



Progress on the true muonium front

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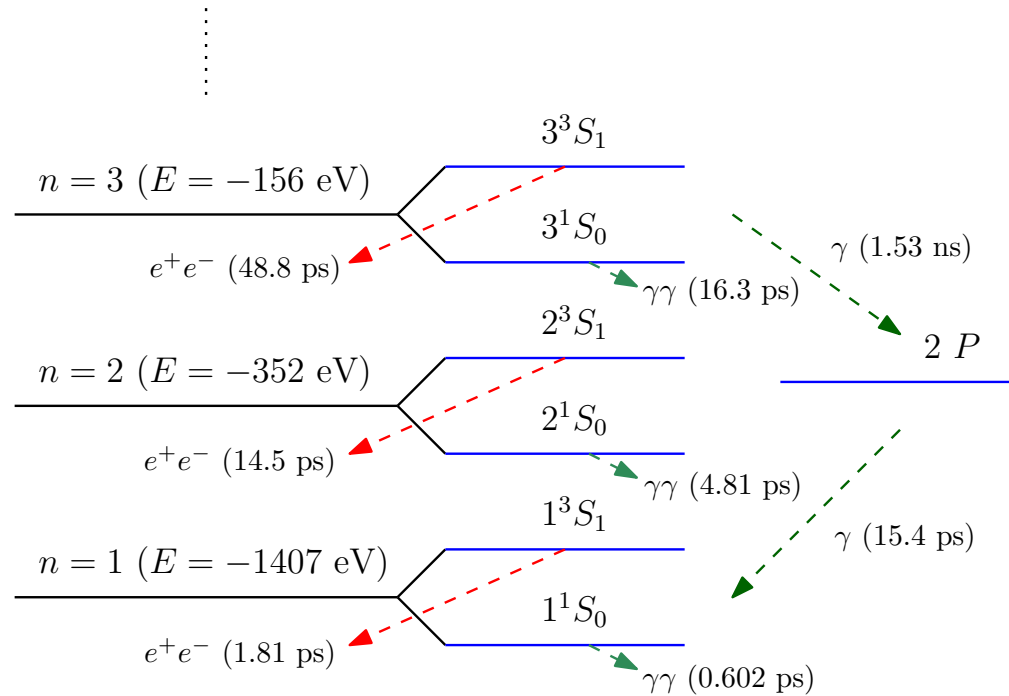
TRUE MUONIUM- properties

BOUND STATE OF $\mu^+\mu^-$ VERY COMPACT QED OBJECT

$$a_{TM}^0 = 2/(\alpha m_\mu) \simeq 512 \text{ fm}$$

$$\mu = m_\mu/2 \simeq 53 \text{ MeV}$$

$$\frac{n = \infty (E = 0)}{E_{TM}^{(n)} = -\frac{\alpha^2 \mu}{2n^2} = -\frac{\alpha^2 m_\mu}{4n^2}}$$



For a review on the theory see e.g H. Lamm and Y. Ji, EPJ Web Conf. 181 (2018) 01016, [[arXiv:1712.0342](https://arxiv.org/abs/1712.0342)].

$$E_{n,l,j,s} = -\frac{m_\mu \alpha^2}{4n^2} + m_\mu \alpha^4 \left[C_0 + C_1 \frac{\alpha}{\pi} + C_{21} \alpha^2 \ln\left(\frac{1}{\alpha}\right) + C_{20} \left(\frac{\alpha}{\pi}\right)^2 + C_{32} \frac{\alpha^3}{\pi} \ln^2\left(\frac{1}{\alpha}\right) + C_{31} \frac{\alpha^3}{\pi} \ln\left(\frac{1}{\alpha}\right) + C_{30} \left(\frac{\alpha}{\pi}\right)^3 + \dots \right],$$

C_{ij} indicate the coefficient of the term proportional to $(\alpha)^i \ln^j(1/\alpha)$

