Linear power corrections and small-q_T resummation

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SWISS NATIONAL SCIENCE FOUNDATION

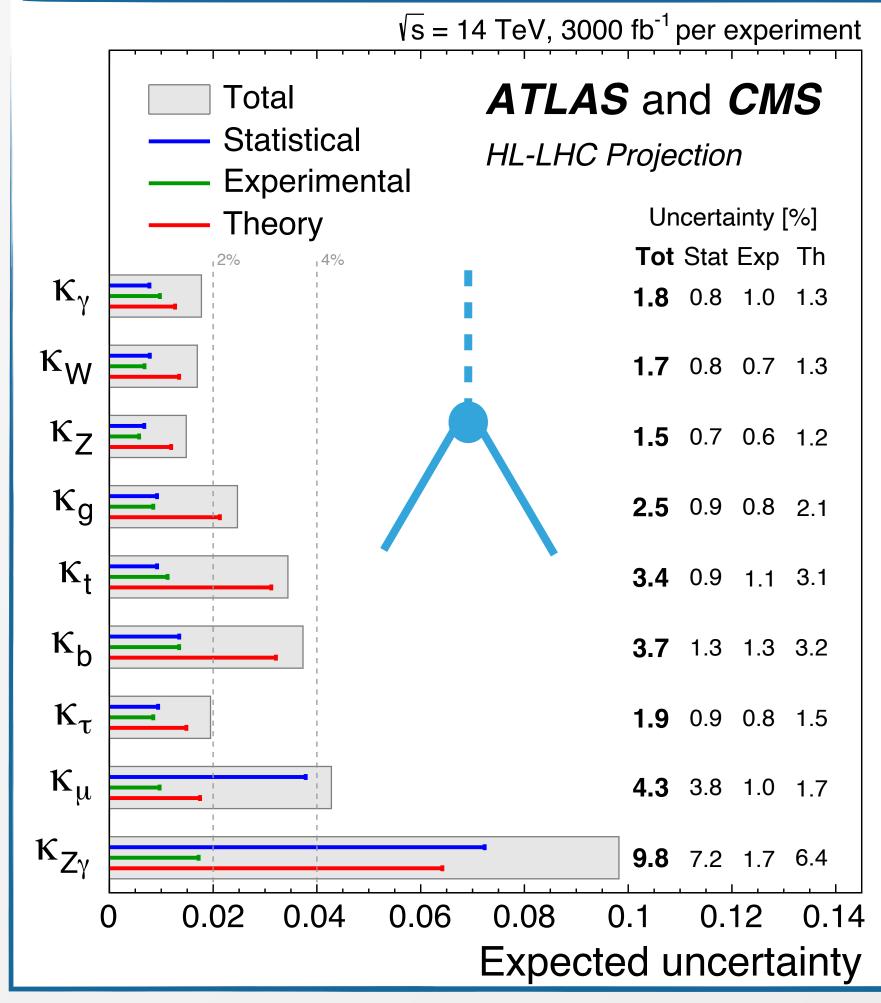
LHC as a precision machine

Luminosity expected to reach 3000 fb⁻¹ at the end of the **HL-LHC** run

Substantial improvement in experimental precision with **increased statistics** and better understanding of systematic uncertainties

Precision target (Higgs couplings): 1-3%

Sensitivity to deviations of Higgs interactions from SM predictions



[Higgs Physics Report at HE/HL-LHC 2019]

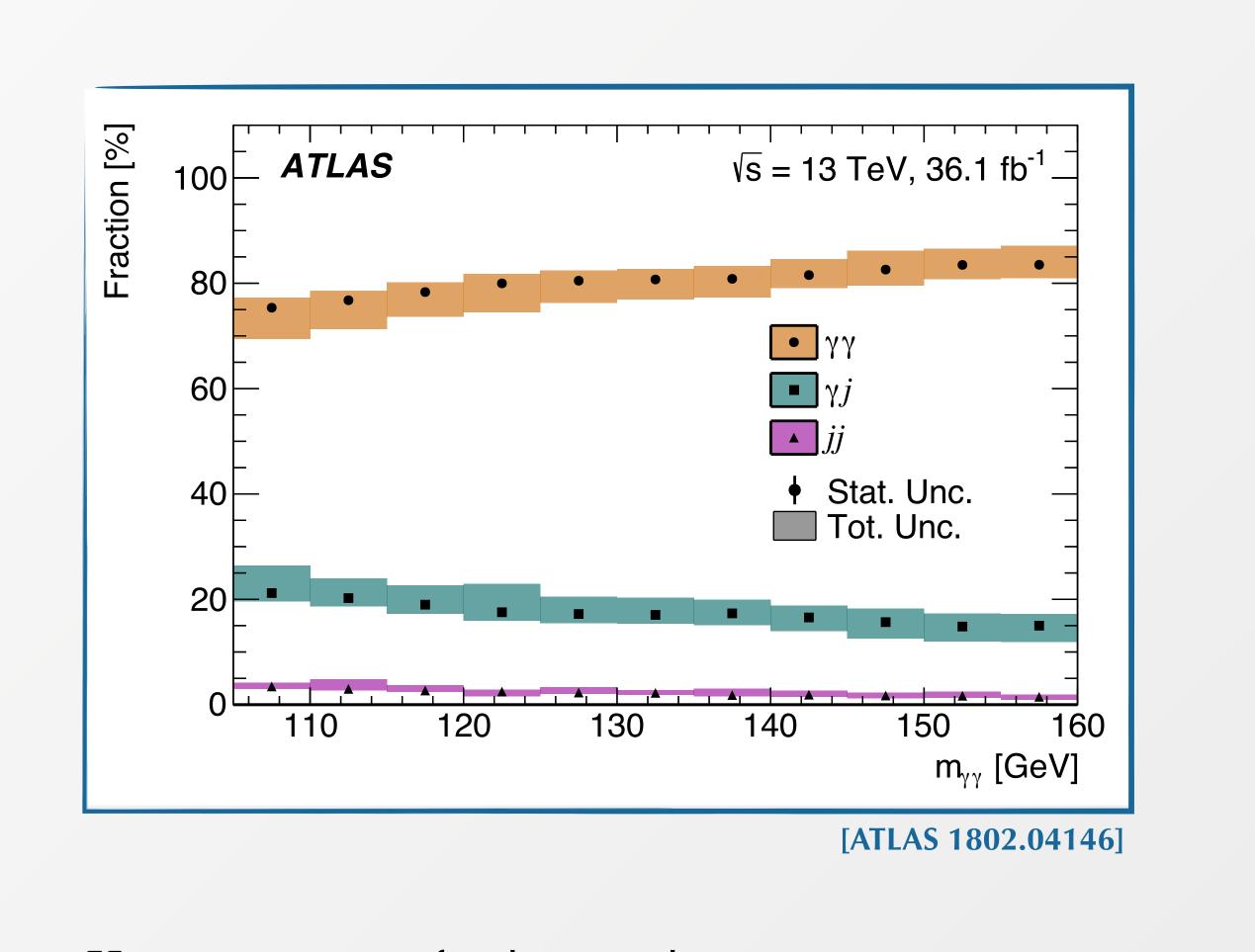


Precision and fiducial acceptances

Experimental analyses performed within fiducial region corresponding to the phase space of experimental apparatuses

Additional selection cuts applied to enhance signal or eliminate/reduce experimental background (e.g. particles with low- p_T)

Data-theory comparison within fiducial region is a core principle in the LHC precision programme



 $H \rightarrow \gamma \gamma$: cuts on final-state photons can improve the efficiency of the selection of pure $\gamma\gamma$ final state

Cut to the chase: fiducial acceptances and perturbative convergence

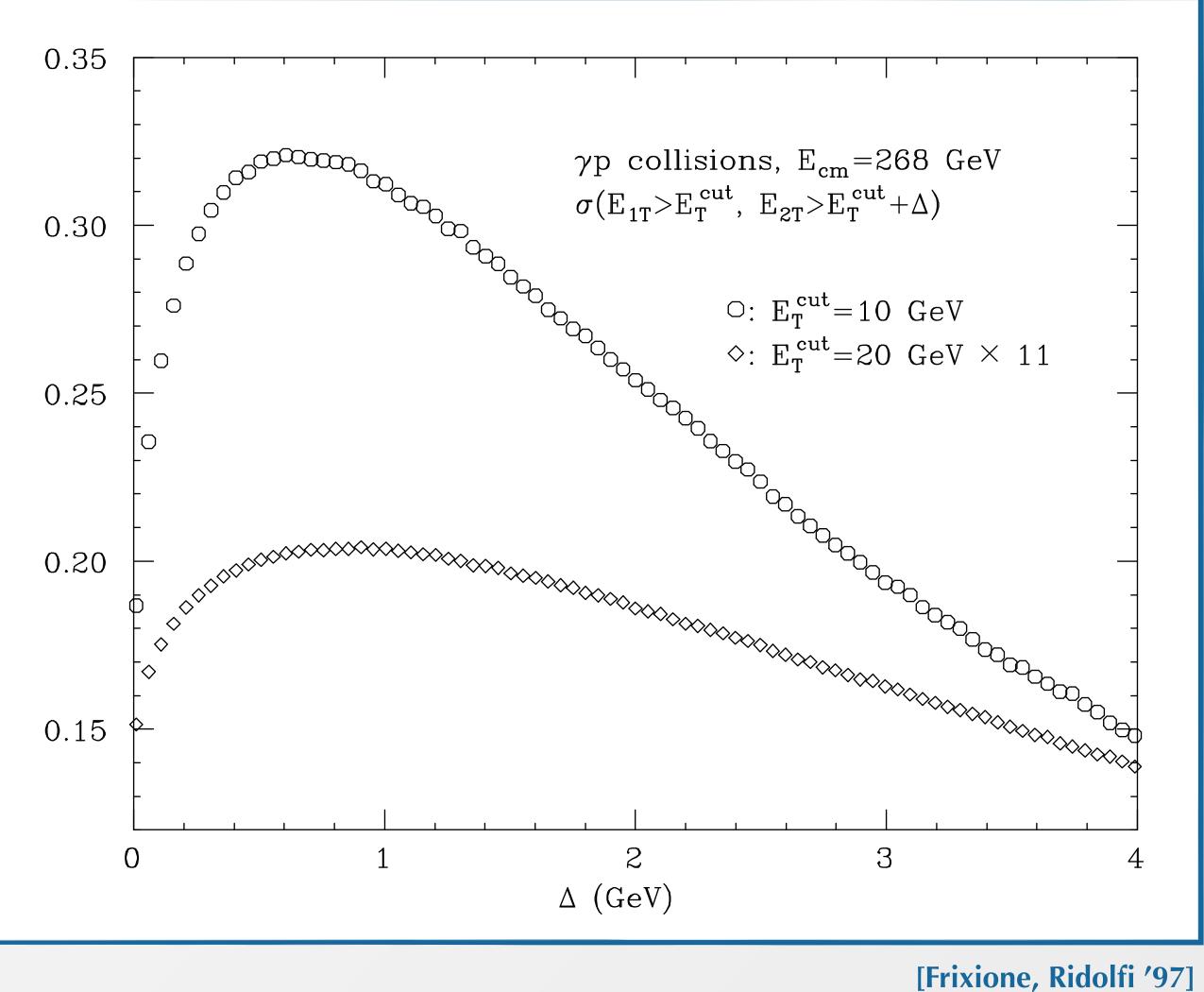
The definition of fiducial cuts can be delicate for configurations with final states with two objects in back-to-back configurations

Perturbative instability induced by sensitivity to soft radiation in configurations close to the back-to-back limit

Some key observations: [Klasen, Kramen '96][Harris, Owen '97][Frixione, Ridolfi '97]

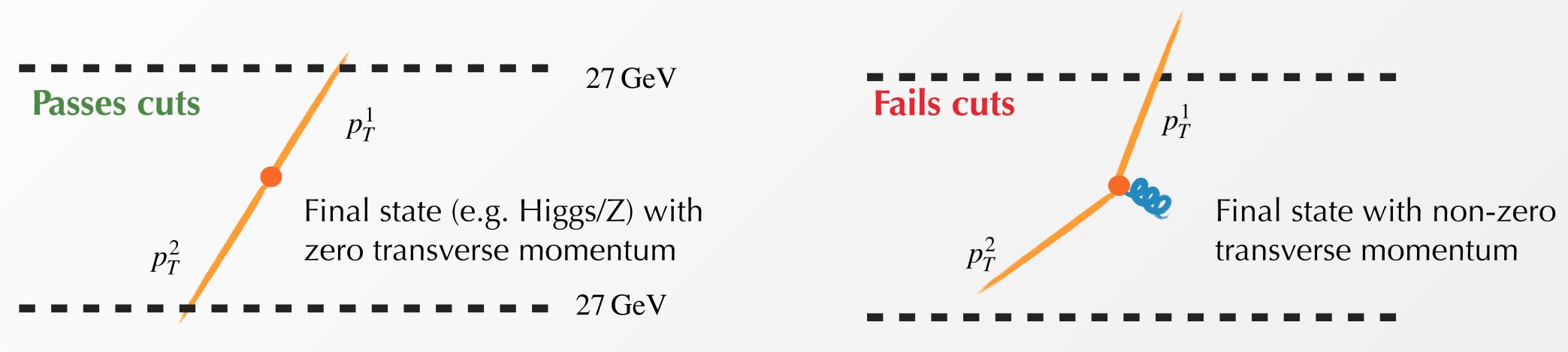
- **Resummation** can be beneficial
- Choice of cuts has an impact on the perturbative convergence
- Subtraction methods based on **slicing** techniques might require special care with certain cuts

 $\sigma_2(\Delta) = \sigma(E_{1T} > E_T^{cut}, E_{2T} > E_T^{cut} + \Delta)$



Cuts and linear power corrections

Symmetric and asymmetric cuts induce a linear dependence on the acceptance



Drell-Yan production cuts (ATLAS, CMS, LHCb...)

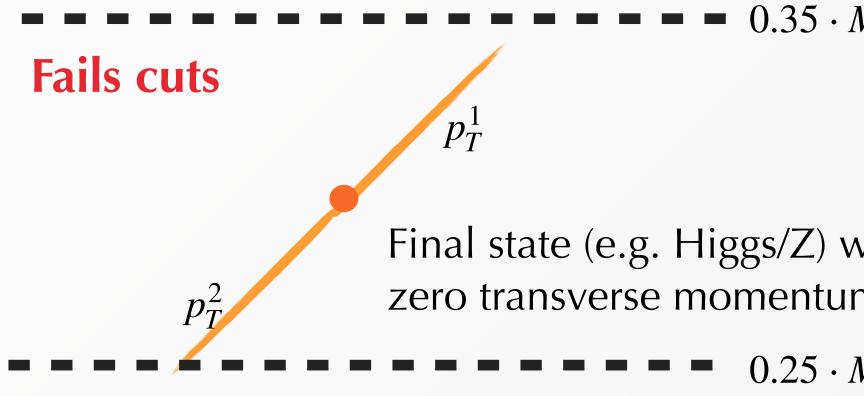
$$f^{\text{sym}}(p_T) = f_0 + f_1^{\text{sym}} \cdot \frac{p_T}{M} + \mathcal{O}_2$$

[Tackmann, Ebert '19][Alekhin, Kardos, Moch, Trócsányi '21][Salam, Slade '21]

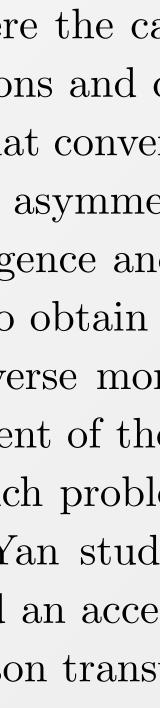
Coefficients depend on the specific choice of cuts

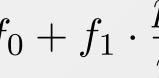
Cuts and linear power corrections

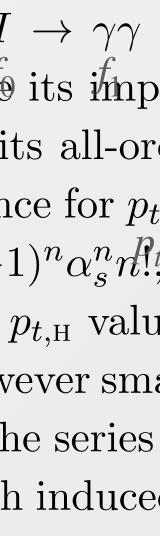
fusion Higgs production studies, where the ca For this process, inclusive cross sections and o rapidity show a perturbative series that conve Symmetric and asymmetric cuts induce a linear dependence on the acceptance sections, which include asymmetric **[Tackmann, Ebert '19]** [Alekhin, Kardos, Moch, Trócsányi '21] [Salam, Slade '21] Alekhin, Kardos, Moch, Trócsányi '21] [Salam, Slade '21] [Salam, Slade '21] Alekhin, Kardos, Moch, Trócsányi '21] [Salam, Slade '21] Alekhin, Kardos, Moch, Trócsányi '21] [Salam, Slade '21] Alekhin, Kardos, Moch, Trócsányi '21] [Salam, Slade '21] [Sala12]. Furthermore, it turns out that to obtain $0.35 \cdot M$ to integrate over Higgs boson transverse mor Passes cuts physically unsettling (albeit reminiscent of the **Fails cuts** p_T^1 Refs. [12, 14] have noted that such probl extent also in the context of Drell-Yan stud Final state with non-zero asymmetric and symmetric cuts yield an acce Final state (e.g. Higgs/Z) with zero transverse momentum p_T^2 a linear dependence on the Higgs boson trans $0.25 \cdot M$ $\mathbf{f}(p_{t,\mathrm{H}}) = f_0 + f_1 \cdot \frac{f_1}{f_1}$ $p_{t,+} > 0.35 m_H$ $p_{t,-} > 0.25 m_H$ 0.80 - $H \rightarrow \gamma \gamma$ selection cuts In section 2, concentrating on the $H \to \gamma \gamma$ also examine its imp dente arises a $f(p_{t,H})$ model for its all-or resummatrionthe acceptance for p_t powor-law dep diverges $(-1)^n \alpha_s^n n!!$ of policial cross : coming predominantly in or very low $p_{t,H}$ value Factorized growth implies that, however small ⁰never converge. Non-convergence of the series cause of the same isign factorial growth induce SM@LHC 2022, 13 Apr 2022



$$f^{\text{asym}}(p_T) = f_0 + f_1^{\text{asym}} \cdot \frac{p_T}{M} + \mathcal{O}_2$$







Linear power corrections and perturbative convergence

What happens at the level of the fiducial cross section?

