



I FOUND THE HUGS BISON.

MINIMUMBLE.COM

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BSM Higgs Bosons at the ILC in the Light of HL-LHC Results

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Matsue, 05/2022

1. Introduction
2. Direct detection of “heavy” BSM Higgs bosons
3. Indirect detection of “heavy” BSM Higgs bosons
4. Direct detection of “light” BSM Higgs bosons
5. Conclusions

1. Introduction

We have discovered an SM-like Higgs!

The SM cannot be the ultimate theory!

Conclusion: The discovered Higgs cannot be “the SM Higgs”!

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⇒ any hints from LHC results (as guideline/toy example)?

Q': Which model?

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Q': Which model?

A1: check changed properties of the h_{125}

A2: check for additional Higgs bosons

check for additional Higgs bosons above and below 125 GeV

Extended Higgs sectors

Compatibility with the experimental results requires:

- A SM-like Higgs at ~ 125 GeV
- Properties of the other Higgs bosons (masses, couplings, ...) have to be such that they are in agreement with the present bounds

The “sum rule”: $\sum_i g_{h_i VV}^2 = g_{H_{\text{SM}} VV}^2$ – and we know $g_{h_{125} VV}^2 \sim g_{H_{\text{SM}} VV}^2$

\Rightarrow not much room left for BSM Higgs couplings to gauge bosons

Sum rule “violated” only by triplets or higher representations ...

Toy example:

Two Higgs Doublet Model (2HDM):

Fields:

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \rho_1 + i\eta_1) \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \rho_2 + i\eta_2) \end{pmatrix}$$

Potential:

$$V = m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + h.c.) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2} [(\Phi_1^\dagger \Phi_2)^2 + h.c.]$$

Physical states: h , H , (\mathcal{CP} -even), A (\mathcal{CP} -odd), H^\pm (charged)

“Physical” input parameters:

$$c_{\beta-\alpha}, \quad \tan \beta, \quad v, \quad M_h, \quad M_H, \quad M_A, \quad M_{H^\pm}, \quad m_{12}^2$$

Alignment limit: $c_{\beta-\alpha} \rightarrow 0$ (for $M_h \sim 125$ GeV)

Assumption (for now): $h \sim h_{125}$

Z_2 symmetry to avoid FCNC:

$$\Phi_1 \rightarrow \Phi_1, \quad \Phi_2 \rightarrow -\Phi_2$$

Extension of the Z_2 symmetry to fermions determines four types:

	u -type	d -type	leptons	
type I	Φ_2	Φ_2	Φ_2	
type II	Φ_2	Φ_1	Φ_1	\rightarrow MSSM type
type III (lepton-specific)	Φ_2	Φ_2	Φ_1	
type IV (flipped)	Φ_2	Φ_1	Φ_2	

Sum rule (with h SM-like): $\sin(\beta - \alpha) \approx 1, \cos(\beta - \alpha) \approx 0$

Unitarity/perturbativity and EWPO (so far): $\Rightarrow M_A \sim M_H \sim M_{H^\pm}$

Second toy example:

Next-Two Higgs Doublet Model (N2HDM): \rightarrow (nearly) NMSSM type

Fields:

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \rho_1 + i\eta_1) \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \rho_2 + i\eta_2) \end{pmatrix}, \quad \Phi_S = v_S + \rho_S$$

Potential:

$$\begin{aligned} V = & m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + h.c.) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ & + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2} [(\Phi_1^\dagger \Phi_2)^2 + h.c.] \\ & + \frac{1}{2} m_S^2 \Phi_S^2 + \frac{\lambda_6}{8} \Phi_S^4 + \frac{\lambda_7}{2} (\Phi_1^\dagger \Phi_1) \Phi_S^2 + \frac{\lambda_8}{2} (\Phi_2^\dagger \Phi_2) \Phi_S^2 \end{aligned}$$

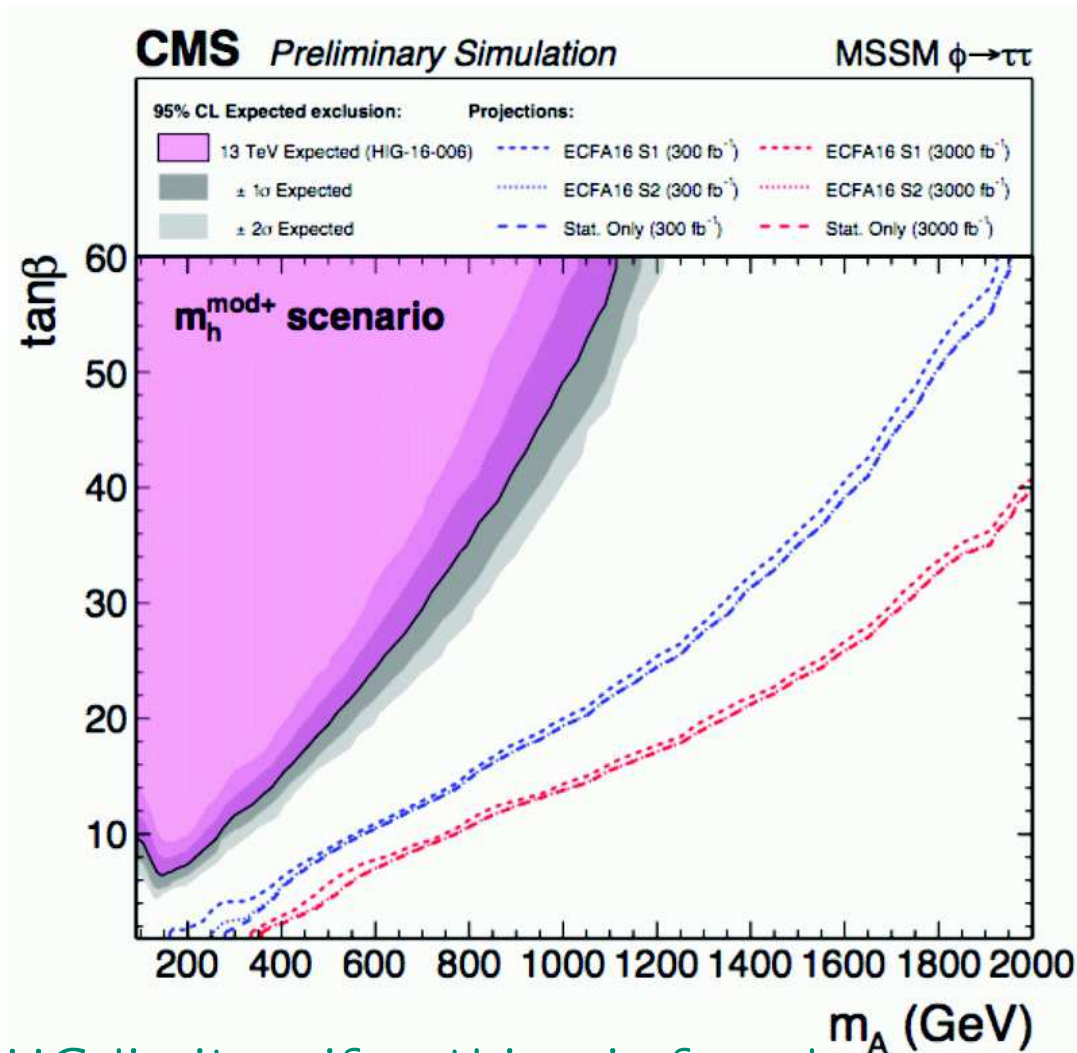
Z_2 symmetry: $\Phi_1 \rightarrow \Phi_1$, $\Phi_2 \rightarrow -\Phi_2$, $\Phi_S \rightarrow \Phi_S$

Z'_2 symmetry: $\Phi_1 \rightarrow \Phi_1$, $\Phi_2 \rightarrow \Phi_2$, $\Phi_S \rightarrow -\Phi_S$ (broken by $v_S \Rightarrow$ no DM)

Physical states: h_1, h_2, h_3 (CP -even), A (CP -odd), H^\pm (charged)

2. Direct Detection of “heavy” BSM Higgs bosons

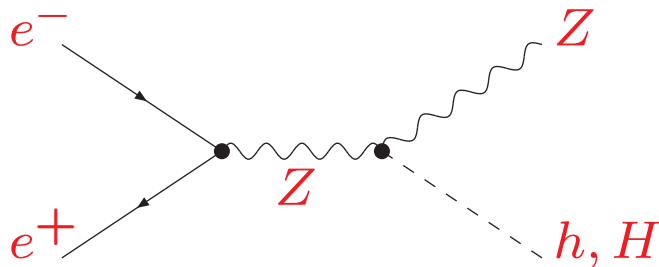
Reach in the MSSM (type II 2HDM Higgs sector):



\Rightarrow strong (HL-)LHC limits - if nothing is found analyzed in detail
 \Rightarrow but if there is something in the kinematical e^+e^- reach, it can be

Search for neutral Higgs bosons in the 2HDM at e^+e^- colliders:

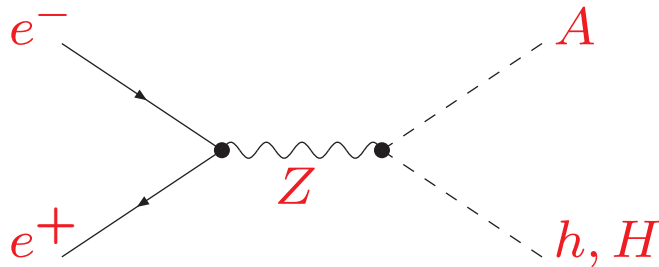
$e^+e^- \rightarrow Zh, ZH$



$$\sigma_{hZ} \approx \sin^2(\beta - \alpha) \sigma_{hZ}^{\text{SM}}$$

$$\sigma_{HZ} \approx \cos^2(\beta - \alpha) \sigma_{hZ}^{\text{SM}}$$

$e^+e^- \rightarrow Ah, AH$



$$\sigma_{hA} \propto \cos^2(\beta - \alpha) \sigma_{hZ}^{\text{SM}}$$

$$\sigma_{HA} \propto \sin^2(\beta - \alpha) \sigma_{hZ}^{\text{SM}}$$

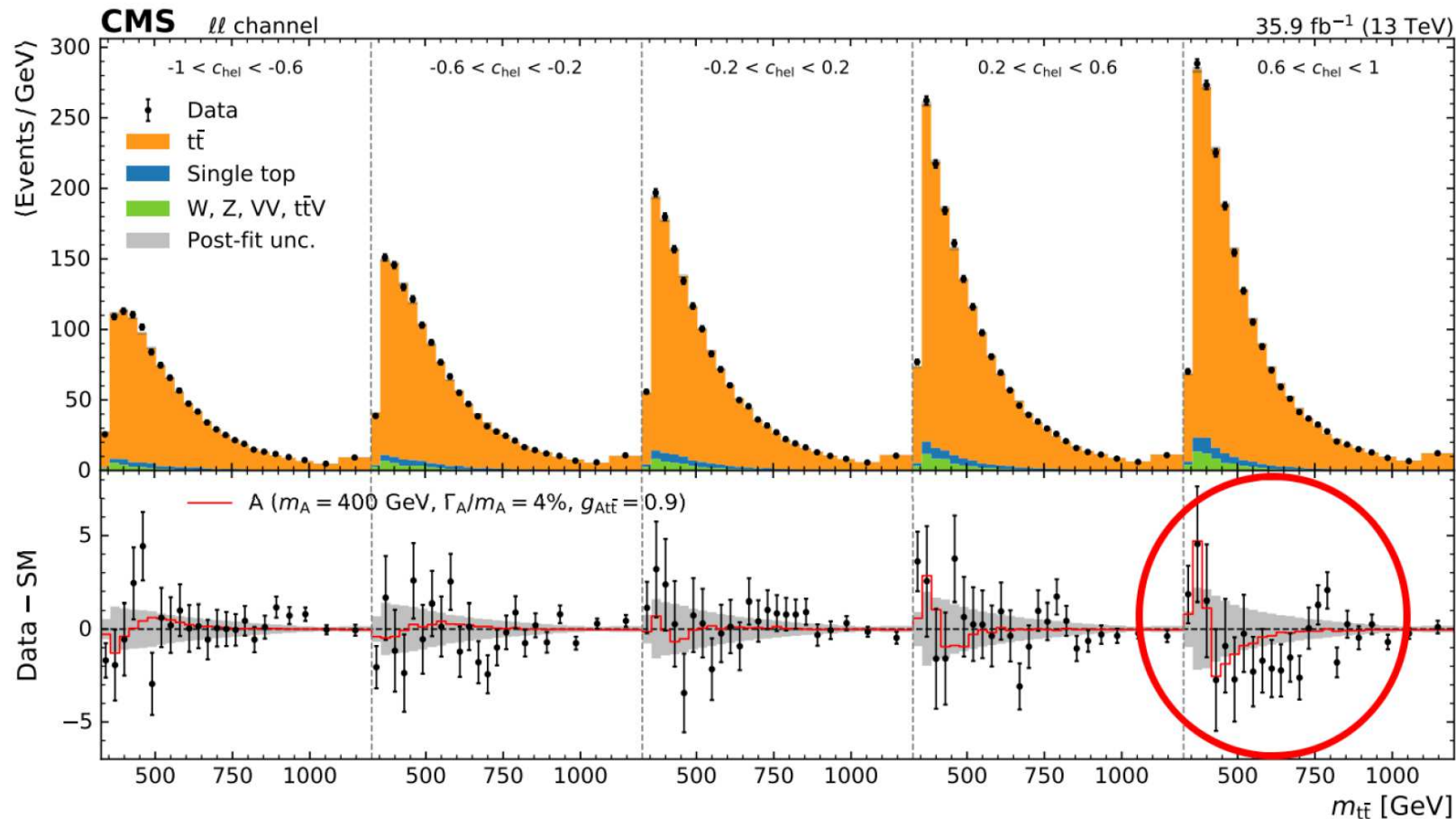
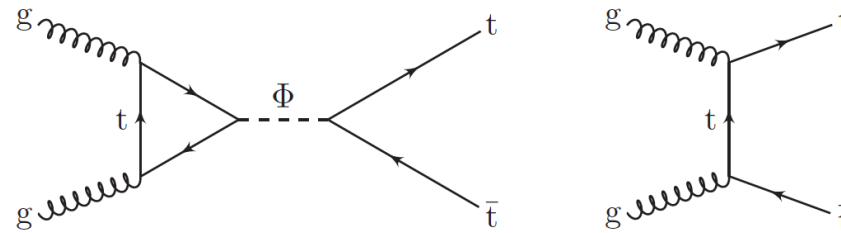
⇒ only pair production of heavy Higgs bosons!

reach: $M_A \lesssim \sqrt{s}/2$

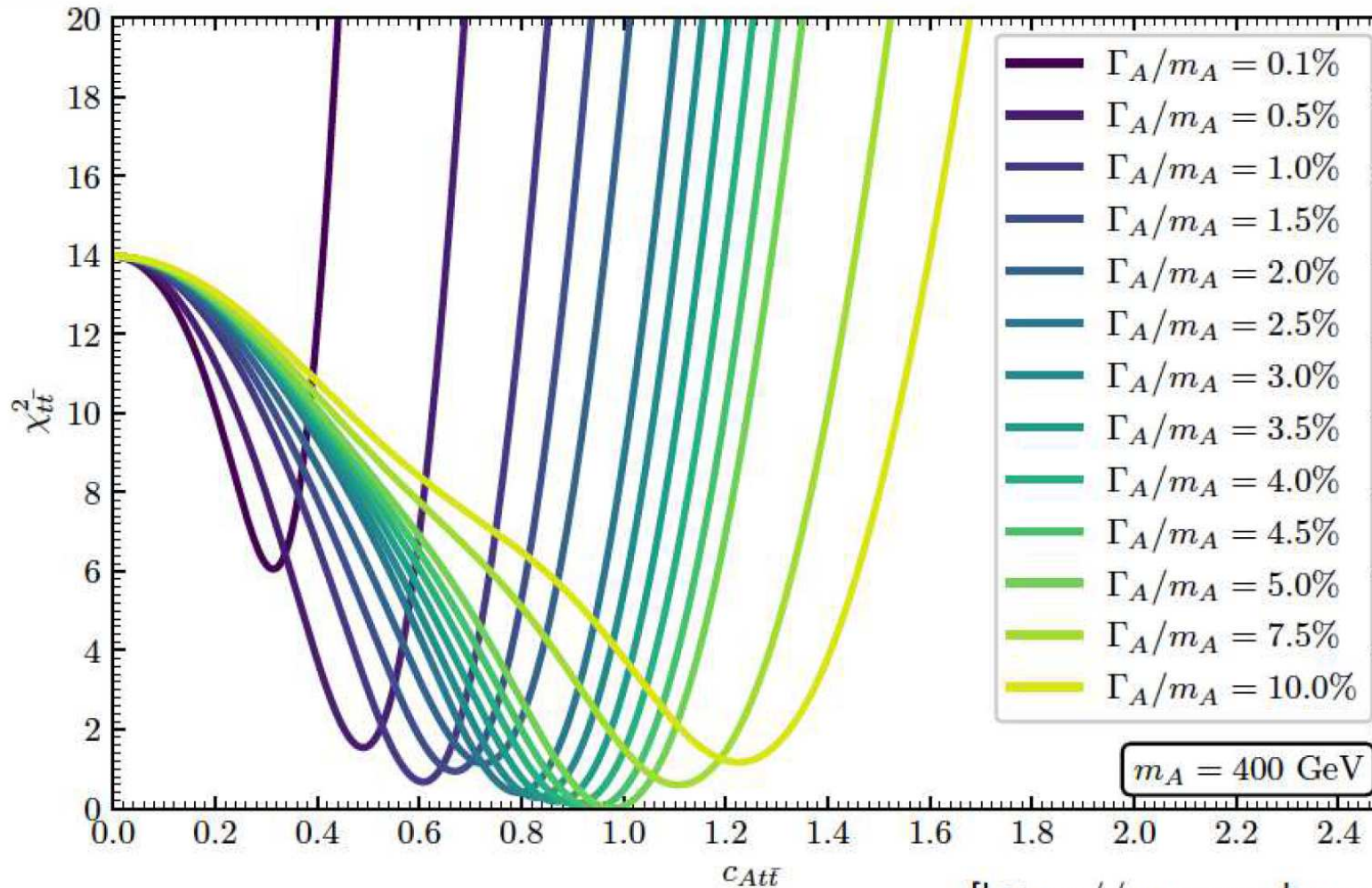
⇒ maximum ILC reach: ~ 500 GeV, CLIC ~ 1500 GeV

Possible hint for heavy Higgses at the LHC:

CMS Higgs-boson search in $pp \rightarrow \phi \rightarrow t\bar{t}$ at $m_\phi \sim 400$ GeV



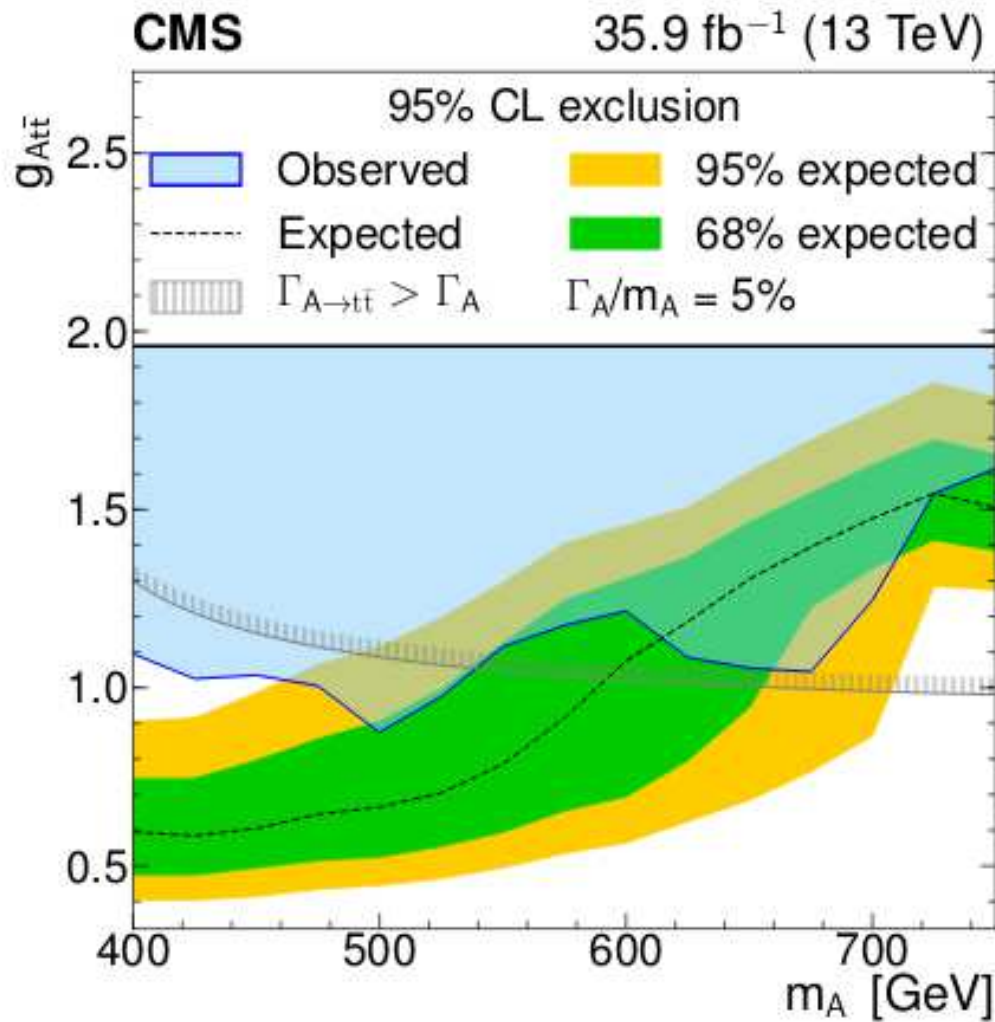
χ^2 distribution from the excess: local: 3.5σ , global: $\lesssim 2\sigma$



[<https://cms-results.web.cern.ch>]

\Rightarrow can be explained in the N2HDM/NMSSM for $\tan\beta \sim 1.5 \Rightarrow$ in ILC reach
[*T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21*]

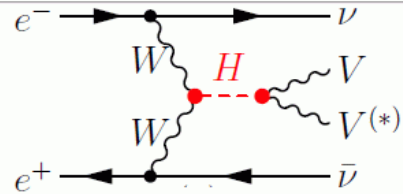
χ^2 distribution from the excess: local: 3.5σ , global: $\lesssim 2\sigma$



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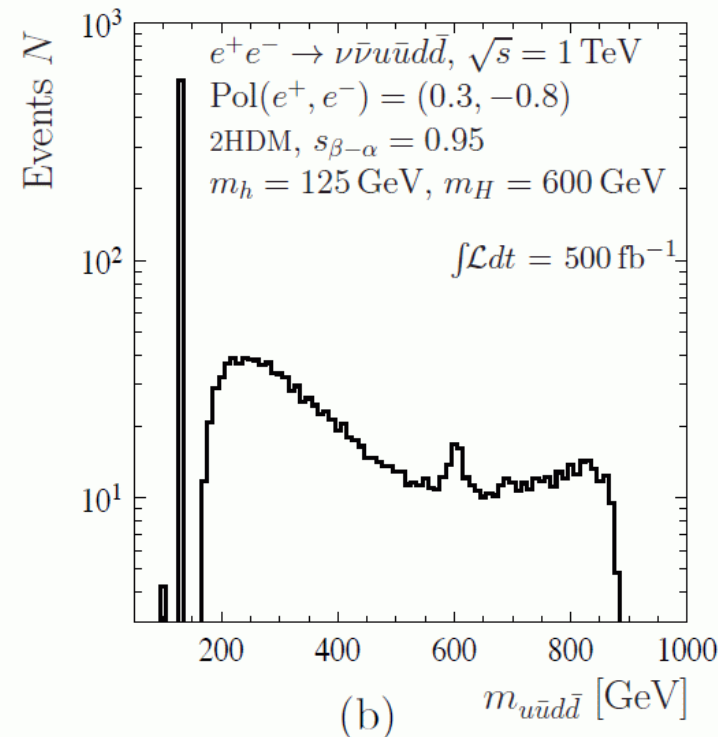
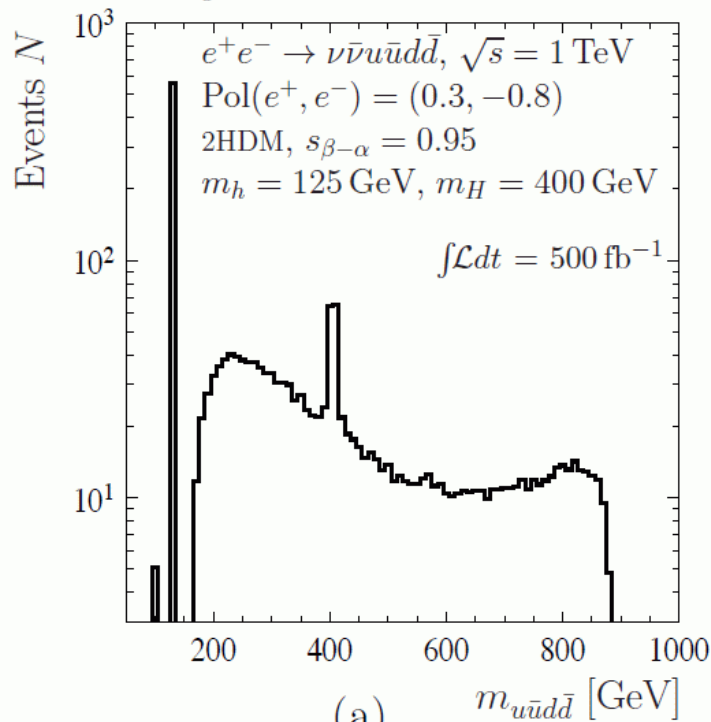
Single heavy Higgs production beyond kinematic reach:

Sensitivity to the small signal of an additional heavy Higgs boson in a Two-Higgs-Doublet model (2HDM)



[S. Liebler et al. '15]

$$g_{hVV} = \sin(\beta - \alpha) g_{HVV}^{\text{SM}}, \quad g_{HV V} = \cos(\beta - \alpha) g_{HVV}^{\text{SM}}, \quad V = W^\pm, Z$$

