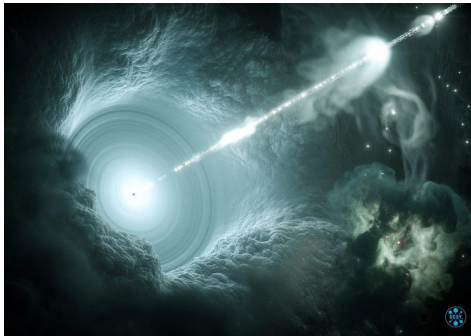


Effects of non-continuous losses during inverse Compton cooling in blazars

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- 1 Introduction
- 2 Modeling
 - Kinetic approach and EMBLEM code
 - Process under study: inverse Compton cooling
 - Modeling approach
- 3 Results
- 4 Summary and outlook

1 Introduction

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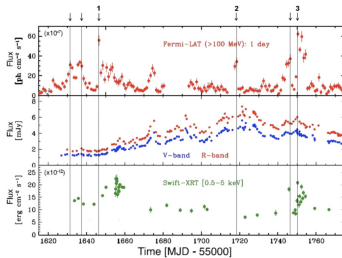
3 Results

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Blazars: phenomenon and properties

Blazars – radio-loud AGN with a jet aligned with the line of sight

- non-thermal emission from radio to γ -rays
- two-bump SED
- highly variable!
 - **flares:** flux \nearrow by factor ~ 10 over time-scale *minutes – weeks*
 - **high states:** time-scale *weeks – years*



3C 279

Blazars: emission origin

Origin of low-energy bump: e^- synchrotron in extended jet + host galaxy (optical)

Origin of γ -ray emission

Leptonic

Hadronic

Inverse Compton

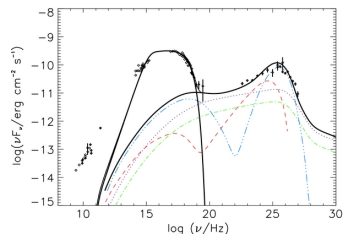
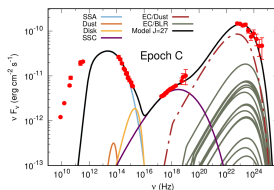
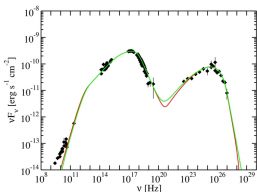
Synchrotron Self-Compton

BL Lac

External Compton

FSRQ

- proton synchrotron
- p - γ interactions
- p - p interactions



Why study blazars?

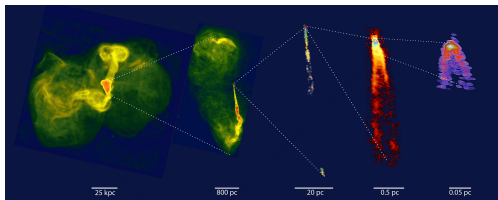
Probing AGN jets physics

- matter content (e^-e^+ or e^-p)
- origin of γ -ray emission (*leptonic?* *hadronic?*)
- VHE γ -ray production site
- nature of flares and high states

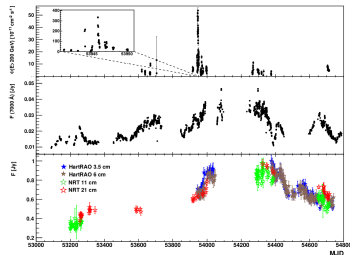
■ Blazar flares carry information about violent physical processes in jets

- details of particle **acceleration** and **cooling** mechanisms

■ Study method: physical modeling of varying MWL emission



FR I radio galaxy M87



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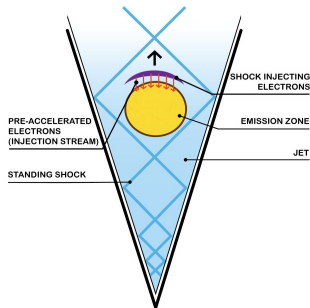
Flare modeling: time-dependent kinetic approach

Fundamental assumptions:

- VHE γ -ray production site: **blob-in-jet**
(e.g. Katarzynski et al., 2001)
- Purely **leptonic** blob (e^-e^+)
- High-energy plasma particles

Physical processes:

- particle injection
- stochastic (*Fermi-II*) or/and shock (*Fermi-I*) acceleration
- escape
- synchrotron and **IC cooling**
(continuous case: $\Delta E_e/E_e \ll 1$)



$$\frac{\partial N_e}{\partial t} = \underbrace{\frac{\partial}{\partial \gamma} \left([b_{\text{cool}} \gamma^2 - a\gamma - 2D_0\gamma] N_e \right)}_{\text{cooling}} + \underbrace{\frac{\partial}{\partial \gamma} \left(D_0 \gamma^2 \frac{\partial N_e}{\partial \gamma} \right)}_{\text{Fermi-II (diffusion in momentum space)}} - \underbrace{\frac{N_e}{t_{\text{esc}}}}_{\text{escape}} + \underbrace{Q_{\text{inj}}}_{\text{injection}}$$

cooling Fermi-I Fermi-II (system. en. gain) Fermi-II (diffusion in momentum space) escape injection

Time-dependent kinetic approach: emission

Radiative processes:

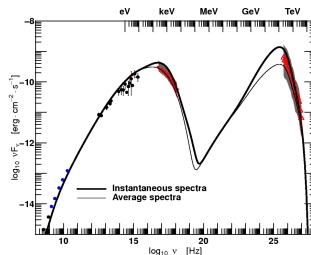
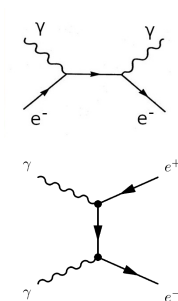
- **Synchrotron emission**
+ self-absorption
- **Synchrotron Self-Compton (SSC) / external Compton (EC)**
+ absorption on EBL

Transformation to observer's frame:

$$\nu = \frac{\delta_b}{1+z} \nu'$$

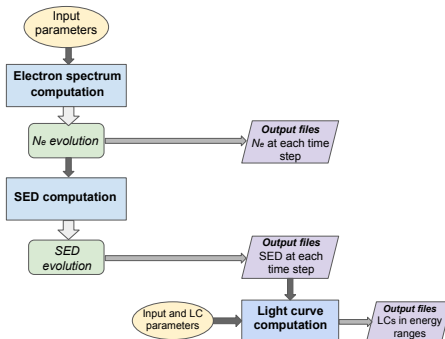
$$I_\nu(\nu) = \delta_b^3 I_{\nu'}(\nu')$$

- Associated SED is computed for electron spectrum at each time step
- Light curves $\Rightarrow \int$ of SEDs



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EMBLEM – Evolutionary Modeling of BLoB EMission

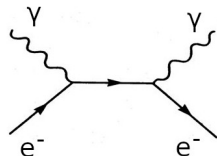


- Time-dependent leptonic code (SSC/EC) for flare modeling (Dmytriiev et al., 2021)
- Self-consistent connection of the blazar low state with the high one
- Flares arise as a perturbation of low state
- Kinetic equation is solved with Chang & Cooper 1970 numerical scheme
- Initial code: BL Lac objects. Extended to FSRQs recently!

>> Cooling is important process damping a flare

IC cooling is significant in blazars with high U_{rad} (FSRQ)

→ leads to *softer spectra* and *lower ν of SED peaks*



– **Thomson regime:** $\Delta E_e/E_e \ll 1$, $E_{\text{IC}} = \gamma^2 \epsilon_s \rightarrow \boxed{\gamma \frac{\epsilon_s}{m_e c^2} \ll 1}$

$$\sigma \sim \sigma_T$$

continuous losses

– **Klein-Nishina (KN) regime:** $\Delta E_e/E_e \sim 1$, $E_{\text{IC}} \sim E_e \sim \gamma m_e c^2 \rightarrow \boxed{\gamma \frac{\epsilon_s}{m_e c^2} \sim 1}$

$$\sigma \approx \frac{3}{8} \sigma_T \frac{\ln(4\chi)}{\chi}, \quad \chi = \gamma \frac{\epsilon_s}{m_e c^2} \Rightarrow \text{cross-section quickly drops with energy}$$

jumps in energy: **NON-continuous losses!**

Inverse Compton cooling: continuous approximation

! The *Fokker-Plank* (kinetic) equation is derived assuming $\Delta E_e/E_e \ll 1$!

▶ KN effects are common in blazars!

