

Probing the $\mathcal{O}(1/\Lambda^4)$ SMEFT Effects in the Drell-Yan process at LHC

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Northwestern
University



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1 Introduction

2 Dilepton invariant mass spectrum

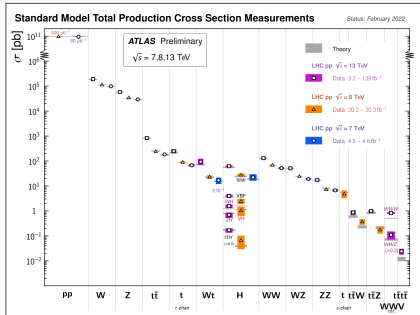
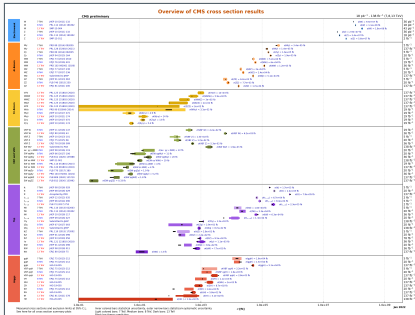
3 Dilepton mass-dependent p_T spectra

- Dilepton p_T spectra with CMS data
- Dilepton p_T spectra with HL-LHC pseudo-data

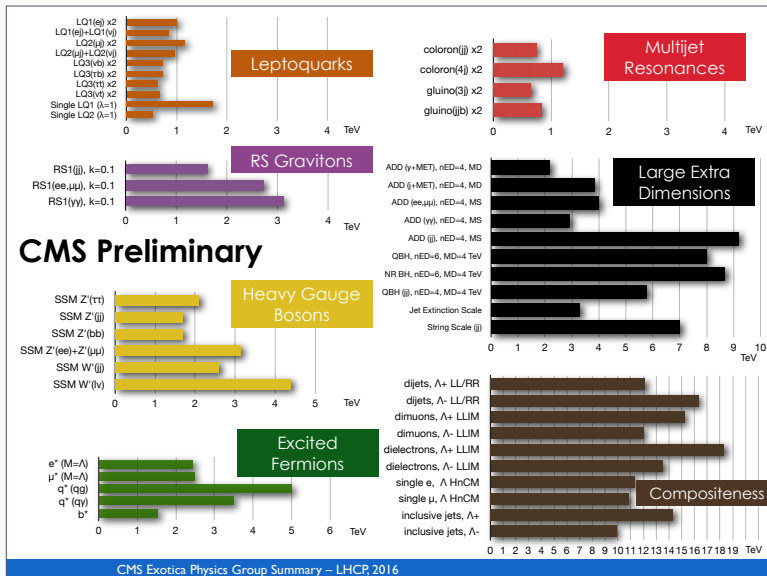
4 Summary

Introduction

Examples:

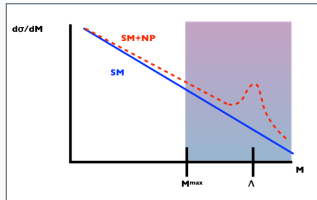


Remarkable agreement between theory predictions and the experiment measurements!



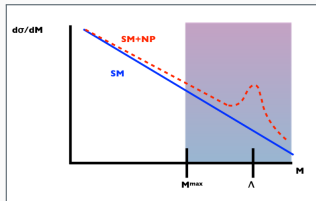
SMEFT a model-independent approach

- No BSM particle found
- Calls for precision test of SM



SMEFT a model-independent approach

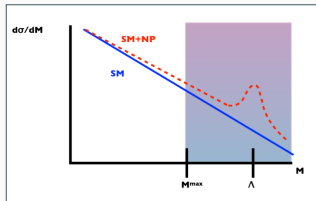
- No BSM particle found
- Calls for precision test of SM



- Standard Model Effective Field Theory (SMEFT)
 - SM particles
 - all possible operators satisfying symmetries of the SM
 - power counting: new physics scale Λ

SMEFT a model-independent approach

- No BSM particle found
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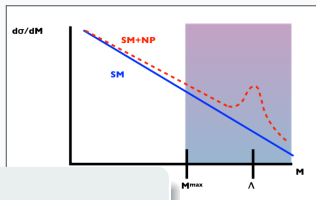
- Standard Model Effective Field Theory (SMEFT)
 - SM particles
 - all possible operators satisfying symmetries of the SM
 - power counting: new physics scale Λ

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum C_6 \mathcal{O}_6 + \frac{1}{\Lambda^4} \sum C_8 \mathcal{O}_8 + \dots$$

- No odd dimensions in this talk
 - ▶ \mathcal{L}_6 : 76 B-preserving Lagrangian terms, 2499 parameters [Grzadkowski et al. 2010](#)
 - ▶ \mathcal{L}_8 : 1031 Lagrangian terms, 44807 parameters [Murphy 2020](#); [Li et al. 2021](#)
- No specific model needed

SMEFT a model-independent approach

- No BSM particle found
- Calls for precision test of SM



In this talk:

Warsaw basis for dimension-6

Murphy's basis for dimension-8

- Standard Model
- SM par
- all pos
- power

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum C_6 \mathcal{O}_6 + \frac{1}{\Lambda^4} \sum C_8 \mathcal{O}_8 + \dots$$

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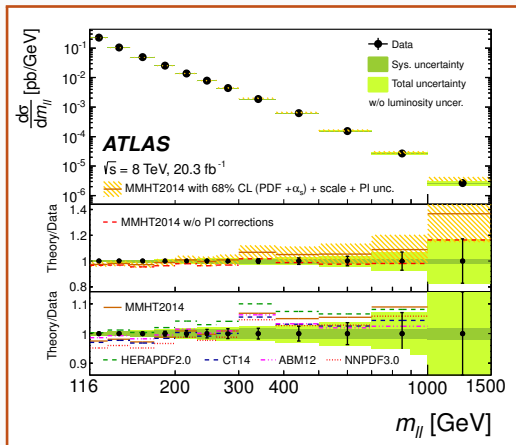
- How important are the dim-8 effects at LHC?
- How sensitive are current fits to the dim-8 effects?

