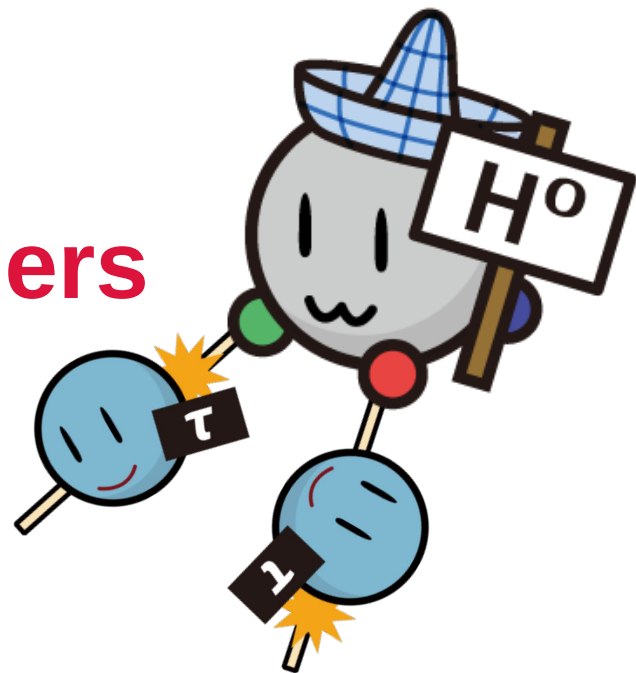


# Measuring the CP state of tau lepton pairs from Higgs decay at ~~the ILC~~ $e^+e^-$ colliders

Phys.Rev. D98 (2018) no.1, 013007  
arXiv:1804.01241 [hep-ex]

Nucl.Instrum.Meth.A 810 (2016)  
51-58 arXiv:1507.01700 [hep-ex]



<https://higstan.com/>



Daniel Jeans, KEK/IPNS



known sources of CP violation are insufficient to explain our universe's matter – anti-matter asymmetry

→ motivates search for CP effects in the Higgs sector

Is the 125 GeV Higgs a CP eigenstate ?

$$h_{125} = \cos \psi_{CP} h^{CP\text{-even}} + \sin \psi_{CP} A^{CP\text{-odd}}$$

pure CP even:  $\psi_{CP} = 0$  [Standard Model]

pure CP odd:  $\psi_{CP} = \pi/2$  [already excluded at LHC]

or a mixture?

Do Higgs couplings conserve CP ?

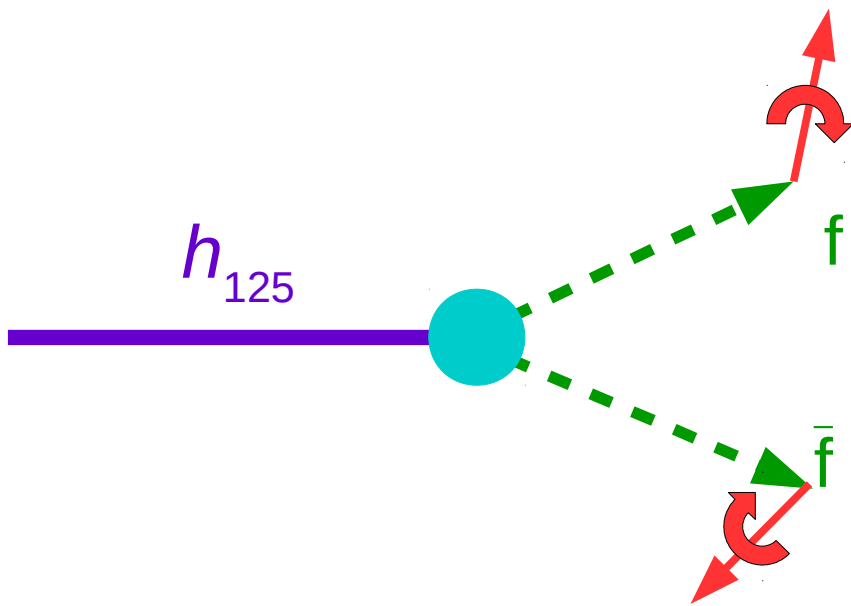
e.g. coupling to fermions:  $\mathcal{L} \sim g \bar{f} ( \cos \psi_{CP} + i \gamma^5 \sin \psi_{CP} ) f H$

CP conserving coupling  $\psi_{CP} = 0$  [Standard Model]

maximally violating  $\psi_{CP} = \pi/2$

or partially violating ?

we can also probe CP nature of Higgs couplings to gauge bosons



$h$  is a spin 0 state:

$$|f \bar{f}\rangle = |\uparrow\downarrow\rangle + e^{2i\psi} |\downarrow\uparrow\rangle$$

$$\begin{array}{ll} \psi = 0 & \text{CP even} \\ \pi/2 & \text{CP odd} \end{array}$$

to probe CP, we consider the correlation between  
the spins of fermions produced in Higgs boson decay

Higgs decays to tau leptons:

large branching ratio ( $\sim 6\%$ )

sensitivity to tau spin orientation

→ reflected in distribution of decay products

use tau decay products to reconstruct **polarimeter**  
 → estimator of tau spin orientation

straightforward to extract in  $\tau^\pm \rightarrow (\pi^\pm \nu)$  [BR~11%]  
 or  $(\pi^\pm \pi^0 \nu)$  [ ~25%]

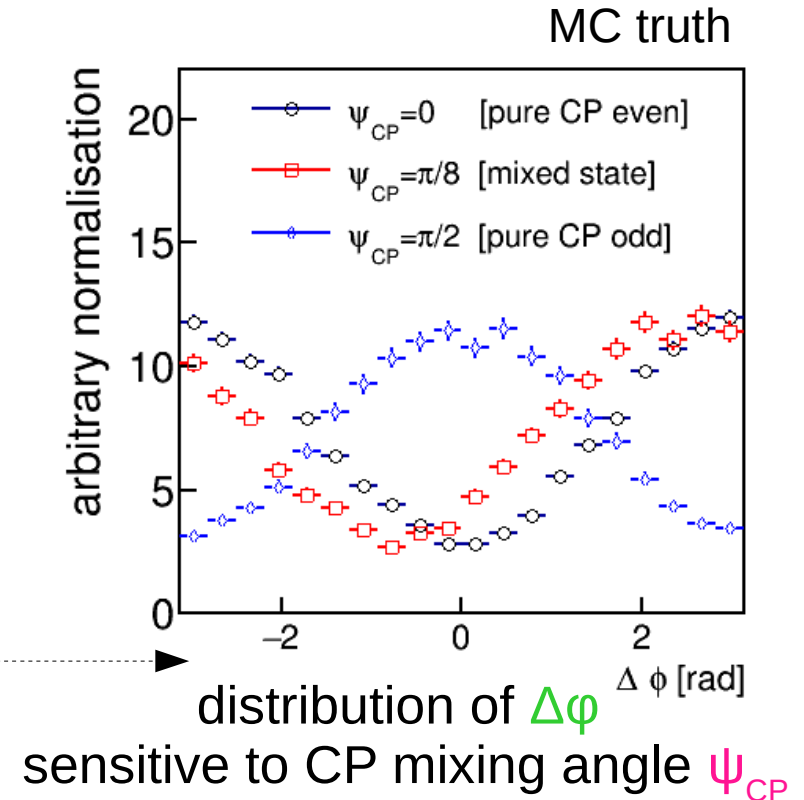
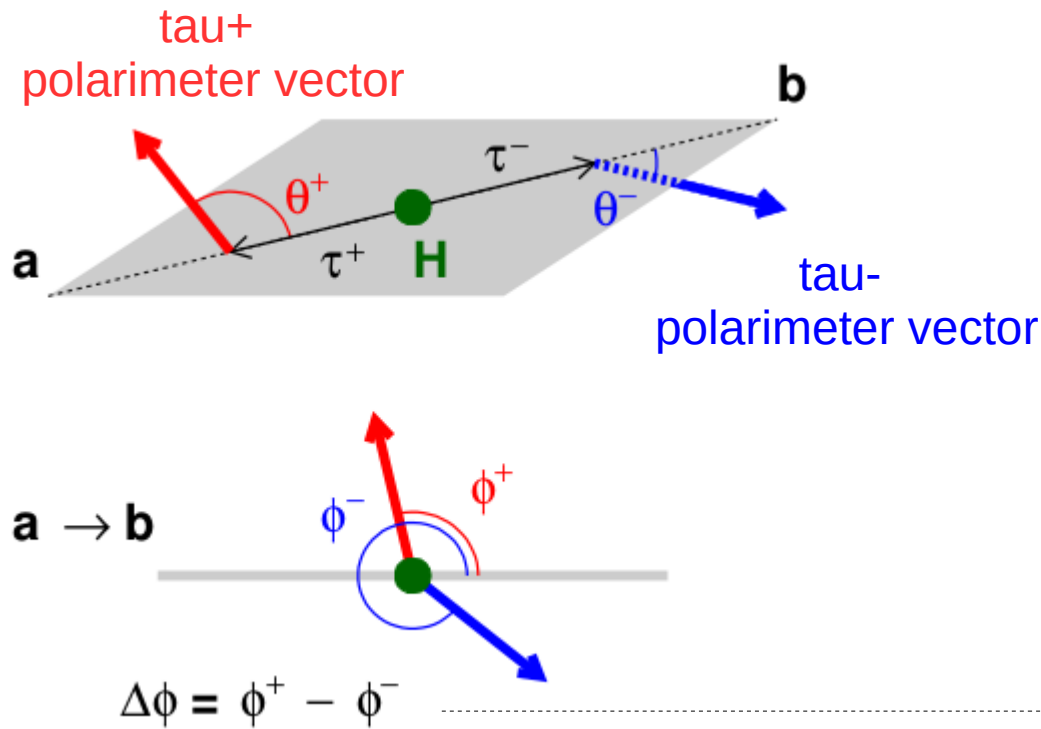
optimal **polarimeter vectors  $\mathbf{h}$**  in terms of  
 tau decay product momenta in the tau rest frame:

$$\mathbf{h} (\tau^\pm \rightarrow \pi^\pm \nu) \sim \mathbf{p}_{\pi^\pm}$$

$$\mathbf{h} (\tau^\pm \rightarrow \pi^\pm \pi^0 \nu) \sim m_\tau (E_{\pi^\pm} - E_{\pi^0}) (\mathbf{p}_{\pi^\pm} - \mathbf{p}_{\pi^0}) + 0.5 (\mathbf{p}_{\pi^\pm} + \mathbf{p}_{\pi^0})^2 \mathbf{p}_\nu$$

for optimal sensitivity, require knowledge of tau rest frame  
 (or equivalently the **neutrino momentum**)

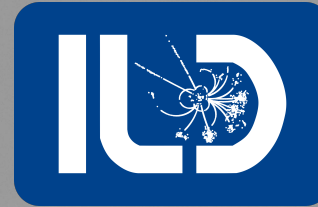
# correlation between transverse polarimeter components is sensitive to CP mixing



$$dN \sim (1 + \cos\theta^+ \cos\theta^-) \left\{ 1 - \frac{\sin\theta^+ \sin\theta^-}{(1 + \cos\theta^+ \cos\theta^-)} \right\} \cos(\Delta\phi - 2\psi_{CP})$$

