

EMWSD

Electromagnetic and Wake Solver Development

Meeting #01

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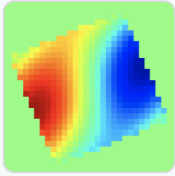
Outline

1. GitHub organization

2. Wake potential algorithm

3. Box resonator

Conclusions and next steps



ImpedanCEI

Switzerland

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People

WarpBasics Public

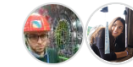
Instructions to install Warp

Python 1

EMcLAW-test Public

Cube resonator experiment to study the FVTD EM solver capabilities

Fortran



Invite someone

Repositories

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Cube resonator experiment to study the FVTD EM solver capabilities

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WarpBasics Public

Instructions to install Warp

Python 0 stars 1 fork 0 issues Updated 5 days ago

New organization for GitHub repositories.

<https://github.com/ImpedanCEI>



Impedance Computations

Updated 7 days ago

Filter cards

1 To do



☰ Evaluation of at least one unstructured grid *** solver (with FEM/DGFEM ideally)

Added by Igiacome

2 In progress



☰ Wake potential computations ***

TODO:

- Evaluate the simple method used in Gdfidl
- Is the Zagodornov method needed?
- Direct method with macroparticles

Added by Igiacome

☰ Comparison WarpX - EMCLAW ***

- assessment of staircasing errors when using mesh refinement
- evaluation of energy dissipation

The properties will be evaluated using the cubic resonator test

Added by Igiacome

2 Done



☰ Installation notes for EMCLAW ***

Added by Igiacome

☰ Installation notes for WarpX ***

Added by Igiacome

GitHub projects: Effective display of tasks to be done, in progress and done

<https://github.com/orgs/ImpedanCEI/projects/1>

WarpBasics repository

ImpedanCEI / WarpBasics Public

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main 1 branch 0 tags

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elenafuengar cleaned scripts folder 6aa3d59 5 days ago 24 commits

Scripts/cube_cavity	cleaned scripts folder	5 days ago
.gitignore	updated the .gitignore	6 days ago
.owncloudsync.log	test commit	7 days ago
README.md	test commit	7 days ago

README.md

Warp Basics

Instructions to install Warp.

1. Install miniconda This is a minimal python installation which is very flexible to install, manipulate and remove. You install miniconda by running the following commands

README.md files with the installation guide and instructions to run in parallel from the server

Scripts with the cube cavity simulations in Warp:

- **_mpi:** prepared to run on parallel in htcondor
- **_impedance:** old algorithm for WP and impedance
- **_poisson:** new algorithm [in progress]

main WarpBasics / Scripts / cube_cavity /

Go to file Add file ...

elenafuengar cleaned scripts folder ... 5 days ago History

..		
README.md	test commit	7 days ago
cube_cavity_impedance.py	test commit	7 days ago
cube_cavity_mpi.py	test commit	7 days ago
cube_cavity_poisson.py	Adding script with PyPIC support	6 days ago

README.md

Run parallel Warp

Setting up a python enviroment + openmpi

tutorial modified from: [https://github.com/PyCOMPLETE/PyECLOUD/wiki/Setup-python-\(including-mpi4py\)-without-admin-rights](https://github.com/PyCOMPLETE/PyECLOUD/wiki/Setup-python-(including-mpi4py)-without-admin-rights) The following guide shows how to get a complete python installation without administrator rights:

EMcLAW-test repository

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main

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About

Cube resonator experiment to study the FVTD EM solver capabilities

Readme

Releases

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Languages

Fortran 69.7% C 16.5%

Installation

Install AMReX

Type in the folder you want to install AMREX:

README.md with installation and user guide, with modelling notes is also available

Scripts with the box resonator simulations:

- **Pron.f90**: where initial conditions are defined
- **metallic_material_3d.f90**: defines the metallic region
- **inputs**: defines the simulation domain, timesteps mesh and AMR refinement

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main EMcLAW-test / Scripts

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elenafluengar Update README.md 5 days ago History

Backtrace.0 added initial conditions for B 5 days ago

CMakeLists.txt added initial conditions for B 5 days ago

DEFINES.H Box_resonator test scripts 7 days ago

GNUmakefile Box_resonator test scripts 7 days ago

Make.package added initial conditions for B 5 days ago

Prob.f90 added initial conditions for B 5 days ago

README.md Update README.md 5 days ago

ep_mu_1d.F90 added initial conditions for B 5 days ago

Outline

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Algorithm overview

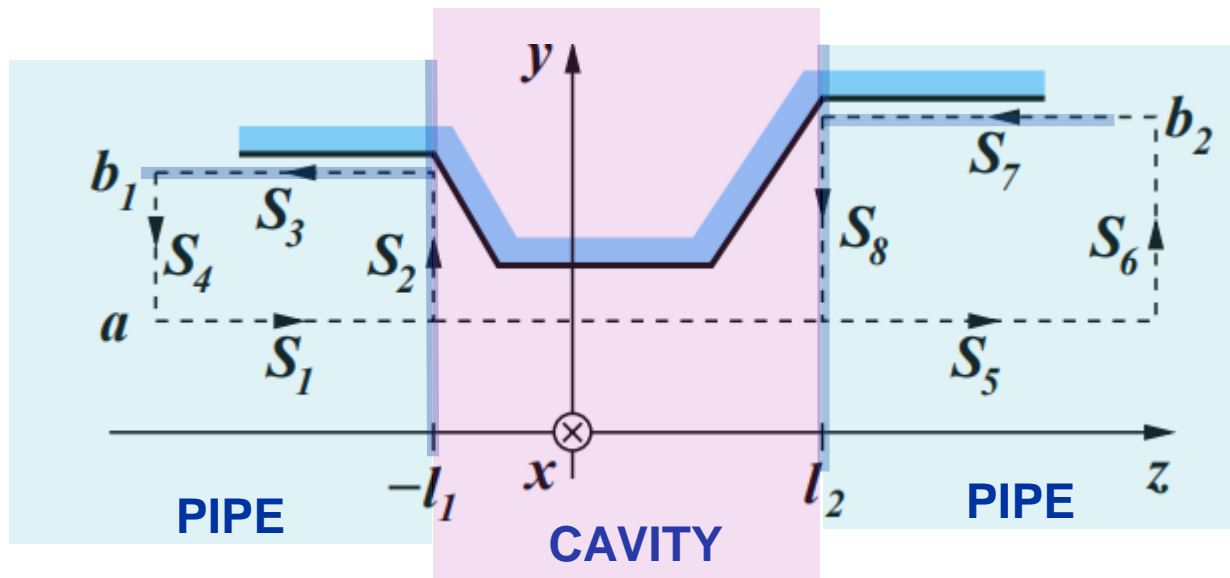
Source:

<https://accelconf.web.cern.ch/e06/PA/PERS/WEPC110.PDF>

Deform the **path of integration** to go from the improper integral:

$$W_z(x, y, s) = -\frac{1}{q} \int_{-\infty}^{\infty} E_z(x, y, z, t = (z + s)/c) dz \quad (1)$$

To a definite integral + 2 poisson problems



$$\begin{aligned}
 qW_z(x, y, s) &= \\
 &= [\varphi(x, y = b_1) - \varphi(x, y)]_{z=-l_1} && \text{Poisson in } z=-l_1 \text{ surface } t=(-l_1+s)/c \\
 &\quad - \int_{-l_1}^{l_2} E_z(x, y, z, t = (z + s)/c) dz && (15) \\
 &\quad + [\varphi(x, y) - \varphi(x, y = b_2)]_{z=l_2} && \text{Poisson in } z=l_2 \text{ surface } t=(l_2+s)/c
 \end{aligned}$$

Calculation steps (I)

Source:
<https://accelconf.web.cern.ch/e06/PA/PERS/WEPC110.PDF>

1) New field component definition:

$$\bar{u}(x, y, z, s) = u(x, y, z, t = (z + s)/c), \quad (3)$$

such that

$$\frac{\partial \bar{u}}{\partial z} = \frac{\partial u}{\partial z} + \frac{1}{c} \frac{\partial u}{\partial t} \quad (4)$$

2) Maxwell eqs for TM/TEM fields yield to an irrotational vector G:

$$\begin{aligned} \int_A (\nabla \times \vec{G}) \cdot d\vec{A} = 0 &= \oint_S \vec{G} \cdot d\vec{s} \\ &= \int_{l_2}^{\infty} G_z(y = a) dz + \int_a^{b_2} G_y(z = \infty) dy - \\ &\quad - \int_{l_2}^{\infty} G_z(y = b_2) dz - \int_a^{b_2} G_y(z = l_2) dy \end{aligned}$$

$$0 = \int_{l_2}^{\infty} \bar{E}_z dz - \int_a^{b_2} (\bar{E}_y - c\bar{B}_x)(z = l_2) dy, \quad (10)$$

This proves that one can change an improper integral to a proper integral using the new path of integration

S8=S5 and S1=S2

3) Combining the equalities found, the wake potential is defined by:

$$\begin{aligned} qW_z(x, y, s) = & \int_a^{b_1} (E_y - cB_x)(z = -l_1, t = (-l_1 + s)/c) dy \\ & - \int_{-l_1}^{l_2} E_z(z, t = (z + s)/c) dz \\ & - \int_a^{b_2} (E_y - cB_x)(z = l_2, t = (l_2 + s)/c) dy. \end{aligned} \quad (11)$$

Calculation steps (II)

Source:
<https://accelconf.web.cern.ch/e06/PA/PERS/WEPC110.PDF>

4) To extract the TM/TEM fields, we use the defined irrotational vector \mathbf{G} since it can be derived from a scalar potential

$$\vec{G} = \vec{e}_x (\bar{E}_x + c\bar{B}_y) + \vec{e}_y (\bar{E}_y - c\bar{B}_x) + \vec{e}_z \bar{E}_z$$

$$(\nabla \times \mathbf{G})_z = 0$$

$$G_x \mathbf{e}_x + G_y \mathbf{e}_y = \nabla \varphi.$$

5) Taking the divergence this leads to a Poisson equation. The driving term has to be taken at $z=-l_1$ and $z=l_2$

$$\begin{aligned} \nabla \cdot (G_x \mathbf{e}_x + G_y \mathbf{e}_y) &= \\ &= \frac{\partial}{\partial x} (\bar{E}_x + c\bar{B}_y) + \frac{\partial}{\partial y} (\bar{E}_y - c\bar{B}_x) \\ &= \underbrace{\frac{1}{c} \frac{\partial}{\partial t} E_z - \frac{\partial}{\partial z} E_z}_{\text{rho}} = \nabla^2 \varphi. \end{aligned} \quad (13)$$

6) The wake potential becomes:

$$\begin{aligned} qW_z(x, y, s) &= \\ &= [\varphi(x, y = b_1) - \varphi(x, y)]_{z=-l_1} \quad \text{Poisson in } z=-l_1 \text{ surface } t=(-l_1+s)/c \\ &\quad - \int_{-l_1}^{l_2} E_z(x, y, z, t = (z + s)/c) dz \quad (15) \\ &\quad + [\varphi(x, y) - \varphi(x, y = b_2)]_{z=l_2} \quad \text{Poisson in } z=l_2 \text{ surface } t=(l_2+s)/c \end{aligned}$$

Scripting

Poisson equations are solved with **PyPIC** for each value of s_n at $x=x_{test}$, $y=y_{test}$, $z=-l_1$ and $x=x_{test}$, $y=y_{test}$, $z=l_2$

```
# PyPIC function to declare the implicit function for the conductors (this acts as BCs)
PyPIC_chamber = poly.polyg_cham_geom_object({'Vx' : np.array([w_rect, -w_rect, -w_rect, w_rect]),
                                             'Vy': np.array([h_rect, h_rect, -h_rect, -h_rect]),
                                             'x_sem_ellip_insc' : 0.99*w_rect, #important to add this
                                             'y_sem_ellip_insc' : 0.99*h_rect})

# solver object
picFD = PIC_FD.FiniteDifferences_Staircase_SquareGrid(chamb = PyPIC_chamber, Dh = dh, sparse_solver = 'PyKLU')

# define the left side of the laplacian (driving term rho = 1/c*dEz/dt-dEz/dz)
# rho = np.ones_like(picFD.rho) #test rho to check the solver. Rho needs
rho = Ez_dt[iz_l1]-Ez_dt[it_l1]/picmi.constants.c*np.ones_like(picFD.rho) #this rho is a constant evaluated

# solve the laplacian and obtain phi(0,0)
picFD.solve(rho = rho) #the dimensions are selected by pyPIC solver
phi[n] = picFD.phi.copy()
```

$$qW_z(x, y, s) = [\varphi(x, y = b_1) - \varphi(x, y)]_{z=-l_1} - \int_{-l_1}^{l_2} E_z(x, y, z, t = (z + s)/c) dz + [\varphi(x, y) - \varphi(x, y = b_2)]_{z=l_2} \quad (15)$$

Poisson in $z=-l_1$ surface $t=(-l_1+s)/c$

Poisson in $z=l_2$ surface $t=(l_2+s)/c$

E_z is interpolated to match the dimensions between t and z so they can be added to obtain ρ

