

Doubly charmed tetraquark at LHCb and future prospects



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*LPHE EPFL Seminar,
29 November 2021*

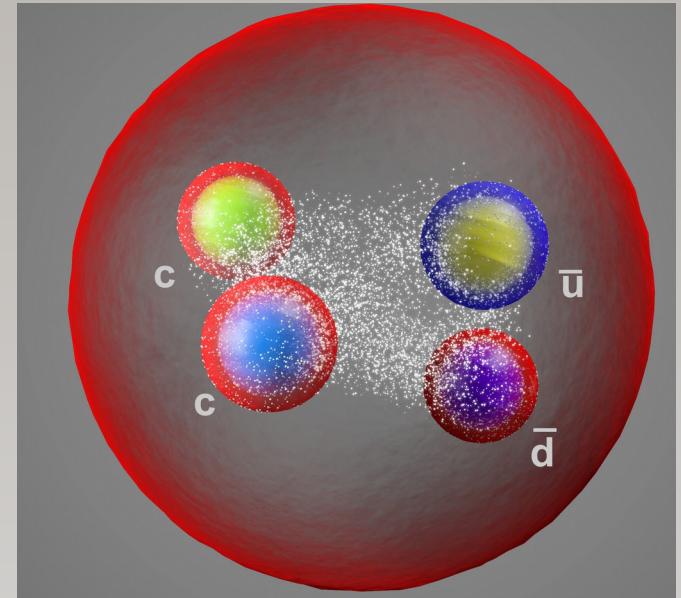
Outlook

- Introduction - QCD, hadron spectroscopy theory and predictions for $QQ\bar{q}q'$
- The T_{cc}^+ tetraquark:
 - LHCb detector & Selection
 - Observation of the signal
 - Study with unitarized model
 - Interpretations
 - Production properties
- Discussion
 - Reflection on the results
 - Open questions
 - Future possibilities

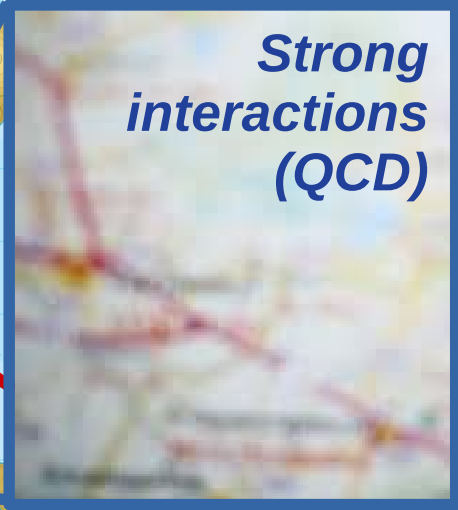
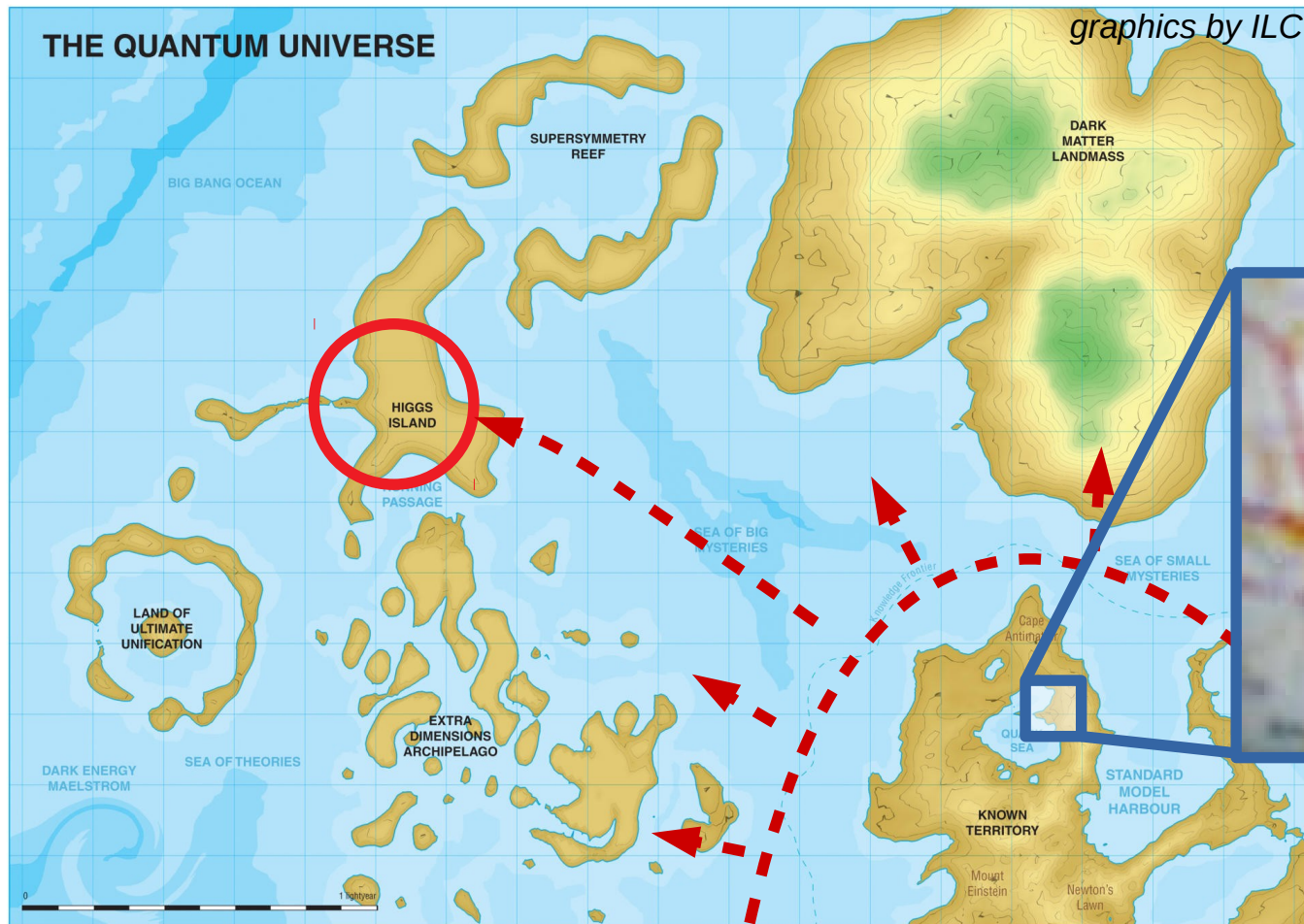
Measurements

[arXiv:2109.01038](https://arxiv.org/abs/2109.01038)

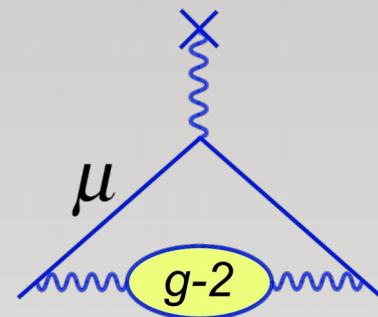
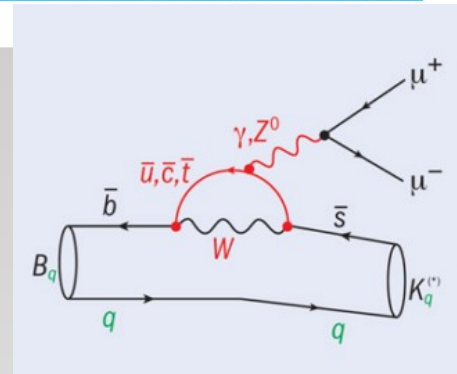
[arXiv:2109.01056](https://arxiv.org/abs/2109.01056)



High Energy Physics frontiers



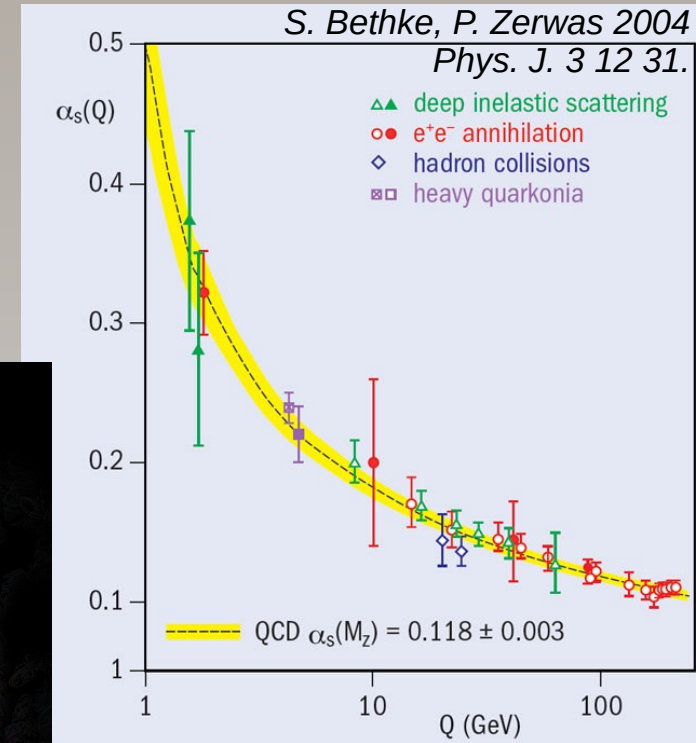
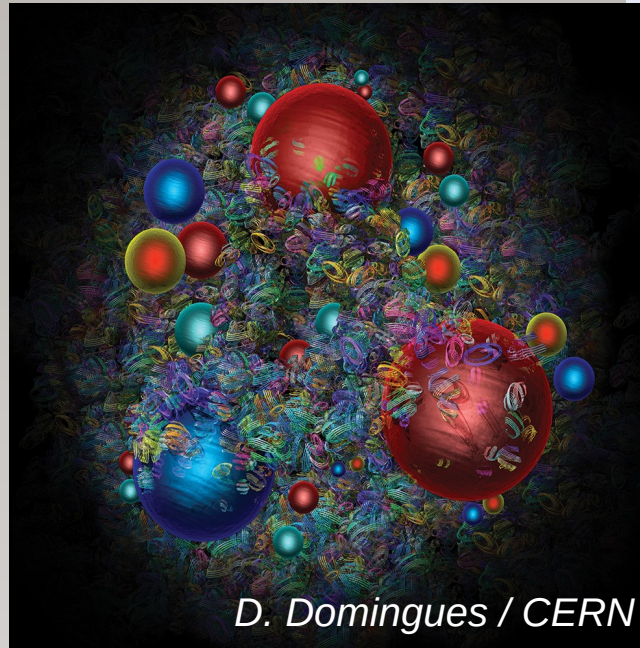
- The known QCD is not that well known
- And it's understanding also limits the hunt for non-direct signs of NP: B-decays, $g-2$ of μ , ...



QCD vs. Hadron Spectroscopy

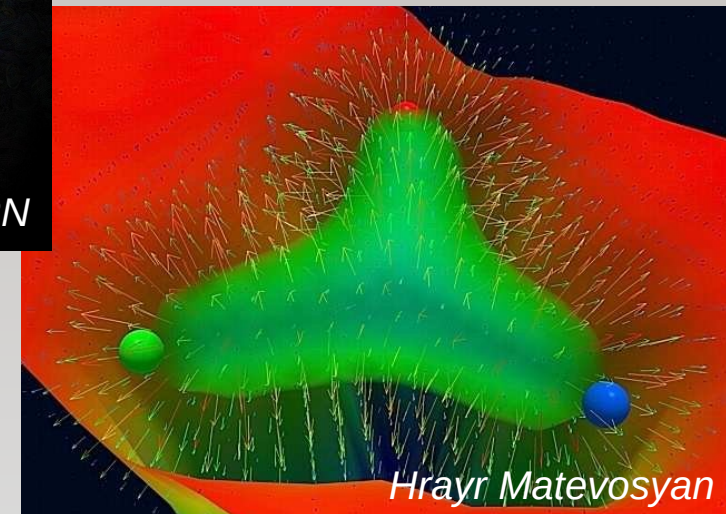
- QCD is successful theory giving in precise predictions at high energies

- However is highly non-perturbative at hadron/nuclei energy scale



- Therefore for hadron spectroscopy (semi-)phenomenological approaches have to be used.

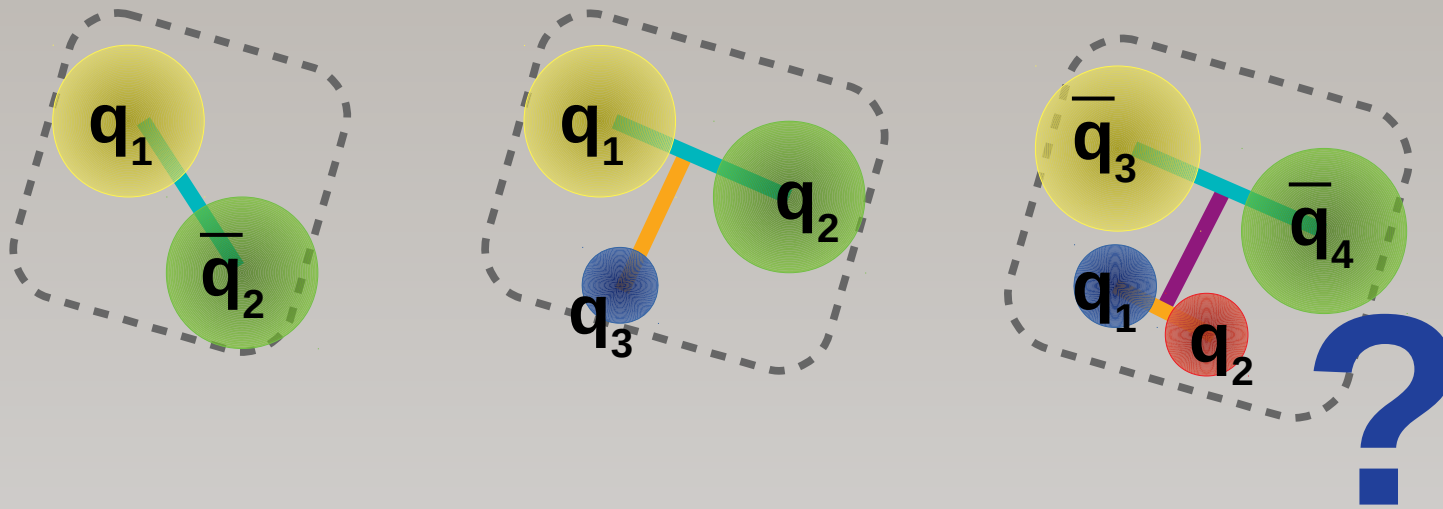
*mini-review in the following
(oversimplified & incomplete)*



Theory approaches, 1

- Effective approach for compact hadrons (“bag” model)
 - Heavy Quark Symmetry – expansion in $1/m_Q$ + kinematic corrections
 - Sum of quark masses, binding, hyperfine interaction
 - ...

*extracting effective parameters from measured hadron masses
- may involve assumptions about diquarks, string, ...*



see in predictions for T_{cc}^{++} :

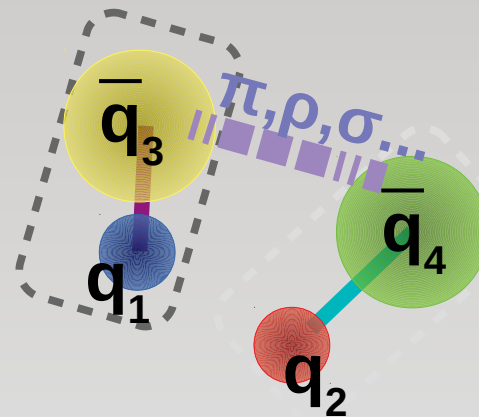
Eichten, Quigg, 2017

Braaten, He, Mohapatra, 2020

Karliner, Rosner, 2017

... and much more ...

- Molecular objects (for exotics)
 - corresponding form-factors
and cut-offs not well controlled*



see in predictions for T_{cc}^{++} :

Pepin, Stancu, Genovese, Richard, 1996

Li, Sun, Liu, Zhu, 2012

Wu, Liu, Wu, Valderrama, Xie, Geng, 2019

... and much more ... 5

Theory approaches, 2

- NR quark constituent model *with semi-phenomenological quark-quark interaction potential*

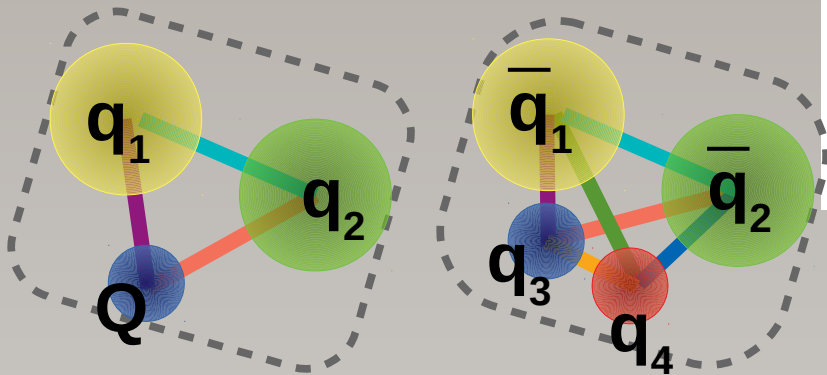
$$H = \sum_i \left(m_i + \frac{\mathbf{p}_i^2}{2m_i} \right) - \frac{3}{16} \sum_{i < j} \tilde{\lambda}_i \tilde{\lambda}_j v_{ij}(r_{ij})$$

color of quarks

$$V_{ij}^B = -\frac{\lambda_i^C}{2} \cdot \frac{\lambda_j^C}{2} \left(U_0 + \frac{\alpha}{r_{ij}} + \beta r_{ij} + \alpha \frac{\hbar^2}{m_i m_j c^2} \frac{e^{-r_{ij}/r_0}}{r_0^2 r_{ij}} \sigma_i \cdot \sigma_j \right),$$

$r_{ij} = |\vec{r}_i - \vec{r}_j|$

one-gluon exchange ("Coulomb") *confinement* *contact spin-spin interaction*



Semay, Silvestre-Brac, 1994

Janc, Rosina, 2003

... and more ...

can also take boson exchange (molecular binding) into account

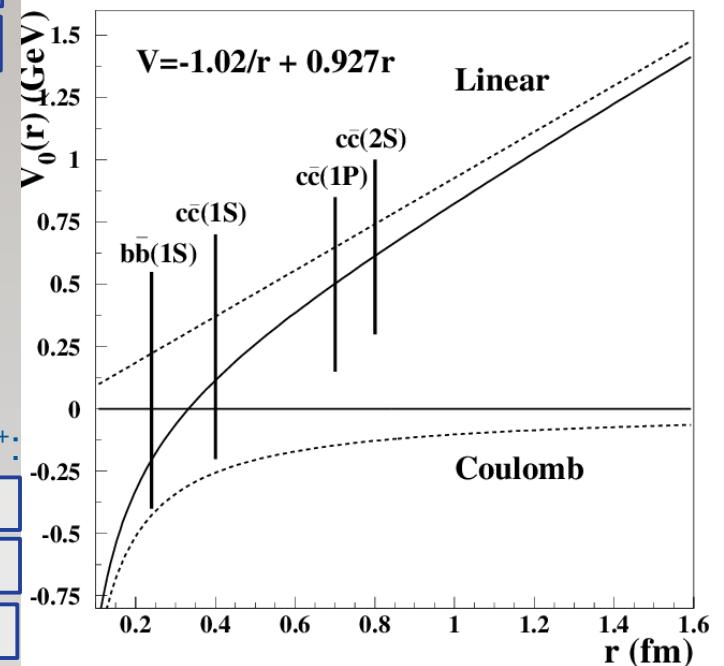
- Heavy quark allows to probe shorter range where OGE dominates
- Lattice QCD *hard to simultaneously work with heavy and light quarks (small lattice step and large lattice)*
- QCD sum rules *typically give >100 MeV uncertainty*

predictions for T_{cc}^{+}

HAL QCD Collaboration, 2014

Hadron Spectrum Collaboration, 2017

Junnarkar, Mathur, Padmanath, 2018



[see Refs. in predictions for T_{cc}^{+}] 6

Exotic hadrons

Understanding is limited by the quark configurations to consider

- Conventional hadrons: $q_1 \bar{q}_2$ and $q_1 q_2 q_3$

- Exotic hadrons: $c\bar{c}q_1 \bar{q}_2$ and $c\bar{c}q_1 q_2 q_3$

~30 tetra/pentaquarks candidates discovered since observation of $\chi_{c1}(3872)$ by Belle in 2003

- most have $Q\bar{Q}$ pair and large width,
- interpretations are still unclear -
molecula/compact
- and even resonance nature is questioned

- $QQ\bar{q}'\bar{q}''$ are prime candidates to be bound and therefore long-lived

- first estimates (based on $V_{qq'}(r) \sim r^{0.1}$ approximation) stated that should happen for $m_Q/m_q > 6-8$ (compare to $m_b/m_u \sim 15$, $m_c/m_u \sim 5-6$)

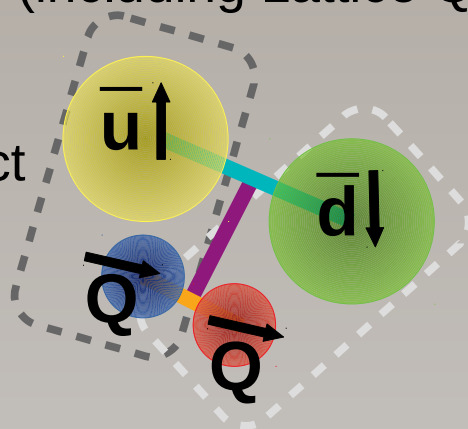
States	Quark content
$X_0(2900), X_1(2900)$ [21, 22]	$\bar{c}du\bar{s}$
$\chi_{c1}(3872)$ [6]	$c\bar{c}q\bar{q}$
$Z_c(3900)$ [23], $Z_c(4020)$ [24, 25], $Z_c(4050)$ [26], $X(4100)$ [27], $Z_c(4200)$ [28], $Z_c(4430)$ [29–32], $R_{c0}(4240)$ [31]	$c\bar{c}u\bar{d}$
$Z_{cs}(3985)$ [33], $Z_{cs}(4000)$, $Z_{cs}(4220)$ [34]	$c\bar{c}u\bar{s}$
$\chi_{c1}(4140)$ [35–38], $\chi_{c1}(4274)$, $\chi_{c0}(4500)$, $\chi_{c0}(4700)$ [38], $X(4630)$, $X(4685)$ [34], $X(4740)$ [39]	$c\bar{c}s\bar{s}$
$X(6900)$ [14]	$c\bar{c}c\bar{c}$
$Z_b(10610)$, $Z_b(10650)$ [40]	$b\bar{b}u\bar{d}$
$P_c(4312)$ [41], $P_c(4380)$ [42], $P_c(4440)$, $P_c(4457)$ [41], $P_c(4357)$ [43]	$c\bar{c}uud$
$P_{cs}(4459)$ [44]	$c\bar{c}uds$

Adler, Richard, Taxil, 1982

Ballot, Richard, 1983

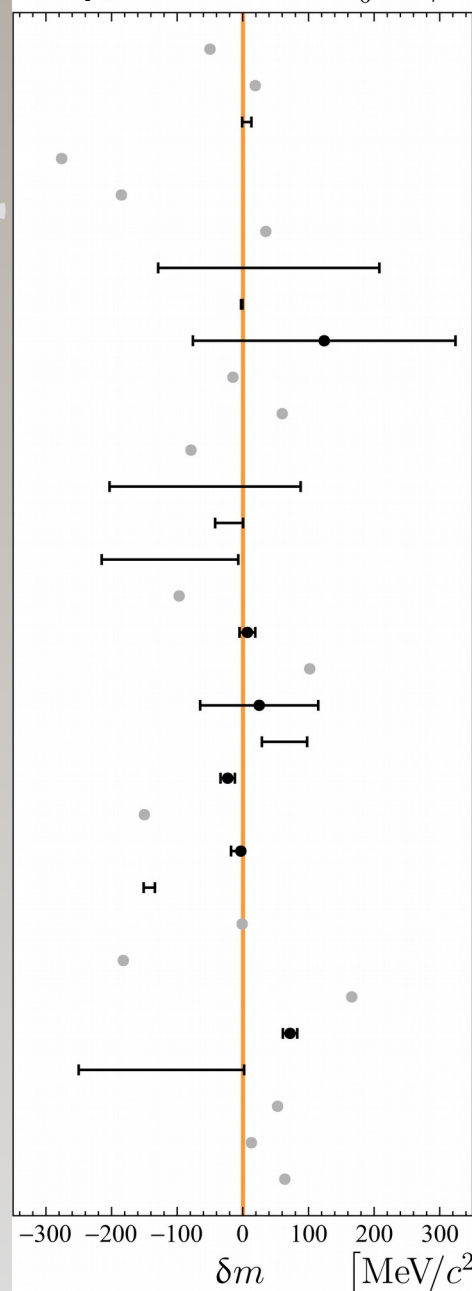
Predictions for $cc\bar{u}\bar{d}$ mass

- More recent calculations (including Lattice QCD) all agree that it should be true for $[bb][\bar{u}\bar{d}]$ with QQ forming compact color anti-triplet and resulting binding of $\sim 150\text{MeV}$



