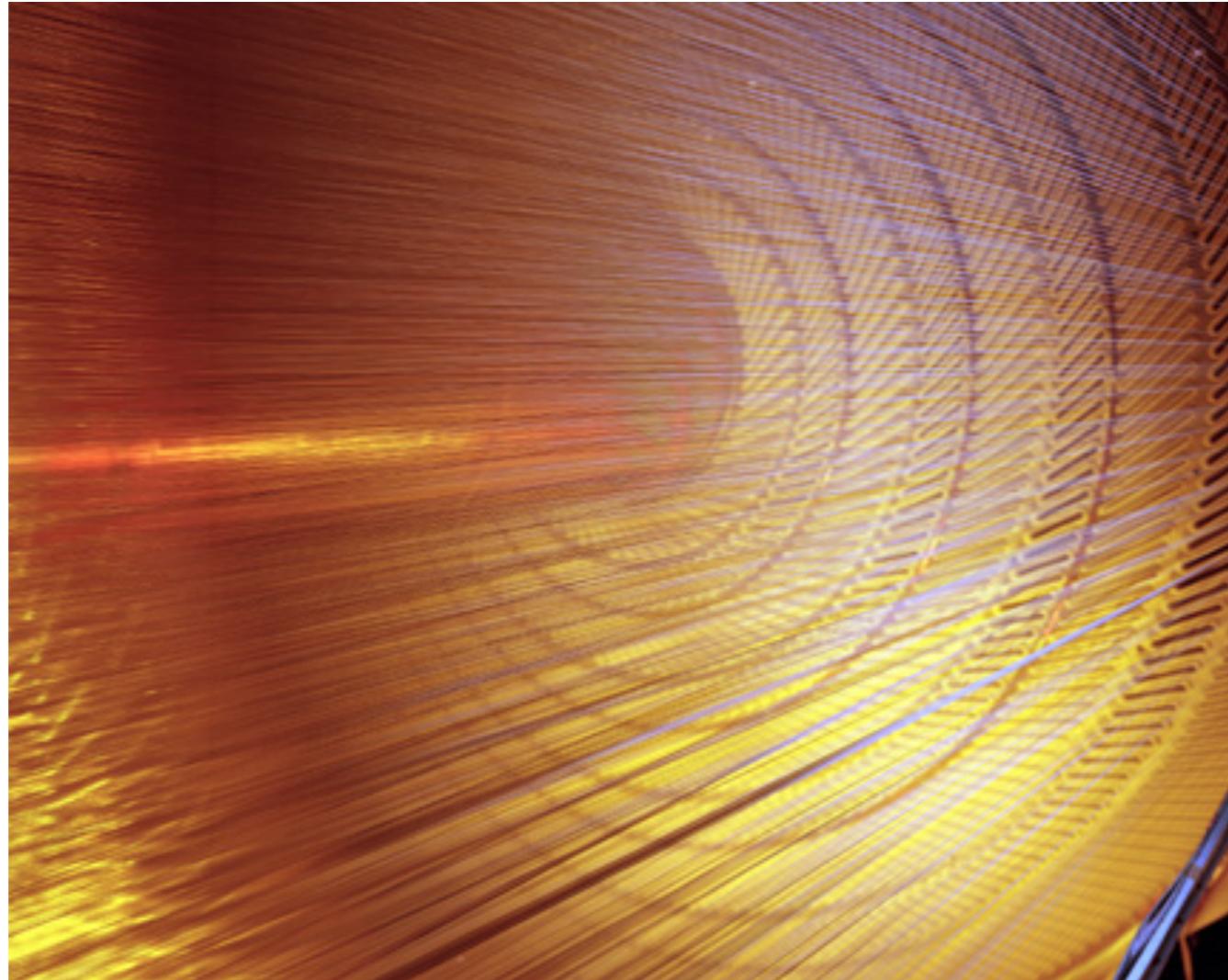


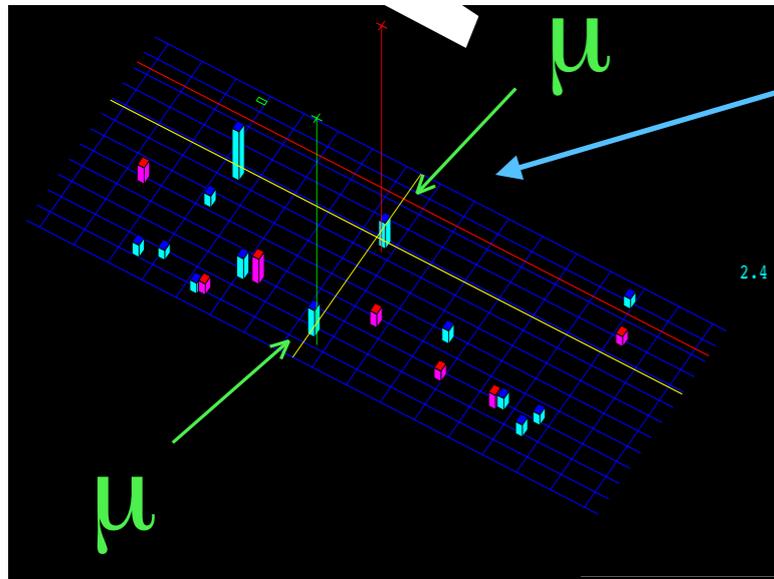
High precision measurement of the W boson mass with the CDF II detector



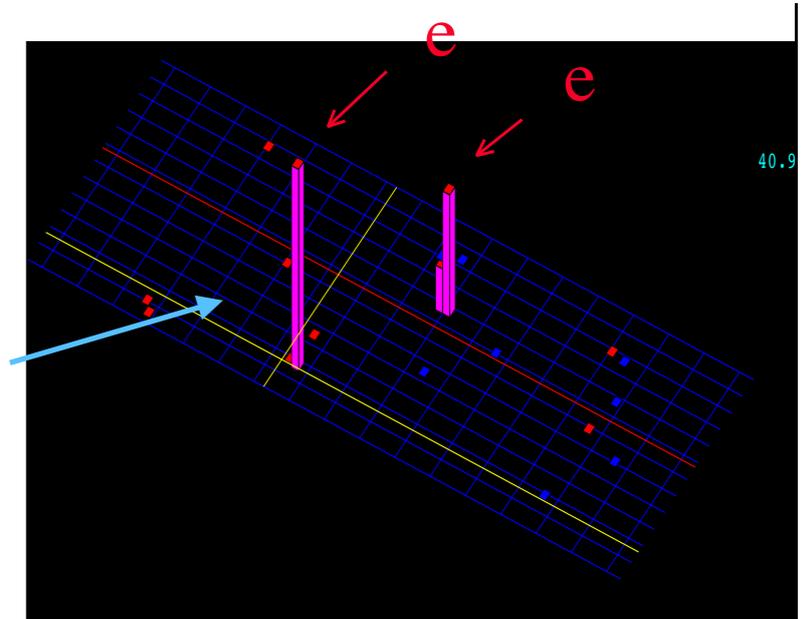
Chris Hays, Oxford University

SM@LHC '22
13 April 2022

Overview

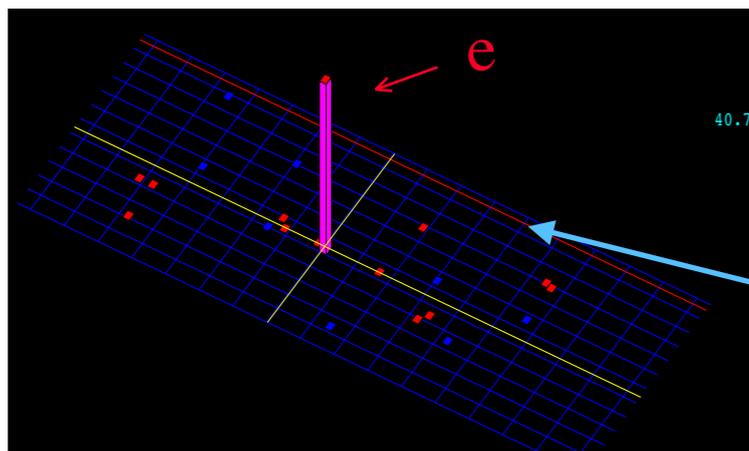


Muon momentum calibration



Electron momentum calibration

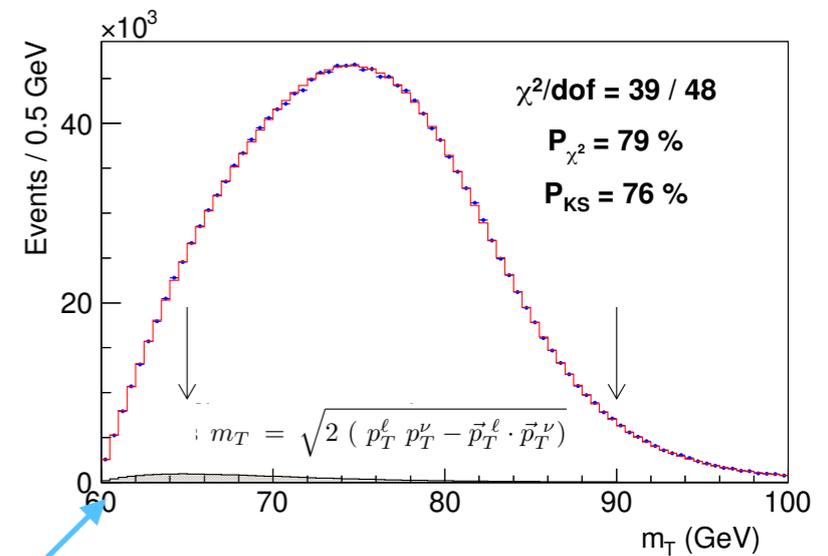
W selection & background



W boson production

Recoil calibration

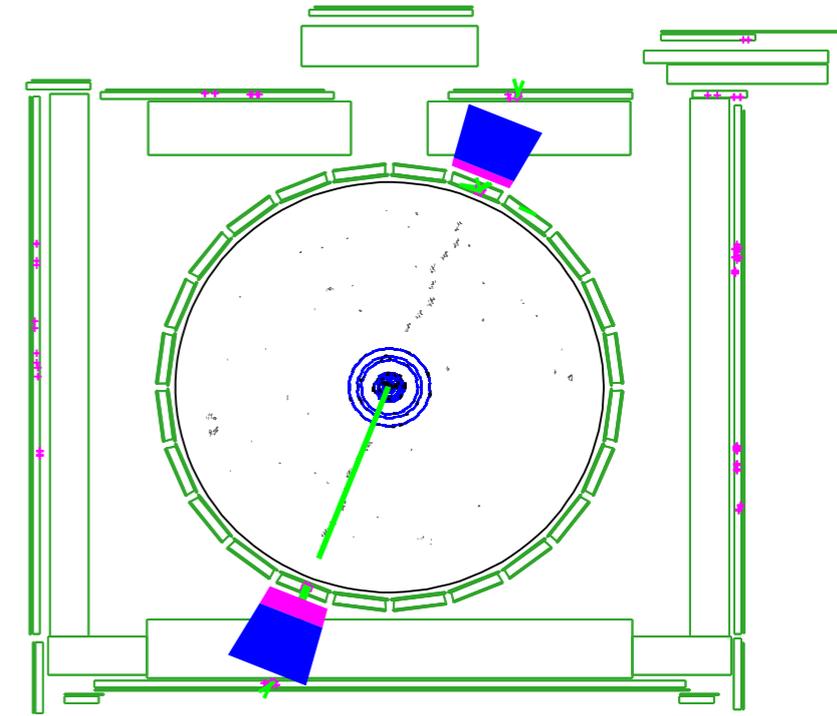
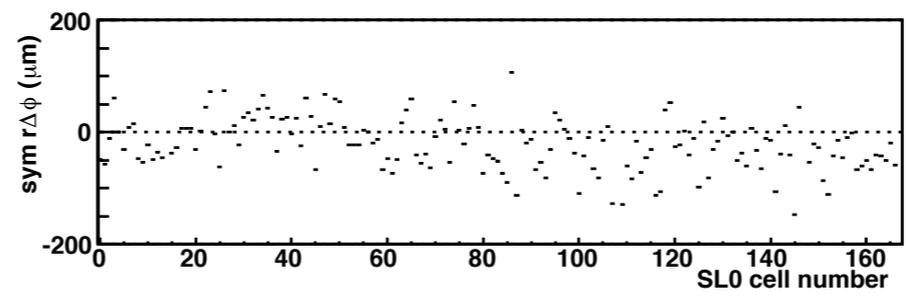
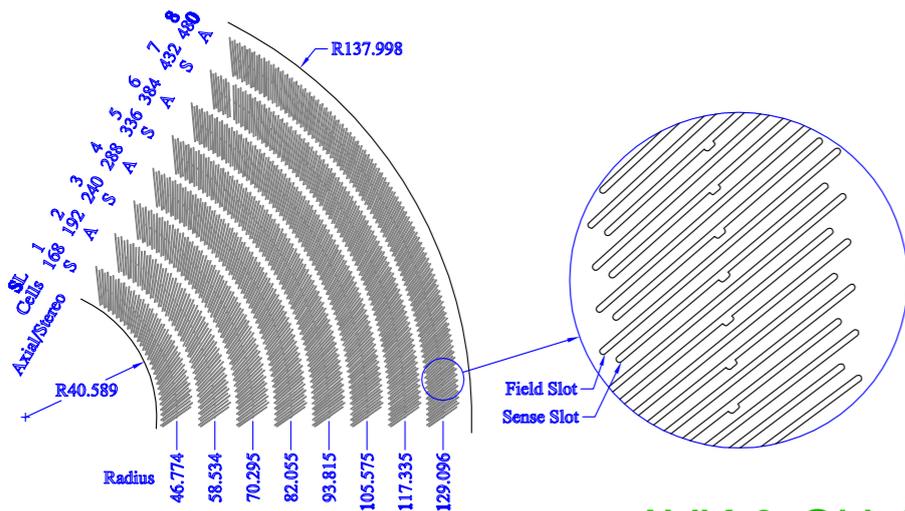
W boson mass measurement



