



# CERN

European Organization for Nuclear Research  
Organisation Européenne pour la Recherche Nucléaire

# Fisica delle particelle oggi

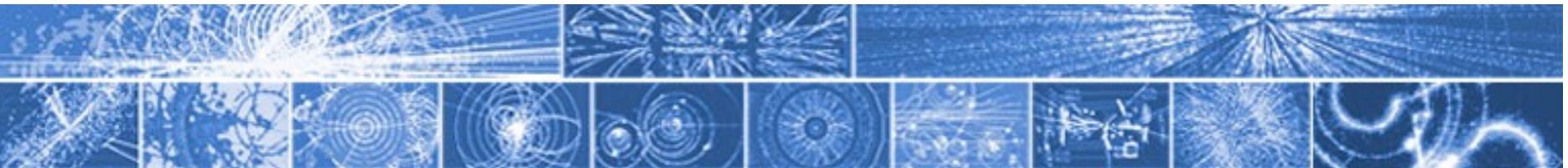
## Il Modello Standard

## and Beyond

- Bosone di Higgs
- SuperSimmetria
- Astroparticle & Materia Oscura

Marco CIRELLI [CNRS LPTHE Jussieu & Sorbonne]

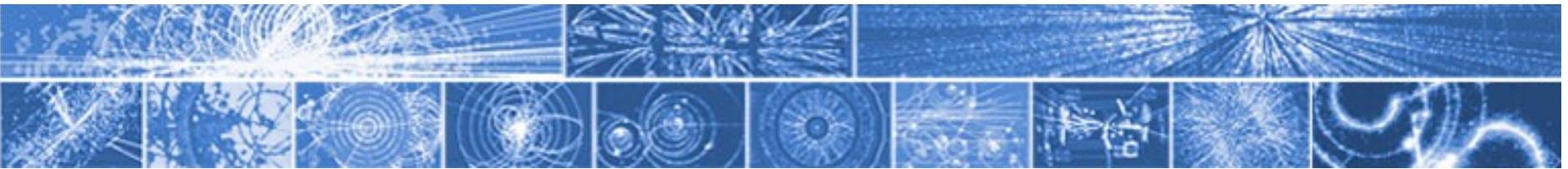
**Mini-intro:**  
- livello variabile  
- non storico  
- about MC



## Cosa si fa al CERN

### Ricerca fondamentale in Fisica delle Particelle

- i costituenti elementari della materia
- le forze fondamentali che li governano
- l'origine, il contenuto e la struttura dell'Universo



## Come risolvere questi problemi? o... Come si fanno le scoperte?

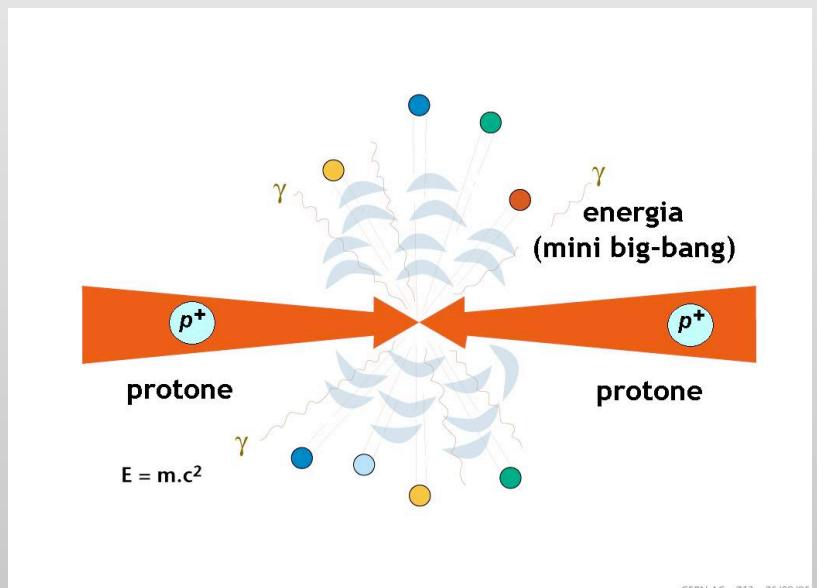
Accelerare le particelle elementari (*protoni, elettroni...*)

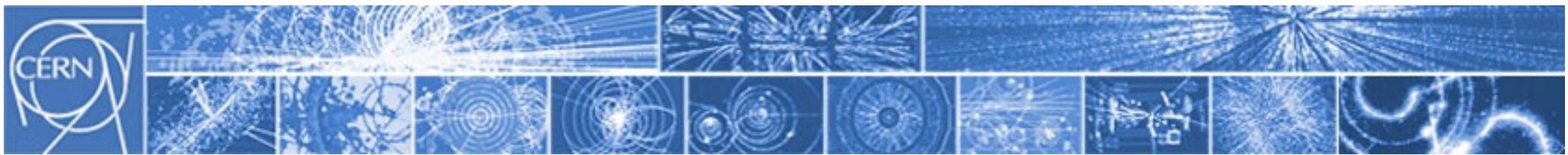
fino a energie elevatissime (14 TeV)

e portarle a collidere.  $E=mc^2$

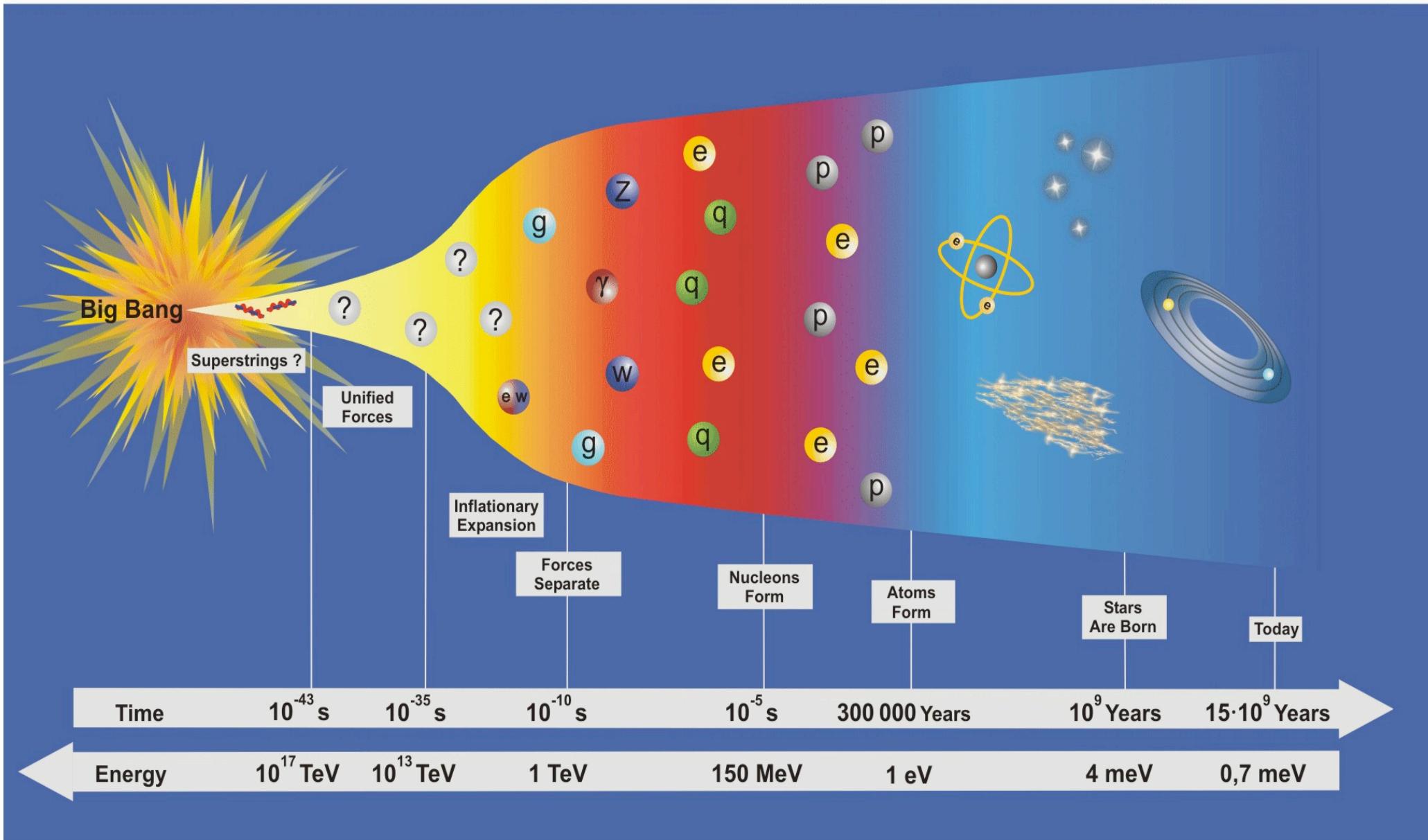
Analizzare accuratamente i prodotti

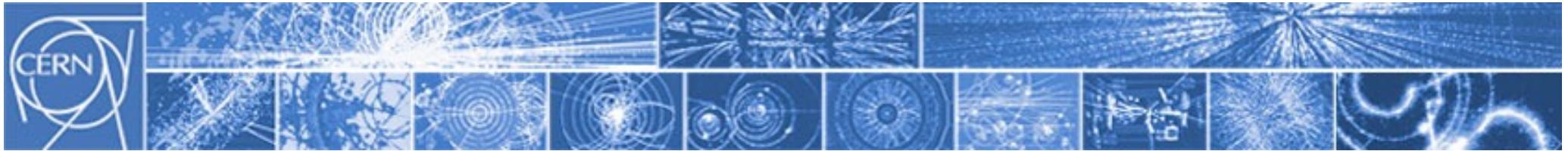
per scoprire nuove particelle,  
nuove forze,  
'nuova fisica'...





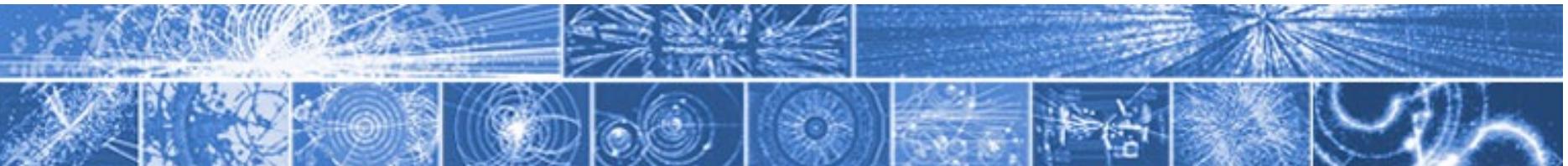
# Ripercorrere all'indietro la storia dell'Universo





# Modello Standard

(della fisica delle particelle elementari)



Il Modello Standard è la costruzione ('scoperta') fondamentale della fisica delle particelle, nella seconda metà del XX secolo.

**XIX secolo** elettromagnetismo

**1932** teoria di Fermi del decadimento beta - interazioni deboli

**1960's** unificazione em-debole: teoria ElectroWeak  
(Glashow, Weinberg, Salam)

**1981** scoperta bosoni W e Z (Rubbia)

**1970's** teoria della QCD - interazioni nucleari forti  
(Gross, Politzer, Wilczek)

1936  $\mu$

1956  $\nu_e$

1962  $\nu_\mu$

1974  $\tau$

2000  $\nu_\tau$

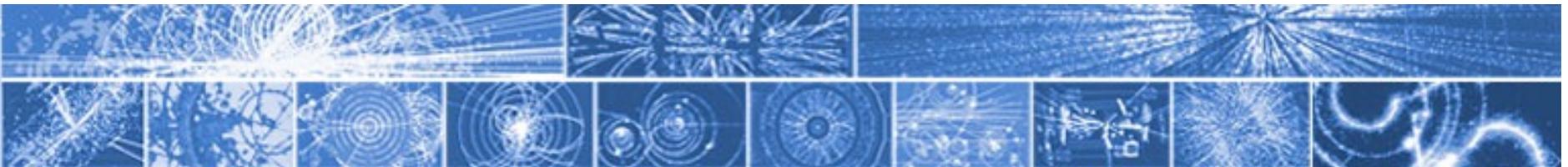
1968  $s$  quark

1974  $c$  quark

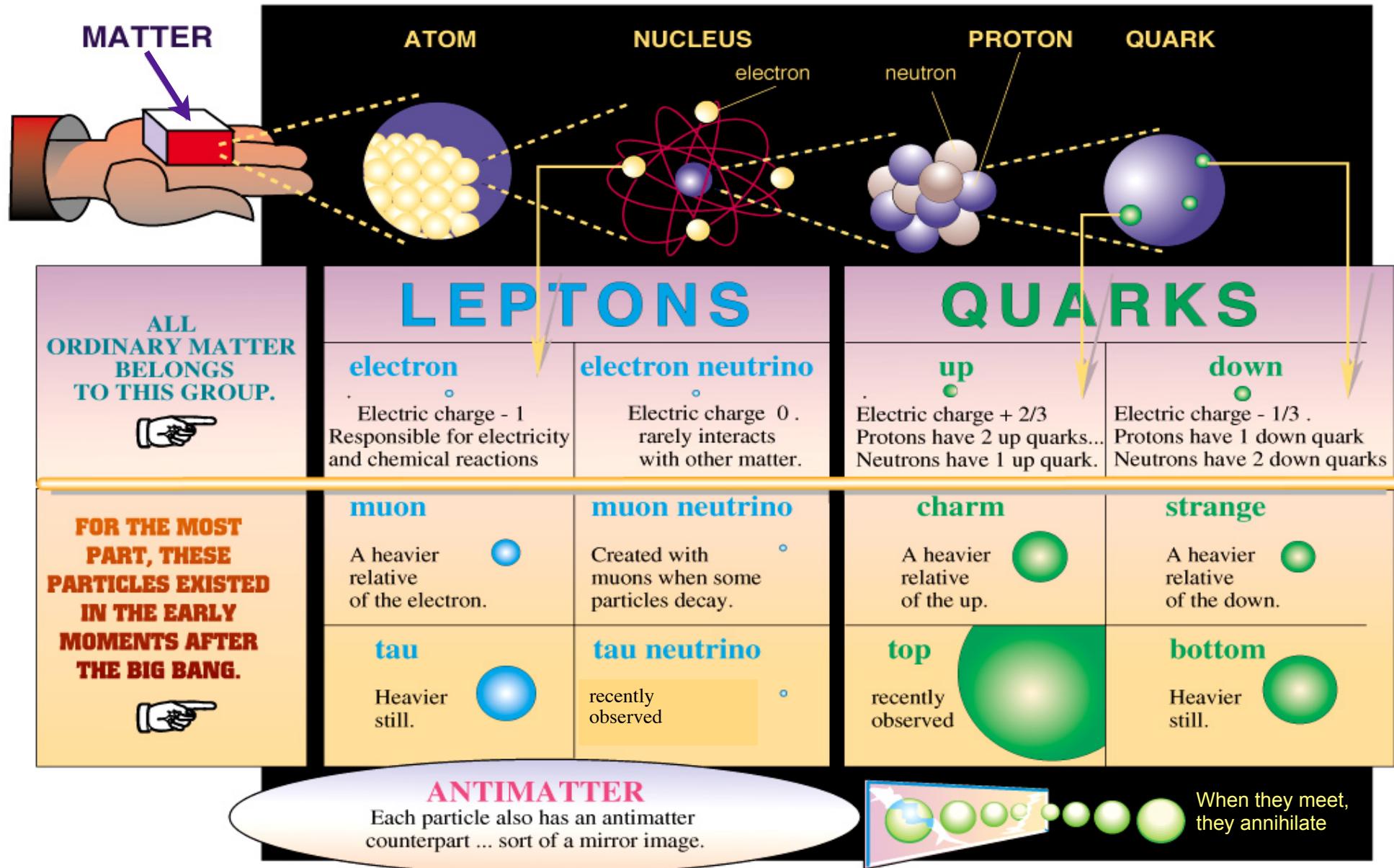
1977  $b$  quark

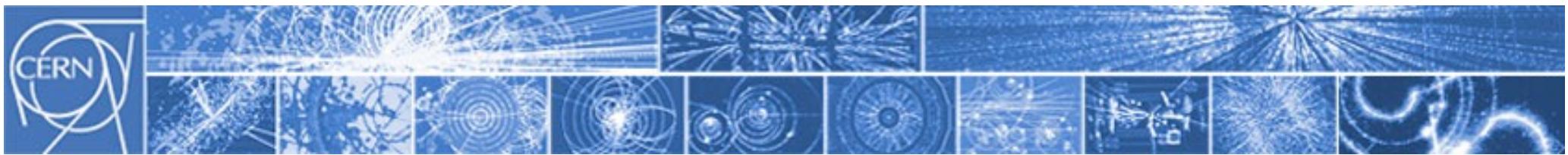
1995  $t$  quark

2012 higgs

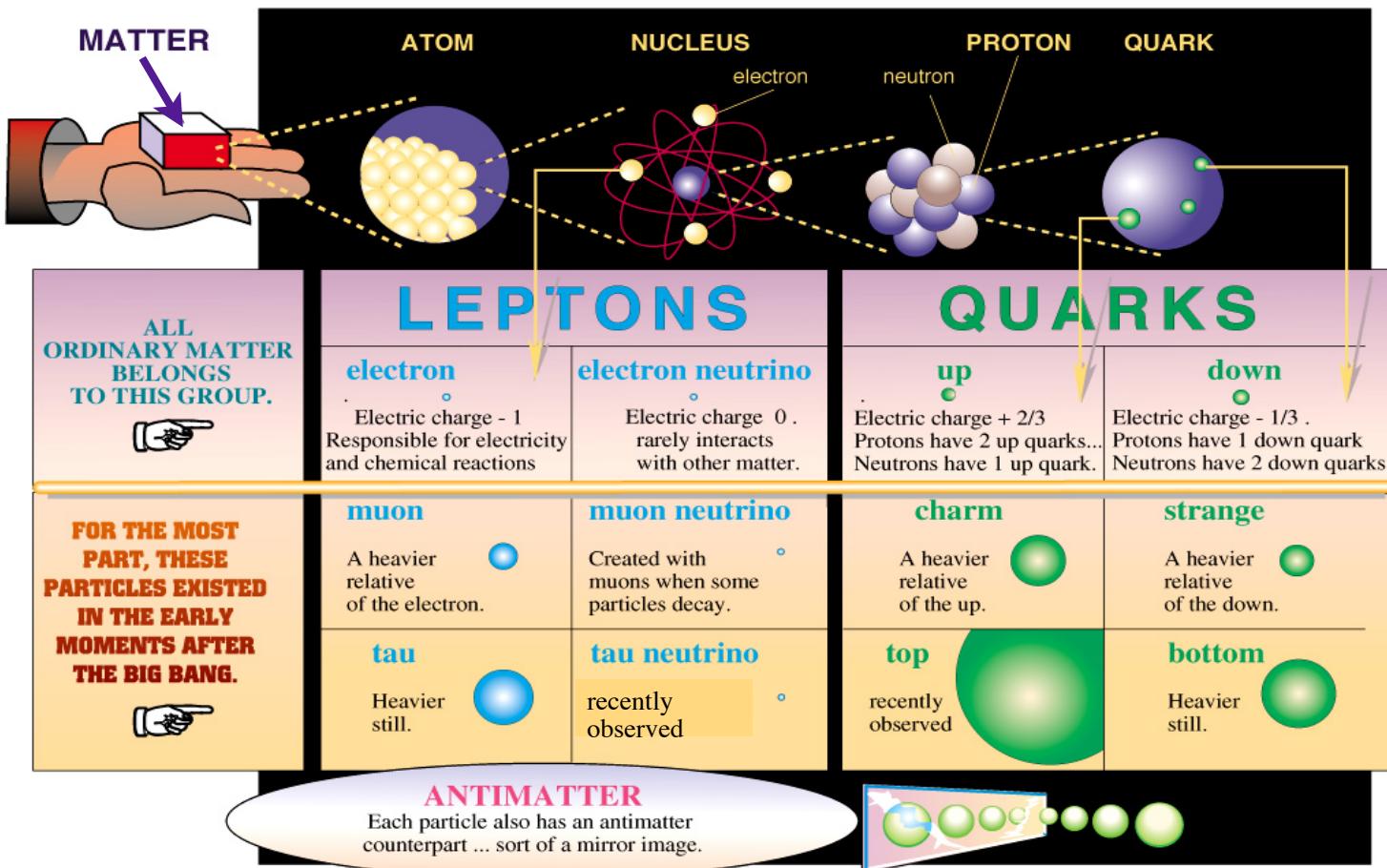


## STANDARD MODEL





## STANDARD MODEL



from Time magazine

## FORCES

### Electromagnetic

Photon



Atoms  
Light  
Chemistry  
Electronics

### Weak

Bosons (W,Z)



Neutron decay  
Beta radioactivity  
Neutrino interactions  
Burning of the sun

### Strong

Gluons (8)



Quarks



Mesons  
Baryons



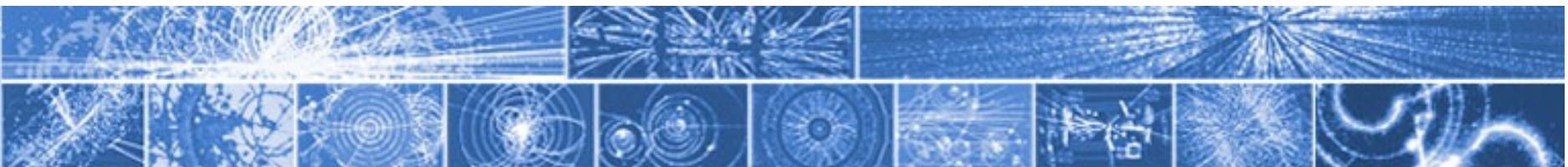
Nuclei

Graviton ?