- However not clear for $[bc][\bar{u}\bar{d}]$ and $[cc][\bar{u}\bar{d}]$
- Predictions for a ground $cc\bar{u}\bar{d}$ state (isoscalar with $J^P=1^+$) vary within $\pm 250\text{MeV}$ wrt to D^0D^{*+} threshold

$$\delta m \equiv m_{T_{cc}^+} - (m_{D^{*+}} + m_{D^0})$$



J. Carlson <i>et al.</i>	1987
B. Silvestre-Brac and C. Semay	1993
C. Semay and B. Silvestre-Brac	1994
M. A. Moinester	1995
S. Pepin <i>et al.</i>	1996
B. A. Gelman and S. Nussinov	2003
J. Vijande <i>et al.</i>	2003
D. Janc and M. Rosina	2004
F. Navarra <i>et al.</i>	2007
J. Vijande <i>et al.</i>	2007
D. Ebert <i>et al.</i>	2007
S. H. Lee and S. Yasui	2009
Y. Yang <i>et al.</i>	2009
N. Li <i>et al.</i>	2012
G.-Q. Feng <i>et al.</i>	2013
S.-Q. Luo <i>et al.</i>	2017
M. Karliner and J. Rosner	2017
E. J. Eichten and C. Quigg	2017
Z. G. Wang	2017
W. Park <i>et al.</i>	2018
P. Junnarkar <i>et al.</i>	2018
C. Deng <i>et al.</i>	2018
M.-Z. Liu <i>et al.</i>	2019
L. Maiani <i>et al.</i>	2019
G. Yang <i>et al.</i>	2019
Y. Tan <i>et al.</i>	2020
Q.-F. Lü <i>et al.</i>	2020
E. Braaten <i>et al.</i>	2020
D. Gao <i>et al.</i>	2020
J.-B. Cheng <i>et al.</i>	2020
S. Noh <i>et al.</i>	2021
R. N. Faustov <i>et al.</i>	2021

[see Refs. in paper]

”Observation of an exotic narrow doubly charmed tetraquark”

arXiv:2109.01038

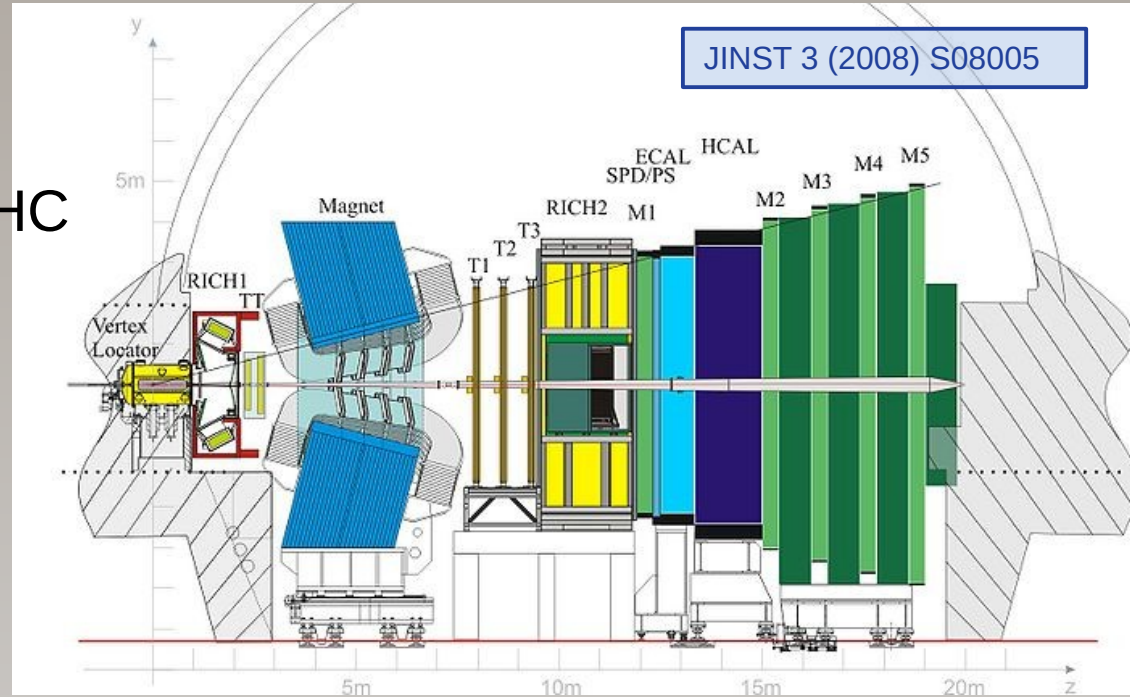
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”Study of the doubly charmed tetraquark T_{cc}^{++} ”

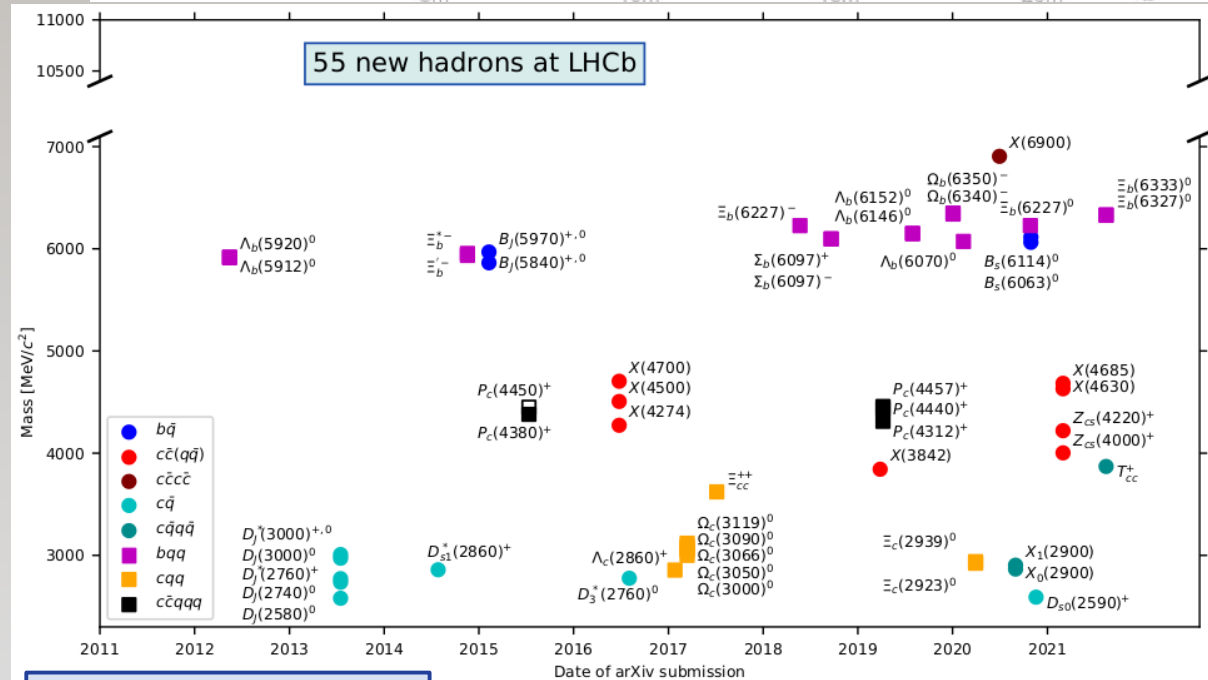
arXiv:2109.01056

The LHCb detector

- LHCb - forward spectrometer at LHC with excellent
 - momenta/mass,
 - vertex/time resolution
 - particle identification ($K/\pi/p/\mu$)

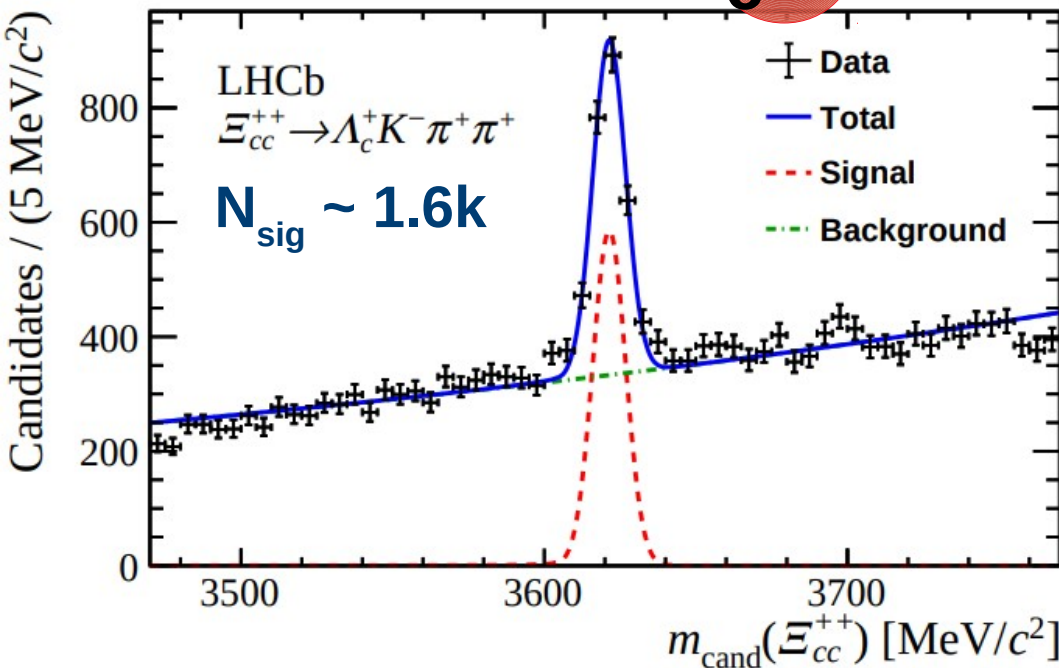
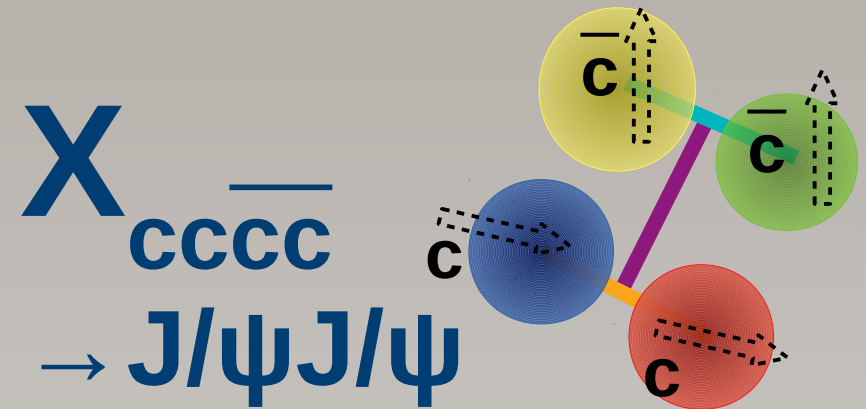
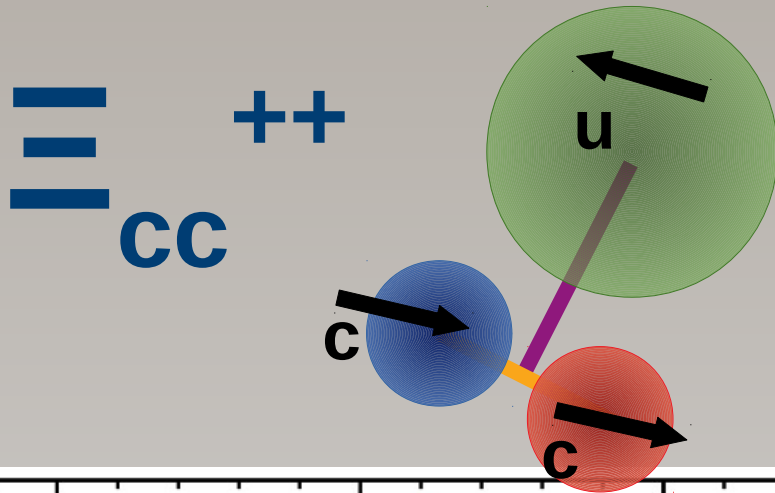


very powerful tool for heavy hadron spectroscopy
 → contribute to major part of hadrons discovered at LHC

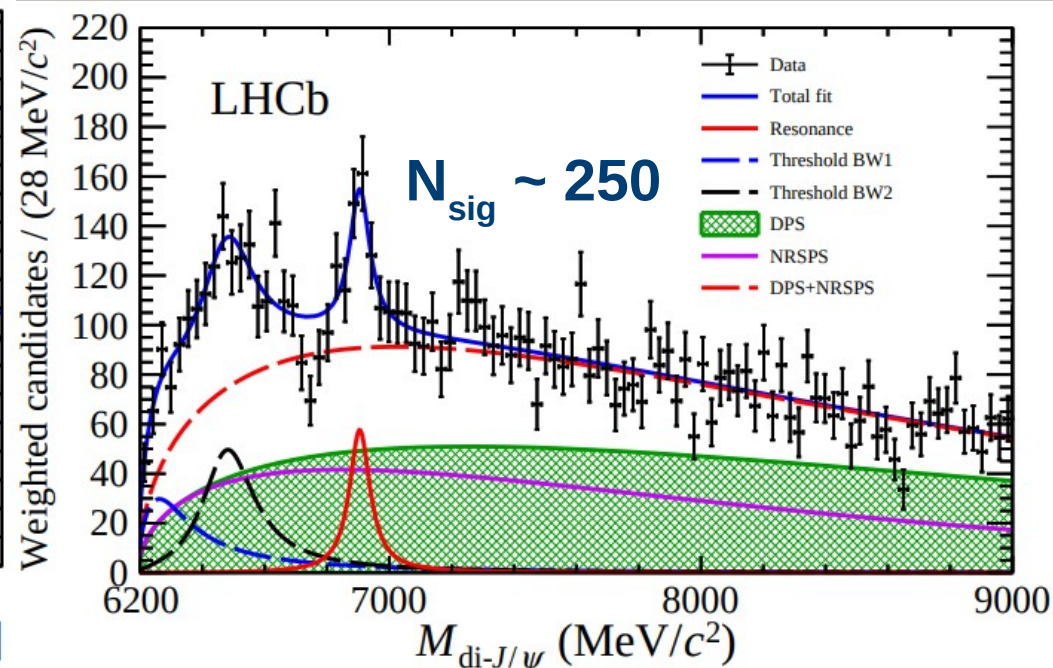


Previous hadrons with two c-quarks

- The observations of Ξ_{cc}^{++} [ccu] and $X[cc\bar{c}\bar{c}] \rightarrow J/\psi J/\psi$ indicate that if the $[cc\bar{u}\bar{d}]$ exists it should be accessible at LHCb in $DD^{(*)}$ final states



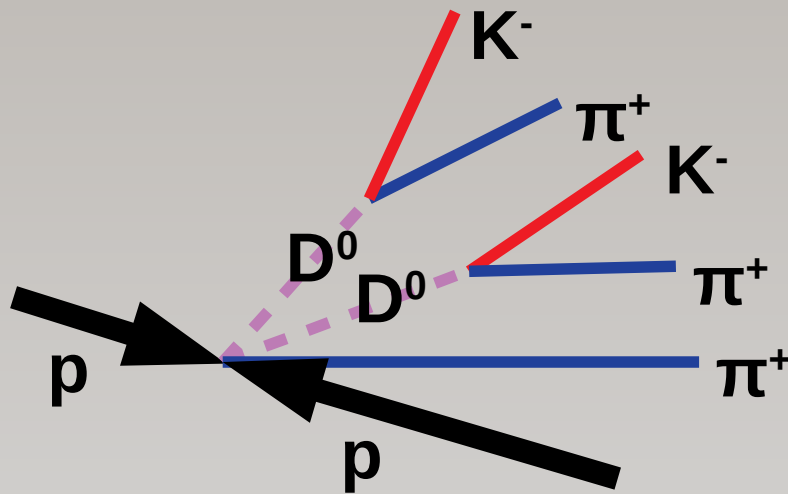
JHEP 02 (2020) 049



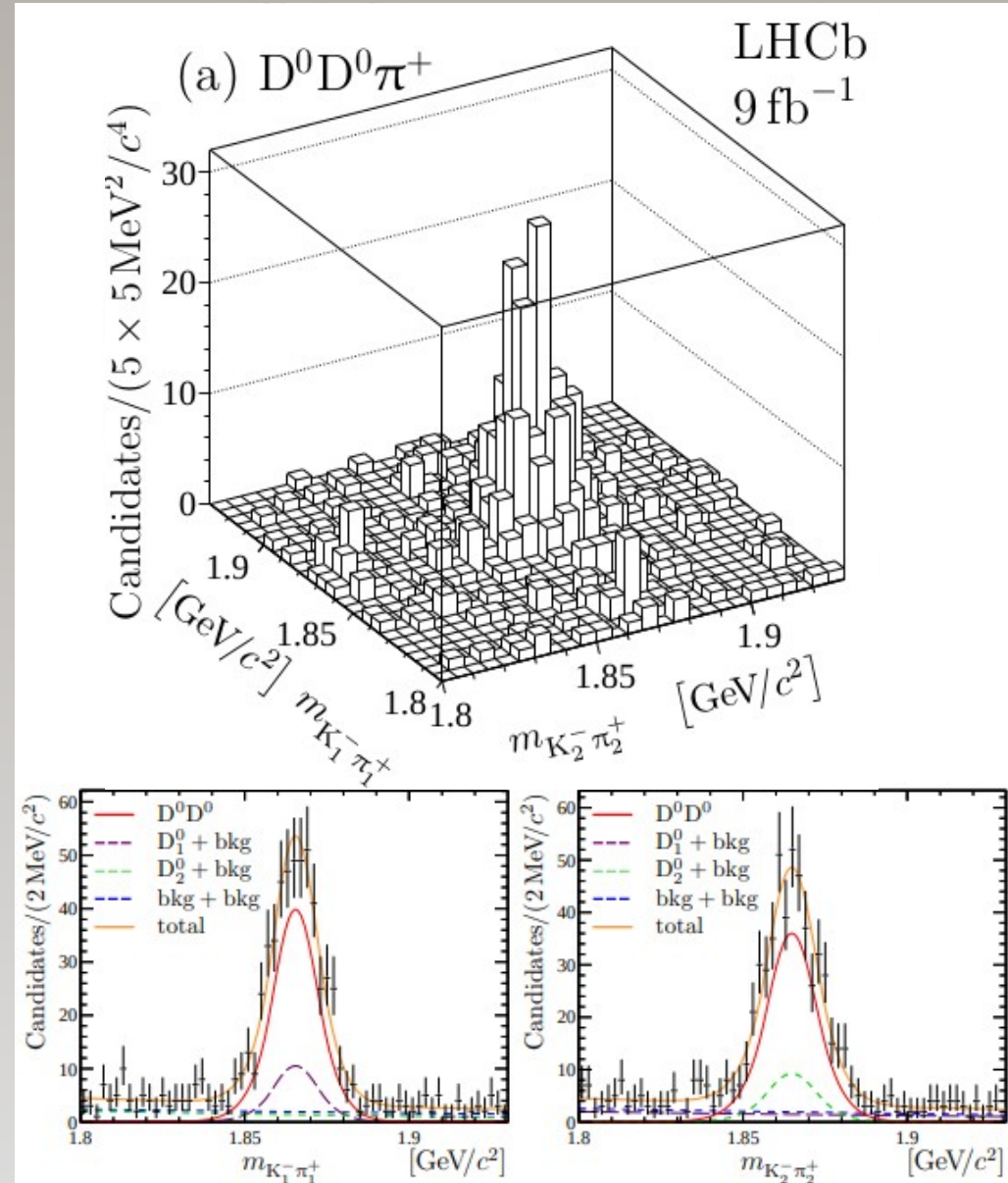
Sci. Bul. 65 (2020) 1983

Selection of $D^0 D^0 \pi^+$

- Select prompt $D^0 D^0 \pi^+$ candidates via $D^0 \rightarrow K^- \pi^+$
- Require non-prompt K^- & π^+ with high p_T
- Require good quality of track, vertexes & particle identification
- Ensure no K/π candidates belong to one track (clones) or duplicates or reflections via mis-ID

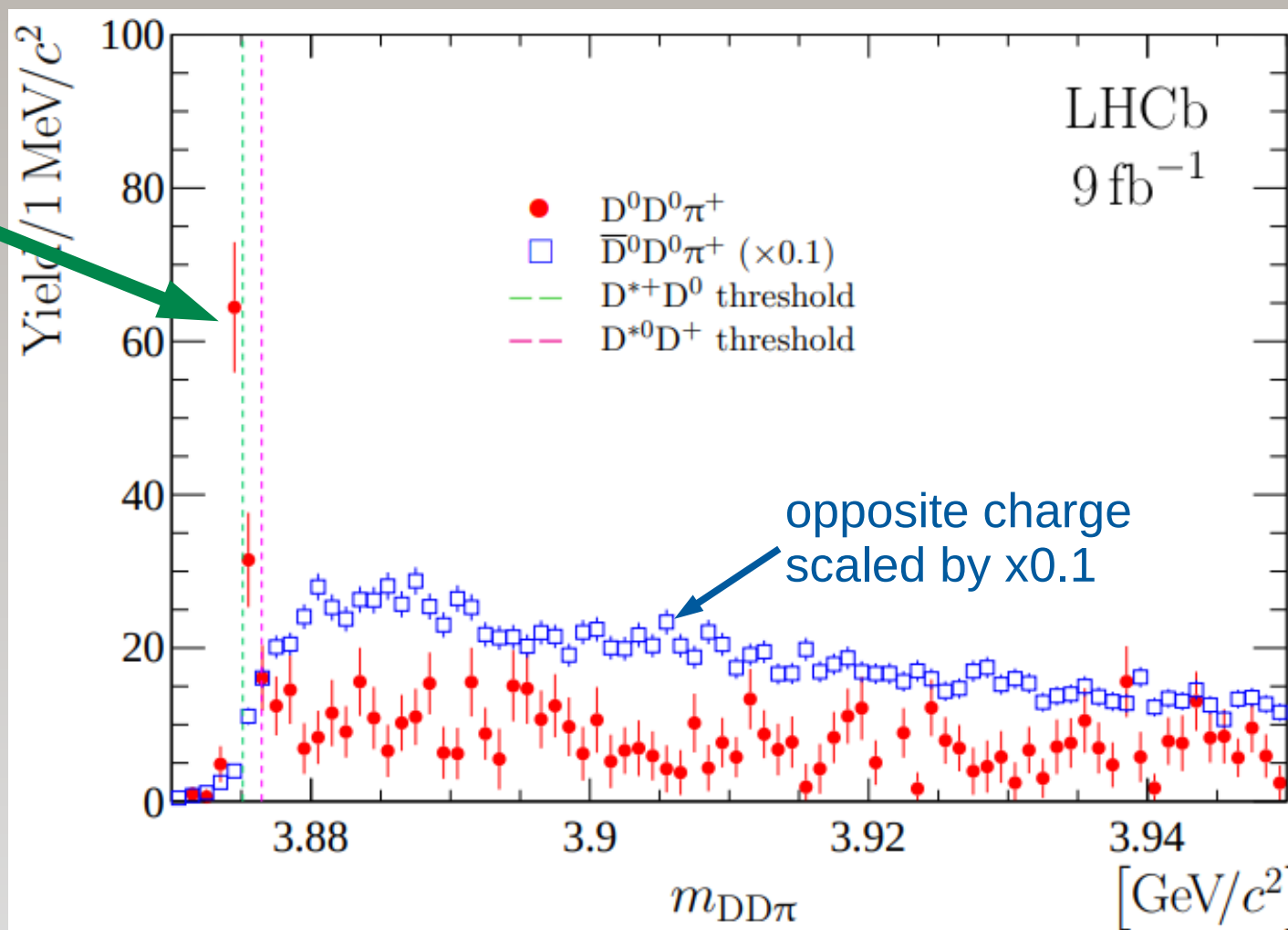


- Subtract fake-D background using 2D fit to $(m_{K\pi}, m_{K\pi})$



Signal

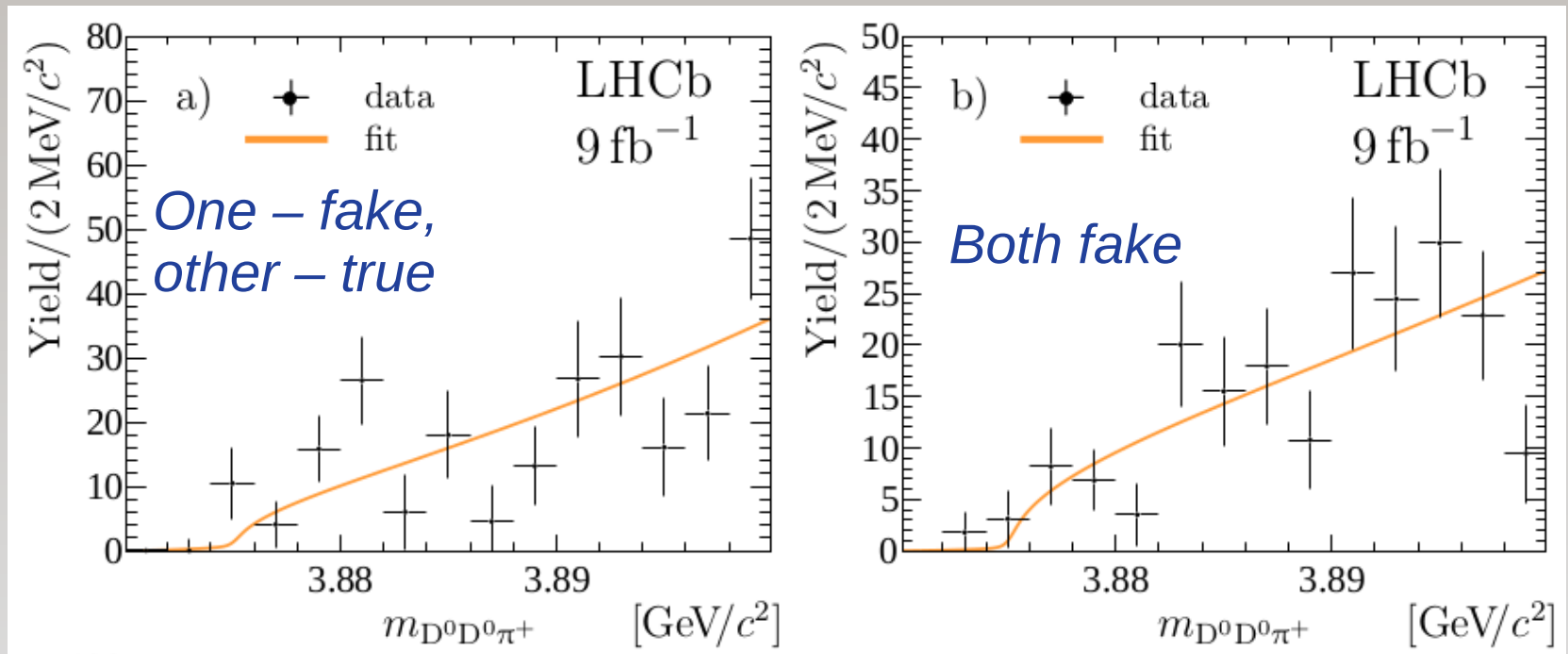
- A narrow peak near DD^* threshold is seen
- No peaking structures in sidebands or opposite-sign mode (can't be explained by DCS decay $D^0 \rightarrow K^+\pi^-$)
- The structure is present in all different data taking condition subsamples



