

# BES/BST in KKM<sub>Cee</sub>

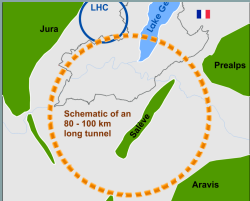


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# Recent developments in KKMCEE



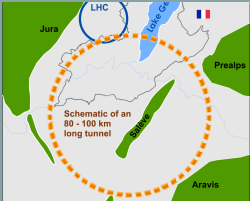
- Upgrade of DIZET electroweak library, hadronic VP routine, more steering parameters for manipulating EW corrections.
- Upgrade of TAUOLA library.
- Output LHE event record.
- Upgraded F77 code including BES and BST is now available on GitHub.
- Complete and well tested version of KKMCEE entirely in C++ (except DIZET and TAUOLA) is there on GitHub but not published yet.

More on GitHub repository:

<https://github.com/KrakovHEPSoft/KKMCEE>

The current version:

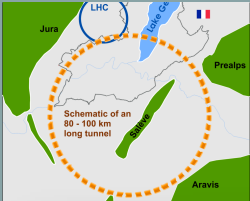
<https://github.com/KrakovHEPSoft/KKMCEE/releases/tag/v4.32.01>



# BES/BST in MC generators



- Generally one may include BES/BST **inside** the MC event generator or **outside**.
- Second method in principle is easy, just generate beam energies  $E_1$  and  $E_2$ , run MC at the reduced CM energy  $s^{1/2} = 2(E_1 E_2)^{1/2}$  and boost events to LAB.
- (Patrick Janot has provided compact algorithm for generating  $E_1$  and  $E_2$  according to correlated double-gaussian distribution of FCCee.)
- In practice it does not work like above, because most of MCs memorise  $s^{1/2}$  and internal variables dependent on  $s^{1/2}$ . Cannot change  $s^{1/2}$  event per event:(
- One may apply workaround proposed by Patrick Janot:  
Using an additional MC create look-up tables of correction due to (small) change of  $s^{1/2}$  for the total cross section and/or for other important observables.  
Next proceed as before, correcting MC events with the weight from tables.
- There will be always some other distributions which will be not corrected:(
- The only perfect solution is **to include** generation of  $E_1$  and  $E_2$  as any other variables in the MC algorithm of the event generator.
- This is presently implemented in KKMCEE.



# BES/BST distribution in KKMCEE



- In KKMCEE there is since long an option of the variable beam energies due to beamstrahlung (BST) distributions of ILC with CIRCE spectra.
- BST distributions reside in the 3-dimensional integrand of **FOAM**, along with the total energy loss due to initial state radiation ISR.
- Recently Gaussian **BES** spectrum from Patrick Janot has been added as another new option in public KKMCEE in the same FOAM integrand.
- Input data activating **BES** `ffbench/Mu/Mu_input_1k_KeFix=4`, looks like:

```

5 BeginX
6 *****
7 *          ACTUAL DATA FOR THIS PARTICULAR RUN
8 *****
9 *indx  data          ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
10 *      Center-of-mass energy [GeV]
11 1      91.0e0        CMSene =xpar( 1) Average Center of mass energy [GeV]
12 25     4            KeyFix=0 normal, =2 beamstrahlung =3,4 for gaussian BES
13 *indx  data          ccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccccc
14 80     0.0e0        ParBES(0) E1=0 will be replaced by CMSene/2
15 81     0.0e0        ParBES(1) E2=0 will be replaced by CMSene/2
16 82     0.132e-2     ParBES(2) sigma1/E1
17 83     0.132e-2     ParBES(3) sigma2/E2
18 84     0.300e0      ParBES(3) rho correlation parameter, dimensionles
19 *****
20 *      Define process
21 413    1            KFFin, muon
22 100    1            store lhe file to (LHE OUT.LHE)
23 ***** one can change the lhe file name between brackets
24 *****
25 EndX

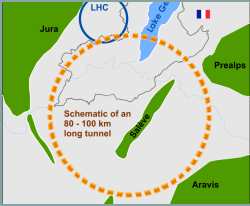
```

```

*****
* Beamstrahlung parameters for Thorsten Ohl's package CIRCE
71      350e0        IRCroots  sqrt(s) [GeV] discrete values 350,500,800GeV
72      3e0          IRCacc
73      5e0          IRCver   version
74      19980505e0   IRCdat   date
75      1e0          IRCxchat printout level
**\\writing vegas grid on the disk, KeyGrid=-1 create and dump, =+1 read\\
76      0e0          KeyGrid=0 create, not read, default\\
*****

```

In the KKMCEE implementation of the CIRCE spectra using FOAM all delta-like components are replaced by the narrow Gaussian distributions!!!