Muon momentum calibration

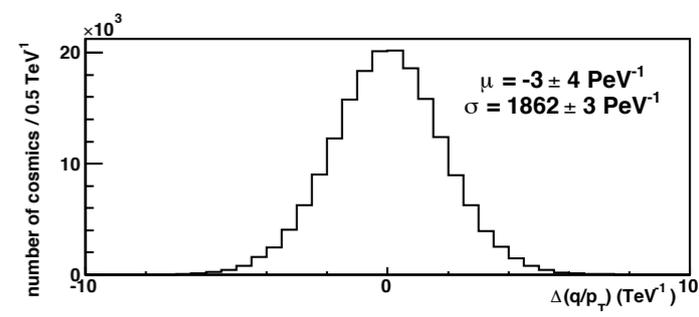
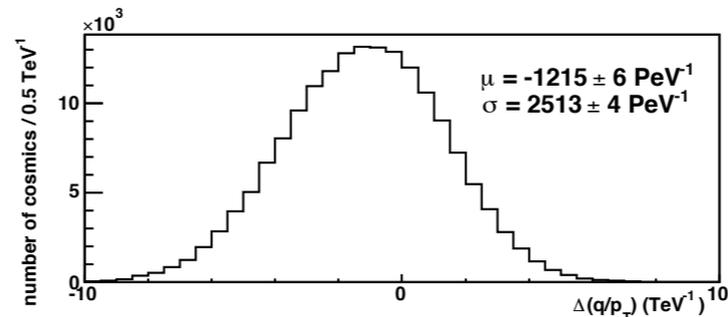
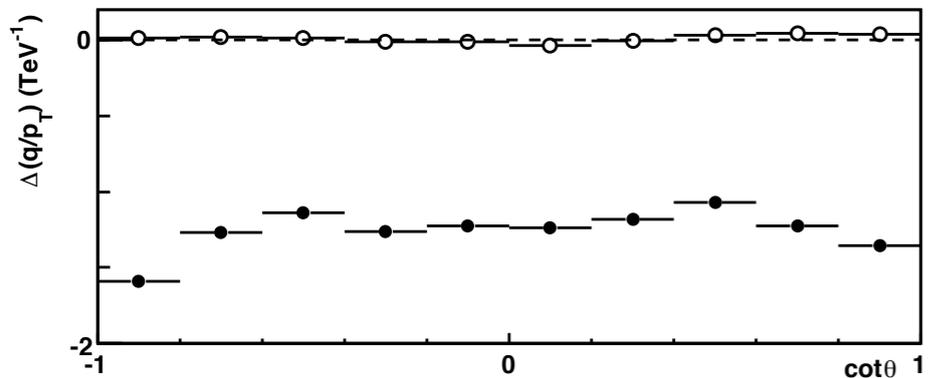
First step is the alignment of the drift chamber (the “central outer tracker” or COT)

Two degrees of freedom (shift & rotation) for each of 2520 cells made up of twelve sense wires constrained using hit residuals from cosmic-ray tracks



AVK & CH, 1404.3457 & NIM A 762, 85 (2014)

Two parameters for the electrostatic deflection of the wire within the chamber constrained using difference between fit parameters of incoming and outgoing cosmic-ray tracks



3

Before

After

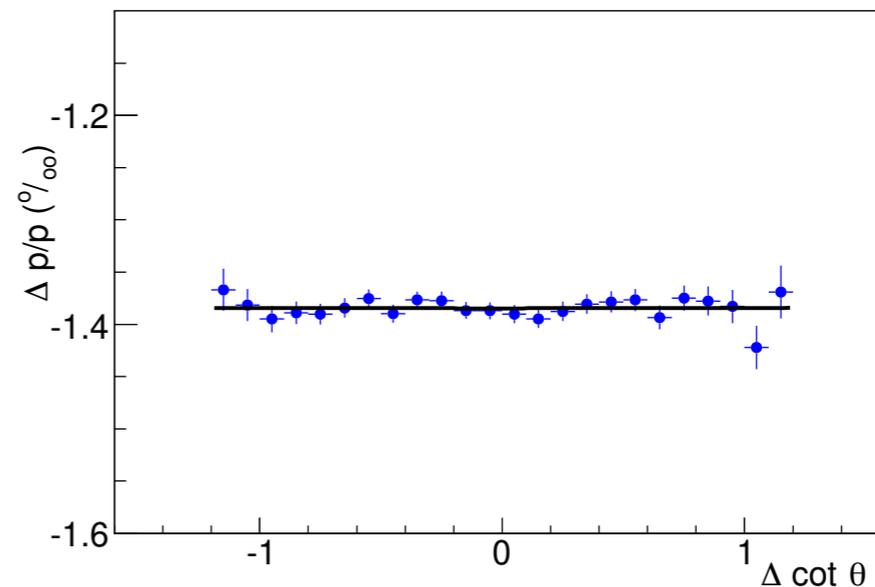
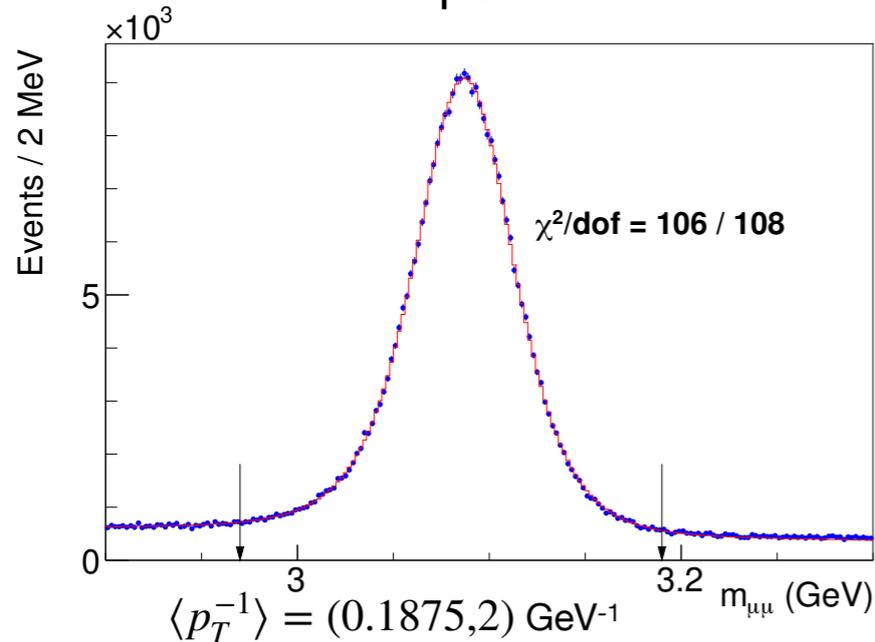
Muon momentum calibration

Second step is the scale calibration from J/ψ decays to muons

Model lineshape using hit-level simulation and NLO form factor for QED radiation

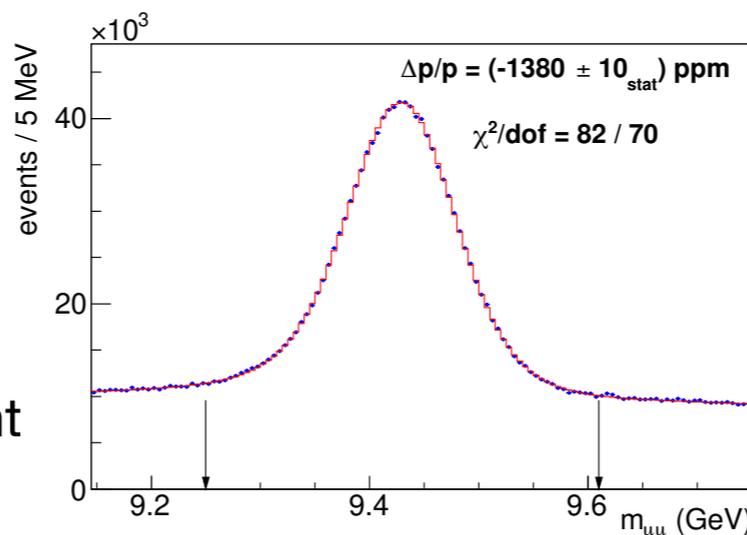
Apply correct the length scale of the tracker with mass measurement as a function of $\Delta \cot \theta$

Correct the amount of upstream material with mass measurement as a function of p_T^{-1}

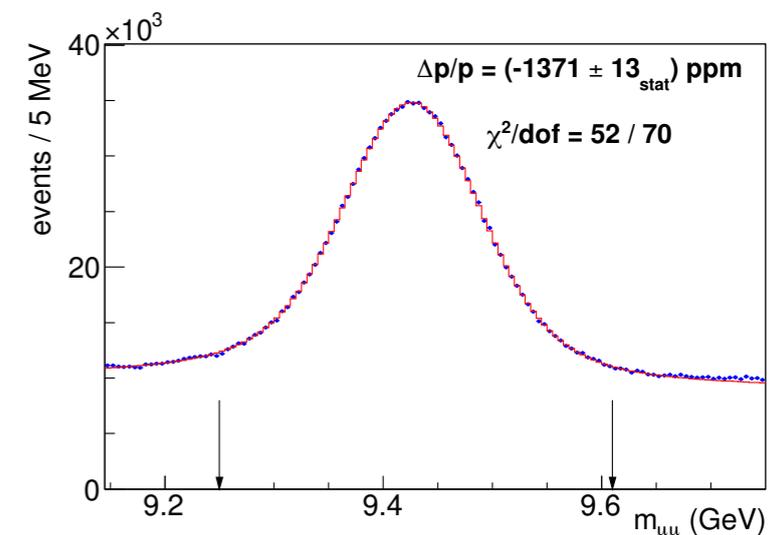


Third step is the scale calibration from Υ decays to muons

Compare fit results with and without constraining the track to the collision point



