

Marco Drewes, Université catholique de Louvain

Heavy Sterile Neutrinos: From Cosmology to Experiment

13. 01. 2022

IAS Program on High
Energy Physics (HEP2022)

HKUST, Hong Kong, China

The Seesaw Mechanism (type I)

$$\mathcal{L} = \mathcal{L}_{SM} + i\bar{\nu}_R \not{\partial} \nu_R - \bar{L}_L F \nu_R \tilde{H} - \tilde{H}^\dagger \bar{\nu}_R F^\dagger L - \frac{1}{2} (\bar{\nu}_R^c M_M \nu_R + \bar{\nu}_R M_M^\dagger \nu_R^c)$$

Three Generations of Matter (Fermions) spin 1/2

	I	II	III	
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0
charge →	2/3	2/3	2/3	0
name →	u Left up Right	c Left charm Right	t Left top Right	g gluon
Quarks	d Left down Right	s Left strange Right	b Left bottom Right	γ photon
	0 eV	0 eV	0 eV	91.2 GeV
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z⁰ weak force
	0.511 MeV	105.7 MeV	1.777 GeV	125 GeV
Leptons	e Left electron Right	μ Left muon Right	τ Left tau Right	H Higgs boson
	-1	-1	-1	spin 0
				80.4 GeV
				W[±] weak force

Bosons (Forces) spin 1

three light neutrinos mostly "active" SU(2) doublet

$$\nu \simeq U_\nu (\nu_L + \theta \nu_R^c)$$

$$\text{with masses } m_\nu \simeq \theta M_M \theta^T = v^2 F M_M^{-1} F^T$$

three heavy mostly singlet neutrinos

$$N \simeq \nu_R + \theta^T \nu_L^c$$

$$\text{with masses } M_N \simeq M_M$$

Minkowski 79, Gell-Mann/Ramond/Slansky 79, Mohapatra/Senjanovic 79, Yanagida 80, Schechter/Valle 80



Minimal vs Non-minimal Scenarios

minimal = literally only add RH neutrinos

- generic EFT description of models with $M < \text{TeV} \ll \Lambda$
- can even be UV complete in the sense $\Lambda = M_P$ (Shaposhnikov 07)
- ... or at least up to the scale of inflation (Bezrukov/Shaposhnikov 14)

non-minimal = anything else (gauge extensions, extended scalar sector, RHN as “portal” to dark sector...)

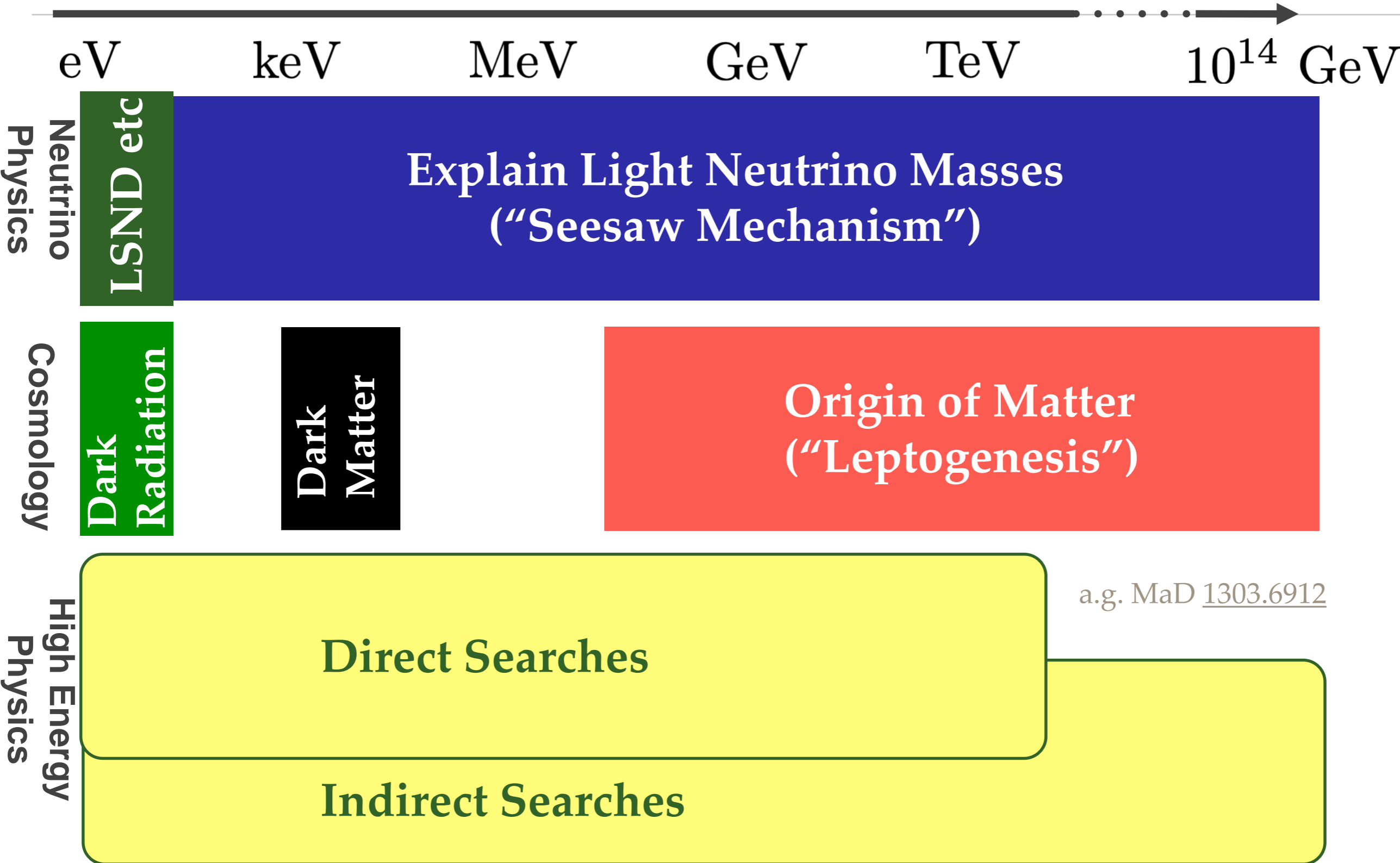
- can use generic EFT description for models with $M < \text{TeV} < \Lambda$
- need full dark sector description if $M, \Lambda < \text{TeV}$

recently growing interest in non-minimal “bottom up” approaches driven by the DM puzzle, MiniBooNE anomaly etc...

For a collection of references see e.g.

- reviews Deppisch/Dev/Pilaftsis [1502.06541](#), Cai/Han/Ruiz [1711.02180](#)
- physics case papers for MATHUSLA ([1806.07396](#)) and SHiP ([1504.04855](#))
- CERN PBC Working Group Report [1901.09966](#)
- Snowmass LoIs on [Opportunities and signatures of non-minimal Heavy Neutral Leptons and Testable Neutrino Mass Models](#)

Heavy Neutrino Mass Scale



Heavy Neutrino Mass Scale

nuclear
decay spectra



fixed target
experiments



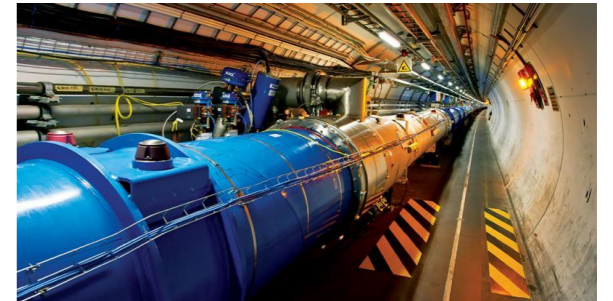
b factories



far detectors



ATLAS/CMS



future colliders



Direct Searches

Indirect Searches

High Energy
Physics

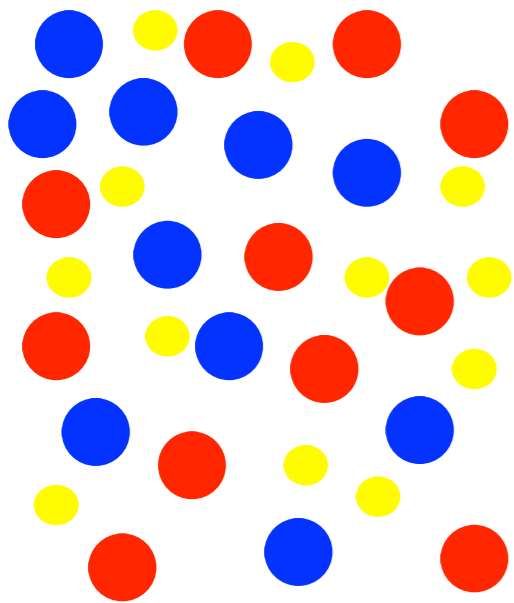
DR

Low Scale Leptogenesis

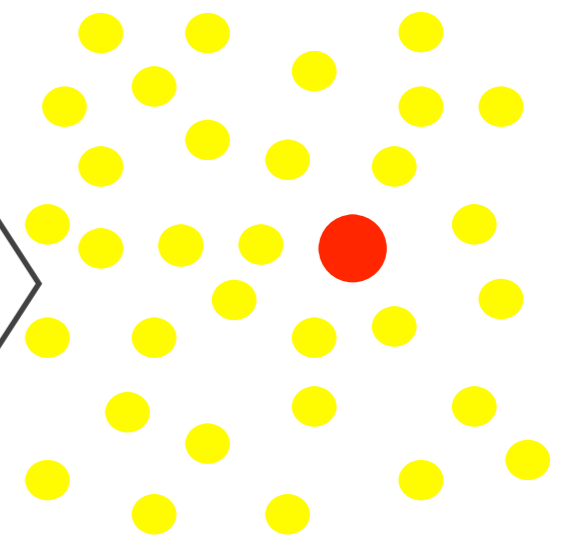
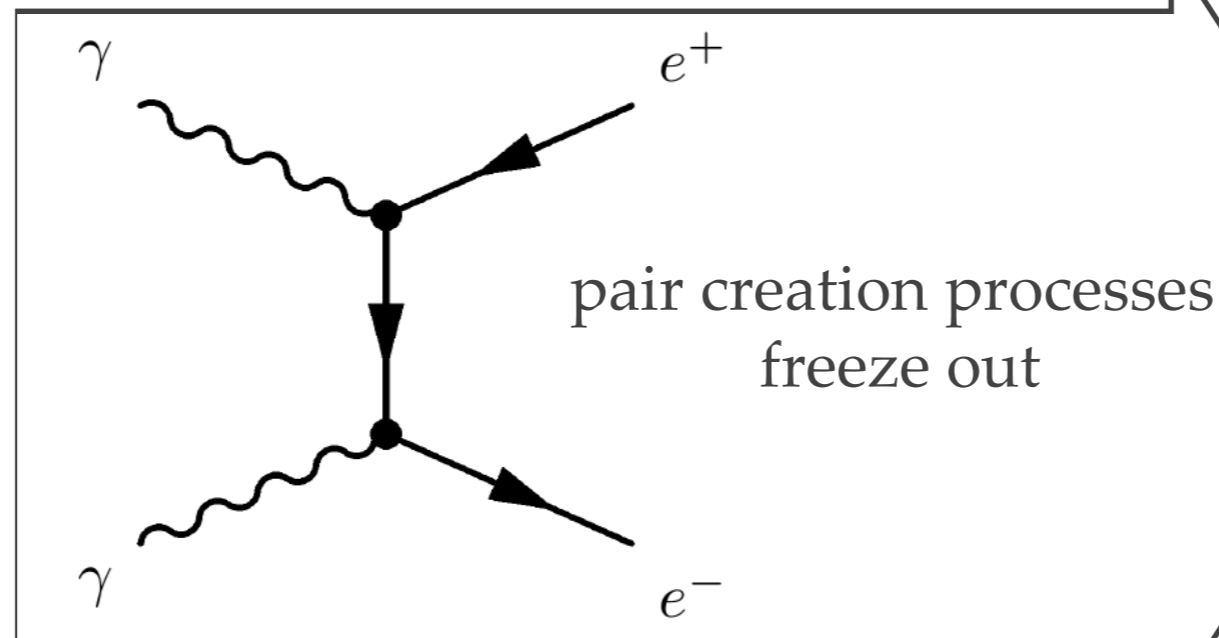
Baryon Asymmetry of the Universe

The observable universe contains almost no antimatter and a lot more photons than baryons.

e.g. Canetti et al [1204.4186](#)



$T > 2 mc^2$



$T < 2 mc^2$

CMB constraint on
baryon-to-photon ratio η :

$$6.03 \times 10^{-10} < \eta < 6.15 \times 10^{-10}$$

(Planck Collaboration)

BBN constraint on baryon-to-
photon ratio η :

$$5.8 \times 10^{-10} < \eta < 6.6 \times 10^{-10}$$

(PDG)

Thermal Leptogenesis

Basic idea

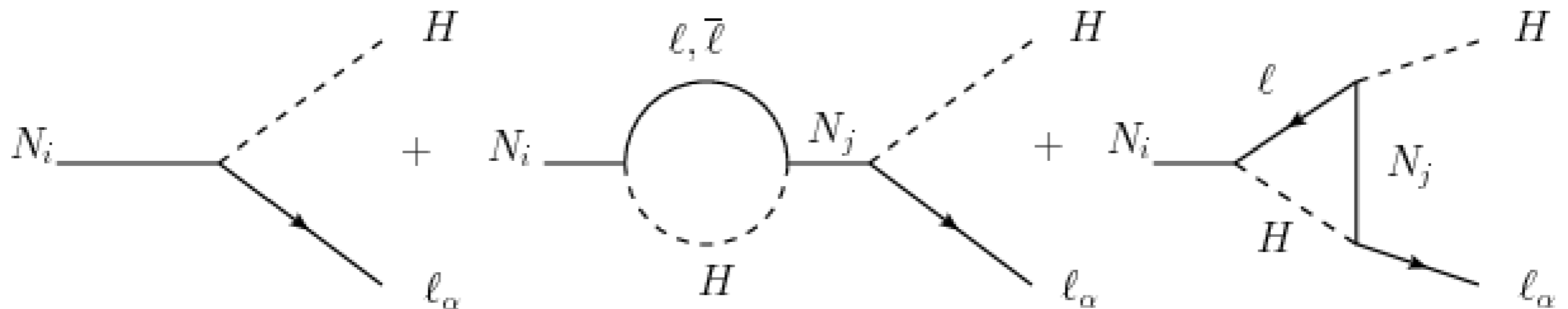
- N are around in the early universe
- N interactions are CP violating
- N may preferably decay into matter

CP violating parameter ϵ

$$\epsilon = \frac{\Gamma_{N \rightarrow \ell H} - \Gamma_{N \rightarrow \bar{\ell} H^*}}{\Gamma_{N \rightarrow \ell H} + \Gamma_{N \rightarrow \bar{\ell} H^*}}$$

