



Experimental access to the three-body forces between hadrons with ALICE



Otón Vázquez Doce (LNF-INFN)
on behalf of the ALICE Collaboration



EuNPC2022, Santiago de Compostela, October 25, 2022

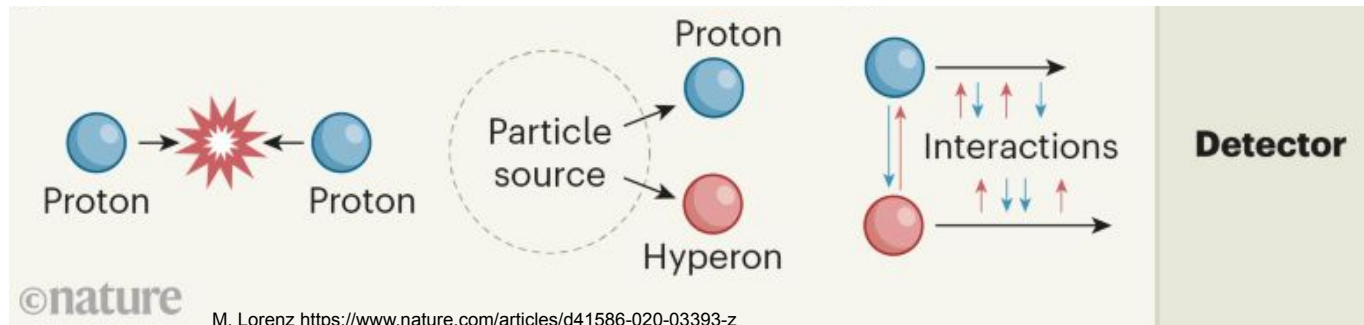


This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 754496

Hadron-hadron interactions via femtoscopy

2

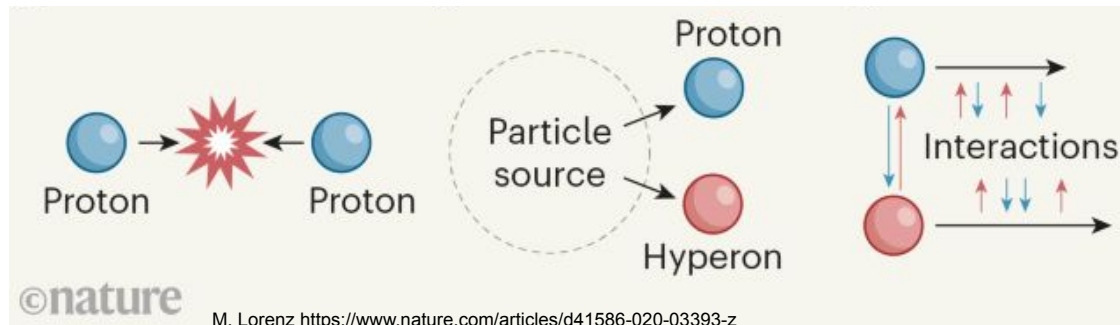
Nucleus-Nucleus collisions at the LHC recorded by ALICE



Hadron-hadron interactions via femtoscopy

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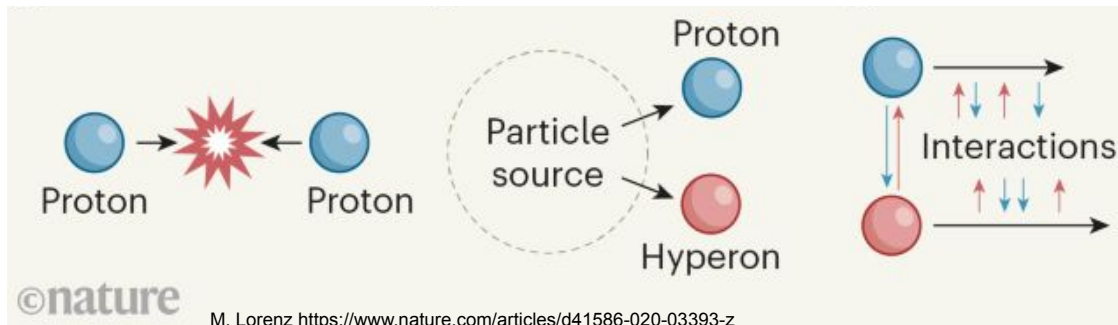


- Charged particle tracking and PID
- Reconstruction of hyperons via weak decay

Hadron-hadron interactions via femtoscopy

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Nucleus-Nucleus collisions at the LHC recorded by ALICE



- Charged particle tracking and PID
- Reconstruction of hyperons via weak decay

Experimental observable: Correlation function of two final-state particles

$$C(k^*) = \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

\longrightarrow Pairs of particles from same collision
 \longrightarrow Particles produced in different collisions

$$k^* = \frac{|\vec{p}_a^* - \vec{p}_b^*|}{2}$$

relative momentum in pair rest frame

Theoretical correlation function

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$$C(k^*) = \int \underbrace{S(\mathbf{r}^*)}_{\text{source}} |\underbrace{\psi(\mathbf{k}^*, \mathbf{r}^*)}_{\text{wave function}}|^2 d^3\mathbf{r}^*$$

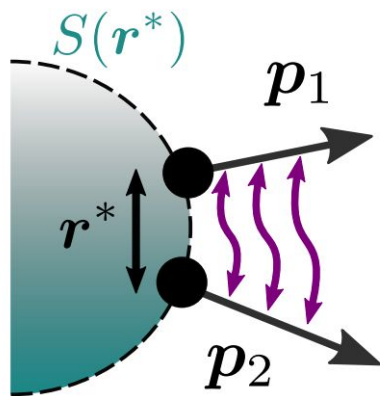
Lisa, Pratt, Wiedemann, Solz, Ann. Rev. Nucl. Part. Sci. 55 (2005) 357

Theoretical correlation function

6

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Lisa, Pratt, Wiedemann, Solz, Ann. Rev. Nucl. Part. Sci. 55 (2005) 357



pp, p-Pb: $r^* \sim 1\text{fm}$

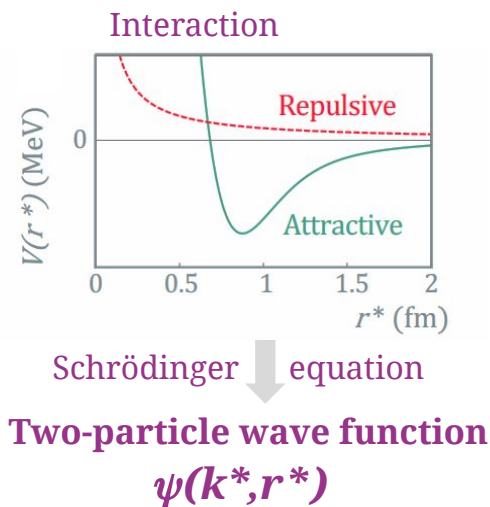
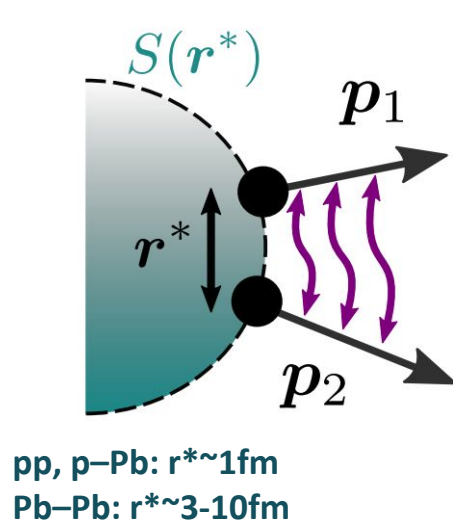
Pb-Pb: $r^* \sim 3\text{-}10\text{fm}$

