# **Atos QLM Fast-Start**



# **Advance tools**

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# Lecture: Optimizers

#### **Some context**

- In order to increase the **fidelity** of outputs of a quantum circuit, some considerations need to be taken into account:
  - Quantum circuits are implemented by real quantum processors with **physical** limitations. These limitations may include a specific, fixed chip topology, or the existence of a preferred set of quantum gates

 Given a quantum circuit, in general it is NP-hard to find the shortest equivalent circuit. Circuit length is specially important for NISQ processors. This problem can approximately solved by using heuristic optimisers

### **Optimizers**

- We will discuss 3 kinds of circuit optimizer:
  - NNizer: Taking as input a quantum circuit and a restricted connectivity graph, it recasts the circuit taking into account the processor topology
  - PBO: It allows to find specific patterns in a circuit and replace them by an equivalent user-defined gate. This can be useful when some gates can be implemented natively faster (or at higher fidelities) than others in a given architecture
  - GraphOpt: It takes a circuit as input and tries to find a shorter equivalent circuit by performing a local search in the space of unitaries

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# **Quantum Circuits Topology Optimizer**

General description

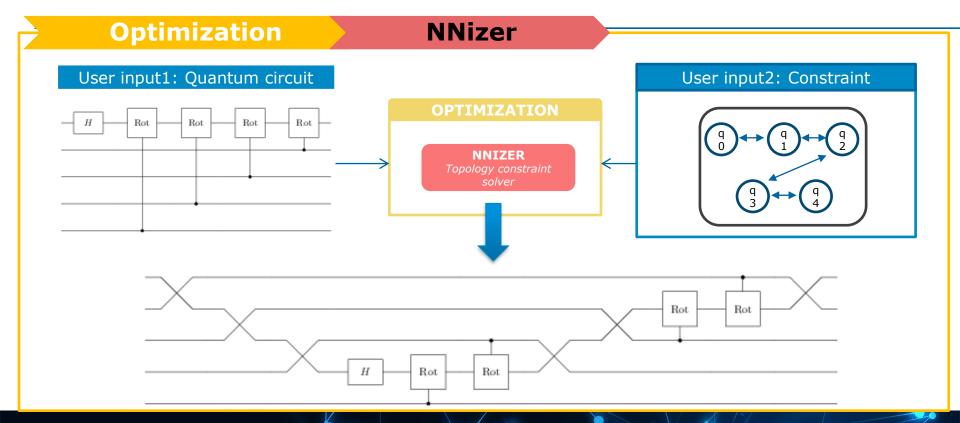
#### **Optimization**

#### **NNizer**

- Depending on the hardware implementation of the qubits, topology constraints for Nearest Neighbors may apply
- ► The NNIZER can be provided with any constraint described by the user. It can then observe the input circuit and perform the necessary changes to allow the run using the given constraints

# **Quantum Circuits Topology Optimizer**

NNizer workflow



#### Topology & HardwareSpecs

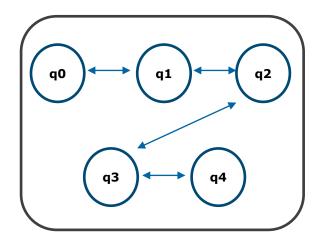
#### from qat.core import Topology

My\_topology=Topology()

for i, j in [(0, 1), (1, 2), (2, 3),(3, 4)]: my topology.add edge(i, j)

from qat.core import HardwareSpecs

My\_hardware = HardwareSpecs(nbqbits=5, topology=my topology)

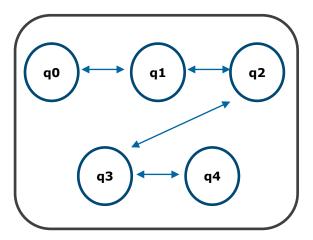


#### Topology & HardwareSpecs

Another way:

from qat.core import Topology, TopologyType, HardwareSpecs

My\_hardware = HardwareSpecs(nbqbits=5, topology=Topology(type=TopologyType.LNN))



#### QuameleonPlugin

from qat.core import QuameleonPlugin from qat.qpus import LinAlg

qpu = QuameleonPlugin(specs=My hardware) | LinAlg()

- QuameleonPlugin adds contraints coming from the hardware specification created previously.
- Only compliant circuit will be executed with this stack.

