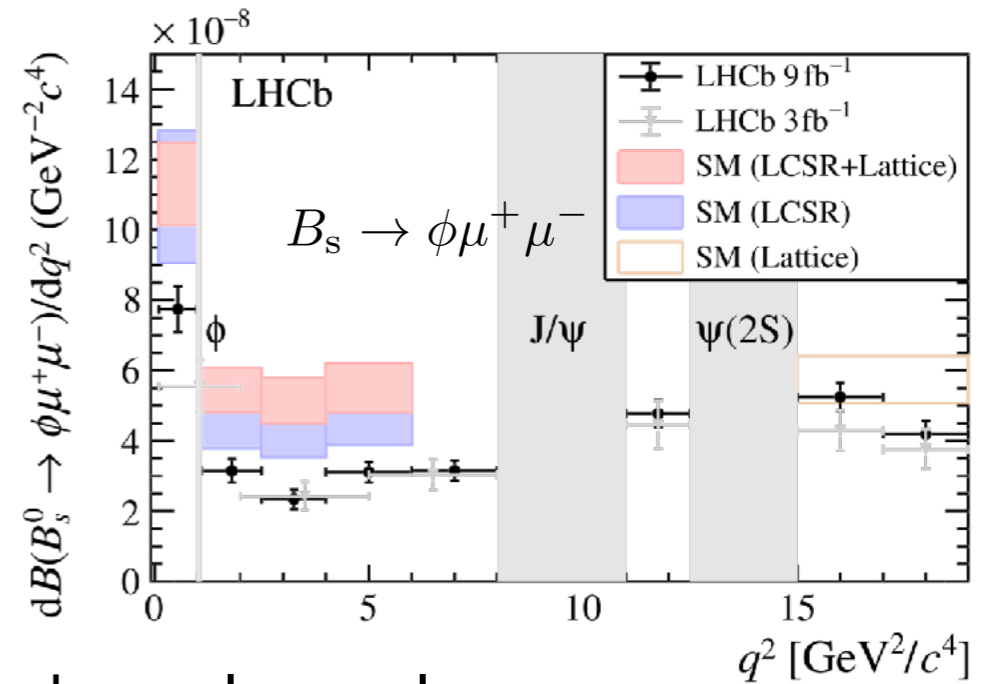
Summary of R_H

credit Martino Borsato

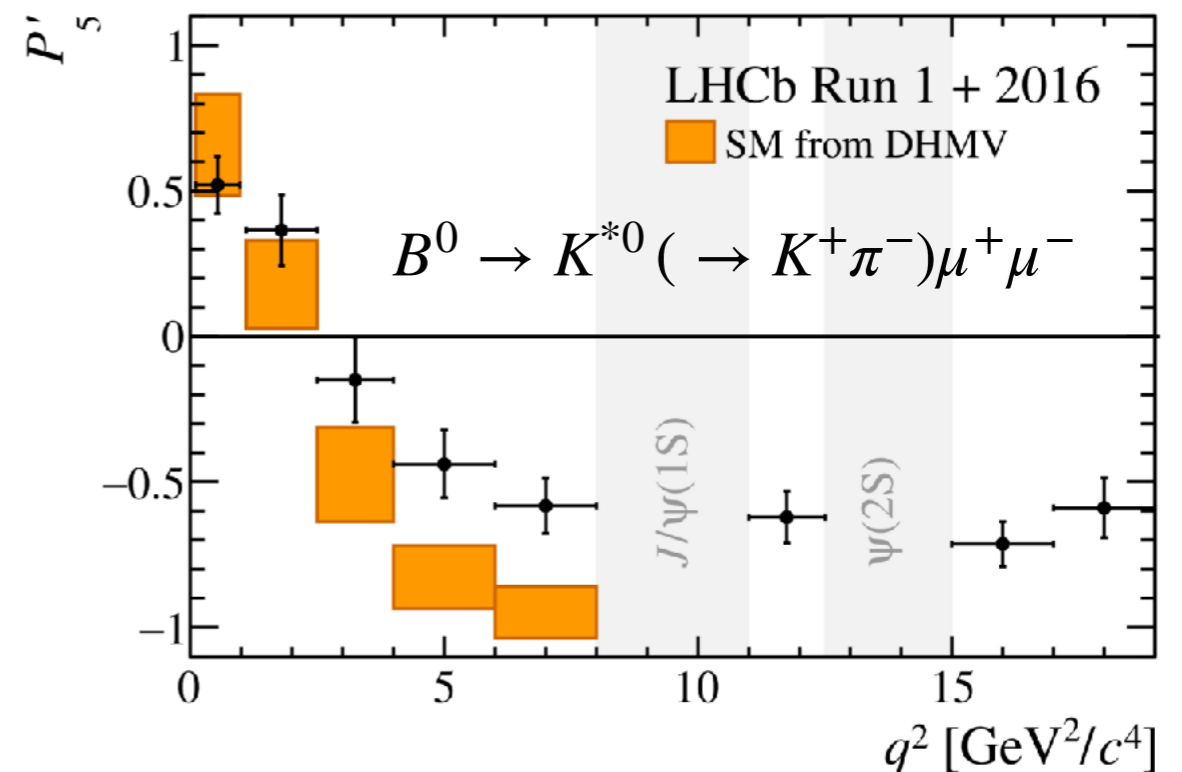


Th. calculated with flavio

- Coherent set of $b \rightarrow s \ell \ell$ tensions in BFs
 $B^+ \rightarrow K^+ \mu^+ \mu^-$, $B^0 \rightarrow K^{(*)0} \mu^+ \mu^-$, $B_s \rightarrow \phi \mu^+ \mu^-$.