Theoretical correlation function

7

$$C(k^*) = \int \underbrace{S(\mathbf{r}^*)}_{\text{source}} \underbrace{|\psi(\mathbf{k}^*, \mathbf{r}^*)|^2}_{\text{wave function}} d^3\mathbf{r}^*$$

Lisa, Pratt, Wiedemann, Solz, Ann. Rev. Nucl. Part. Sci. 55 (2005) 357

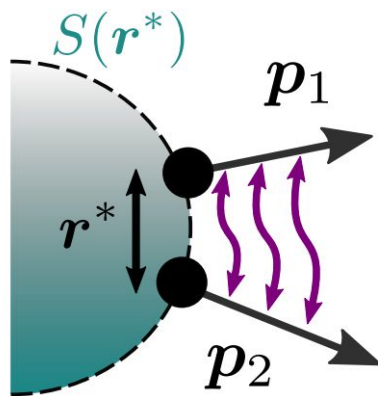


Theoretical correlation function

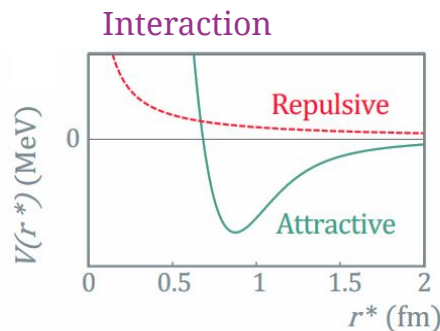
8

$$C(k^*) = \int \underbrace{S(\mathbf{r}^*)}_{\text{source}} |\underbrace{\psi(\mathbf{k}^*, \mathbf{r}^*)}_{\text{wave function}}|^2 d^3\mathbf{r}^* \quad \Rightarrow \quad C(k^*)$$

Lisa, Pratt, Wiedemann, Solz, Ann. Rev. Nucl. Part. Sci. 55 (2005) 357

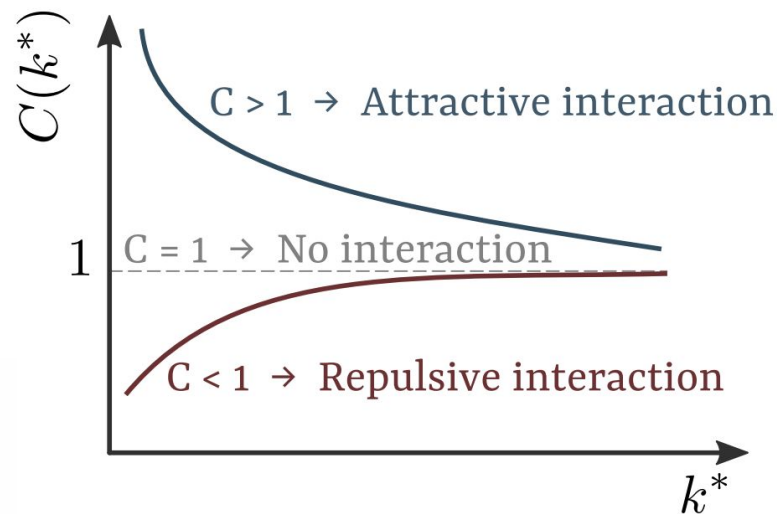


pp, p-Pb: $r^* \sim 1\text{fm}$
Pb-Pb: $r^* \sim 3\text{-}10\text{fm}$



Schrödinger equation

Two-particle wave function
 $\psi(k^*, r^*)$

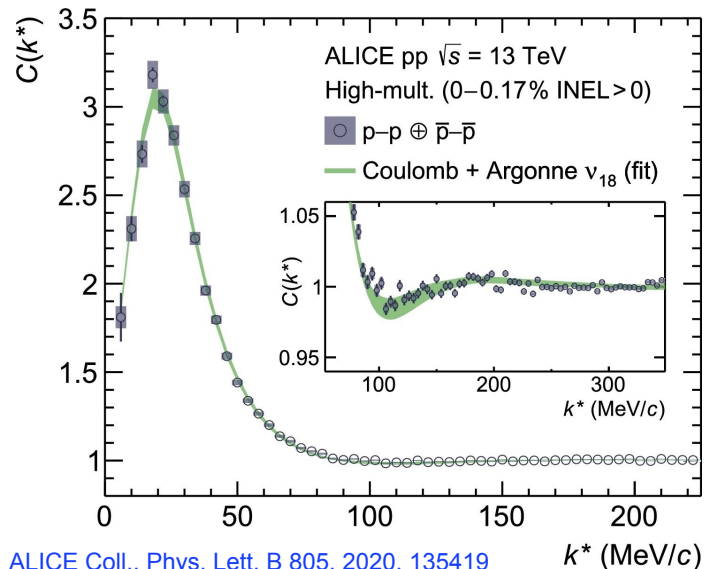


Determination of the source size

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Source size determined via traditional femtoscopy analysis (known interaction)

- fit p-p correlation function \Rightarrow extract gaussian source radius

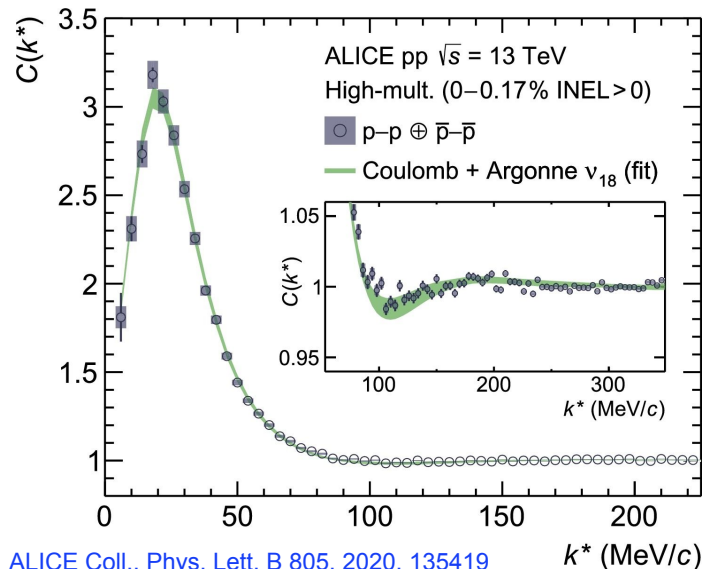


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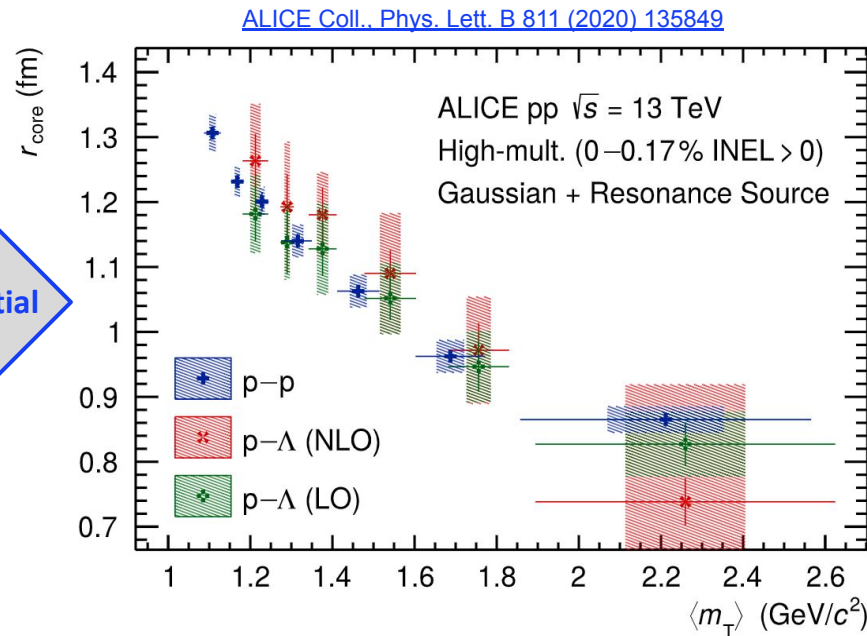
10