#### in the stack

```
from qat.core import QuameleonPlugin
from qat.qpus import LinAlg

qpu = QuameleonPlugin(specs=My_ hardware) | LinAlg()

from qat.plugins import Nnizer

final_stack = Nnizer() | qpu

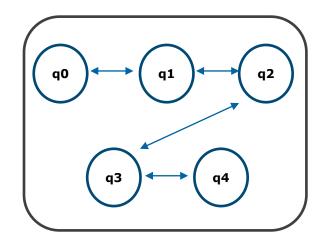
result = final_stack.submit(job)
```

Adding the Nnizer plugin to the stack will solve the issue by modifying the circuit accordingly to the topology.

#### topology options

Example of json file to be passed as argument

```
{"edges": {"0": [1],
            "1": [0, 2],
            "2": [1, 3],
            "3": [2, 4],
            "4": [3]}
```



Topology can be directional (i.e for CNOT)

#### topology options

- ► Few methods are implemented in **Nnize** to solve the swap insertion problem:
  - atos: based on a strict generalization of the algorithm described in <u>An</u>
     <u>Efficient Method to Convert Arbitrary Quantum Circuits to Ones on a</u>
     <u>Linear Nearest Neighbor Architecture</u> by *Hirata and al.*
  - sabre: implementation of <u>Tackling the Qubit Mapping Problem for</u> <u>NISQ-Era Quantum Devices</u> by *Gushu Li, Yufei Ding and Yuan Xie*
  - bka: implementation of <u>Efficient mapping of quantum circuits to the</u>
     <u>IBM QX architectures</u> by *Alwin Zulehner, Alexandru Paler and Robert Wille*
  - pbn: based on a strict generalization of the algorithm described in <u>Synthesis of quantum circuits for linear nearest neighbor</u> <u>architectures</u> by <u>Mehdi Saeedi</u>, <u>Robert Wille and Rolf Drechsler</u>

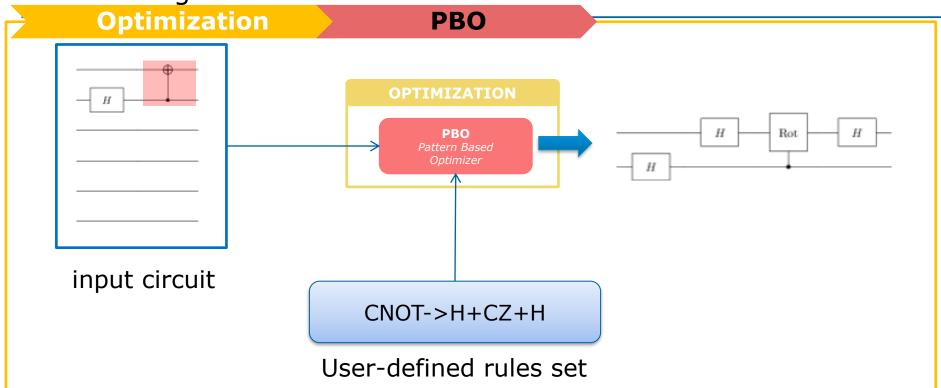
#### compile method

```
from qat.plugins import Nnizer
from qat.core import Batch
nnizer = Nnizer(method="atos")
nnized_batch = nnizer.compile(Batch(jobs=[ansatz]),
                my hardware)
nnized ansatz circuit = nnized batch.jobs[0].circuit
#Number of gates in the circuit
len(nnized ansatz circuit.ops)
#List of the qubits
nnized batch.jobs[0].qubits
```