4 with constraint



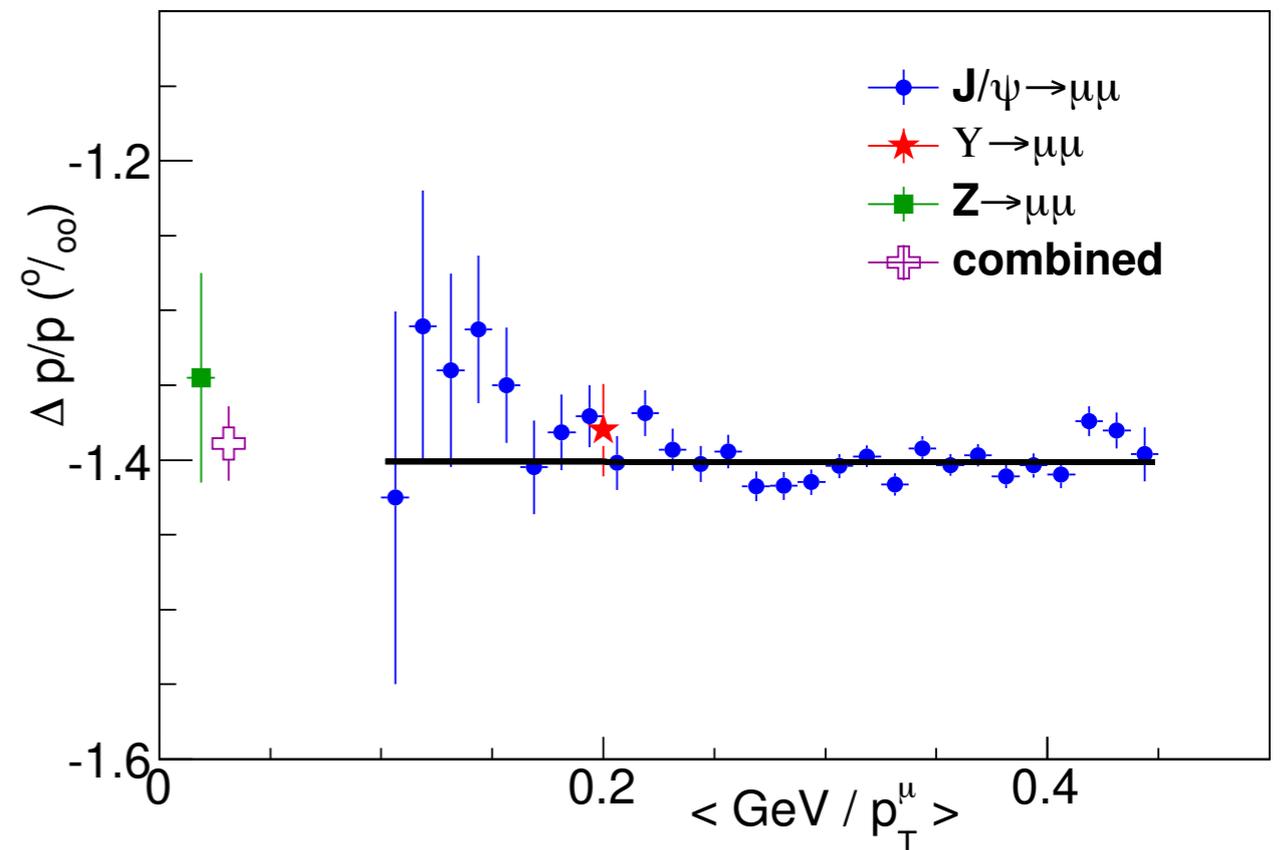
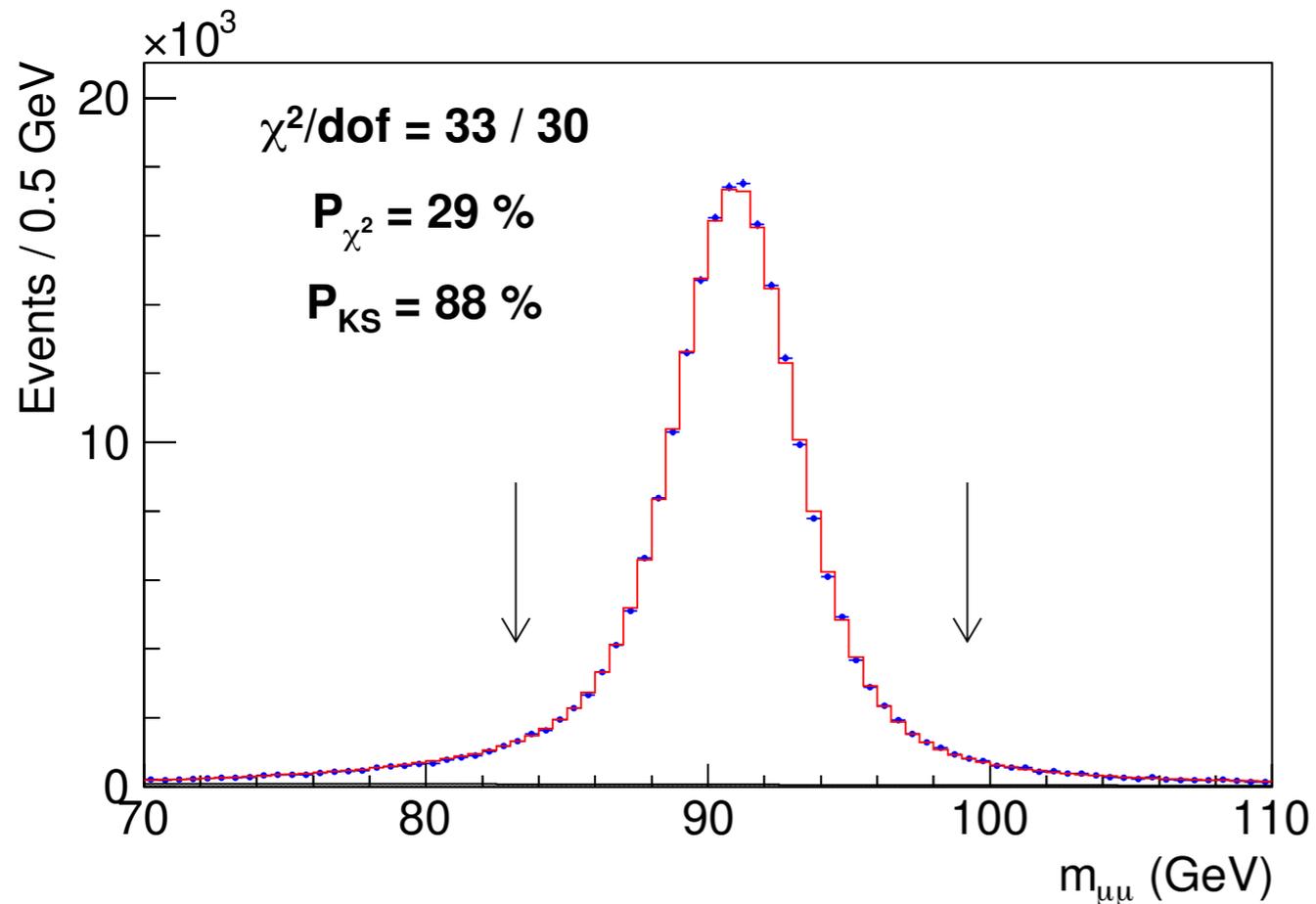
without constraint

Muon momentum calibration

Final step is the measurement of the Z boson mass

$$M_Z = 91\,192.0 \pm 6.4_{stat} \pm 4.0_{sys} \text{ MeV}$$

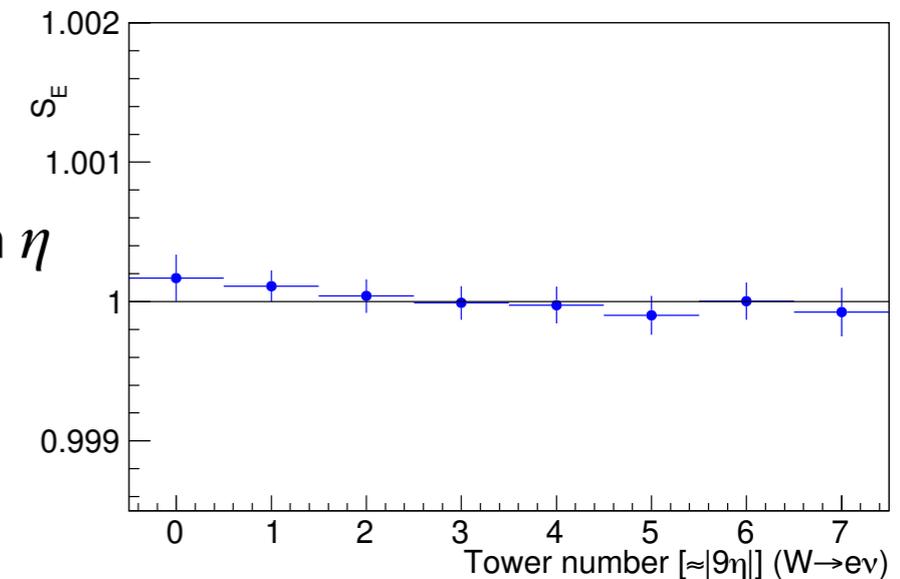
Result blinded with $[-50,50]$ MeV offset until previous steps were complete
Then combine all measurements into a final charged-track momentum scale



Electron momentum calibration

First step is the correction for response variations in space and time

Fit ratio of calorimeter energy to track momentum to correct each tower in η
Use mean E/p to remove time dependence & response variations in tower

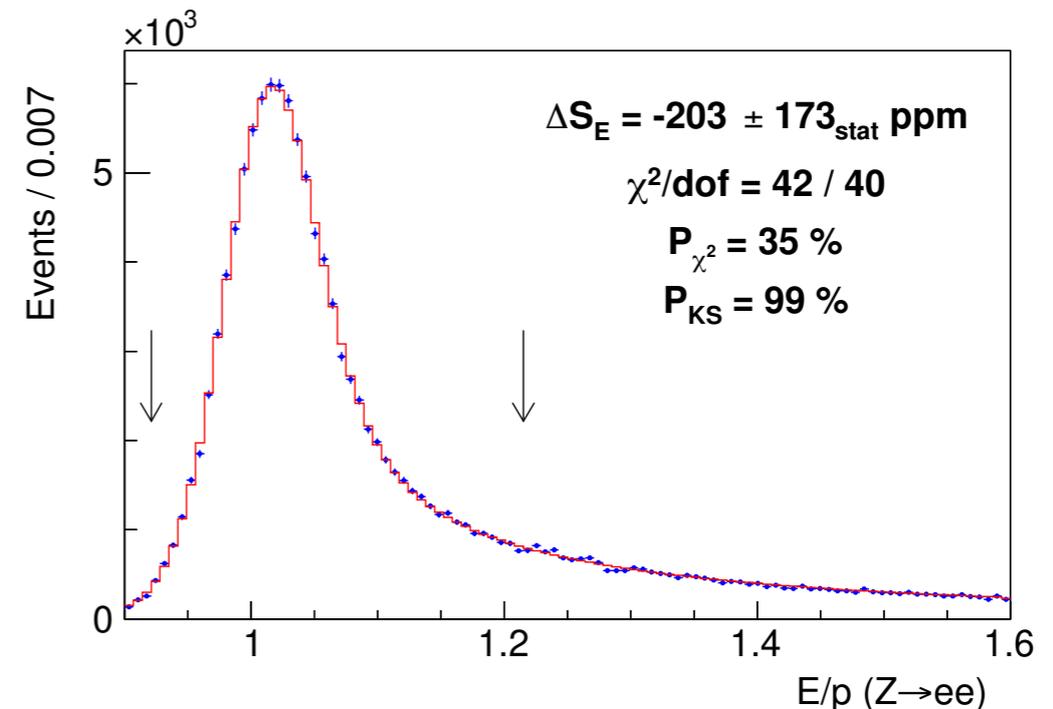
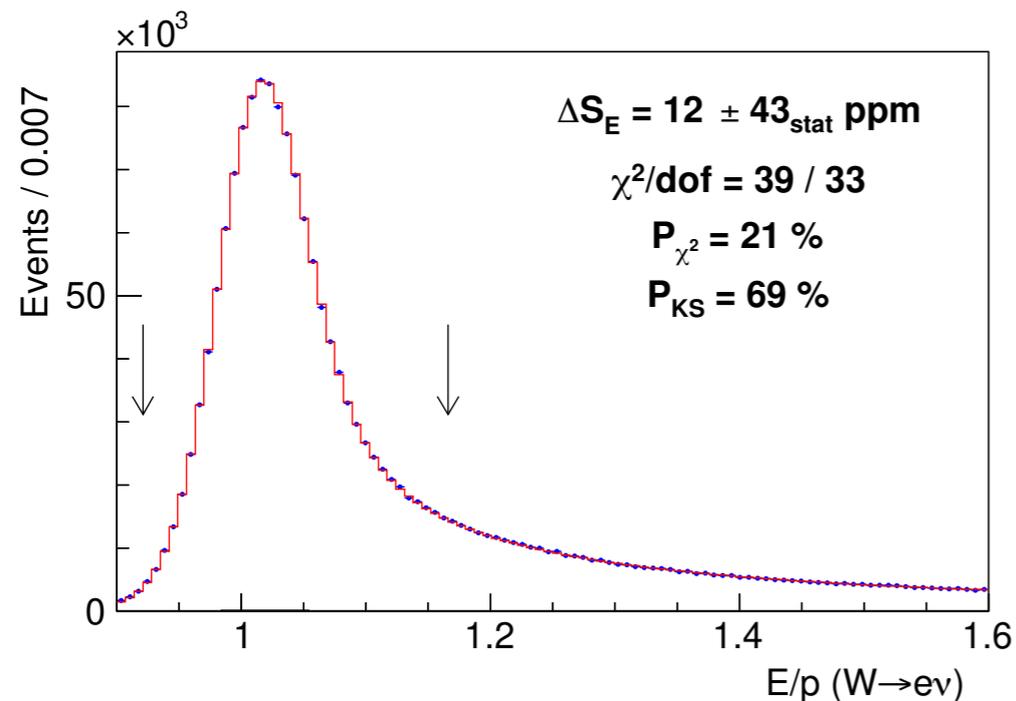


Second step is the calibration of the energy scale using E/p

Custom parameterized GEANT simulation of calorimeter

AVK & CH, 1308.2025 & NIM A 729, 25 (2013)

Use E/p and tail fits to simulate osmall non-linear energy response and variations in calorimeter thickness



