



Nuclear fragmentation cross section measurement with the FOOT experiment

Riccardo Ridolfi

on behalf of the FOOT collaboration

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Hadrontherapy

Space radioprotection

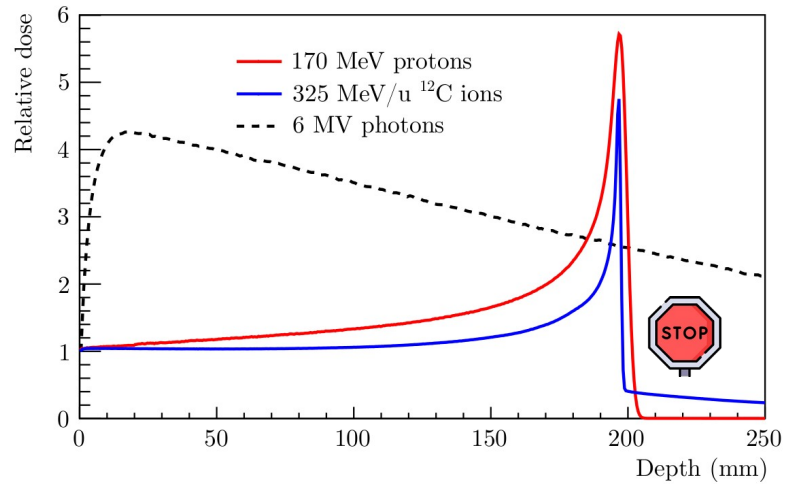
The FOOT experiment

First analysis of GSI2021 data

Hadrontherapy

Nuclear
fragmentation
cross section
measurement
with the FOOT
experiment

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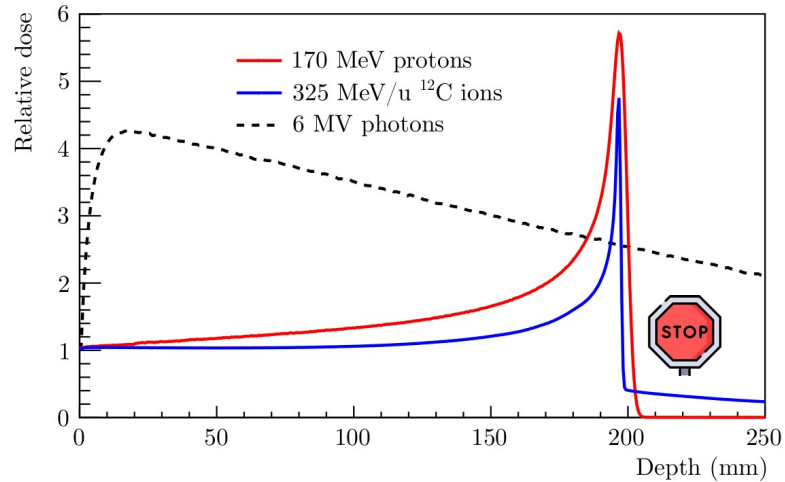


- low dose in the entrance channel
- Bragg peak
- range can be **adjusted** with incident ion energy

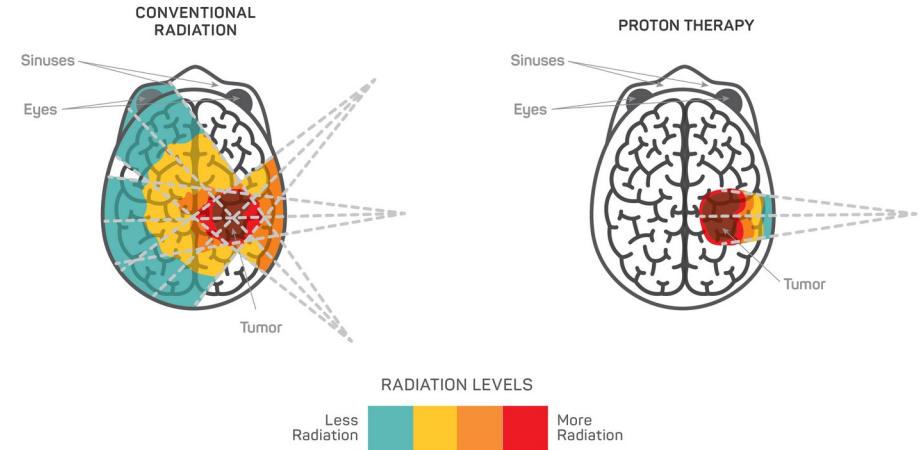
Hadrontherapy

Nuclear
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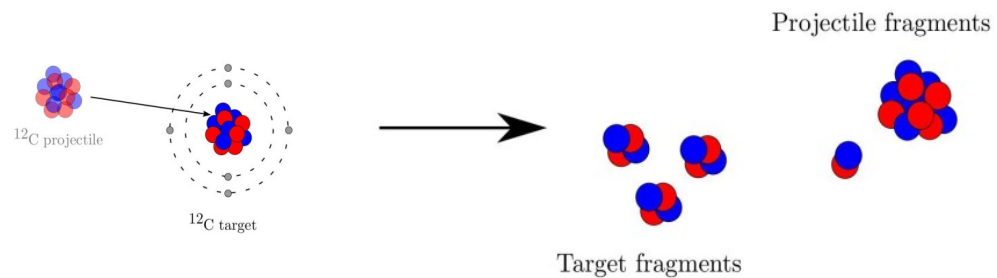
- low dose in the entrance channel
- Bragg peak
- range can be **adjusted** with incident ion energy
- powerful for treatment **near** organs at risk



Nuclear fragmentation

Nuclear
fragmentation
cross section
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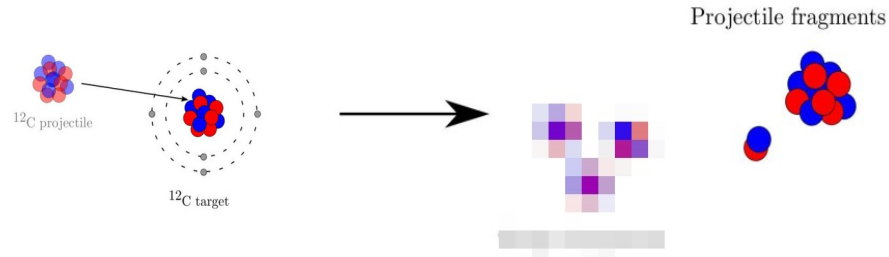
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Nuclear fragmentation

Nuclear
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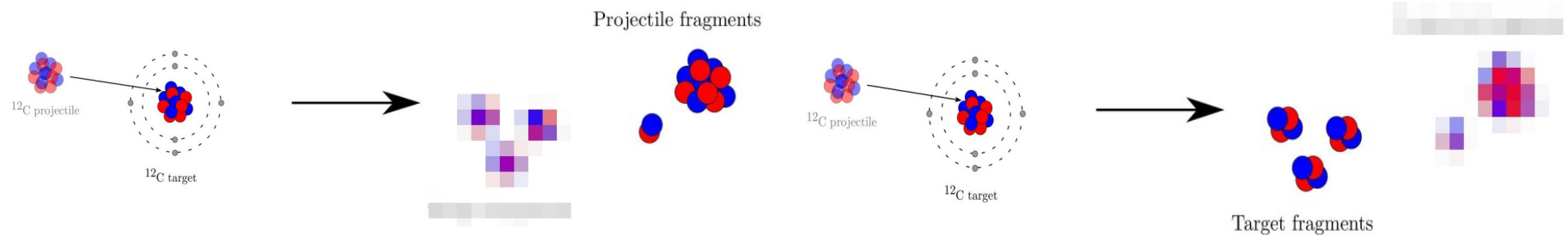


- projectile fragments have a **longer range**
- non-zero dose** beyond the Bragg peak to address
- not present** in protontherapy

Nuclear fragmentation

Nuclear
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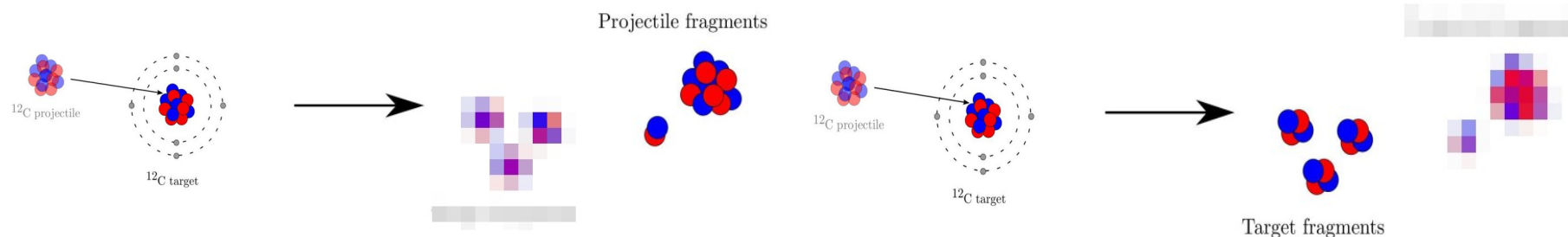
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- target fragments have very **low energies** (short range, hundreds of μm)
- difficult to detect**
- their **damage** can be more important in **healthy tissues**
- biological **effectiveness of protons** still in question

Nuclear fragmentation

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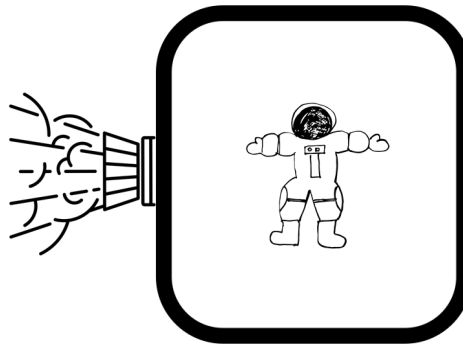
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$$\sigma_R = \int_0^\Omega \int_0^\infty \frac{d^2\sigma}{dE_K d\Omega} dE_K d\Omega$$

Space radioprotection

Nuclear
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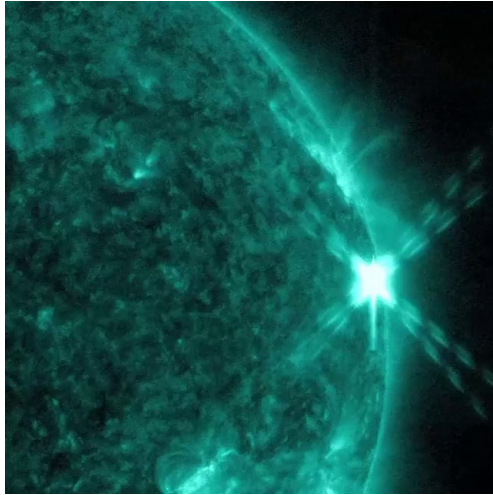
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Space radioprotection

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Solar Particle Events (SPEs)

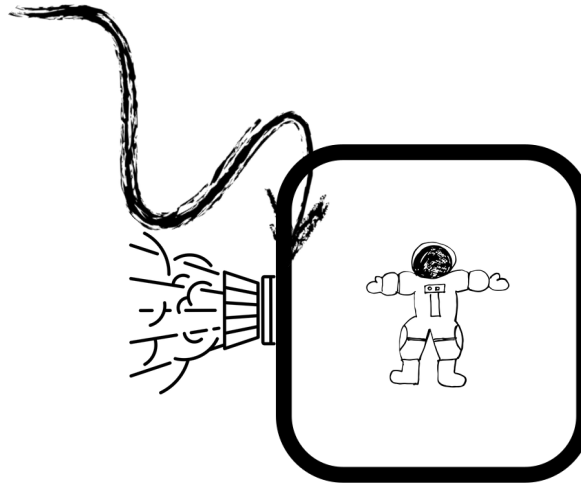
suddenly

92% p

6% He

2% HZE

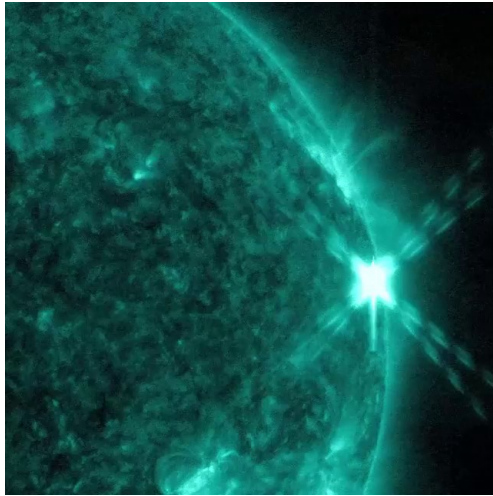
$<1 \text{ GeV/n}$



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$<1 \text{ GeV/n}$

Galactic Cosmic Rays (GCRs)

