

# Flavor symmetries in the SMEFT

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## Standard Model Effective Field Theory

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

$$\mathcal{L}_d = \sum_i C_i \mathcal{O}_i^{(d)} \quad C_i = \text{Wilson coefficients}$$

$\mathcal{O}_i^{(d)}$  = gauge-invariant operators

SMEFT describes any nearly-decoupled ( $\Lambda \gg v$ ) BSM physics  
with “good” analyticity/geometry properties in the scalar sector

- ▶ **SM symmetries** → fully  $SU(3) \times SU(2) \times U(1)$  invariant
- ▶ **SM fields** →  $5 \times 3$  independent fermionic fields

$$q_\alpha, l_\alpha, u_\alpha, d_\alpha, e_\alpha \quad \alpha = 1, 2, 3$$

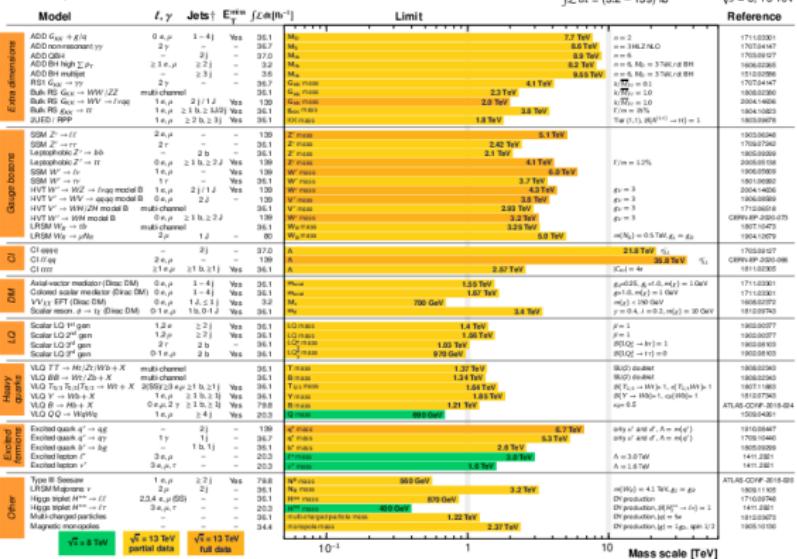
- ▶ no RH neutrinos: only Majorana  $m_\nu$  through  $\mathcal{L}_5$

# The global SMEFT program

resonance searches @ LHC suggest that NP is likely nearly decoupled

ATLAS Exotics Searches\* - 95% CL Upper Exclusion Limits

Status: May 2020



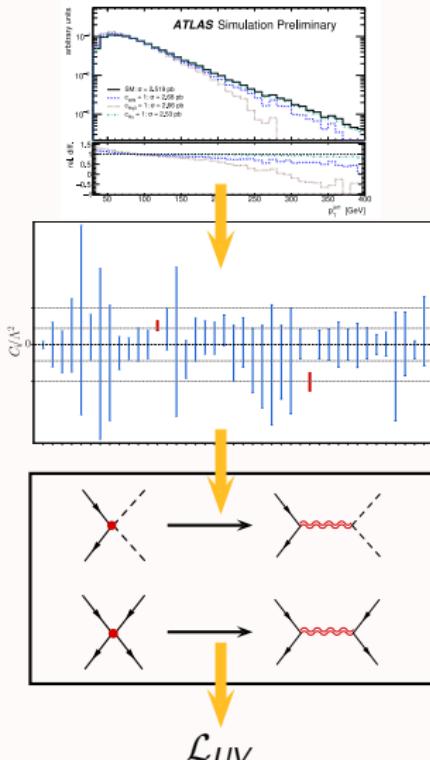
\*Only a selection of the available mass limits on new states or phenomena is shown.