Source size determined via traditional femtoscopy analysis (known interaction)

- fit p-p correlation function \Rightarrow extract gaussian source radius
- differential $\langle m_T \rangle$ fit \Rightarrow “map” of source size
 - take into account effect of strong decaying resonances

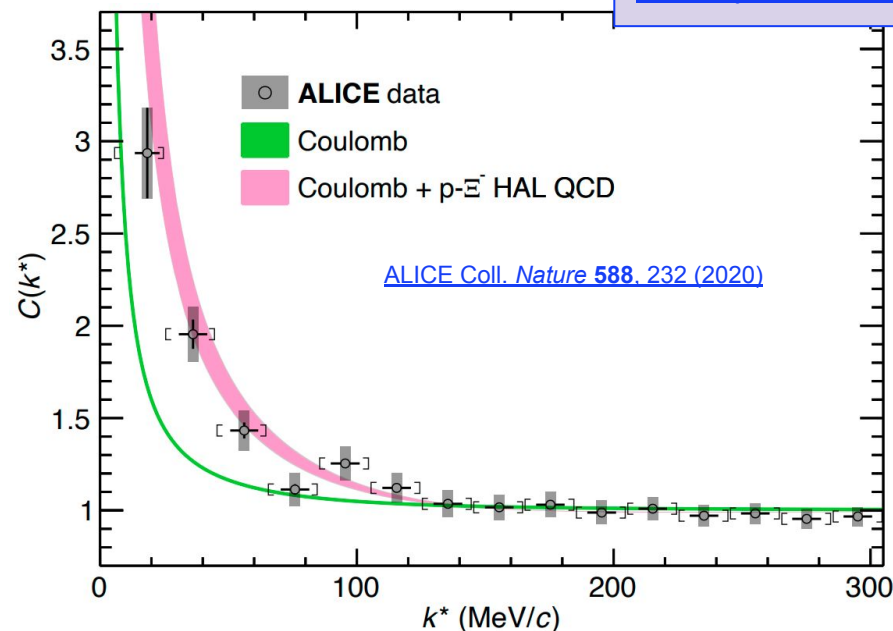


$\langle m_T \rangle$ differential



A practical example: p - Ξ^- correlation

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[see Talk by R. del Grande P7 session](#)

- Observation of the **attractive strong interaction**

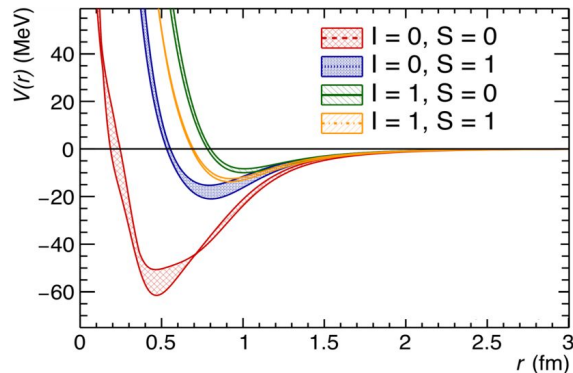
A practical example: $p\text{-}\Xi^-$ correlation

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Source

Given pair $\langle m_T \rangle = 1.9 \text{ GeV}/c^2$ and
effect of strong resonances
 $\Rightarrow r_{\text{eff}} = 1.02 \pm 0.05 \text{ fm}$

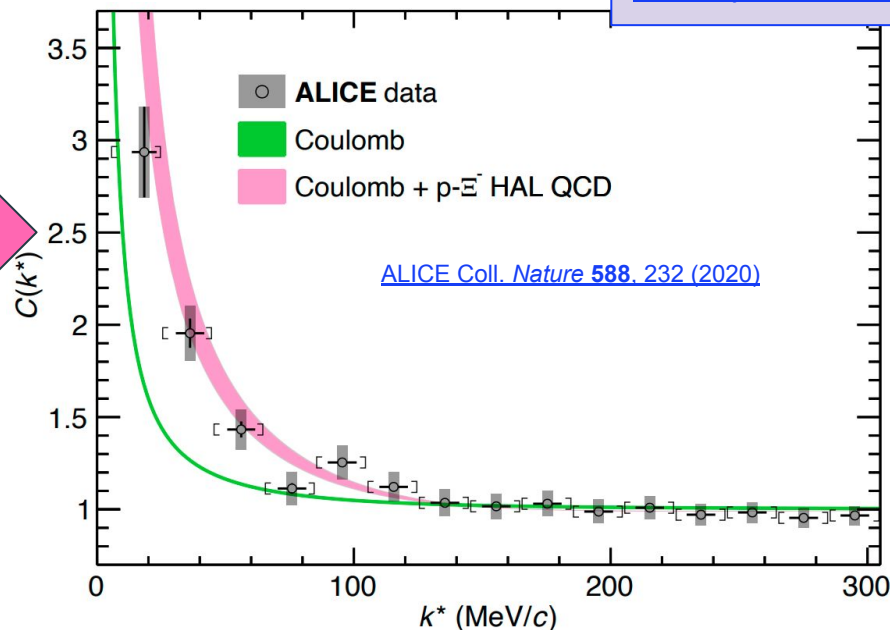
Interaction



Lattice QCD $p\text{-}\Xi^-$ potential

K. Sasaki et al. (HAL QCD), Nucl. Phys. A330, 998 (2020)

[see Talk by R. del Grande P7 session](#)



- Observation of the **attractive strong interaction**
- **Described by Lattice QCD potential**
 \Rightarrow Implications for the EoS of NS

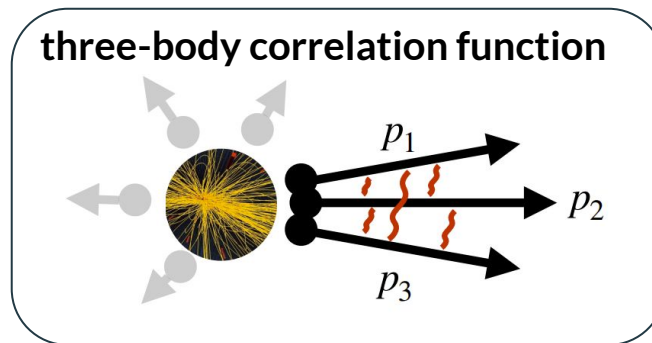
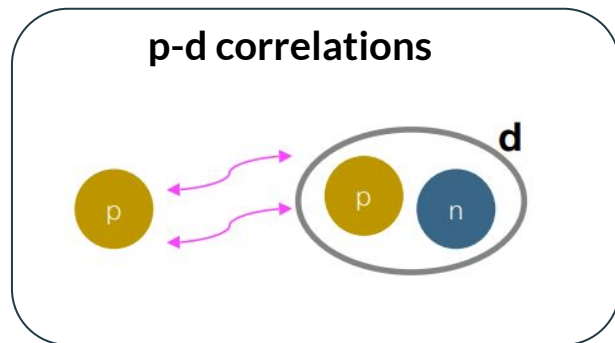
Accessing three-body forces with femtoscopy

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Three-body forces

- Fundamental to **explain the nuclear structure**
 - contribute to 10–15% of nuclear binding energy at normal nuclear density
 - might become more important at higher densities
- Fundamental **ingredients for the Equation of State (EoS) of dense nuclear matter**
- Theory currently anchored to properties of nuclei, hypernuclei and scattering data