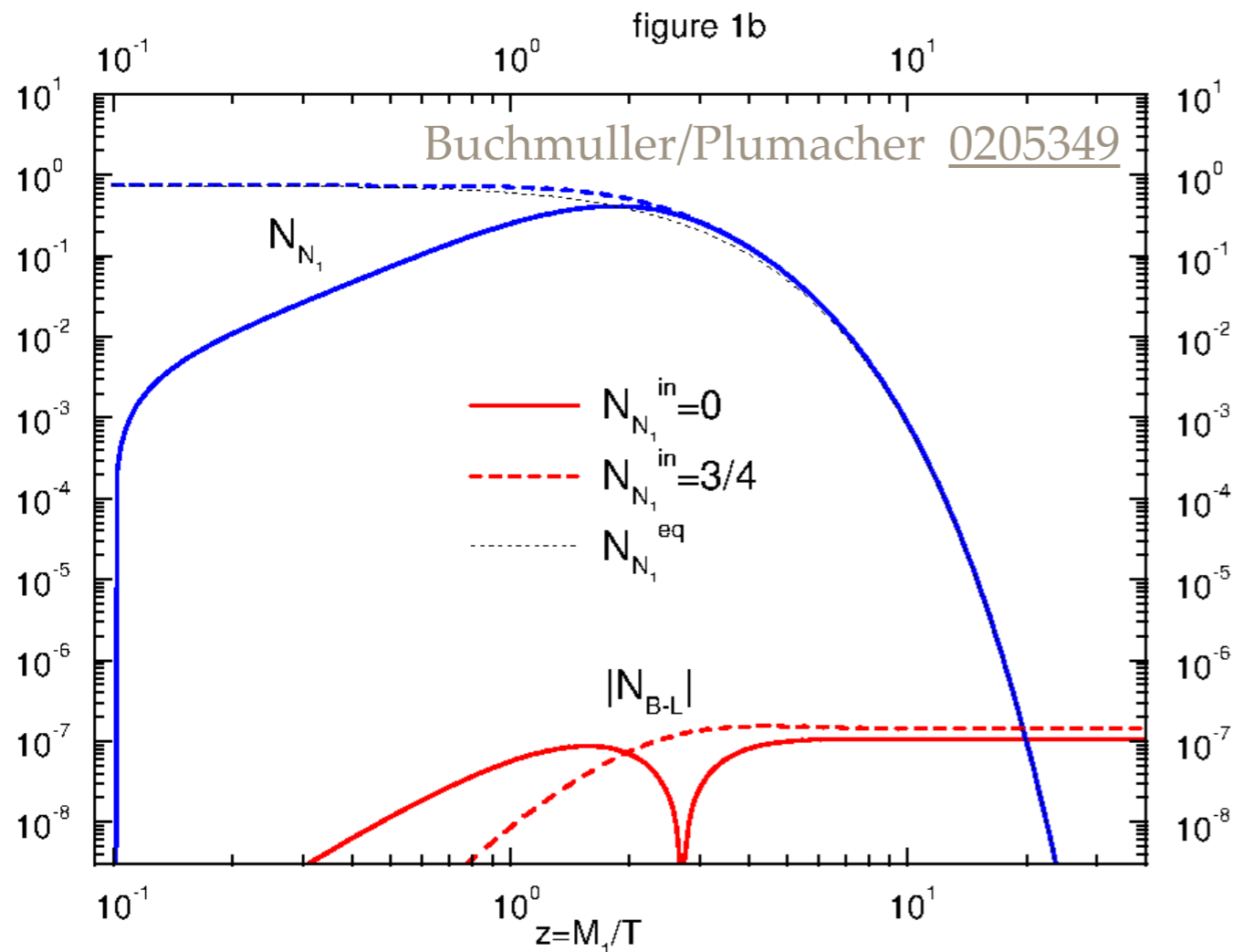
final asymmetry

$$Y_{B-L} \propto \epsilon/g_*$$



asymmetry arises from quantum interference in the plasma

Boltzmann Equation

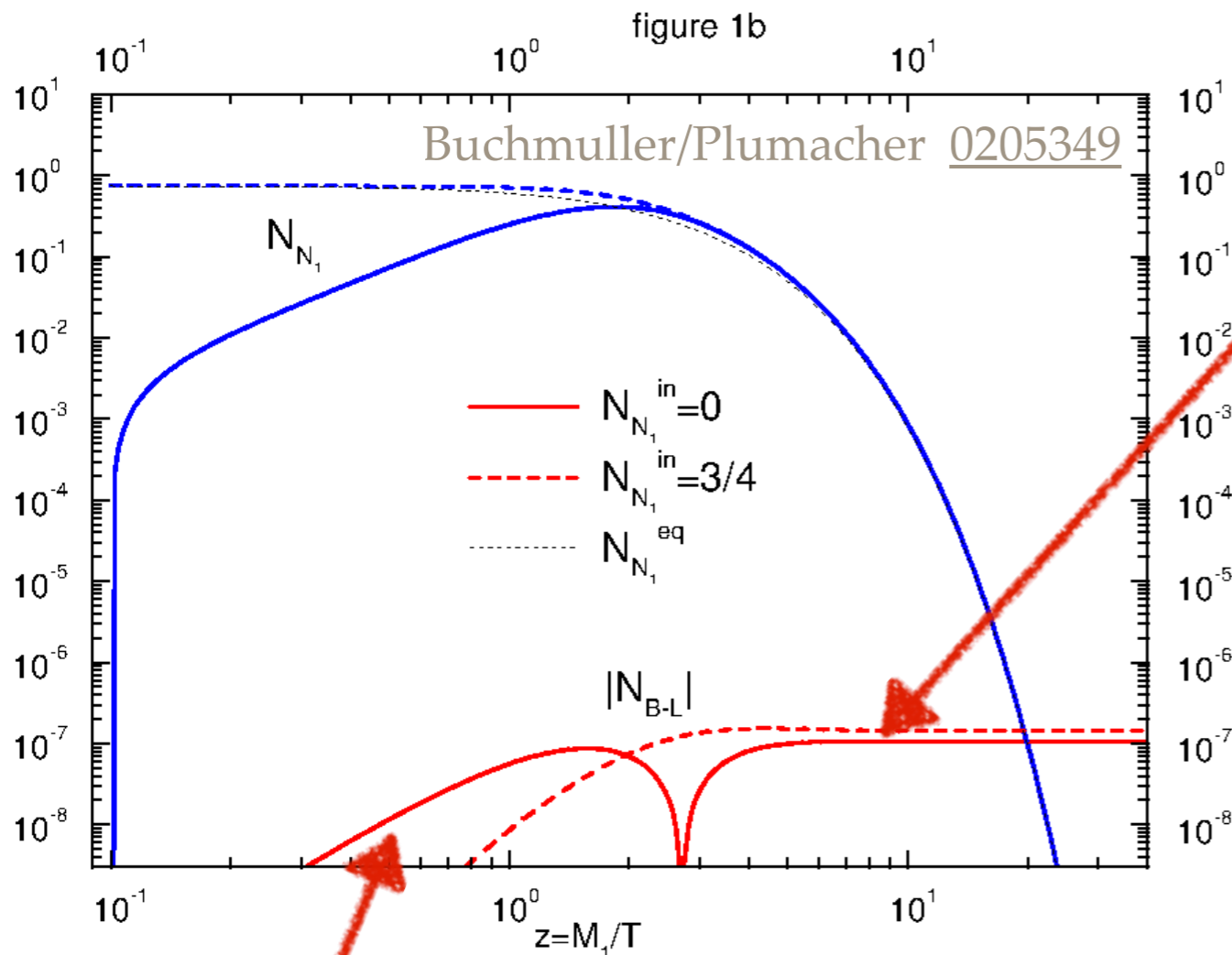


Sakharov's nonequilibrium condition can be fulfilled in two ways.

$$xH \frac{dY_N}{dx} = -\Gamma_N (Y_N - Y_N^{\text{eq}}) \quad x = M/T$$

$$xH \frac{dY_{B-L}}{dx} = \underbrace{\epsilon \Gamma_N (Y_N - Y_N^{\text{eq}})}_{\text{"source"}} - \underbrace{c_W \Gamma_N Y_{B-L}}_{\text{"washout"}}$$

Freeze-in and freeze-out



asymmetry generated during N decay ("freeze-out scenario")

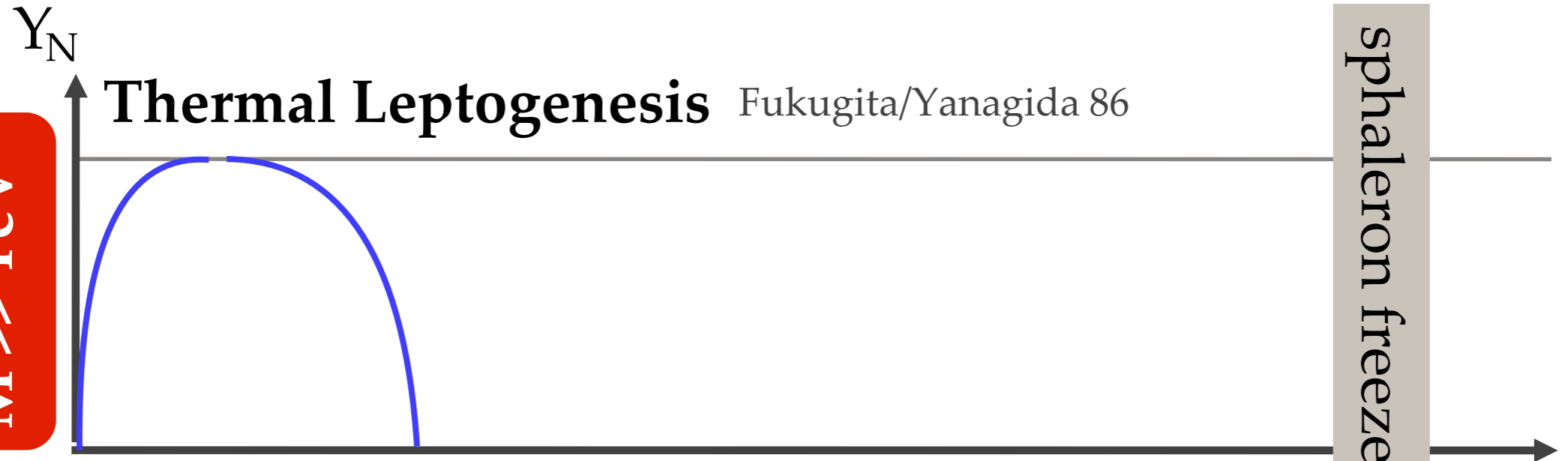
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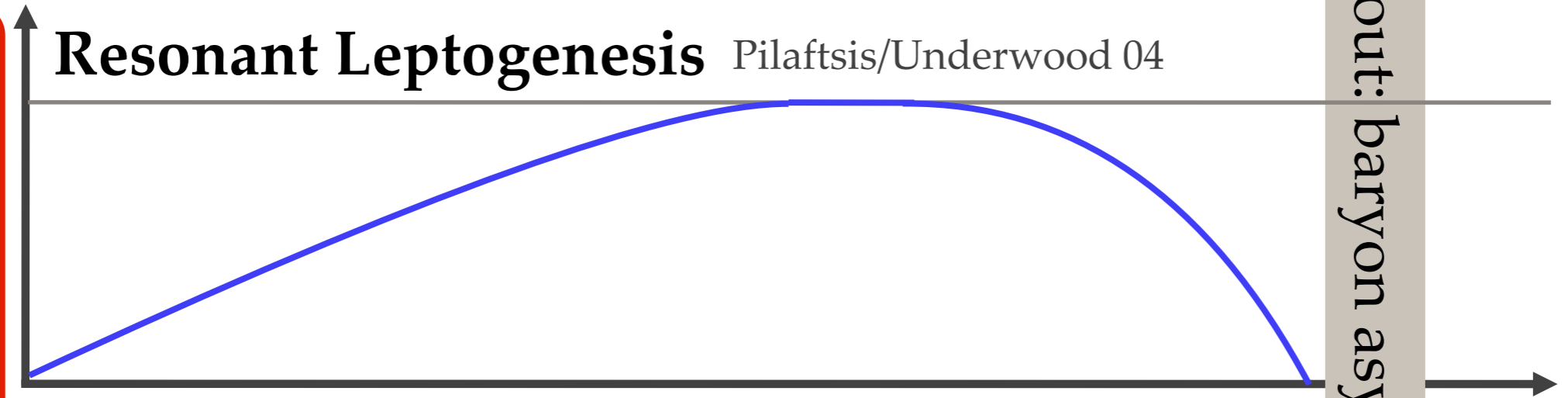
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high scale
 $M \gg \text{TeV}$

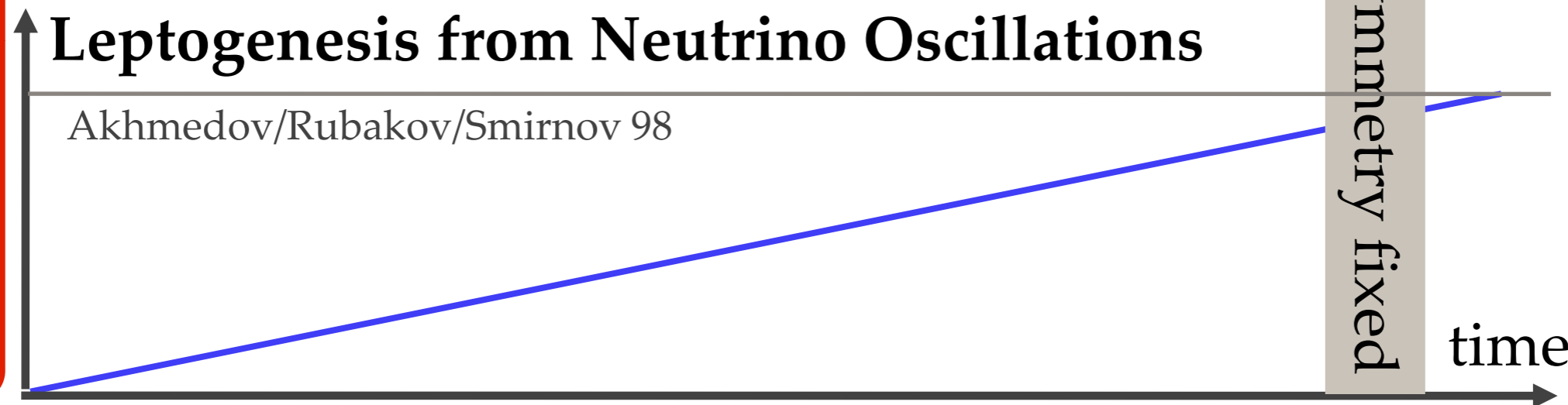


asymmetry generated in
freeze-out and decay

low scale
 $M < \text{TeV}$



asymmetry
generated in
freeze-in

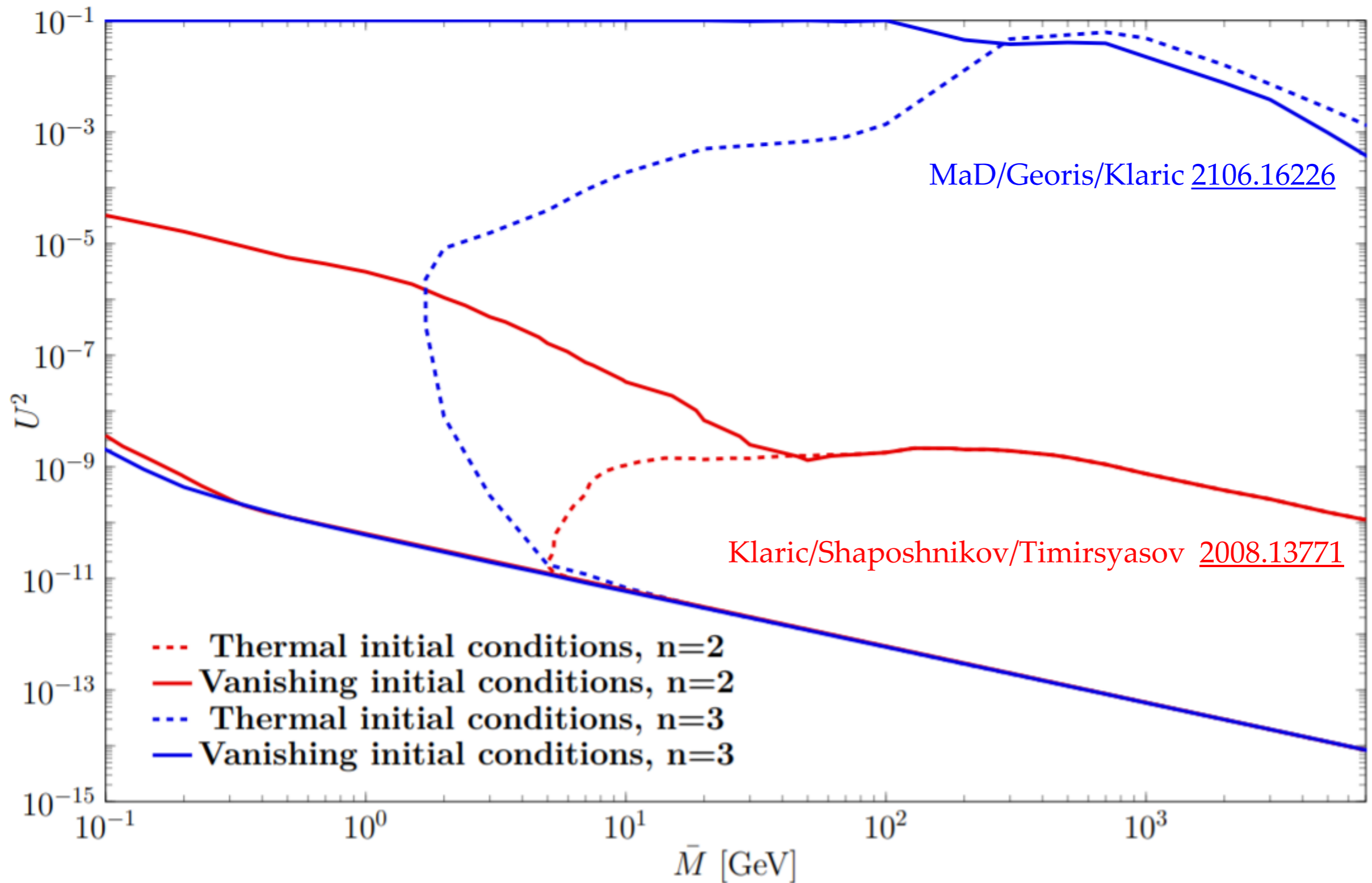


"big bang"

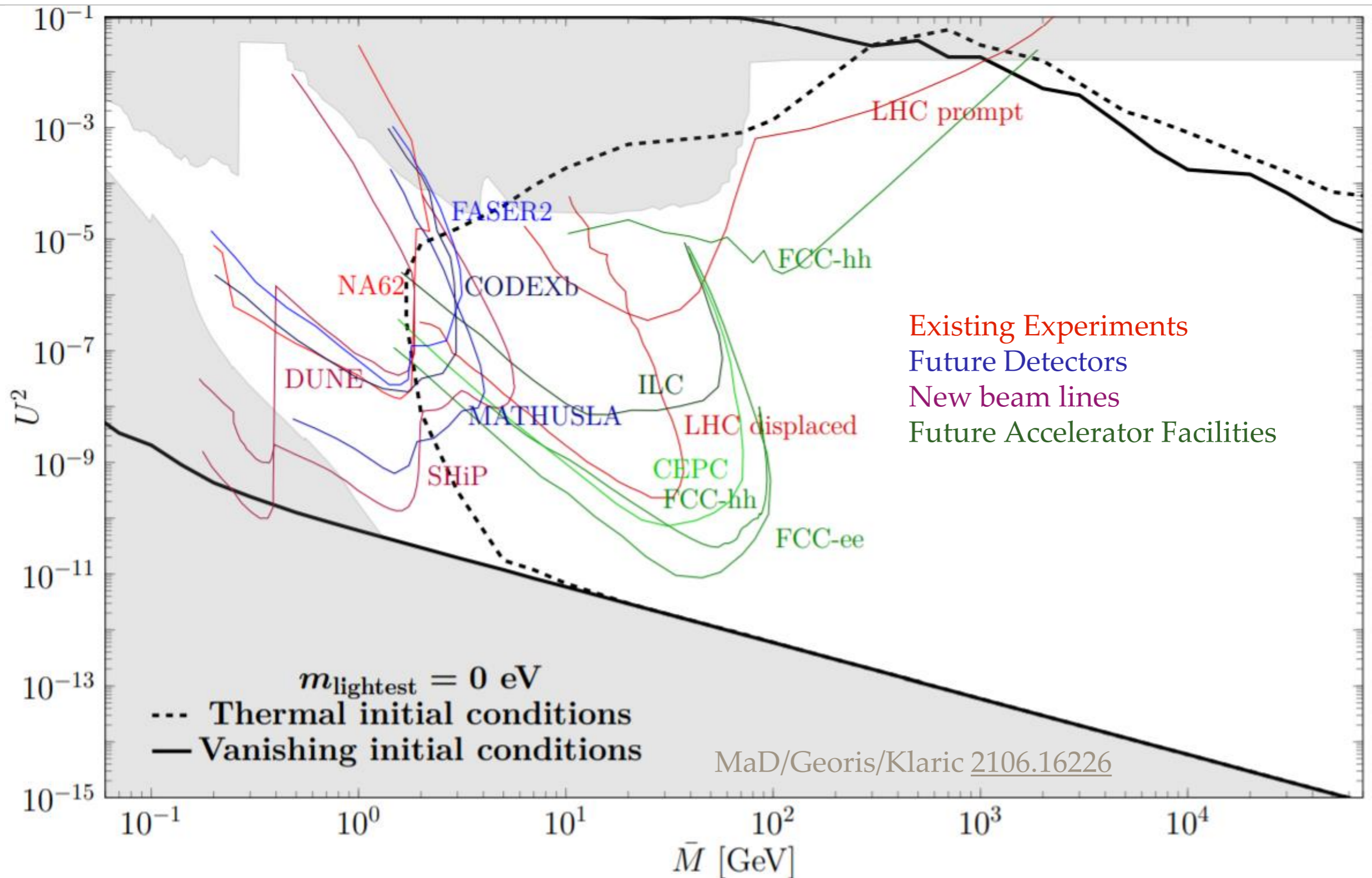
Agrawal et al [2102.12143](#)

