



International Center for Quantum-
field Measurement System for
Studies of the Universe and Particles

Light dark matter detection with collective excitation in matter

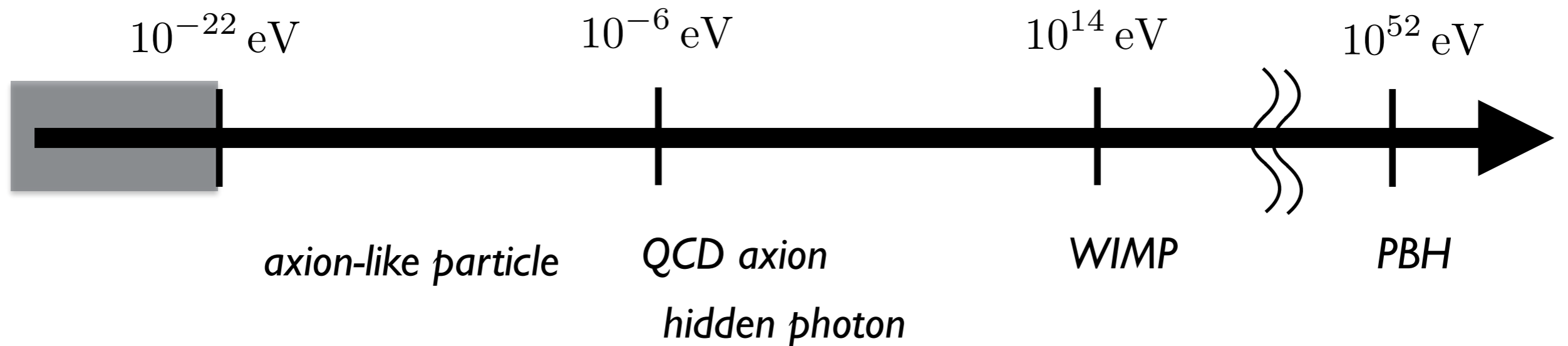
Kazunori Nakayama (Tohoku Univ & QUP)

Physics in LHC and beyond (2022/5/14)

Introduction

Dark matter search

- Dark matter mass range

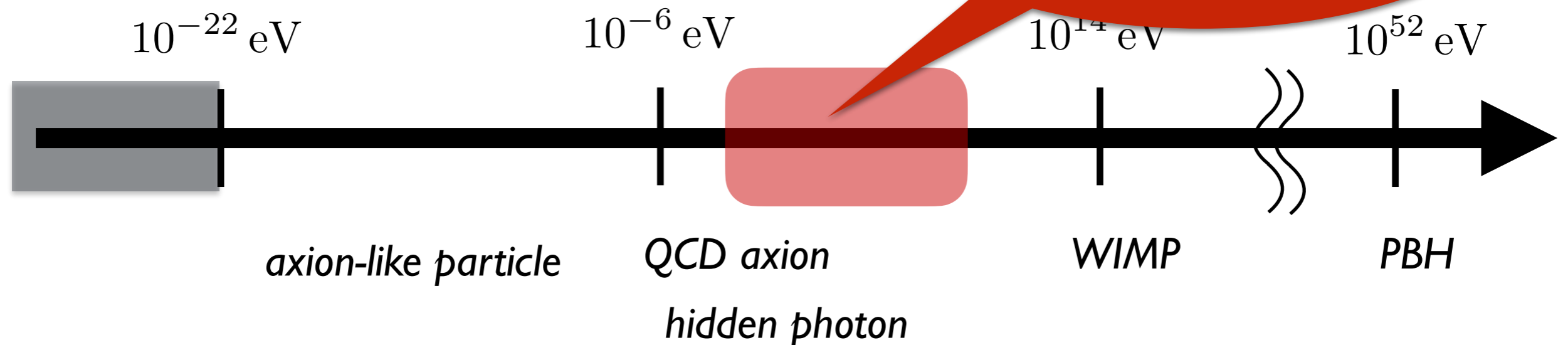


- We need **broad ideas** for **broad energy scales**

Direct detection, cosmic rays, accelerator experiments,
astronomical/cosmological observations,...

Dark matter search

- Dark matter mass range

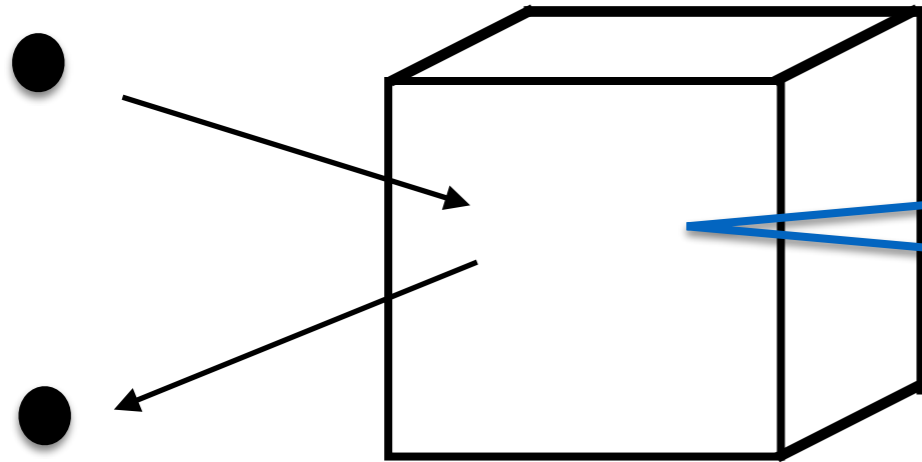


- We need **broad ideas** for **broad energy scales**

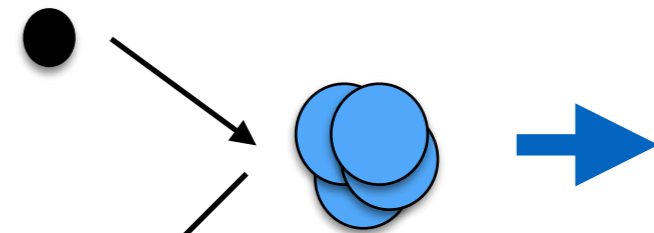
Direct detection, cosmic rays, accelerator experiments, astronomical/cosmological observations,...

Dark matter direct detection

DM



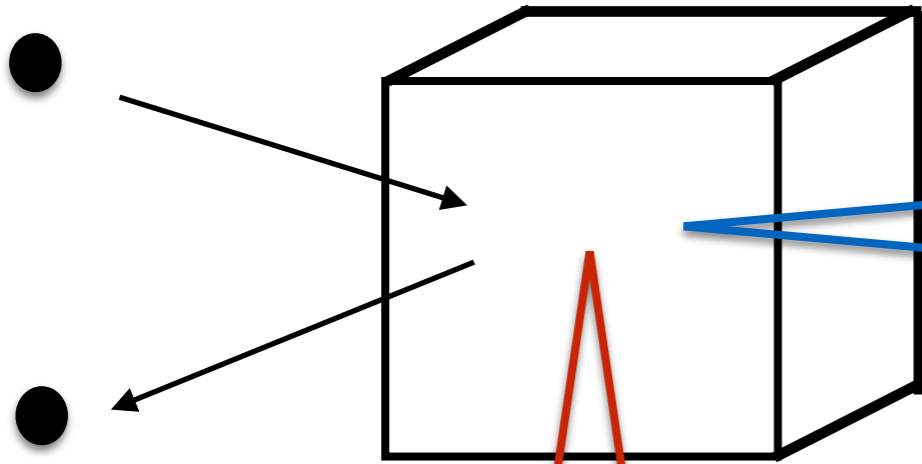
Nuclear recoil



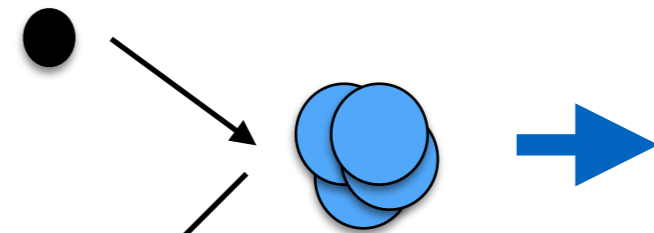
XENONIT, LUX, PandaX, ...

Dark matter direct detection

DM

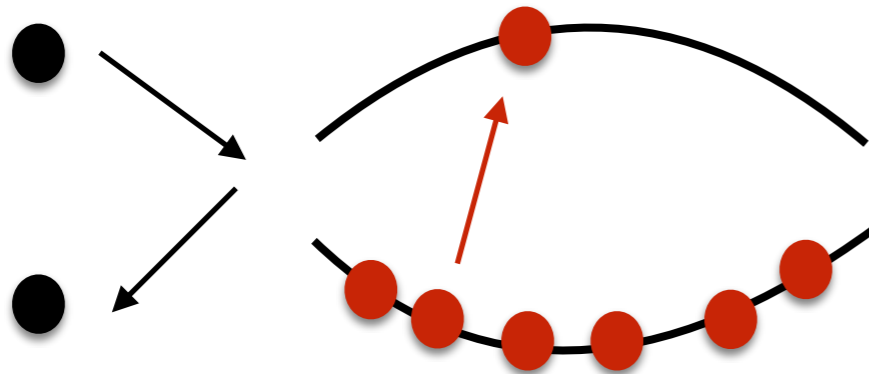


Nuclear recoil



XENONIT, LUX, PandaX, ...

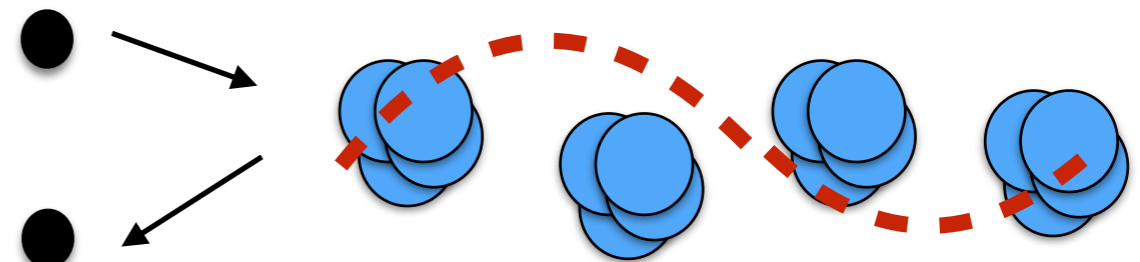
Bloch electron



SENSEI, DAMIC, ...

Collective excitation

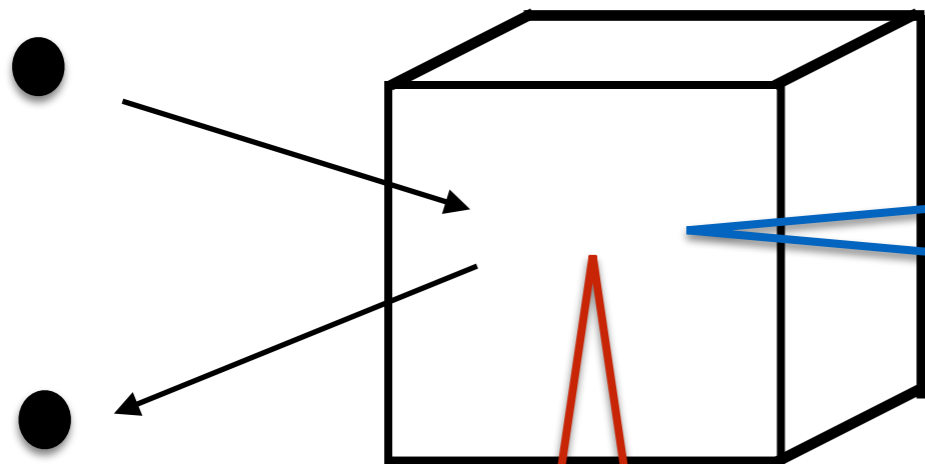
(phonon, magnon, ...)



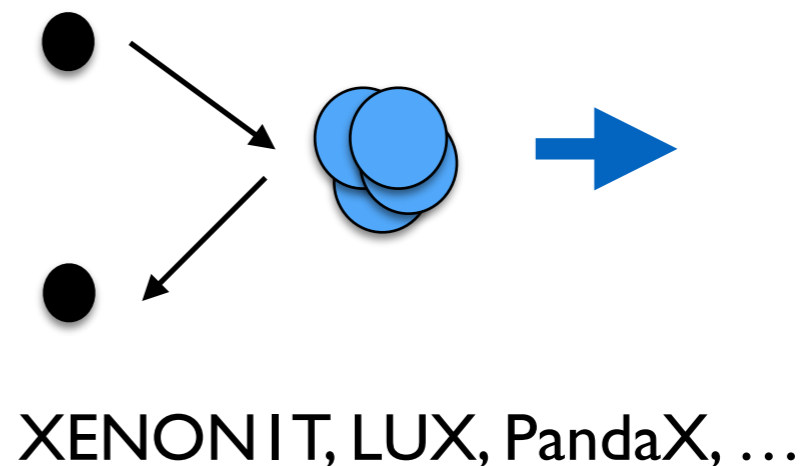
SPICE, HeRALD, ...