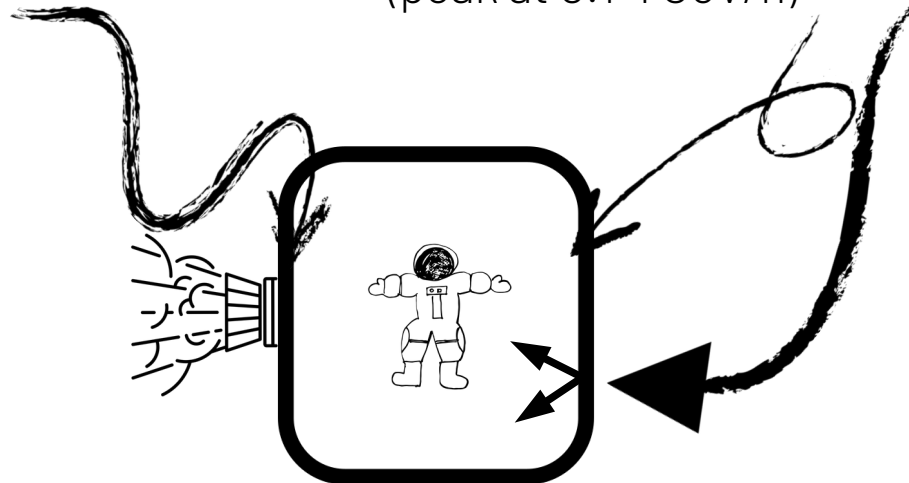
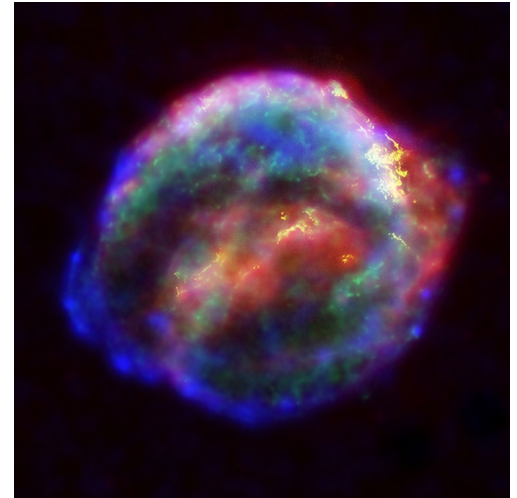
constantly

90% p

9% He

1% HZE

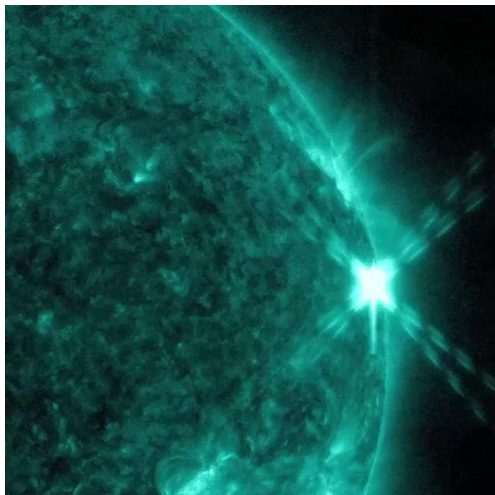
$0.001\text{--}10^{14} \text{ GeV/n}$
(peak at $0.1\text{--}1 \text{ GeV/n}$)



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Solar Particle Events (SPEs)

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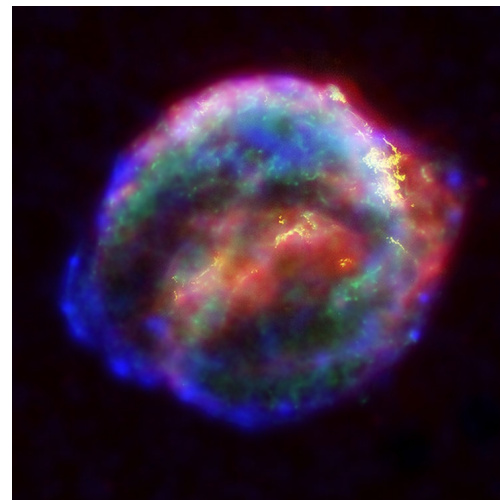
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0.001-10¹⁴ GeV/n
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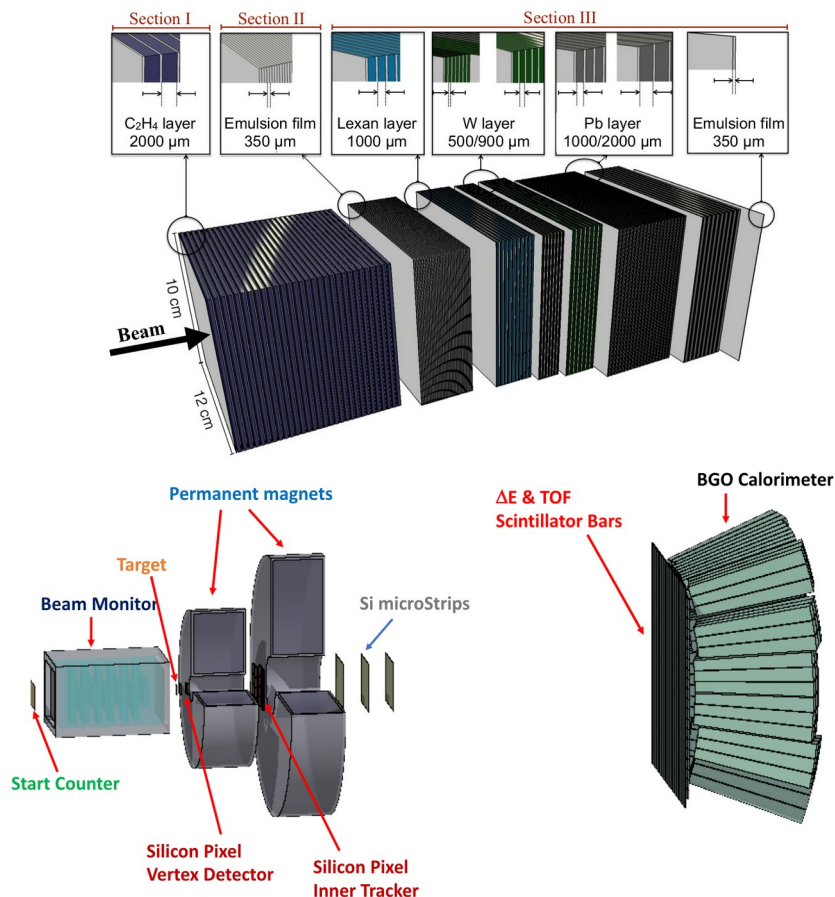


$$\sigma_R = \int_0^\Omega \int_0^\infty \frac{d^2\sigma}{dE_K d\Omega} dE_K d\Omega$$

The FOOT (FragmentatiOn Of Target) experiment

Nuclear
fragmentation
cross section
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measurement of **double differential cross sections** in angle and kinetic energy with a maximum uncertainty of 5%

direct/inverse kinematics and cross section subtraction

isotopic identification by measuring all kinematic quantities

table top setup to be moved according to beam availability

the **core program** can be **extended** thanks to its flexibility

The FOOT experiment: core program

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Physics	Application field	Beam	Target	Upper Energy (MeV/nucleon)	Kinematic approach
Target fragmentation	Hadrontherapy	^{12}C	C, C ₂ H ₄	200	inverse
Target fragmentation		^{16}O	C, C ₂ H ₄	200	inverse
Beam fragmentation	Hadrontherapy	^4He	C, C ₂ H ₄ , PMMA	250	direct
Beam fragmentation		^{12}C	C, C ₂ H ₄ , PMMA	400	direct
Beam fragmentation		^{16}O	C, C ₂ H ₄ , PMMA	500	direct
Beam fragmentation	Space	^4He	C, C ₂ H ₄ , PMMA	800	direct
Beam fragmentation		^{12}C	C, C ₂ H ₄ , PMMA	800	direct
Beam fragmentation		^{16}O	C, C ₂ H ₄ , PMMA	800	direct

The FOOT experiment: core program

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more beam-target settings to explore...



Nuclear
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The diagram illustrates the ATLAS detector structure, showing a 3D perspective view and detailed cross-sections of its various layers. The main 3D view shows a detector with a length of 10 cm and a width of 12 cm, with a beam entering from the left. The detector is composed of several layers, each with a specific function:

- Section I:** C₂H₄ layer (2000 μ m).
- Section II:** Emulsion film (350 μ m).
- Section III:** Lexan layer (1000 μ m).
- W layer:** W layer (500/900 μ m).
- Pb layer:** Pb layer (1000/2000 μ m).
- Emulsion film:** Emulsion film (350 μ m).

The detector is designed for three main purposes, indicated by arrows at the bottom:

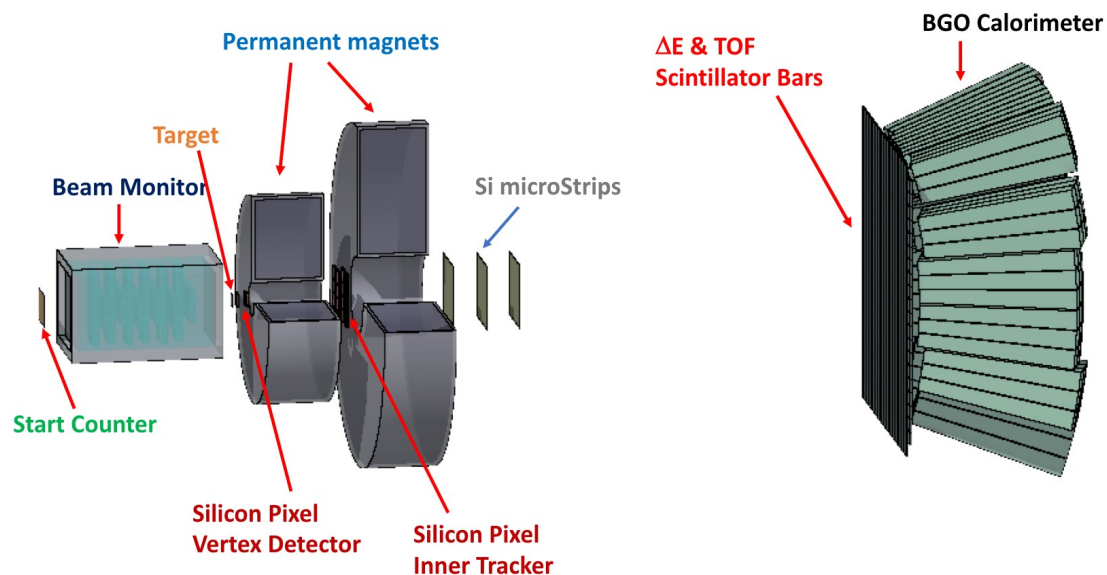
- Vertexing:** Determining the point of particle production.
- Charge identification:** Determining the sign of the particle's electric charge.
- Momentum measurement:** Determining the particle's momentum.

emulsions have to be **developed**
after the irradiation

The FOOT experiment: electronic setup

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large variety of detectors

highly distributed data
acquisition system

designed for **heavier fragments**
($3 \leq Z \leq 8$)

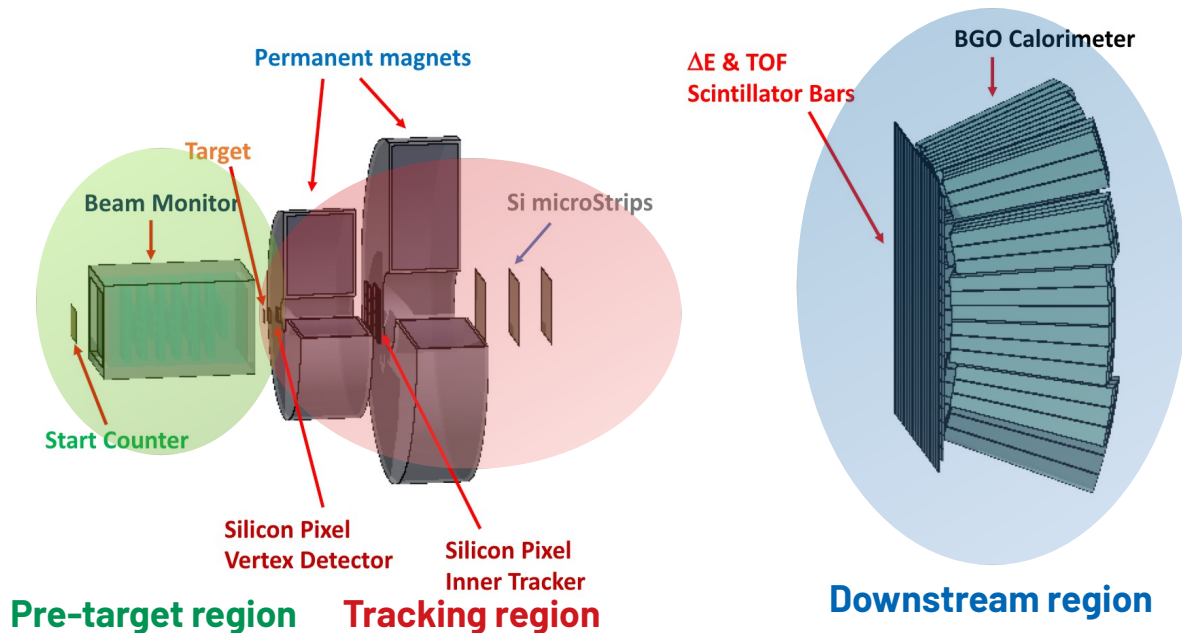
angular acceptance of 10°

to be completed in **2023**

The FOOT experiment: electronic setup

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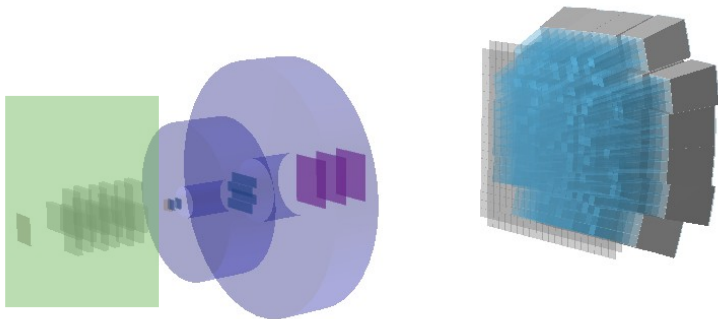
angular acceptance of 10°

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Electronic setup: pre-target region