The derivatives are obtained for each value of z_k , $t_{k,n}$

```
#--- obtain the derivatives
for n in range(tot_nsteps-1):
    Ez_dt[k]= (Ez_interp[n+1, :] - Ez_interp[n, :])/dt
    Ez_dz[k]= (Ez_interp[:, n+1] - Ez_interp[:, n])/dz
```

Scripting

The definite integral is solved for each z_k, s_n . For each pair s, z , the index for the time dimension has to be obtained

```
#-----#
# integral between -l1 and l2 #
#-----#

#int(Ez(xtest, ytest, z, t=(s+z)/c))
for k in range(iz_l1, iz_l1):
    it=int(((z[k]+s[n])/c-t[0])/dt)
    integral=integral+(Ez_interp[k, it])*dz
```

$$\begin{aligned}
 qW_z(x, y, s) &= \\
 &= [\varphi(x, y = b_1) - \varphi(x, y)]_{z=-l_1} \\
 &\quad - \int_{-l_1}^{l_2} E_z(x, y, z, t = (z + s)/c) dz \\
 &\quad + [\varphi(x, y) - \varphi(x, y = b_2)]_{z=l_2}.
 \end{aligned} \tag{15}$$

Poisson in $z=-l_1$ surface $t=(-l_1+s)/c$

Poisson in $z=l_2$ surface $t=(l_2+s)/c$

```
#-----#
# Obtain W(s) #
#-----#
```

All is added obtaining $W(s_k)$

```
# Define phi(x, y=b1)
# This indexes go from x(-w_rect,w_rect) and y(-h_rect,h_rect)
# x direction is gridded with (w_rect*2)/dh + 10 ghost cells
# y direction is gridded with (h_rect*2)/dh + 8 ghost cells
# +info see: class PyPIC_Scatter_Gather(object):
iy_b1=int((b1-picFD.bias_y)/dh)
iy_b2=int((b2-picFD.bias_y)/dh)
ixtest_phi=int((xtest-picFD.bias_x)/dh)
ixtest_phi=int((ytest-picFD.bias_y)/dh)

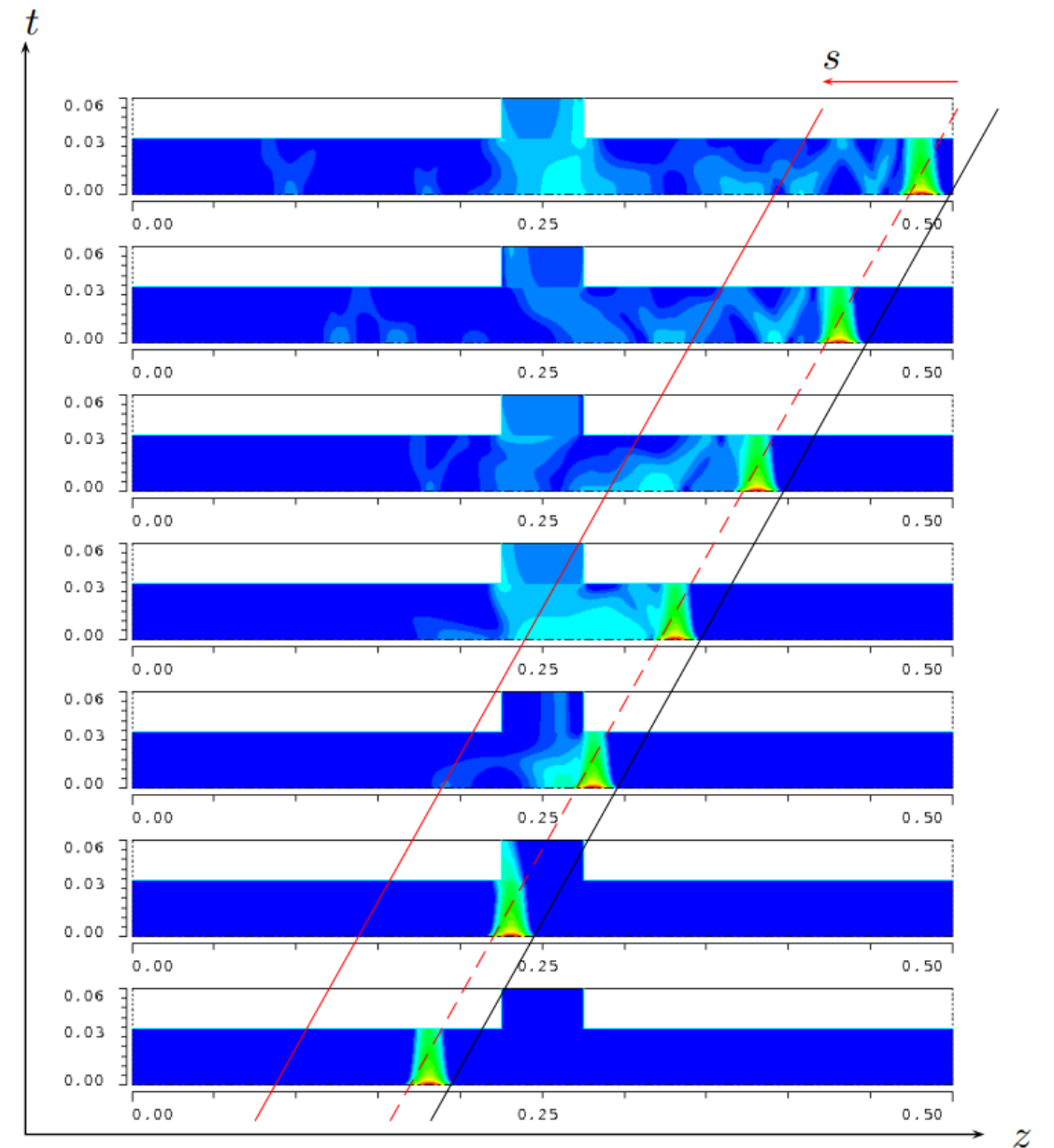
phi_b1=phi(ixtest_phi, iy_b1, n) #phi(x=0, y=b1, s[n])
phi_b2=phi(ixtest_phi, iy_b1, n) #phi(x=0, y=b1, s[n])

Wake_potential[n]=(phi_b1-phi[ixtest_phi, iytest_phi])-integral-(phi[ixtest_phi, iytest_phi]-phi_b2)
```

S vector?