Dark matter direct detection

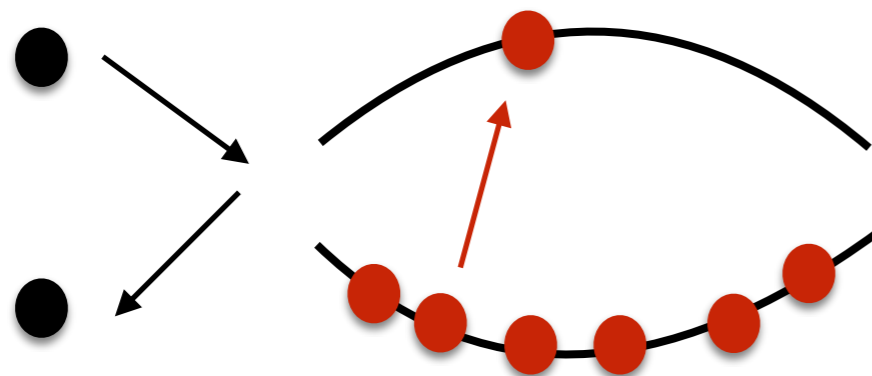
DM



Nuclear recoil

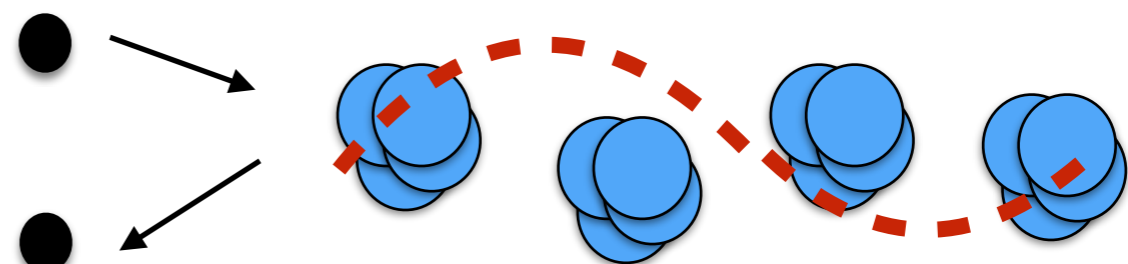


Bloch electron



SENSEI, DAMIC, ...

Collective excitation (phonon, magnon, ...)

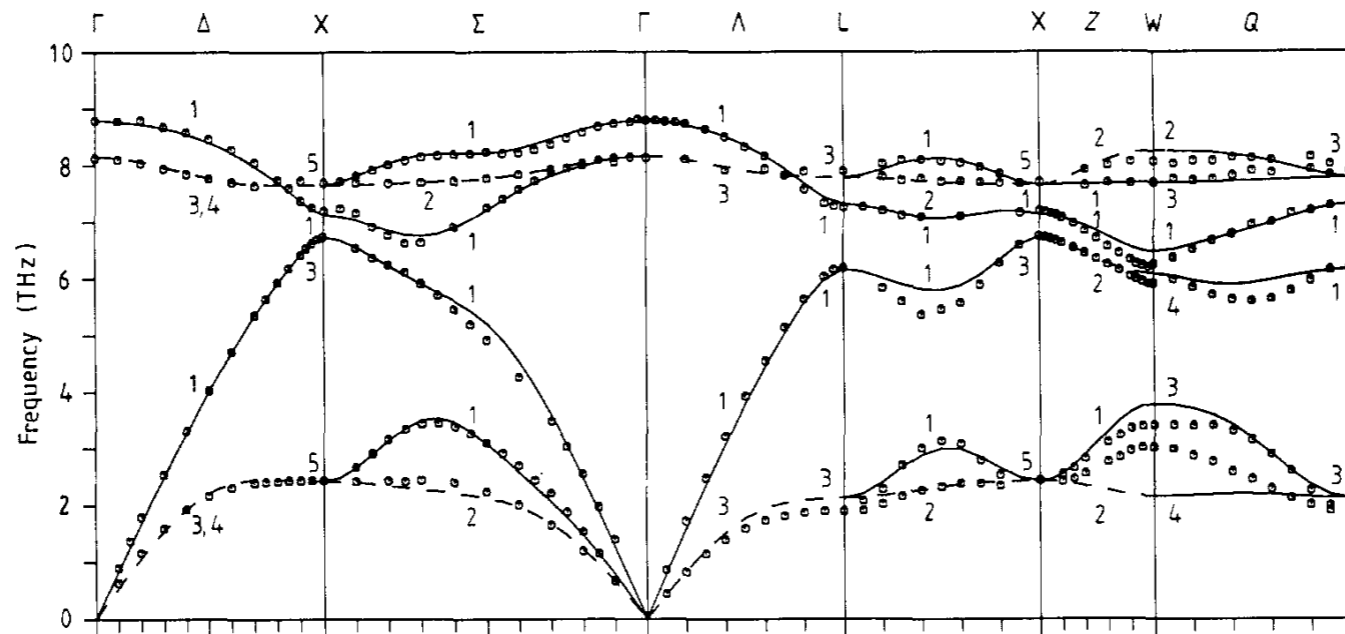


SPICE, HeRALD, ...

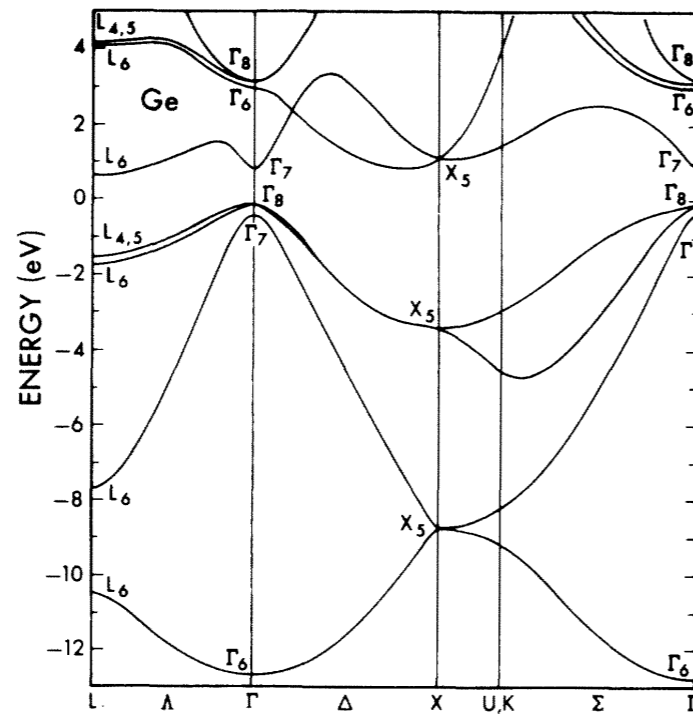
In this talk I will focus on **magnetic** collective excitations.

Dispersion of (quasi)particles in solids

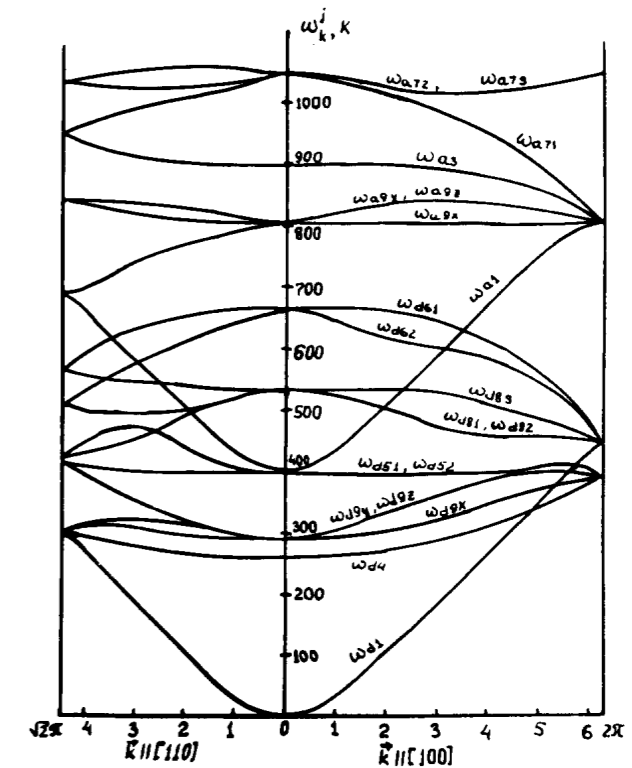
**Phonon
(GaAs)**



**Electron
(Ge)**

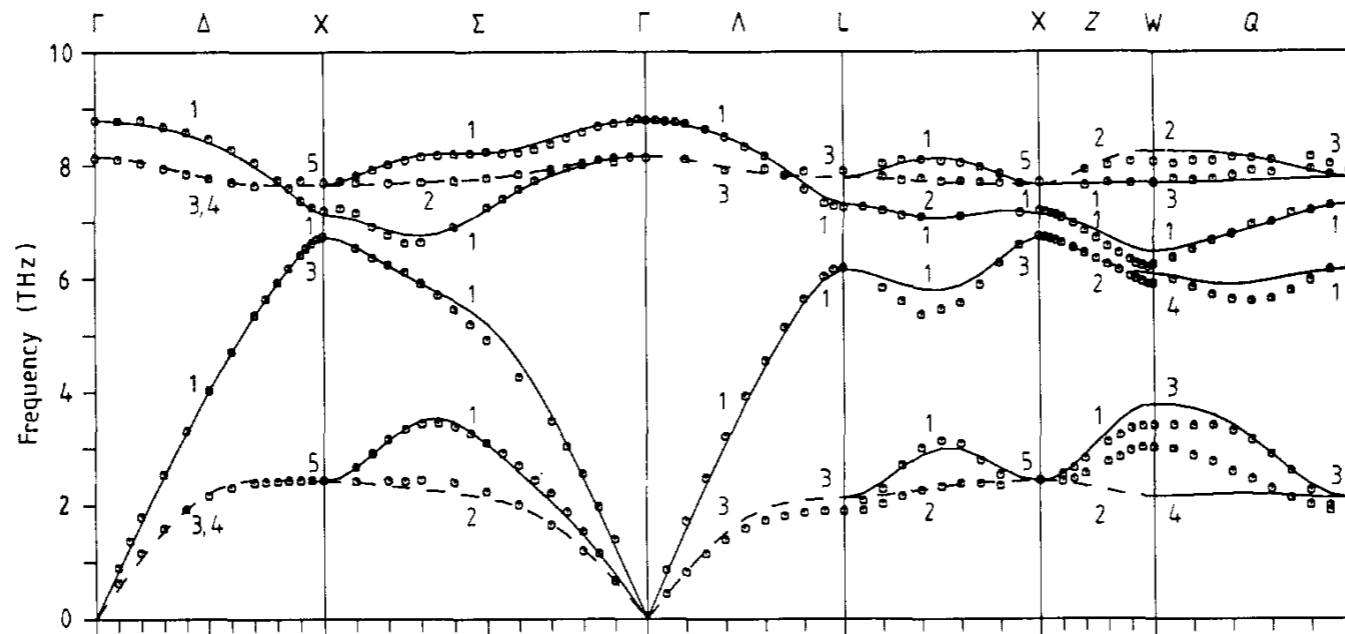


**Magnon
(YIG)**

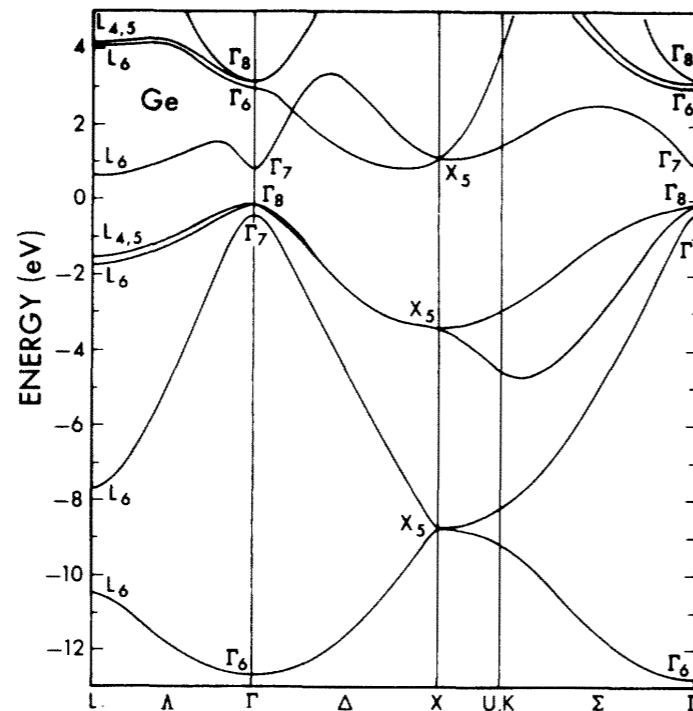


Dispersion of (quasi)particles in solids

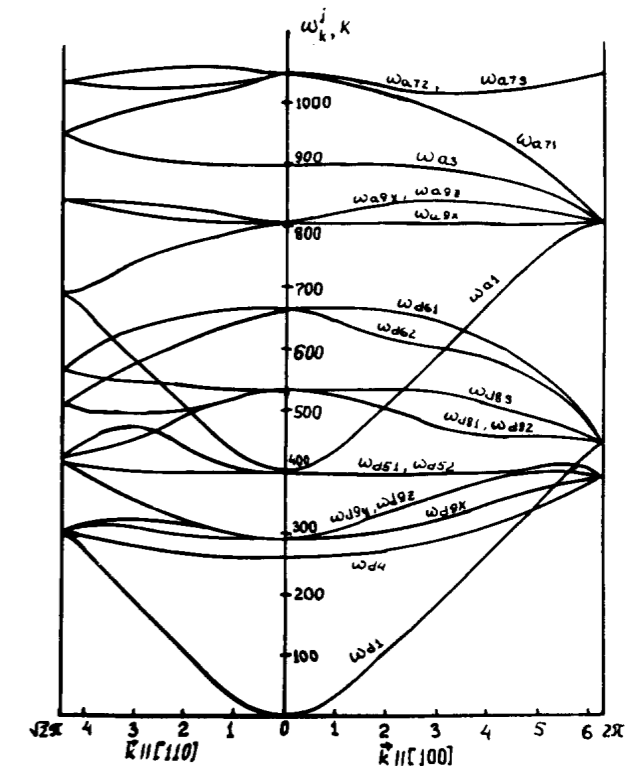
**Phonon
(GaAs)**



**Electron
(Ge)**



**Magnon
(YIG)**



Rich structure: useful for new particle search !