Electron momentum calibration

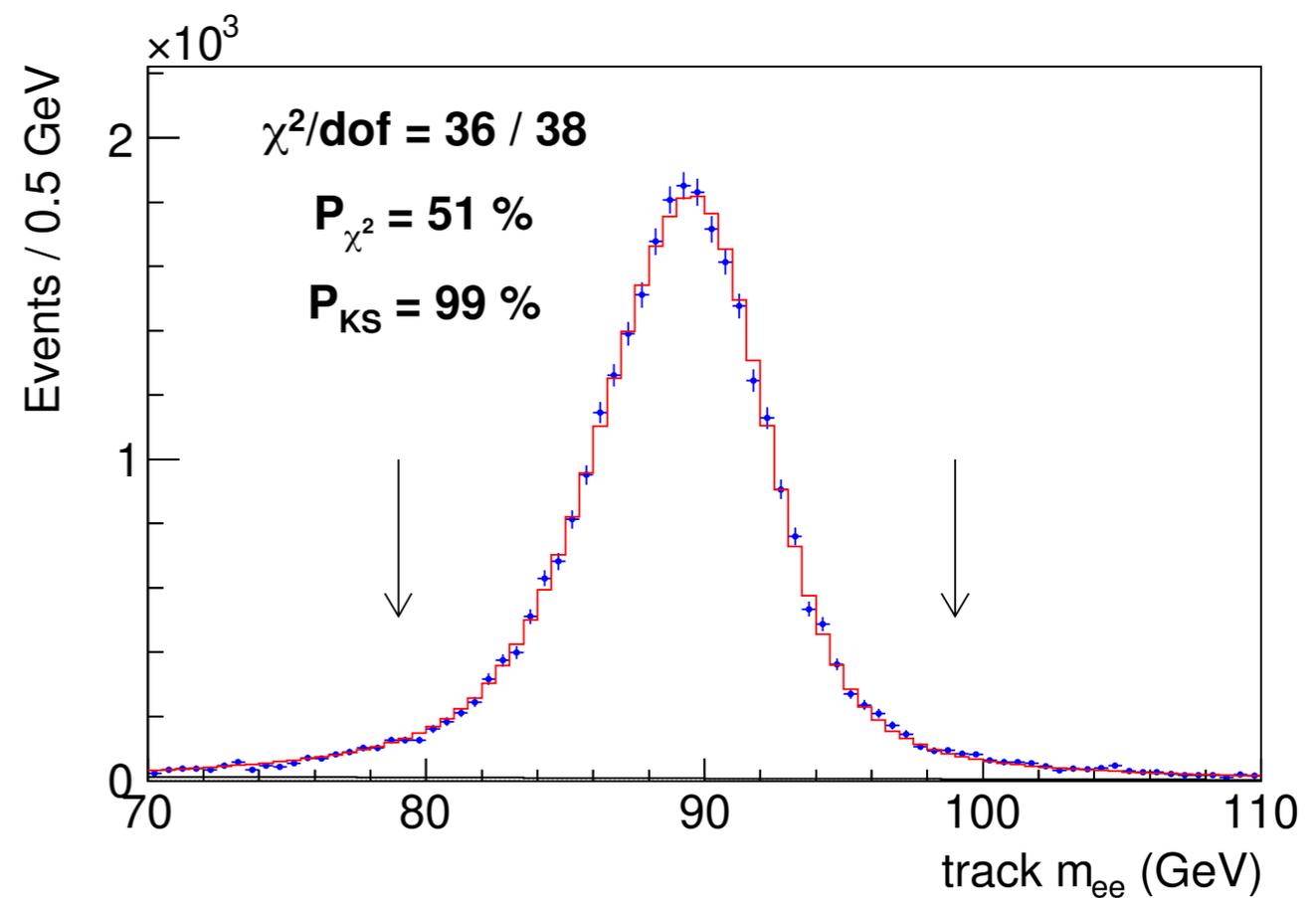
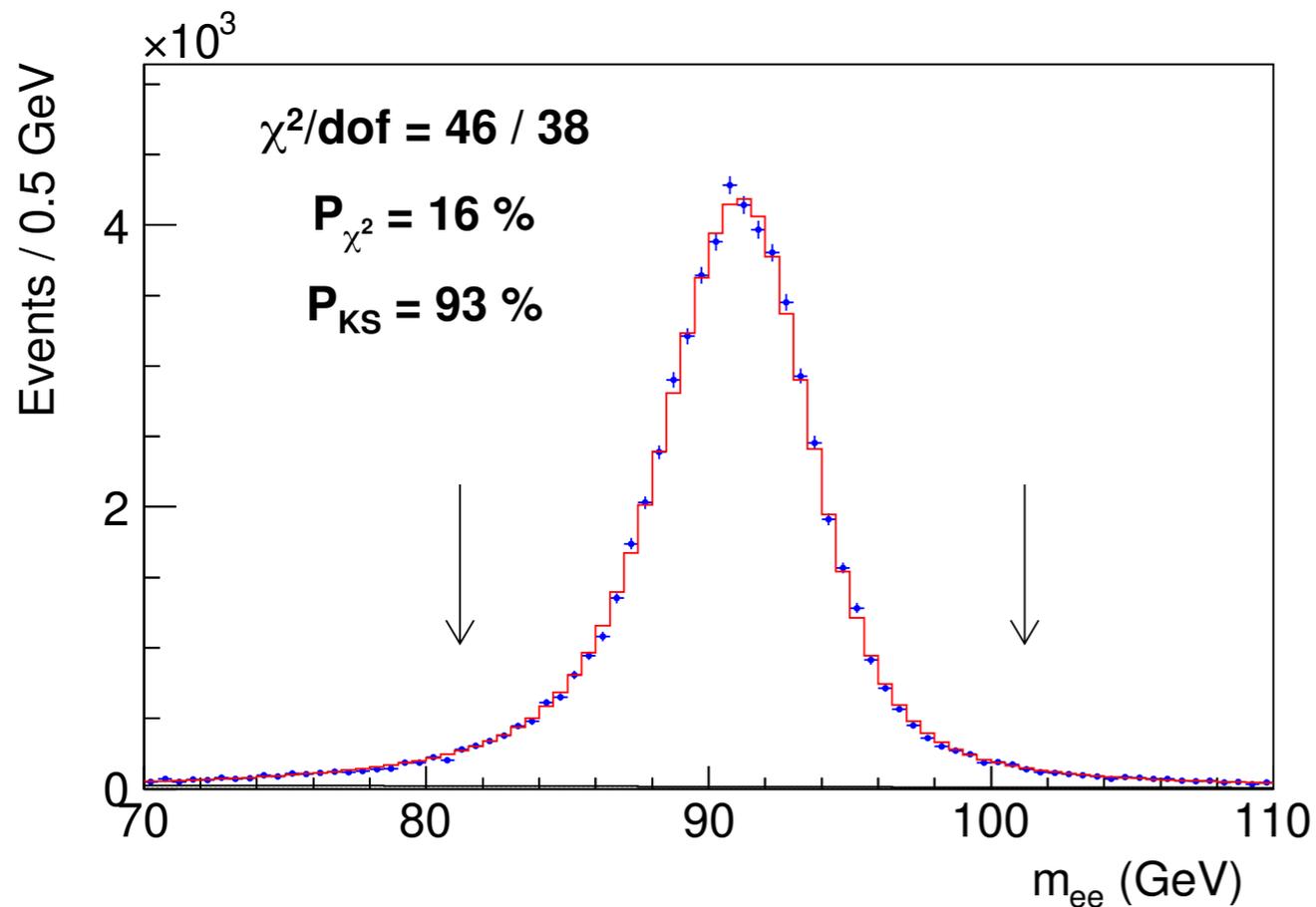
Final step is the measurement of the Z boson mass

$$M_Z = 91\,194.3 \pm 13.8_{stat} \pm 7.6_{sys} \text{ MeV}$$

As a consistency check measure mass using only track information

e.g. $M_Z = 91\,215.2 \pm 22.4 \text{ MeV}$ for non-radiative electrons ($E/p < 1.1$)

Same blinding used as for muon channel

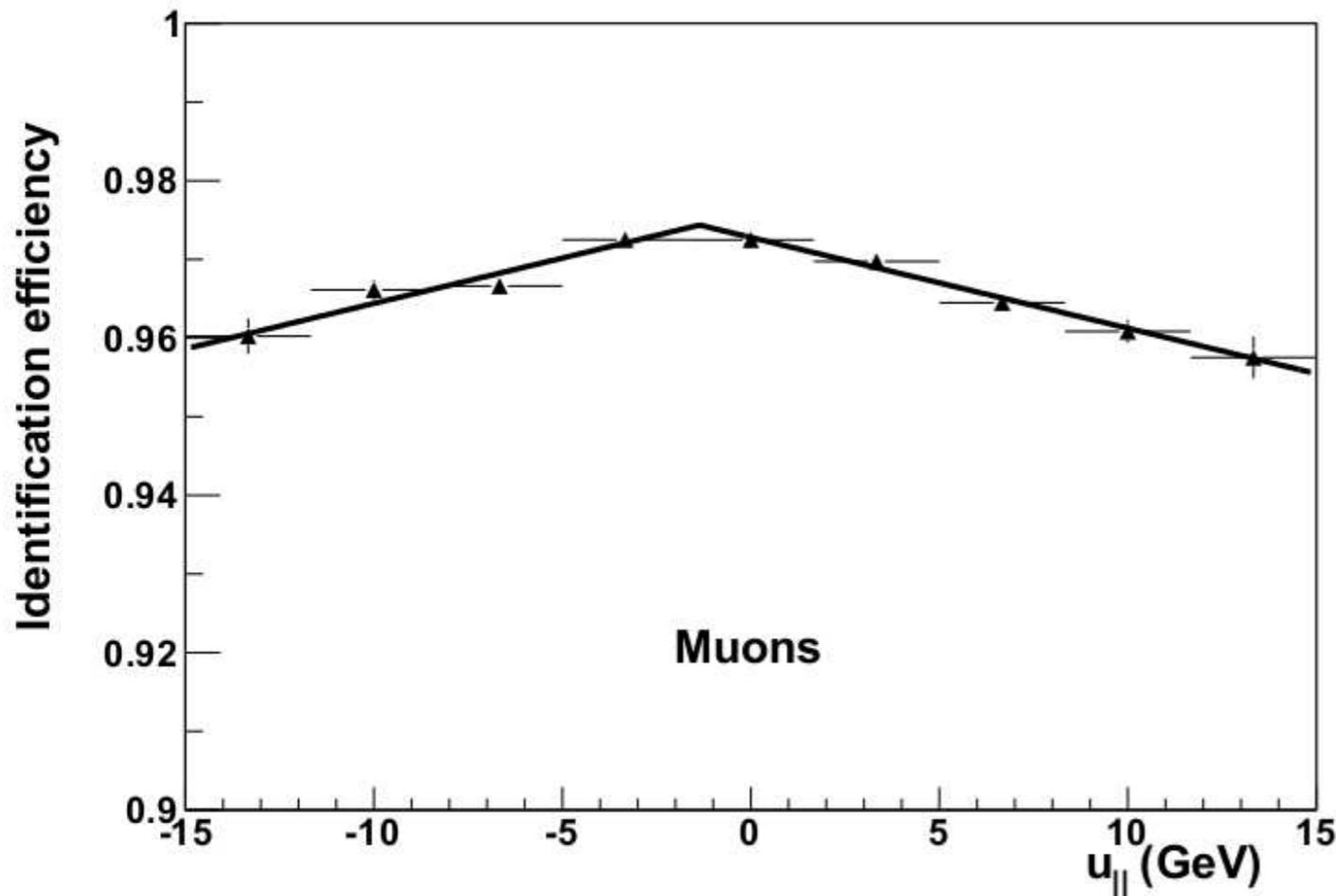
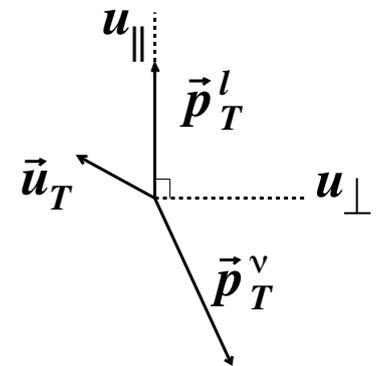


W boson selection

Triggers with low momentum thresholds (18 GeV) and very loose lepton id

Offline id also loose, efficiencies vary by 2% as hadronic recoil direction changes

No lepton isolation requirement in trigger or offline selection



Background suppressed by stringent hadronic recoil requirement:
 $u_T < 15$ GeV

Other kinematic requirements:
lepton and missing p_T in the range 30-55 GeV
Transverse mass in the range 60-100 GeV