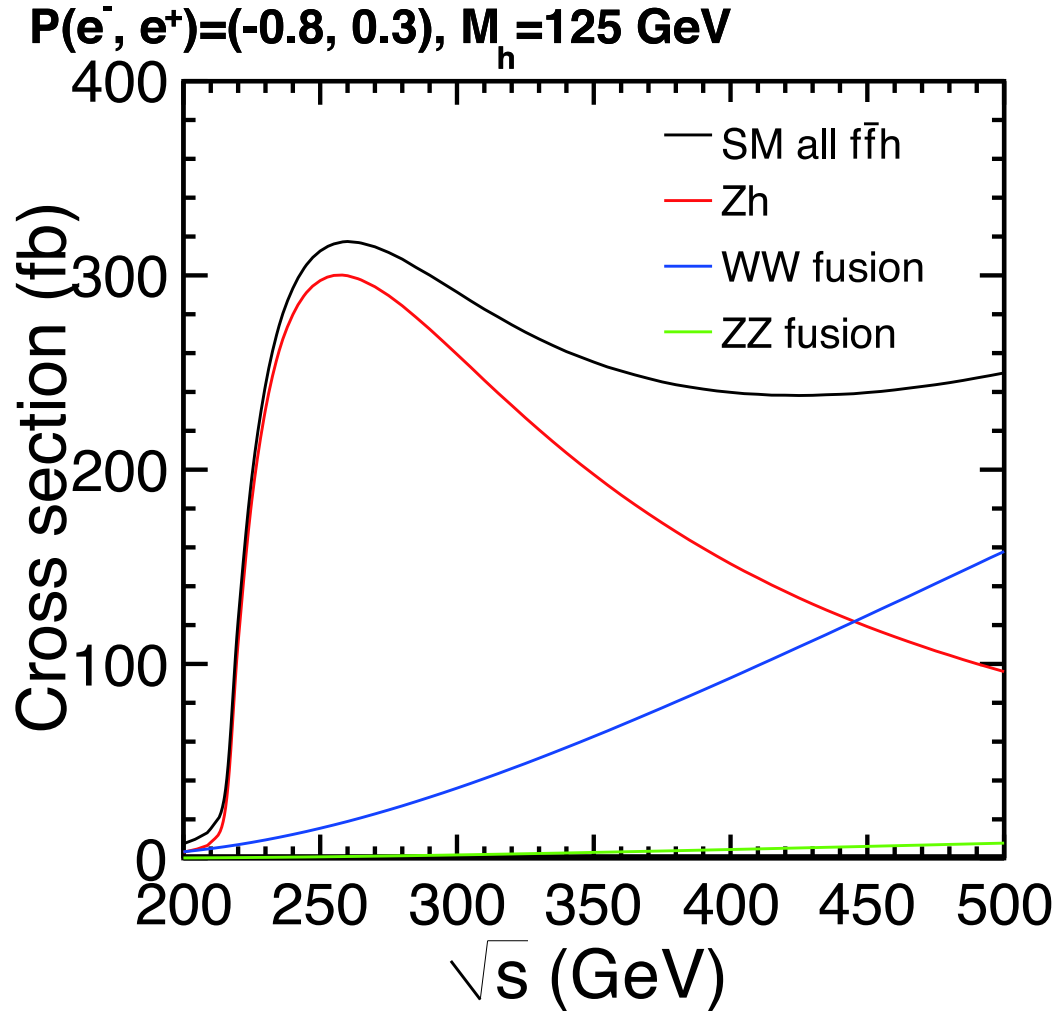


⇒ ILC: Potential sensitivity beyond the kinematic reach of Higgs pair production

[Taken from G. Weiglein '18]

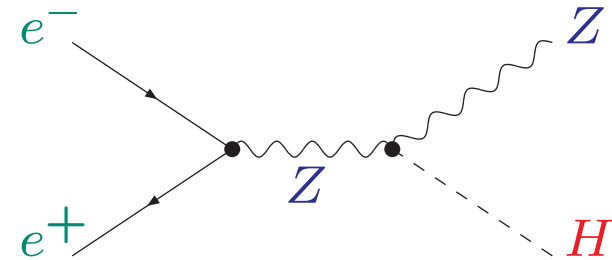
3. Indirect Detection of “heavy” BSM Higgs bosons

⇒ via h_{125} coupling measurements



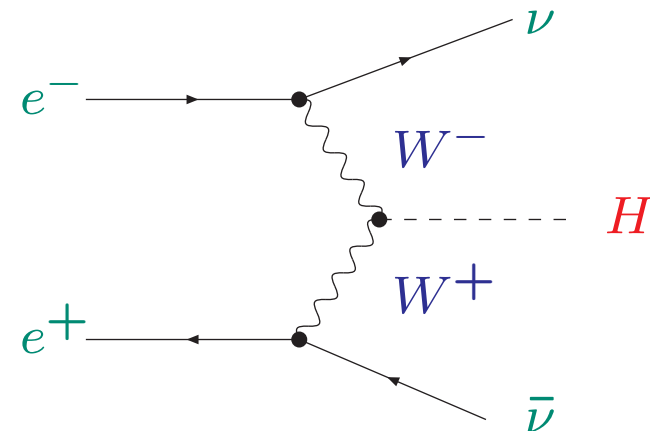
Higgs-strahlung:

$$e^+e^- \rightarrow Z^* \rightarrow ZH$$



weak boson fusion (WBF):

$$e^+e^- \rightarrow \nu\bar{\nu}H$$



$\sqrt{s} \sim 250$ GeV, Higgs-strahlung dominated

Required precision for Higgs couplings?

MSSM example:

$$\kappa_V \approx 1 - 0.5\% \left(\frac{400 \text{ GeV}}{M_A} \right)^4$$

$$\kappa_t = \kappa_c \approx 1 - \mathcal{O}(10\%) \left(\frac{400 \text{ GeV}}{M_A} \right)^2 \cot^2 \beta$$

$$\kappa_b = \kappa_\tau \approx 1 + \mathcal{O}(10\%) \left(\frac{400 \text{ GeV}}{M_A} \right)^2$$

Composite Higgs example:

$$\kappa_V \approx 1 - 3\% \left(\frac{1 \text{ TeV}}{f} \right)^2$$

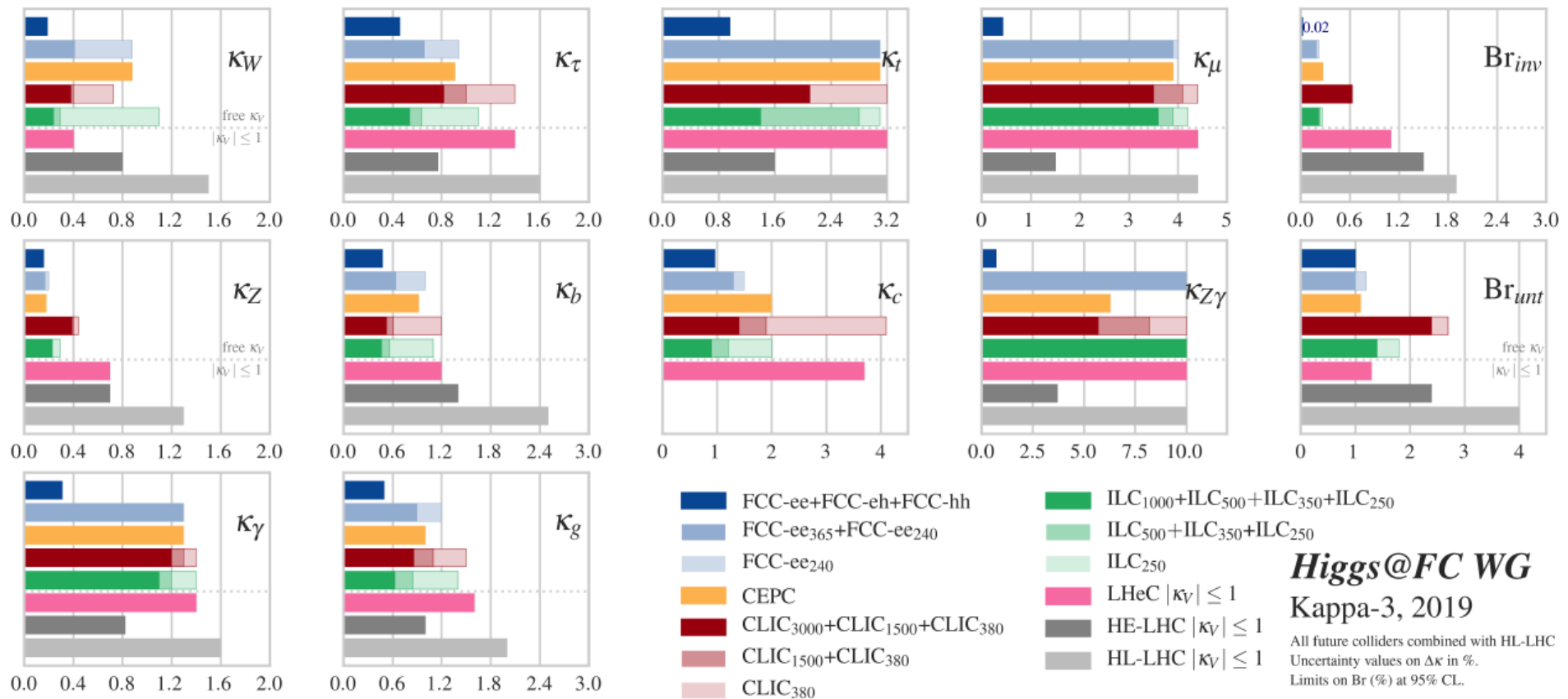
$$\kappa_F \approx 1 - (3 - 9)\% \left(\frac{1 \text{ TeV}}{f} \right)^2$$

⇒ couplings to bosons in the **per mille** range

⇒ couplings to fermions in the **per cent** range

⇒ at which collider can this be reached?

Future expectations for κ (kappa-3 framework)

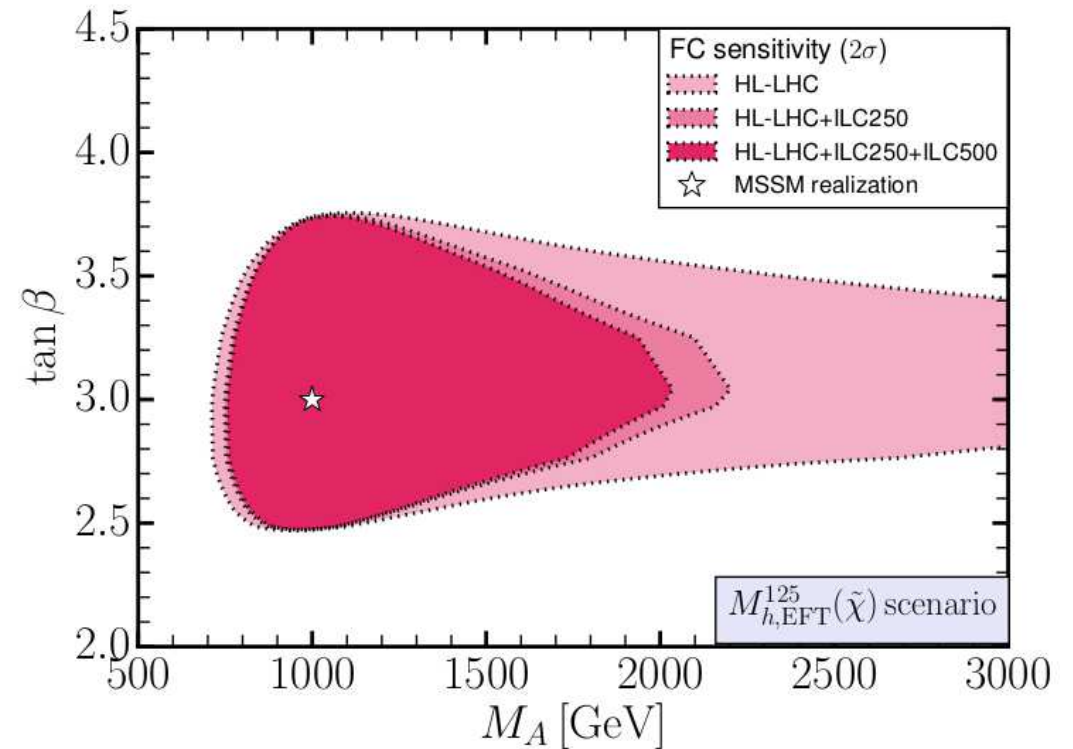
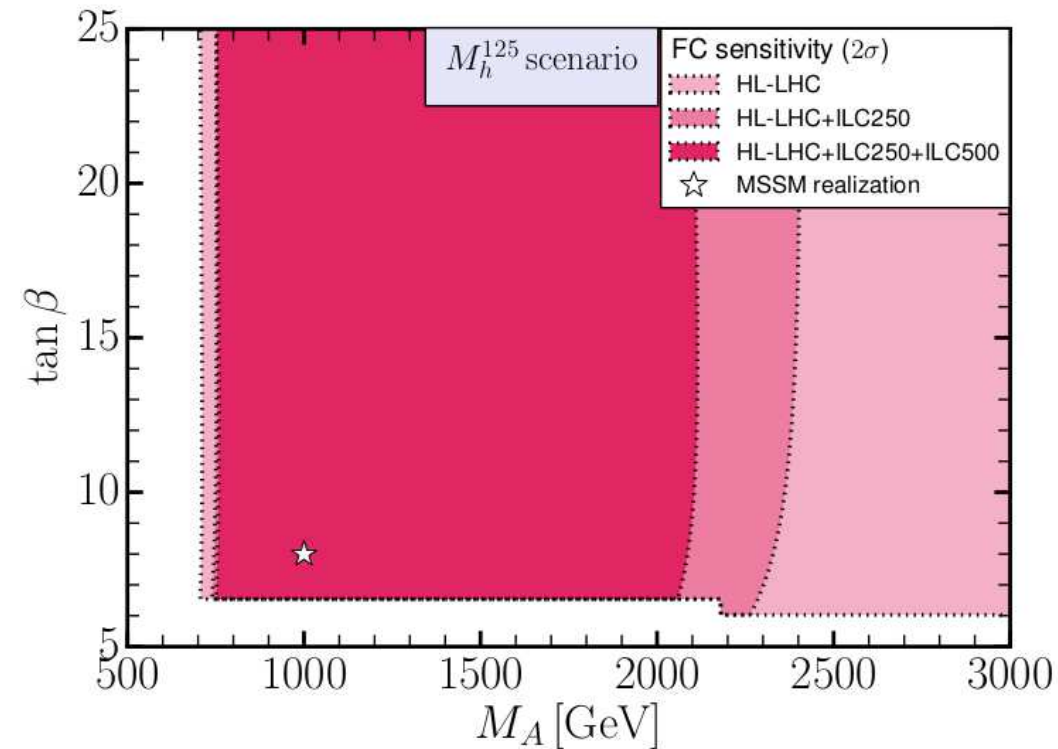


⇒ ILC shows strong improvement over HL-LHC in many cases

⇒ ... and without theory assumptions

⇒ and this improvement could be decisive!

- Assume a realization of an MSSM point: $M_A = 1$ TeV, $\tan \beta = 7 / 3$
- What limits can be set from rate/coupling measurements?

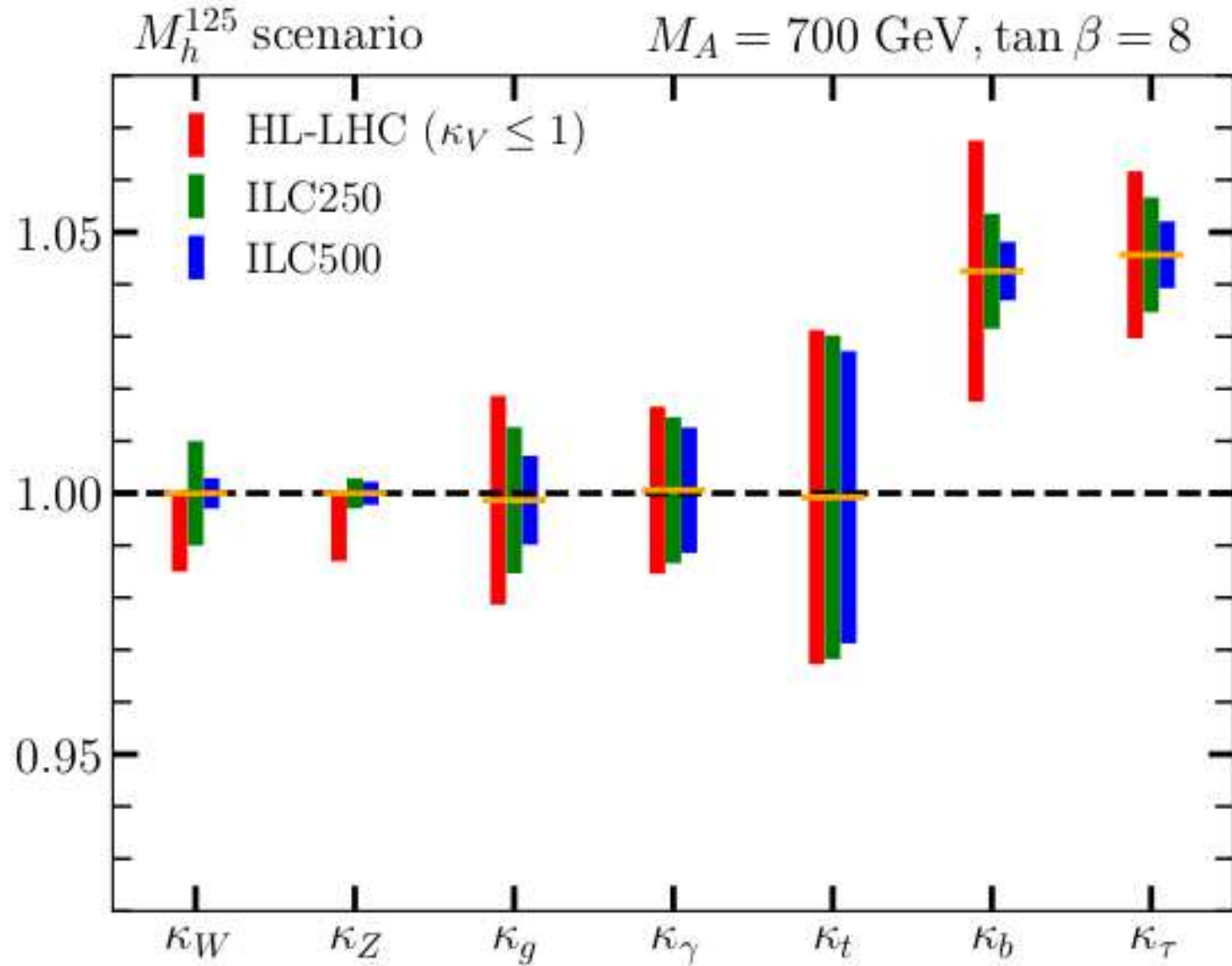


⇒ only ILC measurements give upper limit on M_A

⇒ limits on $\tan \beta$ only for small(er) $\tan \beta$

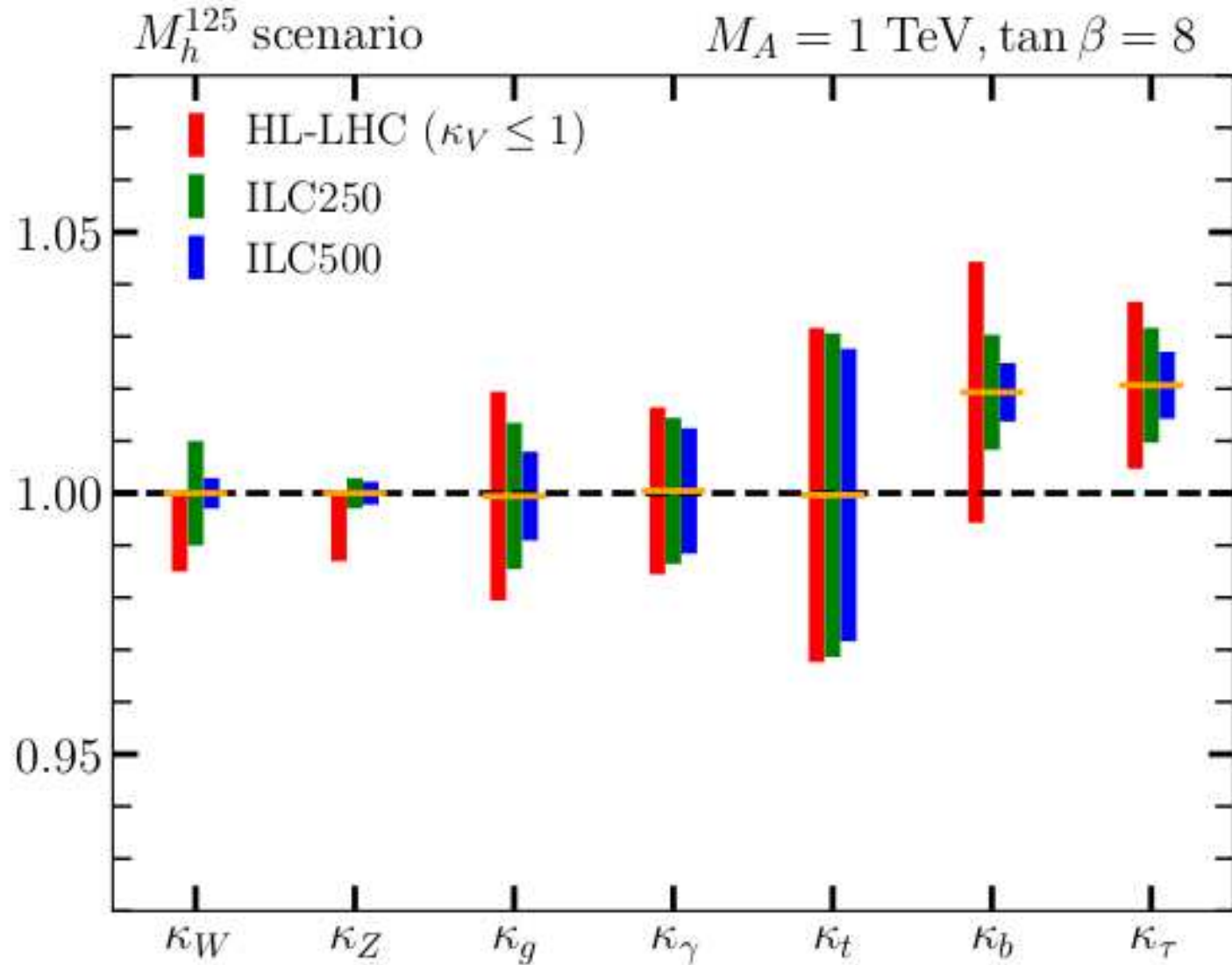
MSSM Wäscheleine I: e^+e^- precision vs. M_h^{125} ($M_A = 700$ GeV, $\tan \beta = 8$)

[H. Bahl et al. '20]



MSSM Wäscheleine II: e^+e^- precision vs. M_h^{125} ($M_A = 1000$ GeV, $\tan\beta = 8$)

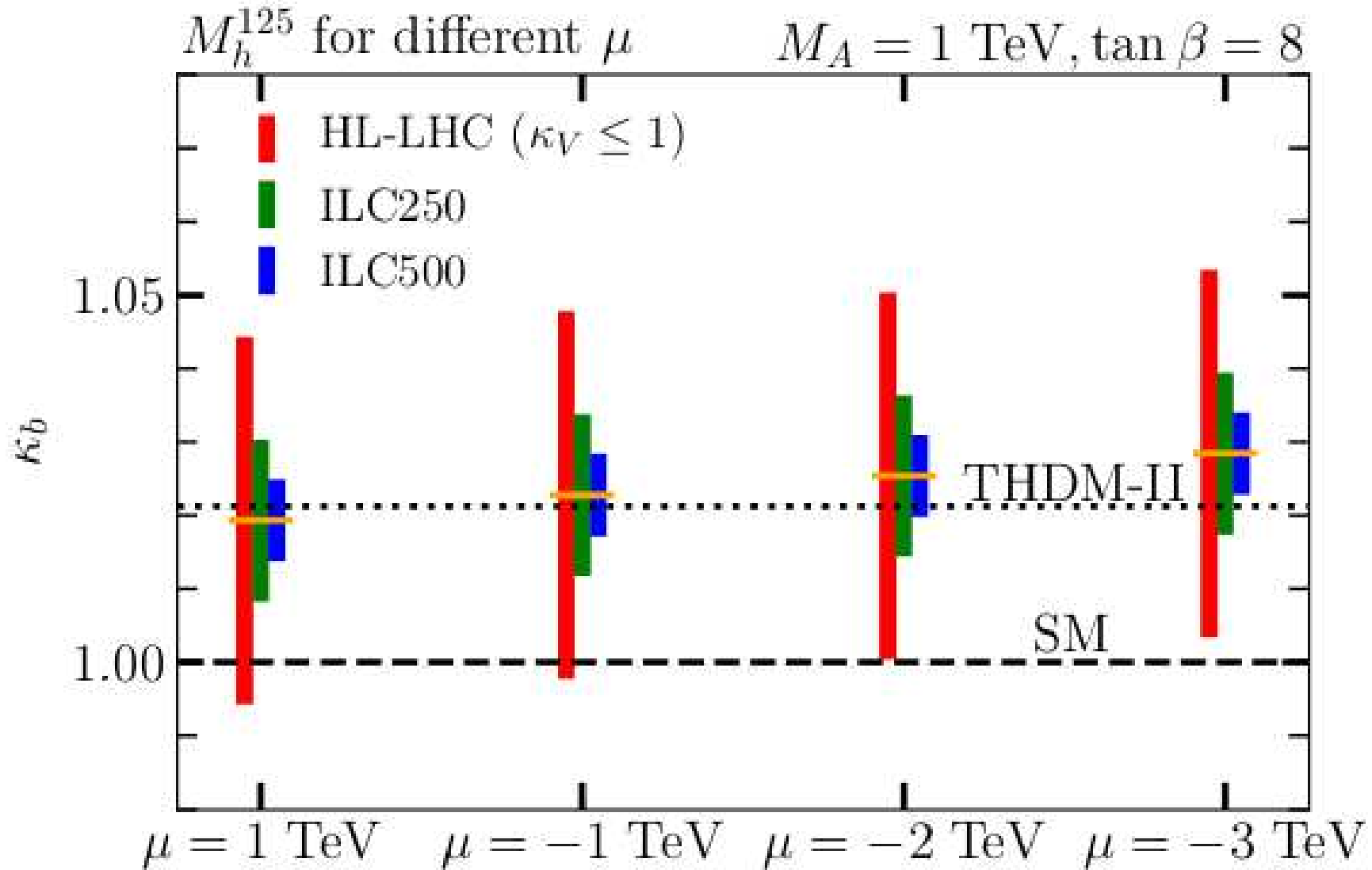
[H. Bahl et al. '20]



\Rightarrow only e^+e^- measurements allows to set upper limit on M_A

MSSM Wäscheleine V: e^+e^- vs. M_h^{125} ($M_A = 1000$ GeV, $\tan \beta = 8$)

[H. Bahl et al. '20]



⇒ MSSM vs. 2HDM: very challenging!