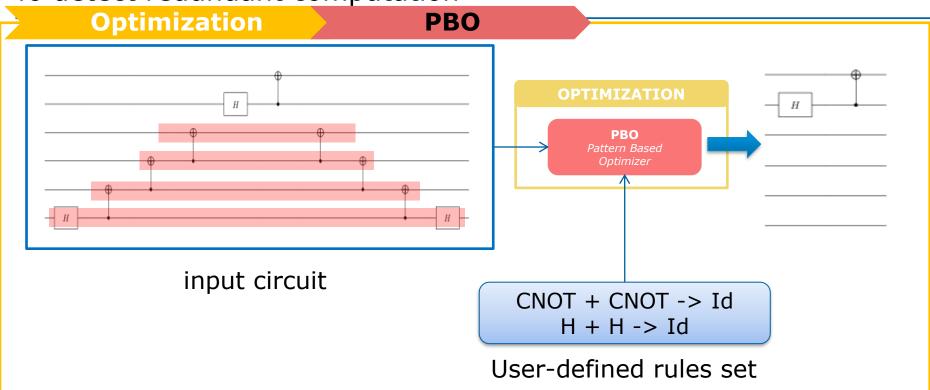
### **Optimizers**

- We will discuss 3 kinds of circuit optimizer:
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  - PBO: It allows to find specific patterns in a circuit and replace them by an
    equivalent user-defined pattern. This can be useful when some gates can be
    implemented natively faster (or at higher fidelities) than others in a given
    architecture
  - GraphOpt: It takes a circuit as input and tries to find a shorter equivalent circuit by performing a local search in the space of unitaries

To re-write gates

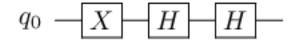


To detect redundant computation



```
from qat.lang.AQASM import Program, H, X

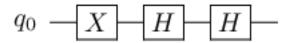
# Define initial circuit (X - H - H circuit)
prog = Program()
qubit = prog.qalloc(1)
prog.apply(X, qubit)
prog.apply(H, qubit)
prog.apply(H, qubit)
circ = prog.to_circ()
%qatdisplay circ
```



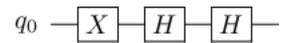
#### Example

from qat.pbo import GraphCircuit

# Create a graph object and load circuit graph = GraphCircuit() graph.load\_circuit(circ)



```
from qat.pbo import GraphCircuit
# Create a graph object and load circuit
graph = GraphCircuit()
graph.load_circuit(circ)
# Define two patterns
left_pattern = [("H", [0]), ("H", [0])]
right_pattern = []
```

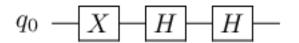


```
from qat.pbo import GraphCircuit

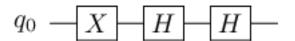
# Create a graph object and load circuit
graph = GraphCircuit()
graph.load_circuit(circ)

# Define two patterns
left_pattern = [("H", [0]), ("H", [0])]
right_pattern = []

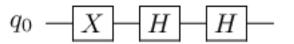
# Replace left_pattern by right_pattern
graph.replace_pattern(left_pattern, right_pattern)
```



```
from qat.pbo import GraphCircuit
# Create a graph object and load circuit
graph = GraphCircuit()
graph.load circuit(circ)
# Define two patterns
left pattern = [("H", [0]), ("H", [0])]
right pattern = []
# Replace left pattern by right pattern
graph.replace pattern(left pattern, right pattern)
while graph.replace pattern(left pattern, right pattern):
  continue
```



```
from qat.pbo import GraphCircuit
# Create a graph object and load circuit
graph = GraphCircuit()
graph.load circuit(circ)
# Define two patterns
left pattern = [("H", [0]), ("H", [0])]
right pattern = []
# Replace left pattern by right pattern
graph.replace pattern(left pattern, right pattern)
while graph.replace pattern(left pattern, right pattern):
  continue
# Get the optimized circuit
optimized circ = graph.to circ()
```





#### Abstract gates

```
# graph.to_circ() won't work since "HZ" gate is not known
from qat.lang.AQASM import AbstractGate
graph.add_abstract_gate(AbstractGate("HZ", [], 1))
# graph.to_circ() is now working
optimized circ = graph.to circ()
```

# **Optimizers**

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  - PBO: It allows to find specific patterns in a circuit and replace them by an
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    implemented natively faster (or at higher fidelities) than others in a given
    architecture
  - GraphOpt: It takes a circuit as input and tries to find a shorter equivalent circuit by performing a local search in the space of unitaries

#### Description

- The main goal of GraphOpt reduce the total number of gates among
  - H, CNOT, X
  - Rz/Ph

These gates represent a set typically available in real quantum hardware implementations.