$T = 130 \text{ GeV}$

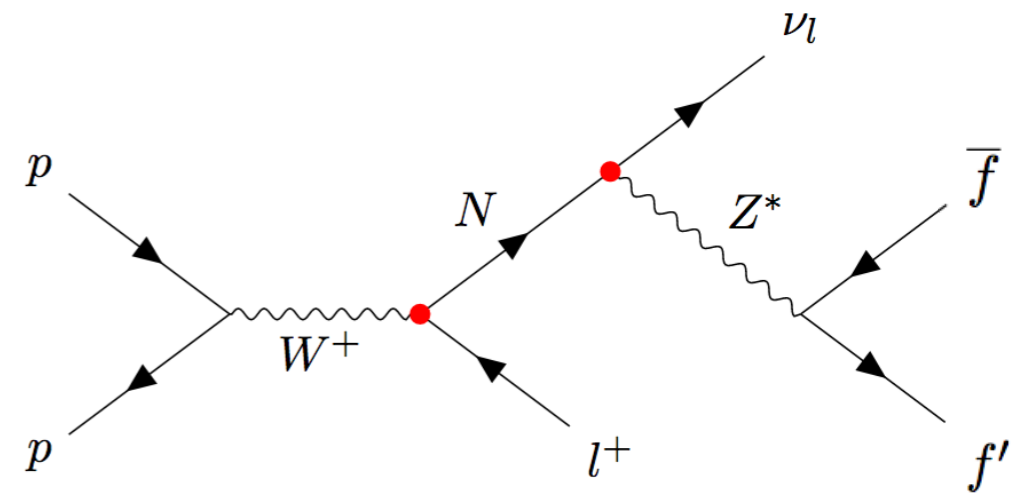
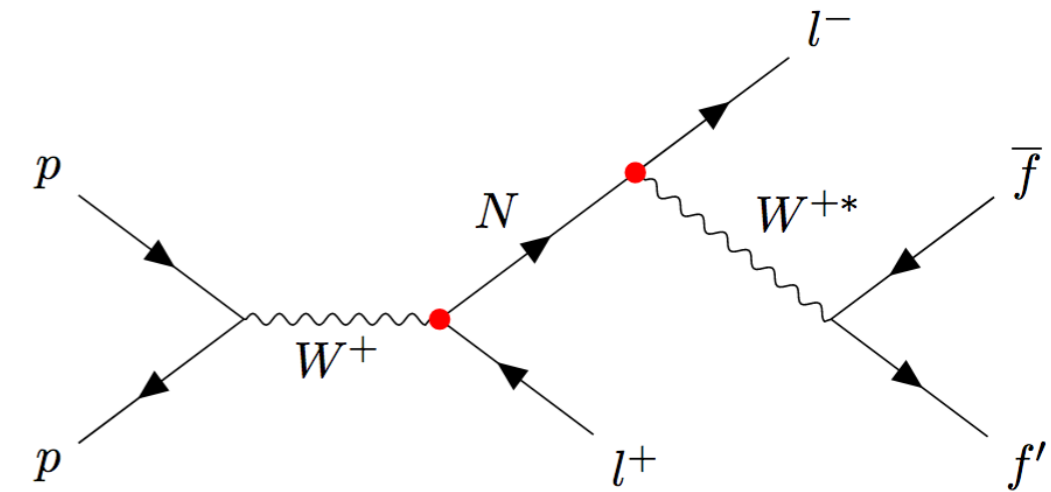
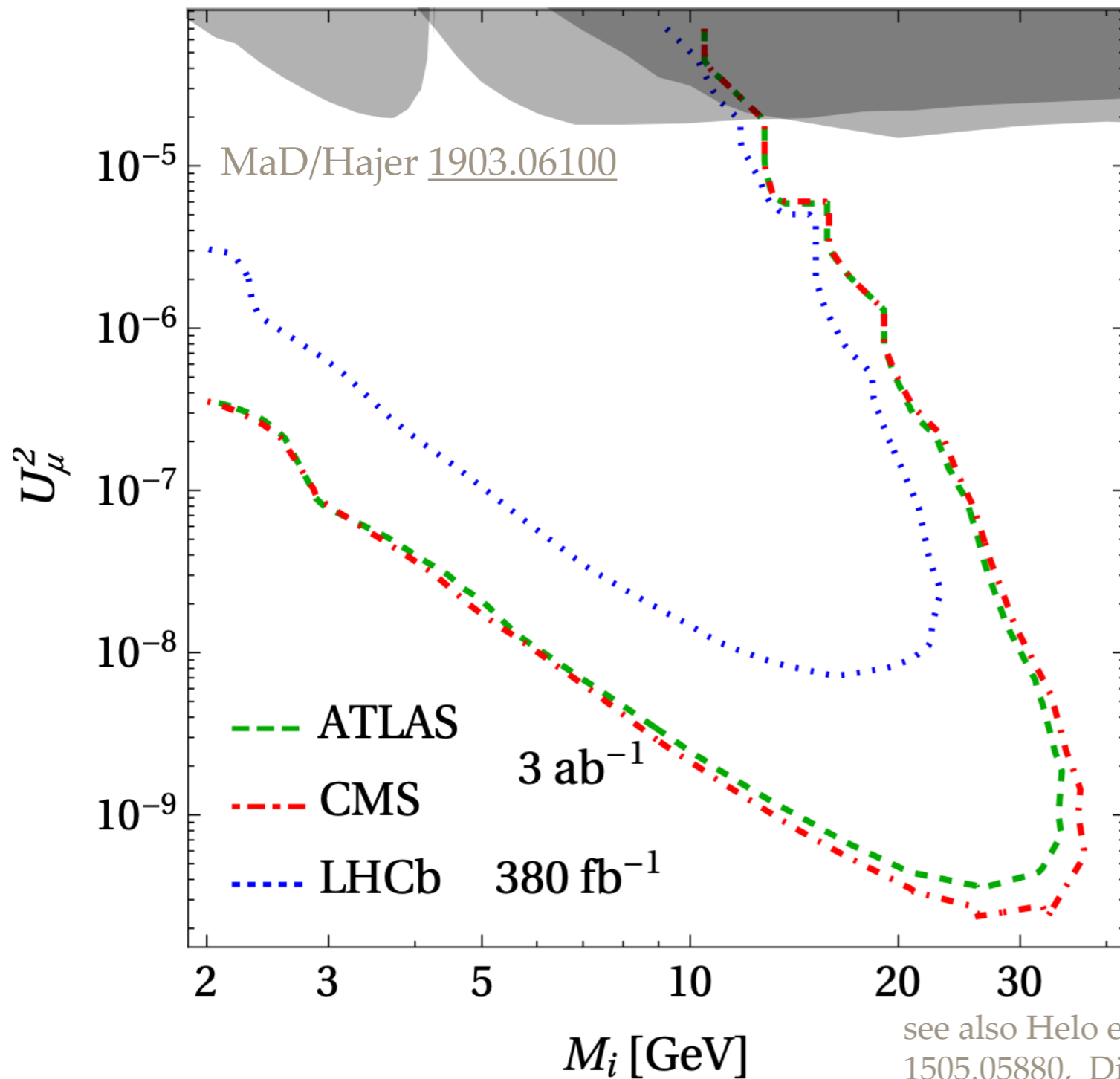
Leptogenesis with 3 HNLs vs 2 HNLs



Leptogenesis with 3 RH Neutrinos



HL-LHC Displaced Vertex Search



see also Helo et al [1312.2900](#), Izaguirre/Shuve [1504.02470](#), Gago et al [1505.05880](#), Dib/Kim [1509.05981](#), Antusch et al [1612.02728](#), Cottin et al [1806.05191](#), Abada et al [1807.10024](#), Boiarska et al [1902.04535](#), Liu et al [1904.01020](#), Dib et al [1903.04905](#), Cvetič et al [1805.00070](#), [1905.03097](#), ...

What can we learn?

Dirac vs Majorana

- **LNV vs LFV decay rates** e.g. Anamiati / Hirsch / Nardi [1607.05641](#)
- **Angular distribution** e.g. Arbelaez et al [1712.08704](#), Balantekin/Gouvea/Kayser [1808.10518](#)
- **Flavour mixing pattern** e.g. Dib / Kim / Wang / Zhang [1605.01123](#)

CP properties

e.g. Cvetič / Dib / Kim / Saa [1503.01358](#)

Mass spectrum

e.g. Antusch / Fischer [1709.03797](#)

Test seesaw mechanism and leptogenesis

Hernandez / Kekic / Lopez-Pavon / Racker / Savaldo [1606.06719](#),

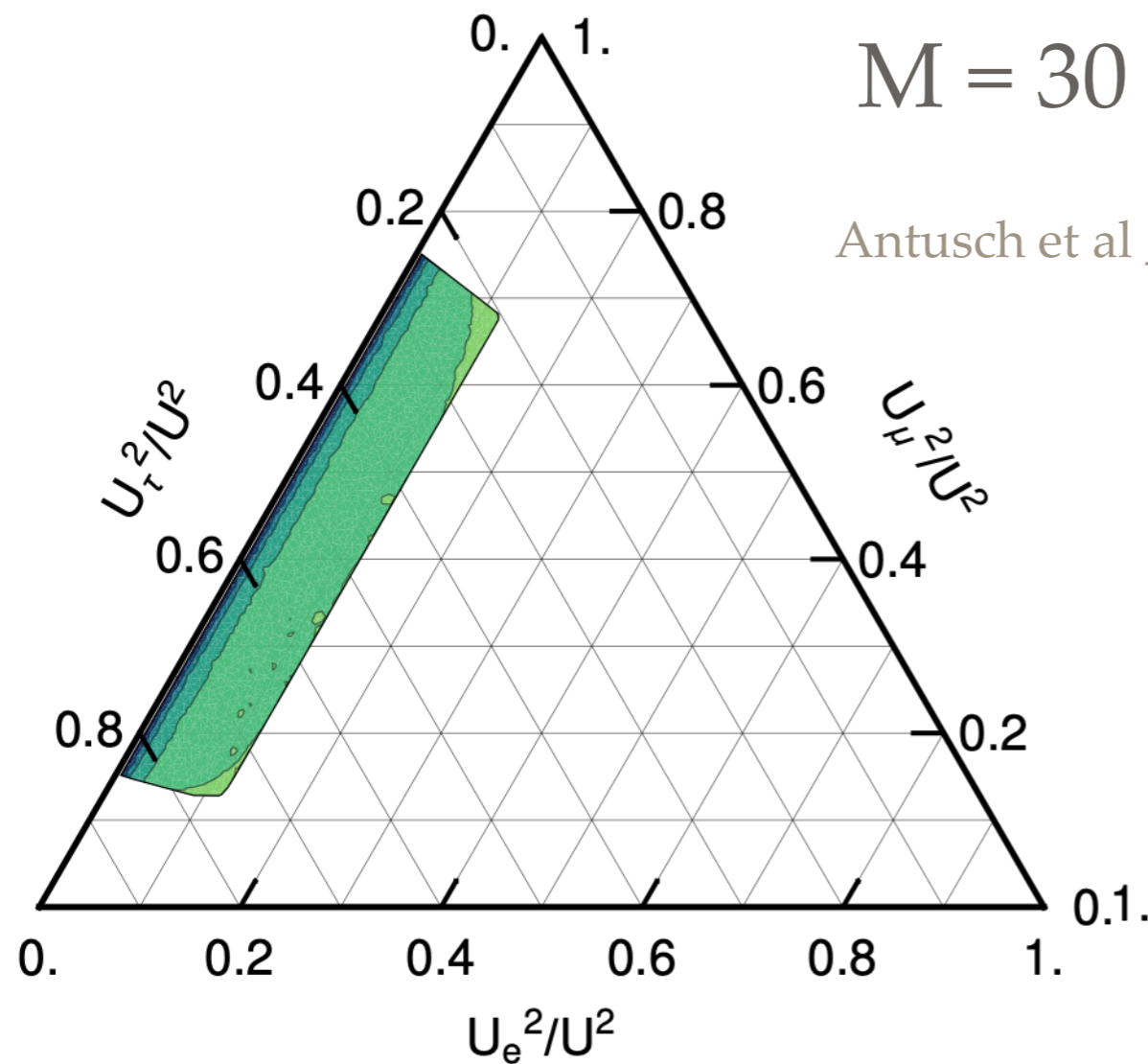
MaD / Garbrecht / Gueter / Klaric [1609.09069](#)

Antusch/Cazzato/MaD/Fischer/Garbrecht/Gueter/Klaric [1710.03744](#)

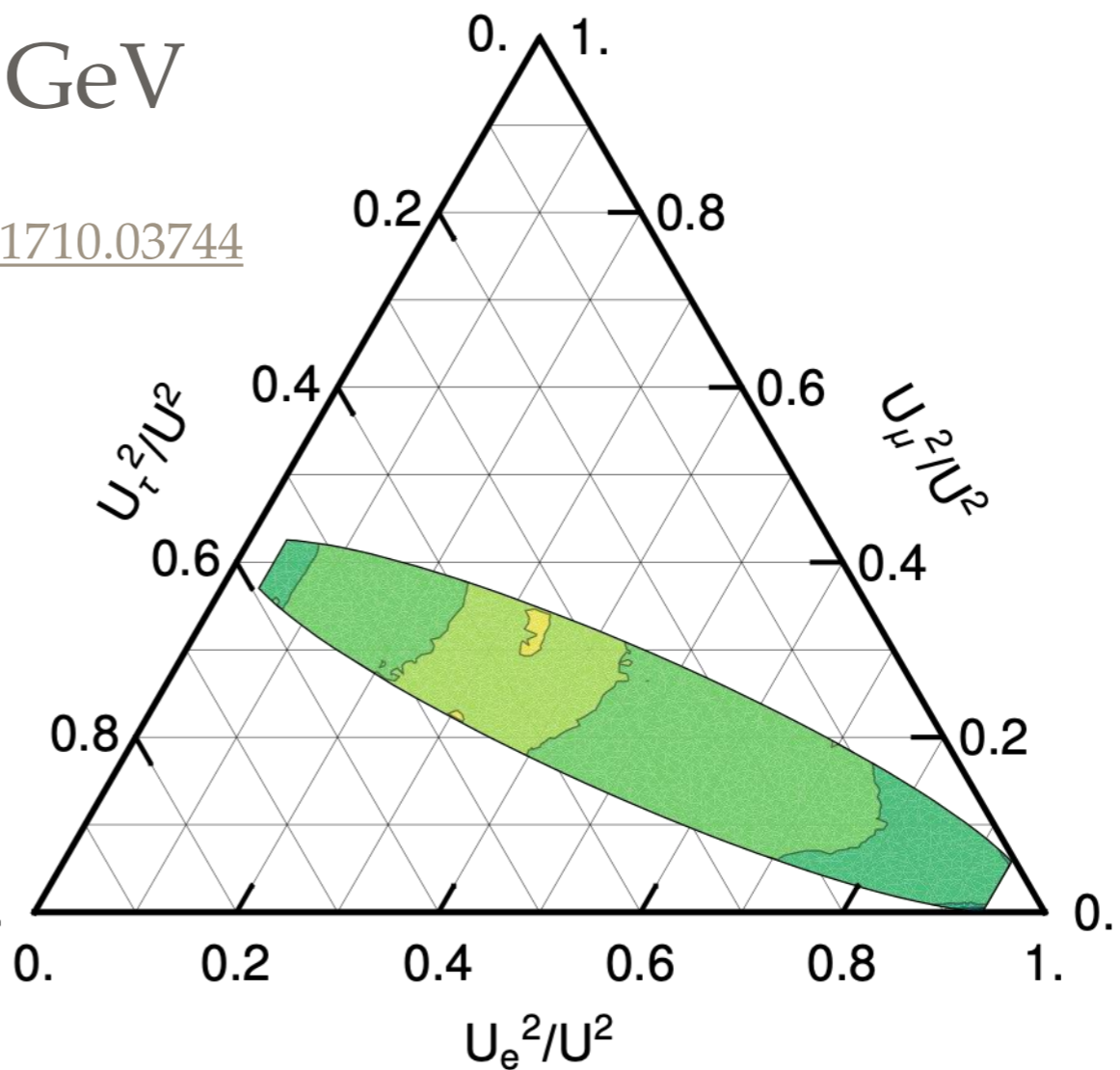
Constraints from Leptogenesis in Model with 2 Heavy Neutrinos

$M = 30 \text{ GeV}$

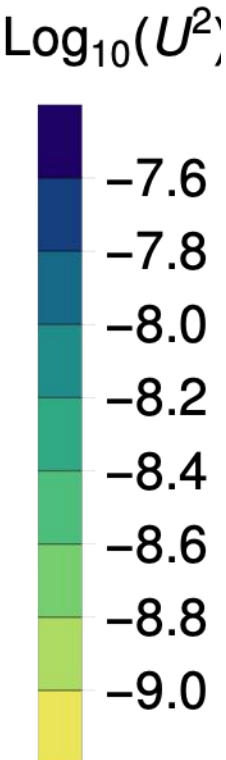
Antusch et al [1710.03744](#)



normal neutrino mass ordering

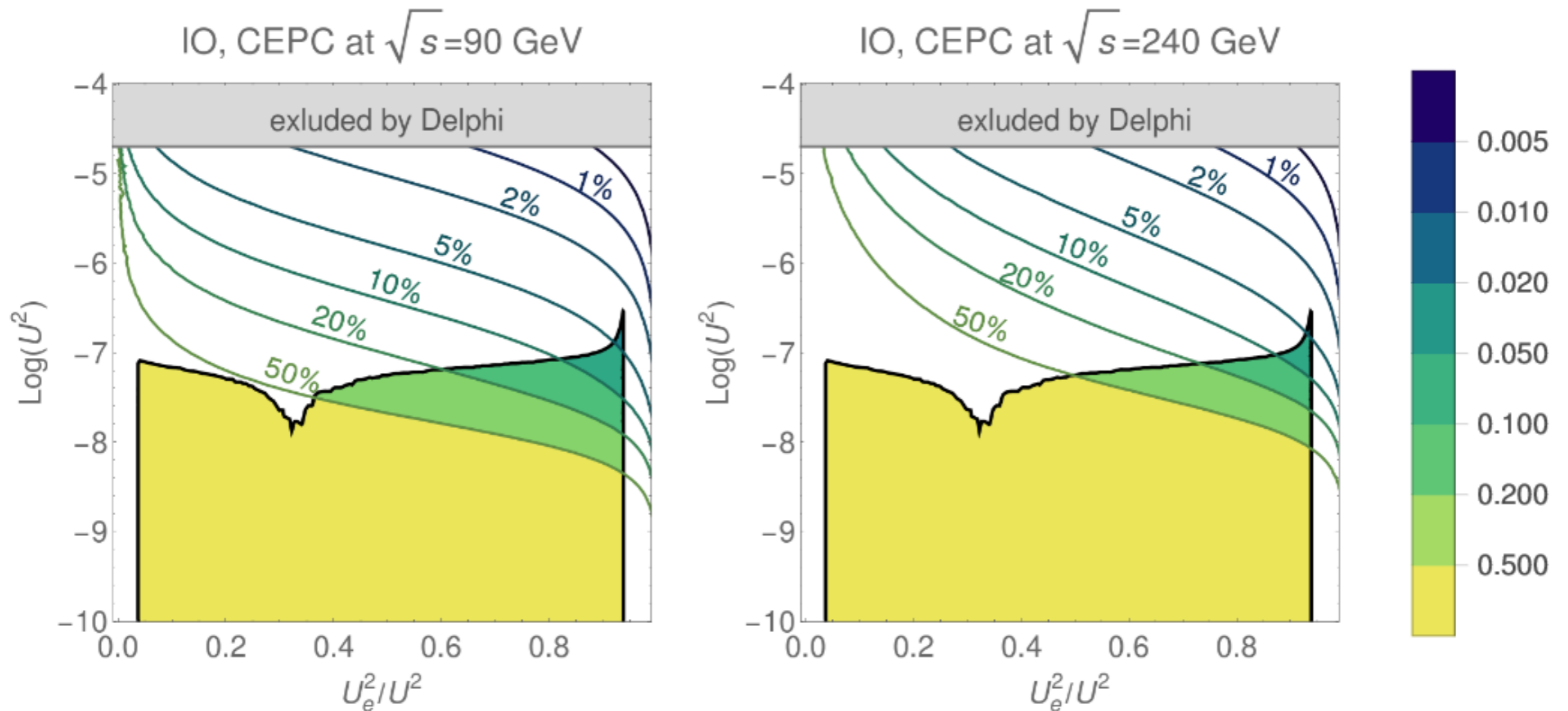


inverted neutrino mass ordering



Large U^2 require strong hierarchies in couplings to SM generations

How well can this be measured?