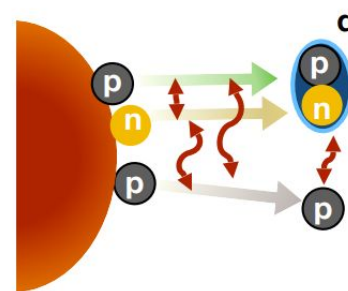
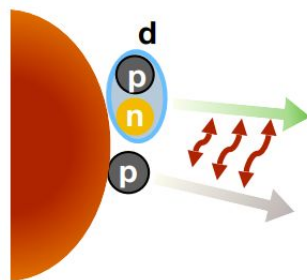
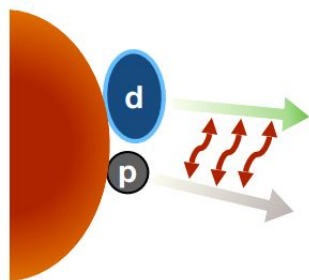
Now femtoscopy studies enable access to three-body forces:



Proton-deuteron femtoscopy

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- Proton-deuteron (p-d) interaction constrained from the scattering experiments
- **Production mechanism of light nuclei not understood**
Models: Statistical Hadronisation^{1,2} or Coalescence³



¹J. Cleymans et al, Phys. Rev. C 74, 034903 (2006)

²J. Cleymans et al, Z. Phys. C 57, 135–147 (1993)

³K. Blum et al, Phys. Rev. C 99, 04491(2019)

p-d correlations in pp collisions at the LHC

⇒ Final-state interaction can help the study of the formation time of deuterons (antideuterons)

p-d correlation function

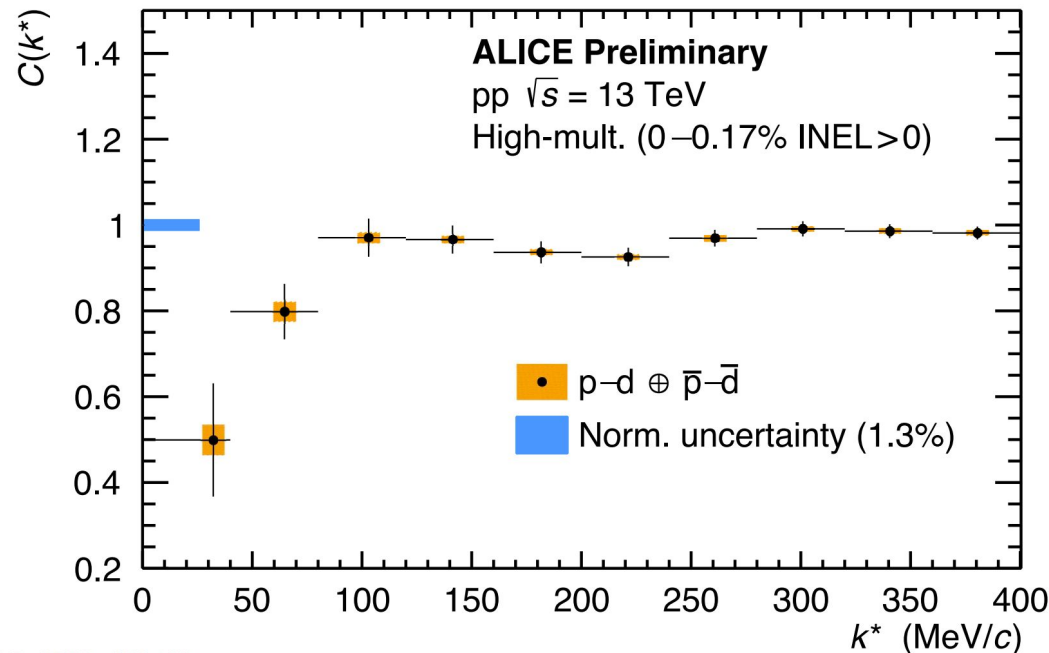
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p-d correlation function in pp collisions at the LHC

Data sample:

- pp 13 TeV Run 2 High-Multiplicity trigger
- 1×10^9 events
- 3000 p-d \oplus pbar-dbar pairs at $k^* < 200$ MeV/c

Data shows **clear depletion at low k^***
 \Rightarrow Repulsive type of interaction



ALI-PREL-486400

p-d correlation function

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p-d correlation function in pp collisions at the LHC

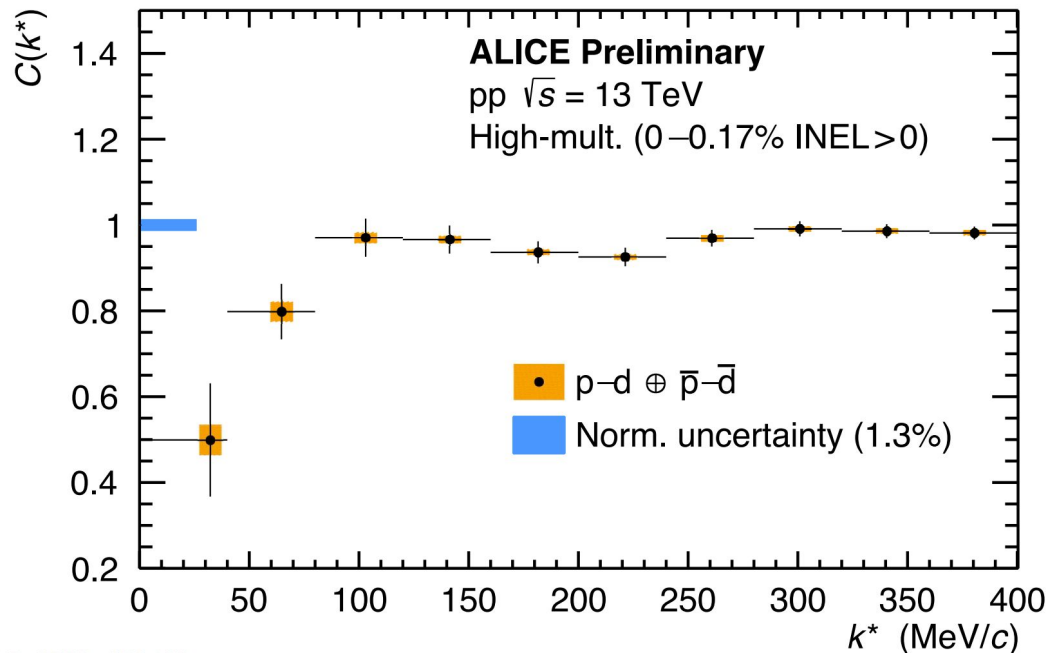
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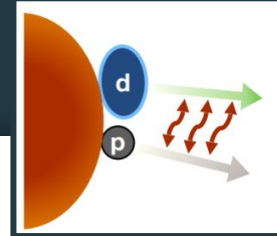
Source size for p-d pairs

Given pair $\langle m_T \rangle = 1.65$ GeV/ c^2 and
effect of Δ -resonances
 $\Rightarrow r_{\text{eff}} = 1.06 \pm 0.04$ fm



ALI-PREL-486400

p-d as two-body problem



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Theoretical model constrained to scattering p-d experiments

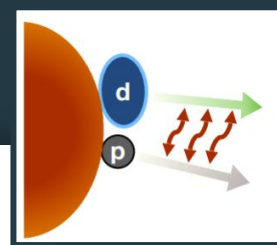
$S = 1/2$		$S = 3/2$		
$f_0(\text{fm})$	$r_0(\text{fm})$	$f_0(\text{fm})$	$r_0(\text{fm})$	
$-1.30^{+0.20}_{-0.20}$	—	$-11.40^{+1.80}_{-1.20}$	$2.05^{+0.25}_{-0.25}$	Van Oers et al. Nucl. Phys. A 561 (1967)
$-2.73^{+0.10}_{-0.10}$	$2.27^{+0.12}_{-0.12}$	$-11.88^{+0.40}_{-0.10}$	$2.63^{+0.01}_{-0.02}$	J.Arviex et al. Nucl. Phys. A92 221 (1973)
-4.0	—	-11.1	—	E.Huttel et al. Nucl. Phys. A406 443 (1983)
-0.024	—	-13.7	—	A.Kievsky et al. Phys. Lett, B406 292 (1997)
$0.13^{+0.04}_{-0.04}$	—	$-14.70^{+2.30}_{-2.30}$	—	T. C. Black Phys. Lett, B471 103 (1999)