- ▶ A preprocessing step has been included in our implementation that splits CPh, CRz and Toffoli gates into subcircuit in the adequate gate set.
- It is inspired by the result:

**Quantum Physics** 

Automated optimization of large quantum circuits with continuous parameters

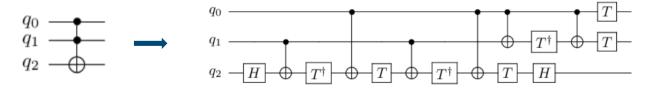
Yunseong Nam, Neil J. Ross, Yuan Su, Andrew M. Childs, Dmitri Maslov

(Submitted on 19 Oct 2017 (v1), last revised 1 Jun 2018 (this version, v2))

To optimize circuits

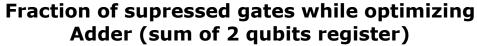
**Optimization GraphOpt** input circuit **GRAPHOPT** 

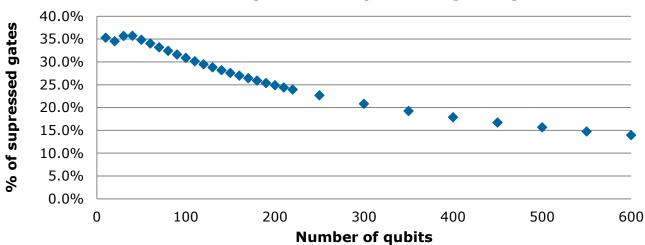
▶ **First step**: expand the circuit using only the set of gates. This leads to an increase of the number of gates



▶ **Second step:** optimize the circuit to reduce the number of gate after expansion







▶ More than 30% of supressed gates for # qubits < 100! (after expansion)

```
from qat.plugins import Graphopt
# from qat.graphopt import Graphopt # Equivalently

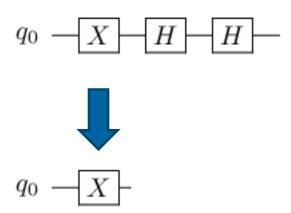
my_stack = Graphopt() | LinAlg()

my_stack.submit(job)
```

from qat.plugins import Graphopt # from qat.graphopt import Graphopt # Equivalently

my\_stack = Graphopt() | LinAlg()

my\_stack.submit(job)



# Hands-on 8: Optimizers

### **Hands-on 8: Optimizers**

► Log on the QLM

Go to Hands-on 8 directory :

http://127.0.0.1:8888/tree/notebooks/Hands-on8

▶ Open and complete the notebook *Optimising-QAOA.ipynb* 

# Lecture: Noisy Simulation

# The Problem of Noise How Quantum and Classical Fluctuations affect QC

- Most quantum algorithms can be implemented by circuits consisting on a fixed sequence of gates.
- ▶ Noise can be thought of as introducing **random gates** in a particular circuit. The nature of these gates depends on the source of noise.
  - The quantum advantage gets slightly modified if noise is very small, but can be destroyed if noise is too large or if circuits are too long. Information about this will be contained in the **hardware specifications**.
- ► The way to fight noise is to implement **quantum error correction**. This is out of reach for NISQ processors. In this case, postprocessing techniques may be used to undo the effects of noise for a particular task.

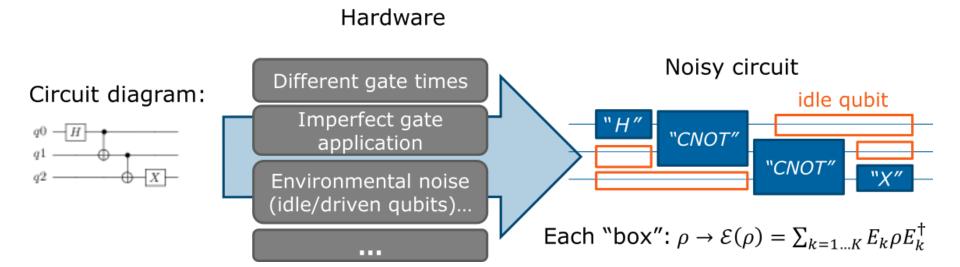
# **The Problem of Noise** On the QLM

- A discrete description of the temporal evolution of a noisy circuit.
- Starting from a perfect quantum circuit, we build a noisy quantum circuit:
  - By specifying the meaning of gates
  - By potentially adding new operations that describe the effect of noise (for e.g. the effect of noise during "idling" periods).
- ► The resulting circuit is made up of "boxes", each of which describes an action on the density matrix of the qubits