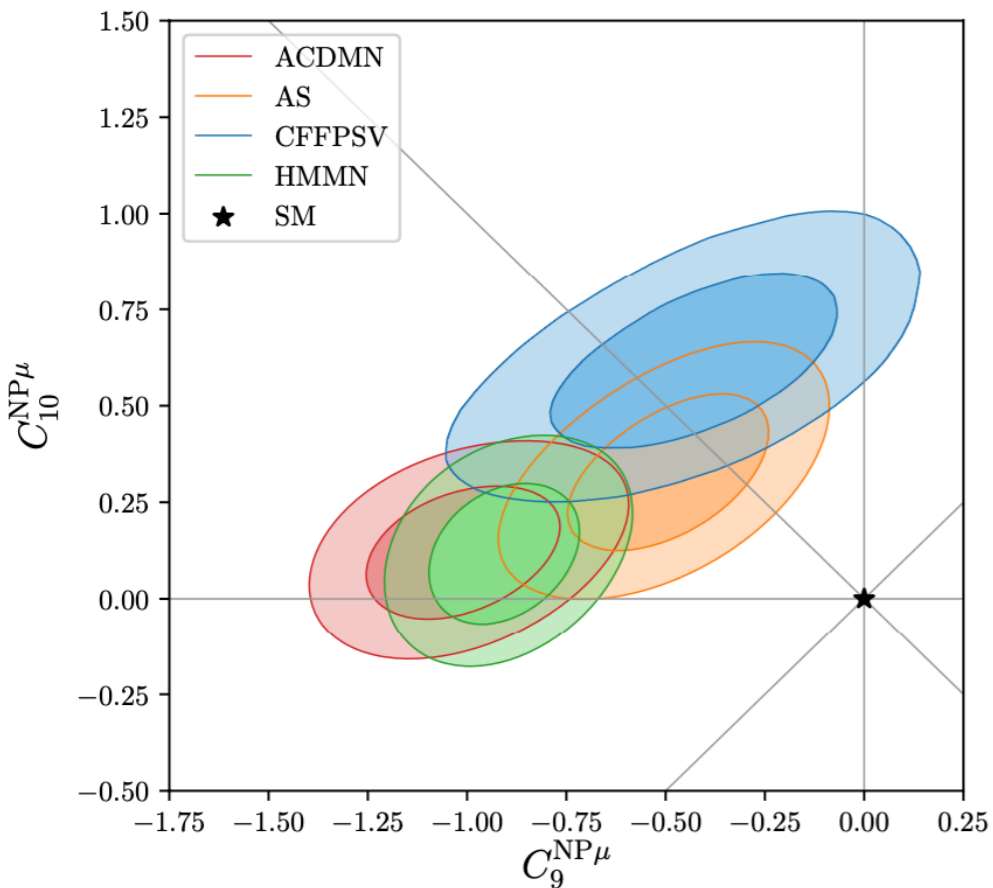


- and angular analyses

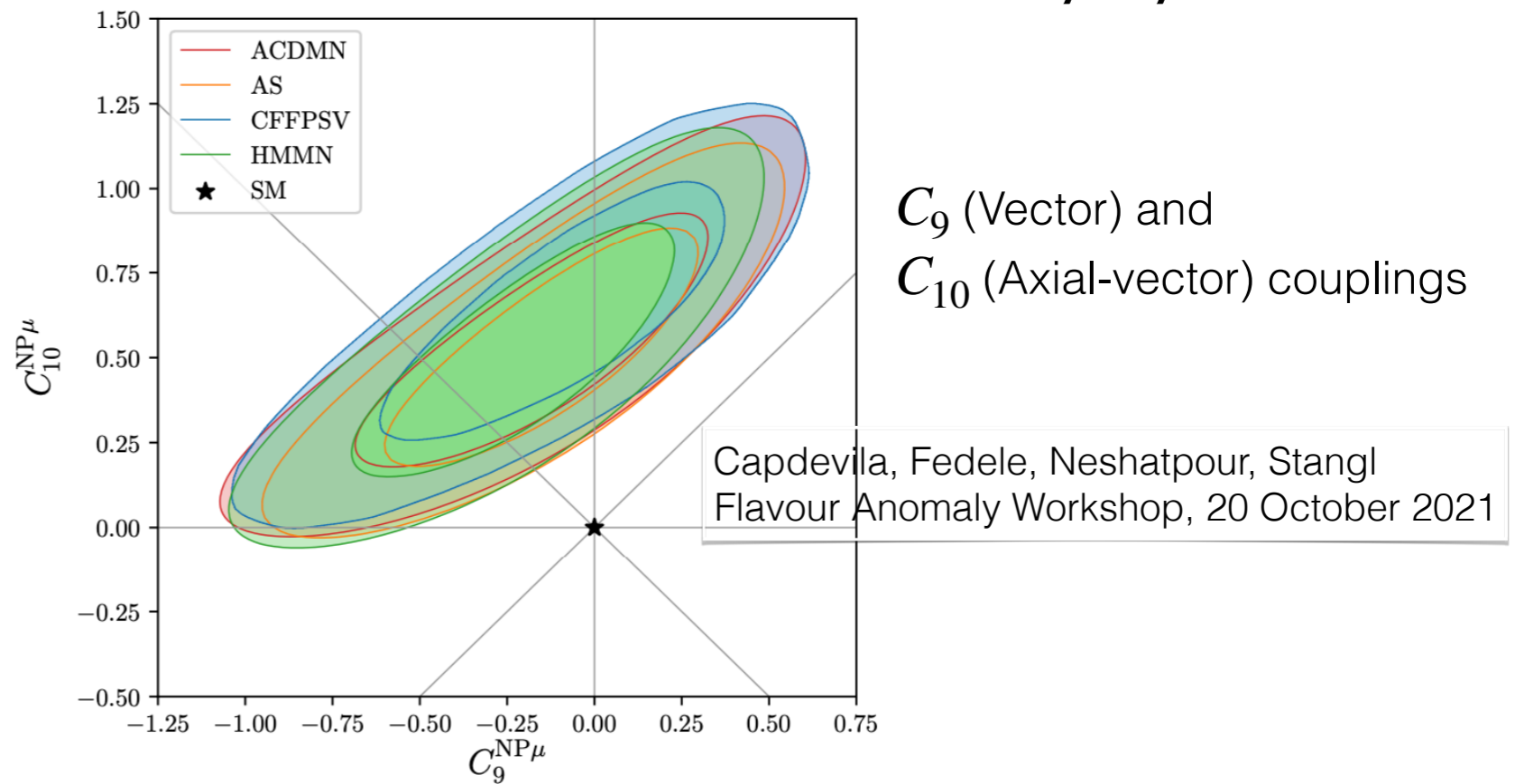


Global fit to $b \rightarrow s\ell^+\ell^-$ data

Global fit of $b \rightarrow s\ell^+\ell^-$



Fit of LFU observables & $B \rightarrow \mu^+\mu^-$



- Discrepancy in numerous $b \rightarrow s\ell^+\ell^-$ observables can be explained consistently

