

# OBSERVABLE PROTON DECAY IN FLIPPED SU(5)

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based on work in collaboration with:

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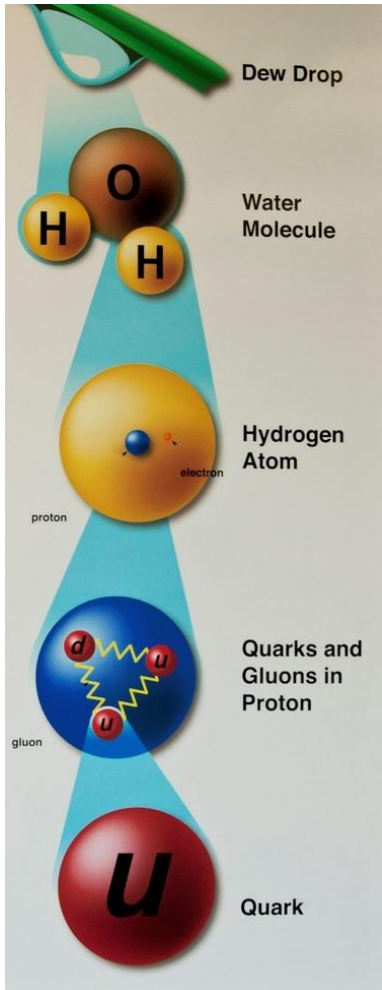
Qaisar Shafi

<https://arxiv.org/abs/2010.01665>

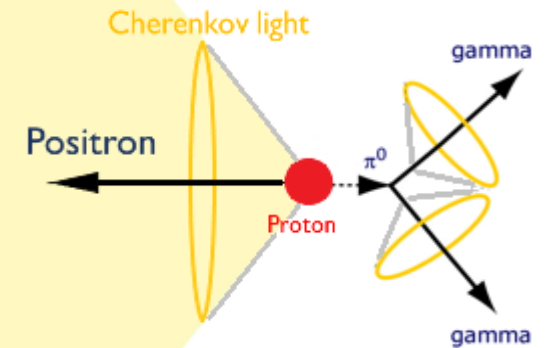
Journal reference: *JHEP* 02 (2021) 181

Pheno 2022  
University of Pittsburgh  
May 10, 2022

# OVERVIEW



- Model: Flipped SU(5)
- Proton Decay in Flipped SU(5)
- Comparison of Flipped SU(5) and SU(5)
- Summary



# MODEL: FLIPPED SU(5)

- Gauge group:  $SU(5) \times U(1)_X$
- Global  $U(1)_R$  symmetry and  $\mathbb{Z}_2$  matter parity
- Superpotential:

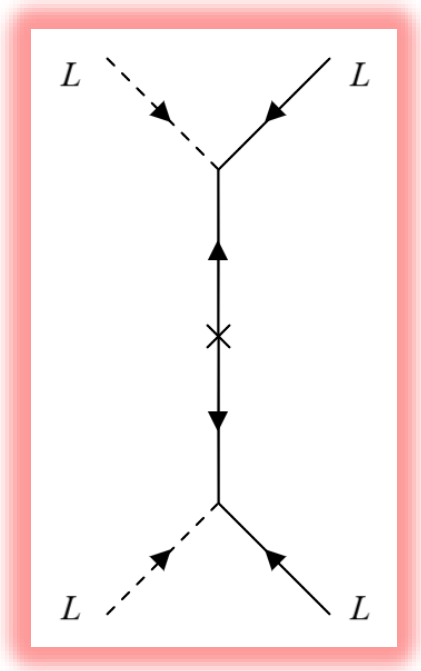
$$\begin{aligned}
 W = & \kappa S \left( 10_H^1 \overline{10}_H^{-1} - M^2 \right) \\
 & + \frac{\lambda}{8} 10_H^1 10_H^1 5_h^{-2} + \frac{\bar{\lambda}}{8} \overline{10}_H^{-1} \overline{10}_H^{-1} \overline{5}_h^2 \\
 & + \frac{1}{8} y_{ij}^{(d)} 10_i^1 10_j^1 5_h^{-2} + y_{ij}^{(u,\nu)} 10_i^1 \overline{5}_j^{-3} \overline{5}_h^2 + y_{ij}^{(e)} 1_i^5 \overline{5}_j^{-3} 5_h^{-2} + W_{HN}
 \end{aligned}$$

- $W_{HN}$ : Inverse seesaw mechanism

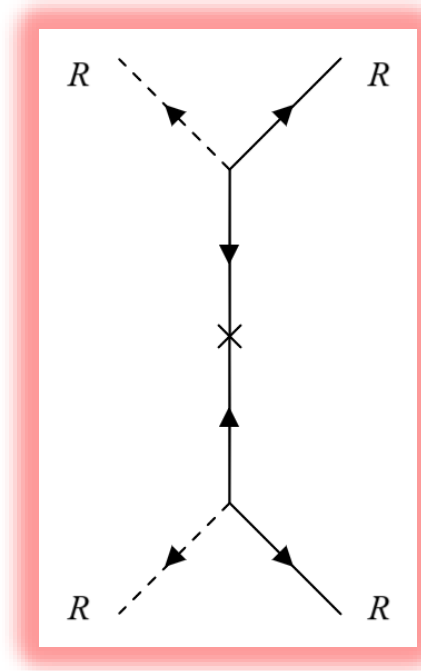
$SU(5)^{q(X)}$	$3_c \times 2_L \times 1_Y$	$q(R)$	$\mathbb{Z}_2$
$10^1$	$Q(3 \ 2 \ 1/6)$ $D^c(\overline{3} \ 1 \ 1/3)$ $N^c(1 \ 1 \ 0)$	0	-1
$\overline{5}^{-3}$	$U^c(\overline{3} \ 1 \ -2/3)$ $L(1 \ 2 \ -1/2)$	0	-1
$1^5$	$E^c(1 \ 1 \ 1)$	0	-1
$10_H^1$	$Q_H(3 \ 2 \ 1/6)$ $D_H^c(\overline{3} \ 1 \ 1/3)$ $N_H^c(1 \ 1 \ 0)$	0	+1
$\overline{10}_H^{-1}$	$\overline{Q}_H(\overline{3} \ 2 \ -1/6)$ $\overline{D}_H^c(\overline{3} \ 1 \ -1/3)$ $\overline{N}_H^c(1 \ 1 \ 0)$	0	+1
$5_h^{-2}$	$D_h(3 \ 1 \ -1/3)$ $H_d(1 \ 2 \ -1/2)$	1	+1
$\overline{5}_h^2$	$\overline{D}_h(\overline{3} \ 1 \ 1/3)$ $H_u(1 \ 2 \ 1/2)$	1	+1
$S$	$S(1 \ 1 \ 0)$	1	+1