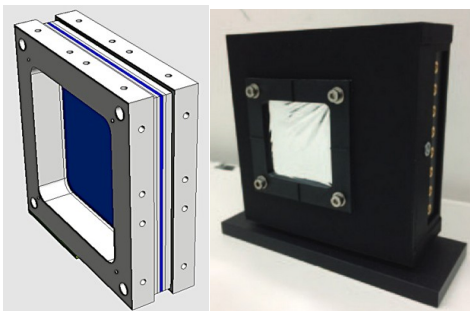
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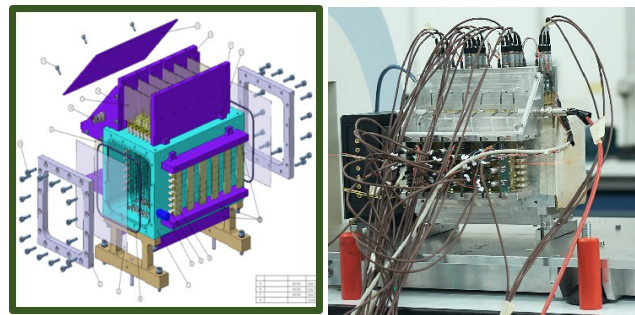
beam
characterization

Start Counter (SC)



Trigger and ToF start
250 μm thick plastic scintillator
5x5 cm^2 active area
48 SiPM \rightarrow 8 channels

Beam Monitor (BM)

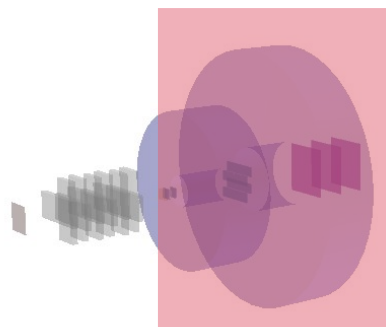


Beam momentum and direction
Rejection of pre-target fragmentation
Drift chamber Ar/CO₂ (80%/20%)
12 layers with 3 cells each (orthogonal
views)

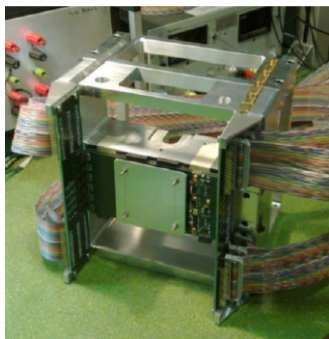
Electronic setup: tracking region

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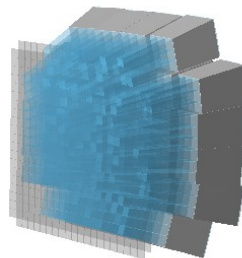
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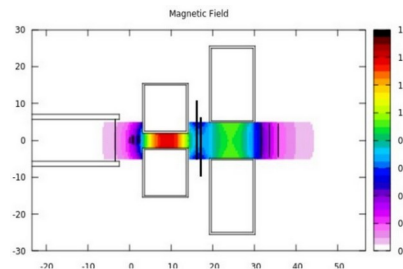
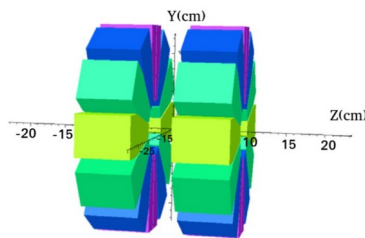
Vertex (VTX) &
Inner Tracker (IT)



Mimosa-28 Si pixel
20 μm pitch
VTX \rightarrow 4 layers IT \rightarrow 2 layers



Magnets

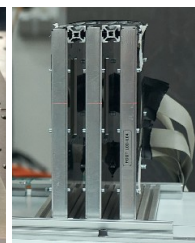
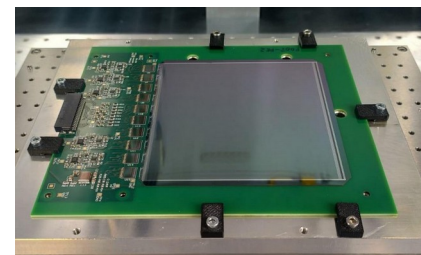


2 permanent magnets Halbach
configuration
B field in y axis up to 1.2 T



fragment tracking
momentum measurement

Microstrip detector
(MSD)

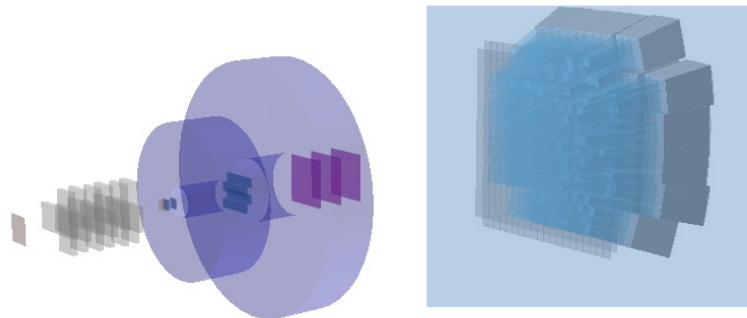


3 pairs of X-Y layers
9 x 9 cm^2 active area
150 μm readout pitch

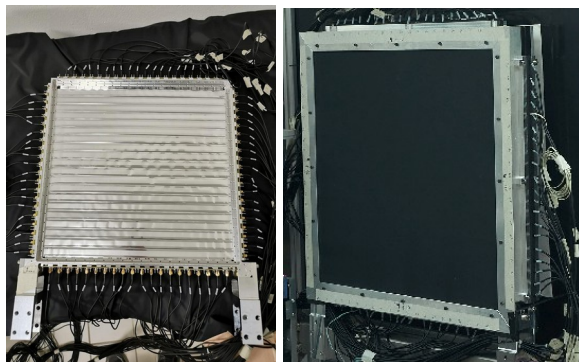
Electronic setup: downstream region

Nuclear
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TOF Wall (TW)



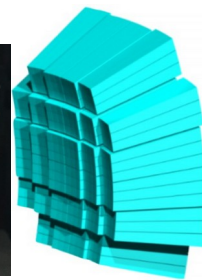
$\Delta E - \text{TOF}$

44 cm x 2 cm x 3 mm plastic scintillator bars
2 layers of 20 bars each
SiPM readout



fragment
identification

Calorimeter (CALO)



Kinetic energy

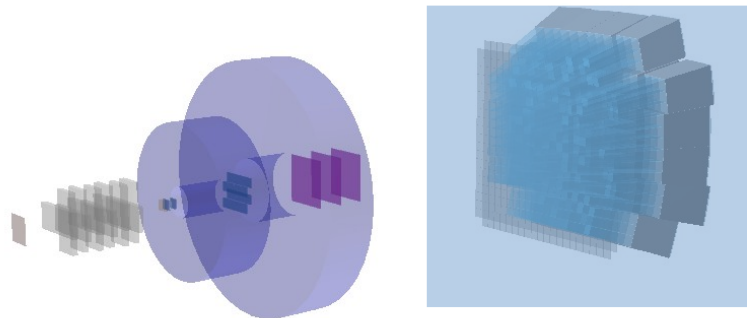
BGO scintillator

320 crystals 2 (3) x 2 (3) x 24 cm³

Electronic setup: downstream region

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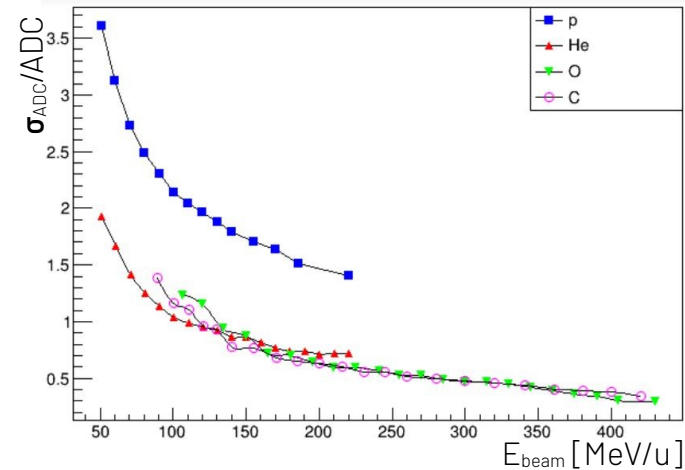
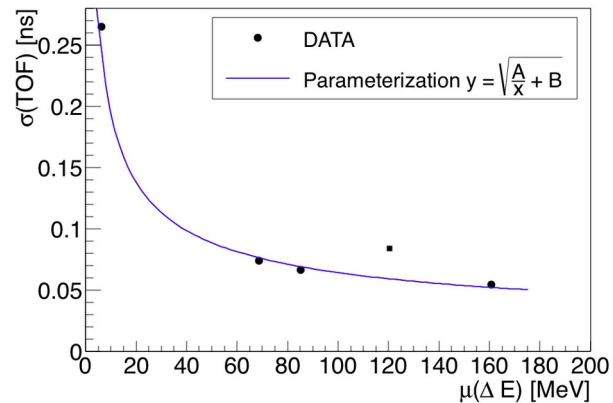


TOF Wall (TW)



fragment
identification

Calorimeter (CALO)



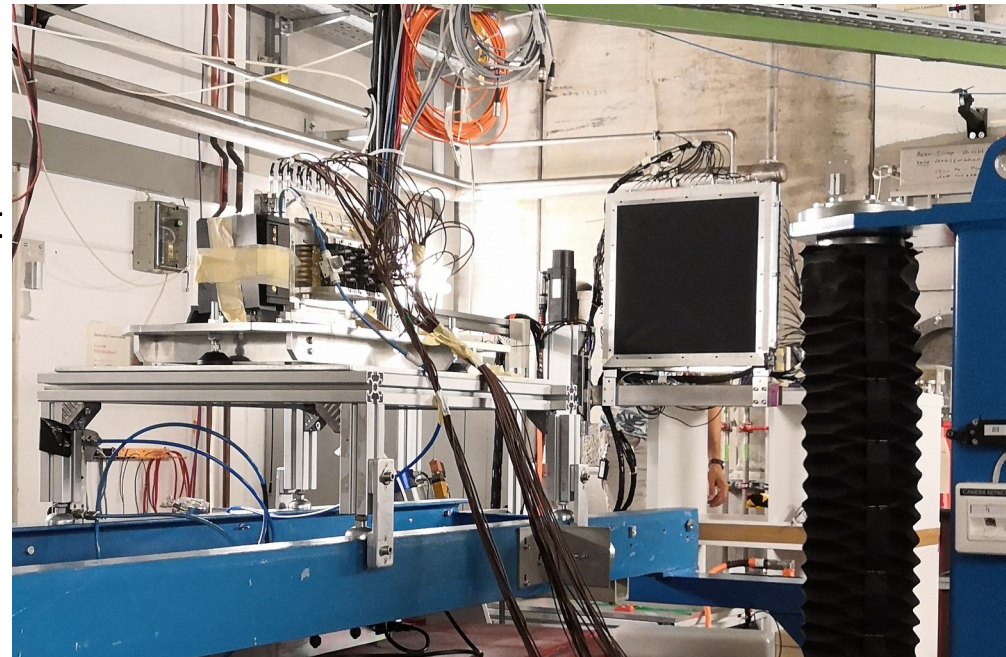
GSI2021 campaign

Nuclear
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400 MeV/u ^{16}O beam on 5mm Carbon target
angular acceptance of 4.85°

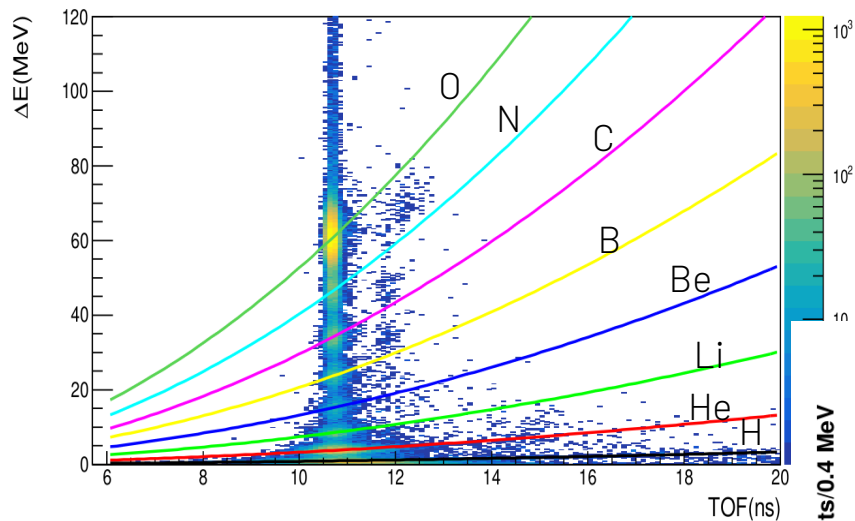
1.3 Mevents Minimum Bias with target
2 Mevents Minimum Bias + frag with target
57 kevents Minimum Bias without target



