

# Quantum Neural Networks force fields generation

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**Keypoint:** We propose a quantum neural network (QNN) for the computation of energy and forces and use it successfully on simple molecules.

**Paper:** Kiss, *et al.*, *Mach. Learn.: Sci. Technol.* **3** 035004 (2022)

# Molecular Force Fields

- 1. Goal:** compute the energy and forces between atoms in a molecule, given its configuration.
- 2. Why:** Being able to run molecular dynamics (MD) by integrating Newton's equations of motion.
- 3. Useful in:** computational physics, chemistry, material sciences, drug design, etc.

# Methods:

- 1. Approximate methods from first principles** (density-functional theory (DFT) or coupled clusters (CC):
  - *precise*
  - *expensive and slow (on the fly)* .
- 2. Machine learning (ML)**
  - trained on DFT or experimental data set
  - *really fast once trained*
- 3. Quantum neural networks:**
  - *seems to be more expressive*

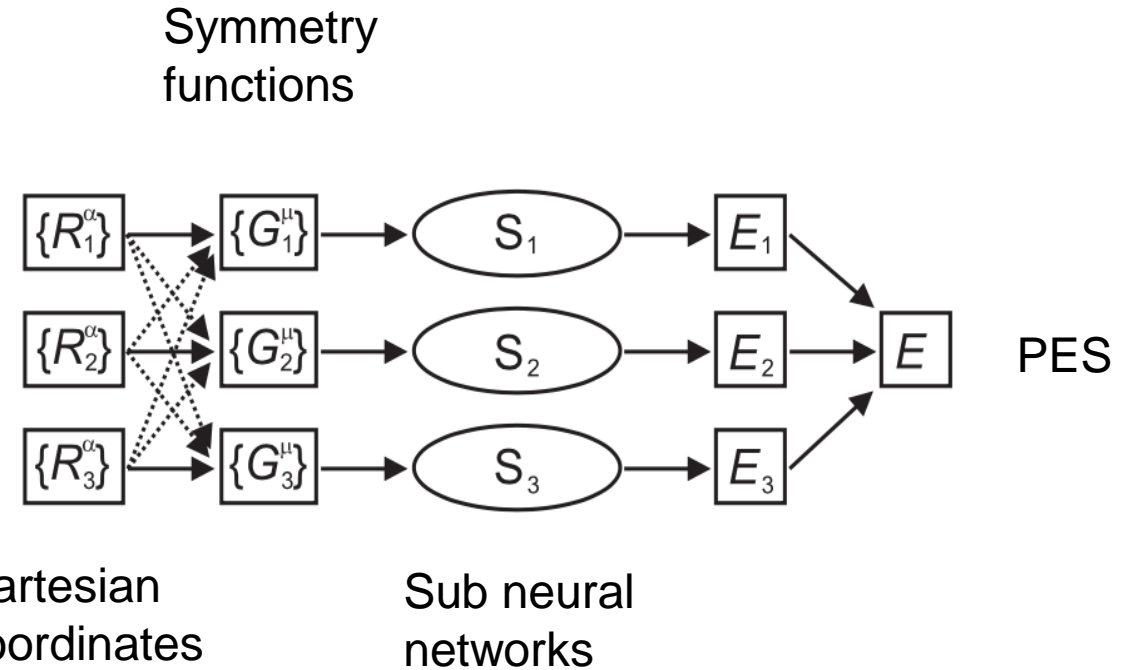
# Classical NNs for Potential Energy Surface (PES) [1]

1. The model should respect the inherent **symmetry** of the system (**rotation**, **translation**, **permutation** of the atoms of the same kind).
2. For every atom, a set of **symmetry functions**  $G_i^\mu$  is constructed from the cartesian coordinates.
3. **Forces** are obtained as negative gradient of the PES:

$$F_{i,j} = -\frac{\partial E}{\partial R_i^j}$$

$$\mathcal{L}(x, \Theta) = \frac{1}{N} \sum_{n=1}^N (E^{(n)} - E_{exact}^{(n)})^2 + \frac{\chi}{3Na} \sum_{n,i,j} (F_{i,j}^{(n)} - F_{exact,i,j}^{(n)})^2$$