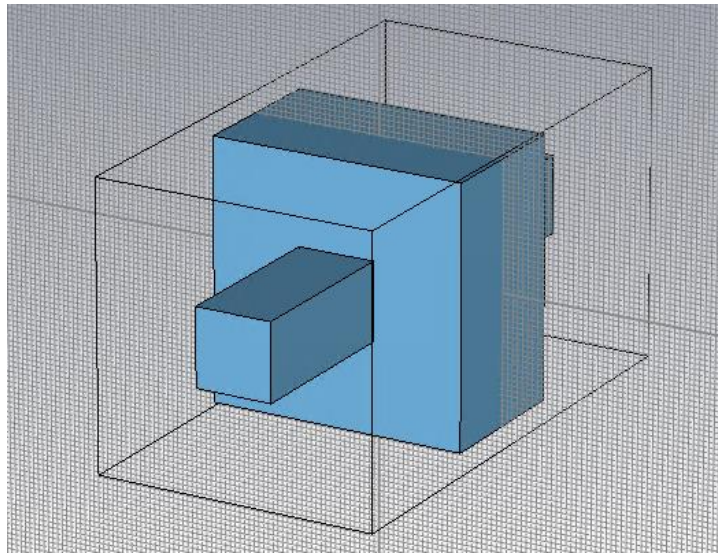
- What resolution and length can the s vector have?
- How is the wake length related to the number of timesteps?

$$W_z(x, y, s) = -\frac{1}{q} \int_{-\infty}^{\infty} E_z(x, y, z, t = (z + s)/c) dz$$



CST study of wavelength and n^0 of timesteps

The aim of these simulations was to obtain the relation between mesh cells, number of timesteps and s vector resolution



Cube cavity surrounded by PEC:

- Total length: 100 mm
- Cavity length: 30 mm
- Pipe width: 15 mm
- Cavity width: 50 mm

$N_x=55,$

$N_y=55,$

$N_z=96$

(ncells = 277020) $\rightarrow \Delta h=1$ mm

Background PEC extended 2.5 mm in x & y

Resonance at ~4.3 GHz

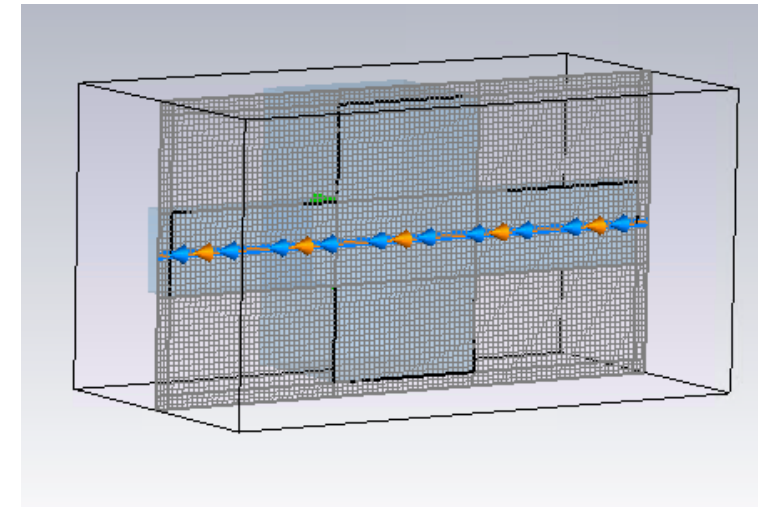
Beam excitation:

$\text{Sigmat}=\frac{1}{4}$ ns \rightarrow $\text{sigmaz}=18.73$ mm

Excitation duration: 6.50460411e-001 ns

LOGFILE

Number of mesh cells:	277020
Excitation duration:	6.50460411e-001 ns
Calculation time for excitation:	0 s
Number of calculated pulse widths:	1.3386
Simulated number of time steps:	450
Maximum number of time steps:	450
Time step width:	
without subcycles:	1.93490105e-003 ns

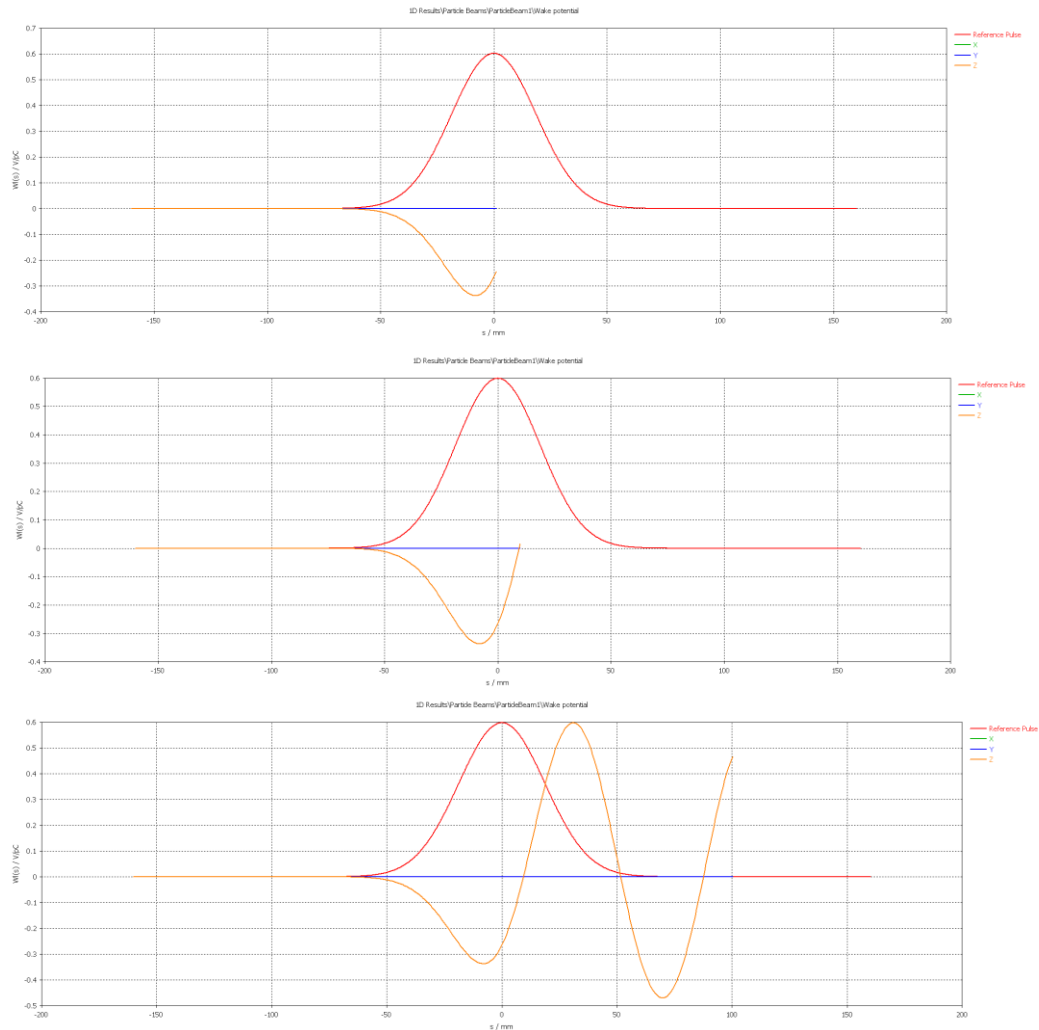


CST study of wavelength and n^0 of timesteps

Wavelength=1 --> nsteps=450,
dt=1.93490105e-003 ns,
Npulse=1.3386 (t=sigmat*npulse)
Length s=279 (277 negative values)