# CHIRALITY TYPES

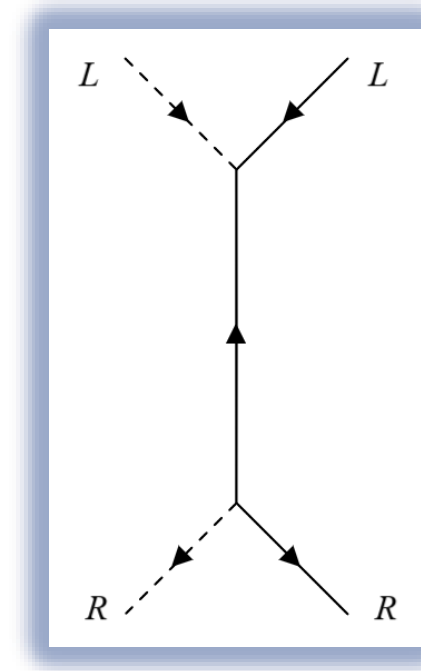
LLLL



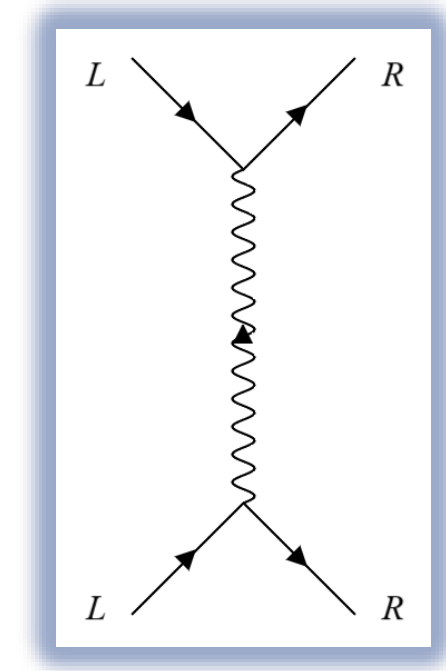
RRRR



LLRR



LRLR



Solid line: fermion, Dashed line: boson, Wavy line: gauge boson  
L: left chiral, R: right chiral

# PROTON DECAY IN FLIPPED SU(5):

- **I- Dimension four operators (rapid proton decay)** forbidden by  $\mathbb{Z}_2$  matter parity and  $U(1)_R$  symmetry
- **II-Dimension five operators (rapid proton decay)** forbidden by  $U(1)_R$  symmetry, no GUT scale mass terms for Higgs 5-plet  $5_h \bar{5}_h$  and Higgs 10-plet  $10_H \bar{10}_H$
- **III-Dimension six operators (observable proton decay)** of chirality type LLRR is mediated via color triplets of 5-plets and chirality type LRLR is mediated via gauge bosons

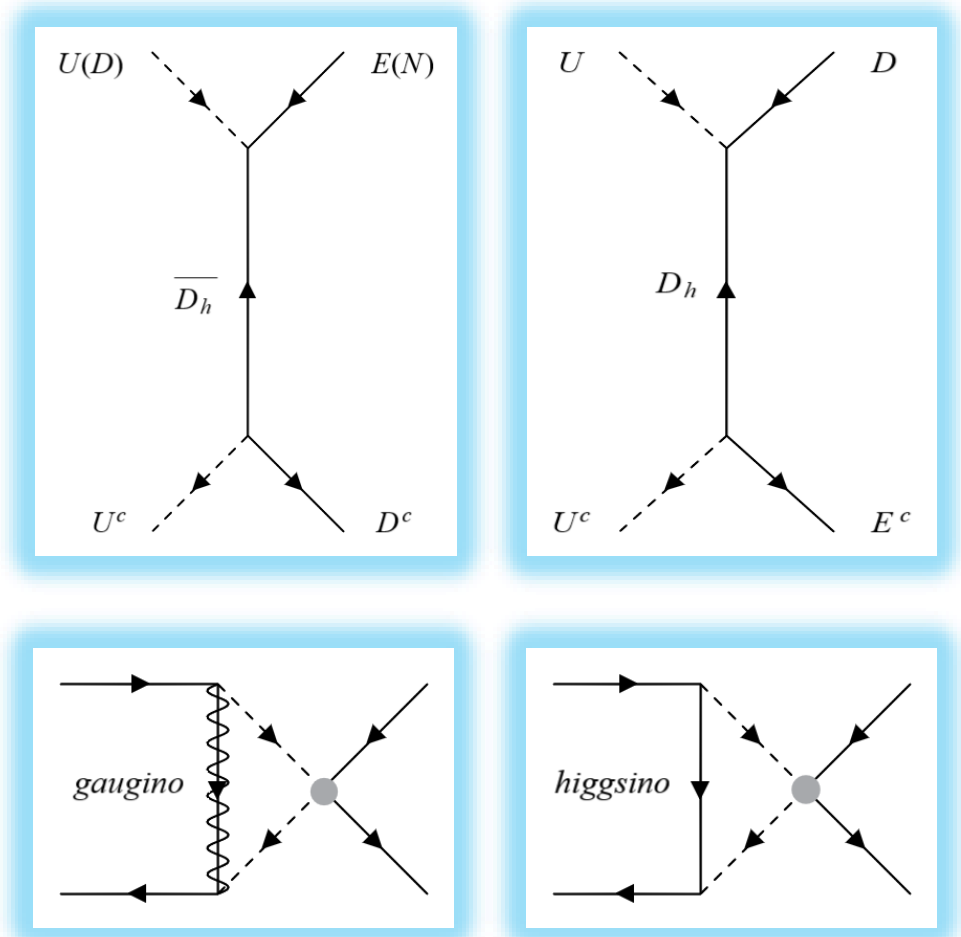
- Proton decay interaction terms from W:

$$W \supset L \left( U_L y_D^{(u,\nu)} \right) Q \bar{D}_h + U^c \left( y_D^{(u,\nu)} V P^* \right) D^c \bar{D}_h \\ - \frac{1}{2} Q \left( V^* P y_D^{(d)} V^\dagger \right) Q D_h + U^c \left( U_L^\dagger y_D^{(e)} \right) E^c D_h.$$

- Proton decay interaction terms from K:

$$K \supset \sqrt{2} g_5 \left( -(U^c)^\dagger \mathcal{X}(U_L^T L) + (Q)^\dagger \mathcal{X}(V P^* D^c) + \text{h.c.} \right)$$

# DIMENSION SIX: I-TWO FERMIONS TWO SCALARS OPERATOR



- Non-chirality flipping operator LLRR with two fermions and two scalars is dimension six operator!