We'll investigate those questions using LHC Drell-Yan data as an example:

- dilepton invariant mass spectrum [Boughezal, Mereghetti and Petriello, 2106.05337](#)
- dilepton double differential distribution (m_{ll} and p_T)
will address as p_T spectra in this talk [Boughezal YH, and Petriello to appear](#)

Dilepton invariant mass spectra

- Probe high m_{ll}
Up to 1.5 TeV
- 12 m_{ll} bins:
[116,130,150,175,200,
230,260,300,380,500,
700,1000,1500]



- Study scaling of cross sections in high energy limit (s, v)
- Only show some examples for each category
- q, l : left-handed fermion doublets
 e, u, d : right-handed fermion singlets
 ϕ : Higgs doublet

$$\mathcal{L}_{\psi^2 X^2 \phi}$$

$$\frac{C_{eB}}{\Lambda^2} \bar{l} \sigma^{\mu\nu} B_{\mu\nu} \phi e$$

$$\frac{C_{uW}}{\Lambda^2} \bar{q} \sigma^{\mu\nu} \tau^I W_{\mu\nu}^I \phi u$$

Dipole coupling

assume massless fermion

$$\sim \mathcal{O}(v^2 s / \Lambda^4)$$

$$\mathcal{L}_{\psi^2 \phi^2 D}$$

$$\frac{C_{Hl}^{(1)}}{\Lambda^2} \phi^\dagger \overleftrightarrow{D}^\mu \phi \bar{l} \gamma_\mu l$$

$$\frac{C_{Hu}}{\Lambda^2} \phi^\dagger \overleftrightarrow{D}^\mu \phi \bar{u} \gamma_\mu u$$

Z-vertex corrections

$$\sim \mathcal{O}(v^2 / \Lambda^2)$$

$$\mathcal{L}_{\psi^4}$$

$$\frac{C_{lq}^{(1)}}{\Lambda^2} \bar{l} \gamma^\mu l q \gamma_\mu q$$

$$\frac{C_{ld}}{\Lambda^2} \bar{l} \gamma^\mu l d \gamma_\mu d$$

Four-fermion interactions

$$\sim \mathcal{O}(s / \Lambda^2)$$

- Study scaling of cross sections in high energy limit (s, v)
- Only show some examples for each category
- q, l : left-handed fermion doublets
 e, u, d : right-handed fermion singlets
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$$\mathcal{L}_{\psi^4 D^2}$$

$$\frac{C_{l^2 q^2 D^2}^{(1)}}{\Lambda^4} \partial_\nu (\bar{l} \gamma^\mu l) \partial^\nu (\bar{q} \gamma_\mu q)$$
$$\frac{C_{l^2 d^2 D^2}^{(1)}}{\Lambda^4} \partial_\nu (\bar{l} \gamma^\mu l) \partial^\nu (\bar{d} \gamma_\mu d)$$

Momentum-dependent four-fermion
interactions
 $\sim \mathcal{O}(s^2/\Lambda^4)$

$$\mathcal{L}_{\psi^4 H^2}$$

$$\frac{C_{l^2 q^2 H^2}^{(1)}}{\Lambda^4} (\bar{l} \gamma^\mu l) (\bar{q} \gamma_\mu q) \phi^\dagger \phi$$
$$\frac{C_{l^2 d^2 H^2}^{(1)}}{\Lambda^4} (\bar{l} \gamma^\mu l) (\bar{d} \gamma_\mu d) \phi^\dagger \phi$$

Momentum-independent four-fermion
interactions
 $\sim \mathcal{O}(v^2 s/\Lambda^4)$

RELEVANT OPERATORS dimension-8 Z-vertex corrections

- Study scaling of cross sections in high energy limit (s, v)
- Only show some examples for each category
- q, l : left-handed fermion doublets
 e, u, d : right-handed fermion singlets
 ϕ : Higgs doublet

$$\mathcal{L}_{\psi^2 D^3}$$

$$\frac{C_{l^2 H^2 D^3}^{(1)}}{\Lambda^4} i \bar{l} \gamma^\mu D^\nu l (D_{(\mu} D_{\nu)} \phi)^\dagger \phi$$

$$\frac{C_{q^2 H^2 D^3}^{(3)}}{\Lambda^4} i \bar{q} \gamma^\mu \tau^I D^\nu q (D_{(\mu} D_{\nu)} \phi)^\dagger \tau^I \phi$$

Momentum-dependent Z-vertex corrections

$$\sim \mathcal{O}(v^2 s / \Lambda^4)$$

$$\mathcal{L}_{\psi^2 H^4 D}$$

$$\frac{C_{l^2 H^4 D}^{(1)}}{\Lambda^4} i (\bar{l} \gamma^\mu l) \left(\phi^\dagger \overleftrightarrow{D}_\mu \phi \right) \left(\phi^\dagger \phi \right)$$

$$\frac{C_{u^2 H^4 D}^{(1)}}{\Lambda^4} i (\bar{u} \gamma^\mu u) \left(\phi^\dagger \overleftrightarrow{D}_\mu \phi \right) \left(\phi^\dagger \phi \right)$$

