

# Hadronic Event Shapes and Transverse Energy-Energy Correlations using the ATLAS detector

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The study of collider observables, including **event-shapes functions**, is well established to test QCD as they characterize the topology of the collisions.

The most recent ATLAS measurements of event shapes are:

- Measurement of hadronic event shapes in multijet final states at  $\sqrt{s} = 13$  TeV with the ATLAS detector. [[JHEP01 \(2021\) 188](#)]
- Determination of the strong coupling constant and test of asymptotic freedom from Transverse Energy-Energy Correlations in multijet events at  $\sqrt{s} = 13$  TeV with the ATLAS detector. [[ATLAS-CONF-2020-025](#)]

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Other relevant ATLAS measurements are:

- Measurement of TEECs in multijet events at 7 TeV using the ATLAS detector and determination of the strong coupling. [[Phys. Let. B 750 \(2015\) 427-447](#)]
- Determination of the strong coupling from TEECs in multijet events at 8 TeV using the ATLAS detector. [[Eur. Phys. J. 77 \(2017\) 872](#)]

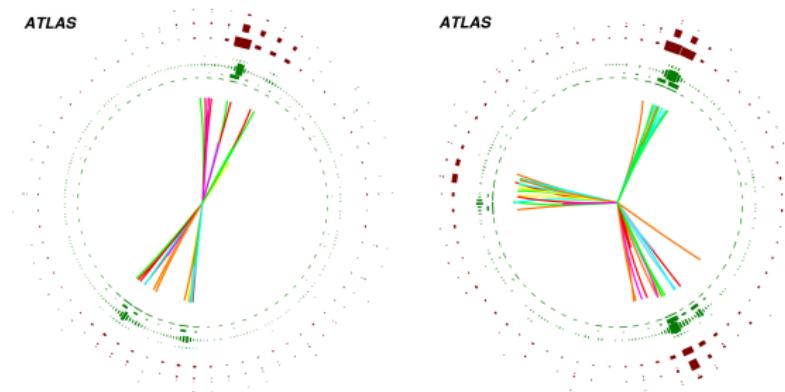
# Transverse thrust

**Transverse thrust:** the idea is to select the axis  $\vec{n}_T$  that maximizes the projection of the jet momenta in the transverse plane,

$$T_{\perp} = \max_{\vec{n}_T} \frac{\sum_i^{\text{jets}} |\vec{p}_{Ti} \cdot \vec{n}_T|}{\sum_i^{\text{jets}} |\vec{p}_{Ti}|}; \quad T_{\text{minor}} = \frac{\sum_i^{\text{jets}} |\vec{p}_{Ti} \times \vec{n}_T|}{\sum_i^{\text{jets}} |\vec{p}_{Ti}|}.$$

It is also useful to define  $\tau_{\perp} = 1 - T_{\perp}$ .

- IR safety, they are not affected by long-distance effects in  $e^+e^-$  collisions.
- $\tau_{\perp} = T_m \simeq 0$  for back-to-back, pencil-like configurations (left).
- $\tau_{\perp} \simeq 1/3$  for planar conf. (right),  $T_m \simeq 2/3$  for spherical configurations.



**Linearised sphericity tensor:** there is a family of event-shape variables derived from its eigenvalues. The formal definition of the tensor is given by

$$\mathcal{M}_{xyz} = \frac{1}{\sum_i^{\text{jets}} |\vec{p}_i|} \sum_i^{\text{jets}} \frac{1}{|\vec{p}_i|} \begin{pmatrix} p_{x,i}^2 & p_{x,i}p_{y,i} & p_{x,i}p_{z,i} \\ p_{y,i}p_{x,i} & p_{y,i}^2 & p_{y,i}p_{z,i} \\ p_{z,i}p_{x,i} & p_{z,i}p_{y,i} & p_{z,i}^2 \end{pmatrix} .$$

This tensor is a good quantity to extract information of the event's isotropy. Its eigenvalues satisfy  $\lambda_1 + \lambda_2 + \lambda_3 = 1$  and are ordered as  $\lambda_1 \geq \lambda_2 \geq \lambda_3$ .