Towards light DM detection

- Low reaction threshold

Dispersion of (quasi-)particles in material

$$1 \text{ meV} \lesssim m_{\text{DM}} \lesssim 1 \text{ keV} \quad (\text{absorption : axion, hidden photon})$$

$$1 \text{ MeV} \lesssim m_{\text{DM}} \lesssim 1 \text{ GeV} \quad (\text{scatter})$$

- Low detection threshold

Developments of TES, Qubits, SNSPD, Opto-mechanical cavity, ...

—————> Single photon/phonon/electron detection

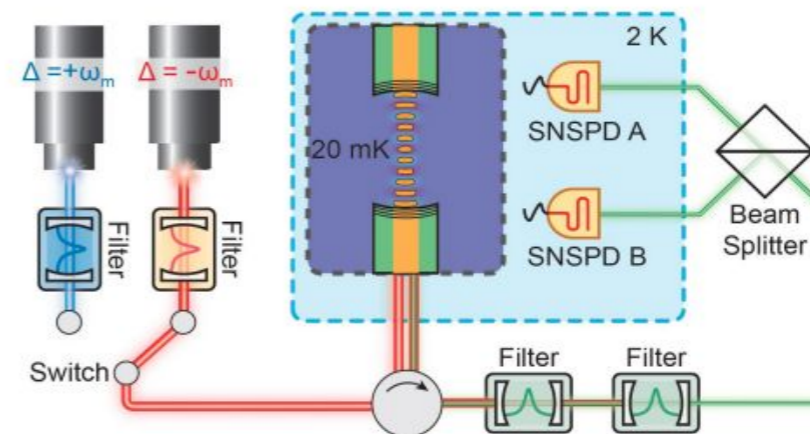
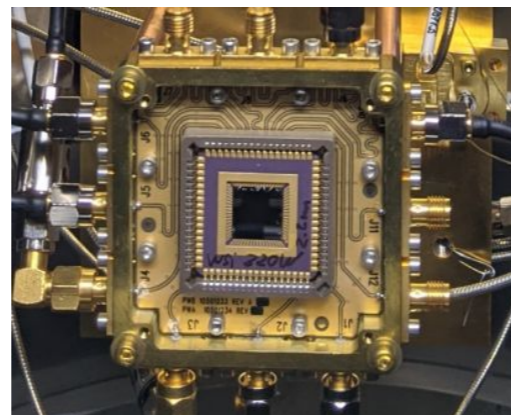
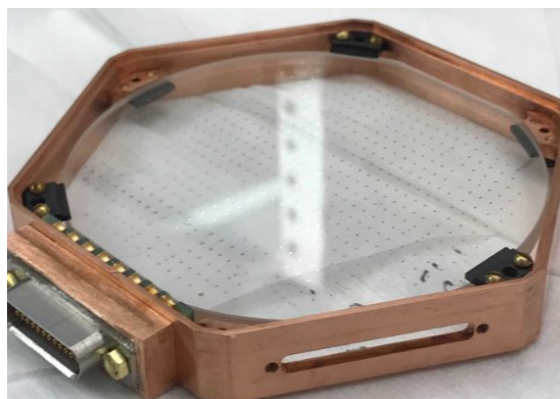
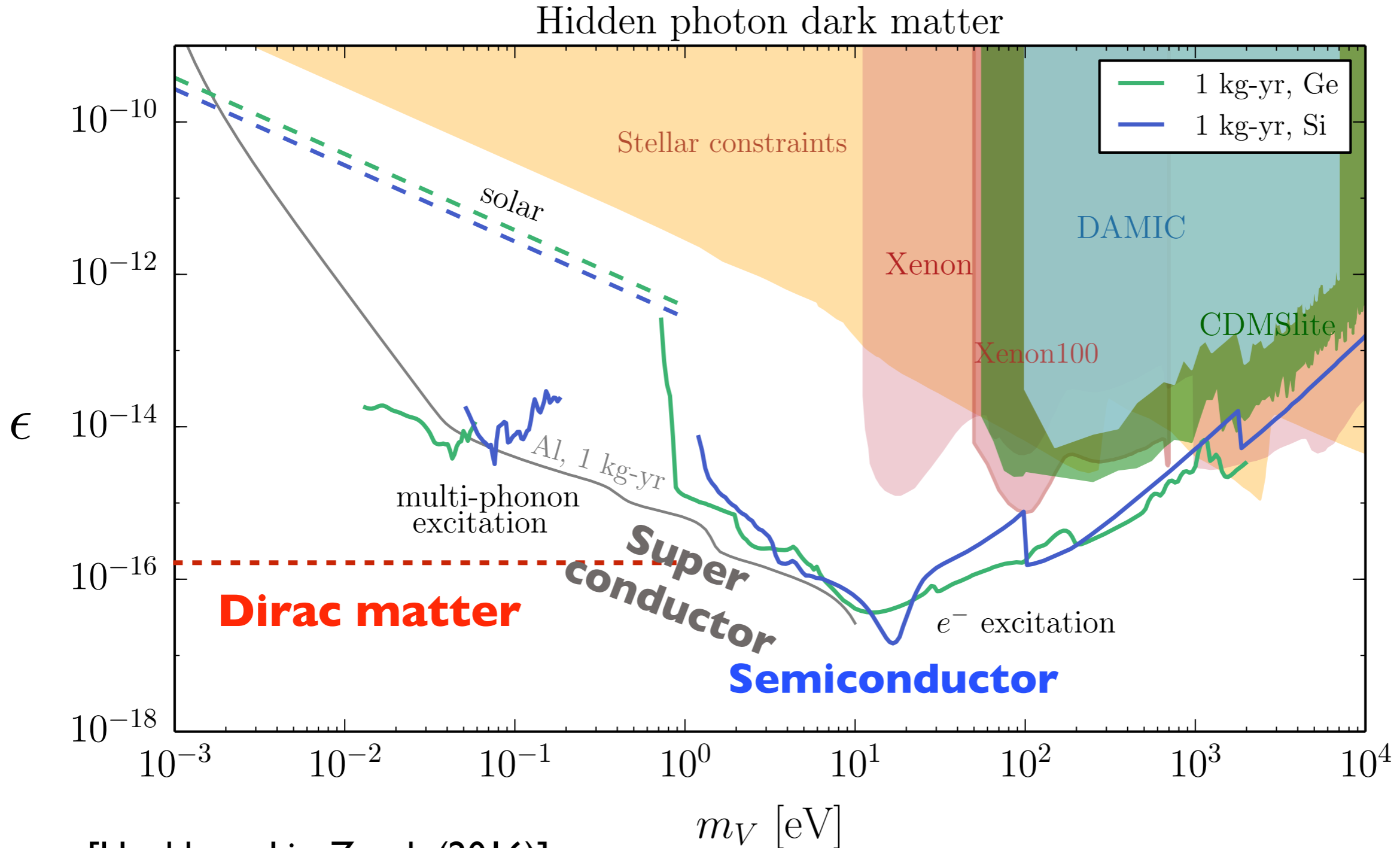


Figure from slides by
M. Garcia-Sciveres
(see Appendix)

DM detection with electron/phonon

DM absorption (hidden photon)

$$\mathcal{L} = -\frac{\epsilon}{2} F_{\mu\nu} H^{\mu\nu}$$



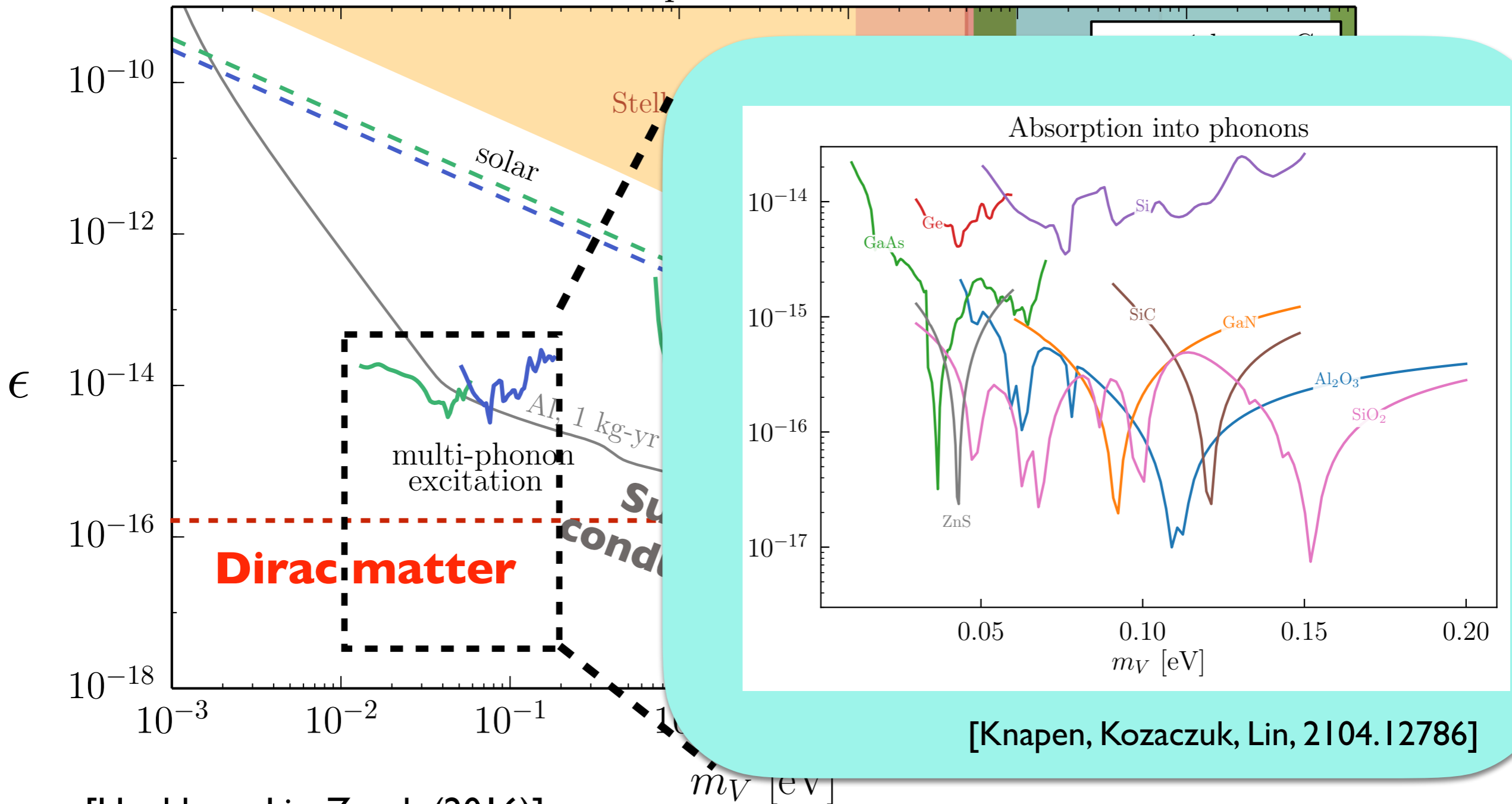
[Hochberg, Lin, Zurek (2016)]

DM detection with electron/phonon

DM absorption (hidden photon)

$$\mathcal{L} = -\frac{\epsilon}{2} F_{\mu\nu} H^{\mu\nu}$$

Hidden photon dark matter

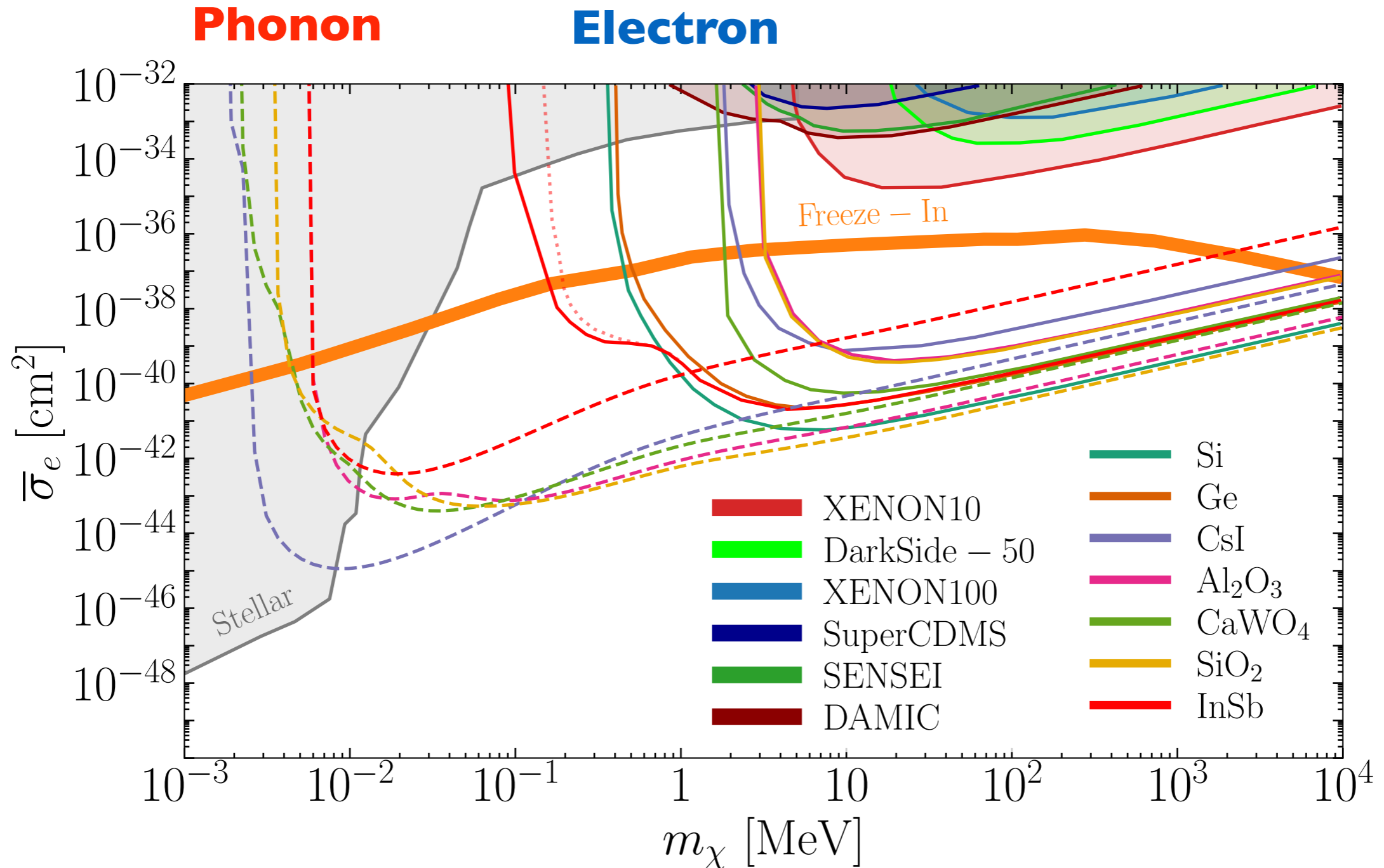


[Hochberg, Lin, Zurek (2016)]