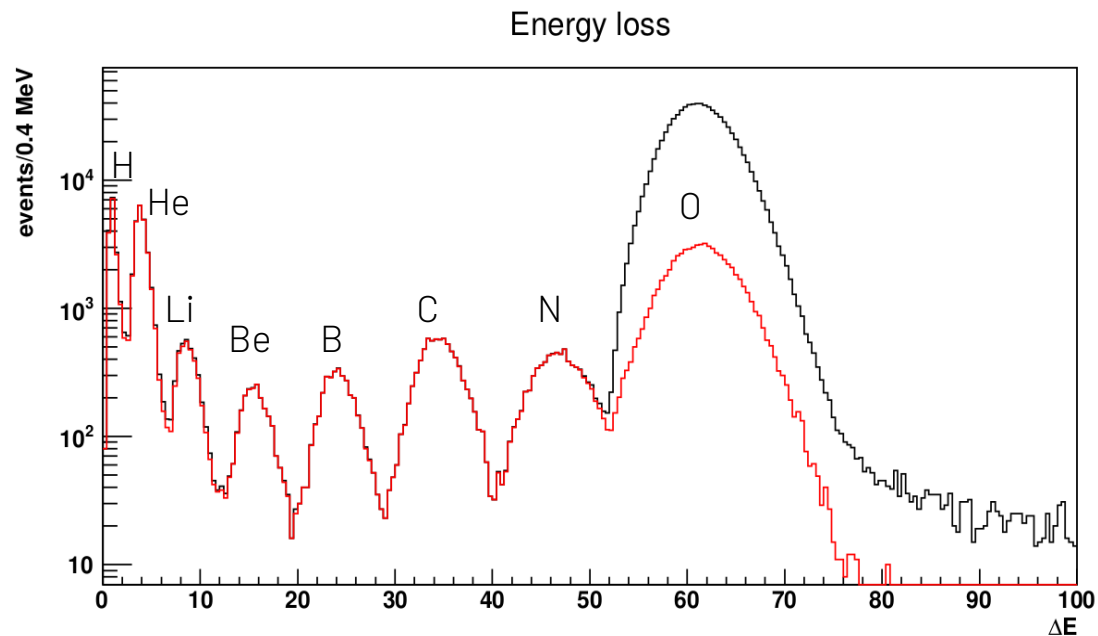
Analysis

Nuclear
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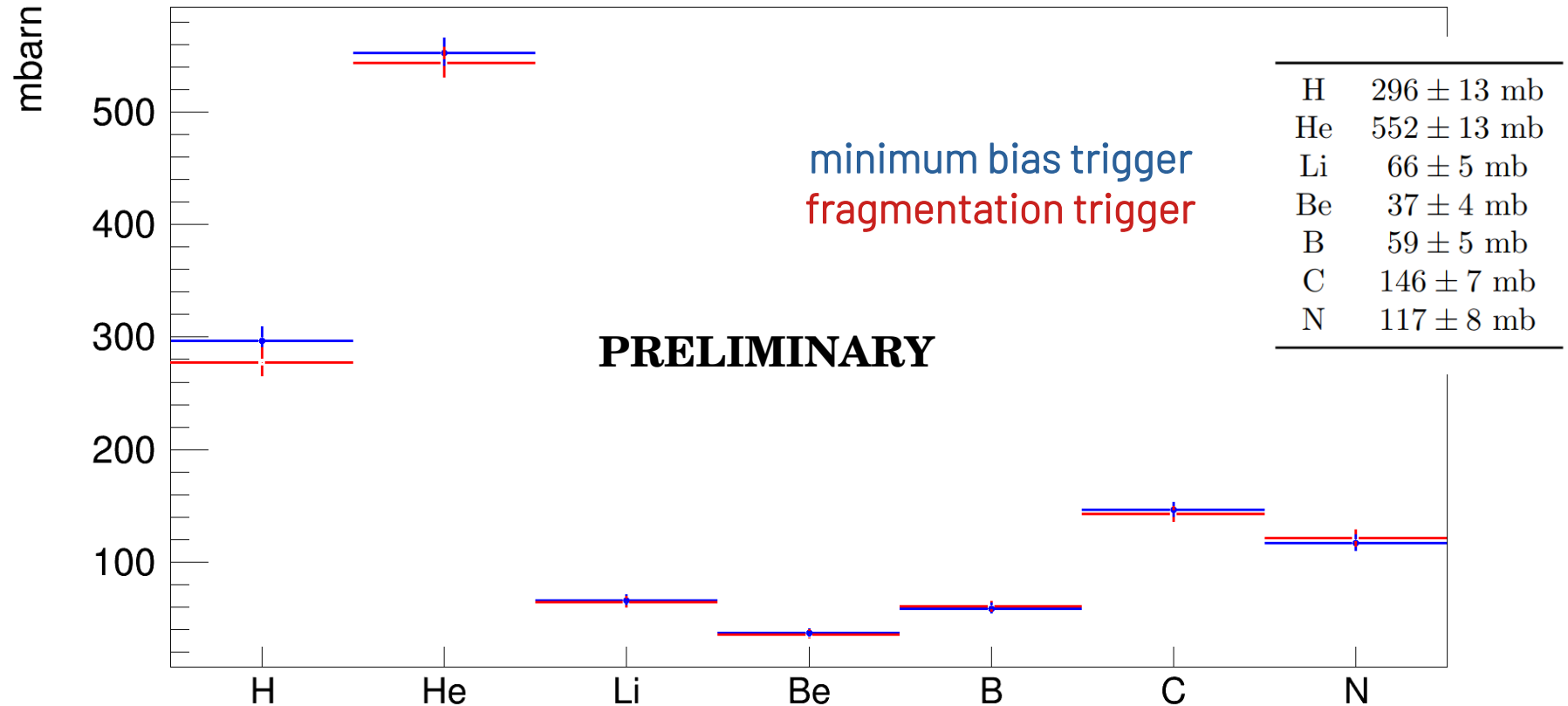
excellent charge separation!



Cross sections

Nuclear
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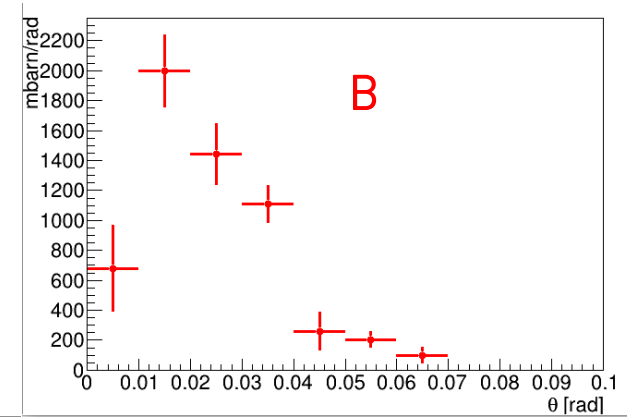
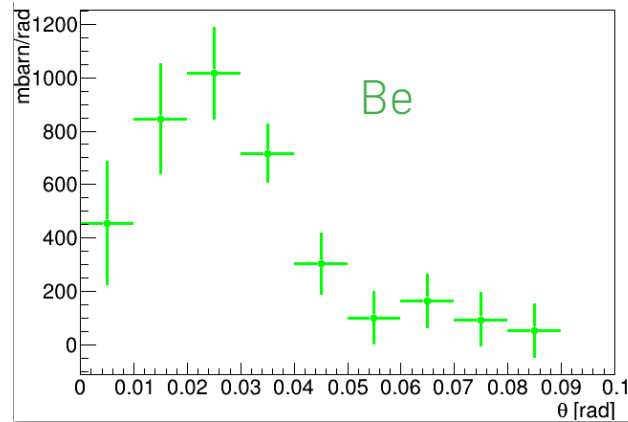
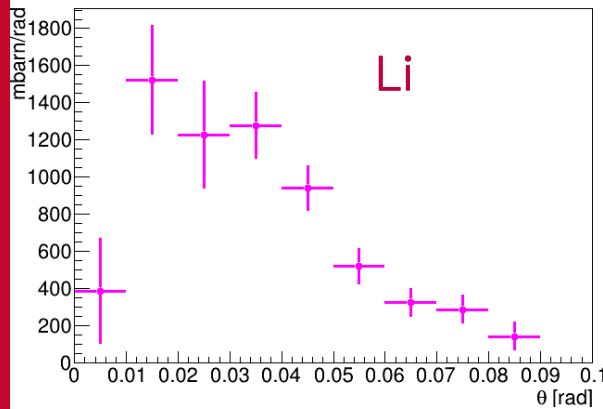
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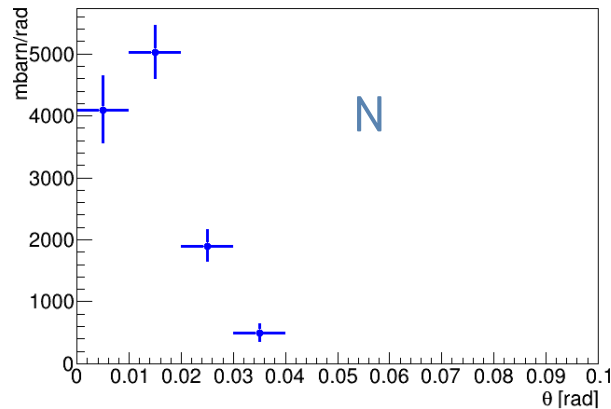
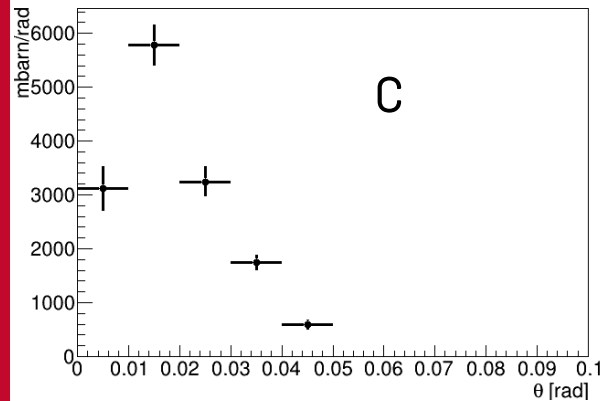
Cross sections

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PRELIMINARY



First available
measurements!

Conclusions

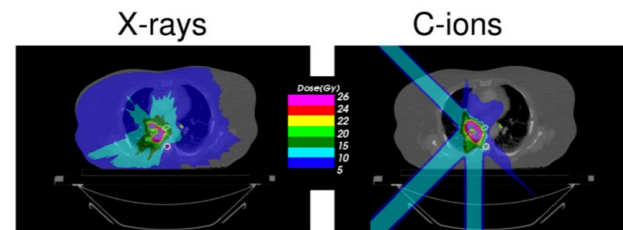
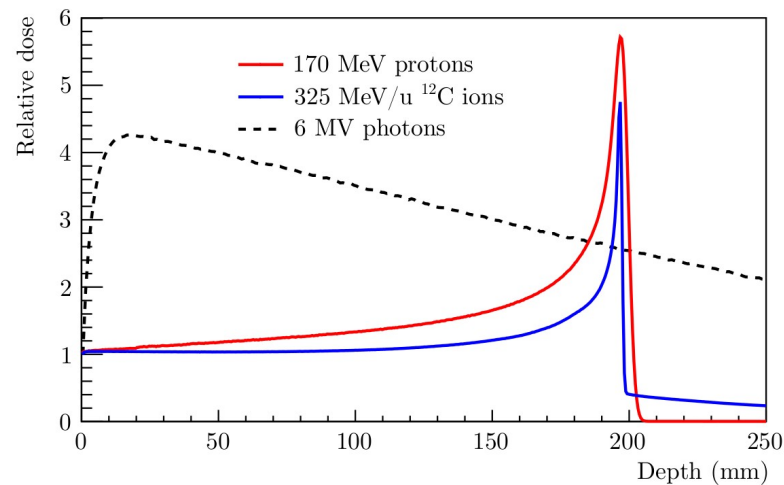
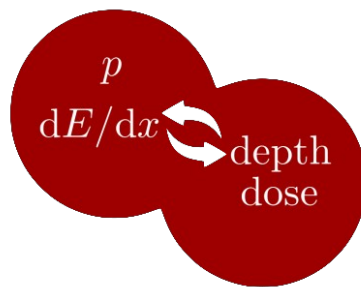
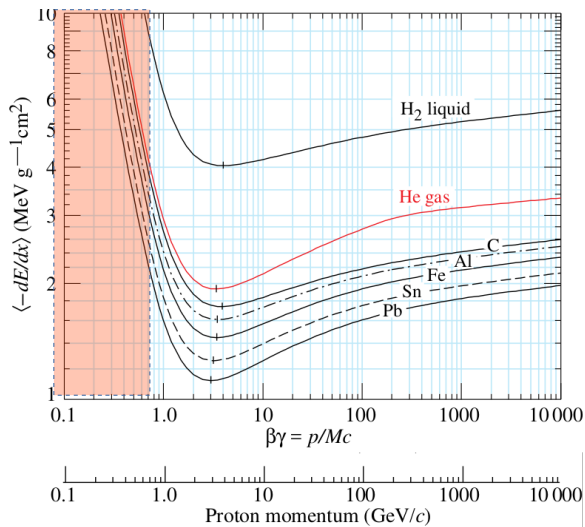
Nuclear
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- several fields can profit from **double differential cross section** measurement (hadrontherapy, space radioprotection...)
- the FOOT experiment aims to **measure double differential cross sections in angle and kinetic energy** for various beam-target settings
- data taking campaigns are ongoing** (GSI2019, GSI2020, GSI2021, HIT2022) with different beams and energies
- electronic setup to be completed in **2023**
- more than **40M events** acquired at GSI in July 2021 with Oxygen beam
- more than **90M events** acquired at HIT in July 2022 with Helium beam
- first cross section measurements** from GSI2021 show good capabilities to fulfill FOOT program
- a **continuous** data taking **activity** will be carried out (CNAO2022, beam request @GSI)



Thanks for listening!