Momentum-independent Z-vertex corrections

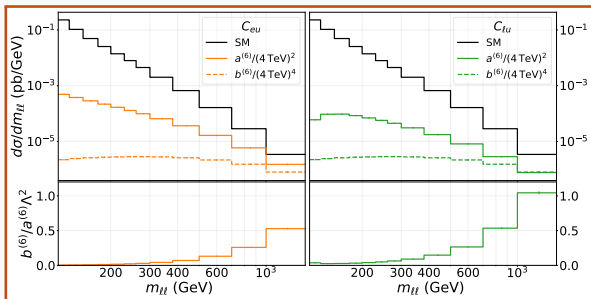
$$\sim \mathcal{O}(v^4 / \Lambda^4)$$

Structure of the SMEFT cross section

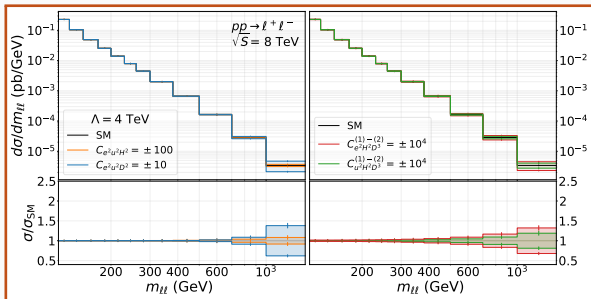
$$\frac{d\sigma}{dm_{\ell\ell}} = \frac{d\sigma_{\text{SM}}}{dm_{\ell\ell}} + \sum_i \left(\frac{a_i^{(6)}(m_{\ell\ell})}{\Lambda^2} C_i^{(6)} + \frac{a_i^{(8)}(m_{\ell\ell})}{\Lambda^4} C_i^{(8)} \right) + \sum_{i,j} \frac{b_{ij}^{(6)}(m_{\ell\ell})}{\Lambda^4} C_i^{(6)} C_j^{(6)}$$

- a_i, b_{ij} terms: NLO QCD corrections included (30%)
- SM: NNLO in QCD, NLL Sudakov logs through $\mathcal{O}(\alpha_s)$
- $\Lambda = 4 \text{ TeV} \gg 1.5 \text{ TeV}$ (the m_{ll} upper bound of the dataset)
- Complete to $\mathcal{O}(\alpha_s/\Lambda^2)$
Complete to $\mathcal{O}(1/\Lambda^4)$
at $\mathcal{O}(\alpha_s/\Lambda^4)$: missing $\psi^4 G$ -type operators

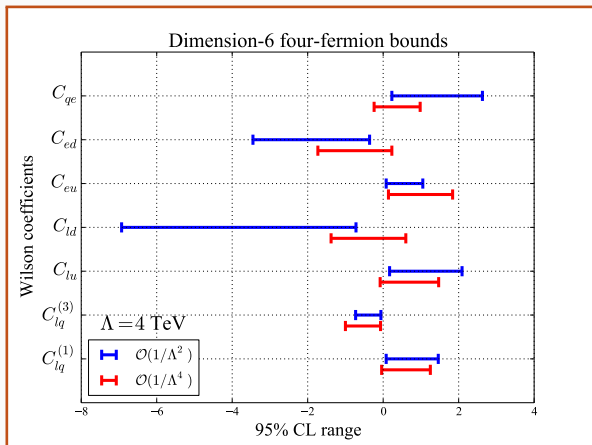
- ψ^4 : C_{eu} , C_{lu}
- Consider linear a_i terms ($1/\Lambda^2$) and quadratic b_{ii} terms ($1/\Lambda^4$)
- Quadratic terms: 50% (C_{eu}) or 100% (C_{lu}) in 1 – 1.5 TeV bin



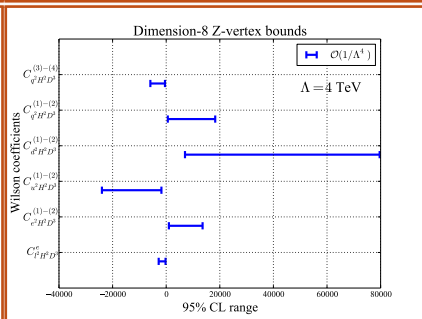
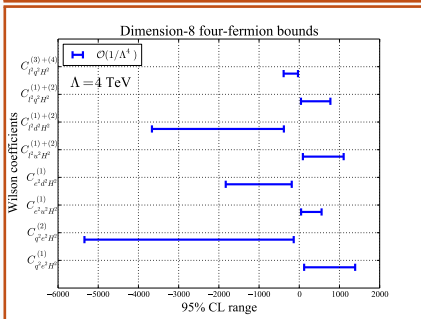
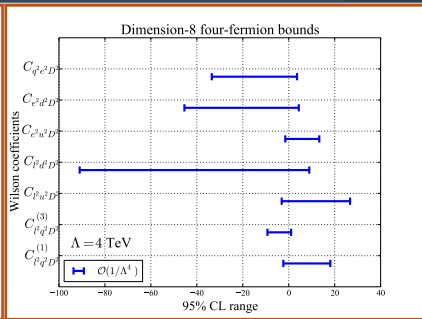
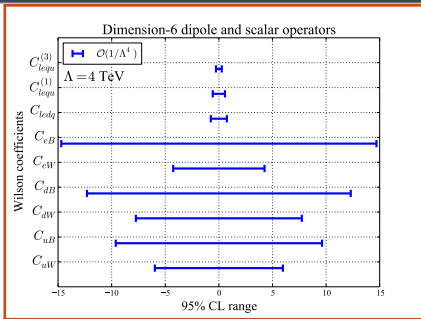
- $\psi^4 D^2$ -type: $C_{e^2 u^2 D^2}$
- $\psi^4 H^2$ -type: $C_{e^2 u^2 H^2}$
- $\psi^2 D^3$ -type:
 $C_{e^2 H^2 D^3}$, $C_{u^2 H^2 D^3}$
- dim-8 terms: major contribution from $\psi^4 D^2$ -type