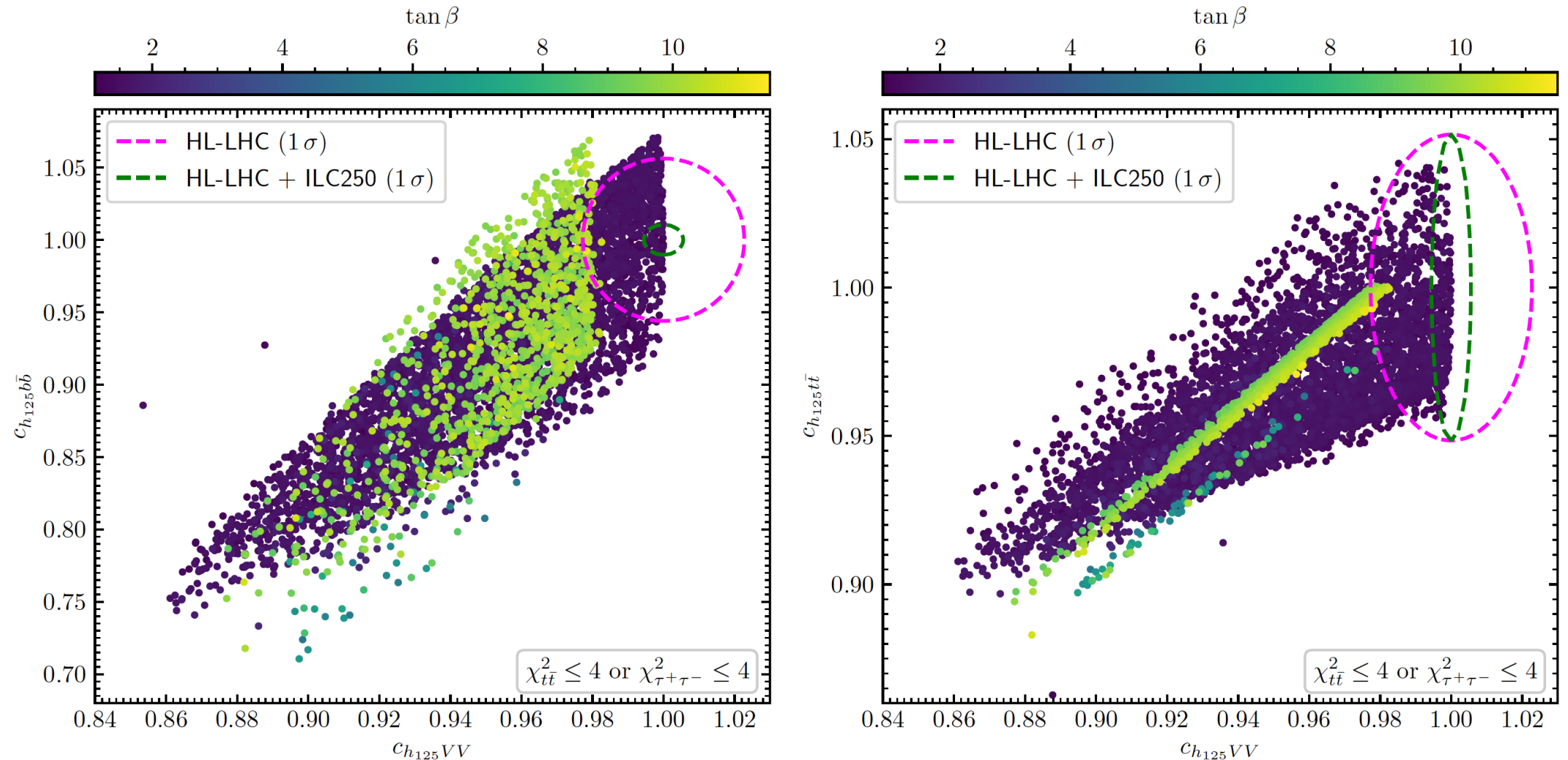
What about the “real hints” at ~ 400 GeV?

→ N2HDM: (NMSSM similar)

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→ N2HDM: (NMSSM similar)

[T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21]



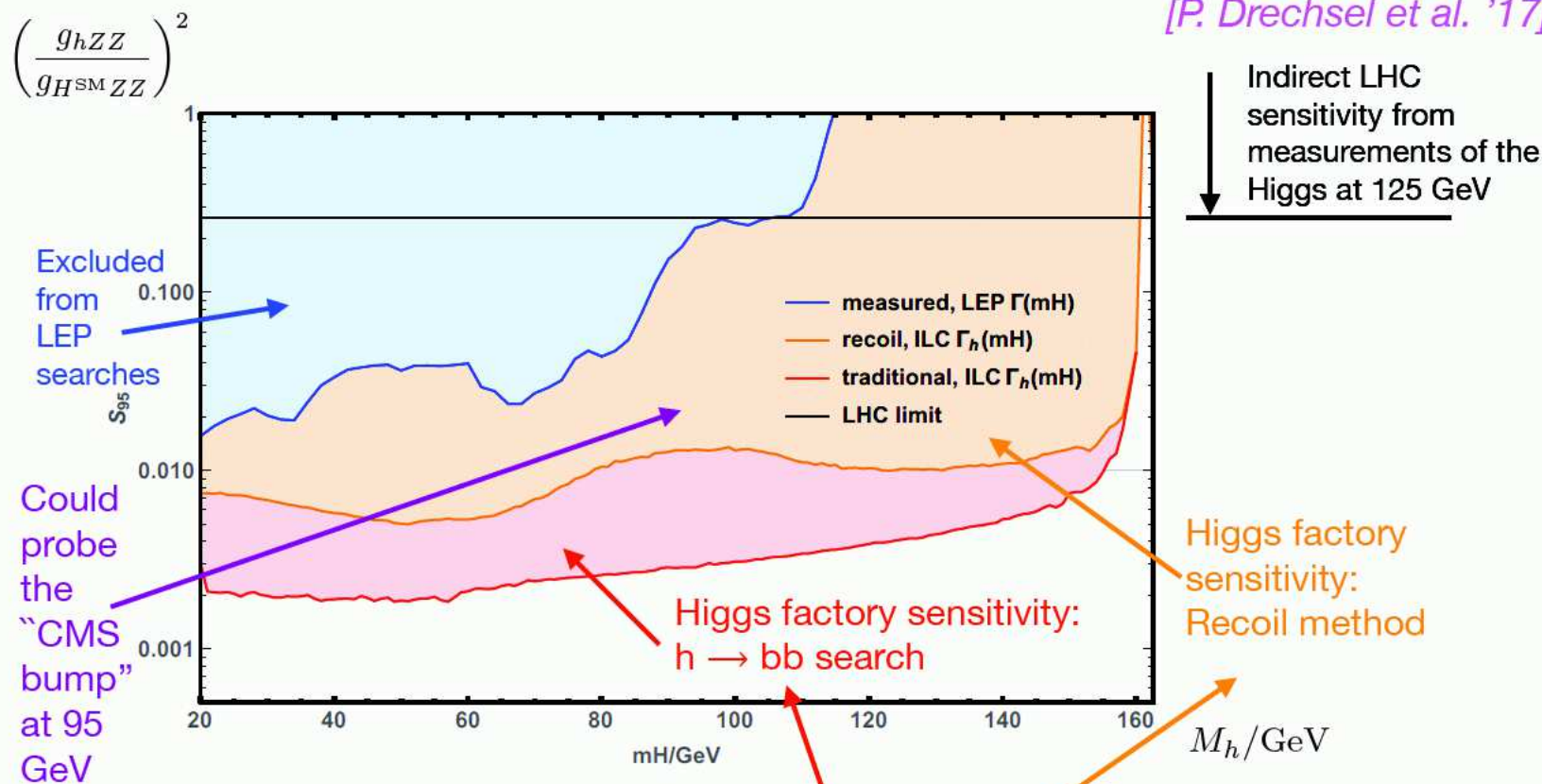
low $\tan\beta$ ($t\bar{t}$): SM limit reached, but many points show large deviation

high $\tan\beta$ ($\tau^+\tau^-$): ILC can always distinguish the SM from the N2HDM

4. Direct detection of “light” BSM Higgs bosons

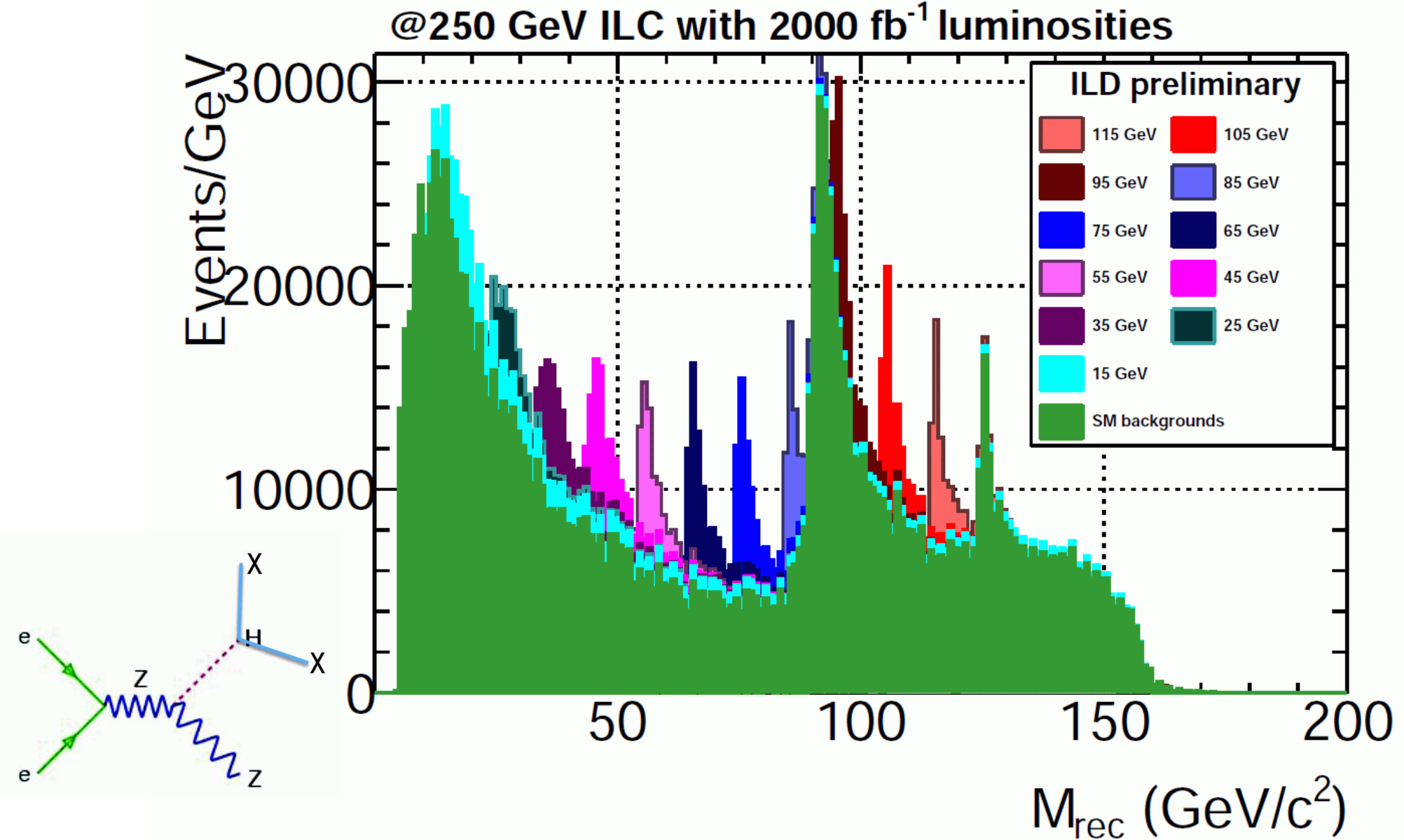
Example for discovery potential for new light states:
Sensitivity at 250 GeV with 500 fb⁻¹ to a new light Higgs

[P. Drechsel et al. '17]



⇒ Higgs factory at 250 GeV will explore a large untested region!

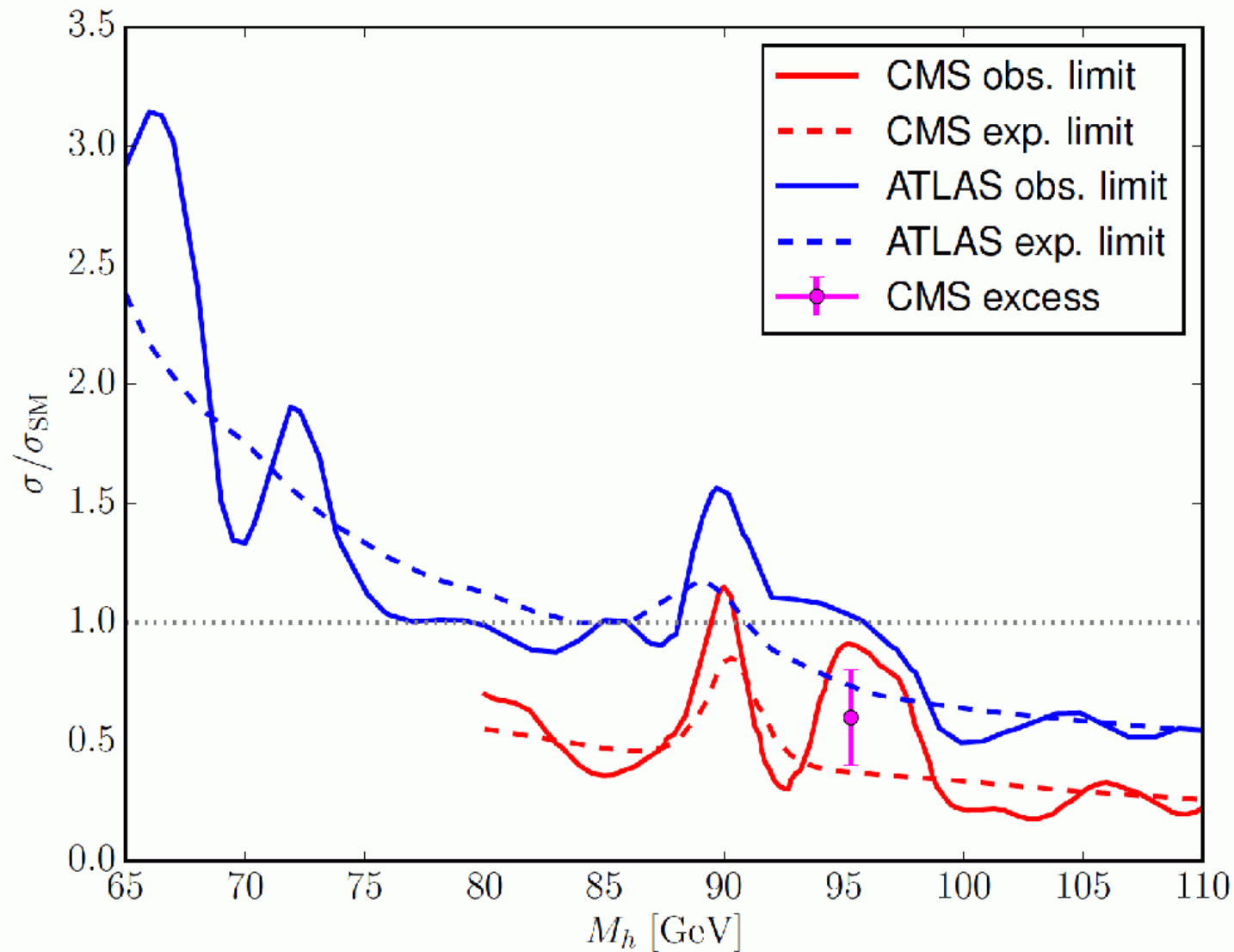
[Taken from G. Weiglein '18]



Case study: Search for $pp \rightarrow \phi \rightarrow \gamma\gamma$: excess at $m_\phi \sim 95$ GeV

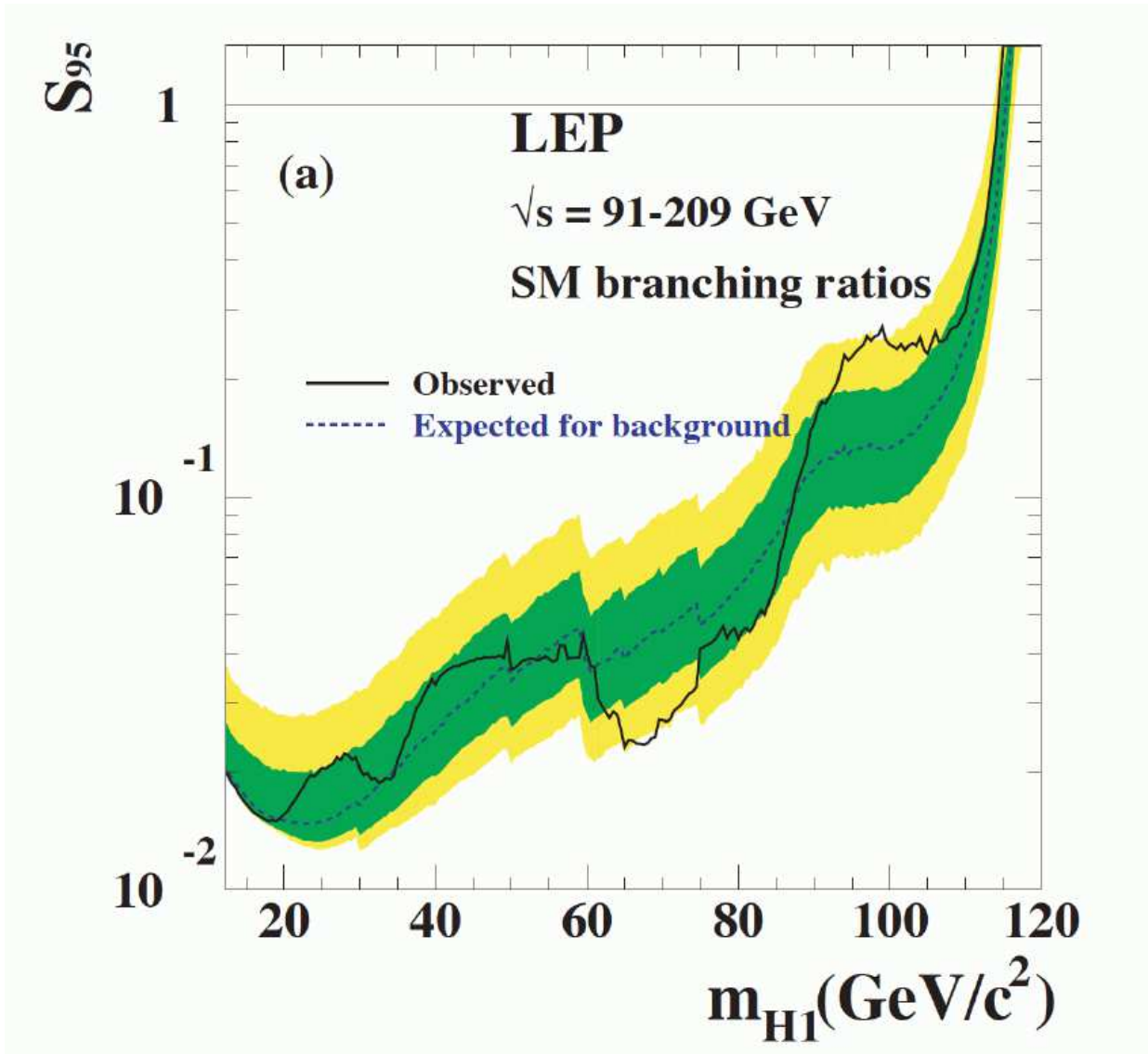
[CMS '17, ATLAS '18, S.H., T. Stefaniak '18]

$$\mu_{\text{CMS}} = 0.6 \pm 0.2$$

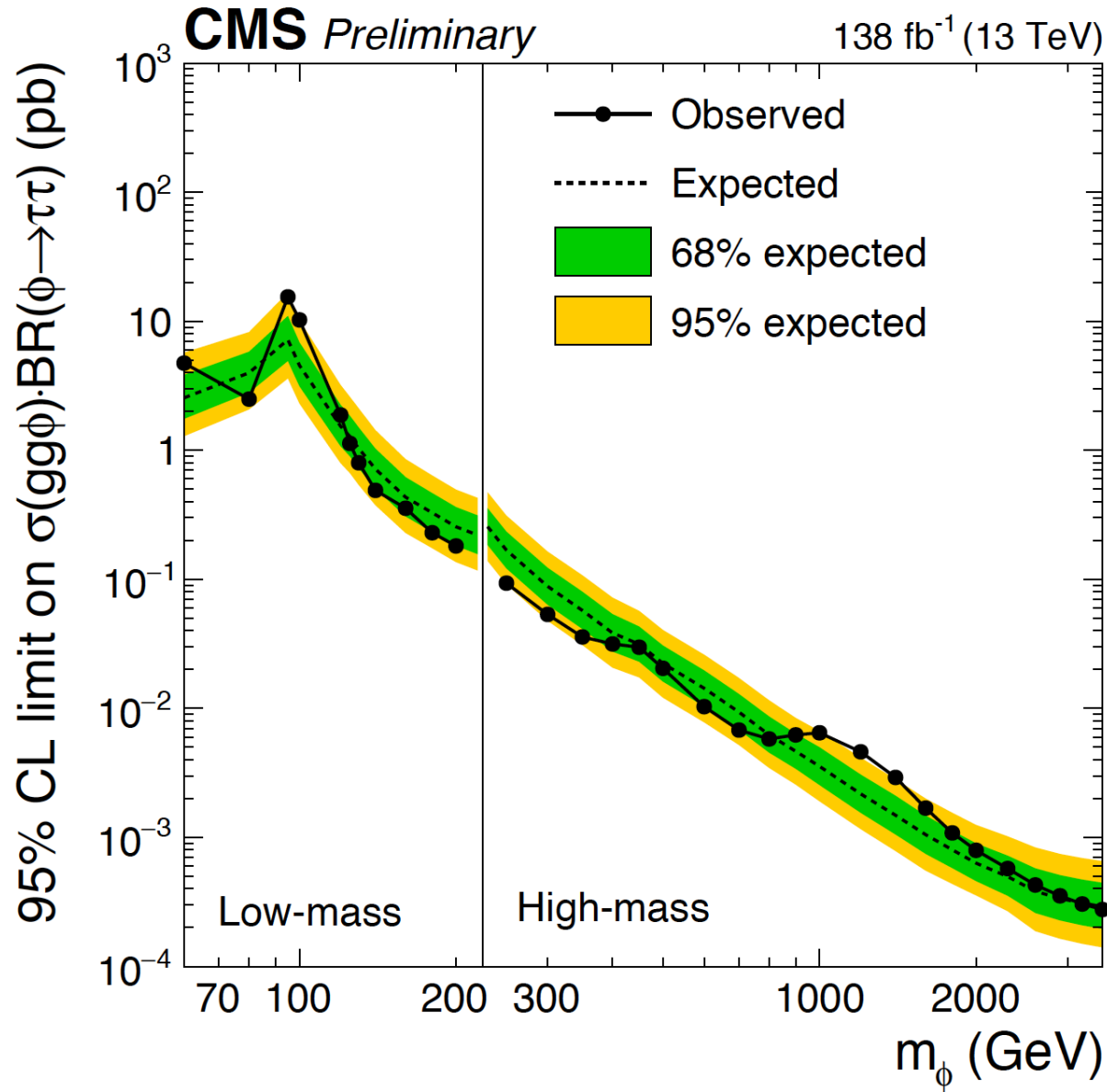


⇒ if there is something, it would look exactly like this!

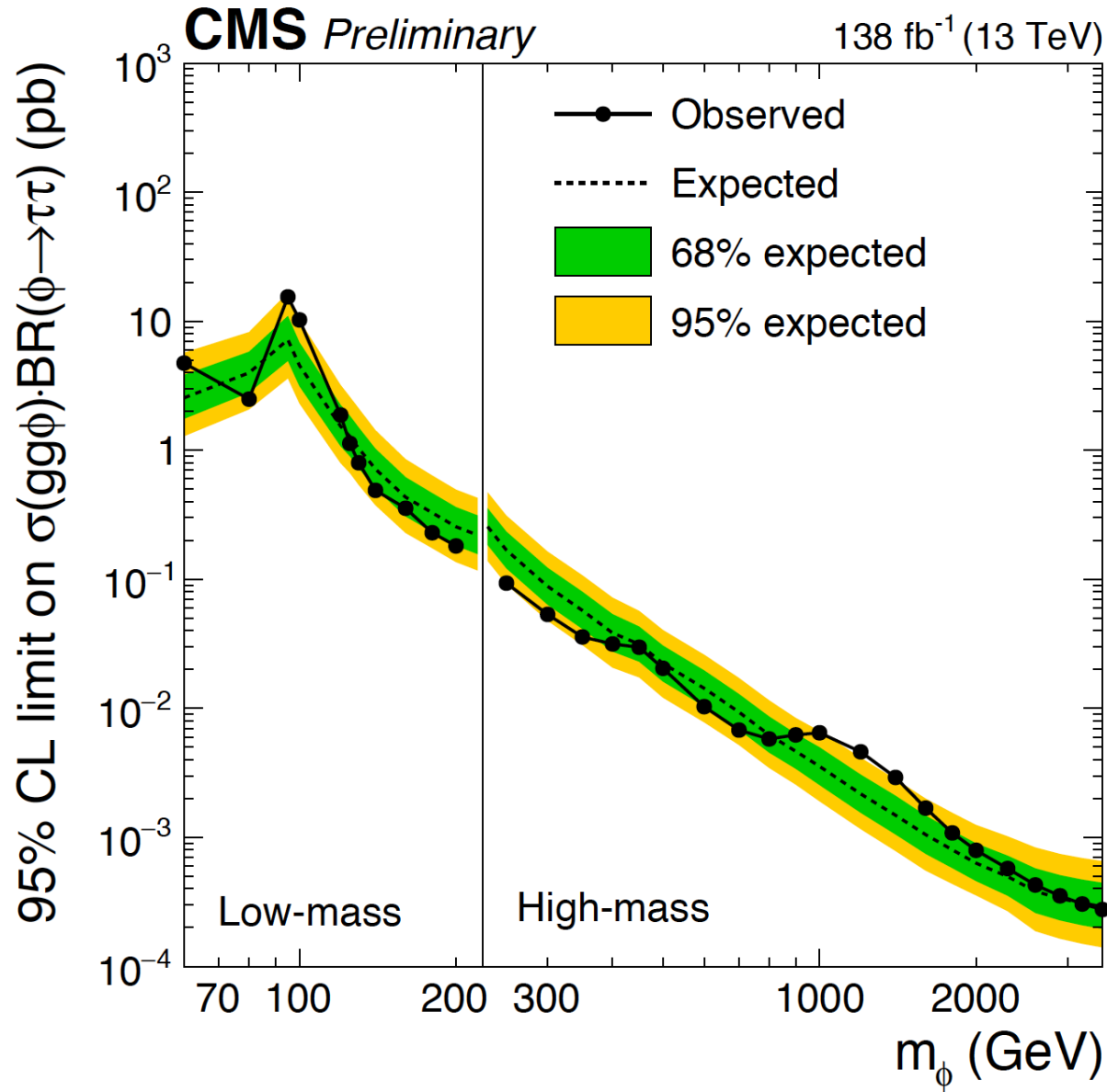
Remember the LEP excess?



$$\mu_{\text{LEP}}(98 \text{ GeV}) = \left[\sigma(e^+e^- \rightarrow Zh_1) \times \text{BR}(h_1 \rightarrow b\bar{b}) \right]_{\text{exp/SM}} = 0.117 \pm 0.057$$



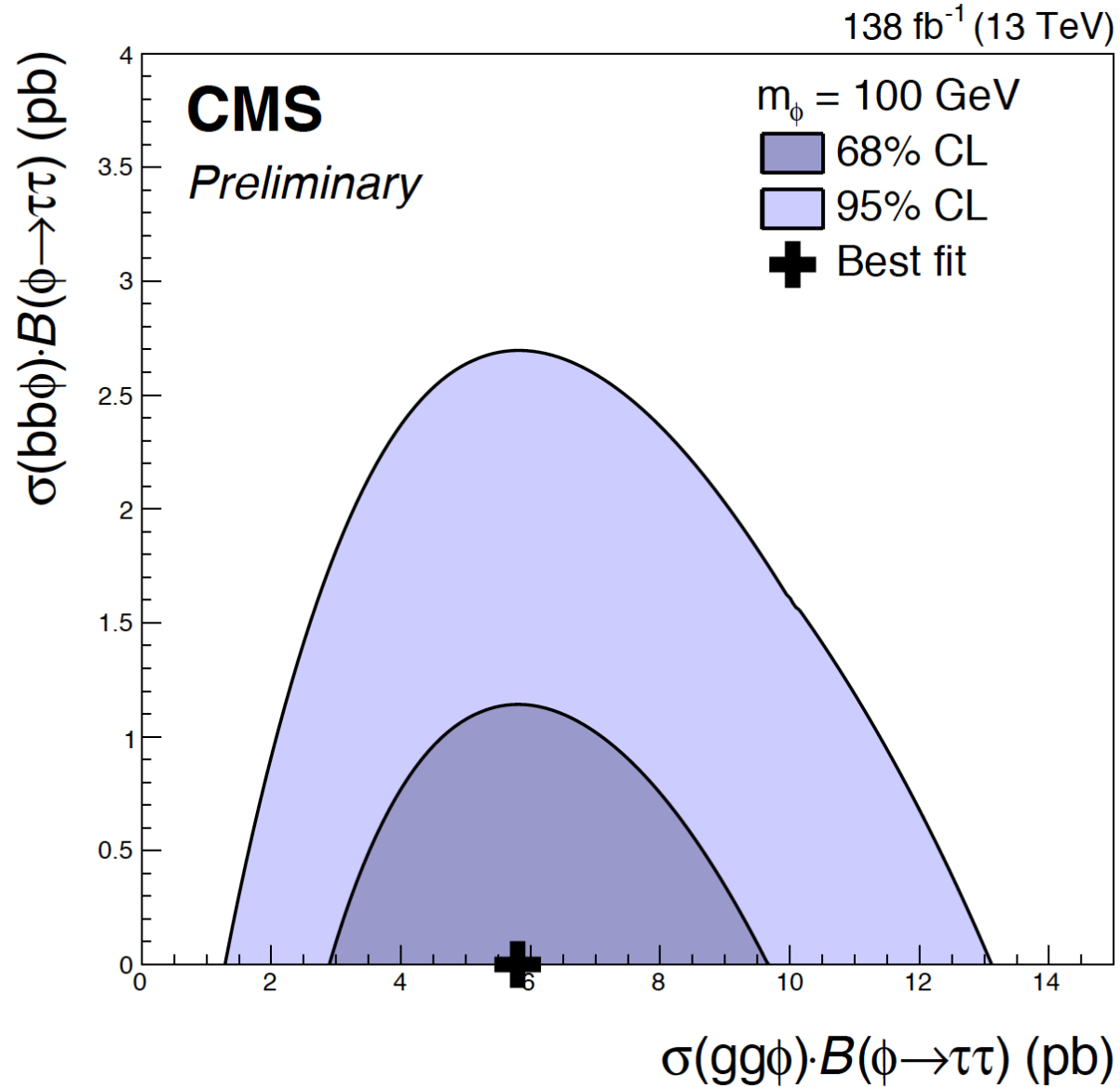
Can you spot the excess?