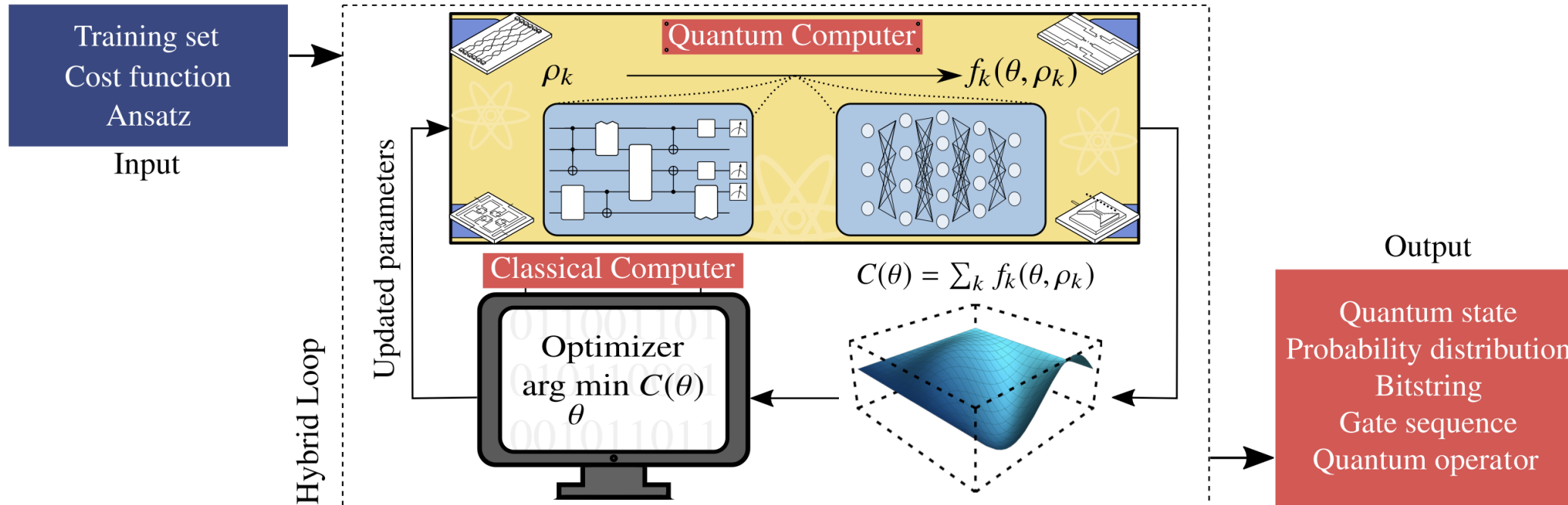
The **loss function** depends in general on both energy and forces.



[1] Jörg Behler and Michele Parrinello. *Generalized Neural-Network Representation of High-Dimensional Potential-Energy Surfaces*. In: Physical Review Letter 98, 146401 (Sept. 2006)

# Quantum machine learning models

Quantum circuits as **heuristic** machine learning models.



Cerezo *et al.*, *Nat Rev Phys* **3**, 625–644 (2021)