**Transverse linearised sphericity tensor:** constructed using only the momentum components in the transverse plane,  $\mathcal{M}_{xy}$ . Its eigenvalues are  $\mu_1$  and  $\mu_2$ .

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The main event-shape variables derived from these tensors are:

$$S = \frac{3}{2}(\lambda_2 + \lambda_3) ; \quad S_\perp = \frac{2\mu_2}{\mu_1 + \mu_2} ; \quad A = \frac{3}{2}\lambda_3 .$$

- **Sphericity:** Larger values of  $S_\perp \in [0, 1]$  for more isotropic events in the T.P.
- **Aplanarity:** Larger values of  $A \in [0, 1/2]$  for less planar events.

## Event selection. Data and MC samples

The data sample corresponds to the full dataset recorded during the LHC  $p$ - $p$  Run 2 at  $\sqrt{s} = 13$  TeV. The available integrated luminosity is  $139 \text{ fb}^{-1}$ .

For this analysis, multi-jet events with the following cuts are selected:

- Jet reconstruction: anti- $k_T$  algorithm with  $R = 0.4$  and PFlow.
- Jet selection:  $p_T > 100$  GeV and  $|\eta| < 2.4$  for each jet.
- Event selection:  $H_{T2} = p_{T1} + p_{T2} > 1$  TeV using trigger HLT\_j460.

The measurements are performed for different regimes given by  $H_{T2}$  and  $n_{\text{jet}}$ .

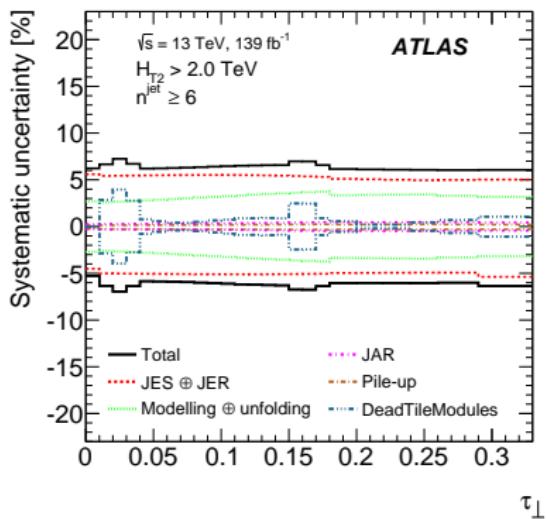
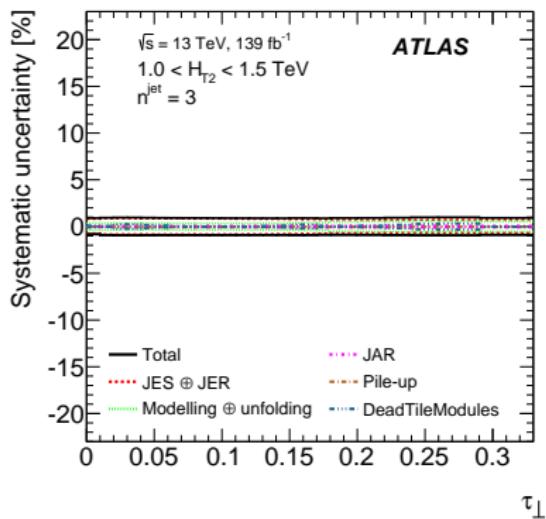
The table below contains the properties of the MC samples used in the analysis:

Generator	ME order	FS partons	PDF set	Parton shower
PYTHIA	LO	2	NNPDF 2.3 LO	$p_T$ -ordered
SHERPA	LO	2,3	CT14 NNLO	dipole
MADGRAPH	LO	2,3,4	NNPDF 3.0 NLO	$p_T$ -ordered
HERWIG	NLO	2,3	MMHT2014 NLO	angle-ordered ⊕ dipole