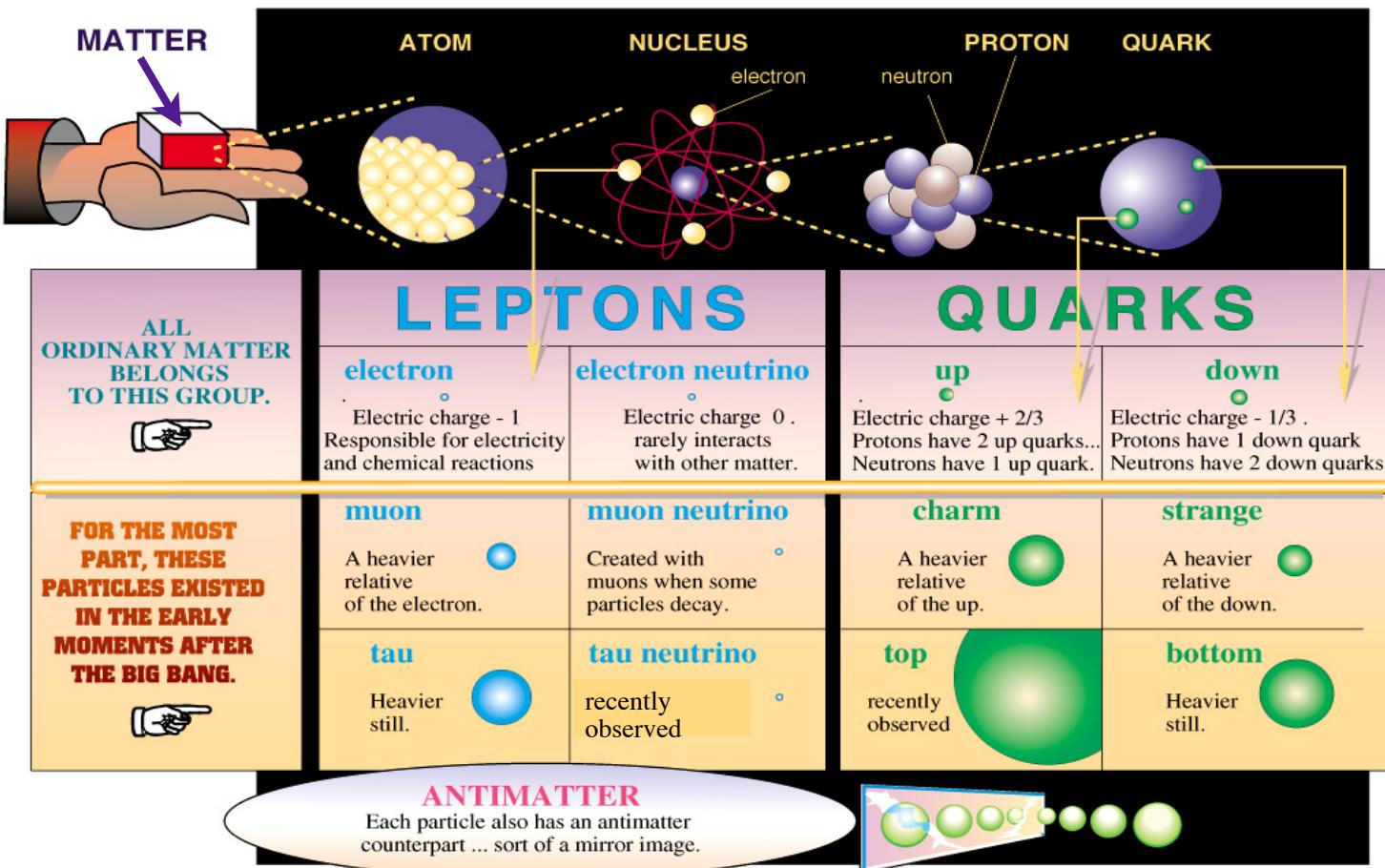


Solar system  
Galaxies  
Black holes





## STANDARD MODEL



## FORCES

### Electromagnetic

Photon



Atoms  
Light  
Chemistry  
Electronics

### Weak

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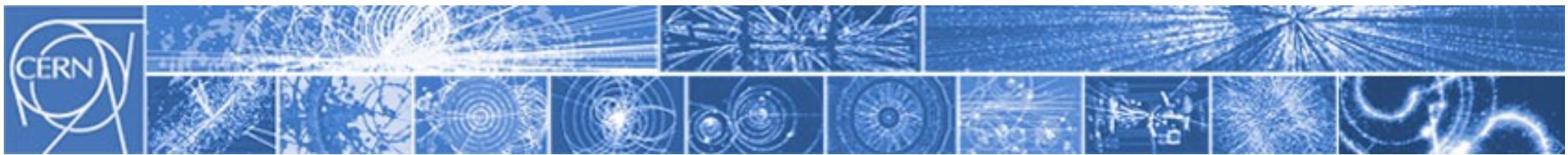
Graviton ?



Solar system  
Galaxies  
Black holes

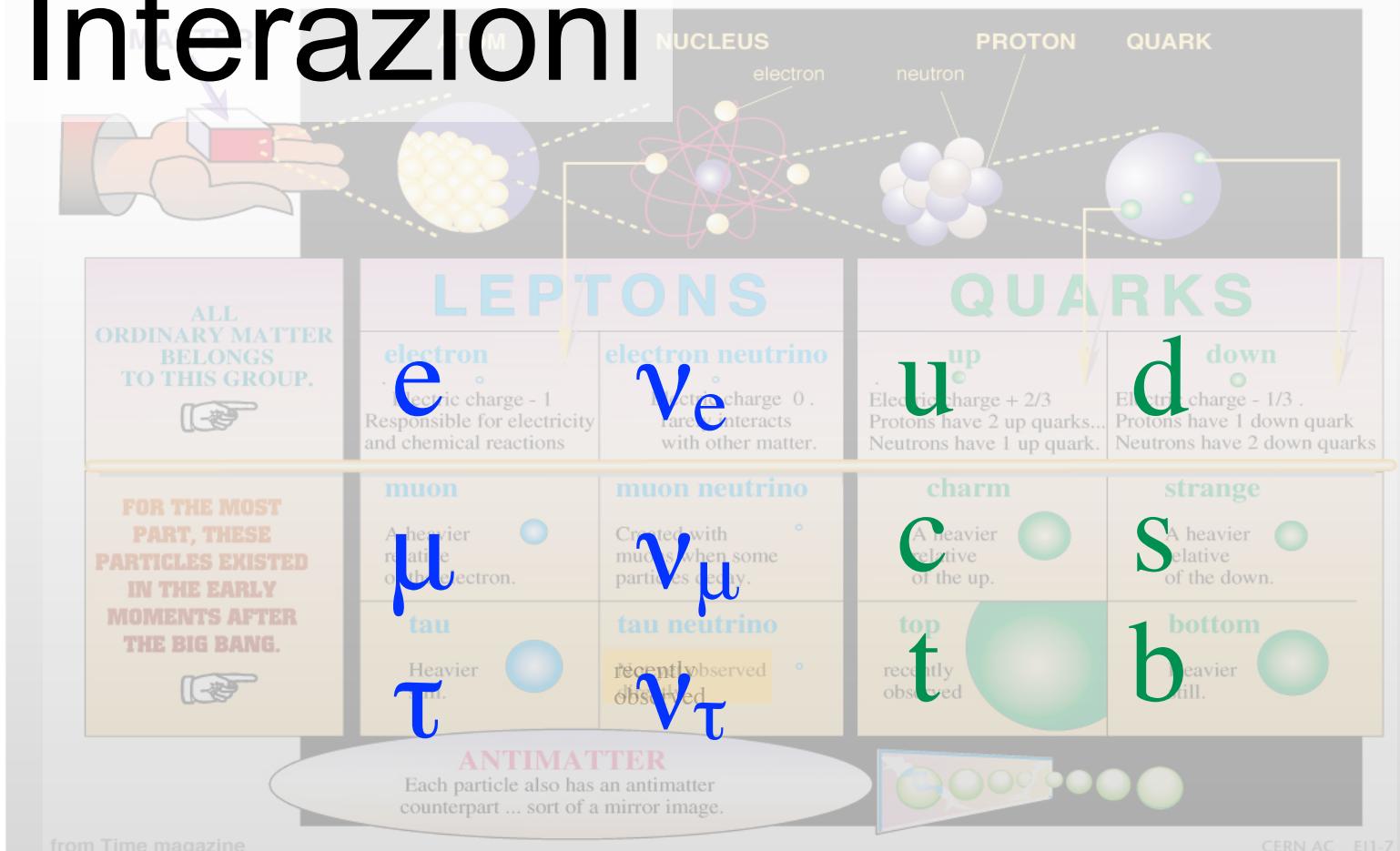
Higgs boson

h

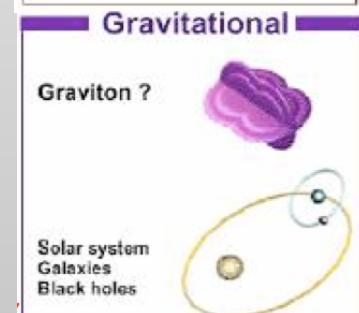
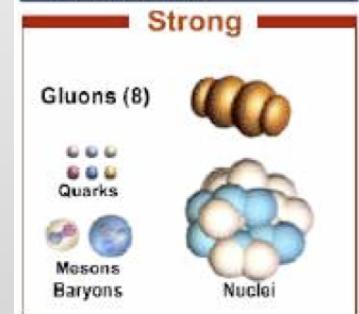
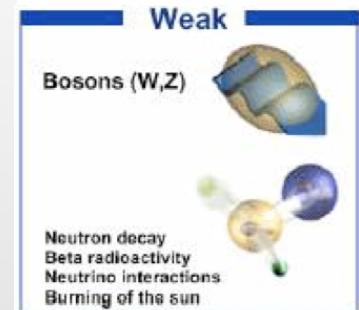
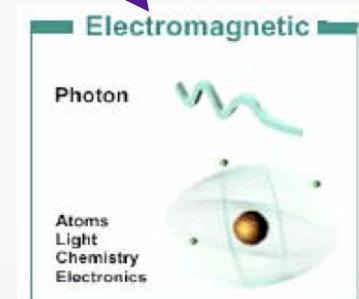


STANDARD MODEL

# Interazioni

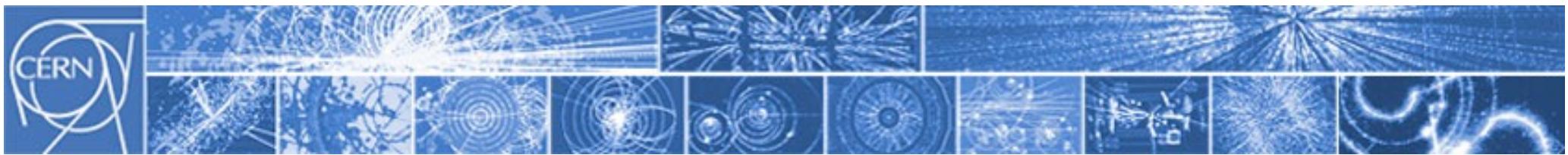


## FORCES



Higgs boson

$h$



STANDARD MODEL

# Interazioni

**ALL ORDINARY MATTER BELONGS TO THIS GROUP.**

**FOR THE MOST PART, THESE PARTICLES EXISTED IN THE EARLY MOMENTS AFTER THE BIG BANG.**

**LEPTONS**

<b>e</b>	<b><math>\nu_e</math></b>
<b>muon</b> A heavier relative of the electron.	<b>muon neutrino</b> Created with muons when some particles decay.
<b><math>\tau</math></b>	<b><math>\nu_\tau</math></b>

**ANTIMATTER**  
Each particle also has an antimatter counterpart ... sort of a mirror image.

**NUCLEUS**  
electron

**PROTON**  
neutron

**QUARK**

**QUARKS**

<b>u<sup>up</sup></b> Electric charge + 2/3 Protons have 2 up quarks... Neutrons have 1 up quark.	<b>d<sup>down</sup></b> Electric charge - 1/3 Protons have 1 down quark Neutrons have 2 down quarks
<b>c<sup>charm</sup></b> A heavier relative of the up.	<b>s<sup>strange</sup></b> A heavier relative of the down.
<b>t<sup>top</sup></b> recently observed	<b>b<sup>bottom</sup></b> heavier still.

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## FORCES

**Electromagnetic**

- Photon
- Atoms
- Light
- Chemistry
- Electronics

**Weak**

- Bosons (W,Z)
- Neutron decay
- Beta radioactivity
- Neutrino interactions
- Burning of the sun

**Strong**

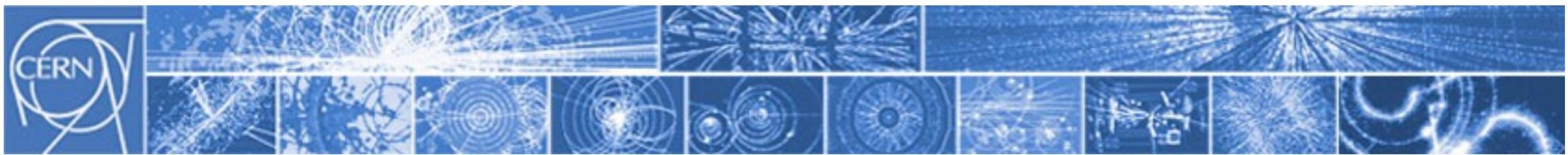
- Gluons (8)
- Quarks
- Mesons
- Baryons
- Nuclei

**Gravitational**

- Graviton ?
- Solar system
- Galaxies
- Black holes

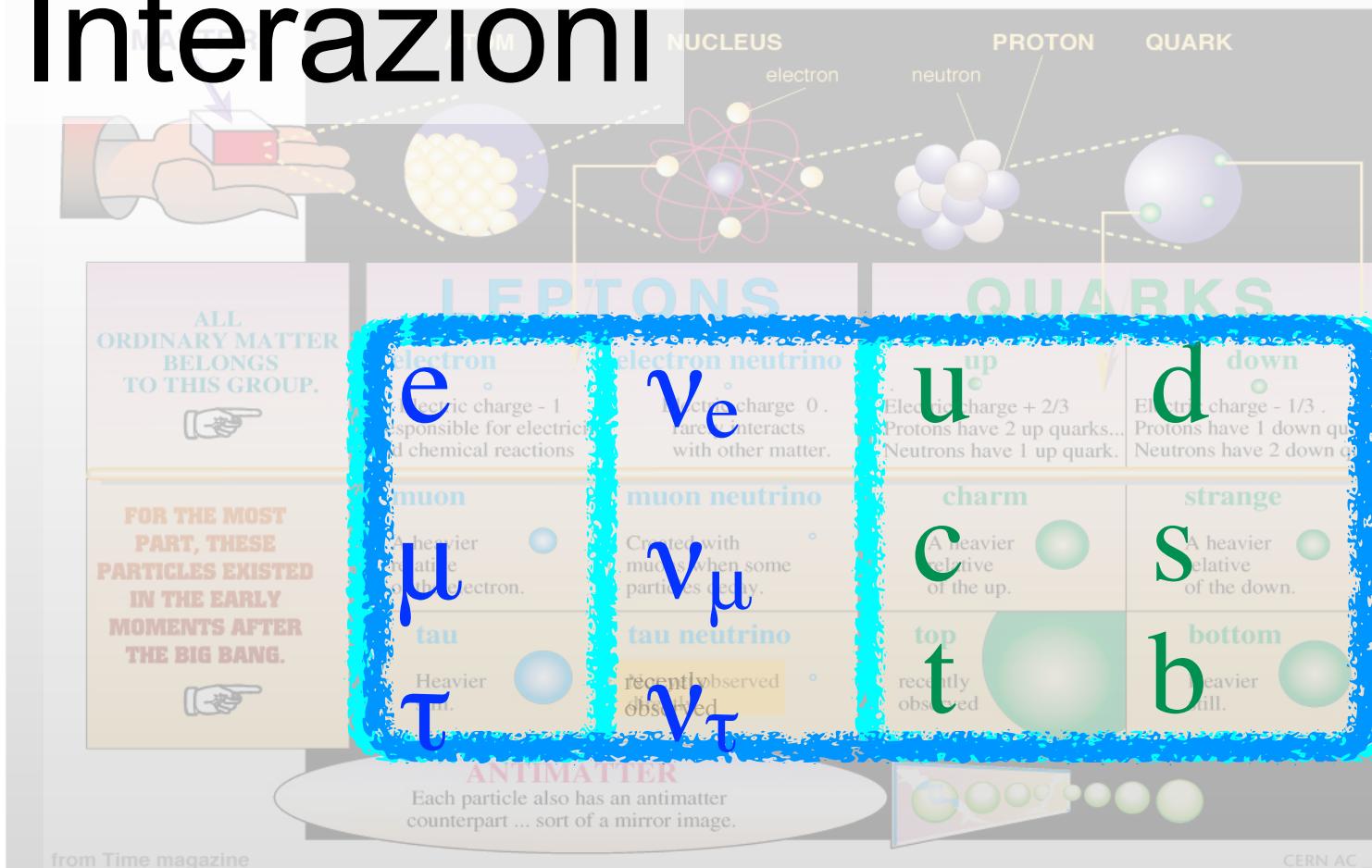
Higgs boson

**h**



STANDARD MODEL

# Interazioni



## FORCES

### Electromagnetic

Photon



### Weak

Bosons (W,Z)



Neutron decay  
Beta radioactivity  
Neutrino interactions  
Burning of the sun

### Strong

Gluons (8)



Quarks



Mesons  
Baryons



Nuclei

### Gravitational

Graviton ?