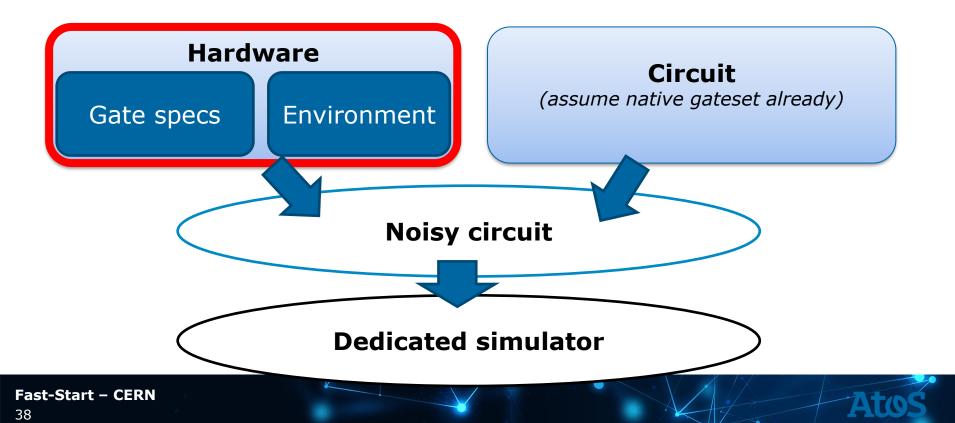
## **Noisy Circuit Generation**

#### From Noiseless to Noisy Circuits

Using a clean circuit and a hardware specification, the Atos QLM generates a noisy circuit object:



## **Noisy quantum simulation** Overview



#### **Noise models**

- ▶ The notion of "noise model" refers to the action of the gates and the environment on the qubits' density matrix p.
- ▶ There are several ways to describe such **noise models**.
- ▶ The only common property is that they represent a **linear map**.
- They sometimes come with extra properties such as trace preservation (TP) and complete positivity (CP).
- ▶ When these two properties are fulfilled, one can speak of **CPTP maps**, or **quantum channels**.

## QuantumChannelKraus

#### Example

```
import numpy as np from qat.quops import QuantumChannelKraus
```

You can define Quantum Channel with a Kraus representation.

In that example, roughly speaking: 80% of the time the Hadamard gate will be applied correctly.

20% of the time nothing will be applied.

## Mathematical Description of Noisy Channels Kraus Representation

Generic mathematical description for quantum processes (imperfect gates, environmental noise...)

completely positive, trace-preserving maps:

$$\mathcal{E}(\rho) = \sum_{k=1...K} E_k \rho E_k^{\dagger}$$

with  $\rho$ : density matrix

 $E_k$ : Kraus operators, with property:  $\sum_k E_k^{\dagger} E_k = 1$ 

"Ideal" gate: special case K = 1,  $E_1 = U$  unitary matrix

Pure state: special case  $\rho = |\psi\rangle\langle\psi|$ 

## **Mathematical Description of Noisy Channels** Kraus Representation

Kraus operators can depend on some parameter t

$$E_k \to E_k(t)$$

Use case: modelling idle noise since the idle times of a qubit can vary during the circuit execution.