- ☺ P'_5 anomaly [$B \rightarrow K^* \mu\mu$ angular distribution]
- ☺ Smallness of all $B \rightarrow H_s \mu\mu$ rates
- ☺ LFU ratios (μ vs. e) in $H_b \rightarrow H_s \ell\ell$ decays
- ☺ Smallness of $\text{BR}(B_s \rightarrow \mu\mu)$

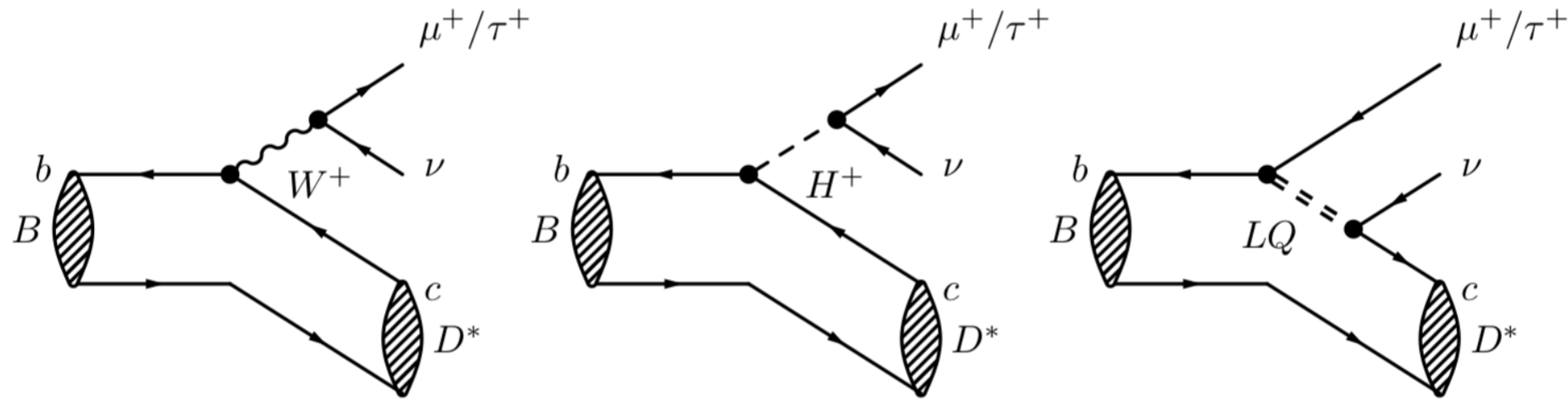
Gino's categorization

- ☺ = th. error $\lesssim 1\%$
- ☺ = th. error few %

Another puzzling result
in tree-level $b \rightarrow c$ transitions



LFU studies in $B \rightarrow D^{(*)} \tau \nu$ decays



- Different class of decays (tree-level charged current with V_{cb} suppression)
- Not at all rare: $B(B^0 \rightarrow D^{*-} \tau^+ \nu_\tau) \sim 1\%$, problem is the background

- Lepton-universality ratio $R(D^*)$:
$$R(D^*) = \frac{B(B^0 \rightarrow D^{*-} \tau^+ \nu_\tau)}{B(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}$$

- sensitive to any NP model coupling preferentially to third generation leptons

- Predicted theoretically at $\sim 1\%$: $R(D)_{\text{SM}} = 0.299 \pm 0.003$
 $R(D^*)_{\text{SM}} = 0.258 \pm 0.005$

HFLAV average,
2019

- Studied by Belle, BaBar and LHCb

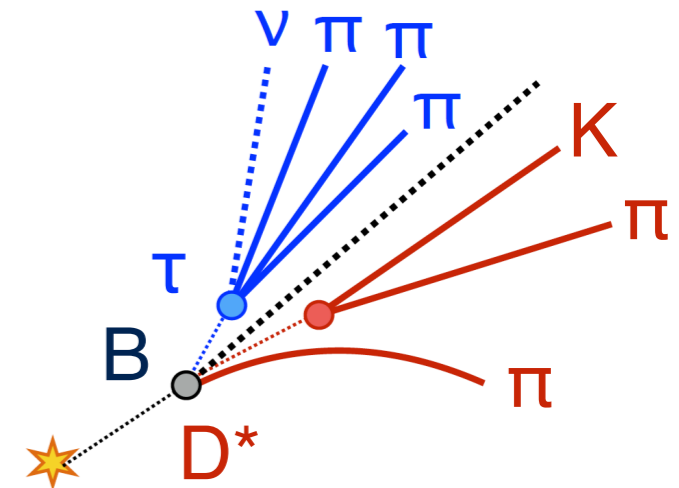
Experimental challenges

- $B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$: at least two neutrinos in the final state (three if using $\tau \rightarrow \mu \nu \nu$)
- At the LHC, as opposed to B factories, the rest of the event does not provide any useful kinematic constraint. However, profit from large boost and excellent vertexing capability