Lednický model for distinguishable particles Phys. Part. Nucl. 40 (2009) 307

- Define the s-wave **two-particle relative wave-function starting from the scattering parameters**
- Assumptions: deuteron as point-like particle

Convention sign: In this presentation positive (negative) f_0 means attractive (repulsive) interaction

p-d as two-body problem



Theoretical model constrained to scattering p-d experiments

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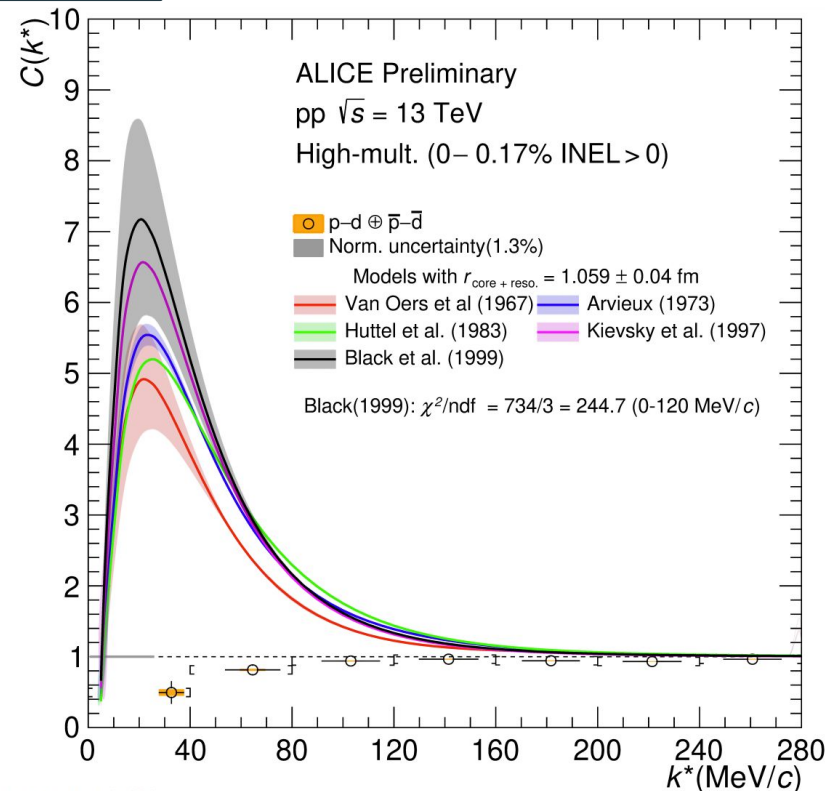
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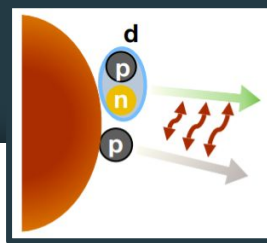
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Model and data disagree for source size = 1.06 ± 0.04 fm

➔ Model does not account for p-(p-n) interaction



p-d as a three-body problem

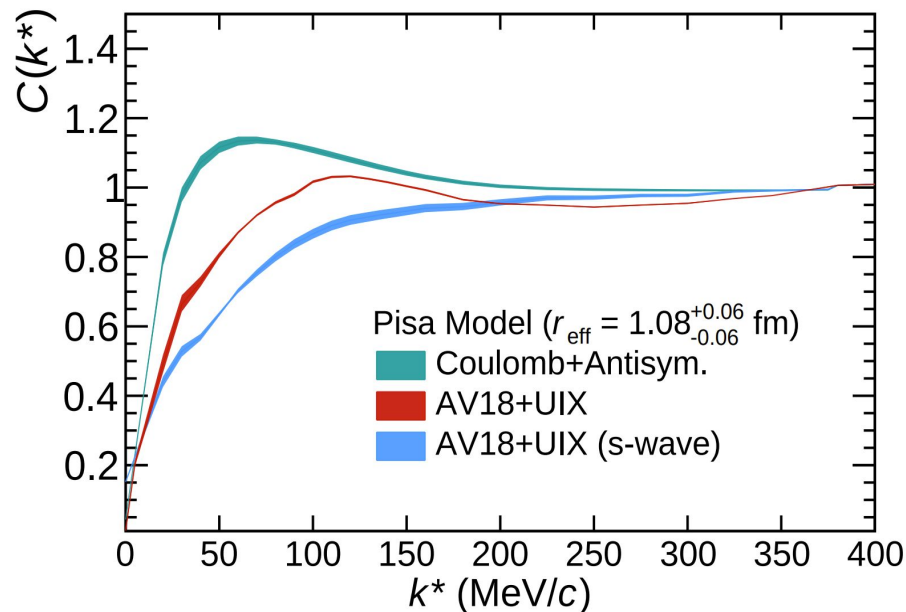


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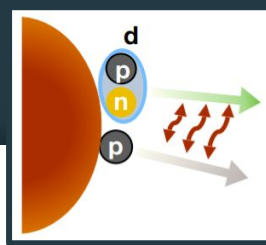
Full calculation of a three-body p-p-n system projected into the p-d final state

Model under construction by PISA theory group (M. Viviani, A. Kievsky, L. Marcucci) qualitatively reproduces the data

- **Two-body interaction** Argonne V18 potential
- **Three-body interaction** Urbana XI potential
- **Deuteron wave-function** from AV18 NN interaction
- Deuteron is formed at the same time as the proton



p-d as a three-body problem



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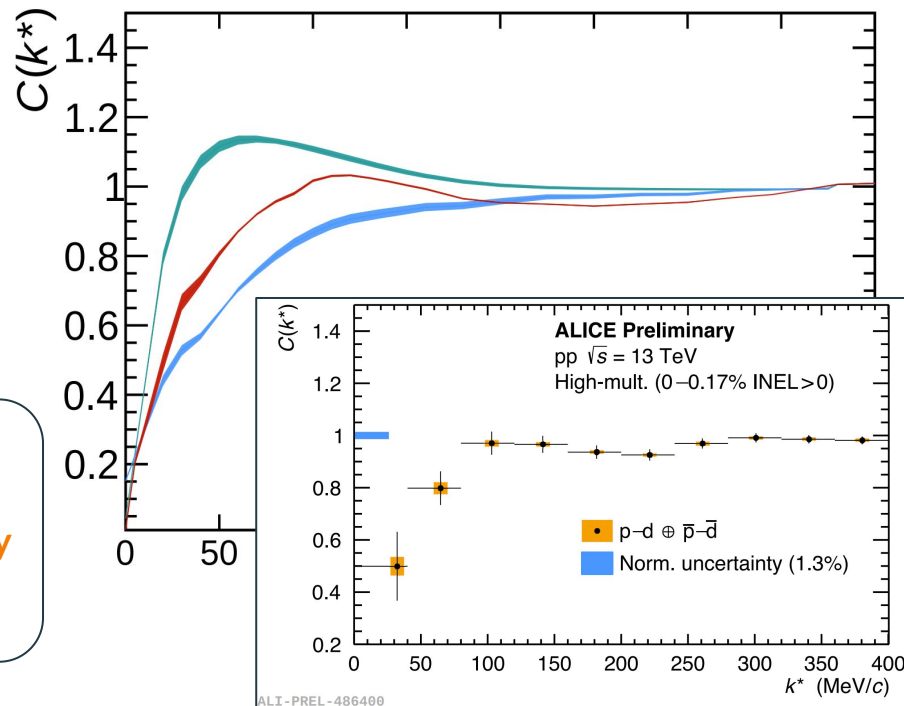
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p-d correlation

- affected by two- and three-body p-p-n interactions
- ⇒ **new way to explore the interaction of the three-body system at short distances**