2.4 M $W \rightarrow \mu\nu$ candidates

1.8 M $W \rightarrow e\nu$ candidates

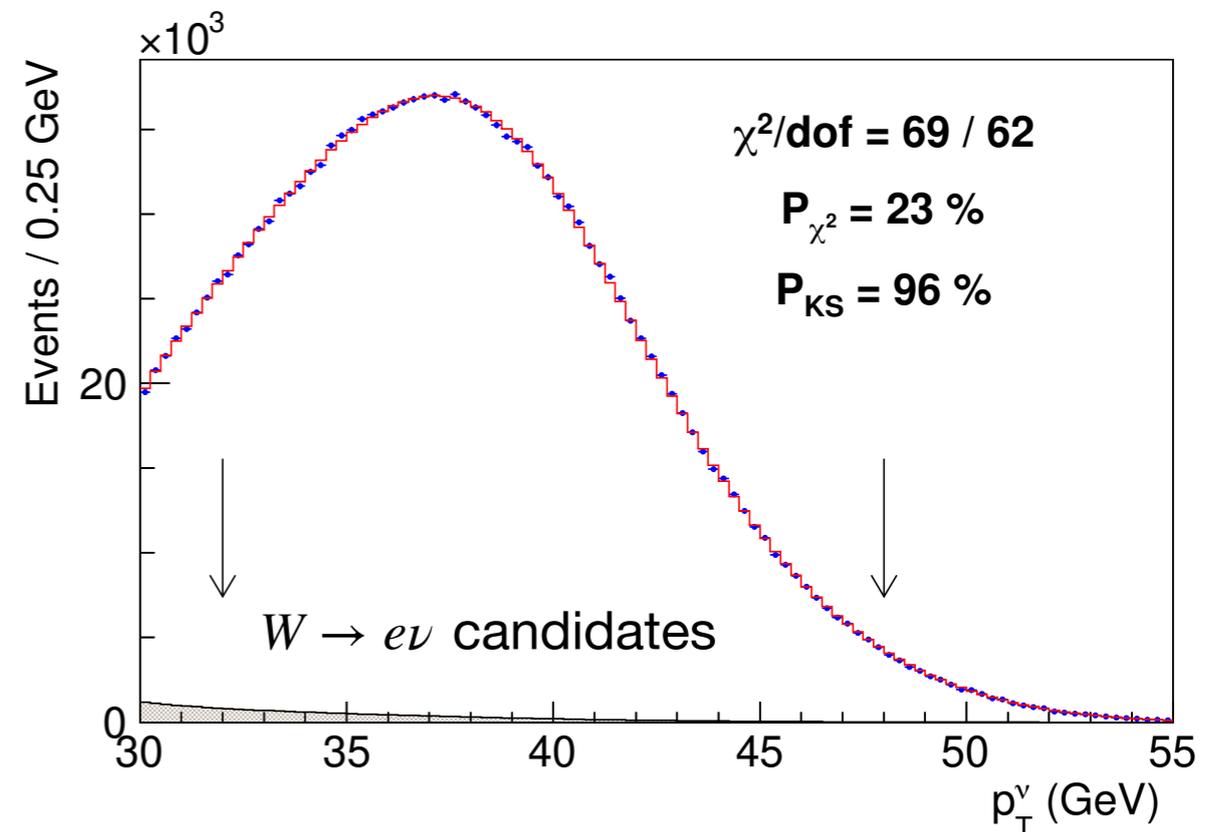
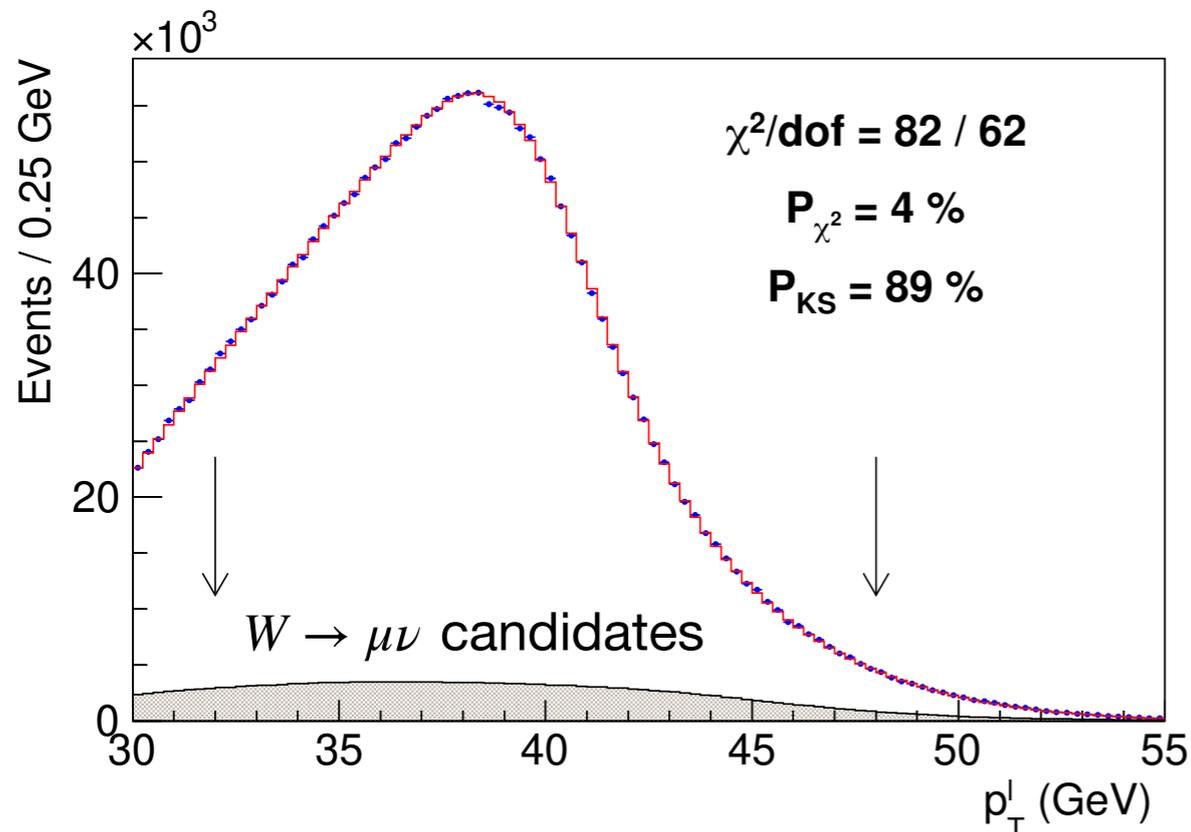
W boson backgrounds

Electroweak backgrounds modelled with fast parameterized simulation tuned with data and full simulation
Cross-checked with full simulation tuned to data

Largest background is $Z \rightarrow \mu\mu$ with one unreconstructed muon: 7.4% of data sample

$W \rightarrow \tau\nu$ background is $\sim 1\%$ in each channel: largest background in electron sample

Background from hadrons misreconstructed as leptons estimated using data: 0.2-0.3%



W boson production

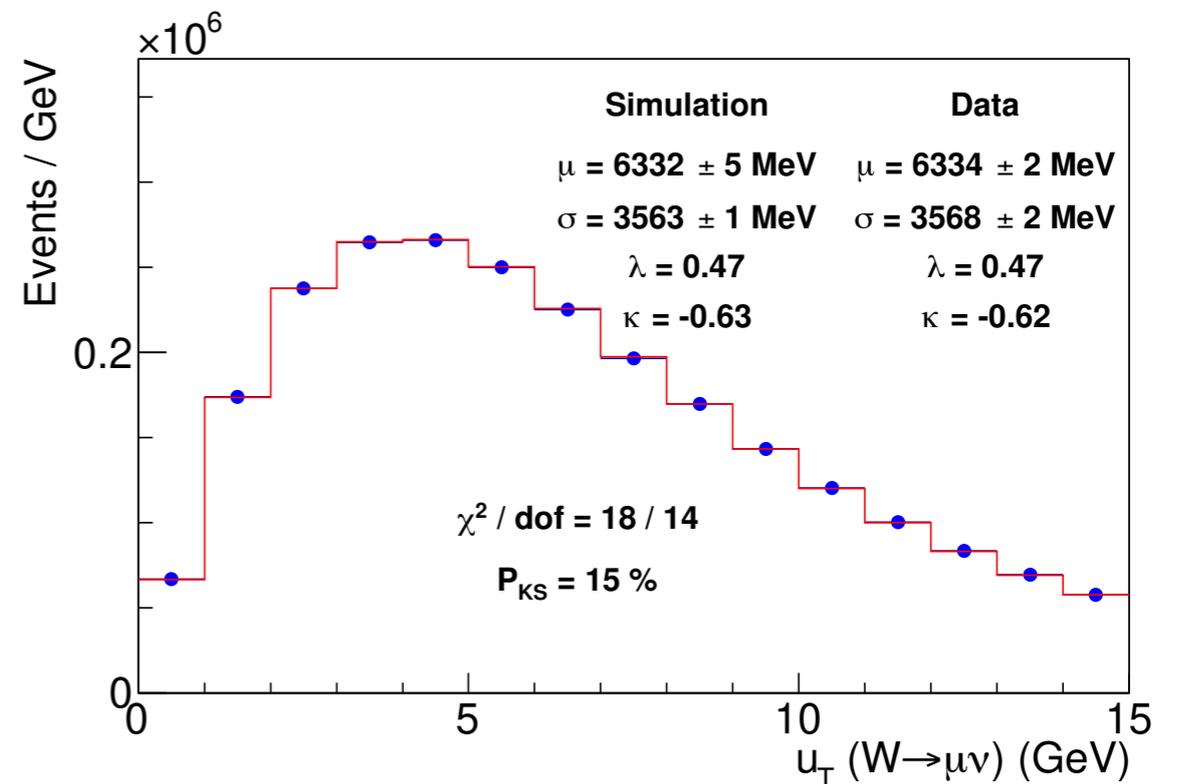
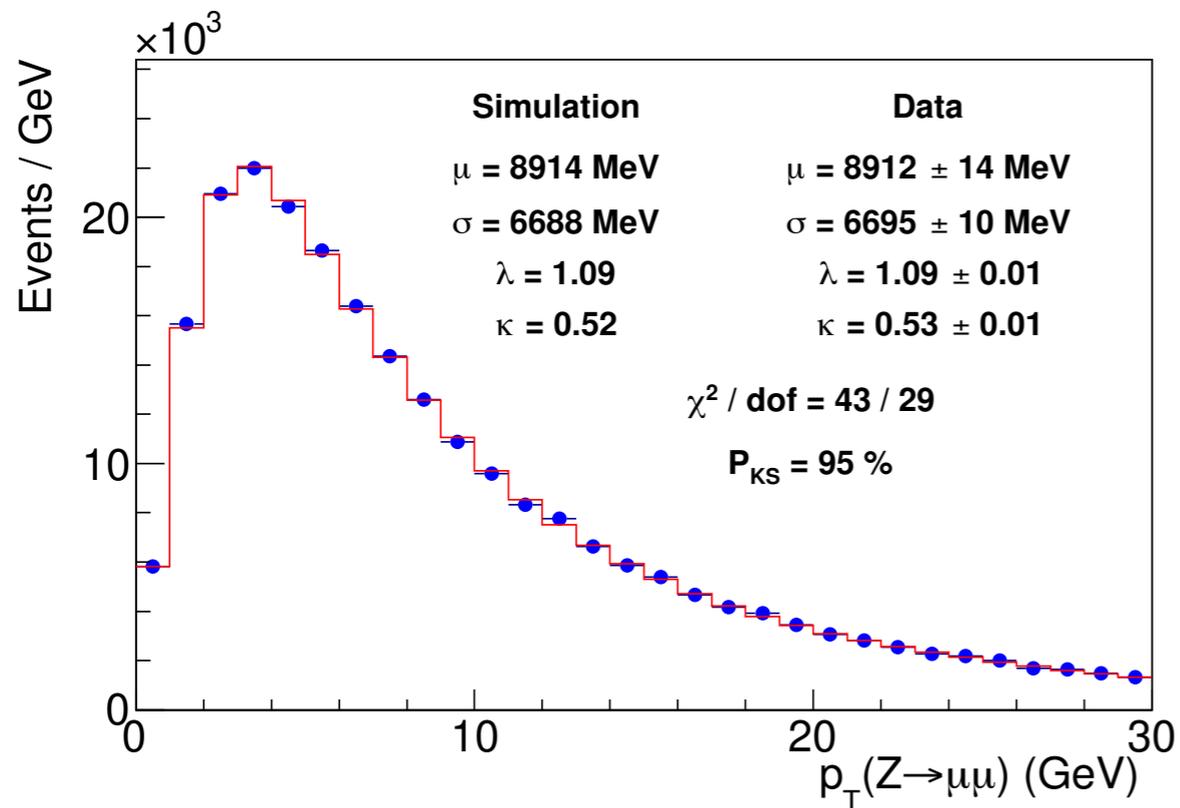
Boson p_T impacts the p_T distributions of the decay leptons

Resbos used to generate events with non-perturbative parameters and NNLL resummation to model the region of low boson p_T

Z boson p_T used to constrain the non-perturbative parameter g_2 and the perturbative coupling α_s

Resbos models W boson p_T well

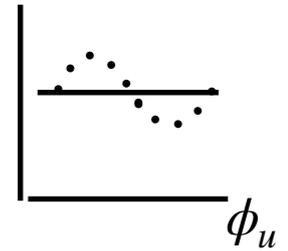
uncertainty estimated using DYQT and constrained with data



