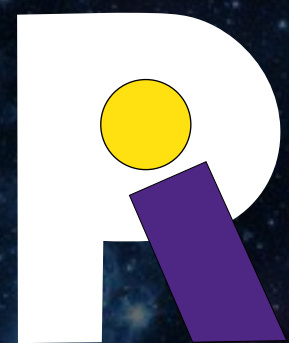


COMPUTING COSMOLOGICAL PRIMORDIAL FLUCTUATIONS

from the full covariant quantum theory

Francesca Vidotto



Rotman Institute
of Philosophy

ENGAGING SCIENCE.



Canada Research Chairs

Western
UNIVERSITY · CANADA



FROM SPINFOAMS TO COSMOLOGY

Primordial fluctuations from quantum gravity, with F. Gozzini

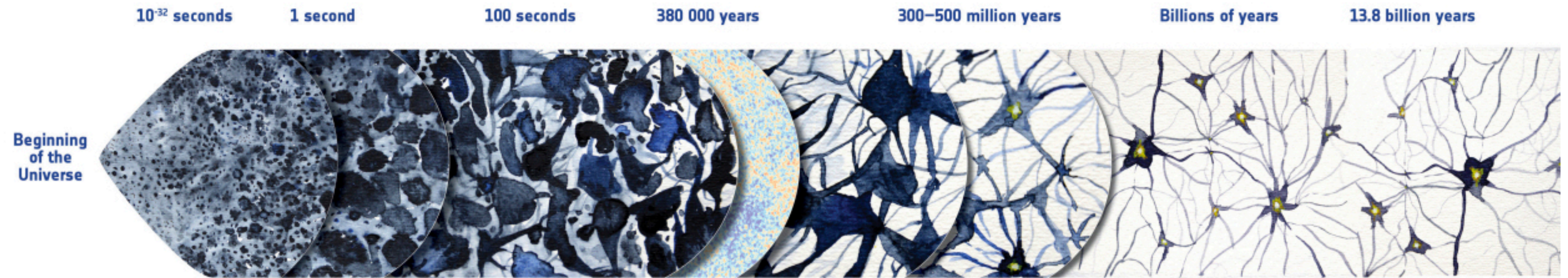


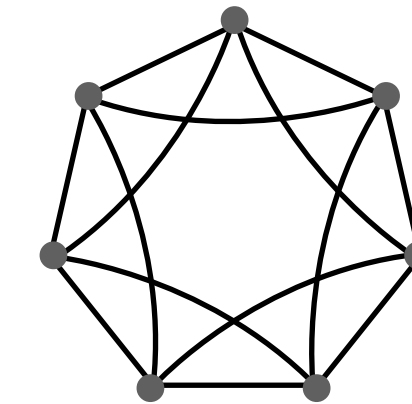
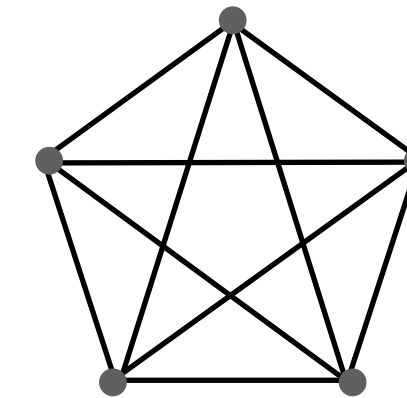
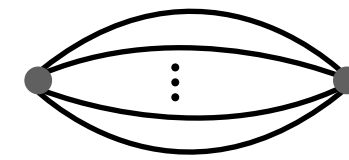
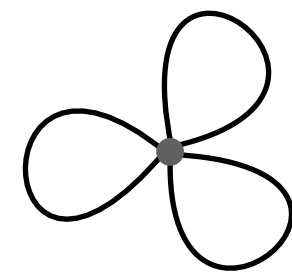
Image credit: ESA

- Quantum Regime
- Graph Approximation
- Hartle-Hawking State
- Transition Amplitude
- Computational Method

FROM SPINFOAMS TO COSMOLOGY

■ Quantum Regime

■ **Graph Approximation**



■ Hartle-Hawking State

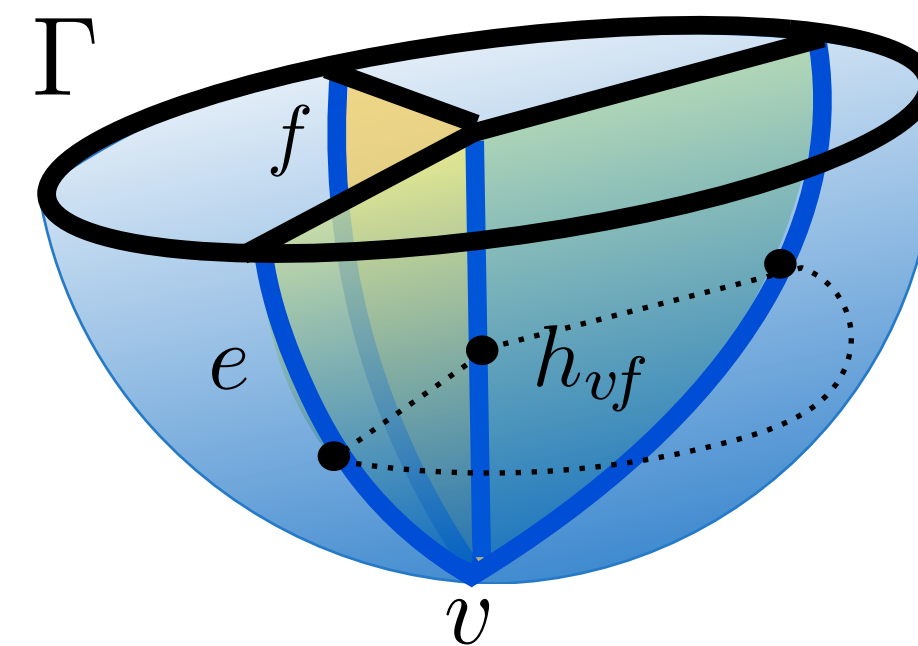
■ Transition Amplitude

■ Computational Method

FROM SPINFOAMS TO COSMOLOGY

Toward Spinfoam Cosmology, with E. Bianchi and C. Rovelli

- Quantum Regime
- Graph Approximation
- **Hartle-Hawking State**
- Transition Amplitude
- Computational Method



APPLYING SPINFOAMS TO COSMOLOGY

Toward Spinfoam Cosmology, with E. Bianchi and C. Rovelli

■ Quantum Regime

■ Graph Approximation

■ Hartle-Hawking State

■ **Transition Amplitude**

$$W_C(h_l) = \int_{SU(2)} dh_{vf} \prod_f \delta(h_f) \prod_v A(h_{vf})$$

■ Computational Method

APPLICATION TO COSMOLOGY

Speziale'17, Boosting Wigner's nj-symbols

- Quantum Regime
- Graph Approximation
- Hartle-Hawking State
- Transition Amplitude
- **Computational Method**

$$W(j_l, i_n) = \sum_{l_f, k_e} \left(\prod_e (2k_e + 1) B(j_l, l_f; i_n, k_e) \right) \{15j\}(l_f, k_e)$$

OBSERVABLES

Primordial fluctuations from quantum gravity, with F. Gozzini

■ Area

■ Volume

$$\langle \mathcal{O} \rangle = \langle \psi_o | \mathcal{O} | \psi_o \rangle$$

■ Dihedral Angles \Rightarrow Curvature

spread

■ Correlations

$$C(\mathcal{O}_1, \mathcal{O}_2) = \frac{\langle \psi_o | \mathcal{O}_1 \mathcal{O}_2 | \psi_o \rangle - \langle \mathcal{O}_1 \rangle \langle \mathcal{O}_2 \rangle}{(\Delta \mathcal{O}_1) (\Delta \mathcal{O}_2)}$$

$$\Delta \mathcal{O} = \sqrt{\langle \psi_o | \mathcal{O}^2 | \psi_o \rangle - \langle \mathcal{O} \rangle^2}$$

■ Entanglement Entropy

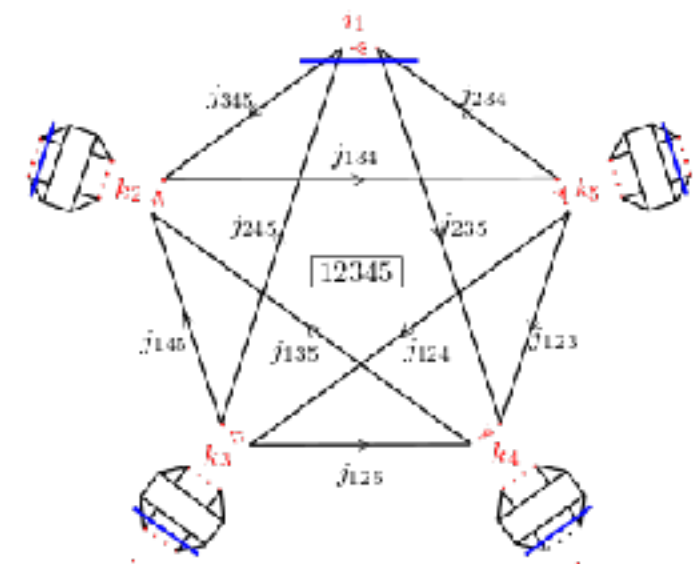
$$S_A = - \text{Tr} (\rho_A \log \rho_A)$$

5-CELL MODEL

Primordial fluctuations from quantum gravity, with F. Gozzini

- Simplest regular 4-polytope

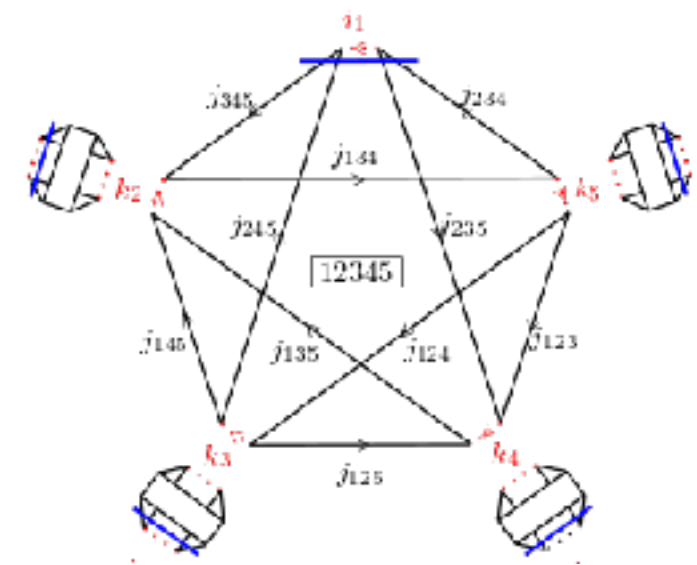
- Regular triangulation of S_3



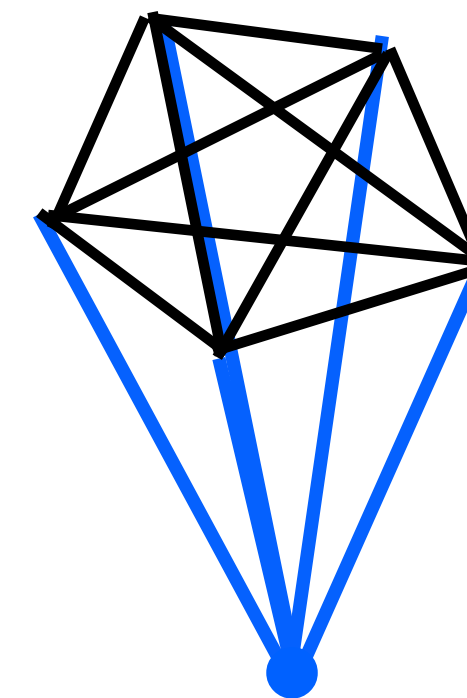
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Primordial fluctuations from quantum gravity, with F. Gozzini

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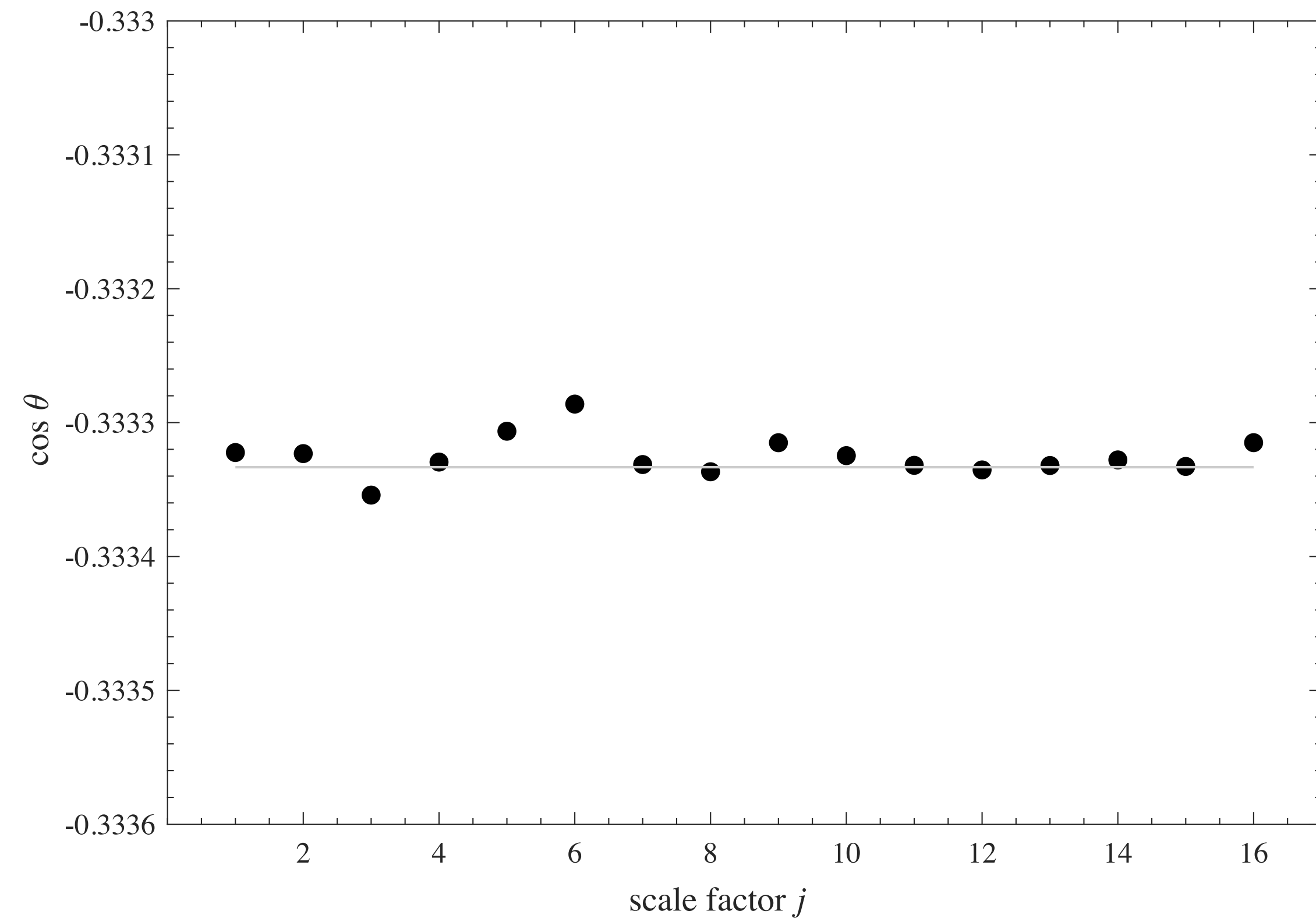
- Regular triangulation of S_3