†Small-radius (large-radius) jets are denoted by the letter J (S).

at the same time, no UV scenario is preferred in a compelling way

# The global SMEFT program

**agnostic approach:** let data tell us what NP looks like



SMEFT parameterizes  
anomalous rates & spectral distortions

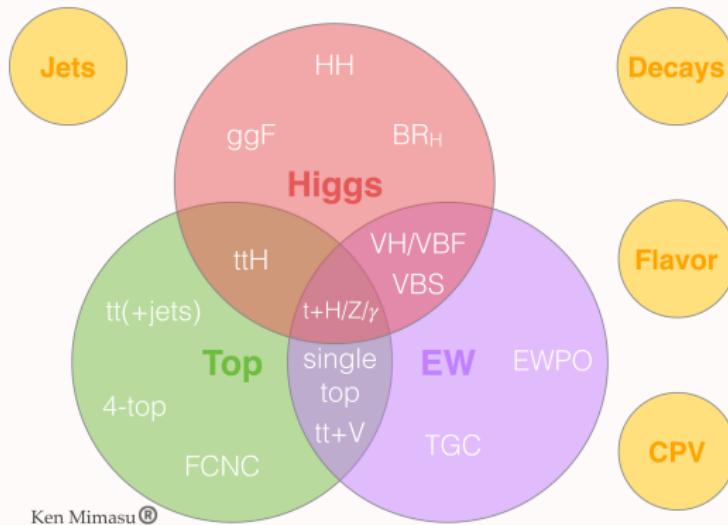
Global analysis → identify  $C_i \neq 0$

Identify compatible simplified models

Embed in UV-complete model

# The SMEFT program at the LHC (and beyond)

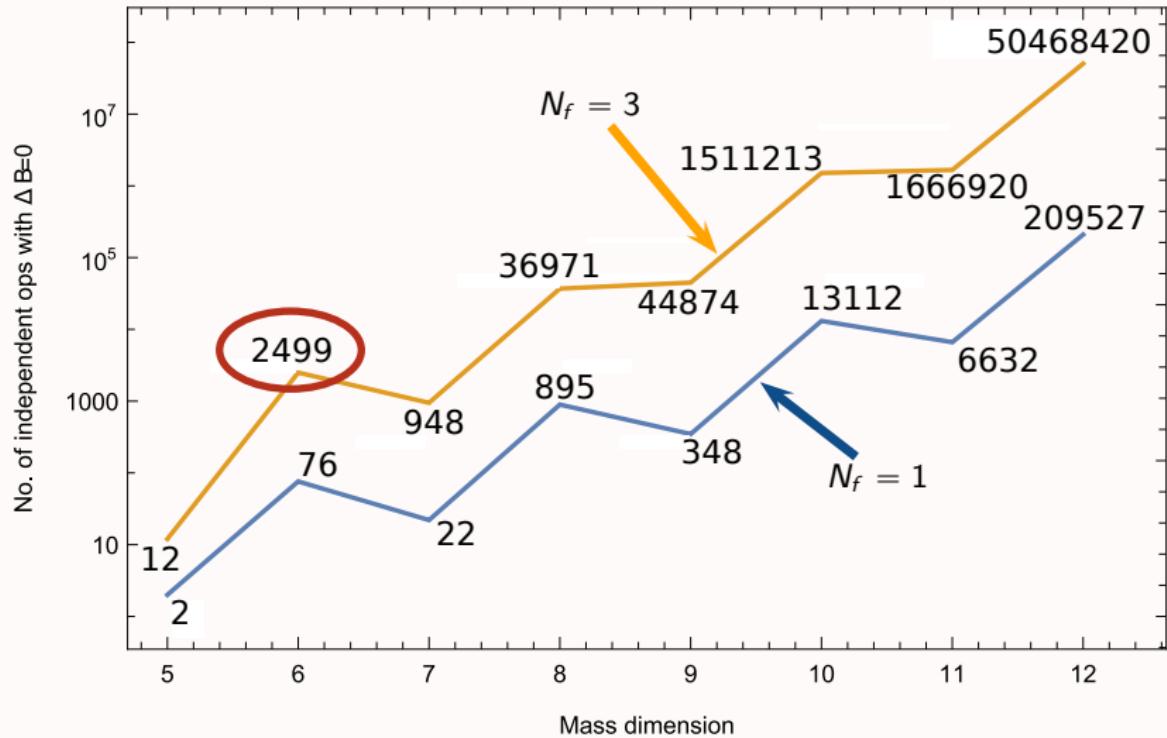
- ▶ “indirect” searches to complement bump hunt
- ▶ make the most of future luminosities → LHC as a precision machine
- ▶ agnostic approach requires **combining** multiple sectors



- ◀ theory studies performed for ~10 years, ATLAS+CMS program starting
- ◀ longer term plan: merge with lower E measurements