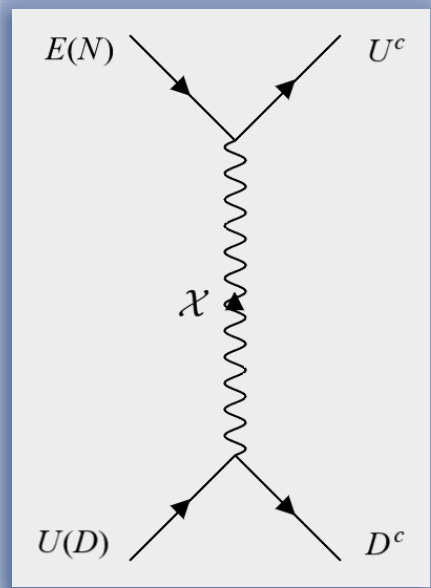
$$\mathcal{L} \supset \frac{1}{m_P^2} \int d^4\theta \Phi \Phi^\dagger \Phi \Phi^\dagger \supset \frac{1}{m_P^2} \bar{\psi} \not{\partial} \psi \phi^* \phi$$

where

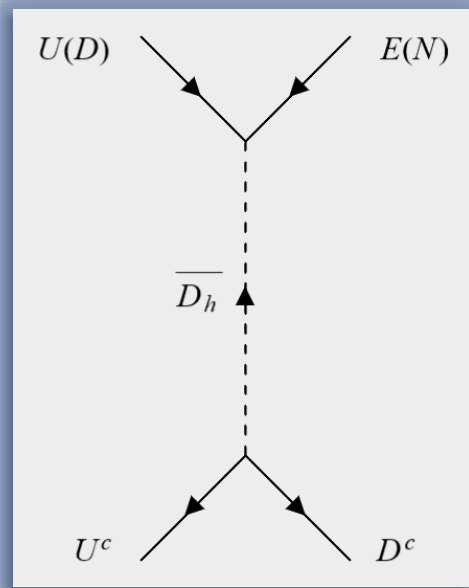
$$\Phi \supset \phi(x) + \sqrt{2}\theta\psi(x) - i\frac{1}{\sqrt{2}}\theta^2\partial^\mu\psi(x)\sigma_\mu\bar{\theta}.$$

- Needs a box diagram to become effective four fermi operator.
- This contribution is suppressed by loop factor

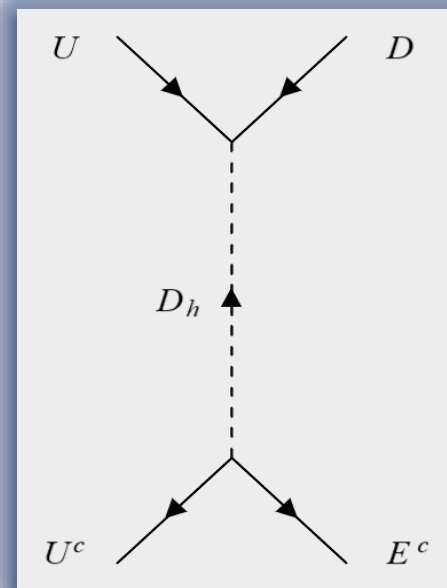
# DIMENSION SIX: II- FOUR FERMIONS PROTON DECAY OPERATORS



(a)



(b)



(c)

Dimension six proton decay mediated via gauge bosons (a) and color triplets of 5-plet (b) and (c).

# DIMENSION SIX: PROTON DECAY OPERATORS

- Effective dimension six proton decay operators:

$$\begin{aligned}\mathcal{L}_6^{\text{eff}} &= C_{6(1)}^{ijkl} (U^c)_i^\dagger (D^c)_j^\dagger Q_k L_l + C_{6(2)}^{ijkl} Q_i Q_j (U^c)_k^\dagger (E^c)_l^\dagger, \\ &\supset (U^c)_i^\dagger (D^c)_j^\dagger C_{6(1)}^{ijkl} (U_k E_l + (V D)_k (U_{PMNS} N)_l) \\ &\quad + (U_i (V D)_j + (V D)_i U_j) C_{6(2)}^{ijkl} (U^c)_k^\dagger (E^c)_l^\dagger,\end{aligned}$$

- Wilson coefficients:

$$\begin{aligned}C_{6(1)}^{ijkl} &= e^{i\varphi_j} \left( \frac{(U_L)_{li} V_{kj}^*}{M^2} + \frac{(V^\dagger y_D^{(u,\nu)})_{ji} (U_L y_D^{(u,\nu)})_{lk}}{M_\lambda^2} \right), \\ C_{6(2)}^{ijkl} &= - \left( \frac{(V^* P y_D^{(d)} V^\dagger)_{ij} (U_L^T y_D^{(e)})_{kl}}{2M_\lambda^2} \right).\end{aligned}$$