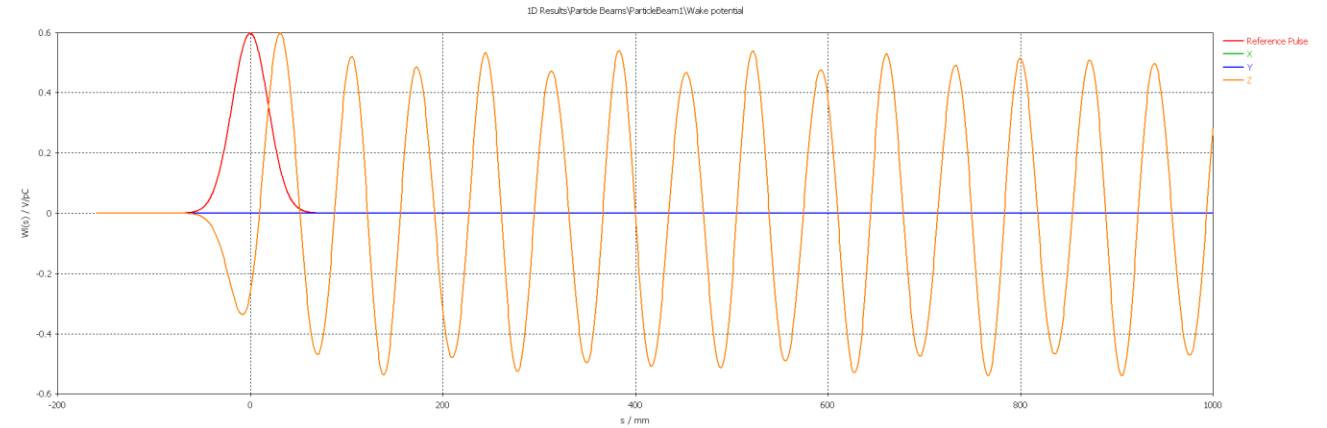
Wavelength = 10 --> nsteps=465,
dt=1.93490105e-003 ns,
Npulse=1.38322
Length s=294 (277 negative values)

Wavelength = 100 --> nsteps=620,
dt=1.93490105e-003 ns,
Npulse=1.84429
Length s=450 (277 negative values)

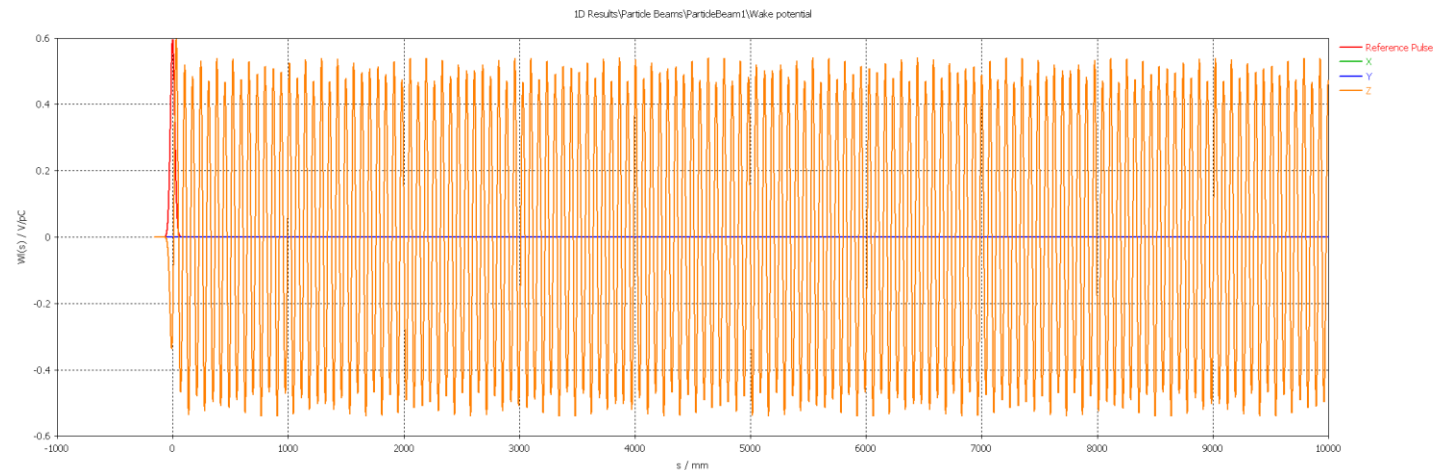


CST study of wavelength and n^0 of timesteps

Wavelength = 1000 --> nsteps=2172,
dt=1.93490105e-003 ns,
Npulse=6.46097
Length s=2001 (277 negative values)



Wavelength = 10000 --> nsteps=17687,
dt=1.93490105e-003 ns,
Npulse=52.6129
Length s=17518 (277 negative values)

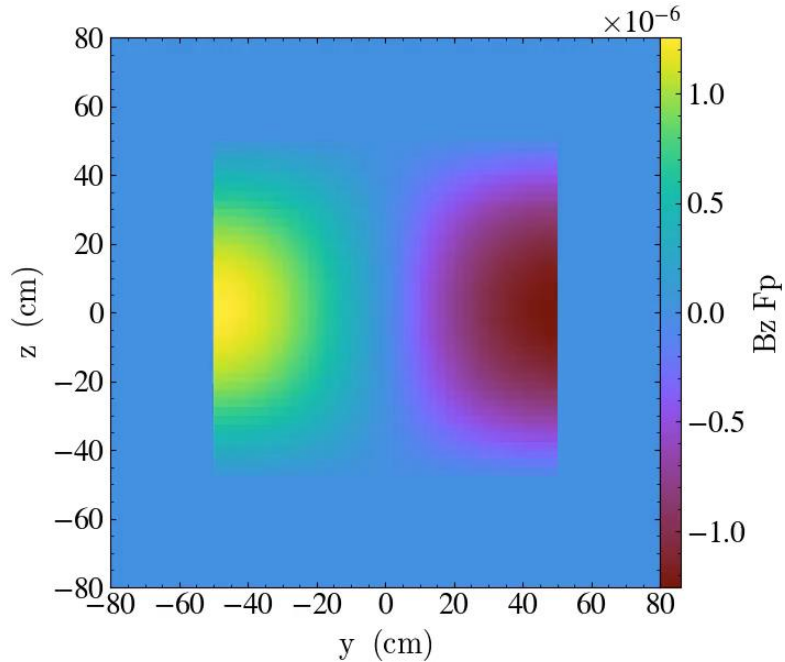


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1. GitHub organization
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 - 3. Box resonator**
- Conclusions and next steps