# A very large parameter space

Henning,Lu,Melia,Murayama 1512.03433



# A very large flavorful parameter space

## Classification within Warsaw basis

Grzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

Class	CP	<del>CP</del>	Total
$X^3$	2	2	4
$\varphi^6 + \varphi^4 D^2$	3	-	3
$\varphi^2 X^2$	4	4	8
$\varphi^2 \psi^2$	27	27	54
$\varphi X \psi^2$	72	72	144
$\varphi^2 D \psi^2$	51	30	81
$(\bar{L}L)(\bar{L}L)$	171	126	297
$(\bar{R}R)(\bar{R}R)$	255	195	450
$(\bar{L}L)(\bar{R}R)$	360	288	648
$(\bar{L}R)(\bar{R}L)$	81	81	162
$(\bar{L}R)(\bar{L}R)$	324	324	648

- 👉 most parameters from **fermionic** terms
- 👉 **flavor** has dramatic impact on counting

Examples:

$$\begin{array}{ll} B_{\mu\nu}(\bar{q}_i \sigma^{\mu\nu} d_j) \varphi & 9 + 9 \\ (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_i \gamma^\mu u_j) & 6 + 3 \\ (\bar{l}_i \gamma_\mu l_j)(\bar{l}_k \gamma^\mu l_l) & 27 + 18 \\ (\bar{e}_i \gamma_\mu e_j)(\bar{u}_k \gamma^\mu u_l) & 45 + 36 \\ (\bar{l}_i^I e_j)(\bar{d}_k q_l^I) & 81 + 81 \end{array}$$

# Good reasons to have flavor symmetries in SMEFT

1. reduce the SMEFT parameter space

# Good reasons to have flavor symmetries in SMEFT

## 1. reduce the SMEFT parameter space

- not all entries are independent, some contractions forbidden

	no sym.	$U(3)^5$	
$B_{\mu\nu}(\bar{q}_i \sigma^{\mu\nu} q_j) \varphi$	$9 + 9$	0	-
$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_i \gamma^\mu u_j)$	$6 + 3$	1	$\delta_{ij}$
$(\bar{l}_i \gamma_\mu l_j)(\bar{l}_k \gamma^\mu l_l)$	$27 + 18$	2	$\delta_{ij}\delta_{kl}, \delta_{il}\delta_{kj}$
$(\bar{e}_i \gamma_\mu e_j)(\bar{u}_k \gamma^\mu u_l)$	$45 + 36$	1	$\delta_{ij}\delta_{kl}$
$(\bar{l}_i' e_j)(\bar{d}_k q_l')$	$81 + 81$	0	-

# Good reasons to have flavor symmetries in SMEFT

## 1. reduce the SMEFT parameter space

- ▶ not all entries are independent, some contractions forbidden
- ▶ parameters organized according to an additional expansion  
→ **multiple NP scales** ( $\Lambda_{\text{sym}}$ ,  $\Lambda_{\text{sym}}$ )

Example: **MFV** =  $U(3)^5$  broken by SM Yukawas as spurions

[up basis]

$$(\bar{u}_i \gamma^\mu u_j) \quad C_{ij} = C^{(0)} \delta_{ij} + C^{(2)} (Y_u^\dagger Y_u)_{ij} + \dots$$

$$(\bar{d}_i \gamma^\mu d_j) \quad C_{ij} = C^{(0)} \delta_{ij} + C^{(2)} (Y_d^\dagger Y_d)_{ij} + \dots$$

$$(\bar{q}_i \tilde{\varphi} u_j) \quad C_{ij} = C^{(1)} (Y_u)_{ij} + C^{(3)} (Y_u Y_u^\dagger Y_u)_{ij} + \dots$$

$$(\bar{q}_i \varphi d_j) \quad C_{ij} = C^{(1)} (Y_d)_{ij} + C^{(3)} (Y_d Y_d^\dagger Y_d)_{ij} + \dots$$

1     $Y$      $Y^2$      $Y^3$

$$\begin{bmatrix} \text{orange} \\ \text{orange} \\ \text{orange} \end{bmatrix} + \begin{bmatrix} \text{yellow} \\ \text{yellow} \\ \text{yellow} \end{bmatrix} + \dots$$