■ Most authors use **continuous** description of IC cooling in **KN regime** in the kinetic equation:

$$\dot{\gamma}_{\text{cool,IC}} = -b_{\text{cool,IC}}(N_e, U_{\text{rad}}) \gamma^2$$

while KN effects have a **non-continuous** nature and *cannot* be handled by that term

■ A continuous approximation by [Moderski et al. \(2005\)](#) is designed to reasonably treat KN effects:

$$\dot{\gamma}_{\text{cool,IC}} = -\frac{4\sigma_T}{3m_e c} \gamma^2 \int_{\epsilon'_{\min}}^{\epsilon'_{\max}} f_{\text{KN}}(4\gamma\epsilon') u'_{\text{rad}}(\epsilon') d\epsilon'$$

$$f_{\text{KN}}(x) = \begin{cases} (1+x)^{-1.5}, & \text{for } x < 10^4 \\ \frac{9}{2x^2} (\ln(x) - \frac{11}{6}) & \text{for } x \geq 10^4 \end{cases}$$

Inverse Compton cooling: NON-continuous case

The proper *transport equation* to treat large jumps of e^- in energy (Zdziarski 1988):

$$\frac{\partial N_e(\gamma, t)}{\partial t} = -N_e(\gamma, t) \int_1^\gamma C(\gamma, \gamma') d\gamma' + \int_\gamma^\infty N(\gamma', t) C(\gamma', \gamma) d\gamma' - \frac{N_e(\gamma, t)}{t_{\text{esc}}} + Q_{\text{inj}}(\gamma, t)$$

downscattering from γ to lower LF downscattering from higher LF to γ

with $C(\gamma, \gamma') = \int_{E_*/\gamma}^\infty dx n_0(x) \frac{3\sigma_T c}{4E\gamma} \left[r + (2-r) \frac{E_*}{E} - 2 \left(\frac{E_*}{E} \right)^2 - \frac{2E_*}{E} \ln \frac{E}{E_*} \right] \rightarrow$ Compton kernel by Jones (1968)

$$x = \frac{\epsilon_s}{m_e c^2}, \quad E = \gamma x, \quad E_* = \frac{1}{4}(\gamma/\gamma' - 1), \quad E > E_*, \quad r = \frac{1}{2}(\gamma/\gamma' + \gamma'/\gamma)$$

■ A transient Fermi-I/II (re-)acceleration term can be added

>> The full kinetic equation becomes **integro-differential** equation !

? How does non-continuous cooling change blazar N_e and SED ?

Goals:

- Test the limits of the continuous-loss approach:
When does the non-continuous cooling becomes important for typical physical conditions in blazars?
- Explore the effect of **non-continuous** cooling in the context of blazar variability and its impact on the *electron spectrum* and *SED*

Methods:

- We extend the EMBLEM code by including non-continuous cooling terms
- We numerically solve the *integro-differential equation* by iteration technique

Application:

- **FSRQ**: strong IC cooling → **we choose 3C 279**
- Model 3C 279 flares in a simple way *with and without* inclusion of the effect

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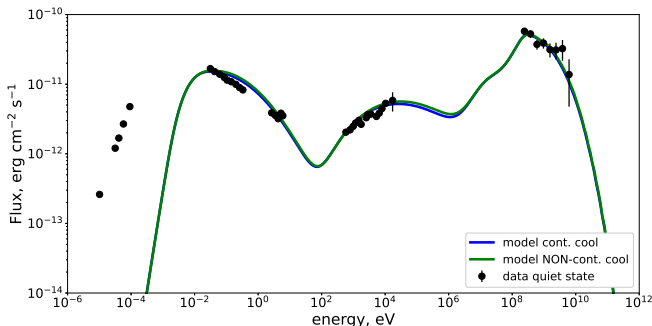
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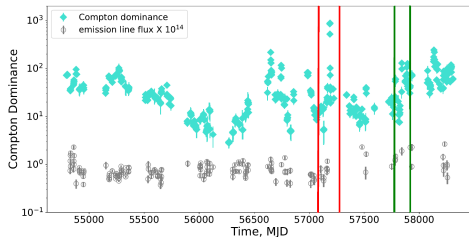
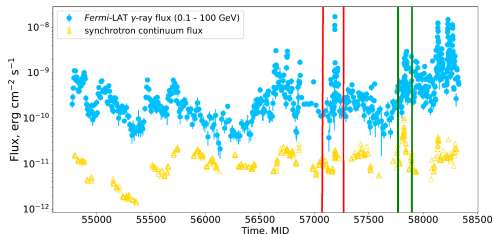
First we model the low state of 3C 279 (data: [Hayashida et al. \(2012\)](#))