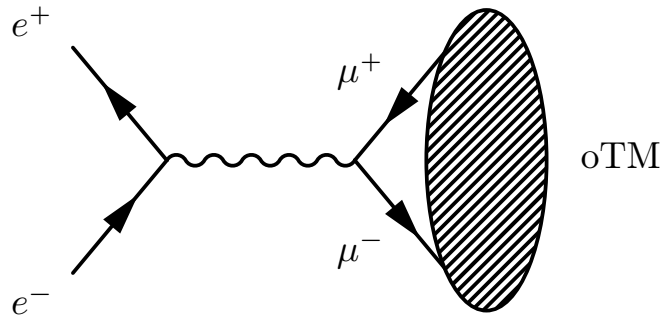
ENHANCED SENSITIVITY TO BSM

compared to Ps,M which are limited by mass suppression $O(m_e/\Lambda_{BSM})$ or uncertainties of nuclear effects (H, μH)

the triplet, ortho-true-muonium ($o-TM$), 1^3S_1 with $J^{PC} = 1^{--}$
 the singlet, para-true-muonium ($p-TM$), 1^1S_0 with $J^{PC} = 0^{-+}$

1) PRODUCTION OF TM via annihilation channel at SPS-H4

RATIO DIMUON PAIR VS BOUND STATES PRODUCTION



$$R = \frac{\sigma^{e^+e^- \rightarrow \mu^+\mu^-}(s_B)}{\sigma_{\text{rel}}^{e^+e^- \rightarrow \mu^+\mu^-}(s_B)} \simeq \frac{\sigma^{e^+e^- \rightarrow (\mu^+\mu^-)}}{\sigma_{\text{rel}}^{e^+e^- \rightarrow \mu^+\mu^-}} \simeq \frac{3\pi\alpha}{2} \simeq 0.03$$

S. J. Brodsky and R. F. Lebed, Phys. Rev. Lett. 102 (2009) 213401

In **fixed targets**

$$\sigma^{e^+e^- \rightarrow \mu^+\mu^-}(E_+) = \frac{2\pi^3\alpha^2}{m_\mu^2} \sqrt{1 - \frac{E_{\text{th}}}{E_+}} = \frac{2\pi^4\alpha^3}{\mu^2} \simeq 2.65 \cdot 10^{-30} \text{ cm}^2$$

Production of **TM** close to threshold in **FIXED TARGET** experiments

$$\begin{aligned} \sigma_{(n)}^{e^+e^- \rightarrow (\mu^+\mu^-)}(E_+) &= \frac{3\pi\alpha}{2} \frac{\delta E_n}{\Delta E_+} \times \sigma^{e^+e^- \rightarrow \mu^+\mu^-}(E_+) \\ &\simeq \frac{\delta E_n}{\Delta E_+} \times 9.11 \cdot 10^{-32} \text{ cm}^2 \end{aligned}$$

where $\delta E_n = \alpha^2 m_\mu / (4n^2)$ is the effective energy window to produce the bound states and ΔE the beam energy resolution

H4 A UNIQUE BEAMLIN:

- > 10^7 POSITRONS per spill @43.7 GeV with (dp/p < 1%)

See TALK of Nikos C.

Estimated **RATE** OF TM $\sim O(1)$ event/month (target optimisation ongoing)

DETECTION OF TM IN NA64 VISIBLE SETUP (X17- search)