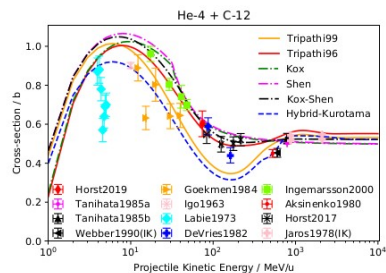


$$-\left\langle \frac{dE}{dx} \right\rangle = \frac{2\pi N_a e^4 \rho}{m_e} \frac{Z}{A} \frac{z^2}{v^2} \left[\ln \left(\frac{2m_e \gamma^2 v^2 W_{\max}}{I^2} \right) - 2\beta^2 - \delta - 2\frac{C}{Z} \right]$$

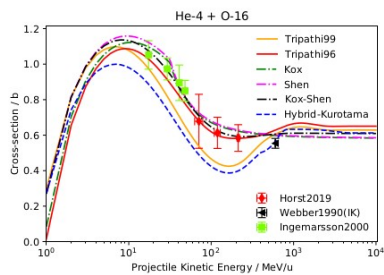
$$p = \frac{\sqrt{E_k (E_k + 2m_0 c^2)}}{c} \quad \mathcal{E} = \frac{E_k}{m_0 c^2} \quad \beta\gamma = \sqrt{\mathcal{E}(\mathcal{E} + 2)}.$$

$$R_{m_x} \approx \frac{m_x}{m_p} \frac{z_p^2}{z_x^2} R_{m_p} \quad \frac{\sigma_{R1}}{\sigma_{R2}} \approx \sqrt{\frac{m_2}{m_1}}.$$

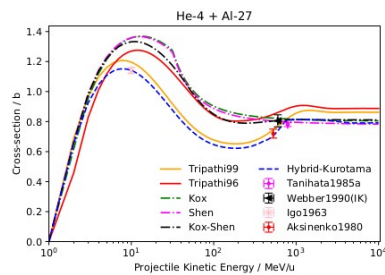
$$\sigma_R = \pi r_0^2 c_1(E) \left(A_p^{1/3} + A_t^{1/3} - c_2(E) \right)^2$$



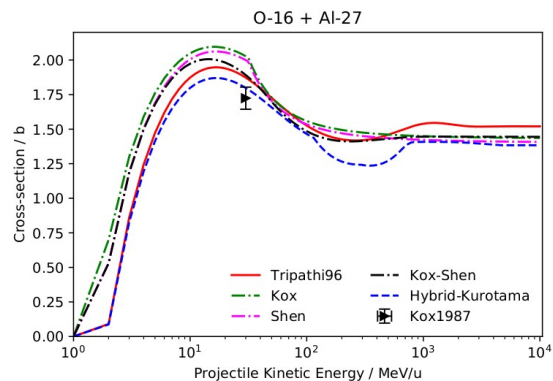
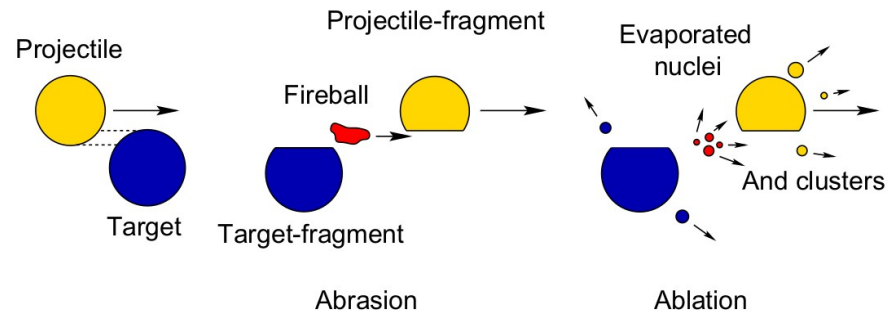
(a)



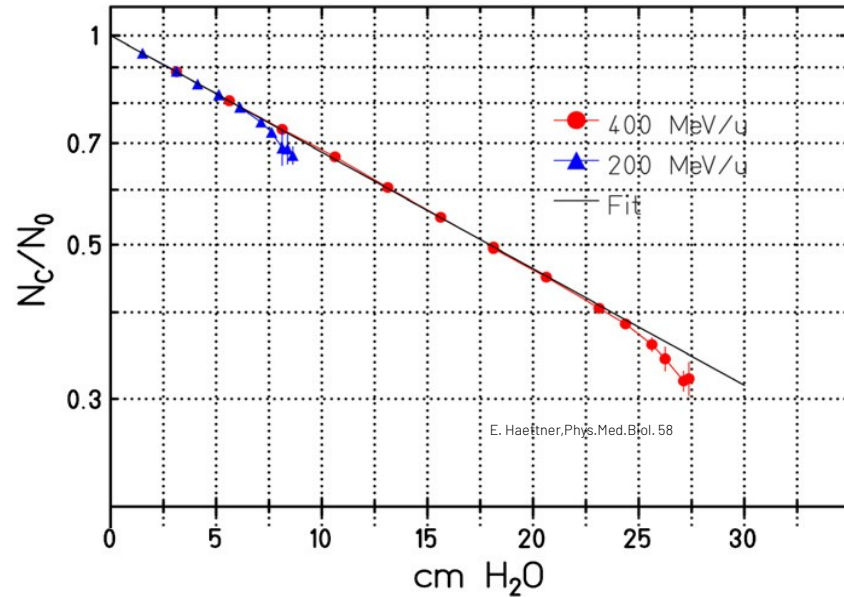
(b)



(c)

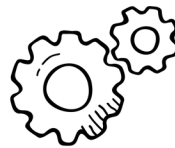


Nuclear fragmentation



- attenuation of primary beam can be important at **large** penetration **depths**
- surviving ions can be counted and related to total reaction cross sections

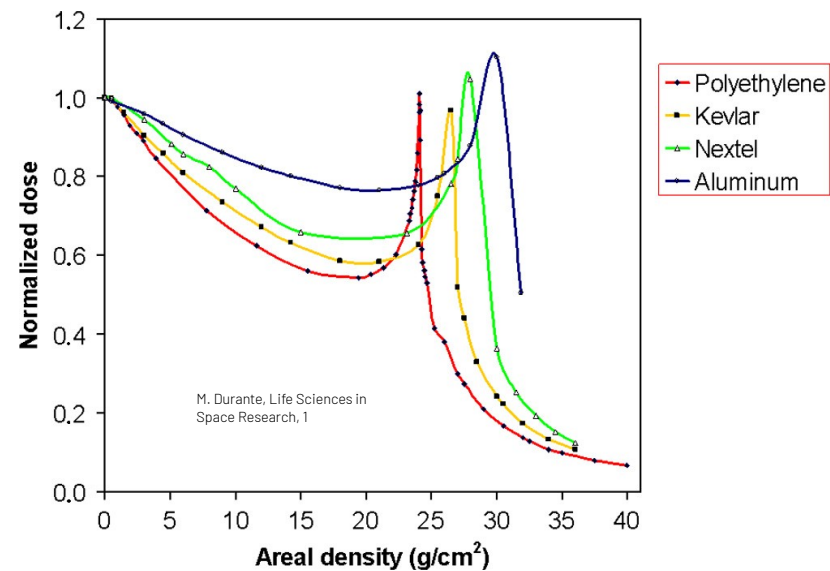
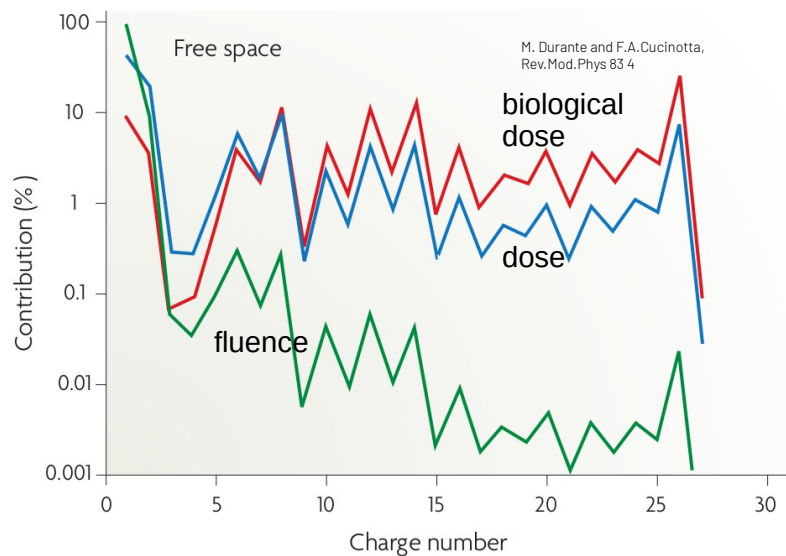
$$P(x) = \frac{N(x)}{N(0)} = \exp(-x/\lambda_{\text{int}})$$



$$\lambda_{\text{int}} = \frac{A_t}{N_a \sigma_R \rho}$$

$$\sigma_R = \int_0^\Omega \int_0^\infty \frac{d^2\sigma}{dE_K d\Omega} dE_K d\Omega$$

Space radioprotection



measurement of Bragg curves
in different materials of different
thicknesses



$$\sigma_R = \int_0^\Omega \int_0^\infty \frac{d^2\sigma}{dE_K d\Omega} dE_K d\Omega$$

Cross sections

400 MeV/u ^{16}O beam on 5mm Carbon target

With available data **total integrated** and angle differential cross section are achievable (no kinetic energy)

$$\Delta\sigma(Z) = \int_{E_{\min}}^{E_{\max}} \int_0^{\theta_{\max}} \left(\frac{\partial^2 \sigma}{\partial \theta \partial E_{\text{kin}}} \right) d\theta dE_{\text{kin}} = \frac{Y(Z)}{N_{\text{prim}} \cdot N_{\text{TG}} \cdot \varepsilon(Z)}$$

Align FOOT detectors and estimate **angular acceptance**

Extract fragment yields from TW

Calculate MC efficiencies for fragments

Cross sections

400 MeV/u ^{16}O beam on 5mm Carbon target

With available data total integrated and **angle differential** cross section are achievable (no kinetic energy)

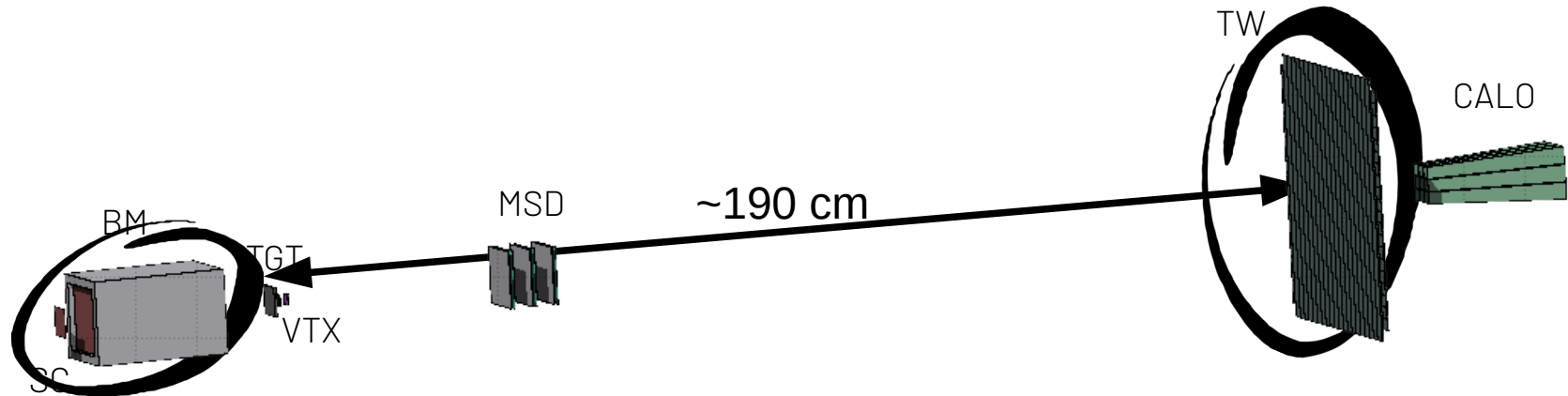
$$\frac{d\sigma}{d\theta}(Z) = \frac{Y(Z, \theta)}{N_{\text{prim}} \cdot N_{\text{TG}} \cdot \Delta\theta \cdot \epsilon(Z, \theta)}$$

Align FOOT detectors and estimate **angular acceptance**

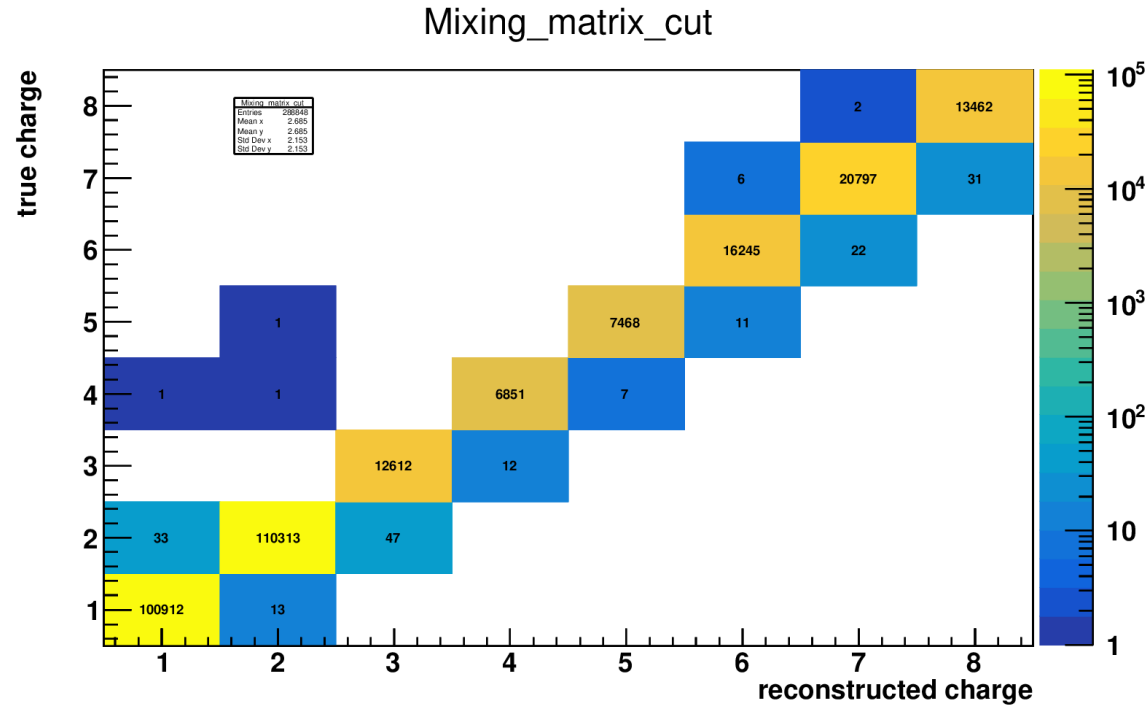
Extract fragment yields from TW

Calculate MC efficiencies for fragments

GSI2021 MC setup



Charge identification performances



Only particles with cut in E_{kin} , produced in target by primary beam inside TW acceptance