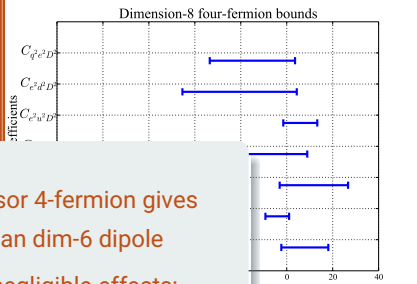
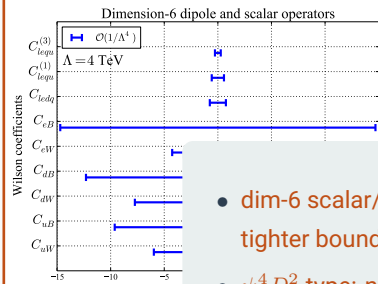


- Turn on one coupling at a time
- Experimental error matrix; **1606.01736**
NNPDF 3.1 PDF errors;
NLO QCD scale variation errors

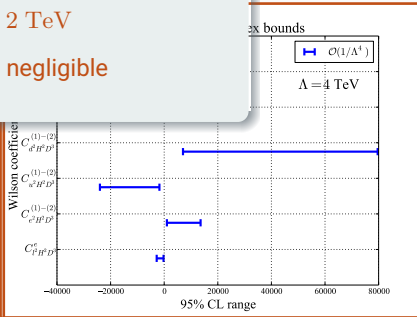
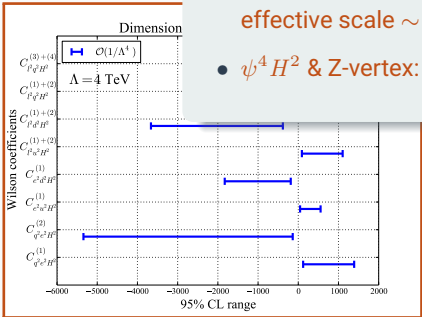


- effective scale $\Lambda/\sqrt{C} \sim 4 \text{ TeV} \gg 1.5 \text{ TeV}$
- Large shift from $1/\Lambda^4$ effects: factors of 2-3 for C_{qe} , C_{ld}





- dim-6 scalar/tensor 4-fermion gives tighter bounds than dim-6 dipole
- $\psi^4 D^2$ -type: non-negligible effects; effective scale $\sim 2 \text{ TeV}$
- $\psi^4 H^2$ & Z-vertex: negligible



	dim-6	single coupling	marginalized	marginalized*
C_{eu}	[0.08, 1.0]	[0.1, 1.8]	[-39, 39]	[-0.6, 2.4]
$C_{e^2 u^2 D^2}$	-	[-1.5, 13]	$[-17, 9.2 \cdot 10^3]$	[-14, 18]
$C_{e^2 u^2 H^2}$	-	[45, 555]	$[-1.9, 1.2] \cdot 10^4$	[-256, 256]
$C_{u^2 H^2 D^3}^{(1)-(2)}$	-	$[-24, -1.8] \cdot 10^3$	$[-1.2, 1.8] \cdot 10^5$	[-256, 256]

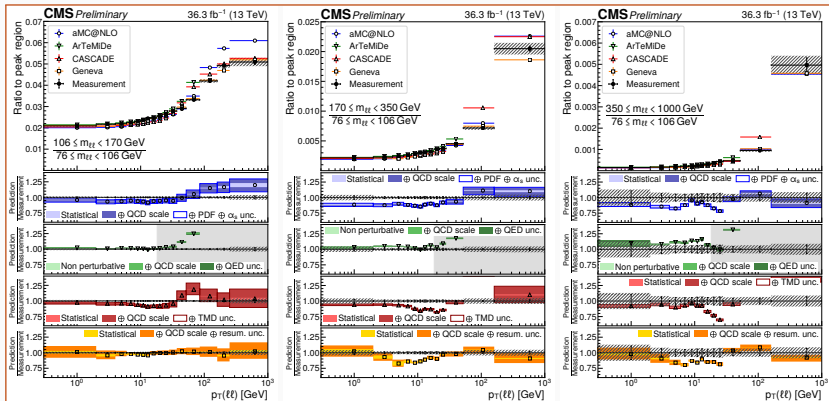
- dim-6: Turn on **one coupling** at a time, **only include** $\mathcal{O}(1/\Lambda^2)$
- single coupling: Turn on **one coupling** at a time, **include** $\mathcal{O}(1/\Lambda^4)$
- marginalized: Turn on **all couplings**
- marginalized*: Turn on **all couplings**, and demand effective scale **greater than 1 TeV** for last two operators

Bounds on dim-6 Wilson coefficient significantly weakened by turning on dim-8 operators

Dilepton mass-dependent p_T spectra

Boughezal, YH, and Petriello, to appear

**Dilepton mass-dependent p_T spectra
with CMS data**



- Ratios of differential unfolded cross sections in $p_T(\ell\ell)$ for invariant mass ranges with respect to the peak region $76 < m_{\ell\ell} < 106$ GeV
- ~~$50 < m_{\ell\ell} < 76$ GeV~~ $106 < m_{\ell\ell} < 170$ GeV (left)
 $170 < m_{\ell\ell} < 350$ GeV (center) $350 < m_{\ell\ell} < 1000$ GeV (right)
- Smaller uncertainties than the cross sections
- We'll use the last 3 $m_{\ell\ell}$ bins as the experimental dataset