RESULTS FOR THE 5-CELL MODEL

Primordial fluctuations from quantum gravity, with F. Gozzini

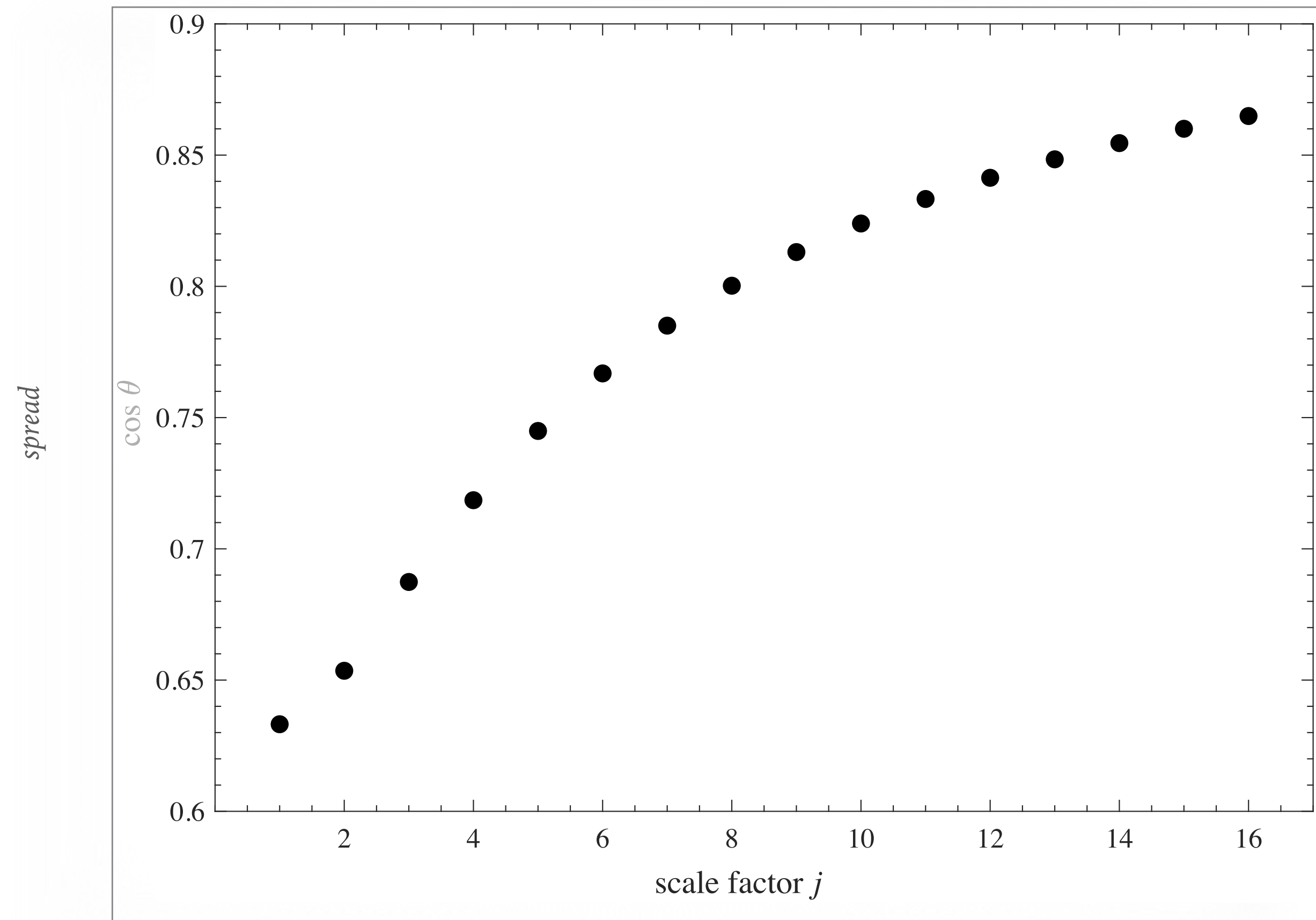
1. 3-sphere as emerging geometry
2. large fluctuations
3. large correlations



RESULTS FOR THE 5-CELL MODEL

Primordial fluctuations from quantum gravity, with F. Gozzini

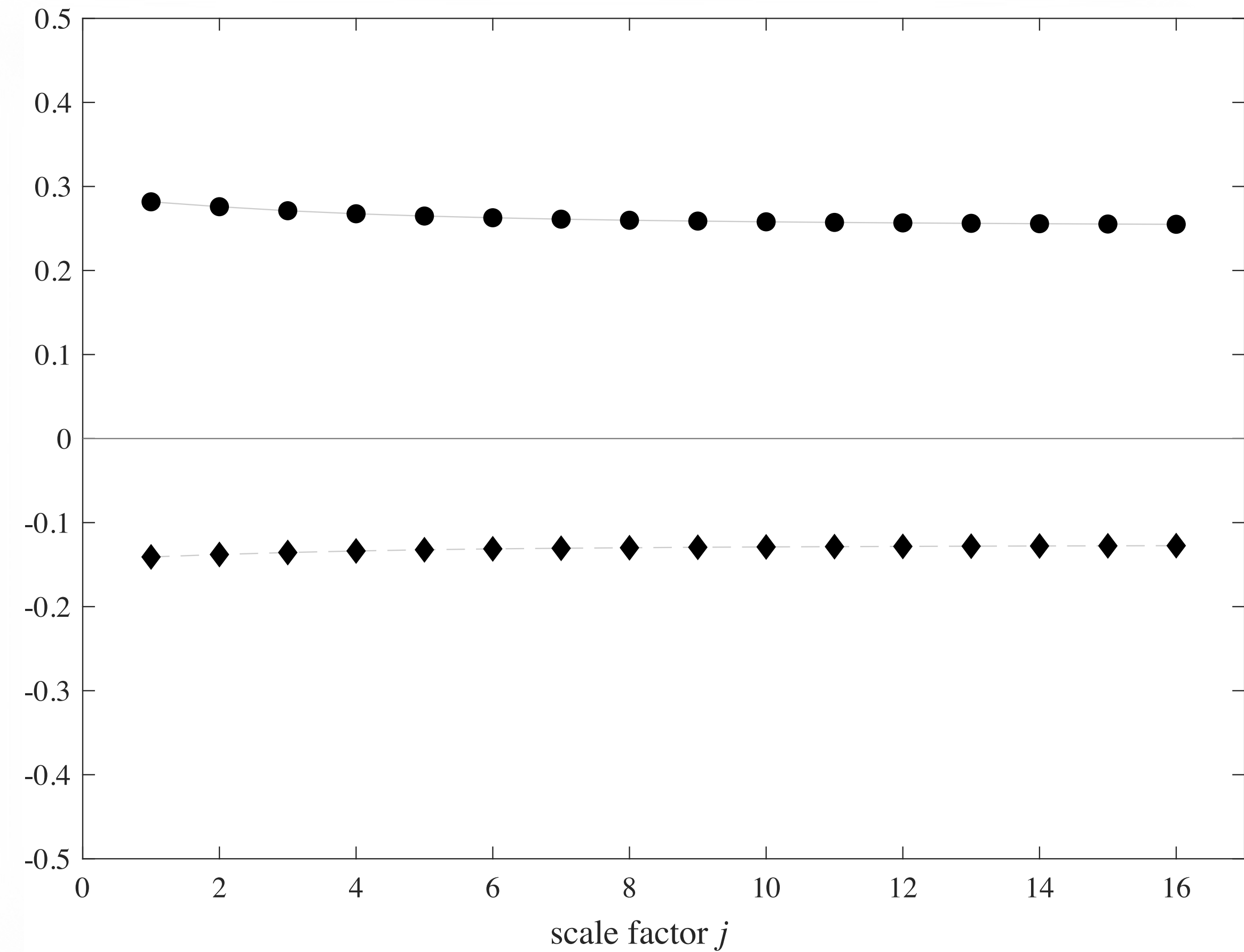
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RESULTS FOR THE 5-CELL MODEL

Primordial fluctuations from quantum gravity, with F. Gozzini

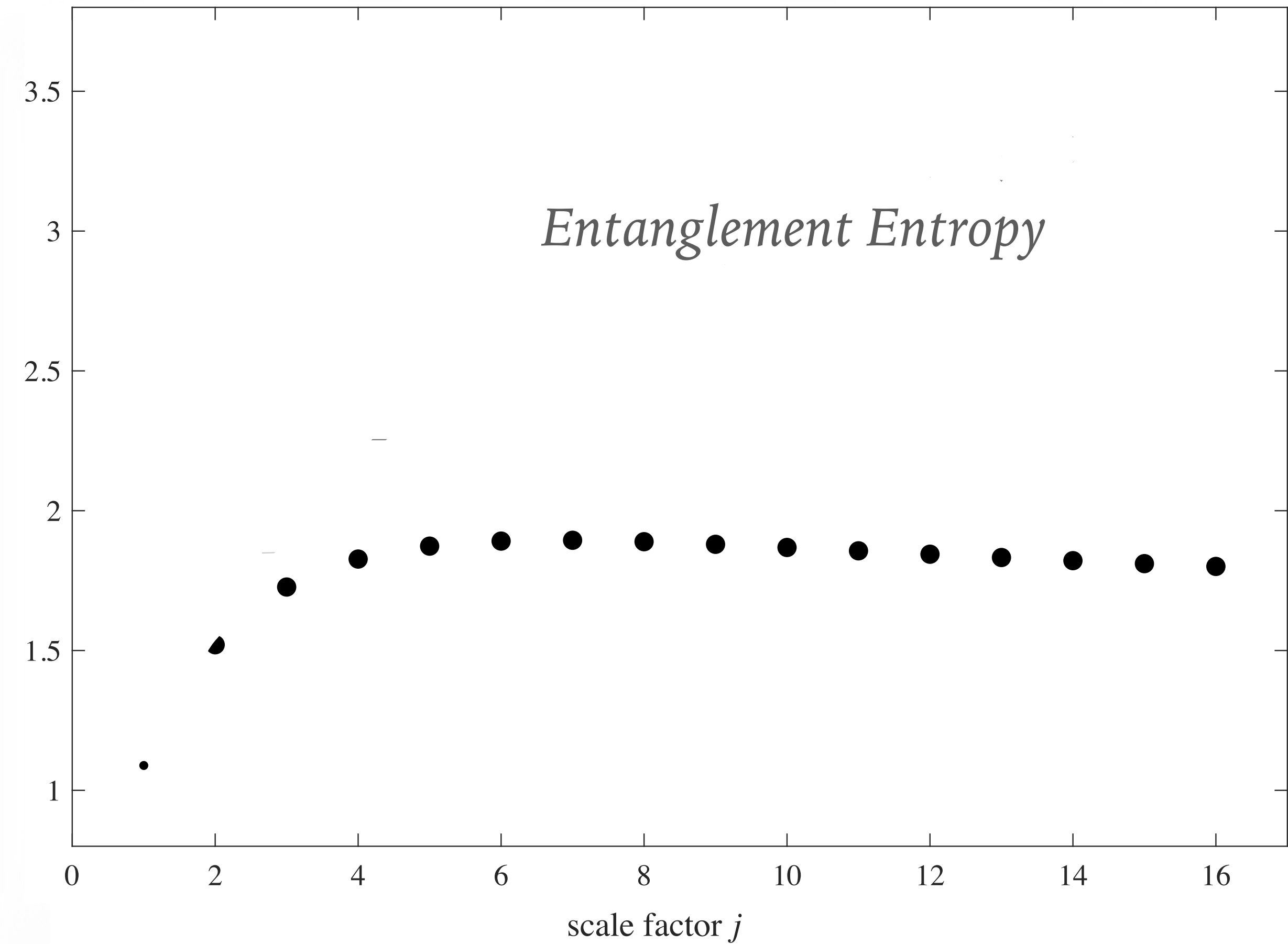
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RESULTS FOR THE 5-CELL MODEL

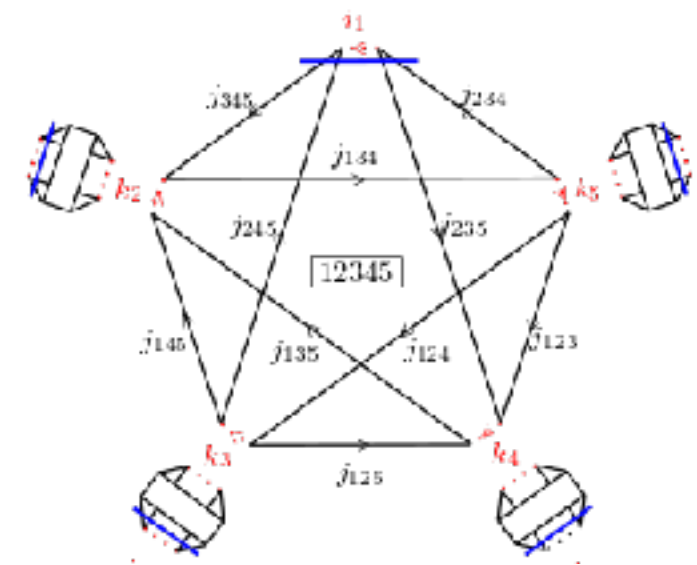
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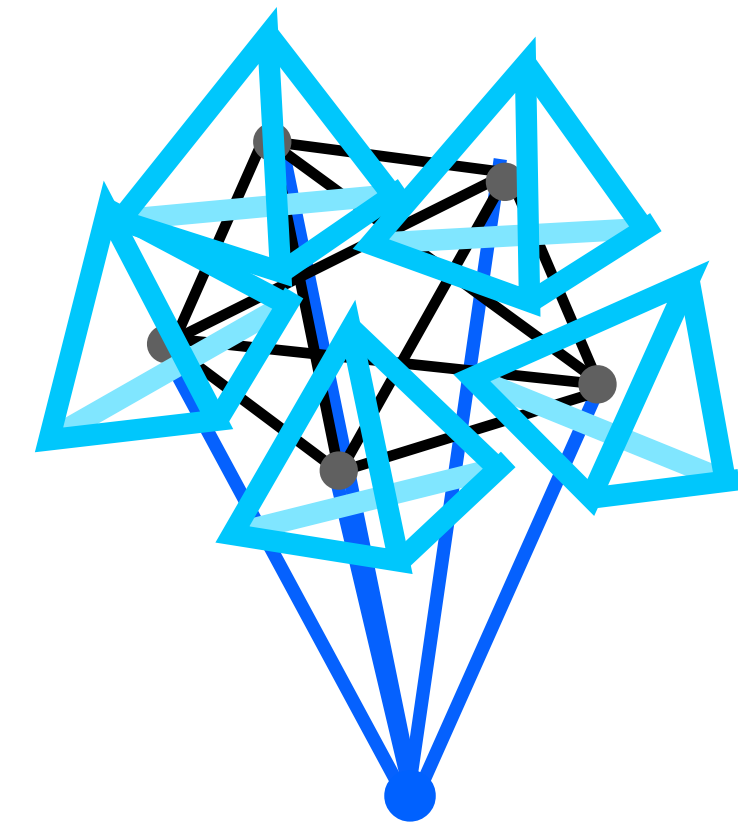
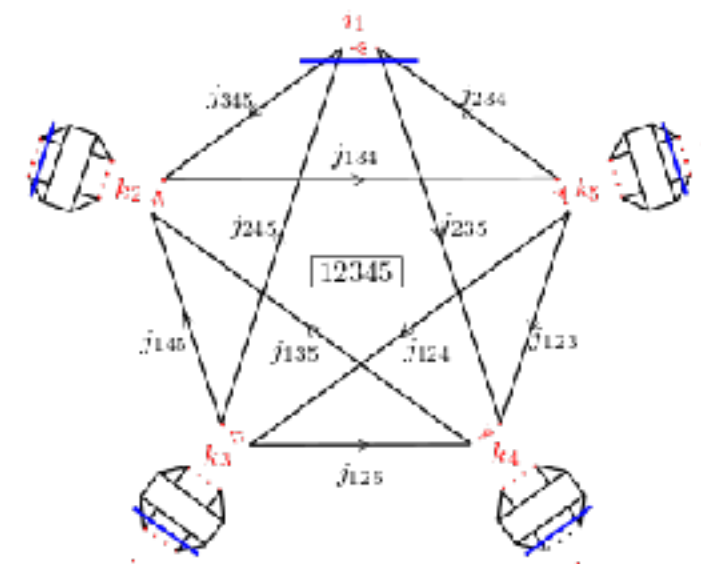
20-CELL MODEL VIA REFINEMENT

MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



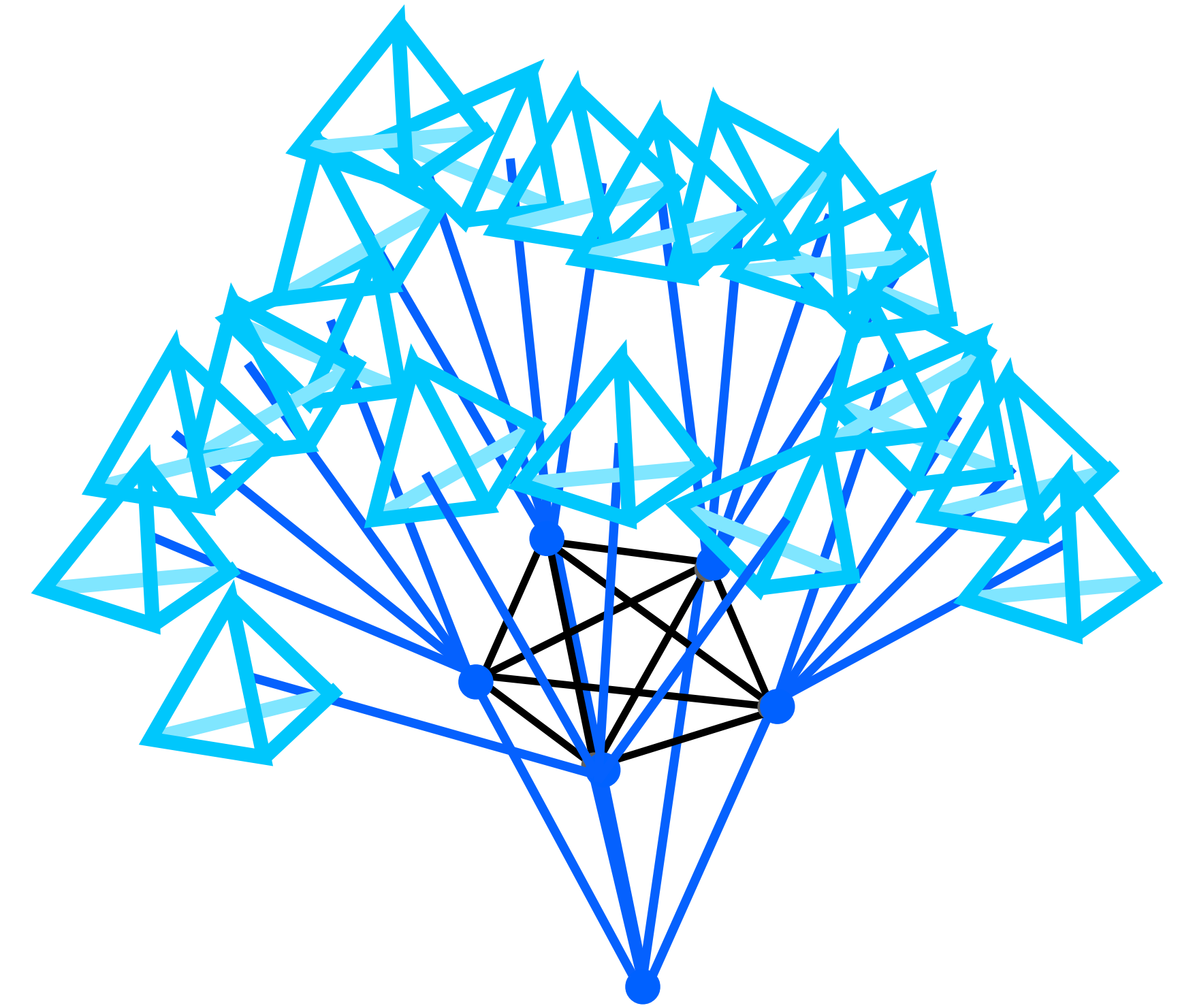
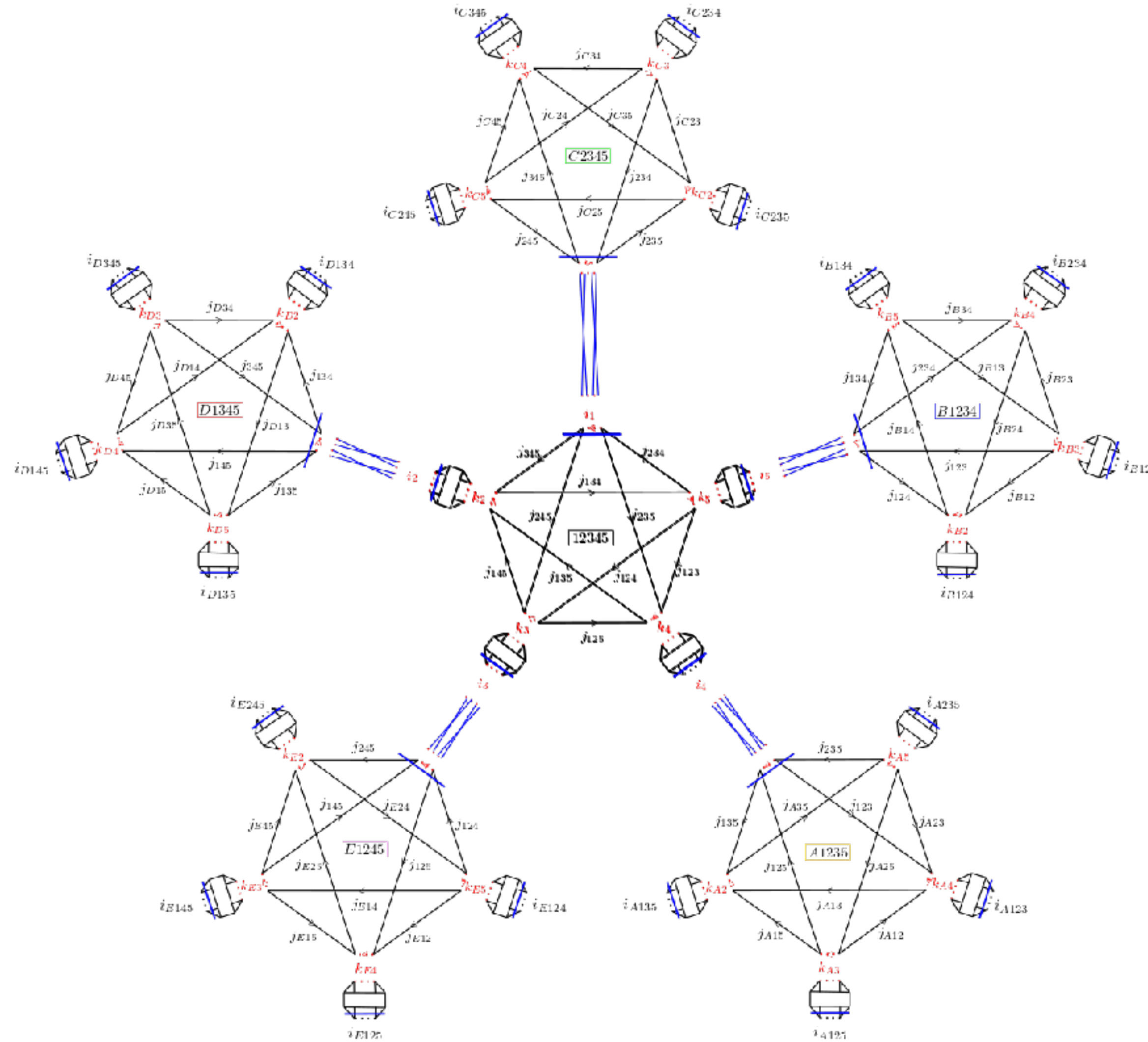
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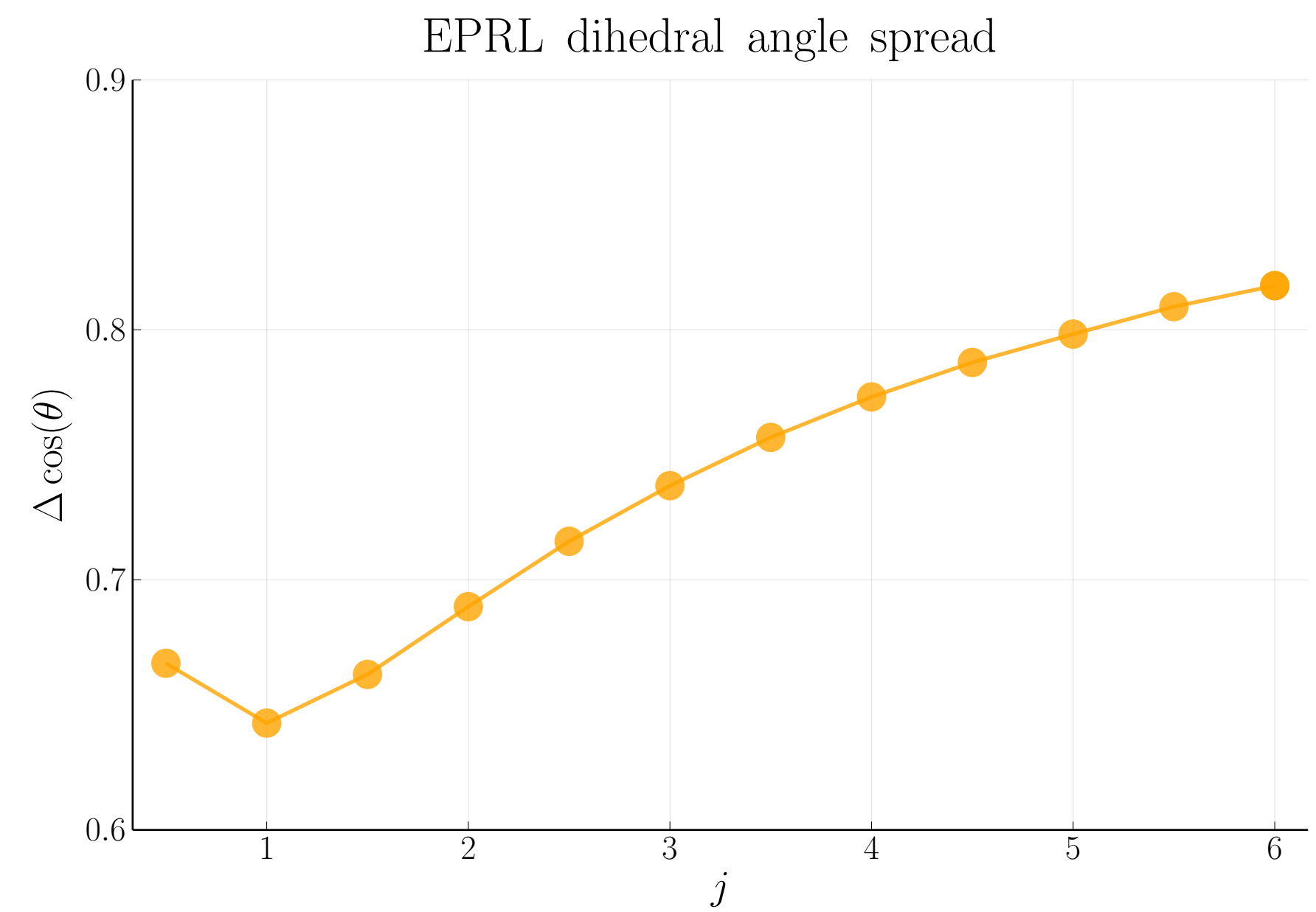
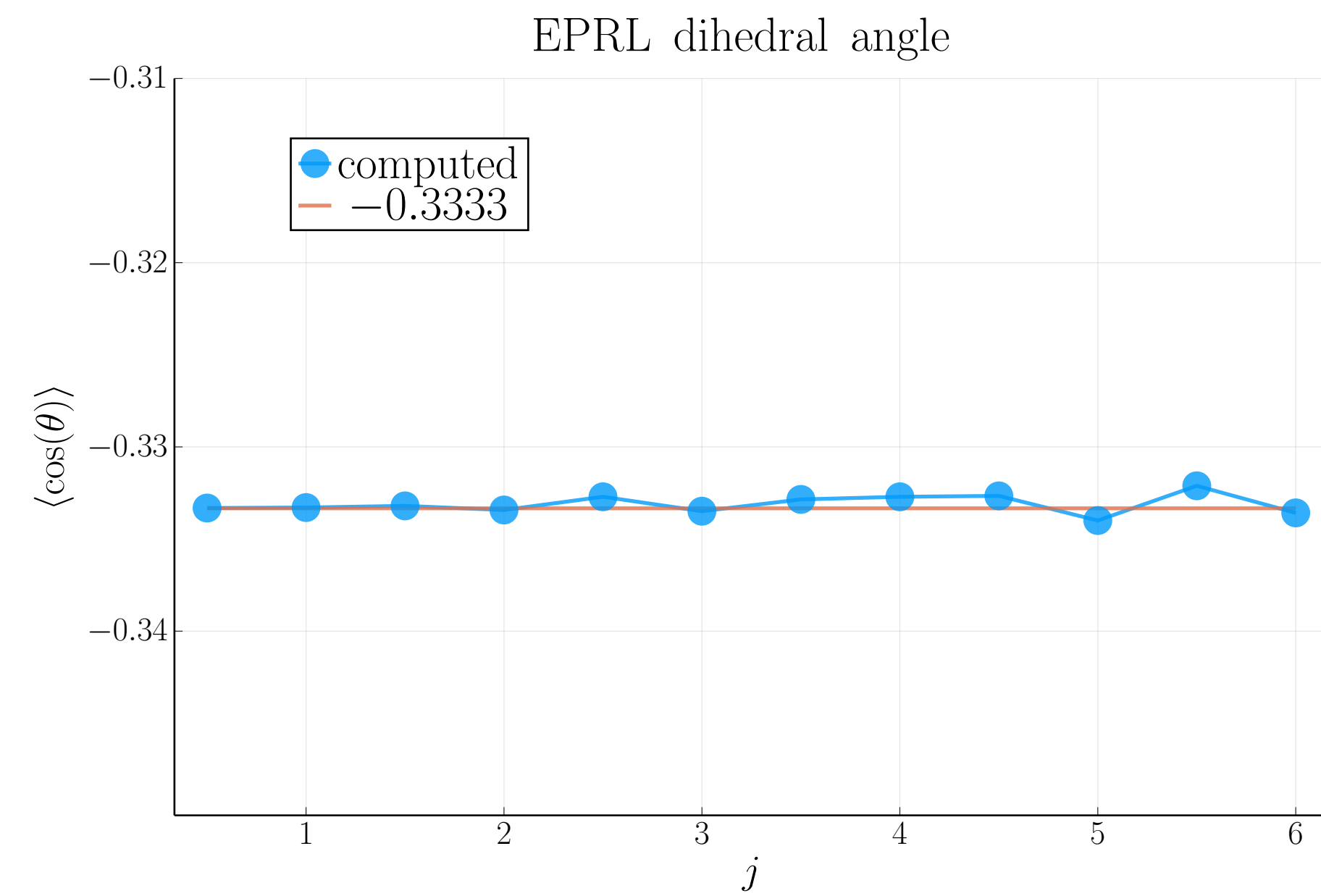
MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