# Unfolding and experimental uncertainties

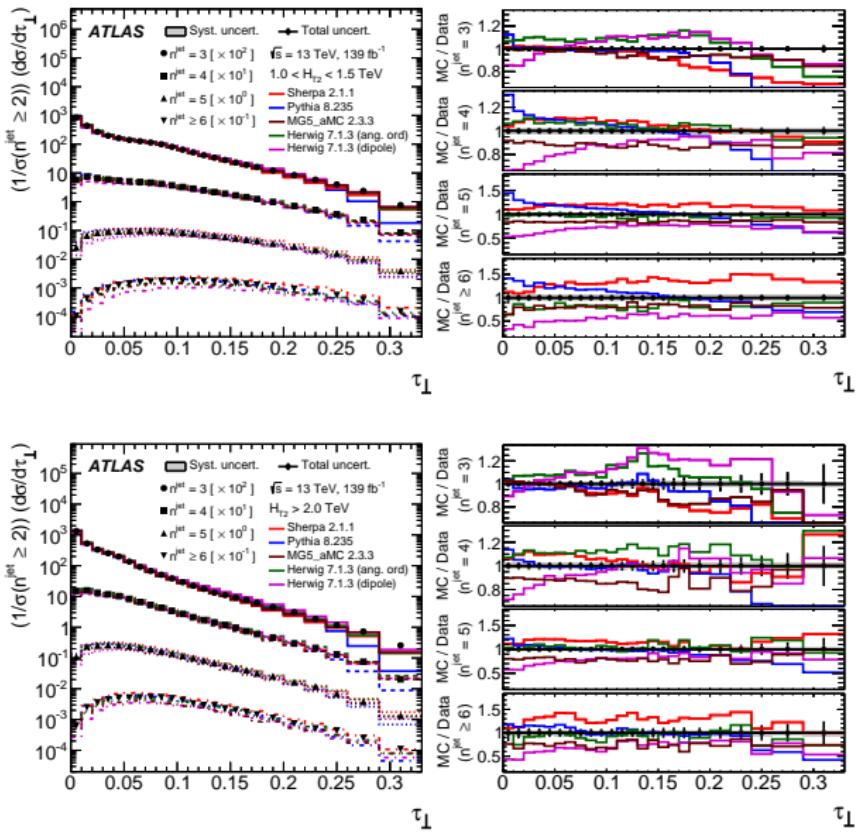
Data at detector level are unfolded to the particle level using the Iterative Bayesian unfolding. The method makes use of a transfer matrix that parameterises the probability of an event generated in one bin to be reconstructed in another bin.

The systematic sources are indicated on the legend from figures below:

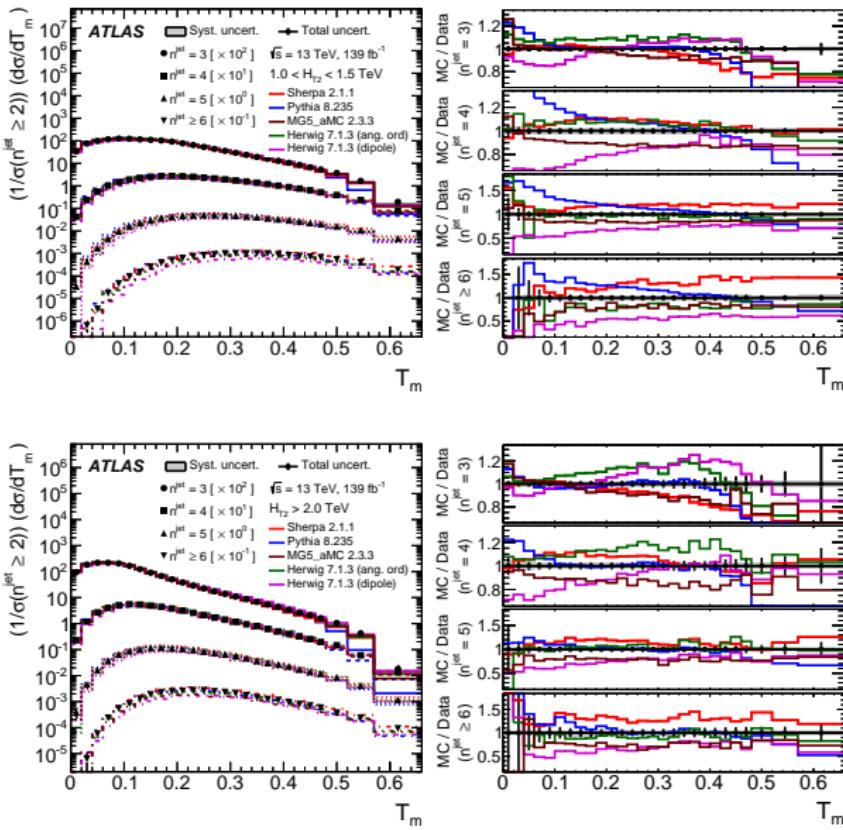


The exp. uncertainties increase for larger values of  $H_{T2}$  and jet multiplicity  $n_{\text{jet}}$ .