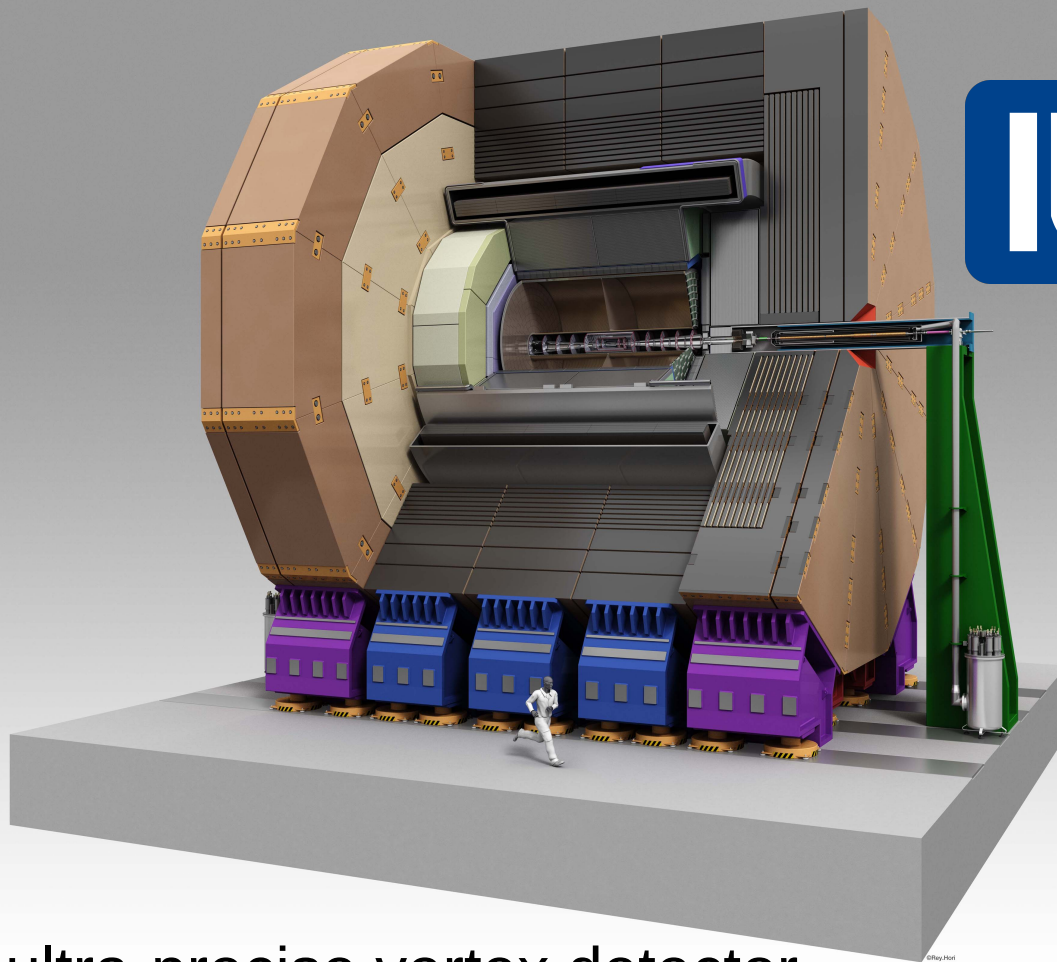
“contrast” → determines event-by-event modulation

if polarimeters aligned with tau momentum ( $\sin\theta \rightarrow 0$ ),  
transverse correlations are less strong

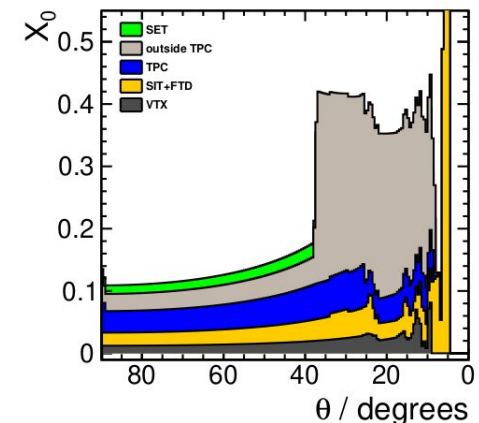
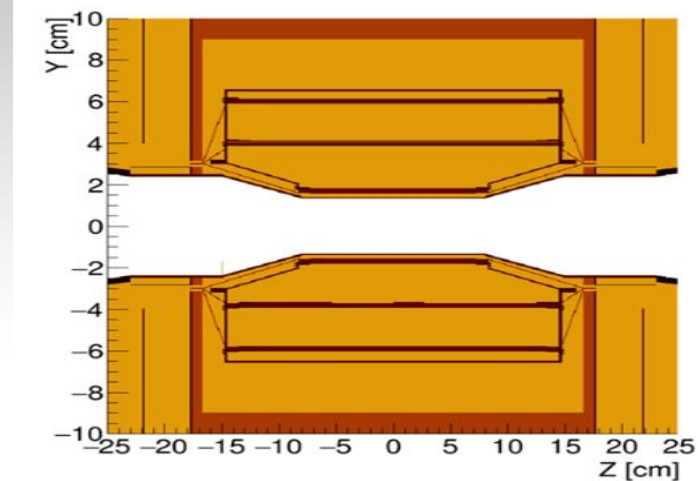


# International Large Detector

detector concept being developed for ILC  
arXiv:2003.01116



- ultra-precise vertex detector
  - first layer @  $r = 16$  mm
  - impact parameter resolution  $\sim 3\mu\text{m}$
- low mass tracker
  - few interactions  $\rightarrow$  helps tau decay mode identification
- highly segmented “PFA” calorimeters
  - 30 layers of  $5 \times 5$  mm<sup>2</sup> cells in ECAL
  - $\pi^0$  & tau decay mode reconstruction



# Full tau reconstruction

to reconstruct optimal tau **polarimeter vectors**, need full reconstruction of tau decay products, including neutrino(s)

event with two hadronic tau decays (1 neutrino per tau),  
**6 unknowns**:  $2 \times$  neutrino 3-momenta

neutrino momenta can be reconstructed if we know:

**visible tau momenta**

tau **production vertex** (from Z decay products)

**impact parameters** of charged tau decay products

$p_T$  of the tau-tau system (balance the Z  $p_T$ )

**6 constraints**:

$2 \times$  impact parameters define the tau momenta plane

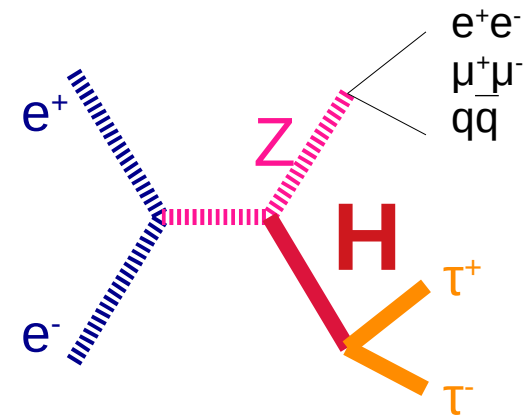
$2 \times$  tau invariant mass

2 from tau-tau  $p_T$  [ $p_x$ ,  $p_y$ ]

requires excellent detector performance:

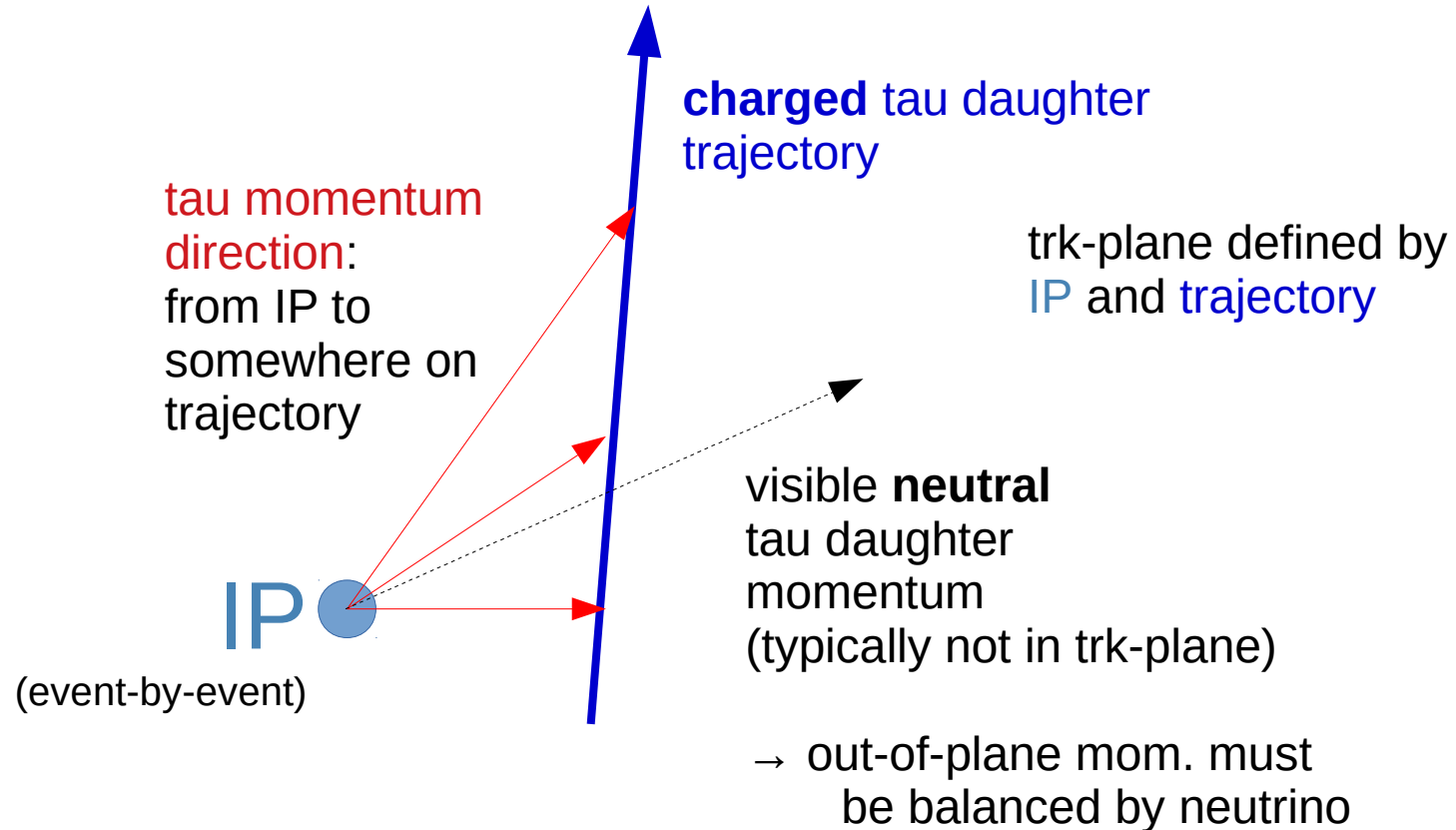
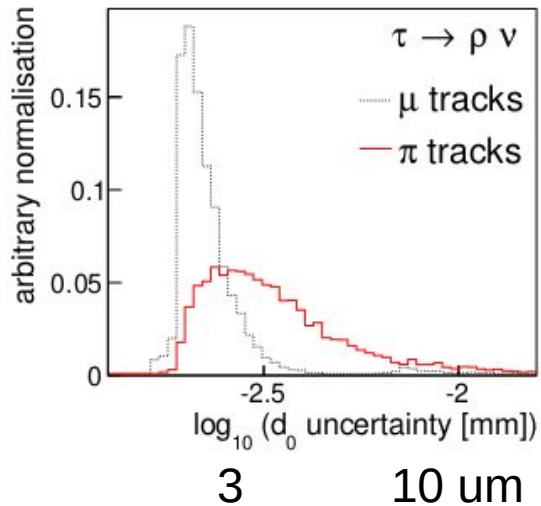
charged particle and photon reconstruction,