- LHCb used both $\tau^+ \rightarrow \mu^+ \nu \bar{\nu}$ and $\tau^+ \rightarrow \pi^+ \pi^- \pi^+$

$$\begin{cases} \tau^+ & \rightarrow \pi^+ \pi^- \pi^+ (\pi^0) \bar{\nu}_\tau \\ D^{*-} & \rightarrow \bar{D}^0 (\rightarrow K^+ \pi^-) \pi^- \end{cases}$$

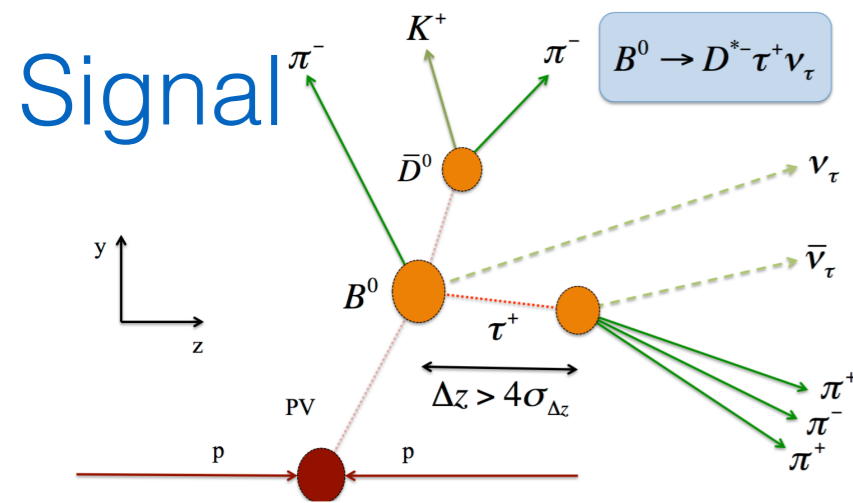
Three-prong mode used for the first time!



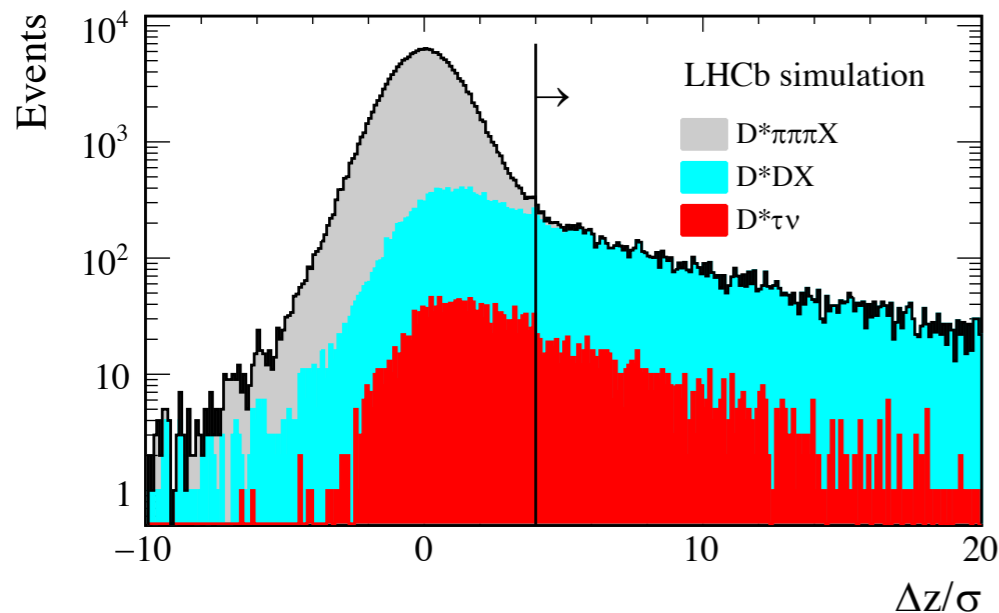
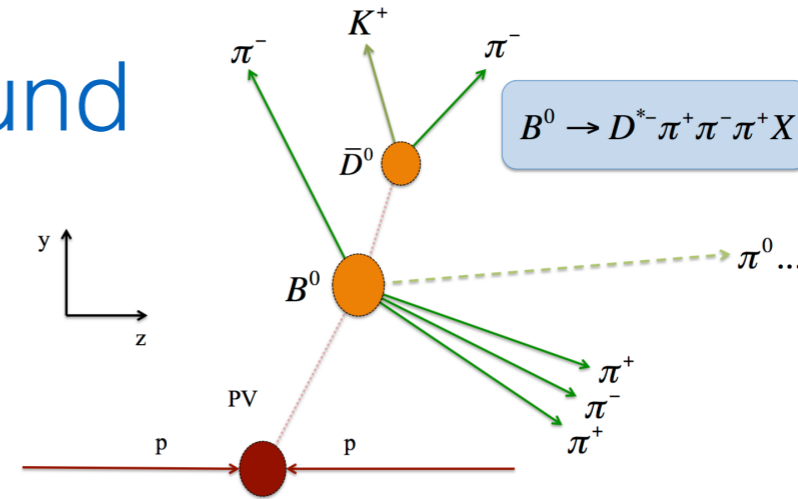
- A semileptonic decay with no (charged) lepton in final state (one K , five π)
 \rightarrow Zero background from $B^0 \rightarrow D^{*-} \mu^+ \nu_\mu X$
- However, signal to noise ratio less than 1% \rightarrow need at least 10^3 rejection!
- Large background, notably from $B \rightarrow D^{*-} 3\pi X$ (BF ~ 100 x signal) and $B \rightarrow D^{*-} D_S^+(X)$ (BF ~ 10 x signal, same vertex topology)

Background reduction

- Separation between B and 3π vertices ($\Delta z > 4\sigma_{\Delta z}$) crucial to obtain the required rejection of $B \rightarrow D^{*-}3\pi X$