where,

$$M_\lambda = \lambda M \qquad M_{\bar{\lambda}} = \bar{\lambda} M$$



# DECAY RATES: I-CHARGED LEPTON (ELECTRON, MUON) CHANNELS

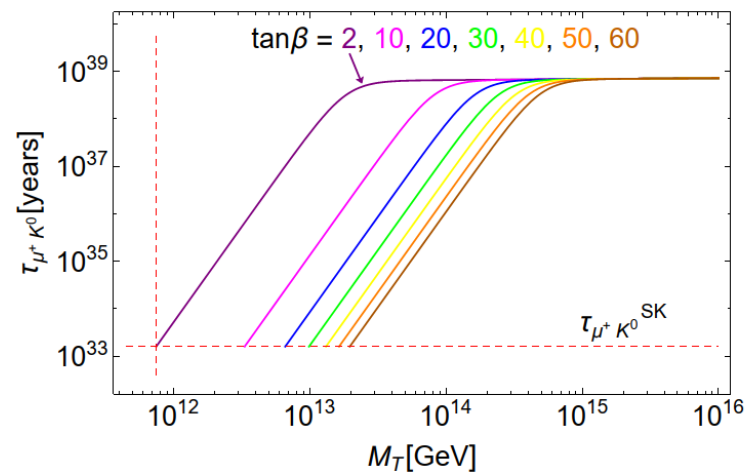
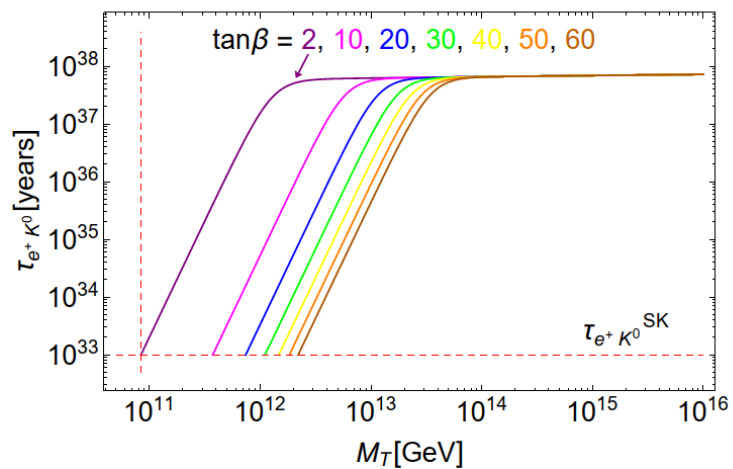
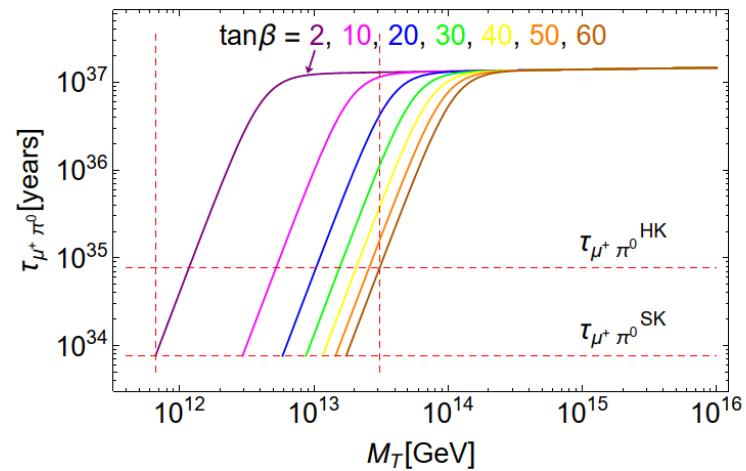
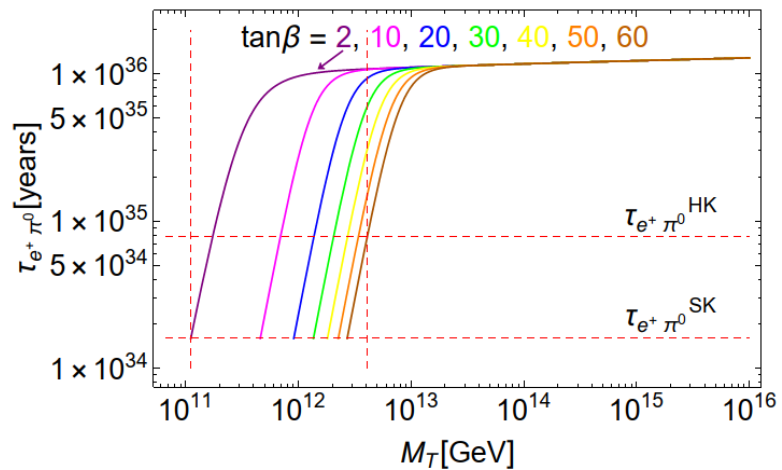
$$\Gamma_{p \rightarrow \pi^0 l_i^+} = k_\pi |C_{\pi^0 l_i^+}|^2 \left( A_{S_1}^2 \left| \frac{1}{M^2} + \left( \frac{m_u}{v_u} \right)^2 \frac{1}{M_\lambda^2} \right|^2 + A_{S_2}^2 \left| \frac{m_d}{v_d} \frac{m_{l_i}}{v_d} \frac{1}{M_\lambda^2} \right|^2 \right),$$

$$\Gamma_{p \rightarrow K^0 l_i^+} = k_K |C_{K^0 l_i^+}|^2 \left( A_{S_1}^2 \left| \frac{1}{M^2} + \left( \frac{m_u}{v_u} \right)^2 \frac{1}{M_\lambda^2} \right|^2 + A_{S_2}^2 \left| \frac{m_s}{v_d} \frac{m_{l_i}}{v_d} \frac{1}{M_\lambda^2} \right|^2 \right),$$