MOST RELEVANT OPERATORS

- Study scaling of cross sections in high energy limit, **only highest in s**
- Only show some examples for each category
- q, l : left-handed fermion doublets
 e, u, d : right-handed fermion singlets
 ϕ : Higgs doublet, G : Gluon field strength tensor

$$\mathcal{L}_{\psi^4}$$

$$\frac{C_{eu}}{\Lambda^2} (\bar{e}\gamma^\mu e)(\bar{u}\gamma_\mu u)$$

$$\frac{C_{qe}}{\Lambda^2} (\bar{q}\gamma^\mu q)(\bar{e}\gamma_\mu e)$$

Four-fermion interactions

$$\sim \mathcal{O}(s/\Lambda^2)$$

$$\mathcal{L}_{\psi^4 D^2}$$

$$\frac{C_{eu}^{(1)}}{\Lambda^4} D^\nu (\bar{e}\gamma^\mu e) D_\nu (\bar{u}\gamma_\mu u)$$

$$\frac{C_{qe}^{(1)}}{\Lambda^4} D^\nu (\bar{q}\gamma^\mu q) D_\nu (\bar{e}\gamma_\mu e)$$

Momentum-dependent
four-fermion interactions

$$\sim \mathcal{O}(s^2/\Lambda^4)$$

$$\mathcal{L}_{\psi^4 G}$$

$$\frac{C_{eu}^{(1)}}{\Lambda^4} (\bar{e}\gamma^\mu e) (\bar{u}\gamma^\nu T^a u) G_{\mu\nu}^a$$

$$\frac{C_{qe}^{(1)}}{\Lambda^4} (\bar{q}\gamma^\mu T^a q) (\bar{l}\gamma_\nu l) G_{\mu\nu}^a$$

Four-fermion interactions with
gluon field strength tensor

$$\sim \mathcal{O}(s^2/\Lambda^4)$$

Structure of the SMEFT cross section

$$\frac{d\sigma}{dp_T(\ell\ell)} = \frac{d\sigma_{\text{SM}}}{dp_T} + \sum_i \left(\frac{a_i^{(6)}(p_T)}{\Lambda^2} C_i^{(6)} + \frac{a_i^{(8)}(p_T)}{\Lambda^4} C_i^{(8)} \right) + \sum_{i,j} \frac{b_{ij}^{(6)}(p_T)}{\Lambda^4} C_i^{(6)} C_j^{(6)}$$

- Choose 3 operators (involving right-handed quarks and leptons) as example:

$$Q_{eu}: \frac{C_{eu}}{\Lambda^2} (\bar{e}\gamma^\mu e)(\bar{u}\gamma_\mu u)$$

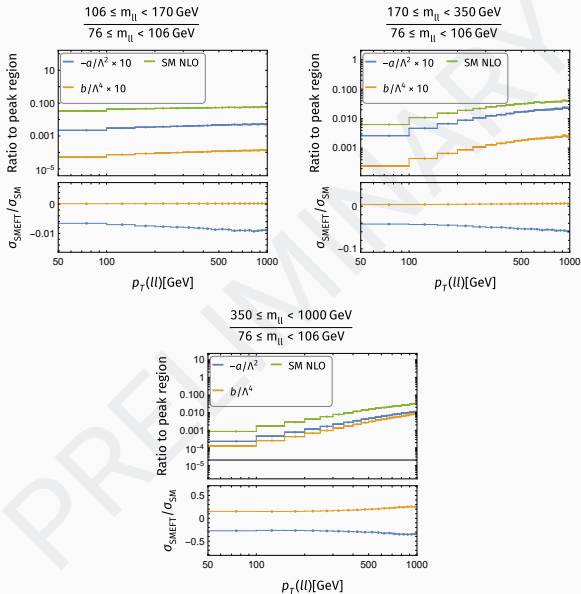
$$Q_{e^2u^2D^2}^{(1)}: \frac{C_{e^2u^2D^2}^{(1)}}{\Lambda^4} D^\nu (\bar{e}\gamma^\mu e) D_\nu (\bar{u}\gamma_\mu u)$$

$$Q_{e^2u^2G}^{(2)}: \frac{C_{e^2u^2G}^{(2)}}{\Lambda^4} (\bar{e}\gamma^\mu e) (\bar{u}\gamma^\nu T^a u) \tilde{G}_{\mu\nu}^a$$

- SM: NLO QCD
- SMEFT corrections: LO
- $\Lambda = 2 \text{ TeV}$

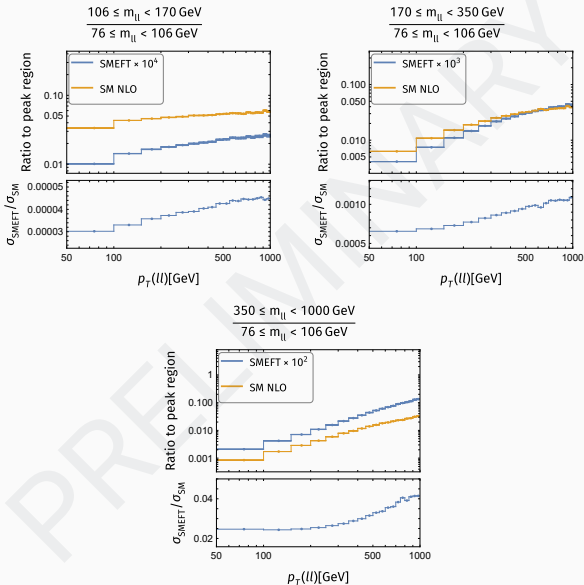
- p_T bins: 50 GeV constant bin widths
- Largest corrections to the ratio
- 10-30% for the highest m_{ll} bin
- Slowest increase as p_T goes higher