Background

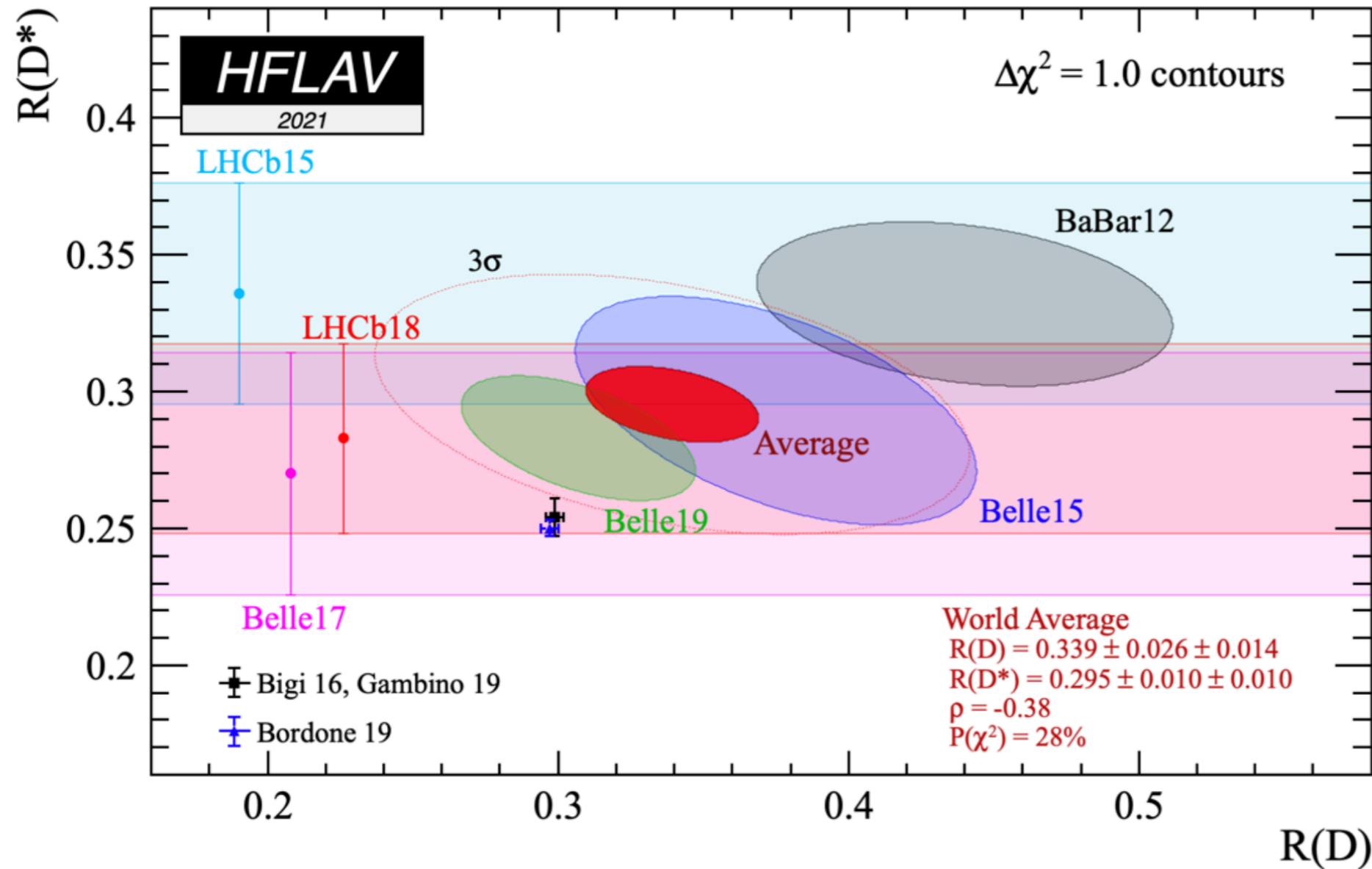


- Remaining double-charm background ($B \rightarrow D^{*-} D_S^+(X)$) suppressed by employing a multivariate classifier

PRL 120 (2018) 171802
PRD 97 (2018) 072013

$$R(D^{*-}) = 0.291 \pm 0.019 \text{ (stat)} \pm 0.026 \text{ (syst)} \pm 0.013 \text{ (ext)} \sim 1.1\sigma > \text{SM}$$