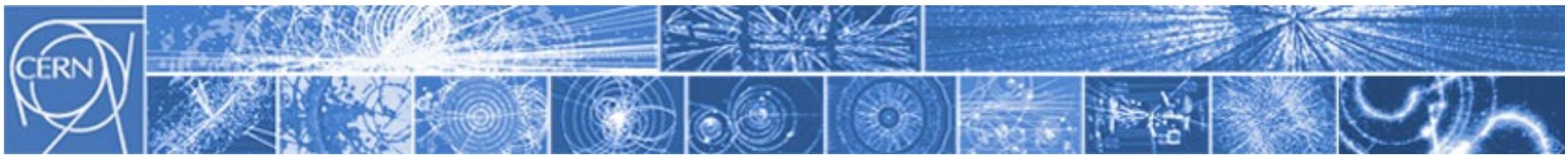


Solar system  
Galaxies  
Black holes



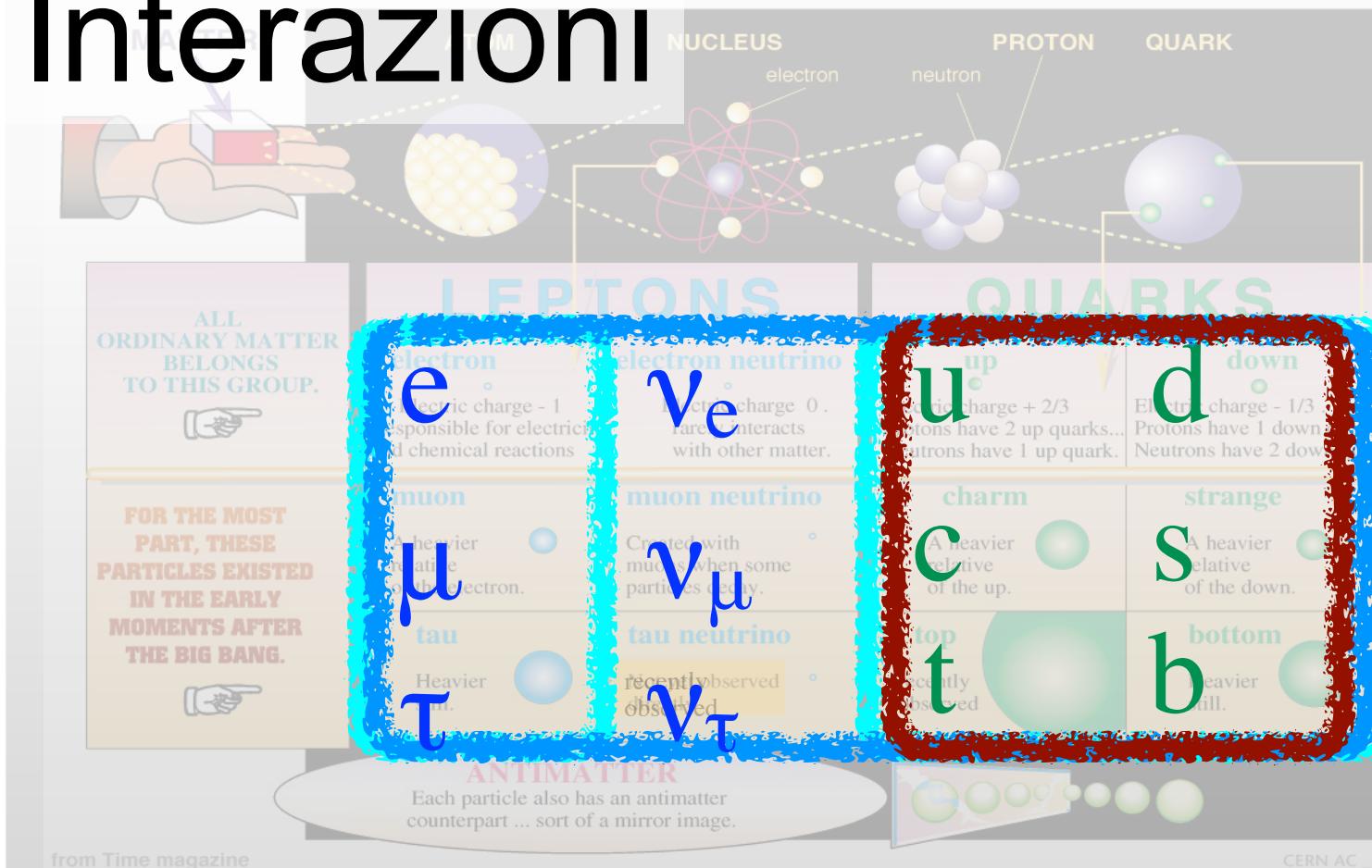
Higgs boson

h

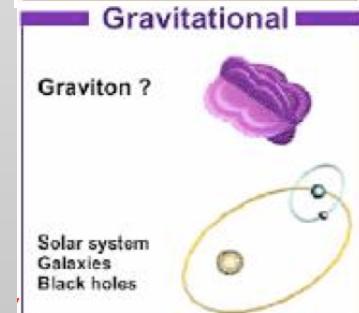
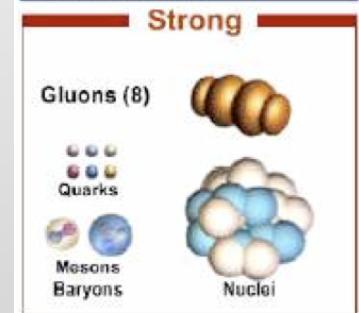
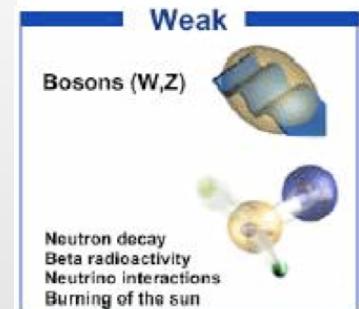
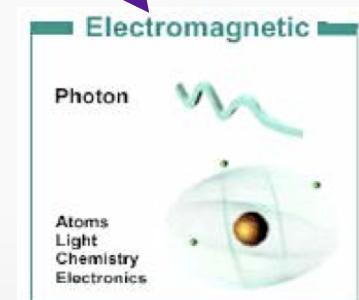


STANDARD MODEL

# Interazioni

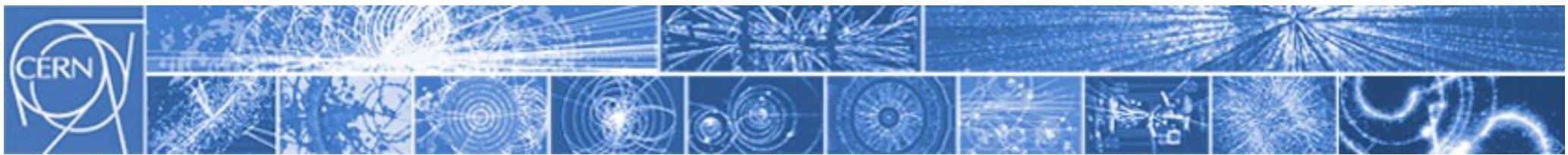


## FORCES



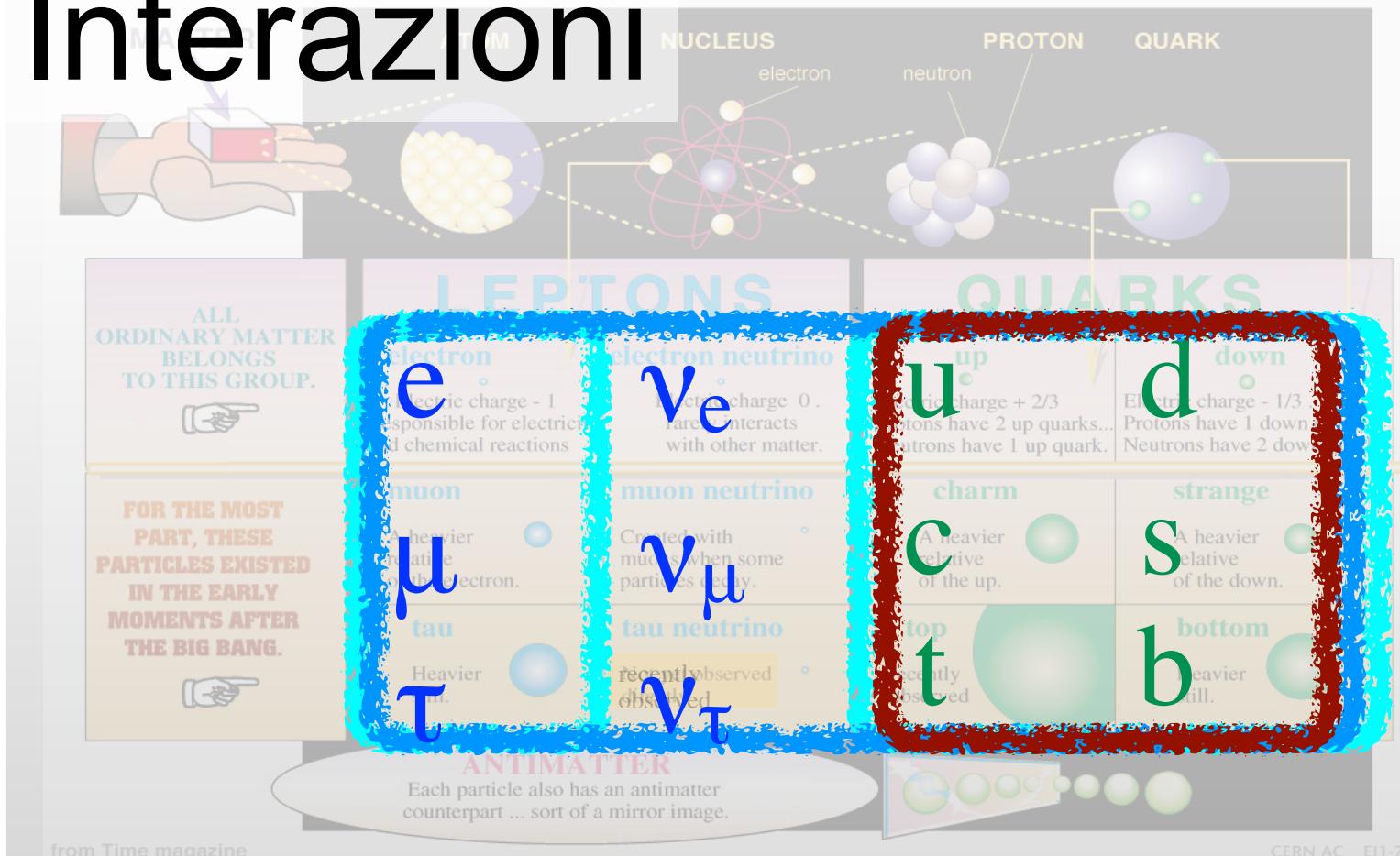
Higgs boson

h



STANDARD MODEL

# Interazioni



FORCES

Electromagnetic



Weak

Bosons (W,Z)

W<sup>+</sup> W<sup>-</sup>

Neutron decay  
Beta radioactive  
Neutrino interaction  
Burning of the sun



Strong

Gluons (8)

g (8)

Gravitational

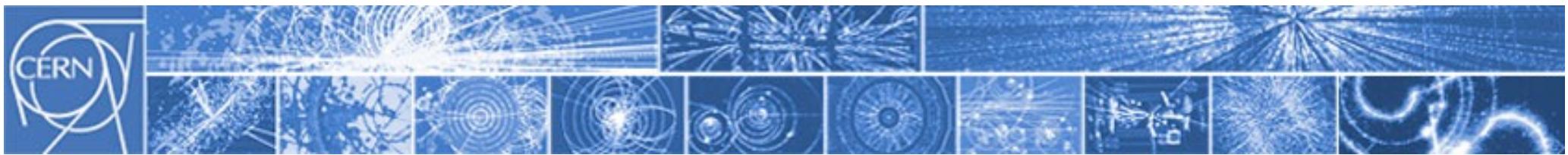
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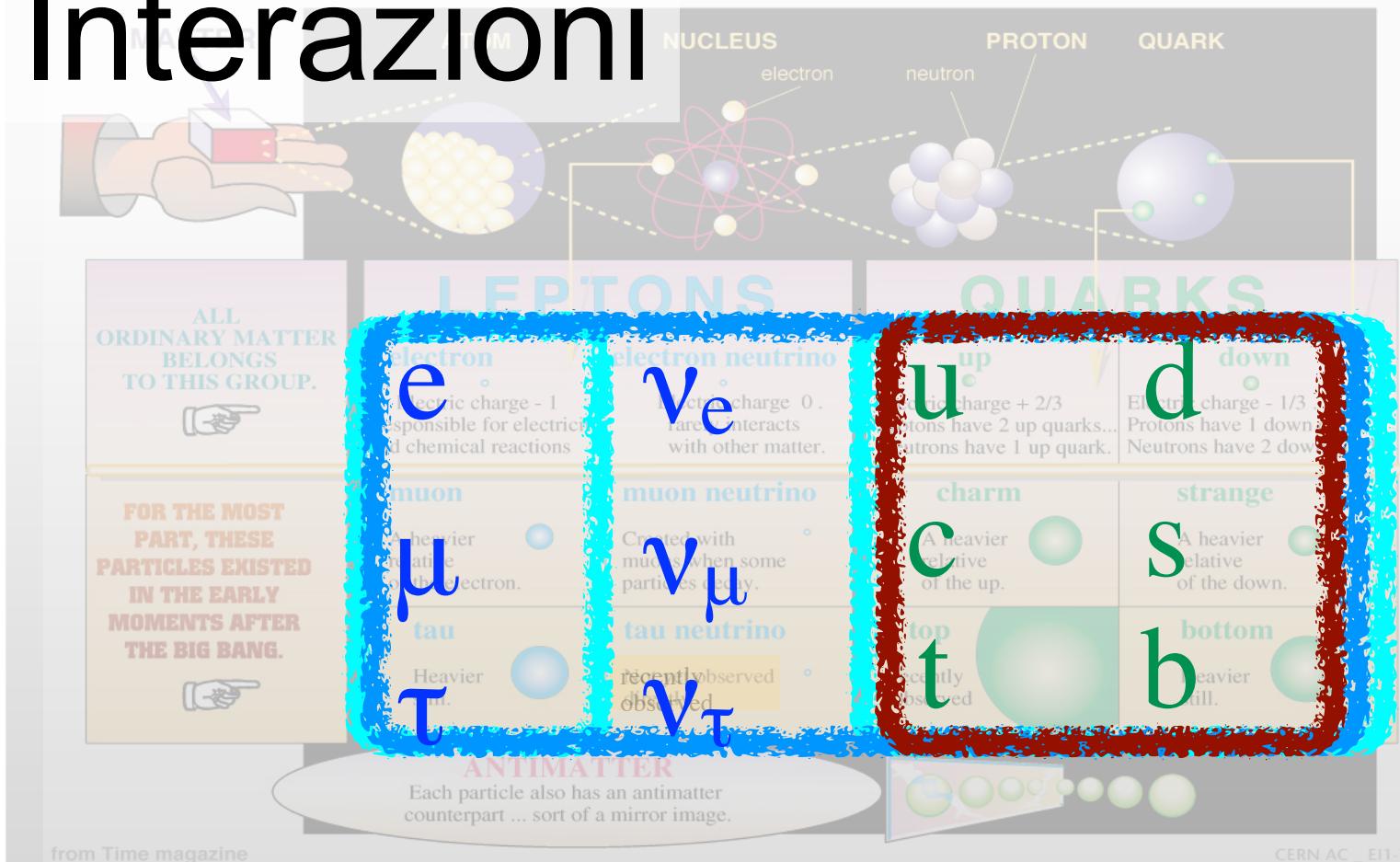
Higgs boson





## STANDARD MODEL

# Interazioni



## FORCES

### Electromagnetic

$\gamma$

### Weak

$W^+$   $W^-$

$Z$

### Strong

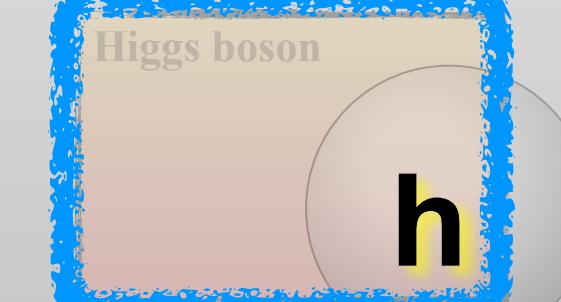
$g$  (8)

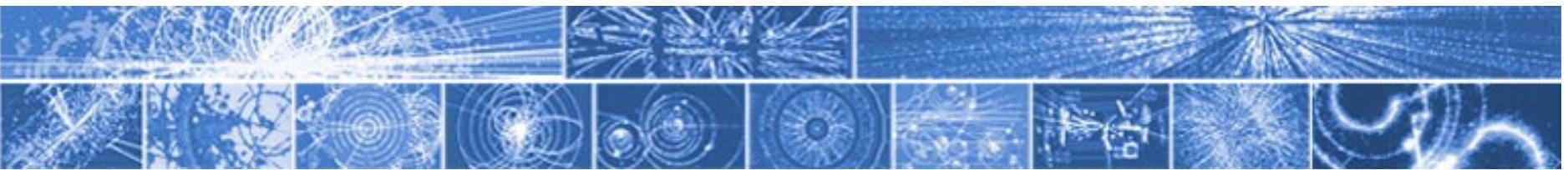
### Gravitational

Graviton ?

$G$

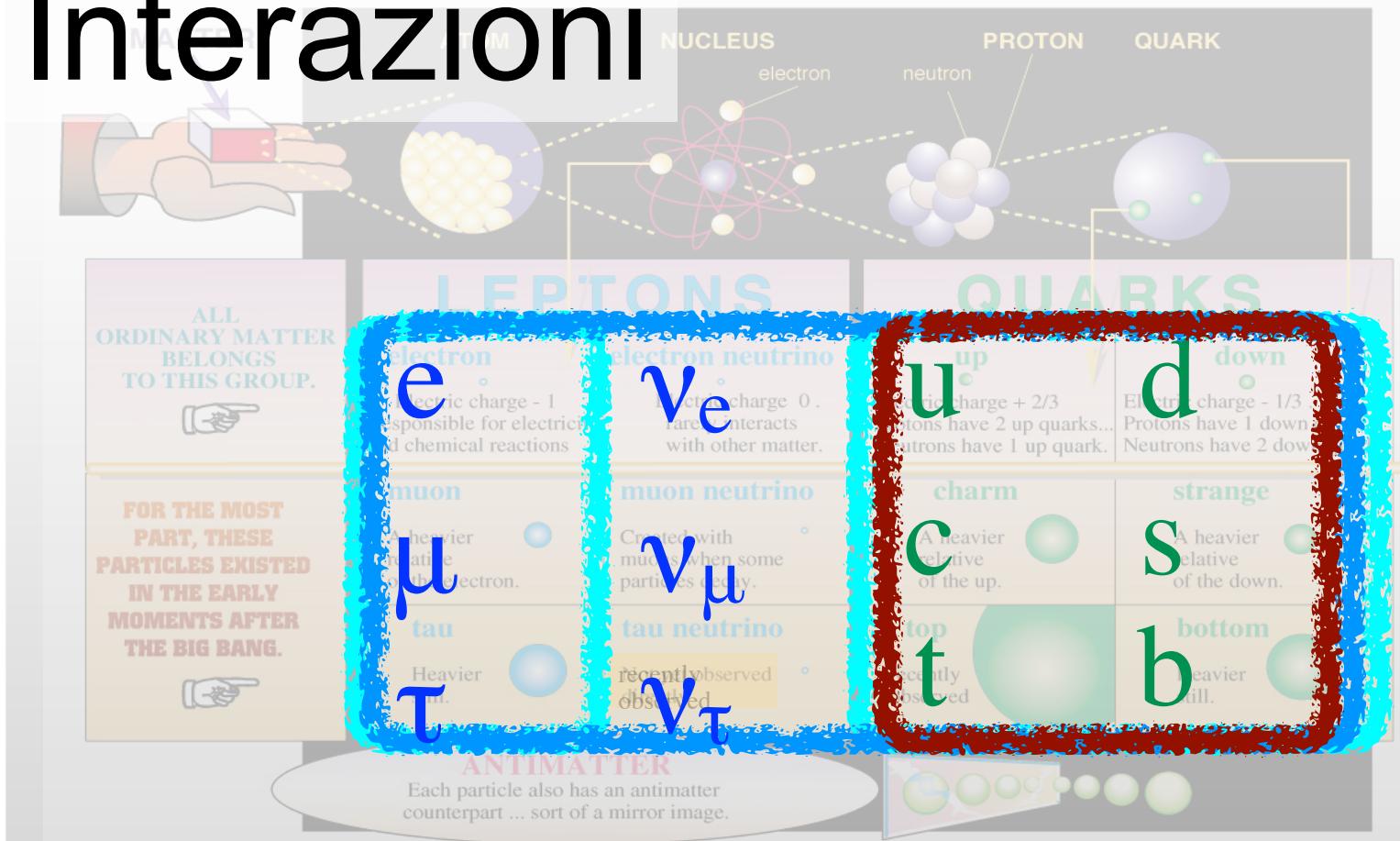
Solar system  
Galaxies  
Black holes



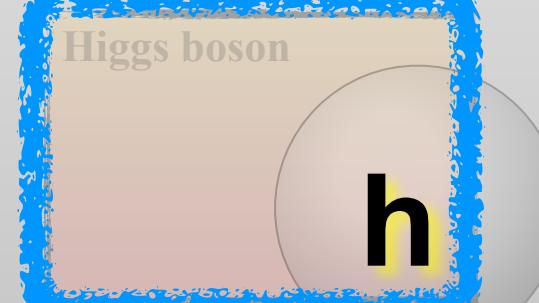
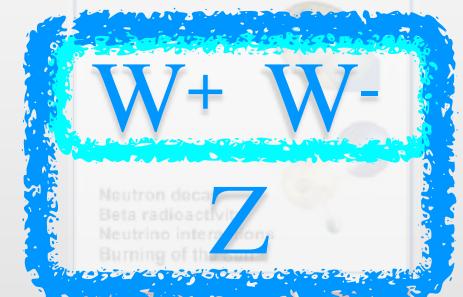
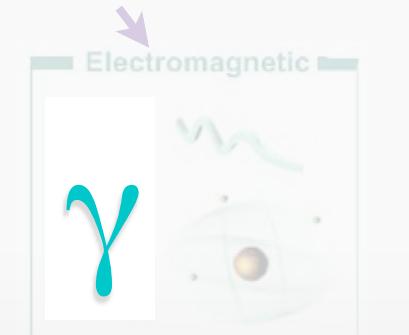