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$$\begin{bmatrix} \text{cyan} \\ \text{cyan} \\ \text{cyan} \end{bmatrix} + \begin{bmatrix} \text{green} \\ \text{green} \\ \text{green} \end{bmatrix} + \dots$$

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## 3. $\mathcal{L}_{\text{SM}}$ has a peculiar flavor structure, so $\mathcal{L}_{\geq 6}$ is unlikely to be fully anarchical

→ approximate potentially realistic patterns

!! symmetries of SMEFT  $\neq$  symmetries of the UV completion  
can be accidental, reflecting specific UV dynamics

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## 4. can be used to reflect the experimental sensitivity

→ a way to resum/combine contributions undistinguishable in the measurement

# Candidate symmetries for SMEFT at the LHC

IB,(Jiang,Trott) 1709.06492, 2012.11343, Bordone,Catá,Feldmann 1910.02641  
Faroughy et al 2005.05366, Greljo et al 2203.09561  
LPCC note 1802.07237, LHC EFT WG discussions [[link](#)]

## Quark sector

- $\mathbf{U(3)^3 = U(3)_q \times U(3)_u \times U(3)_d}$  (MFV) Chivukula,Georgi 1987, Hall,Randall 1990  
D'Ambrosio et al 0207036

- SMEFT effects do not alter SM flavor pattern. mostly capture “flavor blind” NP
- max suppression of non-SM flavor structure: constraints consistent with **lower  $\Lambda$**

gen.  $\Lambda^2/|C_{uW}^{23}| \gtrsim (2.2 \text{ TeV})^2$  from  $t \rightarrow Zc$  ATLAS-CONF-2021-049

MFV  $\Lambda^2/|C_{uW}| \gtrsim |(Y_u^\dagger)_{23}| \cdot (2.2 \text{ TeV})^2 \simeq (0.4 \text{ TeV})^2$  (down b.)

- **correlates** top with  $u, c$  physics, bottom with  $d, s$ .

currently means:

- $tt\gamma, ttZ, tbW$  non-dipole operators most bounded by EWPO
- constraints on  $hdd, hss$  corrections can be inferred from  $h \rightarrow bb$  Greljo,Marzocca 1704.09015
- tension between  $B$  anomalies and  $pp \rightarrow \mu\mu$  1704.09015

...

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- ▶  $\mathbf{U(2)^3} = U(2)_q \times U(2)_u \times U(2)_d$  Barbieri et al 1105.2296, 1203.4218  
Blankenburg et al 1204.0688

- 3rd gen. left out:  $t, b$  independent of light flavors
- spurions are not fully determined in terms of masses and CKM
- chirality-flip (Yukawas, dipoles)  $t, b$  interactions unsuppressed by spurions

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- ▶  $\mathbf{U(2)^3 \times U(1)_b} = U(2)_q \times U(2)_u \times U(2)_d \times U(1)_b$

$U(1)_b$  restores spurion suppression ( $\sim y_b$ ) in chirality-flip bottom couplings  
→ lowers  $\Lambda$  bound from  $h \rightarrow bb$  constraints  
→ gives a rationale to neglect certain operators, e.g.  $b$ -dipoles  $O_{bB}, O_{bW}, O_{bG}$

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- ▶  $\mathbf{U(2)^3 \times U(1)_b} = U(2)_q \times U(2)_u \times U(2)_d \times U(1)_b$
- ▶  $\mathbf{U(2)^2 \times U(3)} = U(2)_q \times U(2)_u \times U(3)_d$

→ symmetry of  $\mathcal{L}_{SM}$  in 5-flavor scheme ( $m_b = 0$ )

→ more complex spurion structure

→ op. structure: like  $U(2)^3$  for up-quarks, like  $U(3)^3$  for down-quarks

# Candidate symmetries for SMEFT at the LHC

## Lepton sector

- ▶  $\mathbf{U(3)^2 = U(3)_I \times U(3)_e}$  (MFV)
  - ▶  $\mathbf{U(2)^2 = U(2)_I \times U(2)_e}$ 
    - allows LFUV only in  $\tau$  vs  $(e, \mu)$
  - ▶  $\mathbf{U(2)^2 \times U(1) = U(2)_I \times U(2)_e \times U(1)_\tau}$ 
    - reintroduces chirality-flip suppression for  $\tau$  currents
  - ▶  $\mathbf{U(1)^3 = (U(1)_{I+e})^3}$ 
    - allows full LFUV but still forbids FCNC
    - exact. no spurions needed!
    - chirality-flip interactions un-suppressed
- 👉 LHC sensitivity  $\sim U(2)_{q,u,d}^3 \times (U(1)_{I+e})^3$
- 👉 less restrictive options required only to compare to other measurements