Three-body femtoscopy

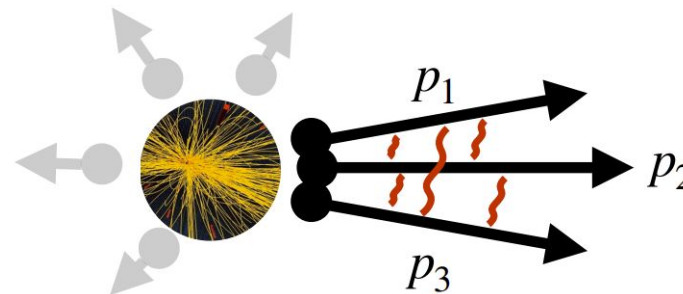
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Study of three-particle correlations

⇒ Direct access to the genuine three-body forces

Three-particle correlation function:

$$C(\mathbf{p}_1, \mathbf{p}_2, \mathbf{p}_3) \equiv \frac{P(\mathbf{p}_1, \mathbf{p}_2, \mathbf{p}_3)}{P(\mathbf{p}_1) P(\mathbf{p}_2) P(\mathbf{p}_3)} = \frac{N_{\text{same}}(Q_3)}{N_{\text{mixed}}(Q_3)}$$



Three-body femtoscopy

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Study of three-particle correlations

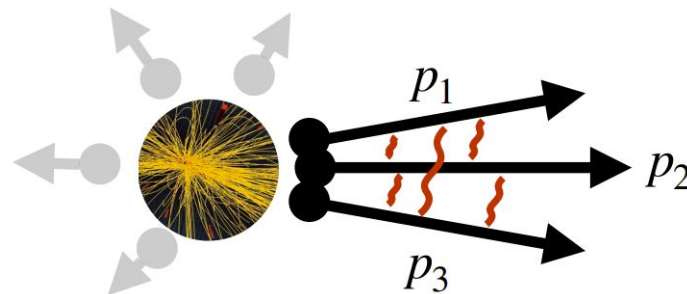
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The Lorentz invariant Q_3 is defined as:

$$Q_3 = \sqrt{-q_{12}^2 - q_{23}^2 - q_{31}^2} \quad q_{ij}^\mu = (p_i - p_j)^\mu - \frac{(p_i - p_j) \cdot P_{ij}}{P_{ij}^2} P_{ij}^\mu \quad P_{ij} \equiv p_i + p_j$$



Three-body femtoscopy

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Study of three-particle correlations

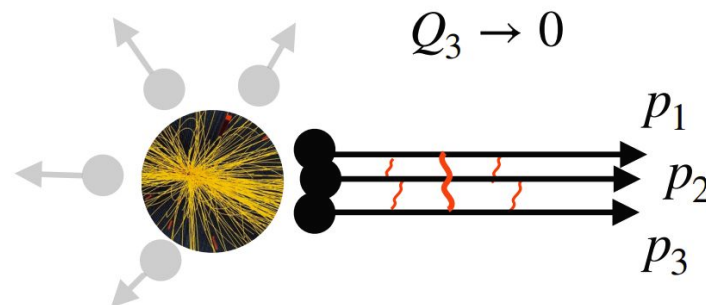
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Three-body femtoscopy

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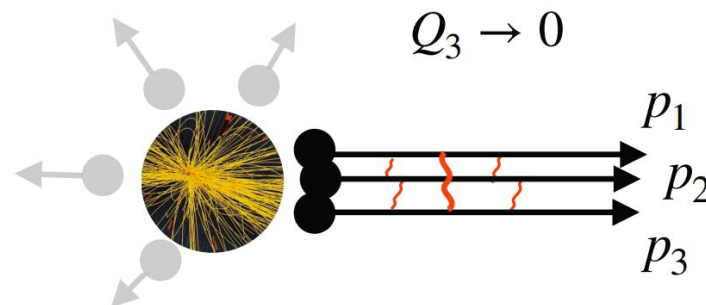
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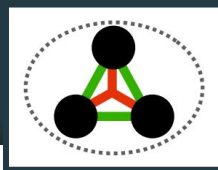
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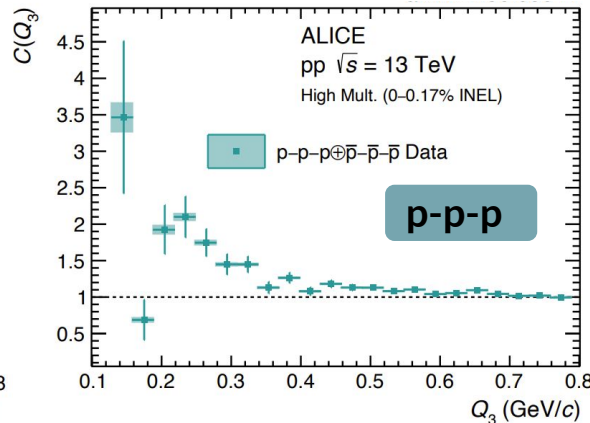
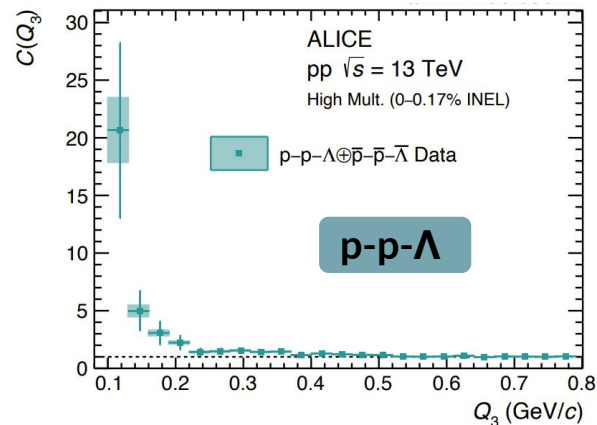
⇒ System studied: **p-p-Λ**, **p-p-p**, **p-p-K⁺**, **p-p-K⁻**



Three-body correlation function



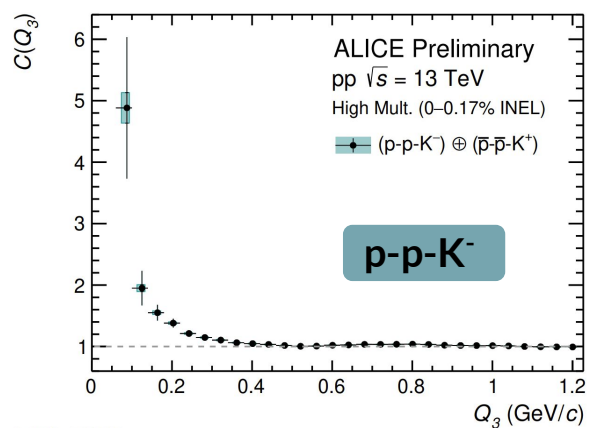
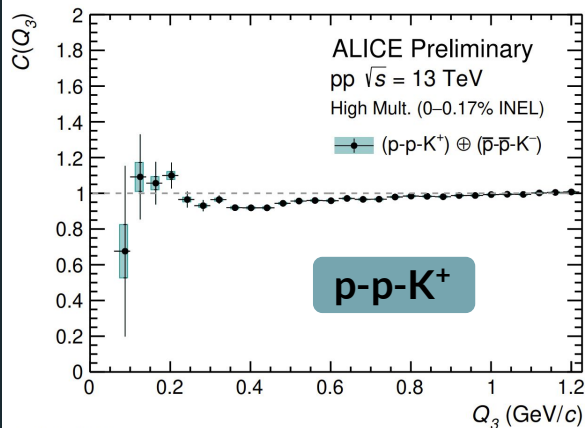
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[ALICE Coll. arXiv:2206.03344 EPJA in press](#)