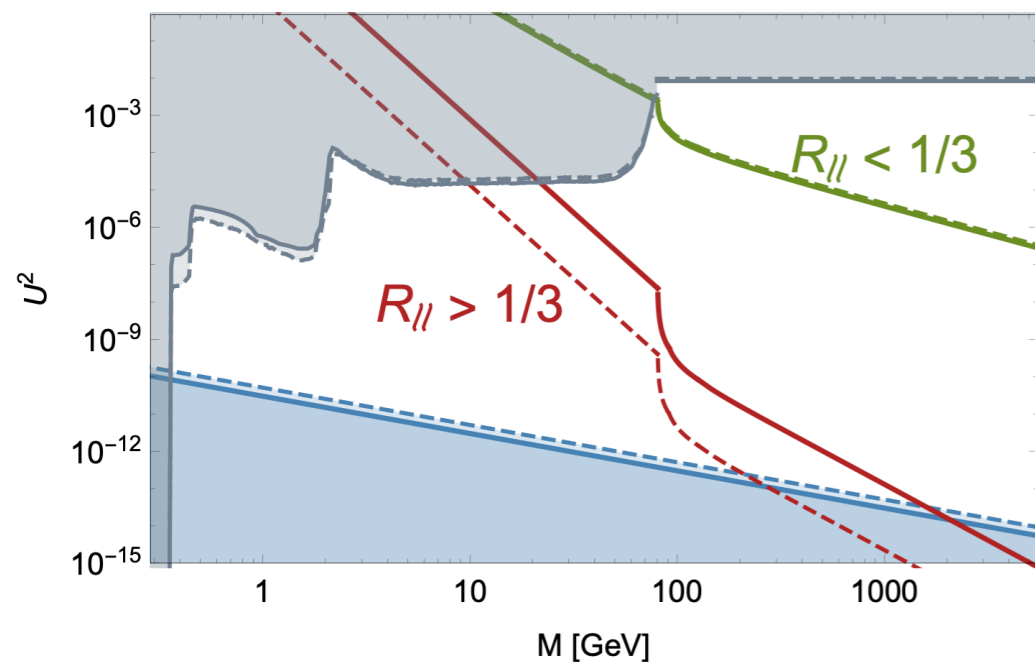
Plots were made for 0.1/ab at Z pole, nowadays expect 16/ab,
⇒ an order of magnitude better accuracy possible!
⇒ **With a bit of luck, CEPC can make percent level measurement**

How to measure ΔM ?

ratio of LNV to LNC decays
is sensitive to ΔM

$$\mathcal{R}_{ll} = \frac{\Delta M_{\text{phys}}^2}{2\Gamma_N^2 + \Delta M_{\text{phys}}^2}$$

Anamiati et al [1607.05641](#)



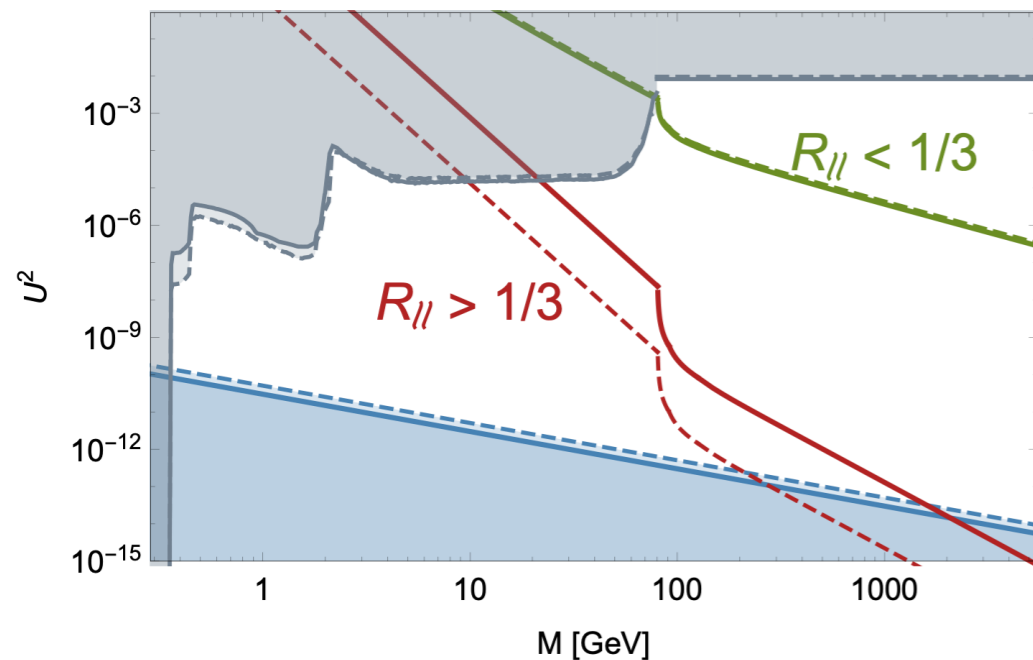
MaD/Klaric/Klose [1907.13034](#)

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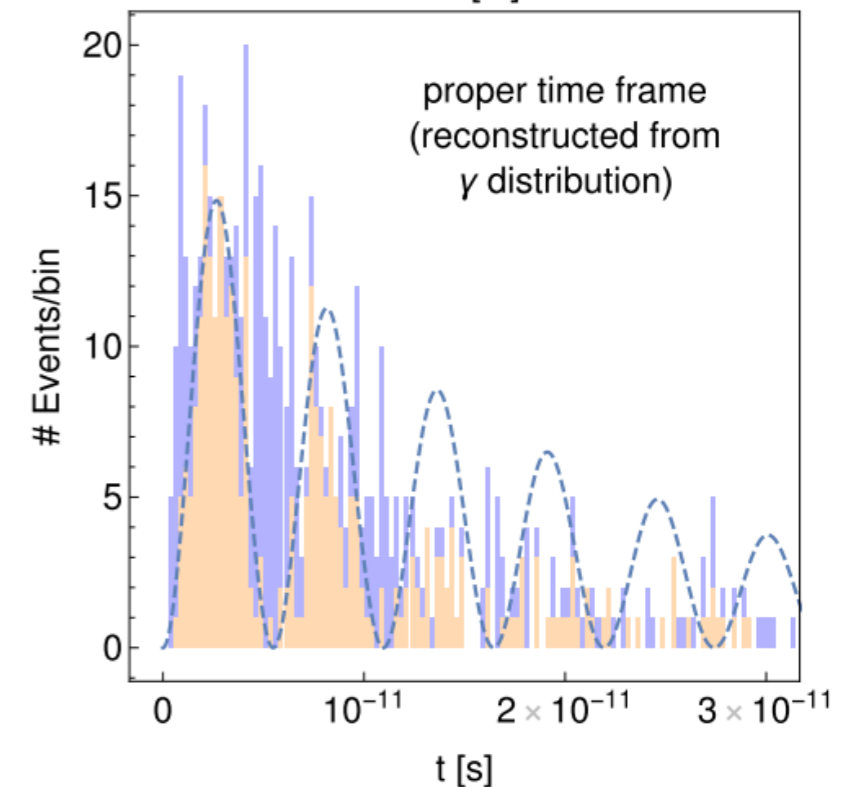
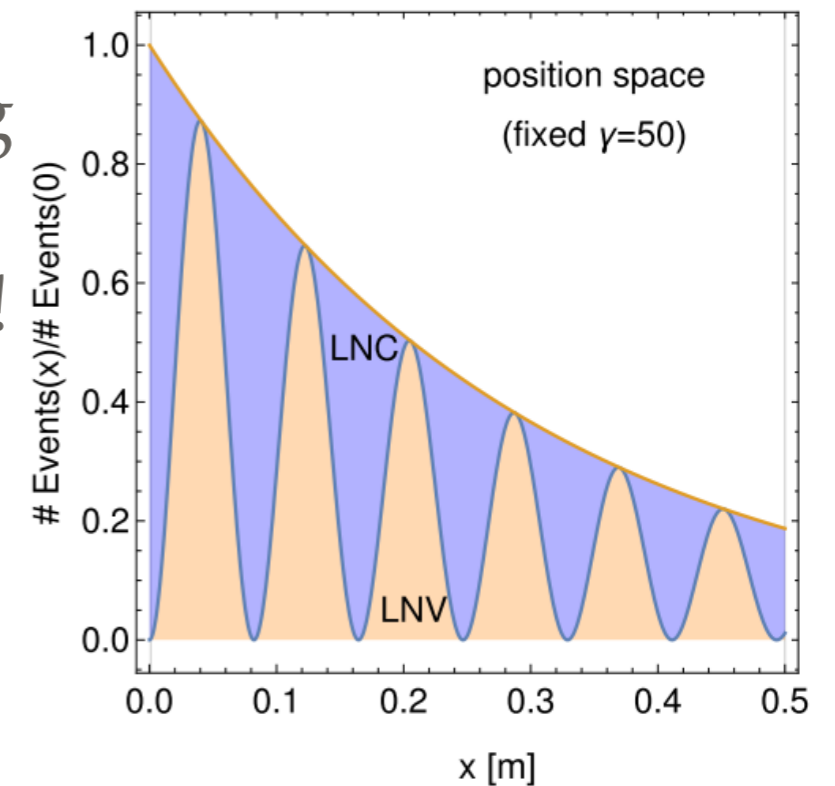
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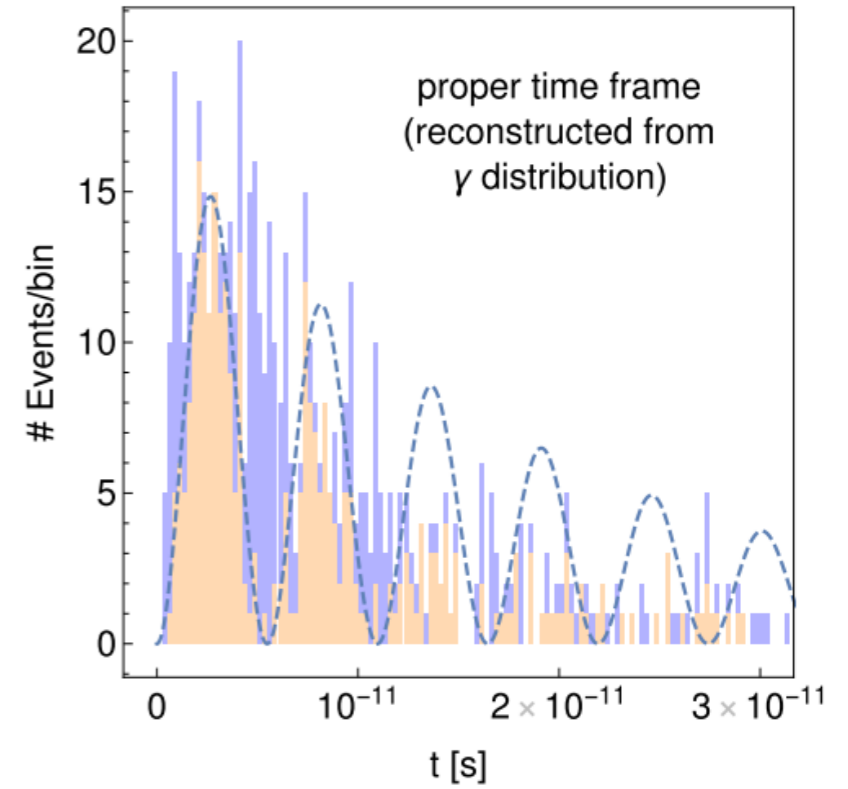
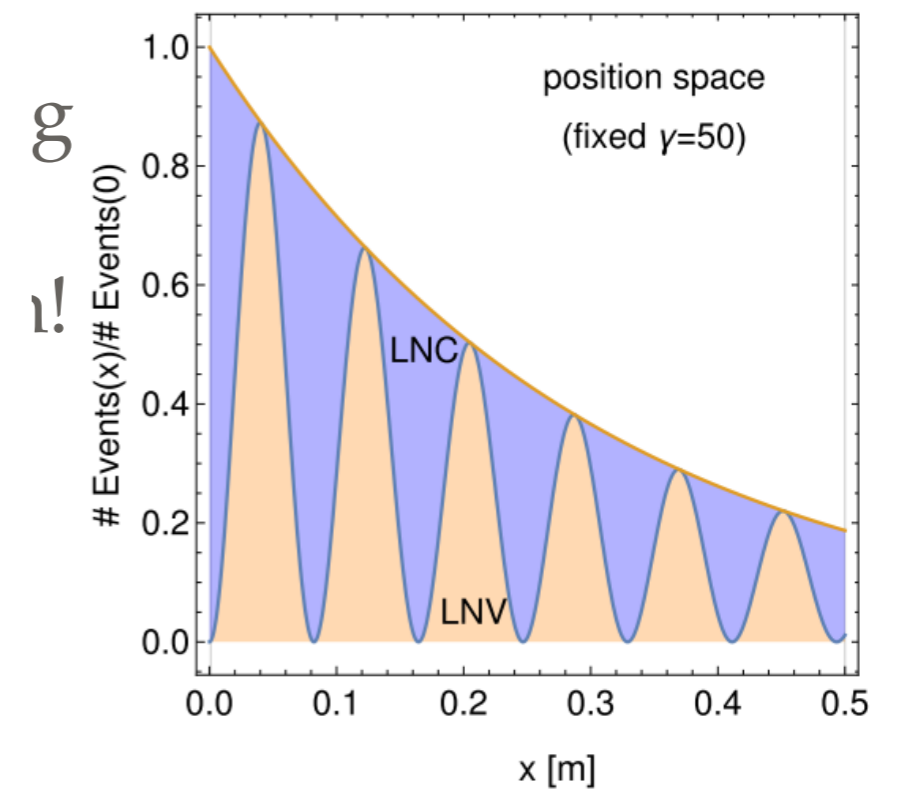
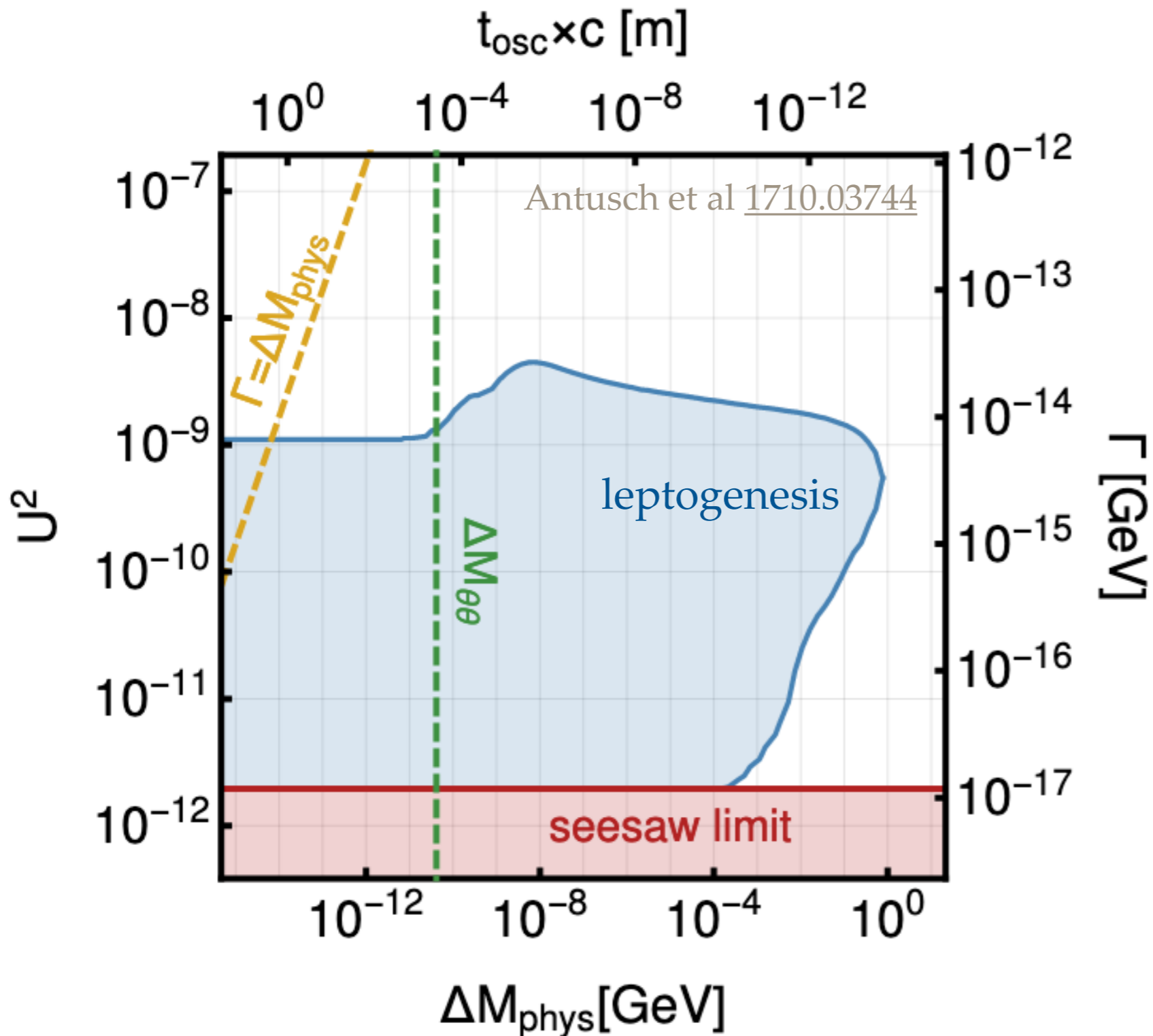
MaD/Klaric/Klose [1907.13034](#)

spatially resolving this ratio gives more information!