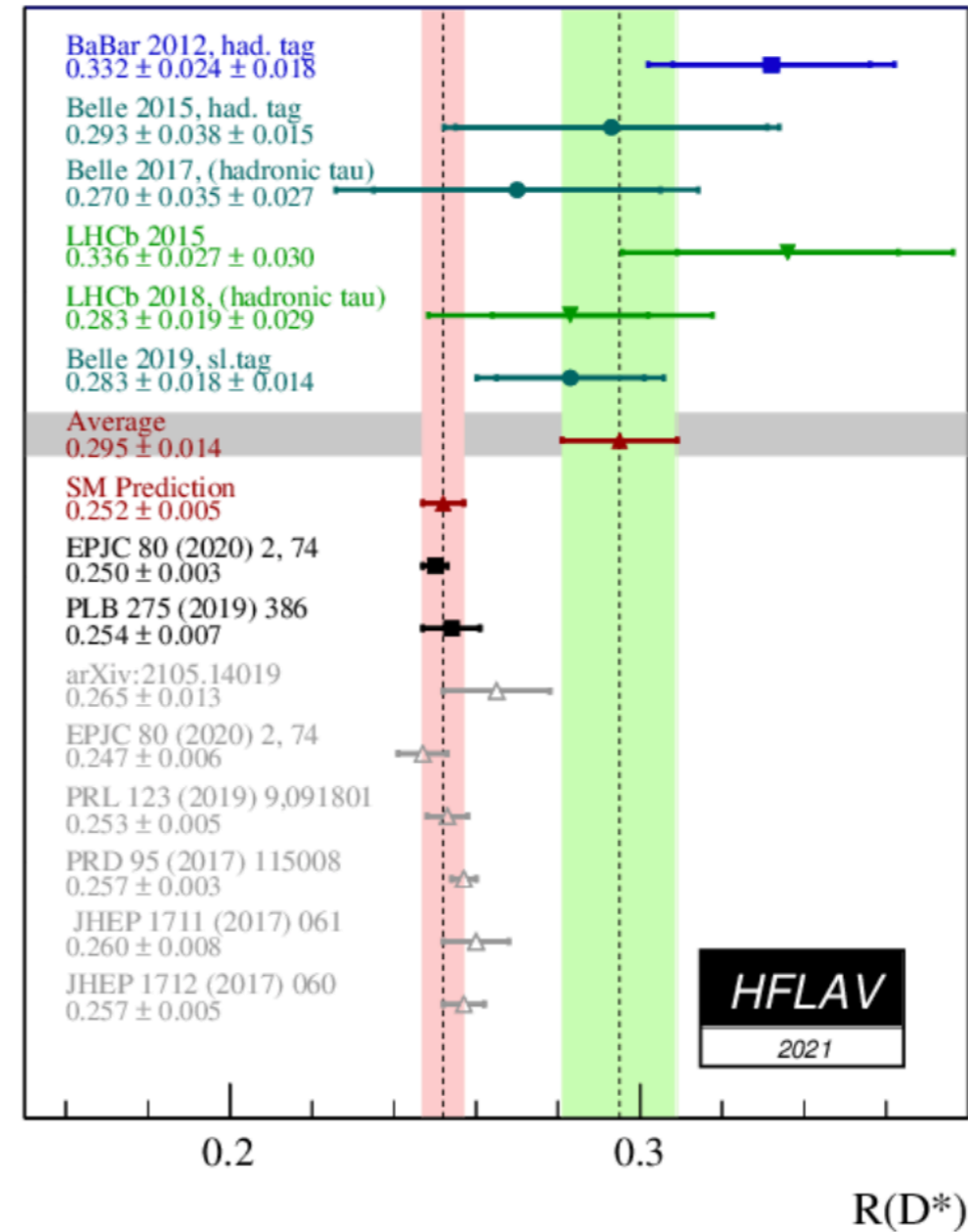
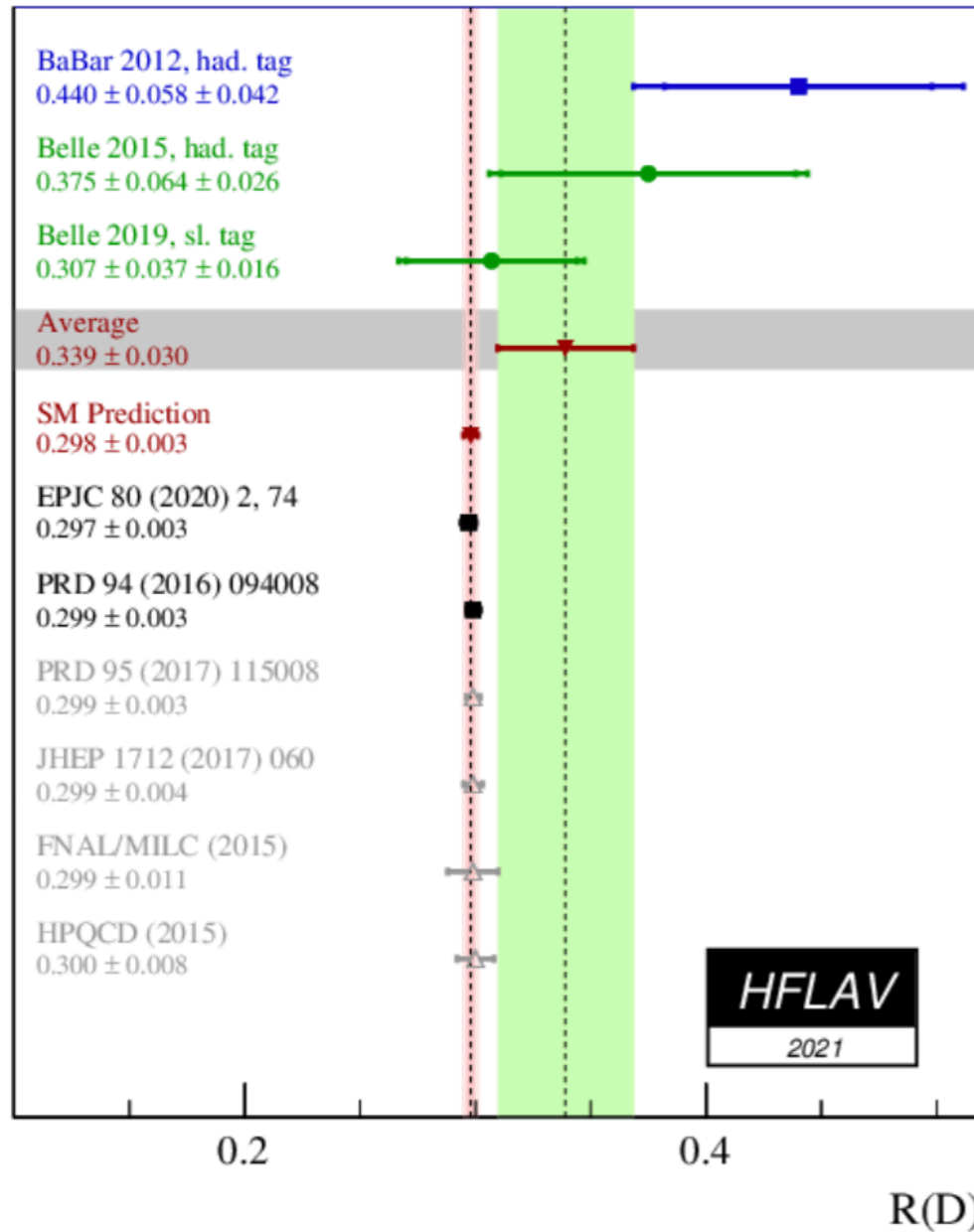
$R(D)$ vs $R(D^*)$