Box resonator (I)

Objective 1: assess the order of the numerical scheme with a convergence analysis

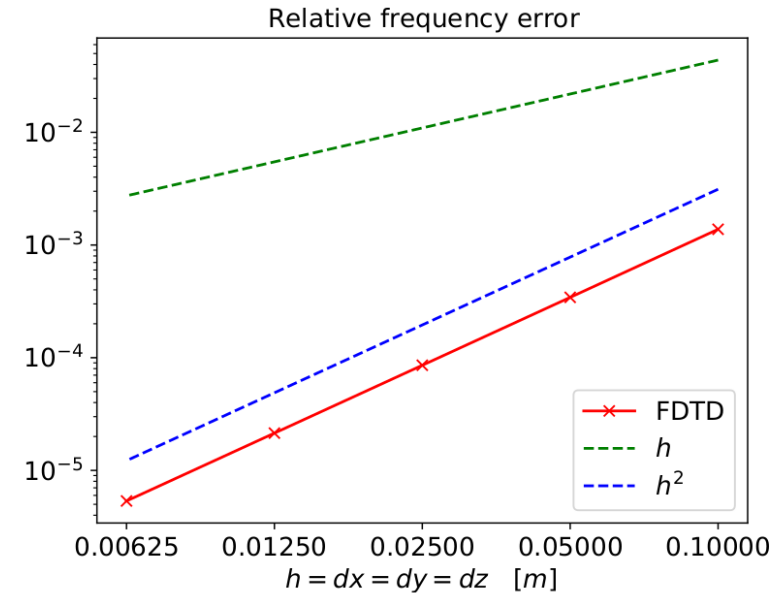


Source: [Lorenzo's presentation](#)

Relative frequency error

$$Err(h) = \frac{Freq(h) - Freq^*}{Freq^*}$$

$Freq(h)$ is the estimated frequency with $h = \Delta x = \Delta y = \Delta z =$ and $Freq^*$ is the analytic frequency.



Box resonator (II)

Source: [Darmstadt thesis](#) "Investigating Finite Volume Time Domain Methods in Computational Electromagnetics"

Objective 2: study the energy dissipation of FVTD

$$E_x(x, y, z) = \frac{-1}{\gamma^2 + k^2} \frac{m\pi p\pi}{a c} E_0 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) \sin\left(\frac{p\pi}{c}z\right)$$

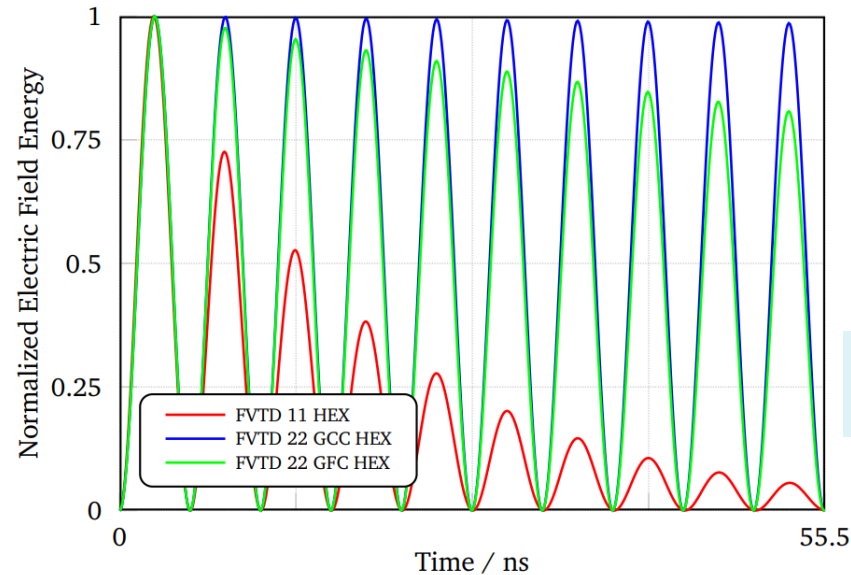
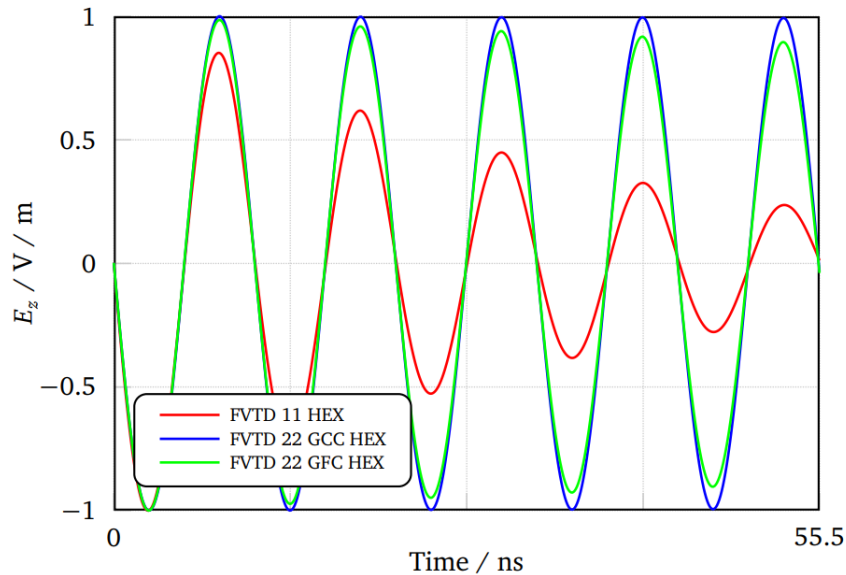
$$E_y(x, y, z) = \frac{-1}{\gamma^2 + k^2} \frac{n\pi p\pi}{b c} E_0 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) \sin\left(\frac{p\pi}{c}z\right)$$

$$E_z(x, y, z) = E_0 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) \cos\left(\frac{p\pi}{c}z\right)$$

$$H_x(x, y, z) = \frac{j\omega\epsilon}{\gamma^2 + k^2} \frac{n\pi}{b} E_0 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) \cos\left(\frac{p\pi}{c}z\right)$$