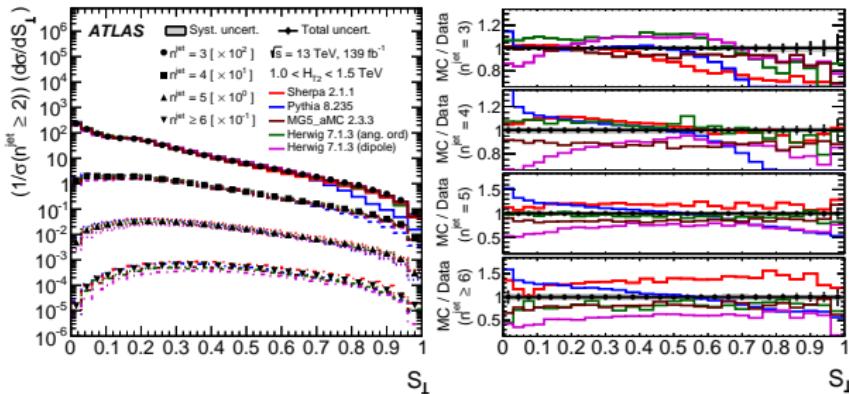
# Transverse thrust unfolded results



# Transverse thrust minor unfolded results



# Transverse sphericity unfolded results



- All MC predictions qualitatively describe the main features of the data.
- At low jet multiplicities, shape discrepancies are observed.
- At high jet multiplicities, shapes are better described but discrepancies in the normalisation are observed.
- These discrepancies show that these data provide a powerful testing ground for the understanding of the strong interaction at high energies.

# Transverse Energy-Energy Correlations

**TEEC function:** transverse energy-weighted azimuthal angular distribution of produced jet pairs in the final state,

$$\frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} = \frac{1}{\sigma} \sum_{i,j}^{\text{jets}} \int d\sigma_{pp \rightarrow \text{jets}} \frac{E_{T,i} E_{T,j}}{E_T^2} \delta(\cos \Delta\varphi_{ij} - \cos \phi) .$$

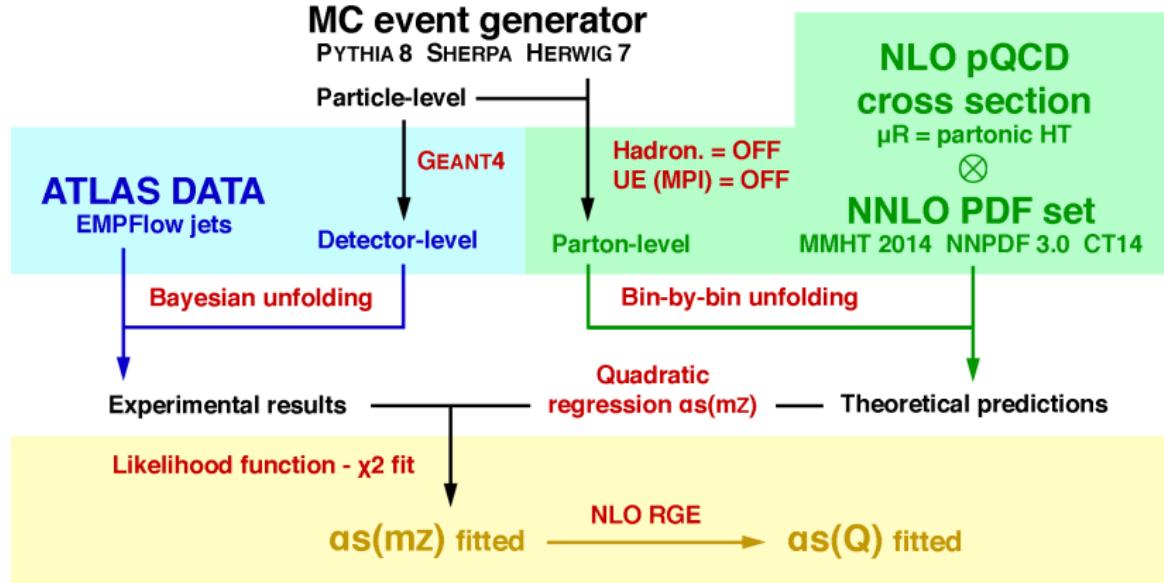
$E_T$  is the sum of the jet transverse energy and the normalization to  $\sigma$  ensures that the integral of the function over  $\cos \phi$  is unity.