impact parameter measurement, jet energy measurement



# e.g. single-prong hadronic tau decays

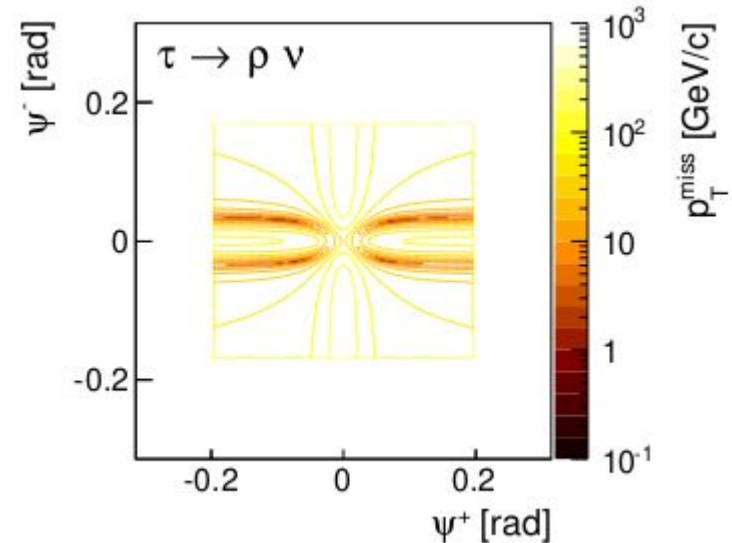
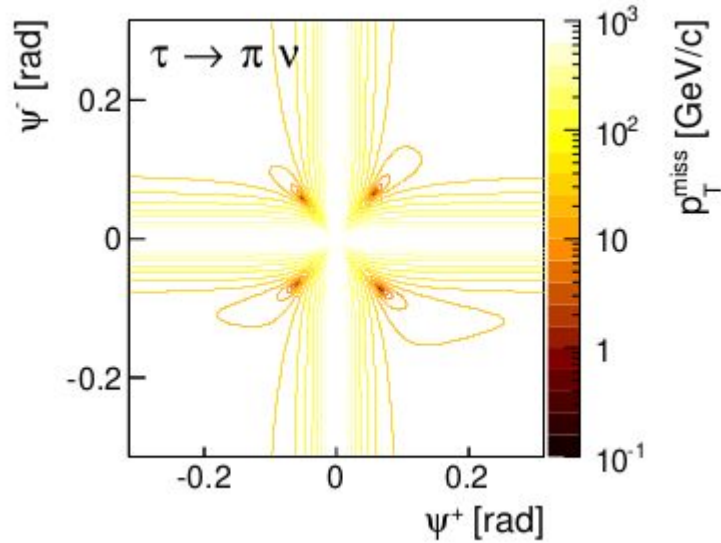
tracks from  $H \rightarrow \tau \tau$   
@250 GeV



one free parameter: orientation of the in-plane neutrino momentum (angle  $\psi$ )  
once orientation is defined, tau mass constraint provides its magnitude



scan neutrinos' orientation to minimise event  $p_T$

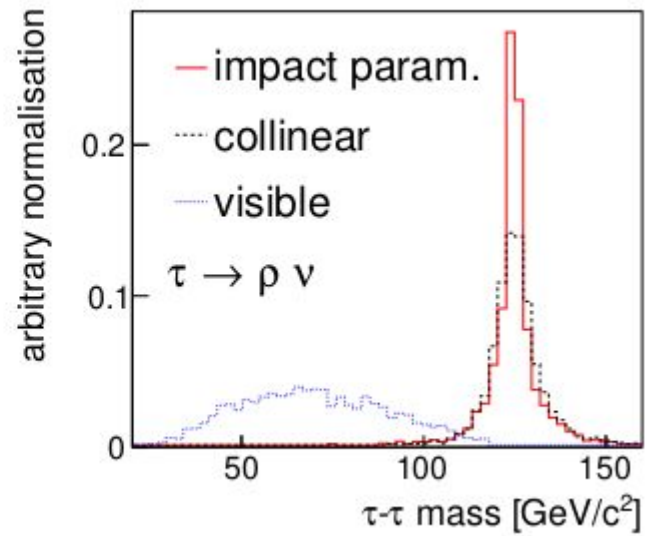
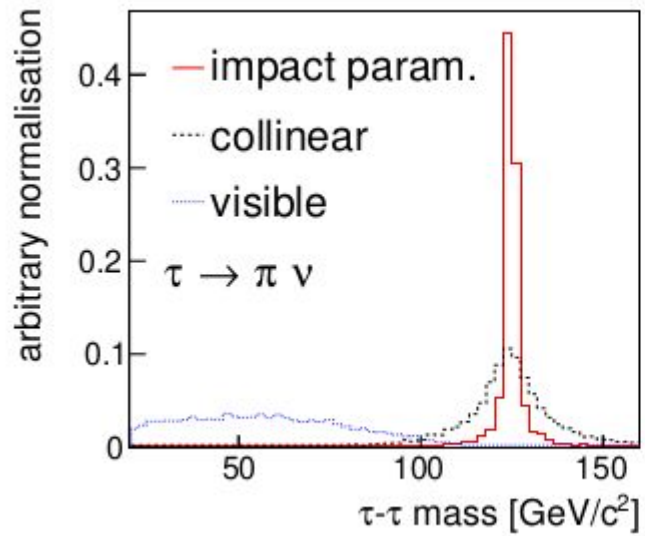


typically several solutions

reject solutions with negative reconstructed tau proper lifetime

choose remaining soln. with smallest event  $p_T$

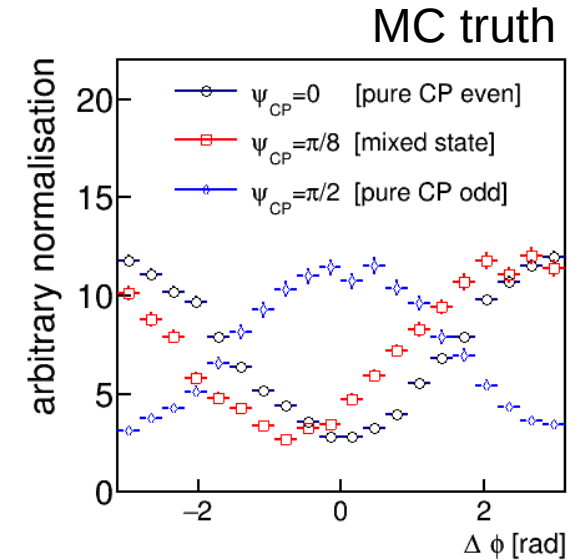
# reconstructed di-tau mass



reconstruct CP-sensitive  $\Delta\phi$  distribution  
at ILC 250GeV

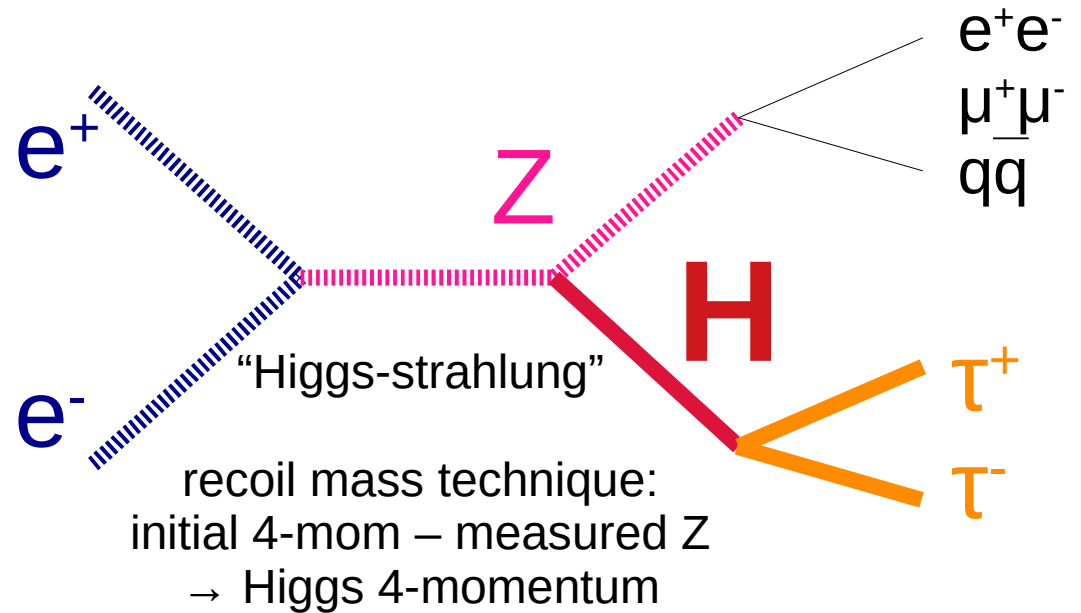
full Geant4 simulation of ILD

realistic reconstruction processing  
ilcsoft, MarlinReco, PandoraPFA, ...



Signal:  $e^+ e^- \rightarrow Z H$   
 $Z \rightarrow e^+e^-, \mu^+\mu^-, q\bar{q}$   
 $H \rightarrow \tau^+\tau^-$   
 $\tau^\pm \rightarrow (\pi^\pm \nu) \text{ or } (\pi^\pm \pi^0 \nu)$

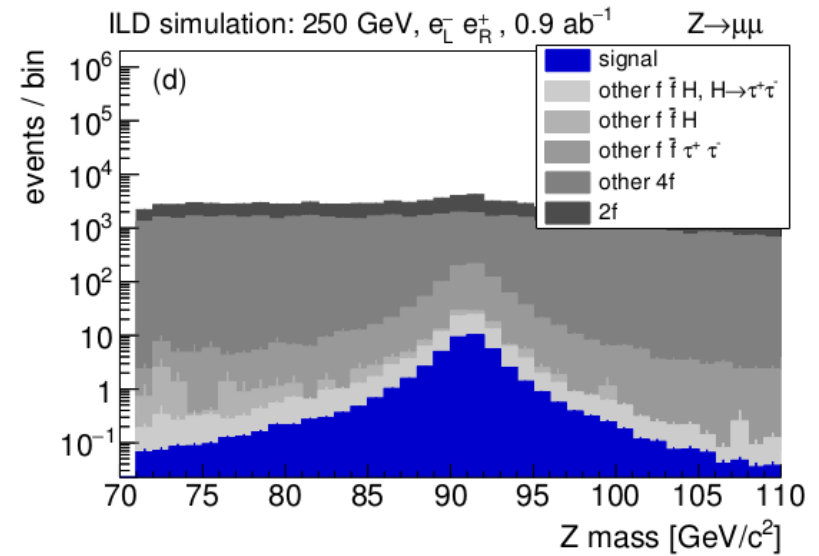
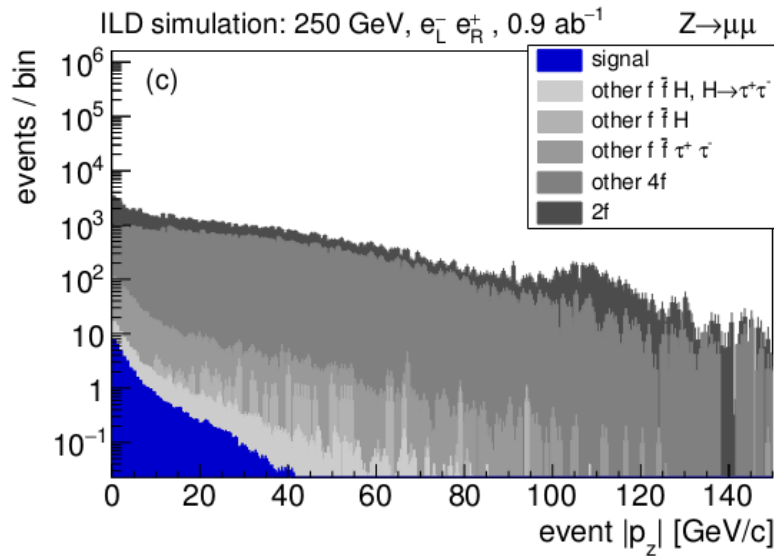
Backgrounds:  
 $e^+ e^- \rightarrow ffH, 4f, 2f$