$$H_y(x, y, z) = \frac{-j\omega\epsilon}{\gamma^2 + k^2} \frac{m\pi}{a} E_0 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) \cos\left(\frac{p\pi}{c}z\right)$$

$$H_z(x, y, z) = 0$$



Energy decay at cavity center:

$$u_e = \frac{1}{2} \epsilon_0 |\mathbf{E}|^2.$$

$$f(t) = a_0 e^{-\alpha t} \sin(\omega t + \delta)$$

EMcLaw simulations set up

inputs: defining domain, n^0 cells, simulation time

```
# ----- INPUTS TO MAIN PROGRAM -----
max_step = 2000
stop_time = 10

em.is_D_wave = 0      # 1 for D-wave and 0 for B-wave (2D)

# PROBLEM SIZE & GEOMETRY
geometry.is_periodic = 0 0 0
lo_bc = 2 2 2          # 2 or 1 for absorbing boundary conditions
hi_bc = 2 2 2
metallic_walls = 1     # 1 if you want metallic walls
# select the places with metallic walls (if metallic_walls = 1)
# the field parallel to the wall must be 1 and the others -1
lo_bcDx = 1 -1 -1
hi_bcDx = 1 -1 -1
lo_bcDy = -1 1 -1
hi_bcDy = -1 1 -1
lo_bcDz = -1 -1 1
hi_bcDz = -1 -1 1
# the field parallel to the wall must be -1 and the others 1
lo_bcBx = 1 1 1
hi_bcBx = 1 1 1
lo_bcBy = 1 1 1
hi_bcBy = 1 1 1
lo_bcBz = 1 1 1
hi_bcBz = 1 1 1

geometry.coord_sys = 0      # 0 => cart
geometry.prob_lo = -1 -1 -1 # [m]
geometry.prob_hi = 1 1 1   # [m]
amr.n_cell = 60 60 60     # number of cells per dimension

# TIME STEP CONTROL
em.cfl = 0.5              # cfl number for hyperbolic system
em.do_reflux = 0          # reflux

# VERBOSITY
em.v = 1                  # verbosity in EM
amr.v = 1                  # verbosity in Amr
#amr.grid_log = grdlog    # name of grid logging file

# REFINEMENT / REGRIDDING
amr.max_level = 0         # maximum level number allowed
amr.ref_ratio = 2 2 2     # refinement ratio
amr.regrid_int = 4        # how often to regrid
amr.grid_eff = 0.7        # what constitutes an efficient grid
```

Prob.f90: initializing Bx, By, Bz field

```
if ((abs(x).lt.0.5).and.(abs(z).lt.0.5) &
    & .and.(abs(y).lt.0.5)) then

!--- resonating magnetic field By, Bx, Bz
em(i,j,k,4) = -2.0d0/h_2*(n*PI/Ly)*(p*PI/Lz) &
& *cos(m*PI/Lx*(x-Lx/2.0d0)) &
& *sin(n*PI/Ly*(y-Ly/2.0d0)) &
& *cos(p*PI/Lz*(z-Lz/2.0d0))*MU0
em(i,j,k,3) = -2.0d0/h_2*(m*PI/Ly)*(p*PI/Lz) &
& *sin(m*PI/Lx*(x-Lx/2.0d0)) &
& *cos(n*PI/Ly*(y-Ly/2.0d0)) &
& *cos(p*PI/Lz*(z-Lz/2.0d0))*MU0
em(i,j,k,5) = cos(m*PI/Lx*(x-Lx/2.0d0)) &
& *cos(n*PI/Ly*(y-Ly/2.0d0)) &
& *cos(p*PI/Lz*(z-Lz/2.0d0))*MU0

!--- constant magnetic field By, Bx, Bz
em(i,j,k,4) = 1.0d0
em(i,j,k,3) = 1.0d0
em(i,j,k,5) = 1.0d0
else
em(i,j,k,0) = 0.d0
endif
```