 $\sigma_{\rm fid} =$

Drastic impact on the behaviour of calculations in perturbative QCD Simple **double-logarithmic** approximation for p_T distribution

$$\frac{d\sigma}{dp_T} \sim \frac{4C_A \alpha_s L}{\pi p_T} e^{-\frac{2C_A \alpha_s}{\pi} L^2} \sim \frac{\sigma_{\text{tot}}}{p_T} \sum_{n=1}^{\infty} (-1)^{n-1} \frac{2\ln^{2n-1} \frac{M}{2p_T}}{(n-1)!} \left(\frac{2C_A \alpha_s}{\pi}\right)^n$$

Upon integration, pathological perturbative behaviour

$$\sigma_{\rm fid} = \sigma_{\rm tot} \left[f_0 + f_1 \sum_{n=1}^{\infty} (-1)^{n+1} \frac{(2n)!}{2(n!)} \left(\frac{2C_A \alpha_s}{\pi} \right)^n + \cdots \right]$$

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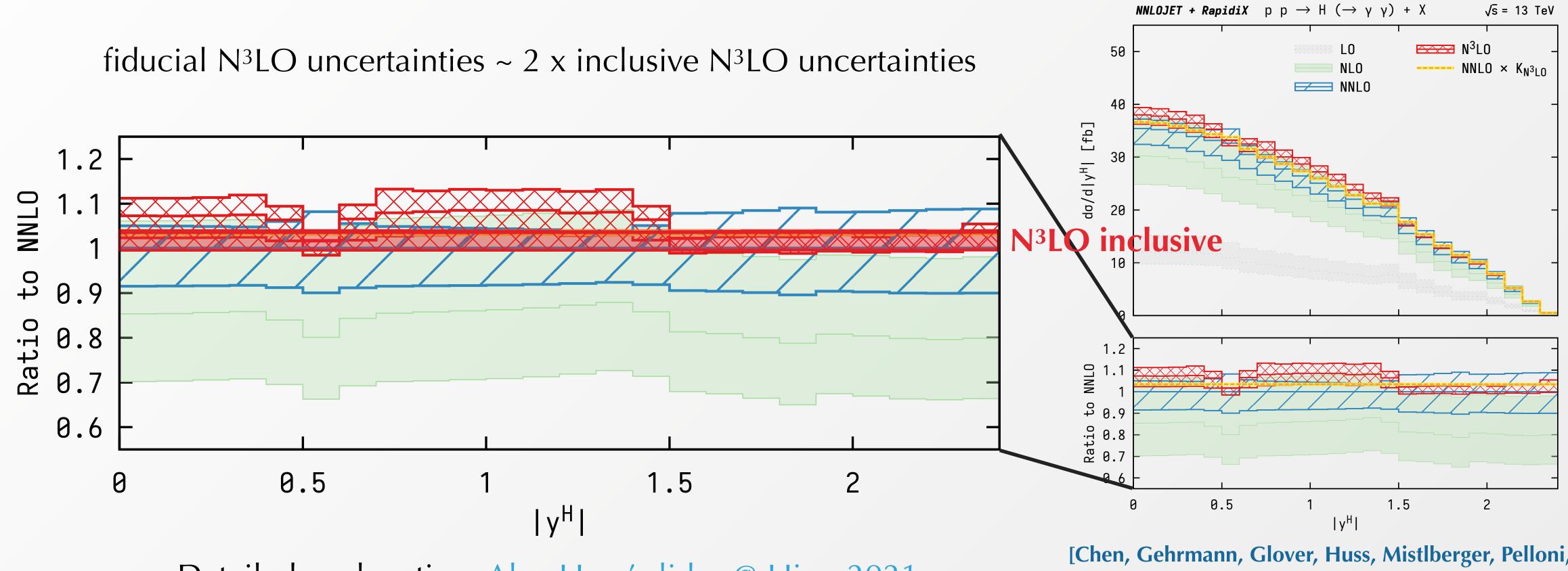
$$\int \frac{d\sigma}{dp_T} f(p_T) dp_T$$

$$L = \ln \frac{p_T}{2M}$$

(alternating sign) factorial growth

Linear power corrections and perturbative convergence

$$\frac{\sigma_{\text{asym}}^{\text{DL}}}{f_0 \sigma_{\text{tot}}} - 1 \simeq \frac{f_1^{\text{asym}}}{f_0} \left(\underbrace{\frac{0.16}{\alpha_s} - \underbrace{0.33}_{\alpha_s^2} + \underbrace{0.82}_{\alpha_s^3} - \underbrace{2.73}_{\alpha_s^4} + \underbrace{11.72}_{\alpha_s^5} + \dots \right)$$



Detailed explanation: <u>Alex Huss' slides @ Higgs2021</u>

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$$pp \rightarrow H(\rightarrow \gamma \gamma)$$

[Salam, Slade '21]

[Chen, Gehrmann, Glover, Huss, Mistlberger, Pelloni, '21]

Linear power corrections and perturbative convergence

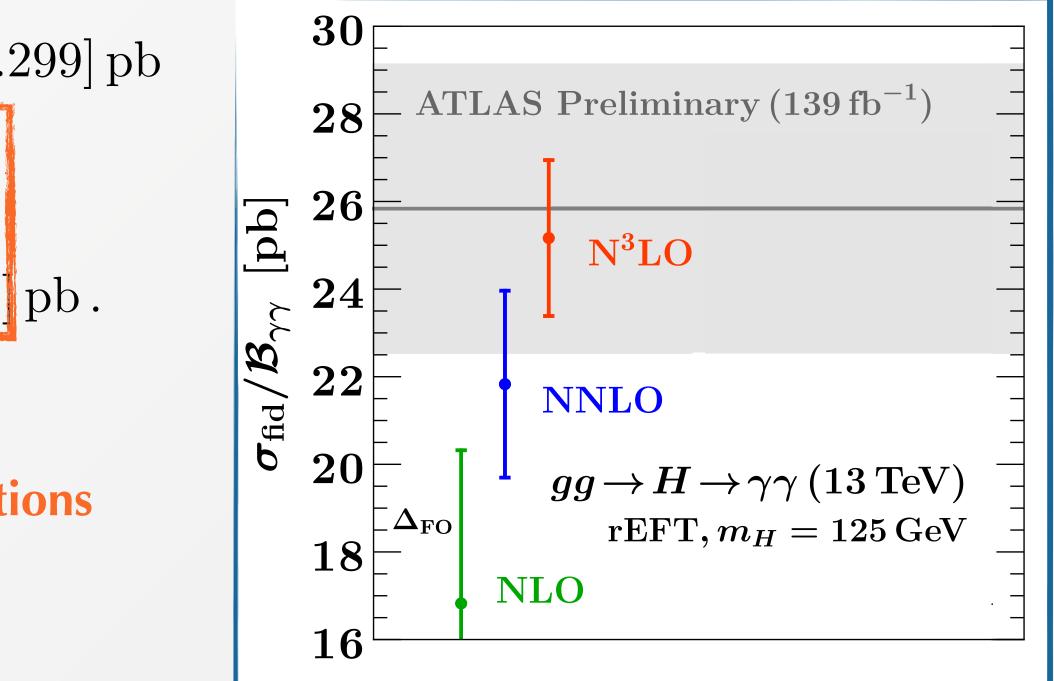
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 $\sigma_{\text{incl}}^{\text{FO}} = 13.80 \left[1 + 1.291 + 0.783 + 0.299 \right] \text{pb}$ $\sigma_{\text{fid}}^{\text{FO}} / \mathcal{B}_{\gamma\gamma} = 6.928 \left[1 + (1.300 + 0.129_{\text{fpc}}) + (0.784 - 0.061_{\text{fpc}}) + (0.331 + 0.150_{\text{fpc}}) \right] \text{pb}.$

> Effect of **linear fiducial corrections**

$$pp \to H(\to \gamma\gamma)$$

[Salam, Slade '21]



[Billis, Dehnadi, Ebert, Michel, Stewart, Tackmann '21]

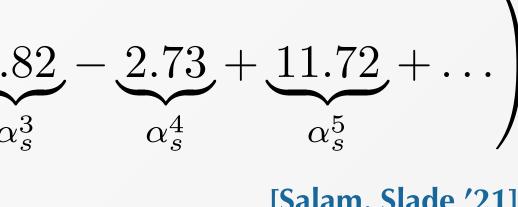
It's the sum that makes up the total **[Totò, '60]**

$$\frac{\sigma_{\text{asym}}^{\text{DL}}}{f_0 \sigma_{\text{tot}}} - 1 \simeq \frac{f_1^{\text{asym}}}{f_0} \left(\underbrace{\begin{array}{c} 0.16 \\ \alpha_s \end{array}}_{\alpha_s} - \underbrace{\begin{array}{c} 0.33 \\ \alpha_s^2 \end{array}}_{\alpha_s^2} + \underbrace{\begin{array}{c} 0.8 \\ \alpha_s^2 \end{array}}_{\alpha_s^2} \right)$$

Sum of divergent series with alternating sign factorial growth is **Borel-summable**

$$\frac{\sigma_{\text{asym}}^{\text{DL}}}{f_0 \sigma_{\text{tot}}} - 1 \simeq \frac{f_1^{\text{asym}}}{f_0} \left(\underbrace{\underbrace{0.16}_{\alpha_s} - \underbrace{0.33}_{\alpha_s^2} + \underbrace{0.82}_{\alpha_s^3} - \underbrace{2.73}_{\alpha_s^4} + \underbrace{11.72}_{\alpha_s^5} + \dots \right) \simeq \frac{f_1^{\text{asym}}}{f_0} \times \underbrace{\underbrace{0.05}_{\text{resummed}}}_{\text{resummed}}.$$

size of the smallest term, $(\Lambda/M)^{0.2}$ (compared to $(\Lambda/M)^2$ expected for inclusive cross sections)



$$pp \to H(\to \gamma\gamma)$$

[Salam, Slade '21]

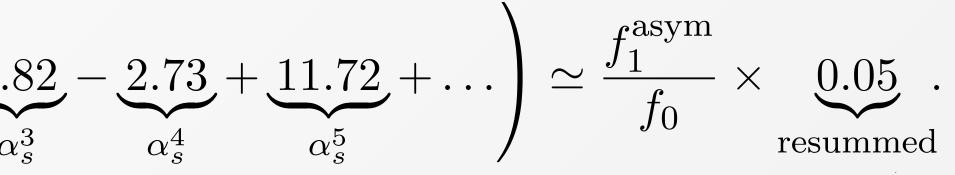
Divergent behaviour can be associated to a theoretical ambiguity, which can be estimated by looking at the

It's the sum that makes up the total **[Totò, '60]**

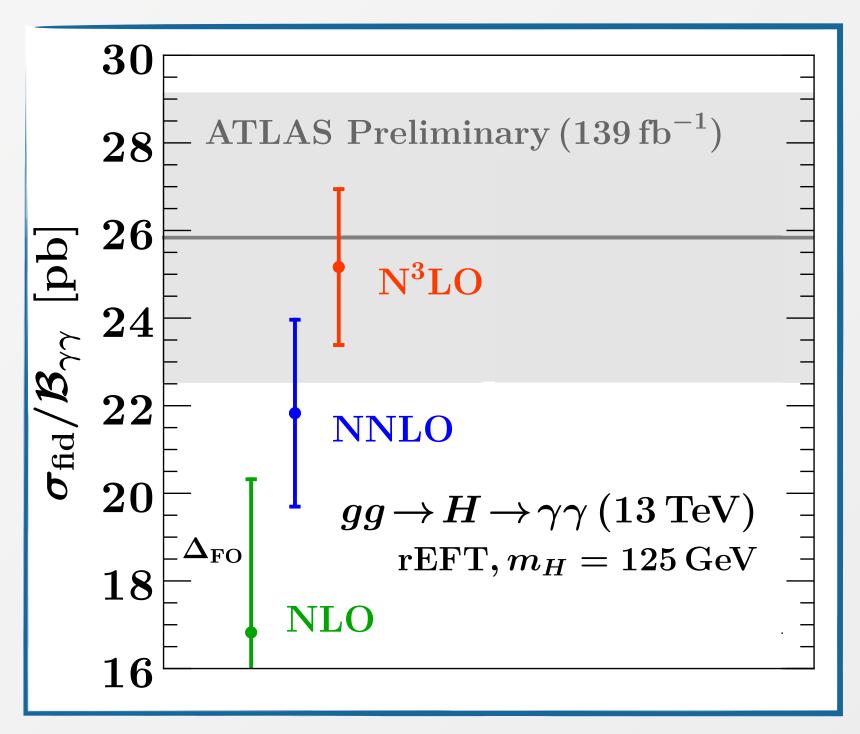
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> Linear fiducial power corrections can be resummed at all orders in perturbation theory [Ebert, Michel, Stewart, Tackmann '20]



[Salam, Slade '21]



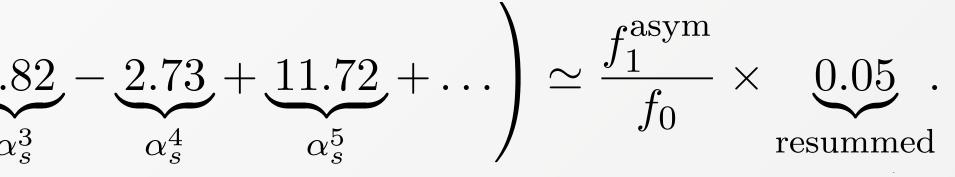
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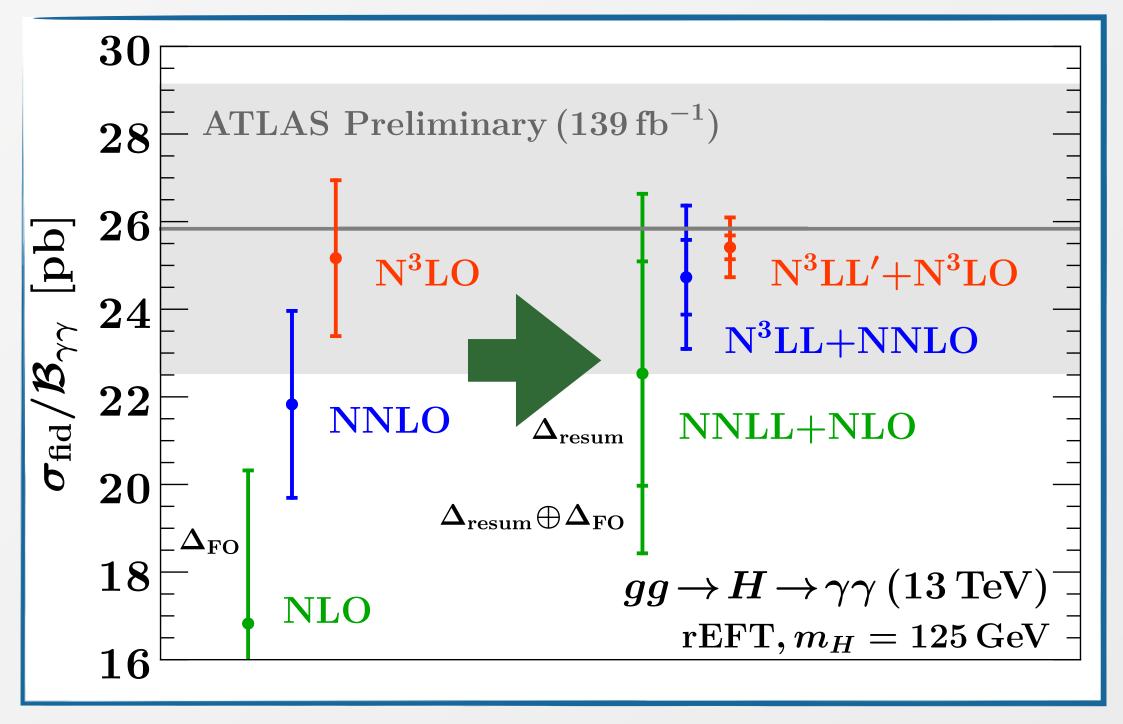
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> Linear fiducial power corrections can be resummed at all orders in perturbation theory



[Salam, Slade '21]



[Billis, Dehnadi, Ebert, Michel, Stewart, Tackmann '21]

All cuts are equal but some cuts are more equal than others [Orwell, '45 (possibly apocryphal)]

Do we need to abandon the idea of **fixed-order accuracy** for fiducial cross sections?

For legacy measurements, resummation appears the only viable solution

Resorting to alternative definition of cuts for future analyses can resolve the issue of linear fiducial power corrections altogether

Simplest options:

Product cuts:

Replace the symmetric/asymmetric cuts on $p_T^{(1)}, p_T^{(2)}$ with a cut on $p_T^{(1)} \cdot p_T^{(2)}$, keeping a cut on the softer final state particle $min(p_T^{(1)}, p_T^{(2)}) > p_T^{min}$

Staggered cuts: [Grazzini, Kallweit, Wiesemann '17][Alekhin, Kardos, Moch, Trócsányi '21] Rather than imposing an asymmetric cut on leading/subleading $p_T^{(1)}$, $p_T^{(2)}$, apply an asymmetric cut on **identified** final state particles (e.g. lepton/antilepton in NC DY production, lepton/neutrino in CC DY, photon with higher/ lower rapidity in $pp \rightarrow H(\rightarrow \gamma \gamma)$)

More performing (and refined) choice of cuts possible [Salam, Slade '21]

[Salam, Slade '21]

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For candle processes like Drell-Yan production it would still be desirable to have predictions at **fixed order** (relevant for e.g. parton densities extraction)

Linear dependence on p_T affects efficiency and precision of non-local subtraction techniques such as q_T -subtraction [Catani, Grazzini '07]

$$d\sigma_{V}^{N^{3}LO} \equiv \mathscr{H}_{V}^{N^{3}LO} \otimes d\sigma_{V}^{LO} + \left(d\sigma_{V+jet}^{NNLO} \right)$$

$$\left[d\sigma_V^{N^3LL}\right]_{\mathcal{O}(\alpha_s^3)} \Theta(p_T > p_T^{\text{cut}}) + \mathcal{O}((p_T^{\text{cut}}/M)^n)$$

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Virtual correction after subtraction of IR singularities and contribution of soft/collinear origin (beam, soft functions)

$$\left[d\sigma_V^{N^3LL}\right]_{\mathcal{O}(\alpha_s^3)} \Theta(p_T > p_T^{\text{cut}}) + \mathcal{O}((p_T^{\text{cut}}/M)^n)$$

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differential *p*_T distribution at NNLO

$$\left[d\sigma_V^{N^3LL}\right]_{\mathcal{O}(\alpha_s^3)} \Theta(p_T > p_T^{\text{cut}}) + \mathcal{O}((p_T^{\text{cut}}/M)^n)$$

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 $\Theta(p_T > p_T^{\text{cut}}) + \mathcal{O}((p_T^{\text{cut}}/M)^n)$ **Expansion of the N³LL resummed** p_T distribution at order $\mathcal{O}(\alpha_s^3)$

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Finite for $p_T \rightarrow 0$: integral over p_T allows one to obtain N³LO predictions within fiducial cuts

For candle processes like Drell-Yan production it would still be desirable to have predictions at **fixed order** (relevant for e.g. parton densities extraction)

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Both contributions are divergent in the $p_T \rightarrow 0$ limit, which requires the introduction of a technical cutoff p_T^{cut}

For candle processes like Drell-Yan production it would still be desirable to have predictions at **fixed order** (relevant for e.g. parton densities extraction)