Cross-checks

- Different years, data taking conditions
- Exclude double-counting, ensure no duplicated tracks
- No reflections from mis-identification
- Ensure peaks produced by true D^0 candidates

Mass distributions with fake D^0 's



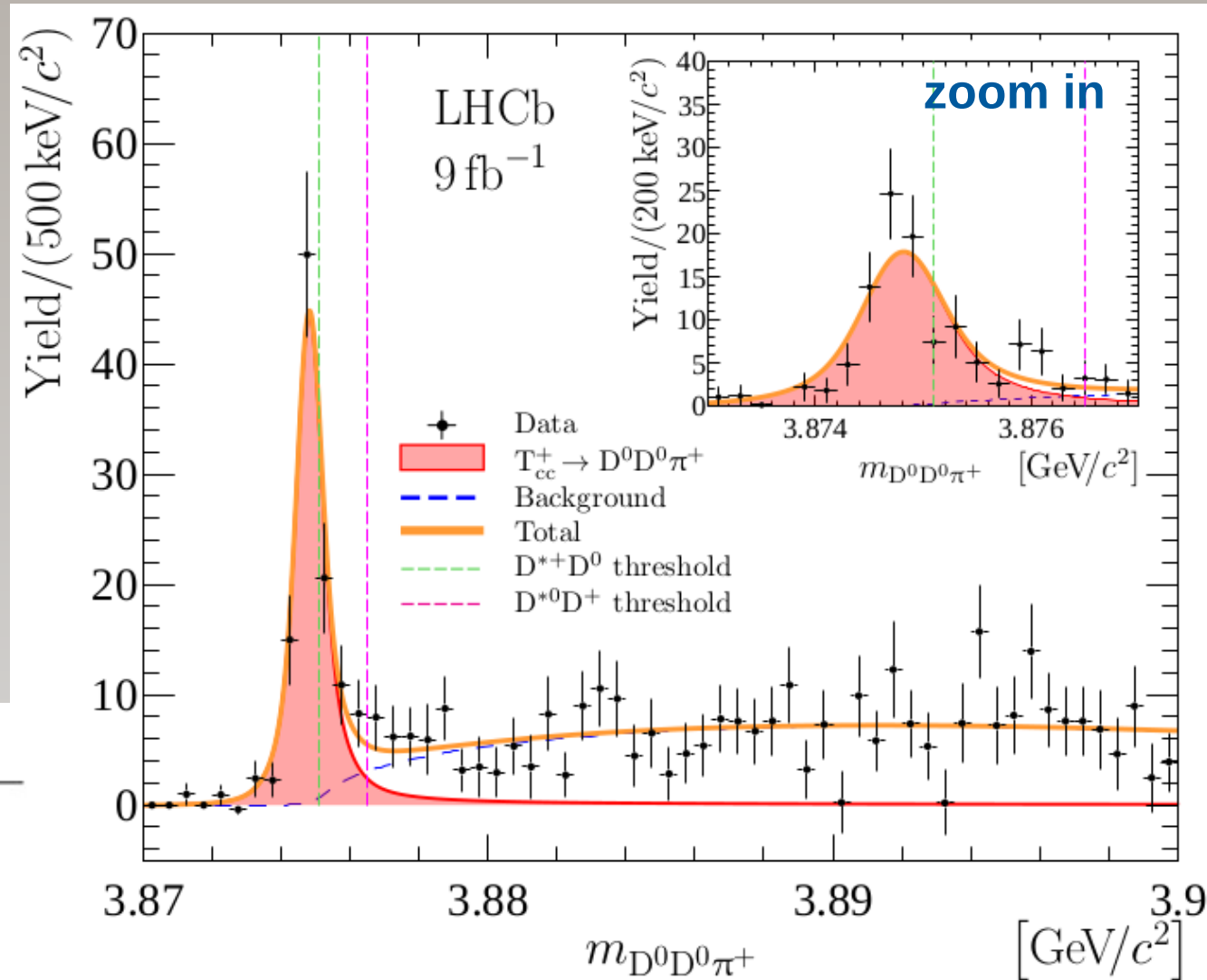
Fit with Breit-Wigner function

- The distribution is fit with a sum of
 - P-wave relativistic Breit-Wigner
 - $D^{*+}D^0$ phase space $\times \text{pol}_1$
 both convolved with resolution of $\sim 400\text{keV}$

- Found to be below the $D^{*+}D^0$ threshold (with 4.3σ significance for “below $D^{*+}D^0$ ”)

Results:

Parameter	Value
N	117 ± 16
δm_{BW}	$-273 \pm 61 \text{ keV}/c^2$
Γ_{BW}	$410 \pm 165 \text{ keV}$



Decay amplitude

- Construct an advanced model assuming
 - T_{cc}^+ is isoscalar
 - $J^P=1^+$
 - Same coupling for decays to DD^*

$$|T_{cc}^+\rangle = \frac{1}{\sqrt{2}} (|D^{*+}D^0\rangle - |D^{*0}D^+\rangle)$$

- Derive amplitudes for $X \rightarrow DD^*$ (as $1^+ \rightarrow 0^-1^-$ in S -wave) and $D^* \rightarrow D\pi/\gamma$ (as $1^- \rightarrow 0^-0^-/1^-$): (parameters f, h, μ – from known BR)

$$\begin{aligned} \mathcal{A}_{T_{cc}^+ \rightarrow D^{*+}D^0}^{S\text{-wave}} &= +\frac{g}{\sqrt{2}} \epsilon_{T_{cc}^+ \mu} \epsilon_{D^*}^{*\mu} \\ \mathcal{A}_{T_{cc}^+ \rightarrow D^{*0}D^+}^{S\text{-wave}} &= -\frac{g}{\sqrt{2}} \epsilon_{T_{cc}^+ \mu} \epsilon_{D^*}^{*\mu} \end{aligned}$$

$$\begin{aligned} \mathcal{A}_{D^{*+} \rightarrow D^0\pi^+} &= f \epsilon_{D^*}^\alpha p_{D\alpha} \\ \mathcal{A}_{D^{*+} \rightarrow D^+\pi^0} &= -\frac{f}{\sqrt{2}} \epsilon_{D^*}^\alpha p_{D\alpha} \\ \mathcal{A}_{D^{*0} \rightarrow D^0\pi^0} &= +\frac{f}{\sqrt{2}} \epsilon_{D^*}^\alpha p_{D\alpha}, \\ \mathcal{A}_{D^* \rightarrow \gamma D} &= i\mu h \epsilon_{\alpha\beta\eta\xi} \epsilon_{D^*}^\alpha p_{D^*}^\beta \epsilon_\gamma^{*\eta} p_\gamma^\xi \end{aligned}$$

and combine them to together

$$\begin{aligned} \mathcal{A}_{\pi^+ D^0 D^0} &= \frac{fg}{\sqrt{2}} \epsilon_{T_{cc}^+ \nu} \left[\mathfrak{F}_+(s_{12}) \times \left(-p_2^\nu + \frac{(p_2 p_{12}) p_{12}^\nu}{s_{12}} \right) + (p_2 \leftrightarrow p_3) \right], \\ \mathcal{A}_{\pi^0 D^+ D^0} &= -\frac{fg}{2} \epsilon_{T_{cc}^+ \nu} \left[\mathfrak{F}_+(s_{12}) \times \left(-p_2^\nu + \frac{(p_2 p_{12}) p_{12}^\nu}{s_{12}} \right) + \left(\begin{array}{c} p_2 \leftrightarrow p_3 \\ \mathfrak{F}_+ \leftrightarrow \mathfrak{F}_0 \end{array} \right) \right] \\ \mathcal{A}_{\gamma D^+ D^0} &= i \frac{hg}{\sqrt{2}} \epsilon_{\alpha\beta\eta\xi} \epsilon_{T_{cc}^+}^\beta \epsilon_\gamma^{*\eta} p_\gamma^\xi [\mu_+ \mathfrak{F}_+(s_{12}) p_{12}^\alpha - \mu_0 \mathfrak{F}_0(s_{13}) p_{13}^\alpha] \end{aligned}$$

$$\mathfrak{F}(s) = \frac{1}{m_{D^*}^2 - s - im_{D^*} \Gamma_{D^*}}$$

Unitarized 3-body BW model

- Constructed advanced 3-body Breit-Wigner model where
 - 3-body phase-space is calculated via integral of $X \rightarrow DD^*[\rightarrow D\pi/\gamma]$ matrix element over $D^0D^{0+}\pi^+/\gamma$ Dalitz plot

$$\mathfrak{F}_f^U(s) = \varrho_f(s) |\mathcal{A}_U(s)|^2,$$

$$\mathcal{A}_U(s) = \frac{1}{m_U^2 - s - im_U \hat{\Gamma}(s)}$$

$$\varrho_f(s) = \frac{1}{(2\pi)^5} \frac{\pi^2}{4s} \iint ds_{12} ds_{23} \frac{|\mathfrak{M}_f(s, s_{12}, s_{23})|^2}{|g|^2}$$

- and where complex width is derived as

$$im_U \hat{\Gamma}(s) \equiv |g|^2 \Sigma(s)$$

**Imaginary part for unitarity
(optical theorem)**

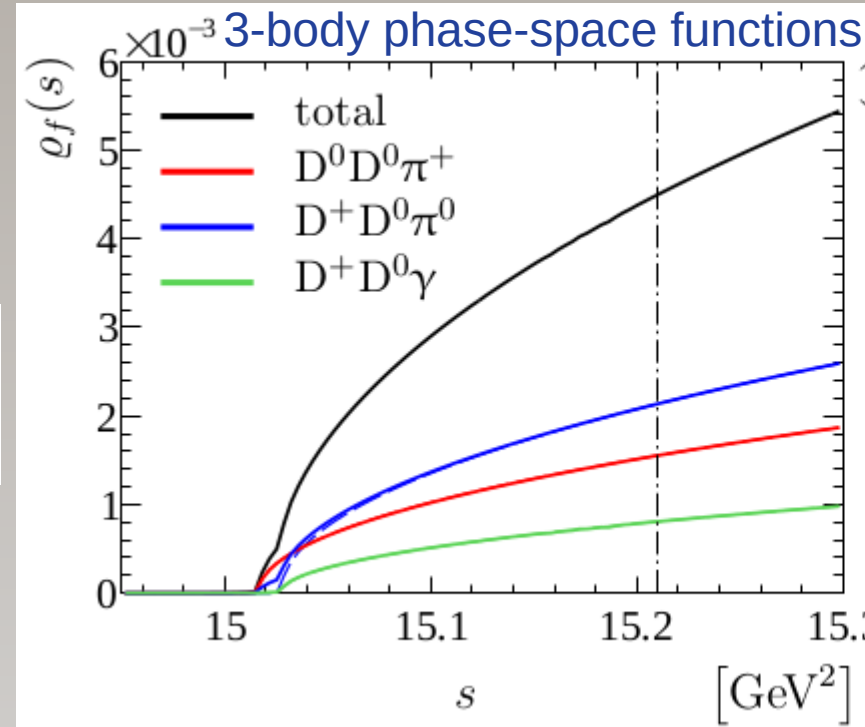
$$\Im \Sigma(s)|_{\Im s=0^+} = \frac{1}{2} \varrho_{\text{tot}}(s),$$

$$\varrho_{\text{tot}}(s) \equiv \sum_f \varrho_f(s)$$

**Real part for analyticity
(Kramers-Kronig relations)**

$$\Re \Sigma(s)|_{\Im s=0^+} = \xi(s) - \xi(m_U^2),$$

$$\xi(s) = \frac{s}{2\pi} \text{p.v.} \int_{s_{\text{th}}^*}^{+\infty} \frac{\varrho_{\text{tot}}(s')}{s'(s' - s)} ds'$$



Fit with unitarized model

- Fit to same data, use same model as before except for the signal function
- Peak position below D^0D^{*+} threshold with $\sim 9\sigma$ significance!

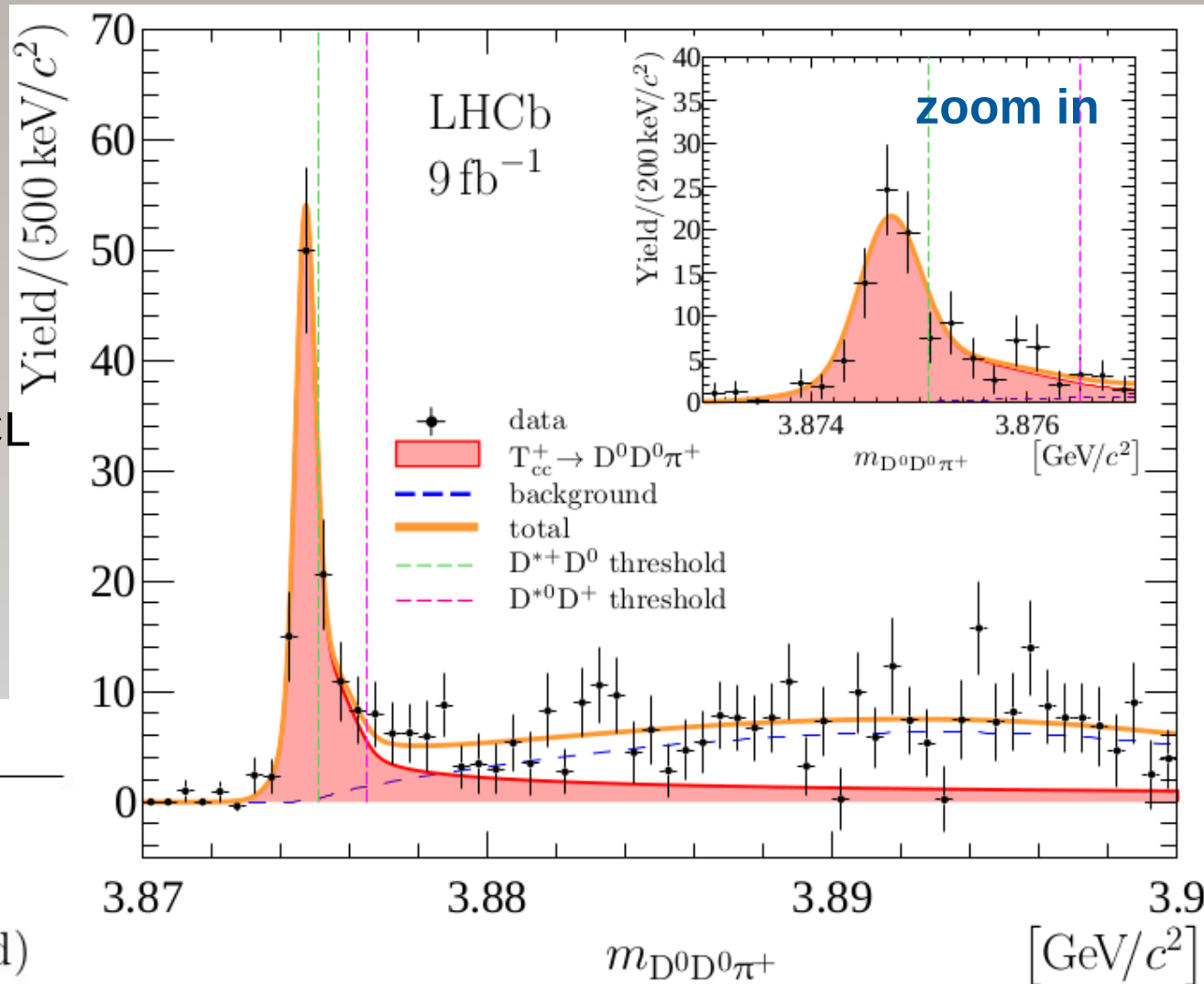
- Peak shape does not depend on $T_{cc} \rightarrow DD^*$ coupling $|g|$ for large values

→ get limit

$|g| > 7.7(6.2)$ GeV at 90(95)% CL

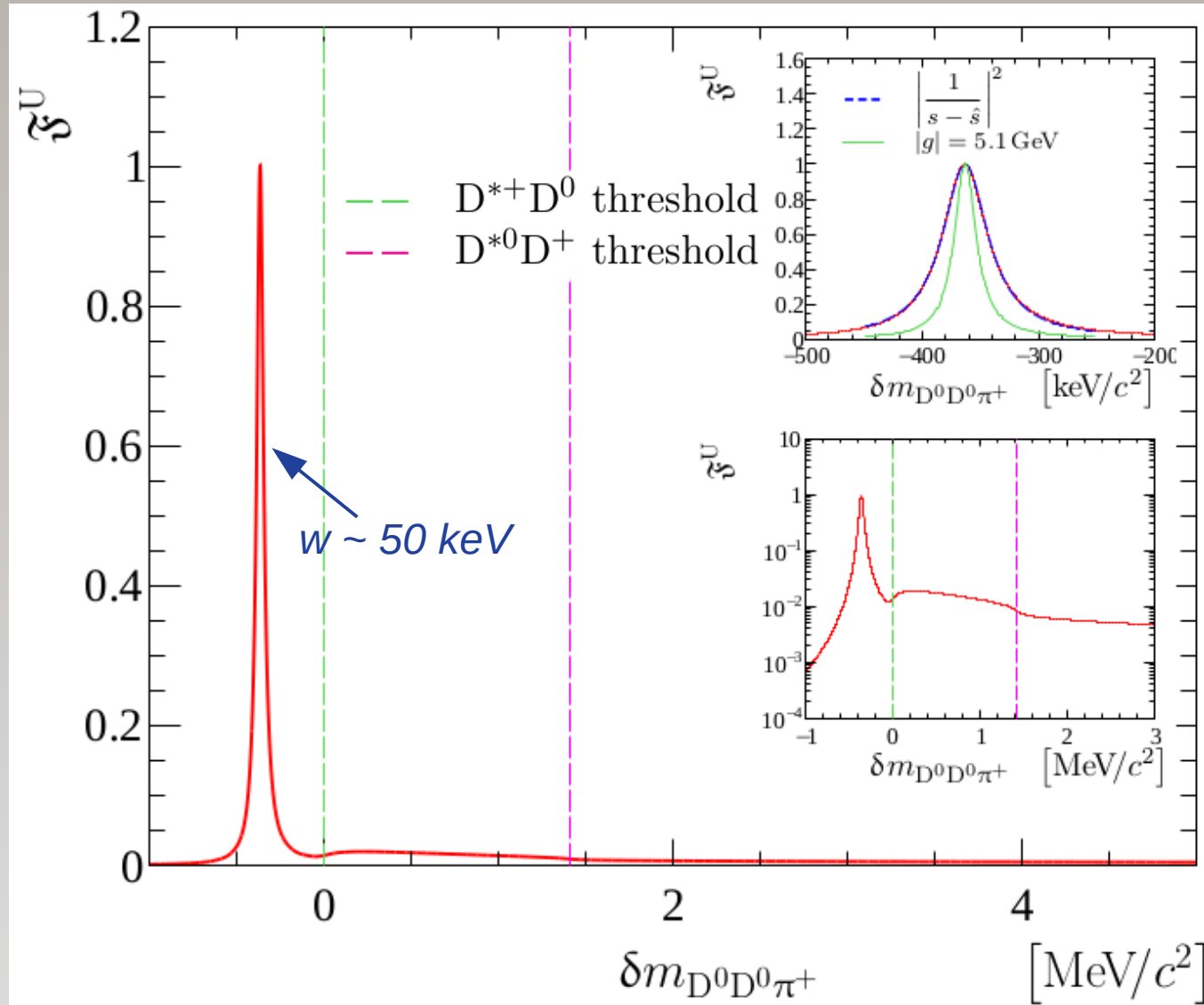
- Results:

Parameter	Value
N	186 ± 24
δm_U	$-359 \pm 40 \text{ keV}/c^2$
$ g $	$3 \times 10^4 \text{ GeV (fixed)}$



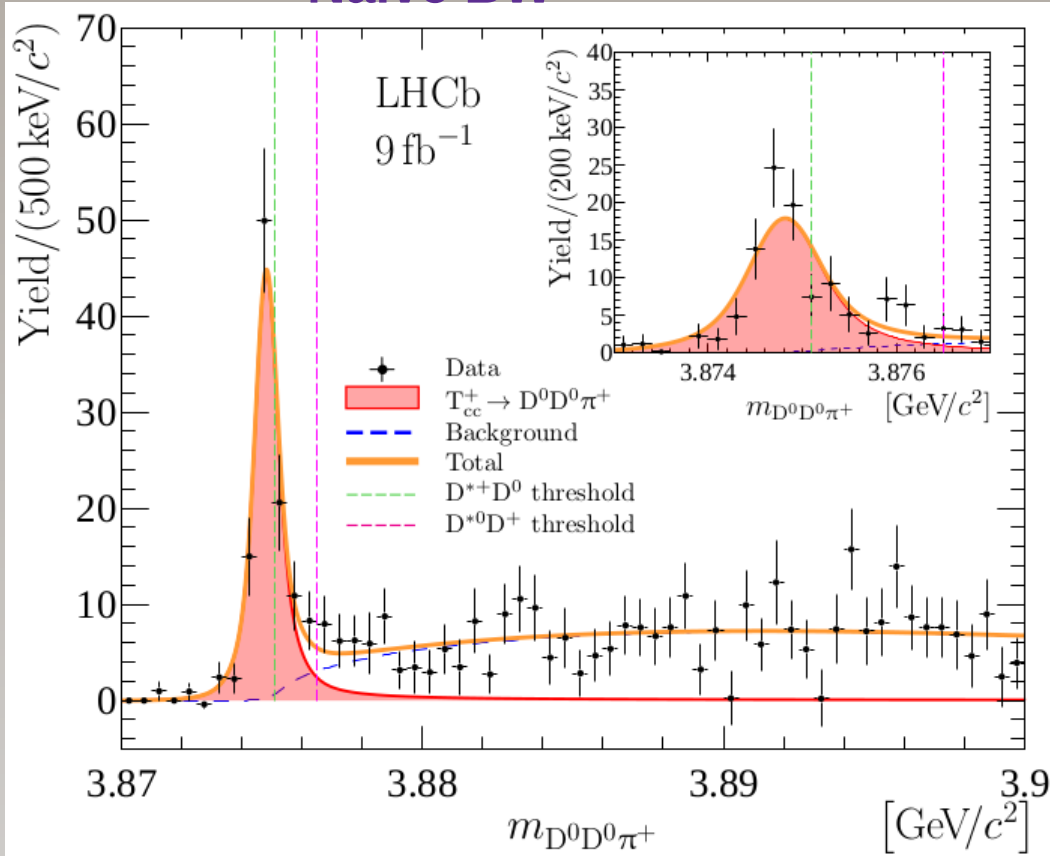
Mass shape in unitarized model

- Fit result (before smearing with resolution)
- Close to Breit-Wigner in proximity to peak maximum
- Large tail above DD^* thresholds