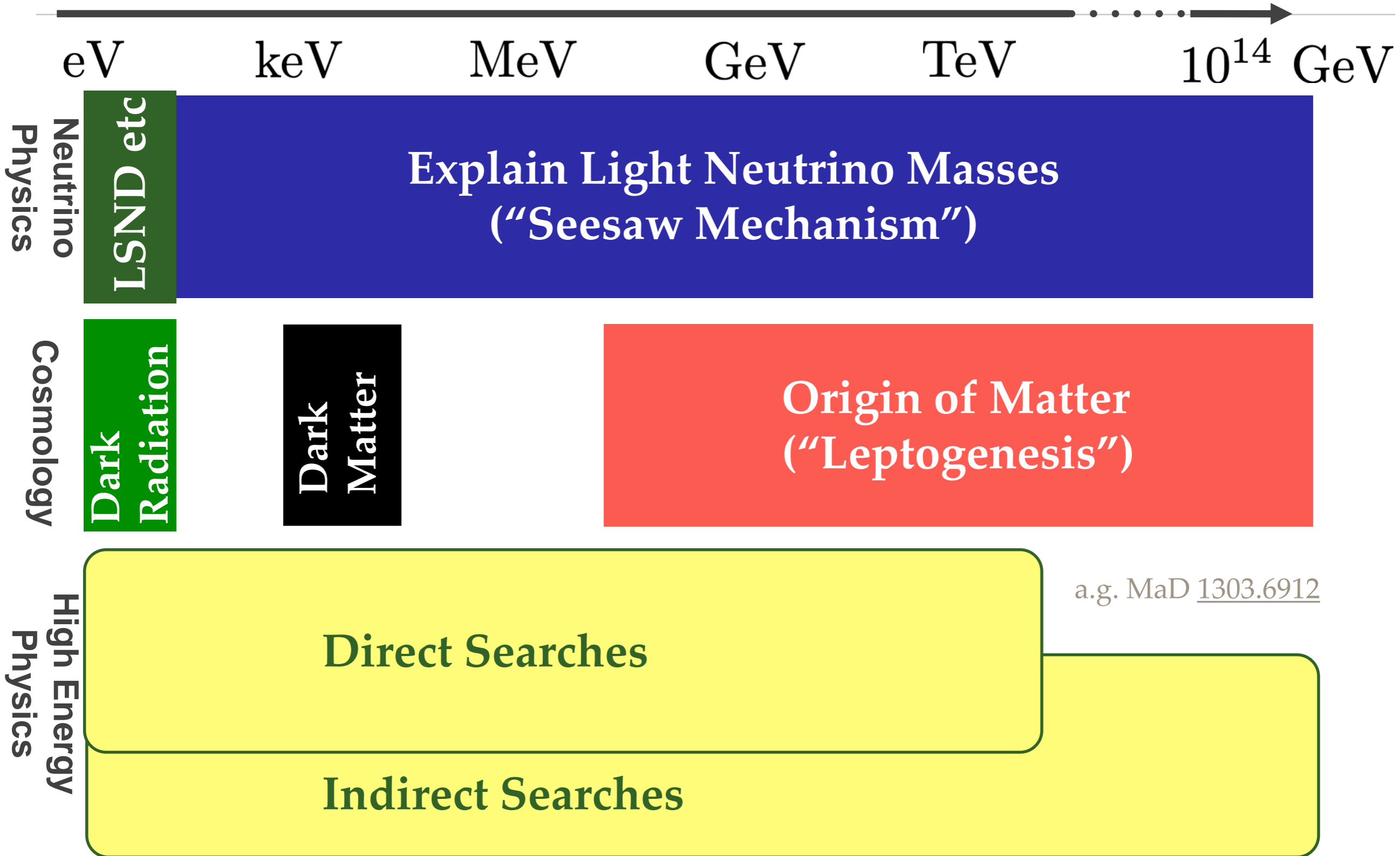
Antusch et al [1709.03797](#)



How to measure ΔM ?



Heavy Neutrino Mass Scale



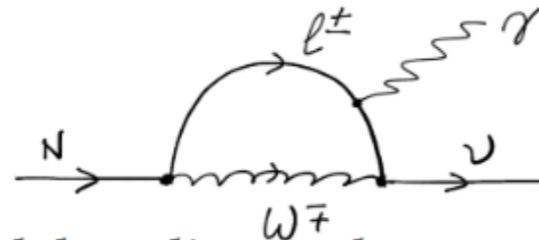
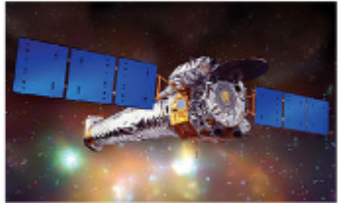
a.g. MaD [1303.6912](#)

Sterile Neutrino DM

How to find Sterile Neutrino DM?

Indirect searches

- radiative decay $N \rightarrow \nu \gamma$ gives emission line at $M/2$



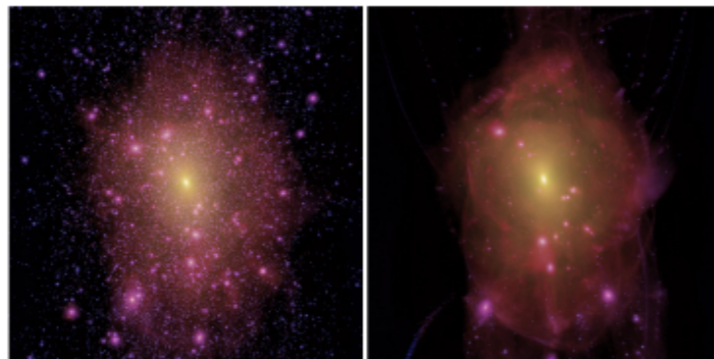
- 3.5 keV excess observed, but disputed
- new missions (XRISM, ATHENA, Lynx...)

Structure formation

Free streaming of DM affects formation of structures at sub-Mpc lengths

- matter power spectrum (Lyman α forest, 21 cm astronomy, weak lensing)
- # collapsed structures (dwarf galaxy counts, reionisation history; collapsed objects at high-z)

- matter distribution within collapsed objects



- uncertainties: baryonic feedback, IGM temperature...

Production mechanisms

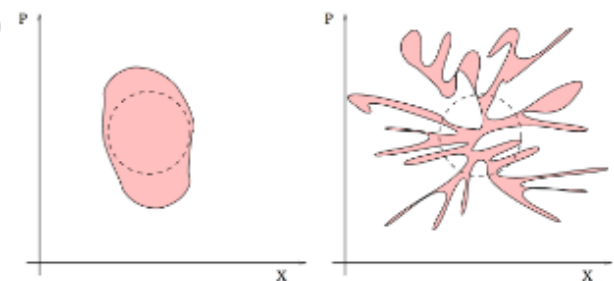
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- thermal production through mixing-suppressed weak interaction (resonant or non-resonant)
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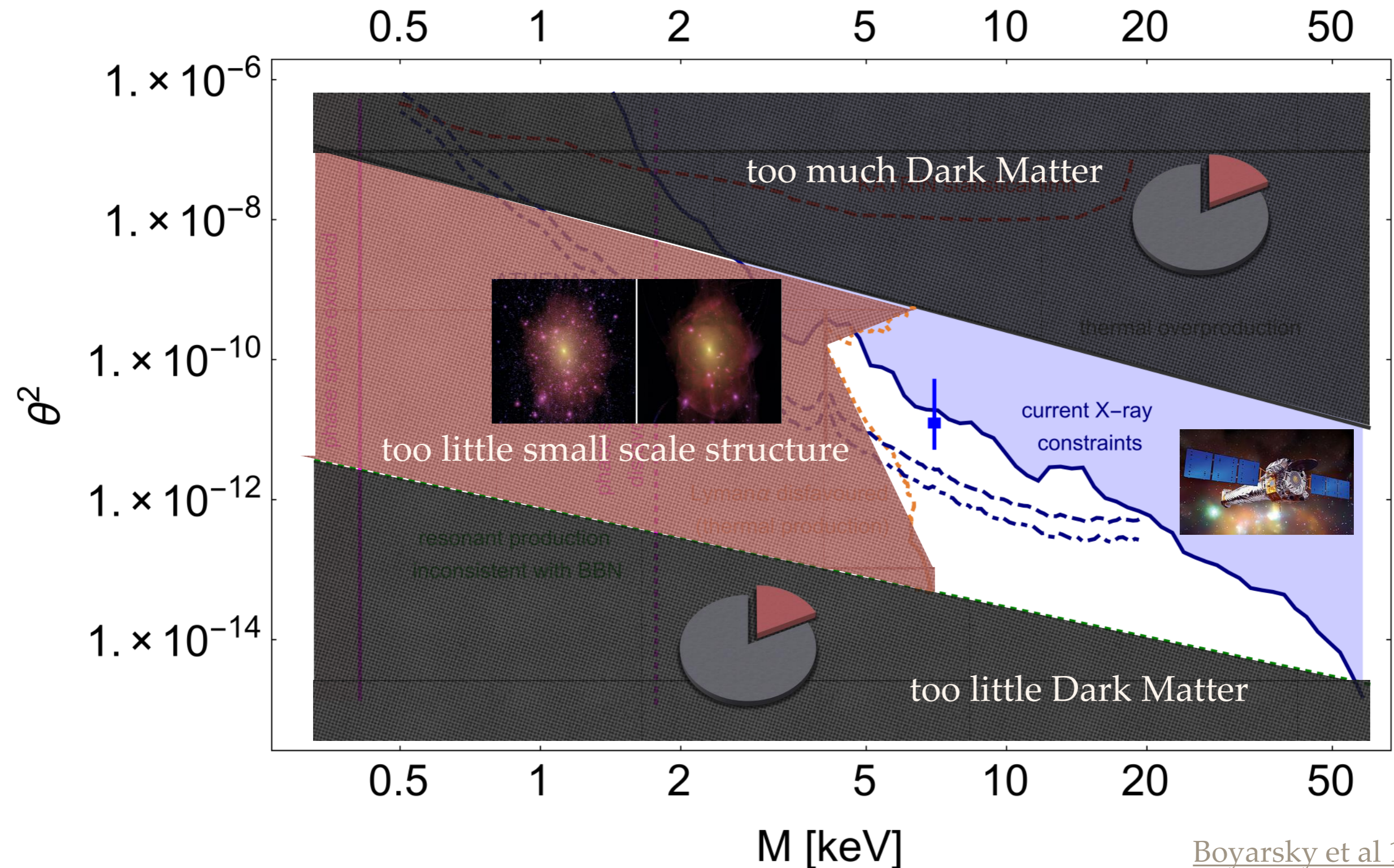
Third Generation of Matter Particles			
max. charge	I	II	III
name	u	c	t
quarks	d	s	b
leptons	ν_e	ν_μ	ν_τ
	e	μ	τ
			g
			γ
			Z
			W
			H

Phase space

- fermions are subject to Pauli principle
 $M > 25 \text{ eV}$
- applying this throughout the history of the universe yields Tremaine-Gunn bound
- Tremaine-Gunn bound depends on production mechanism, excludes $M < 0.5 \text{ keV}$
disfavors $M < 2 \text{ keV}$



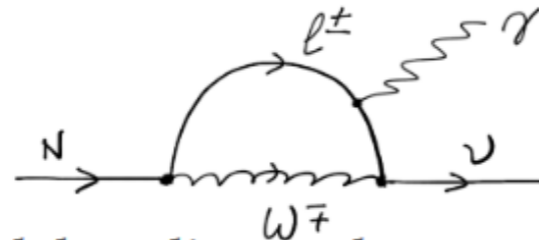
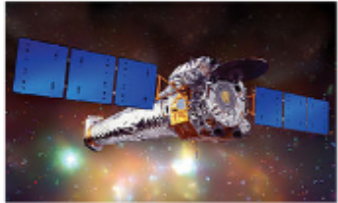
Sterile Neutrino Dark Matter



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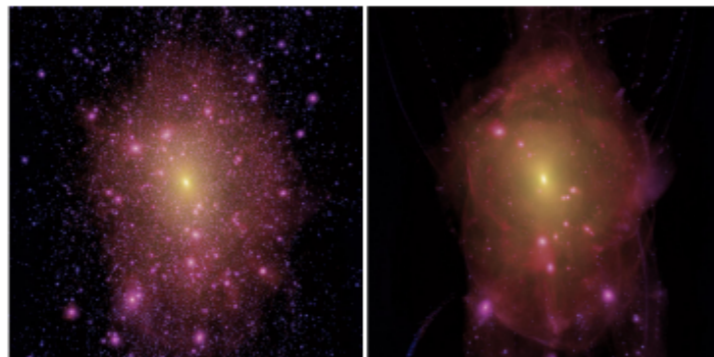
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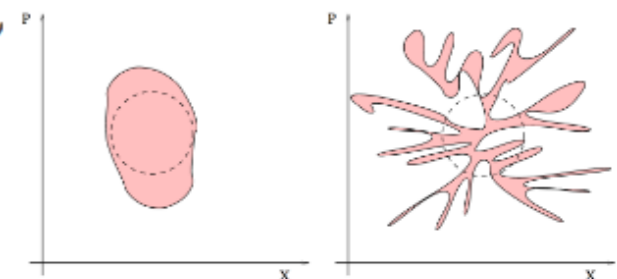
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Third Generation of Matter Particles			
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up	u	c	t
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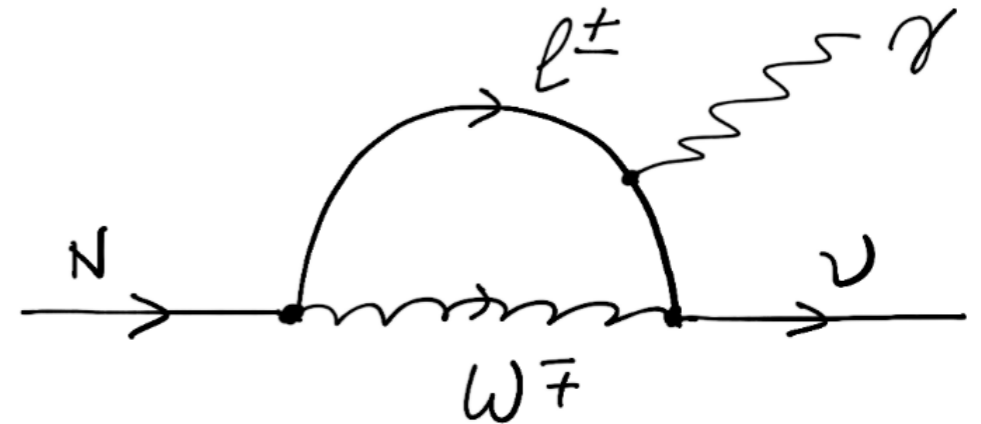
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Indirect DM Searches

loop level decay into photons

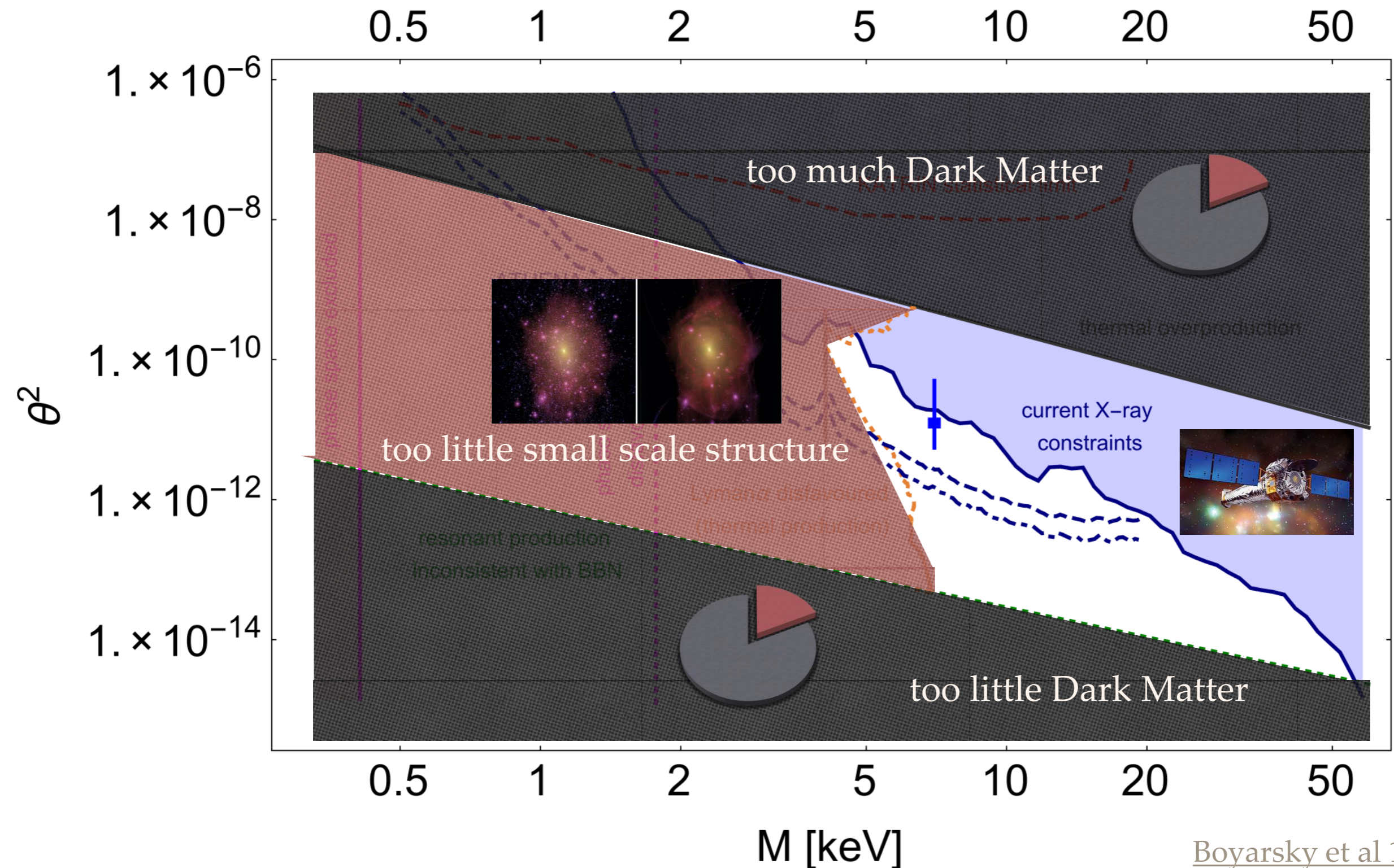


$$\Gamma_{N \rightarrow \gamma \nu} = \frac{9 \alpha G_F^2}{256 \pi^4} \theta^2 M^5 = 5.5 \times 10^{-22} \theta^2 \left[\frac{M}{1 \text{ keV}} \right]^5 \text{ sec}^{-1} .$$