Gozzini'21, A high-performance code for EPRL spin foam amplitudes

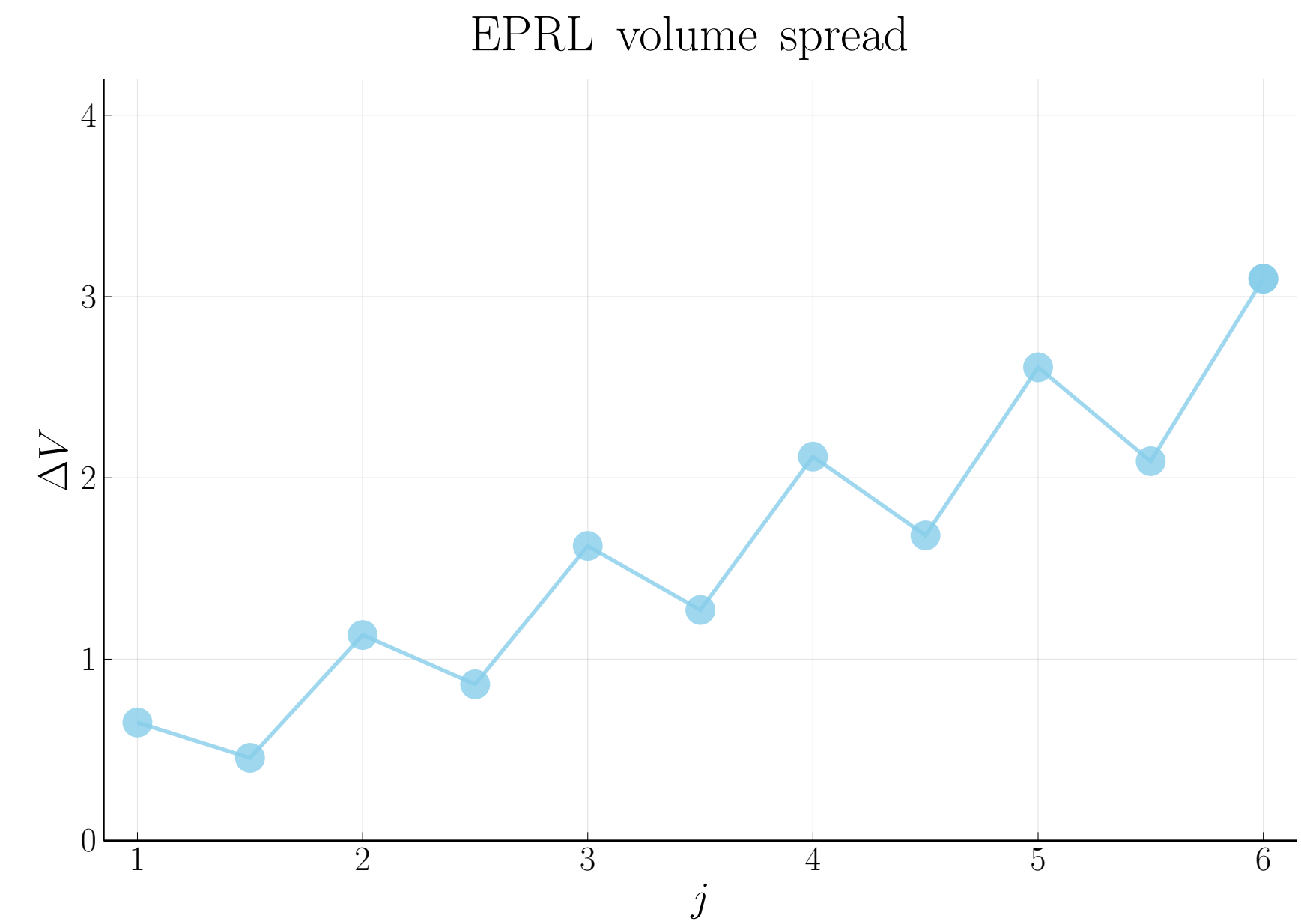
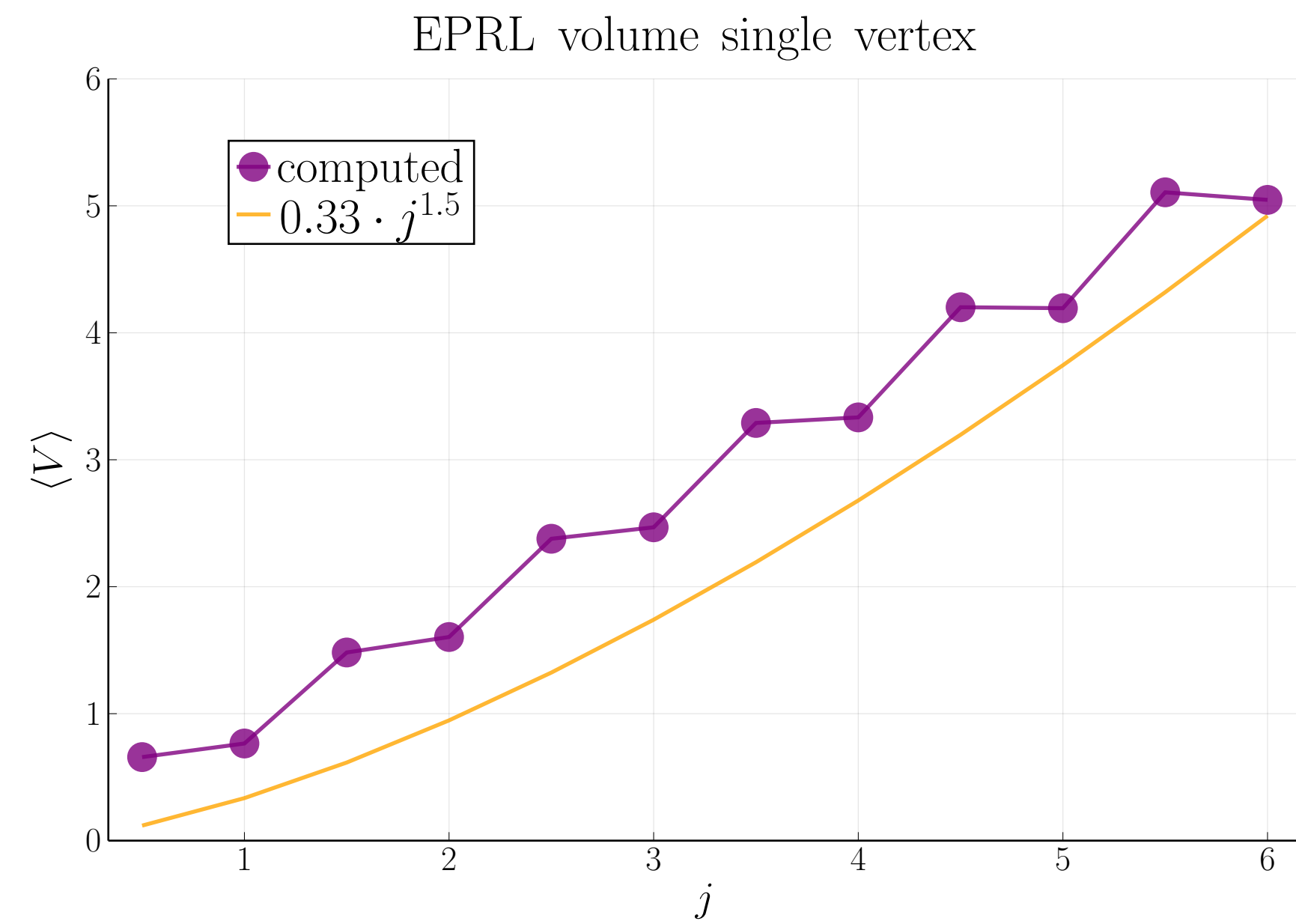
DIHEDRAL ANGLE

MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



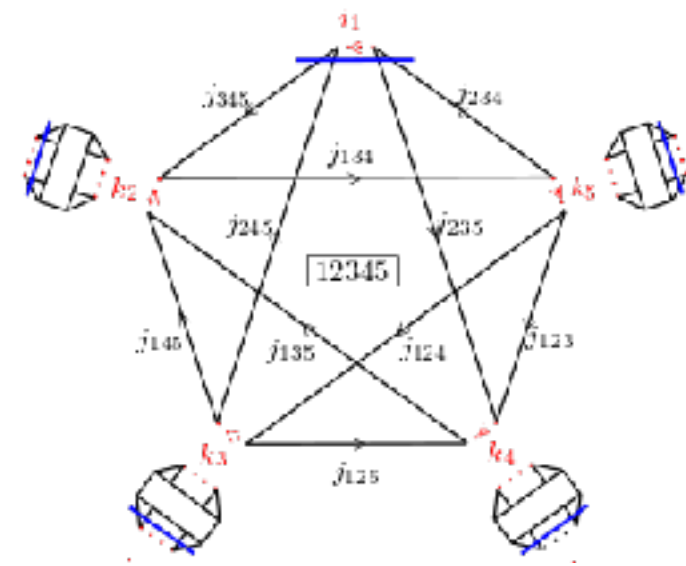
VOLUME

MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



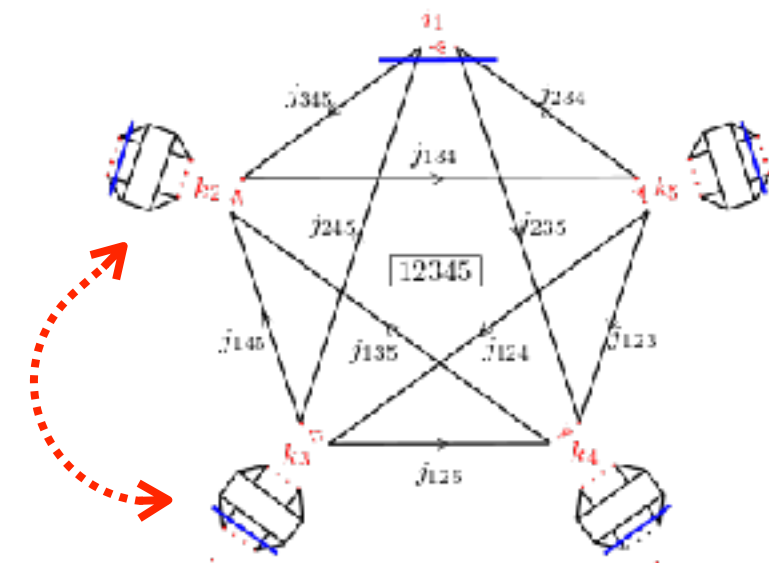
CORRELATION

MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



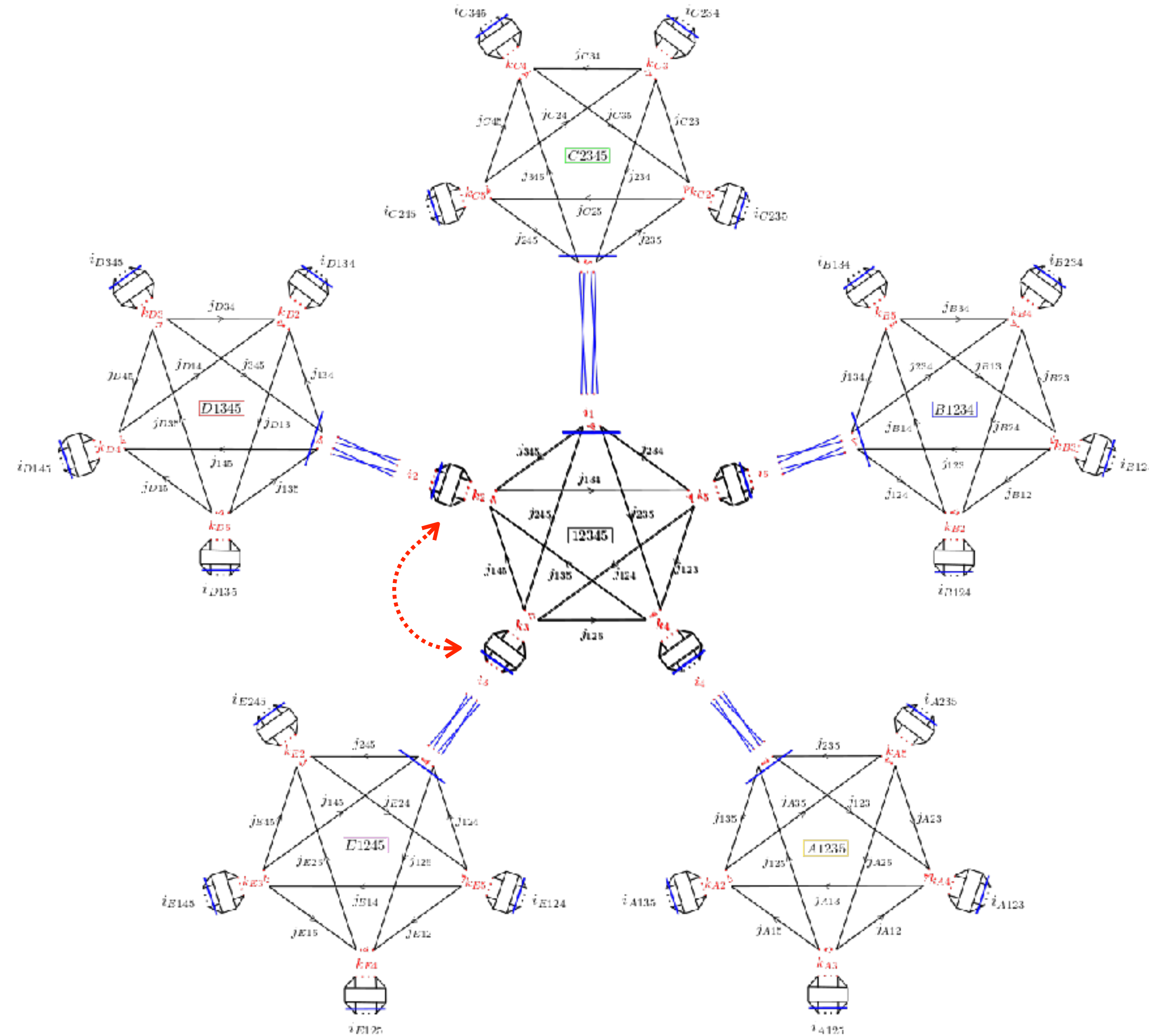
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MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