- One-zone leptonic EC
- Steady state arises as a result of competition between injection, escape and cooling
- **Cooling:** synchrotron and IC
- **Injection spectrum: log-parabola** (e.g. Dermer et al. (2014))
- **External photon fields: BLR** (single Ly α emission line) and **dusty torus** (e.g. Hayashida et al. (2012))



$$B = 1 \text{ G}, \delta = 30, R_b = 5 \times 10^{15} \text{ cm}, L_{\text{disk}} = 0.6 \times 10^{46} \text{ erg/s}, f_{\text{BLR,DT}} = 0.1, t_{\text{esc}} = 1 R_b/c$$

Two extreme flares of FSRQ 3C 279



Dmytriiev et al. (2023) (in prep.)

Flare 1: June 2015

- *Fermi*-LAT γ -ray flux
 $\sim 10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1}$
(historical maximum!)
- Optical synchrotron flux
(at $\lambda \approx 6000 \text{ \AA}$)
 $\sim (1 - 2) \times 10^{-11} \text{ erg cm}^{-2} \text{ s}^{-1}$
- Compton dominance (CD)
 $\sim 500 - 800$ (!)

Flare 2: April 2017

- *Fermi*-LAT γ -ray flux
 $\sim 3 \times 10^{-9} \text{ erg cm}^{-2} \text{ s}^{-1}$
- Optical synchrotron flux
(at $\lambda \approx 6000 \text{ \AA}$)
 $\sim 10^{-10} \text{ erg cm}^{-2} \text{ s}^{-1}$
(historical maximum!)
- Compton dominance (CD)
 ~ 30

Modeling the two extreme flares of 3C 279

Flare 1 (brightest γ -ray)

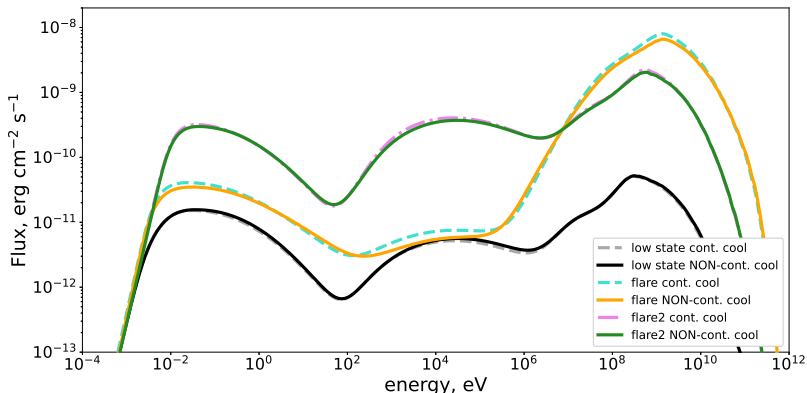
- Simple one-zone model
- Increase of **Doppler factor** δ
- Decrease of **magnetic field** B

$$\delta = 83, B = 0.3 \text{ G}$$

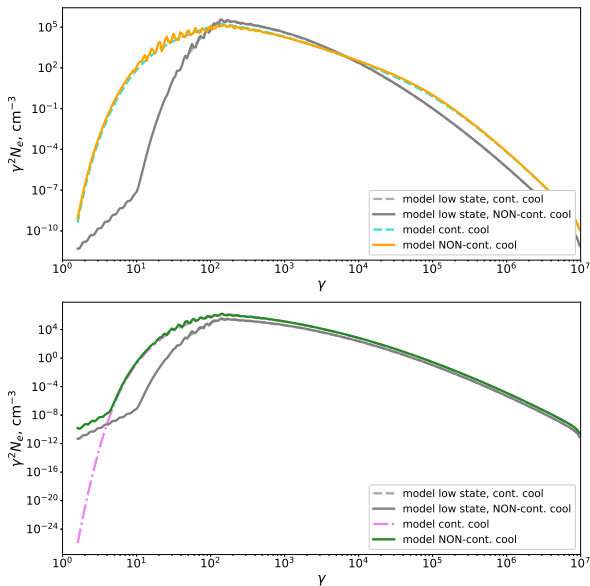
Flare 2 (brightest optical)