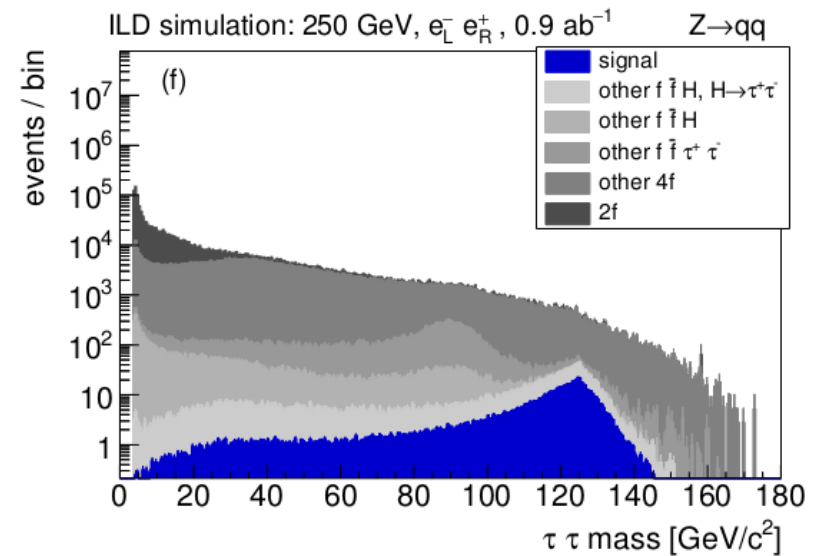
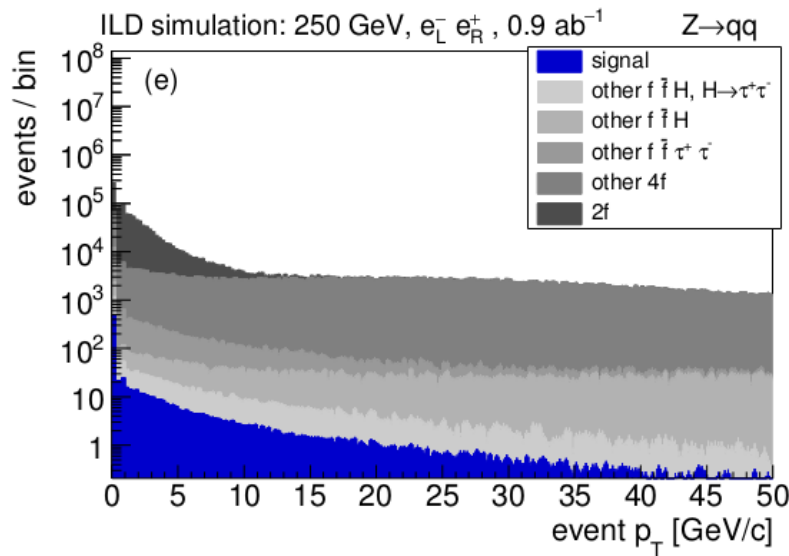
assume  $2 \text{ ab}^{-1}$  of 250 GeV data : after 11 years ILC operation [arXiv:1903.01629]

# some distributions after full simulation and reconstruction and a simple preselection:

$Z \rightarrow \mu^+ \mu^-$



$Z \rightarrow q\bar{q}$



use these and other observables to select signal events

After relatively simple cut-based event selection  
 expected numbers of signal and background events  
 ( 2 ab<sup>-1</sup> integrated luminosity at 250 GeV )

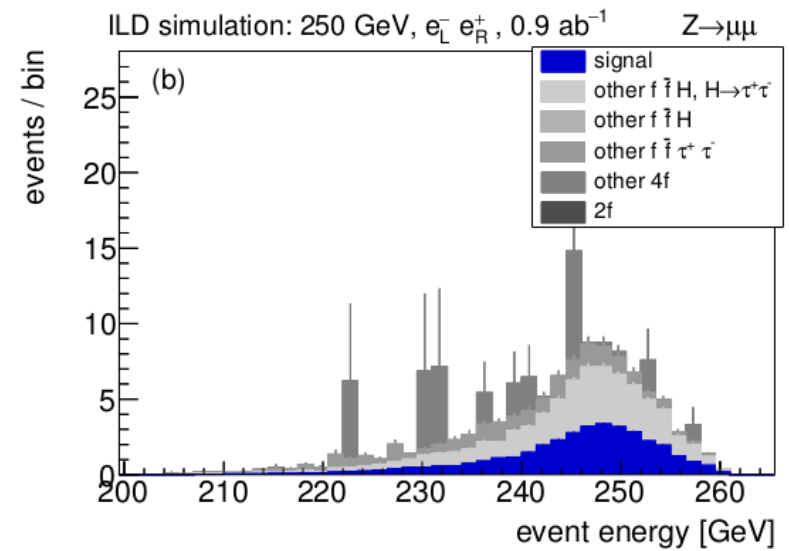
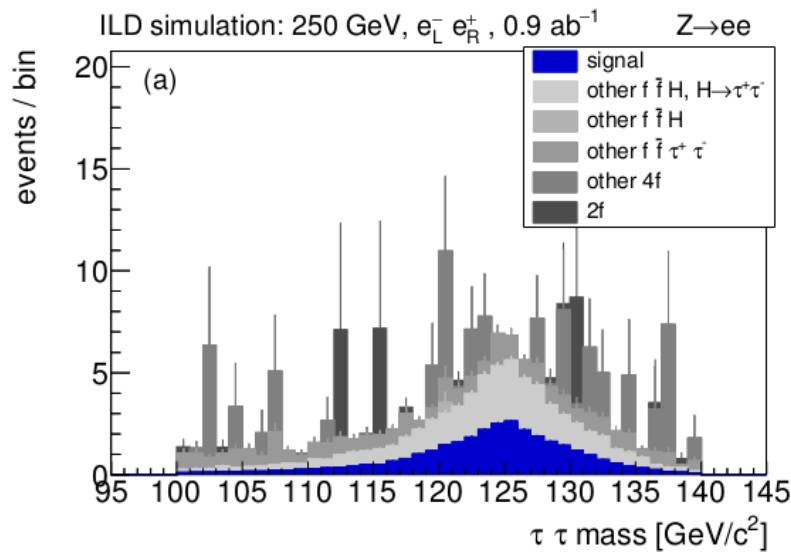
Process	$Z \rightarrow$		
	$e^+e^-$	$\mu^+\mu^-$	$qq$
	$e$	$\mu$	$q$
Signal	32	36	575
Other $f\bar{f}H, H \rightarrow \tau^+\tau^-$	39	43	627
Other $f\bar{f}H$	1	0	58
Other $f\bar{f}\tau^+\tau^-$	32	24	766
Other $4f$	51	35	2834
$2f$	18	0	403

Z decays to leptons: few 10s of signal events; S:B ~ 1:3~4

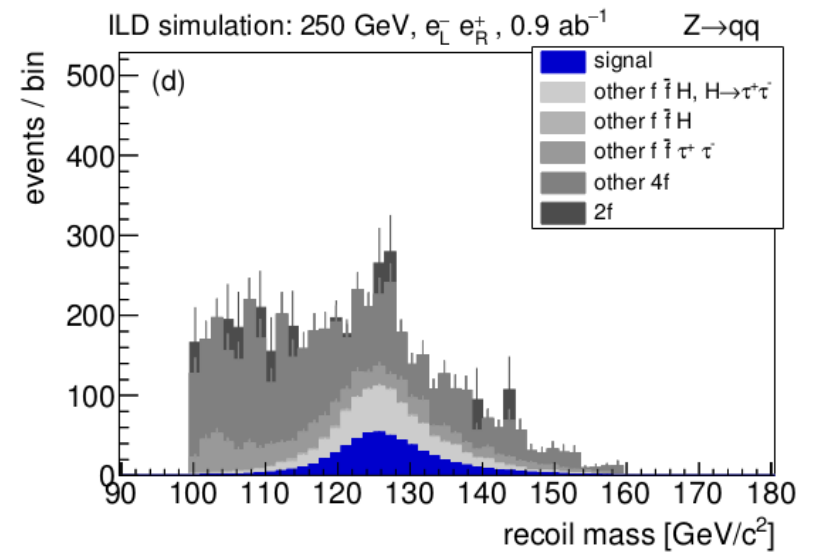
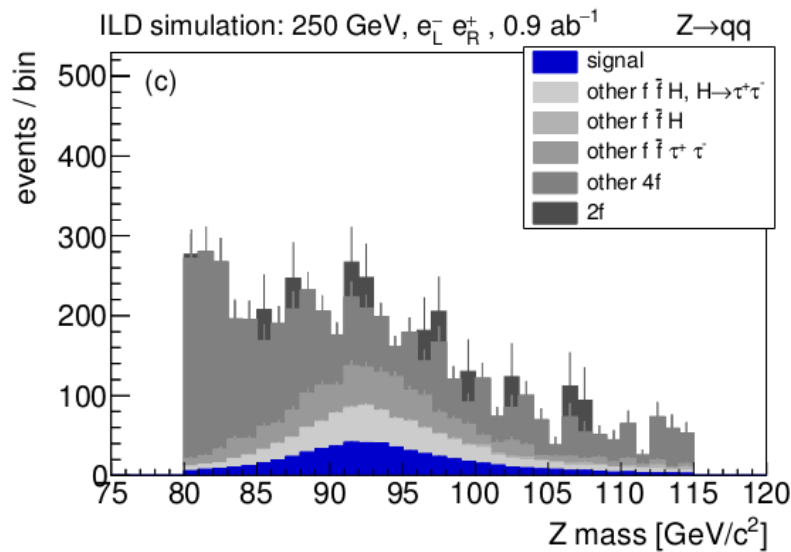
Z decays to quarks: many more signal events; S:B ~ 1:8

# Some distributions after selection

$Z \rightarrow \text{leptons}$



$Z \rightarrow q\bar{q}$



train Neural Networks to further separate signal from backgrounds

to extract tau **polarimeter** (estimator of spin direction),  
 must identify tau decay mode

- consider number of charged particles and photons  
 reconstructed in the tau jet, and their invariant mass  
 simple cut-based classification

Reco. decay	True decay		
	$(\pi\nu, \pi\nu)$	$(\pi\nu, \rho\nu)$	$(\rho\nu, \rho\nu)$
$Z \rightarrow \mu^+ \mu^-$			
$(\pi\nu, \pi\nu)$	93	3	< 1
$(\pi\nu, \rho\nu)$	7	93	6
$(\rho\nu, \rho\nu)$	< 1	4	94
$Z \rightarrow qq(\text{uds})$			
$(\pi\nu, \pi\nu)$	89	6	< 1
$(\pi\nu, \rho\nu)$	11	89	12
$(\rho\nu, \rho\nu)$	< 1	5	87

87% ~ 94% efficiency to correctly identify tau decay modes,  
 better in events with little hadronic activity

# Group events according to expected CP sensitivity, based on:

## intrinsic:

orientation of polarimeters (“contrast” function)