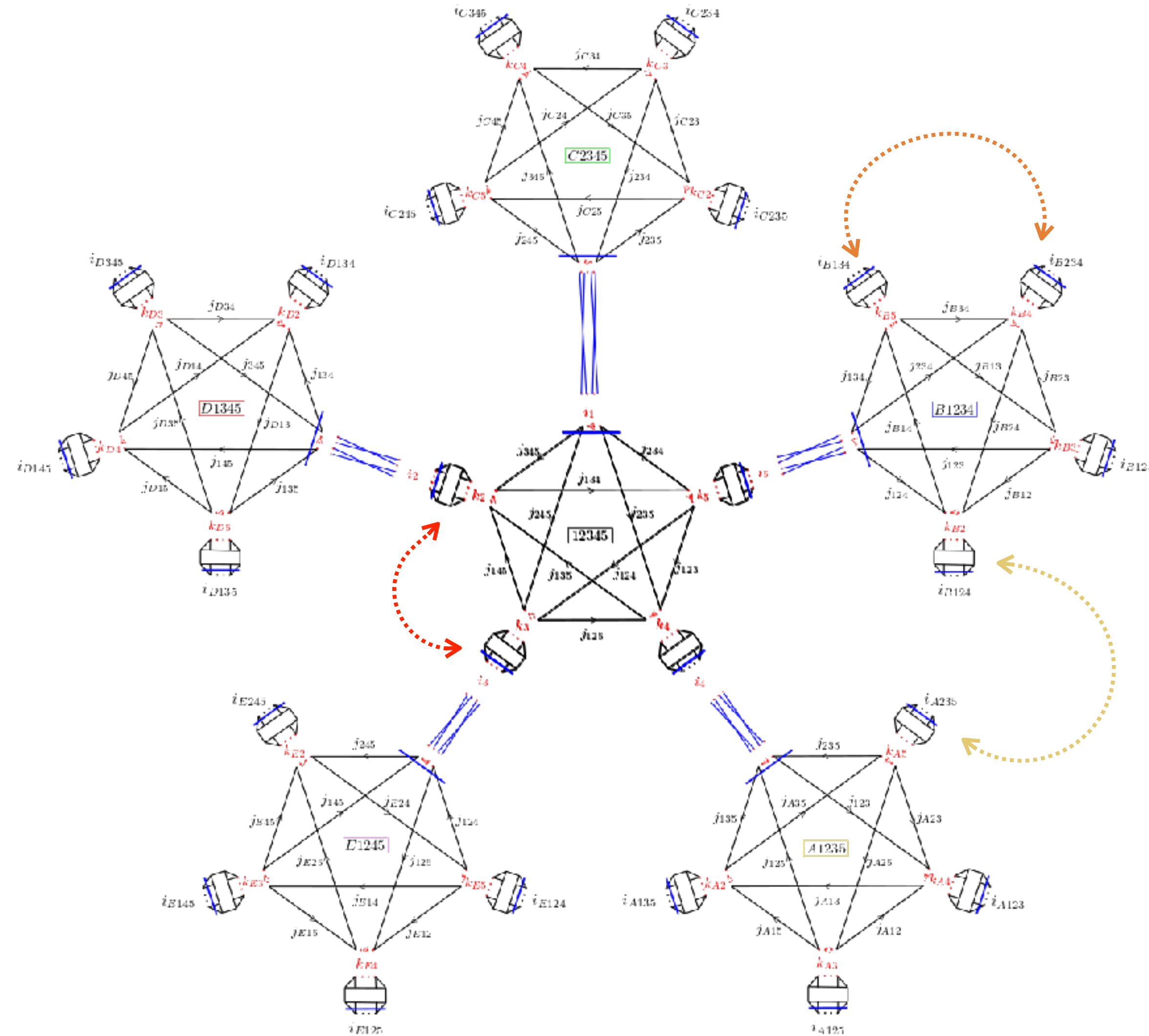
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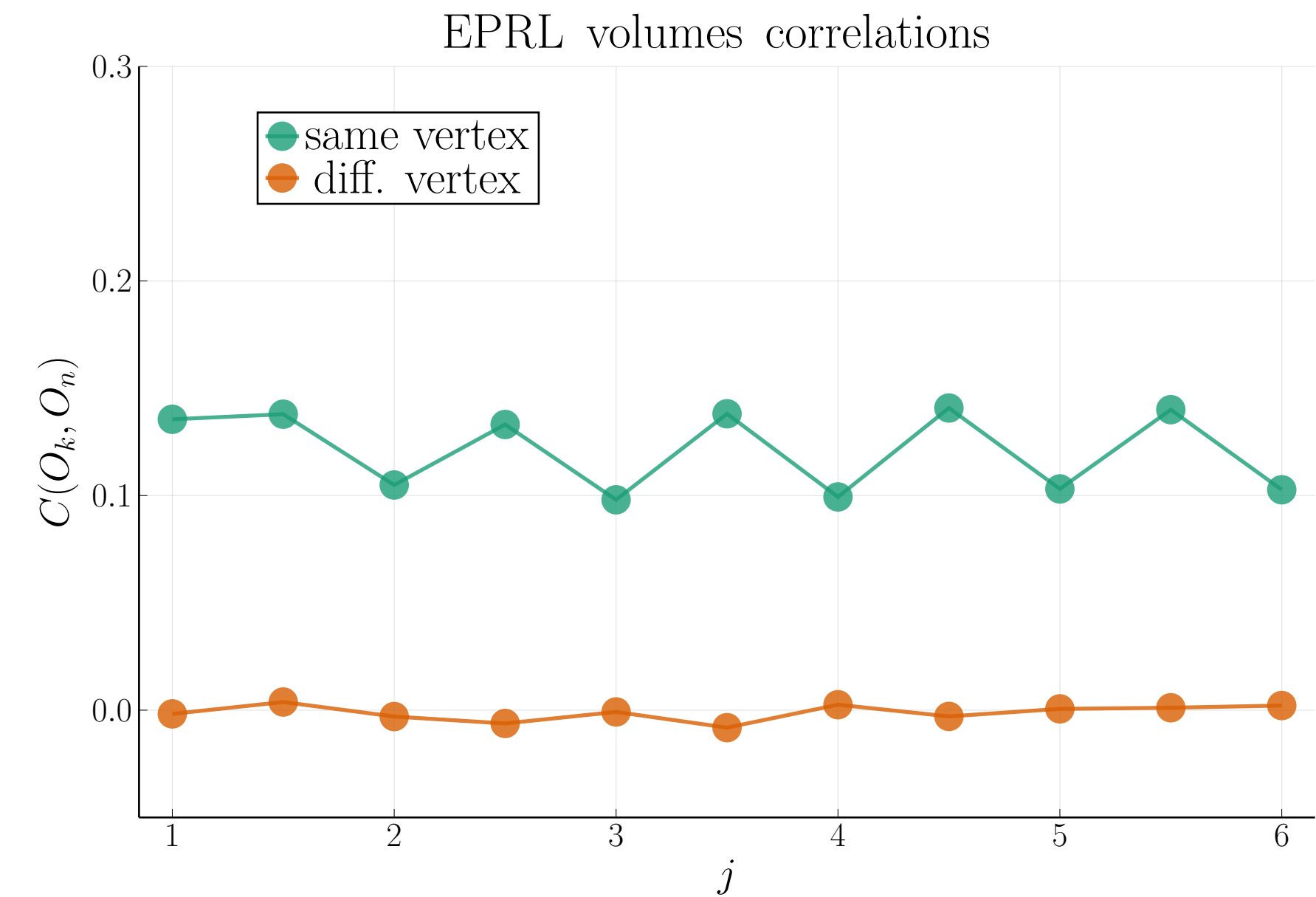
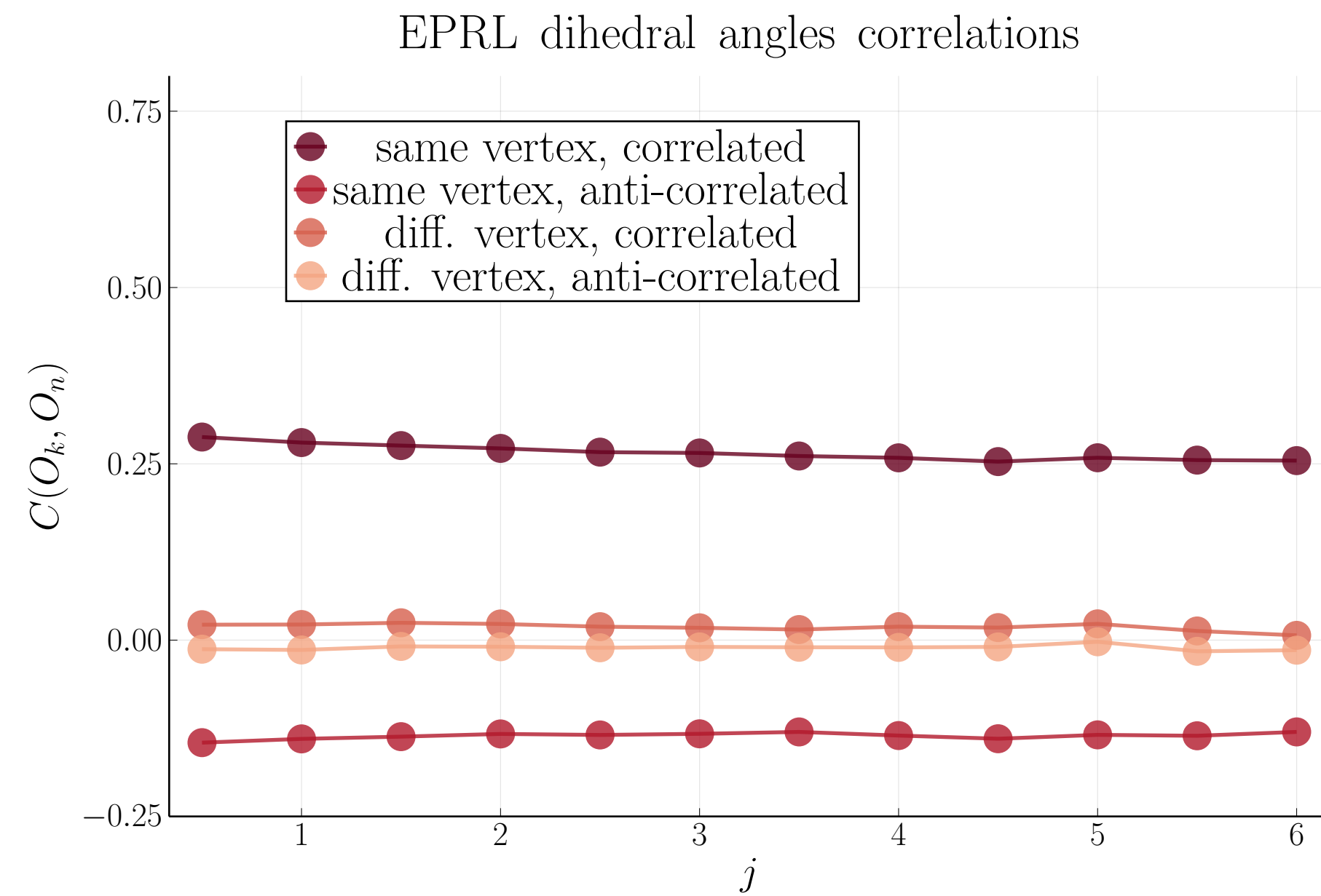
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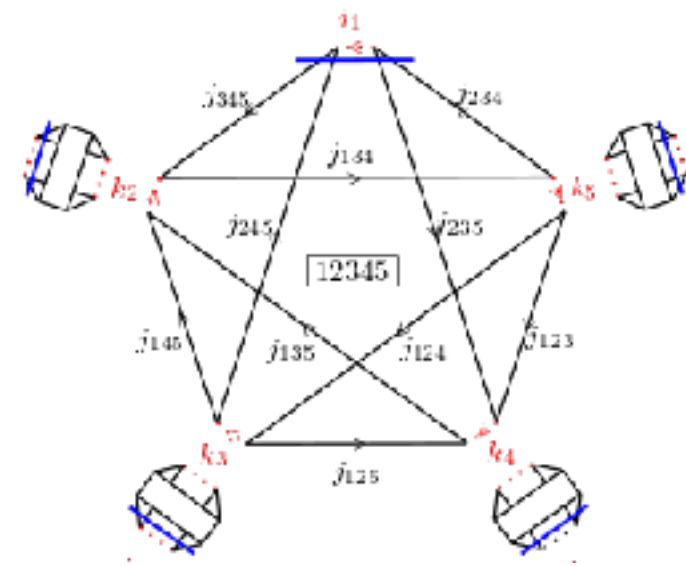
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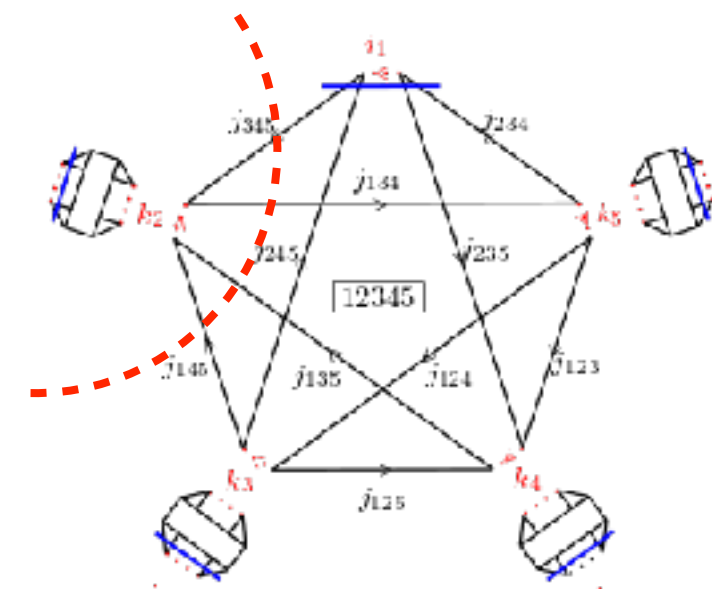
PARTITIONS