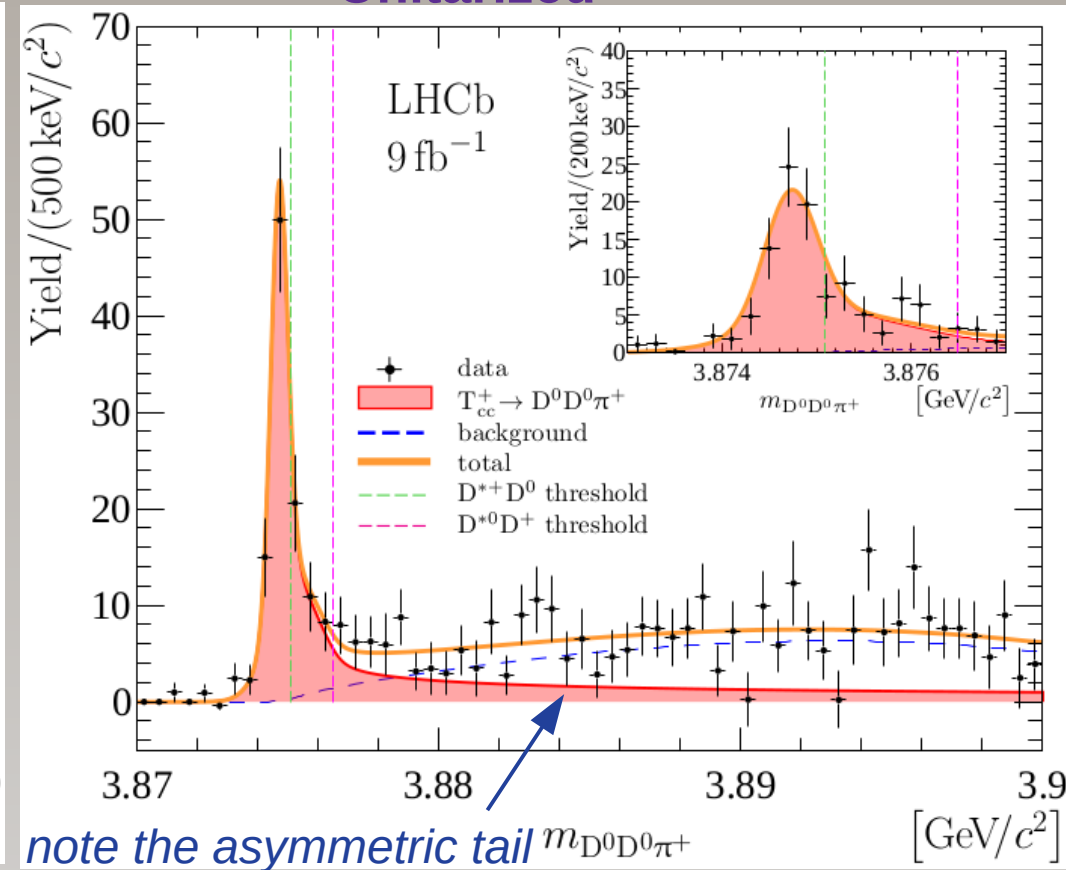


Fits with Naive and Unitarized models

Naive BW



Unitarized



- Compare position of peak maximum and FWHM (before convolving with resolution)

too naive →

	δm [keV/c ²]	w [keV/c ²]
\mathcal{F}^{BW}	-279 ± 59	409 ± 163
\mathcal{F}^{U}	-361 ± 40	47.8 ± 1.9

- Both consistent with data

Consistency of Naive and Unitarized

- Generate 25k pseudoexperiments using **unitarized** BW model, fit them with **naive** BW model.
Get δm_{BW} and Γ_{BW} consistent with values obtained from data
- Generate 4k pseudoexperiments using **naive** BW model, fit them with **unitarized** BW model.
Get δm_0 consistent with values obtained from data
- Consistent considering current **statistics**, **mass resolution** and **background**

Parameter		Pseudoexperiments		Data
		mean	RMS	
δm_{BW}	[keV/c ²]	-301	50	-273 ± 61
Γ_{BW}	[keV]	222	121	410 ± 165
δm_{U}	[keV/c ²]	-378	46	-359 ± 40

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Systematic uncertainties (unitarized model)

- Fit model
 - try alternative resolution functions
 - apply $\pm 5\%$ correction for resolution scale
 - try alternative background models
 - vary coupling constants f, h, μ within related uncertainties from $BR(D^* \rightarrow D\pi/\gamma)$ and $\Gamma(D^*)$
 - try smaller value for $|g|$
- Vary momentum scale by $\pm 0.03\%$
- Vary energy loss correction by $\pm 10\%$
- Uncertainty on D^0 mass cancels out in difference, while account for uncertainty on $m(D^{*+}) - m(D^0)$

Source	$\sigma_{\delta m_U}$ [keV/c ²]
Fit model	
Resolution model	2
Resolution correction factor	2
Background model	2
Coupling constants	1
Unknown value of $ g $	+7 -0
Momentum scaling	3
Energy loss	1
$D^{*+} - D^0$ mass difference	2
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Total	+9 -6

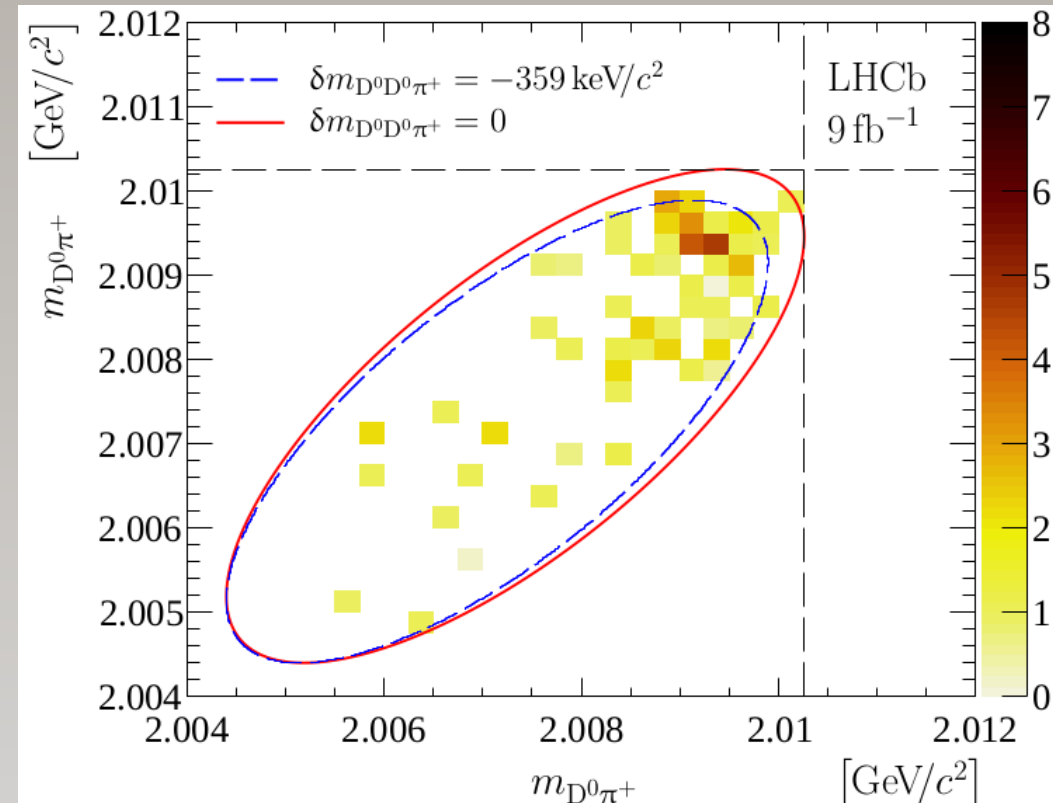
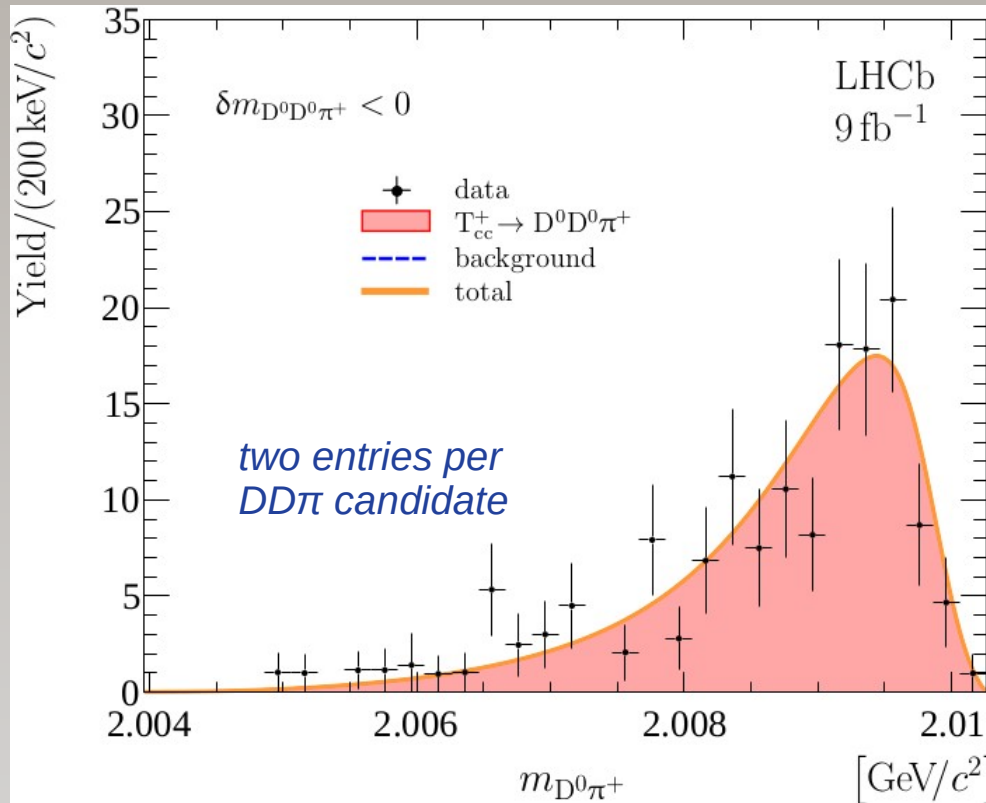
- Fit model systematics considered for the lower limit of $|g|$ changing it to

$$|g| > 5.1 (4.3) \text{ GeV at } 90 (95) \% \text{ CL}$$

Additional Studies

Offshell D^{*+}

- Integrate unitarized model over $D^0 D^0 \pi^+$ and $D^0 D^0$ masses
 → obtain $D^0 \pi^+$ shape

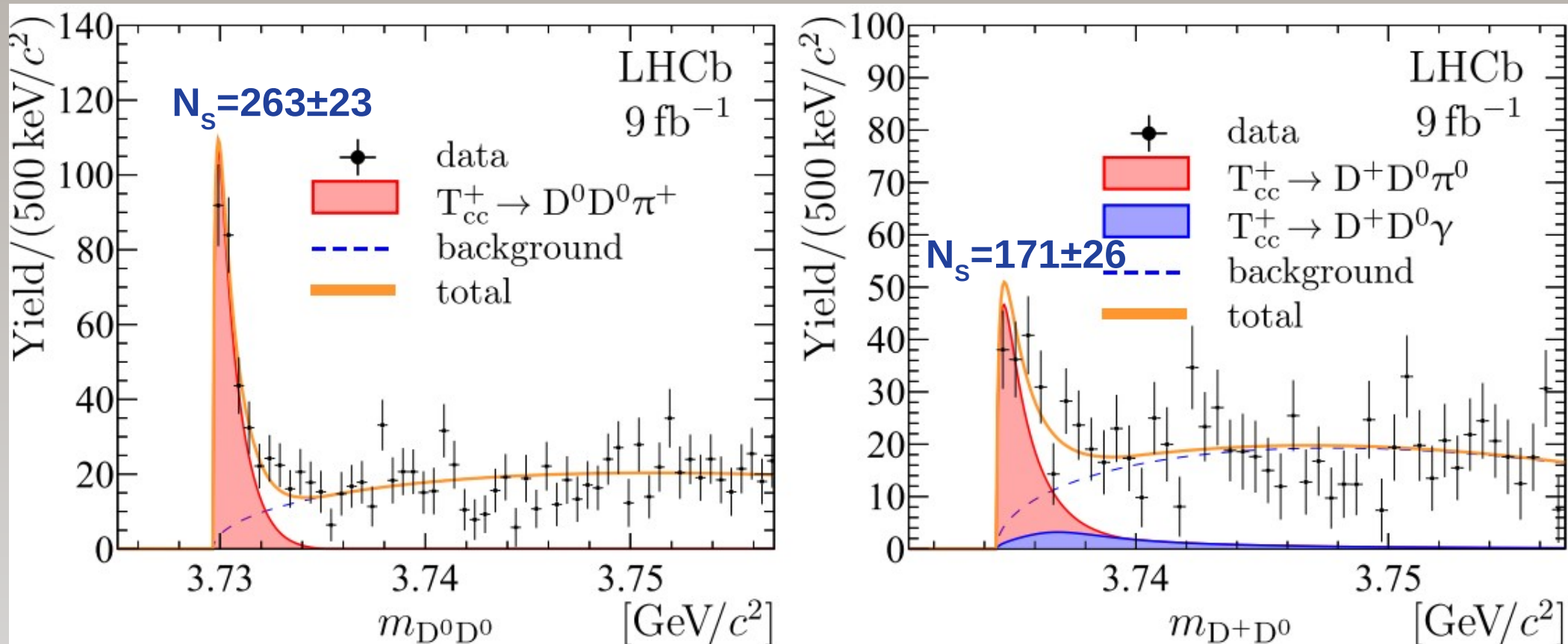


Perfect agreement supports the assumptions:

- $T_{cc} \rightarrow DD^*$ decaying via off-shell D^*
- $J^P=1^+$ assignement for T_{cc}

Partially reconstructed $T_{cc} \rightarrow D^0 D^{0/+} X$

- Obtain $D^0 D^0$ mass shape from $T_{cc} \rightarrow D^0 D^{*+} (\rightarrow D^0 \pi^+)$ and $D^0 D^+$ mass shape from $T_{cc} \rightarrow D^0 D^{*+} (\rightarrow D^+ \pi^0)$ and $T_{cc} \rightarrow D^+ D^{*0} (\rightarrow D^0 \pi^0 / \gamma)$ in the same way as for $D^0 \pi^+$



- Relative yields are in agreement with model expectations for isoscalar T_{cc} with $J^P=1^+$ and $D^{0/+}$ reconstruction efficiencies

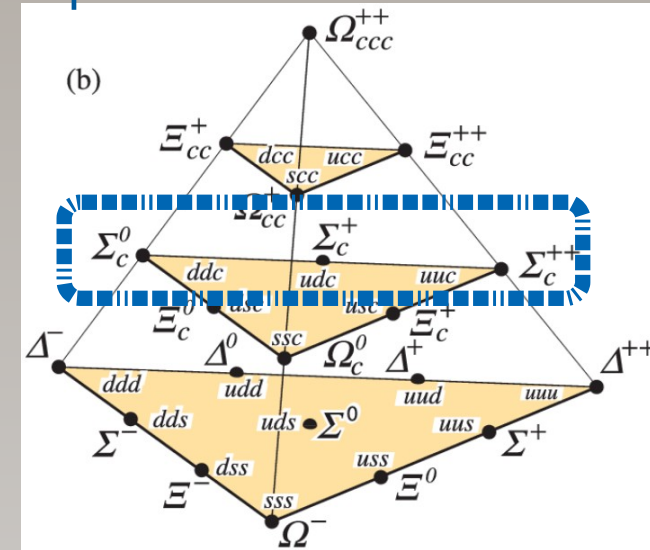
T_{cc} isospin

- If assume that $X \rightarrow D^0 D^0 \pi^+$ signal is part of an iso-triplet, then one can estimate masses of its partners to be:

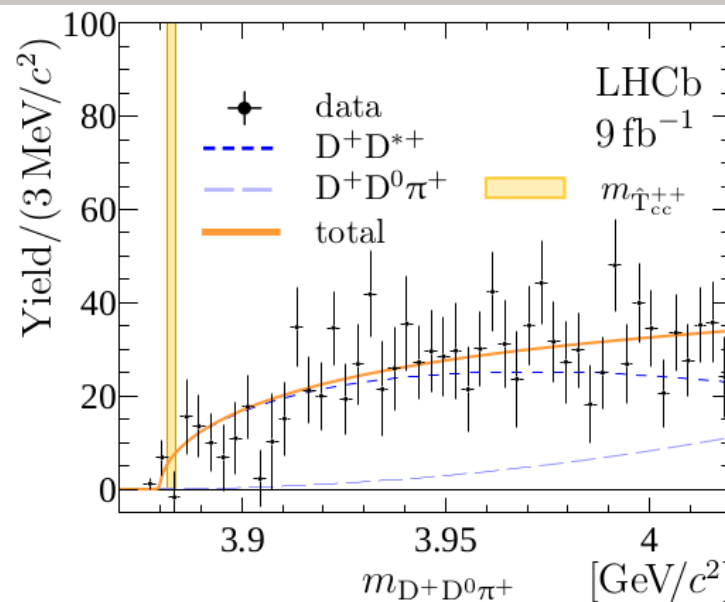
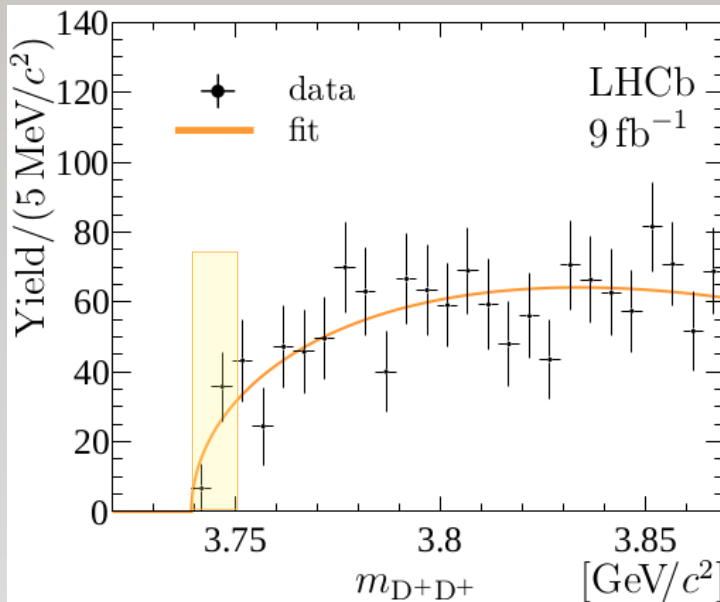
from Σ_b and Σ_c isotriplets

$$\begin{aligned}
 m_{\hat{T}_{cc}^0} &= m_{\hat{T}_{cc}} + m_u + m_u - a' q_{\bar{u}} q_{\bar{u}} - b' q_{cc} (q_{\bar{u}} + q_{\bar{u}}) \\
 m_{\hat{T}_{cc}^+} &= m_{\hat{T}_{cc}} + m_u + m_d - a' q_{\bar{u}} q_{\bar{d}} - b' q_{cc} (q_{\bar{u}} + q_{\bar{d}}) \\
 m_{\hat{T}_{cc}^{++}} &= m_{\hat{T}_{cc}} + m_d + m_d - a' q_{\bar{d}} q_{\bar{d}} - b' q_{cc} (q_{\bar{d}} + q_{\bar{d}})
 \end{aligned}$$

$$\begin{aligned}
 m_{\hat{T}_{cc}^0} - (m_{D^0} + m_{D^{*0}}) &= -2.8 \pm 1.5 \text{ MeV}/c^2 \\
 m_{\hat{T}_{cc}^{++}} - (m_{D^+} + m_{D^{*+}}) &= 2.7 \pm 1.3 \text{ MeV}/c^2
 \end{aligned}$$



- Should therefore see a comparable peak from $T_{cc}^{++} \rightarrow D^+ D^{*+}$ decay (100-200 events) in $D^+ D^+$ and $D^+ D^0 \pi^+$, no signal is seen



Pole position

- Within the advanced decay model (with dominant role of DD* decay mode) find pole position as solution

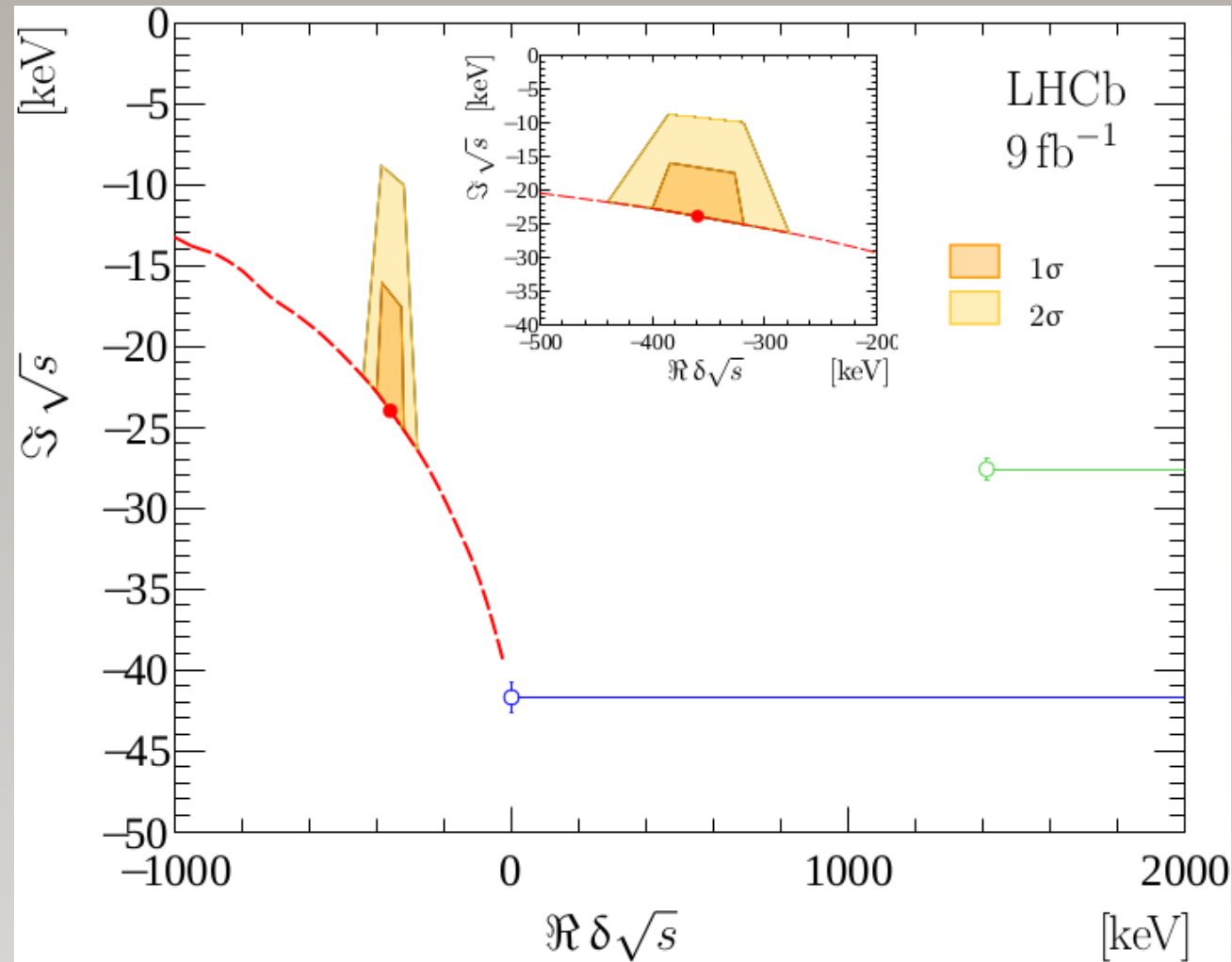
$$\frac{1}{\mathcal{A}_U^{II}(\hat{s})} = 0$$

$$\sqrt{\hat{s}} \equiv m_{\text{pole}} - \frac{i}{2}\Gamma_{\text{pole}}$$

$$\delta\sqrt{s} \equiv \sqrt{s} - (m_{D^{*+}} + m_{D^0})$$

- Result

$$\begin{aligned} \delta m_{\text{pole}} &= -360 \pm 40_{-0}^{+4} \text{ keV}/c^2, \\ \Gamma_{\text{pole}} &= 48 \pm 2_{-14}^{+0} \text{ keV}, \end{aligned}$$