## reconstruction quality and tau flight distance:

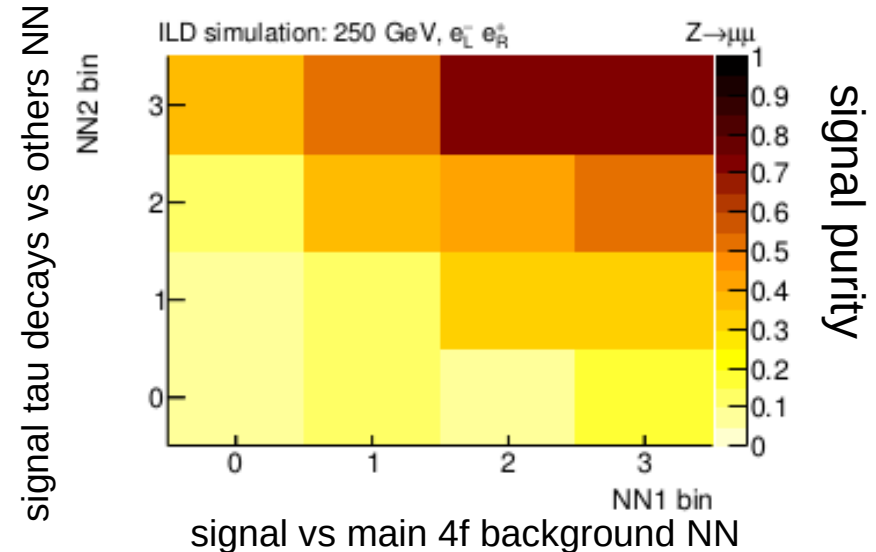
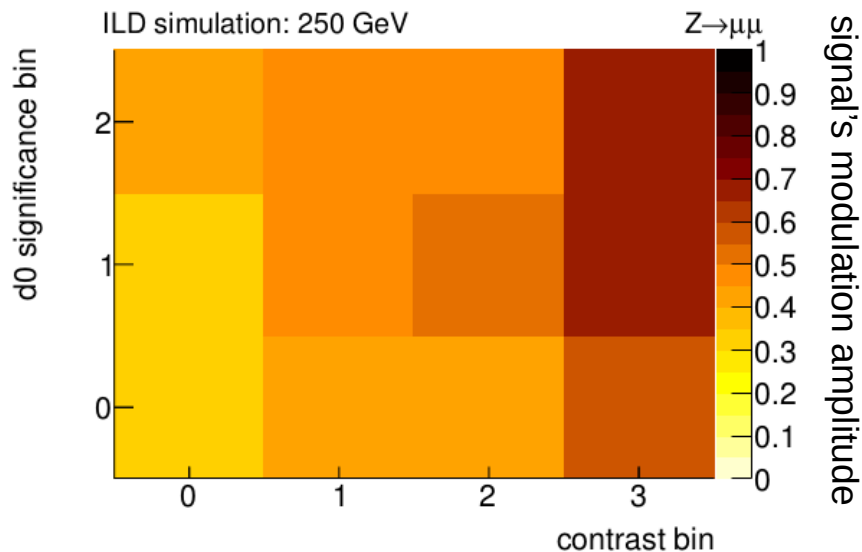
tau decay prongs’ impact parameter measurement significance

## background contamination:

output of simple NN [6 inputs] (signal vs. main 4f bkgs)

## wrong tau decay mode contamination:

output of simple NN [4 inputs] (signal tau decays vs. others)

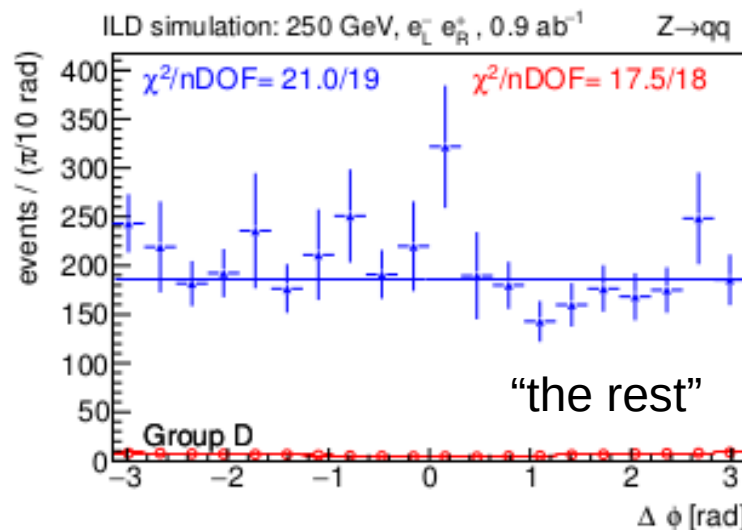
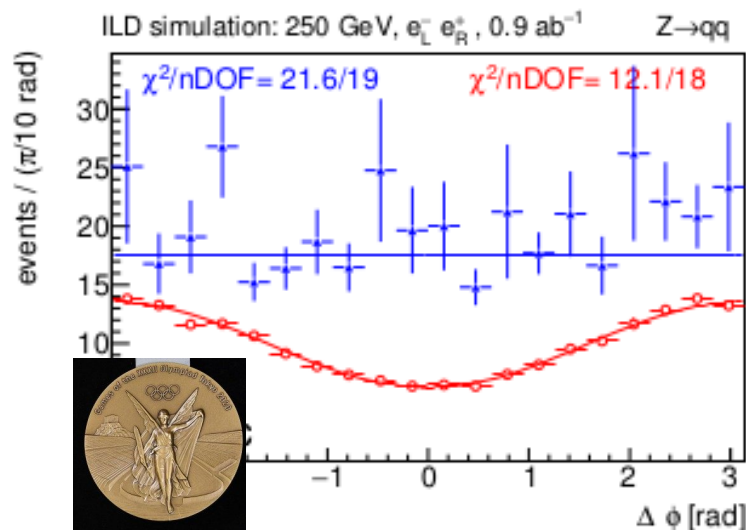
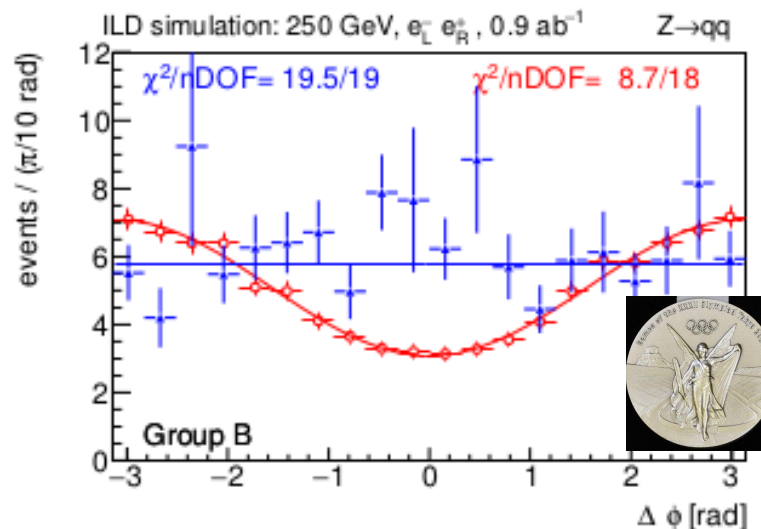
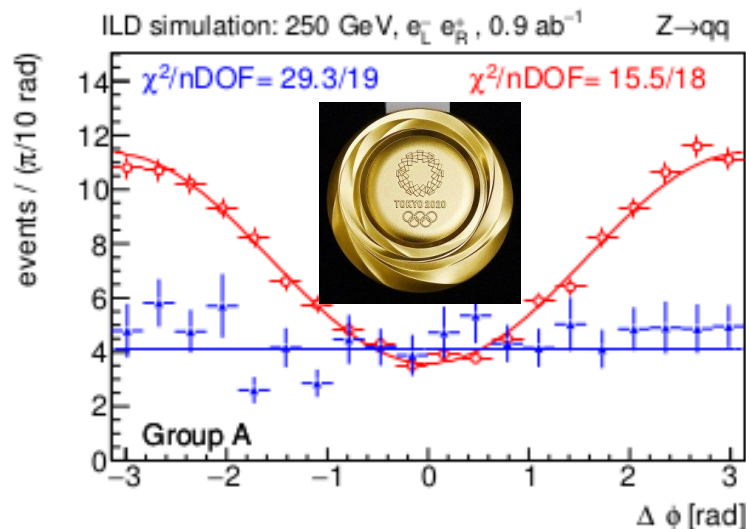




# CP sensitive observable $\Delta\phi$ in different event sensitivity bins

signal background

error bars:  
MC statistics



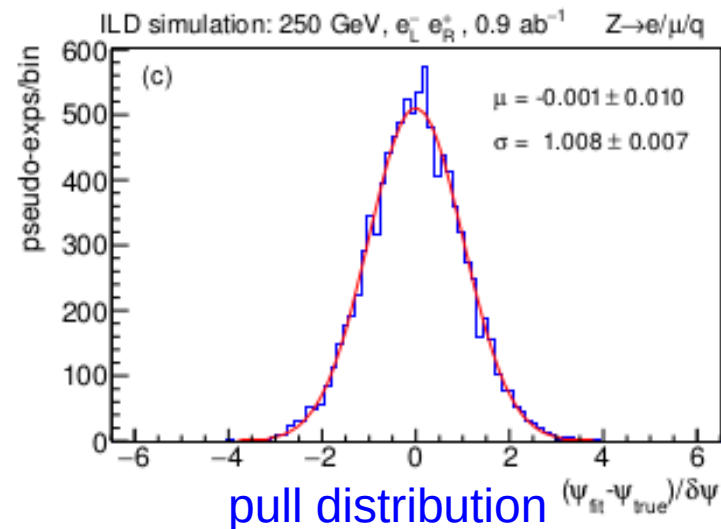
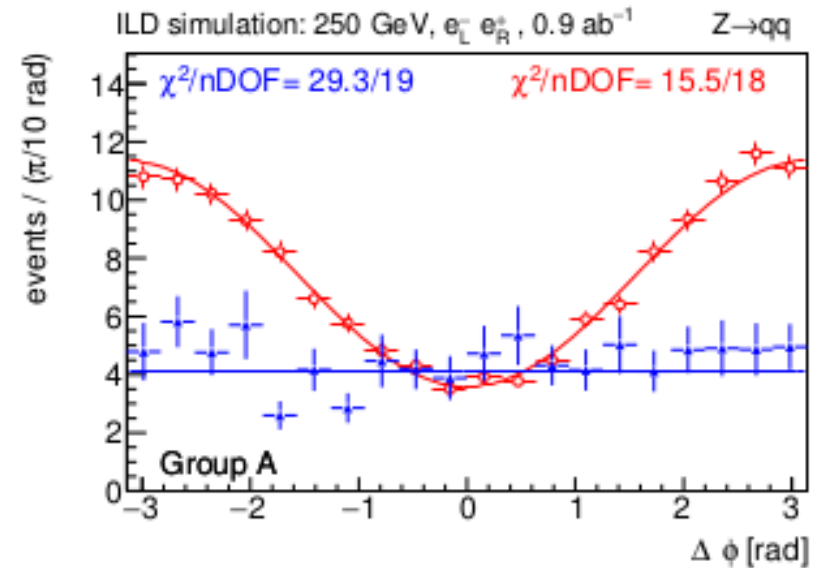
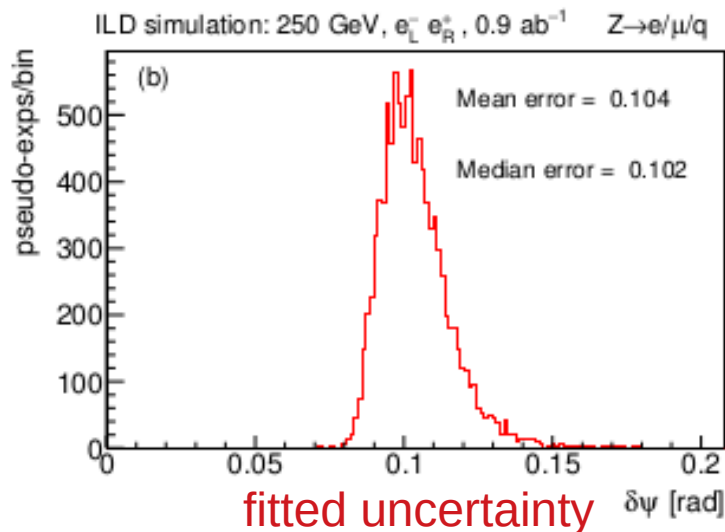
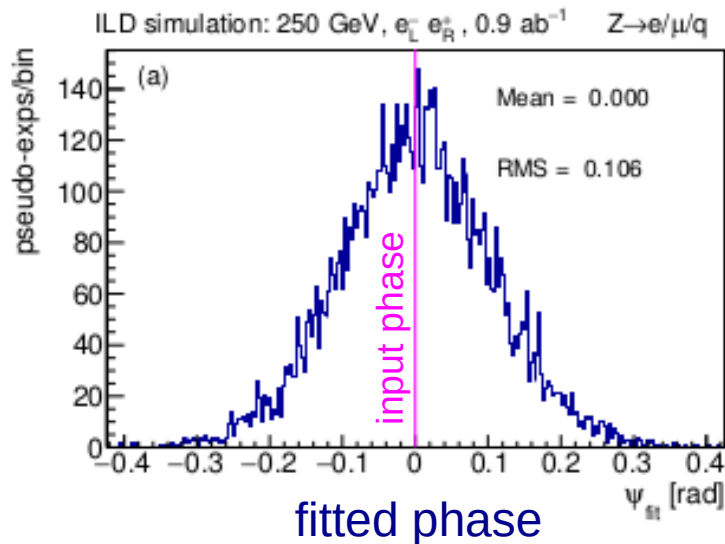
phase of **signal distribution** is sensitive to CP