- Simple one-zone model
- Increase in the **injection rate** (normalization/density)
- Increase of **Doppler factor** δ

$$\delta = 45, n_e \times 6$$



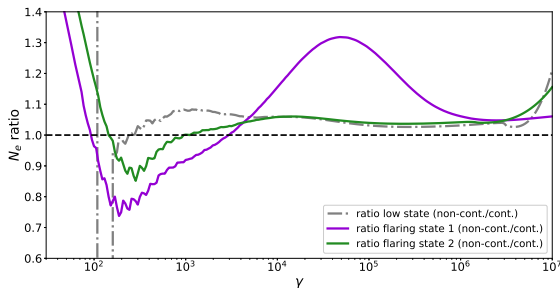
Electron spectra: low and flaring states



Difference in electron spectrum and SED

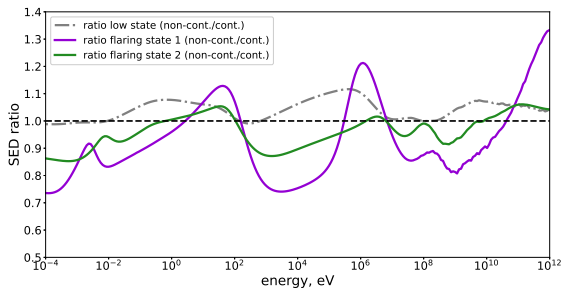
Ratio of **electron spectra**

$$\frac{N_e \text{ with full cooling term}}{N_e \text{ with continuous approx}}$$



Ratio of **SED**

$$\frac{\text{SED with full cooling term}}{\text{SED with continuous approx}}$$



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- We have considered the effect of **non-continuous IC cooling** in the context of blazar variability (with an emphasis on FSRQ)
- The *continuous-loss* approximation is quite reasonable for low states of blazars with the difference $< 10\%$
- The **non-continuous cooling** effects become quite important (difference up to $\sim 35\%$) during **flaring states** with *high Compton dominance*:
 - At **low Lorentz factors** past the *cooling break*: a large number of electrons “miss” this area as they experience jumps to very low γ
 - **spectral softening**
 - At **medium-to-high Lorentz factors** far beyond the *Klein-Nishina transition*: the continuous approximation **overestimates** the cooling effect
 - **spectral hardening**

- **What makes blazar jets cool?**

More profoundly explore the effect in terms of different flare scenarios

> shock/stochastic **re-acceleration**

- Detailed physical modeling of blazar flares with the inclusion of *non-continuous cooling* effect

- Consider the effect within the framework of theory/simulations of **stochastic particle acceleration** (non-continuous acceleration + cooling)

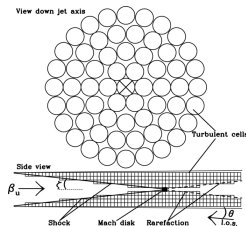
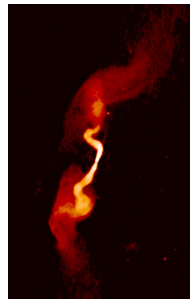
Thank you for your attention!



Back-up slides

Nature of blazar flaring activity. Origin: jet

- **Transient turbulence around the emitting zone**
(Dmytriiev et al., 2019, 2020)
- **EXHALE jet**
Lepto-hadronic cascade developing throughout the entire jet
(Zacharias et al., 2022)
- **Synchrotron mirror model** (orphan flares)
(Böttcher 2021) (Oberholzer 2021)
- **Ablation of a gas cloud** (Zacharias et al. 2017)
- **Transient acceleration processes within em. zone:**
shock, Fermi-II (turbulence), magnetic reconnection
(e.g. Marscher & Gear 1985 ; Tramacere et al. 2011 ; Giannios et al. 2009)
- **Particle injection flash**
(e.g. Mastichiadis & Kirk 1997)
- **Doppler factor increase due to jet bending or helicity**
(Abdo et al. 2010a ; Villata & Raiteri 1999)
- **Large-scale turbulence in the jet**
(e.g. Li et al., 2018)
- **Acceleration + plasma compression (+ turbulence)**
(Marscher (2014))