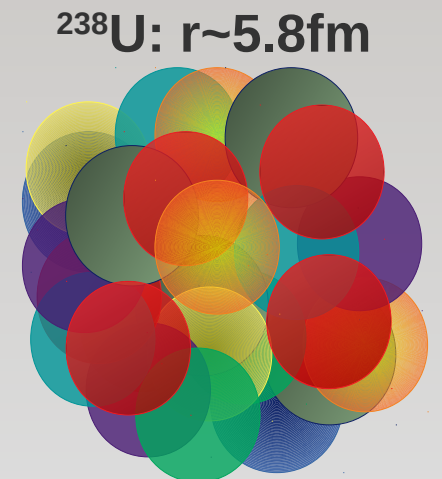
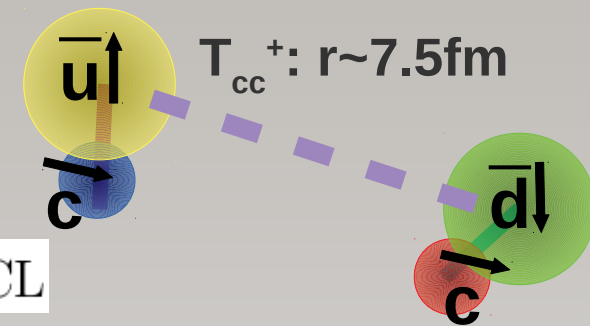
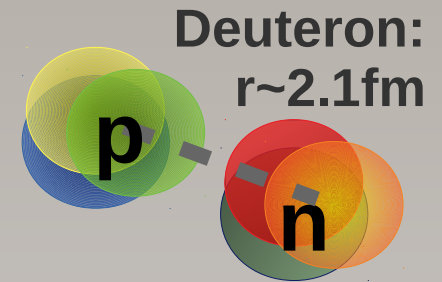
Low-energy expansion

- From expansion near pole can extract low-energy scattering parameters

$$\mathcal{A}_{\text{NR}}^{-1} = \frac{1}{a} + r \frac{k^2}{2} - ik + \mathcal{O}(k^4)$$

- scattering length: $a = \left[-(7.16 \pm 0.51) + i(1.85 \pm 0.28) \right] \text{ fm}$
- characteristic size: $R_a \equiv -\Re a = 7.16 \pm 0.51 \text{ fm}$
- effective range: $0 \leq -r < 11.9 (16.9) \text{ fm}$ at 90 (95)% CL
- Weinberg compositness: $Z < 0.52 (0.58)$ at 90 (95)% CL

- size in case of $D^0 D^{*+}$ molecule: $R_{\Delta E} \equiv \frac{1}{\gamma} = 7.5 \pm 0.4 \text{ fm}$



Production vs track multiplicity

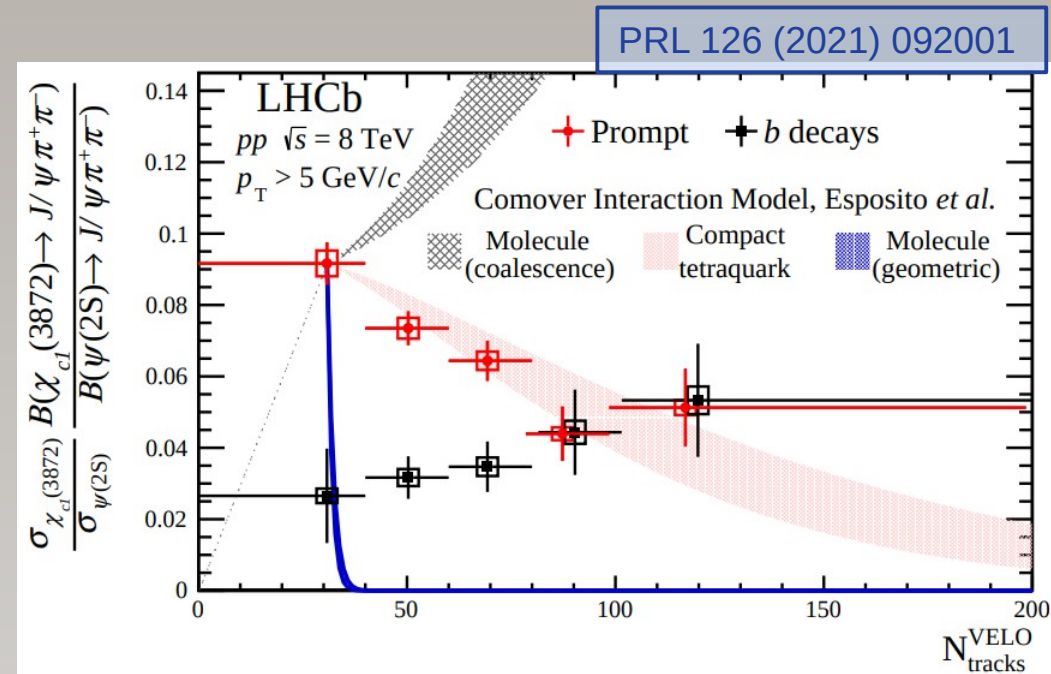
- Based on characteristic size one can expect that T_{cc}^+ has some properties similar to χ_{c1} (3872)
- For χ_{c1} (3872) production a suppression wrt $\psi(2S)$ was observed at high track multiplicities
- Explained in comover model where χ_{c1} (3872) is broken by closely flying pions/gluons
- Therefore probing effective $Q\pi$ break-up cross-section:

$$\langle v\sigma_{\psi'} \rangle = 3.9 \pm 0.8 \text{ mb}$$

$$\langle v\sigma_X \rangle = 2.6 \pm 0.7 \text{ mb}$$

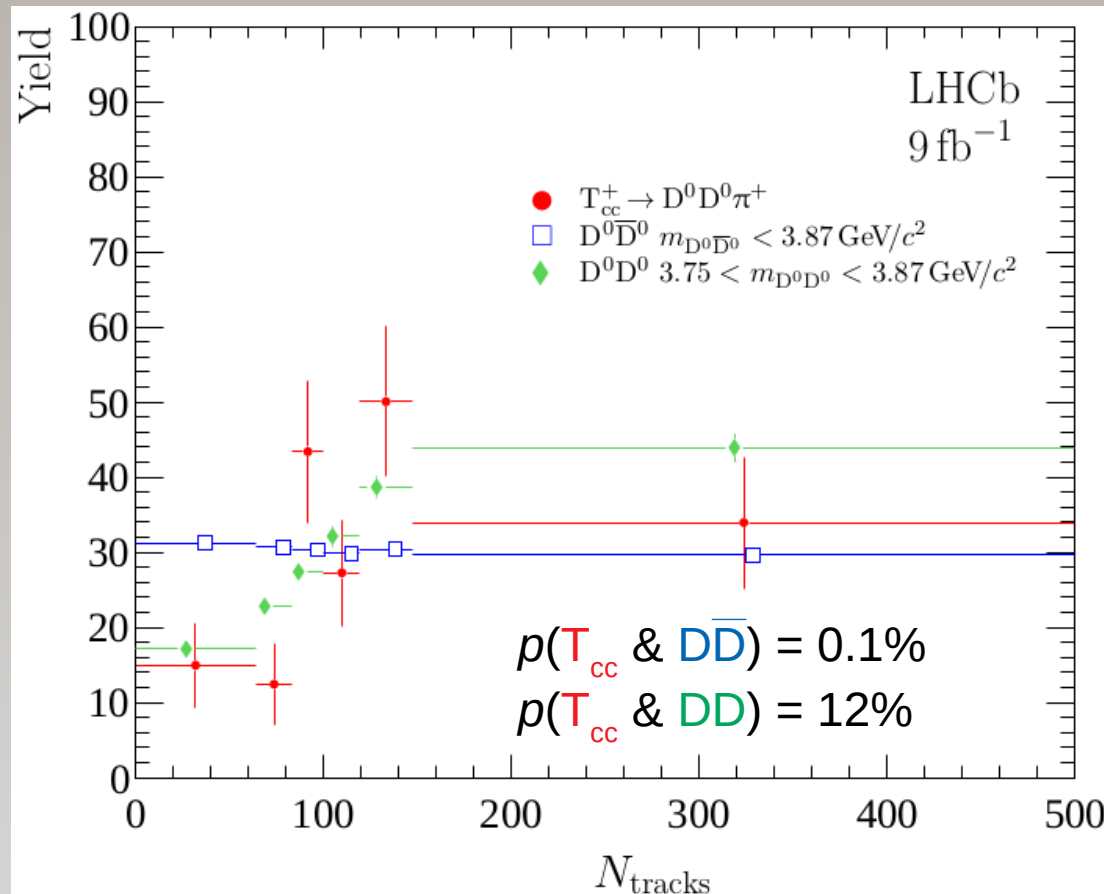
and fractions of Q out of reach of comovers

more details in [Braaten et al., arXiv:2021.13499](#)



T_{cc} multiplicity distribution

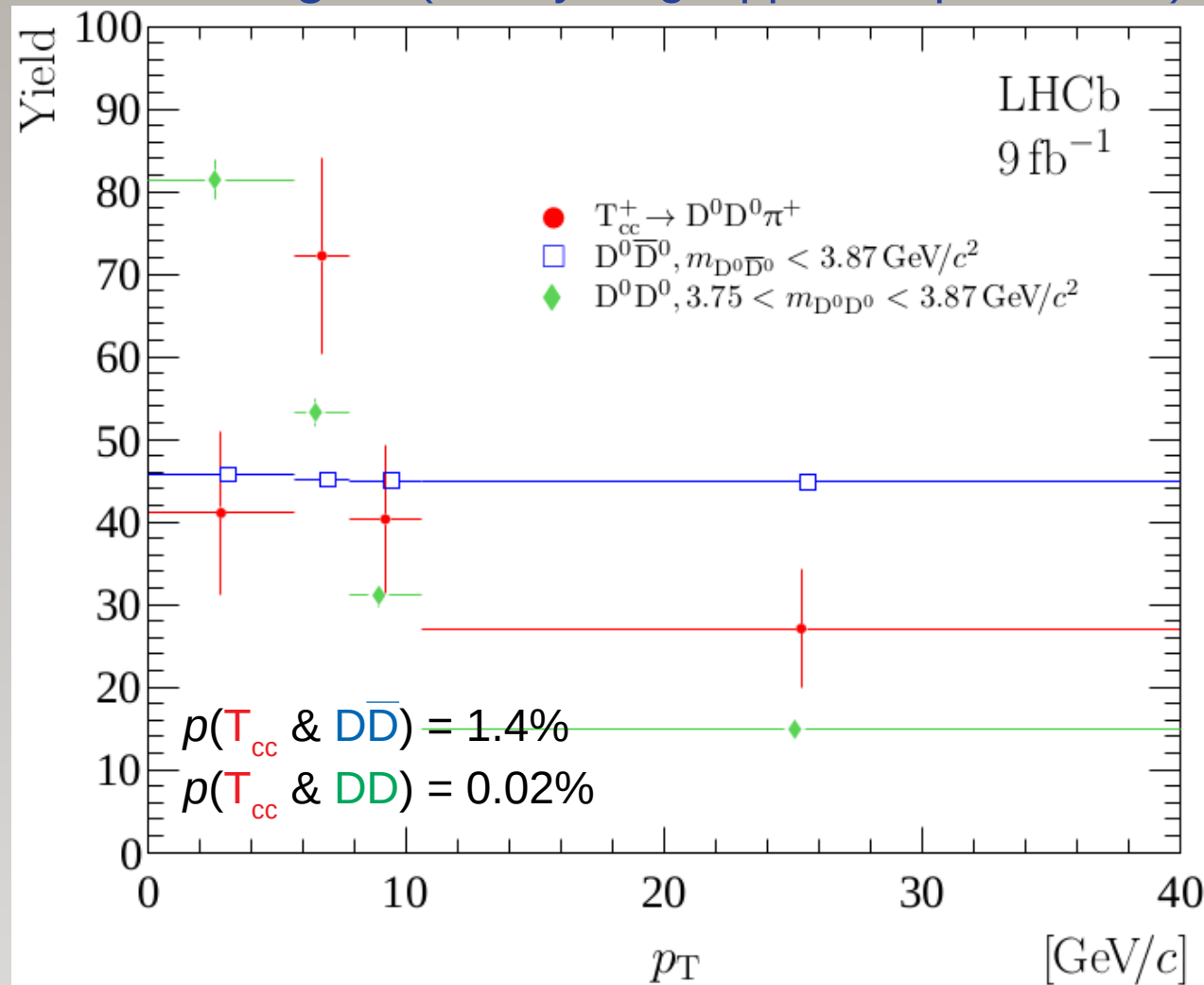
- Compare $T_{cc}^+ \rightarrow D^0 D^0 X$ signal distributions with
 - $D^0 D^0$ in $3.75 < m_{D^0 D^0} < 3.87$ GeV region
(presumably dominated by double-parton scattering)
 - $D^0 \bar{D}^0$ in $m_{D^0 \bar{D}^0} < 3.87$ GeV region (mainly single $pp \rightarrow D\bar{D}$ production)



- No suppression of T_{cc}^+ wrt $D\bar{D}$ (and also to DD) at high multiplicities in contrast to $X(3872)$ wrt $\psi(2S)$
- Intriguing similarity with $cc+cc$

Transverse momenta spectra

- Compare $T_{cc}^+ \rightarrow D^0 D^0 X$ signal distributions with
 - $D^0 D^0$ in $3.75 < m_{D^0 D^0} < 3.87$ GeV region
(presumably dominated by double-parton scattering)
 - $D^0 \bar{D}^0$ in $m_{D^0 \bar{D}^0} < 3.87$ GeV region (mainly single $pp \rightarrow D \bar{D}$ production)



- Intriguing similarity with $c\bar{c} + c\bar{c}$

Discussions

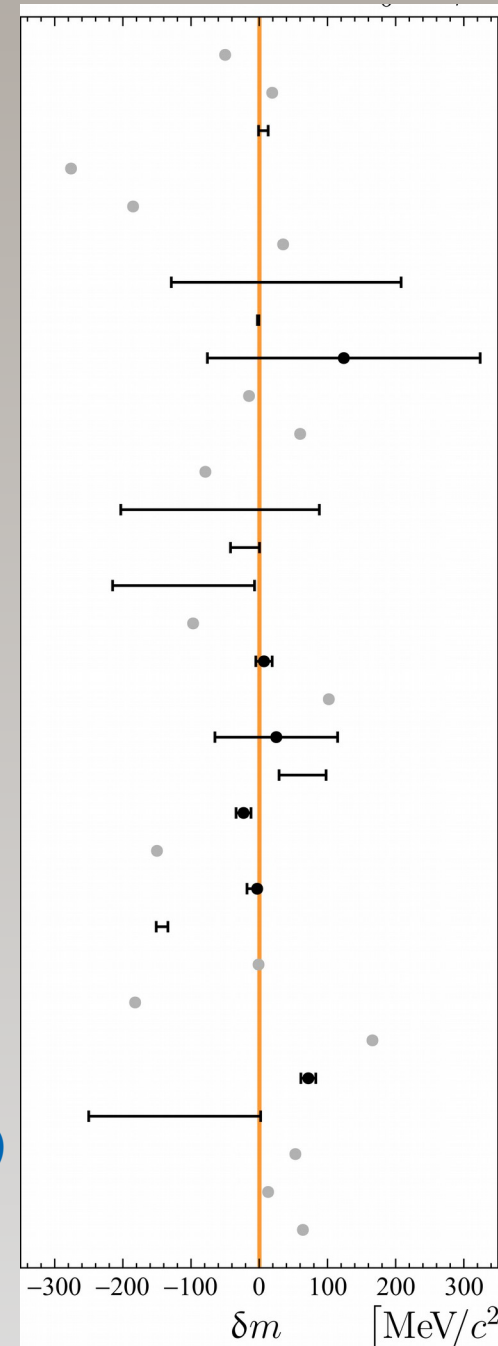
Reflections on measured mass, 1

- The measured mass difference

$$\delta m_U = -359 \pm 40^{+9}_{-6} \text{ keV}/c^2$$

is consistent with some of predictions.

- Few notable matches for δm predictions:
 - [-1,+13] MeV** Semay, Silvestre-Brac, 1994
(NR quark-quark potential model)
 false prediction (1993) for spin-0&1 $c\bar{c}q\bar{q}$ states with masses $\sim 3300\text{-}3400$ MeV
 - [-2.7,-0.6] MeV** Janc, Rosina, 2003
(NR quark-quark potential model)
 -0.6 MeV corresponds to Bhaduri potential
 - [-42.1;+0.3] or [-18;+1] MeV**
(OME exchange in DD^ molecule)*
Li, Sun, Liu, Zhu, 2012 Liu, Wu, Valderrama, Xie, Geng, 2019
 - 1 ± 12 MeV** Karlner, Rosner, 2017
(phenomenology model for compact tetraquark)
 - -23 ± 11 MeV** Junnarkar, Mathur, Padmanath, 2018
(Lattice QCD)



J. Carlson <i>et al.</i>	1987
B. Silvestre-Brac and C. Semay	1993
C. Semay and B. Silvestre-Brac	1994
M. A. Moinester	1995
S. Pepin <i>et al.</i>	1996
B. A. Gelman and S. Nussinov	2003
J. Vijande <i>et al.</i>	2003
D. Janc and M. Rosina	2004
F. Navarra <i>et al.</i>	2007
J. Vijande <i>et al.</i>	2007
D. Ebert <i>et al.</i>	2007
S. H. Lee and S. Yasui	2009
Y. Yang <i>et al.</i>	2009
N. Li <i>et al.</i>	2012
G.-Q. Feng <i>et al.</i>	2013
S.-Q. Luo <i>et al.</i>	2017
M. Karlner and J. Rosner	2017
E. J. Eichten and C. Quigg	2017
Z. G. Wang	2017
W. Park <i>et al.</i>	2018
P. Junnarkar <i>et al.</i>	2018
C. Deng <i>et al.</i>	2018
M.-Z. Liu <i>et al.</i>	2019
L. Maiani <i>et al.</i>	2019
G. Yang <i>et al.</i>	2019
Y. Tan <i>et al.</i>	2020
Q.-F. Lü <i>et al.</i>	2020
E. Braaten <i>et al.</i>	2020
D. Gao <i>et al.</i>	2020
J.-B. Cheng <i>et al.</i>	2020
S. Noh <i>et al.</i>	2021
R. N. Faustov <i>et al.</i>	2021

[see Refs. in paper]

Two of the notable matches

- The measured mass difference

$$\delta m_U = -359 \pm 40^{+9}_{-6} \text{ keV}/c^2$$

- NR quark-quark potential model

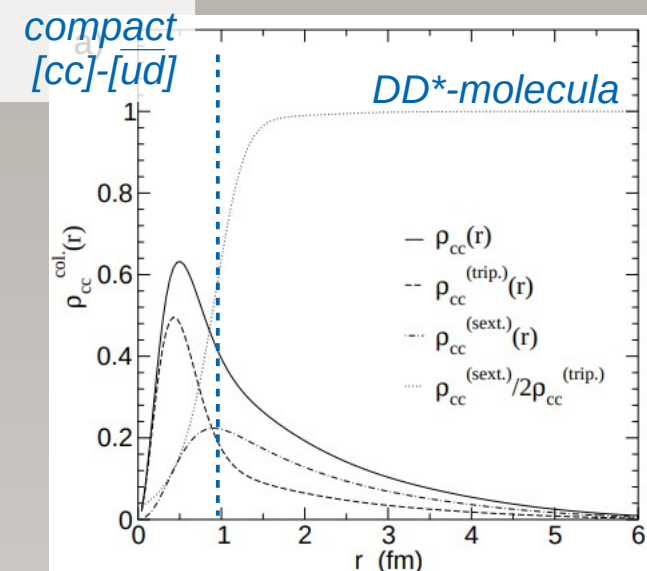
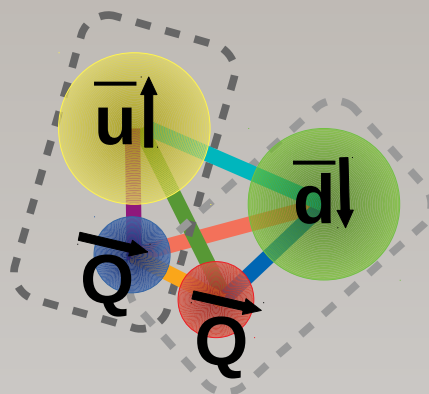
- [-2.7,-0.6] MeV**

-0.6 MeV corresponds to Bhaduri potential

*gives insight into wave function:
spatial & color configuration*

→ dominated by DD component*

Janc, Rosina, 2003



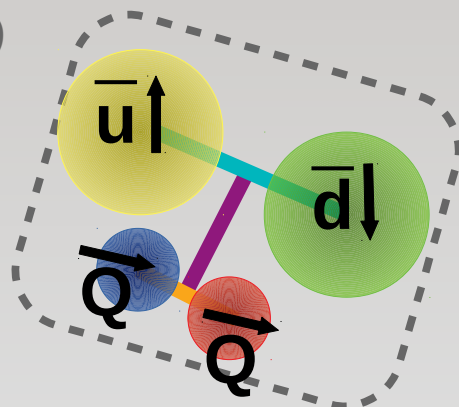
- Phenomenology model for compact tetraquark [cc]-[$\bar{u}\bar{d}$]

- 1±12 MeV**

- using measured Ξ_{cc} mass to calibrate cc binding

($\delta m = 7 \pm 12 \text{ MeV} \rightarrow 1 \pm 12 \text{ MeV}$)

Karliner, Rosner, 2017



Contribution	Value (MeV)
$2m_c^b$	3421.0
$2m_q^b$	726.0
$a_{cc}/(m_c^b)^2$	14.2
$-3a/(m_q^b)^2$	-150.0
cc binding	-129.0
Total	3882.2 ± 12

Reflections on measured mass, 2

- The measured mass difference

$$\delta m_U = -359 \pm 40_{-6}^{+9} \text{ keV}/c^2$$

has the best precision wrt threshold of all exotics

- Demands better theory estimates

→ can start from accounting for isospin splitting

$$\text{note } m_{th}(D^+D^{*0}) - m_{th}(D^0D^{*+}) = 1.3 \text{ MeV}$$

- Using known D^0 and D^{*+} mass can derive

$$\begin{aligned} m(T_{cc}^+) &= 3874.75 \pm 0.04(\text{exp}) \pm 2 \times 0.05(D^0) \text{ MeV} \\ &= 3874.75 \pm 0.11 \text{ MeV} \end{aligned}$$

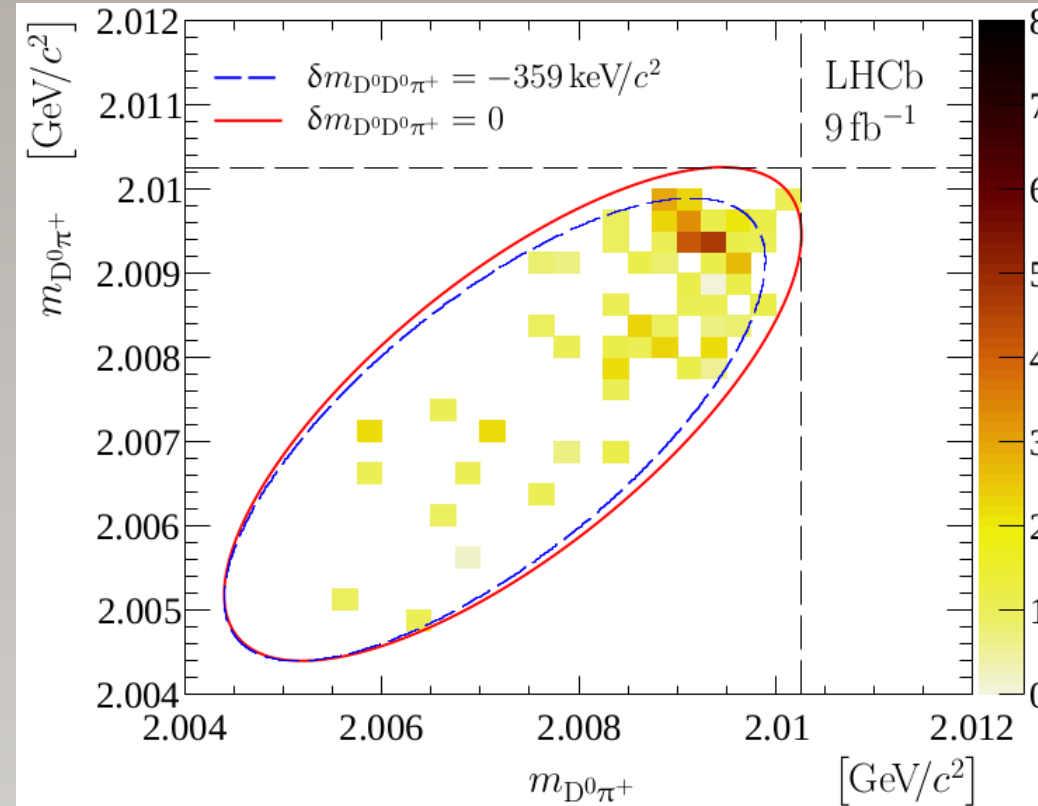
which is better than precision for

Λ_c (0.14 MeV), Σ_c (0.14 MeV), Ξ_{cc}^{++} (0.4 MeV) and η_c (0.4 MeV)