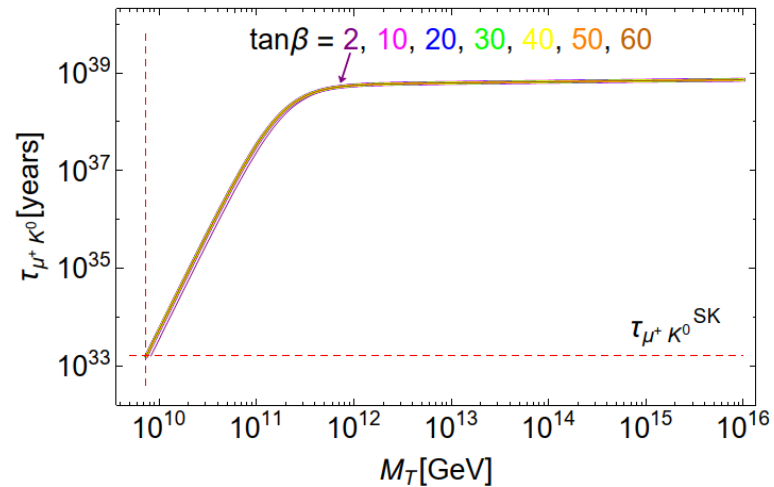
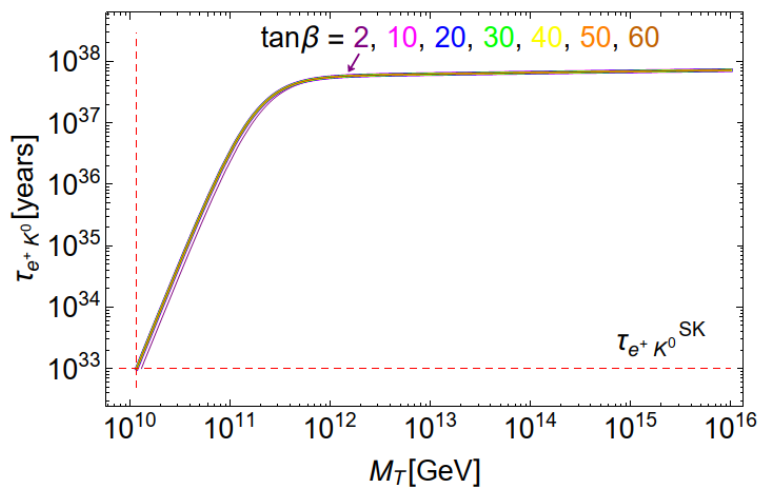
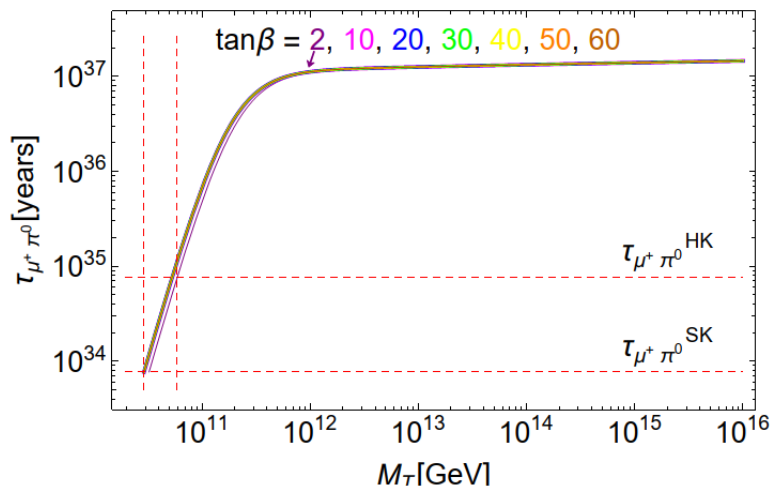
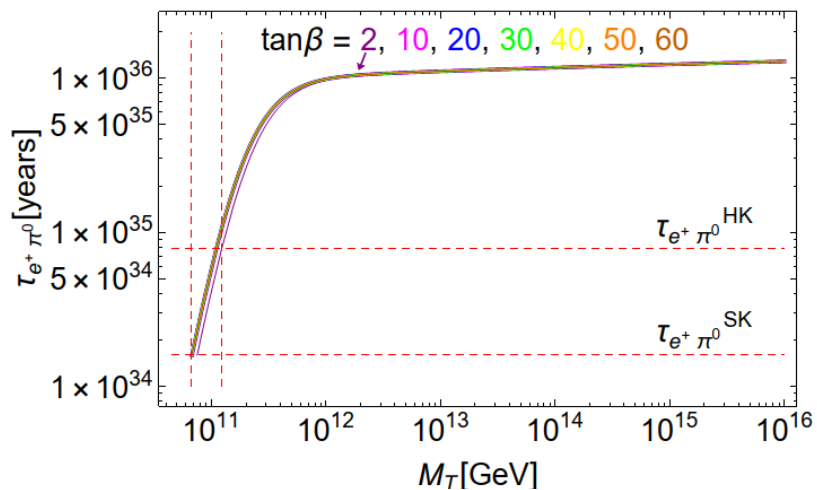
$$k_\pi = \frac{m_p A_L^2}{32\pi} \left( 1 - \frac{m_\pi^2}{m_p^2} \right)^2, \quad k_K = \frac{m_p A_L^2}{32\pi} \left( 1 - \frac{m_K^2}{m_p^2} \right)^2,$$

$$C_{\pi^0 l_i} = T_{\pi^0 l_i} (U_L)_{i1} V_{ud}^*, \quad C_{K^0 l_i} = T_{K^0 l_i} (U_L)_{i1} V_{us}^*.$$