# Quantum Neural Networks

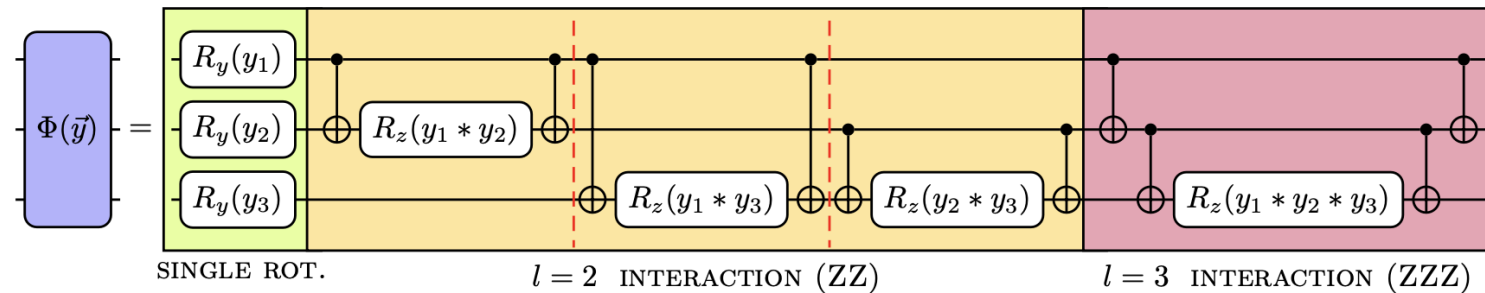
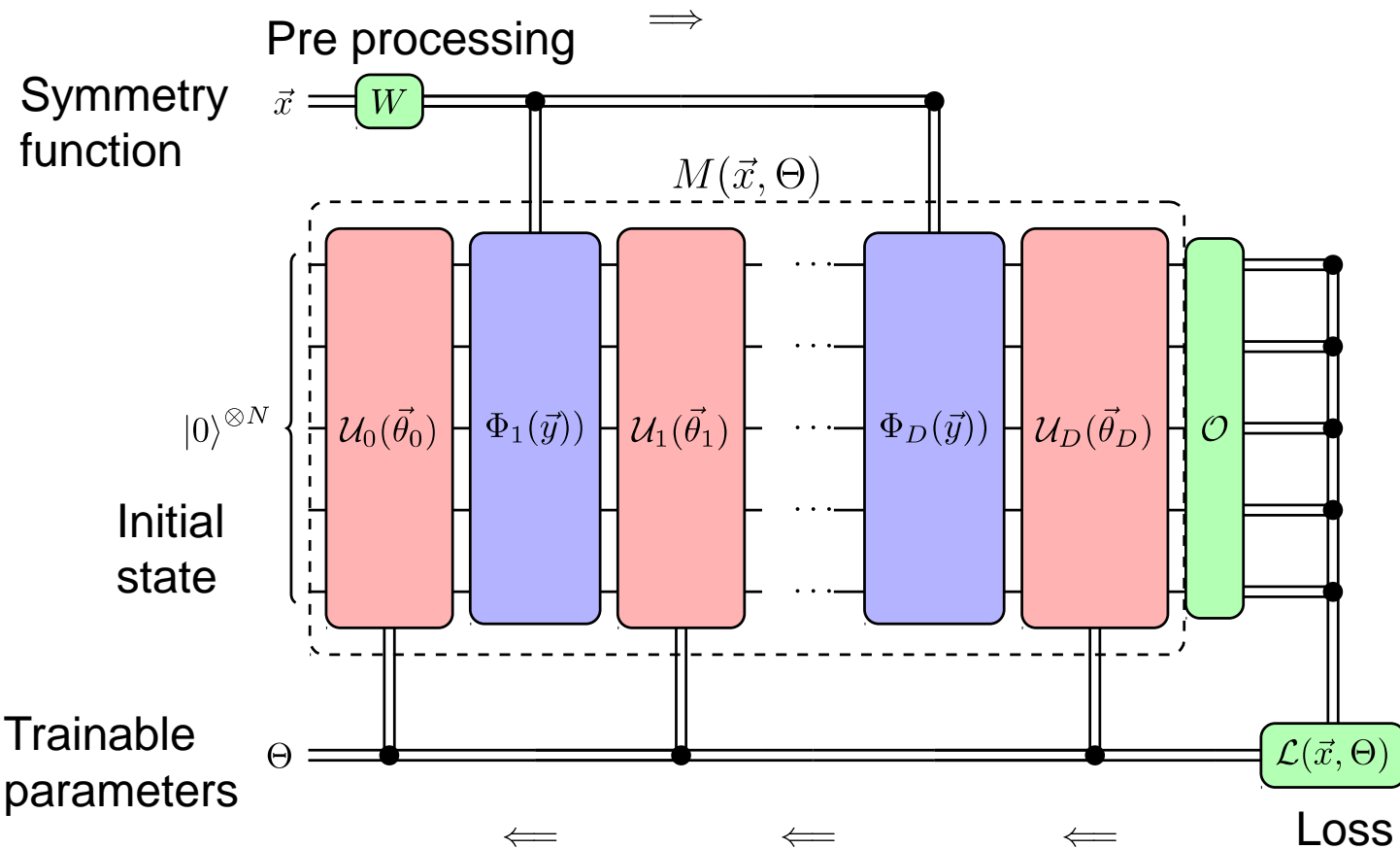
1. QNN:  $f_{\Theta}(x) = \langle 0 | M^\dagger(x, \Theta) \mathcal{O} M(x, \Theta) | 0 \rangle$ ,  
 $M$  is the quantum circuit,  $\mathcal{O} = \sigma_Z^1$ .