Numerical implementation: integration

The Compton kernel $C(\gamma, \gamma')$ has a peculiar point when $\gamma \approx \gamma'$ (small losses)

→ Separate the continuous-loss part, $\gamma/(1+\delta) \leq \gamma' \leq \gamma(1+\delta)$, $\delta \ll 1$ and decompose into Taylor series around $\gamma \approx \gamma'$:

$$\begin{aligned}
 & -N_e(\gamma, t) \int_1^\gamma C(\gamma, \gamma') d\gamma' + \int_\gamma^\infty N(\gamma', t) C(\gamma', \gamma) d\gamma' = \\
 & -N_e(\gamma, t) \int_1^{\gamma/(1+\delta)} C(\gamma, \gamma') d\gamma' + \int_{\gamma(1+\delta)}^\infty N(\gamma', t) C(\gamma', \gamma) d\gamma' + \\
 & \quad \text{non-cont. scatter. from } \gamma \text{ to lower LF} \quad \text{non-cont. scatter. from higher LF to } \gamma \\
 & + \frac{\partial}{\partial \gamma} \left[N_e(\gamma, t) \int_{\gamma/(1+\delta)}^\gamma C(\gamma, \gamma') (\gamma - \gamma') d\gamma' \right] \\
 & \quad \text{continuous cooling losses}
 \end{aligned}$$

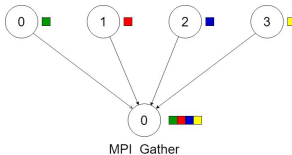
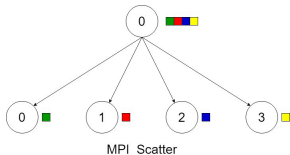
The continuous term $\frac{\partial}{\partial \gamma} [N_e \dot{\gamma}]$ is integrated analytically, $g = \min(\delta/s, 1)$, $s = 4x\gamma$:

$$\dot{\gamma} = \int_{\gamma/(1+\delta)}^\gamma C(\gamma, \gamma') (\gamma - \gamma') d\gamma' = \int_0^\infty dx n_0(x) \sigma_T c s g^2 \left[\frac{3}{2} + \frac{g}{3} + 2g \ln g - \frac{3}{2} g^2 - 9sg \left(\frac{1}{3} + \frac{g}{8} + \frac{g}{2} \ln g - \frac{2}{5} g^2 \right) \right]$$

Numerical implementation: parallelization

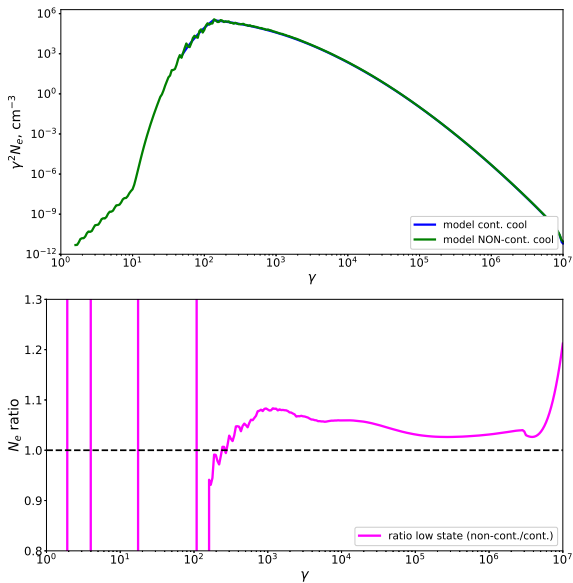
- > One simulation run (without non-continuous cooling): $\sim 10\text{-}15$ min
 - > One simulation run (WITH non-continuous cooling): $\sim 40\text{-}50$ hours !!!
- ⇒ **Parallelization is required!**

We use the MPI4PY module in Python Anaconda to perform *parallel computation* over the Lorentz factor grid



- The Lorentz factor grid array is split into blocks, simultaneously processed on separate cores
- NWU/CSR cluster = **128 cores!!!** → **1 simulation run: ~ 45 min - 1 hour**

Electron spectrum ratio (low state)



SED ratio (low state)