→ new input to tune the models

Future prospects for T_{cc}^+

- Analysis of the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ Dalitz-plot analysis to confirm $J^P=1^+$ spin assignment and probe for isovector component
- Dedicated measurement on $D^0 D^0 X$ and $D^0 D^+ X$ relative yields to probe iso-spin violation
- Production cross-section and multiplicity / momentum spectra



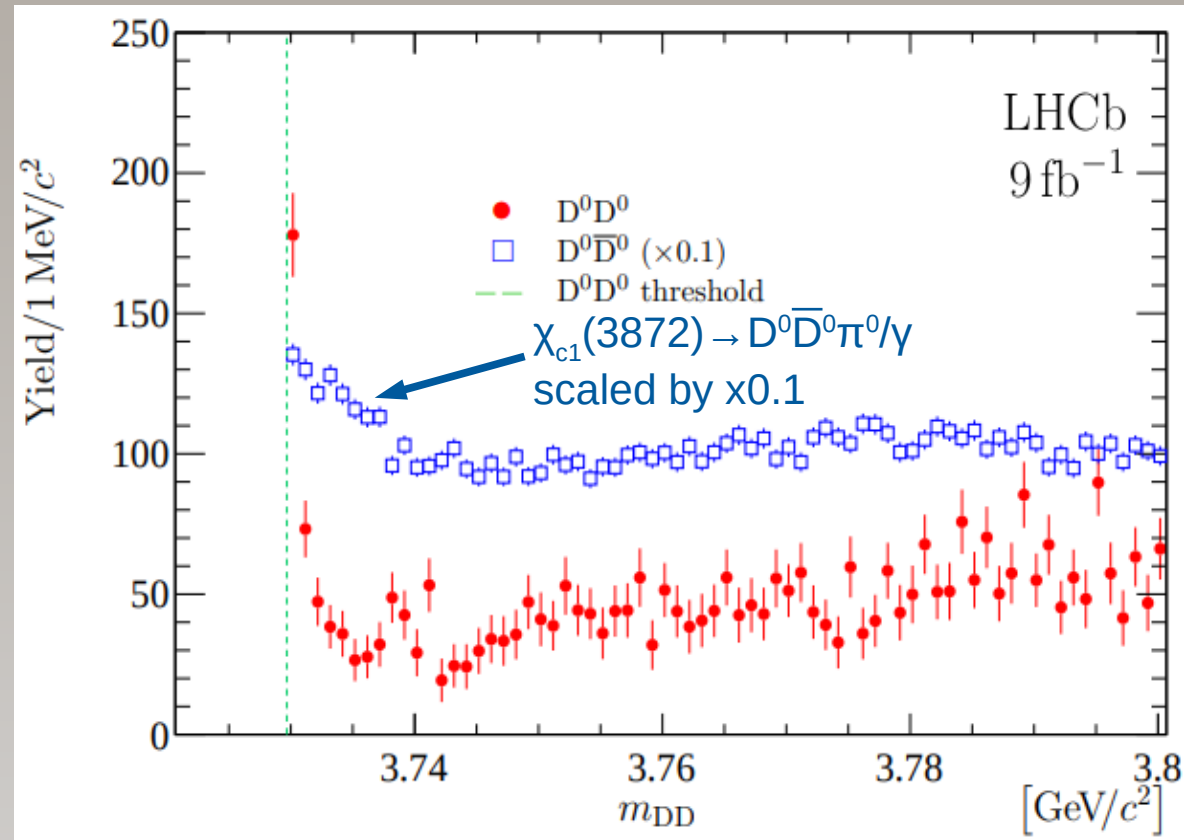
- Inclusion of $D^0 \rightarrow K \pi \pi \pi$ can give $\sim 50\%$ gain in statistics
- Data of Run3 (x5 gain in statistics, possibly x2 in efficiency) will be especially important

Production estimation

- One can estimate yields wrt $\chi_{c1}(3872)$ using D^0D^0 and $D^0\bar{D}^0$ spectra:

$$\frac{N(T_{cc}^+ \rightarrow D^0D^0\pi^+)}{N(\chi_{c1}(3872) \rightarrow D^0\bar{D}^0\pi^0)} \sim 1/20$$

- In future with better understanding of $\chi_{c1}(3872) \rightarrow D^0\bar{D}^0X$ shape a dedicated measurement can be done



- Interesting to determine $\sigma(T_{cc}^+)/\sigma(\Xi_{cc}^{++})$, either closer to $\sigma(\Lambda_c^+)/\sigma(D) \sim 0.1-0.2$ or $\sigma(\Lambda_b^0)/\sigma(B) \sim 1/2$ (in pp at 13 TeV) or less?

will be limited by knowledge of $\text{Br}(\Xi_{cc}^{++} \rightarrow \Lambda_c^+ K \pi \pi) \sim 5-20\%$,
 $\text{Br}(\Xi_{cc}^{++} \rightarrow \Xi_c^+ \pi^+) \sim 1.3-4\%$,
 $\text{Br}(\Xi_c^+ \rightarrow p K \pi) \sim (6.2 \pm 3.0) \times 10^{-3}$

Other doubly-heavy states

- The T_{cc} below DD^* threshold supports predictions for stable T_{bb}

- Interestingly, binding for $[bc][\overline{ud}]$ wrt \overline{BD} threshold is expected to be ~ 10 MeV higher than for T_{cc}^+ wrt DD^*

Karliner, Rosner, 2017

Semay, Silvestre-Brac, 1994

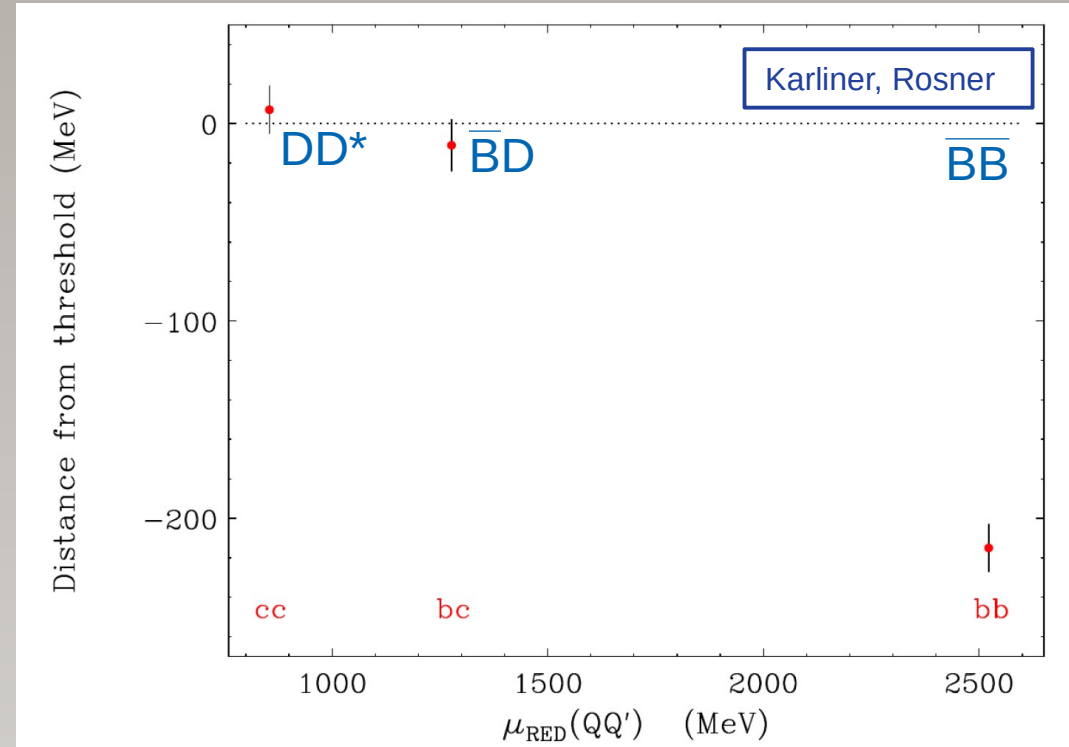
→ Giving stable T_{bc} ?

- Different expectations in molecular models

Li, Sun, Liu, Zhu, 2012

Liu, Wu, Valderrama, Xie, Geng, 2019

- Good test for models



- From naive phenomenology (HQS-like) estimates one can expect that
 - $[cc][\overline{sq}]$ and $[cc][\overline{sq}]$ are above corresponding thresholds.
 - $[cc][\overline{ud}]q$ can decay to $\Xi_{cc} + \text{hadrons}$

Upgrade and Future searches for $T_{bb/c}$

see talk by Steve Blusk
[[the Tcc mini-workshop](#)]

Cons

- $O(2-20)$ suppression with every $c \rightarrow b$ substitution
compare with $\sigma(\Xi_{cc}) : \sigma(\Xi_{bc}) : \sigma(\Xi_{bb}) \sim 1 : 0.4 : 0.015$ at 14TeV in pp
- $\text{Br}(b \rightarrow c + \pi/\mu/X)$ are 0.1-1%

Zhang, Wu, Zhong, Yu, Fang, 2011

Pros

- x5 gain in integrated luminosity in Run3 (2022-2024)
- gain in trigger and reconstruction efficiencies (x2?) from Upgraded LHCb
- larger trigger efficiency for final states with high- p_T muon
- Comparing to ~ 150 events of $T_{cc} \rightarrow D^0 D^0 \pi^+$ one can expect in Run3
 - long-lived $T_{bc} : T_{bc} \rightarrow D^0 D^+ \pi^- , \bar{B}^0 K^- \pi^+ , D^0 D^+ \mu \nu , \Xi_{cc}^+ \bar{p} , T_{cc}^+ \pi^- \sim O(1-10)$
 - promptly-decaying $T_{bc} : T_{bc} \rightarrow B^- D^+ , \bar{B}^0 D^0 \sim O(10)$
 - $T_{bb} \rightarrow B D + X \sim O(0.01)$
 - ...
- Real chances to find T_{bc}
 - especially if combining several modes
 - can further gain from using partially reconstructed semi-leptonic B/T_{bc} decaysnot much hope for T_{bb} yet

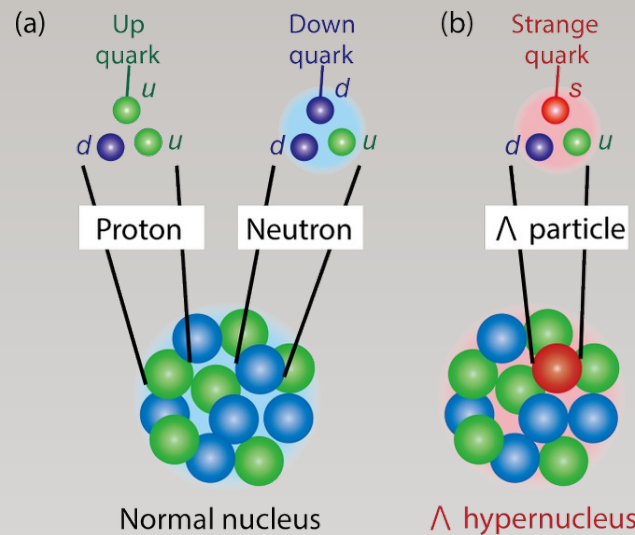
Hadron physics meets Nuclear

- In hadron spectroscopy advances of the theory is limited by the quark configurations to consider
 - conventional hadrons: $q_1 \bar{q}_2$ and $q_1 q_2 q_3$
 - exotic hadrons: $c \bar{c} q_1 \bar{q}_2$ and $c \bar{c} q_1 q_2 q_3 \rightarrow$
 - problems with interpretation in most cases (except for the $T_{cc}^{+!}$)
 - In general presence of heavy quark helps ($m_c \sim 1.5 \text{ GeV}$, $m_b \sim 5 \text{ GeV}$ while $\Lambda_{QCD} \sim 0.3 \text{ GeV}$)

Gal, Hungerford, Millener, 2016

- In nuclear physics systems with only light quarks are usually considered
 - where non-perturbative regime is at its maximum

- Hyper-nuclei with Λ are explored since 50's giving valuable insight into nuclei physics



- Inclusion on b/c-quark will simplify the system and bring such a unique tool to new level

TABLE I Experimental Λ separation energies, B_Λ , of light hypernuclei from emulsion studies. These are taken from a compilation (Davis and Pniewski, 1986) of results from (Cantwell *et al.*, 1974; Jurič *et al.*, 1973), omitting ${}^{15}_\Lambda\text{N}$ (Davis, 1991). A reanalysis for ${}^{12}_\Lambda\text{C}$ (Dłuzewski *et al.*, 1988) gives 10.80(18) MeV.

Hypernucleus	Number of events	$B_\Lambda \pm \Delta B_\Lambda$ (MeV)
${}^3_\Lambda\text{H}$	204	0.13 ± 0.05
${}^4_\Lambda\text{H}$	155	2.04 ± 0.04
${}^4_\Lambda\text{He}$	279	2.39 ± 0.03
${}^5_\Lambda\text{He}$	1784	3.12 ± 0.02
${}^6_\Lambda\text{He}$	31	4.18 ± 0.10
${}^7_\Lambda\text{He}$	16	not averaged
${}^7_\Lambda\text{Li}$	226	5.58 ± 0.03
${}^7_\Lambda\text{Be}$	35	5.16 ± 0.08
${}^8_\Lambda\text{He}$	6	7.16 ± 0.70
${}^8_\Lambda\text{Li}$	787	6.80 ± 0.03
${}^8_\Lambda\text{Be}$	68	6.84 ± 0.05
${}^9_\Lambda\text{Li}$	8	8.50 ± 0.12
${}^9_\Lambda\text{Be}$	222	6.71 ± 0.04
${}^9_\Lambda\text{B}$	4	8.29 ± 0.18
${}^{10}_\Lambda\text{Be}$	3	9.11 ± 0.22
${}^{10}_\Lambda\text{B}$	10	8.89 ± 0.12
${}^{11}_\Lambda\text{B}$	73	10.24 ± 0.05
${}^{12}_\Lambda\text{B}$	87	11.37 ± 0.06
${}^{12}_\Lambda\text{C}$	6	10.76 ± 0.19
${}^{13}_\Lambda\text{C}$	6	11.69 ± 0.12
${}^{14}_\Lambda\text{C}$	3	12.17 ± 0.33

Hyper-nuclei at LHC

- ALICE observed hypertriton in both PbPb, pPb and pp collisions

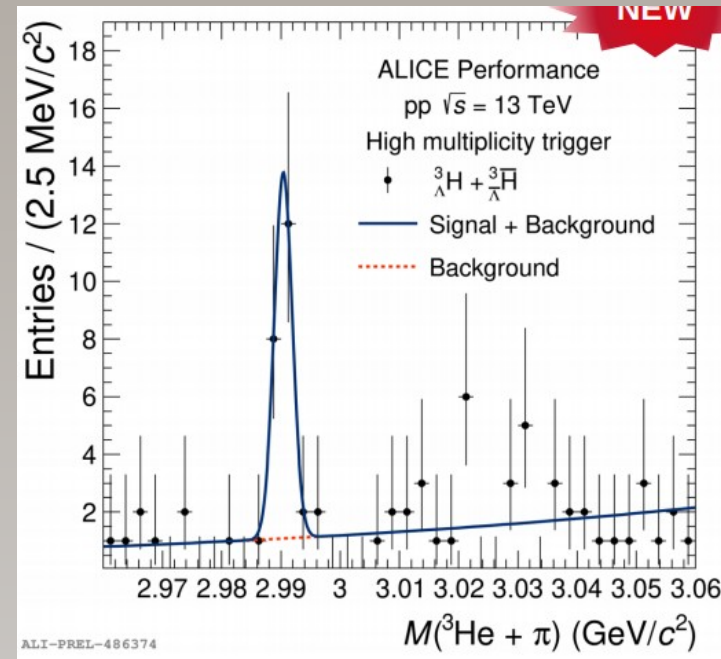
ALICE, 2107.10627

- Searches for $\Lambda\Lambda$ di-baryon (uuddss) are ongoing,
– no success yet

ALICE, 1905.07209

ALICE, 1506.07499

- The [uuddcc] has more chances to exist due to ~ 100 MeV stronger binding between cc quarks *



* M. Karliner

- LHCb has x50-100 larger statistics of pp-collisions than ALICE,
- perfectly suited for reconstructing c-hadron decays ($\tau \sim O(\text{ps})$),
- $c\bar{c}$ produced in $\sim 5\%$ of pp collisions

LHCb, 1205.0975

possible modes for searches:

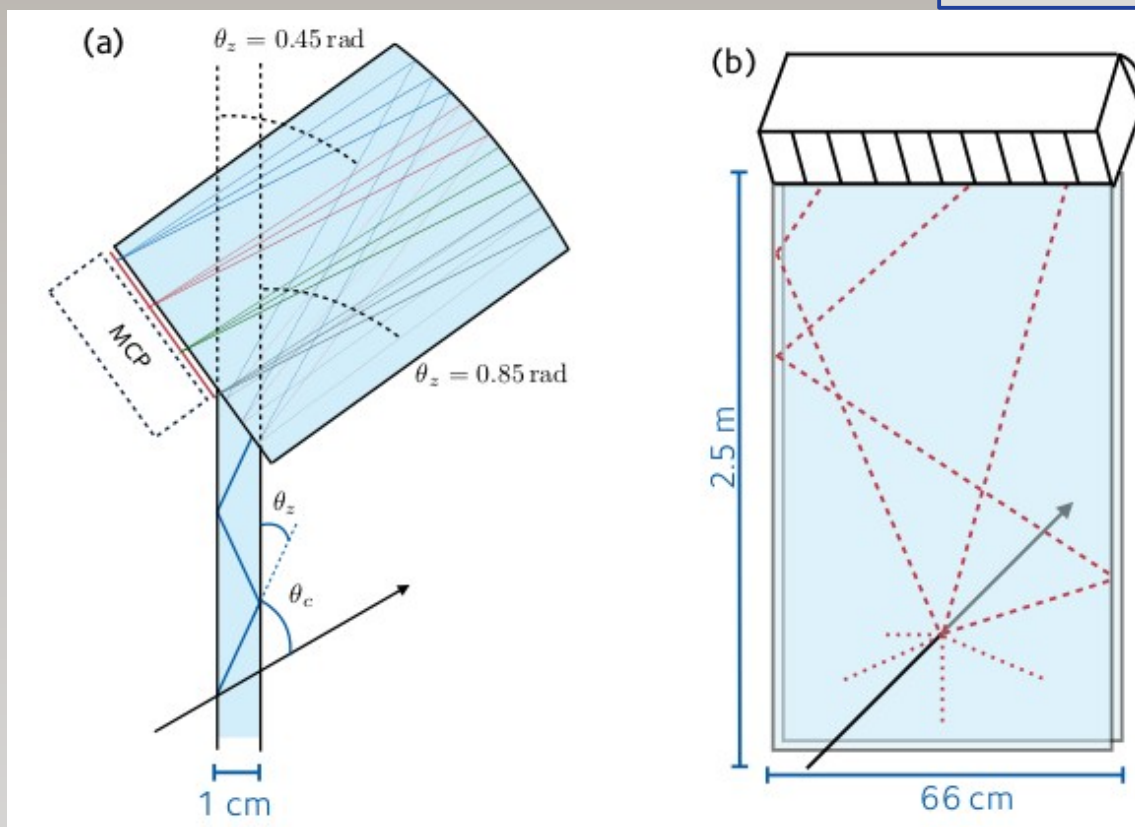
- H_c [cuduud] \rightarrow ppK $^-\pi^+$ / p Λ_c
- H_{cc} [ccuudd] \rightarrow Λ_c pK $^-\pi^+$ / $\Lambda_c\Lambda_c$
- and also H_s , H_b , ...

The TORCH sub-detector

- Time-of-flight detector prepared for LHCb Upgrade II (and in some part in Ib?)
- Aiming to provide $p/K/\pi$ identification in 2-10 GeV/c range where present RICH detectors are not efficient

N. Harnew et al., arXiv:1810.06658

T.H. Hancock et al., NIM A 958 (2020) 162060



- Will also provide identification for **deuteron** and **triton** up to 25-30 GeV/c, thus enriching potential for hyper-nuclei searches

Conclusions

- A novel class of hadrons observed – $[cc\bar{u}d]$, just below D^0D^{*+} threshold, consistent with predicted T_{cc}^+ with $J^P=1^+$
- $D^0D^0\pi^+$, $D^0\pi^+$, D^0D^0 , D^0D^+ spectra described
- Intriguing production properties

[arXiv:2109.01038](https://arxiv.org/abs/2109.01038)

[arXiv:2109.01056](https://arxiv.org/abs/2109.01056)

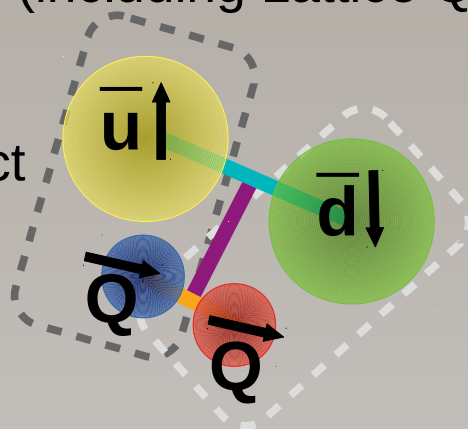


- Run3 (2022-2024) and Upgraded LHCb will bring a lot of possibilities for further studies - T_{cc} , T_{bc} , H_c , H_{cc} , ...

Backup

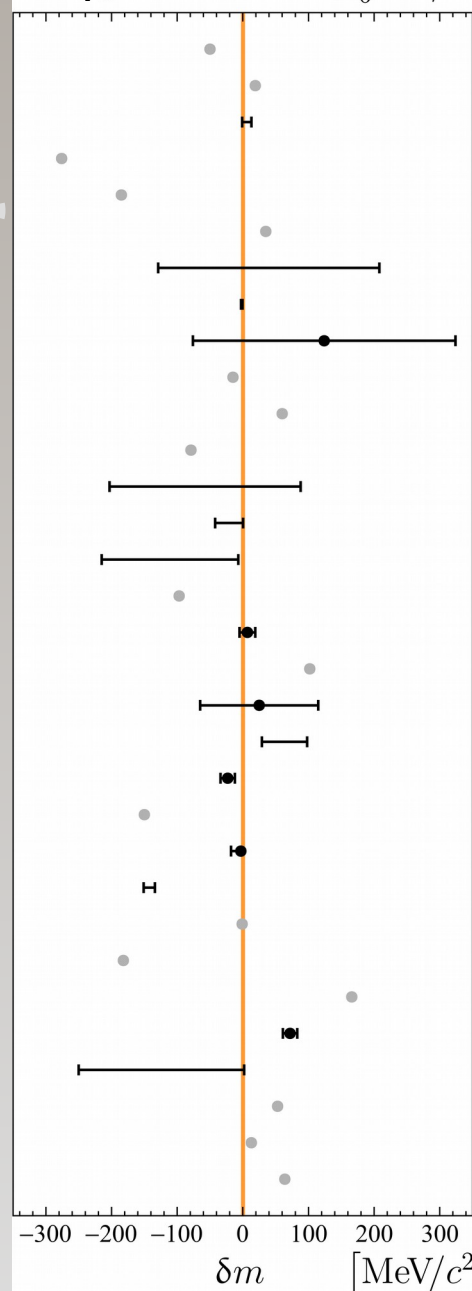
Predictions for $cc\bar{u}d$ mass

- More recent calculations (including Lattice QCD) all agree that it should be true for $[bb][\bar{u}d]$ with QQ forming compact color anti-triplet and resulting binding of $\sim 150\text{MeV}$



- However not clear for $[bc][\bar{u}d]$ and $[cc][\bar{u}d]$
- Predictions for a ground $cc\bar{u}d$ state (isoscalar with $J^P=1^+$) vary within $\pm 250\text{MeV}$ wrt to D^0D^{*+} threshold
- Review few selected in the following *Neither full, nor objective, and oversimplified* → see Ref. List in papers for an overview

$$\delta m \equiv m_{T_{cc}^+} - (m_{D^{*+}} + m_{D^0})$$



J. Carlson <i>et al.</i>	1987
B. Silvestre-Brac and C. Semay	1993
C. Semay and B. Silvestre-Brac	1994
M. A. Moinester	1995
S. Pepin <i>et al.</i>	1996
B. A. Gelman and S. Nussinov	2003
J. Vijande <i>et al.</i>	2003
D. Janc and M. Rosina	2004
F. Navarra <i>et al.</i>	2007
J. Vijande <i>et al.</i>	2007
D. Ebert <i>et al.</i>	2007
S. H. Lee and S. Yasui	2009
Y. Yang <i>et al.</i>	2009
N. Li <i>et al.</i>	2012
G.-Q. Feng <i>et al.</i>	2013
S.-Q. Luo <i>et al.</i>	2017
M. Karliner and J. Rosner	2017
E. J. Eichten and C. Quigg	2017
Z. G. Wang	2017
W. Park <i>et al.</i>	2018
P. Junnarkar <i>et al.</i>	2018
C. Deng <i>et al.</i>	2018
M.-Z. Liu <i>et al.</i>	2019
L. Maiani <i>et al.</i>	2019
G. Yang <i>et al.</i>	2019
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E. Braaten <i>et al.</i>	2020
D. Gao <i>et al.</i>	2020
J.-B. Cheng <i>et al.</i>	2020
S. Noh <i>et al.</i>	2021
R. N. Faustov <i>et al.</i>	2021