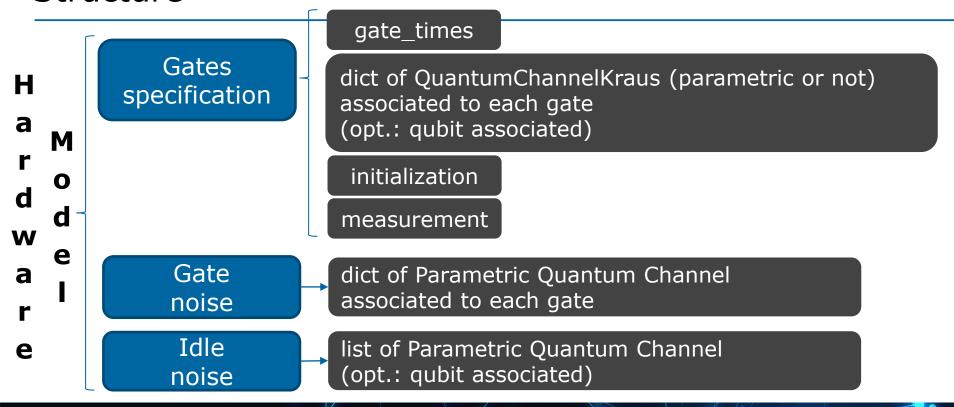
# **Some Noise Models**Noise depends on architecture

Noise models depend on the nature of the physical architecture. Some factors to take into account are the **temperature** of operation, the **lifetime** of qubits and the **quality** of applied gates. Classical noise can be modeled as bit-flips, ie. apply the Pauli X operator with a probability p:

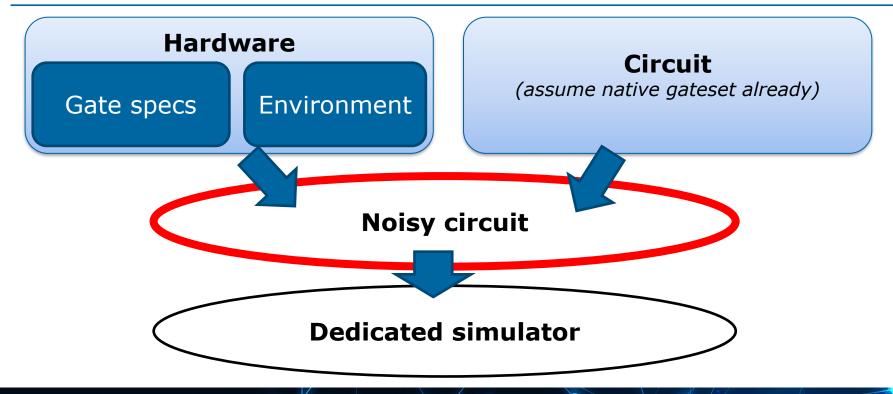
$$\rho = |\psi\rangle\langle\psi| \longrightarrow \mathcal{E}_{classical}(\rho) = (1-p)\rho + pX\rho X$$

- Typical Quantum Noise Channels include:
  - **Amplitude Damping**: This arises when qubits loose their energy to the environment
  - Phase Damping: This is due to quantum processes which do not imply energy transfer

# **Noisy Circuit Generation**Structure



## **Noisy quantum simulation** Overview



# **Noisy Circuit Generation**

## Example: Gates

The definition of gates consists of the specification of (i) duration and (ii) Kraus operators:

```
gate_times = { "Foo": 10,
                      "Bar": lambda theta: theta/5.+5..
                                                                          Duration
                     "RX": lambda theta: theta/10.}
quantum_channels = {
    "Foo": QuantumChannelKraus([np.sqrt(0.75)*foo_mat,
                              np.sqrt(0.25)*np.array([[0,1],[1,0]],
                                                   dtype = np.complex )1),
    "Bar": lambda theta: QuantumChannelKraus([np.array([[1, 0, 0],
                                                   [0, 1, 0, 0],
                                                   [0, 0, np.exp(theta*1j), 0],
                                                   [0, 0, 0, 1.]], dtype = np.complex_)]),
    "RX" : {
                                                                                                                     Operator definition
        0: lambda theta: QuantumChannelKraus([np.array([[np.cos(theta/2+.01), -1j*np.sin(theta/2+.01)],
                                                      [-1j*np.sin(theta/2+.01), 1j*np.cos(theta/2+.01)]],
                                                     dtype = np.complex )]),
        1: lambda theta: QuantumChannelKraus([np.array([[np.cos(theta/2+.02), -1j*np.sin(theta/2+.02)],
                                                      [-1j*np.sin(theta/2+.02), 1j*np.cos(theta/2+.02)]],
                                                     dtype = np.complex )]),
```