Can you spot the excess? At 95 – 100 GeV?

Better visible here, focusing on 100 GeV:

[CMS '22]



⇒ clear excess of $\sim 3\sigma$ at ~ 100 GeV

Now we have three excesses at ~ 95 GeV

$$\mu_{bb}^{\text{exp}} = 0.117 \pm 0.057, \quad \mu_{\gamma\gamma}^{\text{exp}} = 0.6 \pm 0.2, \quad \mu_{\tau\tau}^{\text{exp}} = 1.2 \pm 0.5$$

corresponding to

$$\mu_{bb}^{\text{exp}} \sim 2\sigma, \quad \mu_{\gamma\gamma}^{\text{exp}} \sim 3\sigma, \quad \mu_{\tau\tau}^{\text{exp}} \sim 2.4\sigma$$

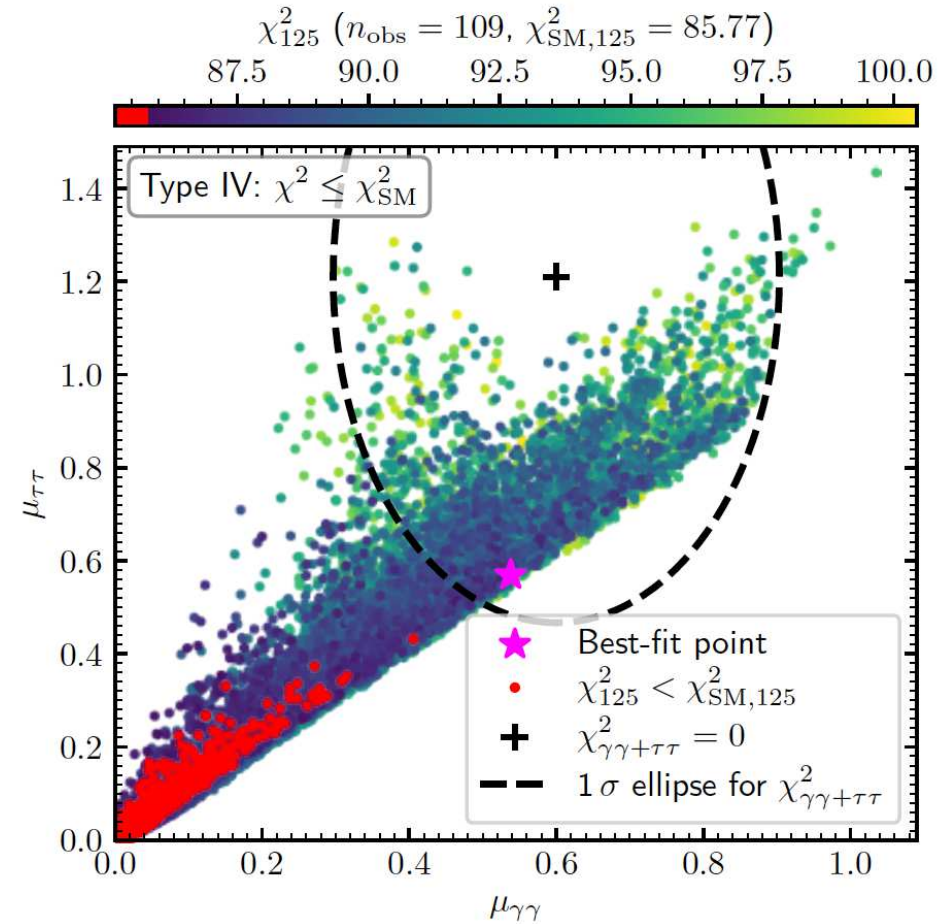
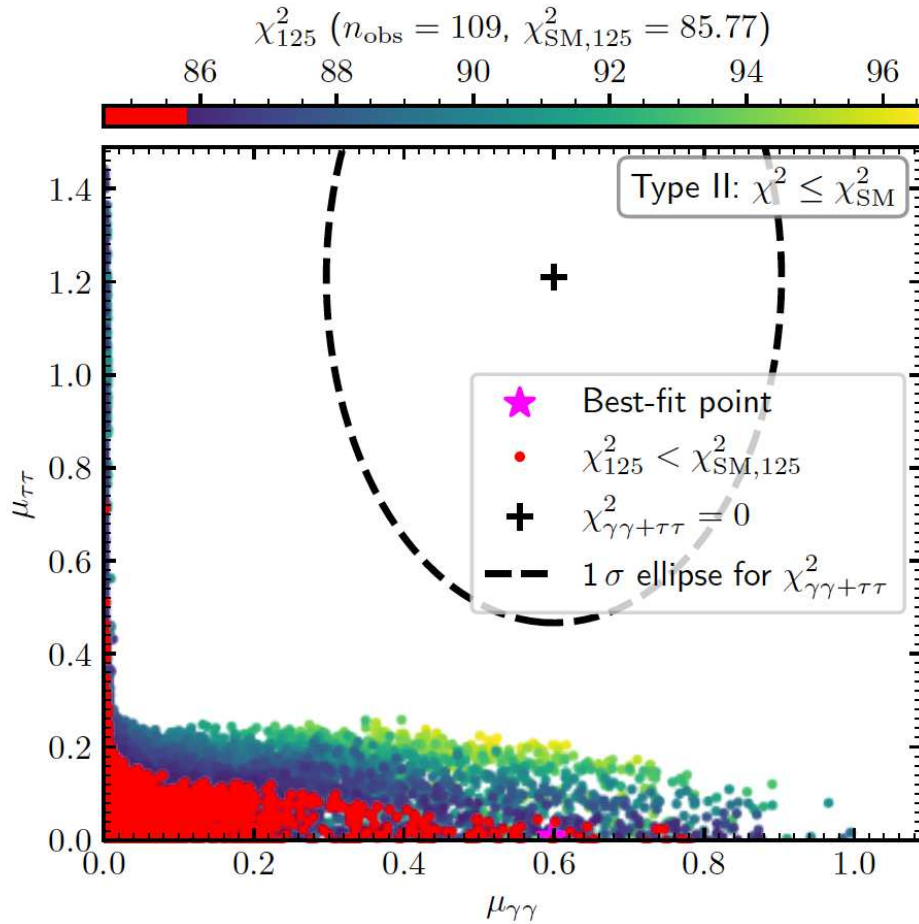
Three (effectively) independent channels

\Rightarrow no LEE (as theorist I am allowed to add naively)

$$\Rightarrow \sim 4.3\sigma$$

$$\chi_{95}^2 = \frac{(\mu_{bb}^{\text{theo}} - 0.117)^2}{(0.057)^2} + \frac{(\mu_{\gamma\gamma}^{\text{theo}} - 0.6)^2}{(0.2)^2} + \frac{(\mu_{\tau\tau}^{\text{theo}} - 1.2)^2}{(0.5)^2}$$

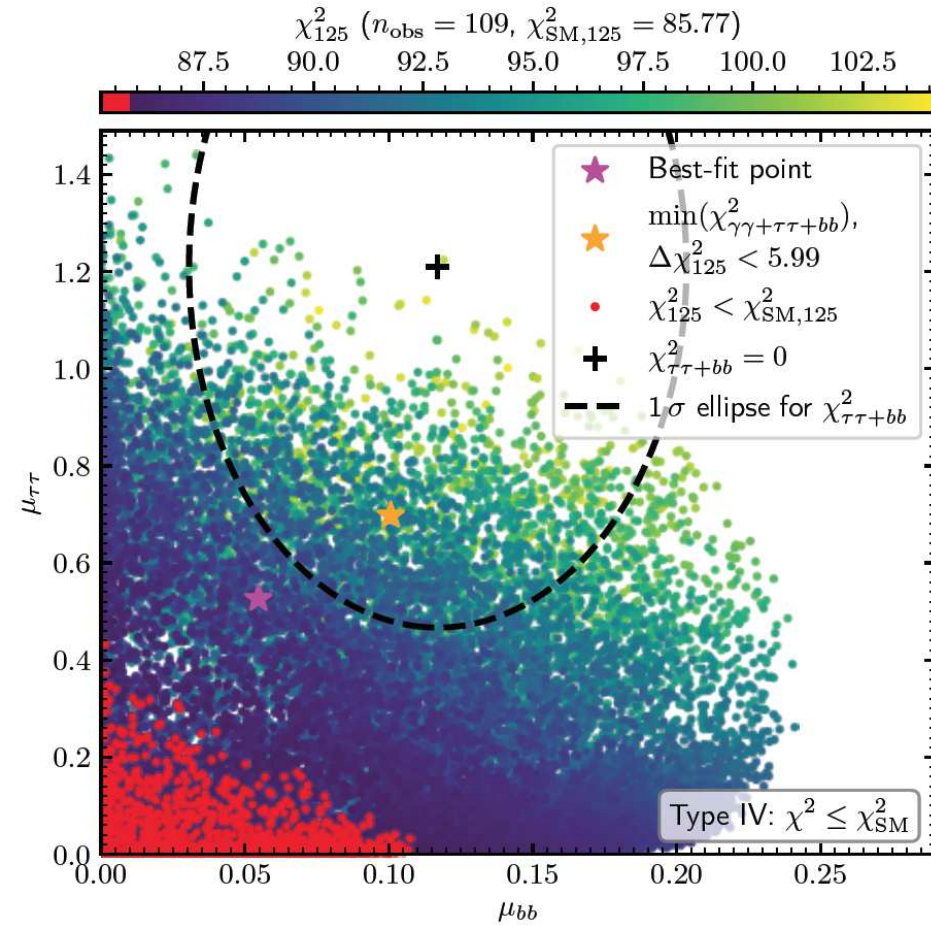
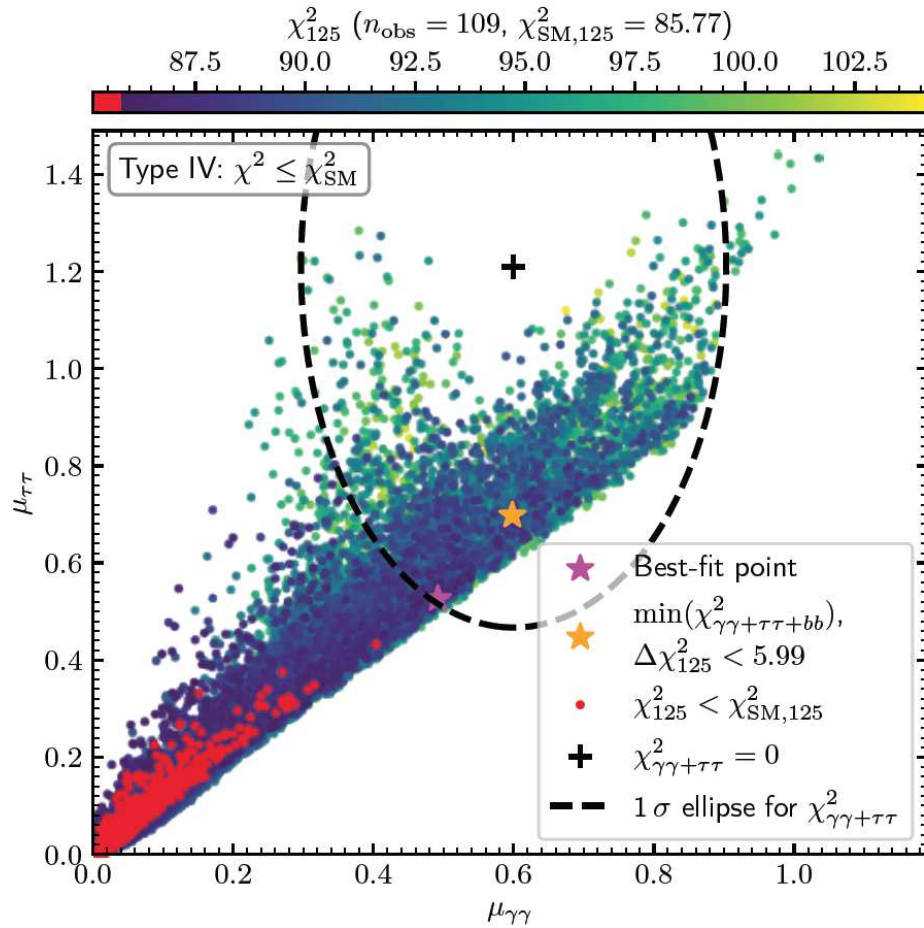
Can we fit all excesses together?



Color coding: χ_{125}^2 from HiggsSignals

⇒ only type IV can fit the $\gamma\gamma$ and $\tau\tau$ excesses

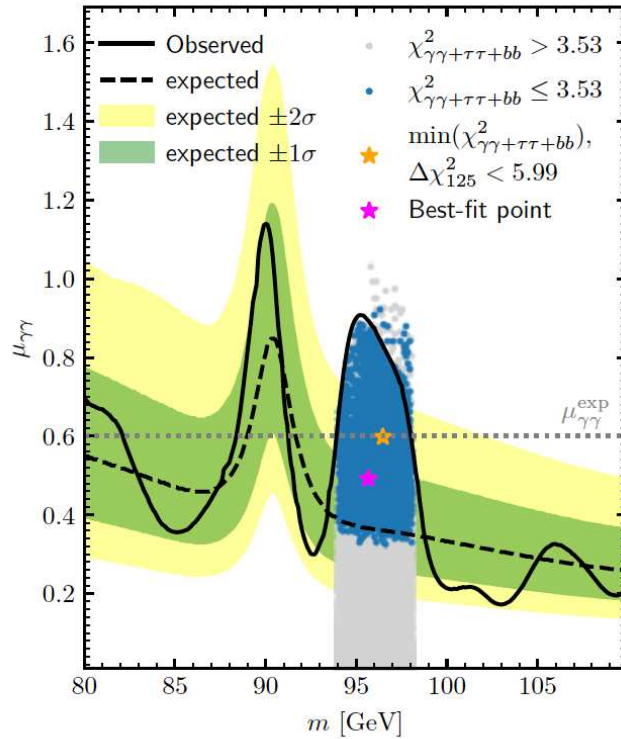
N2HDM type IV: fitting all three excesses: [*T. Biekötter, S.H., G. Weiglein '22*]



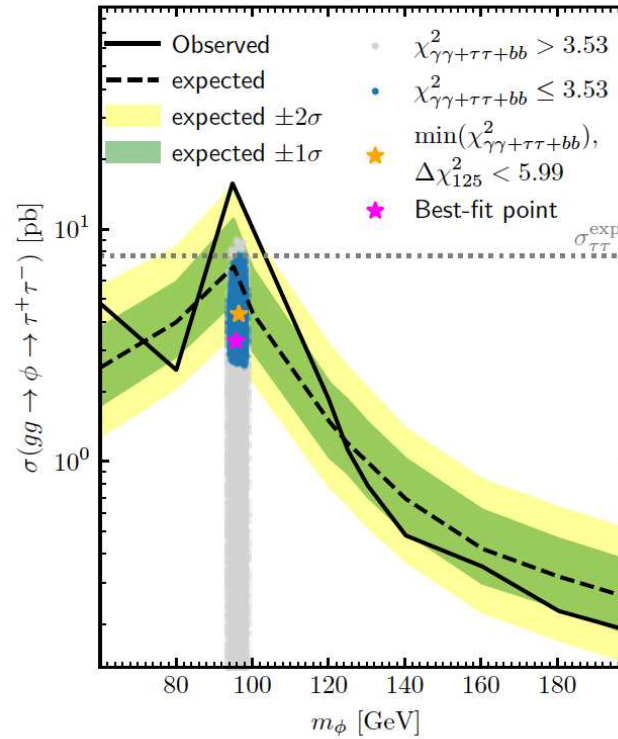
Color coding: χ_{125}^2 from HiggsSignals

⇒ type IV can fit the $\gamma\gamma$, $\tau\tau$ and bb excesses

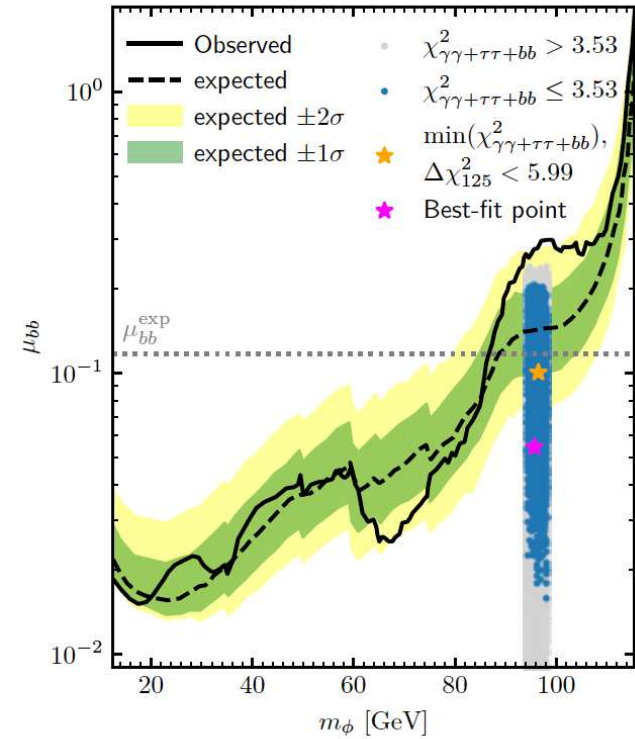
$pp \rightarrow h_{95} \rightarrow \gamma\gamma$



$gg \rightarrow h_{95} \rightarrow \tau^+\tau^-$



$e^+e^- \rightarrow Zh_{95} \rightarrow Zb\bar{b}$

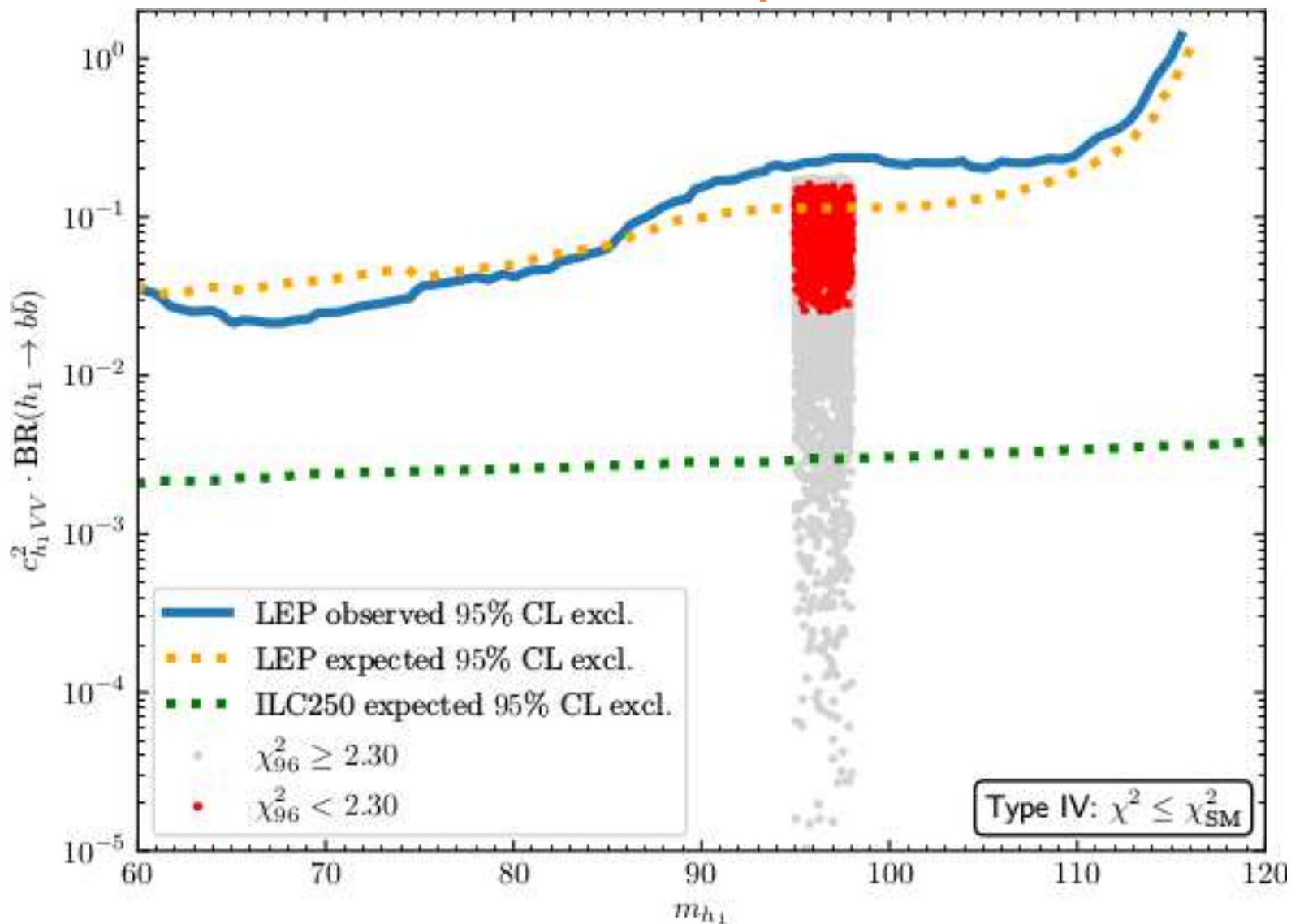


gray lines: central values of excesses

⇒ type IV can fit the $\gamma\gamma$, $\tau\tau$ and $b\bar{b}$ excesses very well

ILC production of the light scalar in the N2HDM type II:

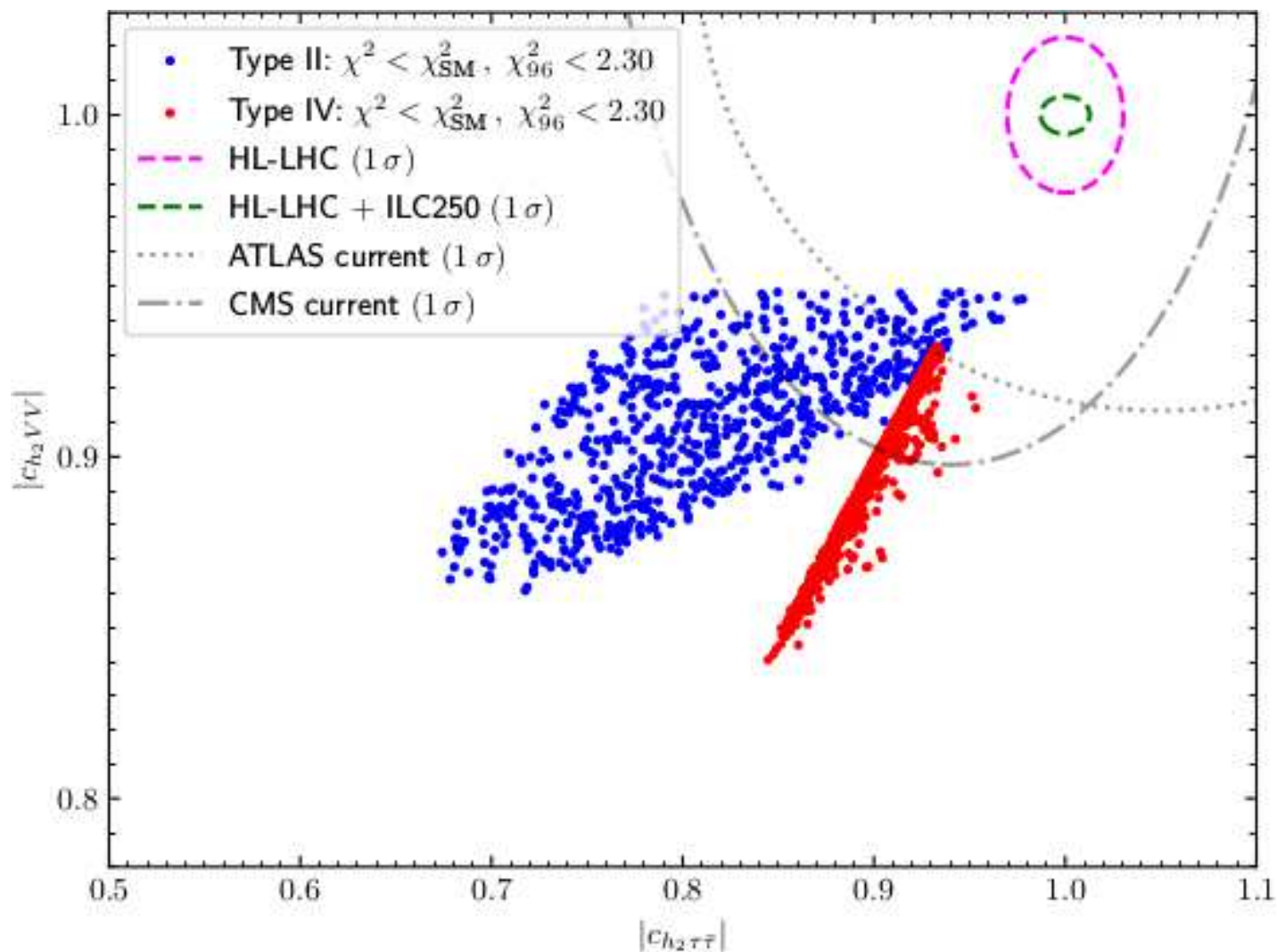
[T. Biekötter, S.H., G. Weiglein – PRELIMINARY]