# Automation

- ▶ **SMEFTflavor**: construction of full set of invariants in Warsaw basis, imposing arbitrary flavor symmetries with spurions

Greljo,Palavric,Thomsen 2203.09561  
github.com/aethomsen/SMEFTflavor

- ▶ **UFO models** for Monte Carlo simulations already implement:

$$U(3)^5 \quad \text{SMEFTsim U35, MFV}$$

$$U(2)_{q,u,d}^3 \times U(3)_{l,e}^2 \quad \text{SMEFTsim topU31}$$

$$U(2)_{q,u,d}^3 \times U(1)_{l+e}^3 \quad \text{SMEFTsim top, dim6top}$$

$$U(2)_{q,u}^2 \times U(3)_d \times U(1)_{l+e}^3 \quad \text{SMEFT@NLO}$$

SMEFTsim: IB,(Jiang,Trott) 1709.06492, 2012.11343 ⓘ

SMEFT@NLO: Degrande,Durieux,Maltoni,Mimasu,Vryonidou,Zhang 2008.11743 ⓘ

dim6top: Durieux,Zhang 1802.07237 ⓘ

→ allow to simulate directly in terms of parameters in symmetric  $\mathcal{L}_6$

# Number of independent parameters

adapted from Greljo,Palavrić,Thomsen 2203.09561

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector									
		MFV <sub>L</sub>	$U(2)^2 \times U(1)^2$	$U(2)^2$	$U(1)^3$	No symm.					
Quark sector	MFV <sub>Q</sub>	41	6	59	6	62	9	93	18	207	132
	$U(2)^2 \times U(3)_d$	72	10	95	10	100	15	140	28	281	169
	$U(2)^3 \times U(1)_{d_3}$	86	10	111	10	116	12	158	28	305	175
	$U(2)^3$	93	17	118	17	124	23	168	38	321	191
	No symmetry	703	570	756	591	786	621	906	705	1350	1149

👉 not all of them enter observables of interest!

typical counts for current H + EW + top fits: between 25 and 50

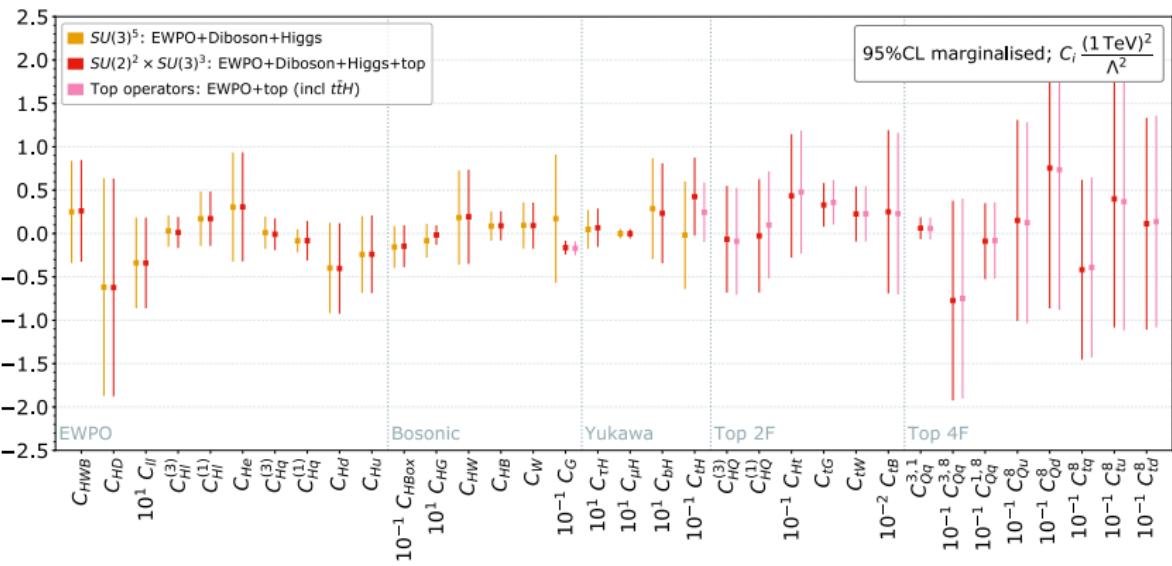
largely depends on:

- processes included
- tree / loop
- linear / quadratic

state-of-the-art fitting tools can handle 30 – 35 simultaneously

# Example global fit results

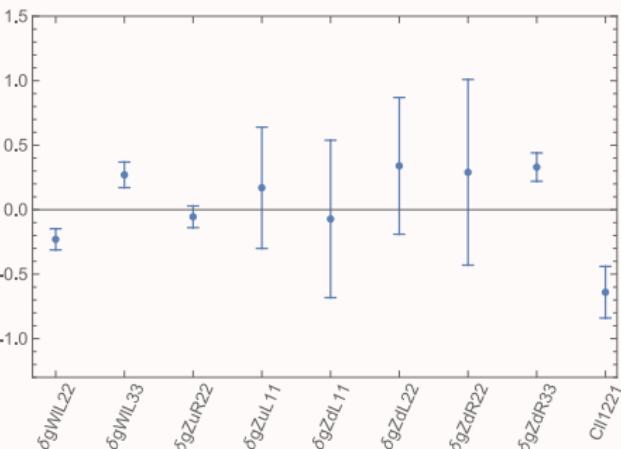
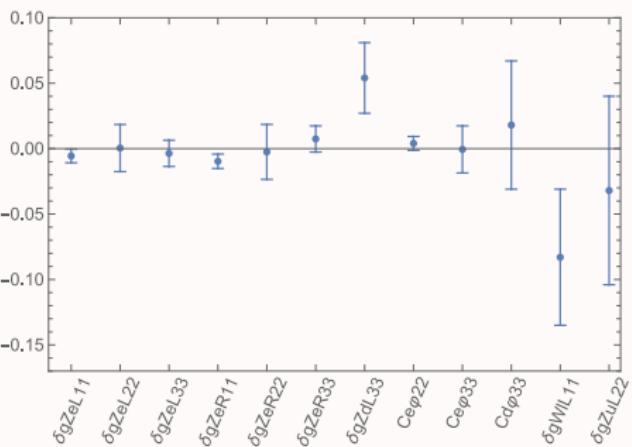
Ellis, Madigan, Mimasu, Sanz, You 2012.02779



# Flavor sensitivity from EWPO

Falkowski,Straub 1911.07866  
also: Efrati,Falkowski,Soreq 1503.07872

- ▶ EWPO + Higgs signal strengths + diboson (no top) → **31** parameters
- ▶ no FCNC, but each flavor treated independently
- ▶ linear parameterization