[Knapen, Kozaczuk, Lin, 2104.12786]

DM detection with electron/phonon

DM scatter



[Griffin et al. (2019)]

1. DM detection with magnon

[Chigusa, Moroi, KN (2020)]

2. DM detection with condensed-matter axion

[Chigusa, Moroi, KN (2021)]

I. DM detection with magnon

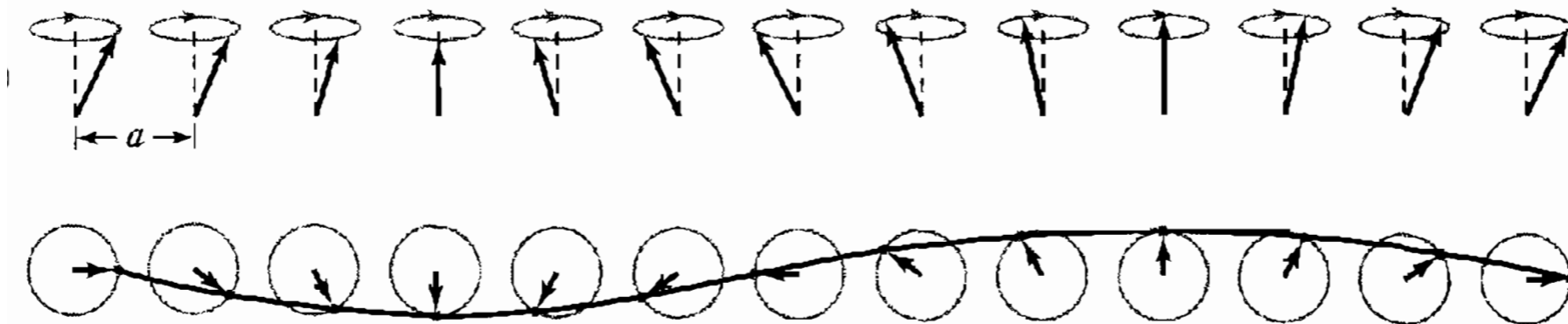
Heisenberg model for ferromagnet

- Heisenberg Hamiltonian

$$H_{\text{eff}} = -g\mu_B \sum_{\ell} \vec{B}^0 \cdot \vec{S}_{\ell} - \frac{J}{2} \sum_{\ell, \ell'} \vec{S}_{\ell} \cdot \vec{S}_{\ell'},$$

$J > 0$: spins are aligned for $T=0$ and $B=0$ (**Ferromagnet**)

- Fluctuation around the ground state : collective spin wave

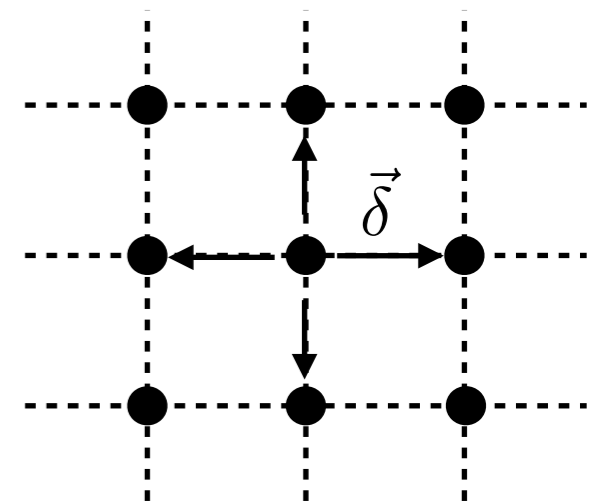


Magnon

- Quantized Hamiltonian in momentum space

$$S_\ell^+ = \sqrt{2s - \tilde{c}_\ell^\dagger \tilde{c}_\ell} \tilde{c}_\ell \quad S_\ell^- = \tilde{c}_\ell^\dagger \sqrt{2s - \tilde{c}_\ell^\dagger \tilde{c}_\ell} \quad S_\ell^z = s - \tilde{c}_\ell^\dagger \tilde{c}_\ell \quad (S_\ell^\pm \equiv S_\ell^x \pm iS_\ell^y)$$

$$H = \sum_k \left[\omega_L + Js \sum_{\vec{a}} (1 - \gamma_{\vec{k}}) \right] c_{\vec{k}}^\dagger c_{\vec{k}} = \sum_k \omega_k c_{\vec{k}}^\dagger c_{\vec{k}}$$



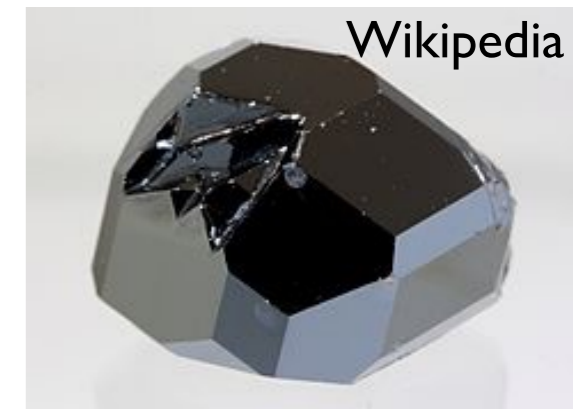
- Magnon dispersion relation:

$$\omega_{\vec{k}} \simeq \omega_L + JsL^2 k^2 \equiv \omega_L + \frac{k^2}{2M}$$

$$\gamma_{\vec{k}} = \frac{1}{z} \sum_{\vec{\delta}} e^{i\vec{k} \cdot \vec{\delta}}$$

$$\omega_L \equiv g\mu_B B_z^0 \simeq 1.2 \times 10^{-4} \text{ eV} \left(\frac{B_z^0}{1 \text{ T}} \right) \quad \text{: Larmor frequency}$$

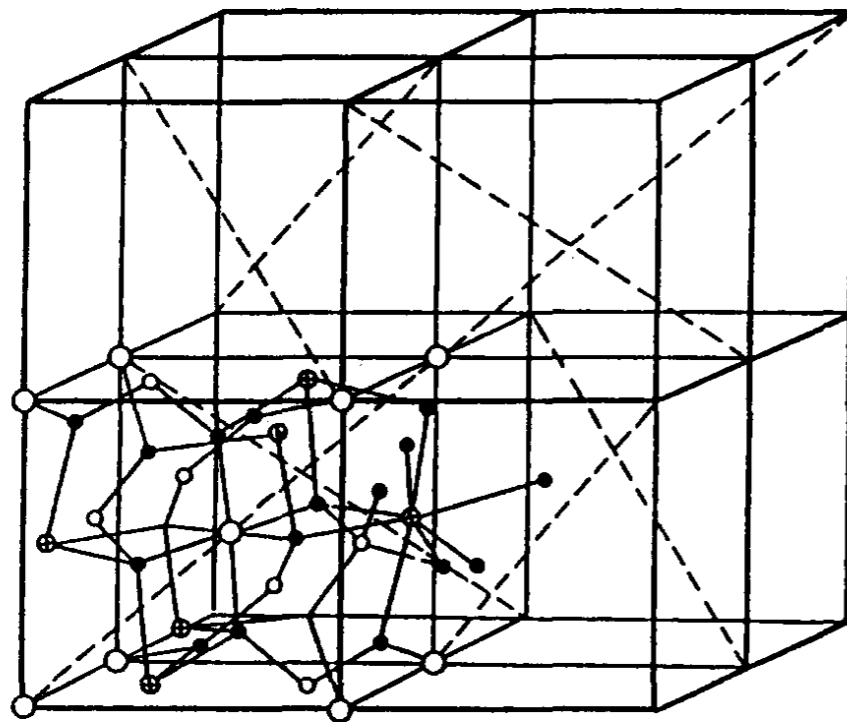
Magnon dispersion (YIG)



- 20 Fe³⁺ ions in magnetic unit cell
- “Ferri-magnet”

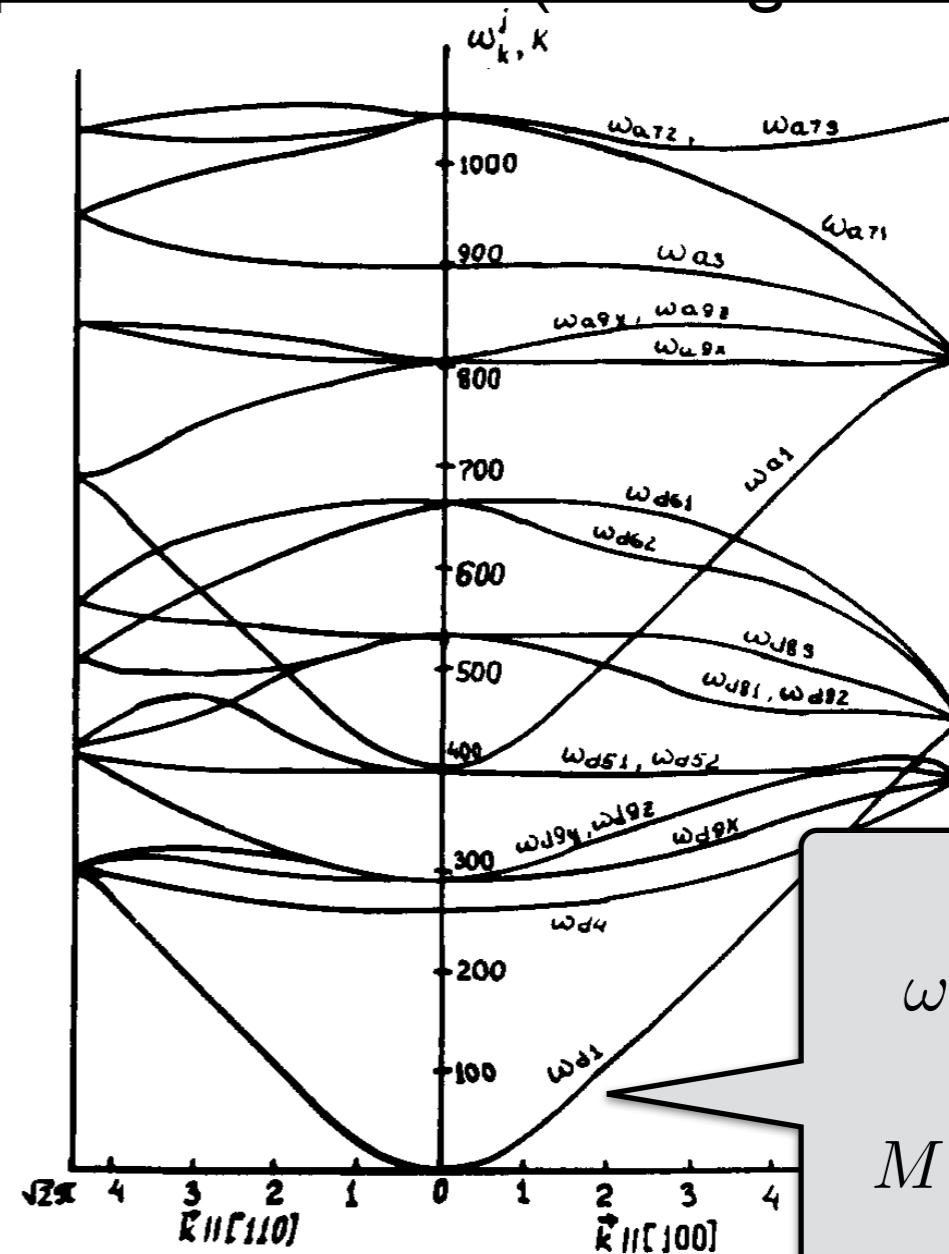
$$12 \text{ Fe} : \frac{5}{2} \mu_B \times 12 \quad \uparrow$$

$$8 \text{ Fe} : -\frac{5}{2} \mu_B \times 8 \quad \downarrow$$



○1 ⊕2 ○3 ●4
 Fe Y Fe O

dispersion relation (20 magnon branches)



$$\omega \approx \frac{k^2}{2M}$$

$$M \sim 7 \text{ MeV}$$

Axion-magnon conversion

[Barbieri et al (1989,2016), Chigusa, Moroi, KN (2020)]