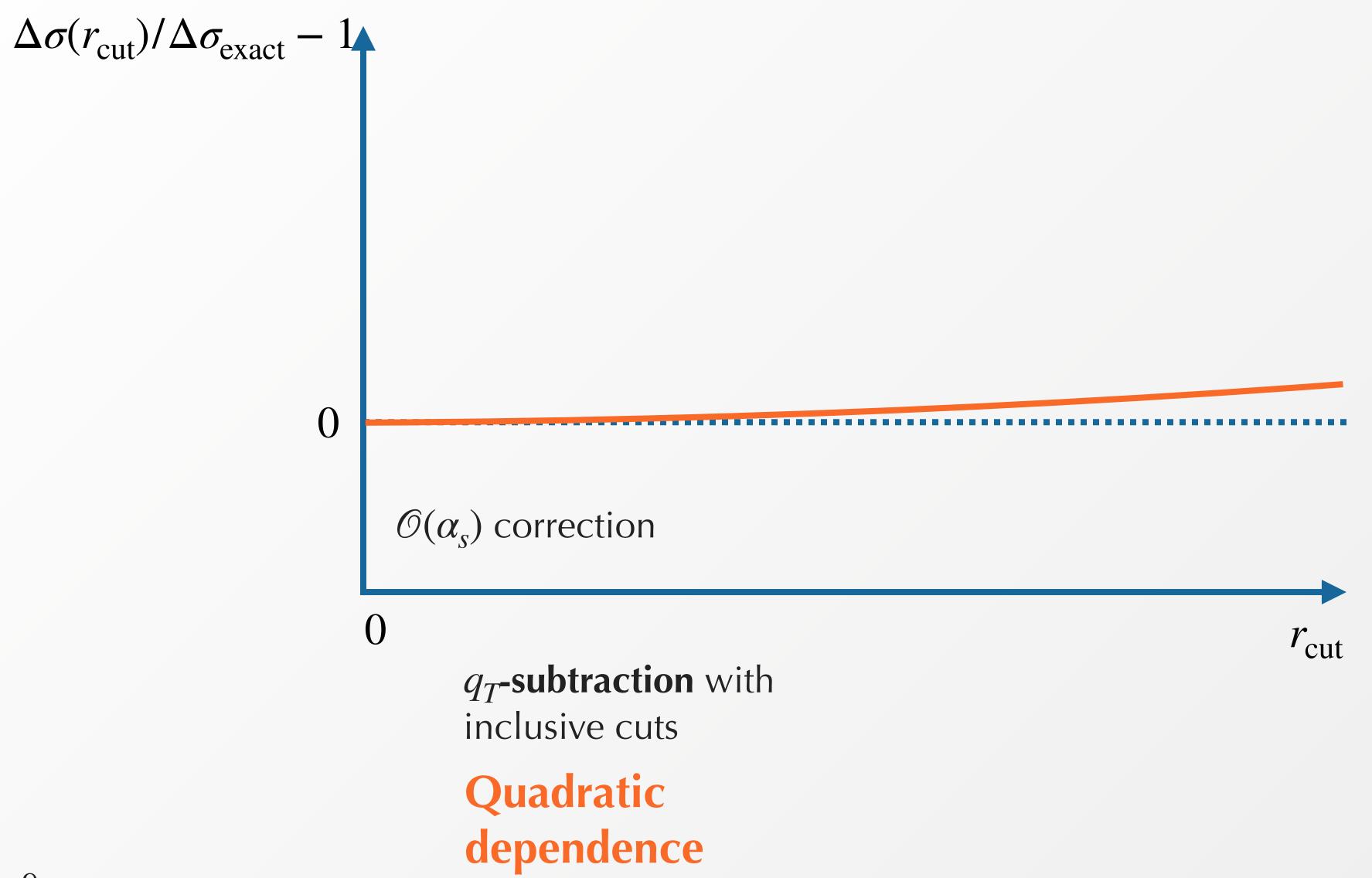
Linear dependence on p_T affects efficiency and precision of non-local subtraction techniques such as q_T -subtraction [Catani, Grazzini '07]

$$d\sigma_V^{N^3LO} \equiv \mathcal{H}_V^{N^3LO} \otimes d\sigma_V^{LO} + \left(d\sigma_{V+jet}^{NNLO} \right)$$

Relative size of **power corrections** affects **stability and performance** of non-local subtraction methods

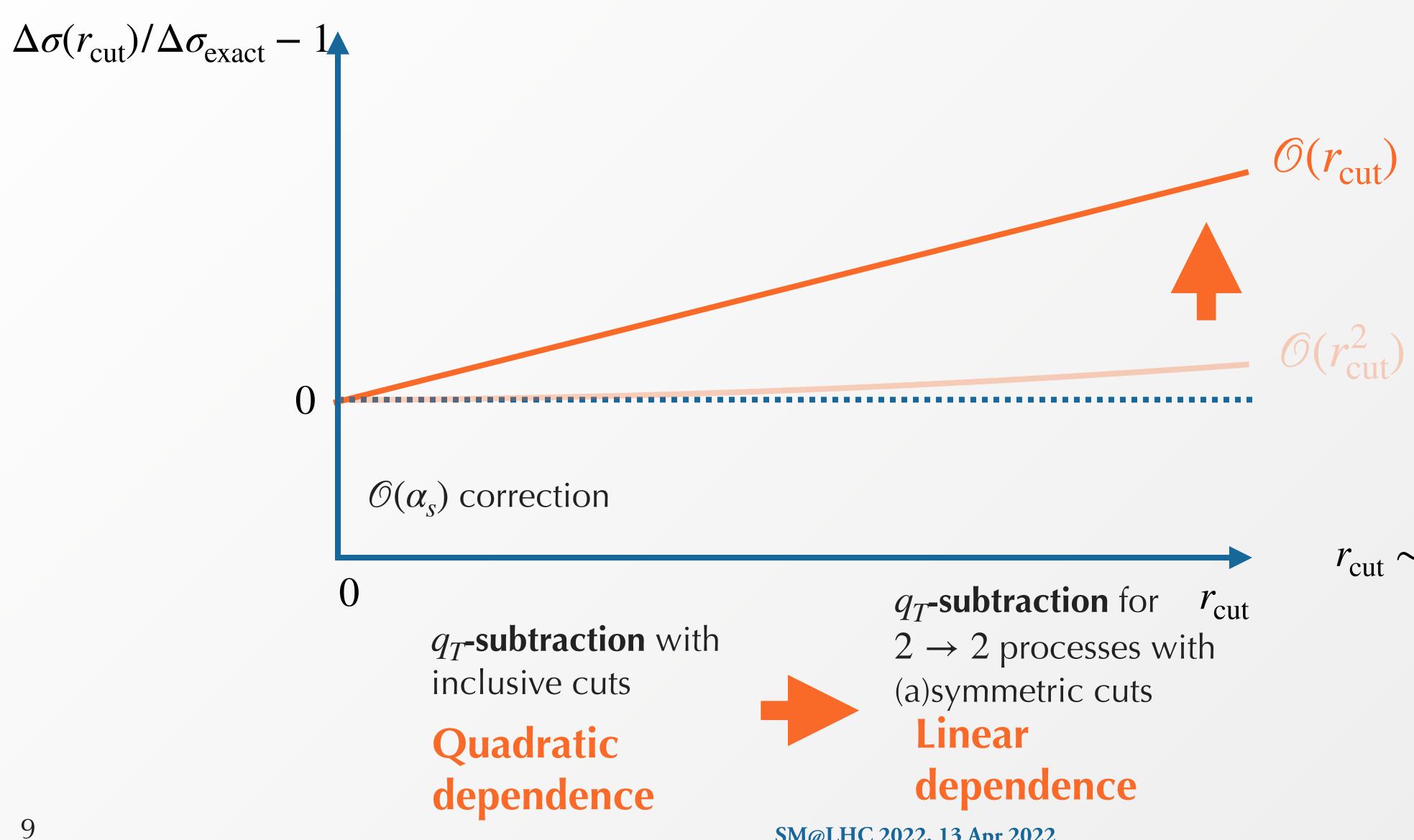
$$\left[d\sigma_{V}^{N^{3}LL}\right]_{\mathcal{O}(\alpha_{s}^{3})} \bigoplus \Theta(p_{T} > p_{T}^{cut}) + \mathcal{O}((p_{T}^{cut}/M)^{n})$$
Missing power corrections
below the slicing out off

below the slicing cut-on





 $r_{\rm cut} \sim p_T/Q$



 $r_{\rm cut} \sim p_T/Q$

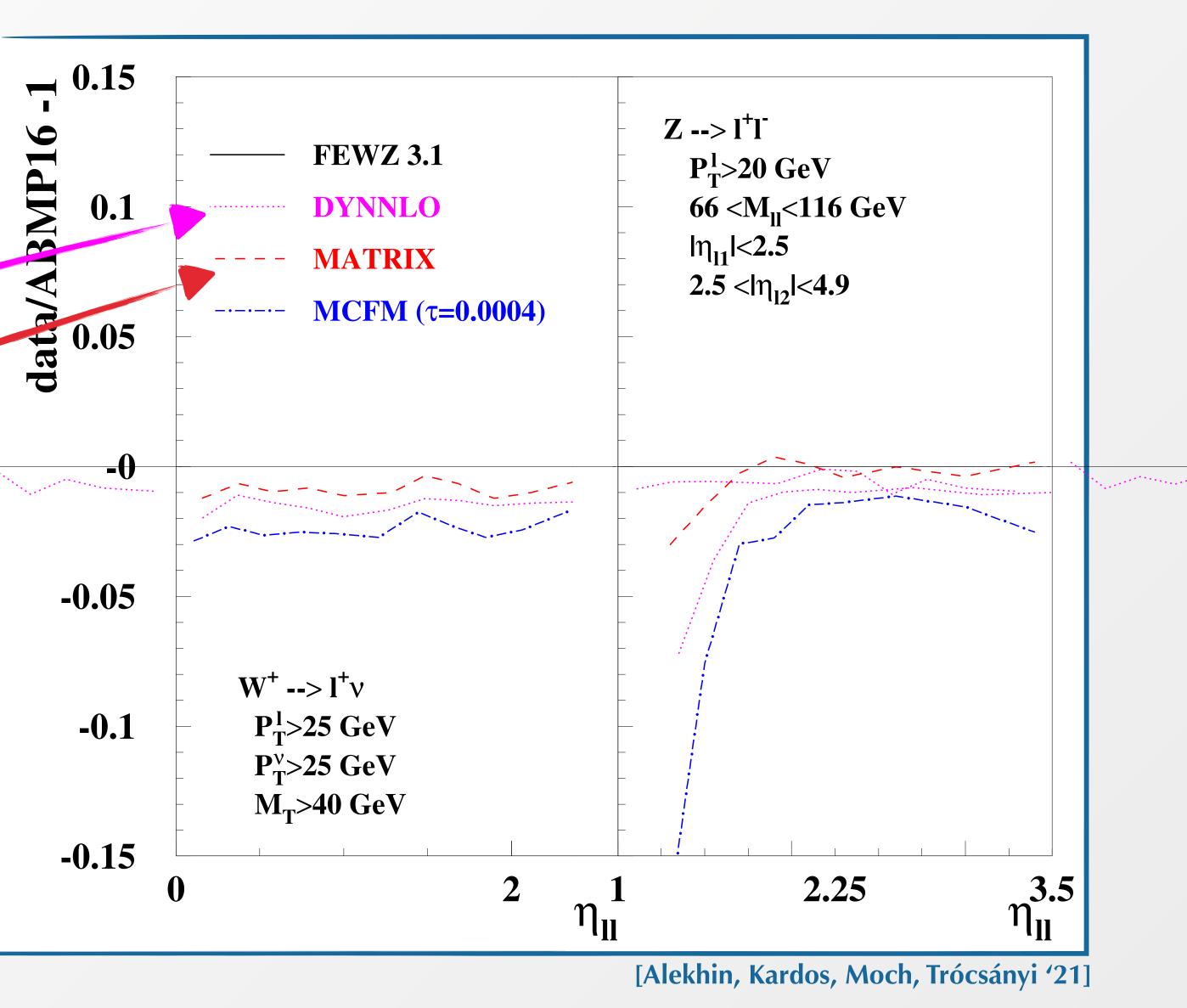
Perturbative convergence within fiducial cuts

Values of $r_{\rm cut} \sim p_T/Q$ too large, or lack of extrapolation to $r_{\rm cut} \rightarrow 0$, can lead to percent-level effects when compared to results obtained with local subtractions



$r_{\rm cut} \sim 0.0005 - 0.001$

Can this situation be improved?



Perturbative convergence within fiducial cuts

Values of $r_{\rm cut} \sim p_T/Q$ too large, or lack of extrapolation to $r_{\rm cut} \rightarrow 0$, can lead to percent-level effects when compared to results obtained with local subtractions



Can this situation be improved?

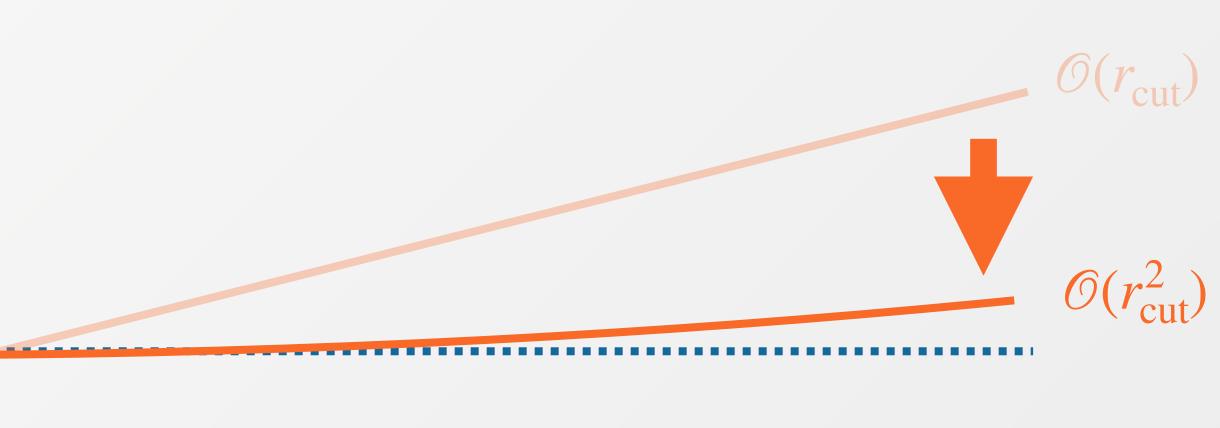
Yes! For $2 \rightarrow 2$ **processes with** (a)symmetric cuts, fiducial linear power corrections can be calculated via a simple recoil prescription

[Catani, de Florian, Ferrera, Grazzini '15] [Ebert, Michel, Stewart, Tackmann '20]

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0

0



 $\mathcal{O}(\alpha_{\rm s})$ correction

r_{cut}



Resorting to the recoil prescription allows for the inclusion of all missing fiducial linear power corrections below p_T^{cut} , improving dramatically the efficiency of the non-local subtraction[Buonocore, Kallweit, LR, Wiesemann'21][Camarda, Cieri, Ferrera '21]

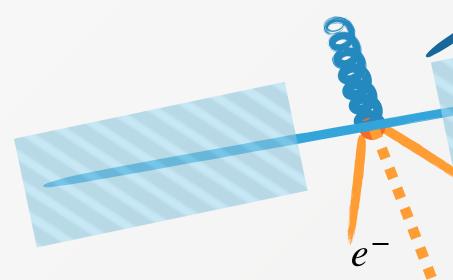
$$d\sigma_{V}^{N^{3}LO} \equiv \mathscr{H}_{V}^{N^{3}LO} \otimes d\sigma_{V}^{LO} + \left(d\sigma_{V+jet}^{NNLO} - \left[d\sigma_{V}^{N^{3}LL} \right]_{\mathcal{O}(\alpha_{s}^{3})} \right) \Theta(p_{T} > p_{T}^{eut}) + \Delta\sigma^{linPCs}(p_{T}^{eut}) + \mathcal{O}((p_{T}^{eut}/M))$$

$$\Delta\sigma^{linPCs}(p_{T}^{eut}) = \int_{0}^{r_{eut}} dr' \left[d\sigma_{V}^{N^{3}LL} \right]_{\mathcal{O}(\alpha_{s}^{3})} \left(\Theta_{euts}^{recoil} - \Theta_{euts}^{Born} \right)$$

$$e^{+}$$

$$\Delta \sigma^{\text{linPCs}}(p_T^{\text{cut}}) = \int_0^{r_{\text{cut}}} dr' [d\sigma_V^{\text{N}^3\text{LL}}]_{\mathcal{O}(\alpha_s^3)} \Theta(p_T > p_T^{\text{cut}}) + \Delta \sigma^{\text{linPCs}}(p_T^{\text{cut}}) + \mathcal{O}((p_T^{\text{cut}}/M))$$

$$\Delta \sigma^{\text{linPCs}}(p_T^{\text{cut}}) = \int_0^{r_{\text{cut}}} dr' [d\sigma_V^{\text{N}^3\text{LL}}]_{\mathcal{O}(\alpha_s^3)} \Theta^{\text{recoil}} - \Theta_{\text{cuts}}^{\text{Born}} - \Theta_{\text{cuts}}^{\text{Born}} + e^+$$



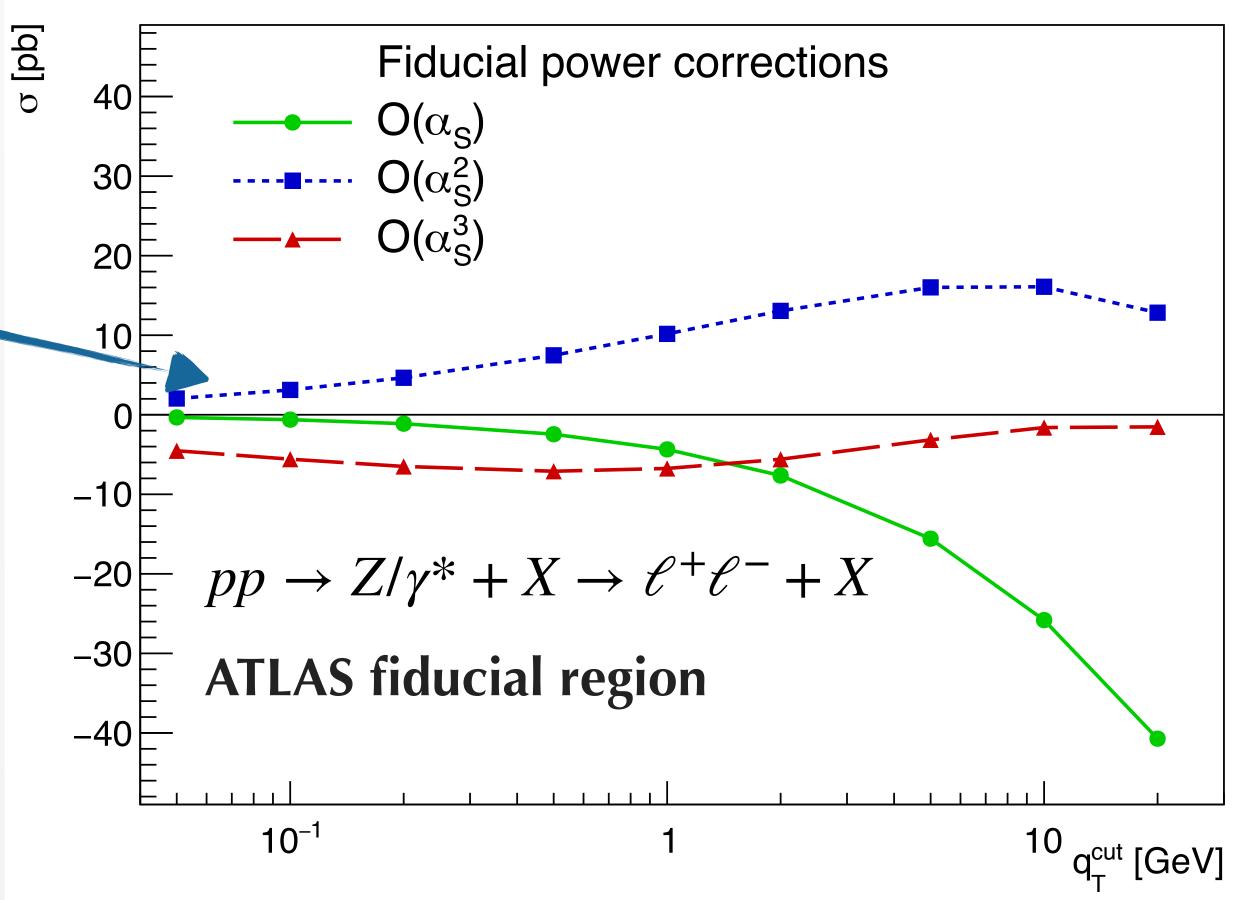
Linear power corrections have a purely kinematical origin and can be predicted by factorisation



$\Delta \sigma^{\text{linPCs}}(p_T^{\text{cut}}) = \int_0^{r_{\text{cut}}} dr' \left[d\sigma_V^{\text{N^3LL}} \right]_{\mathcal{O}(\alpha_s^3)} (\Theta_{\text{cuts}}^{\text{recoil}} - \Theta_{\text{cuts}}^{\text{Born}})$