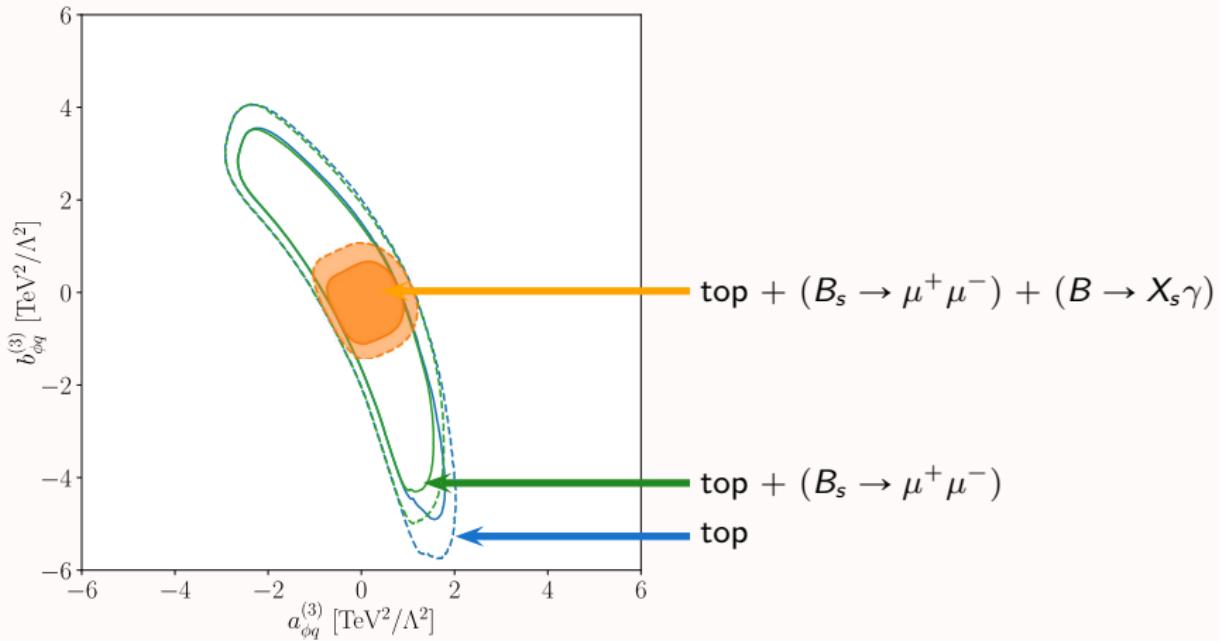


# Combining top constraints with B physics

Bruggisser,Schäfer,vanDyk,Westhoff 2101.07273  
also: Auode,Hurth,Renner,Shepherd 2003.05432  
Bißman,Grunwald,Hiller,Kröninger 2012.10456

$$C_{\phi q}^{(3)} = a_{\phi q}^{(3)} \mathbb{1} + b_{\phi q}^{(3)} (Y_u Y_u^\dagger) \text{ in up basis}$$

$$O_{\phi q}^{(3)} = (\phi^\dagger i \overleftrightarrow{D}_\mu \phi)(\bar{q} \gamma^\mu \tau^I q)$$



# Summary

- ▶ SMEFT allows an ambitious program of “**agnostic**” NP searches
- ▶ Flavor symmetries play a major role in
  - the classification of (ir)relevant SMEFT parameters
  - the interpretation of constraints in terms of NP
- ▶ candidate flavor symmetries for LHC program:  
 $U(2)_{q,u,d}^3 \times (U(1)_{l+e})^3$  and larger  $\leftrightarrow$  exp. sensitivity
- ▶ **EWPO** can already help distinguish flavors in current fits.  
main block: too many parameters
- ▶ Interplay with **B physics** interesting! only a few studies yet
- ▶ Future: incorporating more and more flavor observables  
→ “global SMEFT likelihood”

# **Backup slides**

# $\mathcal{L}_6$ : the Warsaw basis

Grzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\widetilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \widetilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \widetilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

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$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$

$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^\alpha)^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^\alpha)^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

# More symmetry cases

Greljo, Palavric, Thomsen 2203.09561

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>	U(3) <sub>V</sub>	U(2) <sup>2</sup> × U(1) <sup>2</sup>	U(2) <sup>2</sup>	U(2) <sub>V</sub>	U(1) <sup>6</sup>	U(1) <sup>3</sup>	No symm.								
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d<sub>3</sub></sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
	No symmetry	703	570	734	600	756	591	786	621	818	652	813	612	906	705	1350	1149

# Counting with spurions

Faroughy, Isidori, Wilsch, Yamamoto 2005.05366

Class	Operators	No symmetry				$U(3)^5$			
		3 Gen.	1 Gen.	Exact	$\mathcal{O}(Y_{e,d,u}^1)$	$\mathcal{O}(Y_e^1, Y_d^1 Y_u^2)$	9	6	9
1-4	$X^3, H^6, H^4 D^2, X^2 H^2$	9	6	9	6	9	6	9	6
5	$\psi^2 H^3$	27	27	3	3	—	—	3	3
6	$\psi^2 X H$	72	72	8	8	—	—	8	8
7	$\psi^2 H^2 D$	51	30	8	1	7	—	7	—
8	$(\bar{L}L)(\bar{L}L)$	171	126	5	—	8	—	8	—
	$(\bar{R}R)(\bar{R}R)$	255	195	7	—	9	—	9	—
	$(\bar{L}L)(\bar{R}R)$	360	288	8	—	8	—	8	—
	$(\bar{L}R)(\bar{R}L)$	81	81	1	1	—	—	—	—
	$(\bar{L}R)(\bar{L}R)$	324	324	4	4	—	—	—	4
total:		1350	1149	53	23	41	6	52	17
						85	26		