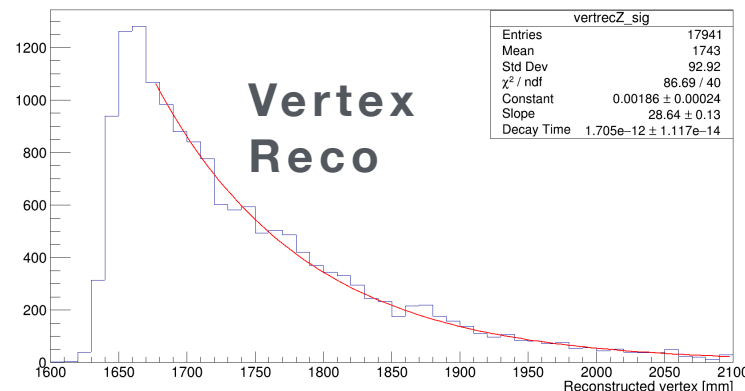
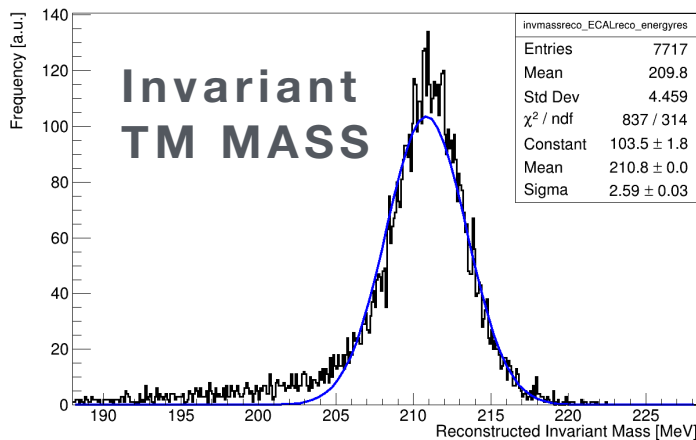
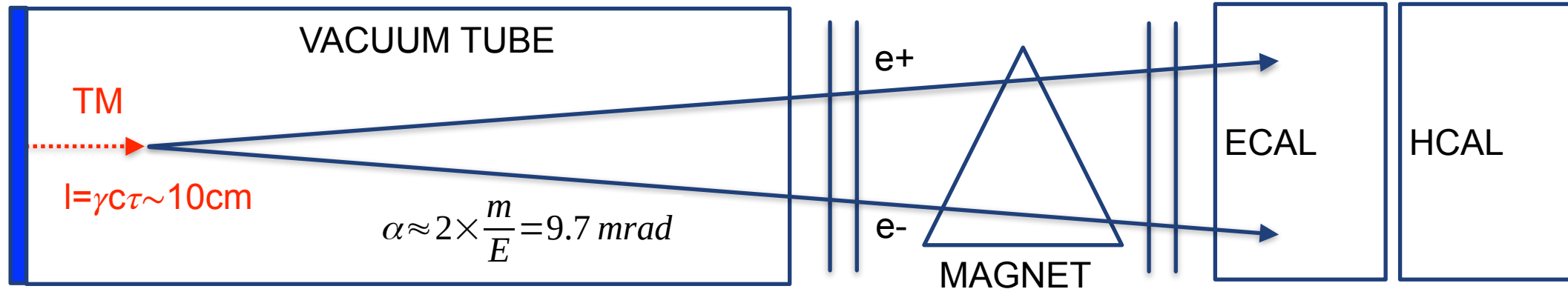
Phys.Rev.Lett. 120 (2018) 23, 231802, *Phys.Rev.D* 101 (2020) 7, 071101, *Eur.Phys.J.C* 80 (2020) 12, 1159

SIGNATURE:

- 1) HIGH P_T e^+e^- PAIR WITH $2m_\mu$ INVARIANT MASS
- 2) RECONSTRUCTED DISPLACED VERTEX

See NA64-TALK of Dima K.

Tagged
 e^+ , 43,7 GeV



PRELIMINARY CONCLUSION

The experiment is background free at a level of 10^{12} positrons on target. The efficiency of detection is estimated to be 40%.