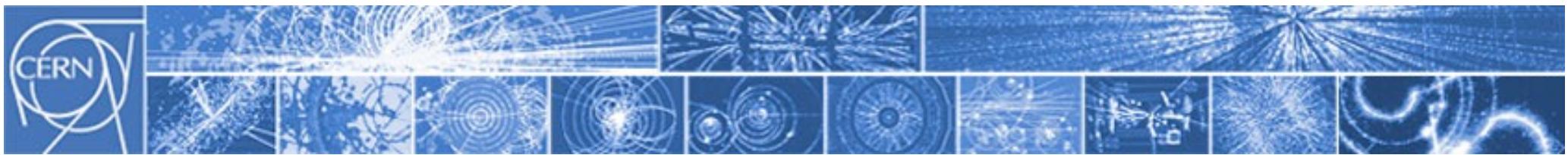
## STANDARD MODEL

# Interazioni



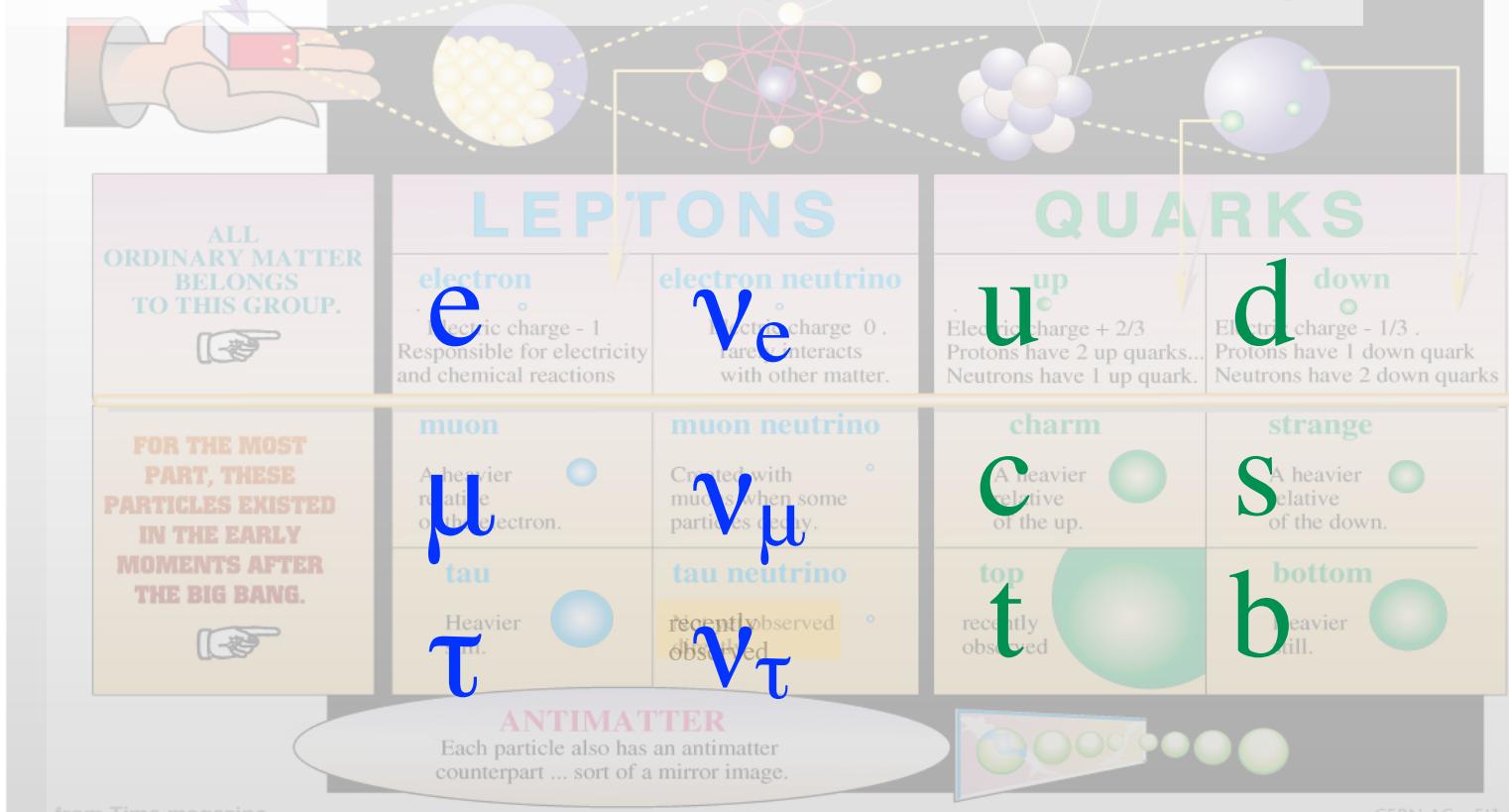
## FORCES



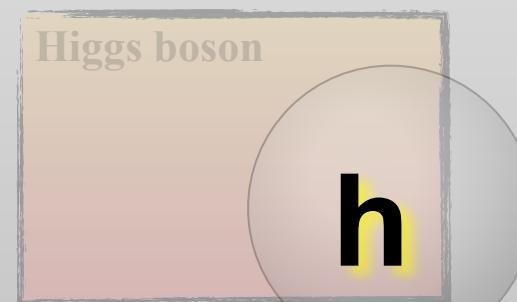


STANDARD MODEL

# Interazioni (& simmetrie)



$$\rightarrow \text{SU}_c(3) \times \text{SU}_w(2) \times \text{U}_Y(1) \rightarrow \text{SU}_c(3) \times \text{U}_{\text{em}}(1)$$



FORCES

Electromagnetic



Weak

Bosons ( $W, Z$ )

$W^+$   $W^-$



Strong

Gluons (8)

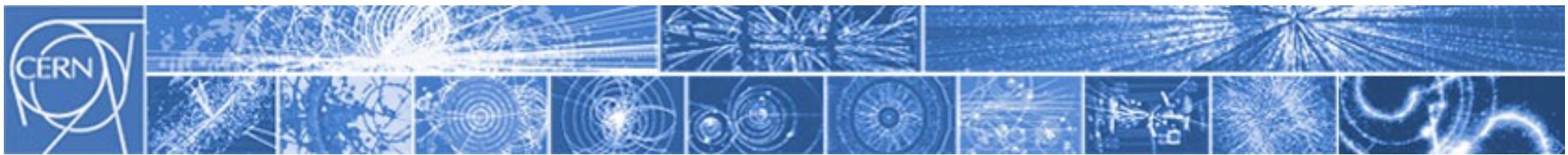
$g$  (8)

Gravitational

Graviton ?

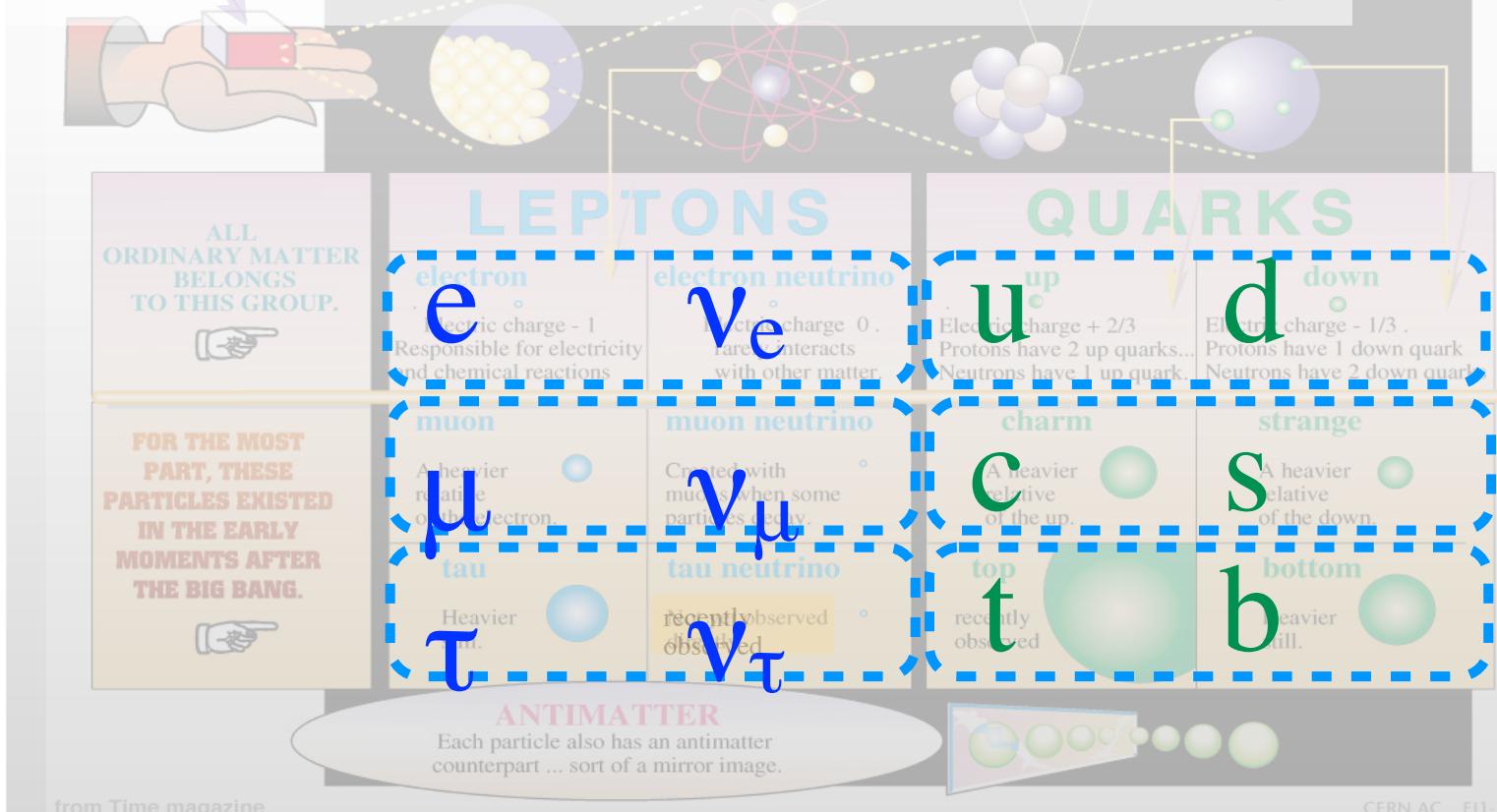
$G$

Solar system  
Galaxies  
Black holes

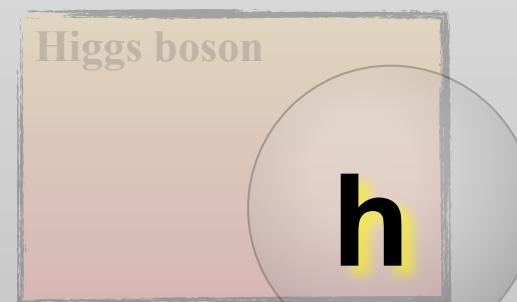


STANDARD MODEL

# Interazioni (& simmetrie)



$$\rightarrow \text{SU}_c(3) \times \text{SU}_w(2) \times \text{U}_Y(1) \rightarrow \text{SU}_c(3) \times \text{U}_{\text{em}}(1)$$



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**g** (8)

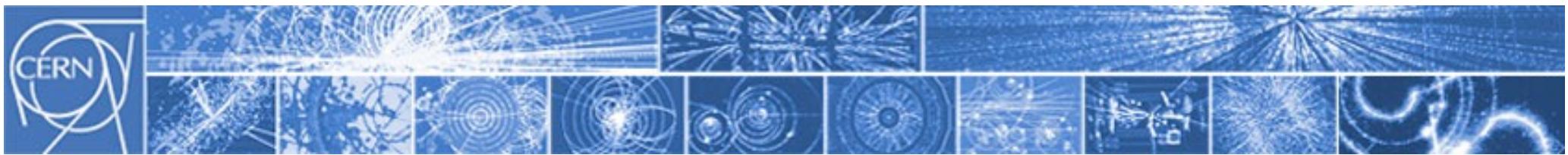
Nuclei

Gravitational

Graviton ?

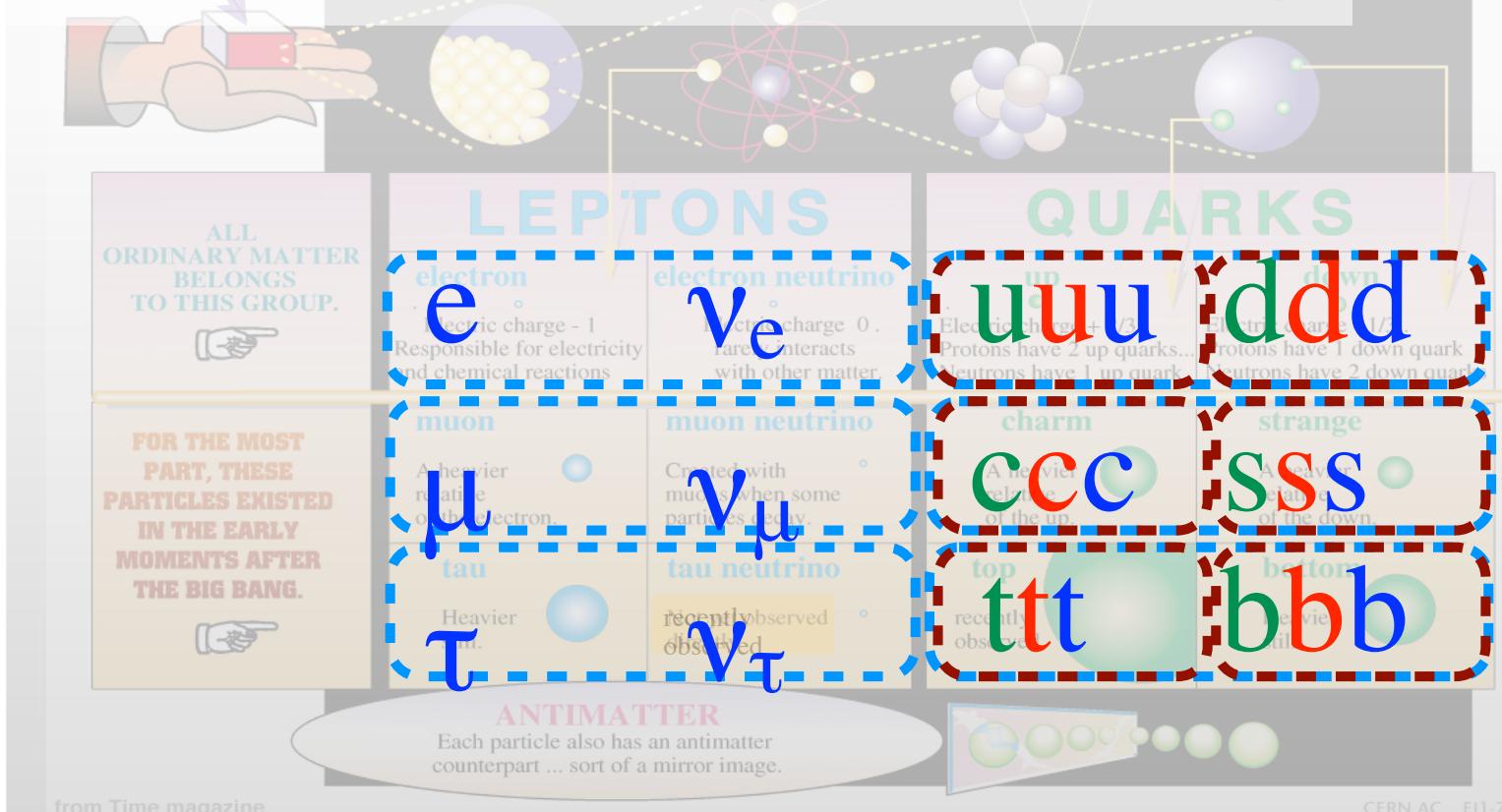


Solar system  
Galaxies  
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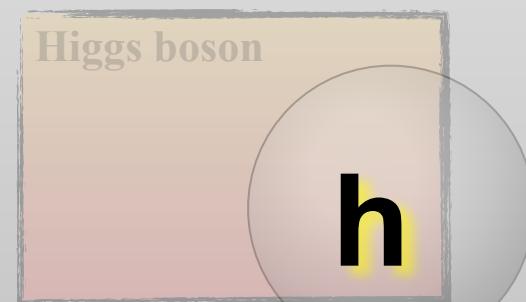


STANDARD MODEL

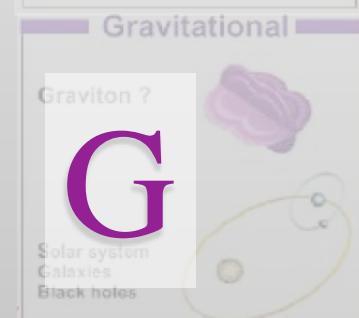
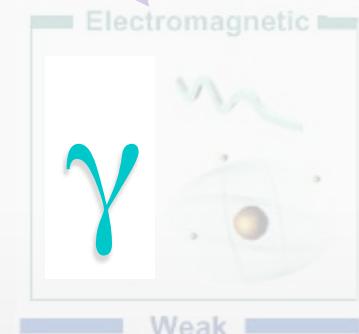
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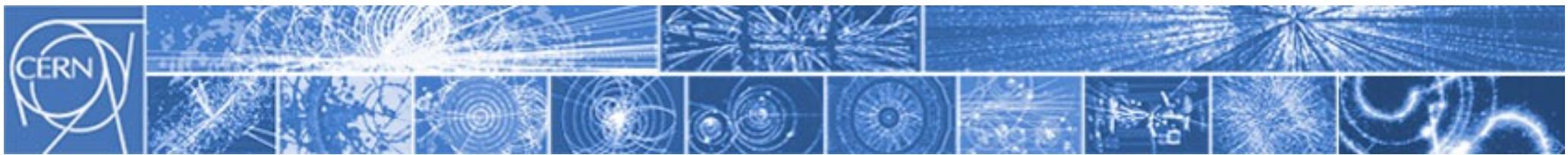


$$\rightarrow \text{SU}_c(3) \times \text{SU}_w(2) \times \text{U}_Y(1) \rightarrow \text{SU}_c(3) \times \text{U}_{\text{em}}(1)$$



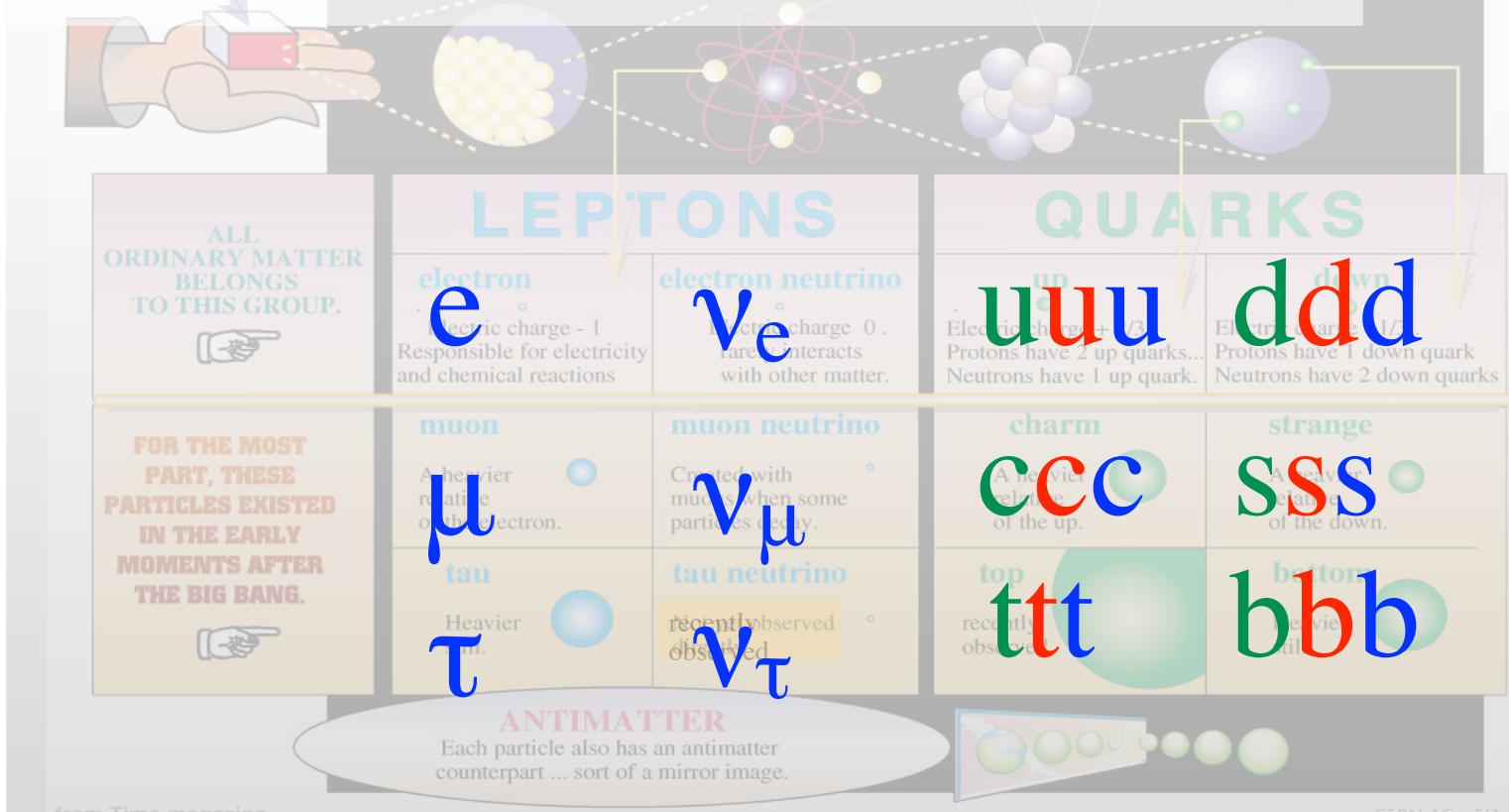
FORCES



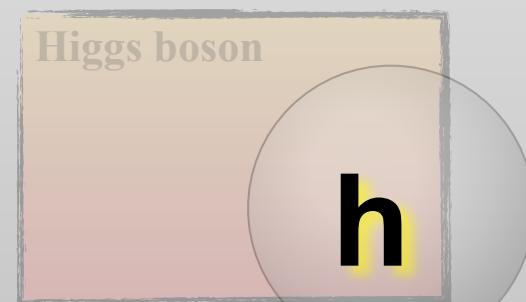


STANDARD MODEL

# Interazioni (& simmetrie)



- $SU_c(3) \times SU_w(2) \times U_Y(1) \rightarrow SU_c(3) \times U_{\text{em}}(1)$
- colore e carica elettrica



FORCES

Electromagnetic



Weak

Bosons ( $W, Z$ )

$W^+$   $W^-$



Strong

Gluons (8)

$g$  (8)

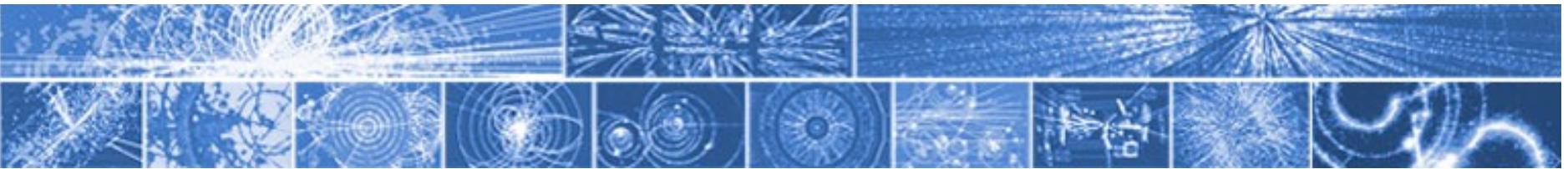
Nuclei

Gravitational

Graviton ?