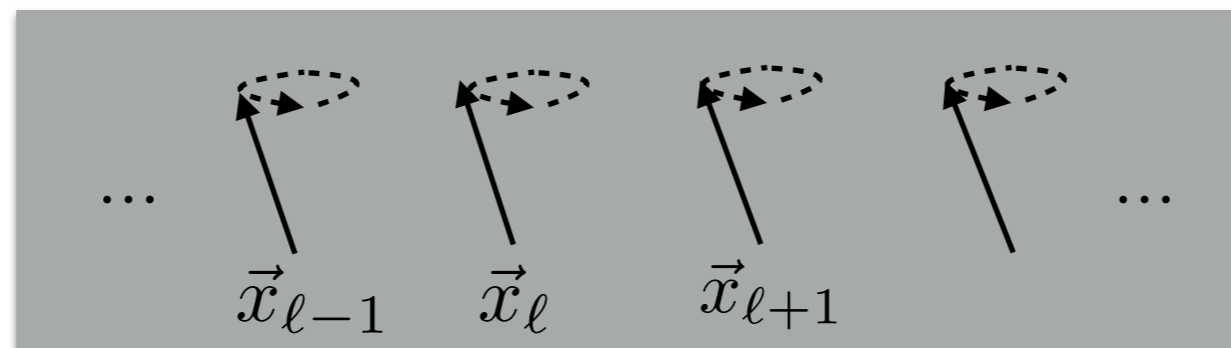
- Axion-electron interaction

$$\mathcal{L} = \frac{\partial_\mu a}{2f} \bar{\psi} \gamma^\mu \gamma_5 \psi \longrightarrow H_{\text{int}} = \frac{1}{f} \sum_{\ell} \vec{\nabla} a(\vec{x}_\ell) \cdot \vec{S}_\ell$$

- **Axion-magnon interaction Hamiltonian**

$$H_{\text{int}} = \frac{m_a a_0 \sin(m_a t + \delta)}{f} \sqrt{\frac{s}{2}} \sum_{\ell} \left(v_a^- \tilde{c}_\ell + v_a^+ \tilde{c}_\ell^\dagger \right)$$

Axion DM: $a(\vec{x}, t) = a_0 \cos(m_a t - m_a \vec{v}_a \cdot \vec{x} + \delta)$

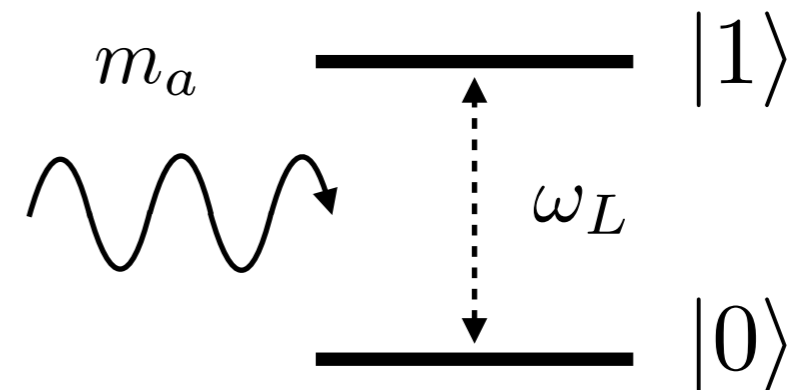


Resonant conversion

- 2-level system

$|0\rangle$: 0-magnon state

$|1\rangle$: 1-magnon state (k=0 mode)



- Signal power at resonance: $m_a = \omega_L$

$$\frac{dE_{\text{signal}}}{dt} = \frac{\omega_L P(t)}{2t} = \frac{\omega_L |V|^2 t}{8}$$

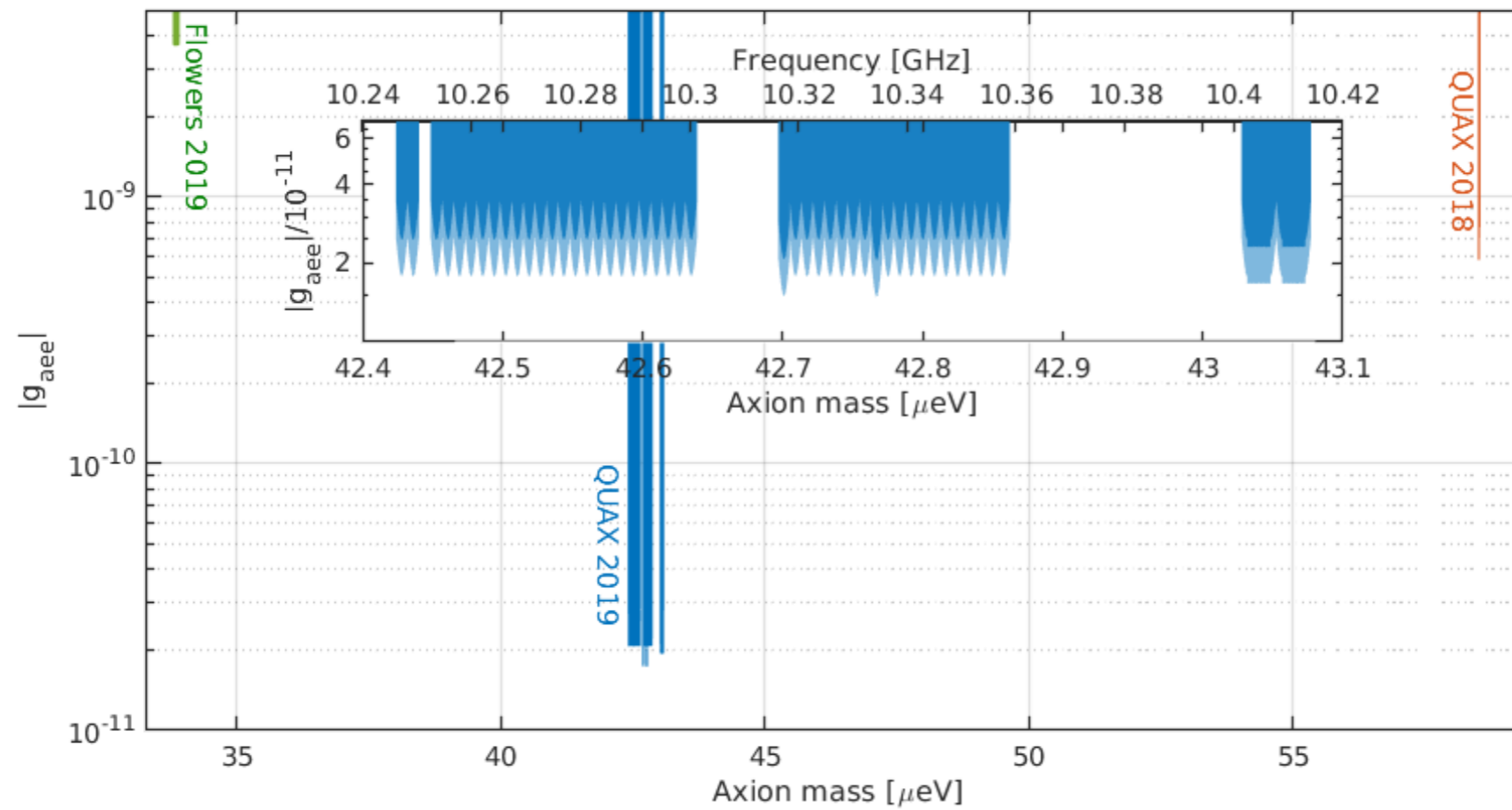
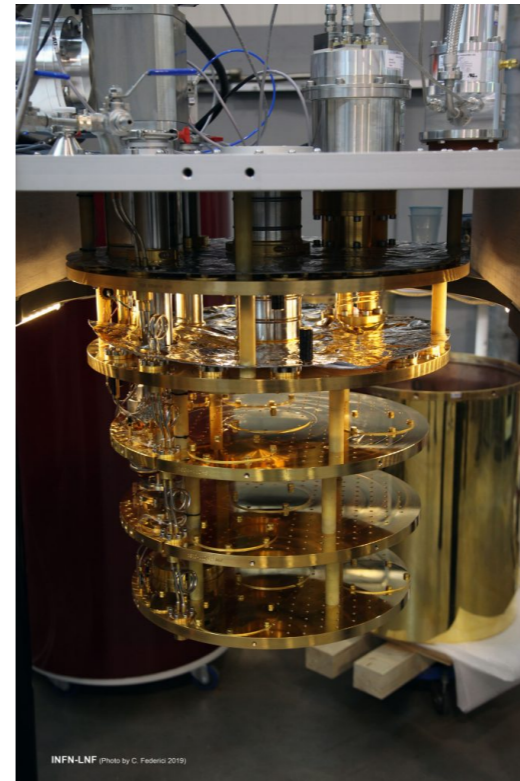
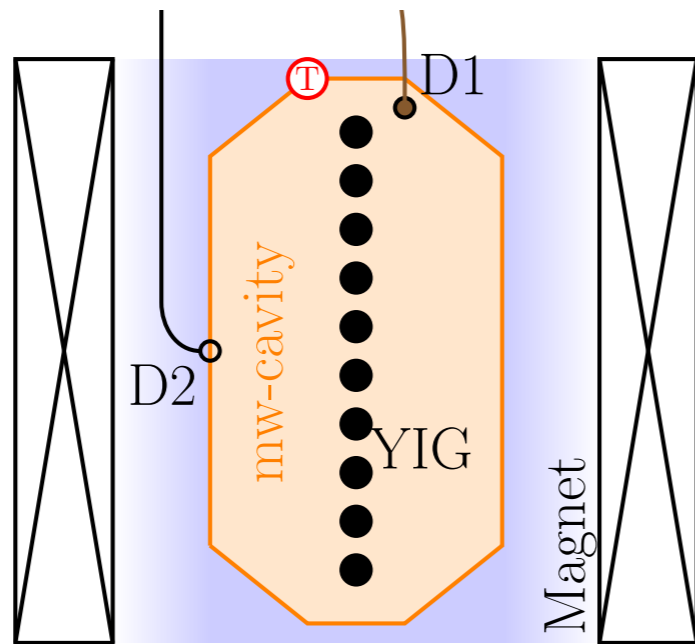
$$V \equiv \sqrt{\frac{sN}{2} \frac{m_a a_0 v_a^+}{f}}$$

- Limitation:

- Axion coherence time $\tau_a \sim (m_a v_a^2)^{-1}$

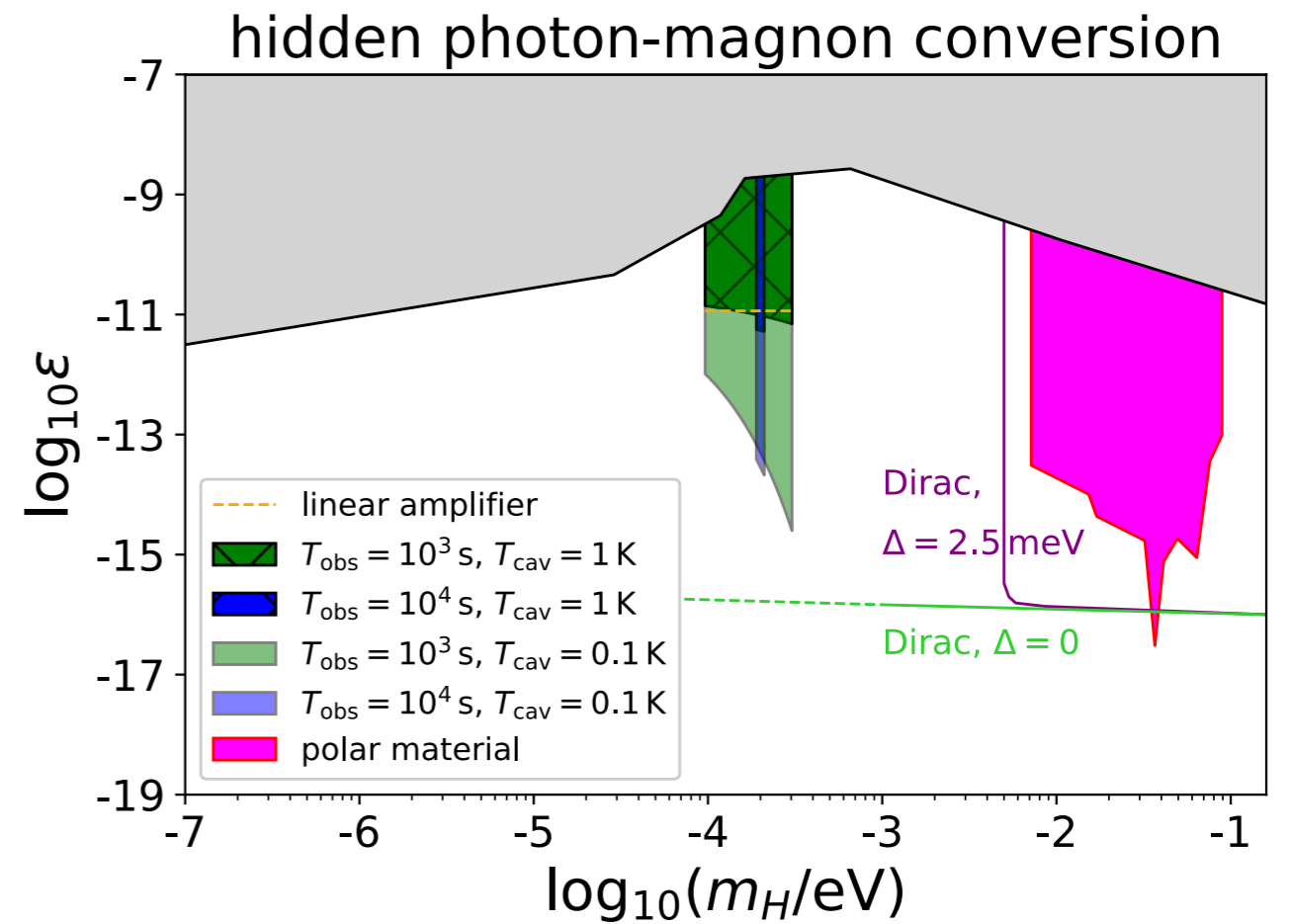
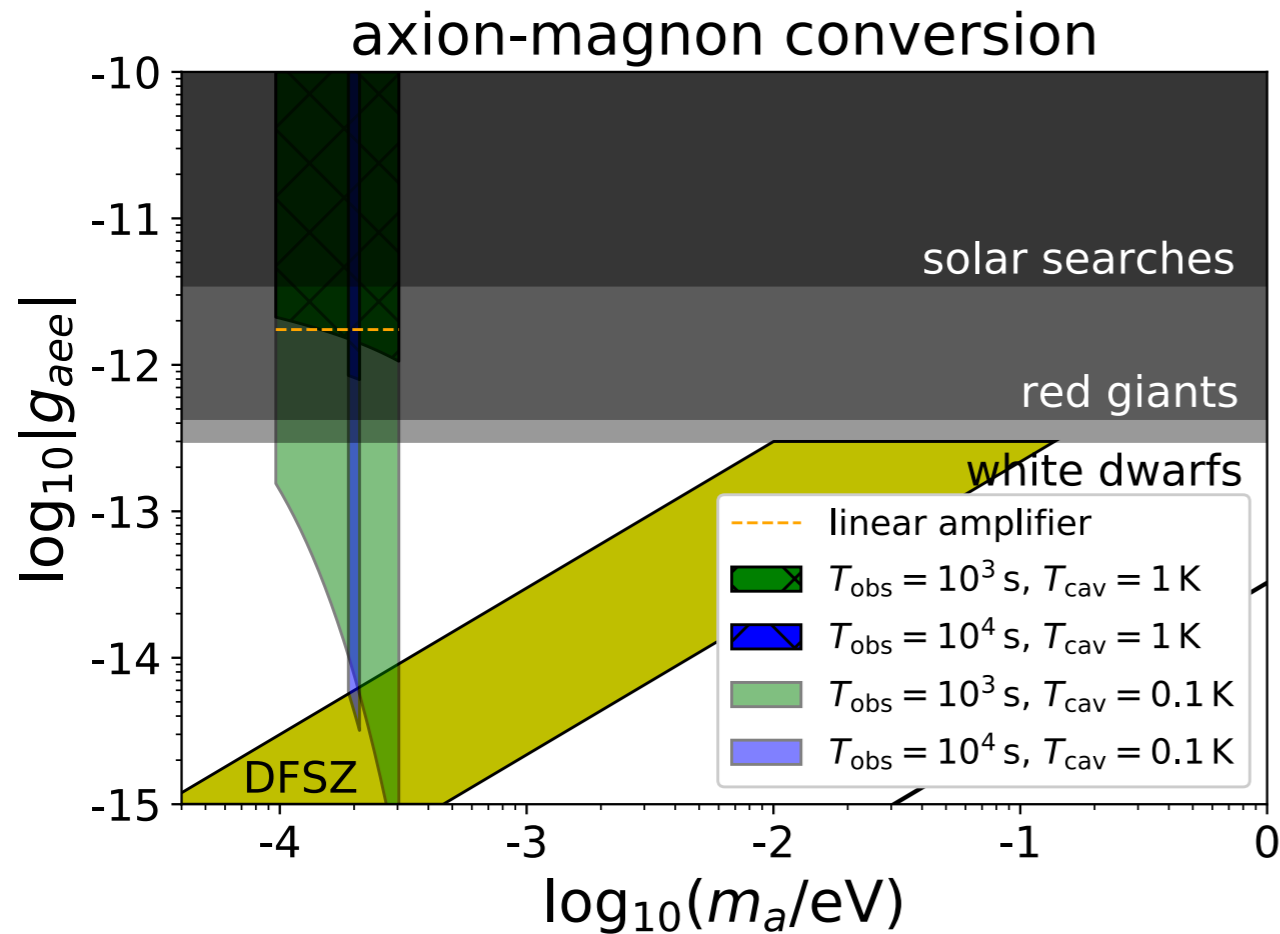
- Magnon relaxation time $\tau_{\text{magnon}} \sim (1/\tau_{\text{spin-spin}} + 1/\tau_{\text{spin-lattice}})^{-1}$

QUAX experiment



[QUAX collaboration (2020)]

Ultimate sensitivity from DM-magnon conversion



2. DM detection with condensed-matter axion

Axion in condensed-matter

- Topological insulator [Kane, Mele (2005), Fu, Kane, Mele (2007)]

$$\mathcal{L} = \theta \frac{\alpha_e}{4\pi} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

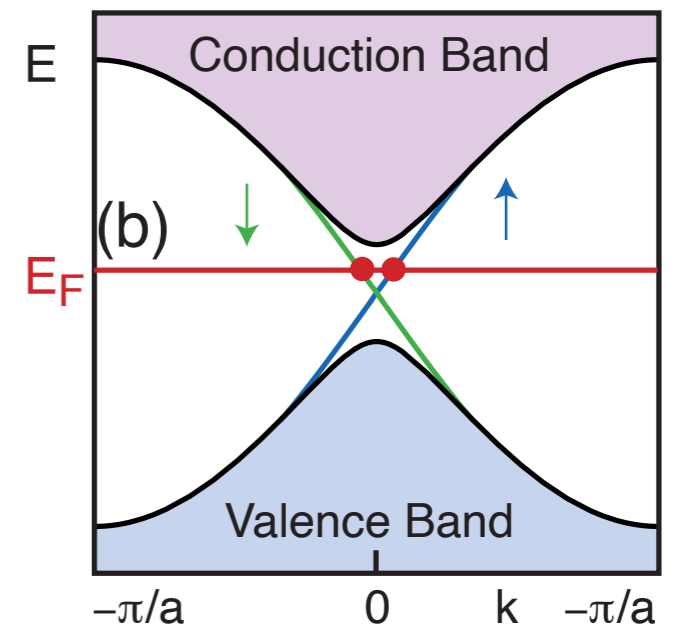
$\theta = 0$: normal insulator
 $\theta = \pi$: topological insulator

- Can θ be dynamical? [Wilczek (1987)]

- Arbitrary value if there is no T, P invariance
- Magnetic ordering can violate T, P-invariance

Dynamical axion

(axion quasi-particle, condensed-matter axion,...)



[Hasan, Mele (2010)]

- “**Axion**” in topological (anti-)ferromagnet

First proposal: Fe-doped Bi_2Se_3 [Li, Wang, Qi, Zhang (2009)]

Example: Fu-Kane-Mele-Hubbard model

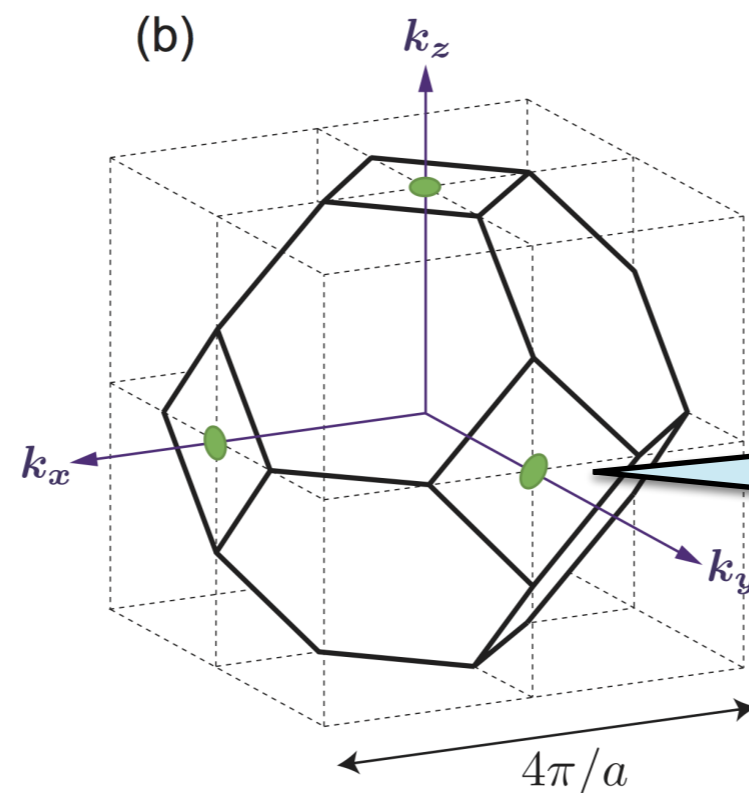
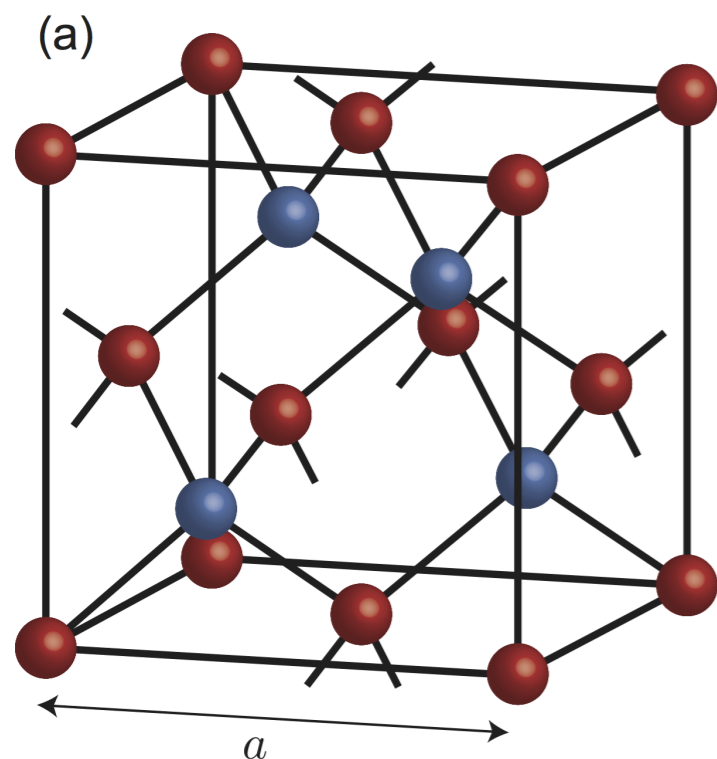
[Sekine, Nomura (2014)]

$$H_0 = \sum_{\langle i,j \rangle \sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + i \frac{4\lambda}{a^2} \sum_{\langle\langle i,j \rangle\rangle} c_i^\dagger \vec{\sigma} \cdot (\vec{d}_{ij}^1 \times \vec{d}_{ij}^2) c_j$$

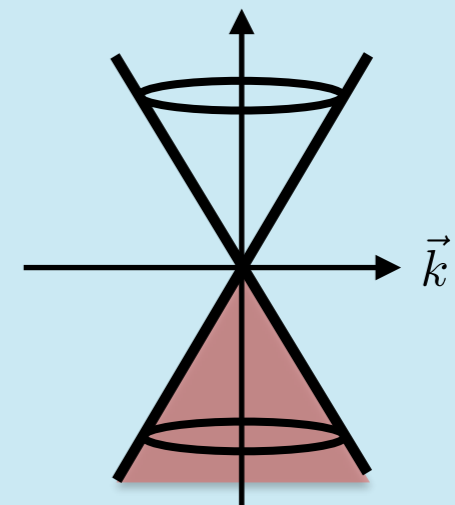
nearest neighbor
tight-binding term

next nearest neighbor
spin-orbit interaction term

$$H_U = U \sum_i n_{i\uparrow} n_{i\downarrow} \quad \text{Hubbard interaction term}$$



3 Dirac points in
Brillouin zone



- Dirac-like electron interacts with spin through

$$S = \int d^4x \sum_{r=1,2,3} \bar{\psi}_r [i\gamma^\mu (\partial_\mu - ieA_\mu) - \delta t - i\gamma_5 U m_r] \psi_r$$

$$\langle \vec{S}_{i,A} \rangle = - \langle \vec{S}_{i,B} \rangle \equiv \vec{m} \quad : \text{anti-ferromagnetic order for } U/t \gg 1$$

- Chiral rotation of Dirac fermion gives axion-photon interaction:

$$S = \int d^4x \theta \frac{\alpha_e}{4\pi} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$\theta \equiv \theta_0 + \sum_r \theta_r = \theta_0 + \sum_r \tan^{-1} \left(\frac{U m_r}{\delta t} \right)$$

Axion ~ magnon in FKMH anti-ferromagnet model.