C_{eu}



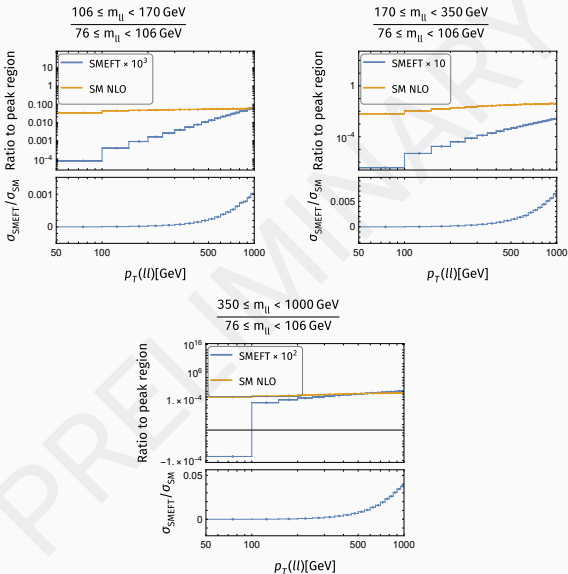
- p_T bins: 50 GeV constant bin widths
- Smaller corrections to the ratio than dim-6
- Slower increase than $\psi^4 G$ -type as p_T goes higher, but faster than dim-6

$$C_{e^2 u^2 D^2}^{(1)}$$



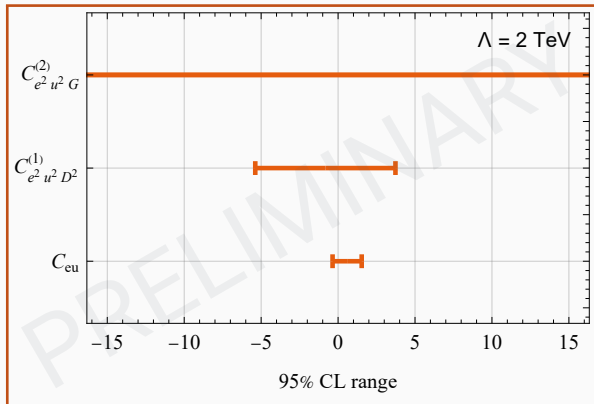
- p_T bins: 50 GeV constant bin widths
- Smaller corrections to the ratio than dim-6
- Fastest increase as p_T goes higher

$$C_{e^2 u^2 G}^{(2)}$$



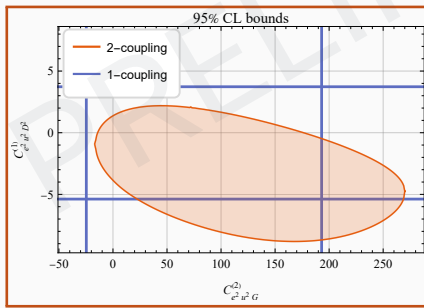
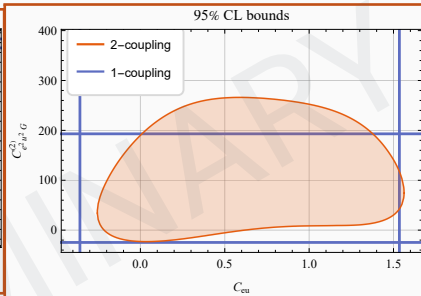
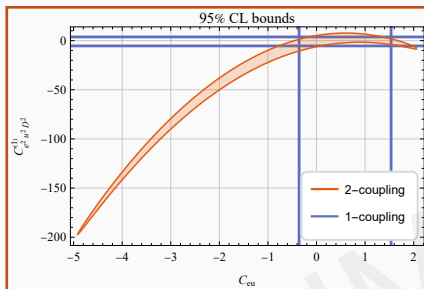
SINGLE-COUPLING FITS

- Fit with CMS data
- Experimental error matrix;
[CMS-PAS-SMP-20-003](#)
NNPDF 3.1 PDF errors;
SM NLO QCD +
LO SMEFT corrections
for scale variation errors
- Only includes bins with $p_T \geq 52$ GeV

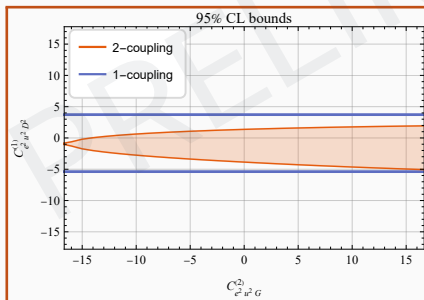
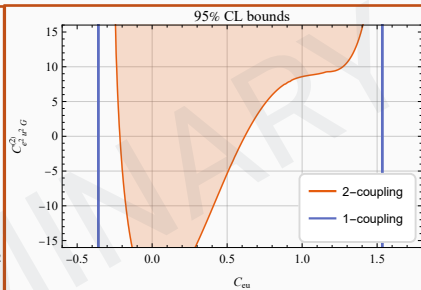
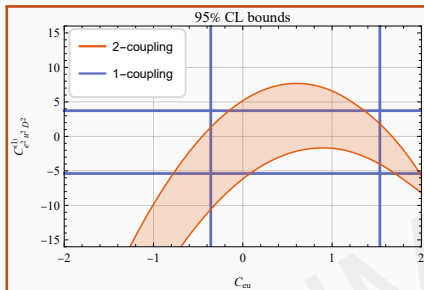


- effective scale $\gtrsim 1$ TeV $\Rightarrow |C_6| \leq 4, |C_8| \leq 16$

MULTI-COUPLING FITS Enabling 2 operators



MULTI-COUPLING FITS Enabling 2 operators



- effective scale $\gtrsim 1$ TeV
 $\Rightarrow |C_6| \leq 4, |C_8| \leq 16$

MULTI-COUPLING FITS Enabling 2 or 3 operators

Wilson coefficient	Single coupling	Marginalized	Marginalized*
$C_{eu} & C_{e^2 u^2 D^2}^{(1)}$			
C_{eu}	[-0.358, 1.53]	[-4.12, 1.72]	[-1.42, 1.43]
$C_{e^2 u^2 D^2}^{(1)}$	[-5.38, 3.73]	[-122., 53.7]	[-15.6, 8.03]
$C_{eu} & C_{e^2 u^2 G}^{(2)}$			
C_{eu}	[-0.358, 1.53]	[-0.197, 1.40]	[-0.581, 1.43]
$C_{e^2 u^2 G}^{(2)}$	[-24.7, 193.]	[-7.05, 231.]	[-14.6, 16.0]
all 3 operators			
C_{eu}	[-0.358, 1.53]	[-4.57, 2.00]	[-1.41, 1.44]
$C_{e^2 u^2 D^2}^{(1)}$	[-5.38, 3.73]	[-155., 69.6]	[-15.5, 7.94]
$C_{e^2 u^2 G}^{(2)}$	[-24.7, 193.]	[-5.95, 250.]	[-15.1, 16.0]