$G$

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# Interazioni (& simmetrie)

Family 1

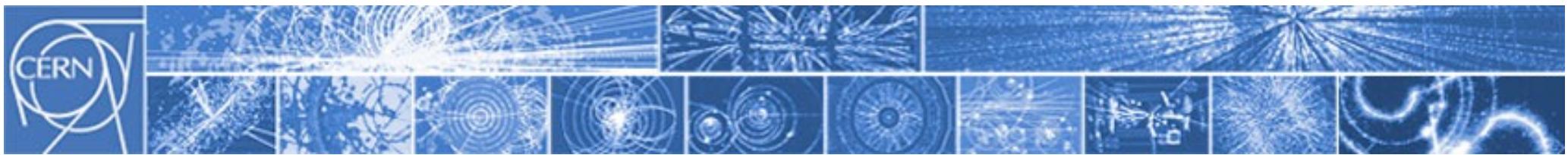
Particle	Mass	Electric Charge	Strong Charge	Weak Charge
<i>Electron</i>	.0054	-1	0	-1/2
<i>Electron-Neutrino</i>	<10 <sup>-8</sup>	0	0	1/2
<i>Up Quark</i>	.0047	2/3	red, green, blue	1/2
<i>Down Quark</i>	.0074	-1/3	red, green, blue	-1/2

Family 2

Particle	Mass	Electric Charge	Strong Charge	Weak Charge
<i>Muon</i>	.11	-1	0	-1/2
<i>Muon-Neutrino</i>	<.0003	0	0	1/2
<i>Charm Quark</i>	1.6	2/3	red, green, blue	1/2
<i>Strange Quark</i>	.16	-1/3	red, green, blue	-1/2

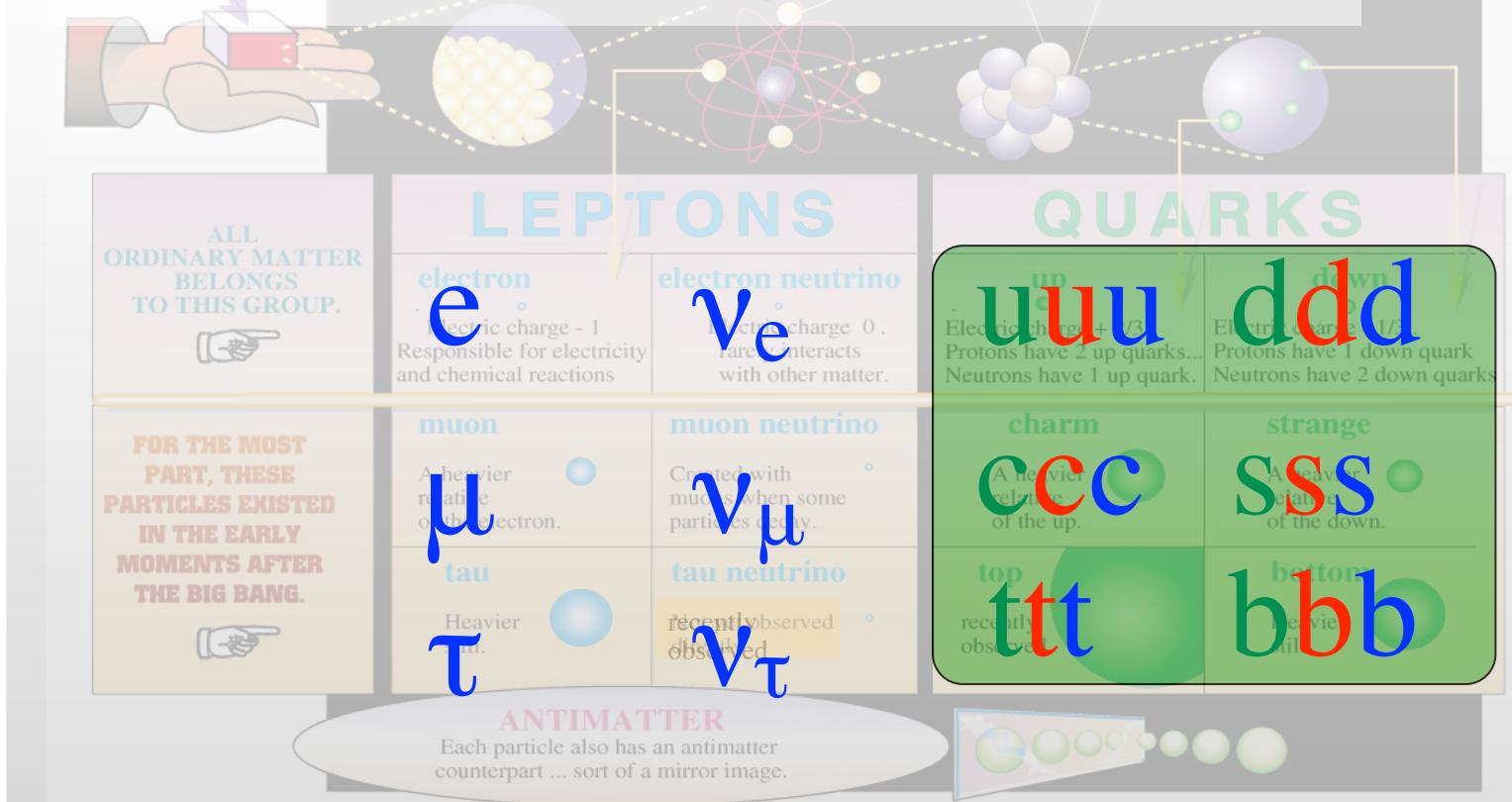
Family 3

Particle	Mass	Electric Charge	Strong Charge	Weak Charge
<i>Tau</i>	1.9	-1	0	-1/2
<i>Tau-Neutrino</i>	<.033	0	0	1/2
<i>Top Quark</i>	189	2/3	red, green, blue	1/2
<i>Bottom Quark</i>	5.2	-1/3	red, green, blue	-1/2



STANDARD MODEL

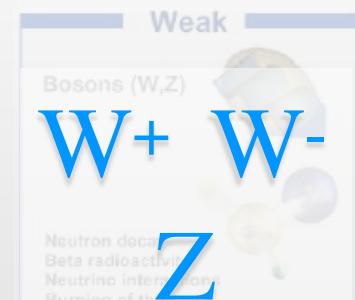
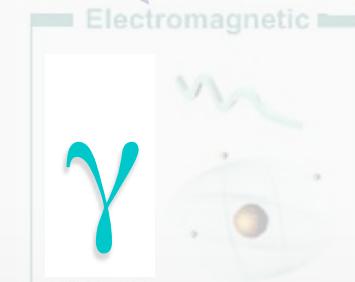
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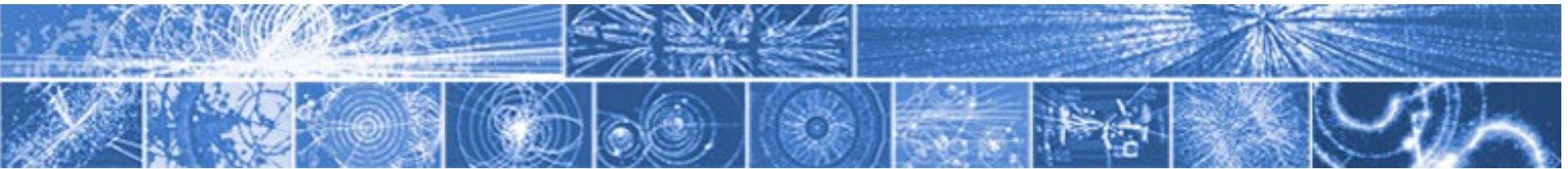


- $SU_c(3) \times SU_w(2) \times U_Y(1) \rightarrow SU_c(3) \times U_{\text{em}}(1)$
- colore e carica elettrica
- sapore barionico totale



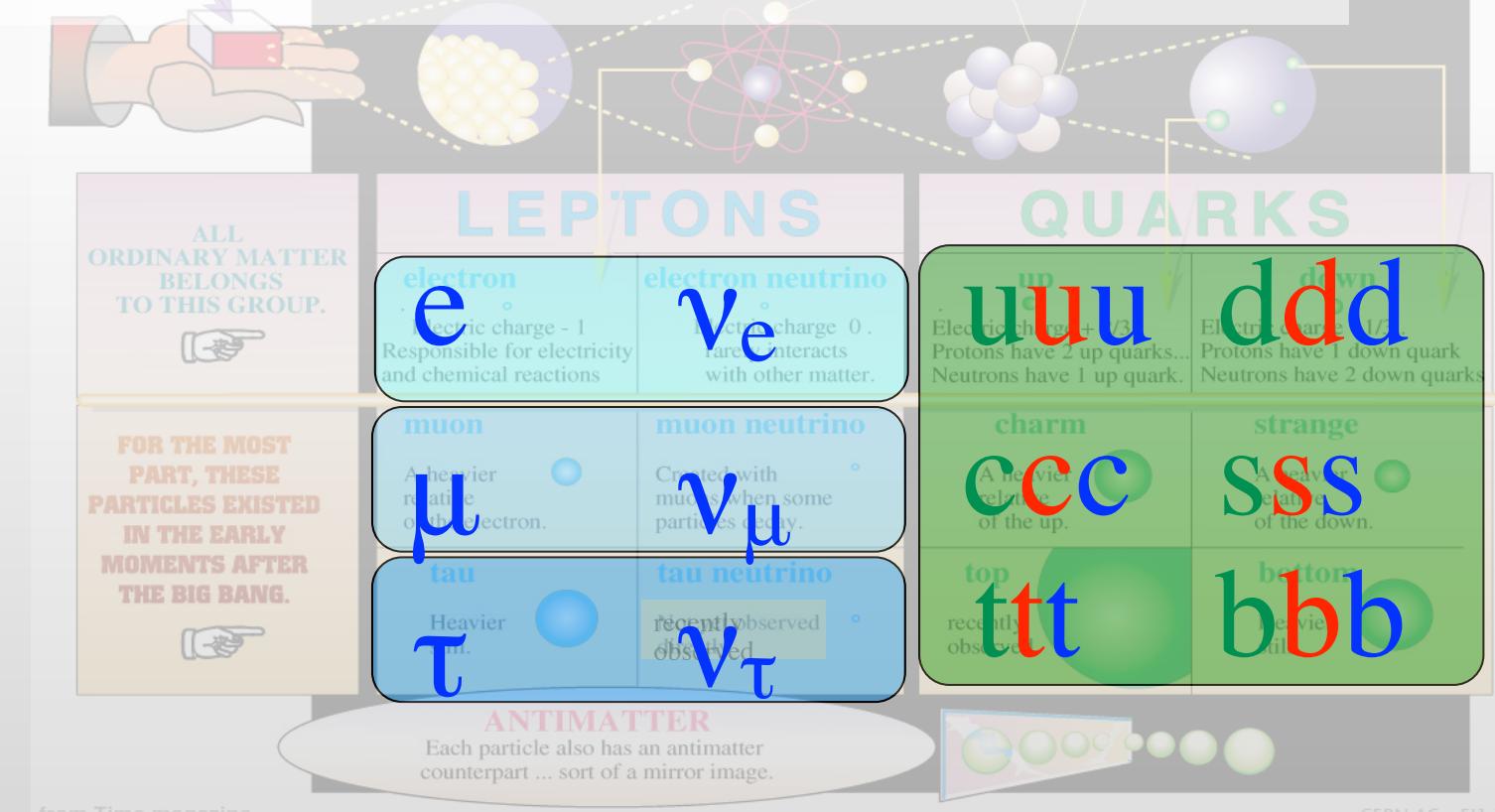
FORCES



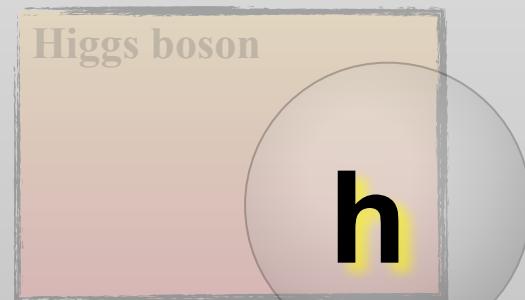


STANDARD MODEL

# Interazioni (& simmetrie)



- $SU_c(3) \times SU_w(2) \times U_Y(1) \rightarrow SU_c(3) \times U_{\text{em}}(1)$
- colore e carica elettrica
- sapore barionico totale
- sapore leptonico individuale (ma: oscillazioni  $\nu$ )



FORCES

Electromagnetic



Weak

Bosons (W,Z)

$W^+$   $W^-$



Strong

Gluons (8)

$g$  (8)

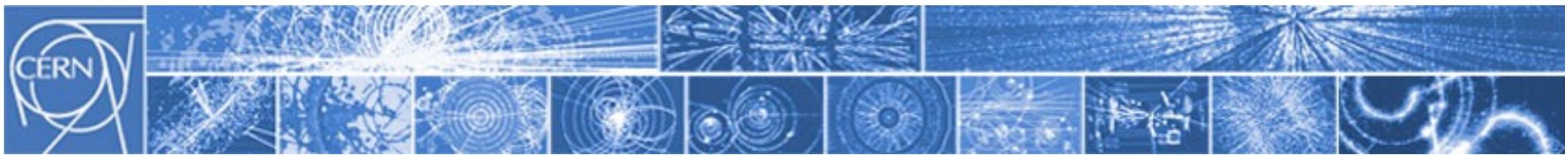
Nuclei

Gravitational

Graviton ?

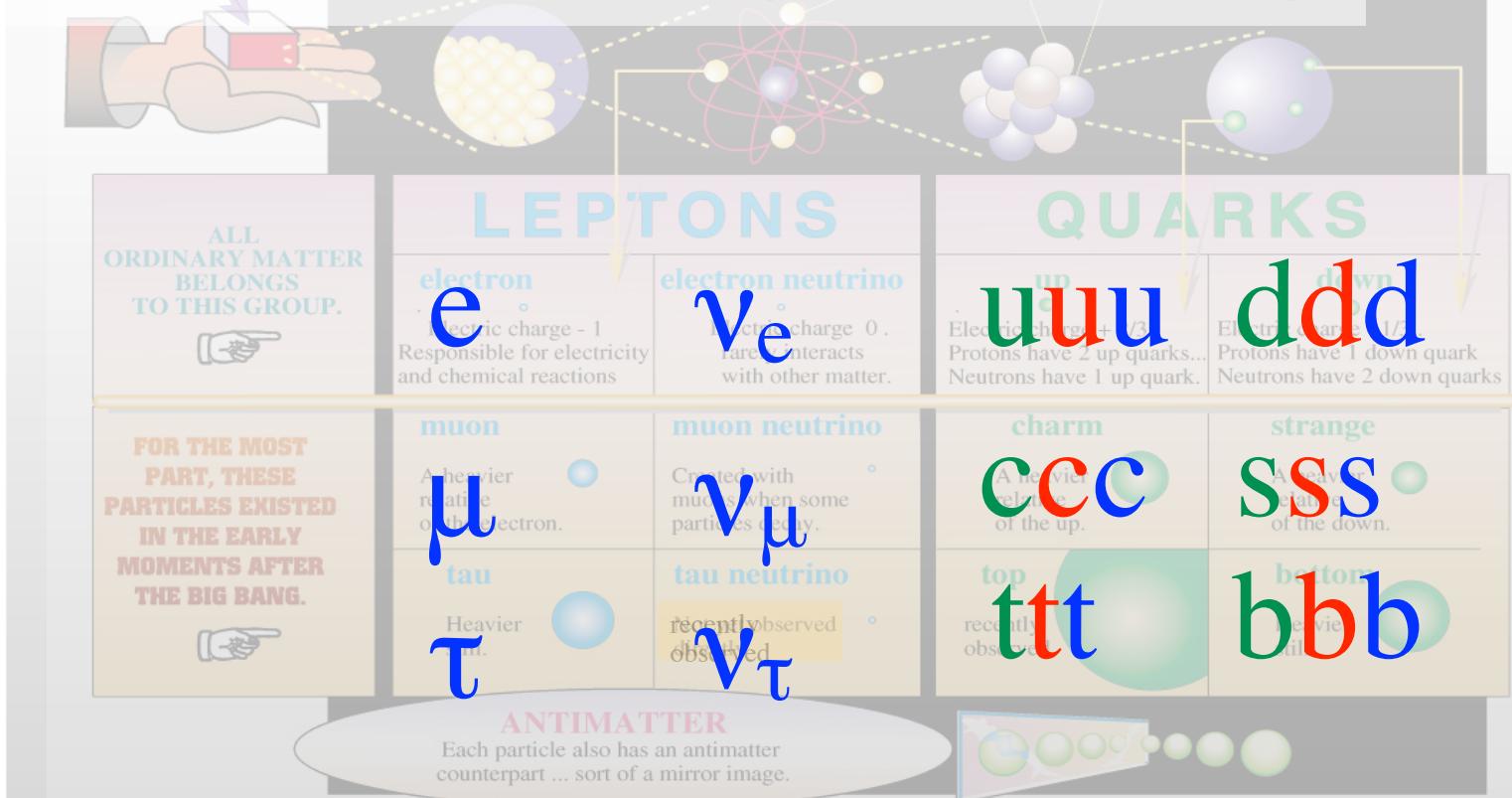
$G$

Solar system  
Galaxies  
Black holes



STANDARD MODEL

# Interazioni (& simmetrie)



**Adroni: stati composti di quarks**

FORCES

Electromagnetic



Weak

Bosons (W,Z)

$W^+$   $W^-$

Neutron decay  
Beta radioactive  
Neutrino interaction  
Burning of the sun



Strong

Gluons (8)

$g$  (8)



Gravitational

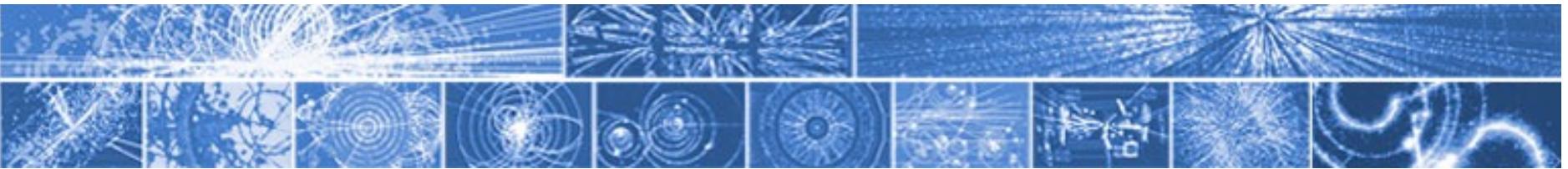
Graviton ?