[see Refs. in paper]

Selected theory approaches

- Few selected approaches discussed in following
 - Phenomenological approach for compact hadrons
 - Non-relativistic quark constituent model
 - Molecula object
 - Hydrogen bond in QCD
 - Lattice QCD
 - ... others

Neither full, nor objective, and oversimplified → see Ref. List in papers for an overview

Phenomenology approach for compact hadrons

- Extracting effective quark masses and binding or hyperfine interaction terms from measured hadron masses and assuming cc are in anti-triplet color configuration

- 1a. Heavy Quark Symmetry

- $m(ccud) = m(\Xi_{cc}) + 315 \text{ MeV} \sim m(\Xi_{cc}) + [m(\Lambda_c) - m(D^0)] + \text{kinematic correction}$

$\rightarrow \delta m = +102 \text{ MeV} \xrightarrow{\text{using measured } \Xi_{cc} \text{ mass}} \delta m = +65 \text{ MeV} \quad (\sim 3 \text{ MeV})$

Eichten, Quigg, 2017

- 1b. More detailed calculation with estimation of uncertainties

$\rightarrow \delta m = 72 \pm 11 \text{ MeV}$
Braaten, He, Mohapatra, 2020

- 1c. Different treatment of meson/baryon quark masses & splitting parameters

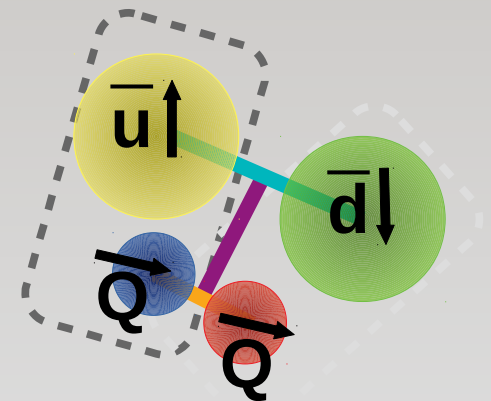
Contribution	Value (MeV)
$2m_c^b$	3421.0
$2m_q^b$	726.0
$a_{cc}/(m_c^b)^2$	14.2
$-3a/(m_q^b)^2$	-150.0
cc binding	-129.0
Total	3882.2 ± 12

$\rightarrow \delta m = 7 \pm 12 \text{ MeV}$

\downarrow using measured Ξ_{cc} mass

$\delta m = 1 \pm 12 \text{ MeV}$

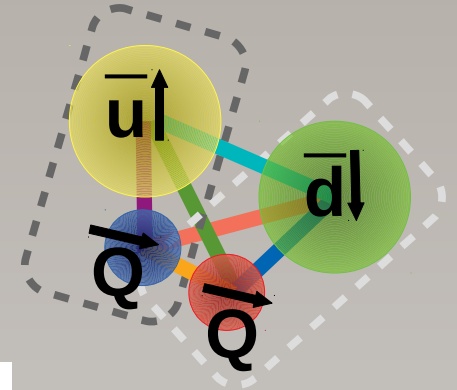
Karlner, Rosner, 2017



Non-relativistic quark constituent model

- Solve Schrodinger equation considering interaction between every pair of quarks

$$H = \sum_i \left(m_i + \frac{\mathbf{p}_i^2}{2m_i} \right) - \frac{3}{16} \sum_{i < j} \tilde{\lambda}_i \tilde{\lambda}_j v_{ij}(r_{ij})$$



- Different variants for exact potential are used (modifications of Cornell potential)

$$V_{ij}^B = -\frac{\lambda_i^C}{2} \cdot \frac{\lambda_j^C}{2} \left(U_0 + \frac{\alpha}{r_{ij}} + \beta r_{ij} + \alpha \frac{\hbar^2}{m_i m_j c^2} \frac{e^{-r_{ij}/r_0}}{r_0^2 r_{ij}} \sigma_i \cdot \sigma_j \right),$$

color of quarks (points to λ_i^C)
one-gluon exchange ("Coulomb") (points to $\frac{\alpha}{r_{ij}}$)
confinement (points to βr_{ij})
contact spin-spin interaction (points to $\sigma_i \cdot \sigma_j$)
 $r_{ij} = |\vec{r}_i - \vec{r}_j|$

- Results

→ $\delta m = [-1; +13] \text{ MeV}$

Semay, Silvestre-Brac, 1994

$\delta m = [-2.7; -0.6] \text{ MeV}$

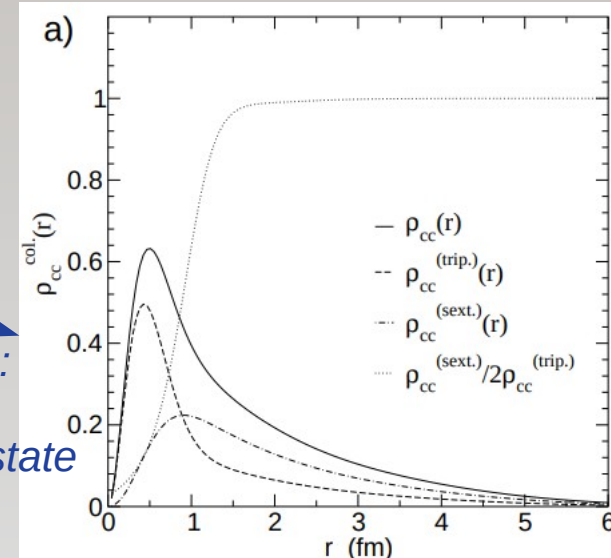
Janc, Rosina, 2003

... + more within

$[-200; +100] \text{ MeV range}$

(choice of basic, parameters, ...)

gives insight into wave-function: spatial & color configuration, fractions of molecule/compact state



Molecula object

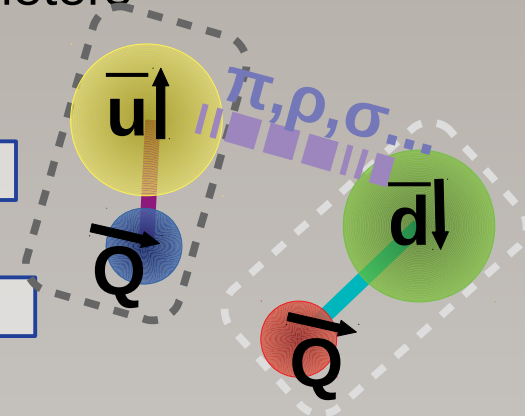
- Consider one-boson-exchange between DD* forming a molecula
 - get (much stonger) binding depending on particular parameters (mainly cut-off value $\Lambda \sim 1\text{GeV}$ (0.2fm))

$$\begin{aligned} \delta m &= [-332;-185] \text{ MeV} \\ &= [-42;0.3] \text{ MeV} \\ &= [-18;+1] \text{ MeV} \end{aligned}$$

Pepin, Stancu, Genovese, Richard, 1996

Li, Sun, Liu, Zhu, 2012

Wu,Liu, Wu, Valderrama, Xie, Geng, 2019



- 2&3. Adding meson-exchange ($\pi, \rho, K, \sigma, \eta, \dots$) terms to the potential in NR model (quark-quark interaction)
 - results vary a lot, indicate 100-200 MeV increase in binding wrt no-OBE,

$$\begin{aligned} \delta m &= -129 \text{ MeV} \\ &= -15 \text{ MeV} \\ &= -203 \text{ MeV} \\ &= [-150;-1] \text{ MeV} \end{aligned}$$

Vijande, Fernandez, Valcarce, Silvestre-Brac, 2003

Vijande, Weissman, Valcarce, Barnea, 2007

Yang, Deng, Ping, Goldman, 2009

Yang, Ping, Segovia, 2019

(though do not agree with other calculations w/o OBE)

Hydrogen bond of QCD

- Consider interaction between two D-mesons by solving Schrodinger equation for light quarks (q) given fixed distance between the heavy ones (Q)
 - get effective interaction between QQ

$$H = \frac{1}{2M} \sum_{\text{heavy}} P_i^2 + \frac{1}{2m} \sum_{\text{light}} p_i^2 + V(\mathbf{x}_A, \mathbf{x}_B) + V_I(\mathbf{x}_A, \mathbf{x}_B, \mathbf{x}_1, \mathbf{x}_2)$$

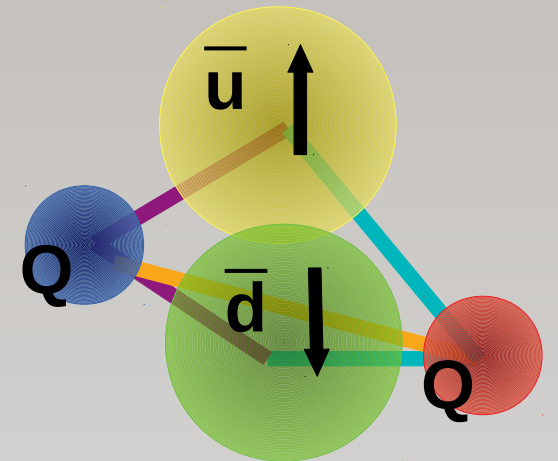
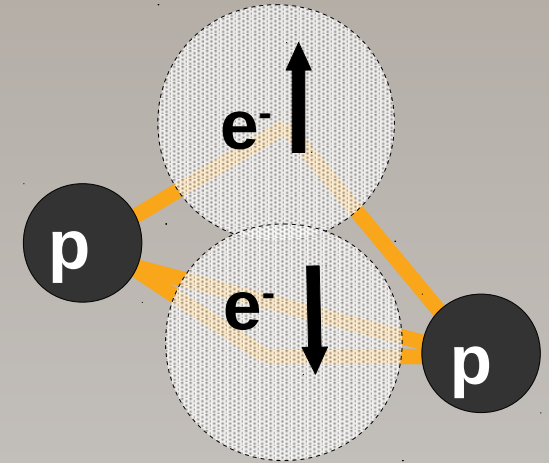
Q-Q interaction

Q-q and q-q interaction

→ get **O(MeV)** binding between D mesons:
and thus $\delta m \sim -135 \text{ MeV}$

Maiani, Polosa, Riquer, 2019

*is it analogous to quark constituent model with OGE?
should it be re-considered for DD* interaction?*



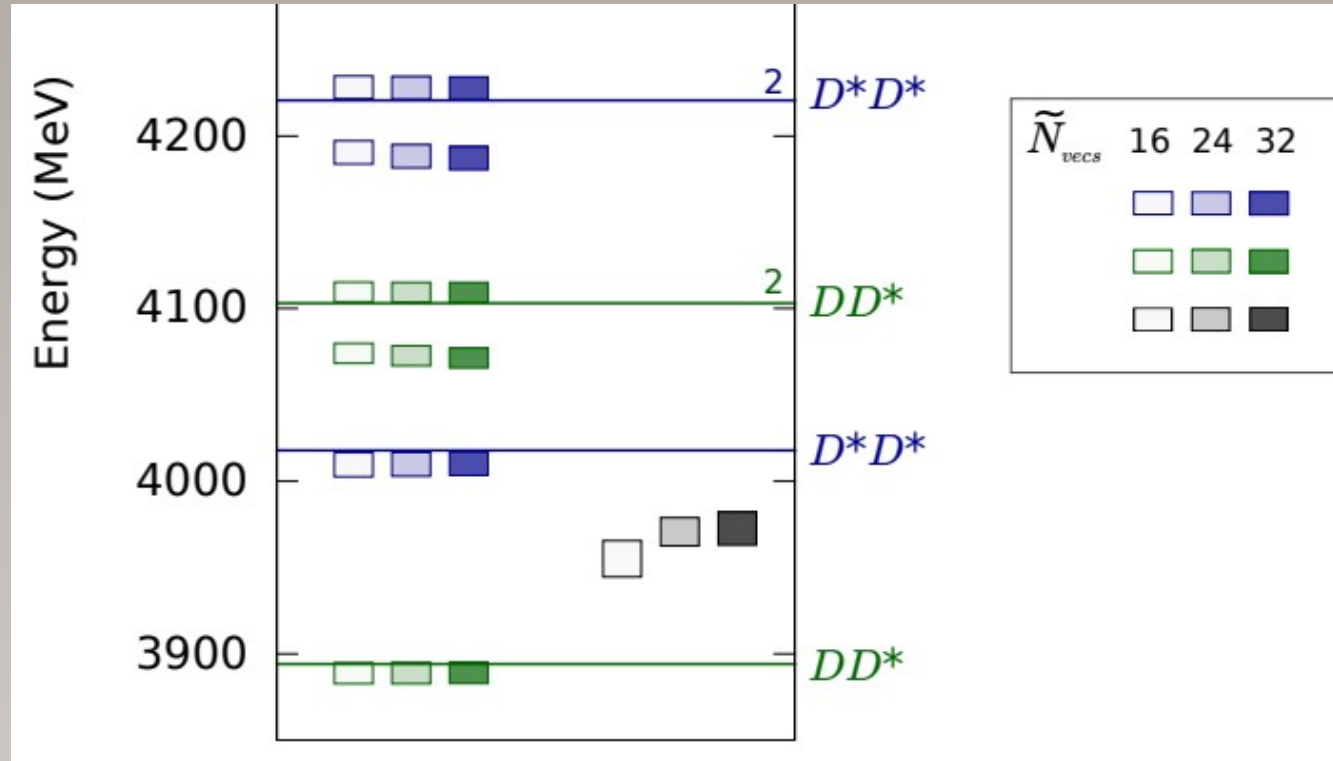
Lattice QCD

- Inconclusive

- no binding

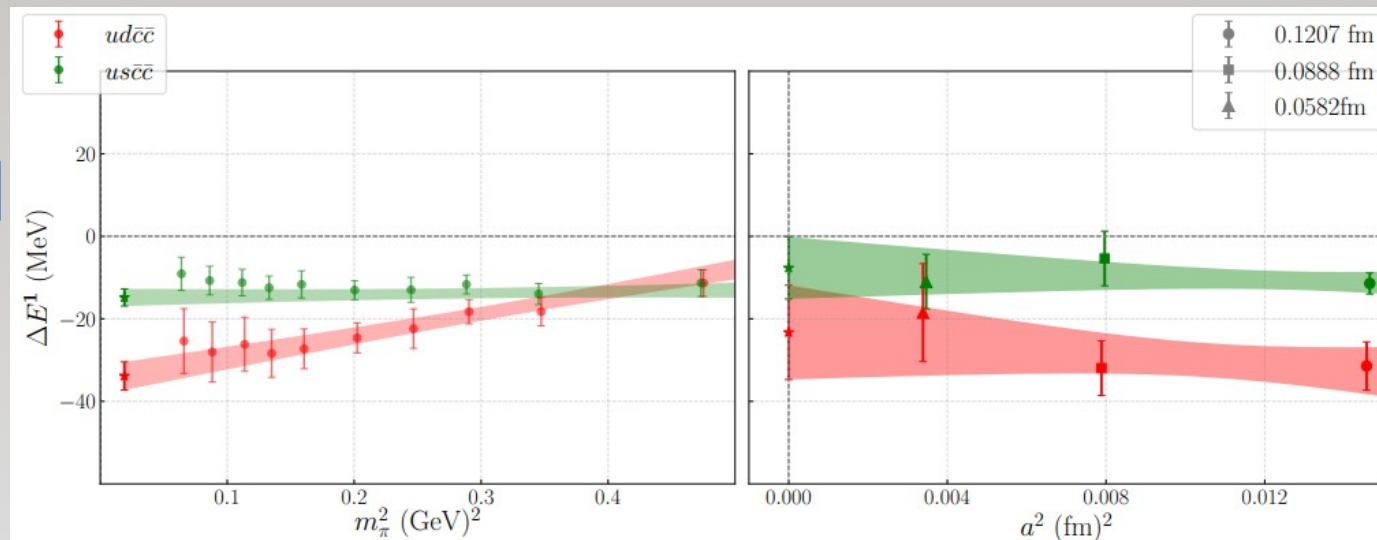
HAL QCD Collaboration, 2014

Hadron Spectrum Collaboration, 2017



- $\delta m \sim -23 \pm 11$ MeV

Junnarkar, Mathur, Padmanath, 2018



Summary of Results

- A narrow peak in $D^0 D^0 \pi^+$ below $D^0 D^{*+}$ threshold is observed with $S > 20\sigma$

- Naive BW parameters:

$$\begin{aligned}\delta m_{\text{BW}} &= -273 \pm 61 \pm 5 \begin{matrix} +11 \\ -14 \end{matrix} \text{ keV}/c^2, \\ \Gamma_{\text{BW}} &= 410 \pm 165 \pm 43 \begin{matrix} +18 \\ -38 \end{matrix} \text{ keV},\end{aligned}$$

- Consistent with $[\overline{ccud}]$ isoscalar tetraquark T_{cc}^+ with $J^P=1^+$ for which

$$\delta' m_0 = -359 \pm 40 \begin{matrix} +9 \\ -6 \end{matrix} \text{ keV}/c^2$$

is determined using dedicated model

- A lower limit is set on $T_{cc}^+ \rightarrow DD^*$ coupling: $|g| > 5.1$ (4.3) GeV at 90 (95) % CL

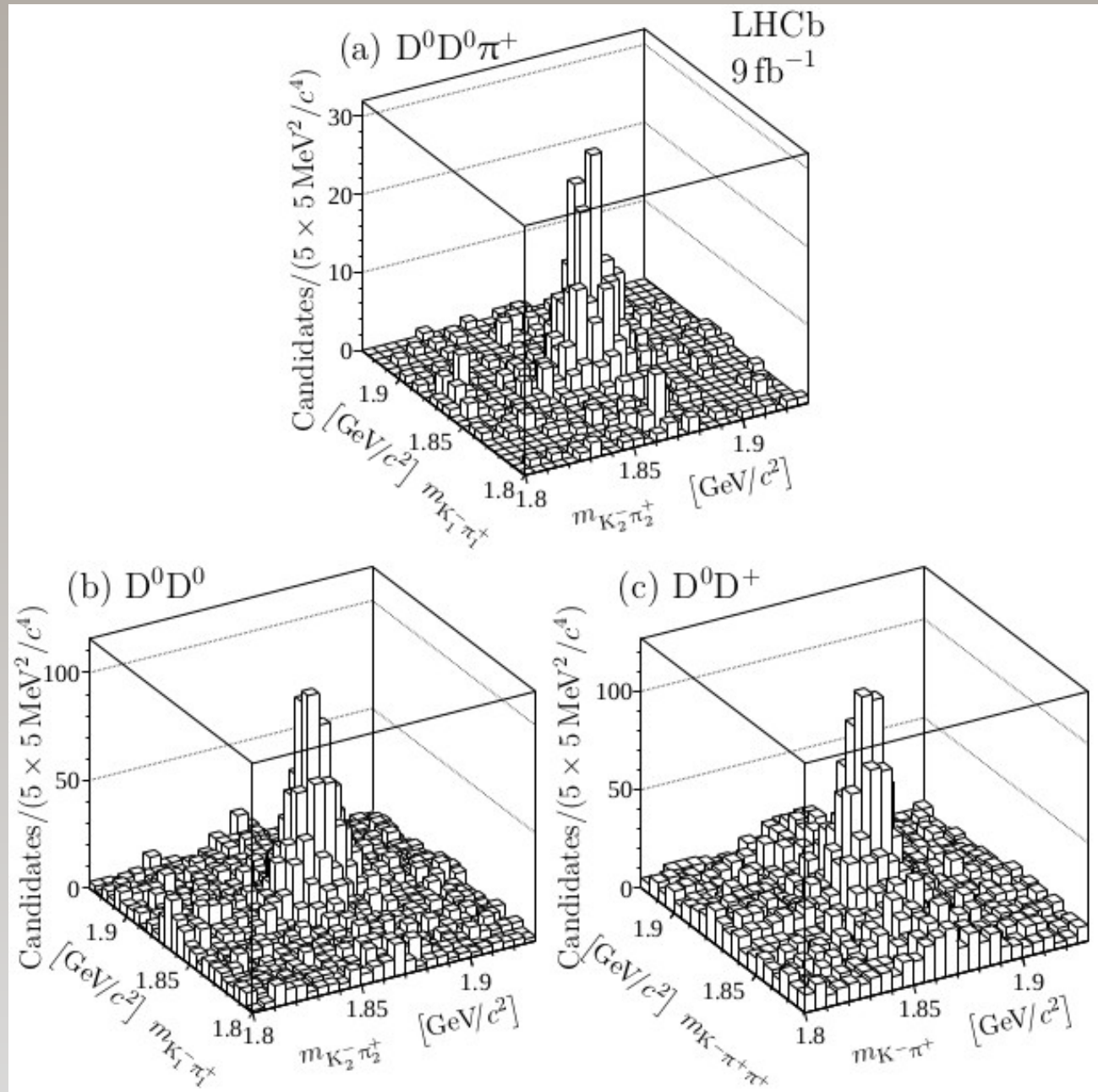
- Threshold structures observed in $D^0 D^0$ and $D^0 D^+$ are found to be consistent with $T_{cc}^+ \rightarrow D^0 D^{0/+} \pi^{+/0} / \gamma$ decays via off-shell D^* mesons

- Matching to low-energy DD^* scattering amplitude we get

- Pole position:

$$\begin{aligned}\delta' m_{\text{pole}} &= -360 \pm 40 \begin{matrix} +4 \\ -0 \end{matrix} \text{ keV}/c^2, \\ \Gamma_{\text{pole}} &= 48 \pm 2 \begin{matrix} +0 \\ -14 \end{matrix} \text{ keV},\end{aligned}$$

2D LEGO Plots



Resolution model

- Sum of two gaussian functions, where widths and relative fractions are determined from simulation:

$$\sigma_1 = 263 \text{ keV} \times 1.05$$

$$\sigma_2 = 2.413 \times \sigma_1$$

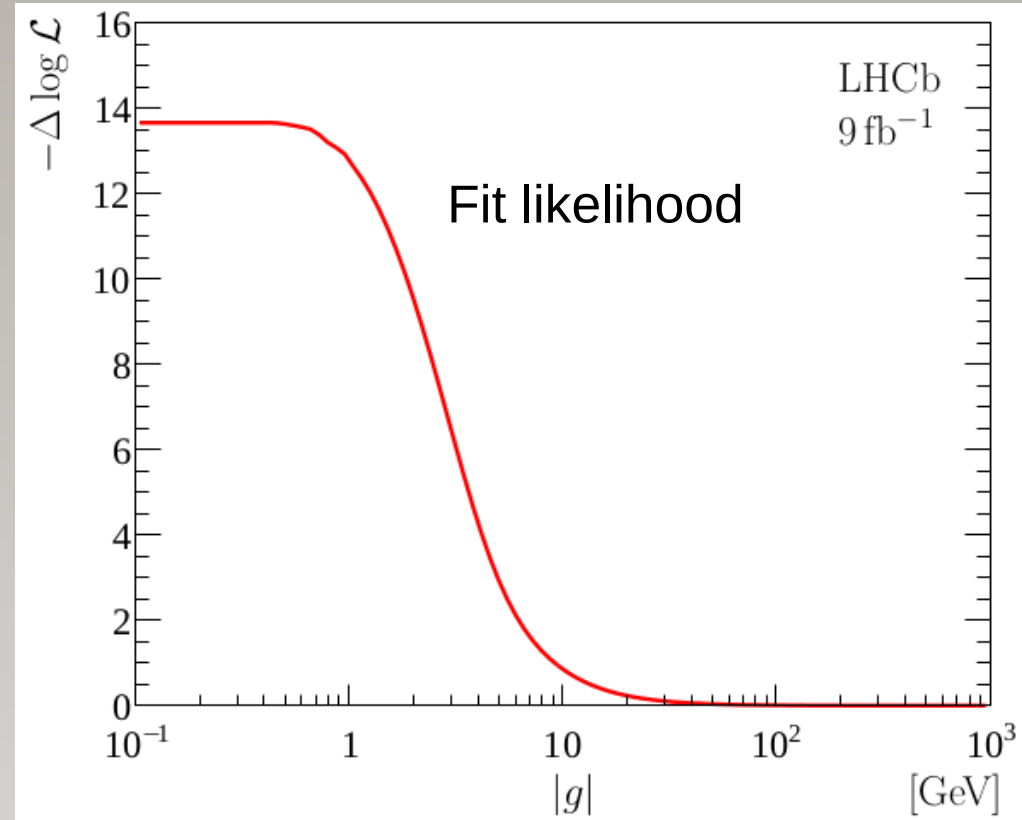
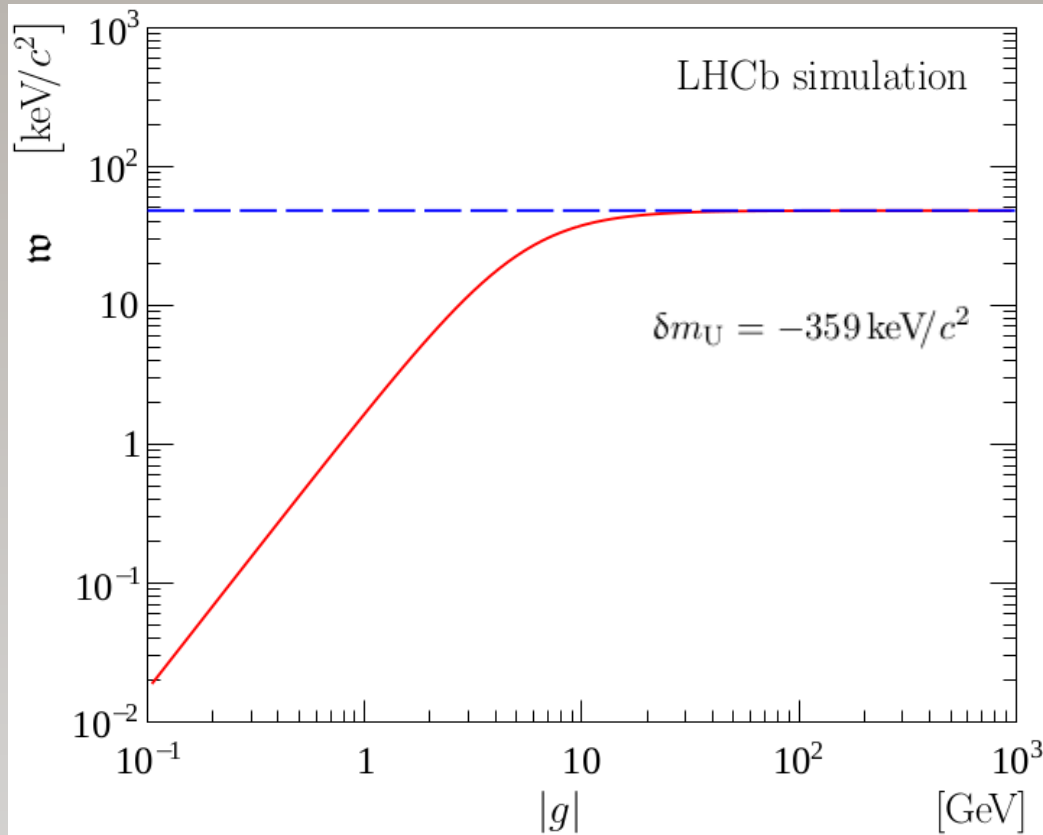
$$f_1 = 0.778$$

a 1.05 correction motivated by data-simulation comparison in various decay channels