No sign of perturbative convergence in the size of linear power corrections

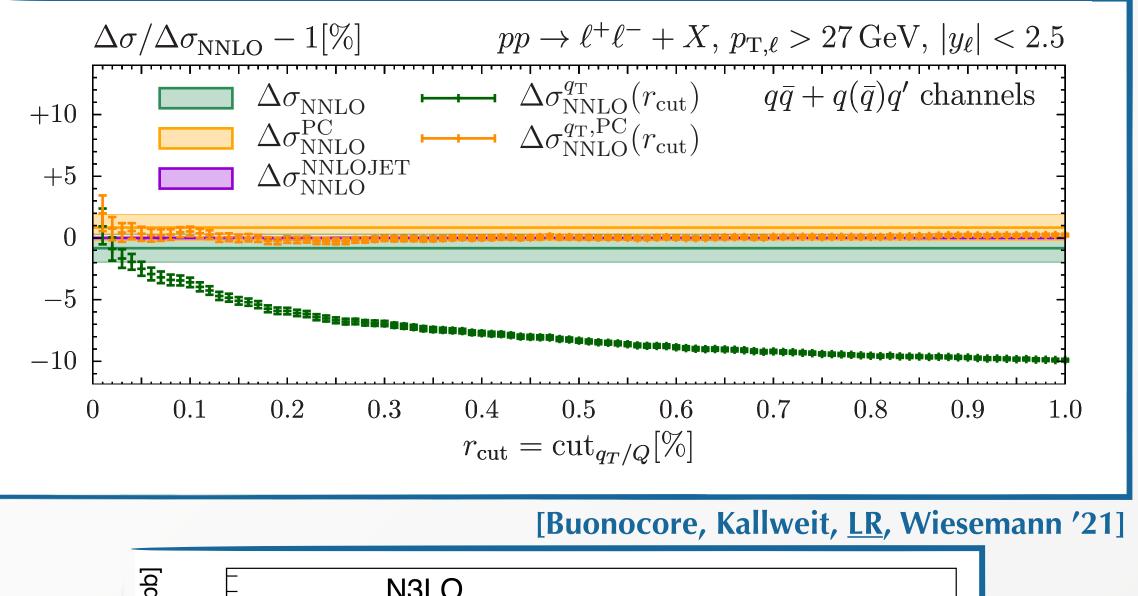


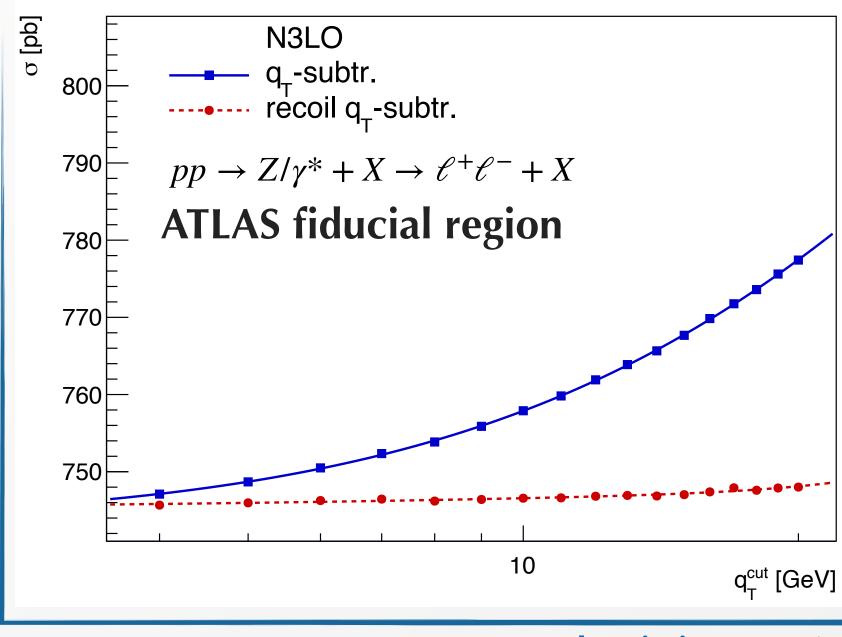


[Camarda, Cieri, Ferrera '21]



Linear power corrections for q_T -subtraction





[Camarda, Cieri, Ferrera '21] SM@LHC 2022, 13 Apr 2022

Much improved convergence over linear power correction case

Accurate computation of the NNLO correction without the need to push $r_{\rm cut}$ to very low values

Nice agreement up to NNLO with NNLOJET, which uses a local subtraction method

Now available in the new public version of MATRIX 2.1

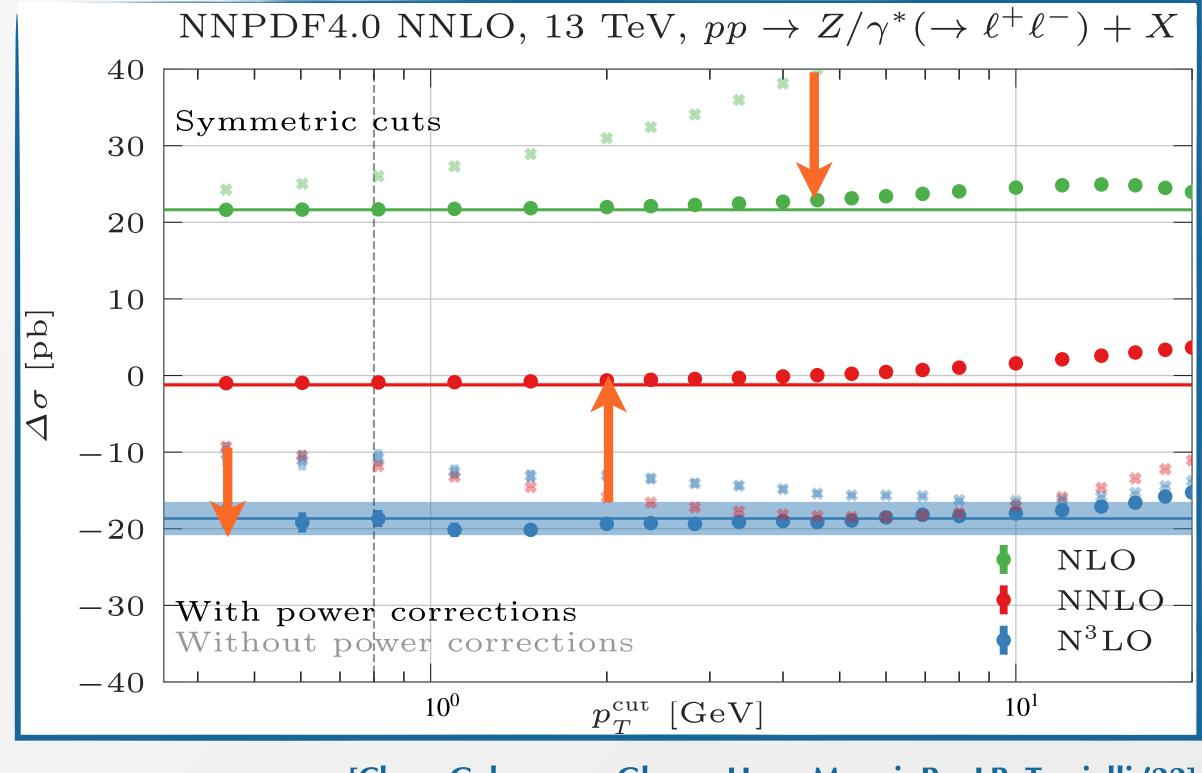
Resorting to this prescription allows one to obtain predictions at N³LO with q_T slicing

The Drell-Yan fiducial cross section at N³LO

ATLAS fiducial region

- Exquisite control on the **fixed order component** (from NNLOJET) allows to push to low values of the slicing parameter p_T^{cut}
- Mandatory to include missing linear **power** corrections to reach a precise control of the **N**^k**LO correction** down to small values of p_T^{cut}
- Plateau at small p_T^{cut} indicates the desired independence of the slicing parameter
- Result without power correction does not converge yet to the correct value at N^kLO

 $p_T^{\ell^{\pm}} > 27 \,\text{GeV} \qquad |\eta^{\ell^{\pm}}| < 2.5$ $d\sigma_V^{N^3LO} \equiv \mathscr{H}_V^{N^3LO} \otimes d\sigma_V^{LO} + \left(\frac{d\sigma_{V+jet}^{NNLO} - \left[d\sigma_V^{N^3LL} \right]_{\mathcal{O}(\alpha_s^k)} \right) \Theta(p_T > p_T^{cut}) + \mathcal{O}((p_T^{cut}/M)^n)$



[Chen, Gehrmann, Glover, Huss, Monni, Re, <u>LR</u>, Torrielli '22]

The Drell-Yan fiducial cross section at N³LO

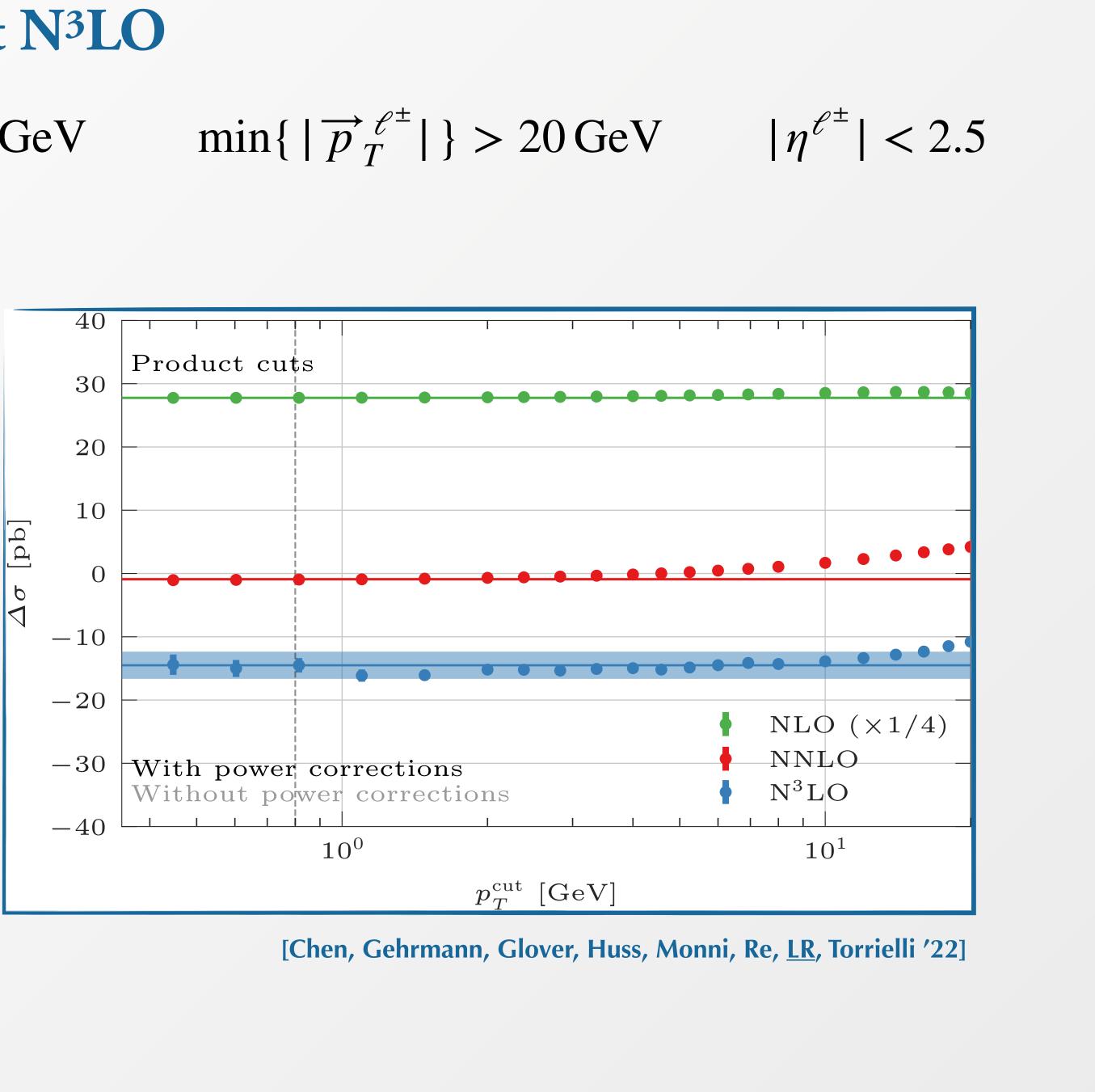
Product cuts [Salam, Slade '21]

 $\sqrt{|\overrightarrow{p}_T^{\ell^+}||\overrightarrow{p}_T^{\ell^-}|} > 27 \,\text{GeV}$

• Alternative set of cuts which does not suffer from linear power corrections

• Improved convergence, result independent of the recoil procedure

$\min\{|\overrightarrow{p}_T^{\ell^{\pm}}|\} > 20 \,\text{GeV}$

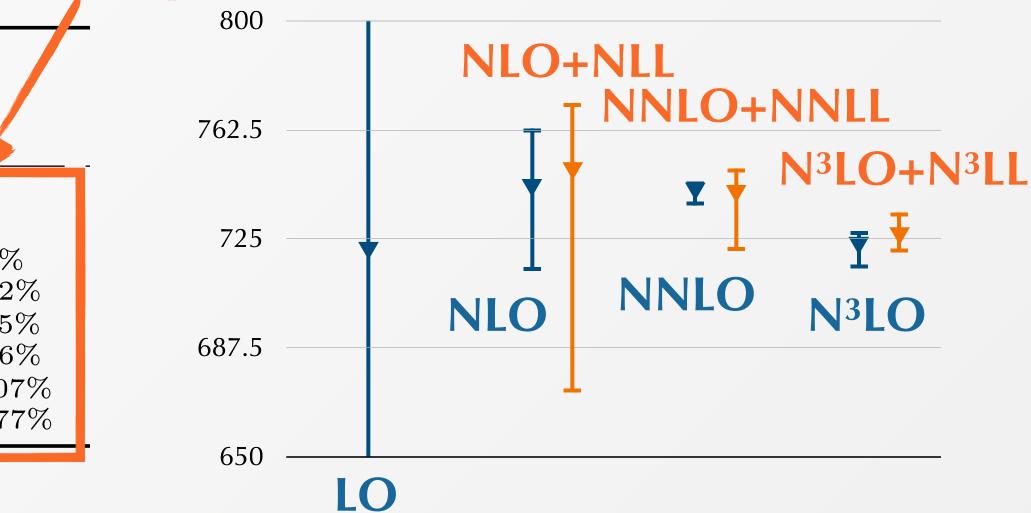


The Drell-Yan fiducial cross section at N³LO and N³LO+N³LL [Chen, Gehrmann, Glover, Huss, Monni, Re, LR, Torrielli '22]

Includes resummation of linear power corrections

	Order	σ [pb] Symmetric cuts	
	k	$N^k LO$	N^kLO+N^kLL
	0	$721.16^{+12.2\%}_{-13.2\%}$	
	1	$742.80(1)^{+2.7\%}_{-3.9\%}$	$748.58(3)^{+3.1\%}_{-10.29}$
	2	$741.59(8)^{+0.42\%}_{-0.71\%}$	$740.75(5)^{+1.15}_{-2.66}$
$q_T^{\rm cut} = 0.8 {\rm GeV}$	3	$722.9(1.1)^{+0.68\%}_{-1.09\%}\pm 0.9$	$748.58(3)^{+3.1\%}_{-10.2}$ $740.75(5)^{+1.159}_{-2.66}$ $726.2(1.1)^{+1.07}_{-0.77}$

- 2.5% negative correction at N³LO in the ATLAS fiducial region. N³LO larger than the NNLO correction and outside its error band
- interval



• More robust estimate of the theory uncertainty when resummation effects are included

• Slicing error computed conservatively by considering the cutoff within the [0.45-1.5] GeV

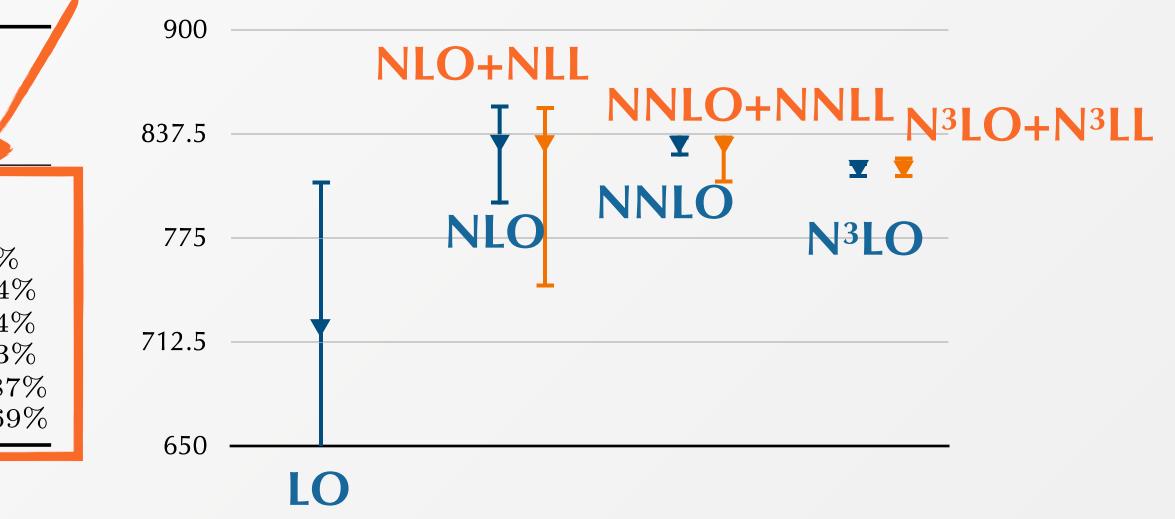
The Drell-Yan fiducial cross section at N³LO and N³LO+N³LL

Includes resummation of linear power corrections

	Order	σ [pb] Product cuts	
	k	$N^k LO$	N ^k LO+N ^k LL
	0	$721.16^{+12.2\%}_{-13.2\%}$	
	1	$832.22(1)^{+2.7\%}_{-4.5\%}$	$831.91(2)^{+2.7\%}_{-10.4\%}$
	2	$831.32(3)^{+0.59\%}_{-0.96\%}$	$830.98(4)^{+0.749}_{-2.739}$
$q_T^{\rm cut} = 0.8 {\rm GeV}$	3	$816.8(1.1)^{+0.45\%}_{-0.73\%} \pm 0.8$	$831.91(2)^{+2.7\%}_{-10.4\%}$ $830.98(4)^{+0.74\%}_{-2.73\%}$ $816.6(1.1)^{+0.87}_{-0.6\%}$

- 2.5% negative correction at N³LO in the ATLAS fiducial region. N³LO larger than the NNLO correction and outside its error band
- interval
- absence of linear power corrections

[Chen, Gehrmann, Glover, Huss, Monni, Re, LR, Torrielli '22]

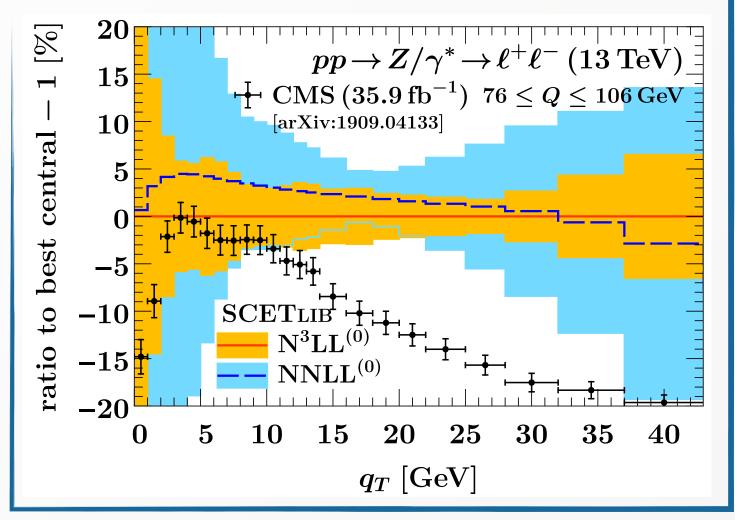


• More robust estimate of the theory uncertainty when **resummation effects are included**