# Estimating measurement sensitivity

unbinned maximum likelihood fit: simultaneously in all sensitivity bins and selection channels  
fit a single parameter: the phase of the  $\Delta\phi$  distribution

perform series of toy pseudo-experiments using simulated distributions

results of 10k pseudo-exps



# sensitivity on $\psi_{CP}$ under various conditions

TABLE IV. Estimated experimental precision  $\delta\psi_{CP}$  on the CP phase in different scenarios.

$\int \mathcal{L}$ [ab <sup>-1</sup> ]	beam pol.		notes	$\delta\psi_{CP}$
	$e^-$	$e^+$		[mrad]
1.0	0	0	full analysis	116
1.0	0	0	only $Z \rightarrow ee$	450
1.0	0	0	only $Z \rightarrow \mu\mu$	412
1.0	0	0	only $Z \rightarrow qq$	122
1.0	0	0	only $(\pi\nu, \pi\nu)$	387
1.0	0	0	only $(\pi\nu, \rho\nu)$	198
1.0	0	0	only $(\rho\nu, \rho\nu)$	166
1.0	-1.0	+1.0	pure $e_L^- e_R^+$	97
1.0	+1.0	-1.0	pure $e_R^- e_L^+$	113
1.0	0	0	$\sigma_{ZH} + 20\%$	104
1.0	0	0	$\sigma_{ZH} - 20\%$	133
1.0	0	0	no bg.	76
1.0	0	0	perf. pol.	100
1.0	0	0	no bg., perf. pol./eff.	25
H20-staged: 250 GeV, 2 ab <sup>-1</sup>				
0.9	-0.8	+0.3	only $e_L^- e_R^+$	102
0.9	+0.8	-0.3	only $e_R^- e_L^+$	120
0.1	-0.8	-0.3	only $e_L^- e_L^+$	359
0.1	+0.8	+0.3	only $e_R^- e_R^+$	396
2.0	mixed		full analysis	75

dominated by events with hadronic Z

1 ab<sup>-1</sup> (unpolarised):

realistic : 116 mrad

perfect detector/analysis: 25 mrad

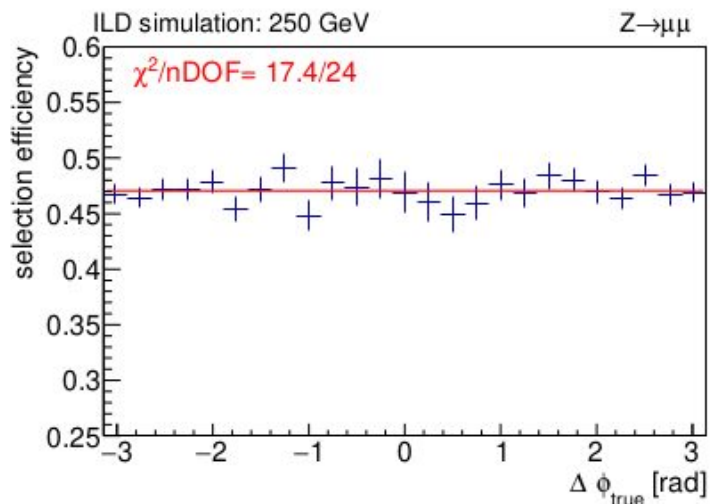
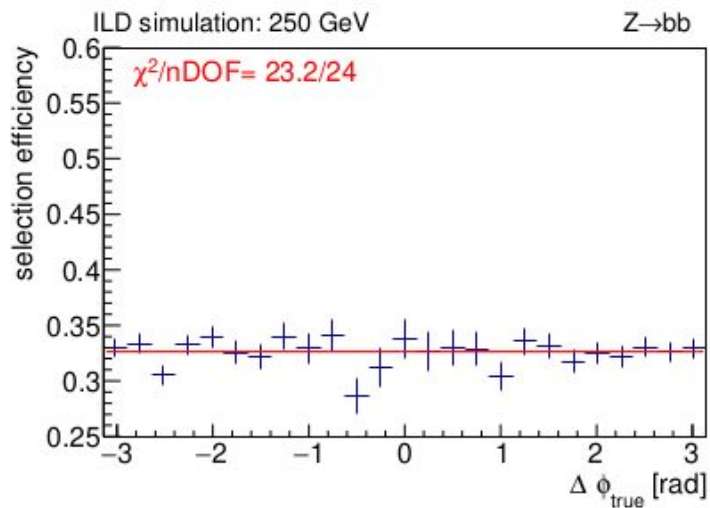
significant instrumental effects

→ full simulation essential

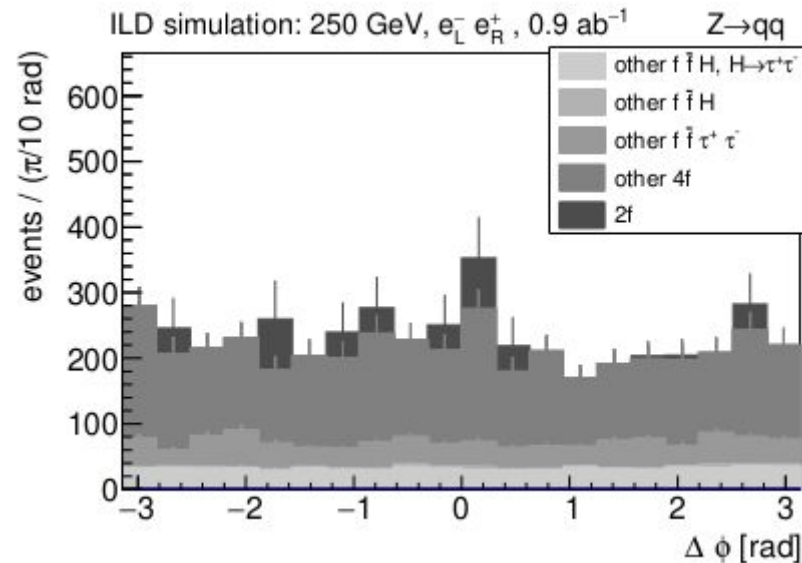
2 ab<sup>-1</sup> @ ILC-250: 75 mrad  $\approx 4.3^\circ$

# thoughts on systematics

signal acceptance vs. CP-sensitive angle  
is rather flat



as is the selected background



**data-driven:**  $e^+ e^- \rightarrow Z (\rightarrow \text{tau tau}) Z (\rightarrow e, \mu, q)$   
larger xsec, similar kinematics  
expected to be flat in  $\Delta\phi$   
 $\rightarrow$  verify @ Z-pole

# Summary

Precision studies of the Higgs sector are of great interest

→ point the way to physics beyond SM

CP properties are one aspect of such precision Higgs studies

studied prospects for measurement of CP in Yukawa coupling

full simulation of the ILC and the ILD detector

realistic reconstruction algorithms

full SM backgrounds

tau lepton reconstruction

→ precision vertex detector

→ PFA calorimeter

The CP even-odd mixing angle of  $\tau^+\tau^-$  from Higgs decay  
can be determined to  $75 \text{ mrad} \approx 4.3^\circ$  at ILC250

Scope for further improvement:

better tau reconstruction, polarimeter reco., BG suppression,  
additional tau decay modes, systematic controls...

*end*

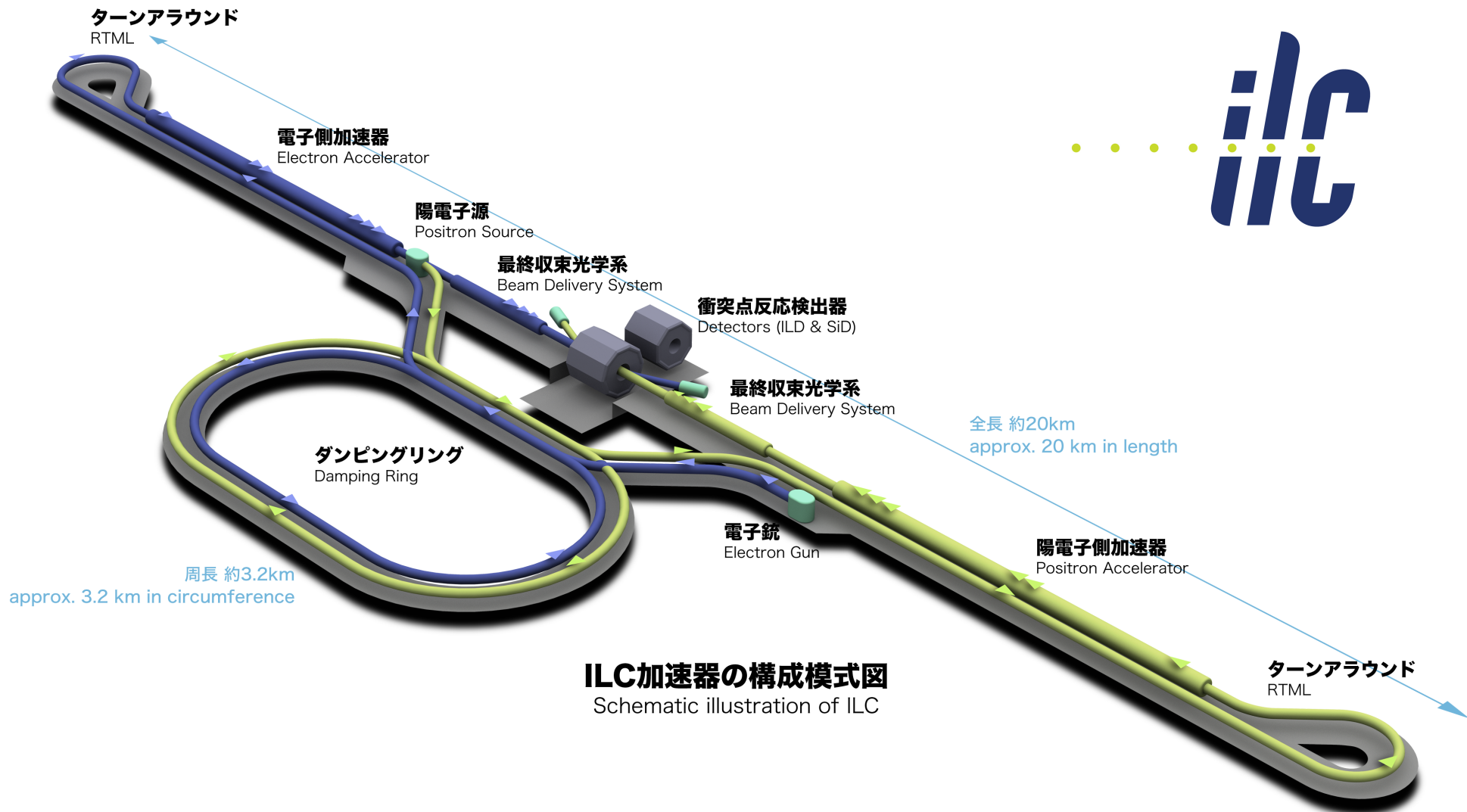
backup

The Higgs boson presents us a  
once-in-a-generation opportunity to  
study properties of a  
new type of particle