**ATEEC function:** its forward-backward azimuthal angular asymmetry,

$$\frac{1}{\sigma} \frac{d\Sigma^{\text{asym}}}{d \cos \phi} = \frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \Big|_{\phi} - \frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \Big|_{\pi-\phi} .$$

- Large sensitivity to QCD radiation and the strong coupling  $\alpha_s(Q^2)$ .
- IR safety, they are not affected by IR divergences in  $e^+e^-$  collisions.
- Smaller sensitivity to IR divergences than other variables in  $pp$  collisions.
- Mild sensitivity to PDFs and factorization and renormalization scale variations.

# Analysis workflow



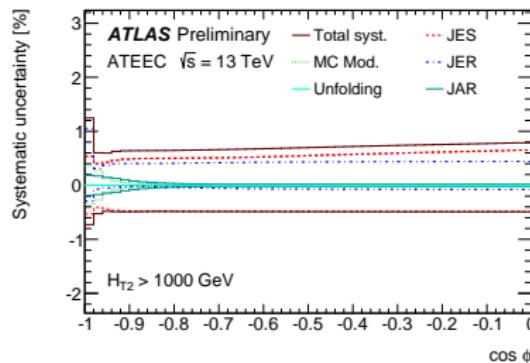
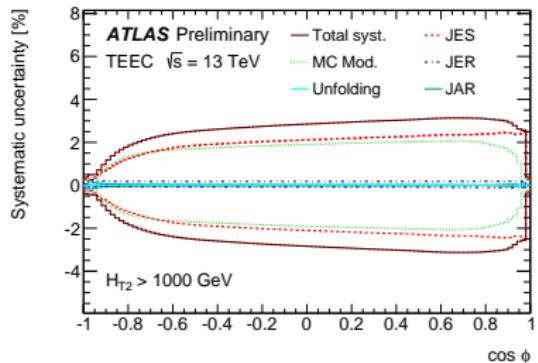
- TEEC function computed at fixed-order with a collinear cut  $|\cos \phi| < 0.92$ .
- Non-pQCD corrections computed with PYTHIA 8 tunes A14, AU2 and 4C.