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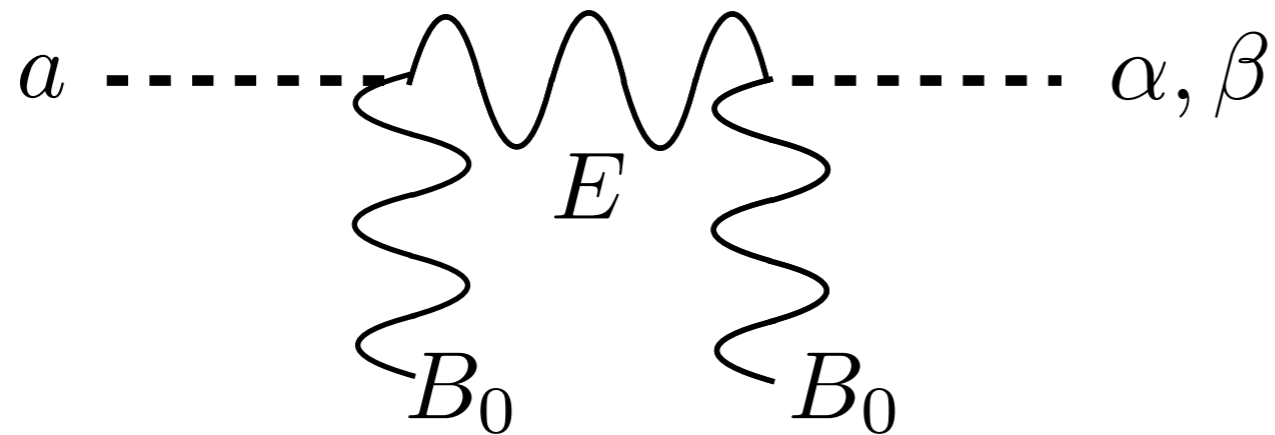
Fluctuation of magnetic order parameter
= **dynamical axion**

Axion ~ magnon in FKMH anti-ferromagnet model.

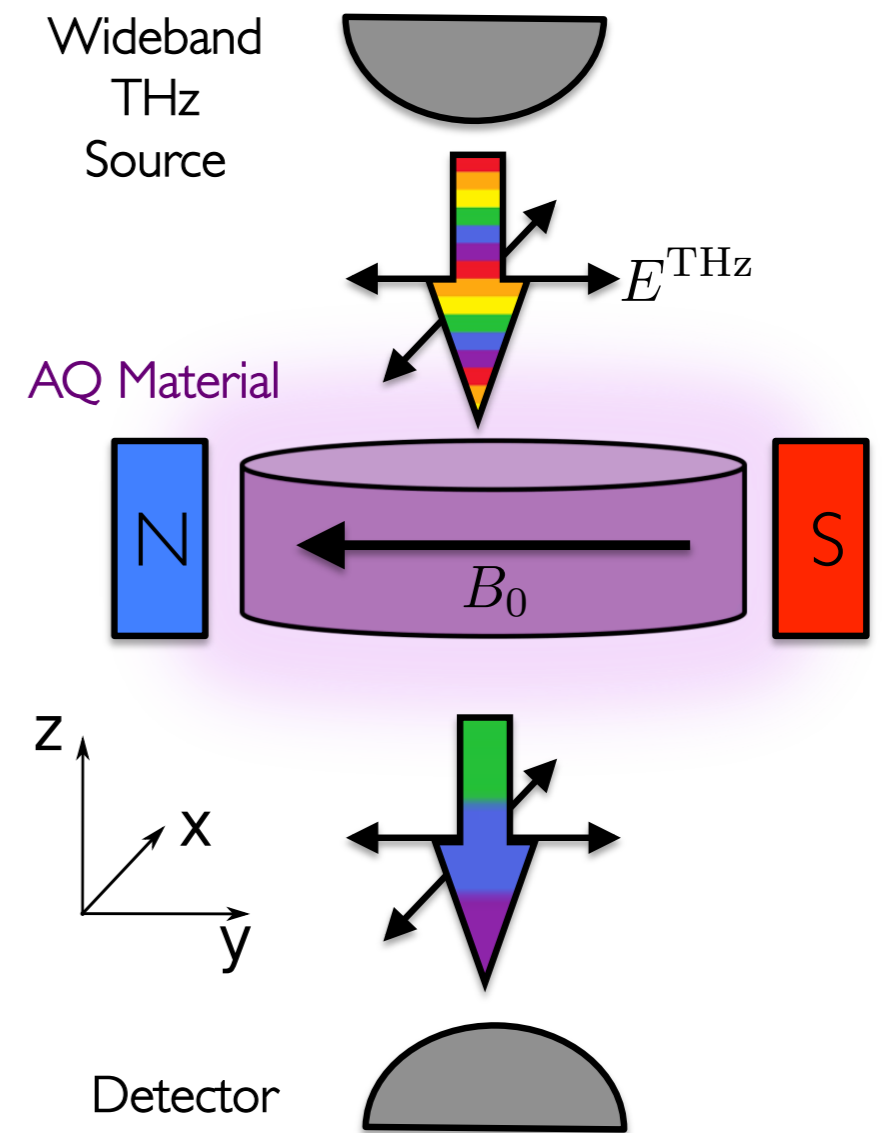
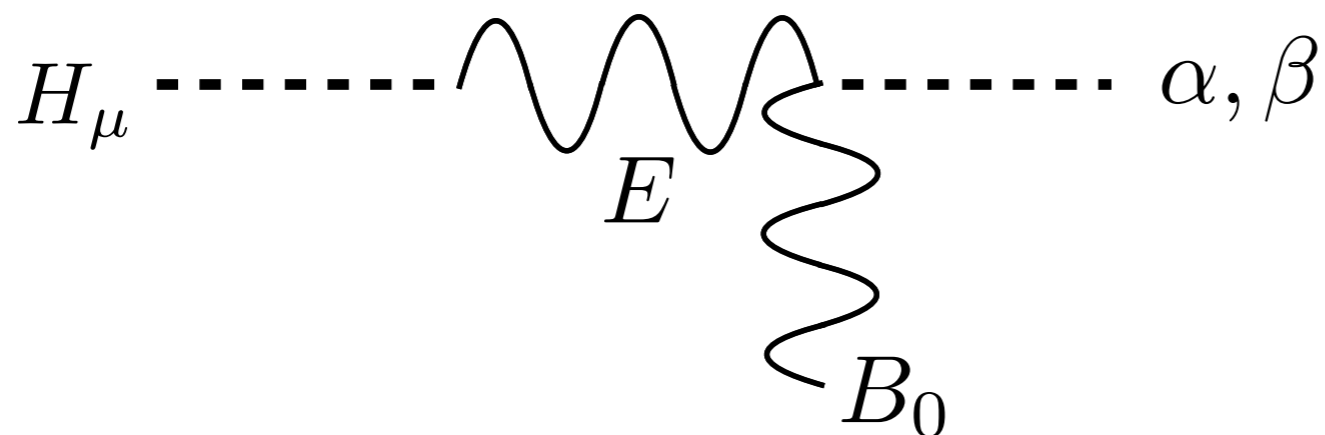
DM-axion to CM-axion

[Marsh et al (2018), Schutte-Engel et al. (2021), Chigusa, Moroi, KN (2021)]

- DM axion to CM axion conversion under magnetic field

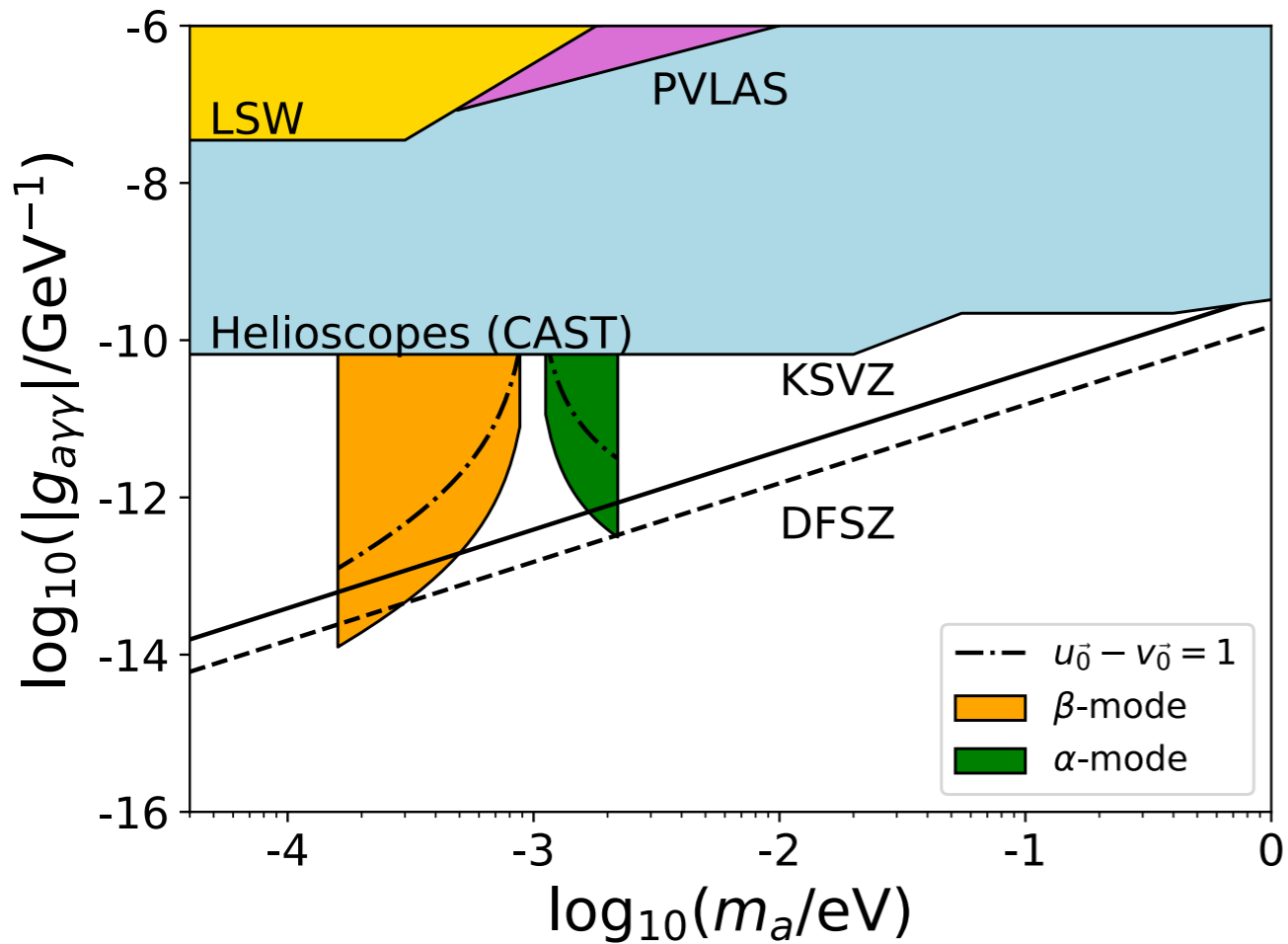


- DM hidden photon to CM axion

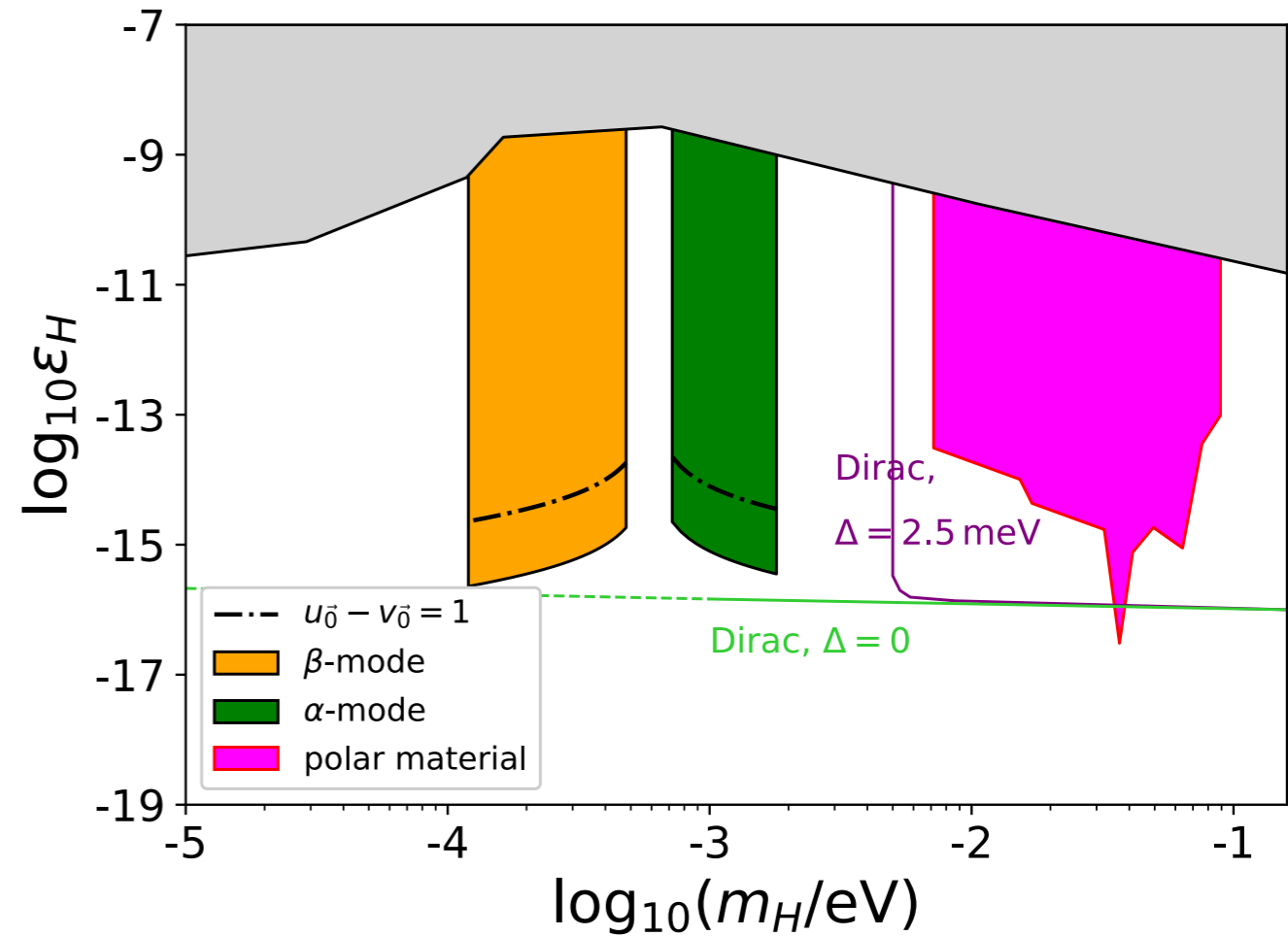


[Schutte-Engel et al. (2021)]