# CASE I: $M_T = M_\lambda = M_{\bar{\lambda}}$



# CASE II: $M_T = M_{\tilde{\lambda}^-} \ll M_{\tilde{\lambda}}$



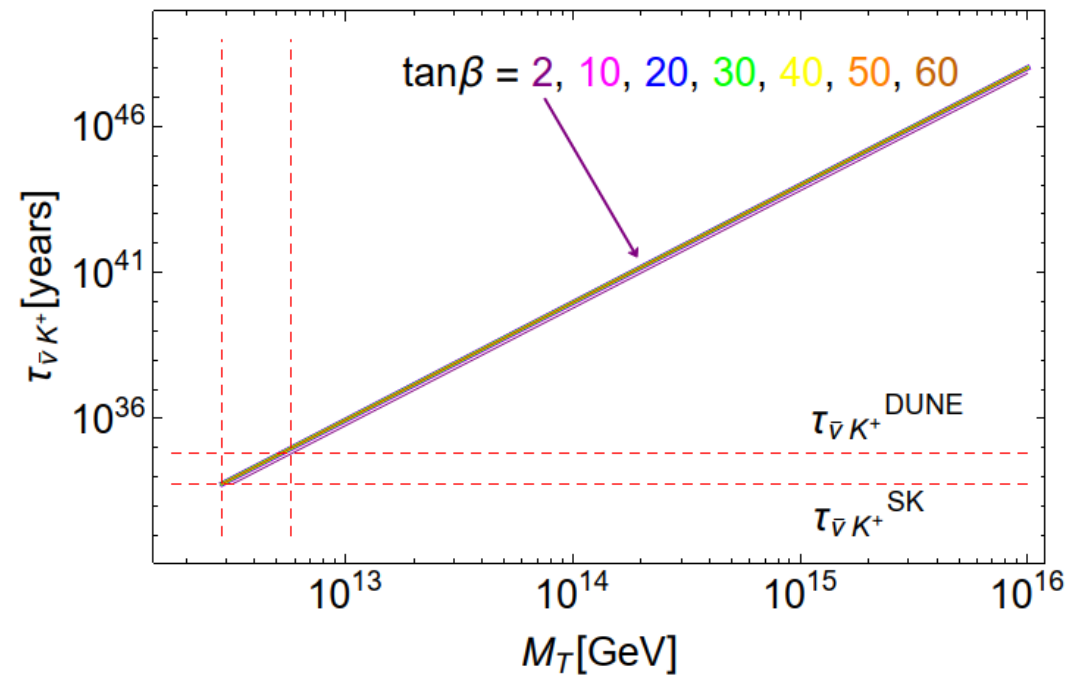
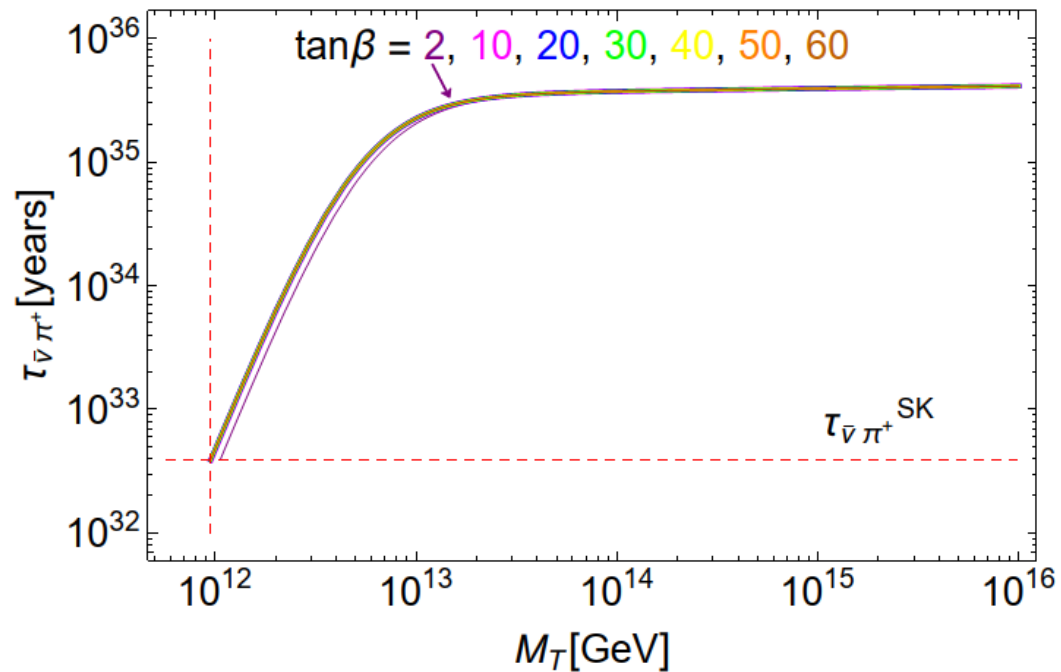
# DECAY RATES: II-NEUTRAL LEPTON (NEUTRINO) CHANNELS

$$\Gamma_{p \rightarrow \pi^+ \bar{\nu}_i} = k_\pi |T_{\pi^+ \bar{\nu}}|^2 A_{S_1}^2 \left| \frac{(U_N^*)_{i1}}{M^2} + V_{ud} \frac{m_u}{v_u} \sum_j \frac{(m^{(u)})_j}{v_u} \frac{(U_N^*)_{ij} (V)_{j1}}{M_\lambda^2} \right|^2,$$