MCMC methods for graph refinement in covariant LQG, with P. Frisoni & F. Gozzini



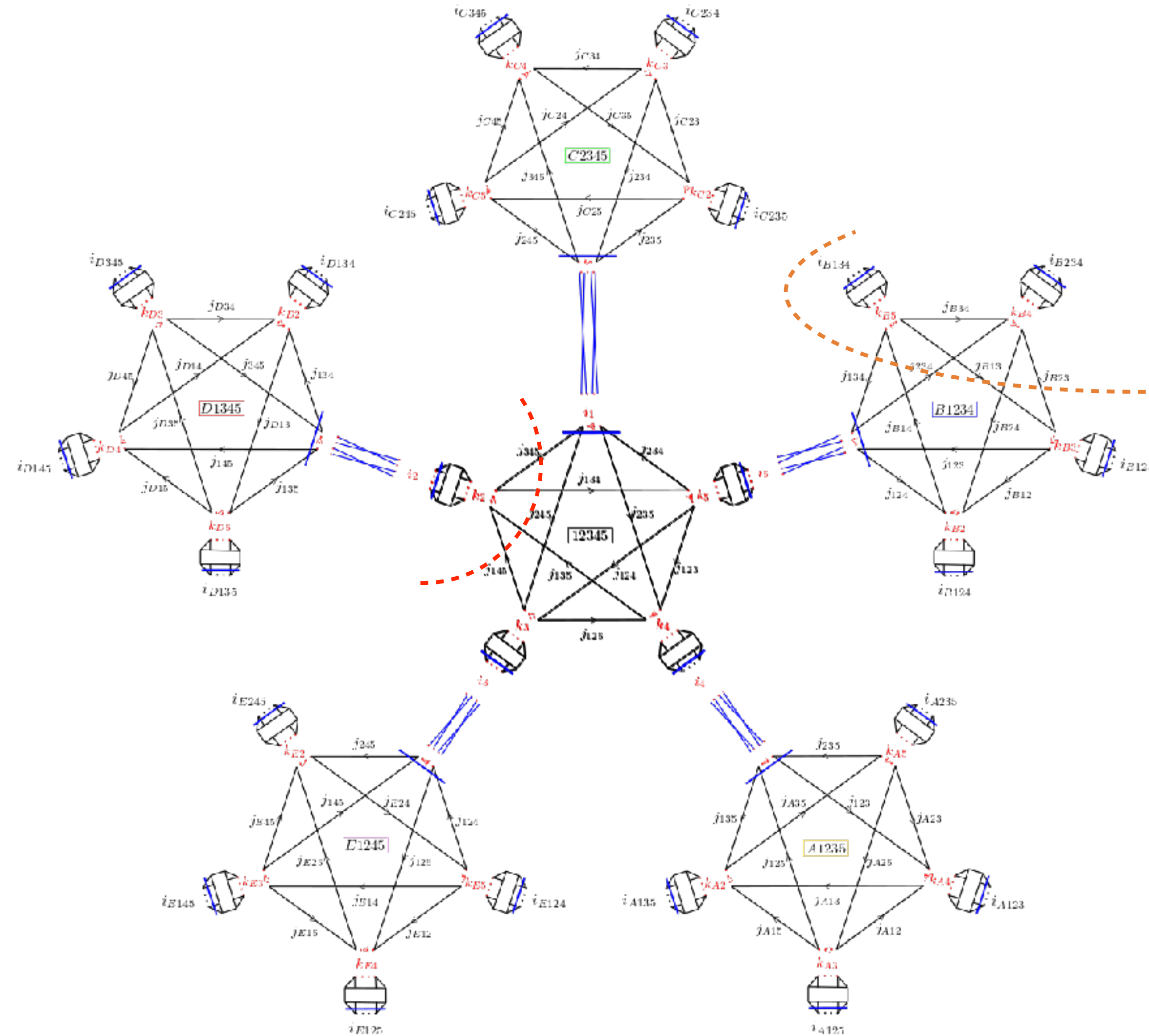
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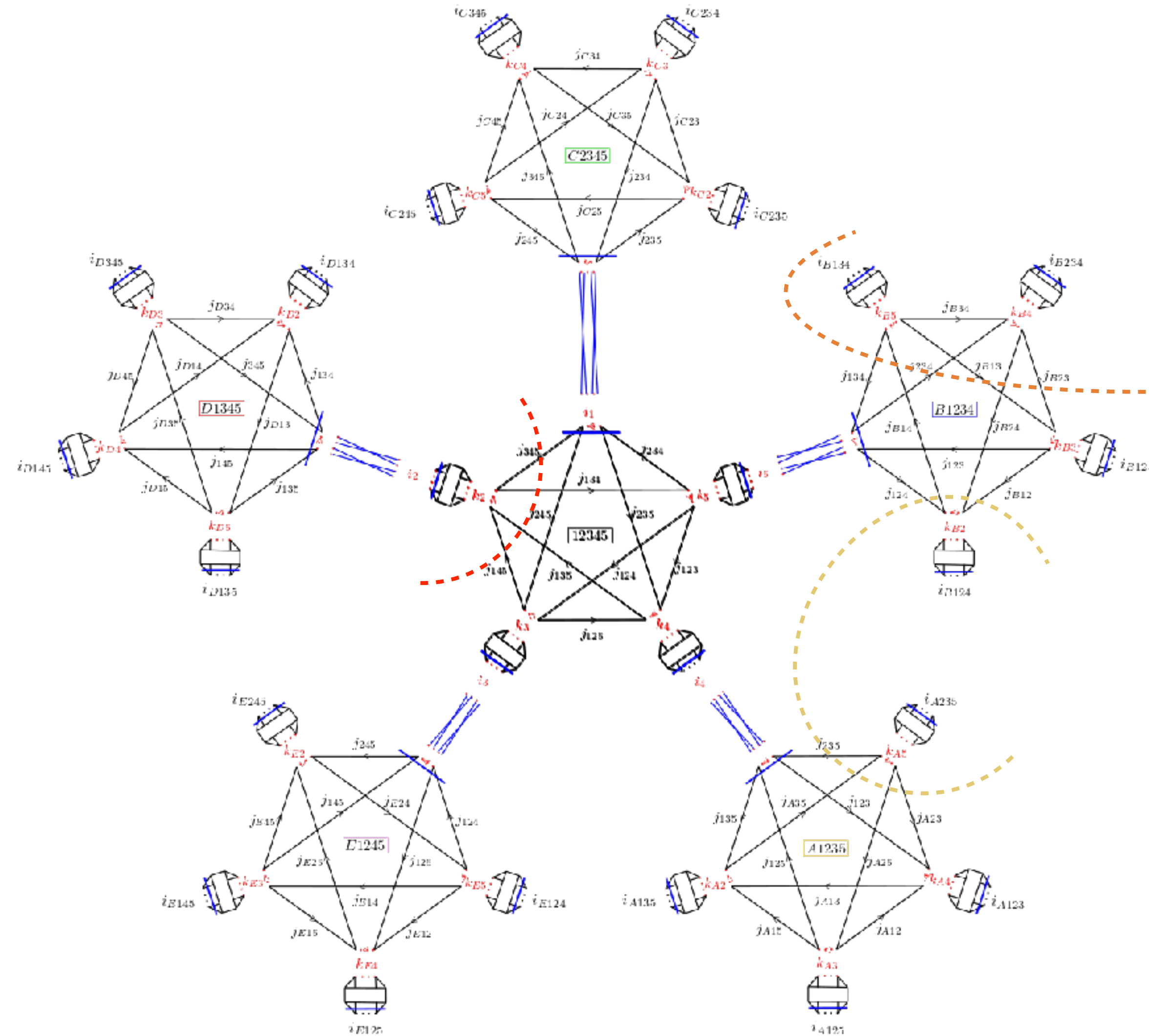
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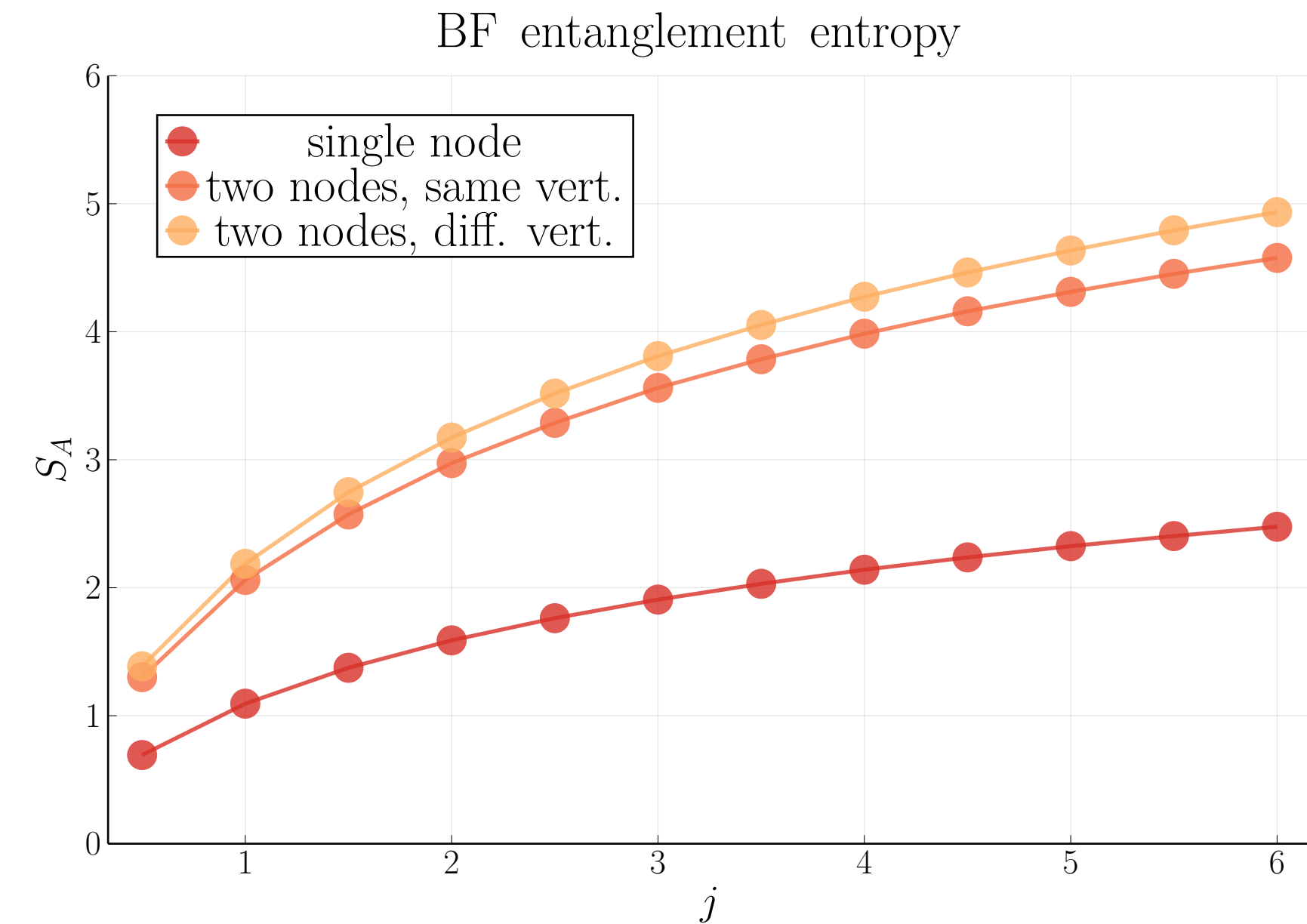
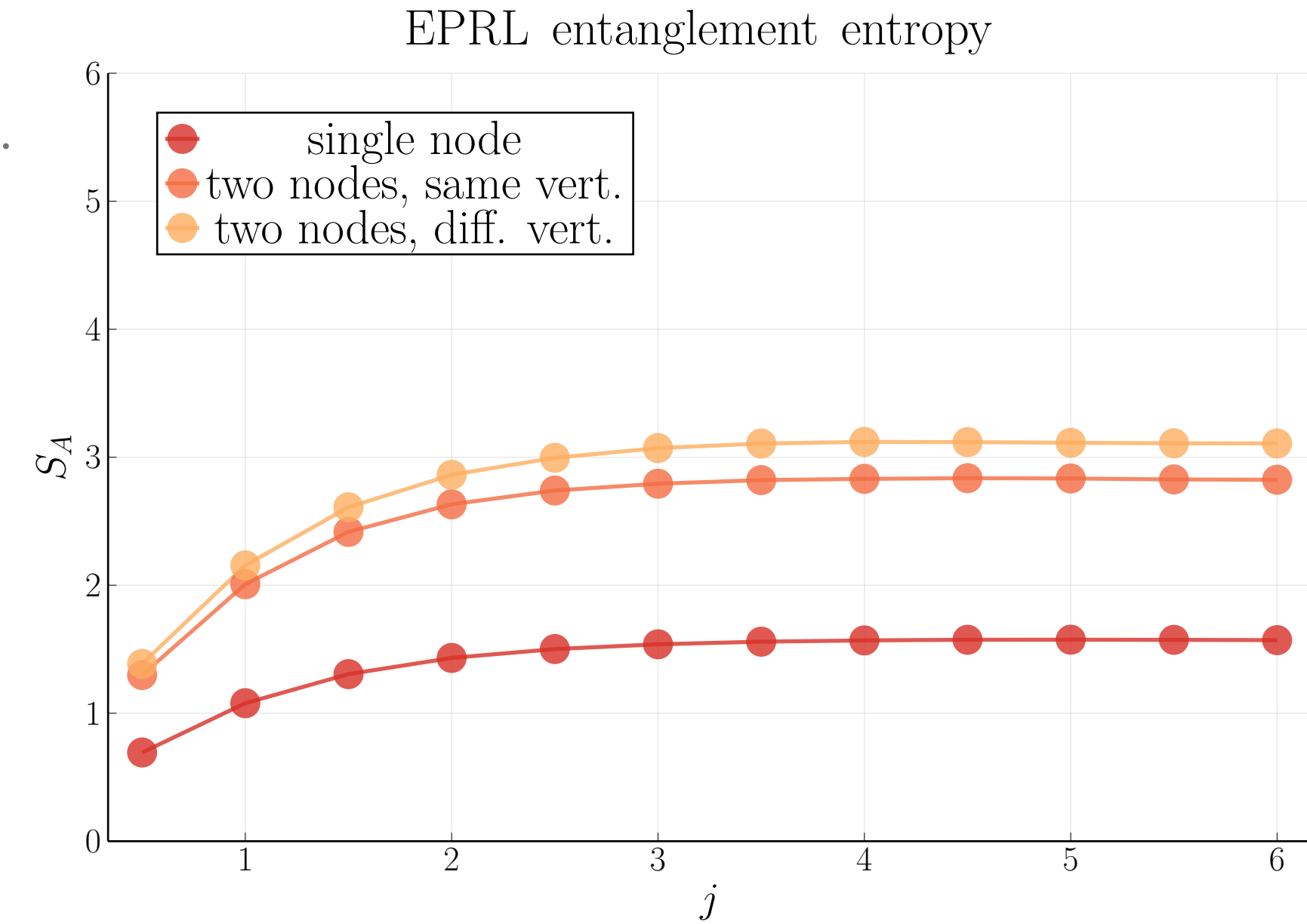
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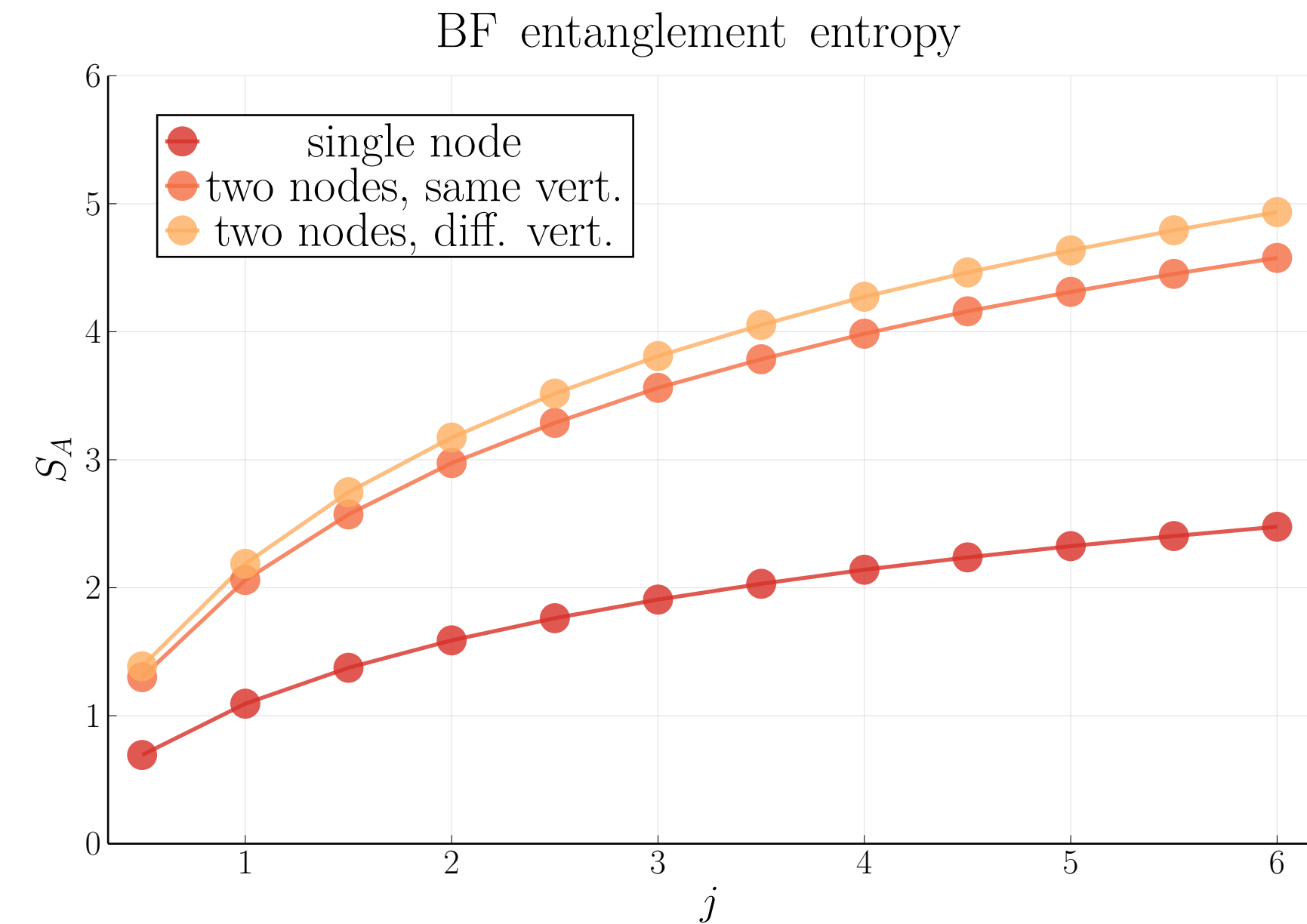
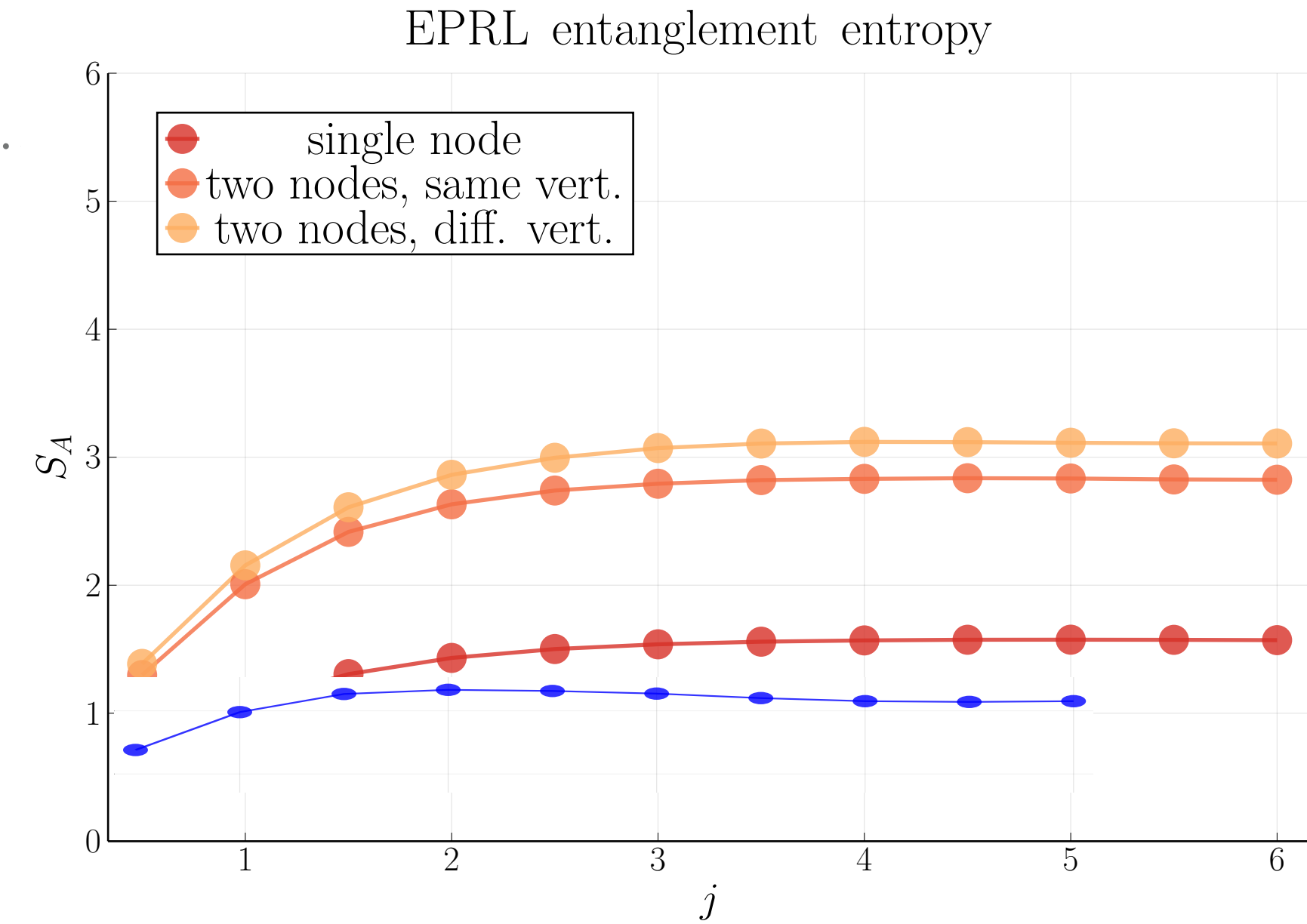
ENTANGLEMENT ENTROPY