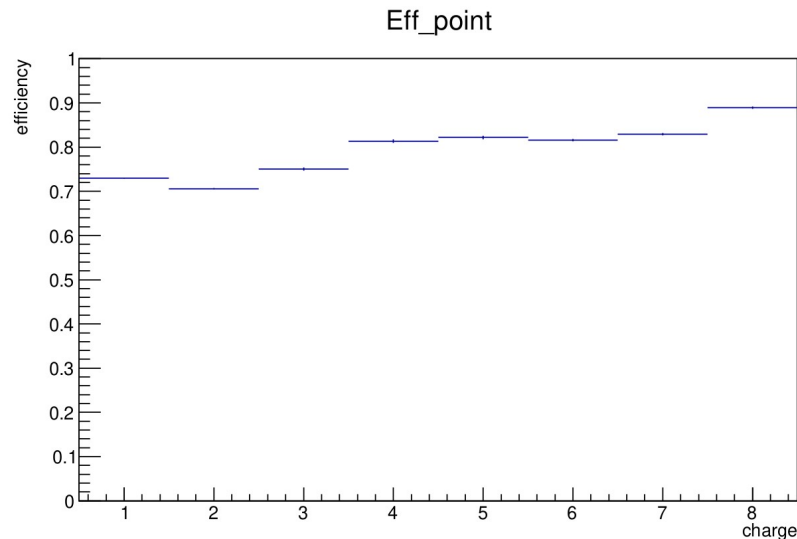
Efficiency

$$\varepsilon(Z) = \frac{N_{\text{TW}}(Z)}{N_{\text{track}}(Z)}$$

asking for a good TW point matched to a fragment produced in TG and kinetic energy between [100,600] MeV/u

asking for a fragment produced in TG within TW acceptance and kinetic energy between [100,600] MeV/u

$$\epsilon_{\varepsilon}(Z) = \sqrt{\varepsilon(Z) \frac{1 - \varepsilon(Z)}{N_{\text{track}}(Z)}}$$

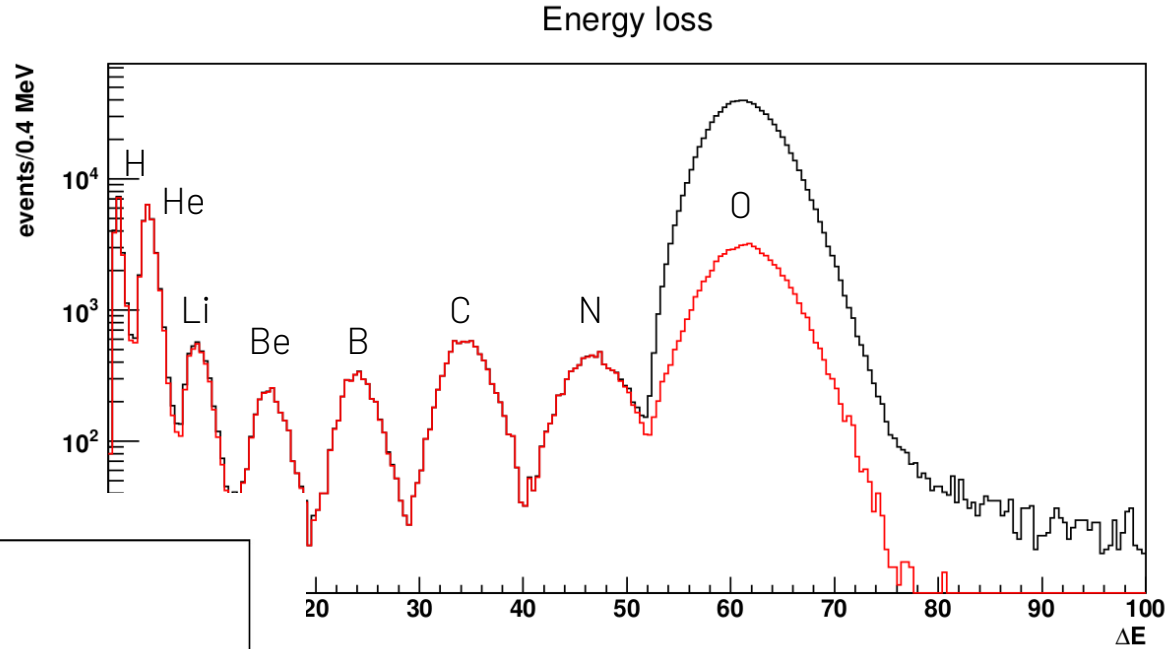
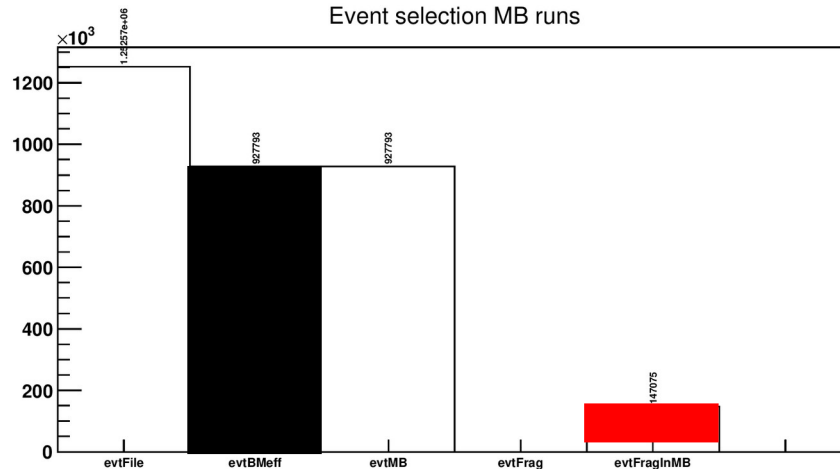


Number of primaries estimation

$$R = \frac{N_{\text{evtFragInMB}}}{N_{\text{evtMB}}} \approx 0.1585$$

$$\varepsilon_{\text{frag}}(Z) = \frac{N_{\text{evtFragInMB}}(Z)}{N_{\text{evtMB}}(Z)}.$$

H	He	Li	Be
95.7 ± 0.2	98.2 ± 0.1	99.1 ± 0.2	99.3 ± 0.2
B	C	N	O
99.6 ± 0.1	99.8 ± 0.1	98.2 ± 0.1	8.46 ± 0.03

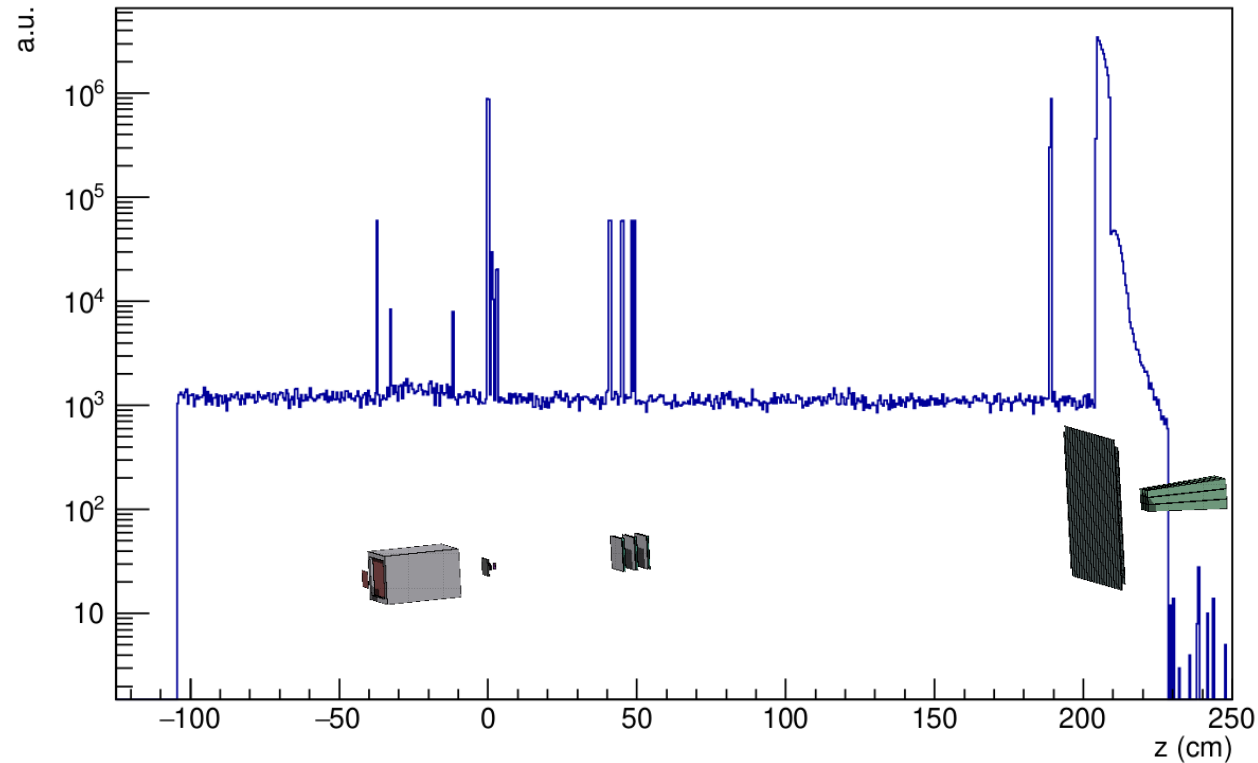


$$N_{\text{prim}} = N_{\text{frag}}/R$$

$$Y(Z) \rightarrow Y(Z)/\varepsilon_{\text{frag}}(Z).$$

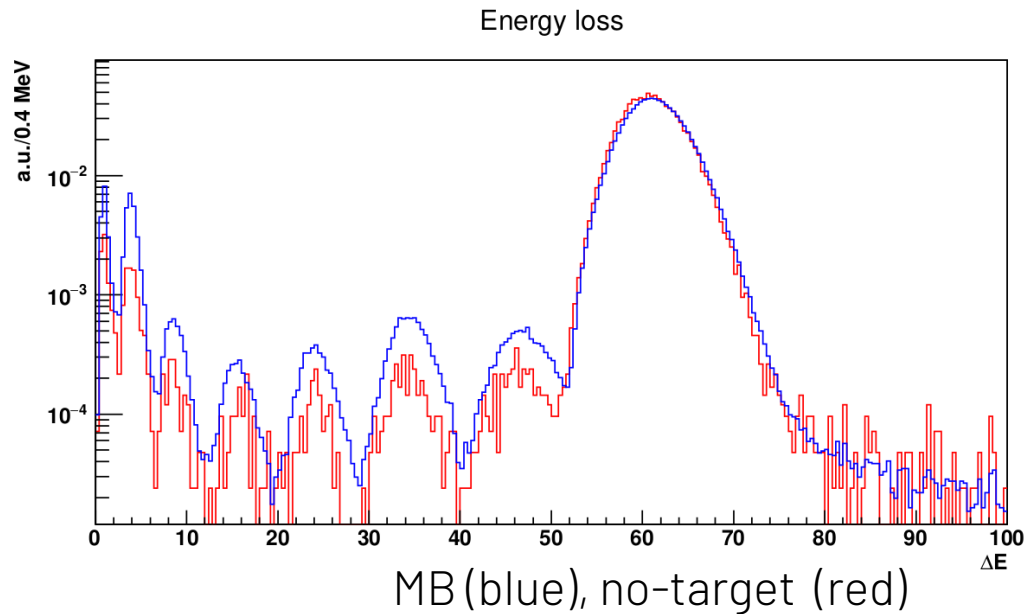
Out of target fragmentation from MC

Starting coordinate of primary daughters



Out of target fragmentation from data

Fragment	Y^{sig}	Y^{bkg}
H	16696 ± 129	339 ± 18
He	24213 ± 156	350 ± 19
Li	3591 ± 60	56 ± 8
Be	2242 ± 47	48 ± 7
B	3497 ± 59	61 ± 8
C	7944 ± 89	131 ± 11
N	8004 ± 89	179 ± 13
O	846504 ± 920	40603 ± 202



$$\Delta\sigma(Z) = \frac{1}{N_{\text{TG}} \cdot \varepsilon(Z)} \left(\frac{Y^{\text{sig}}(Z)}{N_{\text{prim}}^{\text{sig}}(Z)} - \frac{Y^{\text{bkg}}(Z)}{N_{\text{prim}}^{\text{bkg}}(Z)} \right)$$

Comparison with literature

PHYSICAL REVIEW C **83**, 034909 (2011)

Fragmentation of ^{14}N , ^{16}O , ^{20}Ne , and ^{24}Mg nuclei at 290 to 1000 MeV/nucleon