- For systematics :
 - correction factor varied within 1.0-1.1
 - many alternative parametrisations tried:
Apolonios, CrystalBall, Student-t, Johnson-U, Novosibirsk

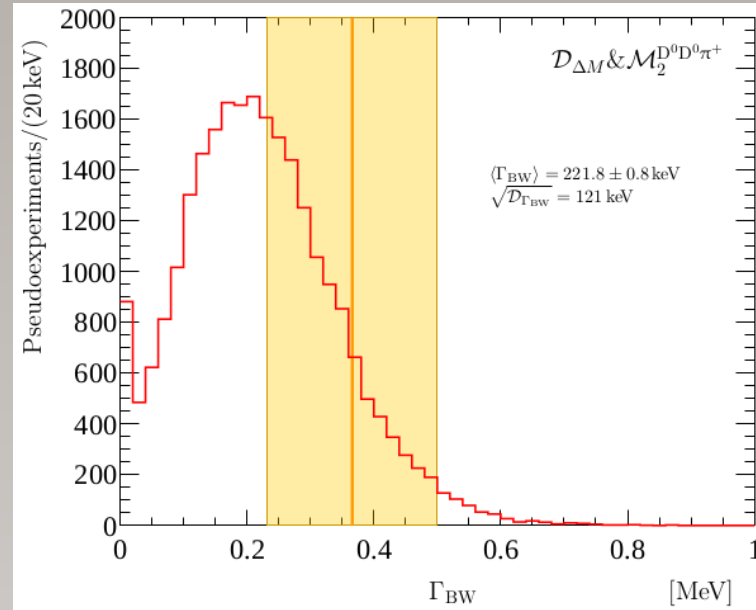
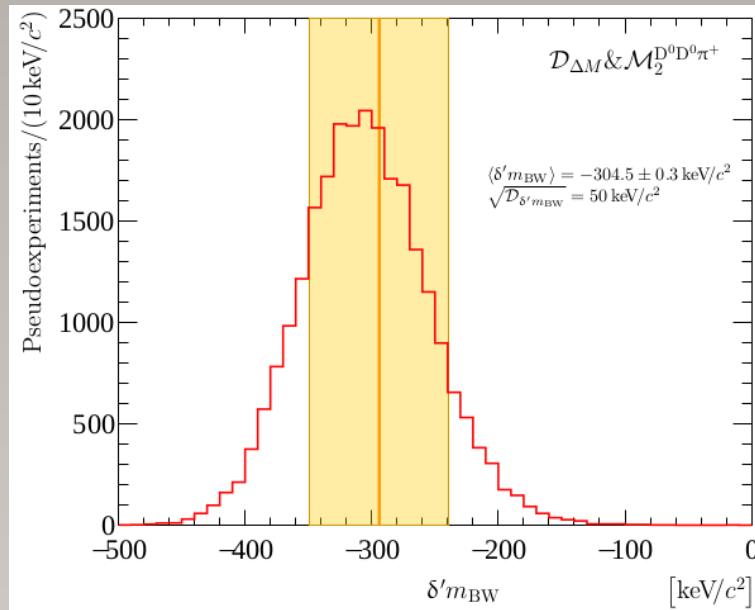
Scaling in unitarized model

- For large values of $|g|$ a scaling of overall shape is in place and visible width depends only on mass and $\Gamma(D^{*+})$



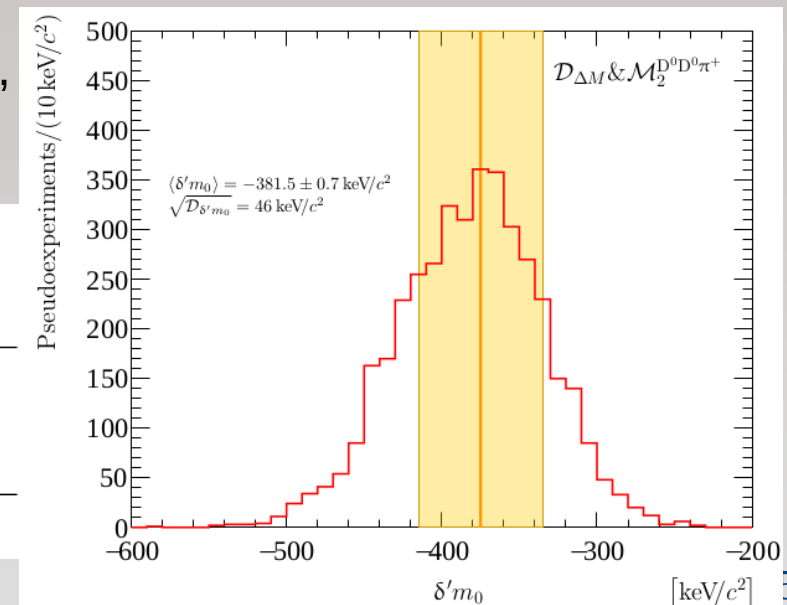
Consistency of Naive and Advanced

- Generate 25k pseudoexperiments using **advanced** BW model, fit them with **naive** BW model.
Get $\delta'm_{\text{BW}}$ and Γ_{BW} consistent with values obtained from data



- Generate 4k pseudoexperiments using **naive** BW model, fit them with **advanced** BW model.
Get $\delta'm_0$ consistent with values obtained from data

Parameter	Pseudoexperiments		Data
	mean	RMS	
δm_{BW} [keV/c ²]	-301	50	-273 ± 61
Γ_{BW} [keV]	222	121	410 ± 165
δm_{U} [keV/c ²]	-378	46	-359 ± 40



84

Low-energy scattering approximation

- Relation between unitarized amplitude and low-energy expansion

$$\mathcal{A}_{\text{NR}}^{-1} = \frac{1}{a} + r \frac{k^2}{2} - ik + \mathcal{O}(k^4),$$

$$\frac{2}{|g|^2} \mathcal{A}_{\text{U}}^{-1} = -[\xi(s) - \xi(m_{\text{U}}^2)] + 2 \frac{m_{\text{U}}^2 - s}{|g|^2} - i\rho_{\text{tot}}(s)$$

- Proportionality factor

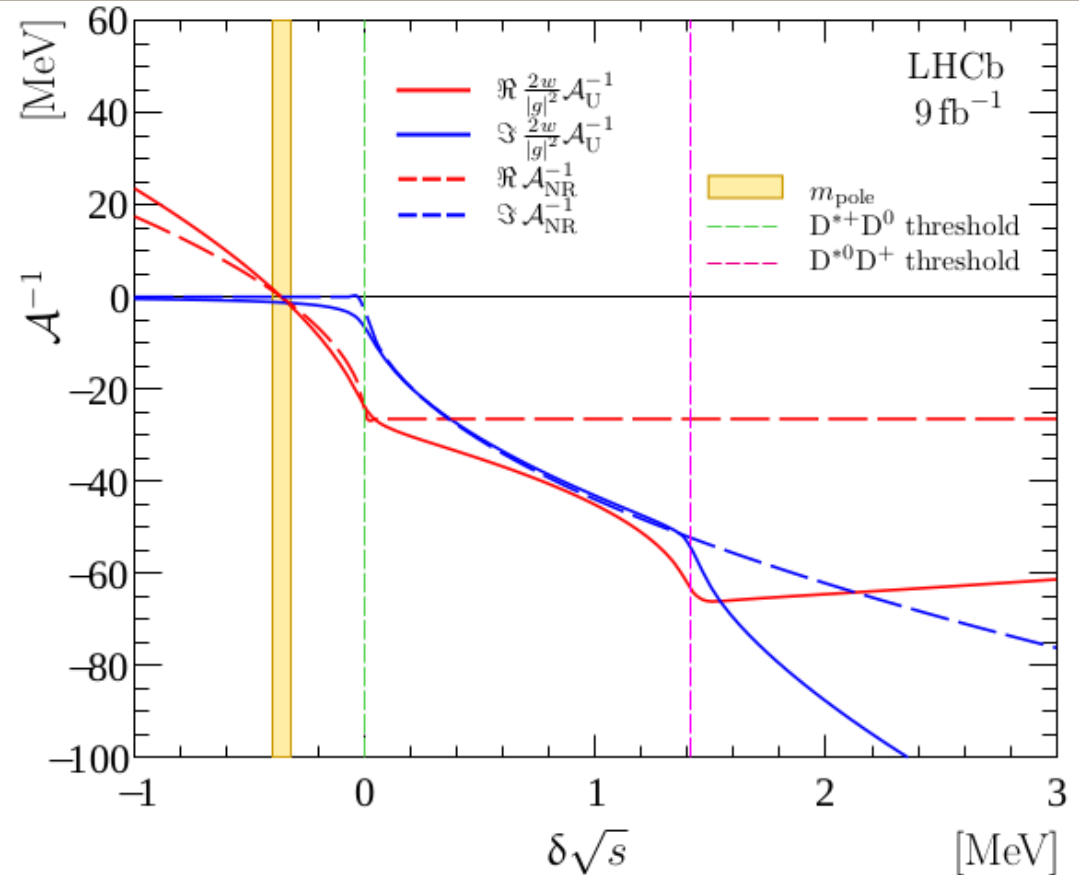
$$w = \frac{24\pi}{m_{\text{D}^{*+}} + m_{\text{D}^0}} \frac{1}{c_1}$$

- Inverse scattering length

$$\frac{1}{a} = -\frac{1}{w} \left\{ [\xi(s_{\text{th}}) - \xi(m_{\text{U}}^2)] + i\rho_{\text{tot}}(s_{\text{th}}) \right\}$$

- Slope of linear term

$$r = -\frac{1}{w} \frac{16}{|g|^2}$$



Extended Data Fig. 9: Comparison of the \mathcal{A}_{U} and \mathcal{A}_{NR} amplitudes. The real and imaginary parts of the inverse \mathcal{A}_{U} and \mathcal{A}_{NR} amplitudes. The yellow band correspond to the pole position and vertical dashed lines show the D^{*+}D^0 and D^{*0}D^+ mass thresholds.

Analytic continuation

- To study poles analytic continuation of amplitude and hence complex width and phase-space functions onto complex plane is required

$$\Sigma(s) = \frac{s}{2\pi} \int_{s_{\text{th}}^*}^{+\infty} \frac{\varrho_{\text{tot}}(s')}{s'(s'-s)} ds' - \xi(m_U^2),$$

$$\frac{1}{\mathcal{A}_U^{\text{II}}(s)} = m_U^2 - s - |g|^2 \Sigma(s) + i |g|^2 \varrho_{\text{tot}}(s)$$

- For ρ functions

$$\int_{\mathcal{D}} |\mathfrak{M}|^2 d\Phi_3 = \frac{1}{2\pi(8\pi)^2 s} \int_{(m_2+m_3)^2}^{(\sqrt{s}-m_1)^2} ds_{23} \int_{s_{12}^-(s,s_{23})}^{s_{12}^+(s,s_{23})} |\mathfrak{M}|^2 ds_{12}$$

$$s_{12}^{\pm}(s, s_{23}) = m_1^2 + m_2^2 - \frac{(s_{23} - s + m_1^2)(s_{23} + m^2 + m_3^2)}{2s_{23}} \pm \frac{\lambda^{1/2}(s_{23}, s, m_1^2) \lambda^{1/2}(s_{23}, m_2^2, m_3^2)}{2s_{23}}$$

ccsq tetraquarks

Considering that mass of $[cc]$ system should fall in between of c-quark and b-quark masses we may expect that mass of tetraquark states with s-quark scales similarly to that in D- and B-hadrons. And therefore one can make some very naive estimation for masses of $[cc\bar{s}q]$ and $[cc\bar{s}\bar{s}]$ with respect to threshold. We may suppose that substitution of one light quark in $[cc\bar{u}\bar{d}]$ to \bar{s} will increase its mass by either

$$m_{\Xi_c^{+(0)}} - m_{\Lambda_c^+} = 181(184) \text{ MeV}/c^2 \quad \text{or} \quad (\text{U.1})$$

$$m_{\Xi_b^{0(-)}} - m_{\Lambda_b^0} = 172(177) \text{ MeV}/c^2 \quad (\text{U.2})$$

while the corresponding threshold will be increased by either

$$m_{D_s^+} - m_{D^+(D^0)} = 99(104) \text{ MeV}/c^2 \quad \text{or} \quad (\text{U.3})$$

$$m_{B_s^0} - m_{B^0(B^+)} = 87(88) \text{ MeV}/c^2 . \quad (\text{U.4})$$

Thus, the mass of $[cc\bar{s}q]$ state will be 80 – 89 MeV/c^2 above $D_s^+D^*$ threshold and therefore existence of a narrow state is unlikely.

Similarly we may suppose that substitution of $[\bar{u}\bar{d}]$ to $[\bar{s}\bar{s}]$ will increase its mass by either

$$m_{\Omega_c} - m_{\Lambda_c^+} = 409 \text{ MeV}/c^2 \quad \text{or} \quad (\text{U.5})$$

$$m_{\Omega_c} - m_{\Lambda_c^+} = 427 \text{ MeV}/c^2 \quad (\text{U.6})$$

while the corresponding threshold will be increased by either

$$2 \times m_{D_s^+} - m_{D^+} - m_{D^0} = 202 \text{ MeV}/c^2 \quad \text{or} \quad (\text{U.7})$$

$$2 \times m_{B_s^0} - m_{B^0} - m_{B^+} = 175 \text{ MeV}/c^2 . \quad (\text{U.8})$$

Production vs track multiplicity

- Can expect that T_{cc}^+ has some properties similar to $\chi_{c1}(3872)$
- For $\chi_{c1}(3872)$ production a suppression wrt $\psi(2S)$ was observed at high track multiplicities
- Explained in comover model where $\chi_{c1}(3872)$ is broken by closely flying pions/gluons

- Therefore probing effective $Q\pi$ break-up cross-section:

$$\langle v\sigma_{\psi'} \rangle = 3.9 \pm 0.8 \text{ mb}$$

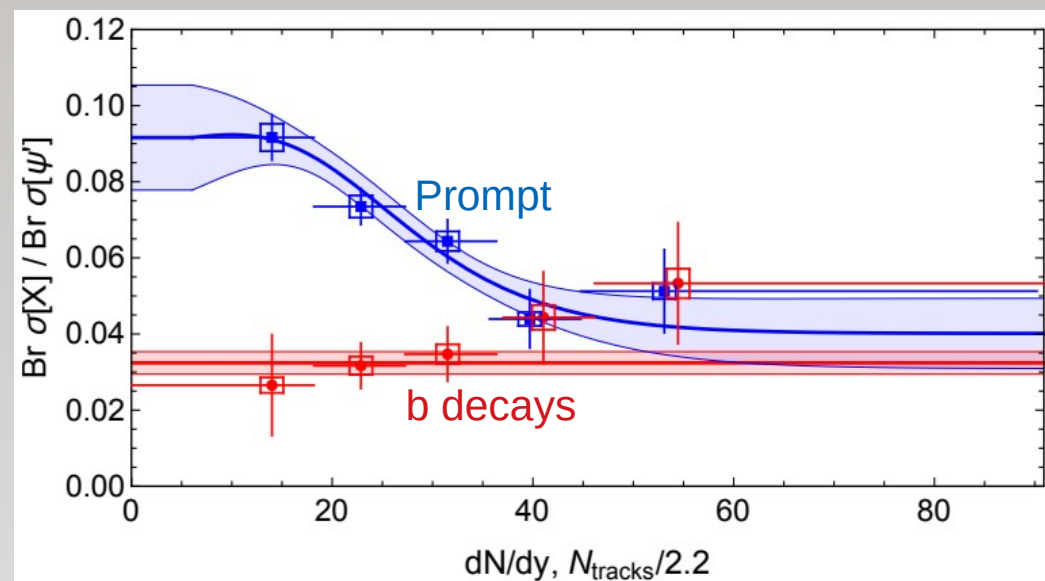
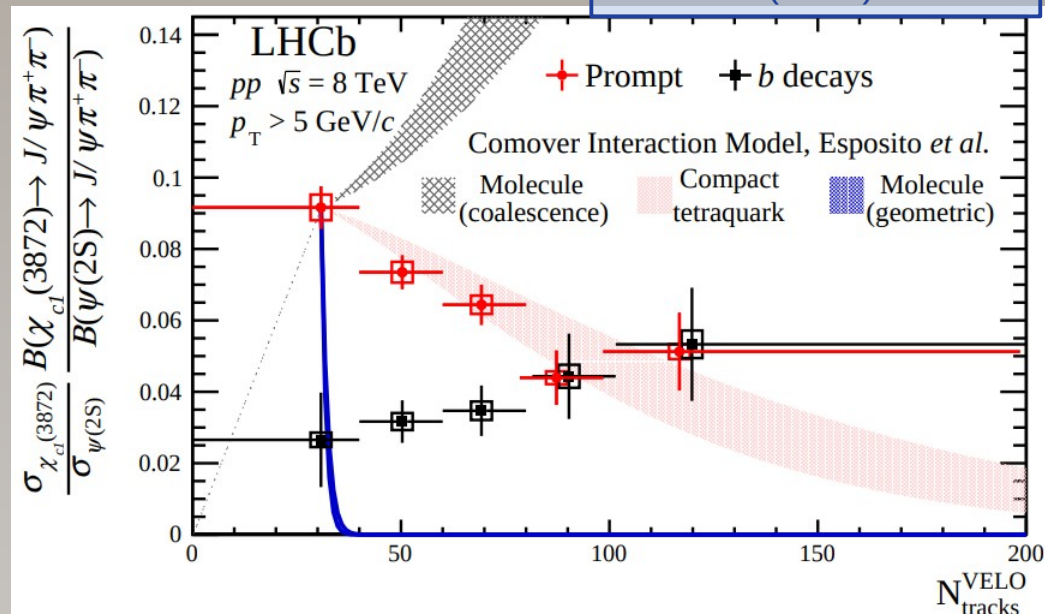
$$\langle v\sigma_X \rangle = 2.6 \pm 0.7 \text{ mb}$$

and fractions of Q out of reach of comovers

$$f_{\text{out},\psi'} = 0.40 \pm 0.03 \text{ and } f_{\text{out},X} = 0.18 \pm 0.04$$

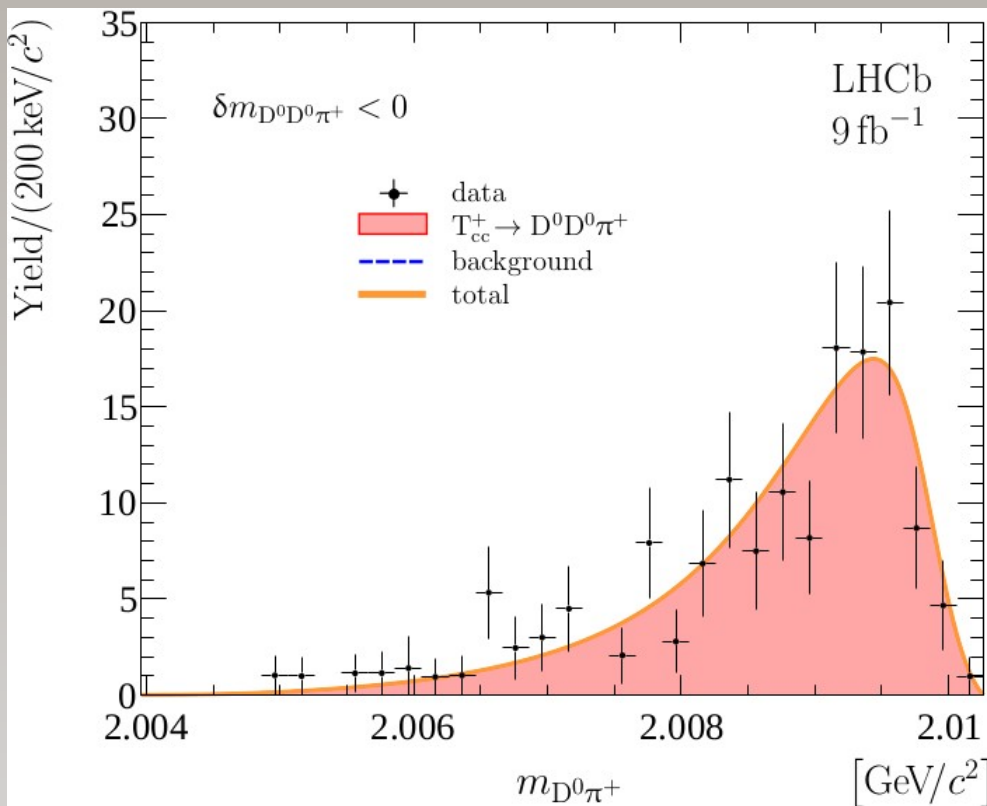
more details in [Braaten et al., arXiv:2021.13499](#)

PRL 126 (2021) 092001



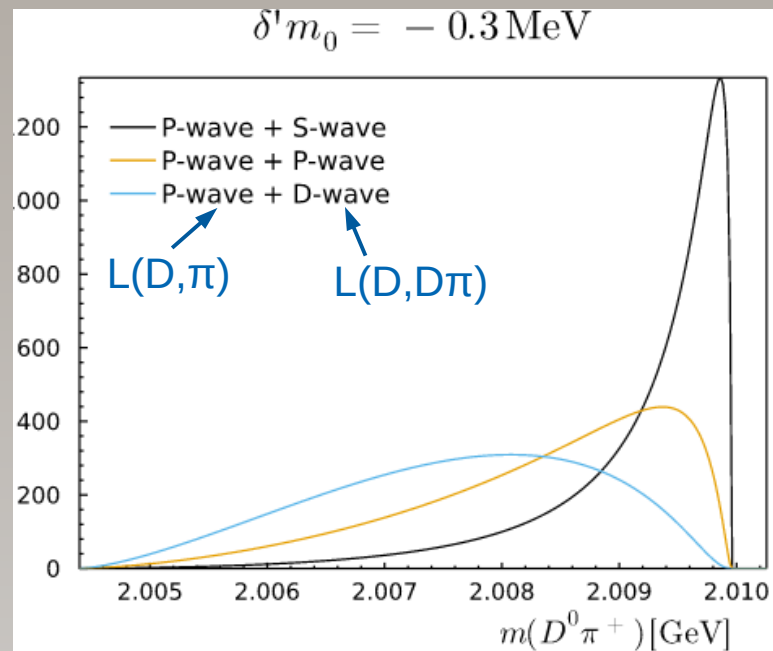
Offshell D^{*+}

- Integrate unitarized model over $D^0 D^0 \pi^+$ and $D^0 D^0$ masses
 \rightarrow obtain $D^0 \pi^+$ shape



Perfect agreement confirms

- $T_{cc} \rightarrow DD^*$ decaying via off-shell D^*
- and the $J^P=1^+$ assignment for T_{cc}



with no D^* propagator