- $C_{e^2 u^2 G}^{(2)}$ does not change the bounds on C_{eu} very much
- $C_{e^2 u^2 D^2}^{(1)}$ changes the bounds on C_{eu} by a lot

Marginalized*: effective scale constraint ($\gtrsim 1$ TeV) on dim-8 operators

**Dilepton mass-dependent p_T spectra
with HL-LHC pseudo-data**

GENERATION OF PSEUDO-DATA

- m_U bins: [Panico, Ricci, and Wulzer 2021](#)

[300, 360, 450, 600, 800, 1100, 1500, 2000, 2600]

- p_T bins:

- Assuming all **stat. errors < 5%**, coarser binning

m_U/GeV	p_T/GeV bins
300 – 360	[100, 110, 120, 130, 140, 150, 160, 170, 180, 190, 200, 210, 220, 230, 250, 270, 290, 310, 330, 360, 380, 410, 440, 490, 570, 7000]
360 – 450	[100, 110, 120, 130, 140, 150, 160, 170, 180, 200, 230, 250, 270, 290, 310, 330, 350, 370, 400, 440, 490, 580, 7000]
450 – 600	[100, 110, 120, 130, 140, 150, 160, 170, 180, 190, 210, 230, 250, 270, 290, 320, 340, 360, 390, 430, 480, 580, 7000]
600 – 800	[100, 110, 120, 130, 150, 170, 200, 220, 250, 290, 320, 360, 420, 520, 7000]
800 – 1100	[100, 110, 120, 150, 170, 200, 230, 270, 330, 430, 7000]
1100 – 1500	[100, 200, 290, 7000]
1500 – 2000	[100, 7000]
2000 – 2600	[100, 7000]

GENERATION OF PSEUDO-DATA

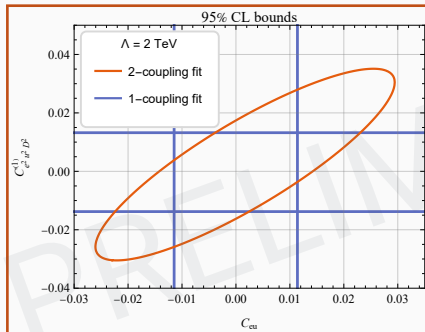
- m_U bins:
[300, 360, 450, 600, 800, 1100, 1500, 2000, 2600]
- p_T bins:
 - Assuming all **stat. errors < 5%**, **coarser binning**
 - Assuming all **stat. errors < 10%**, **finer binning**

m_U/GeV	p_T bins/GeV
300 – 360	[100, 110, 120, 130, 140, 150, 160, 170, 180, 190, 200, 210, 220, 230, 250, 270, 290, 310, 330, 350, 370, 400, 420, 440, 470, 500, 530, 560, 600, 660, 760, 7000]
360 – 450	[100, 110, 120, 130, 140, 150, 160, 170, 180, 190, 200, 210, 220, 240, 260, 290, 310, 330, 350, 370, 390, 410, 440, 470, 500, 530, 560, 610, 670, 770, 7000]
450 – 600	[100, 110, 120, 130, 140, 150, 160, 190, 210, 230, 250, 270, 290, 320, 340, 370, 390, 420, 460, 490, 520, 550, 580, 620, 680, 780, 7000]
600 – 800	[100, 110, 120, 130, 150, 170, 200, 220, 240, 260, 280, 310, 340, 380, 410, 440, 470, 510, 550, 620, 730, 7000]
800 – 1100	[100, 110, 120, 140, 160, 180, 200, 220, 250, 270, 300, 330, 360, 410, 460, 540, 660, 7000]
1100 – 1500	[100, 130, 160, 190, 230, 270, 320, 400, 520, 7000]
1500 – 2000	[100, 210, 330, 7000]
2000 – 2600	[100, 7000]

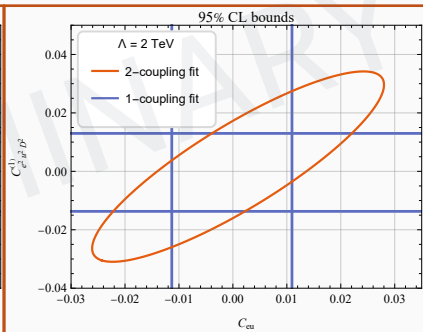
GENERATION OF PSEUDO-DATA

- m_U bins:
[300, 360, 450, 600, 800, 1100, 1500, 2000, 2600]
- p_T bins:
 - Assuming all stat. errors < 5%, coarser binning
 - Assuming all stat. errors < 10%, finer binning
- assume 1% uncorrelated sys. error and 2% correlated sys. error