- Partition: $\mathcal{H} = \mathcal{H}_A \otimes \mathcal{H}_{\bar{A}}$
- Reduced density matrix: $\rho_A = \frac{1}{Z} \text{Tr}_{\bar{A}} |\psi_0\rangle\langle\psi_0|$
- Entanglement entropy: $S_A = -\text{Tr}(\rho_A \log \rho_A)$



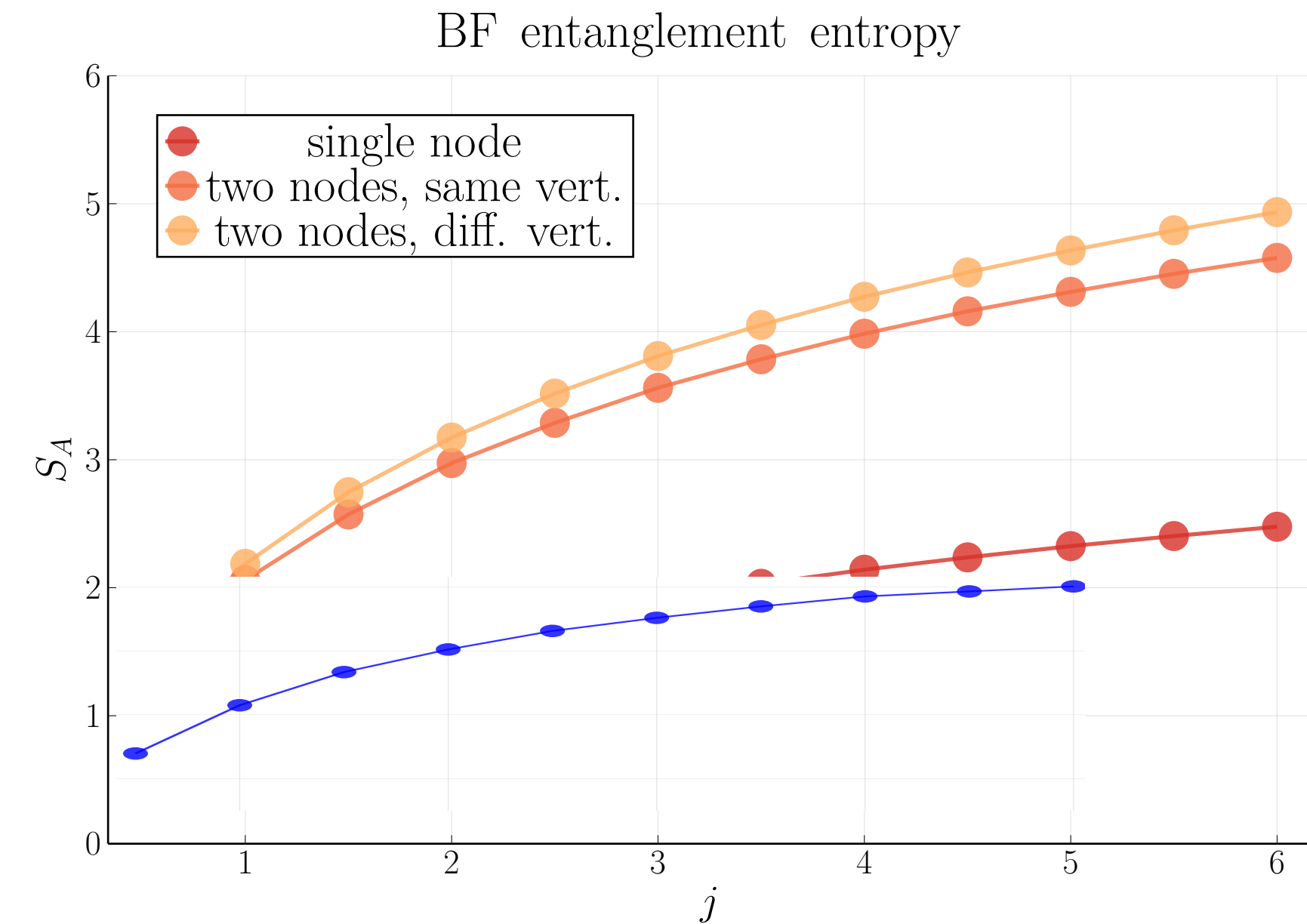
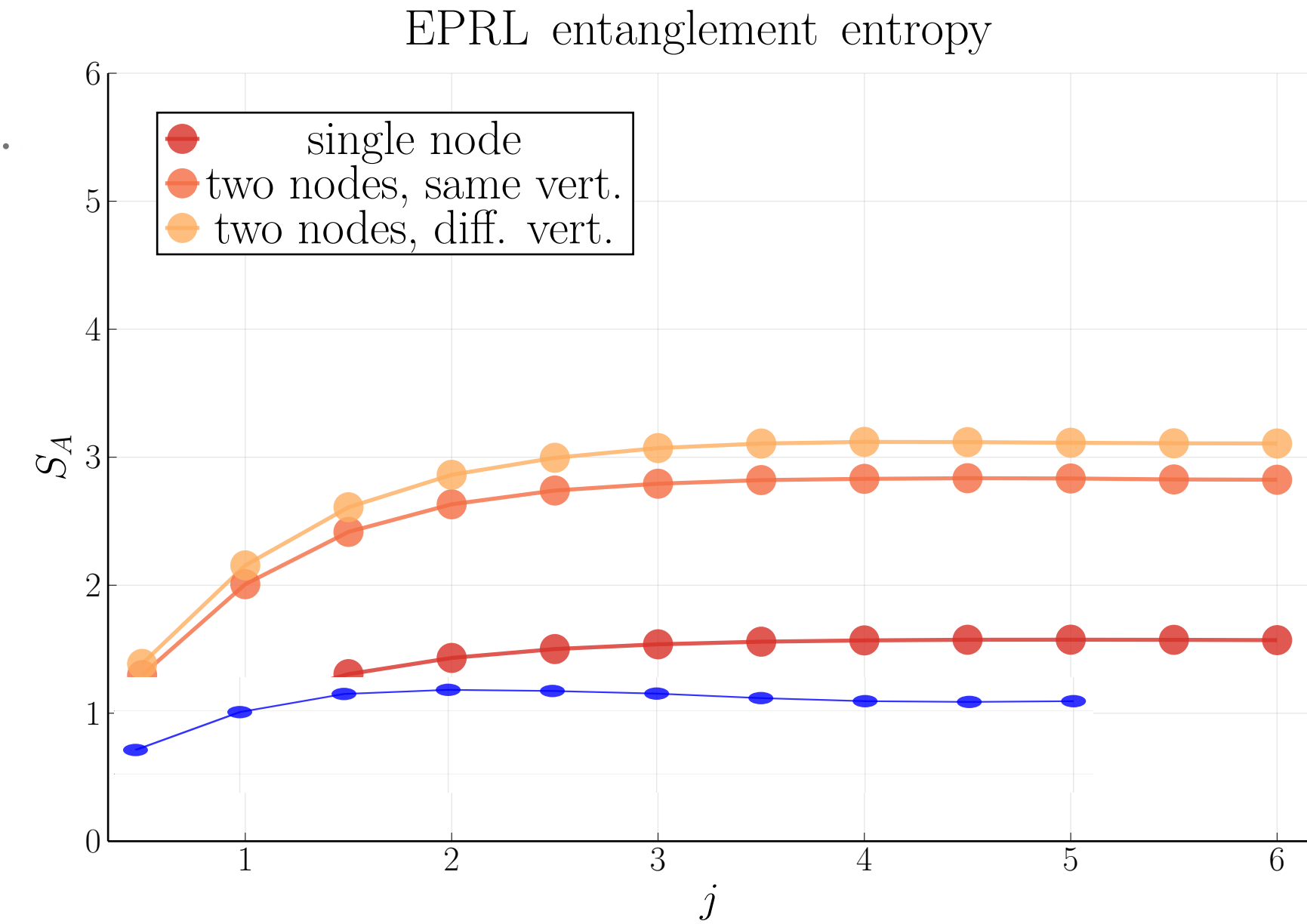
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ENTANGLEMENT ENTROPY