⇒ new state easily in the reach of the ILC ⇒ coupling measurements

HL-LHC/ILC h_{125} coupling measurements

[T. Biekötter, S.H., G. Weiglein – PRELIMINARY]



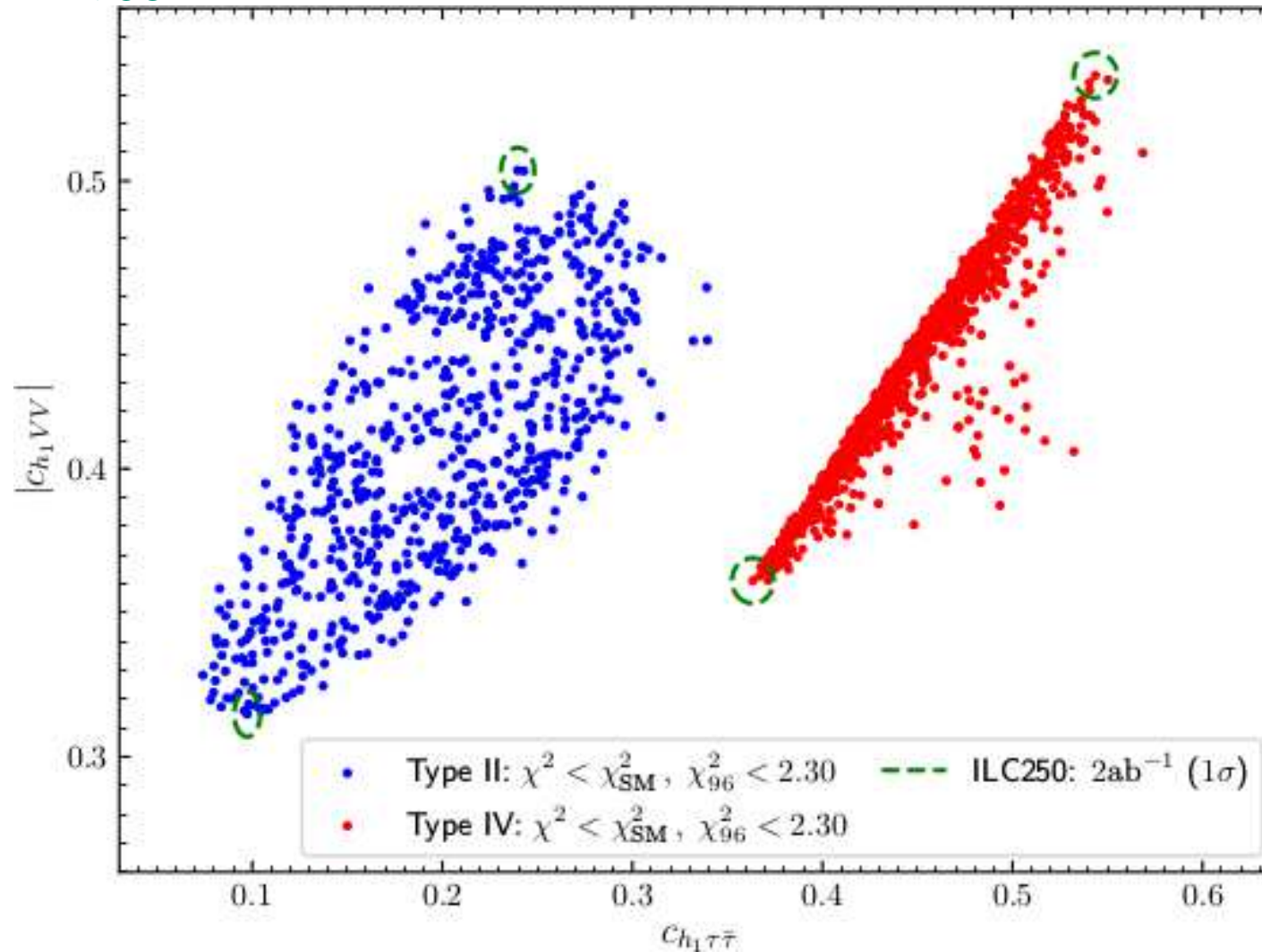
⇒ type II and IV show strong deviations from SM

⇒ N2HDM can always be distinguished from SM at the ILC

ILC ϕ_{95} coupling measurements at the ILC

[T. Biekötter, S.H., G. Weiglein – PRELIMINARY]

green circles: ϕ_{95} coupling precision at the ILC250



⇒ model distinction possible via coupling measurements at the ILC

5. Conclusinos

- The discovered Higgs boson **cannot be the SM Higgs boson**
 - check **changed properties** of h_{125}
 - search for additional Higgs bosons **above and below** 125 GeV
- Experimental hints (as motivation/toy examples)
 - $t\bar{t}$ (CMS) (and $\tau^+\tau^-$ (ATLAS)) at ~ 400 GeV
 - $\gamma\gamma$ (CMS) and $b\bar{b}$ (LEP) and $\tau^+\tau^-$ (CMS) at ~ 95 GeV ($\Rightarrow 4.3\sigma?$)
- ILC physics opportunities:
 - **ILC** direct detection (at least) up to $\sqrt{s}/2$ ($400 < 500$:-)
 - **ILC250**: light Higgs bosons up to ~ 160 GeV detectable
 - **ILC250/500**: h_{125} **coupling meas.** are likely to see a deviation
 \Rightarrow ILC can set **upper limits** on NP scales
 - **ILC250**: **precision study** of light Higgs bosons possible
 \Rightarrow to disentangle the underlying model
- No time for BSM triple Higgs couplings ...

Higgs Days at Santander 2022

Theory meets Experiment

5 – 9 September

Contact: Sven.Heinemeyer@cern.ch
Local: Alicia.Calderon@cern.ch
Gervasio.Gomez@cern.ch
<http://hdays.csic.es>



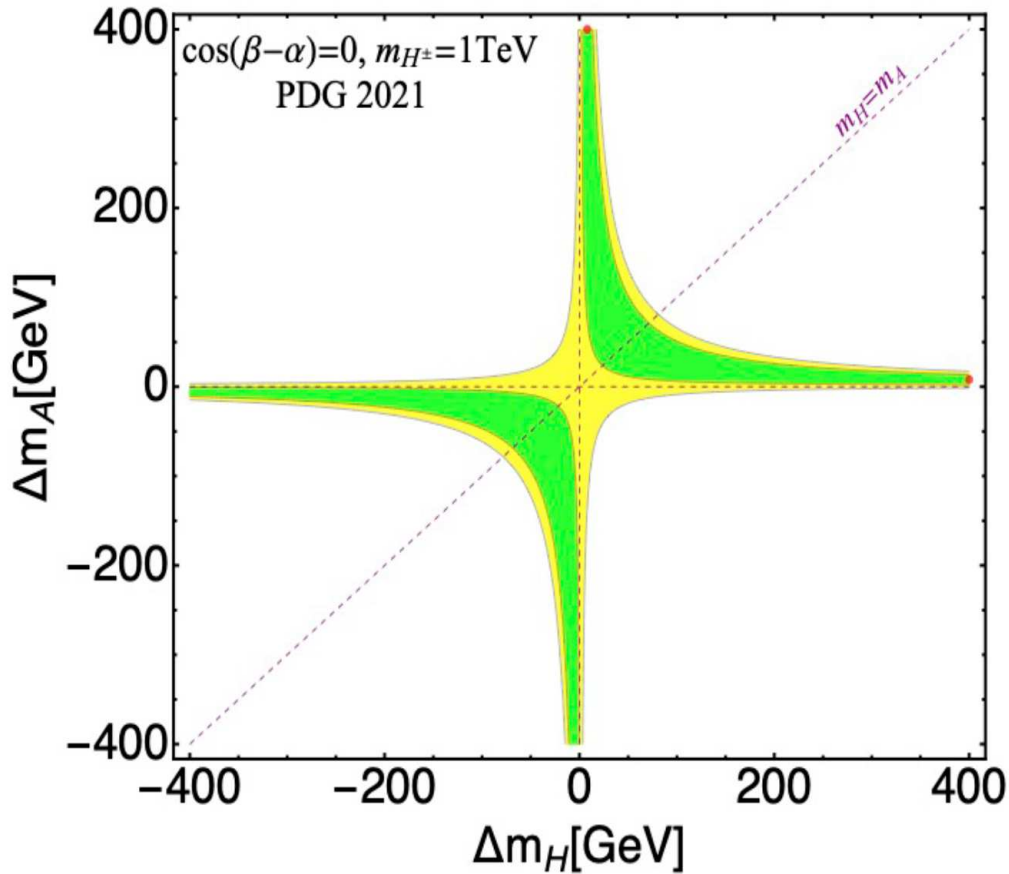
A photograph of a man with reddish-brown hair looking up at a full-body Darth Vader costume. The scene is set in a dark, industrial environment with blue lighting from overhead fixtures. The text "Further Questions?" is overlaid in white on the left side of the image.

Further Questions?

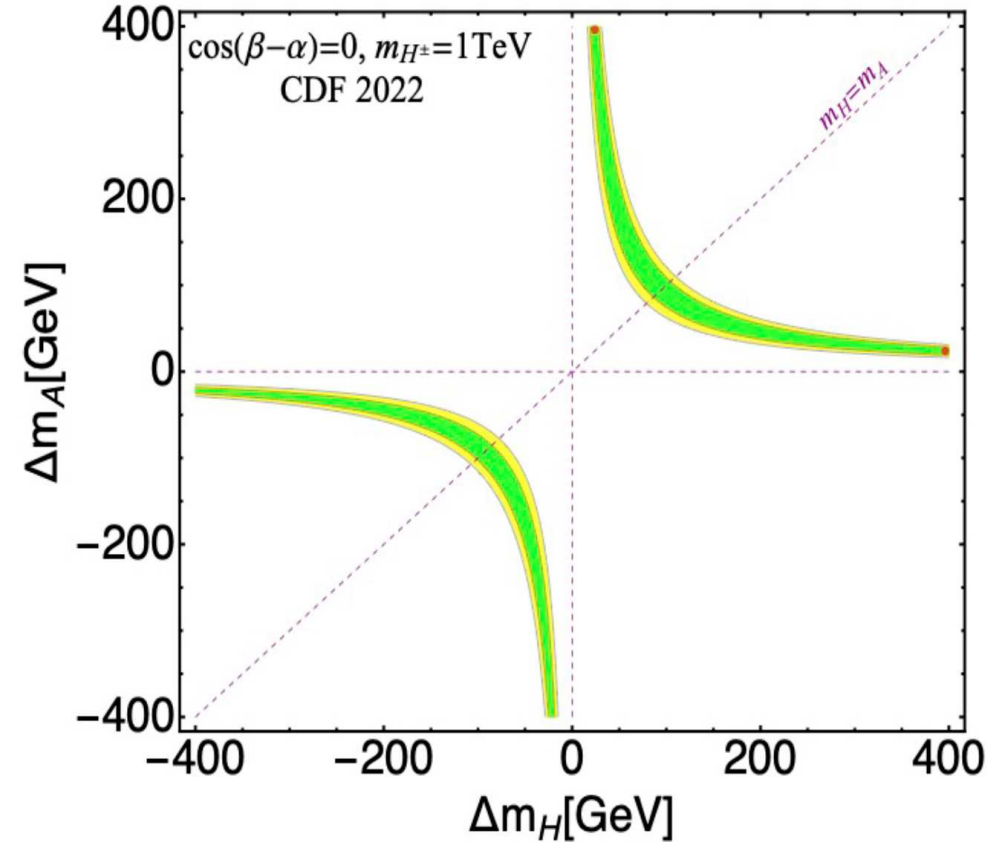
Example: $m_{H^\pm} = 1000 \text{ GeV}$, $\cos(\beta - \alpha) = 0$

[C. Lu, L. Wu, Y. Wu, B. Zhu '22]

PDG 2021



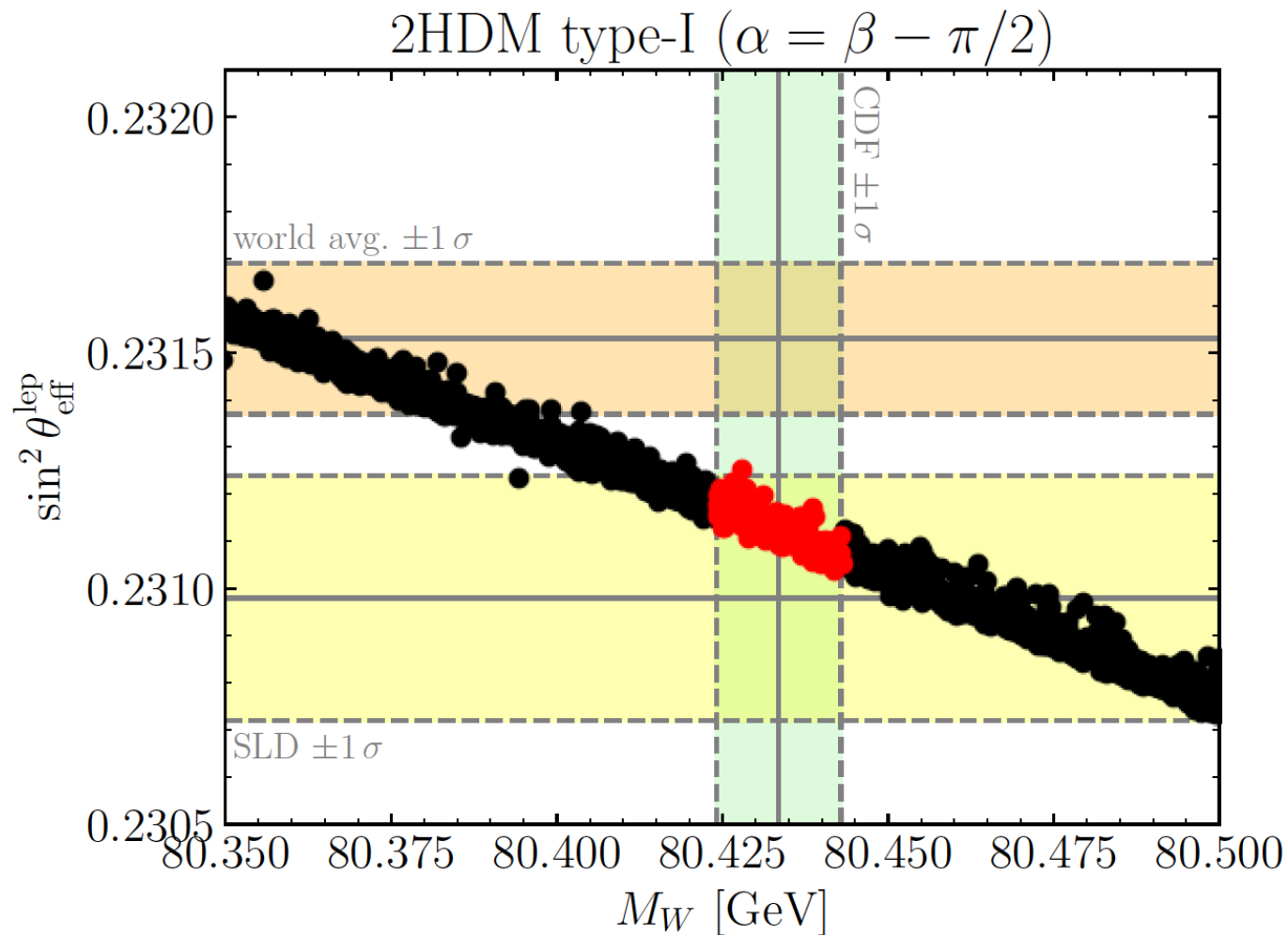
M_W^{CDF}



\Rightarrow nearly no overlap of the 2σ regions

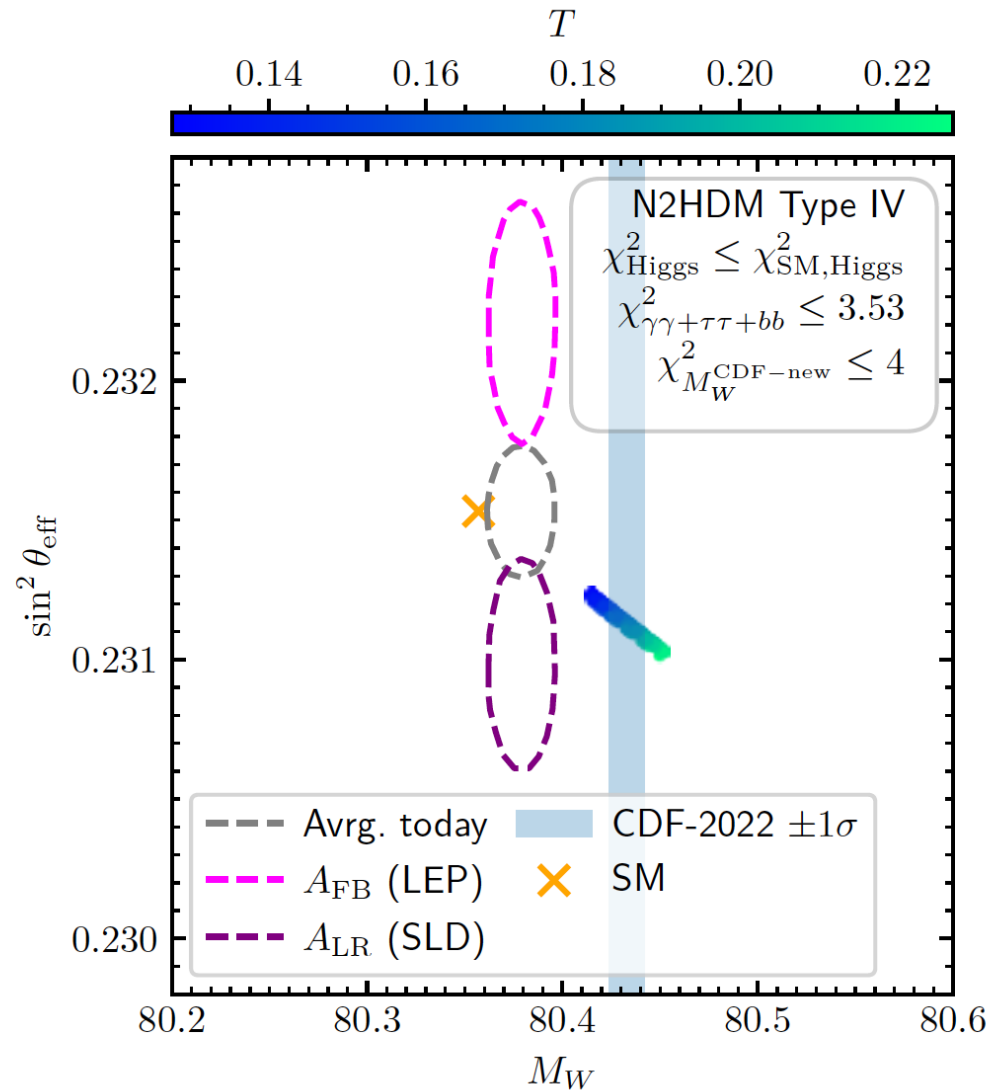
\Rightarrow new CDF value requires relatively large BSM Higgs mass splitting

\Rightarrow but no upper limit on heavy Higgs-boson mass scale



Remember: $\Delta\rho$ goes up $\Rightarrow M_W$ goes up, $\sin^2 \theta_{\text{eff}}$ goes down
 \Rightarrow agreement only with SLD value of $\sin^2 \theta_{\text{eff}}$

⇒ N2HDM favored by 3 independent excesses in Higgs searches at ~ 95 GeV



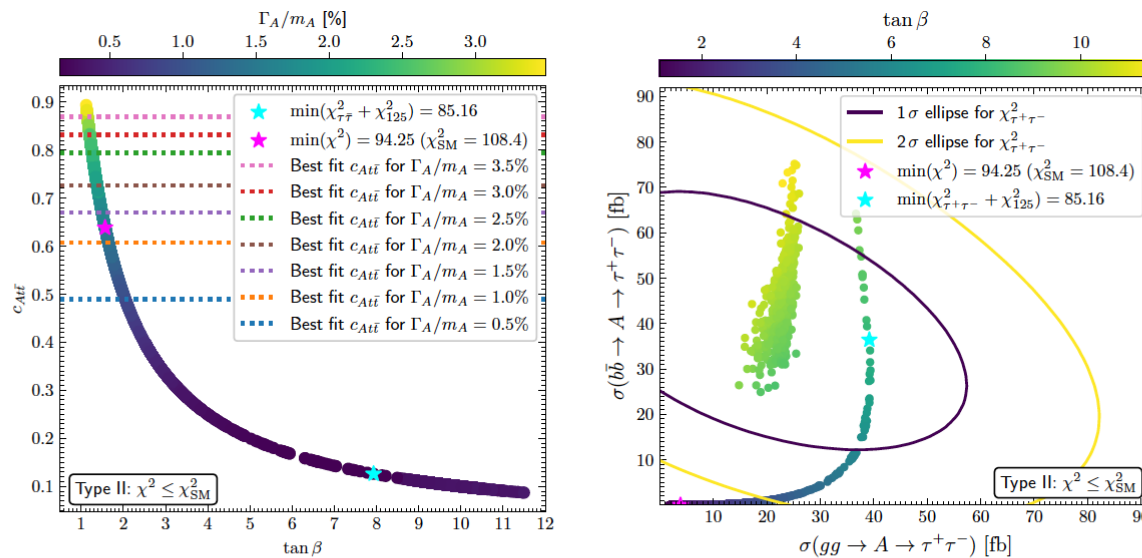
Remember: $\Delta\rho$ goes up $\Rightarrow M_W$ goes up, $\sin^2 \theta_{\text{eff}}$ goes down
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A 400 GeV pseudoscalar in the type II N2HDM

$$\chi^2 = \chi_{125}^2 + \chi_{t\bar{t}}^2 + \chi_{\tau^+\tau^-}^2, \text{ we demand: } \chi^2 \leq \chi_{\text{SM}}^2$$

$$20 \text{ GeV} \leq m_{h_{a,c}} \leq 1000 \text{ GeV}, \quad m_{h_b} = 125.09 \text{ GeV}, \quad m_A = 400 \text{ GeV},$$

$$550 \text{ GeV} \leq m_{H^\pm} \leq 1000 \text{ GeV}, \quad 10 \text{ GeV} \leq v_s \leq 1500 \text{ GeV}, \quad 0.5 \leq \tan \beta \leq 12.5$$



(Also the “ $A \rightarrow Zh$ ” excess can be realized)

Both the $t\bar{t}$ and the $\tau^+\tau^-$ excesses can be realized, but not simultaneously

