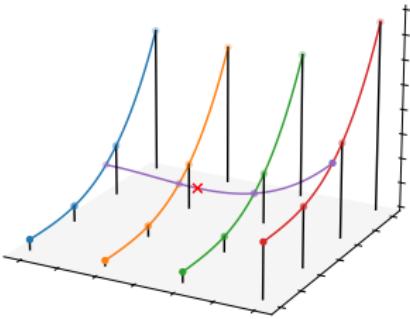


# Performance Improvements in LHAPDF

Max Knobbe  
23. MCnet Meeting

# (Very) brief Introduction

- LHAPDF-6 is a general purpose C++ interpolator, initially released in 2013  
→ Mostly used for PDF+ $\alpha_s$  interpolations
- Interfaced to core MCnet software projects (Herwig, Pythia, Sherpa, ...)
- Today (December 6, 2021) 1153 different PDF sets available via  
<https://lhapdf.hepforge.org/pdfsets>  
→ Interpolations grids provided by fitting groups (CTEQ, NNPDF, MMHT, ...) → LHAPDF interpolates between these grids/knots



LHAPDF ID	Set name and links	Number of set members	Latest data version	Notes
201	GRV91	1 (link)	1	alpha_s is broken in LHAPDF. This version uses approximate 1st order running from reported Lamda(s) values.
212	GRV91	1 (link)	1	
273	xInterPLMLO_05	9 (link)	1	
280	xInterPLMLO_05R	6 (link)	1	
1000	JAM21ProxFit0	795 (link)	1	Negative signs PDF's to fit D0117 and NALQCD Drell-Yan data using NLO theory and H1 and 2010 leading neutrino data. Overall chi^2/ndf = 1.011. Chi^2/ndf = 1.011. Chi^2/ndf = 1.012.
2000	JAM21ProxFit0_gT	795 (link)	1	Negative signs PDF's to fit E6111 (part of gT) and E6112 and NALQCD Drell-Yan data using NLO theory and H1 and 2010 leading neutrino data. Overall chi^2/ndf = 0.65. Chi^2/ndf = 0.65. Chi^2/ndf = 0.65.
3000	JAM21ProxFit0coll_cowrie	796 (link)	1	Negative signs PDF's to fit E6111 and MCFM Drell-Yan data using NLO theory and H1 and 2010 leading neutrino data. Overall chi^2/ndf = 1.012. Chi^2/ndf = 1.012.
4000	JAM21ProxFit0coll_reapar	790 (link)	1	Negative signs PDF's to fit E6111 and MCFM Drell-Yan data using NLO theory and H1 and 2010 leading neutrino data. Overall chi^2/ndf = 0.95.

# Room for improvement / Issues with the current LHAPDF version

[Tim Martin at SwiftHep/ExcaliburHep workshop]

## Identified shortcomings / Outline

### ① Interpolation Speed

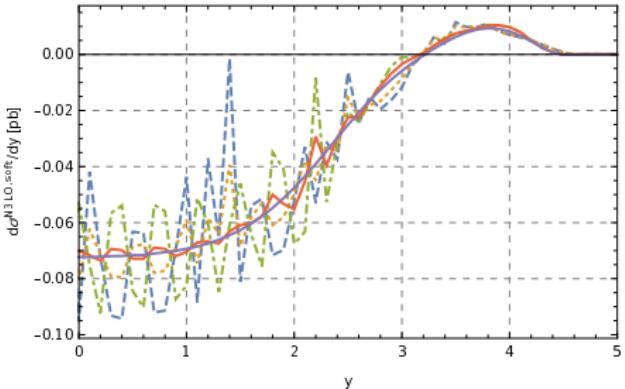
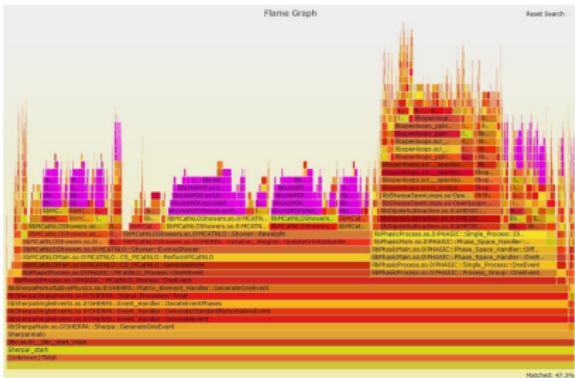
→ Known problem, HL-LHC requires too much CPU hours with current software