• Slicing error computed conservatively by considering the cutoff within the [0.45-1.5] GeV

• Central value very similar at N^kLO and N^kLO+N^kLL for product cuts, compatible with the

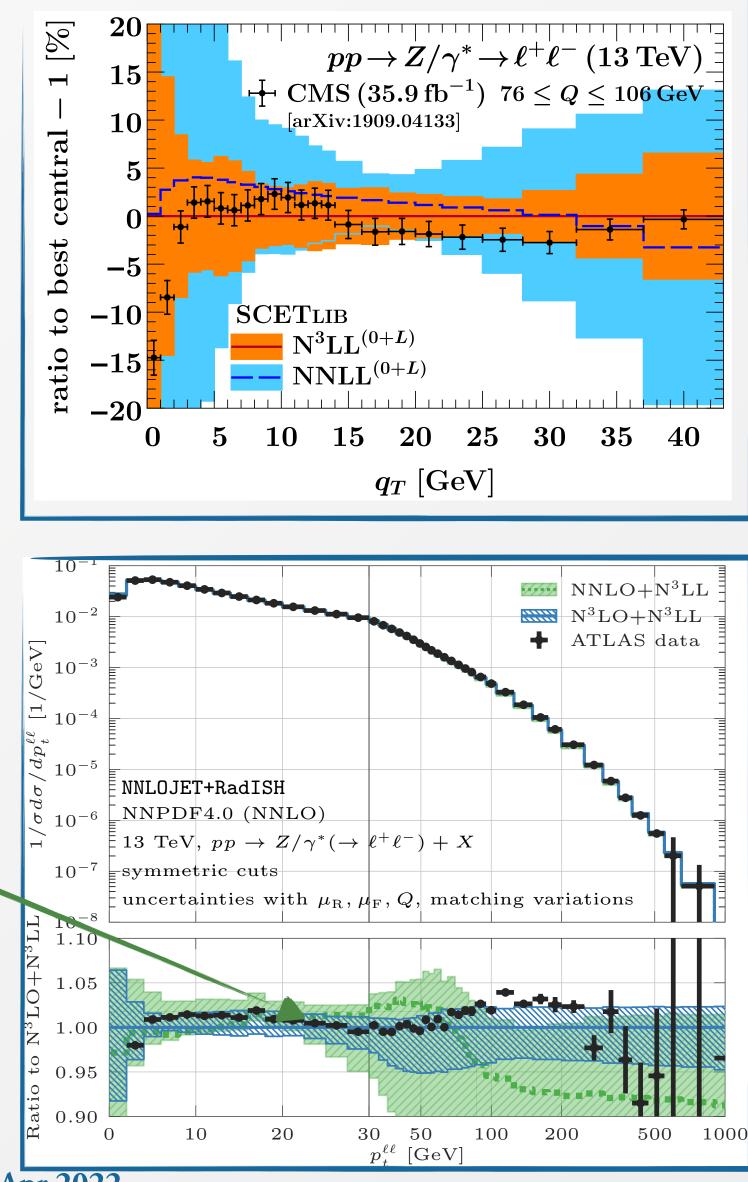
Transverse momentum resummation and power corrections



[Ebert, Michel, Stewart, Tackmann '20]

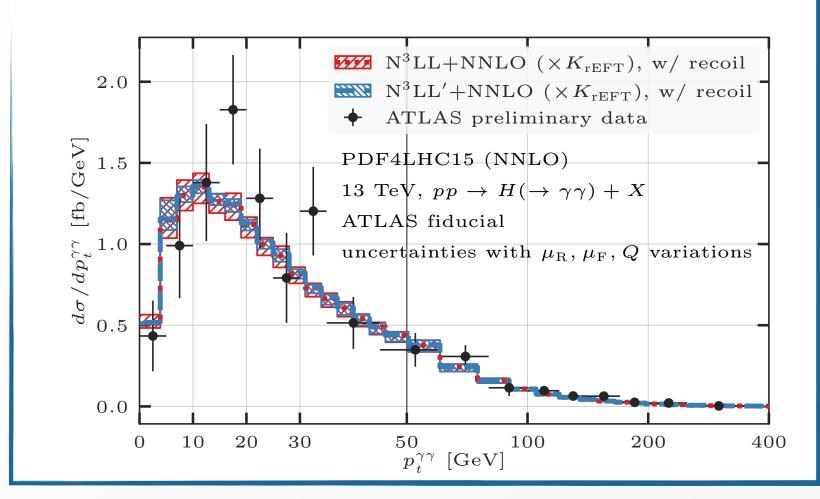
However, effect of higher-order power correction from fixed-order corrections has 1-3% effect even at low values of the transverse momentum [Chen, Gehrmann, Glover, Huss, Monni, Re, <u>LR</u>, Torrielli '22] Fixed order matching at small values of transverse momentum essential for applications in **Drell-Yan precision physics** (PDF, α_s extraction, ...)

Resummation of **linear power corrections** captures the bulk of the non-singular component at low values of p_T

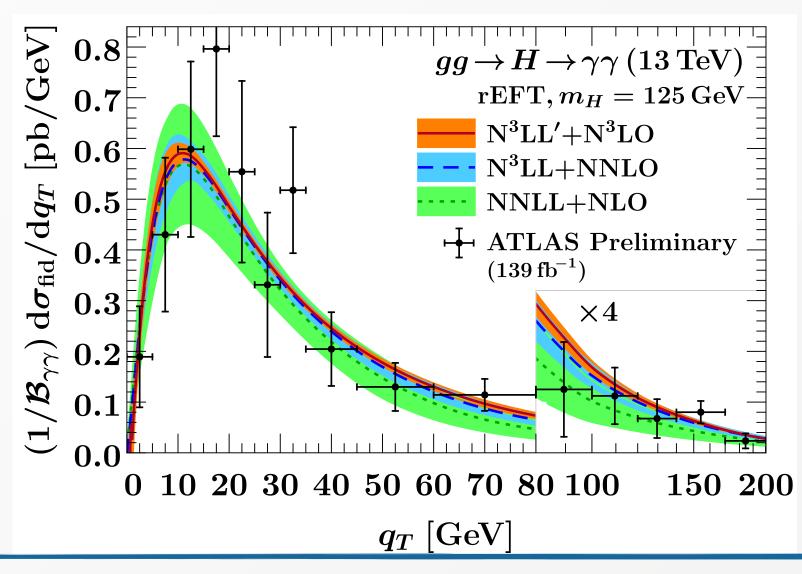


Transverse momentum resummation at NNLO+N³LL

Higgs production



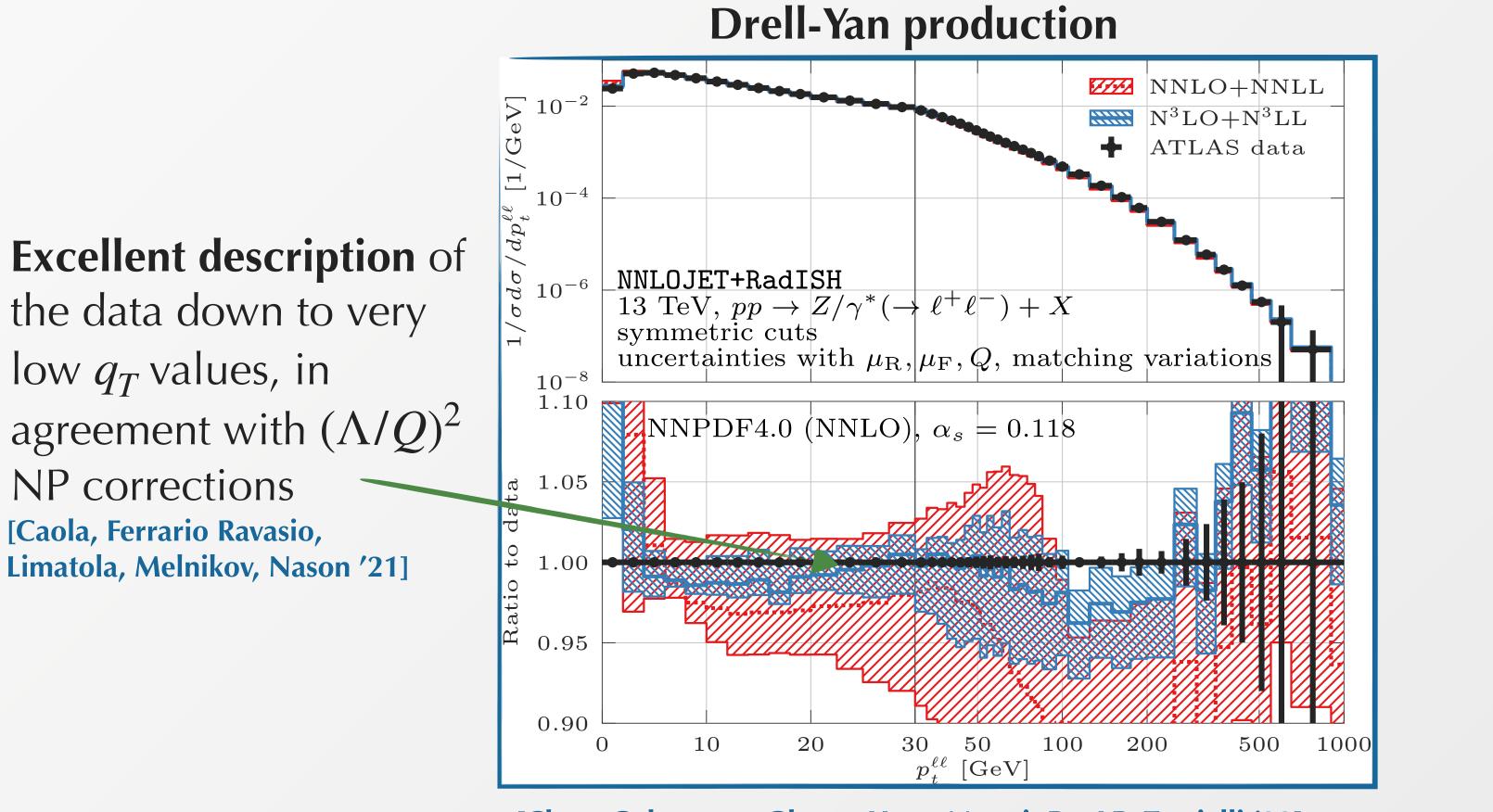
[Re, <u>LR</u>, Torrielli '21]



the data down to very low q_T values, in NP corrections [Caola, Ferrario Ravasio, Limatola, Melnikov, Nason '21]

[Billis, Dehnadi, Ebert, Michel, Stewart, Tackmann '21]

NNLO+N³LL description allows for a **very** precise description of experimental data across the whole transverse momentum spectrum both in Drell-Yan and Higgs production

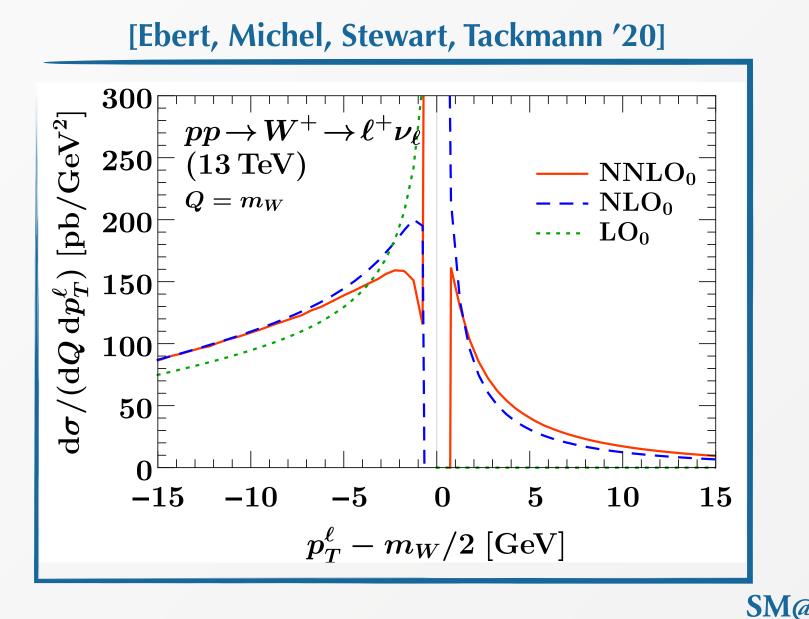


[Chen, Gehrmann, Glover, Huss, Monni, Re, <u>LR</u>, Torrielli '22] See also J. Michel's talk for preliminary SCETLib results

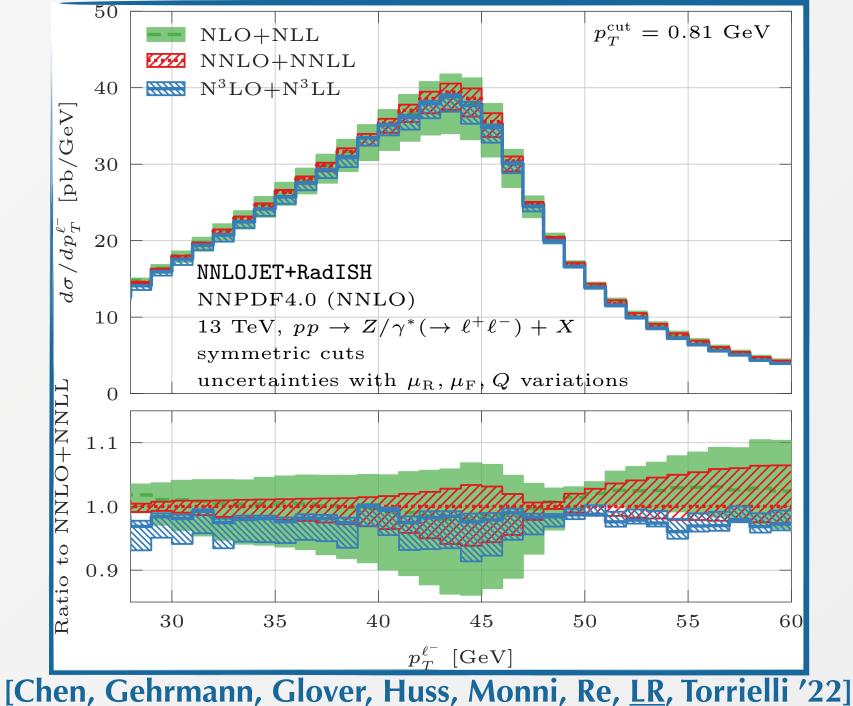


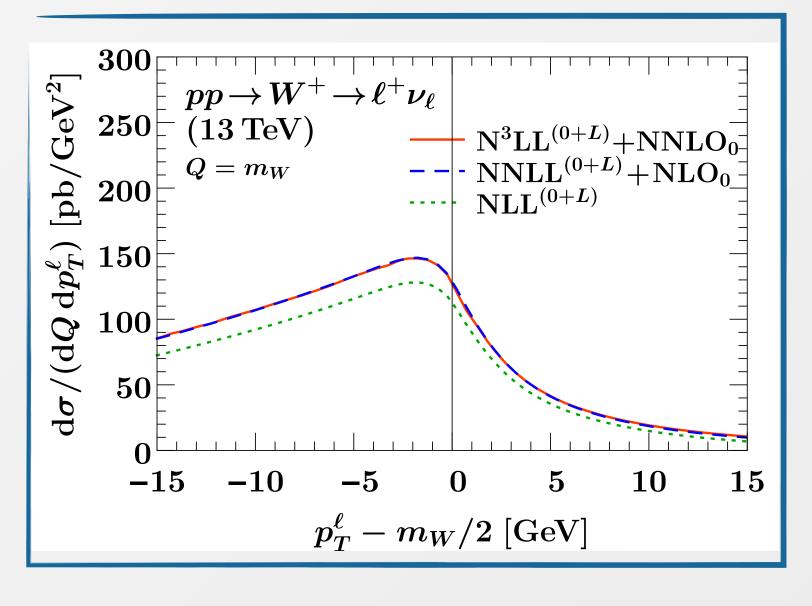
Fiducial distributions and transverse momentum resummation

- Transverse momentum resummation affects observables sensitive to soft gluon emission as the lepton transverse momentum in Drell-Yan [Balázs, Yuan '97] [Catani, de Florian, Ferrera, Grazzini '15]
- Leptonic transverse momentum is a particularly relevant observable due to its importance in the extraction of the W mass
- Inclusion of resummation effects necessary to cure (integrable) divergences due to the presence of a **Sudakov shoulder** at $m_{ee}/2$
- NB: **EW corrections** also relevant for correct shape See A. Vicini's and C. Schwan talks



[Catani, Webber '97]







Summary

- diphotons) cause **undesired instabilities** in fixed-order perturbation theory
- **fixed order predictions** for practical applications (e.g. PDF extraction)
- N³LO accuracy for key processes (e.g. **fiducial DY production**)
- power corrections
- **Resummation of linear fiducial power corrections** can be performed alongside q_T -resummation to provide reliable all-order results for legacy measurements
- Robustness of data-theory comparison within fiducial regions require rethinking of fiducial acceptances for future LHC measurements in run 3

• Fiducial cuts currently applied in experimental analyses in two-body final states (Drell-Yan, Higgs to

• **Resummation** provides a viable solution for legacy measurements. Robust physical results also require

• Sensitivity to unresolved region challenges non-local subtraction methods, which are widely used in data-theory comparison at NNLO (e.g. MATRIX, MCFM) or are currently the only viable method to get to

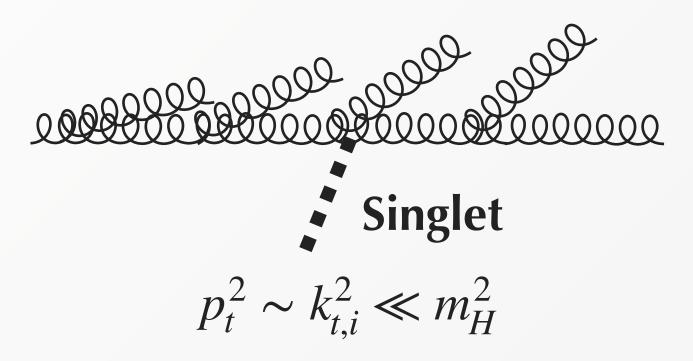
• Reliable results up to N³LO can be obtained using q_T -subtraction methods by computing fiducial linear



Resummation of the transverse momentum spectrum

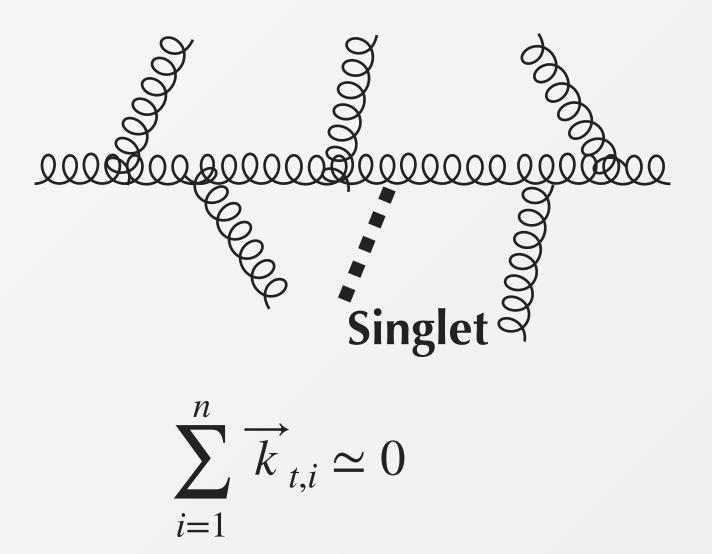
Resummation of transverse momentum is delicate because p_t is a vectorial quantity