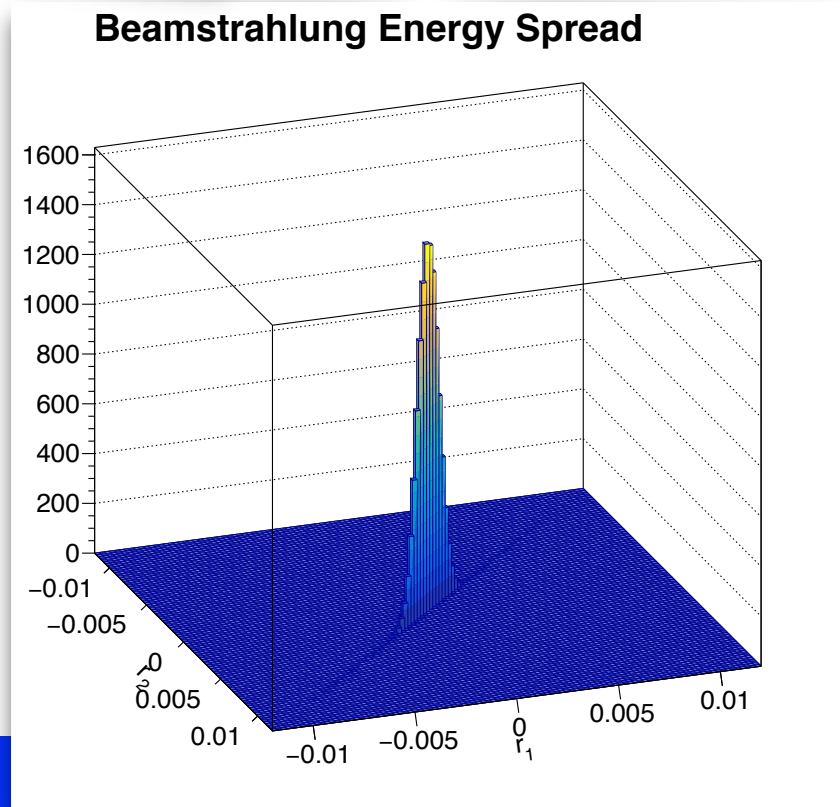
# Gaussian BES in KKMCEE



- Correlated double-Gaussian BES from Patrick Janot implemented in KKMCEE:

$$P(x, y) = \frac{1}{2\pi\sigma_x\sigma_y\sqrt{1-\rho^2}} \exp\left[-\frac{1}{2(1-\rho^2)}\left[\left(\frac{x-x_0}{\sigma_x}\right)^2 + \left(\frac{y-y_0}{\sigma_y}\right)^2 - 2\rho\left(\frac{x-x_0}{\sigma_x}\right)\left(\frac{y-y_0}{\sigma_y}\right)\right]\right]$$

Histogram of two beam energies (relative deviations from central values) from KKMCEE, 1M events.



# BES: technical point

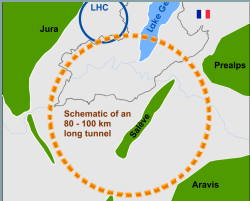
- Correlated double-Gaussian BES from Patrick Janot is implemented twice in KKMCEE, using two different methods — once using mapping invented by Patrick (KeyFix=3):

```
429 C mapping of Patrick Janot for 2-dim Gaussian BES with optional correlation
430 C in this case Jacobian*distribution=1 is omitted.
431 E1 = m_BES_ene1
432 E2 = m_BES_ene2
433 corho = m_BES_rho
434 x1 = sqrt(-2.*log(r1)) * cos(2.*m_PI*r2)
435 x2 = sqrt(-2.*log(r1)) * sin(2.*m_PI*r2)
436 y1 = x1
437 y2 = corho * x1 + sqrt(1.-corho*corho) * x2
438 rr1= y1 * m_BES_sig1
439 rr2= y2 * m_BES_sig2
440 Ebeam1 = E1 * (1.0 + y1 * rr1)
441 Ebeam2 = E2 * (1.0 + y2 * rr2)
```

- and alternatively by providing FOAM with the distribution — mapping is done by FOAM (KeyFix=4).

```
449 ! the same BES distribution from Patrick Janot
450 E1 = m_BES_ene1
451 E2 = m_BES_ene2
452 sigma1= m_BES_sig1*E1
453 sigma2= m_BES_sig2*E2
454 corho = m_BES_rho
455 ! standard distribution for FOAM
456 sigma = SQRT(sigma1*sigma2)
457 delE1 = 10*sigma*(2*r1-1.0) ! range is +-10sigma
458 delE2 = 10*sigma*(2*r2-1.0) ! range is +-10sigma
459 Rho = Rho * (20*sigma)**2 ! Jacobian
460 m_x1 = delE1/E1 ! can be negative
461 m_x2 = delE2/E2 ! can be negative
462 dGauss = (delE1/sigma1)**2 + (delE2/sigma2)**2 - 2*corho*(delE1/sigma1)*(delE2/sigma2)
463 dGauss = EXP(-0.5/(1-corho**2)*dGauss)
464 dGauss = dGauss * 1/(2.0*m_PI)/(sigma1*sigma2)/SQRT(1-(corho)**2) ! Normalization factor
465 Rho = Rho * dGauss;
```

- The resulting generated distribution is the same (providing proof/cross-check of the Patrick's mapping :).



# C++ version of KKM<sub>Cee</sub>



- Complete code in C++ of KKM<sub>Cee</sub> is already there in the non-public repository on GitHub since a few months, waiting for publication...
- It is interfaced with electroweak library DIZET 6.24 and TAUOLA, both in F77.
- It reproduces exactly all classic benchmarks of KKMC from the 1999 LEP workshop and from PRD63 (2000) article.
- From the physics point of view it is identical with F77 version, but is planned as a starting point for the future development.
- It is armed with LHE interface and includes BES of FCC<sub>ee</sub>.
- Complete documentation (CPC article) is urgently needed.
- Repository to be cleaned up of unused F77 source code.

# Summary

- KKMC legacy code written F77 is alive and is available for FCCee/ILC related studies since long.
- KKMCee in C++ is already there, to be published soon.
- Two web pages and public GitHub repository with the F77 source codes and extensive documentation are available.
- Both CIRCE BST and Gaussian BES are in public F77 KKMCee
- BES is presently in the C++ version.