2. Partial Fourier series

Schuld, et al., *Phys. Rev. A* **103**, 032430 (2021)

3. **Trainable:** Hardware efficient ansatz.

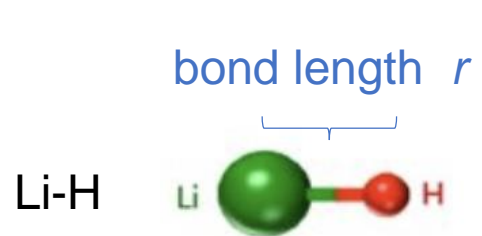
4. Input: classical feature map  $W$  + repeated quantum feature map encoding to increase expressivity.



Kiss, et al., *Mach. Learn.: Sci. Technol.* **3** 035004 (2022)

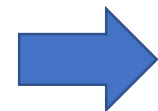
# Application to Force Fields (Chemistry)

Kiss, Tacchino, *et al.*, *Mach. Learn.: Sci. Technol.* **3** 035004 (2022)

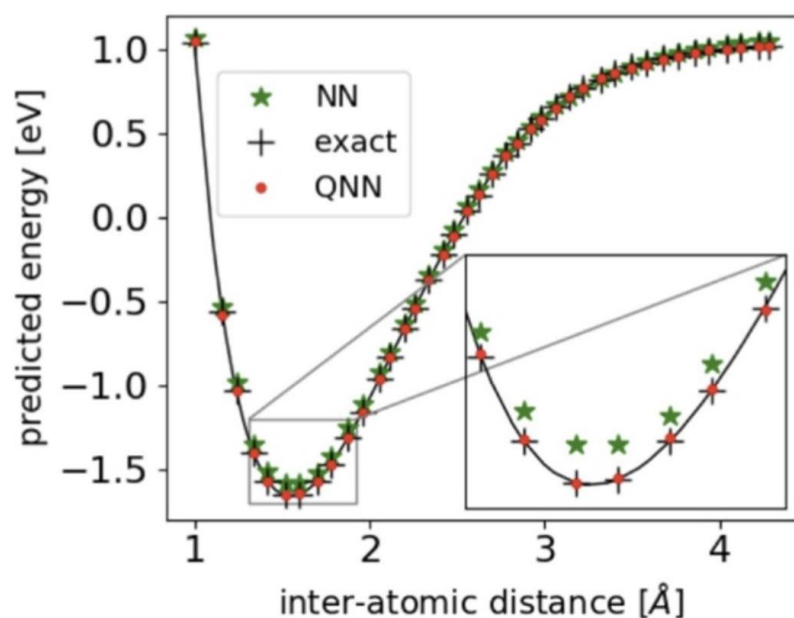


$$W : [-1, 1] \rightarrow [-\pi, \pi]^3$$

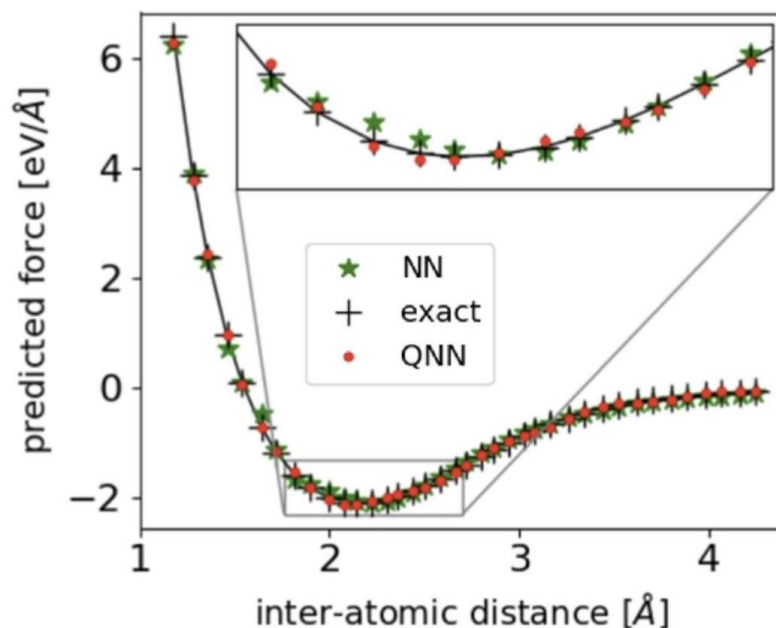
$$r \mapsto \begin{pmatrix} \pi r \\ \arcsin(r) \\ \arccos(r) \end{pmatrix}$$



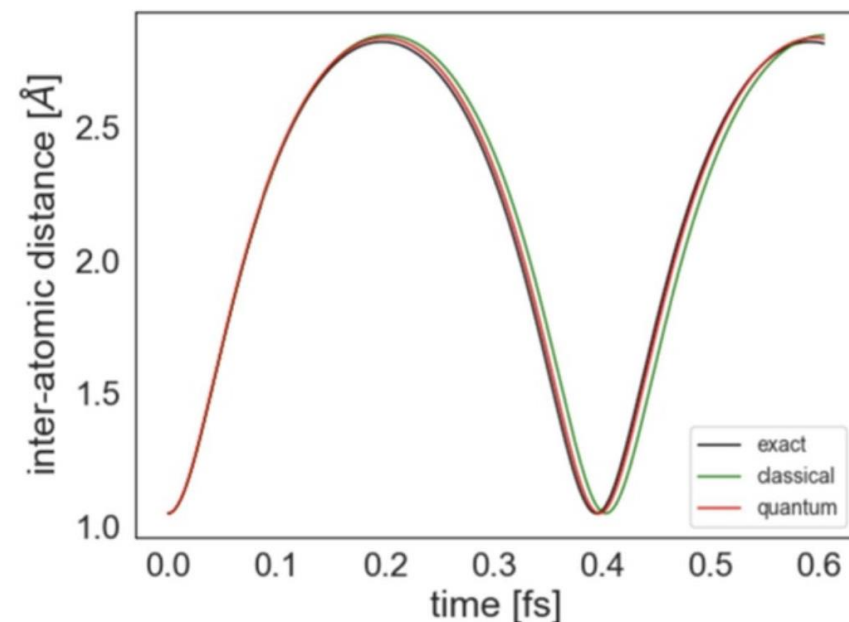
QNN with 10 layers (50 parameters)