- (HL-)LHC
- electron-positron Higgs factory
- muon collider, ...

almost all models of new physics at  $\sim$ TeV scale  
leave an imprint on Higgs boson properties  
O(few-%) deviations from SM (eg for decay branching ratios)  
→ O(%) or better precision desired





initial centre-of-mass energy  
upgrade energy

250 GeV : 2/ab in first ~11 years  
>1000 GeV possible

electron (positron) beam polarisation

80% (30%)

political status

under consideration by Japanese govt.  
as host of an international project

TABLE II. Selection cuts [see text for details; (energies, momenta, and masses) in GeV/c<sup>(0,1,2)</sup>], signal selection efficiencies  $\epsilon$  (in %), and number of expected background events (BG) at various stages of the selection in the three selection channels  $e, \mu, q$ . Event numbers are scaled to the 2 ab<sup>-1</sup> of 250 GeV data of the “H20-staged” running scenario.

event property	leptonic preselection			hadronic preselection				
	requirement	$\epsilon_e$	$\epsilon_\mu$	BG <sub>lep</sub>	requirement	$\epsilon_q$	BG <sub>had</sub>	
		100	100	142 M		100	142 M	
chg. PFOs	4 $\rightarrow$ 7	91	93	10.1 M	$\geq 8$	98	95.7 M	
$Z \rightarrow ll$ candidate	$\geq 1$	88	90	1.03 M				
isolated prongs					$\geq 2$	91	45.8 M	
opp. chgd. prongs		84	87	903 k		84	33.5 M	
min. prong score					$> 0.8$	77	14.5 M	
impact par. error	$< 25\mu m$	76	79	491 k	$< 25\mu m$	74	13.2 M	
extra cone energy		72	75	438 k				
$m_Z$					60 $\rightarrow$ 160	72	5.58 M	
$m_{\text{recoil}}$					50 $\rightarrow$ 160	71	4.90 M	
$\tau$ decay mode		63	65	236 k		64	1.99 M	
full selection		$Z \rightarrow ee$		$Z \rightarrow \mu\mu$		$Z \rightarrow qq$		
event property	requirement	$\epsilon_e$	BG <sub>e</sub>	$\epsilon_\mu$	BG <sub><math>\mu</math></sub>	requirement	$\epsilon_q$	BG <sub>q</sub>
good $\tau^+\tau^-$ fit		57	112 k	59	99.5 k		58	1.64 M
$m_{\tau\tau}$	100 $\rightarrow$ 140	46	618	52	366	100 $\rightarrow$ 140	42	43.5 k
event $p_T$	$< 5$	43	309	50	268	$< 20$	42	31.6 k
$m_{\text{recoil}}$	$> 120$	42	252	50	162	$> 100$	41	23.5 k
$m_Z$	80 $\rightarrow$ 105	41	186	49	136	80 $\rightarrow$ 115	38	6.93 k
$ \cos\theta_Z $	$< 0.96$	40	168	47	124	$< 0.96$	37	6.22 k
event $p_z$	$< 40$	40	144	47	105	$< 40$	37	5.26 k
$ \cos\theta_P _{\text{min}}$	$< 0.95$	40	140	47	102	$< 0.95$	37	5.26 k
Sample purity (%)		19		26		11		

amplitude of modulation in  $\Delta\phi$  varies from event to event, depending on  $\theta^\pm$ , according to the contrast function:

$$c(\theta^+, \theta^-) \equiv \sin \theta^+ \sin \theta^- / (1 + \cos \theta^+ \cos \theta^-)$$

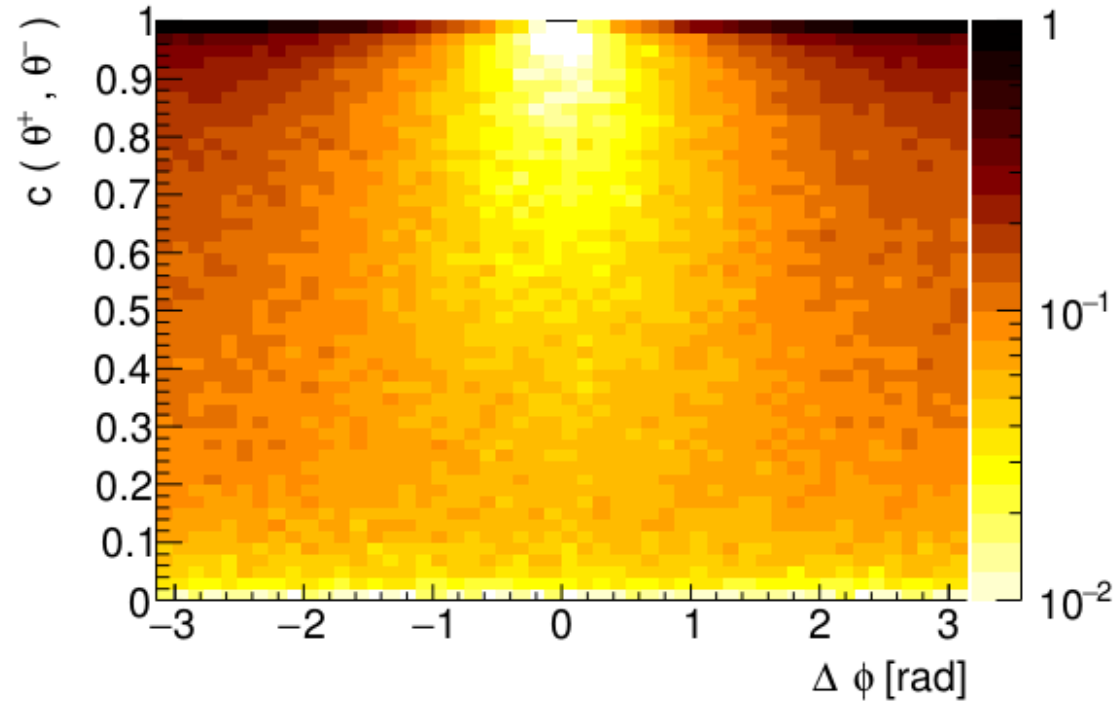
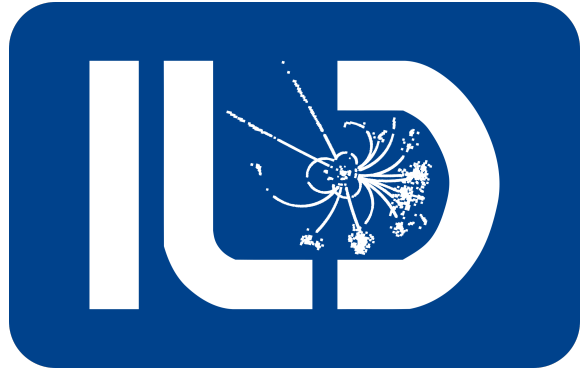
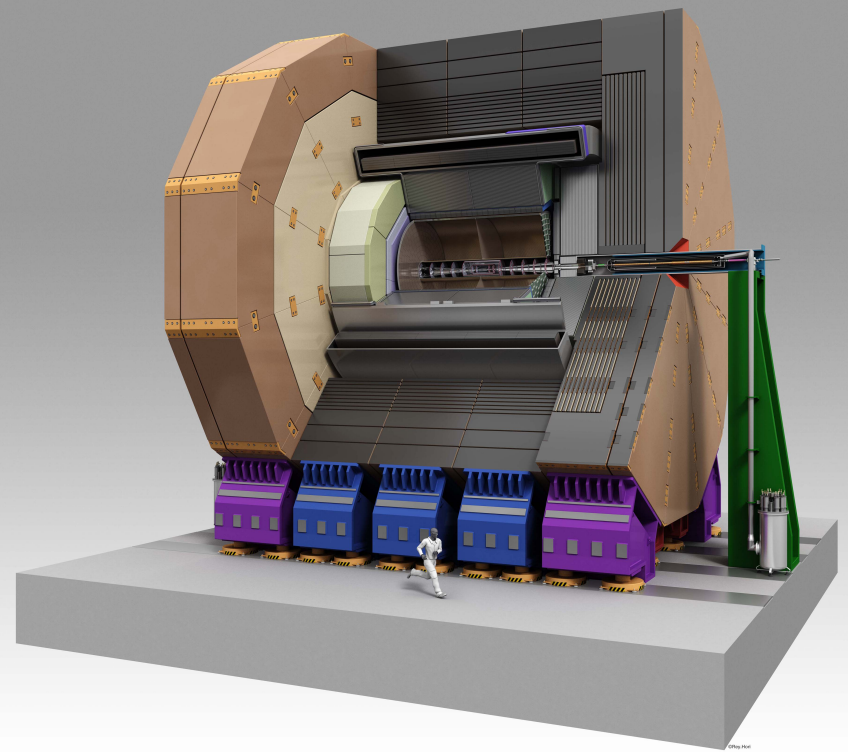


FIG. 3. Two-dimensional distribution of events in  $\Delta\phi$  and  $c(\theta^+, \theta^-)$  at MC truth level, for the case  $\psi_{\text{CP}} = 0$ .