$G$

Solar system  
Galaxies  
Black holes

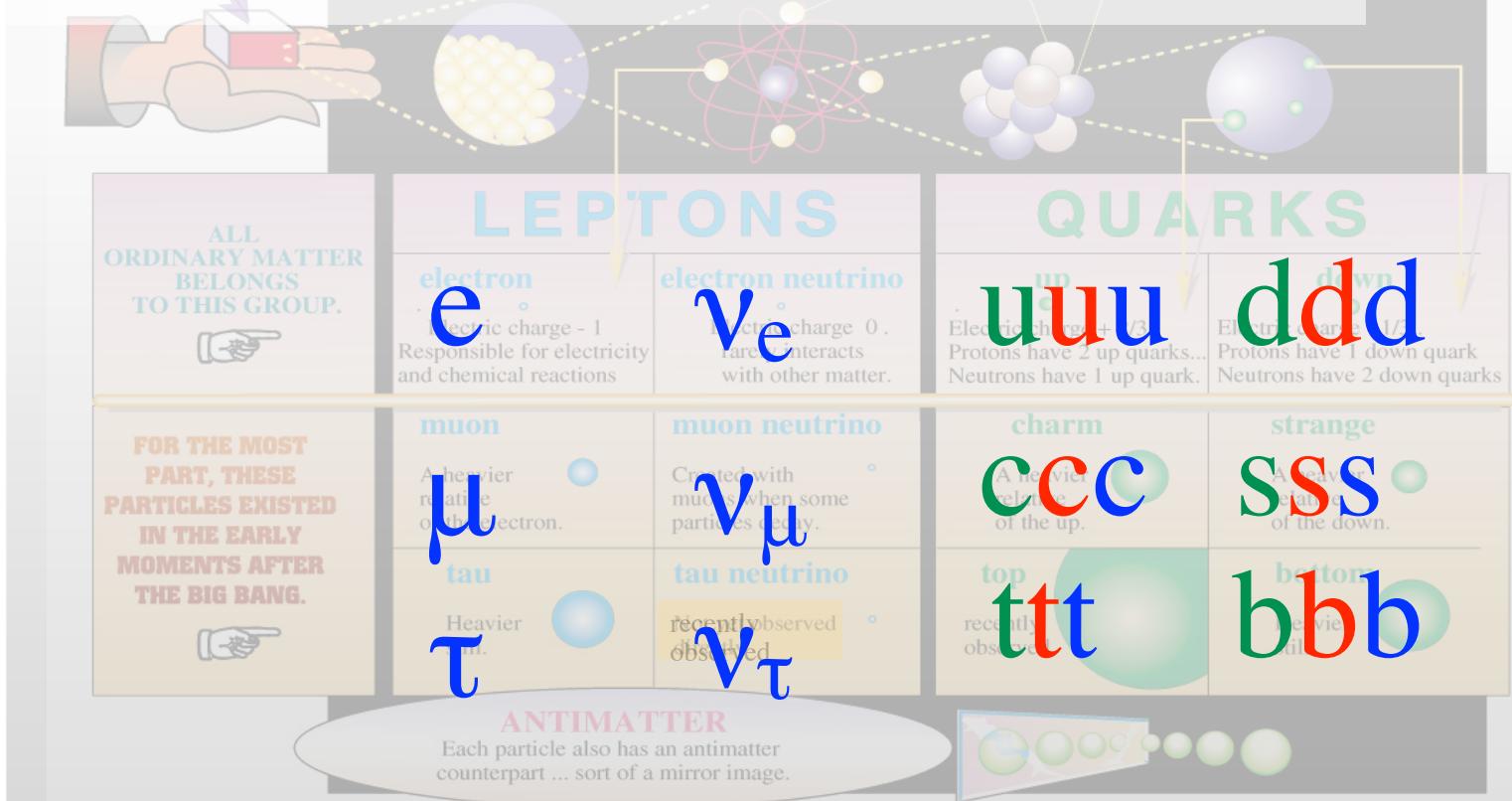
Higgs boson

$h$

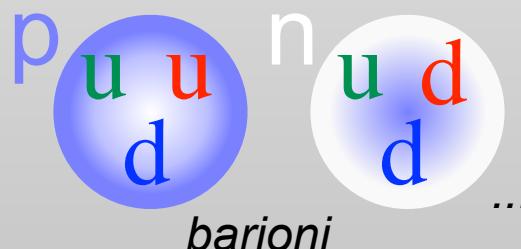


STANDARD MODEL

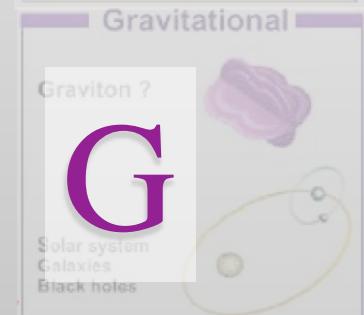
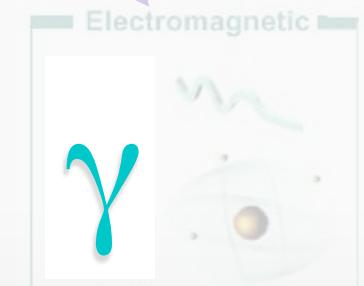
# Interazioni (& simmetrie)

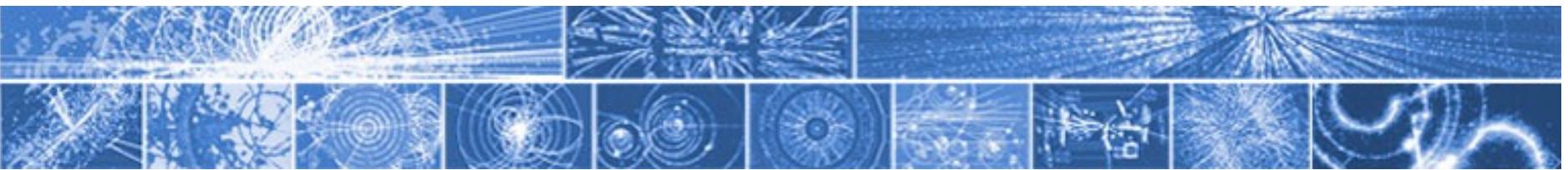


Adroni: stati composti di quarks



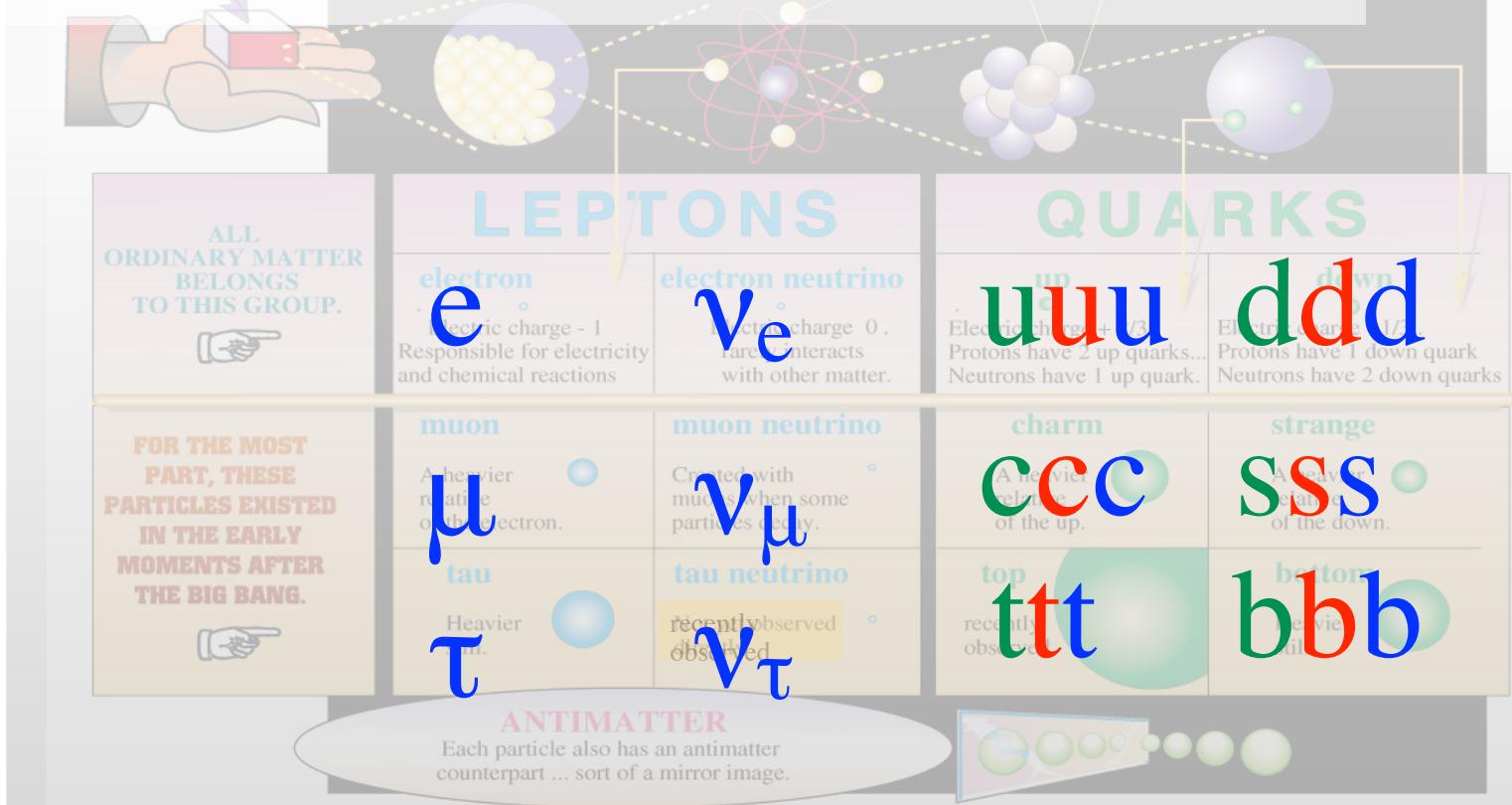
FORCES





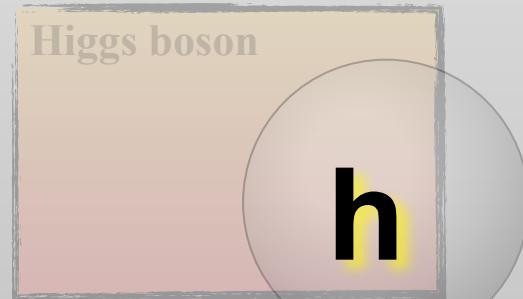
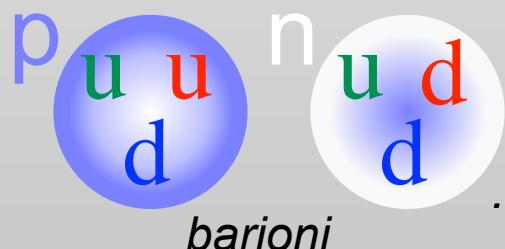
STANDARD MODEL

# Interazioni (& simmetrie)



from Time magazine

**Adroni: stati composti di quarks**



FORCES

Electromagnetic



Weak

Bosons ( $W, Z$ )

$W^+$   $W^-$



Strong

Gluons (8)

$g$  (8)

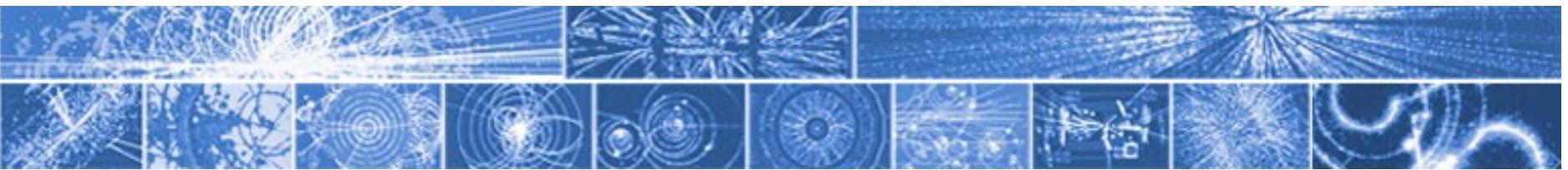
Nuclei

Gravitational

Graviton ?

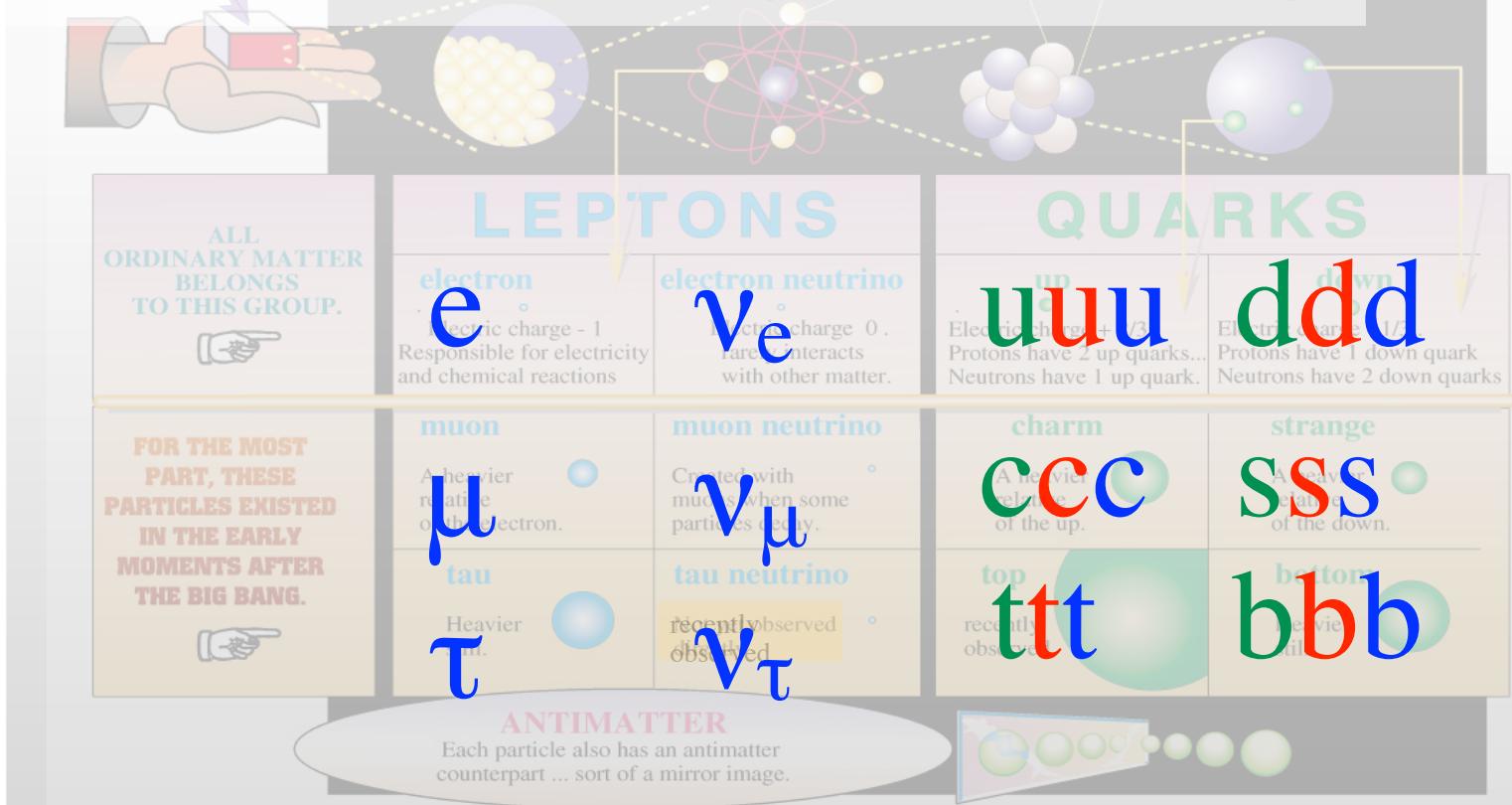


Solar system  
Galaxies  
Black holes



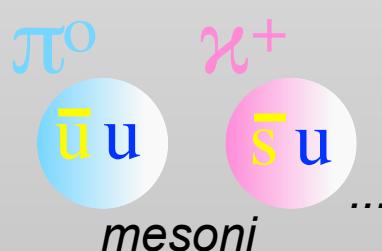
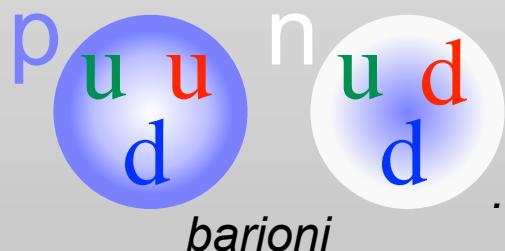
STANDARD MODEL

# Interazioni (& simmetrie)

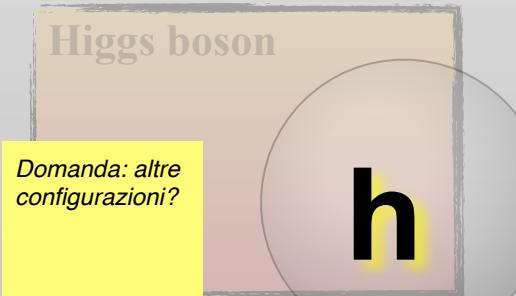


from Time magazine

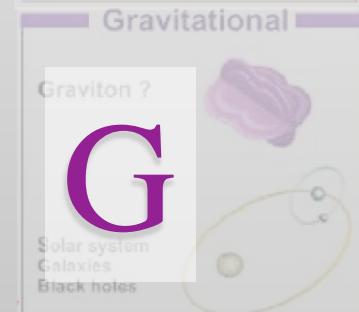
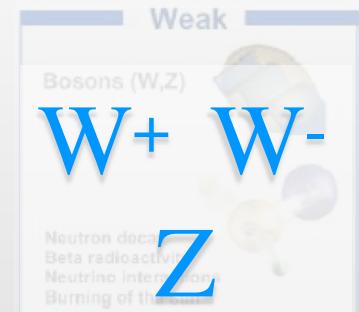
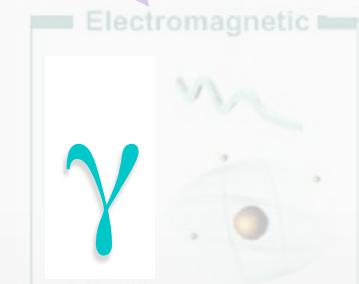
**Adroni: stati composti di quarks**

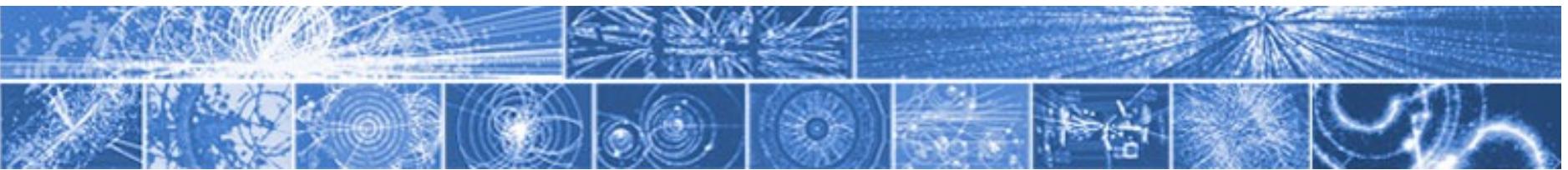


Domanda: altre configurazioni?