Same equations used in the WarpX test

EMcLaw simulations set up

Metallic_materials_rd.f90: changing the if sentences to impose material relations (in this case, PEC)

```
! fill metallic materials
subroutine fill_metallic_materials( prob_lo, lo, hi, &
&      uout, uo_lo, uo_hi, &
&      dx, nGhost, nComp, Dwave) bind(C, name="fill_metallic_materials")

implicit none

integer, intent(in) :: lo(3), hi(3), nGhost, nComp, Dwave
integer, intent(in) :: uo_lo(3), uo_hi(3)
double precision, intent(in) :: prob_lo(3), dx(3)
double precision, intent(inout) :: uout(uo_lo(1):uo_hi(1),uo_lo(2):uo_hi(2),uo_lo(3):uo_hi(3),0:nComp-1)

integer :: i, j, k
double precision :: x,y,z,r2

do k = lo(3), hi(3)
  z = prob_lo(3) + (dble(k)+0.5d0) * dx(3)
  if((z.le.1.0).and.(z.ge.0.5)) then

    do j = lo(2), hi(2)
      y = prob_lo(2) + (dble(j)+0.5d0) * dx(2)
      if((y.le.1.0).and.(y.ge.0.5)) then

        do i = lo(1), hi(1)
          x = prob_lo(1) + (dble(i)+0.5d0) * dx(1)
          if((x.le.1.0).and.(x.ge.0.5)) then

            uout(i,j,k,0) = 0.0d0
            uout(i,j,k,1) = 0.0d0
            uout(i,j,k,2) = 0.0d0

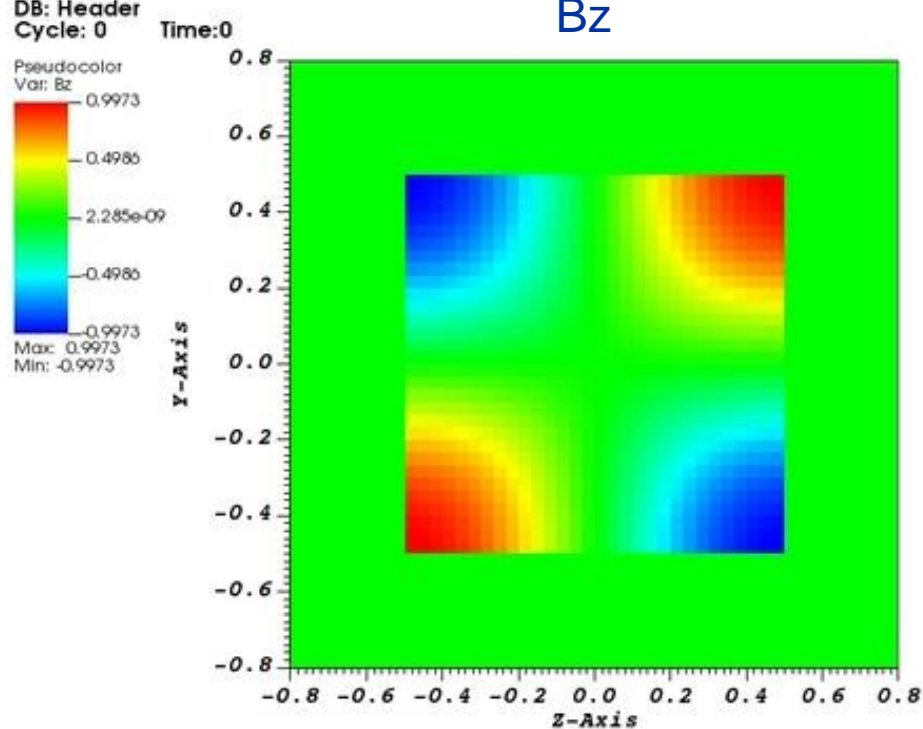
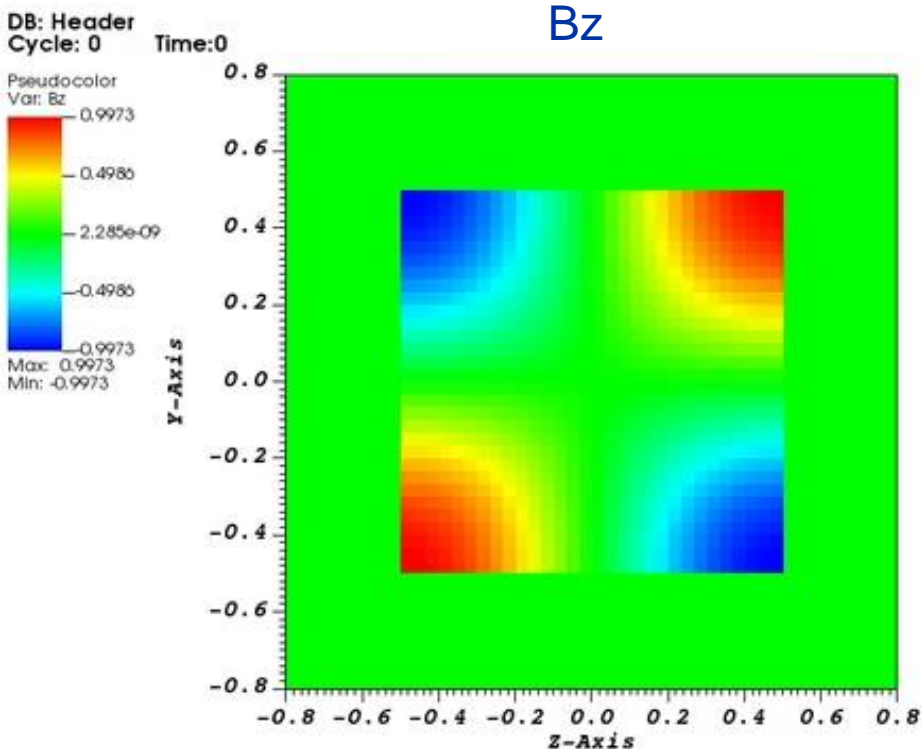
          endif
        end do
      endif
    end do
  endif
end do

end subroutine fill_metallic_materials
```

Seems to be some issue with the material properties defined in the DEFINES.H, and the routines in ep_mu_3d.f90

Already contacted Eduardo to look at this

First simulations



Material definition is not working correctly.
Also, initial conditions need to be checked

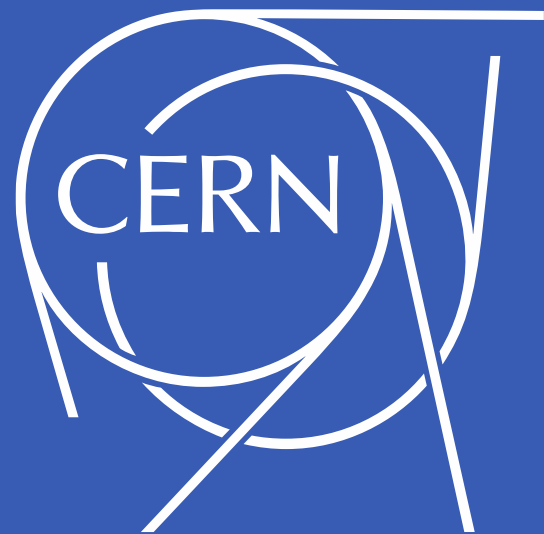
Outline

1. GitHub organization
2. Wake potential algorithm
3. Box resonator

Conclusions and next steps

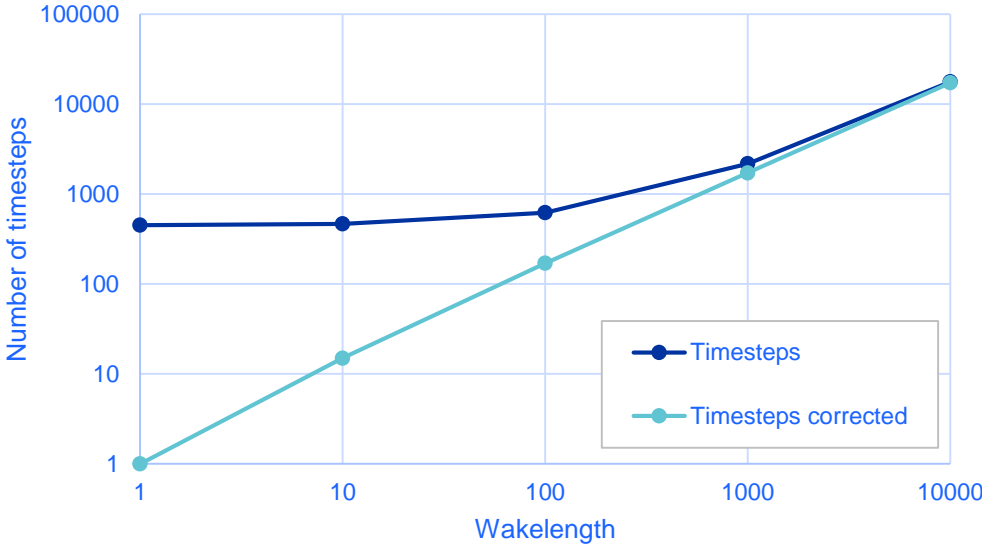
Next steps

- Debug and try the implemented algorithm
- Define the relation between time and the s vector
- Fix the problems with the Box resonator test and continue with the convergence analysis and the energy dissipation test
- Is the [Napoly alogorithm](#) needed?



Plots of the wakelength vs timestep study

Timesteps vs wakelength



s (source-test particle distance)