Recoil calibration

First step is the alignment of the calorimeters

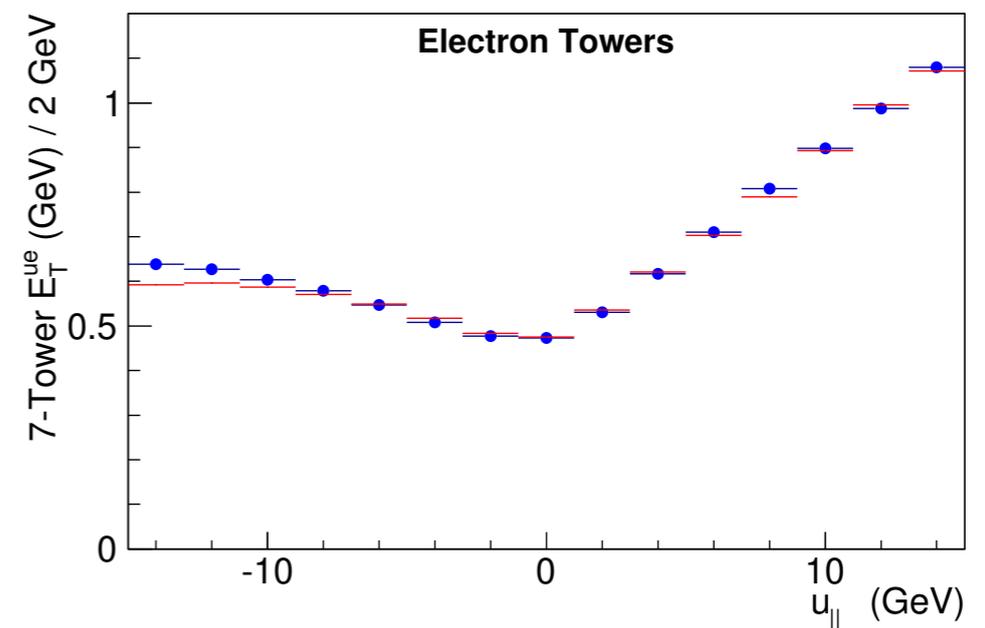
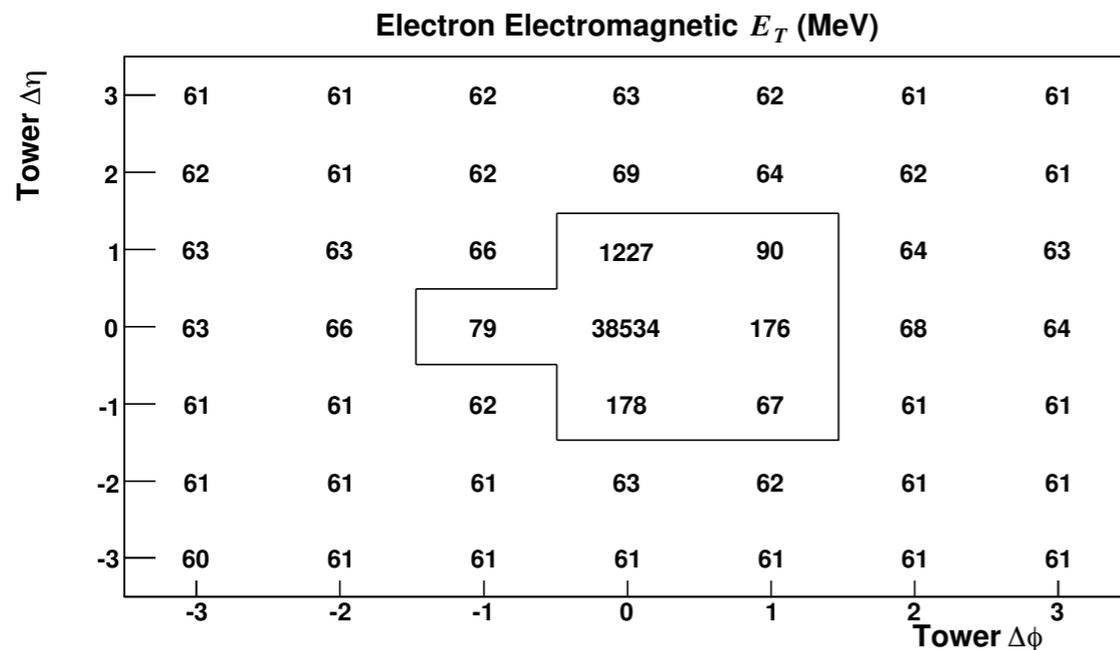
Misalignments relative to the beam axis cause a modulation in the recoil direction
Alignment performed separately for each run period using min bias data



Second step is the reconstruction of the recoil

Remove towers traversed by identified leptons

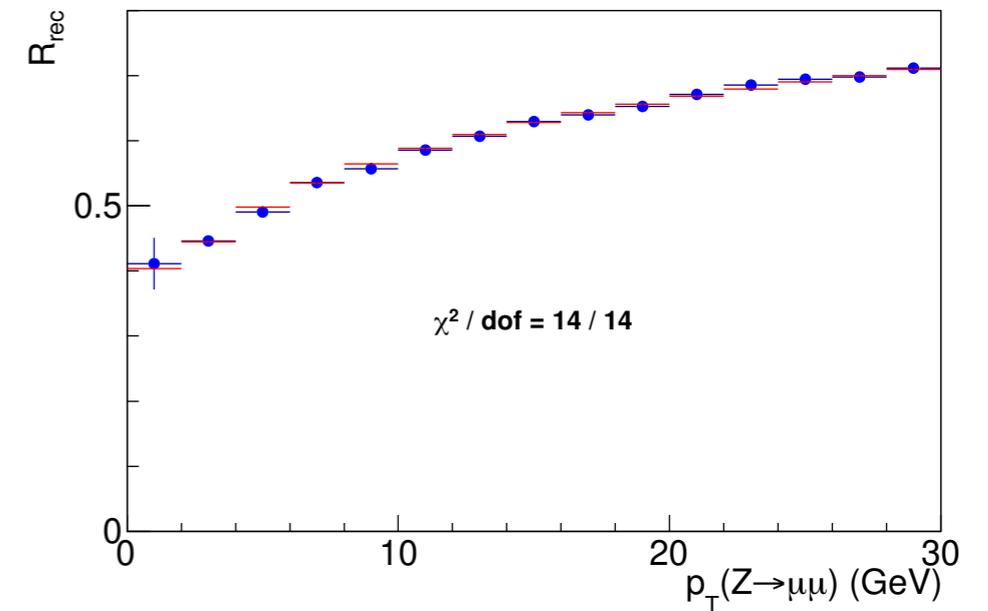
Remove corresponding recoil energy in simulation using towers rotated by 90°
validate using towers rotated by 180°



Recoil calibration

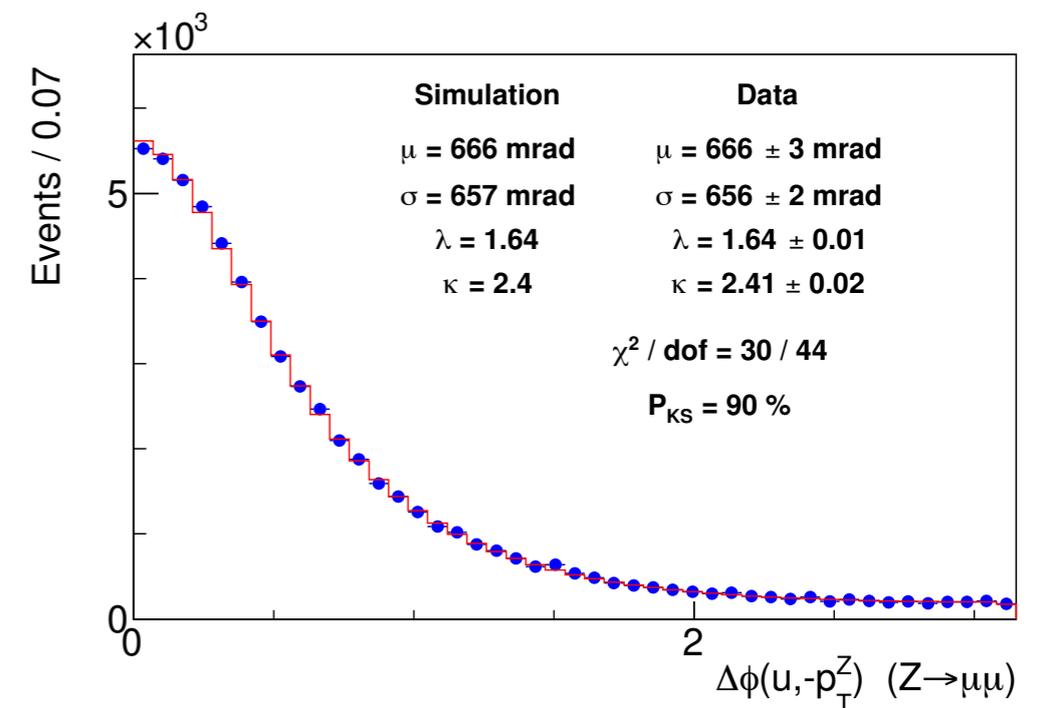
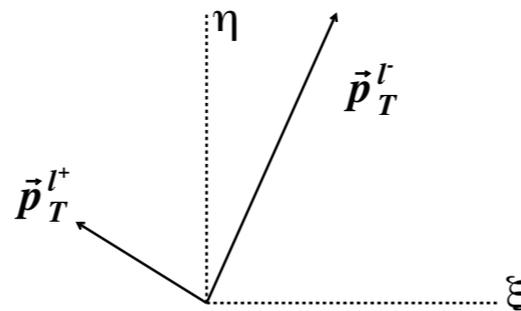
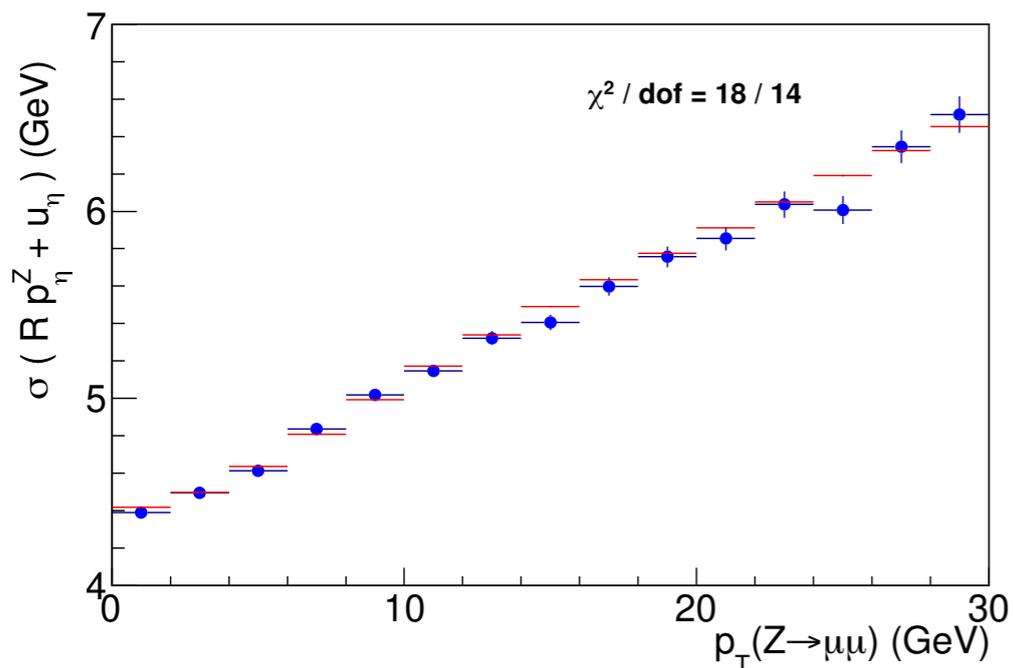
Third step is the calibration of the recoil response

Use ratio of recoil magnitude to p_{T^Z} along direction of p_{T^Z}



Fourth step is the calibration of the recoil resolution

Includes jet-like energy and angular resolution, additional dijet fraction term, and pileup