Data sample: pp 13 TeV Run 2
High-Multiplicity trigger

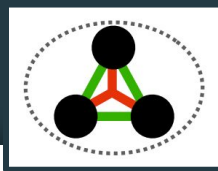
Three-body correlation function:
**Full calculations of a three-body
system are necessary to interpret the
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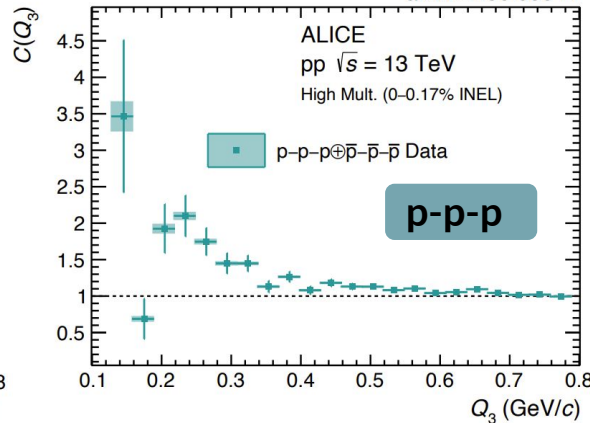
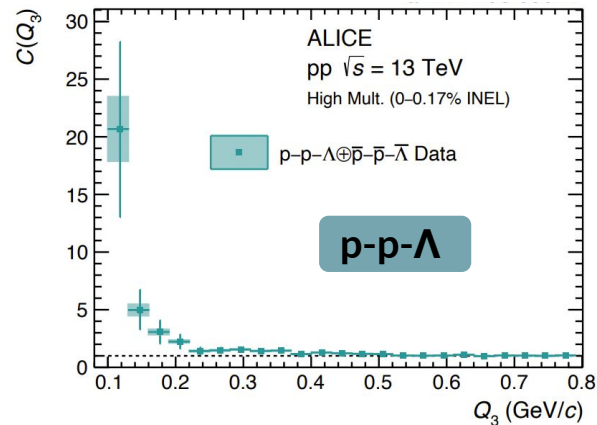
→ First preliminary calculations available
motivated by ALICE data

[A. Kievsky @ EXOTICO workshop](#)

Three-body correlation function



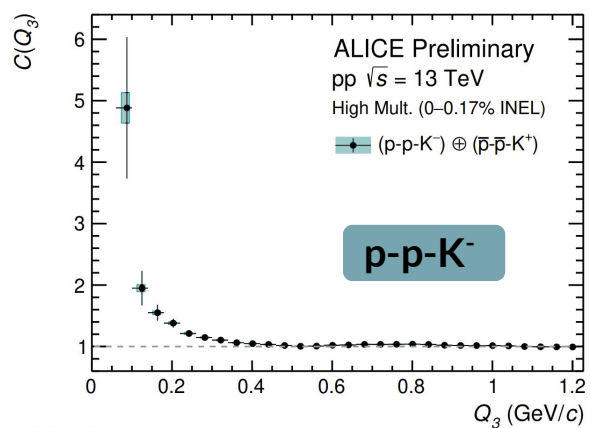
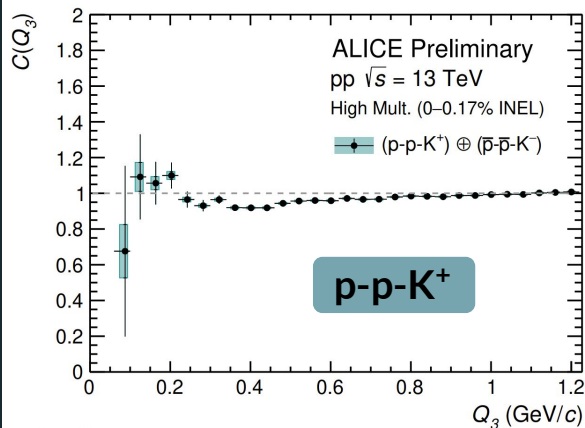
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[ALICE Coll. arXiv:2206.03344 EPJA in press](#)

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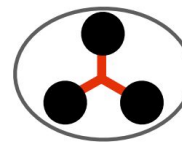


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[A. Kievsy @ EXOTICO workshop](#)



two-body
tree-body



three-body

Isolation of three-body effect: Cumulant

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Genuine three-body
correlations (cumulant)

Measured three-body
correlation function

Lower-order correlations

$$c_3(Q_3) = C(Q_3) - [C_{12}(Q_3) + C_{23}(Q_3) + C_{31}(Q_3) - 2]$$

R. Kubo, J. Phys. Soc. Jpn. 17, 1100 (1962)

Isolation of three-body effect: Cumulant

28

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Measured three-body
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R. Kubo, J. Phys. Soc. Jpn. 17, 1100 (1962)

Two alternative methods to obtain the lower-order correlations

- Projector method: Project into Q_3 via kinematic transformation the measured/theoretical two-particle correlation function Del Grande, Šerkšnytė et al. EPJC 82 (2022) 244
 - measured two-body correlations used for projection
- Data driven approach validates the projector method
 - use of mixed events: two particles from the same event and one particle from a different event

Isolation of three-body effect: Cumulant

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Genuine three-body
correlations (cumulant)

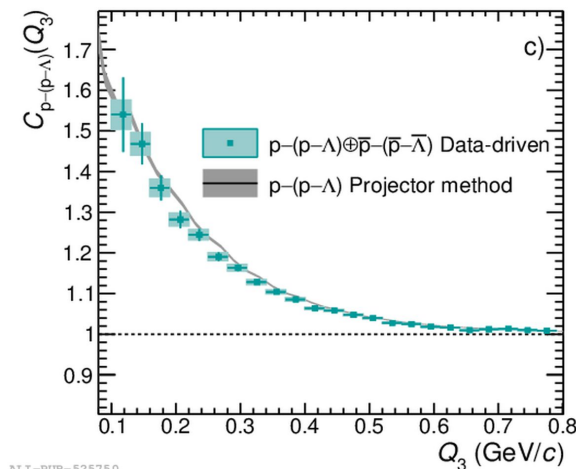
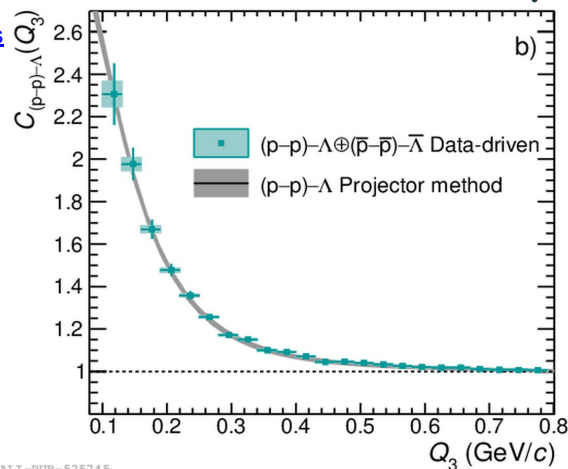
Measured three-body
correlation function

Lower-order correlations

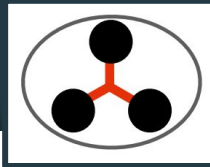
$$c_3(Q_3) = C(Q_3) - [C_{12}(Q_3) + C_{23}(Q_3) + C_{31}(Q_3) - 2]$$

R. Kubo, J. Phys. Soc. Jpn. 17, 1100 (1962)

[ALICE Coll. arXiv:2206.03344 EPJA in press](#)



p-p- Λ cumulant



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Only two identical and charged particles