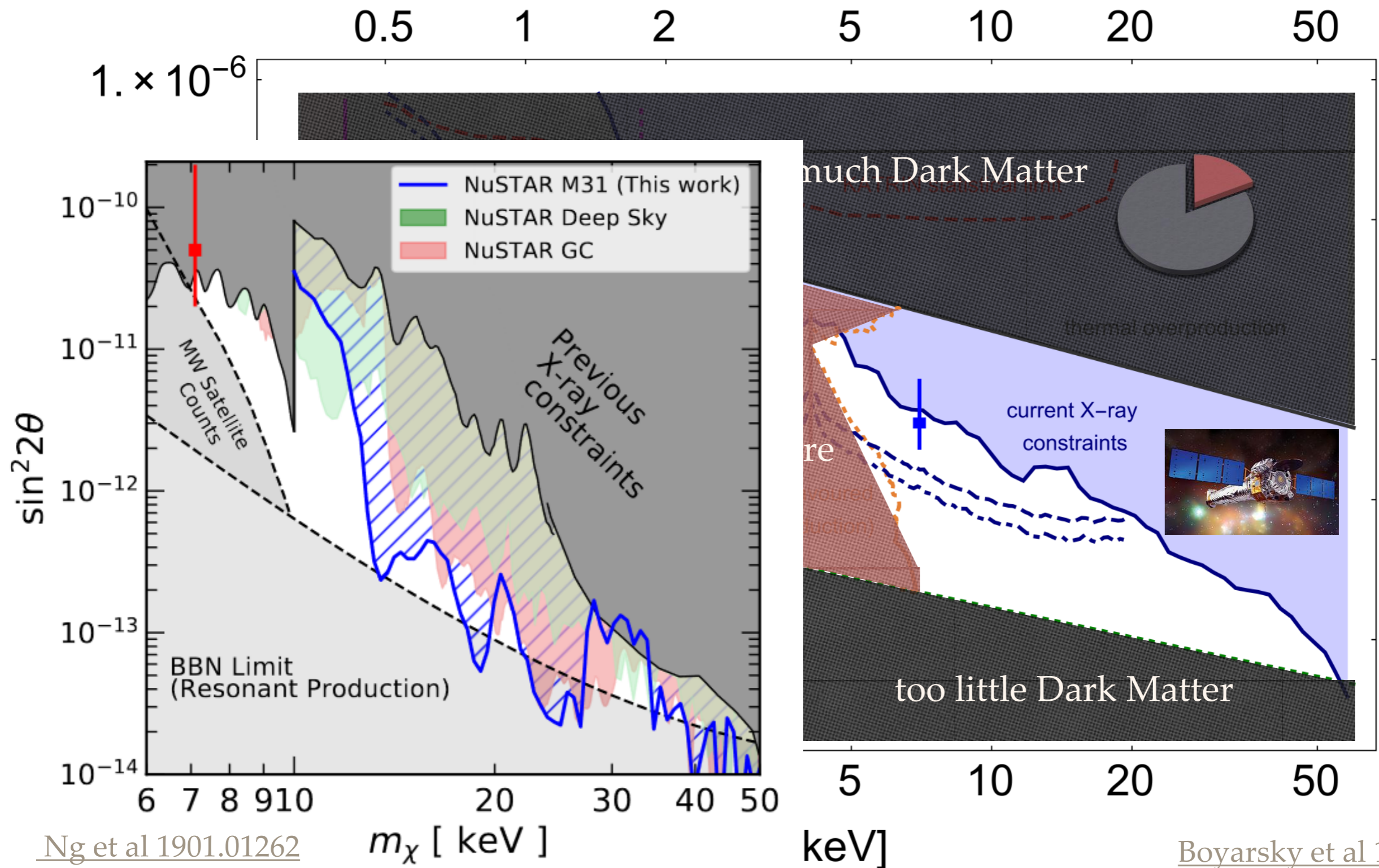
One can search for an emission line!



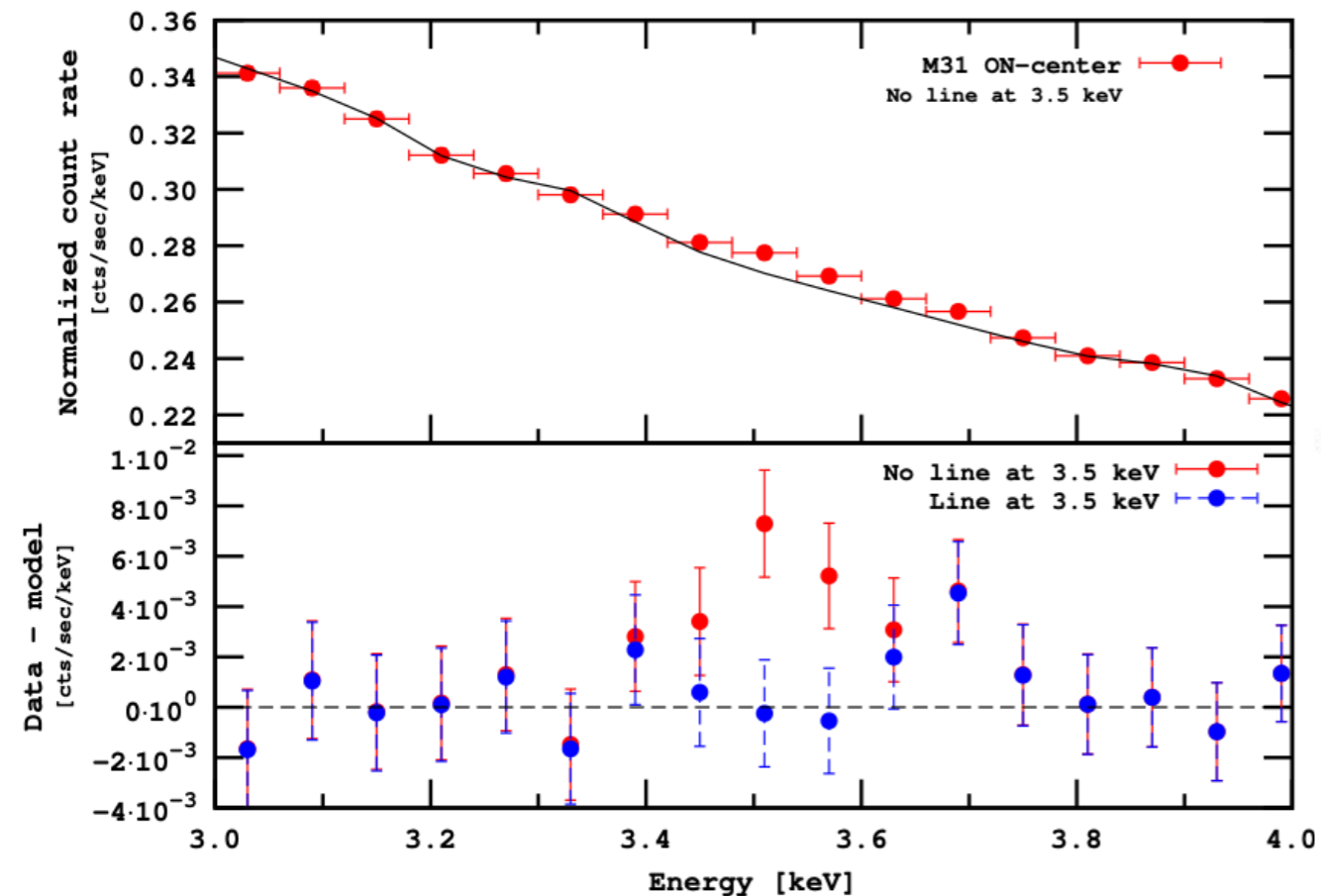
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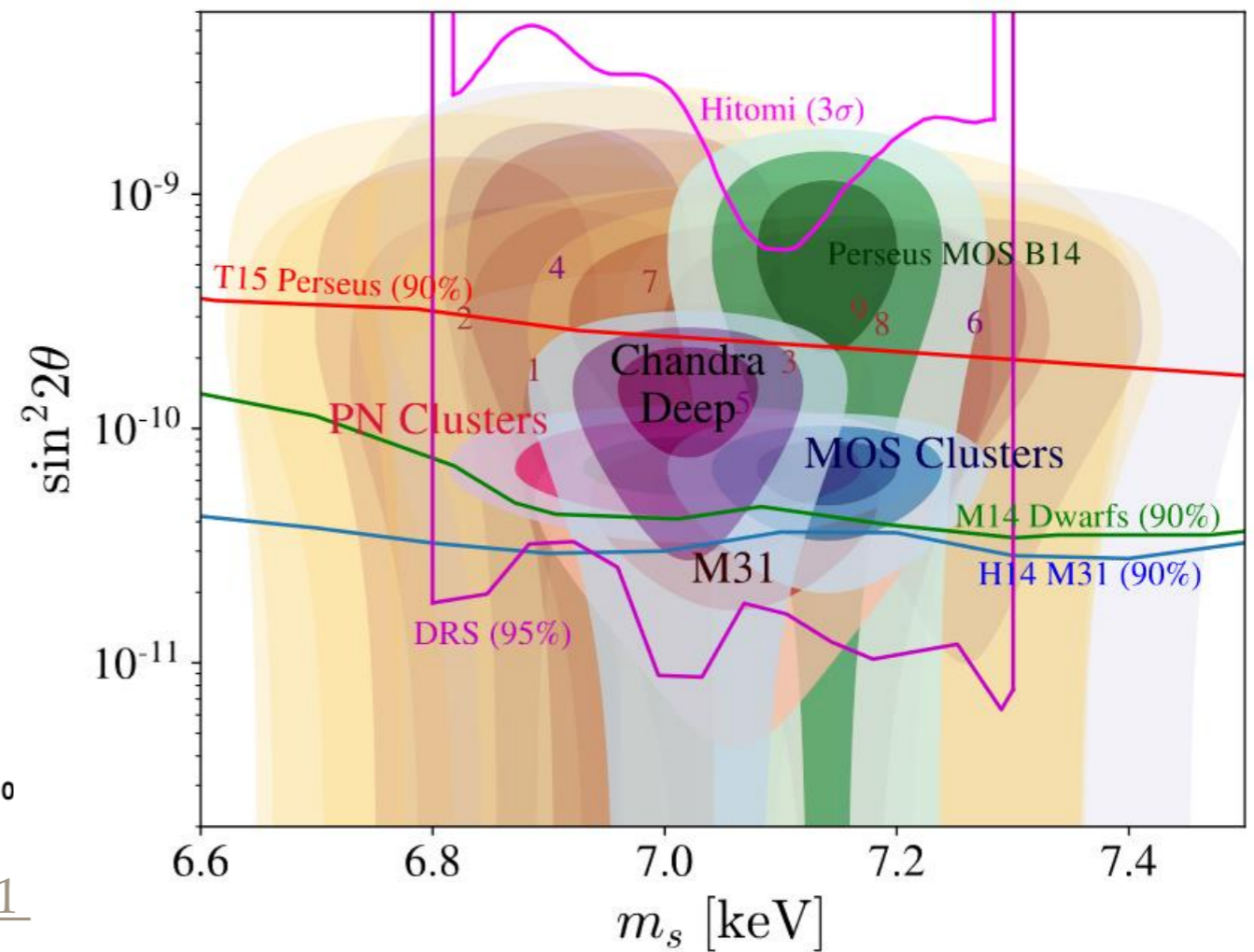
Sterile Neutrino Dark Matter



Has the line been seen?



Boyarsky et al [1402.4119](#) Bulbul et al [1402.2301](#)



Abazajian [2004.06170](#)

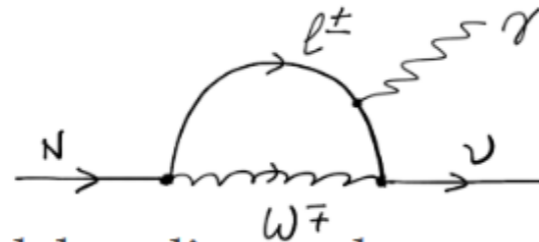
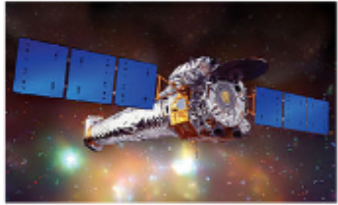
Situation unclear...

need better spectral resolution (XARM and ATHENA will help)

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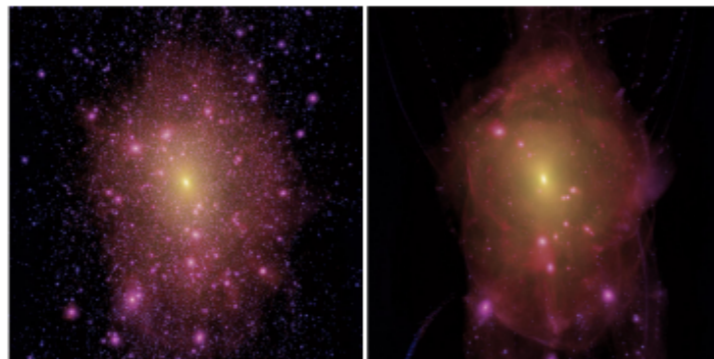
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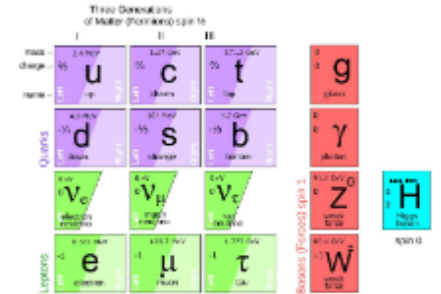


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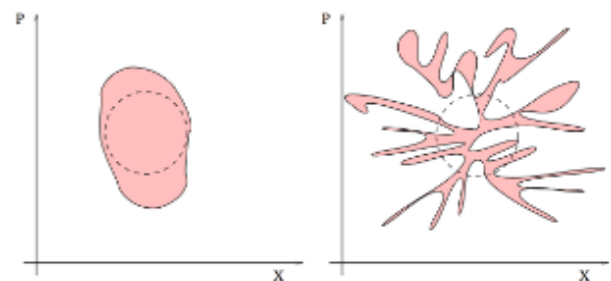
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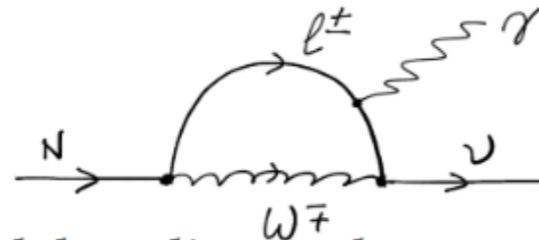
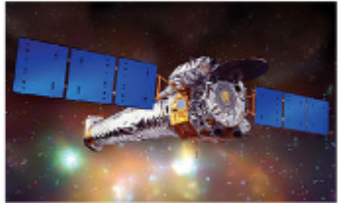
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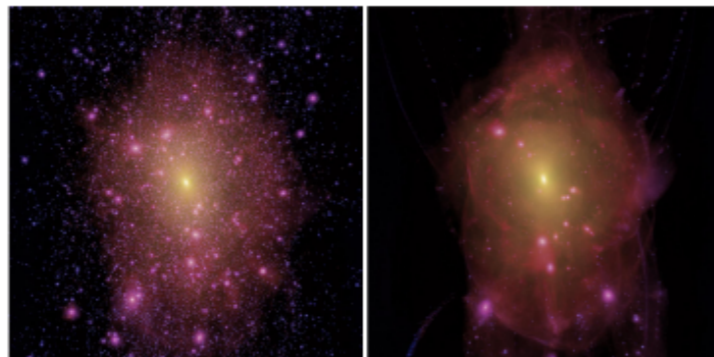
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- uncertainties: baryonic feedback, IGM temperature...

Production mechanisms

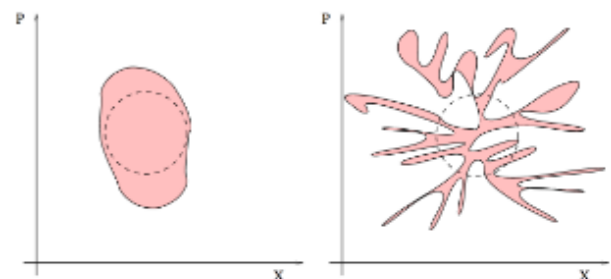
Three known production mechanisms:

- thermal production through mixing-suppressed weak interaction (resonant or non-resonant)
- thermal production through new interactions at high energies (e.g. gauge interactions in L-R symm. model)
- decay of heavy particle / field (e.g. inflaton during reheating)

Third Generation of Matter Particles			
max. charge	I	II	III
up	u	c	t
down	d	s	b
lepton	ν_e	ν_μ	ν_τ
electron	e	μ	τ
gauge bosons	γ	Z	W
scalar bosons			H

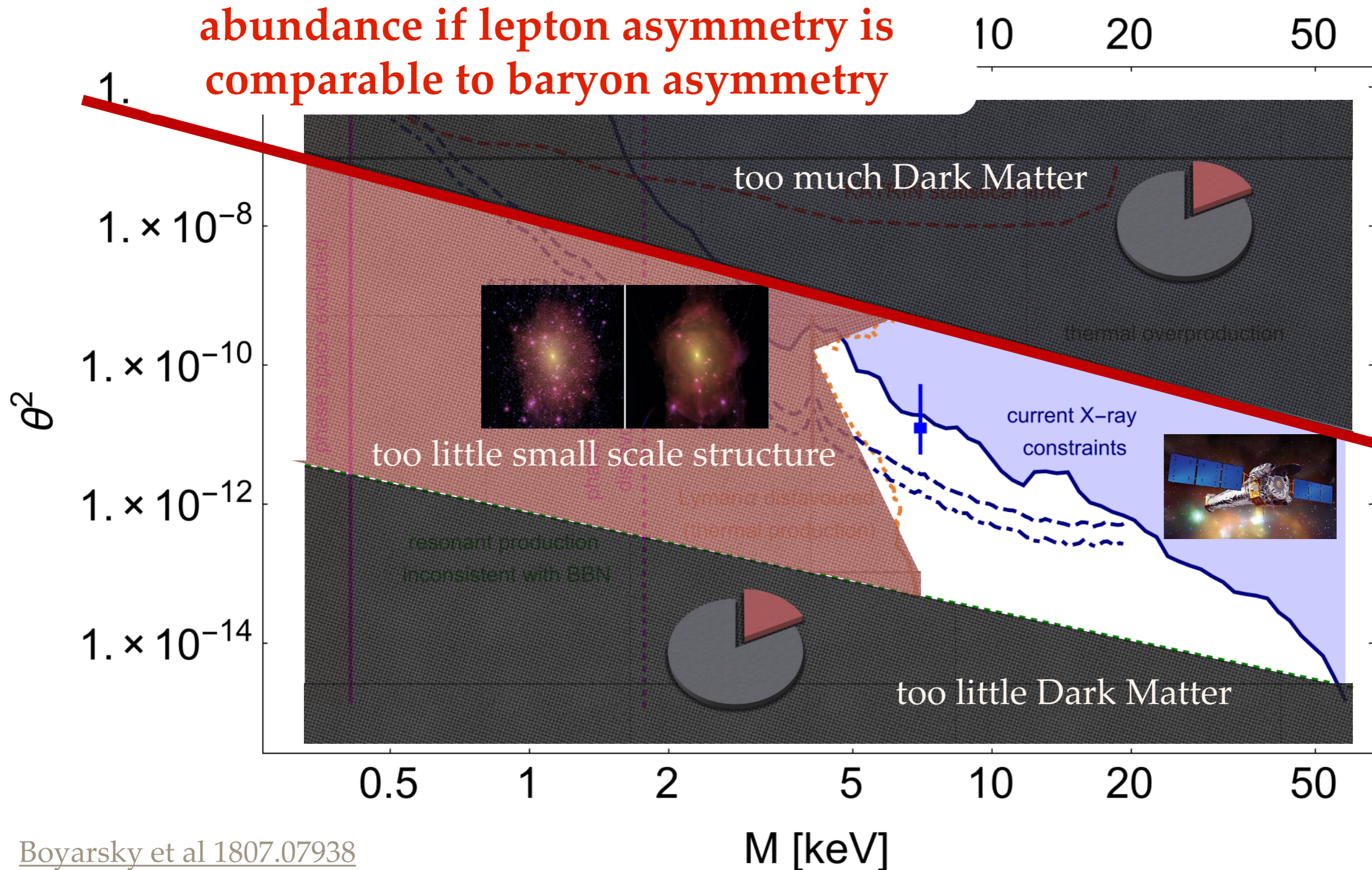
Phase space

- fermions are subject to Pauli principle
 $M > 25 \text{ eV}$
- applying this throughout the history of the universe yields Tremaine-Gunn bound
- Tremaine-Gunn bound depends on production mechanism, excludes $M < 0.5 \text{ keV}$
disfavours $M < 2 \text{ keV}$