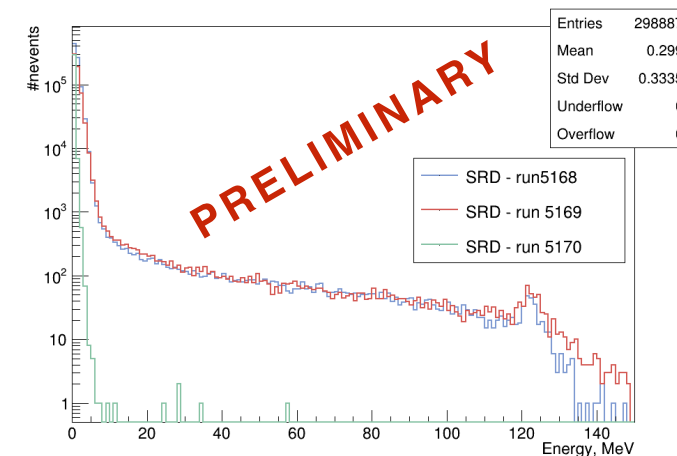
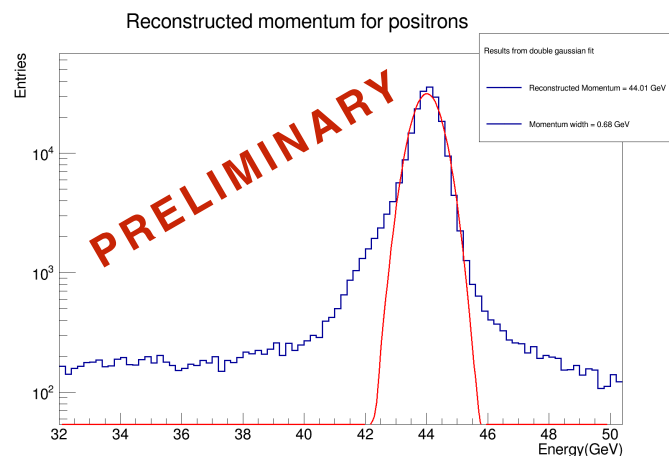
UPDATE- 43.7 GeV positron beam in H4 at SPS



1st QUICK TEST (2 hours) DURING NA64 BEAMTIME (September 2021)

GOAL: Cross check beam simulation, i.e. **positron intensity, momentum resolution** and measure **hadron contamination**

Run	Type	Spills	Intensity
5168	e ⁺	30	1.7 x 10 ⁶
5169	e ⁺	20	7.7 x 10 ⁶
5170	hadron	90	5 x 10 ³



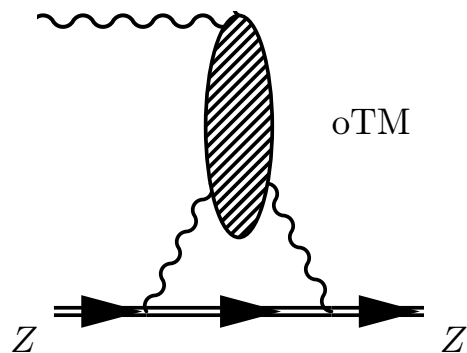
Preliminary results are encouraging: $\sim 10^7$ POSITRONS per spill @43.7 GeV with ($dp/p < 1\%$). New measurements in 2022 are planned including background measurements in visible setup.

2) “Low energy” TM production @ the GAMMA Factory

CROSS SECTION FOR oTM PRODUCTION FOR $E \gg m_\mu$:

$$\sigma_{\gamma Z} = Z^2 \times 2.4 \cdot 10^{-39} \text{ cm}^2$$

Ginzburg, et al., Phys. Rev. C58, 3565 (1998)



Dimuons production in G4 now extended down to the muon pair production threshold on request of GF design group