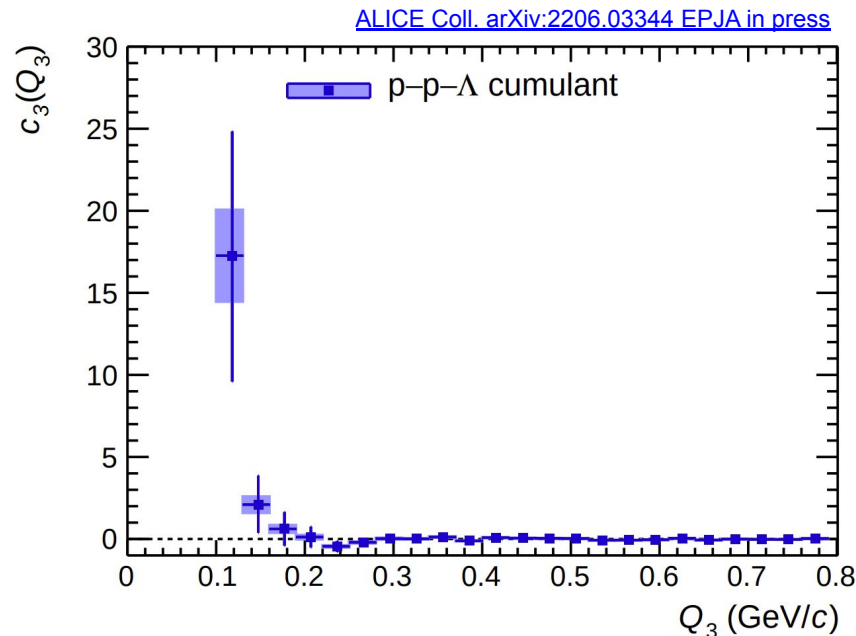
- Main expected contribution from three-body strong interaction
- **Relevant measurement for EoS of NS**

ALICE data: positive cumulant for p-p- Λ

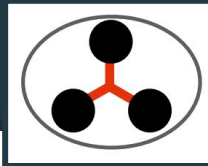
Statistical significance: $n_\sigma = 0.8$ for $Q_3 < 0.4$ GeV/c

⇒ **No significant deviation from null hypothesis.**

Dedicated acquisition trigger in Run 3,
two orders of magnitude gain in statistics expected!



p-p-p cumulant



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Negative cumulant for p-p-p

Statistical significance: $n_\sigma = 6.7$ for $Q_3 < 0.4 \text{ GeV}/c$

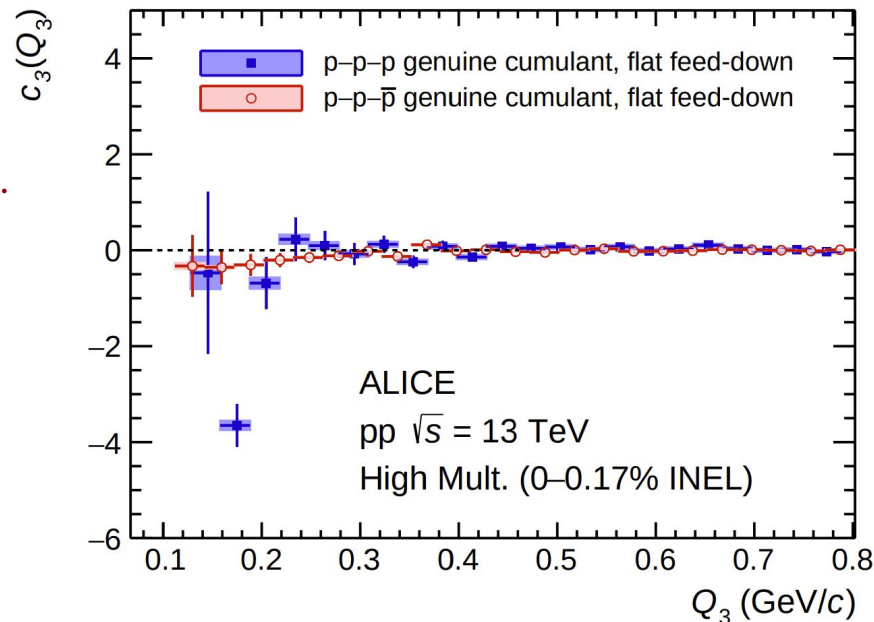
- Test with mixed-charge particles, cumulant negligible.

Effect beyond two-body interactions

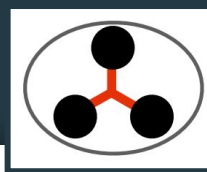
Possible origin:

- Pauli blocking at the three-particle level
- three-body strong interaction
- long-range Coulomb effects

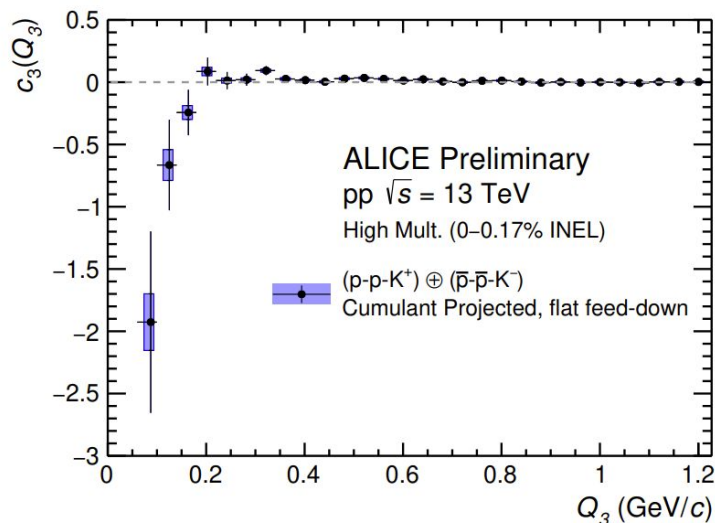
[ALICE Coll. arXiv:2206.03344 EPJA in press](#)



p-p-K⁺ and p-p-K⁻ cumulants



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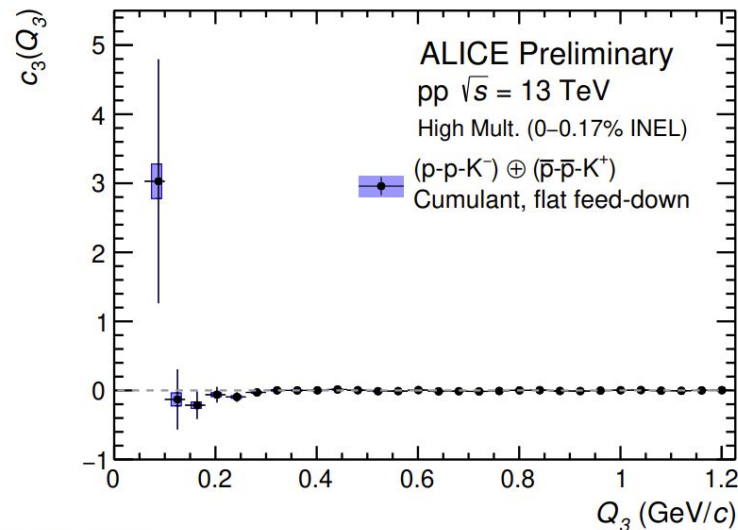


ALI-PREL-513592

Negative cumulant for p-p-K[±]

Compatible with zero within the uncertainties.

Statistical significance: $n_\sigma = 2.3$ for $Q_3 < 0.4$ GeV/c



ALI-PREL-513634

p-p-K⁻ cumulant compatible with zero within uncertainties

⇒ p-p-K⁻ system shows only two-body interactions

⇒ three-body strong interaction might not be relevant in the formation of K⁻barNN nucleus

Conclusions and outlook

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Three-particle systems can be accessed and studied at the LHC in pp collisions by ALICE with a novel technique

Three-body cumulant: first direct measurement of the three-body force using femtoscopy

- p-p-p: negative cumulant with a significance of 6.7σ
- p-p- Λ , p-p- K^+ , p-p- K^- : no evidence of a genuine three-body force

p-d femtoscopy: two hypotheses tested

- Data cannot be described with the assumption of point-like distinguishable particles
- Models considering three-body dynamics with a projection of p-(p-n)

to the p-d state describe qualitatively the data

⇒ Precision studies within reach with the large data samples in Run 3

More statistics = more physics. A $\langle m_T \rangle$ dependent study would enable access to shorter distances for the three-body system in the near future.