(a) LiH Energy



(b) LiH Force



(a) Time evolution of the inter-atomic distance

Comparison with a neural network of equal complexity

$$\vec{F} = -\vec{\nabla}_r E(r)$$

Molecular Dynamics

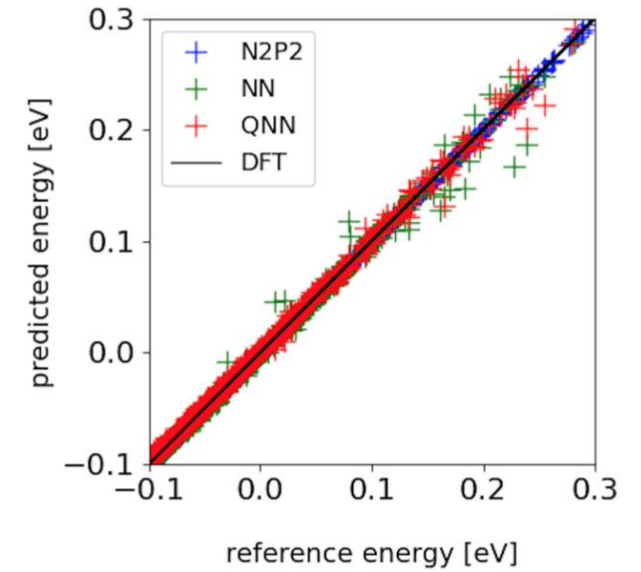
# Triatomic Molecule (H2O)

1. 3 degrees of freedom: 1 angle, 2 bond lengths.
2. **Data Preprocessing:** scale between -1 and 1, apply  $W(x) = \arcsin(x)$ .
3. **Circuit design:**  $N=3$ ,  $D=12$ , full feature map ( $l=3$ ), full trainable feature map ( $l=3$ ).
4. **Optimization:** Cobyala ( $\chi = 1$ ) on 300 data points.

Effective dimension

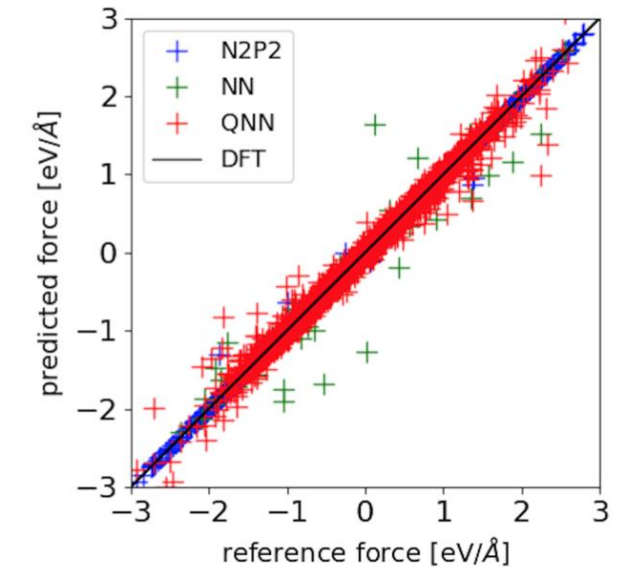
H <sub>2</sub> O	RMSE(E)	RMSE(F)	$d_{300}/d$	d	# params
QNN	0.005	0.06	0.72	87	
NN	0.006	0.1	0.25	87	
n2p2	$7 \times 10^{-4}$	0.01	0.04	1642	

Energy



(a) H<sub>2</sub>O Energy

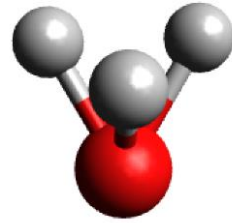
Forces



(b) H<sub>2</sub>O Forces

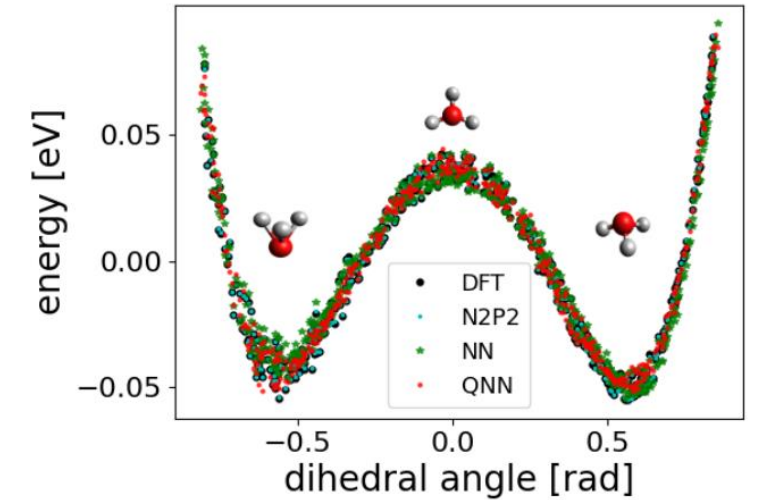
Abbas et al, *the power of quantum neural networks*, In Nat. Comput. Sci Comput. Sci **1** 403–409, (2021)