Sterile Neutrino Dark Matter

abundance if lepton asymmetry is comparable to baryon asymmetry



Effective Mixing Angle

$$\sin^2(2\theta_m) = \frac{\Delta^2(p) \sin^2(2\theta)}{\Delta^2(p) \sin^2(2\theta) + [\Delta(p) \cos(2\theta) - V_D - V_T]^2}.$$

The active-sterile mass splitting enters via $\Delta(p) = \Delta m^2 / (2p)$

And the “matter potentials” are

$$V_T \simeq -\frac{8}{3} \sqrt{2} G_F \left[\frac{\rho_\nu}{m_Z^2} + \frac{\rho_\ell}{m_W^2} \right] E_\nu$$

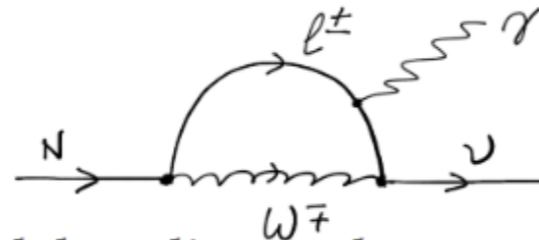
$$V_D \simeq 2\sqrt{2} G_F n_\gamma l_\nu = 2\sqrt{2} G_F \frac{2\zeta(3)}{\pi^2} T^3 l_\nu,$$

- **In matter-antimatter symmetric universe:** Dodelson/Widrow [9303287](#)
abundance determined by M and θ alone,
phase space distribution roughly thermal
- **In presence of large lepton asymmetry l_ν :** Shi/Fuller [9810076](#)
MSW-like resonant enhancement of DM abundance, cooler spectrum

How to find Sterile Neutrino DM?

Indirect searches

- radiative decay $N \rightarrow \nu \gamma$ gives emission line at $M/2$



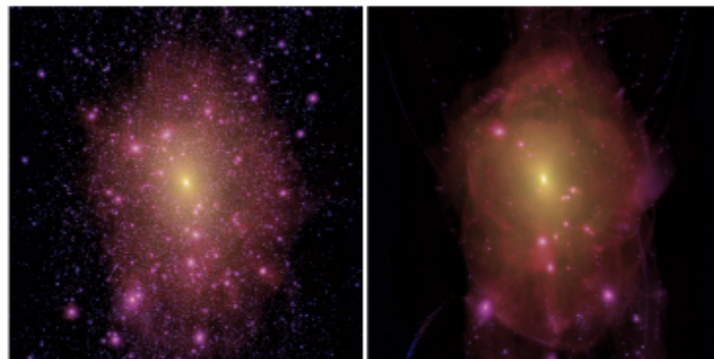
- 3.5 keV excess observed, but disputed
- new missions (XRISM, ATHENA, Lynx...)

Structure formation

Free streaming of DM affects formation of structures at sub-Mpc lengths

- matter power spectrum (Lyman α forest, 21 cm astronomy, weak lensing)
- # collapsed structures (dwarf galaxy counts, reionisation history; collapsed objects at high-z)

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Production mechanisms

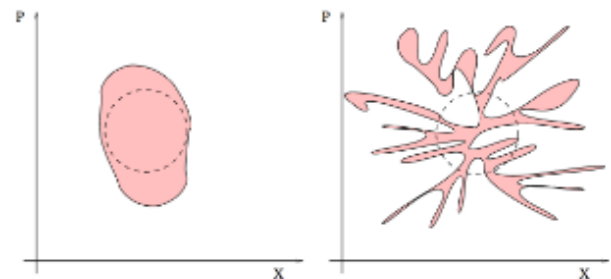
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Third Generation of Matter Particles			
max. charge	I	II	III
1/3	u (up)	c (charm)	t (top)
2/3	d (down)	s (strange)	b (bottom)
0	ν_c (charm)	ν_s (strange)	ν_b (bottom)
1	e (electron)	μ (muon)	τ (tau)
0	ν_e (electron)	ν_μ (muon)	ν_τ (tau)
0	Z^0	W^\pm	H^0

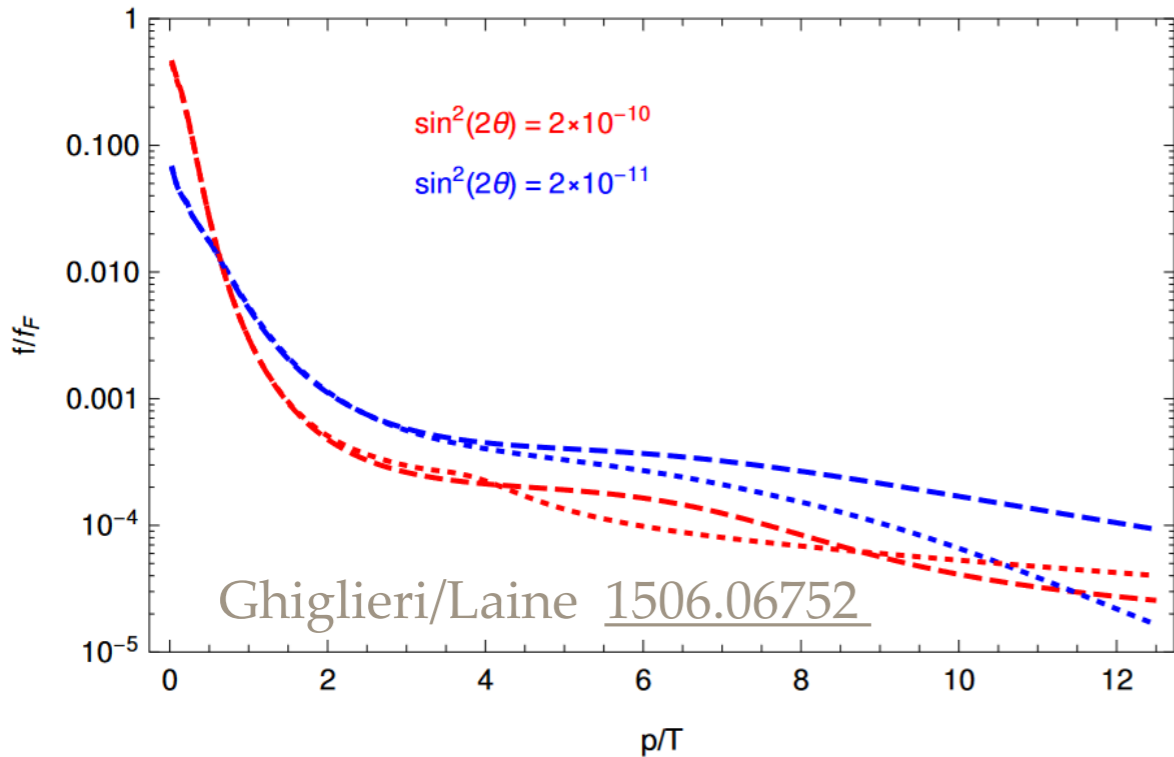
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Structure Formation

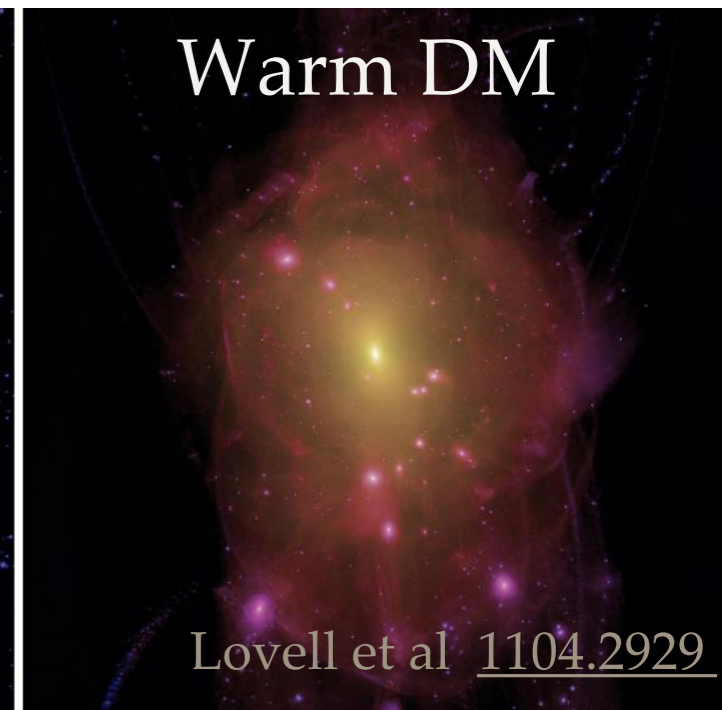
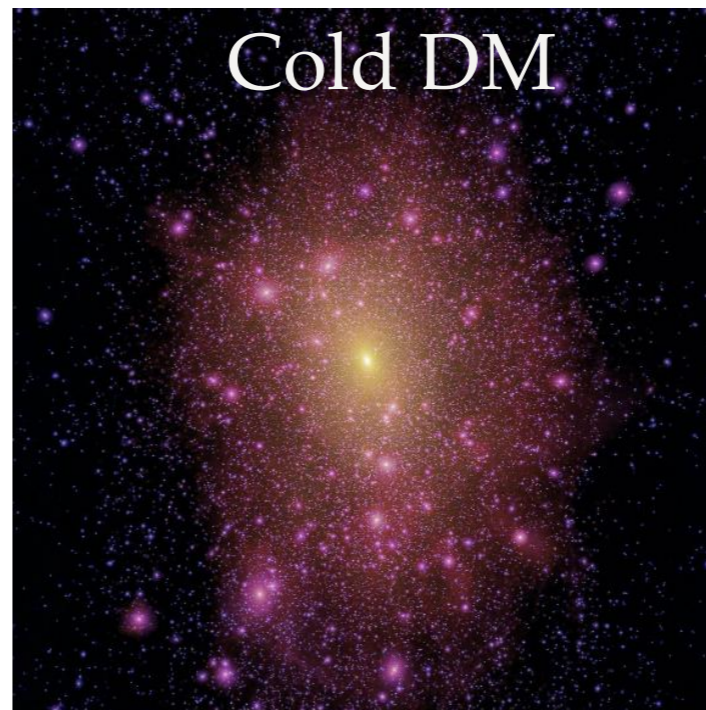
DM momentum distribution



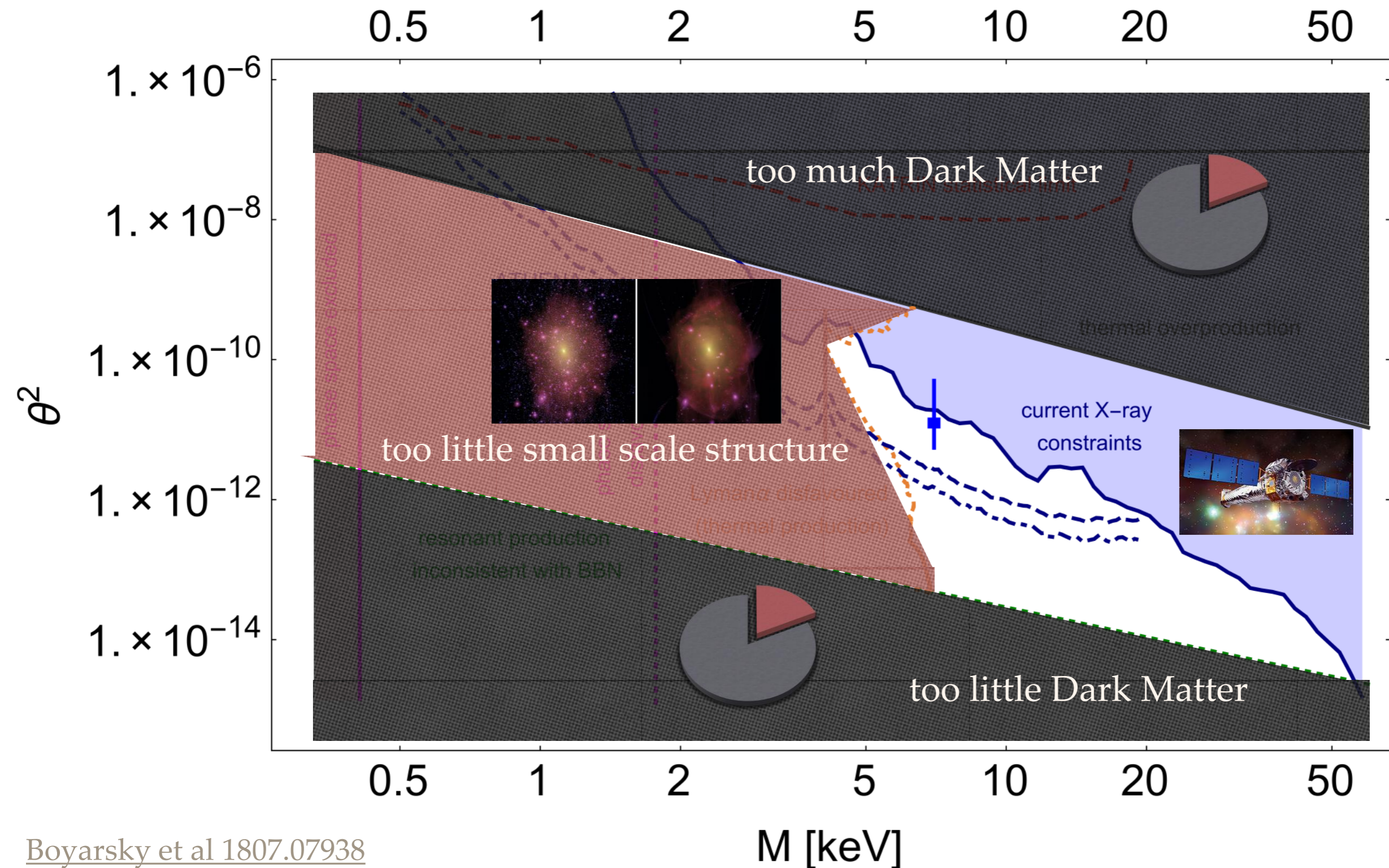
DM free streaming length

$$\lambda_{\text{fs}}(t) \equiv a(t) \int_{t_i}^t dt' \frac{v(t')}{a(t')} \approx 1 \text{ Mpc} \frac{\text{keV}}{M} \frac{\langle p_{\text{DM}} \rangle}{\langle p_\nu \rangle}$$

- Free streaming leads to (relative) suppression of small scale structures (galactic to sub-galactic scales)
- Visible in dwarf galaxy counts, subhalo counts, Lyman forest, lensing, 21cm ...



Sterile Neutrino Dark Matter



Large Lepton Asymmetries

- Lepton asymmetries needed for resonant DM production at $T \sim 200$ MeV exceed observed baryon asymmetry by orders of magnitude
- Recall: at $T > 130$ GeV lepton and baryon asymmetries are kept in equilibrium by electroweak sphalerons
- How did the lepton asymmetry grow by orders of magnitude between $T = 130$ GeV and $T = 200$ MeV?

Cold DM

Warm DM

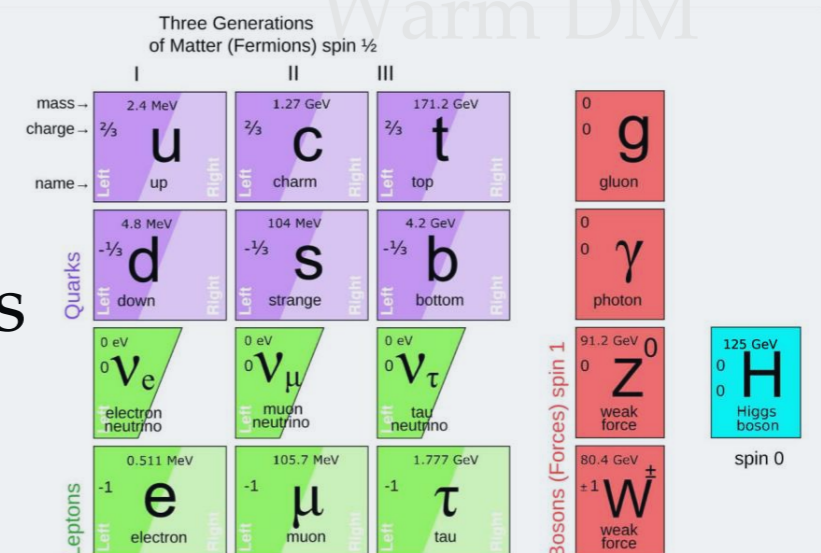
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- How did the lepton asymmetry grow by orders of magnitude between $T = 130$ GeV and $T = 200$ MeV?