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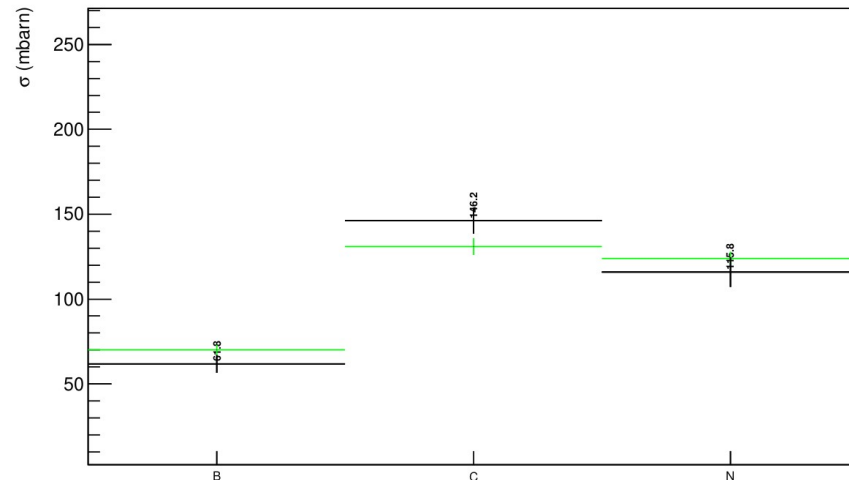
Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

(Received 27 October 2010; revised manuscript received 20 January 2011; published 24 March 2011)

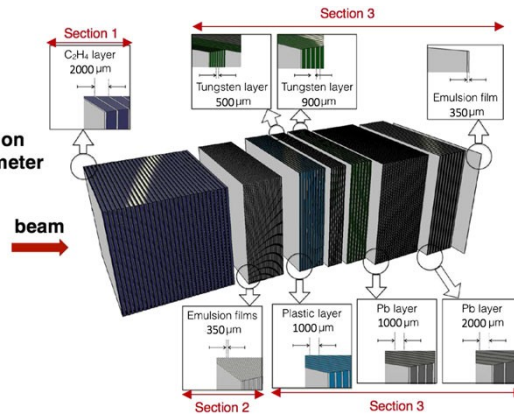
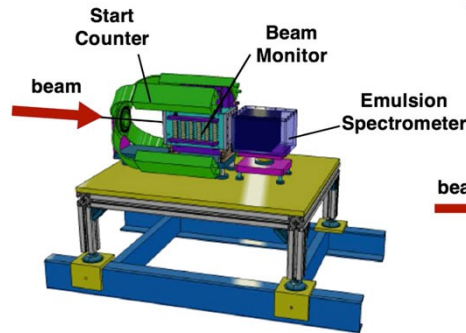
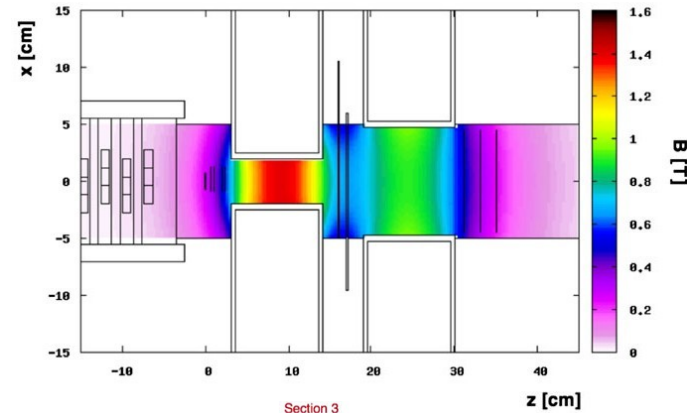
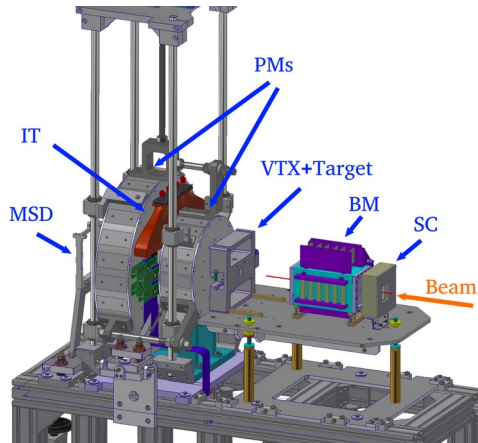
[10.1103/PhysRevC.83.034909](https://doi.org/10.1103/PhysRevC.83.034909)

We report fragmentation cross sections measured at 0° for beams of ^{14}N , ^{16}O , ^{20}Ne , and ^{24}Mg ions, at energies ranging from 290 MeV/nucleon to 1000 MeV/nucleon. Beams were incident on targets of C, CH_2 , Al, Cu, Sn, and Pb, with the C and CH_2 target data used to obtain hydrogen-target cross sections. Using methods established in earlier work, cross sections obtained with both large-acceptance and small-acceptance detectors are extracted from the data and, when necessary, corrected for acceptance effects. The large-acceptance data yield cross sections for fragments with charges approximately half of the beam charge and above, with minimal corrections. Cross sections for lighter fragments are obtained from small-acceptance spectra, with more significant, model-dependent corrections that account for the fragment angular distributions. Results for both charge-changing and fragment production cross sections are compared to the predictions of the Los Alamos version of the quark gluon string model (LAQGSM) as well as the NASA Nuclear Fragmentation (NUCFRG2) model and the Particle and Heavy Ion Transport System (PHITS) model. For all beams and targets, cross sections for fragments as light as He are compared to the models. Estimates of multiplicity-weighted helium production cross sections are obtained from the data and compared to PHITS and LAQGSM predictions. Summary statistics show that the level of agreement between data and predictions is slightly better for PHITS than for either NUCFRG2 or LAQGSM.

Comparison final cross section



	This work	Ref.[69]	Weighted average	t
B	62 ± 5	70 ± 3	68.0 ± 2.6	-1.37
C	146 ± 8	131 ± 5	135.5 ± 4.2	1.66
N	116 ± 9	124 ± 4	122.6 ± 3.6	-0.86



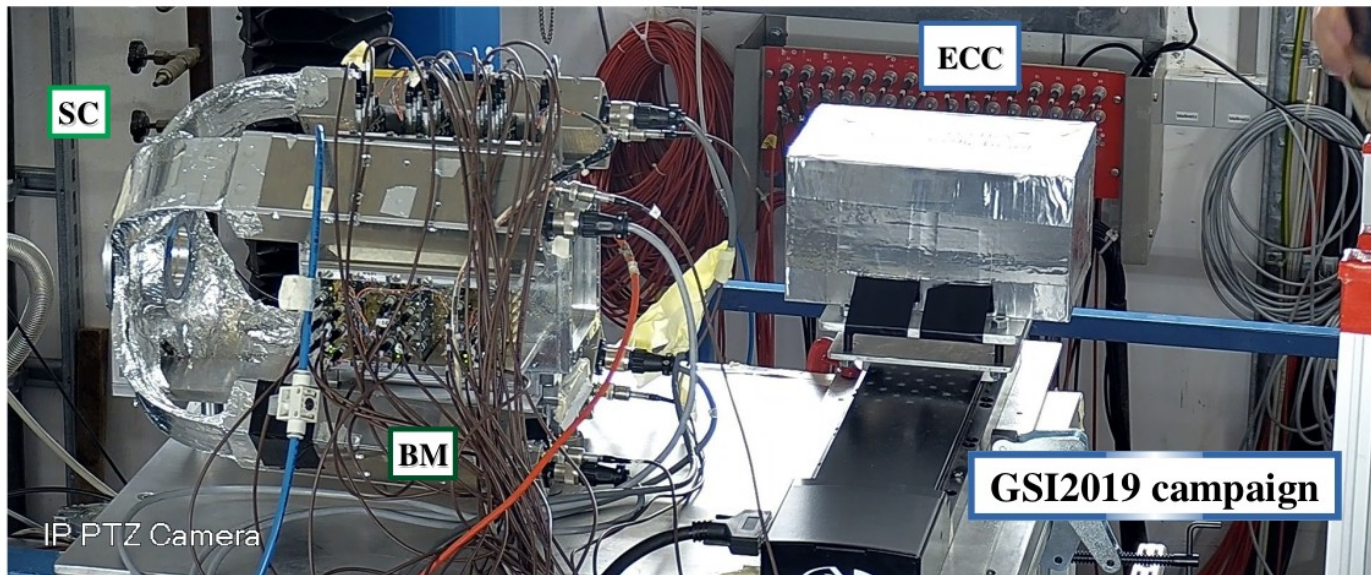
$$p = mc\beta\gamma$$

$$E_{\text{kin}} = mc^2(\gamma - 1)$$

$$E_{\text{kin}} = \sqrt{p^2c^2 + m^2c^4} - mc^2$$

- $\sigma(p)/p$ at level of 4 – 5%;
- $\sigma(T_{\text{tof}})$ at level of 100 ps;
- $\sigma(E_{\text{kin}})/E_{\text{kin}}$ at level of 1 – 2%;
- $\sigma(\Delta E)/\Delta E$ at level of 5%;

Emulsion setup: first results



- Data acquisitions started in 2019
- SC + BM for primary beam monitoring
- Only charge identification up to now

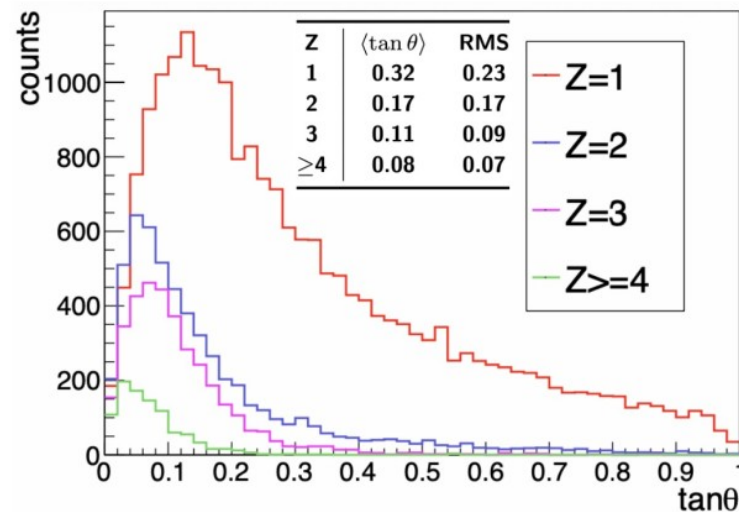
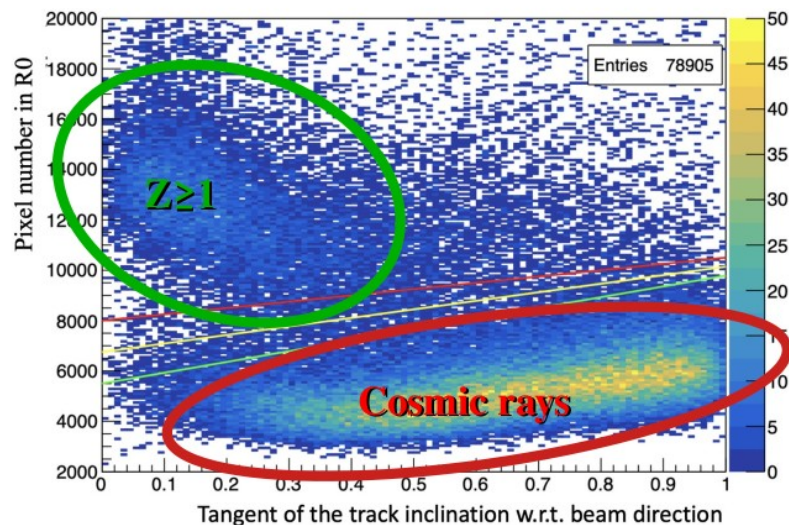
$^{16}\text{O} + \text{C}/\text{C}_2\text{H}_4 @ 200 \text{ MeV/u}$

Emulsion setup: first results



Charge identification in Section2:

- Different thermal treatment for track etching
- Cosmic rays cut-based rejection
- Principal Component Analysis for $Z \geq 1$



$^{16}\text{O} + \text{C}/\text{C}_2\text{H}_4 @ 200 \text{ MeV/u}$

Emulsion setup: first results

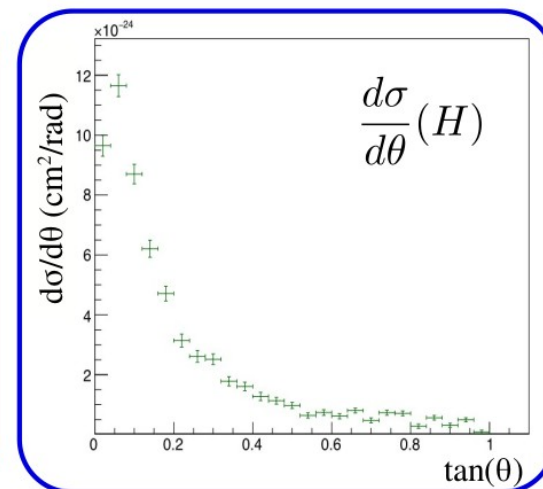
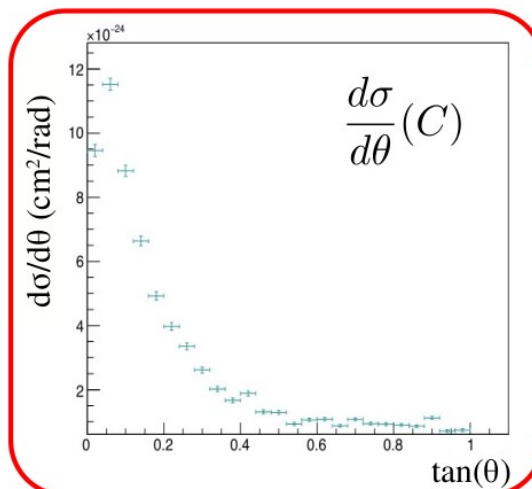
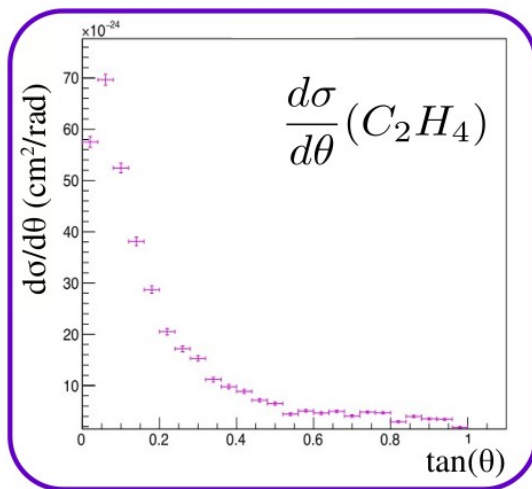