Two concurring mechanisms leading to a system with small *p*_t



cross section naturally suppressed as there is no phase space left for gluon emission (Sudakov limit)

Exponential suppression



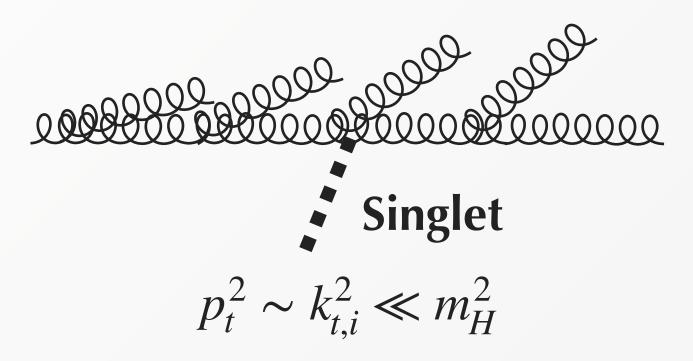
Large kinematic cancellations *p*_t ~0 far from the Sudakov limit

Power suppression

Resummation of the transverse momentum spectrum

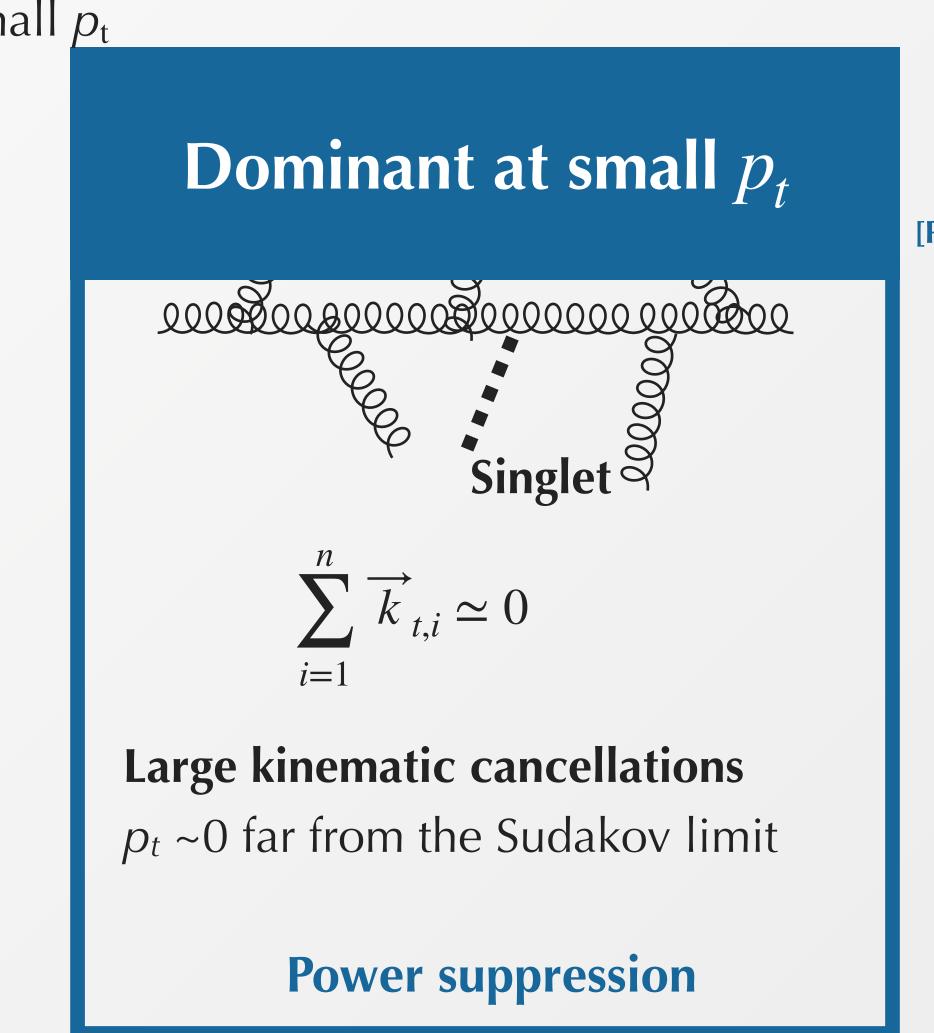
Resummation of transverse momentum is delicate because p_t is a vectorial quantity

Two concurring mechanisms leading to a system with small *p*_t



cross section naturally suppressed as there is no phase space left for gluon emission (Sudakov limit)

Exponential suppression



[Parisi, Petronzio, '79]



Resummation of the transverse momentum spectrum in b space

two-dimensional momentum conservation $\delta^{(2)} \left(\overrightarrow{p}_t - \right)$

Expo

onentiation in conjugate space

$$\sigma = \sigma_0 \int d^2 \overrightarrow{p}_{\perp}^H \int \frac{d^2 \overrightarrow{b}}{4\pi^2} e^{-i \overrightarrow{b} \cdot \overrightarrow{p}_{\perp}^H} \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=1}^n \int [dk_i] |M(k_i)|^2 \left(e^{i \overrightarrow{b} \cdot \overrightarrow{k}_{i,i}} - 1 \right) = \sigma_0 \int d^2 \overrightarrow{p}_{\perp}^H \int \frac{d^2 \overrightarrow{b}}{4\pi^2} e^{-i \overrightarrow{b} \cdot \overrightarrow{p}_{\perp}^H} e^{-k}$$

 $L = \ln(m_H b/b_0)$ $R_{\rm NLL}(L) = -Lg_1(\alpha_s L) - g_2(\alpha_s L)$

Logarithmic accuracy defined in terms of $\ln(m_H b/b_0)$

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$$\left(\sum_{i=1}^{n} \overrightarrow{k}_{t,i}\right) = \int d^{2}b \frac{1}{4\pi^{2}} e^{i\overrightarrow{b}} \cdot \overrightarrow{p}_{t} \prod_{i=1}^{n} e^{-i\overrightarrow{b}} \cdot \overrightarrow{k}_{t,i}$$

NLL formula with scale-independent PDFs

Talk by Ignazio Scimemi





Now include effect of **collinear radiation** and terms beyond NLL accuracy

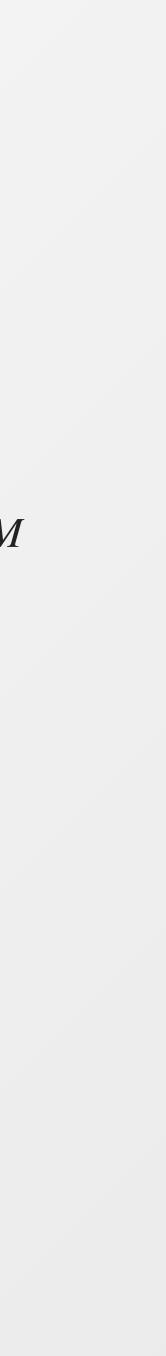
$$\frac{d\Sigma(v)}{d\Phi_B} = \int_{\mathscr{C}_1} \frac{dN_1}{2\pi i} \int_{\mathscr{C}_2} \frac{dN_2}{2\pi i} x_1^{-N_1} x_2^{-N_2} \sum_{c_1,c_2} \frac{d|M_B|_{c_1c_2}^2}{d\Phi_B} \mathbf{f}_{N_1}^T(\mu_0) \hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) \mathbf{f}_{N_2}(\mu_0),$$

$$\begin{split} \hat{\Sigma}_{N_{1},N_{2}}^{c_{1},c_{2}}(v) &= \left[\mathbf{C}_{N_{1}}^{c_{1};T}(\alpha_{s}(\mu_{0}))H(\mu_{R})\mathbf{C}_{N_{2}}^{c_{2}}(\alpha_{s}(\mu_{0})) \right] \int_{0}^{M} \frac{dk_{t1}}{k_{t1}} \int_{0}^{2\pi} \frac{d\phi_{1}}{2\pi} e^{-\mathbf{R}(\varepsilon k_{t1})} \\ &\times \exp\left\{ -\sum_{\ell=1}^{2} \left(\int_{\varepsilon k_{\ell}}^{\mu_{0}} \frac{dk_{t}}{k_{t}} \frac{\alpha_{s}(k_{t})}{\pi} \mathbf{\Gamma}_{N_{\ell}}(\alpha_{s}(k_{t})) + \int_{\varepsilon k_{\ell}}^{\mu_{0}} \frac{dk_{t}}{k_{t}} \mathbf{\Gamma}_{N_{\ell}}^{(C)}(\alpha_{s}(k_{t})) \right) \right\} \\ &\times \sum_{\ell_{1}=1}^{2} \left(\mathbf{R}_{\ell_{1}}'\left(k_{t1}\right) + \frac{\alpha_{s}(k_{t1})}{\pi} \mathbf{\Gamma}_{N_{\ell_{1}}}(\alpha_{s}(k_{t1})) + \mathbf{\Gamma}_{N_{\ell_{1}}}^{(C)}(\alpha_{s}(k_{t1})) \right) \right) \\ &\times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\varepsilon}^{1} \frac{d\zeta_{i}}{\zeta_{i}} \int_{0}^{2\pi} \frac{d\phi_{i}}{2\pi} \Theta\left(v - V(\{\tilde{p}\}, k_{1}, \dots, k_{n+1})\right), \\ &\times \sum_{\ell_{i}=1}^{2} \left(\mathbf{R}_{\ell_{i}}'\left(k_{ti}\right) + \frac{\alpha_{s}(k_{ti})}{\pi} \mathbf{\Gamma}_{N_{\ell_{i}}}(\alpha_{s}(k_{ti})) + \mathbf{\Gamma}_{N_{\ell_{i}}}^{(C)}(\alpha_{s}(k_{ti})) \right) \end{split}$$

[Bizon, Monni, Re, LR, Torrielli '17] [Re, LR, Torrielli '21]

Unresolved

 $v = p_t/M$



Now include effect of **collinear radiation** and terms beyond NLL accuracy

$$\frac{d\Sigma(v)}{d\Phi_B} = \int_{\mathscr{C}_1} \frac{dN_1}{2\pi i} \int_{\mathscr{C}_2} \frac{dN_2}{2\pi i} x_1^{-N_1} x_2^{-N_2} \sum_{c_1,c_2} \frac{d|M_B|_{c_1c_2}^2}{d\Phi_B} \mathbf{f}_{N_1}^T(\mu_0) \hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) \mathbf{f}_{N_2}(\mu_0),$$

Sudakov radiator

$$\hat{\Sigma}_{N_{1},N_{2}}^{c_{1}c_{2}}(v) = \left[C_{N_{1}}^{c_{1}T}(\alpha_{s}(\mu_{0}))H(\mu_{R})C_{N_{2}}^{c_{2}}(\alpha_{s}(\mu_{0}))\right] \int_{0}^{M} \frac{dk_{t1}}{k_{t1}} \int_{0}^{2\pi} \frac{d\phi_{1}}{2\pi} e^{-\mathbf{R}(\epsilon k_{n})}$$

$$R(k_{t1}) = -\log \frac{M}{k_{t1}}g_{1} - g_{2} - \left(\frac{\alpha_{s}}{\pi}\right)g_{3} - \left(\frac{\alpha_{s}}{\pi}\right)^{2}g_{4} - \left(\frac{\alpha_{s}}{\pi}\right)^{3}g_{5} \qquad \times \exp\left\{-\sum_{\ell'=1}^{2}\left(\int_{ck_{1}}^{\mu_{0}} \frac{dk_{1}}{k_{1}}\frac{\alpha_{s}(k_{1})}{\pi}\Gamma_{N_{\ell}}(\alpha_{s}(k_{1})) + \int_{ck_{n}}^{\mu_{0}} \frac{dk_{1}}{k_{1}}\Gamma_{N_{\ell}}^{(C)}(\alpha_{s}(k_{1}))\right)\right\}$$
Resummation scale $Q \sim M$

$$\sum_{\ell'=1}^{2}\left(\mathbf{R}_{\ell_{1}}^{\prime}(k_{t1}) + \frac{\alpha_{s}(k_{1})}{\pi}\Gamma_{N_{\ell_{1}}}(\alpha_{s}(k_{1})) + \Gamma_{N_{\ell_{1}}}^{(C)}(\alpha_{s}(k_{1}))\right)$$

$$\ln \frac{M}{k_{t1}} \rightarrow \ln \frac{Q}{k_{t1}} + \ln \frac{M}{Q} \qquad \qquad \times \sum_{n=0}^{2}\frac{1}{n!}\prod_{i=2}^{n+1}\int_{c}^{1}\frac{d\zeta_{i}}{\zeta_{i}}\int_{0}^{2\pi}\frac{d\phi_{i}}{2\pi}\Theta\left(v - V(\{\bar{p}\}, k_{1}, \dots, k_{n+1})\right),$$
Constant terms expanded in α_{s} and included in H

$$\times \sum_{\ell'=1}^{2}\left(\mathbf{R}_{\ell_{1}}^{\prime}(\mathbf{k}_{\ell_{1}}) + \frac{\alpha_{s}(k_{n})}{\pi}\Gamma_{N_{\ell_{1}}}(\alpha_{s}(k_{n})) + \Gamma_{N_{\ell_{1}}}^{(C)}(\alpha_{s}(k_{n}))\right)$$

$$\ln \frac{M}{k_{t1}} \to \ln \frac{Q}{k_{t1}} + \ln \frac{M}{Q}$$

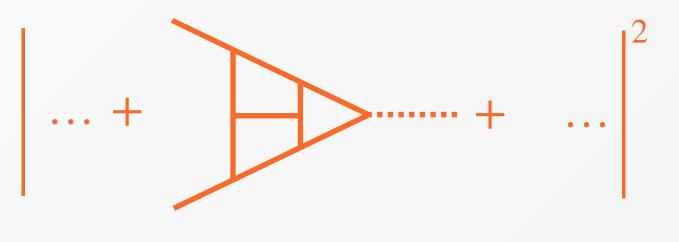
[Bizon, Monni, Re, LR, Torrielli '17] [Re, LR, Torrielli '21]



Now include effect of **collinear radiation** and terms beyond NLL accuracy

Three-loop hard-virtual coefficient

$$H(\alpha_s) = 1 + \left(\frac{\alpha_s}{2\pi}\right) H_1 + \left(\frac{\alpha_s}{2\pi}\right)^2 H_2 + \left(\frac{\alpha_s}{2\pi}\right)^3 H_3$$



[Gehrmann et al. '10]

[Bizon, Monni, Re, LR, Torrielli '17] [Re, LR, Torrielli '21]

$$\frac{d\Sigma(v)}{d\Phi_B} = \int_{\mathscr{C}_1} \frac{dN_1}{2\pi i} \int_{\mathscr{C}_2} \frac{dN_2}{2\pi i} x_1^{-N_1} x_2^{-N_2} \sum_{c_1,c_2} \frac{d|M_B|_{c_1c_2}^2}{d\Phi_B} \mathbf{f}_{N_1}^T(\mu_0) \hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) \mathbf{f}_{N_2}(\mu_0),$$

$$\begin{split} \hat{\Sigma}_{N_{1},N_{2}}^{c_{1},c_{2}}(v) &= \left[\mathbf{C}_{N_{1}}^{c_{1};T}(\alpha_{s}(\mu_{0})) \boldsymbol{H}(\boldsymbol{\mu_{R}}) \mathbf{C}_{N_{2}}^{c_{2}}(\alpha_{s}(\mu_{0})) \right] \int_{0}^{M} \frac{dk_{t1}}{k_{t1}} \int_{0}^{2\pi} \frac{d\phi_{1}}{2\pi} e^{-\mathbf{R}(\epsilon k_{t1})} \\ &\times \exp\left\{ -\sum_{\ell=1}^{2} \left(\int_{\epsilon k_{t1}}^{\mu_{0}} \frac{dk_{t}}{k_{t}} \frac{\alpha_{s}(k_{t})}{\pi} \Gamma_{N_{\ell}}(\alpha_{s}(k_{t})) + \int_{\epsilon k_{t1}}^{\mu_{0}} \frac{dk_{t}}{k_{t}} \Gamma_{N_{\ell}}^{(C)}(\alpha_{s}(k_{t})) \right) \\ &\times \sum_{\ell=1}^{2} \left(\mathbf{R}_{\ell_{1}}'\left(k_{t1}\right) + \frac{\alpha_{s}(k_{t1})}{\pi} \Gamma_{N_{\ell_{1}}}(\alpha_{s}(k_{t1})) + \Gamma_{N_{\ell_{1}}}^{(C)}(\alpha_{s}(k_{t1})) \right) \\ &\times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\epsilon}^{1} \frac{d\zeta_{i}}{\zeta_{i}} \int_{0}^{2\pi} \frac{d\phi_{i}}{2\pi} \Theta\left(v - V(\{\tilde{p}\}, k_{1}, \dots, k_{n+1})\right), \\ &\times \sum_{\ell=1}^{2} \left(\mathbf{R}_{\ell_{i}}'\left(k_{ti}\right) + \frac{\alpha_{s}(k_{ti})}{\pi} \Gamma_{N_{\ell_{i}}}(\alpha_{s}(k_{ti})) + \Gamma_{N_{\ell_{i}}}^{(C)}(\alpha_{s}(k_{ti})) \right) \end{split}$$



Now include effect of **collinear radiation** and terms beyond NLL accuracy

$$C(\alpha_s, z) = \delta(1-z) + \left(\frac{\alpha_s}{2\pi}\right)C_1(z) + \left(\frac{\alpha_s}{2\pi}\right)^2 C_2(z) + \left(\frac{\alpha_s}{2\pi}\right)^3 C_3(z)$$

[Li, Zhu '16][Vladimirov '16][Luo et al. '19][Ebert et al. '20]

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[Bizon, Monni, Re, LR, Torrielli '17] [Re, LR, Torrielli '21]

$$\frac{d\Sigma(v)}{d\Phi_B} = \int_{\mathscr{C}_1} \frac{dN_1}{2\pi i} \int_{\mathscr{C}_2} \frac{dN_2}{2\pi i} x_1^{-N_1} x_2^{-N_2} \sum_{c_1,c_2} \frac{d|M_B|_{c_1c_2}^2}{d\Phi_B} \mathbf{f}_{N_1}^T(\mu_0) \hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) \mathbf{f}_{N_2}(\mu_0),$$

$$\hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) = \left[\mathbf{C}_{N_1}^{c_1;T}(\boldsymbol{\alpha}_s(\mu_0)) H(\mu_R) \mathbf{C}_{N_2}^{c_2}(\boldsymbol{\alpha}_s(\mu_0)) \right] \int_0^M \frac{dk_{t1}}{k_{t1}} \int_0^{2\pi} \frac{d\phi_1}{2\pi} e^{-\mathbf{R}(\epsilon k_{t1})}$$

$$\times \exp\left\{-\sum_{\ell=1}^{2}\left(\int_{\epsilon k_{t1}}^{\mu_{0}}\frac{dk_{t}}{k_{t}}\frac{\alpha_{s}(k_{t})}{\pi}\Gamma_{N_{\ell}}(\alpha_{s}(k_{t}))+\int_{\epsilon k_{t1}}^{\mu_{0}}\frac{dk_{t}}{k_{t}}\Gamma_{N_{\ell}}^{(C)}(\alpha_{s}(k_{t}))\right\}$$

$$\times \sum_{\ell_1=1}^2 \left(\mathbf{R}_{\ell_1}'(k_{t1}) + \frac{\alpha_s(k_{t1})}{\pi} \mathbf{\Gamma}_{N_{\ell_1}}(\alpha_s(k_{t1})) + \mathbf{\Gamma}_{N_{\ell_1}}^{(C)}(\alpha_s(k_{t1})) \right)$$

$$\times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\epsilon}^{1} \frac{d\zeta_{i}}{\zeta_{i}} \int_{0}^{2\pi} \frac{d\phi_{i}}{2\pi} \Theta\left(v - V(\{\tilde{p}\}, k_{1}, \dots, k_{n+1})\right), \\ \times \sum_{\ell=1}^{2} \left(\mathbf{R}_{\ell_{i}}'\left(k_{ti}\right) + \frac{\alpha_{s}(k_{ti})}{\pi} \Gamma_{N_{\ell_{i}}}(\alpha_{s}(k_{ti})) + \mathbf{\Gamma}_{N_{\ell_{i}}}^{(C)}(\alpha_{s}(k_{ti}))\right)$$