One possibility: the Neutrino Minimal Standard Model (ν MSM)

- one heavy neutrino is DM (keV mass)
- the two others (GeV masses) generate baryon asymmetry during freeze-in at $T > 130$...
- ...and generate additional lepton asymmetries during freeze-out and decay at $T < 130$ GeV
- late time lepton asymmetry causes resonant DM production

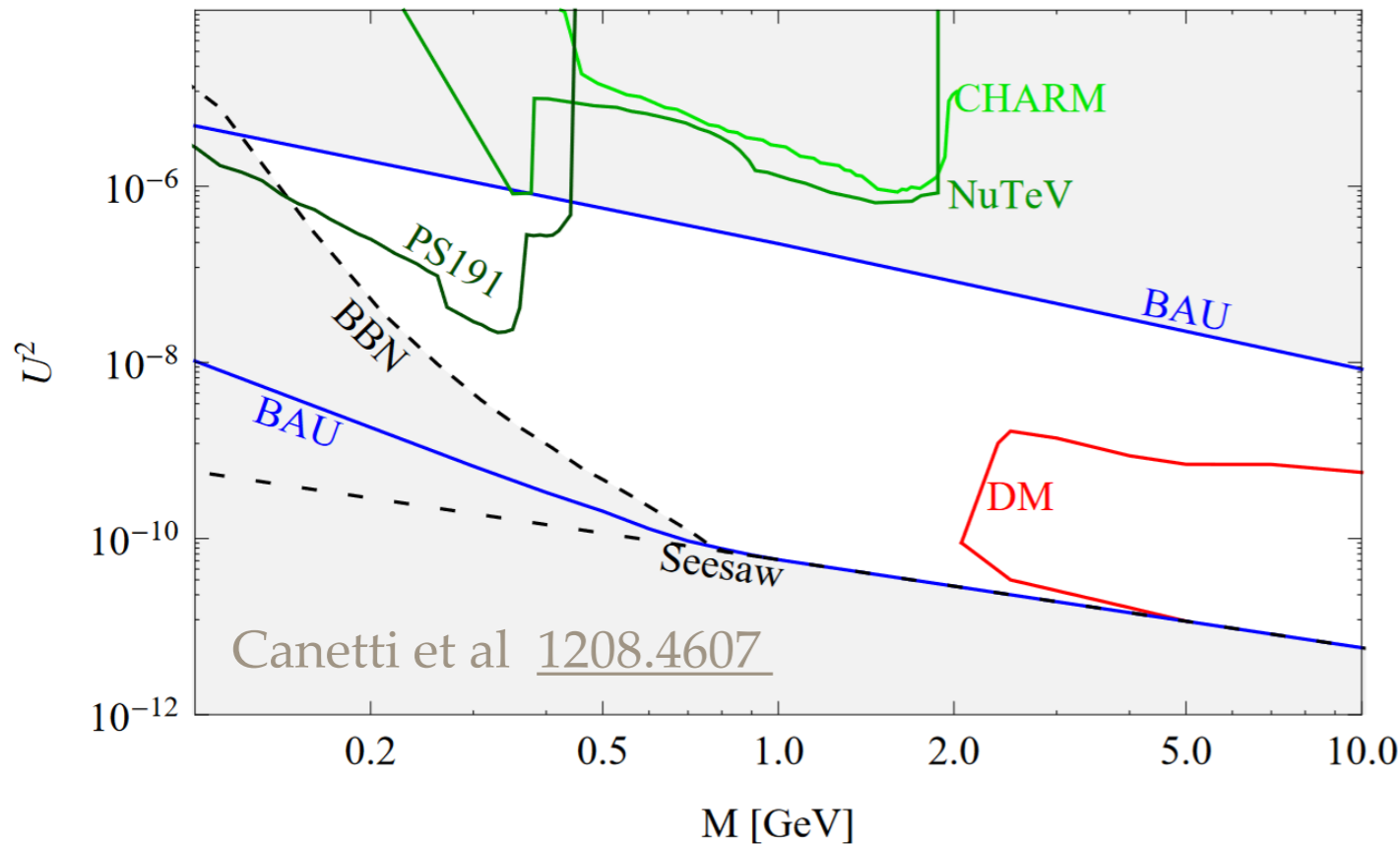
Asaka/Shaposhnikov [0505013](#)



Laine/Shaposhnikov [0804.4543](#)

Can ν MSSM produce enough DM?

- Only parameter scan to date finds viable region!



DM production may be probed indirectly at colliders by discovering GeV scale heavy neutrinos that produced the large lepton asymmetry (which resonantly enhanced DM production...)

Cold DM

- Since then: considerable progress in computational methods

Biondini et al [1711.02864](#)

Garbrecht [1812.02651](#)

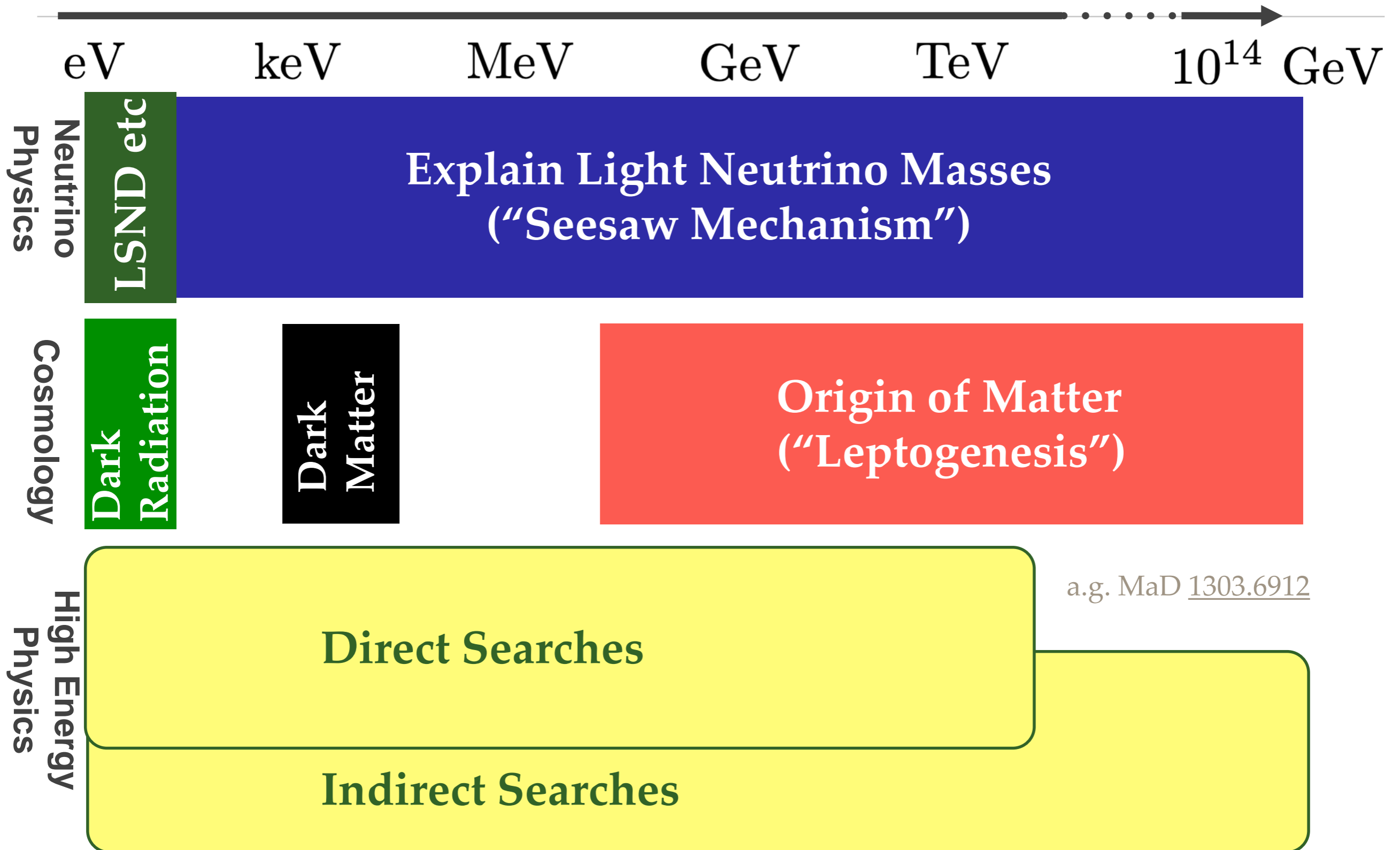
- Recent analysis confirms existence of viable region

Ghilieri/Laine [2004.10766](#)

- Currently field of active research...

Eijima/Shaposhnikov./Timiryasov [2011.12637](#)

Heavy Neutrinos in Particle Physics and Cosmology



The Hunt for RH Neutrinos: A Multi Frontier Problem!

Indirect probes at accelerators
rare decays, EWPD,
lepton universality)

new detectors
(FASER, Codex-b,
MATHUSLA, A13X,
ANUBIS

Collider searches for heavy neutrinos

absolute neutrino mass
searches (KATRIN ect.)

X-ray searches: eROSITA, ART-XC,
ATHNEA, XRISM, Lynx...

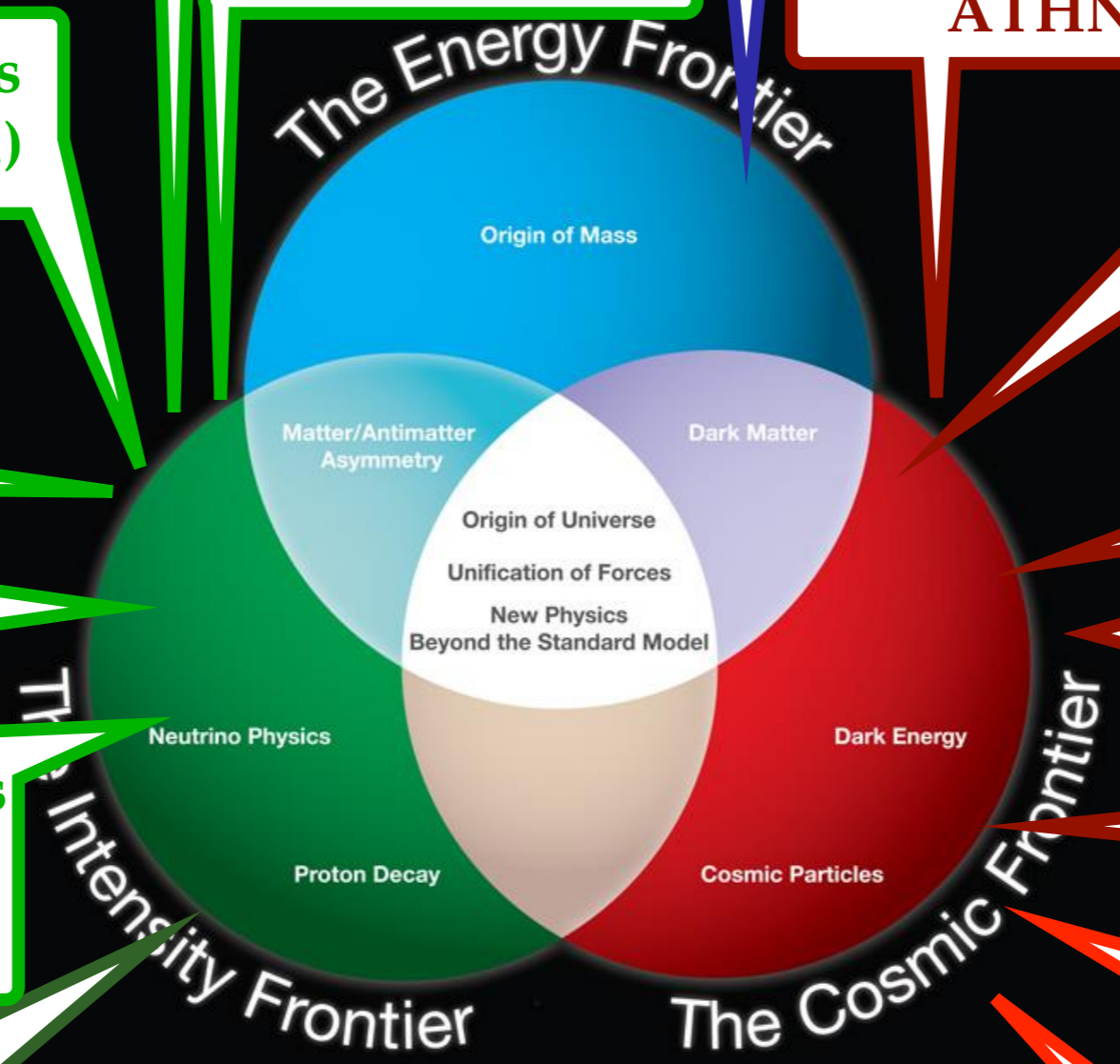
non-accelerator
searches
(TRISTAN...)

CMB and LSS :
absolute neutrino mass

neutrinoless
double β decay

astrophysics:
supernovae etc.

fixed target experiments
(SHiP, NA62, DUNE,
T2K..)



Structure formation:
simulation, observation

IGM temperature:
WDM vs CDM

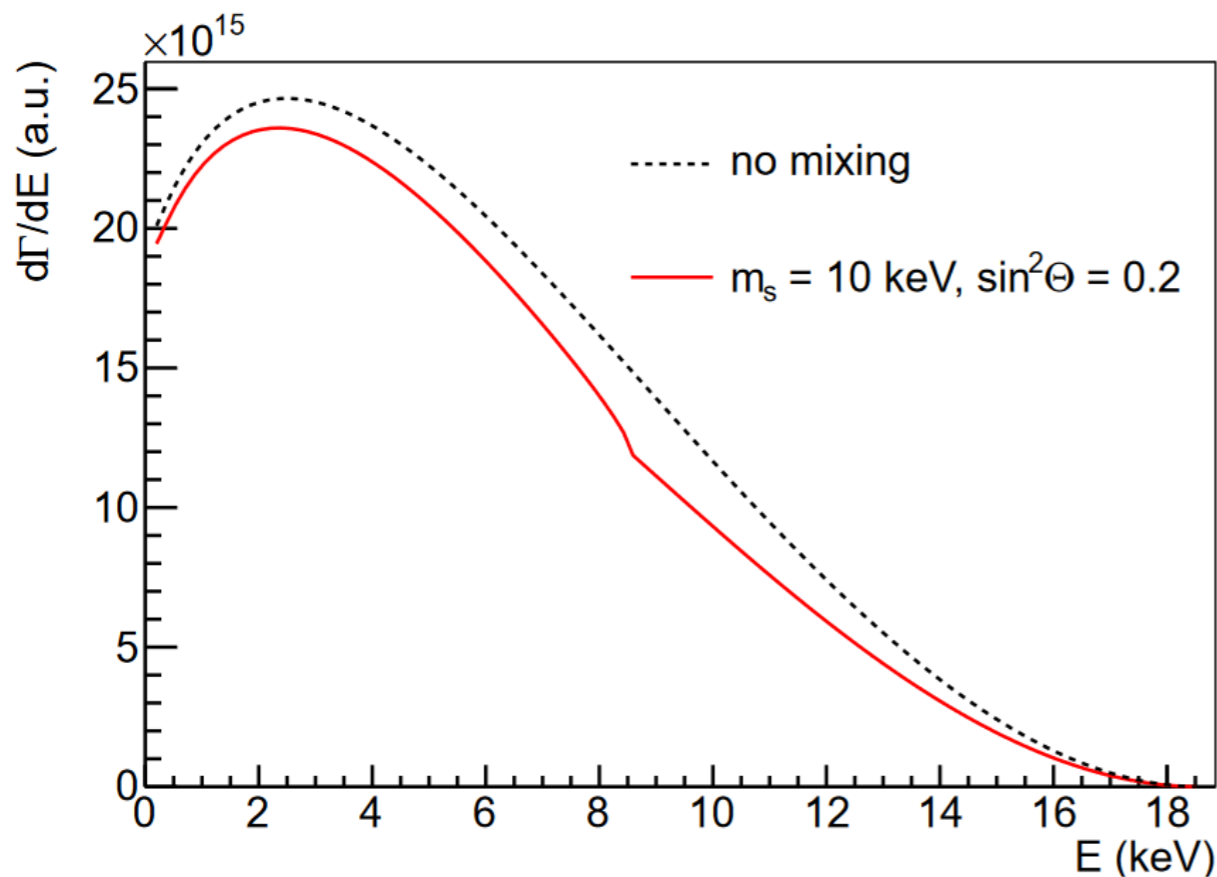
Theory: leptogenesis
parameter region

neutrino oscillation
experiments
DUNE, Hyper-K

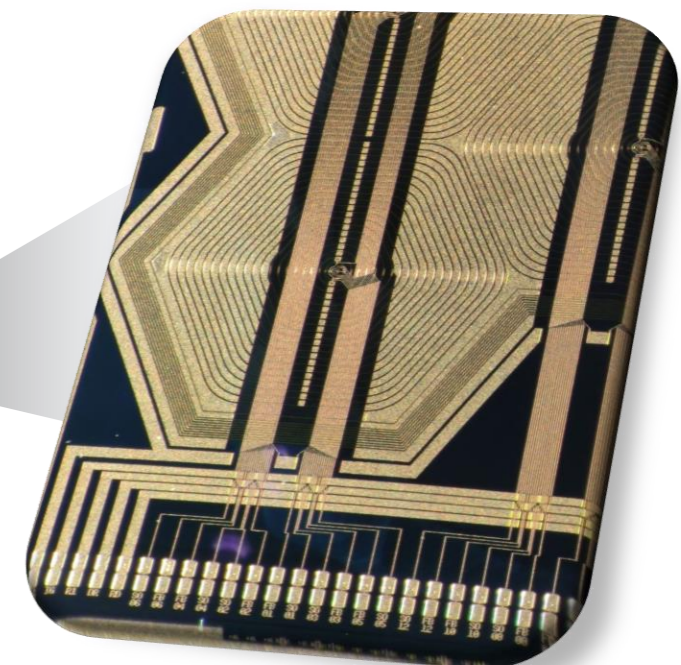
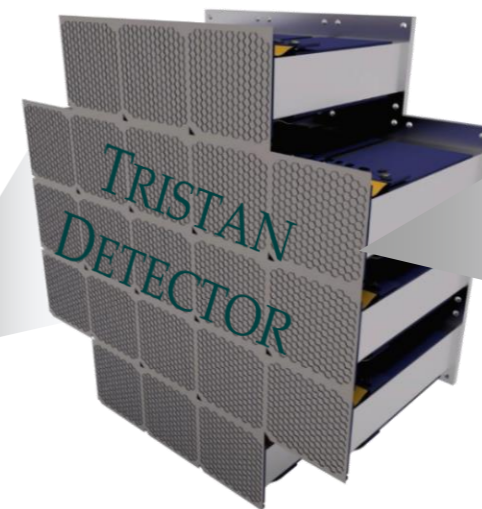
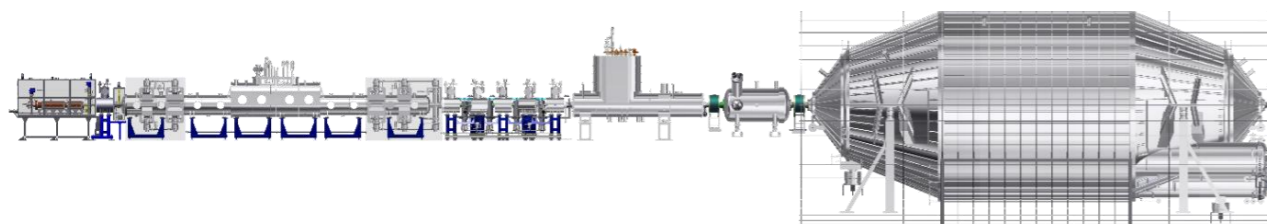
Theory: Sterile neutrino
DM production

RF, NF, EF, CF, TF

Novel Detector System for KATRIN



Mertens et al. JCAP 1502 (2015)
Mertens et al. J. Phys. G46 (2019)



- keV mass sterile neutrinos can be discovered via their impact on β decay spectra
- This can e.g. be done with an upgrade to KATRIN