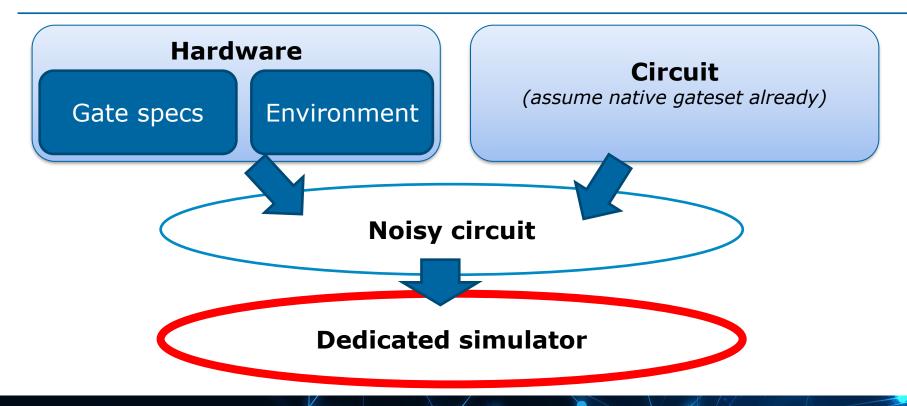
gates\_spec = GatesSpecification(gate\_times, quantum\_channels=quantum\_channels)

## **Noisy Circuit Generation** Example: Environment Modeling

 An environment model consists of a user-defined noise for gates (in this example it is obviated) and environment (applied to qubits when idle)

```
# custom noise
def my custom noise(idling time):
    error prob = 1 - np.exp(-idling time / 400.)
    return QuantumChannelKraus([np.sqrt(1-error prob)*np.identity(2), np.sqrt(error prob)* np.array([[0,1],[1,0]])],
                                                                                                                       Effect of
                              name = "MyCustomNoise")
                                                                                                                       environment
# we assume that each qubit experiences a different AD/PD noise, and the same custom noise
idle noise = {
   0: [ParametricAmplitudeDamping(T 1=210), ParametricPureDephasing(T phi=105), my custom noise],
   1: [ParametricAmplitudeDamping(T 1=208), ParametricPureDephasing(T phi=95), my custom noise],
   2: [ParametricAmplitudeDamping(T 1=199), ParametricPureDephasing(T phi=101), my custom noise],
# note: in the case of identical noise parameters for each qubit, we could have written:
                                                                                                                        No noise to be
# idle noise = [ParametricAmplitudeDampinq(T 1=200), ParametricPureDephasinq(T phi=100), my custom noise]
                                                                                                                       introduced after
                                                                                                                        each gate
hardware model = HardwareModel(gates spec, None, idle noise)
```

## **Noisy quantum simulation** Overview



# **Noisy Circuit Simulators**Two Approaches for Noisy Circuit Simulation

Deterministic simulation of the matrix evolution

$$\mathcal{E}(\boldsymbol{\rho}) = \sum_{k_M} \left( E_{k_M}^{(M)} \dots \left( \sum_{k_1} E_{k_1}^{(1)} \boldsymbol{\rho} E_{k_1}^{(1)\dagger} \right) \dots E_{k_M}^{(M)\dagger} \right)$$

- Advantages: returns the full density matrix after evolution
- Drawbacks: resource-intensive. Subject to discretization error

Stochastic sampling of trajectories

$$\mathcal{E}(\boldsymbol{\rho} = |\boldsymbol{\psi_0}\rangle\langle\boldsymbol{\psi_0}|) = \sum_{k_1..k_M} E_{k_M}^{(M)} ... E_{k_1}^{(1)} |\boldsymbol{\psi_0}\rangle\langle\boldsymbol{\psi_0}| E_{k_1}^{(1)\dagger} ... E_{k_M}^{(M)\dagger}$$