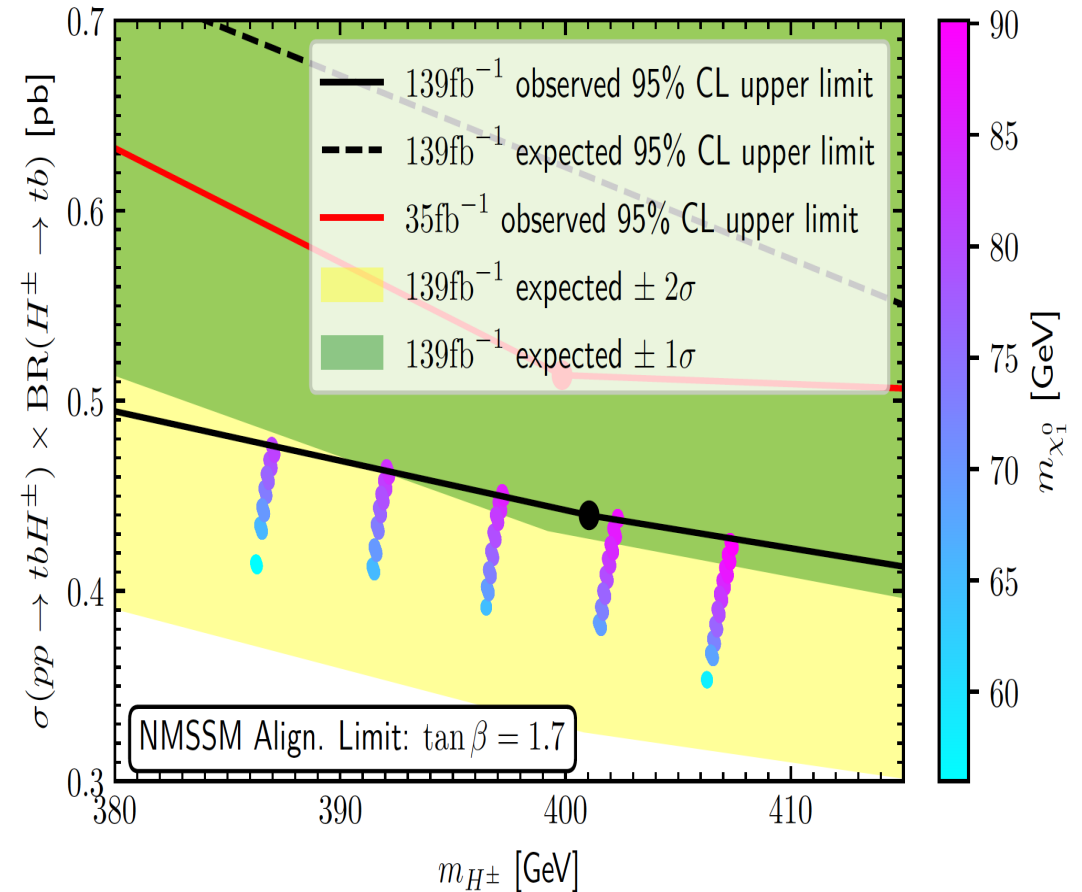
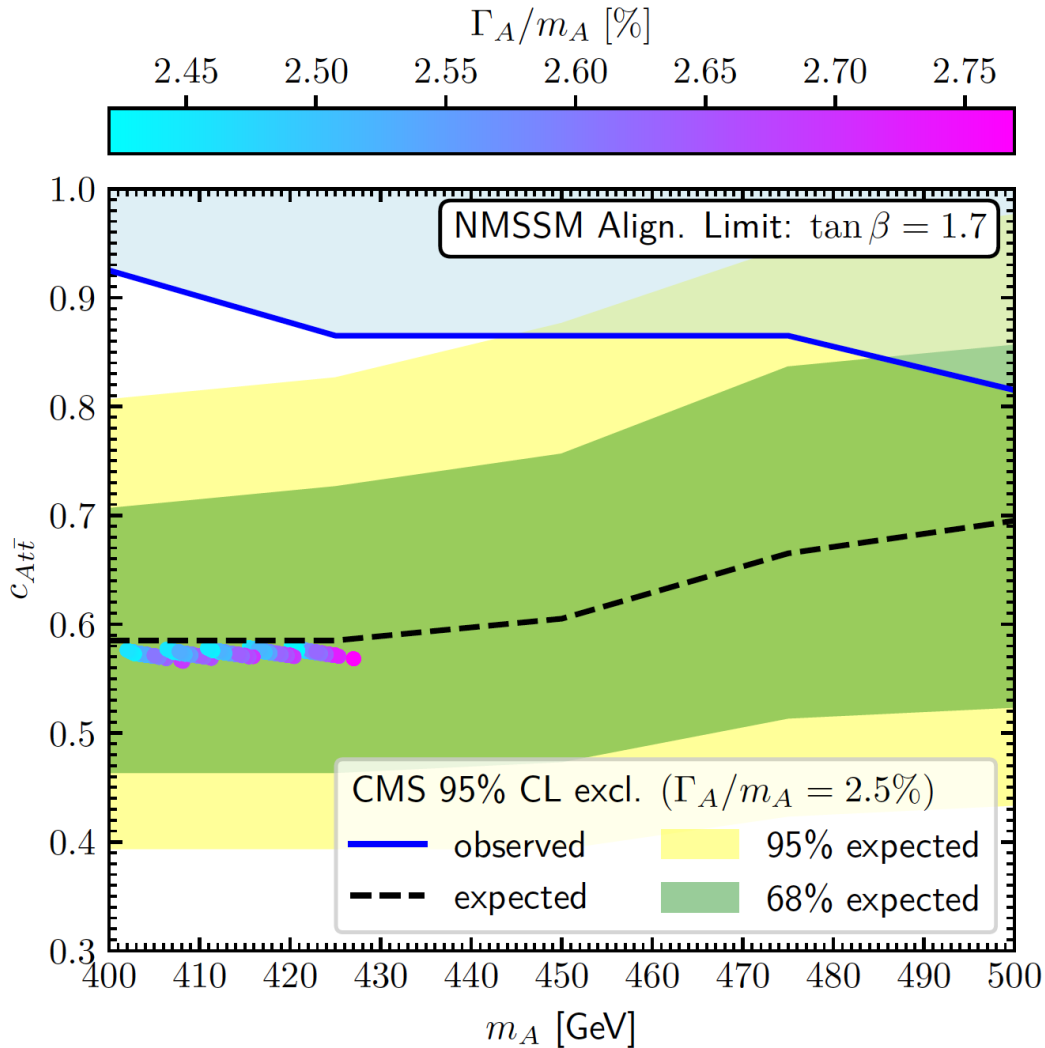
→ Later

$$\tan \beta \lesssim 2.5 \text{ for } t\bar{t} \text{ excess}$$

$$\tan \beta \gtrsim 5.5 \text{ for } \tau^+\tau^- \text{ excess}$$

[T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21]

Possible hint for heavy Higgses in the NMSSM (with $\tan\beta = 1.7$):



$\Rightarrow t\bar{t}$ excess can be explained in the NMSSM (with $\tan\beta \sim 1.7$)

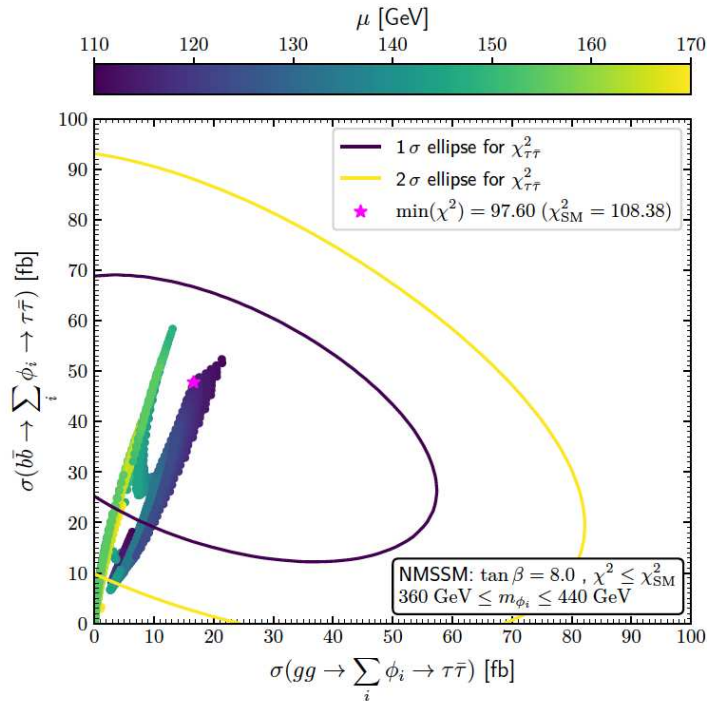
[T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21]

Possible hint for heavy Higgses in the NMSSM (with $\tan \beta = 8$):

[taken from T. Biekötter '21]

A pseudoscalar at ~ 400 GeV in the NMSSM

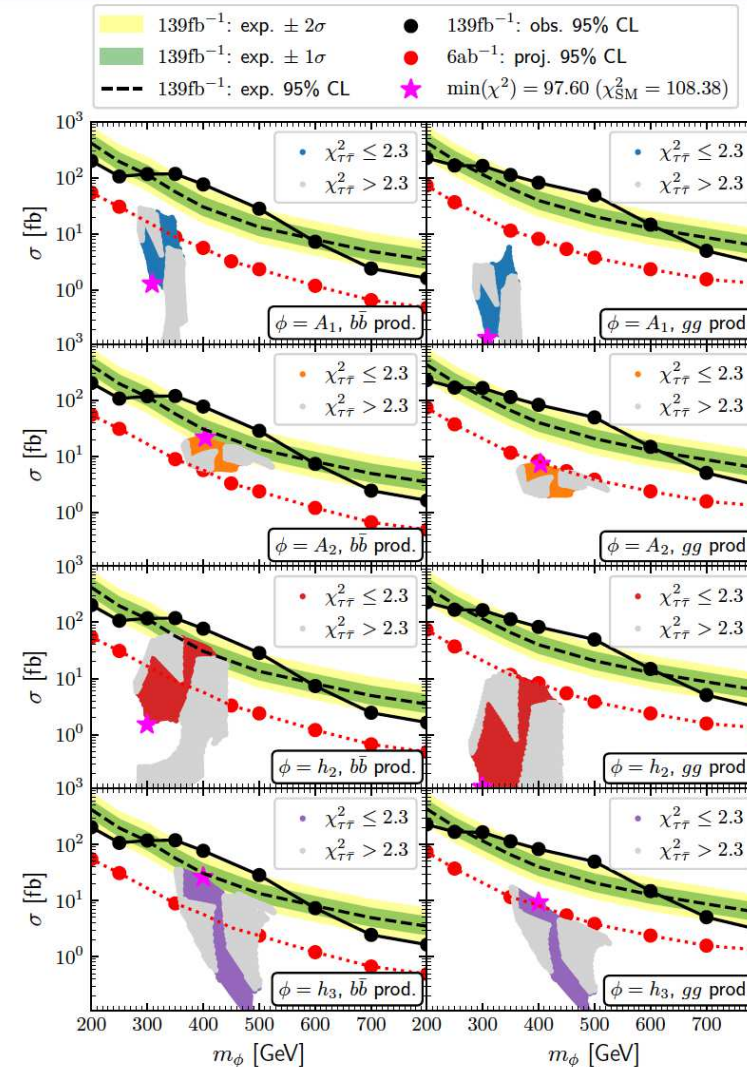
$\tau^+ \tau^-$ excess \rightarrow moderate $\tan \beta = 8$



Interference effects not important:

$$m_{h_3} - m_{h_2} \gg \Gamma_{h_2} + \Gamma_{h_3}$$

$$m_{A_2} - m_{A_1} \gg \Gamma_{A_1} + \Gamma_{A_2}$$

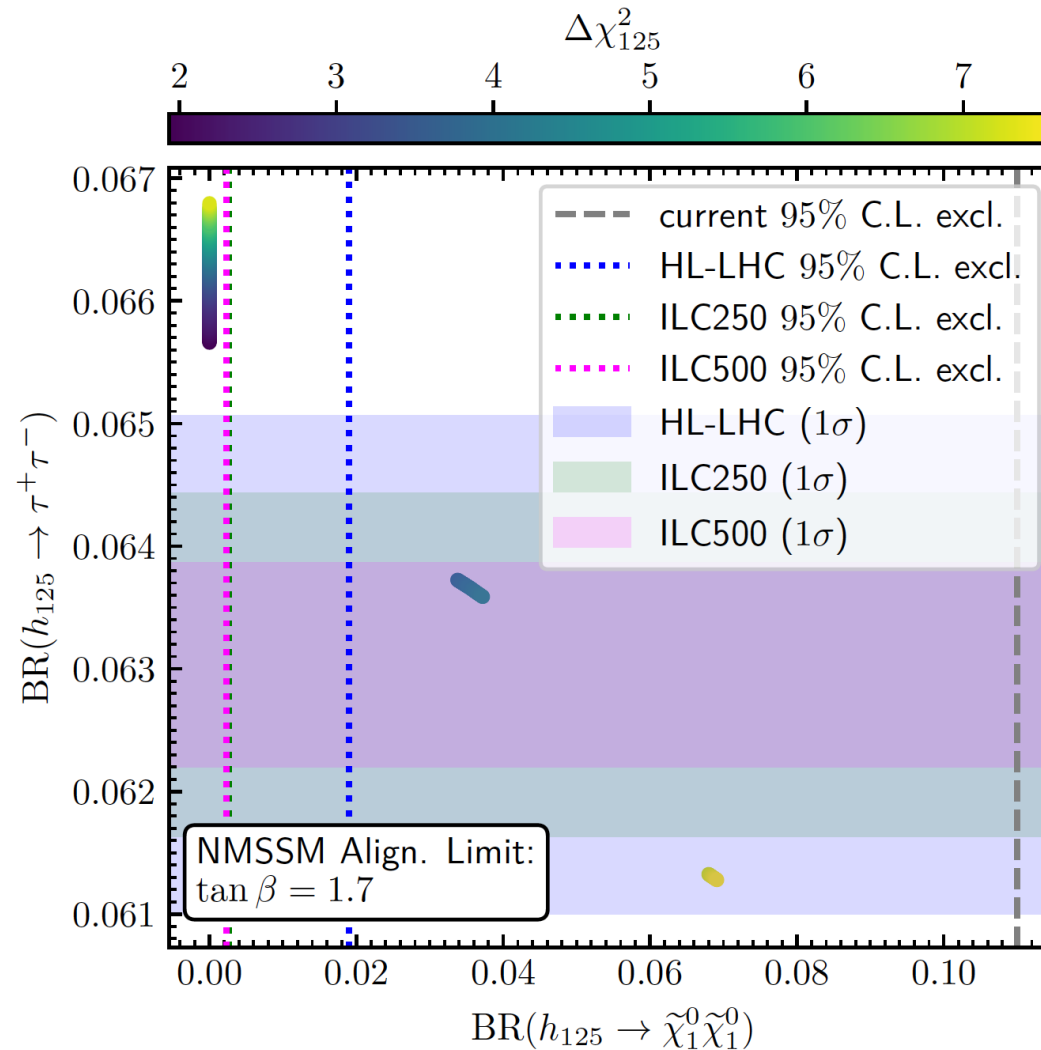


[T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21]

What about the “real hints” at ~ 400 GeV? → NMSSM:

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[*T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21*]

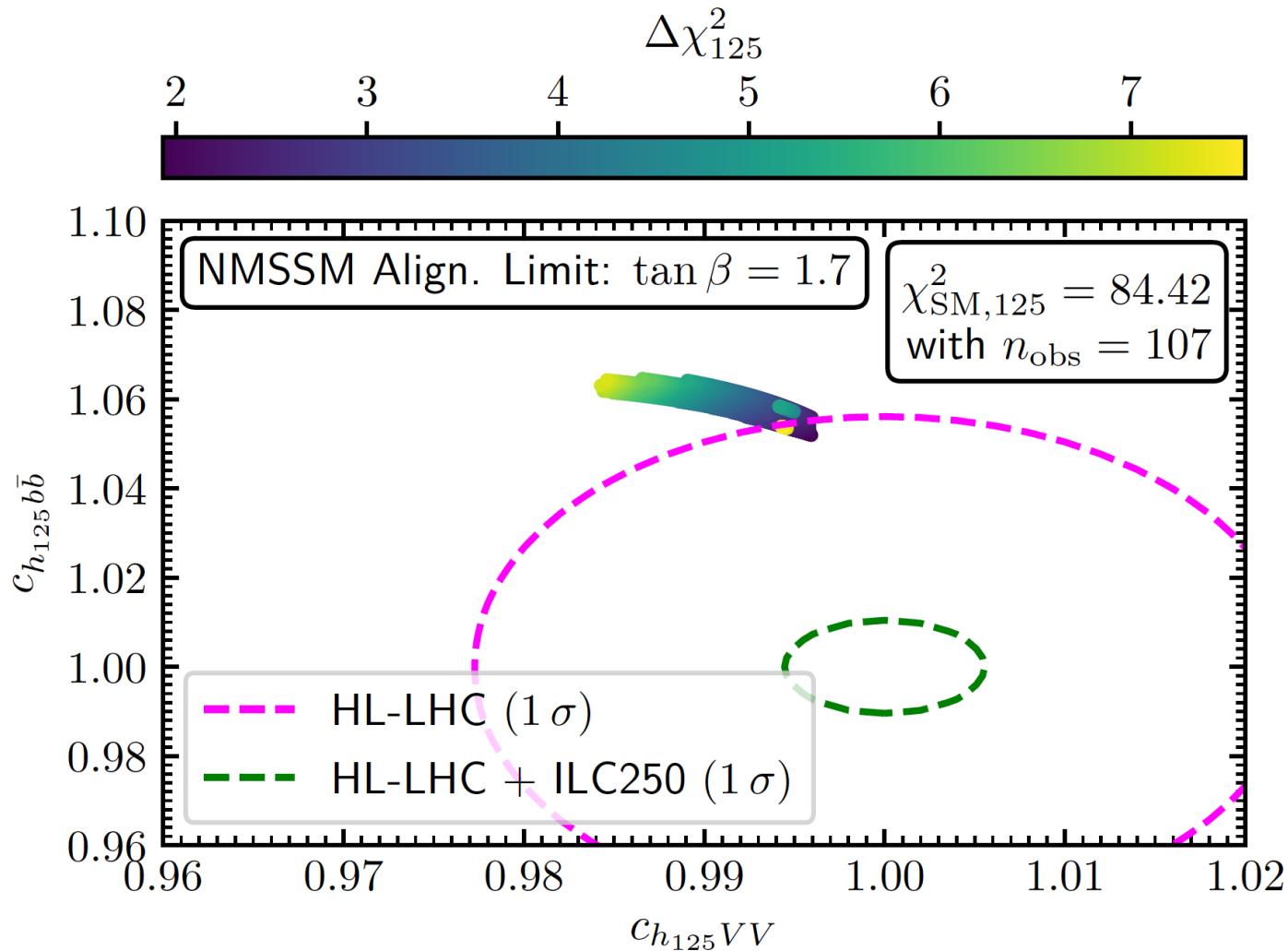


\Rightarrow HL-LHC can test $h_{125} \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0$ (small part of allowed parameter space)

\Rightarrow ILC can test all points via $h_{125} \rightarrow \tau^+ \tau^-$ (and via $h_{125} \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0$)

What about the “real hints” at ~ 400 GeV? \rightarrow NMSSM:

[*T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21*]



\Rightarrow HL-LHC cannot resolve the h_{125} coupling deviations

\Rightarrow ILC can easily test this scenario via $c_{h_{125}VV}$ and $c_{h_{125}bb}$

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Q: Can the models fit the excesses **despite** the additional SUSY constraints on the Higgs sector **???**

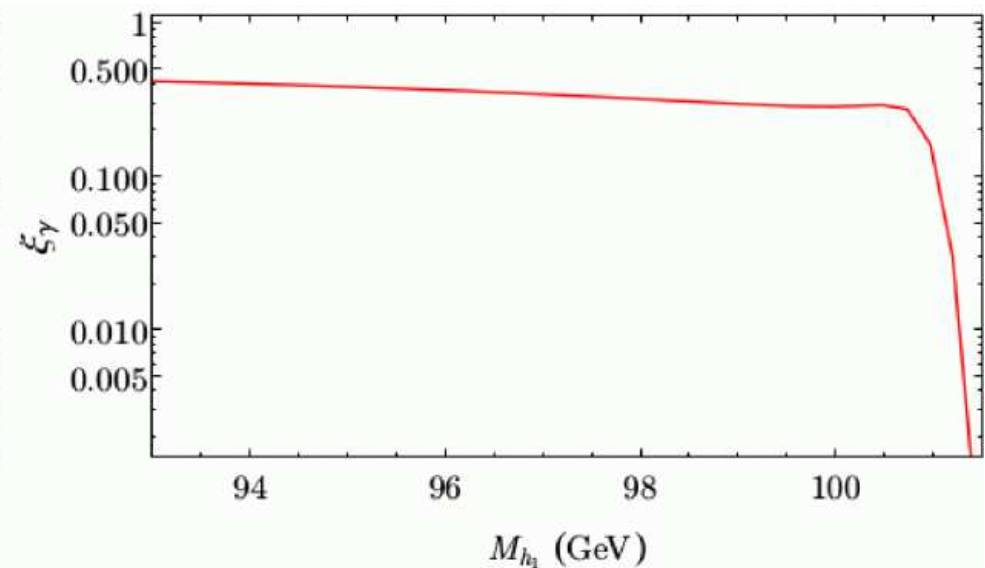
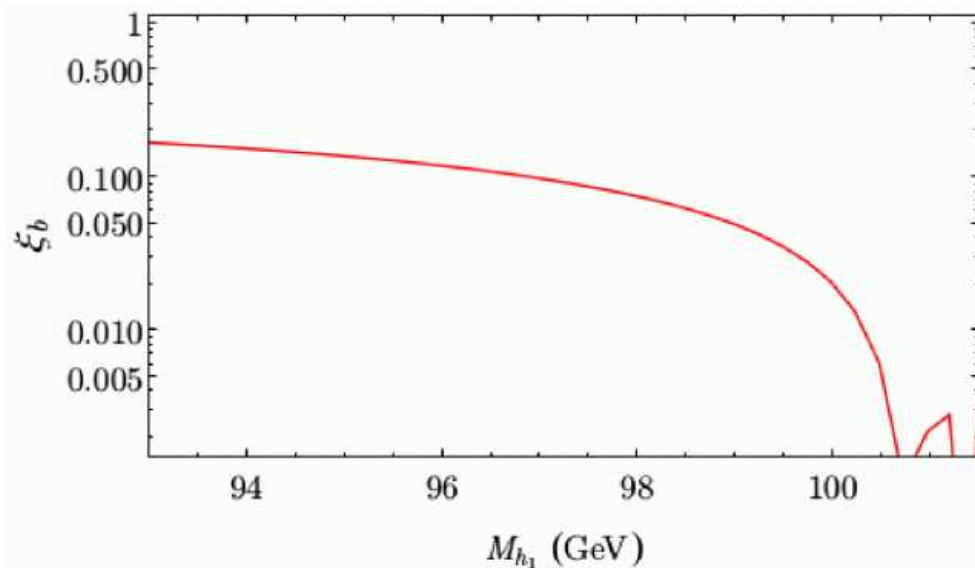
What about the NMSSM?

[F. Domingo, S.H., S. Passehr, G. Weiglein '18]

Parameters:

$\lambda = 0.6$, $\kappa = 0.035$, $\tan\beta = 2$, $\mu_{\text{eff}} = (397 + 15x)$ GeV, $M_{H^\pm} = 1$ TeV,
 $A_\kappa = -325$ GeV, $M_{\text{SUSY}} = 1$ TeV, $A_t = A_b = 0$

$$\xi_b \equiv \frac{\Gamma[h_1 \rightarrow ZZ] \cdot \text{BR}[h_1 \rightarrow b\bar{b}]}{\Gamma[H_{\text{SM}}(M_{h_1}) \rightarrow ZZ] \cdot \text{BR}[H_{\text{SM}}(M_{h_1}) \rightarrow b\bar{b}]} \sim \frac{\sigma[e^+e^- \rightarrow Z(h_1 \rightarrow b\bar{b})]}{\sigma[e^+e^- \rightarrow Z(H_{\text{SM}}(M_{h_1}) \rightarrow b\bar{b})]}$$
$$\xi_\gamma \equiv \frac{\Gamma[h_1 \rightarrow gg] \cdot \text{BR}[h_1 \rightarrow \gamma\gamma]}{\Gamma[H_{\text{SM}}(M_{h_1}) \rightarrow gg] \cdot \text{BR}[H_{\text{SM}}(M_{h_1}) \rightarrow \gamma\gamma]} \sim \frac{\sigma[gg \rightarrow h_1 \rightarrow \gamma\gamma]}{\sigma[gg \rightarrow H_{\text{SM}}(M_{h_1}) \rightarrow \gamma\gamma]}.$$



⇒ both excesses can be fitted simultaneously (at $1 - 1.5 \sigma$)!

What about the $\mu\nu$ SSM?

$\mu\nu$ SSM: [D. Lopez-Fogliani, C. Muñoz '06]

$\mu\nu$ SSM: NMSSM + well motivated RPV (in simple terms)
 \Rightarrow EW scale seesaw to reproduce the neutrino data

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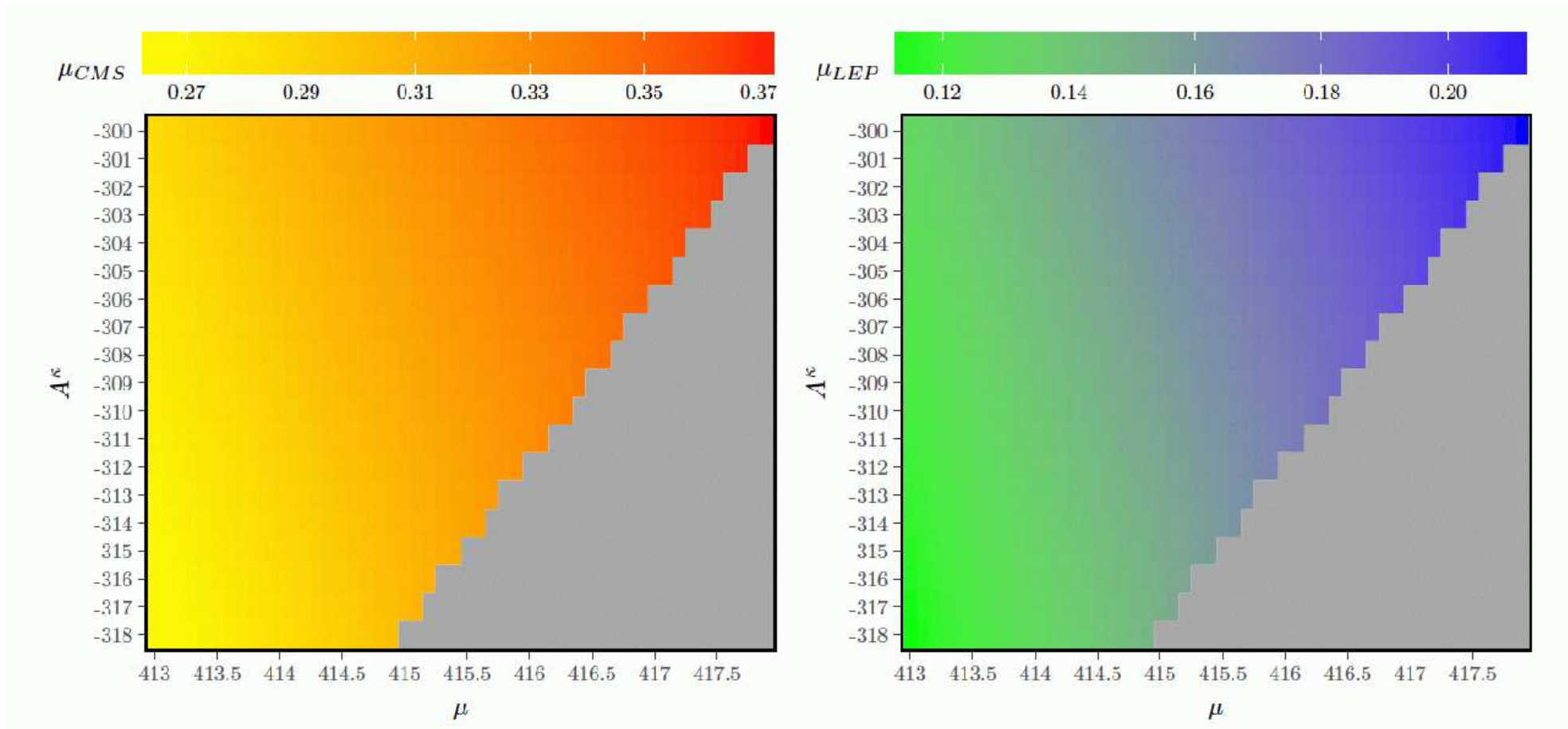
Can the $\mu\nu$ SSM explain the two excesses?

[T. Biekötter, S.H., C. Muñoz '17]

v_{iL}	Y_i^ν	A_i^ν	$\tan\beta$	μ	λ	A^λ	κ	A^κ	M_1
$\sqrt{2} \cdot 10^{-5}$	10^{-7}	-1000	2	[413; 418]	0.6	956.035	0.035	[-300; -318]	100
M_2	M_3	$m_{\tilde{Q}_{iL}}^2$	$m_{\tilde{u}_{iR}}^2$	$m_{\tilde{d}_{iR}}^2$	A_1^u	$A_{2,3}^{u,d}$	$(m_e^2)_{ii}$	A_{33}^e	$A_{11,22}^e$
200	1500	800^2	800^2	800^2	0	0	800^2	0	0

Can the $\mu\nu$ SSM explain the two excesses?