# Event selection and experimental uncertainties

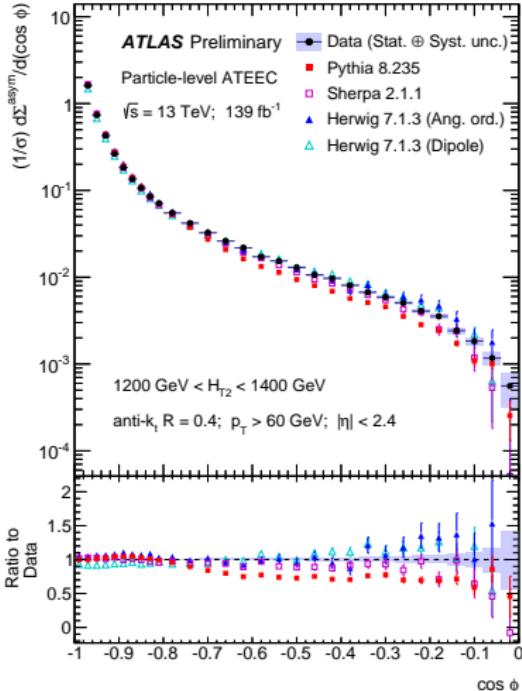
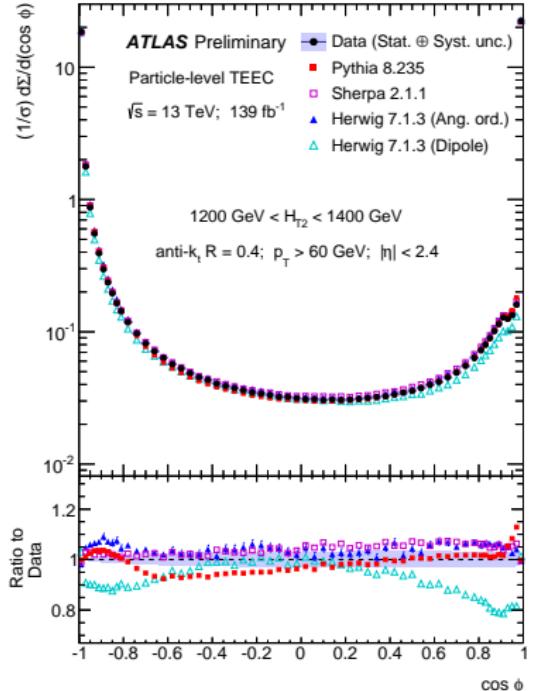
The data sample corresponds to the full dataset recorded during the LHC  $p\text{-}p$  Run 2 at  $\sqrt{s} = 13 \text{ TeV}$ . The available integrated luminosity is  $139 \text{ fb}^{-1}$ .

- PFlow anti- $k_{\text{T}}$   $R=0.4$  reconstructed jets with  $p_{\text{T}} > 60 \text{ GeV}$  and  $|\eta| < 2.4$ .
- Multi-jet events  $H_{\text{T}2} = p_{\text{T}1} + p_{\text{T}2} > 1 \text{ TeV}$  using the HLT\_j460 single-jet trigger.

The dominant uncertainties arise from knowledge of the jet energy scale and resolution and the modelling of the strong interaction in the unfolding.