- Advantages: less resource consuming. Not subject to discretization error
- **Drawbacks**: provides estimates of the expectation values. Storage exponential on number of trajectories

# **Noisy Circuit Simulators** Example

```
import qat.noisy, qat.linalg
# We define a first noisy quantum processor with this hardware model,
# and a deterministic method to simulate the computation of the circuit
noisy_qpu_1 = NoisyQProc(hardware_model = hardware_model, sim method = "deterministic")
# We define a second noisy quantum processor with the same hardware model,
# but this time with a stochastic method to simulate the computation of the circuit
noisy qpu 2 = NoisyQProc(hardware model=hardware model,
                         sim method="stochastic",-
                         backend simulator=qat.linalg.LinAlg(),
                         n samples=10000)
```

a noisy qpu is a pair of (hardware model, simulator method)

2 types of noisy simulators

the task can then be executed as usual

# **Noisy Circuit Simulators** Summing Up

- Density matrix simulation is a costly **deterministic** method. It is limited to few qubits.
- To reach large number of qubits: Monte-Carlo methods i.e **stochastic** sampling:
  - number of samples (hence accuracy) is defined by user
  - The error corresponds to the error bar on the probability, evolving like 1/sqrt(nb samples)
  - You can also specify the backend simulator (linalg, MPS, Feynman)

Note that contrary to ideal circuit simulators, we do not have access to the quantum amplitudes, but merely the probabilities.

# Hands-on 9: QAQA noisy simulation

## Hands-on 9: noisy simulation

► Log on the QLM

► Go to Hands-on 9 directory :

http://127.0.0.1:8888/tree/notebooks/Hands-on9

▶ Open and complete the notebook *Noisy-QAOA.ipynb* 

# Lecture: Simulators

Linalg

#### **Simulation**

#### Linalg

Based on linear algebra. N qubits represented by a  $2^N$  vector. Heavy load on memory bandwidth and memory access latency.

- general purpose simulator, any gate, any arity
- +
- linear simulation time in function of number of gates
- Predictable run-time and memory usage
- Access to entire amplitude vector

- Memory usage: 2<sup>N</sup>
  - Execution time grows exponentially with number of qubits

Feynman

#### **Simulation**

#### Feynman

Based on Feynman path integral. Computes all final reachable states and sums the contributions of each path.



- Depending on the number of "touched" states, memory usage can be very low.
- Fast for circuits with few dense gates
- Any gate up to arity 3



Run-time exponential in the number of dense gates (like Hadamard)

MPS

#### **Simulation**

#### **MPS**

Based on Matrix product states representation

- MPS is suited to simulate circuit with low entanglement
- Simulation time and memory size depend on circuit entanglement.
- For low/medium entangled circuit, low memory usage, fast simulation
- Up to 1000 qubits could be simulated with low entanglement.
- Cutoff threshold on Schmidt coefficients can be specified

- Limited to gates with at most arity 3
- Only accepts gates acting on neighbouring qubits. Circuit need to be nnized

Stabs

#### **Simulation**

#### **Stabs**

Based on stabilizer formalism



- Allows to simulate a very large number of qubits
- Very efficient simulation of Clifford circuits

- Restricted available gates: CNOT,H,CZ,S,X,Y,Z,SWAP (gate T and Toffoli not accepted)
- Amplitudes are only determined up to a global phase

Binary Decision Diagrams

#### **Simulation**

**BDD** 

Based on QMDDs (Quantum Multi-valued Decision Diagrams)



- Accepts any gate, with arbitrary arity (but connectivity restrictions)
- Allow to simulate more qubits than linalg



gates need to act on neighboring qubits, except for controls, which can be taken arbitrarily far from the gate application.

#### **Use cases:**

- Shor, especially Toffoli-based arithmetics
- circuits containing "a lot of 0,1-valued unitaries" tend to behave well on QMDDs

# Hands-on 10: Simulators

#### **Hands-on 10: Simulators**

► Log on the QLM

Go to Hands-on10 directory :

http://127.0.0.1:8888/tree/notebooks/Hands-on10

Open and complete the notebook Simulators.ipynb

# Thank you.

#### **Gaëtan Rubez**

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