BaBar to deliver another precise measurement of $R(D^{(*)})$ after a decade, more data-driven

- All experiments see an excess wrt SM predictions: $\sim 3.4\sigma$ tension
- intriguing as it occurs in a tree-level SM process ($\Lambda_{\text{NP}} \lesssim 3 \text{ TeV}$)
- 2.9σ effect on $R(D^*)$

$R(D)$ vs $R(D^*)$



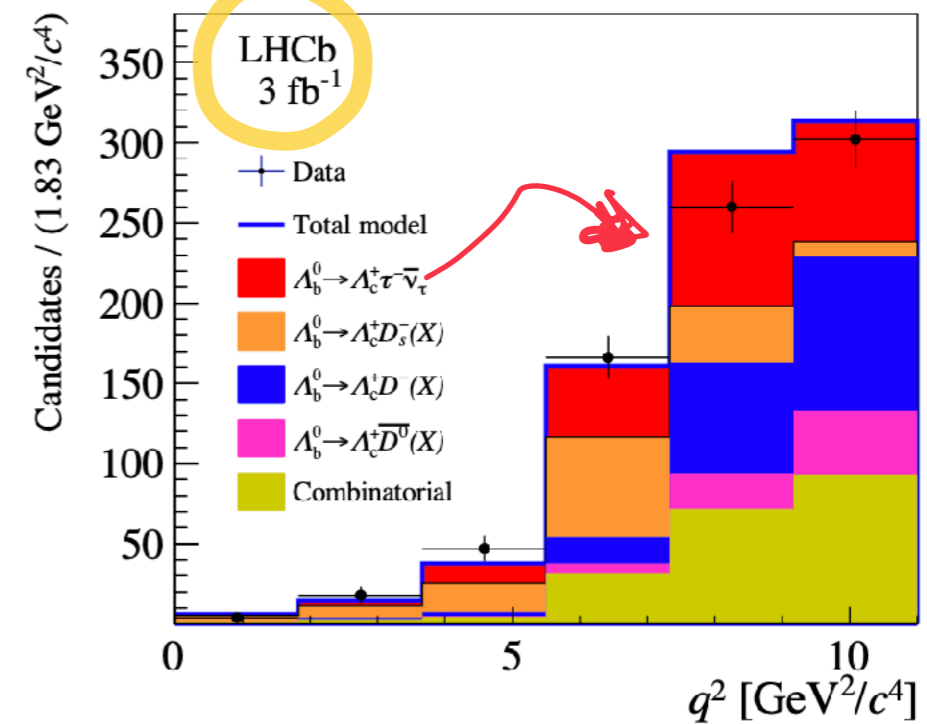
- All experiments see an excess wrt SM predictions: $\sim 3.4\sigma$ tension
- intriguing as it occurs in a tree-level SM process ($\Lambda_{\text{NP}} \lesssim 3 \text{ TeV}$)
- 2.9σ effect on $R(D^*)$

Measurement of $B(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)$ and $R(\Lambda_c)$ with $\tau \rightarrow 3\pi$

arXiv:2201.03497

- Decay observed for the first time with 6.1σ significance
- Measure

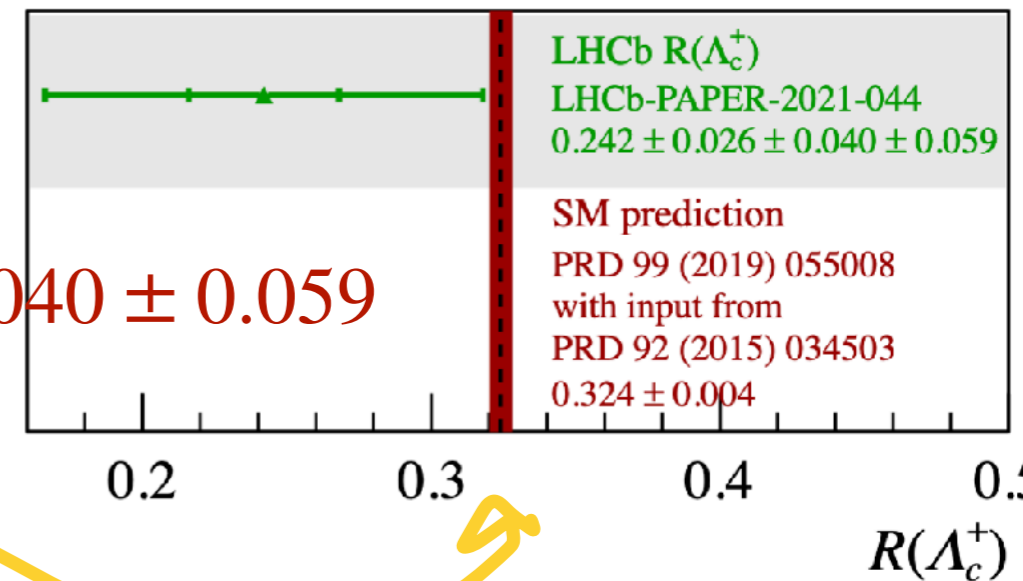
$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ 3\pi)} = \frac{N_{\text{sig}} \epsilon_{\text{norm}}}{N_{\text{norm}} \epsilon_{\text{sig}}} \frac{1}{\mathcal{B}(\tau^- \rightarrow 3\pi(\pi^0)\nu_\tau)}$$



- Input from CDF+LHCb on $B(\Lambda_b^0 \rightarrow \Lambda_c^+ 3\pi)$ gives $B(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau) = (1.50 \pm 0.16 \pm 0.25 \pm 0.23) \%$