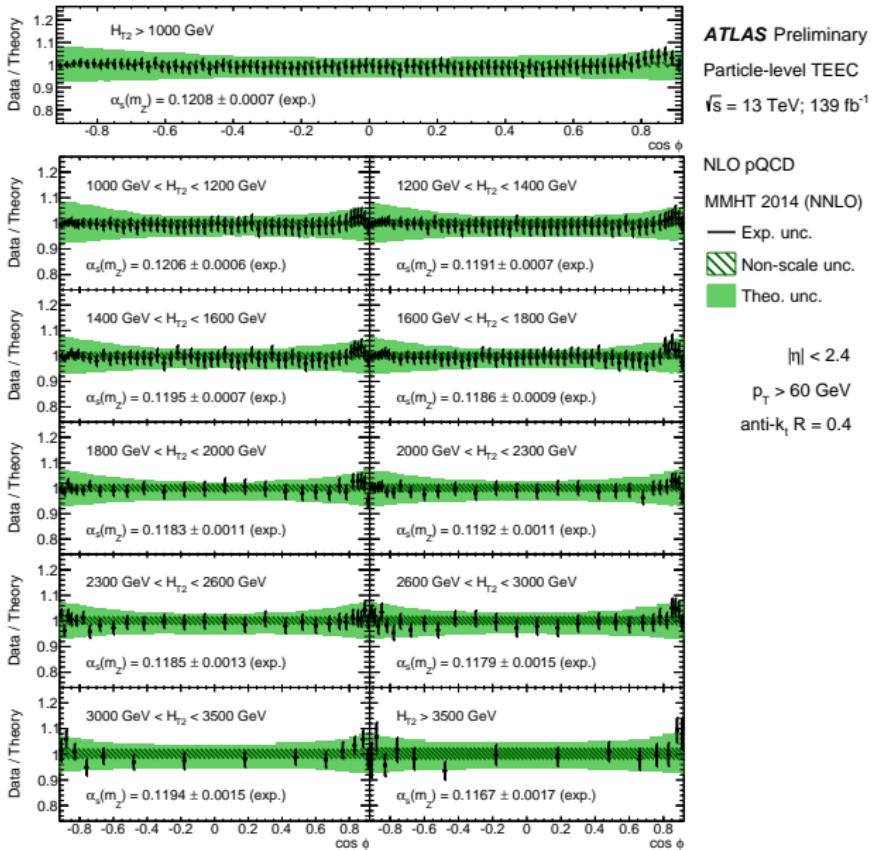


# TEEC and ATEEC unfolded results

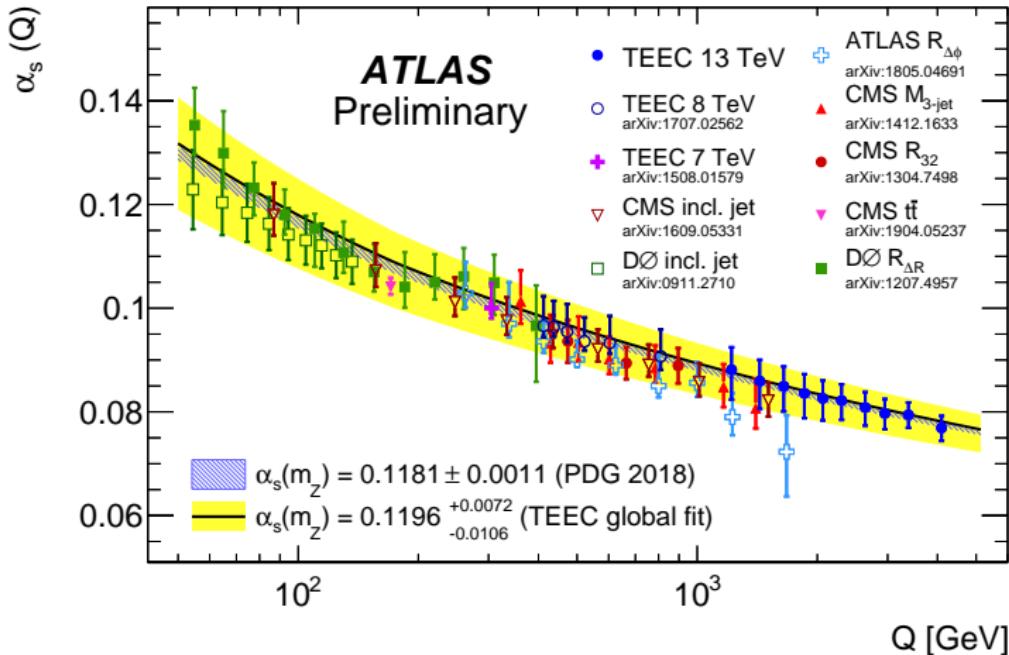


- SHERPA and HERWIG7 (Ang. ord.) give similar overall good description of data.
- The  $\alpha_s(Q^2)$  values are extracted from fits of the pQCD calculations to the data.

# Determination of the strong coupling from TEECs



# Test of asymptotic freedom from TEECs



- The  $\alpha_s(m_Z)$  values are evolved to  $\mu_R$  using the NLO solution of the RGE.
- These data can be used also as a test for new physics at large scales.  
[\[arXiv:1807.00894\]](https://arxiv.org/abs/1807.00894)

**TEEC analysis tests asymptotic freedom beyond TeV scale at NLO accuracy.**

$$\alpha_s(m_Z) = 0.1196 \pm 0.0004 \text{ (exp.)}^{+0.0072}_{-0.0105} \text{ (theo.)} \quad [\text{TEEC global fit}]$$

$$\alpha_s(m_Z) = 0.1195 \pm 0.0006 \text{ (exp.)}^{+0.0084}_{-0.0107} \text{ (theo.)} \quad [\text{ATEEC global fit}]$$

- Data results can be used to validate multi-jet production from MC event generators and to test new physics at large scale regimes.
- The agreement between data and theoretical predictions at NLO in pQCD is excellent at large momentum transfers.
- The strong coupling  $\alpha_s$  is determined in ten intervals, testing asymptotic freedom beyond the TeV scale.
- The extracted values are in good agreement with the current world average and with previous determinations.
- **NNLO corrections will reduce the scale uncertainties which are dominant.**