PRELIMINARY

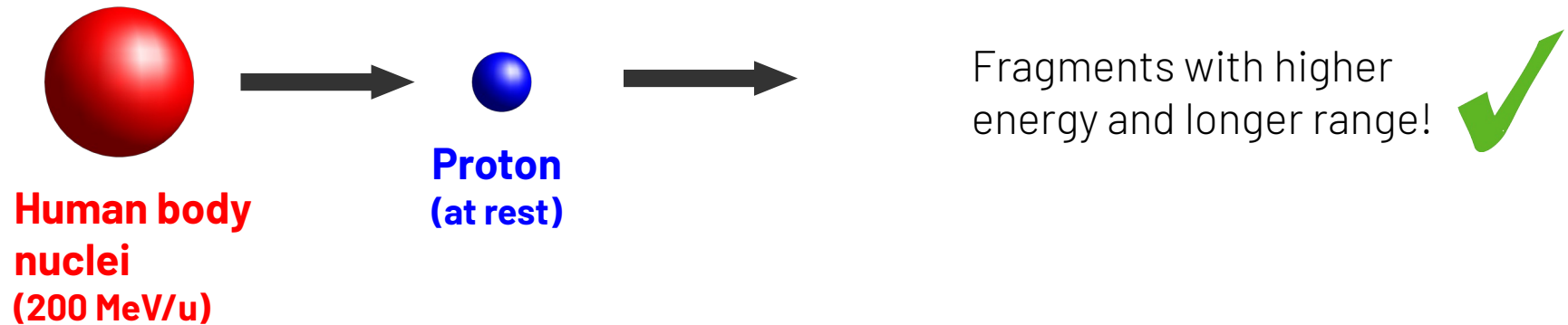
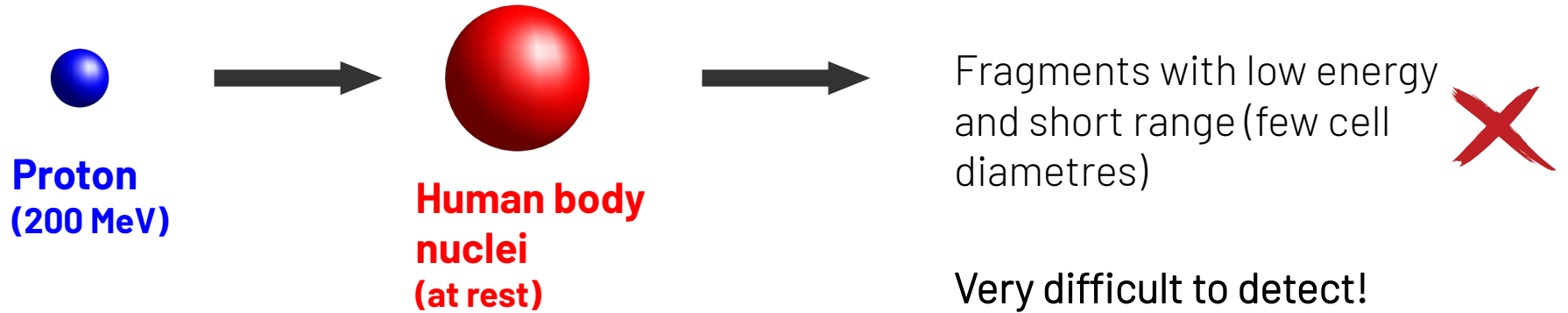
$$\left. \frac{d\sigma(\theta)}{d\theta} \right|_{C \text{ or } C_2H_4} = \frac{Y_i(\theta)}{N_B N_{TG} \Delta\theta \epsilon_{reco}^i(\theta)}$$

^{16}O (200 MeV/u) + C/C₂H₄

Differential Cross Sections



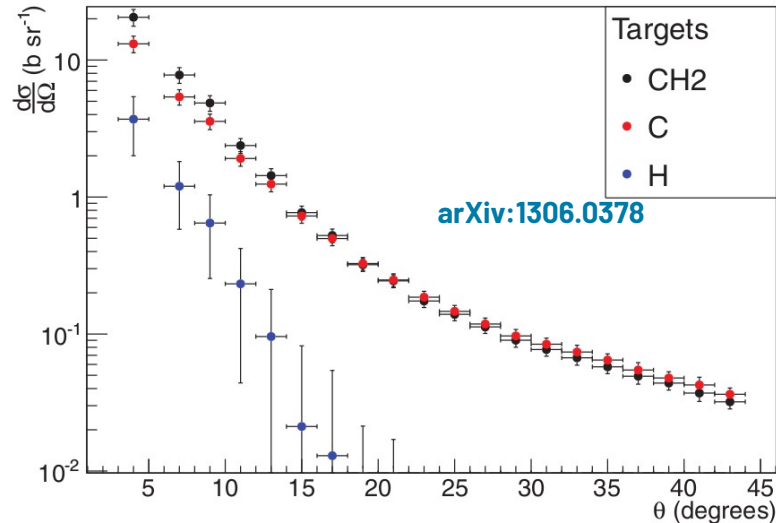
Courtesy of G. Galati



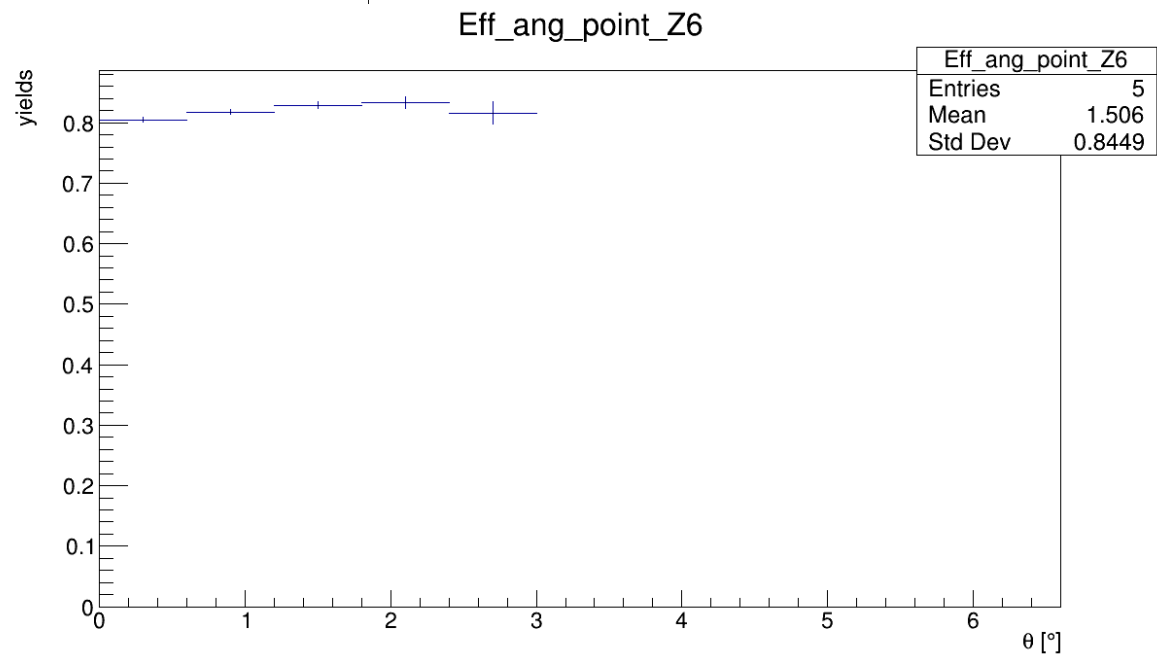
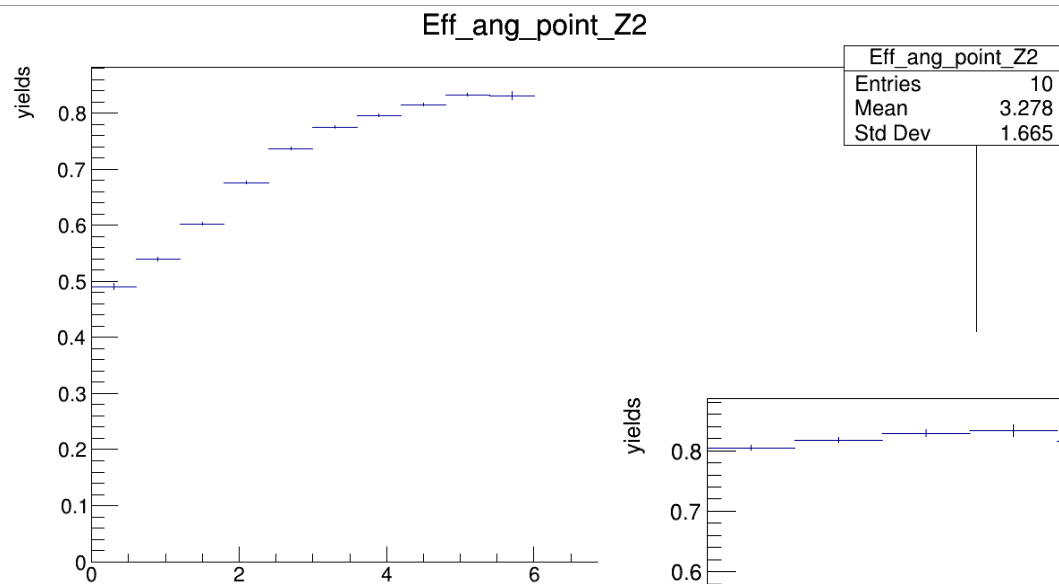
Problem: hydrogen target

- ✗ gas is not allowed in all experimental rooms
- ✗ gas is too sparse (low interaction probability)

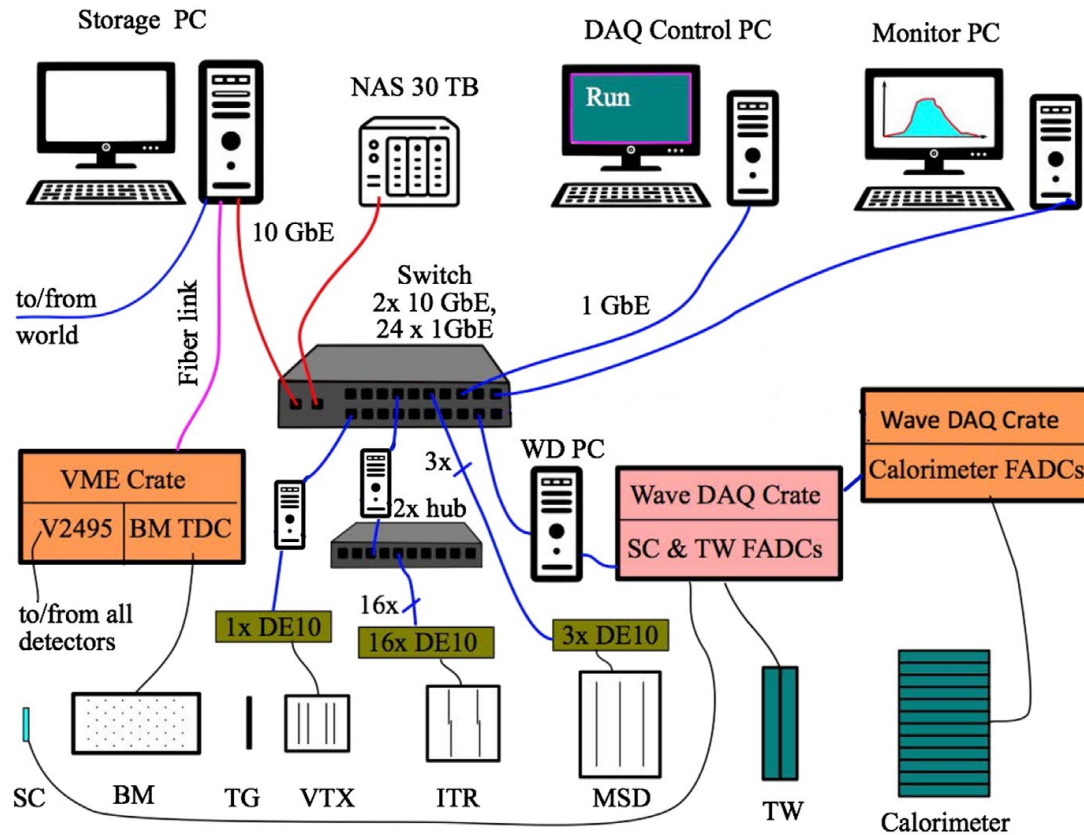
Polyethylene target (C_2H_4)_n and Carbon target



$$\frac{d\sigma}{d\Omega}(H) = \frac{1}{4} \cdot \left(\frac{d\sigma}{d\Omega}(\text{C}_2\text{H}_4) - 2 \cdot \frac{d\sigma}{d\Omega}(\text{C}) \right)$$



TDAQ infrastructure



- flexible and distributed system
- VME, Linux PC, custom boards, Ethernet, optical fibers
- 70 kB/event
- 1 kHz acquisition rate
- 2 TB/day
- V2495 handles **trigger and busy signals**
- data path is not signal path