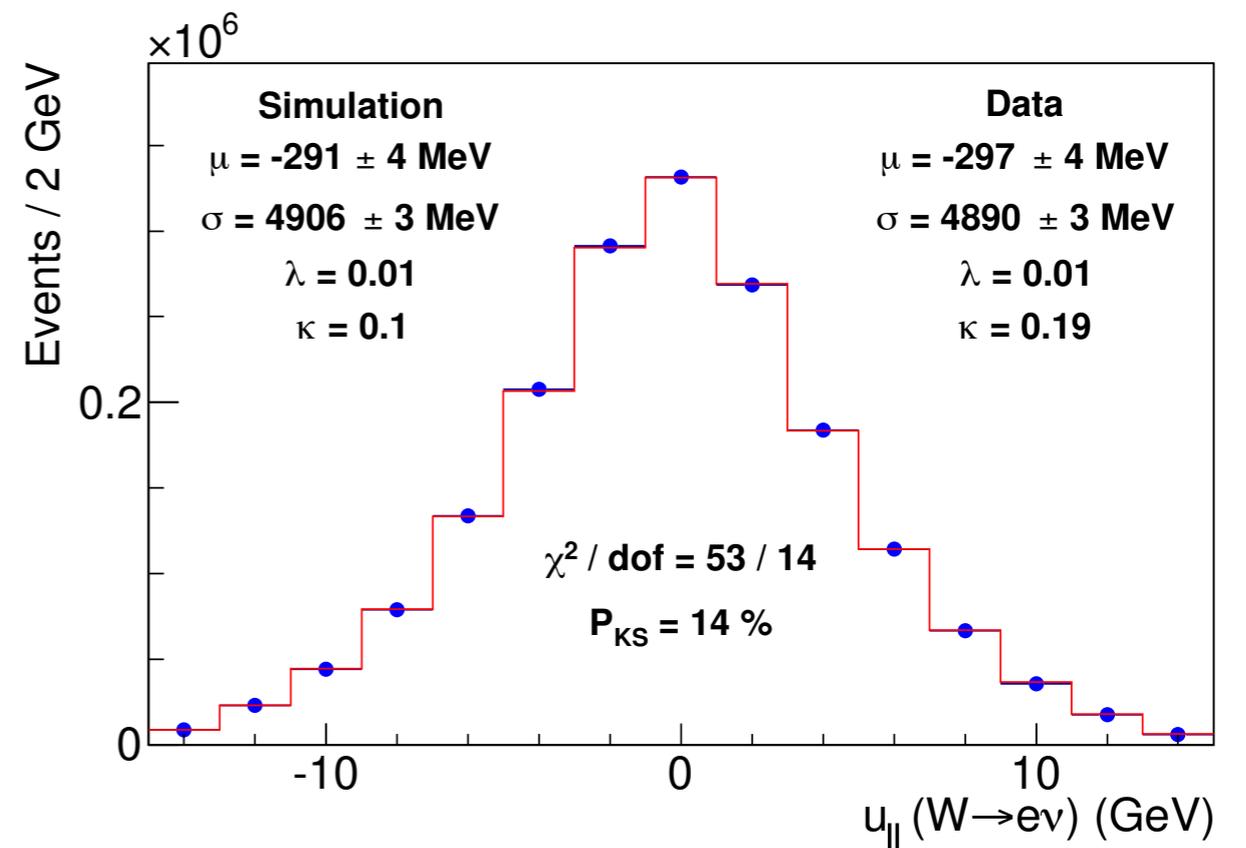
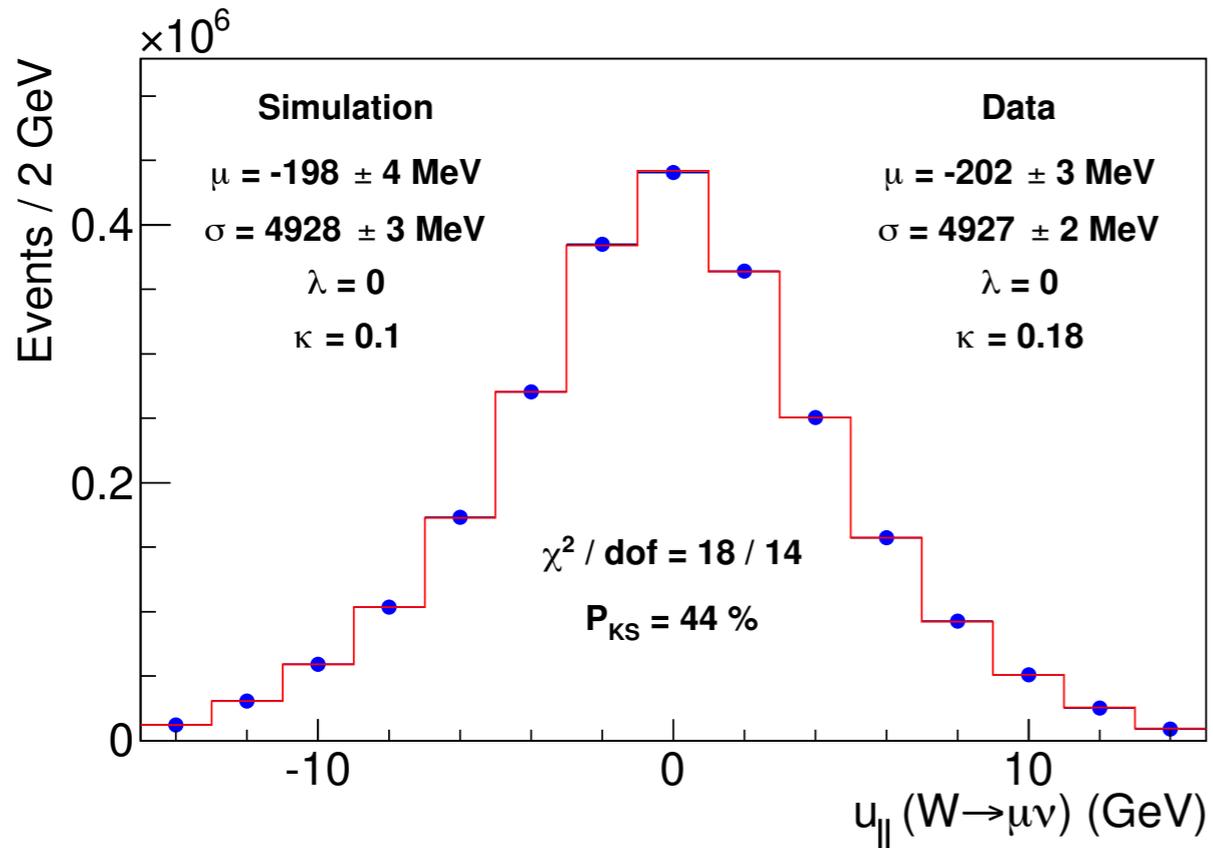


Recoil validation

W boson recoil distributions validate the model

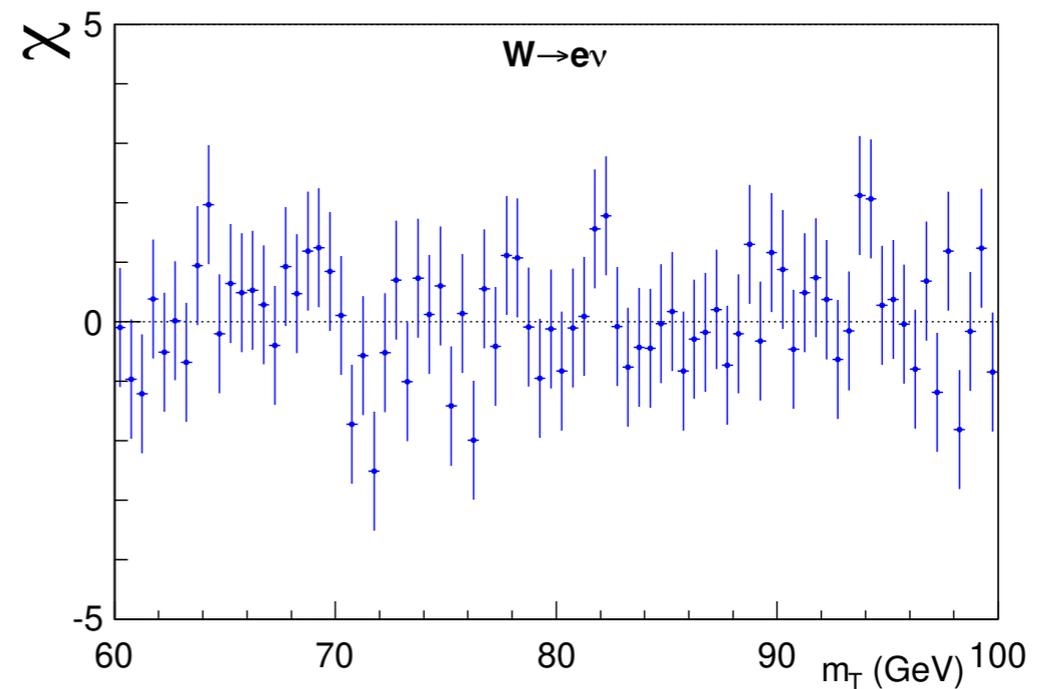
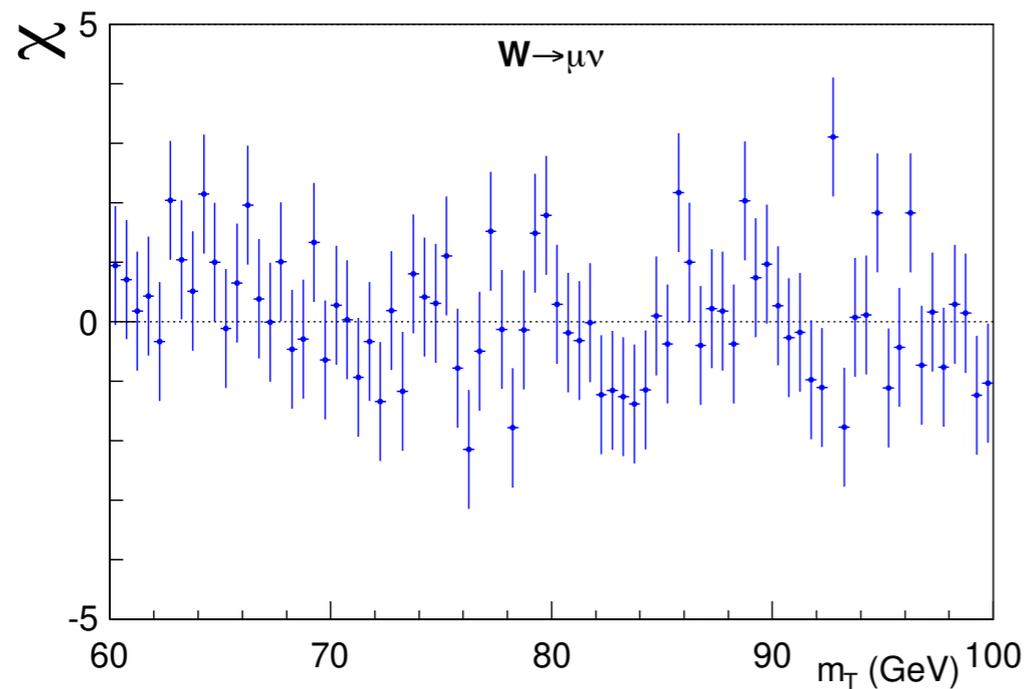
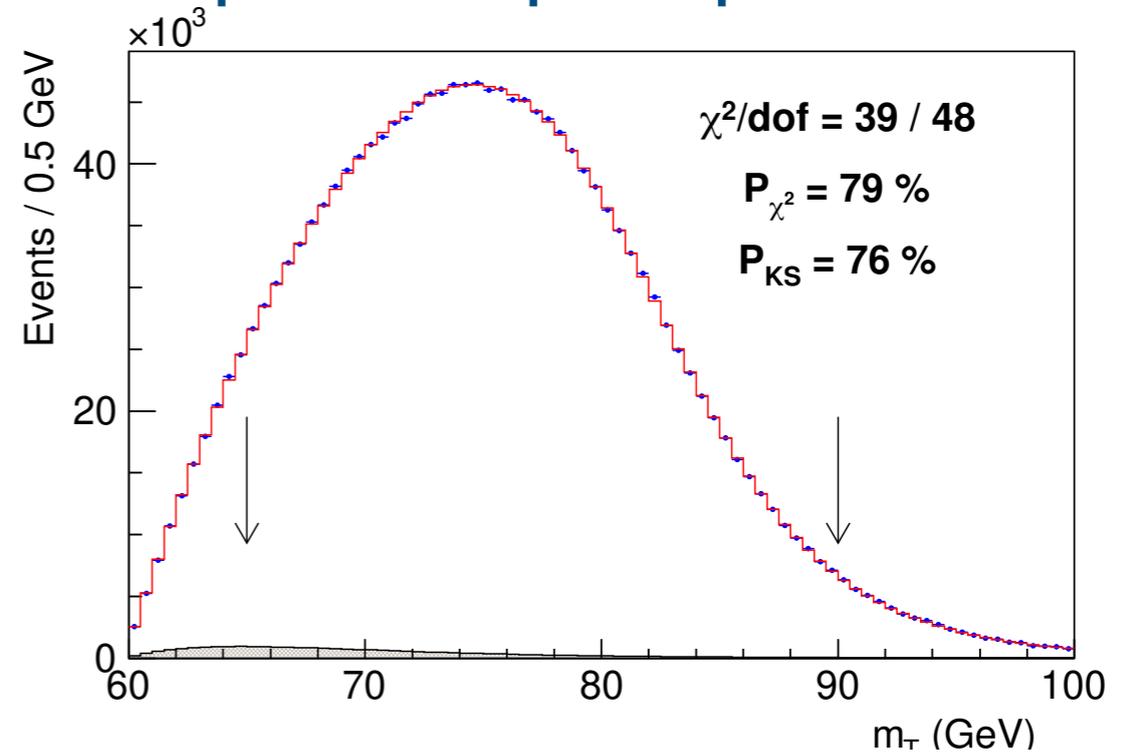
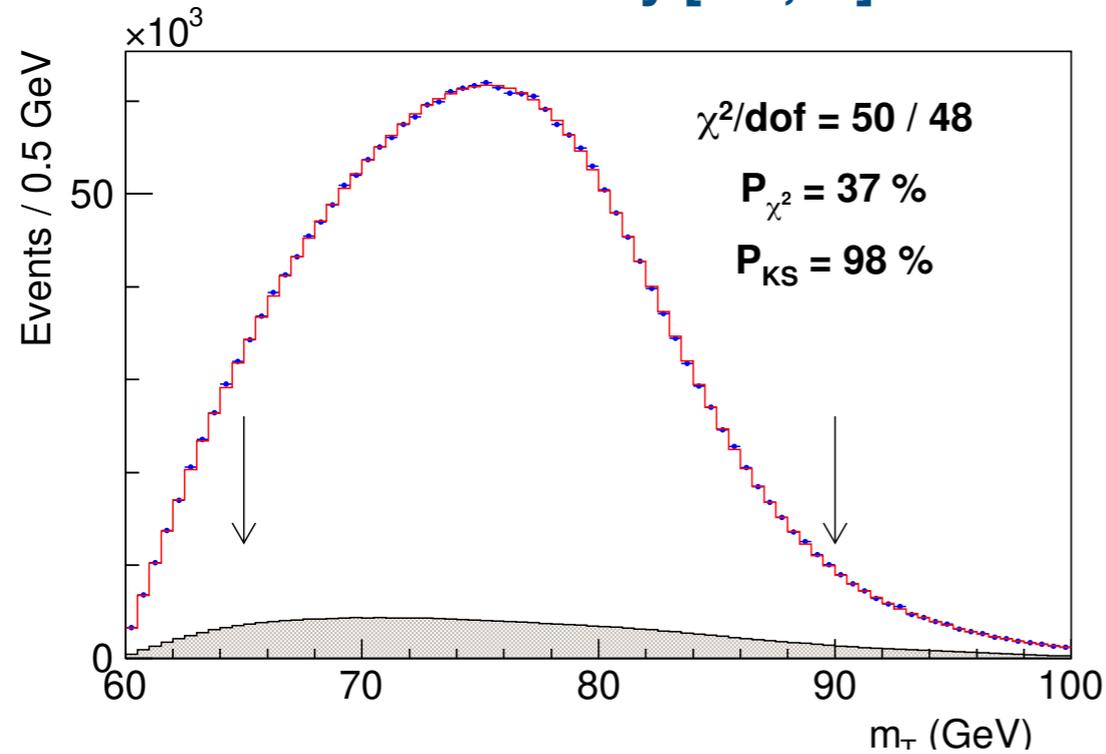
Most important is the recoil projected along the charged-lepton's momentum ($u_{||}$)

$$m_T \approx 2p_T \sqrt{1 + u_{||}/p_T} \approx 2p_T + u_{||}.$$



W boson mass measurement

Result blinded by [-50,50] MeV offset until all previous steps complete



W boson mass measurement

Combination	m_T fit		p_T^ℓ fit		p_T^ν fit		Value (MeV)	χ^2/dof	Probability (%)
	Electrons	Muons	Electrons	Muons	Electrons	Muons			
m_T	✓	✓					80 439.0 ± 9.8	1.2 / 1	28
p_T^ℓ			✓	✓			80 421.2 ± 11.9	0.9 / 1	36
p_T^ν					✓	✓	80 427.7 ± 13.8	0.0 / 1	91
m_T & p_T^ℓ	✓	✓	✓	✓			80 435.4 ± 9.5	4.8 / 3	19
m_T & p_T^ν	✓	✓			✓	✓	80 437.9 ± 9.7	2.2 / 3	53
p_T^ℓ & p_T^ν			✓	✓	✓	✓	80 424.1 ± 10.1	1.1 / 3	78
Electrons	✓		✓		✓		80 424.6 ± 13.2	3.3 / 2	19
Muons		✓		✓		✓	80 437.9 ± 11.0	3.6 / 2	17
All	✓	✓	✓	✓	✓	✓	80 433.5 ± 9.4	7.4 / 5	20