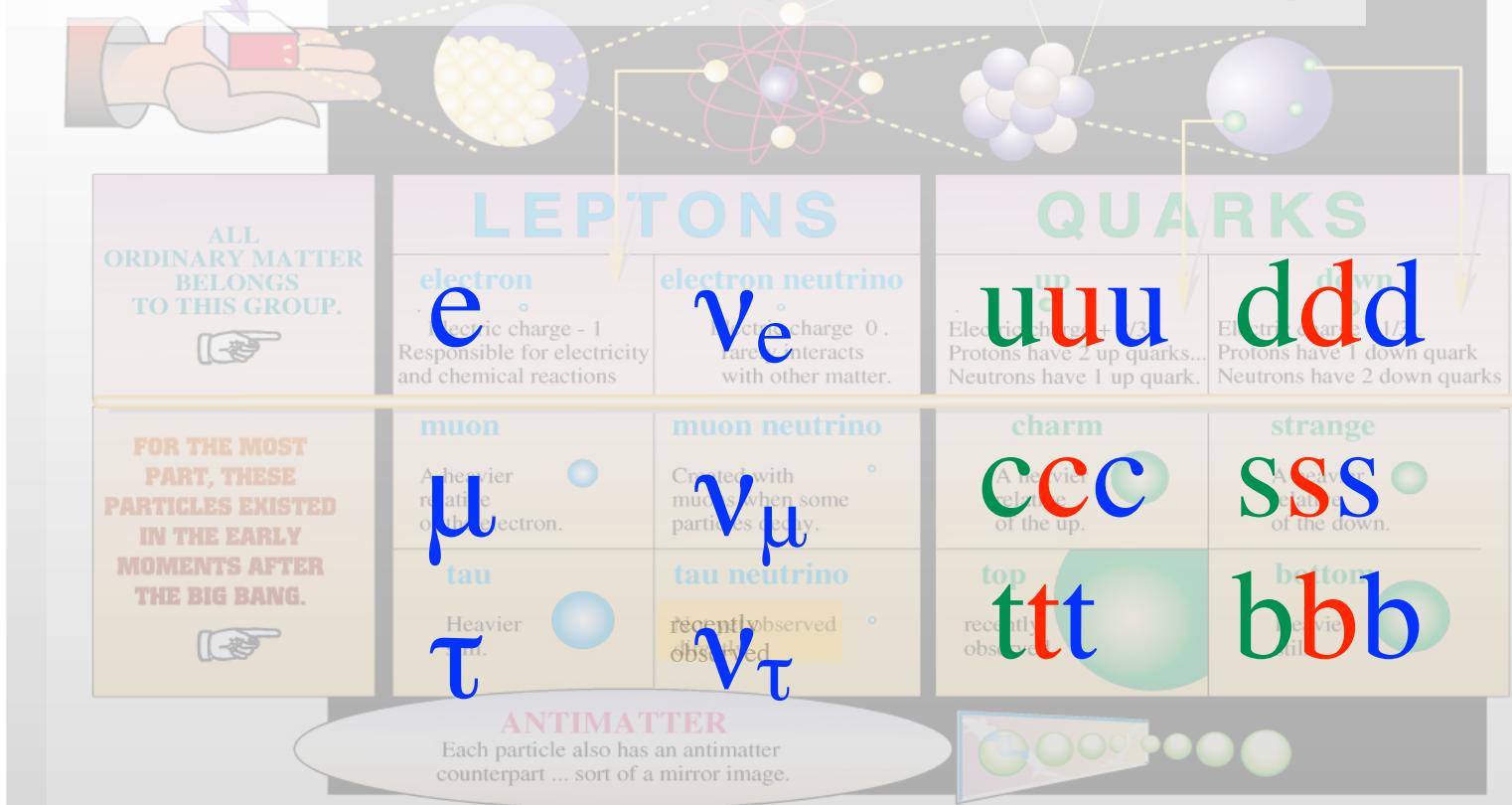
FORCES





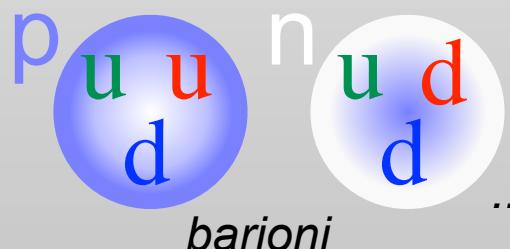
STANDARD MODEL

# Interazioni (& simmetrie)

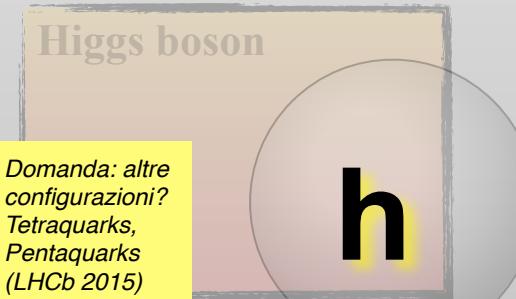


from Time magazine

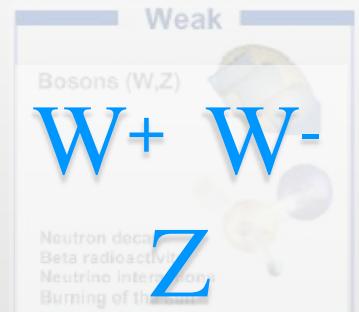
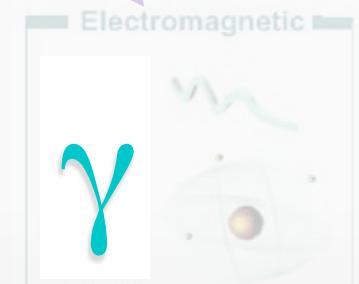
**Adroni: stati composti di quarks**

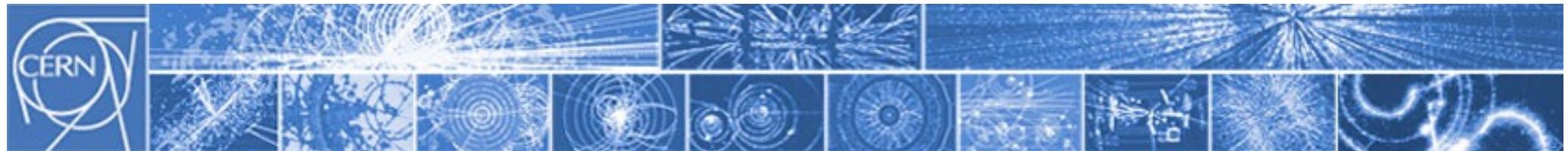


Domanda: altre configurazioni?  
Tetraquarks,  
Pentaquarks  
(LHCb 2015)

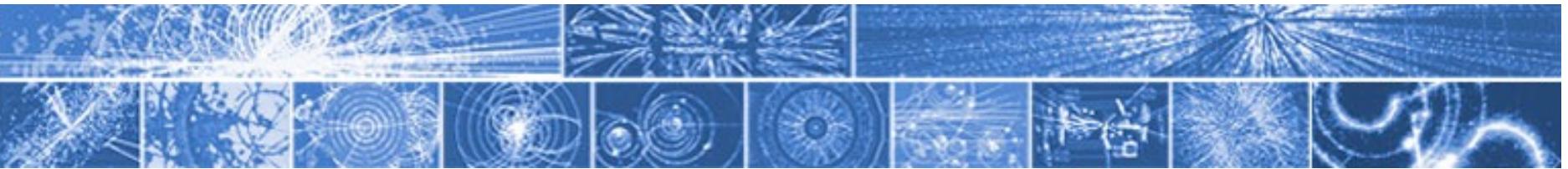


FORCES





# Mass



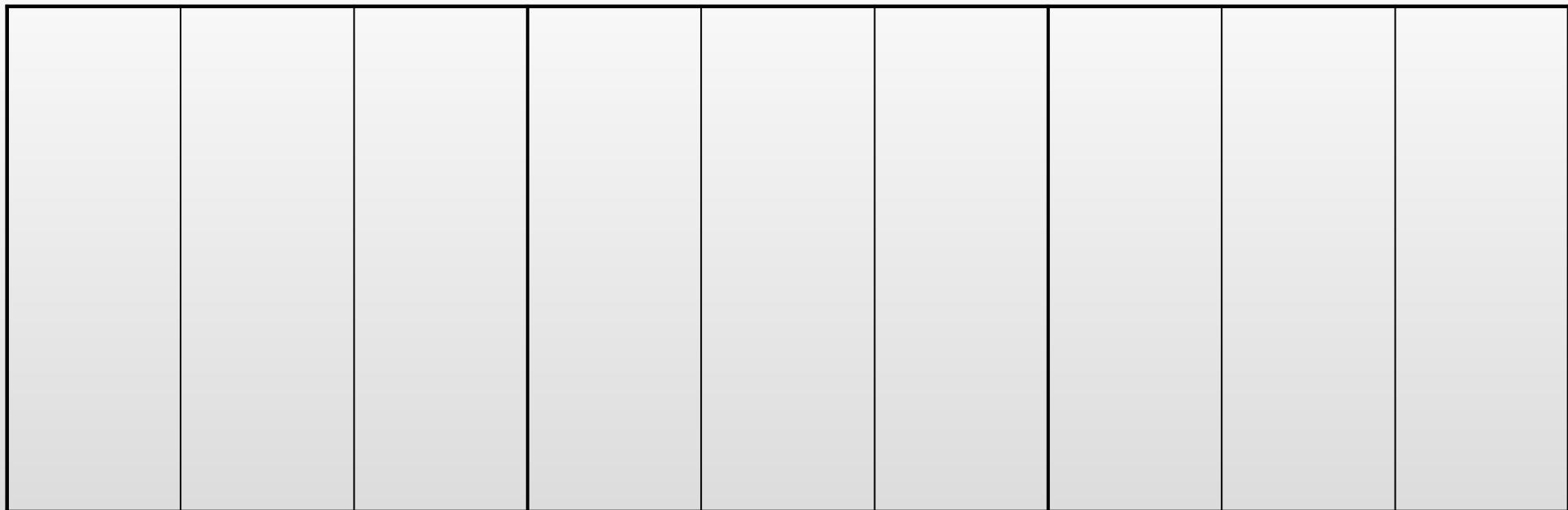
# Mass

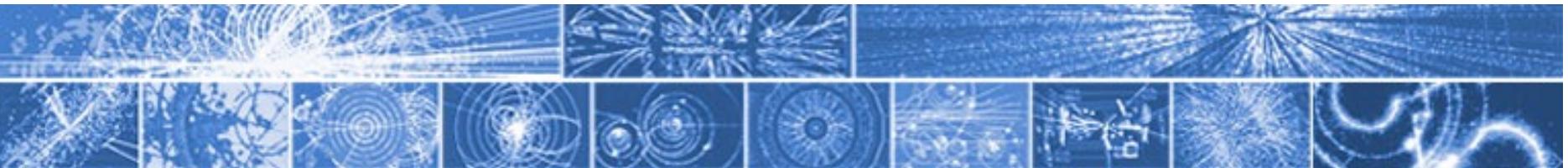
KeV

MeV

GeV

TeV





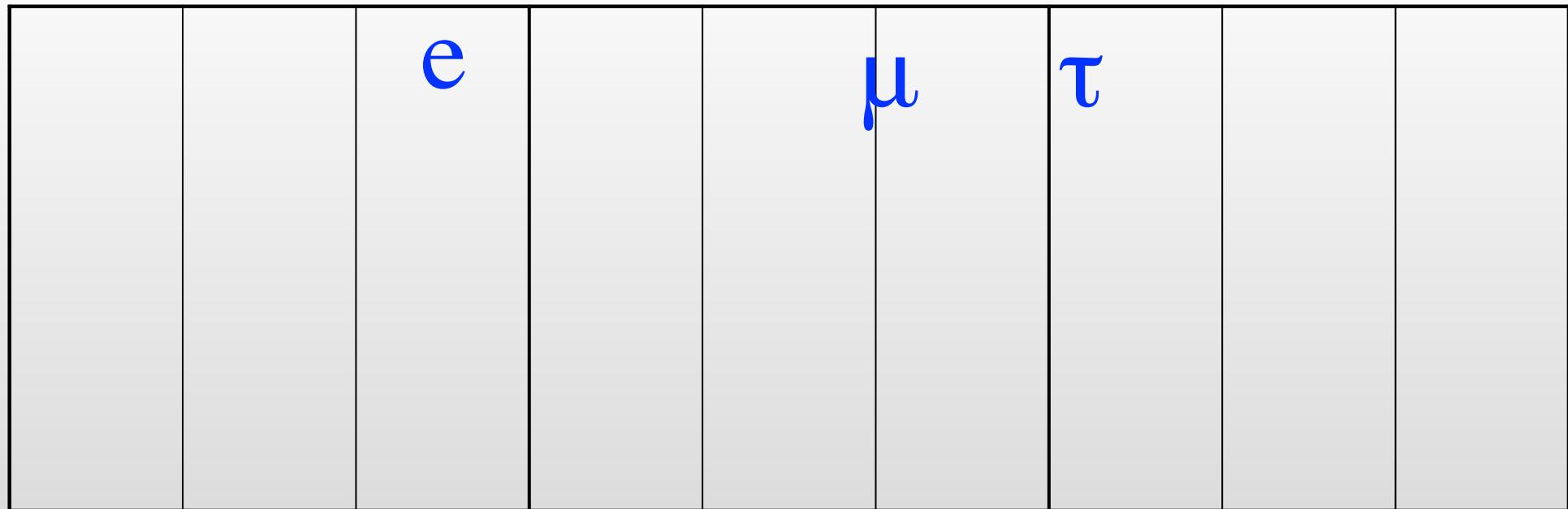
# Mass

KeV

MeV

GeV

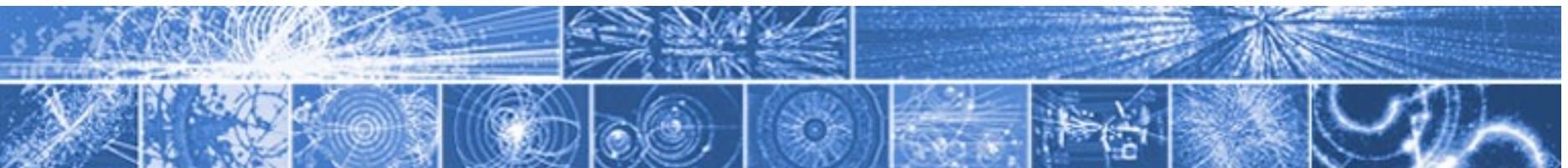
TeV



e 511 KeV

μ 105.7 MeV

τ 1.777 GeV



# Mass

KeV

MeV

GeV

TeV

		e	u d		$\mu$ s		$\tau$ c b		t
--	--	---	--------	--	------------	--	------------------	--	---

e 511 KeV

$\mu$  105.7 MeV

$\tau$  1.777 GeV

u ~2.3 MeV

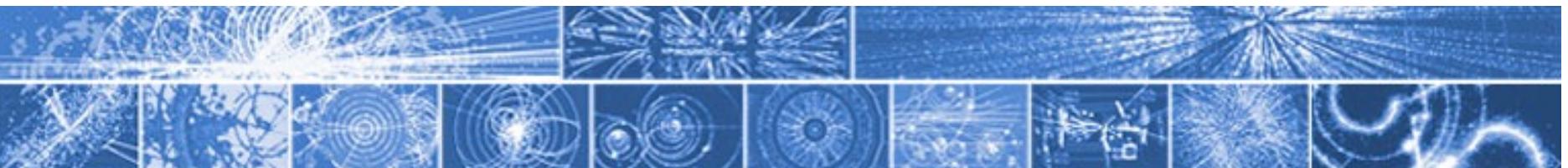
d ~5 MeV

s ~95 MeV

c 1.27 GeV

b 4.2 GeV

t 173.2 GeV



# Mass

KeV

MeV

GeV

TeV

		e	u d		$\mu$ s		$\tau$ c b		t  W Z
--	--	---	--------	--	------------	--	------------------	--	-----------------

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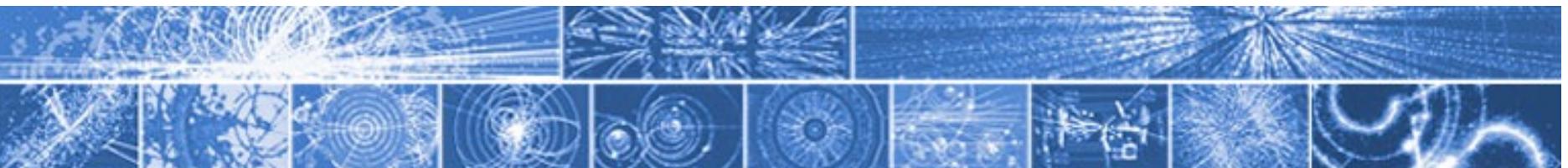
c 1.27 GeV