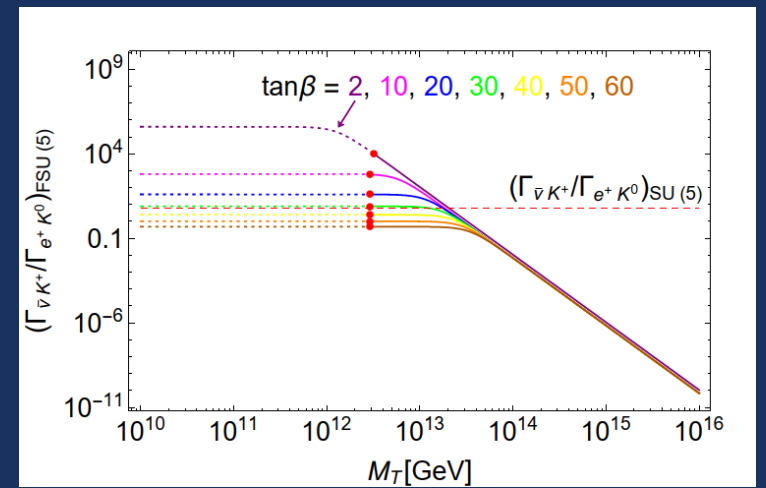
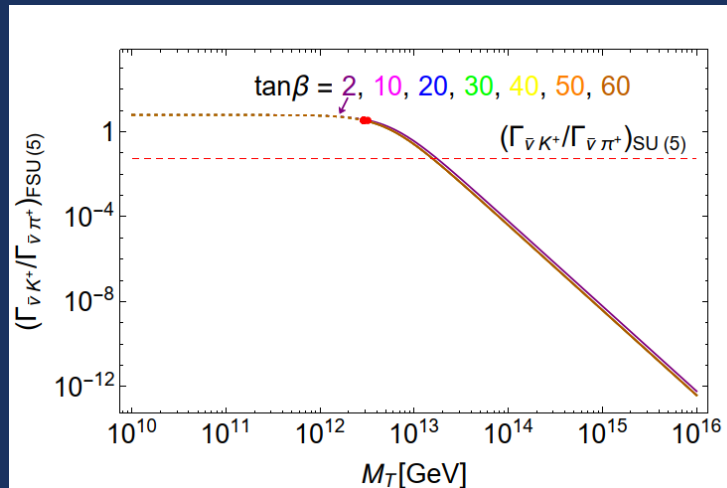
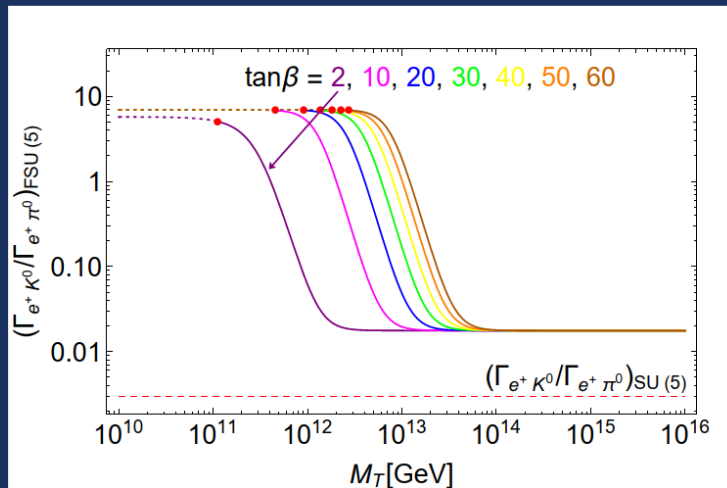
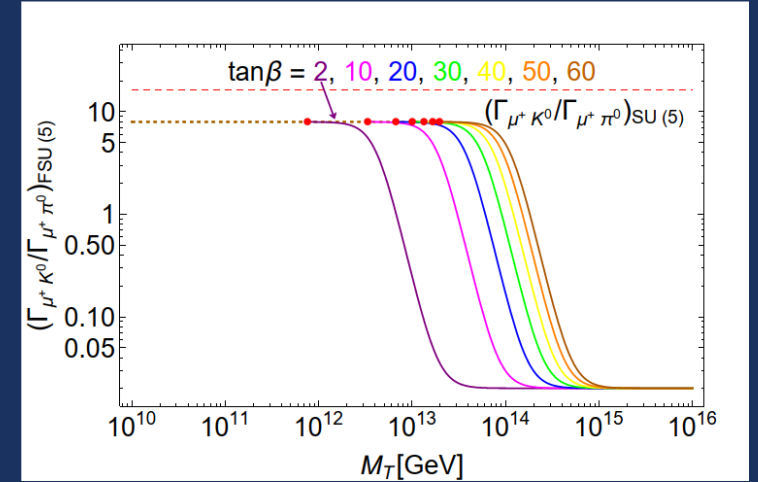
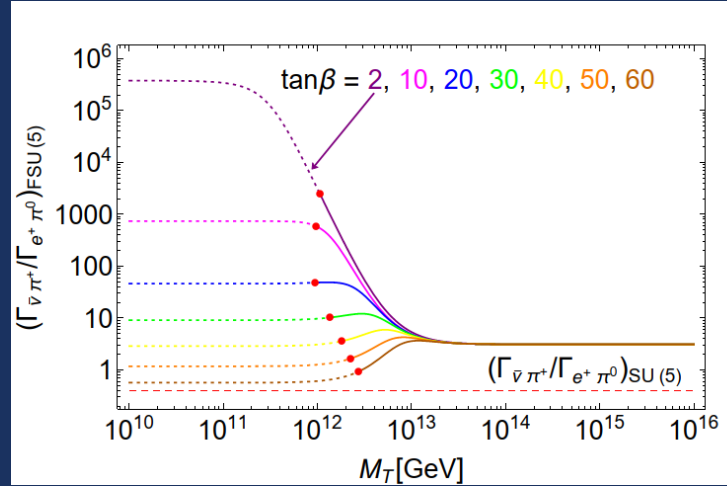
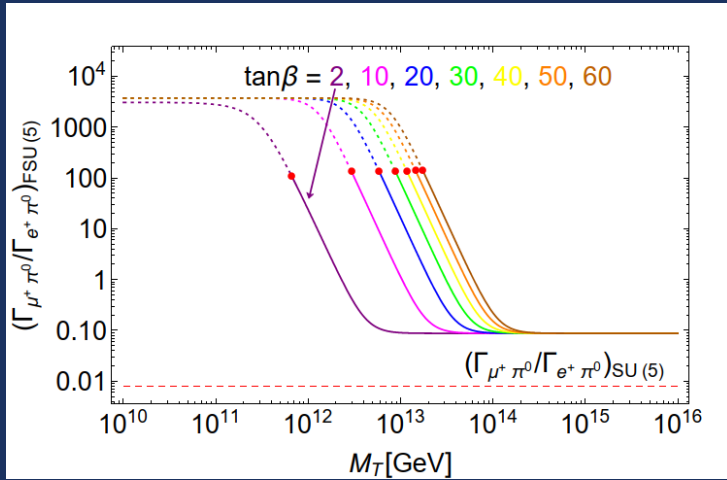
$$\Gamma_{p \rightarrow K^+ \bar{\nu}_i} = k_K A_{S_1}^2 \left| e^{i\varphi_1} T'_{K^+ \bar{\nu}} (V^*)_{ud} \frac{m_u}{v_u} \sum_j \frac{(m^{(u)})_j}{v_u} \frac{(U_N^*)_{ij} (V)_{j2}}{M_\lambda^2} \right.$$

$$\left. + e^{i\varphi_2} T''_{K^+ \bar{\nu}} (V^*)_{us} \frac{m_u}{v_u} \sum_j \frac{(m^{(u)})_j}{v_u} \frac{(U_N^*)_{ij} (V)_{j1}}{M_\lambda^2} \right|^2.$$