### ② Non-physical side effects in high-order computations

→ New interpolation strategy for special computations

### ③ Modern/Heterogeneous Systems

→ Currently no support for e.g. GPU computations



[1710.03016]

# 1. Reduce execution speed / changes in LHAPDF-6.4.0

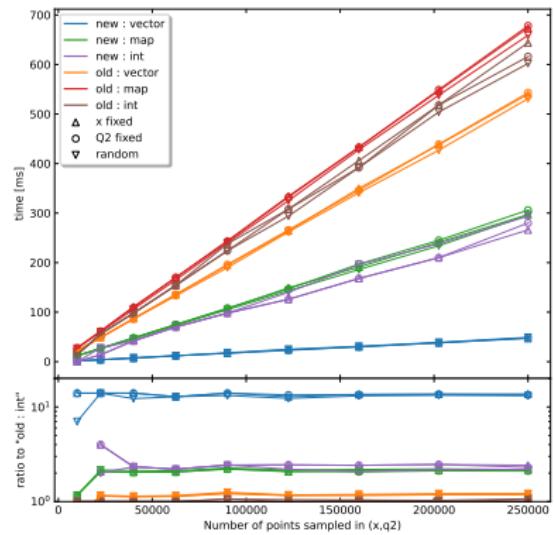
LHAPDF workflow – what is using up the computing time?

- ① Find the right grid / knots  
Grids allow for maximal flexibility (discontinuous grids, different grids for each particle)  
→ 3 (binary) searches
- ② Compute new anchor points
- ③ Perform final interpolation

Significant Changes:

- New memory layout
    - Remove unused freedom in grids
    - Smart memory layout
    - Single binary search
  - Cache common computation if multiple pid's requested
  - Reduce number of transcendental calls
- Significant speedup of factor 3-10

**Released in LHAPDF-6.4.0**



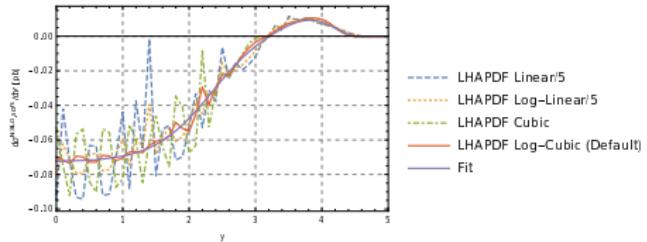
## 2. LHAPDF for higher-order calculations

Observed in [Dulat, Mistlberger, Pelloni](#), soft-virtual term of rapidity contribution in the soft limit

$$\frac{d\sigma_{gg}}{dY} = \frac{\sigma_0}{9v^2} \left(\frac{\alpha_s}{\pi}\right)^5 \int_\tau^1 dz f_g \left(\sqrt{\frac{\tau}{zY}}\right) f_g \left(\sqrt{\frac{\tau Y}{z}}\right) \left\{ 1124.31 \delta(1-z) + 1466.48 \left[ \frac{1}{1-z} \right]_+ - 6062.09 \left[ \frac{\log(1-z)}{1-z} \right]_+ + 7116.02 \left[ \frac{\log^2(1-z)}{1-z} \right]_+ - 1824.36 \left[ \frac{\log^3(1-z)}{1-z} \right]_+ - 230 \left[ \frac{\log^4(1-z)}{1-z} \right]_+ + 216 \left[ \frac{\log^5(1-z)}{1-z} \right]_+ \right\} \quad (5.1)$$

Problem:

- Higher order terms seem to be sensitive to interpolation polynomial
- Introduces oscillations in differential cross-section



[1710.03016]

## 2. LHAPDF for higher-order calculations

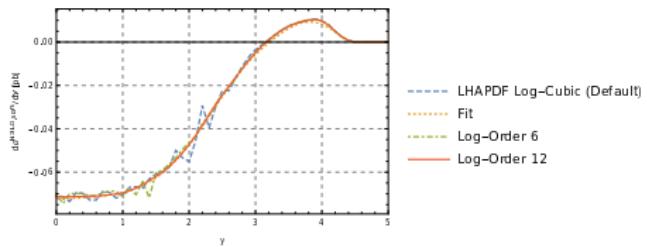
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Solution: higher order Polynomials (Lagrange)