b 4.2 GeV

t 173.2 GeV

$W^\pm$  80.385 GeV

Z 91.1876 GeV



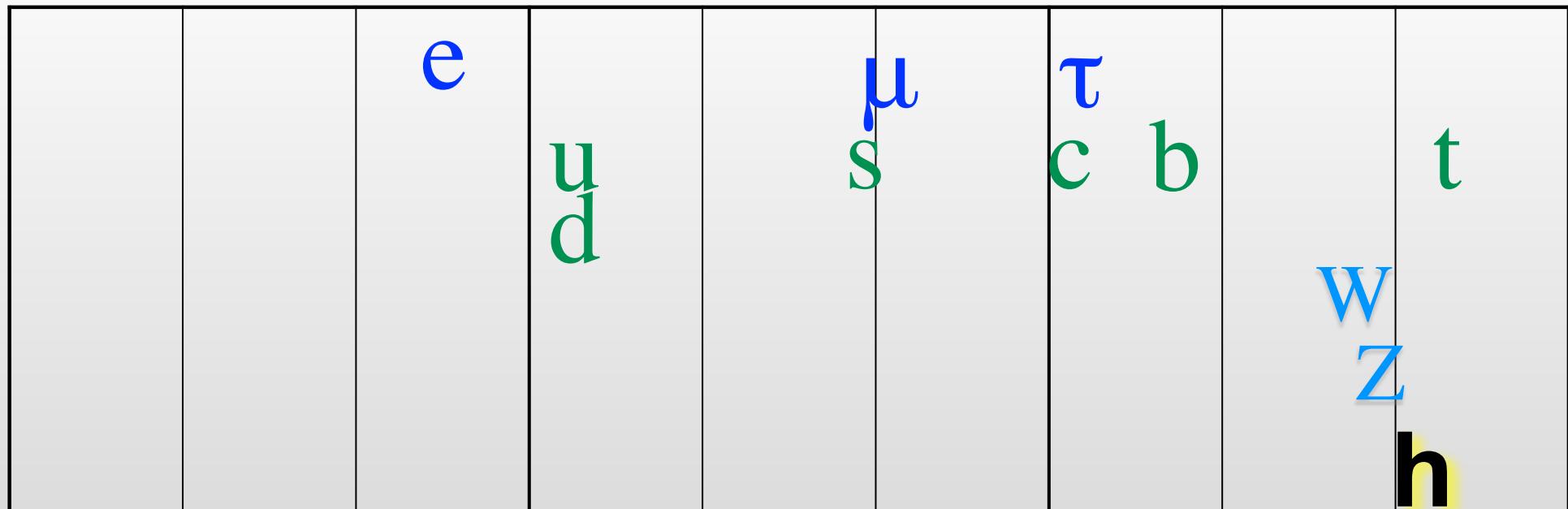
# Mass

KeV

MeV

GeV

TeV



$e$  511 KeV

$\mu$  105.7 MeV

$\tau$  1.777 GeV

$u$  ~2.3 MeV

$d$  ~5 MeV

$s$  ~95 MeV

$c$  1.27 GeV

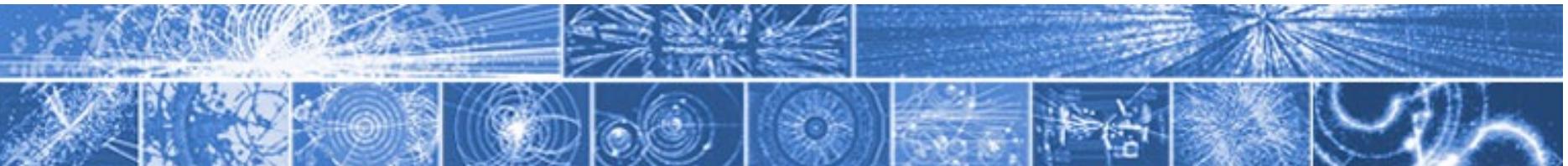
$b$  4.2 GeV

$t$  173.2 GeV

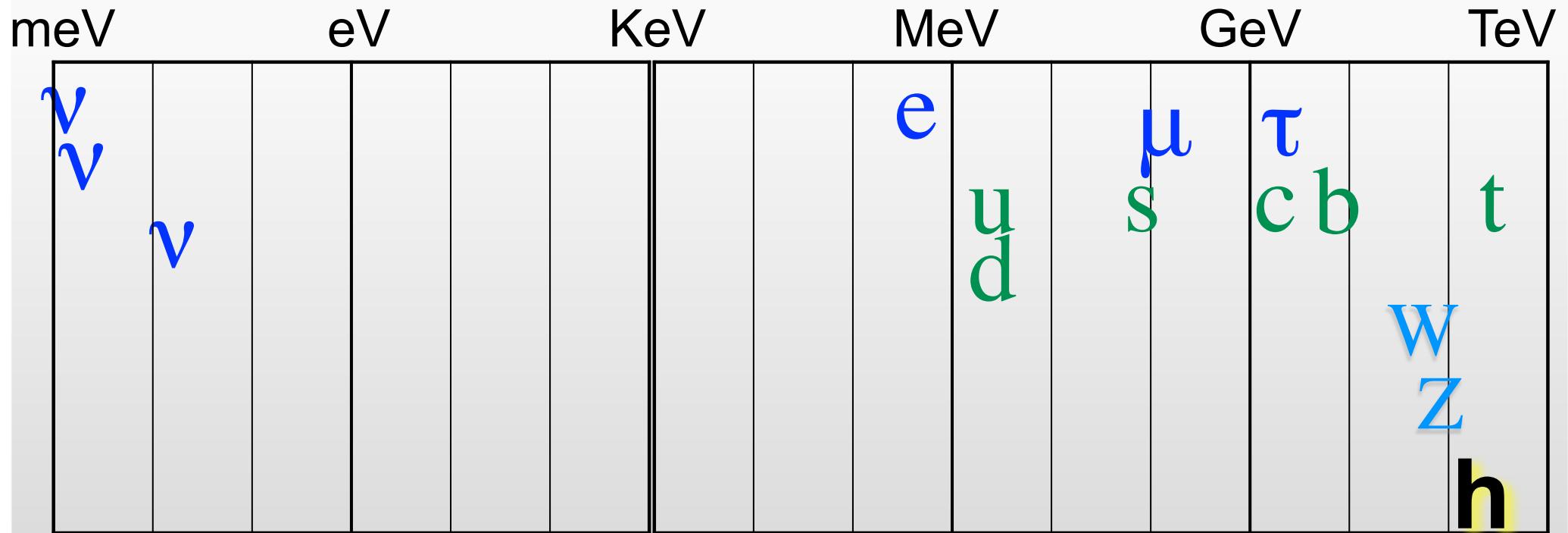
$w^\pm$  80.385 GeV

$Z$  91.1876 GeV

$h$  125.09 GeV



# Mass



e 511 KeV

μ 105.7 MeV

τ 1.777 GeV

$9 \cdot 10^{-3} \text{ eV} \leq \nu_i \leq 0.2 \text{ eV}$

u ~2.3 MeV

d ~5 MeV

s ~95 MeV

c 1.27 GeV

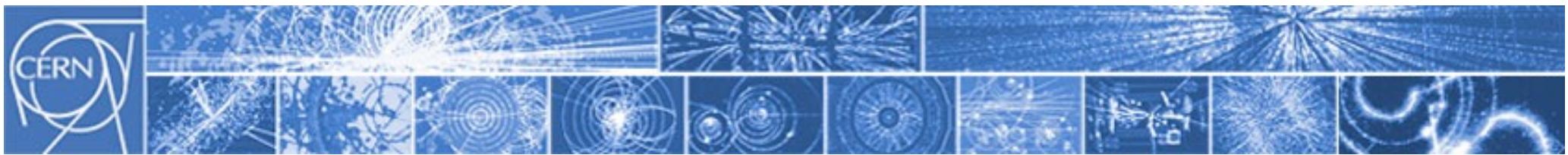
b 4.2 GeV

t 173.2 GeV

W<sup>±</sup> 80.385 GeV

Z 91.1876 GeV

h 125.09 GeV

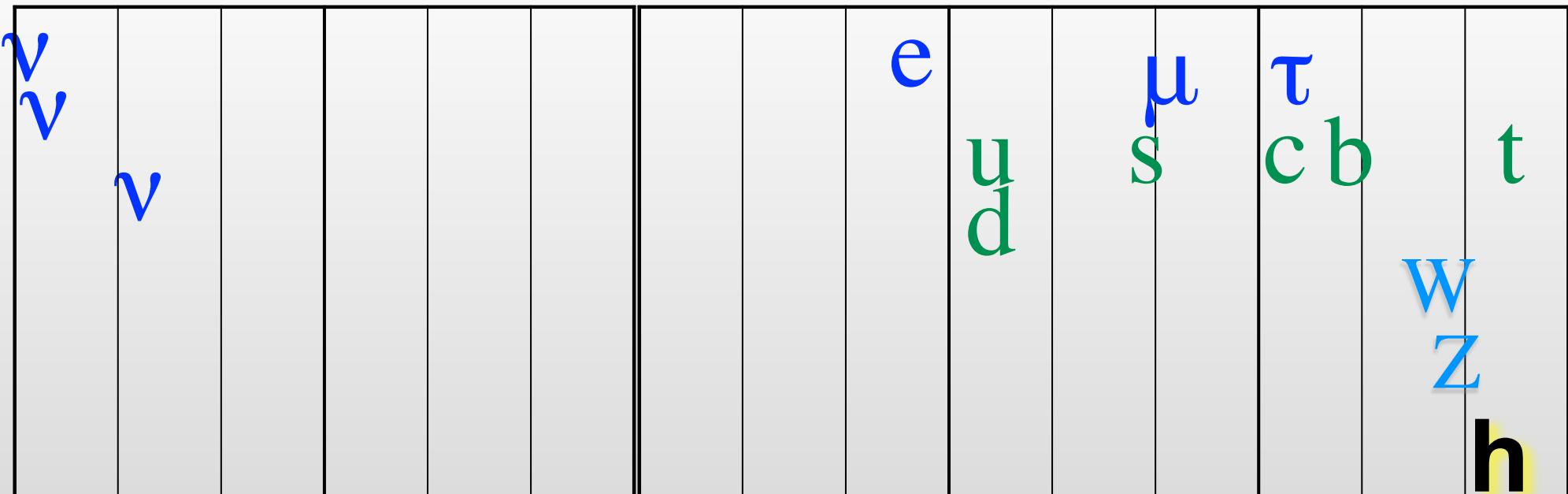


# Mass

massa zero:  $\gamma$   $g$   $G$

$^{238}U$

meV eV KeV MeV GeV TeV



$e$  511 KeV

$\mu$  105.7 MeV

$\tau$  1.777 GeV

$9 \cdot 10^{-3} \text{ eV} \leq \nu_i \leq 0.2 \text{ eV}$

$u$  ~2.3 MeV

$d$  ~5 MeV

$s$  ~95 MeV

$c$  1.27 GeV

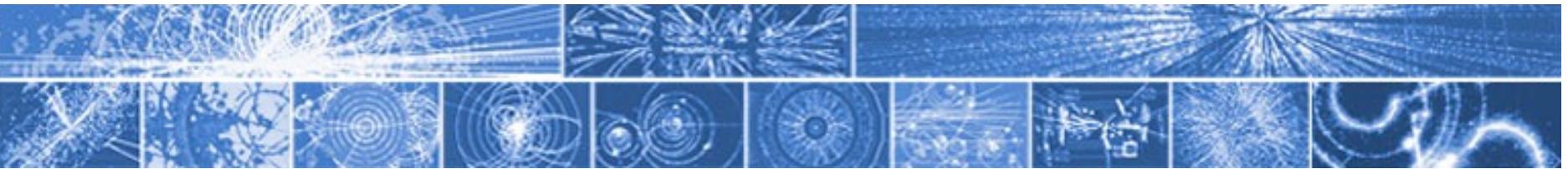
$b$  4.2 GeV

$t$  173.2 GeV

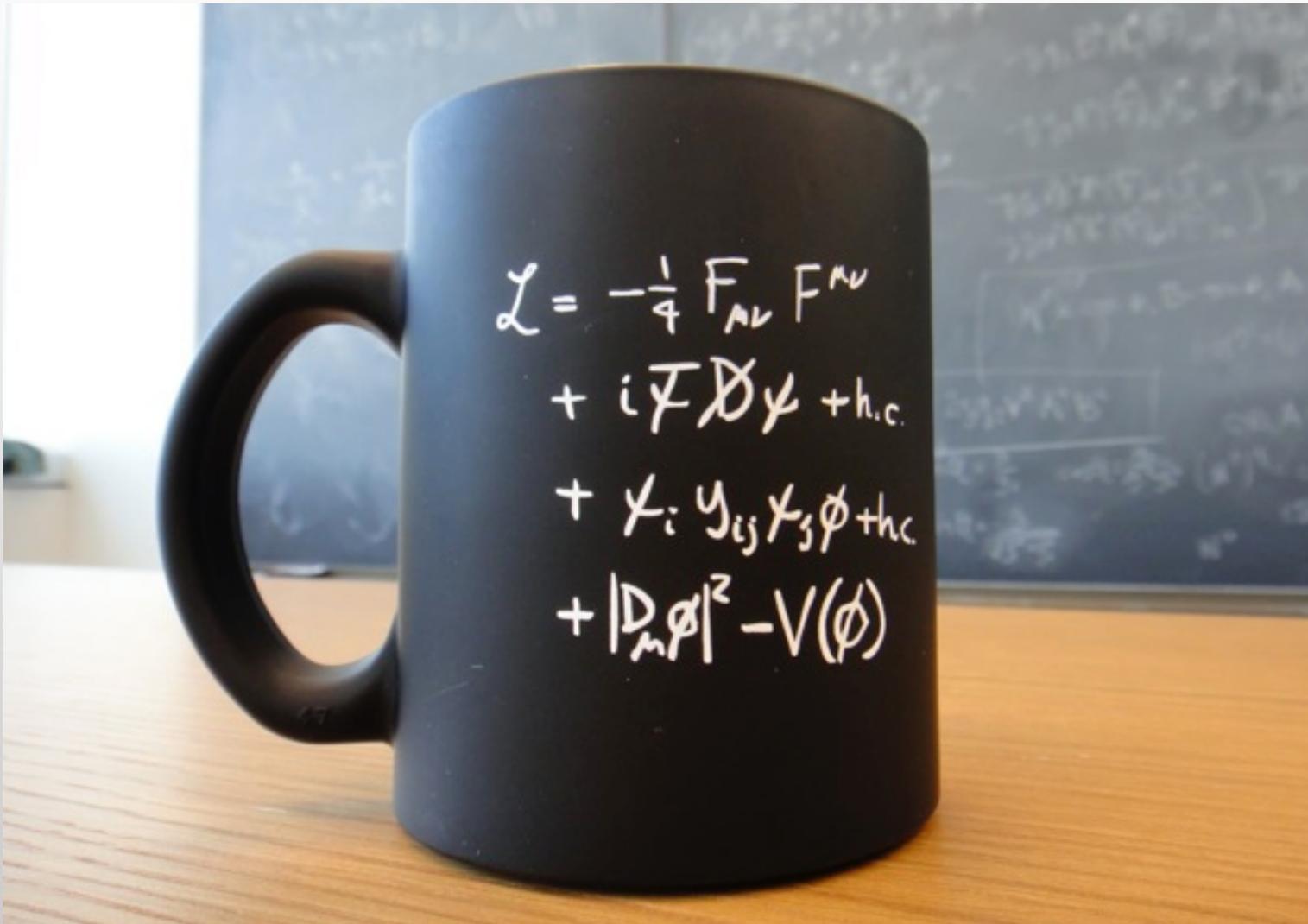
$w^\pm$  80.385 GeV

$Z$  91.1876 GeV

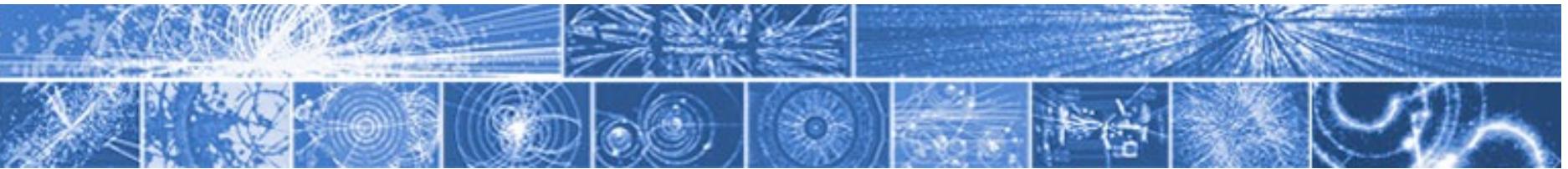
$h$  125.7 GeV



# Lagrangiana del Modello Standard



Credit: Flip Tanedo, QuantumDiaries.org



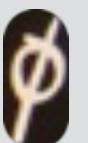
# Lagrangiana del Modello Standard

mediatori delle forze

$$F_{\mu\nu} \rightarrow \gamma^W Z g$$

campi di materia

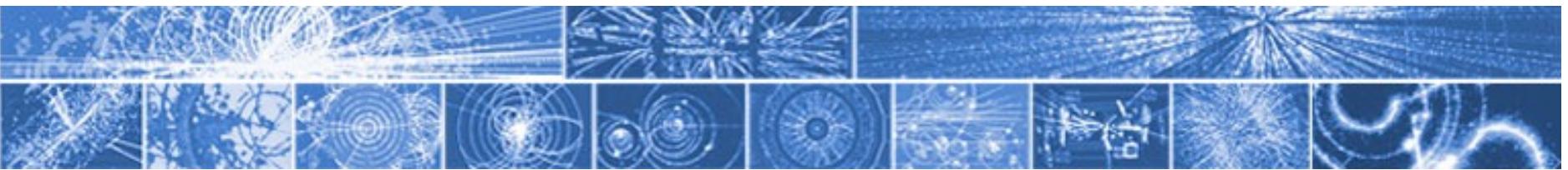
$$\psi \rightarrow e^\pm \mu^\pm \tau^\pm \nu u d s c b t$$



campo scalare  
(-> di higgs)

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} D^\mu \psi + h.c. \\ & + Y_i Y_{ij} Y_j \phi + h.c. \\ & + |\partial_\mu \phi|^2 - V(\phi)\end{aligned}$$

Credit: Flip Tanedo, QuantumDiaries.org



# Lagrangiana del Modello Standard

mediatori delle forze

$$F_{\mu\nu} \rightarrow \gamma^W Z g$$

campi di materia

$$\psi \rightarrow e^\pm \mu^\pm \tau^\pm \nu u d s c b t$$

campo scalare  
(-> di higgs)

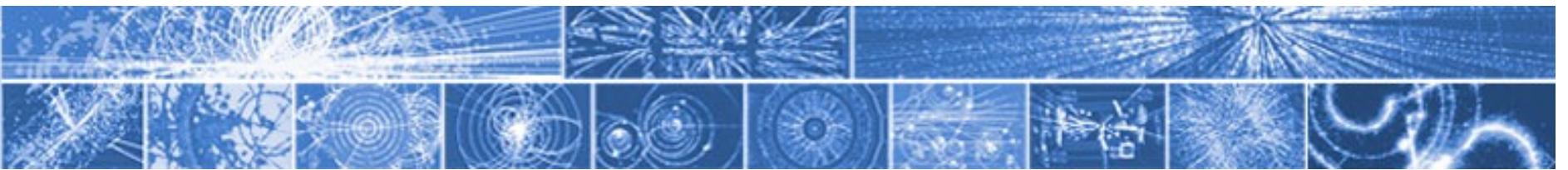
propagazione  
delle forze

interazione  
forze-materia

interazione  
higgs-materia

'settore  
di higgs'

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} D_\mu \psi + h.c. \\ & + Y_i Y_{ij} Y_j \phi + h.c. \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$



# Lagrangiana del Modello Standard

mediatori delle

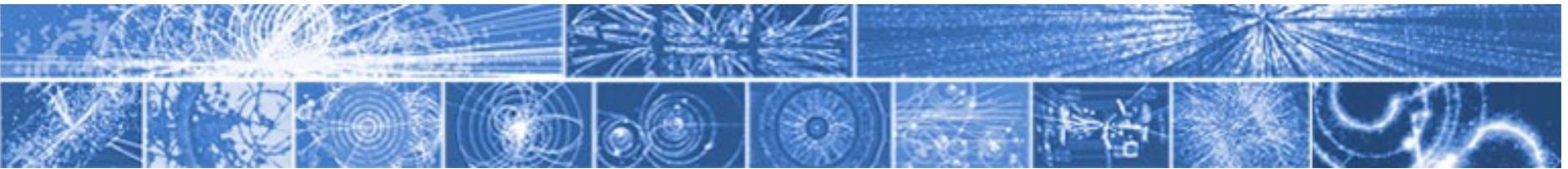


campi di materia

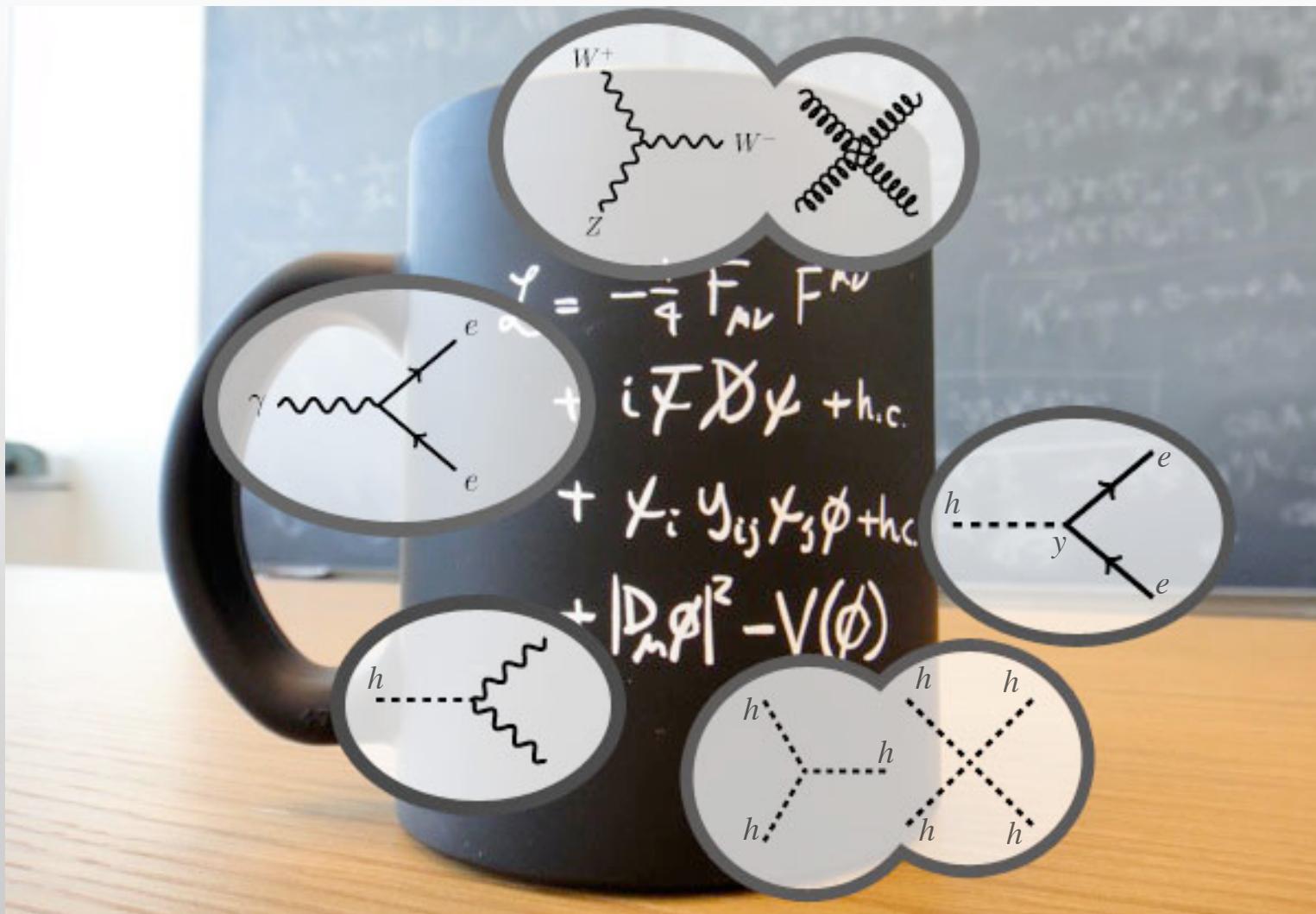


campo scalare  
(-> di higgs)

$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \\
 & \frac{1}{2}ig_s^2 (q_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h [\frac{2M^2}{g^2} + \\
 & \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-)] + \frac{2M^4}{g^2} \alpha_h - ig c_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\nu W_\mu^+)] - ig s_w [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\mu (W_\mu^+ \partial_\nu W_\nu^- - \\
 & W_\nu^- \partial_\nu W_\mu^+) + A_\mu (W_\mu^+ \partial_\nu W_\nu^- - W_\nu^- \partial_\nu W_\mu^+)] - \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\nu^+ W_\mu^- + \\
 & \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\nu^0 W_\nu^+ W_\nu^-) + \\
 & g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
 & W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^-] - g \alpha [H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^- + 2(\phi^0)^2 H^2] - \\
 & \frac{1}{8}g^2 \alpha_h [H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2] - \\
 & g M W_\mu^+ W_\mu^- H - \frac{1}{2}g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H - \frac{1}{2}ig [W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - \\
 & W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)] + \frac{1}{2}g [W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \\
 & \phi^+ \partial_\mu H)] + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \\
 & ig s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + \\
 & ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4}g^2 W_\mu^+ W_\mu^- [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \\
 & \frac{1}{4}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
 & W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma \partial \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - \\
 & d_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + ig s_w A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] + \\
 & \frac{ig}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - \\
 & 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 - \gamma^5) d_j^\lambda)] + \frac{ig}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + \\
 & (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa)] + \frac{ig}{2\sqrt{2}} W_\mu^- [(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \\
 & \gamma^5) u_j^\lambda)] + \frac{ig}{2\sqrt{2}} \frac{m_e^\lambda}{M} [-\phi^+ (\bar{\nu}^\lambda (1 - \gamma^5) e^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) \nu^\lambda)] - \\
 & \frac{g}{2} \frac{m_e^\lambda}{M} [H (\bar{e}^\lambda e^\lambda) + i\phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda)] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa)] + \\
 & m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa)] + \frac{ig}{2M\sqrt{2}} \phi^- [m_d^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \\
 & \gamma^5) u_j^\kappa)] - \frac{g}{2} \frac{m_\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{ig}{2} \frac{m_\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \\
 & \frac{ig}{2} \frac{m_\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + X^0 (\partial^2 - \\
 & \frac{M^2}{c_w^2}) X^0 + \bar{Y} \partial^2 Y + ig c_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + ig s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \\
 & \partial_\mu \bar{X}^+ Y) + ig c_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + ig s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \\
 & \partial_\mu \bar{Y} X^+) + ig c_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) + ig s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \\
 & \partial_\mu \bar{X}^- X^-) - \frac{1}{2}g M [\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w^2} \bar{X}^0 X^0 H] + \\
 & \frac{1-2c_w^2}{2c_w} ig M [\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} ig M [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \\
 & ig M s_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2}ig M [\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
 \end{aligned}$$



# Lagrangiana del Modello Standard



Credit: Flip Tanedo, QuantumDiaries.org

presentazione  
per insegnanti:

J. Woithe, J. Wiener, F. Van der Veken, *Let's have a coffee with the Standard Model of particle physics!*, Phys. Educ. 52 (2017) 034001