Fit to data with <5% error

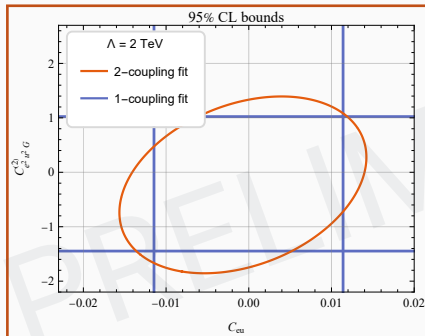


Fit to data with <10% error

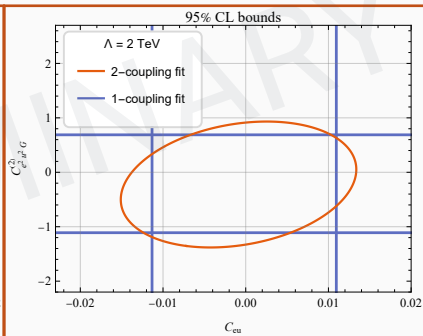


- C_{eu} & $C_{e^2 u^2 D^2}^{(1)}$ are highly correlated
- need other experiments to independently constrain C_{eu}
i.e. low-energy PVES experiments such as SoLID
- Tighter bounds from “<10%” dataset

Fit to data with <5% error



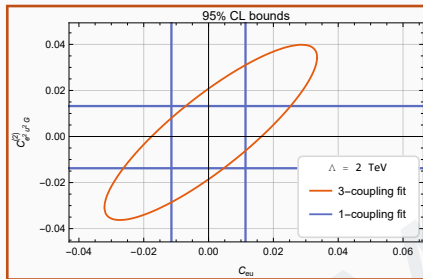
Fit to data with <10% error



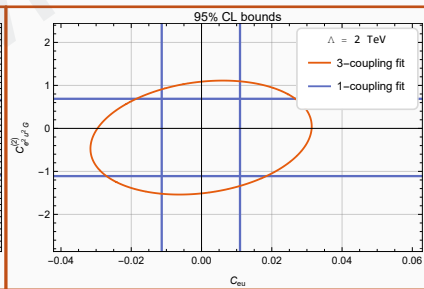
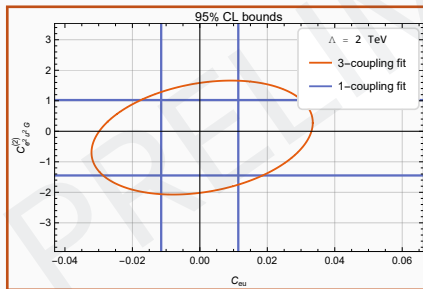
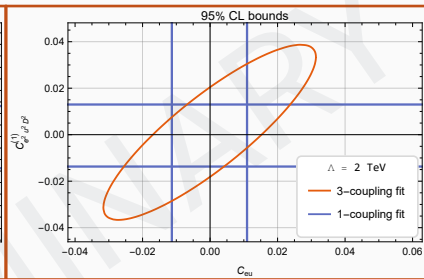
- C_{eu} & $C_{e^2 u^2 G}^{(2)}$ are almost uncorrelated
- Can independently determine C_{eu} with m_{ll} and $C_{e^2 u^2 G}^{(2)}$ with p_T spectra
- Tighter bounds from “<10%” dataset

3-COUPLING FITS project to 2-d

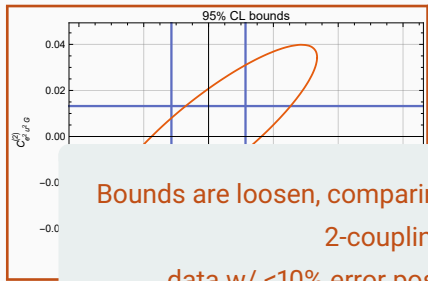
Fit to data with <5% error



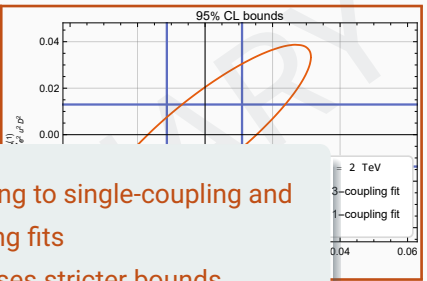
Fit to data with <10% error



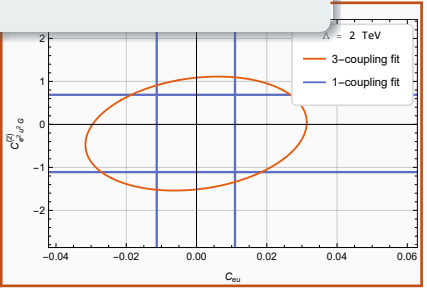
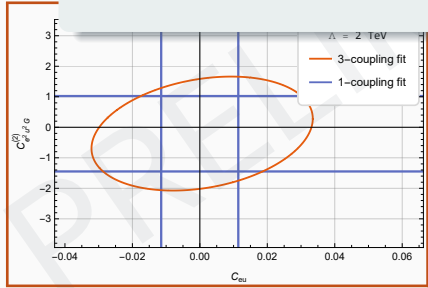
Fit to data with <5% error



Fit to data with <10% error



Bounds are looser, comparing to single-coupling and 2-coupling fits
data w/ <10% error poses stricter bounds



Summary

- Included $\mathcal{O}(1/\Lambda^4)$ effects
- Analyzed scaling in high energy limit: justified to only include operators with $\mathcal{O}(s/\Lambda^2)$ or $\mathcal{O}(s^2/\Lambda^4)$ scaling
- Effects of those dim-8 operators with highest scaling can not be neglected
- Study on Drell-Yan m_{ll} and p_T spectra both indicate strong correlation between C_{eu} & $C_{e^2u^2D^2}^{(1)}$
- Study on Drell-Yan p_T spectra reveals nearly no correlation between C_{eu} & $C_{e^2u^2G}^{(2)}$
- C_{eu} & $C_{e^2u^2D^2}^{(1)}$: flat direction; calls for other experiments such as PVES

Thanks for your attention!

Backup