# Umbrella motion of Hydronium ( $\text{H}_3\text{O}^+$ )

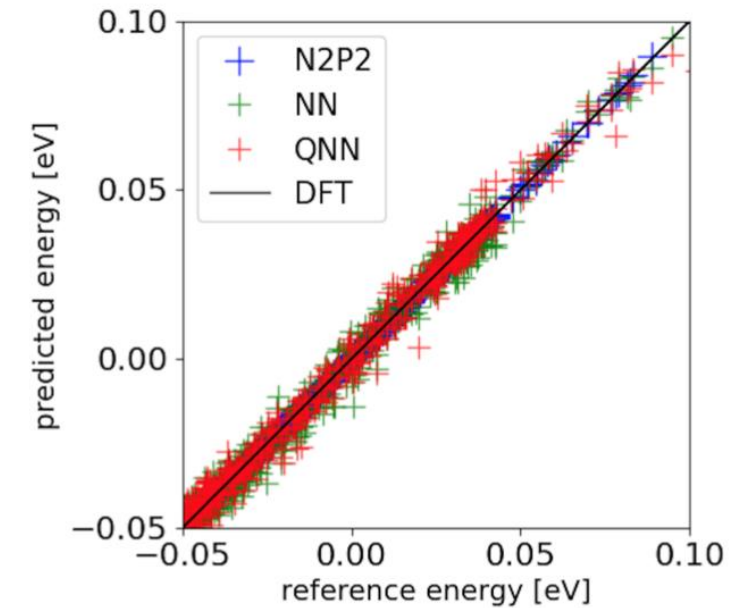


1. **6 degrees of freedom:** 1 dihedral angle, 2 angle, 3 bond lengths.
2. **Data Preprocessing:** scale between -1 and 1, apply  $W(x) = \arcsin(x)$ .
3. **Circuit design:**  $N=6$ ,  $D=10$ , linear feature map ( $l=3$ ), linear trainable feature map ( $l=3$ ).
4. **Optimization:** ADAM ( $\chi = 0$ ) on 500 data points.

$\text{H}_3\text{O}^+$	RMSE(E)	RMSE(F)	$d_{500}/d$	$d$
QNN	$3.7 \times 10^{-3}$	0.26	0.67	135
NN	$4.2 \times 10^{-3}$	0.207	0.19	135
N2P2	$5 \times 10^{-4}$	0.19	0.03	2214



(a)  $\text{H}_3\text{O}$  Energy



(b)  $\text{H}_3\text{O}$  Energy



# Conclusions, potential advantages & outlook

1. QNNs are able to compete with **similar neural networks** in the task of learning PES and force fields.
2. Potential quantum advantages are primarily linked to **the better expressivity and higher effective dimension** of QNNs with respect to classical counterparts.
3. **Future work:**
  - More complex architectures (**quantum convolutional NN**) or **equivariant QNN**.
  - Work with **quantum data** (from dynamical VQA).
  - Incorporate fragmentation techniques.

# Thank you for your attention!

## Questions?

Kiss, Tacchino, *et al.*, *Mach. Learn.: Sci. Technol.* **3** 035004 (2022)

Jörg Behler and Michele Parrinello. : *Physical Review Letter* 98, 146401 (2006)

Schuld *et al.*, *Phys. Rev. A* **103**, 032430 (2021)

Abbas *et al.*, *In Nat. Comput. Sci* **1** 403–409, (2021)



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