- Input from DELPHI on $B(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu)$ gives

$$R(\Lambda_c^+) \equiv \frac{B(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{B(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu)} = 0.242 \pm 0.026 \pm 0.040 \pm 0.059$$



in agreement with SM

A word on LFV

- Many models proposed to explain these tensions naturally allow for LFV processes with rates that are experimentally accessible
- Searches for $b \rightarrow s\mu^\pm e^\mp$ are particularly important in view of the anomalies. Published limits from LHCb:

$$B(B_{(s)}^0 \rightarrow \mu^\pm e^\mp) < 5.4 \times 10^{-9} @ 90\% \text{ CL}$$

$$B(B^+ \rightarrow K^+ \mu^+ e^-) < 6.4 \times 10^{-9} @ 90\% \text{ CL}$$

$$B(B^+ \rightarrow K^+ \mu^- e^+) < 7.0 \times 10^{-9} @ 90\% \text{ CL}$$
- Most stringent new limits on semileptonic LFV $b \rightarrow s\mu^\pm e^\mp$ decays to date:

Limits at 90% CL: (LHCb preliminary)

$$B(B^0 \rightarrow K^{*0} \mu^+ e^-) < 5.69 \times 10^{-9}$$

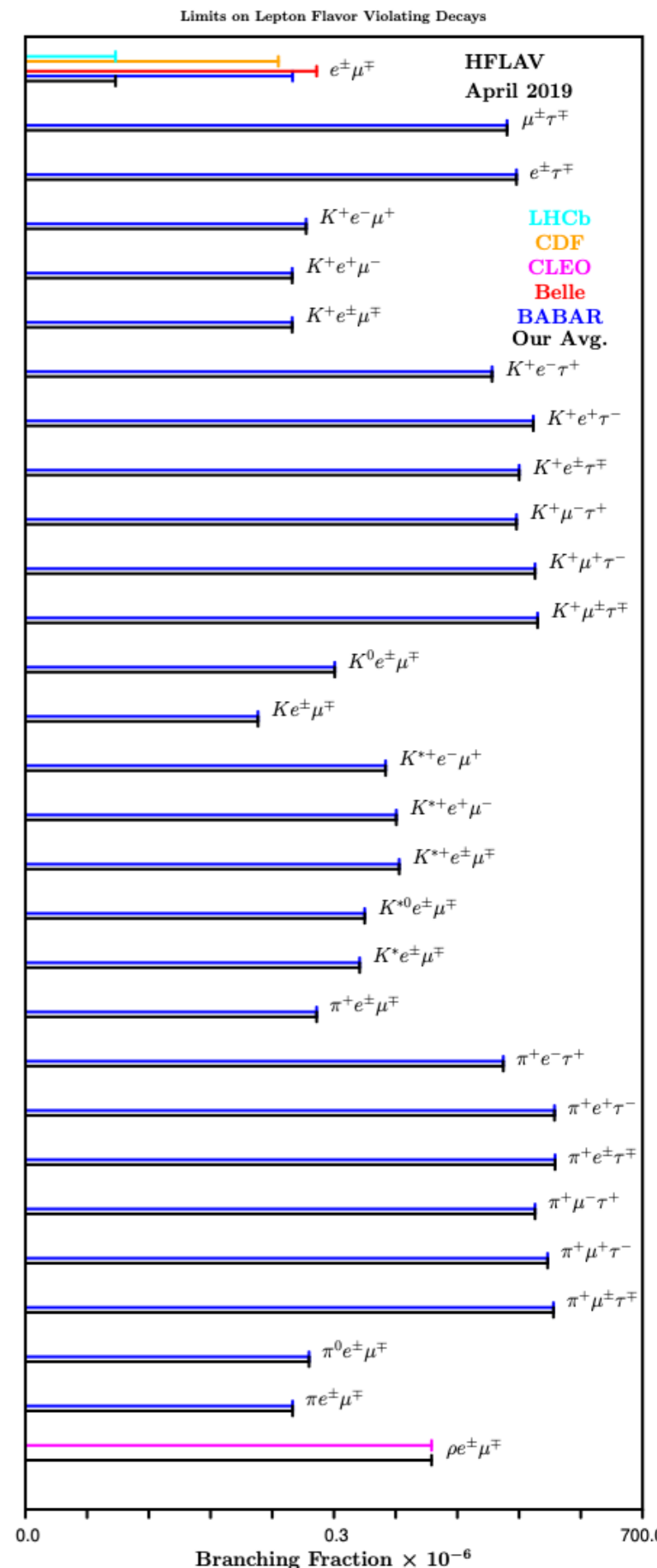
$$B(B^0 \rightarrow K^{*0} \mu^- e^+) < 6.73 \times 10^{-9}$$

$$B(B^0 \rightarrow K^{*0} \mu^\pm e^\mp) < 9.94 \times 10^{-9}$$

$$B(B_s^0 \rightarrow \phi \mu^\pm e^\mp) < 15.9 \times 10^{-9}$$

3 fb^{-1}

B decays



Take home message

- Precise measurements of flavour observables provide a powerful way to probe for NP effects beyond the SM, complementing direct searches for NP. This is particularly relevant in the absence of direct collider production of new particles.
- Many world record results. For some topics we have moved from exploration to precision measurements.
- Most of these results show good compatibility with the SM, but hints of LFU violation are still persisting! This has generated a lot of interesting theoretical ideas.
- Need more data to test these hints: full analysis of Run 2 but also results from ATLAS and CMS (ATLAS, CMS), while waiting for the high-precision results from the LHCb upgrade and Belle II



In case you would like to know more

- V. Vagnoni: [MISP 2019 lectures](#)
- T. Gershon: CERN Summer Student Programme 2016 [lecture 1](#), [lecture 2](#), [lecture 3](#), [lecture 4](#)
- G. Isidori: CERN, Summer Student Programme 2017, [Lectures on Flavour Physics and CP Violation](#)
- The recent “Flavour Anomalies in Heavy Quark Decays”, Albrecht, van Dyk, Langenbruch, [arXiv:2107.04822](#)
-
- Excellent book about to be published “New Physics in b decays”, by Artuso, Isidori and Stone, which I should acknowledge. This was something that kept Sheldon busy until the very last moments of his life.