Applied in

- ➊ Global fit:
  - definitely continuous, smooth
  - potential numerical problems  
(Runge's phenomenon, interpolation errors)
- ➋ Local fit:
  - continuation of LHAPDF-approach
  - relatively simple implementation
  - continuous, not smooth



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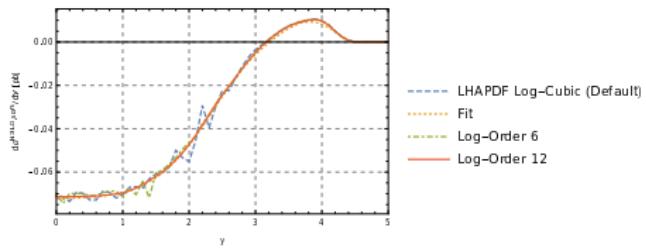
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### 3. Modern Architectures – why do we have to care?

#### Machine Learning Efforts:

- Almost every part of MC tool-chain is investigated  
→ Naturally, GPU-based computations

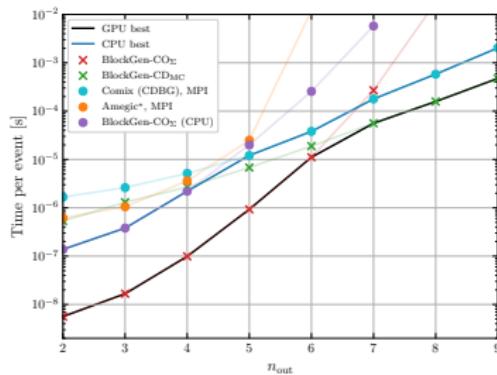
#### GPU Monte Carlo's

Some, (recent) developments in chronological order:

- Tess [Giele, Stavenga, Winter]  
C++, Cuda
- BlockGen [Bothmann, Giele, Höche, Isaacson, MK]  
C++, Cuda, (Kokkos)
- MadFlow [Carrazza, Cruz-Martinez, Rossi, Zaro]  
Python, Tensorflow
- MadGraph-GPU [Valassi, Roiser, Mattelaer, Hageboeck]  
C++, Cuda, (Alpaka, Kokkos, Sycl)

#### New Clusters/Supercomputer:

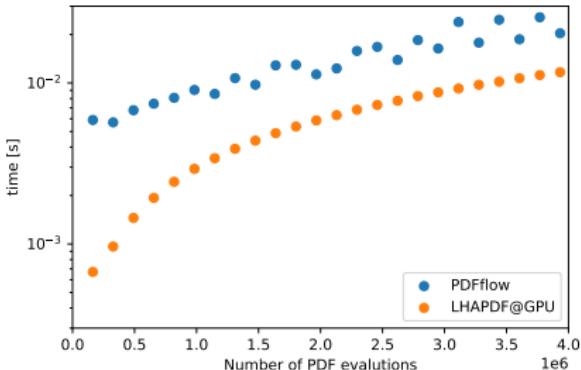
- Aurora (2×Intel CPU + 6×Intel GPU per note)
- More to come..?



[Aurora]

### 3. LHAPDF@Heterogenous

- Kokkos code, build on top of LHAPDF
  - receiving LHAPDF updates
  - minimal code doubling
- Can provide PDF's to aforementioned projects
- only competitor: PDFFlow  
[Carrazza, Cruz-Martinez, Rossi]
  - Probably more natural for ML



Possible application in classical frameworks:

- Many variations at once?
  - All-pid version for single PS-point?
  - ...
  - Suggestions, ideas, requests?
- Not released yet, more testing needed

# Conclusion / Outlook

## Conclusion:

- Significant interpolation speedup, Sherpa+LHAPDF benchmark pending
- Fixed higher order computations problems
- New interpolator, suitable for modern systems

## Possible future projects:

- Higher Resolution?
- TMD's, much easier to include with generalised memory/interpolator structure

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Thank you

MCnet: for giving me the opportunity  
You: for your attention!