Now include effect of **collinear radiation** and terms beyond NLL accuracy

DGLAP evolution

SM@LHC 2022, 13 Apr 2022

[Bizon, Monni, Re, LR, Torrielli '17] [Re, LR, Torrielli '21]

$$\frac{d\Sigma(v)}{d\Phi_B} = \int_{\mathscr{C}_1} \frac{dN_1}{2\pi i} \int_{\mathscr{C}_2} \frac{dN_2}{2\pi i} x_1^{-N_1} x_2^{-N_2} \sum_{c_1,c_2} \frac{d|M_B|_{c_1c_2}^2}{d\Phi_B} \mathbf{f}_{N_1}^T(\mu_0) \hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) \mathbf{f}_{N_2}(\mu_0),$$

$$\hat{\boldsymbol{\Sigma}}_{N_1,N_2}^{c_1,c_2}(v) = \left[\mathbf{C}_{N_1}^{c_1;T}(\alpha_s(\mu_0))H(\mu_R)\mathbf{C}_{N_2}^{c_2}(\alpha_s(\mu_0)) \right] \int_0^M \frac{dk_{t1}}{k_{t1}} \int_0^{2\pi} \frac{d\phi_1}{2\pi} e^{-\mathbf{R}(\epsilon k_{t1})}$$

$$\times \exp\left\{-\sum_{\ell=1}^{2}\left(\int_{\epsilon k_{t1}}^{\mu_{0}}\frac{dk_{t}}{k_{t}}\frac{\alpha_{s}(k_{t})}{\pi}\Gamma_{N_{\ell}}(\alpha_{s}(k_{t}))+\int_{\epsilon k_{t1}}^{\mu_{0}}\frac{dk_{t}}{k_{t}}\Gamma_{N_{\ell}}^{(C)}(\alpha_{s}(k_{t}))\right\}\right\}$$

$$\times \sum_{\ell_1=1}^2 \left(\mathbf{R}_{\ell_1}'(k_{t1}) + \frac{\alpha_s(k_{t1})}{\pi} \mathbf{\Gamma}_{N_{\ell_1}}(\alpha_s(k_{t1})) + \mathbf{\Gamma}_{N_{\ell_1}}^{(C)}(\alpha_s(k_{t1})) \right)$$

$$\times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\epsilon}^{1} \frac{d\zeta_{i}}{\zeta_{i}} \int_{0}^{2\pi} \frac{d\phi_{i}}{2\pi} \Theta\left(v - V(\{\tilde{p}\}, k_{1}, \dots, k_{n+1})\right),$$

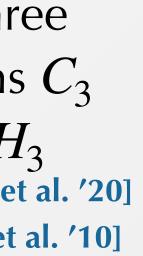
$$\times \sum_{\ell_i=1}^2 \left(\mathbf{R}_{\ell_i}'(k_{ti}) + \frac{\alpha_s(k_{ti})}{\pi} \mathbf{\Gamma}_{N_{\ell_i}}(\alpha_s(k_{ti})) + \mathbf{\Gamma}_{N_{\ell_i}}^{(C)}(\alpha_s(k_{ti})) \right)$$



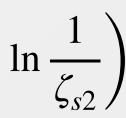
All-order formula in Mellin space at N³LL [Bizon, Monni, Re, LR, Torrielli '17] [Re, LR, Torrielli '21]

$$\frac{d\Sigma(v)}{d\Phi_{R}} = \int \frac{dk_{i1}}{k_{i1}} \frac{d\phi_{1}}{2\pi} \partial_{L} \left(-e^{-Rk_{0}j} \mathscr{D}_{NFLL}(k_{fl})\right) \int d\mathscr{T}\Theta \left(v - V([\bar{p}], k_{1}, \dots, k_{n+1}]\right)$$
Luminosity factor: contains the full loop collinear coefficient function: and the three loop hard function R is $\int \frac{dk_{i1}}{k_{i1}} \frac{d\phi_{1}}{2\pi} \left(d\mathscr{L}_{n} \int d\mathscr{T}_{n} \int \frac{d\mathscr{T}_{n}}{\zeta_{n}} \frac{d\phi_{n}}{2\pi} \left(\left(R'(k_{fl})\mathscr{D}_{NNLL}(k_{fl}) - \partial_{L}\mathscr{D}_{NNLL}(k_{fl})\right)\right) \\ \times \left(R''(k_{fl}) \ln \frac{1}{\zeta_{n}} + \frac{1}{2}R'''(k_{fl}) \ln^{2}\frac{1}{\zeta_{n}}\right) - R'(k_{fl}) \left(\partial_{L}\mathscr{D}_{NNLL}(k_{fl}) - 2\frac{\beta_{0}}{\pi} a_{2}^{2}(k_{fl})\hat{p}^{(0)} \otimes \mathscr{D}_{NLL}(k_{fl}) \ln \frac{1}{\zeta_{n}}\right)$

$$+ \frac{a_{i}^{2}(k_{fl})}{\pi^{2}} \hat{p}^{(0)} \otimes \hat{p}^{(0)} \otimes \mathscr{D}_{NLL}(k_{fl}) - \beta_{0}\frac{a_{i}^{2}(k_{fl})}{\pi^{2}} \left(\hat{p}^{(0)} \otimes \hat{c}^{(1)} + \hat{c}^{(1)} \otimes \hat{p}^{(0)}\right) \otimes \mathscr{D}_{NLL}(k_{fl}) + \frac{a_{i}^{2}(k_{fl})}{\pi^{2}} 2\beta_{0} \ln \frac{1}{\zeta_{n}} \hat{p}^{(0)} \otimes \hat{p}^{(0)} \otimes \mathscr{D}_{NL} \left(\frac{1}{\zeta_{n}} + \frac{a_{i}^{2}(k_{fl})}{2\pi}\right) - \Theta\left(v - V(\{\bar{p}\}, k_{1}, \dots, k_{n+1}, k_{i})\right) - \Theta\left(v - V(\{\bar{p}\}, k_{1}, \dots, k_{n+1}, k_{i})\right) - \Theta\left(v - V(\{\bar{p}\}, k_{1}, \dots, k_{n+1}, k_{n+1})\right)\right)$$
NILL corrections
$$\left\{ + \frac{1}{2} \int \frac{dk_{i1}}{k_{fl}} \frac{d\phi_{1}}{2\pi} - \frac{d\varphi_{1}}{\pi} \int_{0}^{1} \frac{d\zeta_{n}}{\zeta_{n}} \frac{d\phi_{n}}{4\pi} \int_{0}^{1} \frac{d\zeta_{n}}{\zeta_{n}} \frac{d\phi_{n}}{4\pi} \int_{0}^{1} \frac{d\zeta_{n}}{\xi_{n}} \frac{d\phi_{n}}{4\pi} \int_{0}^{1} \frac{d\zeta_{n}}{\xi_{n}} \frac{d\phi_{n}}{4\pi} \int_{0}^{1} \frac{d\zeta_{n}}{\xi_{n}} \frac{d\phi_{n}}{2\pi} \frac{d\phi_{n}}{2\pi} - \frac{\partial_{n}}{2\pi} \mathcal{D}_{n} \frac{d\phi_{n}}{4\pi} \int_{0}^{1} \frac{d\zeta_{n}}{2\pi} \frac{d\phi_{n}}{2\pi} \frac{$$







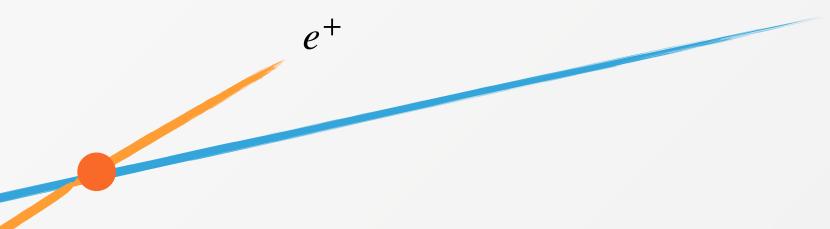




[Catani, de Florian, Ferrera, Grazzini '15]

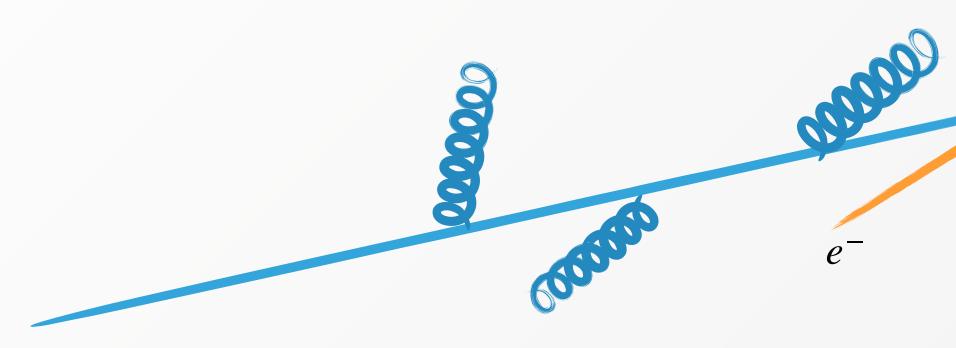




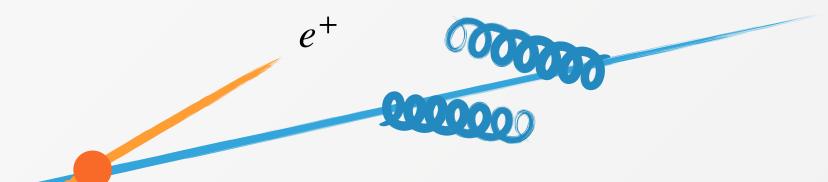


Born matrix element evaluated at $q_T = 0$

[Catani, de Florian, Ferrera, Grazzini '15]

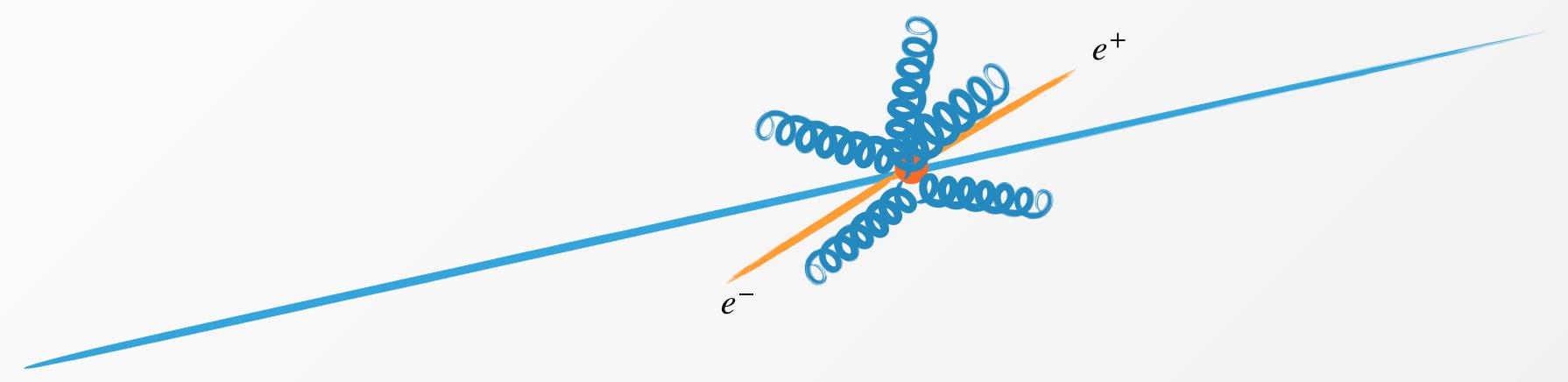






Generate singlet q_T by QCD radiation

[Catani, de Florian, Ferrera, Grazzini '15]

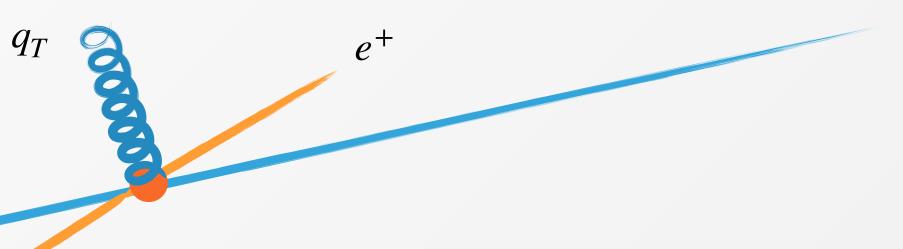




Generate singlet q_T by QCD radiation

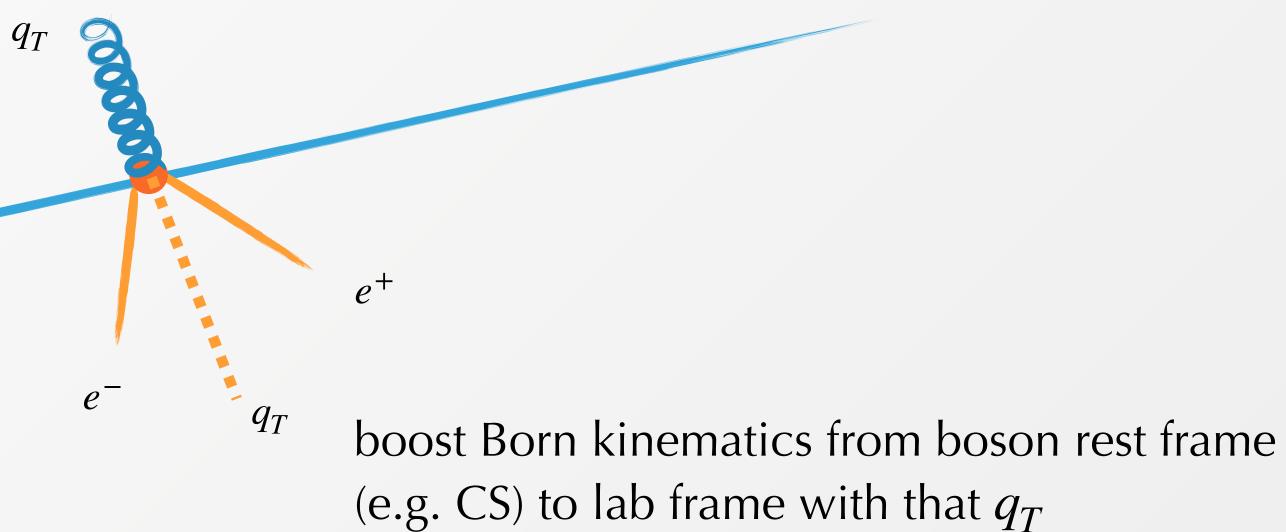
[Catani, de Florian, Ferrera, Grazzini '15]

e



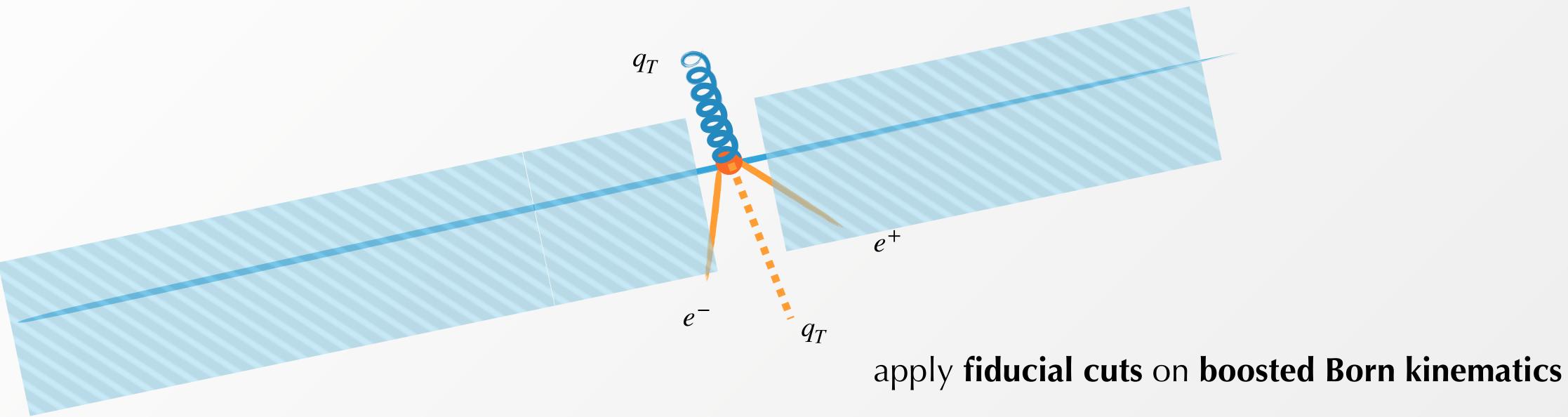
Generate singlet q_T by QCD radiation

[Catani, de Florian, Ferrera, Grazzini '15]

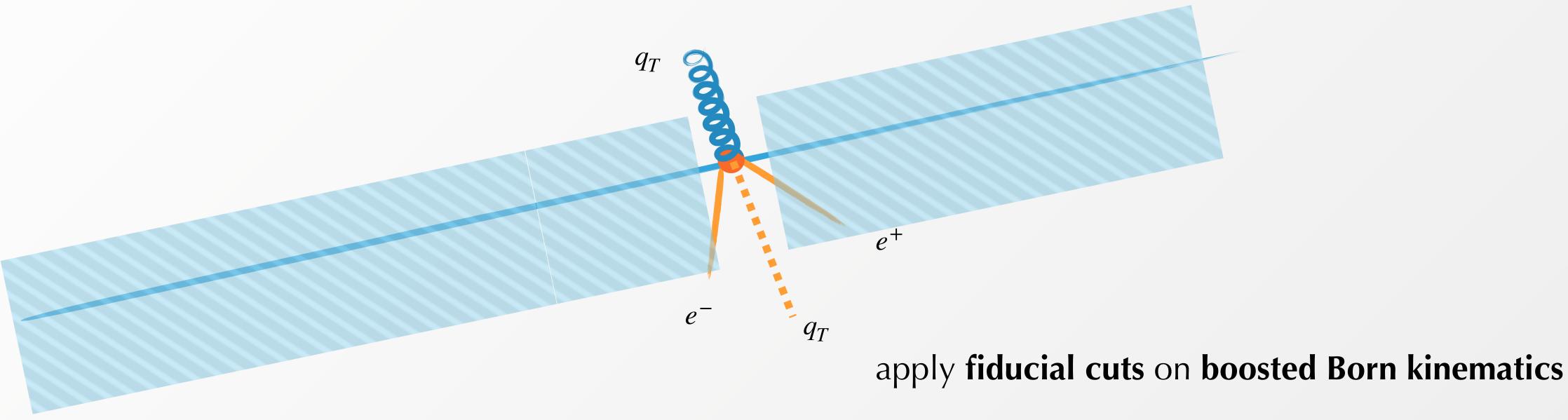




[Catani, de Florian, Ferrera, Grazzini '15]