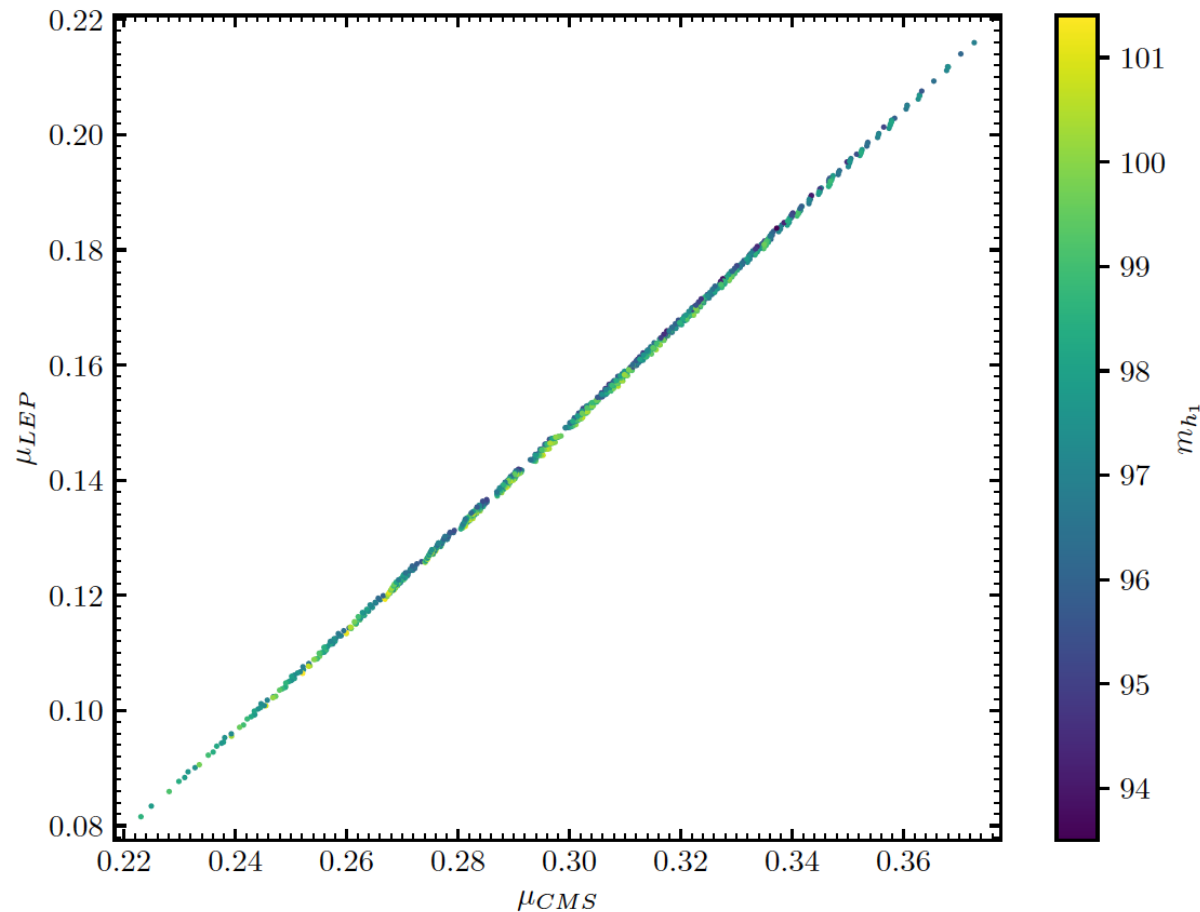
[*T. Biekötter, S.H., C. Muñoz '17*]



⇒ YES, WE CAN! :-)
at the 1 – 1.5 σ level

Why can SUSY explain the excesses only at $1 - 1.5 \sigma$?

[*T. Biekötter, S.H., C. Muñoz '19*]



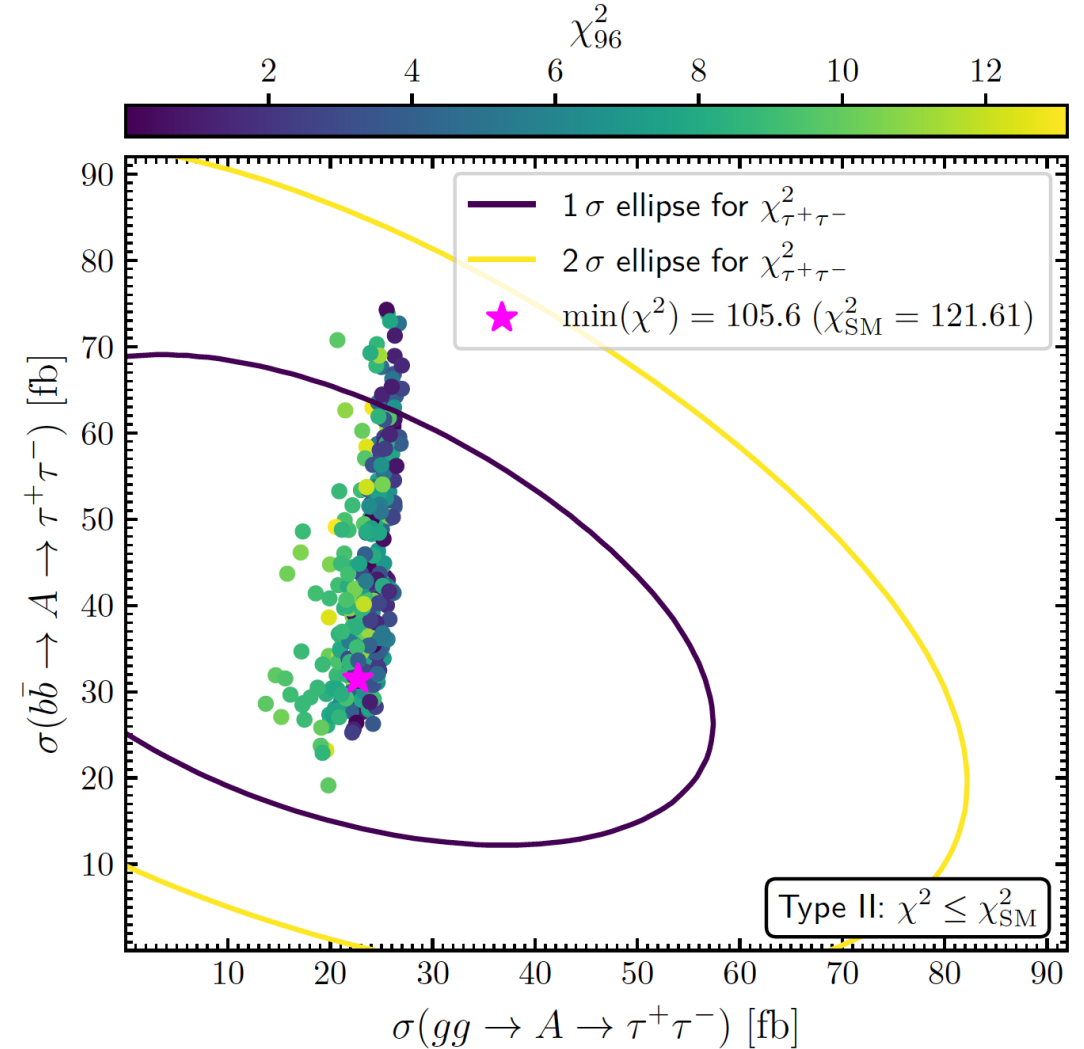
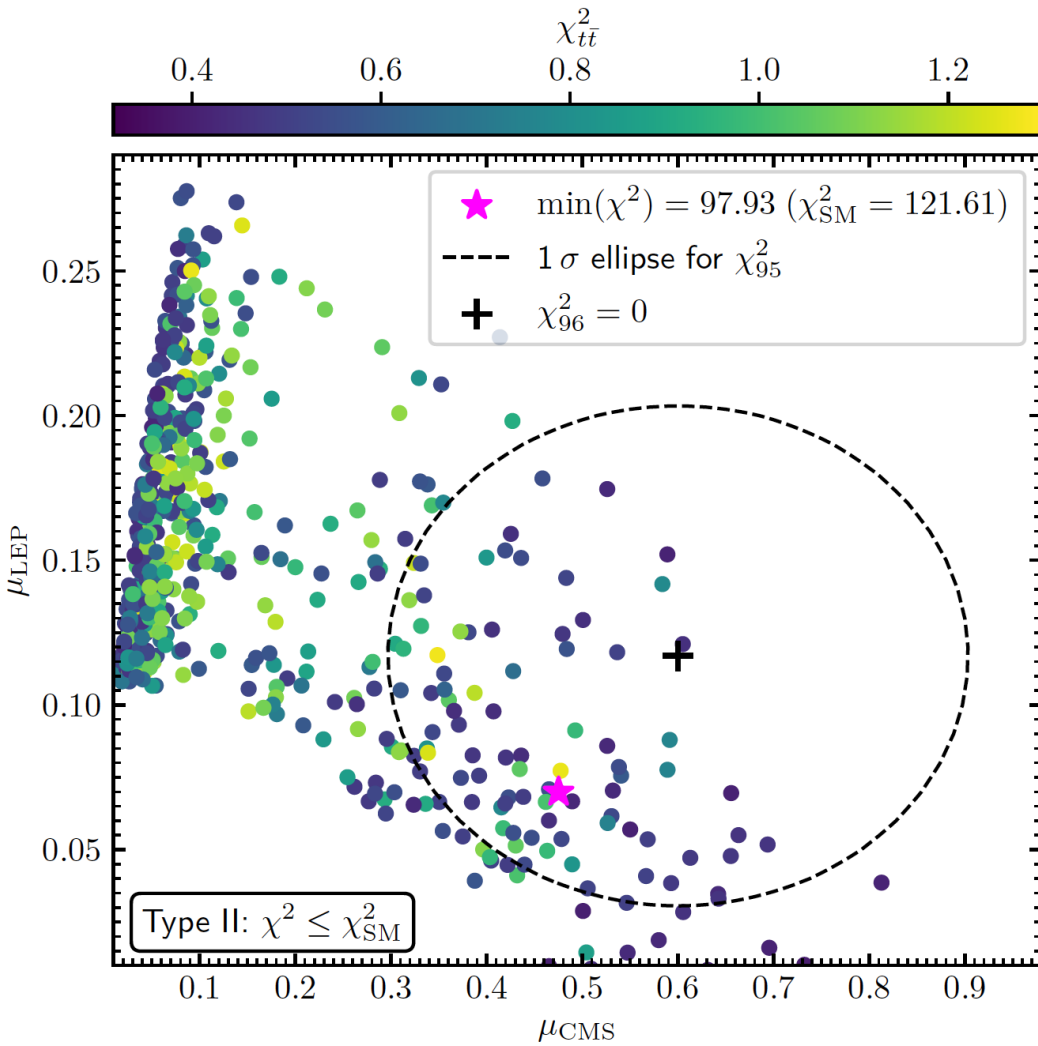
⇒ SUSY enforces strong correlation!

⇒ note: ATLAS limits and CMS “observation”
will likely result in a lower μ_{LHC} !

The final challenge:
can the excesses at 400 GeV and 96 GeV be explained simultaneously?

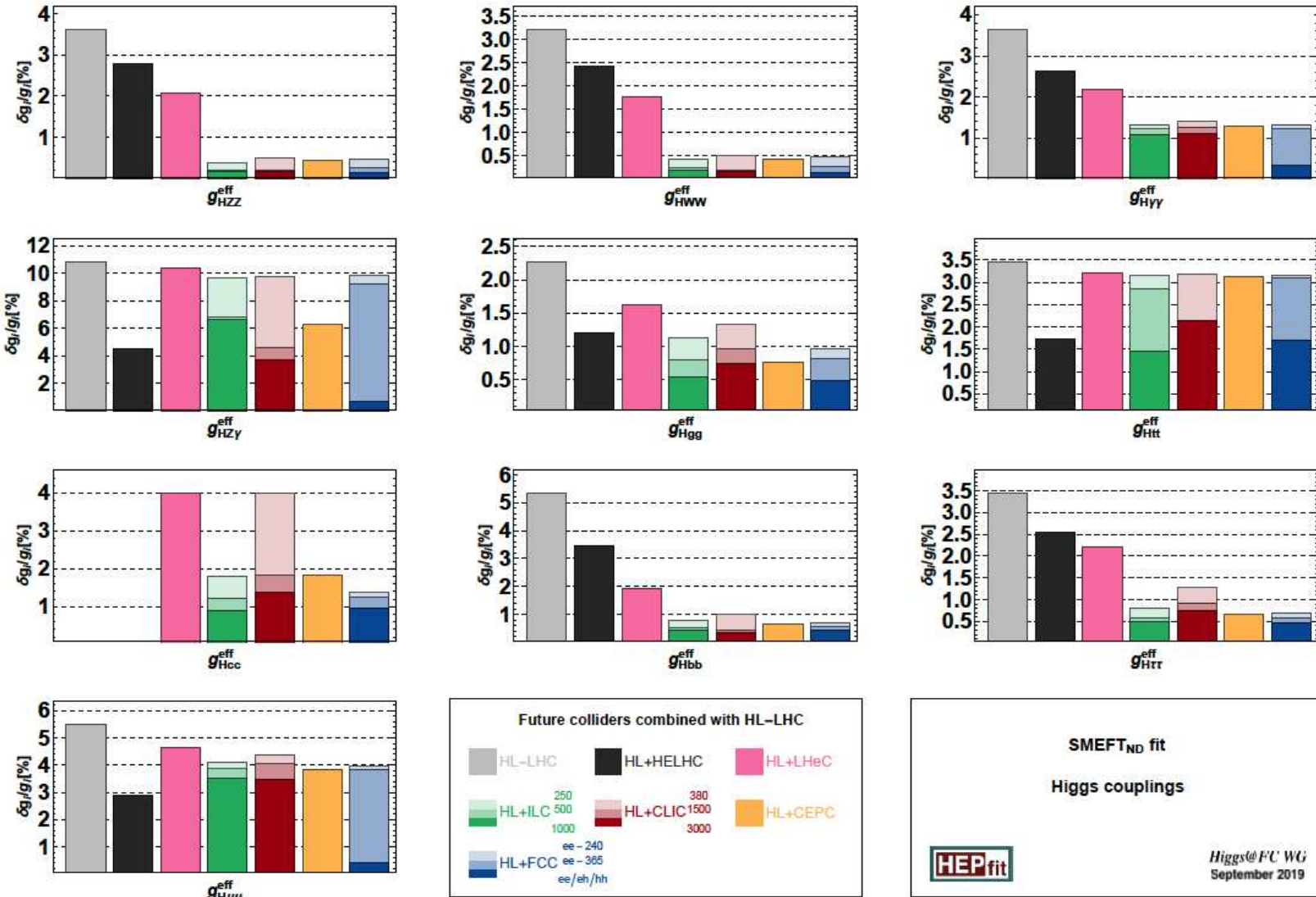
The final challenge: can the excesses at 400 GeV and 96 GeV be explained simultaneously?

⇒ Yes, in the N2HDM



[T. Biekötter, A. Grohsjean, S.H., C. Schwanenberger, G. Weiglein '21]

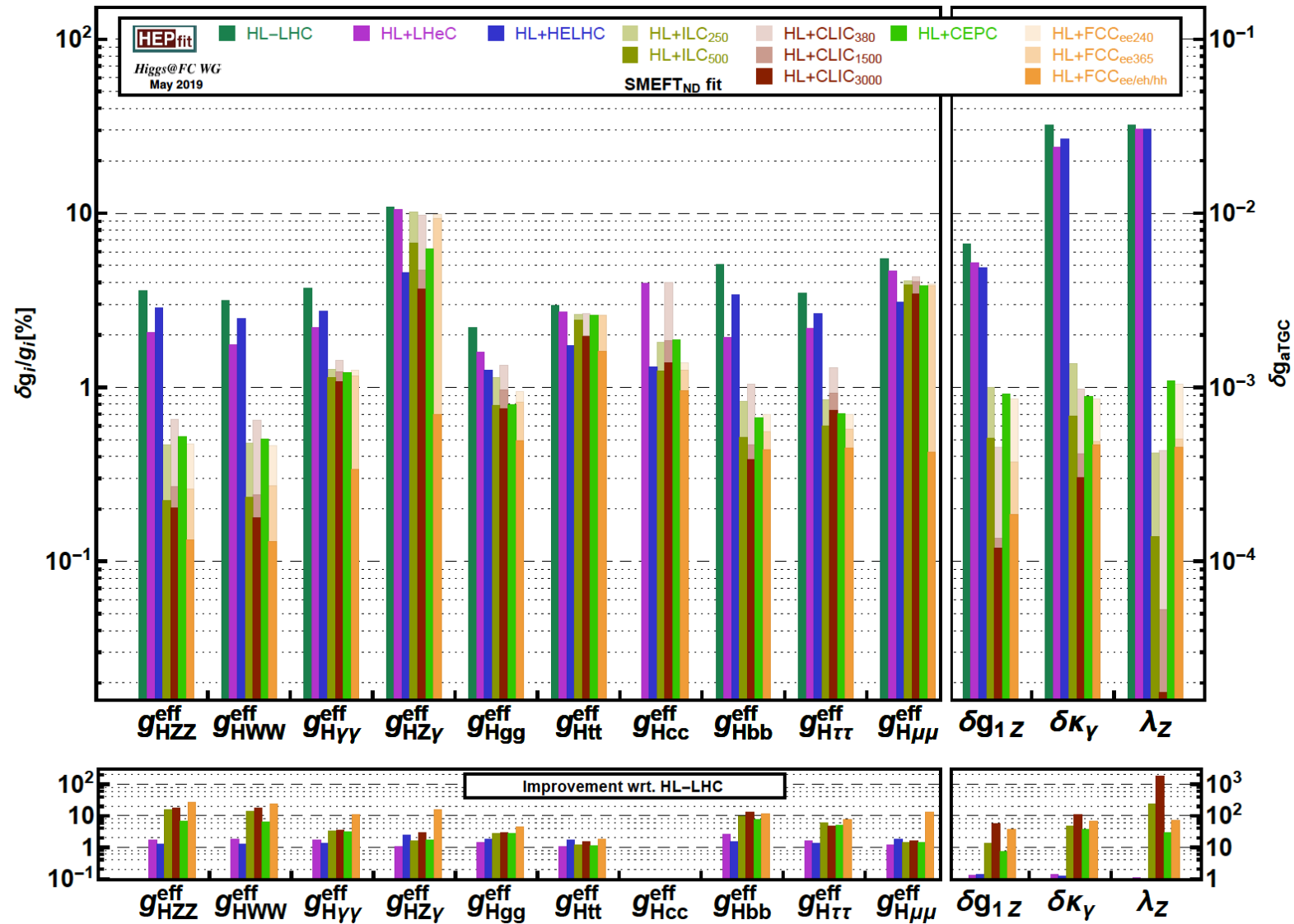
Future expectations for Higgs couplings in SMEFT (I)



⇒ clear improvement with the ILC!

⇒ polarization important to disentangle BSM coupling structures

Future expectations for Higgs couplings in SMEFT (II)

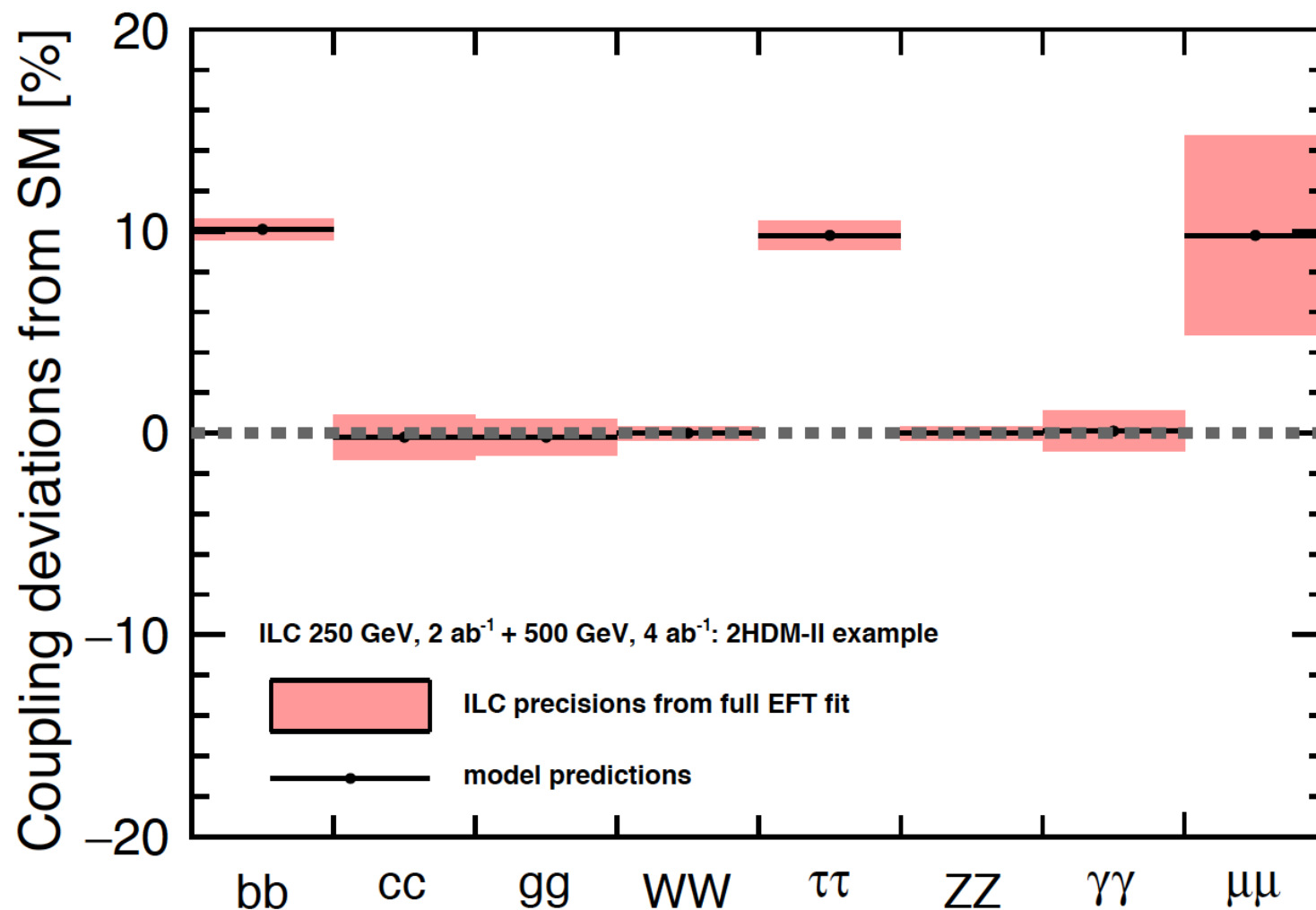


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Wäscheleine I: e^+e^- precision vs. 2HDM type II prediction:

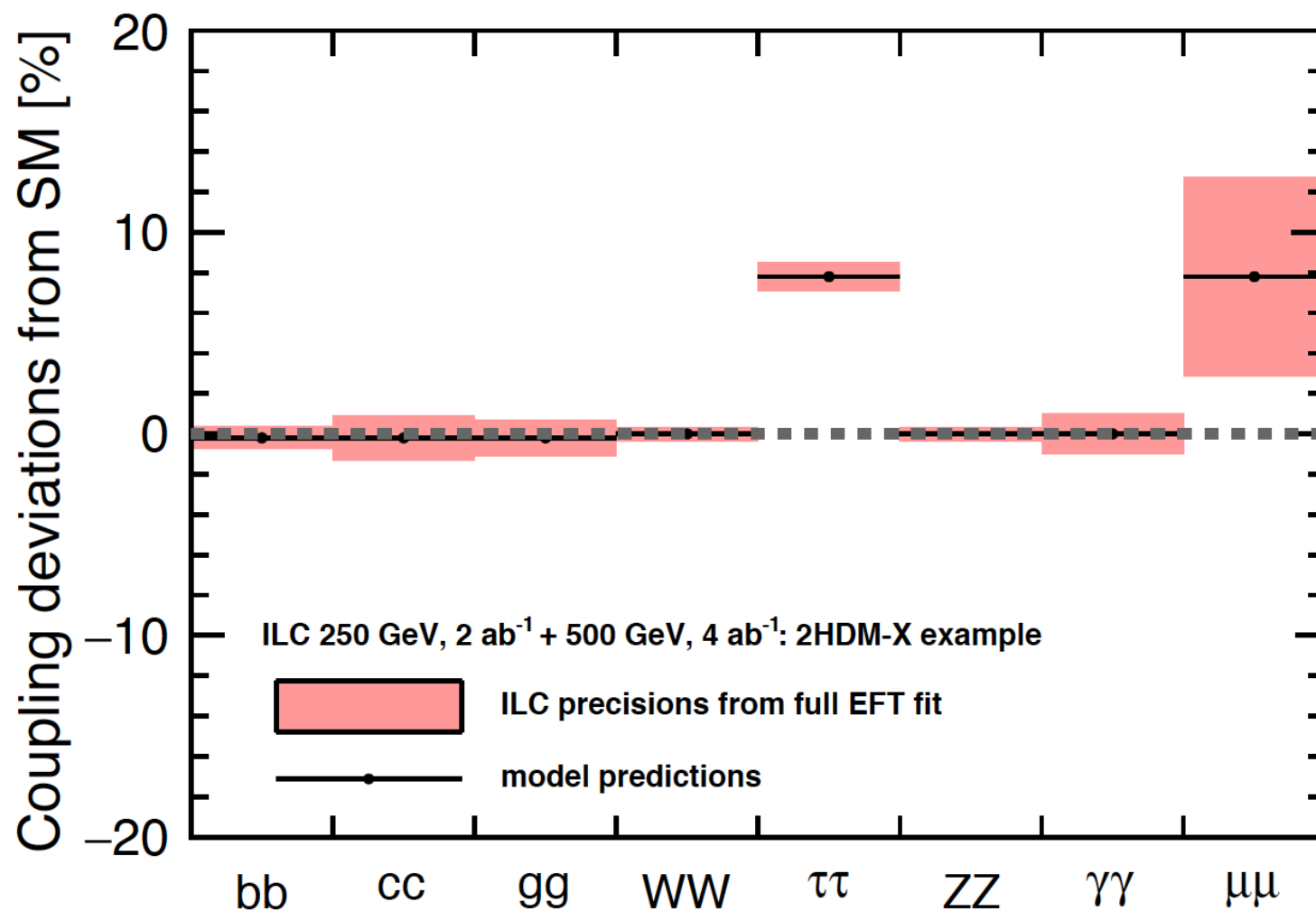
[*T. Barklow et al., '17*]



⇒ clear pattern, distinctive for 2HDM type II?!