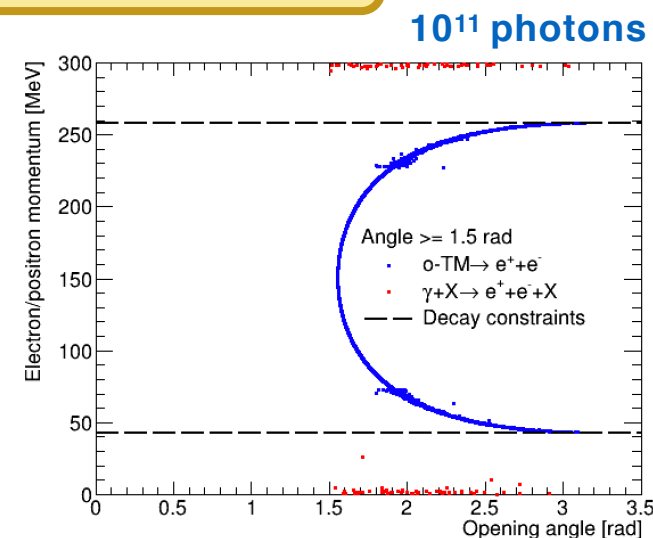
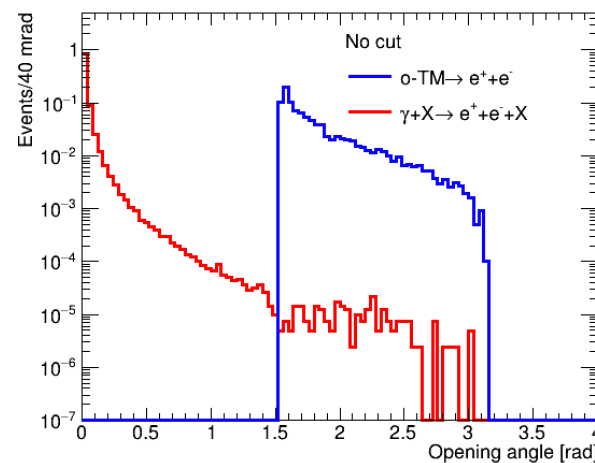
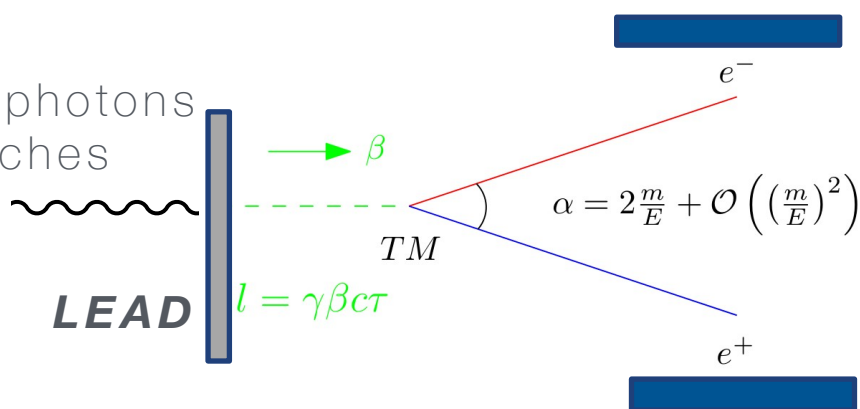
EPJ Web of Conferences **245**, 02009 (2020)

Production & detection of **TM** at GAMMA FACTORY:

See GF-TALK of M. Gorshteyn

TRACKERS & DETECTORS

300 MeV 10^9 photons in 500 ps bunches at 20 MHz



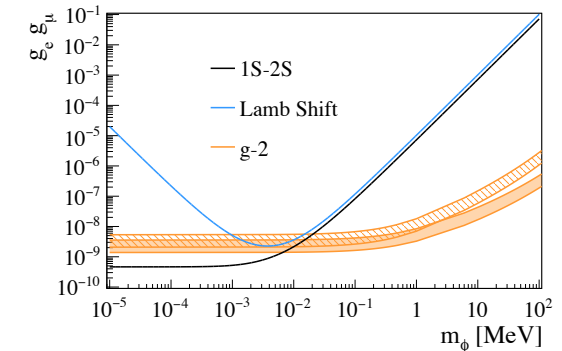
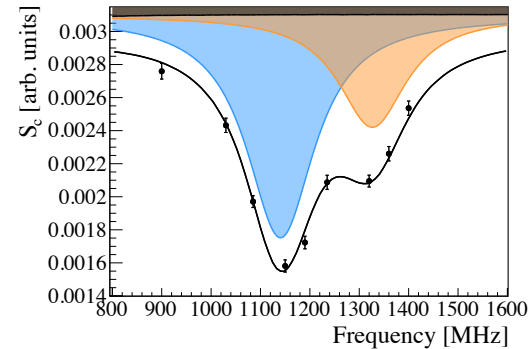
Estimated **RATE OF $\sim O(10^4-5)$ TM (1^3S_1)/day and $\sim O(10^2-3)$ TM (2^3S_1)/day**

MEASUREMENT OF TM LAMB SHIFT AND FINE AND HFS STRUCTURE

Similar measurement
as for μ^+e^-



TRUE MUONIUM



<https://arxiv.org/abs/2108.12891>

TRUE MUONIUM TRANSITIONS:

Transition	E_{theory} [MHz]
$1^3S_1 - 1^1S_0$	$42329355(51)_{\text{had}}(700)$
$2^3S_1 - 1^3S_1$	$2.550014(16) \times 10^{11}$
$2^3P_0 - 2^3S_1$	$1.002(3) \times 10^7$
$2^3P_1 - 2^3S_1$	$1.115(3) \times 10^7$
$2^3P_2 - 2^3S_1$	$1.206(3) \times 10^7$
$2^1P_1 - 2^3S_1$	$1.153(3) \times 10^7$

42 THz **HFS accessible via 7 micron LASER**
(e.g. with Quantum Cascade Lasers, P. Täschler et al., *Nat. Photon.* **15**, 919–924 (2021).)

Natural line width of 350 GHz

LS 10 THz, Natural line width of 20 GHz

SIGNATURE HFS or 2S-2P TRANSITIONS: COUNT NUMBER OF HIGH P_T e^+e^- PAIRS VS LASER FREQUENCY

SUMMARY AND OUTLOOK

- Feasibility of TM DETECTION WITH NA64 VISIBLE SETUP:
 - analysis of H4 with 43.7 GeV positrons ongoing,
 - cross check simulation with data on NA64 visible setup (2022)
- Proof of principle in NA64 for measuring TM properties @ FUTURE CERN FACILITIES

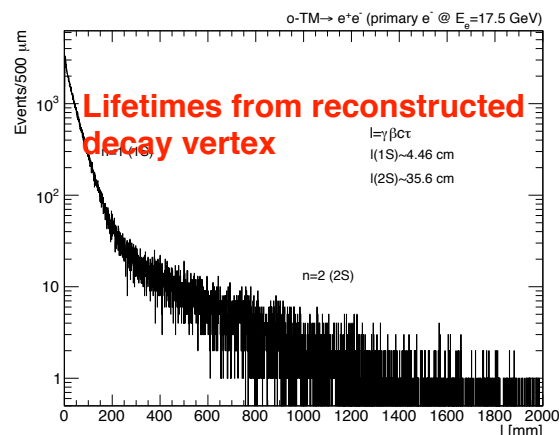
e.g @LEMMA in beam dump mode: for 10^{16} e^+ , $dE=1$ MeV, 10^4 TM M. Boscolo et al. Phys.Rev.Accel.Beams 21 (2018) 6, 061005 N. Amapane et al 2020 JINST 15 P01036

or @GAMMA FACTORY (10^{17} gamma/s @up to 400MeV), 10^{4-5} TM/day”

Precision study of TM properties such as decay rate, Lamb shift, Fine and HFS structure

IN PBC CONTEXT

- Complementarity of TM to search for NP in muonic sector
- Synergies (simulation/detectors/calculations) with other projects at the high intensity frontier



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