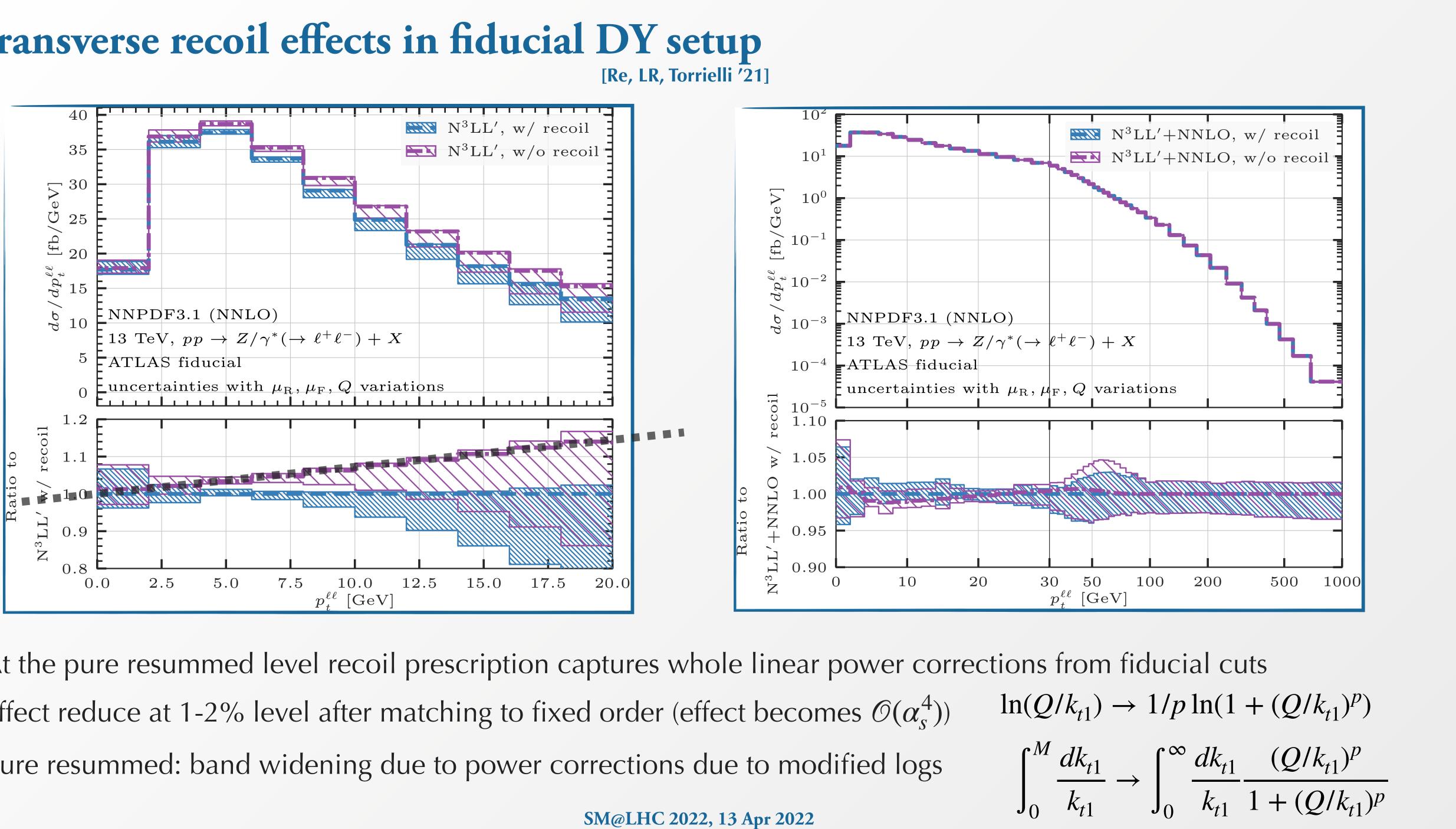


[Catani, de Florian, Ferrera, Grazzini '15]



Sufficient to capture the full linear fiducial power correction for q_T [Ebert, Michel, Stewart, Tackmann '20]

Transverse recoil effects in fiducial DY setup [Re, LR, Torrielli '21]



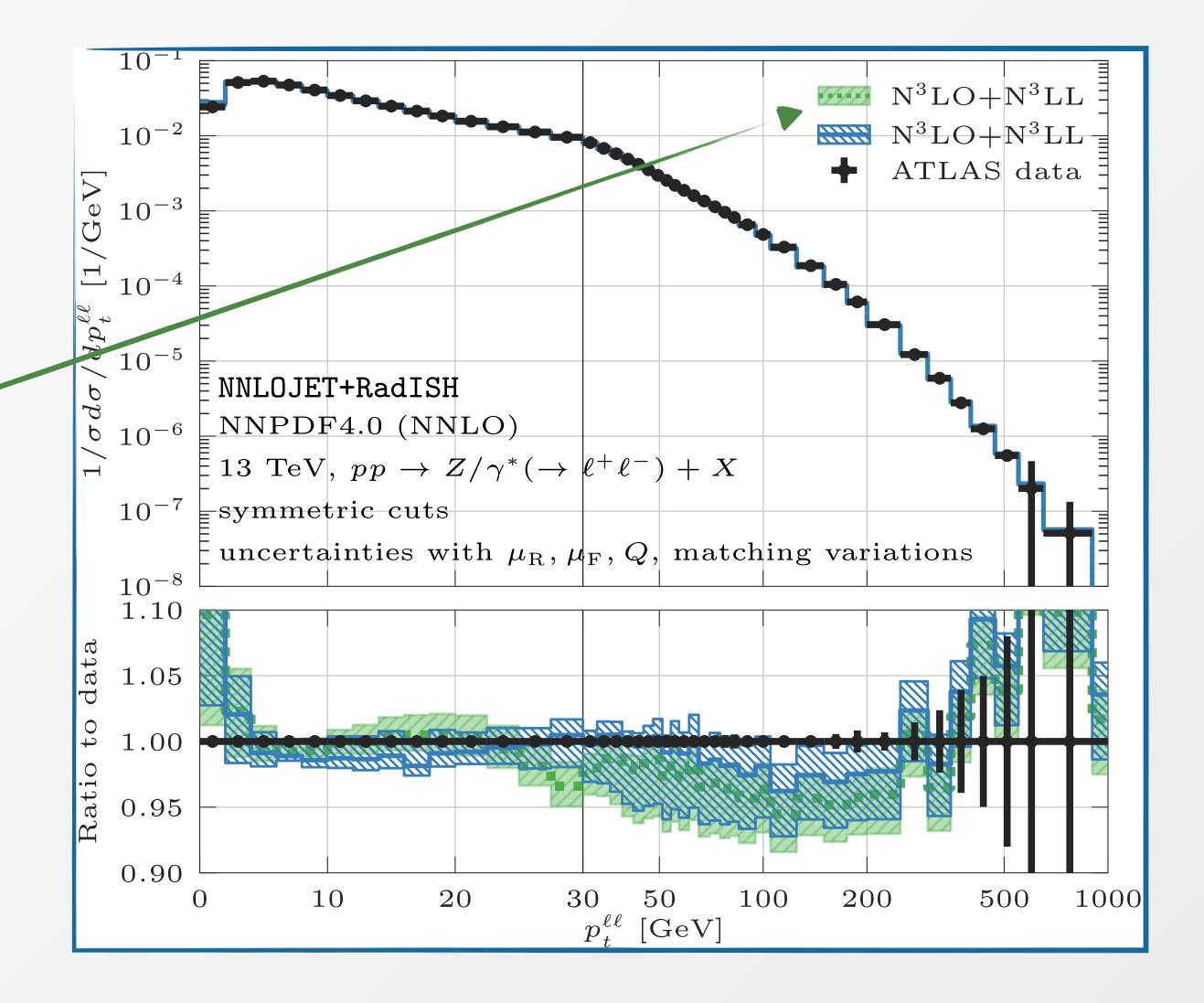
At the pure resummed level recoil prescription captures whole linear power corrections from fiducial cuts Effect reduce at 1-2% level after matching to fixed order (effect becomes $\mathcal{O}(\alpha_s^4)$) Pure resummed: band widening due to power corrections due to modified logs

Transverse momentum spectrum at N³LO+N³LL [Chen, Gehrmann, Glover, Huss, Monni, Re, LR, Torrielli '22]

$$d\sigma_V^{N^kLO+N^kLL} \equiv d\sigma_V^{N^kLL} + d\sigma_{V+jet}^{N^{k-1}LO} - \left[d\sigma_V^{N^kLL}\right]_{\mathcal{O}(\alpha_s^k)}$$

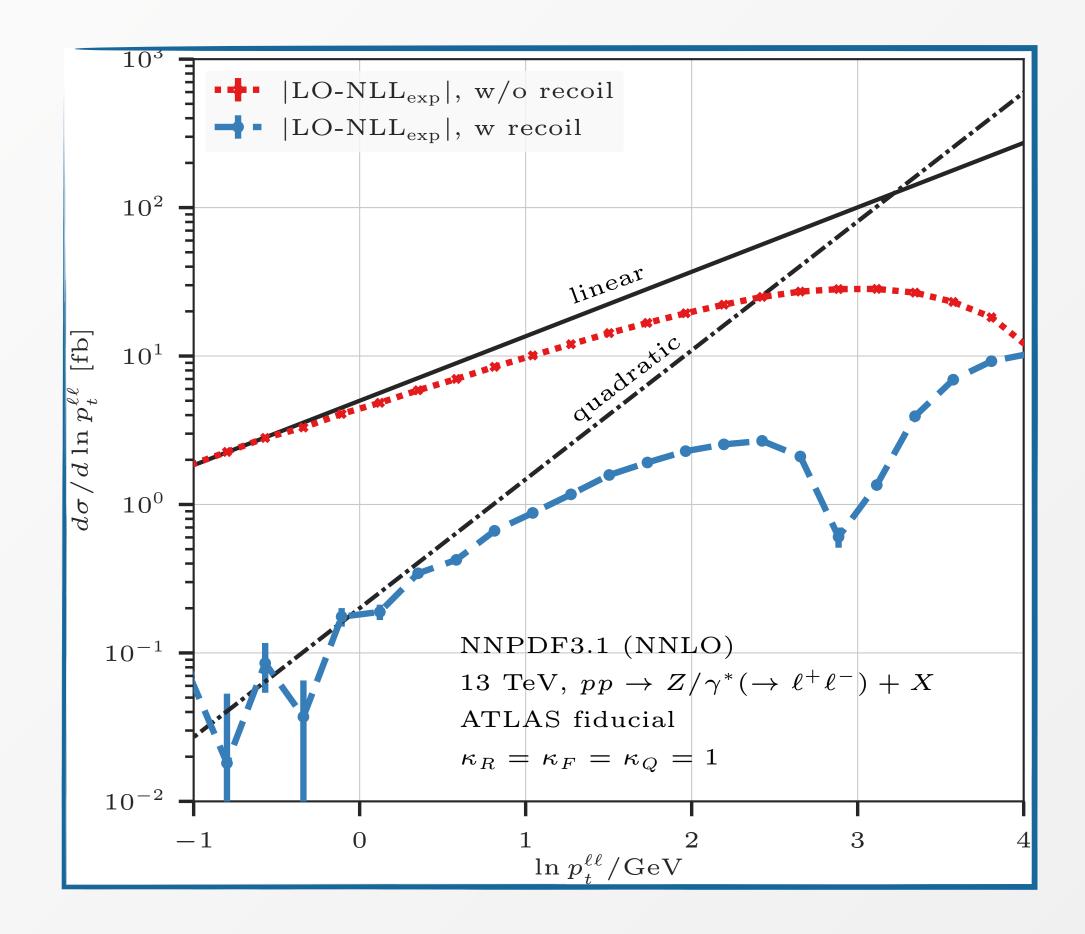
No fixed order component below 30 GeV

- Non-singular (matching) correction **nonnegligible** even below $q_T \lesssim 15$ GeV
- Fixed order matching **crucial** to get correct shape



Transverse recoil effects in fiducial DY setup

Symmetric cuts on the dileptons induce linear power corrections in the fiducial spectrum Can be avoided by suitable choice of cuts [Salam, Slade '21]



SM@LHC 2022, 13 Apr 2022



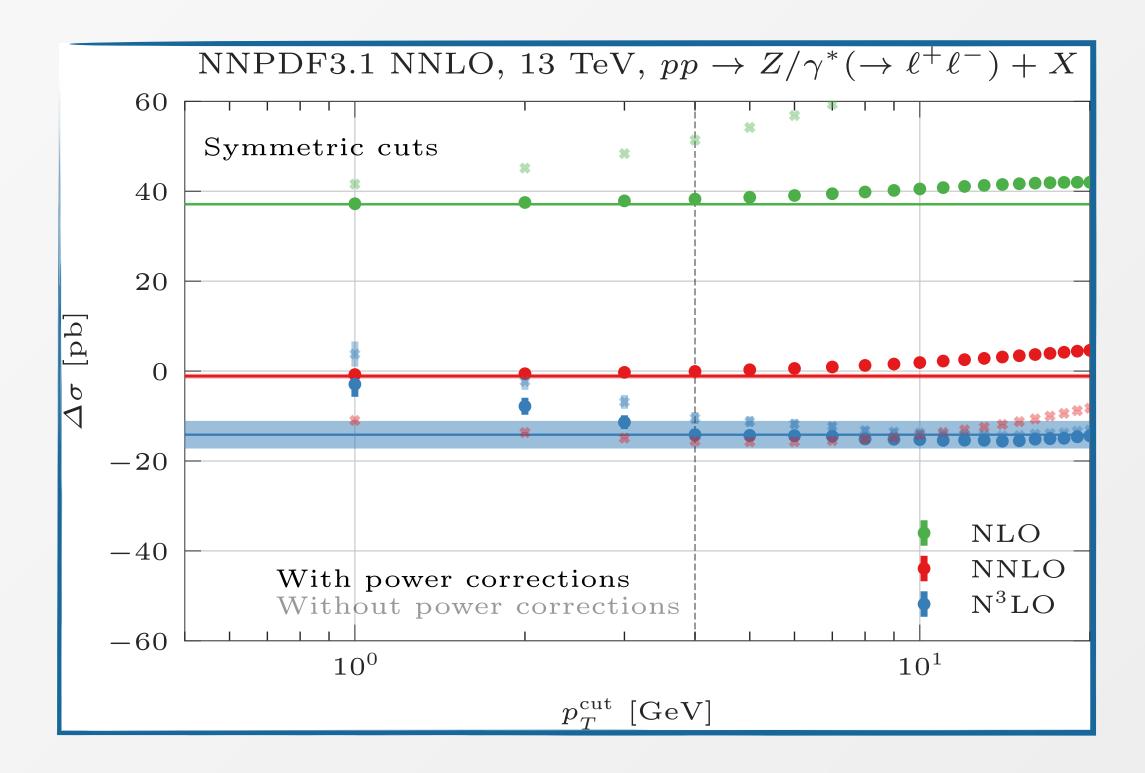
Recoil effectively captures the **full linear fiducial power correction** for p_t

Comparison with previous N³LO estimates

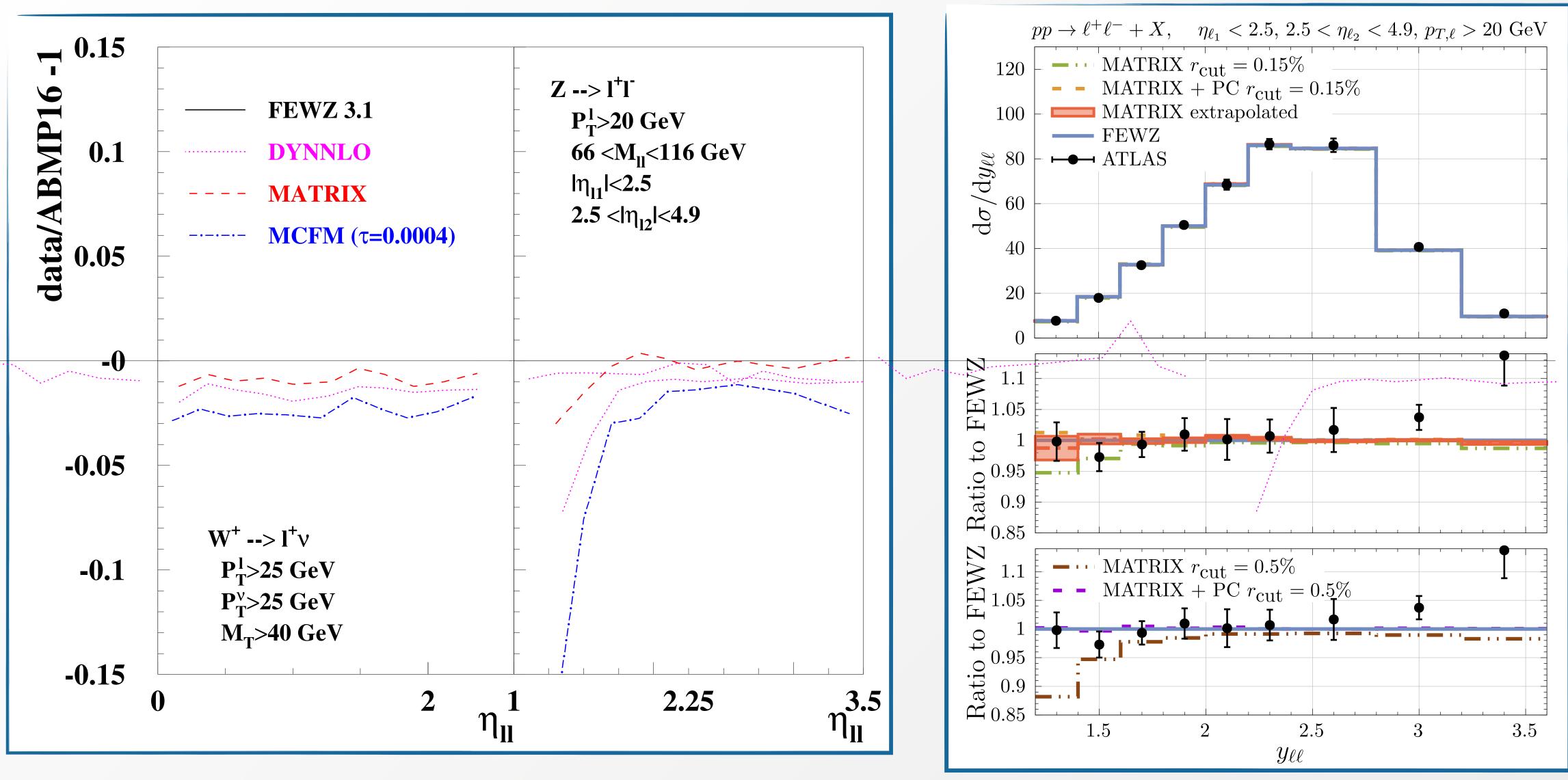
Symmetric cuts

- Omission of linear power corrections leads to incorrect estimate of N^kLO corrections
 [Camarda, Cieri, Ferrera '21]
- Data at N³LO not of sufficient quality to observe a stable plateau, inducing larger systematic uncertainties

 $p_T^{\ell^{\pm}} > 25 \,\text{GeV} \qquad |\eta^{\ell^{\pm}}| < 2.5$



Inclusion of linear power corrections in differential distributions



[Buonocore, Kallweit, <u>LR</u>, Wiesemann '21]