## *International Large Detector*

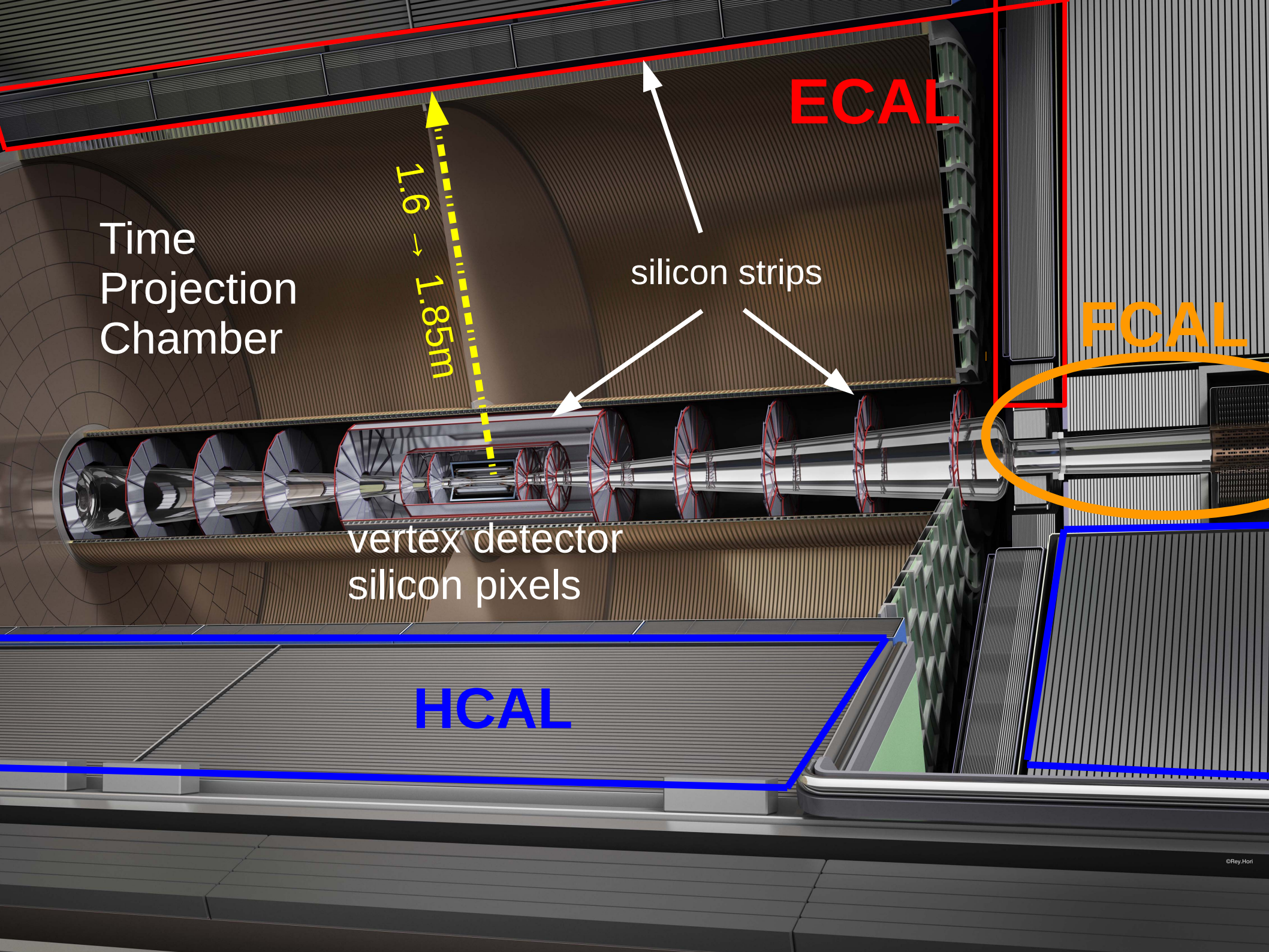


One of two detector designs being studied for the ILC

## **Design principles**

- excellent vertexing: identification of  $b$ ,  $c$ ,  $\tau$ 
  - high precision and lightweight vertex detector
- highly efficient and precise charged particle tracking
  - large TPC in  $\sim 3.5$  T field
- excellent jet energy resolution
  - make best use of dominant hadronic decays of  $W$ ,  $Z$ ,  $H$
- highly granular calorimeters





Time  
Projection  
Chamber

1.6 → 1.85m

ECAL

silicon strips

FCAL

vertex detector  
silicon pixels

HCAL

## Neural Network Details

Variables for ZH / 4f separation (NN1):

1. tau tau invariant mass
2. event energy
3. invariant mass of the Z
4. recoil mass to the Z
5. tau+ cone ( $\pm 20^\circ$ ) excess energy
6. tau- cone excess energy

Variables for distinguishing ZH events from signal tau decay modes from other tau decay modes (NN2):

1. tau+ cone excess energy
2. tau- cone excess energy
3. tau+ visible mass
4. tau- visible mass

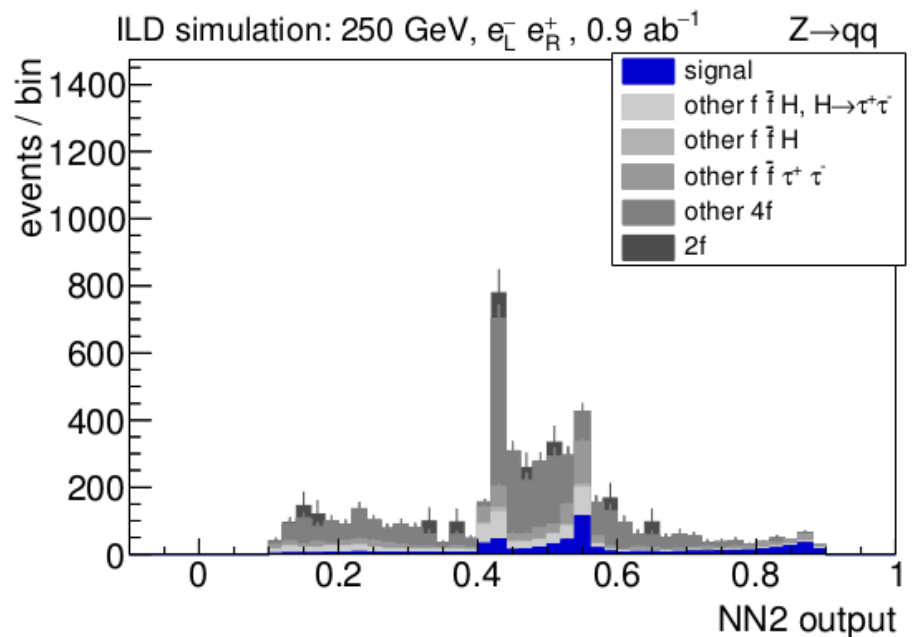
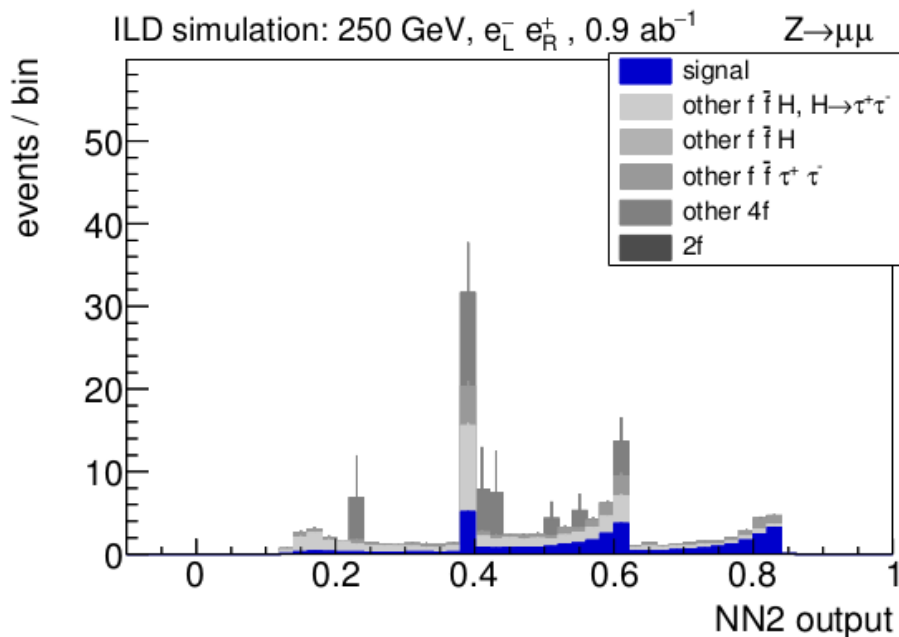
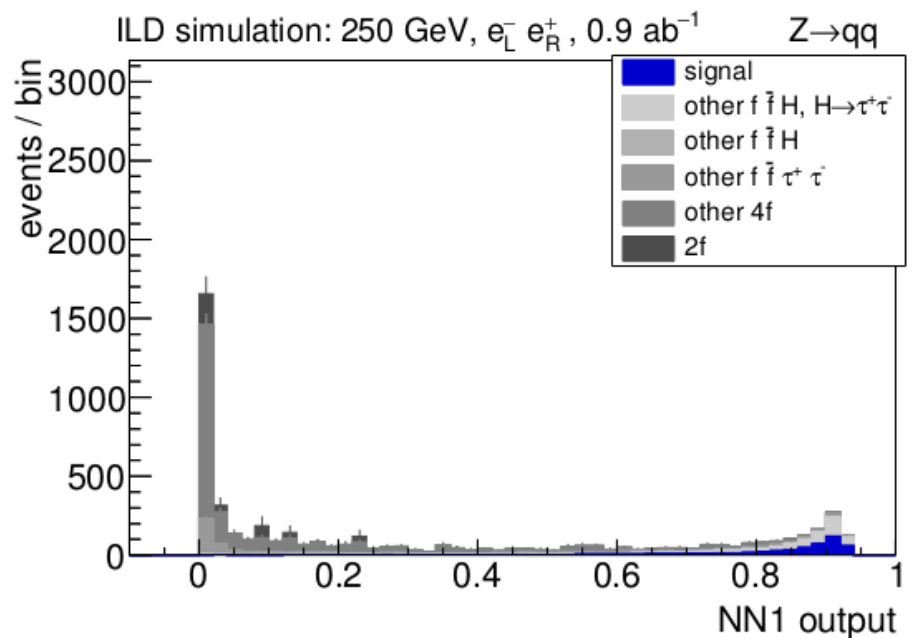
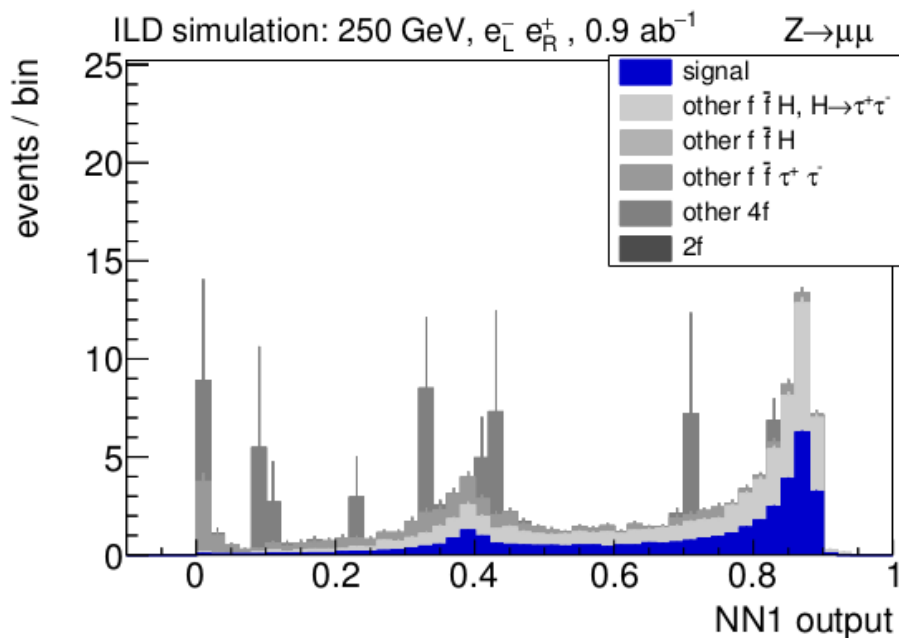


FIG. 7. Distributions of the two Neural Network outputs in the muon and hadronic selection channels. The structure in the output of NN2 is due to the three different combinations of  $\tau$  lepton decay modes. Distributions are normalized to  $0.9 \text{ ab}^{-1}$  of data in the  $e_L^- e_R^+$  beam polarization.