Fit difference	Muon channel	Electron channel
$M_W(\ell^+) - M_W(\ell^-)$	$-7.8 \pm 18.5_{\text{stat}} \pm 12.7_{\text{COT}}$	$14.7 \pm 21.3_{\text{stat}} \pm 7.7_{\text{stat}}^{\text{E/P}} (0.4 \pm 21.3_{\text{stat}})$
$M_W(\phi_\ell > 0) - M_W(\phi_\ell < 0)$	$24.4 \pm 18.5_{\text{stat}}$	$9.9 \pm 21.3_{\text{stat}} \pm 7.5_{\text{stat}}^{\text{E/P}} (-0.8 \pm 21.3_{\text{stat}})$
$M_Z(\text{run} > 271100) - M_Z(\text{run} < 271100)$	$5.2 \pm 12.2_{\text{stat}}$	$63.2 \pm 29.9_{\text{stat}} \pm 8.2_{\text{stat}}^{\text{E/P}} (-16.0 \pm 29.9_{\text{stat}})$

Summary

Measurement of W boson mass with <10 MeV precision achieved with complete CDF data set

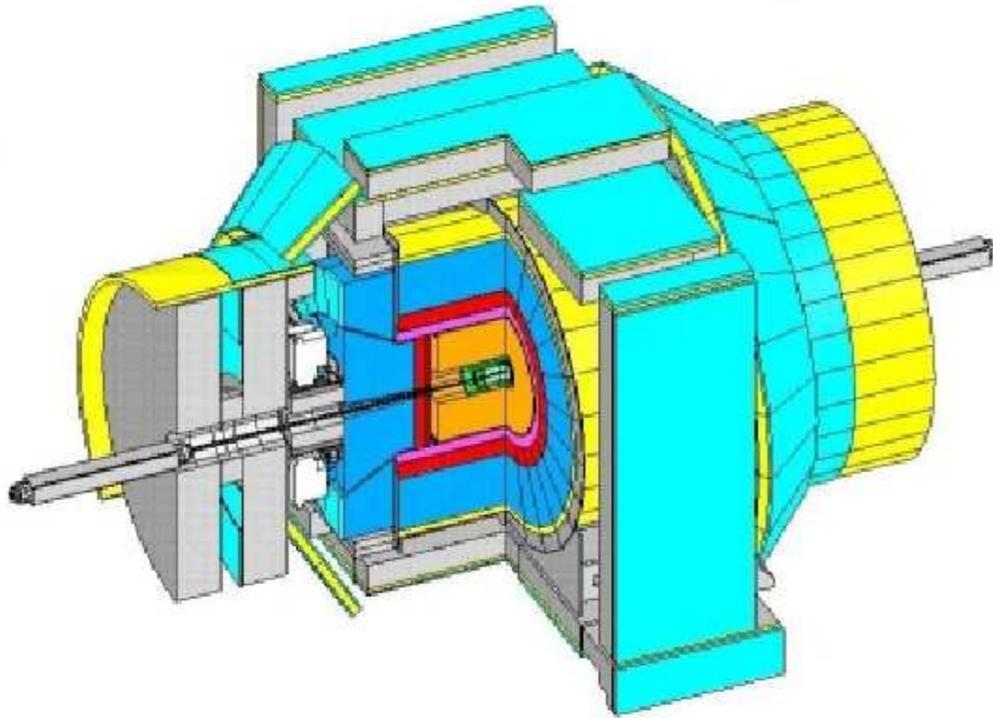
Result of >20 years of experience with the CDF II detector

Achieved precision required flexibility: all experimental aspects controlled by the analysis team
Reconstruction, alignment, calibration, simulation, analysis

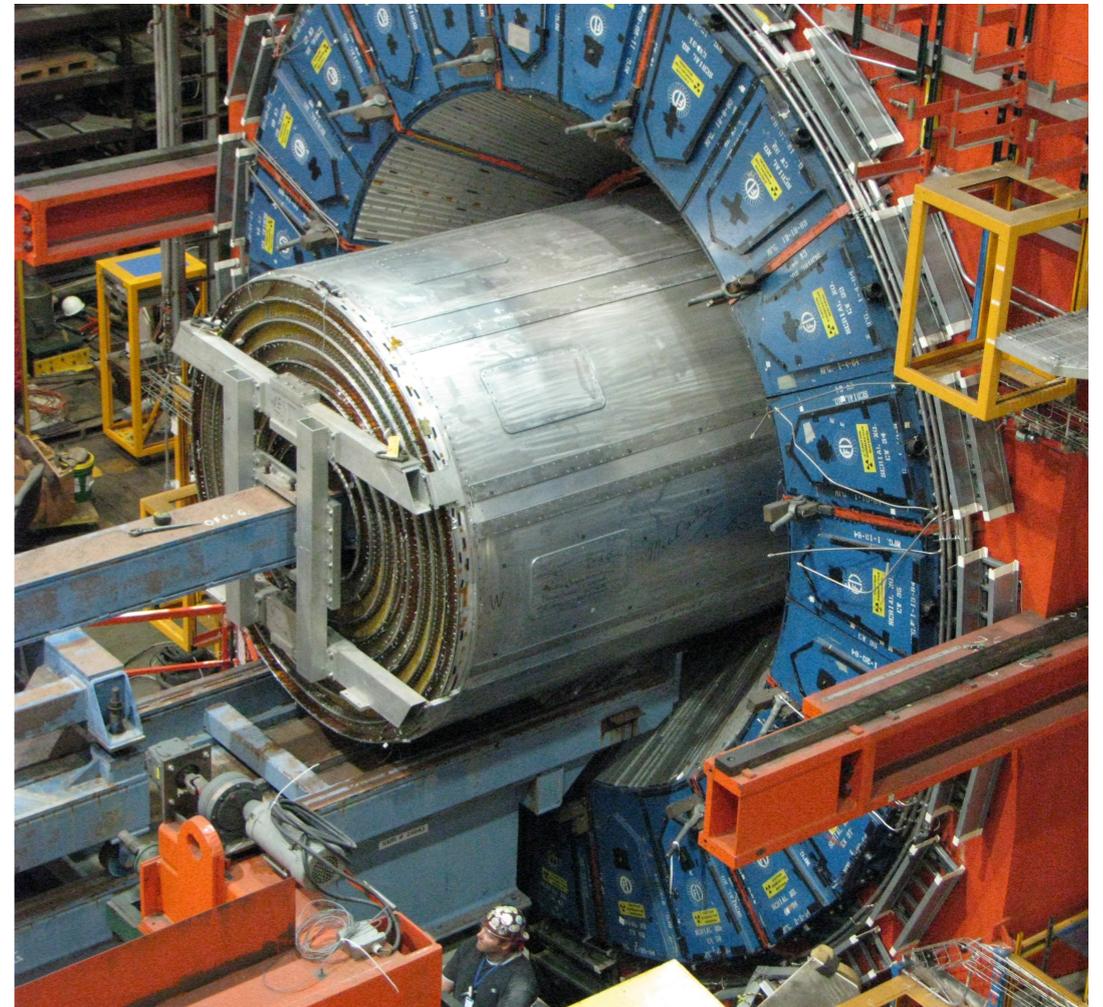
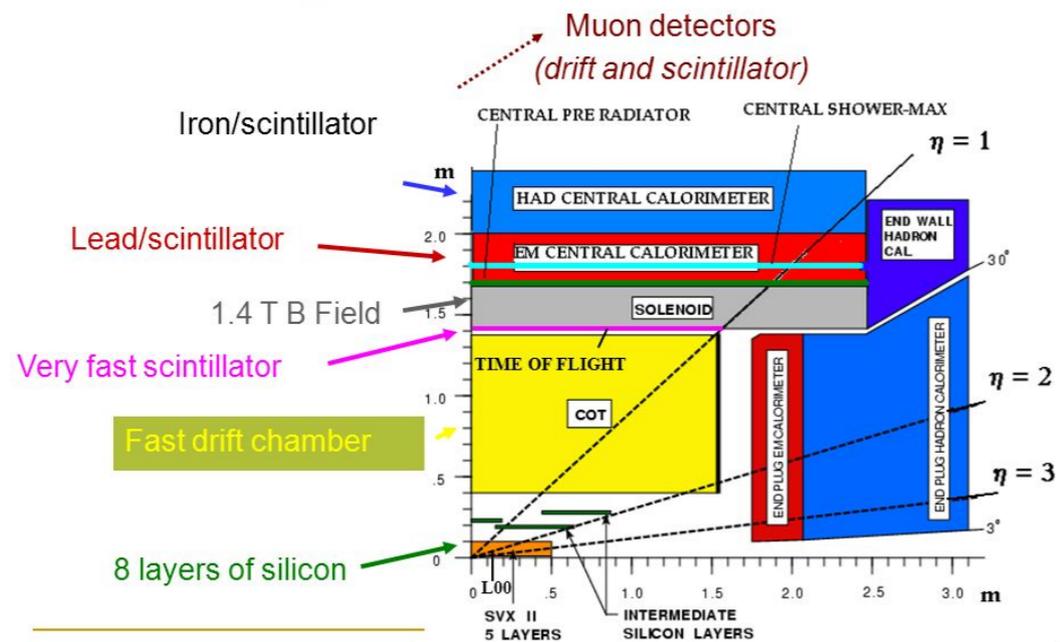
Analysis procedures approved pre-blinding and frozen

Surprising result motivates expanded study of m_W measurements and procedures

Backup



CDF Components



$$\xi = m(\phi) [0.29(1 - |Z|) + (1 - Z^2)]$$

$$m(\phi) = a \cos \phi_{wp} + o$$

Uncertainties

Source of systematic uncertainty	m_T fit			p_T^ℓ fit			p_T^ν fit		
	Electrons	Muons	Common	Electrons	Muons	Common	Electrons	Muons	Common
Lepton energy scale	5.8	2.1	1.8	5.8	2.1	1.8	5.8	2.1	1.8
Lepton energy resolution	0.9	0.3	-0.3	0.9	0.3	-0.3	0.9	0.3	-0.3
Recoil energy scale	1.8	1.8	1.8	3.5	3.5	3.5	0.7	0.7	0.7
Recoil energy resolution	1.8	1.8	1.8	3.6	3.6	3.6	5.2	5.2	5.2
Lepton $u_{ }$ efficiency	0.5	0.5	0	1.3	1.0	0	2.6	2.1	0
Lepton removal	1.0	1.7	0	0	0	0	2.0	3.4	0
Backgrounds	2.6	3.9	0	6.6	6.4	0	6.4	6.8	0
p_T^Z model	0.7	0.7	0.7	2.3	2.3	2.3	0.9	0.9	0.9
p_T^W / p_T^Z model	0.8	0.8	0.8	2.3	2.3	2.3	0.9	0.9	0.9
Parton distributions	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9
QED radiation	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7
Statistical	10.3	9.2	0	10.7	9.6	0	14.5	13.1	0
Total	13.5	11.8	5.8	16.0	14.1	7.9	18.8	17.1	7.4

Initial state LO & NLO

W+ initial	Type	Pythia LO	Madgraph LO	Madgraph NLO
u dbar	v-v	81.7%	82.0%	82.7%
dbar u	s-s	8.9%	9.0%	8.8%
u sbar	v-s	1.6%	1.9%	1.8%
sbar u	s-s	0.3%	0.3%	0.3%
c sbar	s-s	2.9%	2.9%	-
sbar c	s-s	2.9%	2.9%	-
c dbar	s-v	0.7%	0.7%	-
dbar c	s-s	0.2%	0.2%	-
u g	v-g		-	3.7%
g dbar	g-v		-	1.8%
g u	g-s		-	0.4%
dbar g	s-g		-	0.5%
g sbar	g-s		-	0.02%
sbar g	s-g		-	0.02%