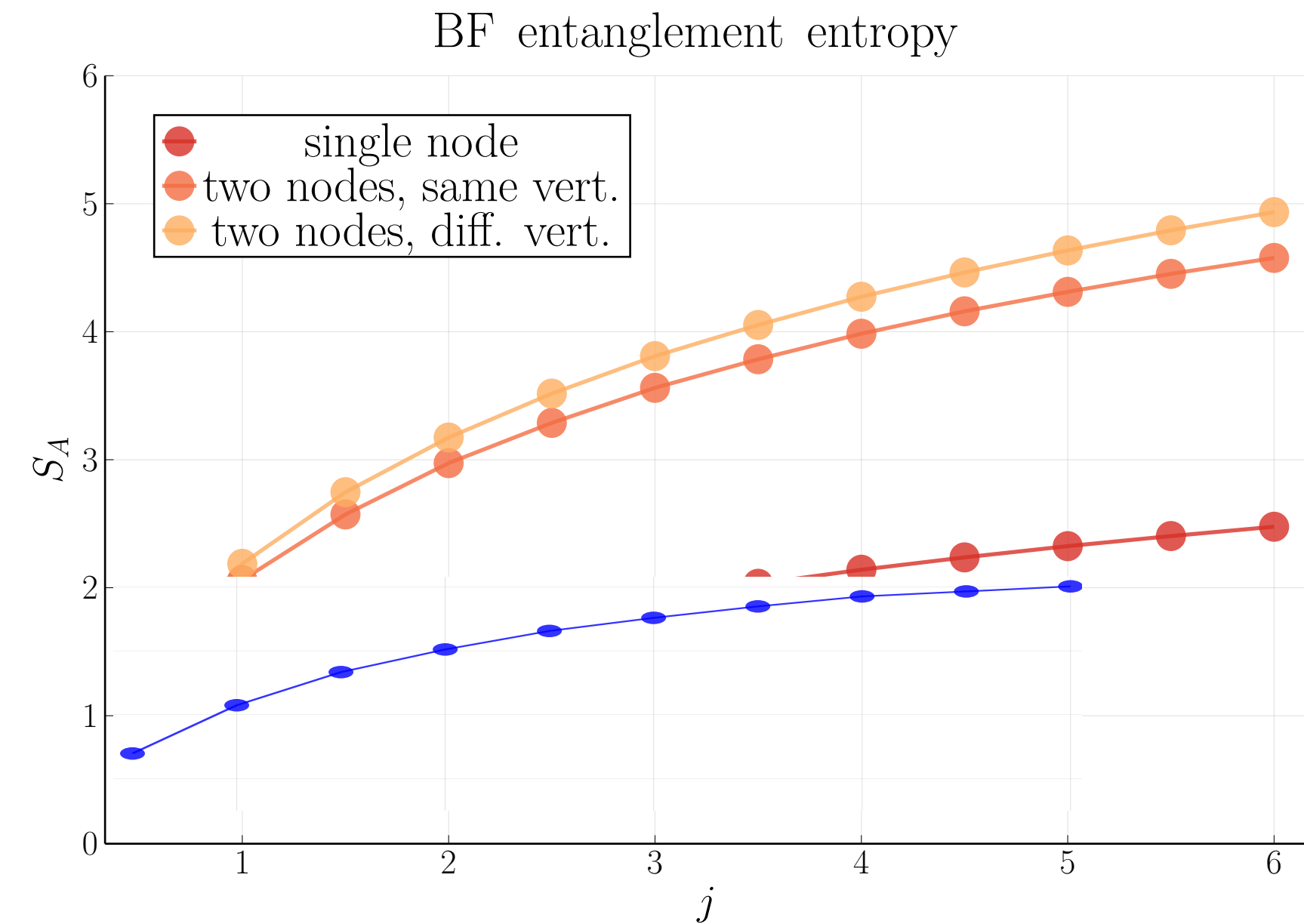
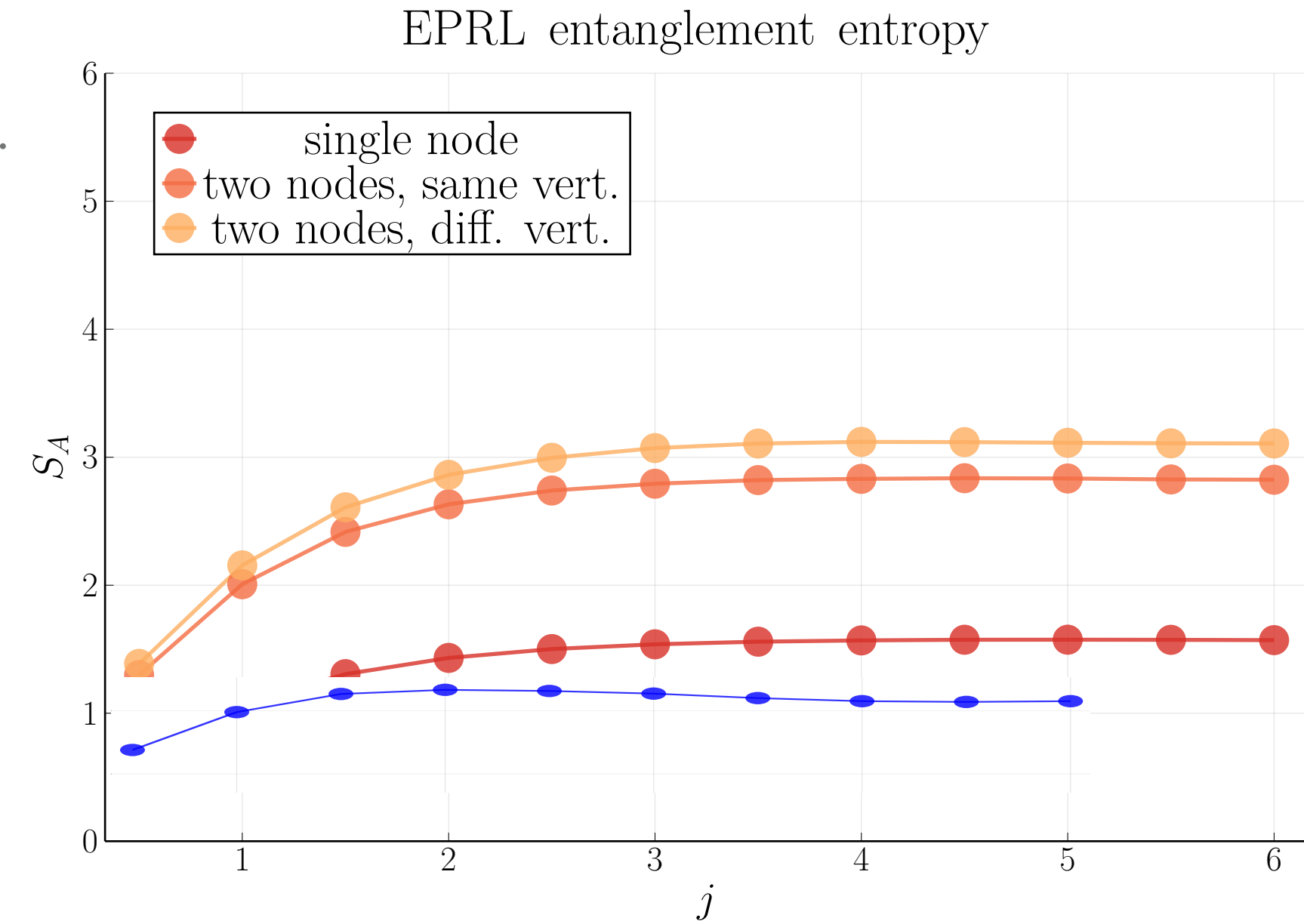
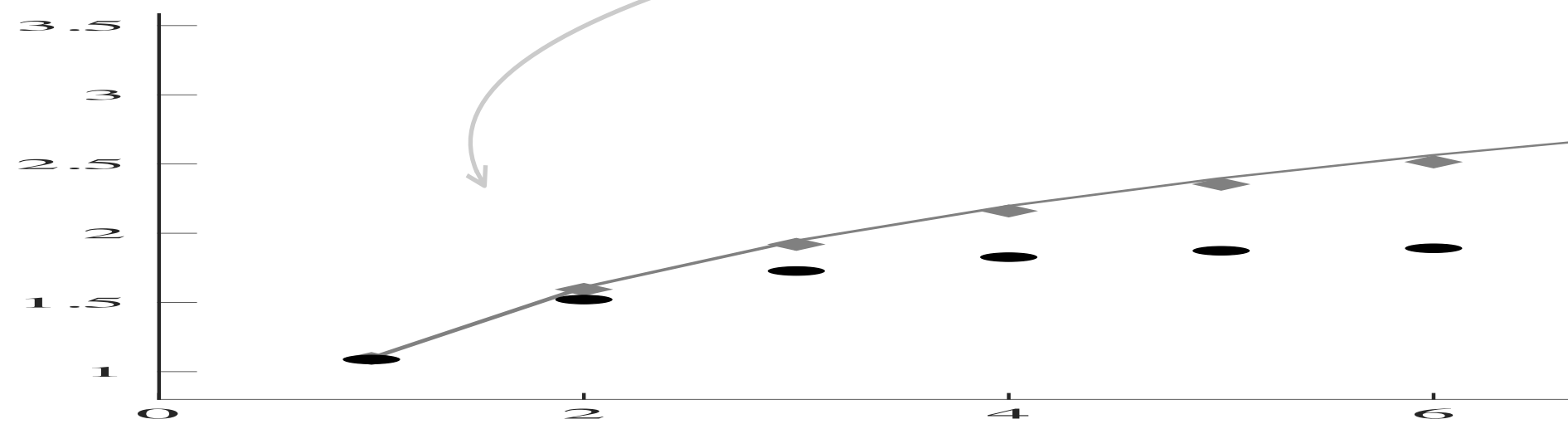
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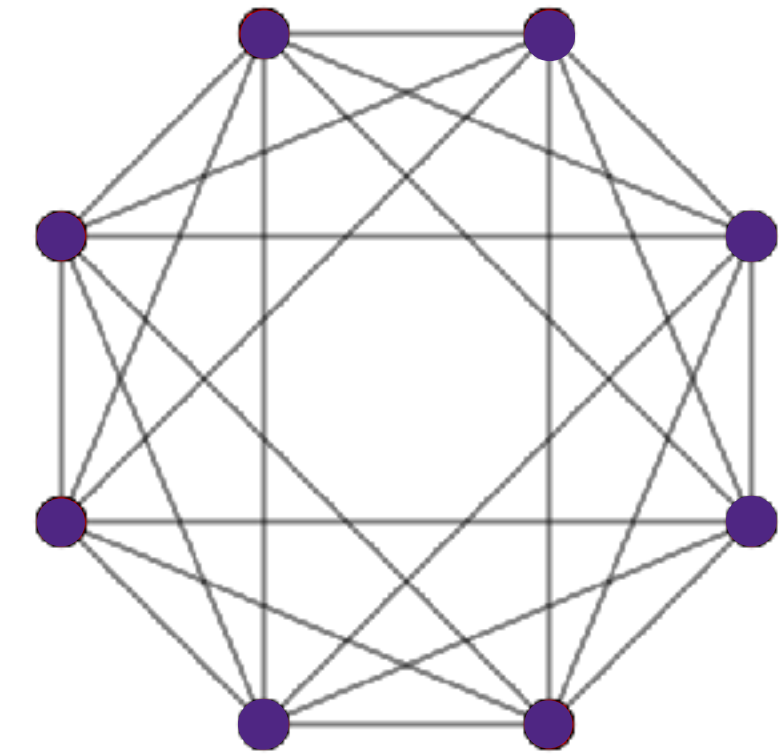
Bianchi, Donà, Vilensky “Entanglement entropy of Bell-network states in LQG”



16-CELL MODEL

Primordial fluctuations from quantum gravity: 16-cell model, with P. Frisoni (in preparation)

- The 20-cell refined model is not a regular triangulation of S_3
- 5-cell regular triangulation \rightarrow 16-cell regular triangulation
- Results for the dihedral angles: \checkmark
- Correlations and entanglement entropy?



SUMMARY

- Computing primordial quantum fluctuations from the full theory is one of the main goals of a quantum theory of gravity!
- Proposal: use Spinfoam Hartle-Hawking States
- Graph truncation: 5-cell ✓, 20-cell ✓, 16-cell *in progress*
- Computational challenge: compute expectation values for observables (using MCMC?)
- Results:
 1. emerging S_3 geometry
 2. large fluctuations
 3. large correlations (for adjacent nodes) \longrightarrow 16-cell needed for richer structure

RESULTS, RESEARCH DIRECTIONS AND COLLABORATIONS

■ FIRST SIMPLE MODEL

- 1 vertex
- 5-cells boundary graph
- computation of observables
- high correlations

with Francesco Gozzini (Heidelberg)



■ RELATION TO COSMOLOGICAL VACUUM

- properties of standard cosmological vacua
- classical limit of the quantum model
- entanglement entropy

with Federico Scali (Pisa)



■ MORE COMPLEX RELIABLE MODELS

- 1 vertex, 6 vertices
- 16-cells and 20-cells boundary graphs
- MCMC to compute observables
- rich behaviour of correlations

with Pietropaolo Frisoni (Western)



■ NON-INFLATIONARY MODELS

- cosmological perturbations from an effective highly-correlated vacuum states
- matter bounce as an alternative to the inflationary models

with Mateo Pascual (Western)