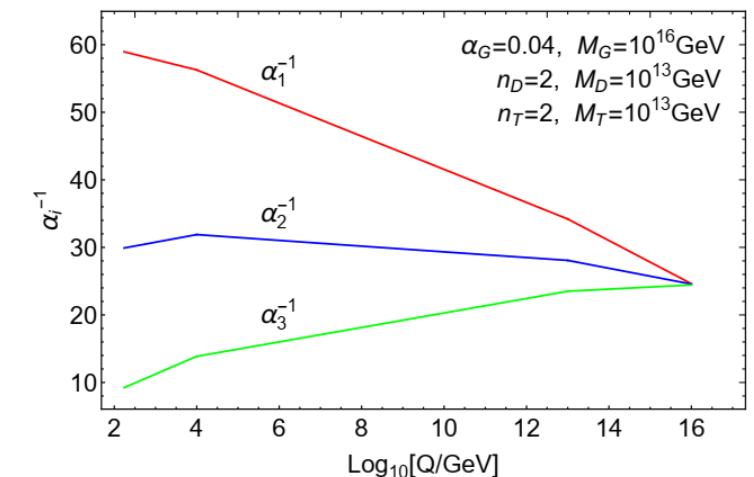
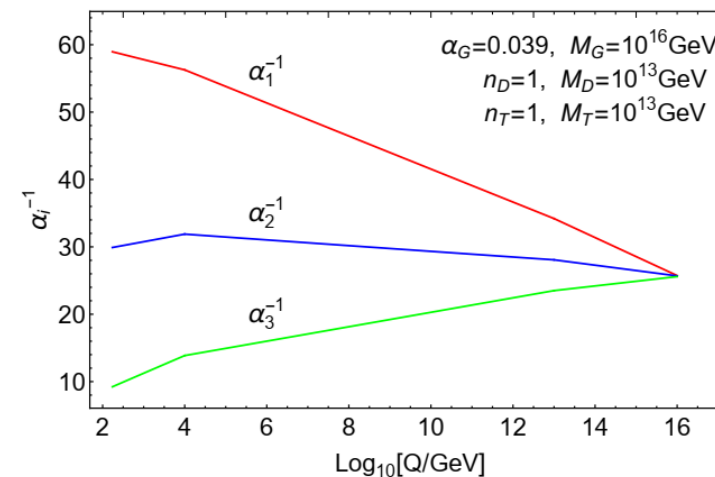
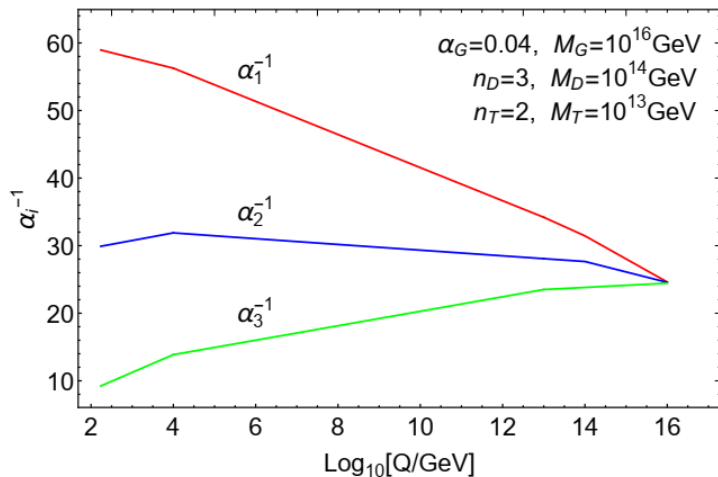
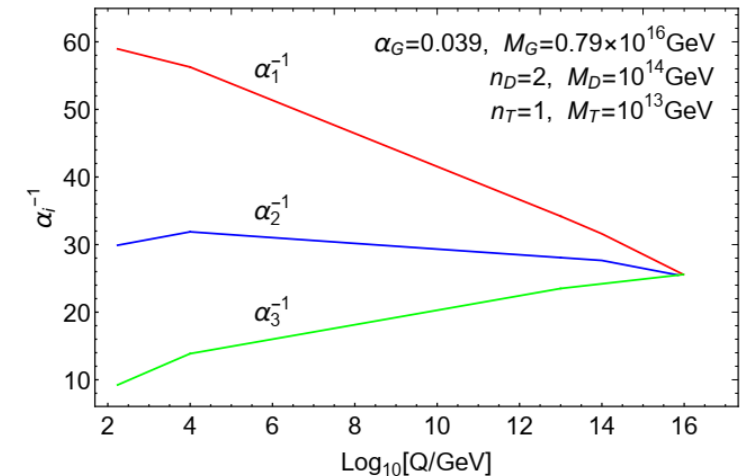
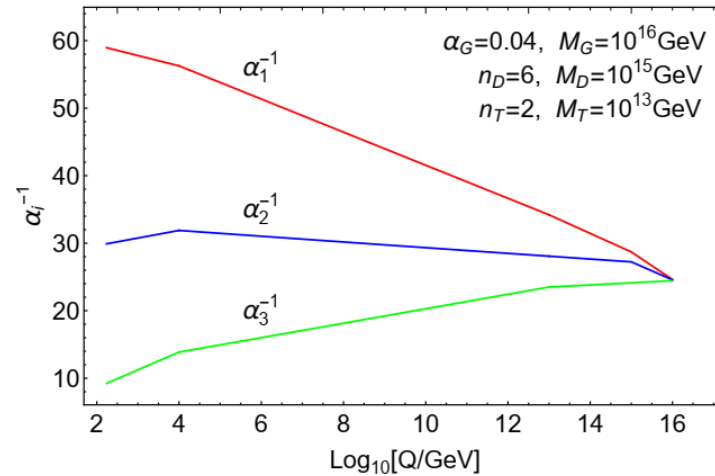
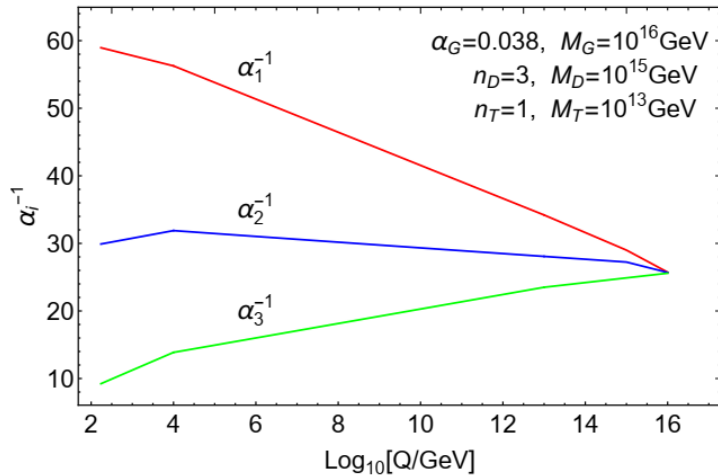
$M_T = M_{\bar{\lambda}}$  ,  $M_{\lambda}$  not involved!



# FLIPPED SU(5) vs. SU(5)



# GAUGE COUPLING UNIFICATION



# SUMMARY

R-symmetric flipped SU(5) model.

R symmetry forbids rapid proton decay via dimension four or five operators.

Color triplets of intermediate mass from Higgs 5-plets mediate proton decay with lifetime that lie in the observable range of future experiments.

Anti-neutrino and Kaon channel plays a pivotal role in distinguishing our model from SU(5) and other flipped SU(5) models.

Flipped SU(5) model can be embedded into SO(10) group.

*Thank you!*

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