Axion DM



Hidden photon DM



Scan of magnetic field: $1 \text{ T} < B_0 < 10 \text{ T}$

Each time step: $\Delta t = 10^2 \text{ s}$

Total observation time: 1 yr

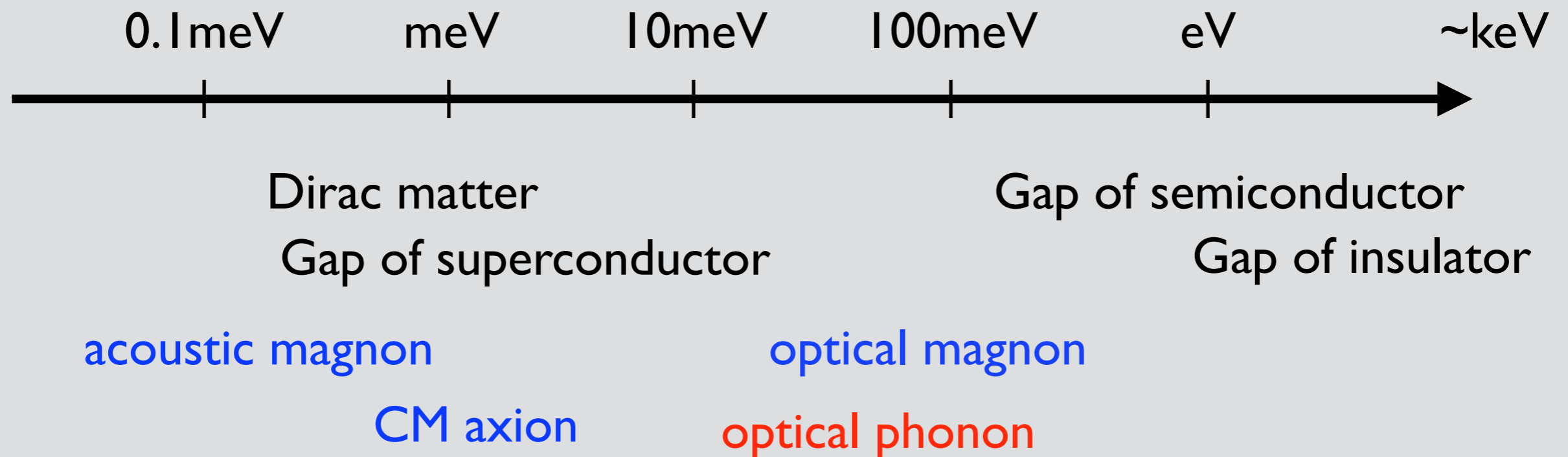
Target volume: $V = (10 \text{ cm})^3$

Noise rate: $dN_{\text{noise}}/dt \sim 10^{-3} \text{ s}^{-1}$

[Chigusa, Moroi, KN (2021)]

Summary

- Quantum fields in **condensed-matter**
: useful for DM detection!



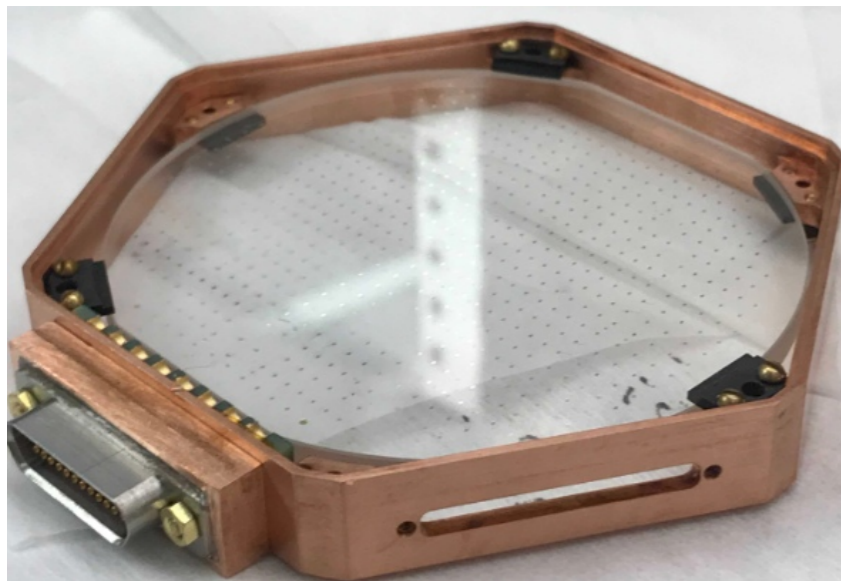
- New particle search frontier in particle and condensed-matter interdisciplinary field ?

Appendix

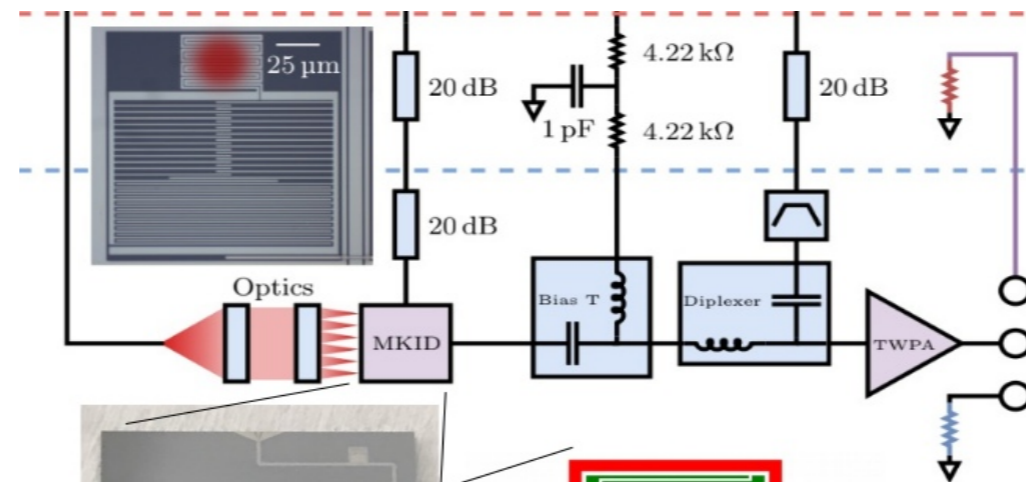
Development of sensors

Additional sensors of interest besides TES APDs

Golden reference TES athermal phonon detector

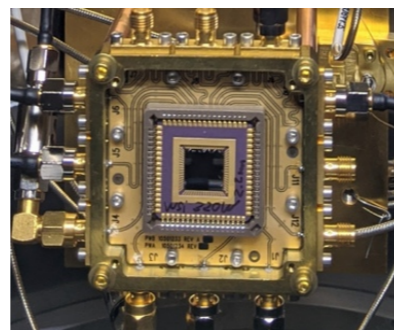
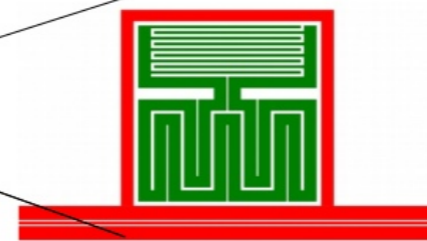
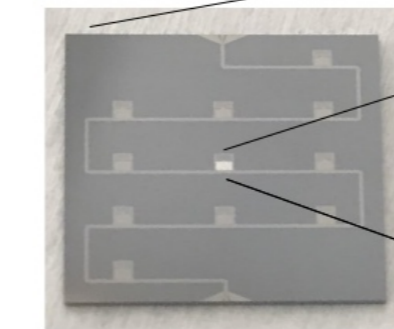


we're close to achieving 1eV energy threshold in a large area (3" dia.)
This is the current world's best microcalorimeter



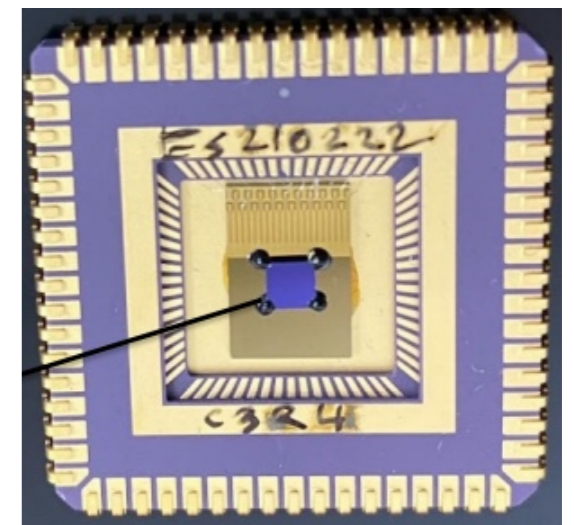
MKIDs

Limited by readout-dominated noise. Need to reduce and apply squeezing



SNSPDs

Have to increase area while keeping threshold low. Want to reach 20meV threshold

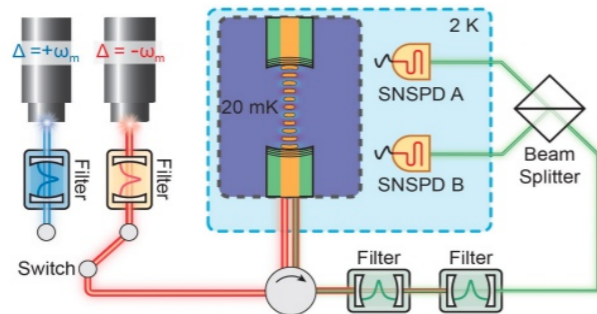
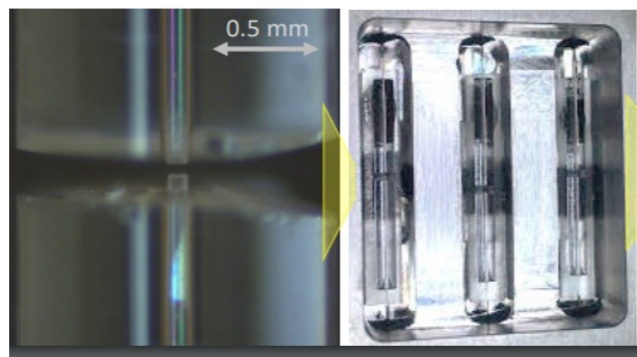


1sq.mm. SNSPD with GaAs crystal on top

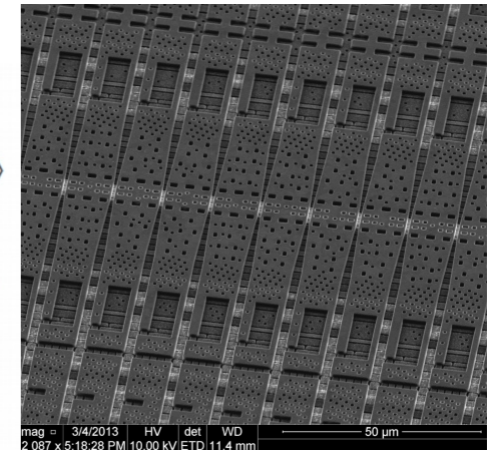
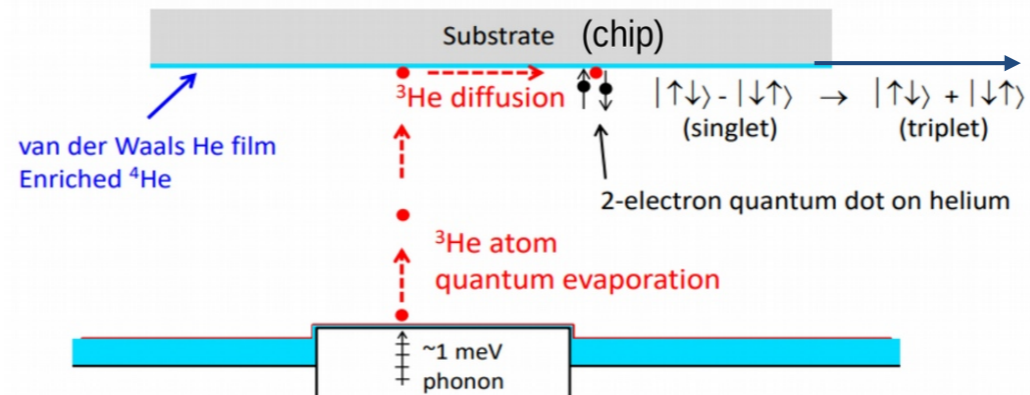
Development of sensors

Additional quantum sensors under investigation

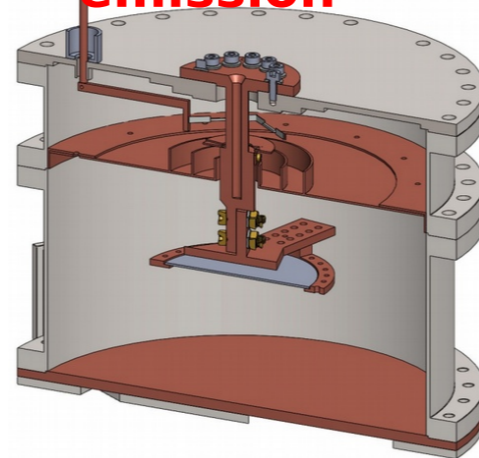
Opto-Mechanical I cavities



Electron surface states in LHe



He Quantum Evaporation emission



film-stopping setup
to suspend
dry sensor above
LHe bath is
up and running.

He surface