Wäscheleine II: e^+e^- precision vs. 2HDM type X prediction:

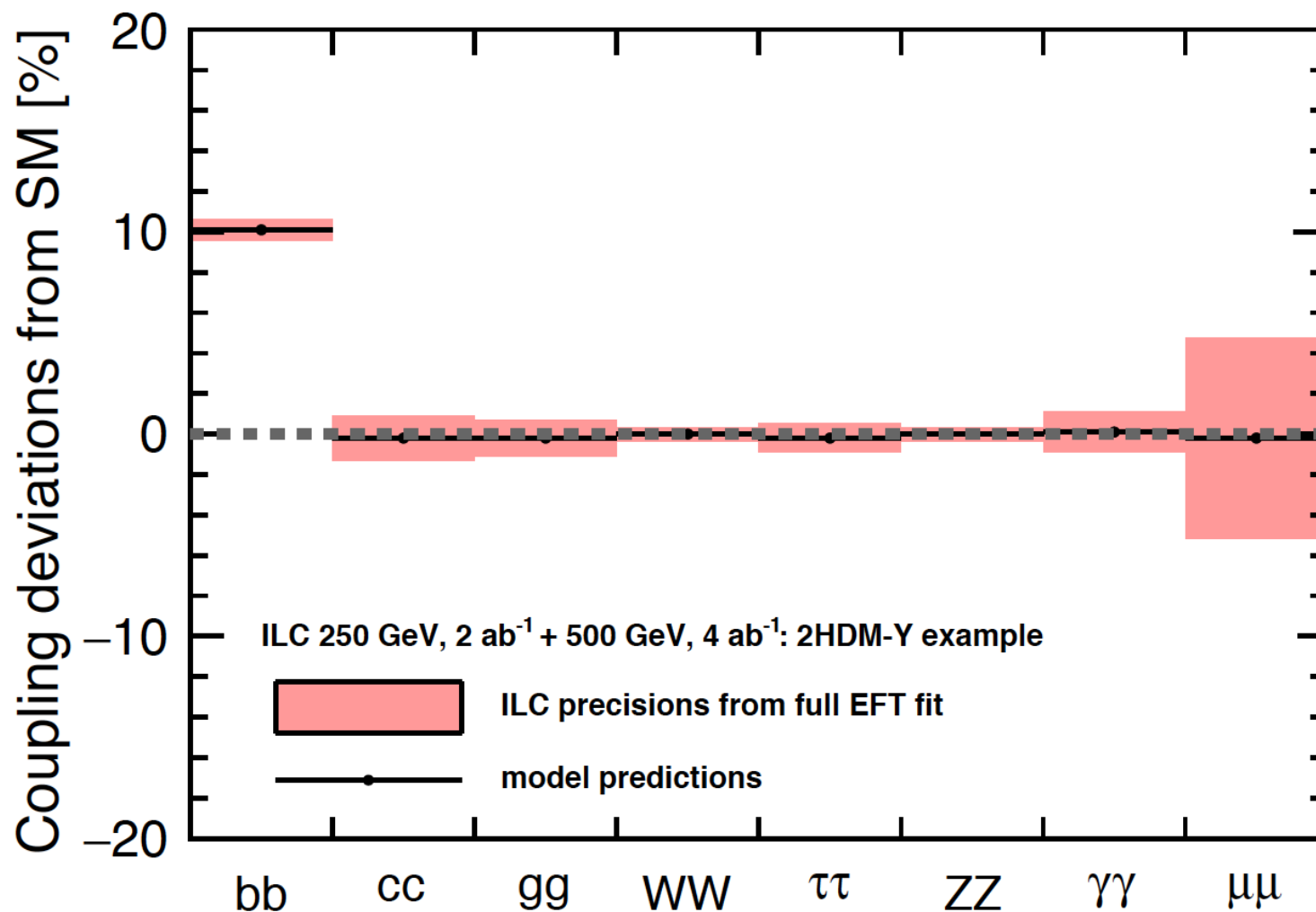
[*T. Barklow et al., '17*]



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Wäscheleine III: e^+e^- precision vs. 2HDM type Y prediction:

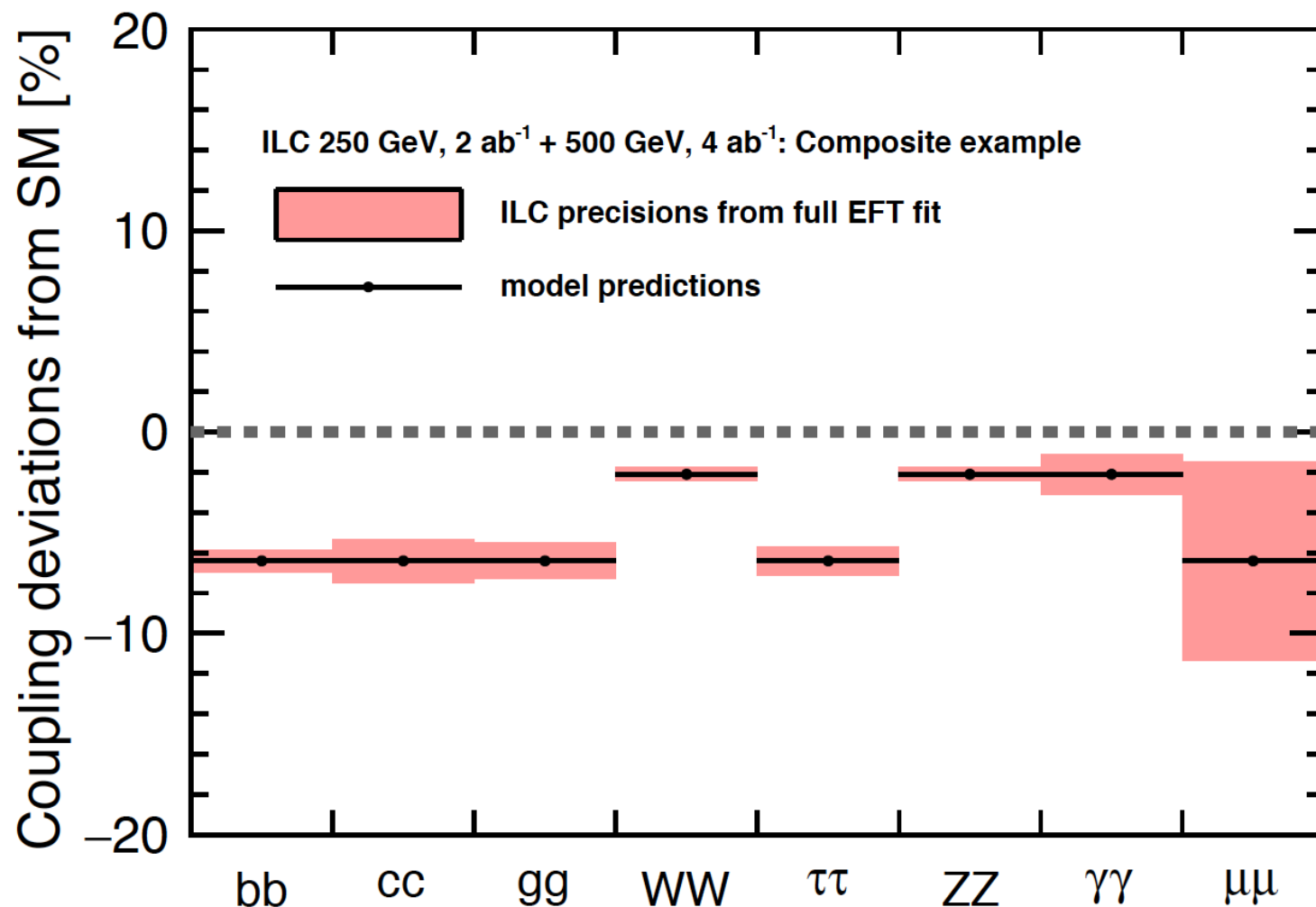
[*T. Barklow et al., '17*]



⇒ clear pattern, distinctive for 2HDM type Y?!

Wäscheleine IV: e^+e^- precision vs. Composite Higgs prediction:

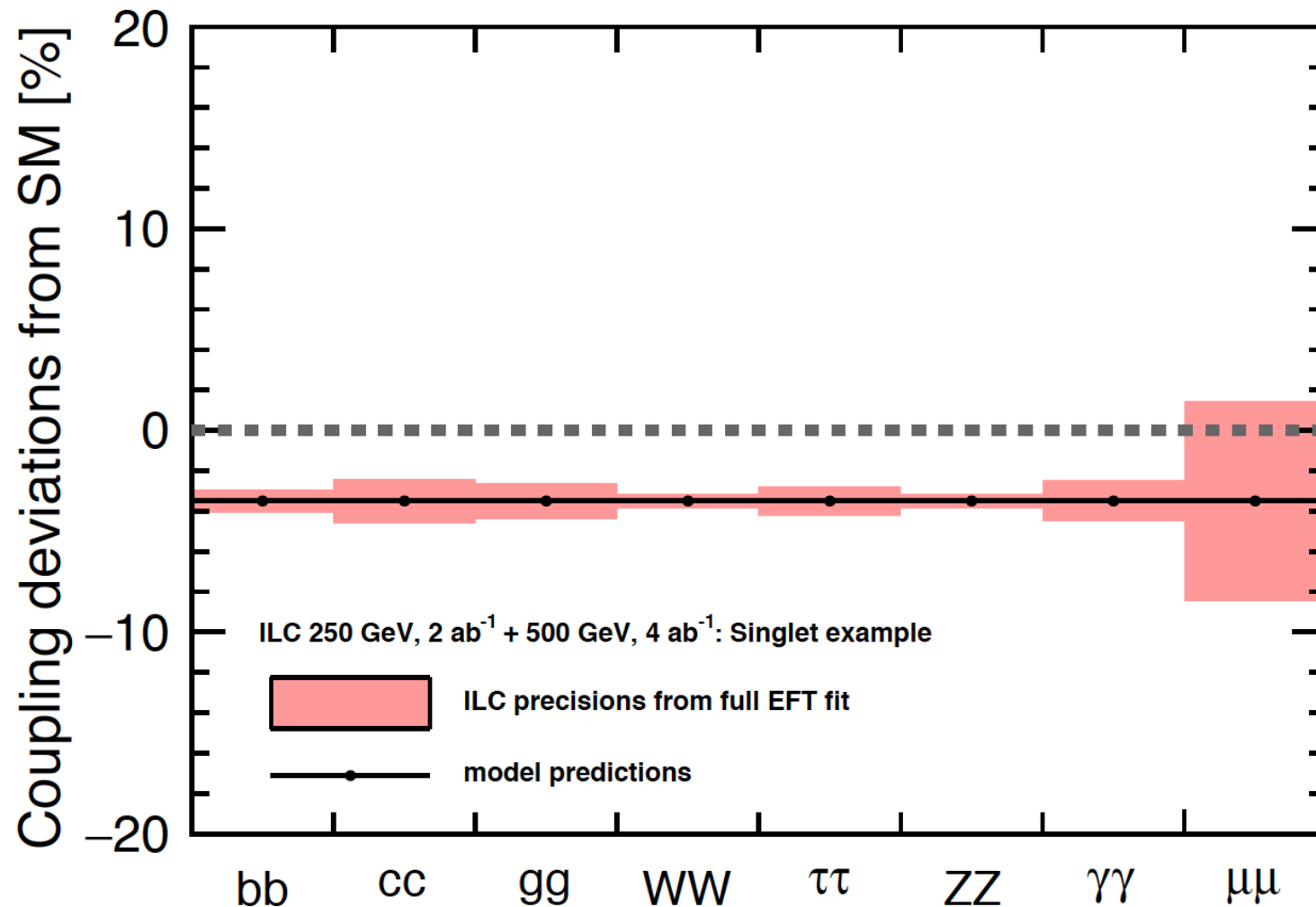
[*T. Barklow et al., '17*]



⇒ clear pattern, distinctive for Composite Higgs?!

Wäscheleine V: e^+e^- precision vs. HxSM prediction:

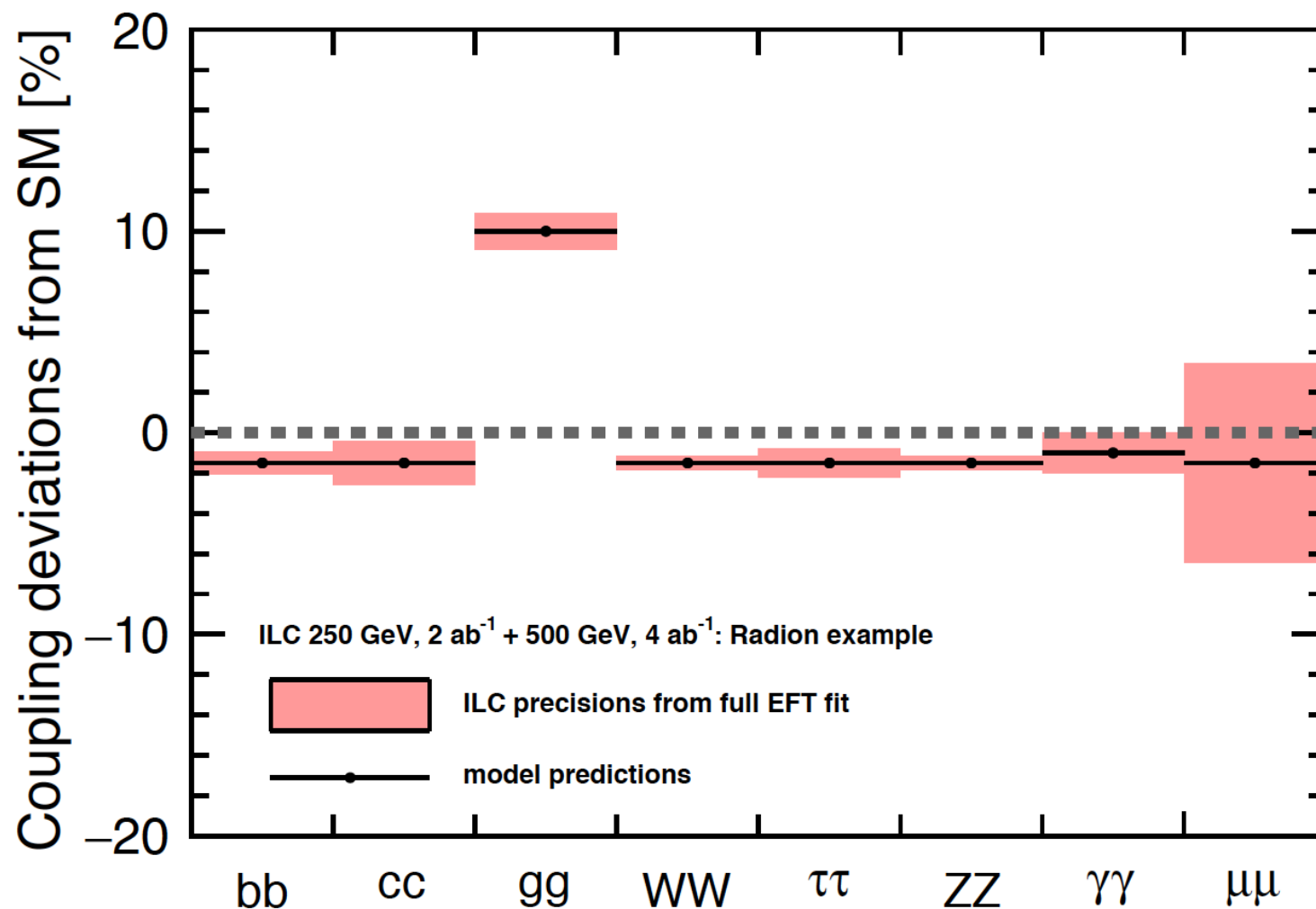
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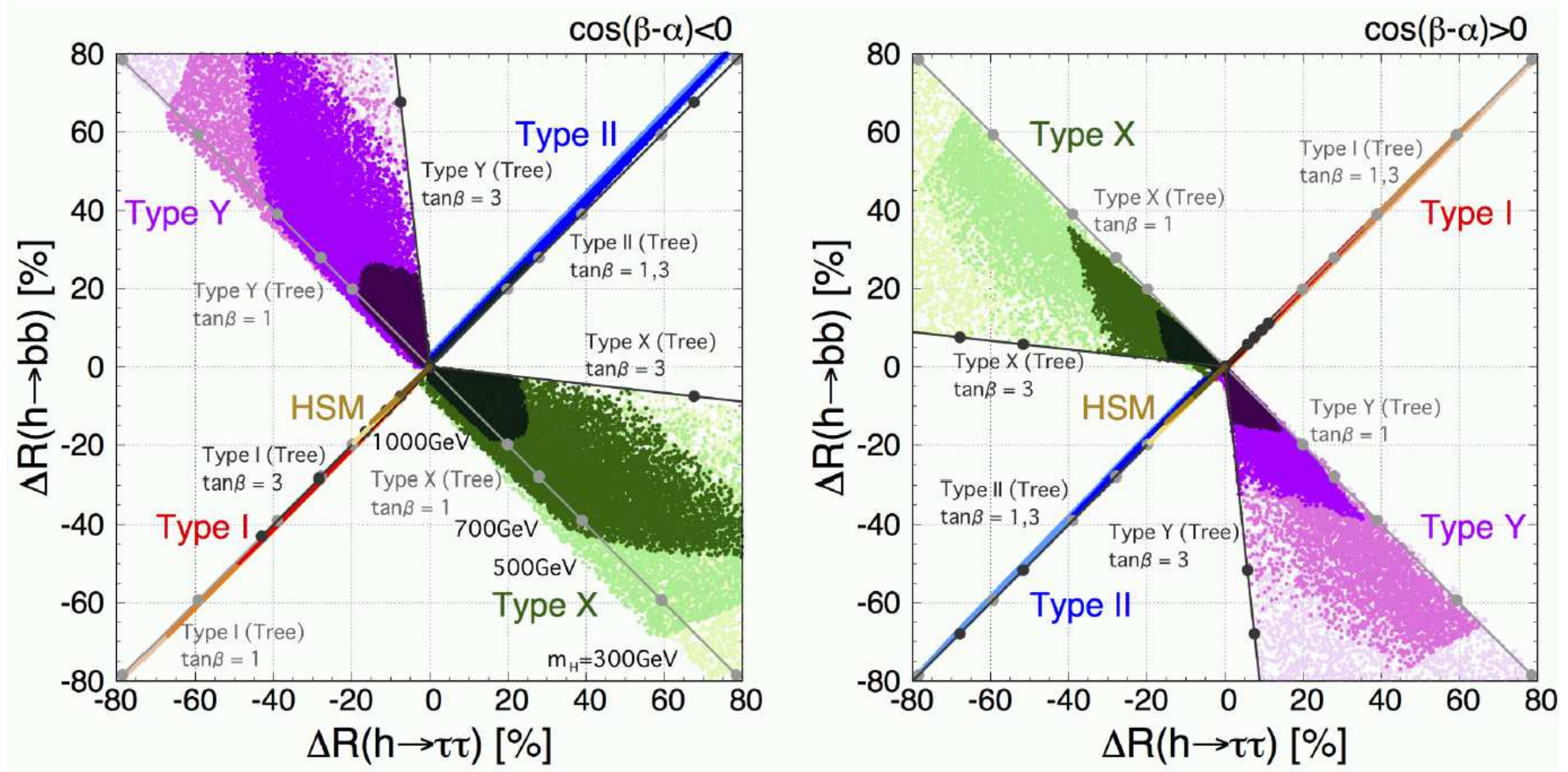
⇒ clear pattern, distinctive for HxSM?!

Wäscheleine VI: e^+e^- precision vs. Higgs-Radion prediction:

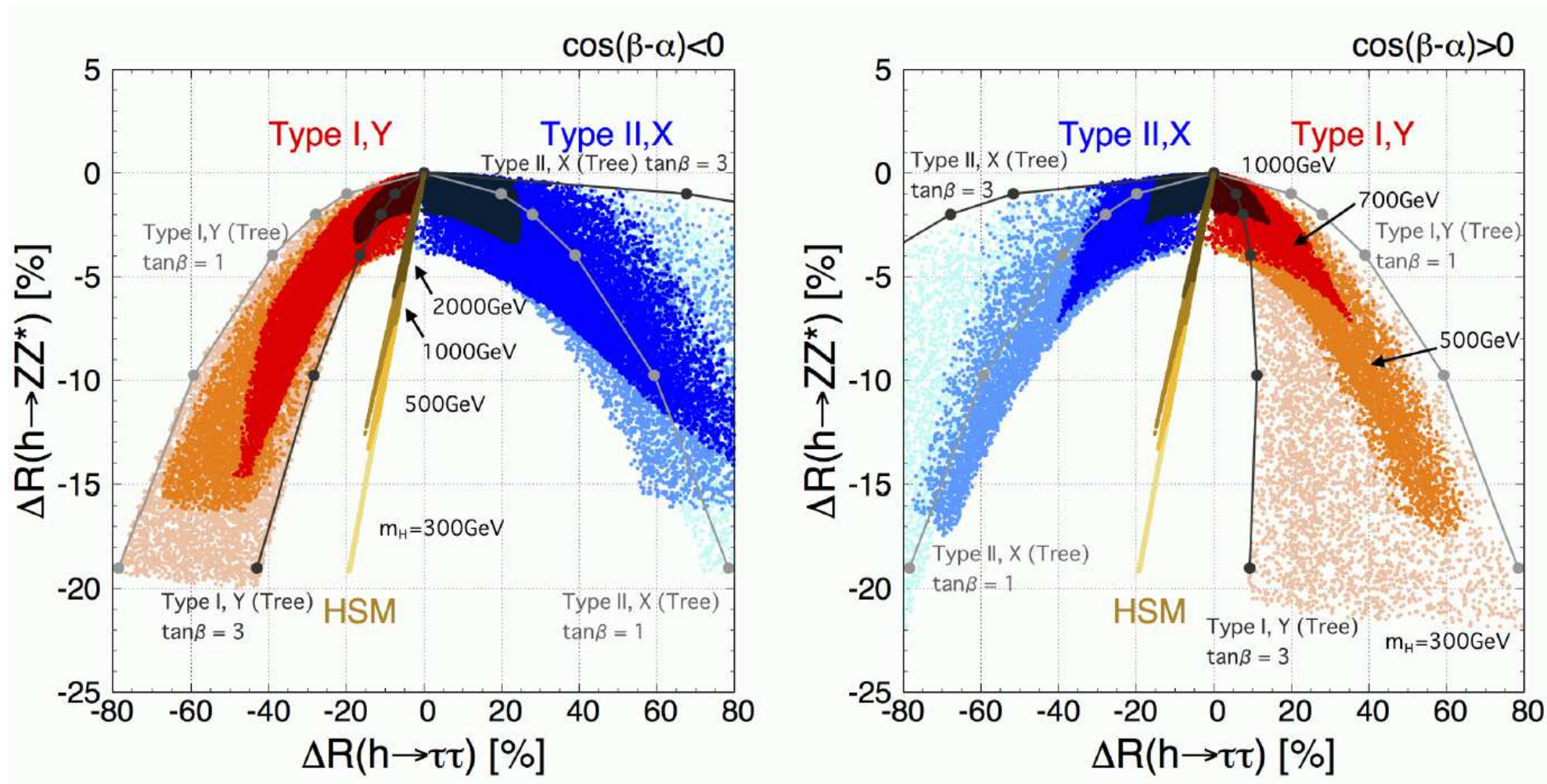
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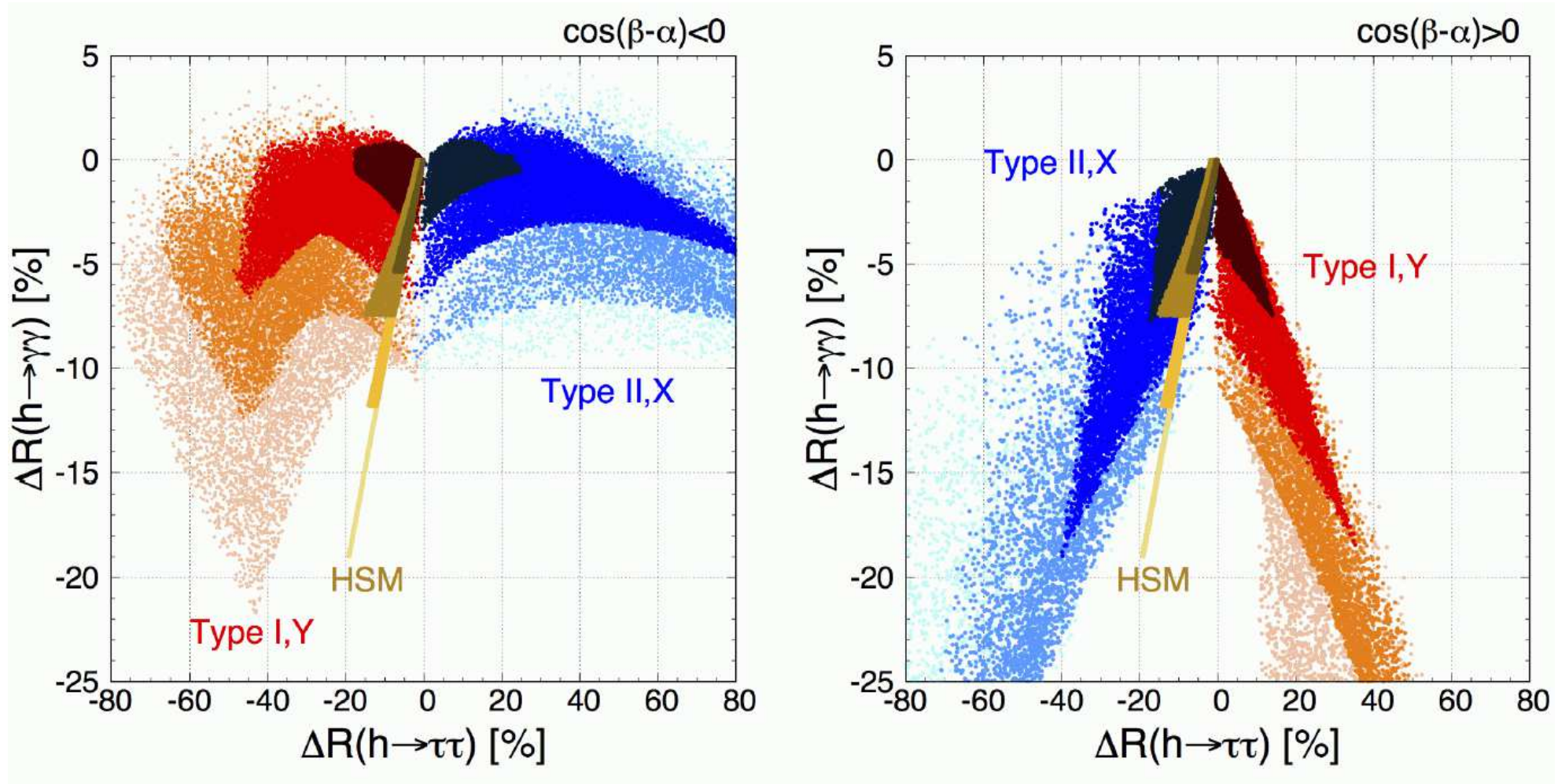
⇒ clear pattern, distinctive for Higgs Radion?!



⇒ LC precision has a great potential to discriminate the models!



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