# Counting with spurions

Faroughy, Isidori, Wilsch, Yamamoto 2005.05366

$$Y_e = y_\tau \begin{pmatrix} \Delta_e & x_\tau V_I \\ 0 & 1 \end{pmatrix} \quad Y_u = y_t \begin{pmatrix} \Delta_u & x_t V_q \\ 0 & 1 \end{pmatrix} \quad Y_d = y_b \begin{pmatrix} \Delta_d & x_b V_q \\ 0 & 1 \end{pmatrix}$$

Operators	$U(2)^5$ [terms summed up to different orders]							
	Exact	$\mathcal{O}(V^1)$	$\mathcal{O}(V^2)$	$\mathcal{O}(V^1, \Delta^1)$	$\mathcal{O}(V^2, \Delta^1)$	$\mathcal{O}(V^2, \Delta^1 V^1)$	$\mathcal{O}(V^3, \Delta^1 V^1)$	
Class 1–4	9 6	9 6	9 6	9 6	9 6	9 6	9 6	9 6
$\psi^2 H^3$	3 3	6 6	6 6	9 9	9 9	12 12	12 12	
$\psi^2 XH$	8 8	16 16	16 16	24 24	24 24	32 32	32 32	
$\psi^2 H^2 D$	15 1	19 5	23 5	19 5	23 5	28 10	28 10	
$(\bar{L}L)(\bar{L}L)$	23 –	40 17	67 24	40 17	67 24	67 24	74 31	
$(\bar{R}R)(\bar{R}R)$	29 –	29 –	29 –	29 –	29 –	53 24	53 24	
$(\bar{L}L)(\bar{R}R)$	32 –	48 16	64 16	53 21	69 21	90 42	90 42	
$(\bar{L}R)(\bar{R}L)$	1 1	3 3	4 4	5 5	6 6	10 10	10 10	
$(\bar{L}R)(\bar{L}R)$	4 4	12 12	16 16	24 24	28 28	48 48	48 48	
<b>total:</b>	124 23	182 81	234 93	212 111	264 123	349 208	356 215	

# Counting with spurions

Faroughy, Isidori, Wilsch, Yamamoto 2005.05366

$$Y_e = \begin{pmatrix} \Delta_e & x_\tau V_I \\ 0 & \kappa_\tau X_\tau \end{pmatrix} \quad Y_u = y_t \begin{pmatrix} \Delta_u & x_t V_q \\ 0 & 1 \end{pmatrix} \quad Y_d = \begin{pmatrix} \Delta_d & x_b V_q \\ 0 & \kappa_b X_b \end{pmatrix}$$

Operators	$U(2)^5 \otimes U(1)_b \otimes U(1)_\tau$ [terms summed up to different orders]														
	Exact		$\mathcal{O}(X^2)$		$\mathcal{O}(V^1, X^2)$		$\mathcal{O}(V^2, V^1 X^2)$		$\mathcal{O}(\Delta^1, V^1 X^2)$		$\mathcal{O}(V^2, \Delta^1, V^1 X^2)$		$\mathcal{O}(\Delta^1 V^1, V^2 X^2, \Delta^1 X^1)$		$\mathcal{O}(V^3, \Delta^1 V^1, V^2 X^2, \Delta^1 X^1)$
Class 1-4	9	6	9	6	9	6	9	6	9	6	9	6	9	6	
$\psi^2 H^3$	1	1	3	3	4	4	6	6	9	9	9	9	12	12	
$\psi^2 XH$	3	3	8	8	11	11	16	16	24	24	24	24	32	32	
$\psi^2 H^2 D$	14	-	15	1	19	5	23	5	19	5	23	5	25	7	
$(\bar{L}L)(\bar{L}L)$	23	-	23	-	40	17	67	24	40	17	67	24	67	24	
$(\bar{R}R)(\bar{R}R)$	29	-	29	-	29	-	29	-	29	-	29	-	38	9	
$(\bar{L}L)(\bar{R}R)$	32	-	32	-	48	16	64	16	50	18	66	18	77	29	
$(\bar{L}R)(\bar{R}L)$	-	-	1	1	1	1	3	3	3	3	3	3	6	6	
$(\bar{L}R)(\bar{L}R)$	-	-	4	4	4	4	12	12	18	18	18	18	38	38	
<b>total:</b>	111	10	124	23	165	64	229	88	201	100	248	107	304	163	
													311	170	