
Practical Quantum Computing with Trapped Ions

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Duke Quantum Center



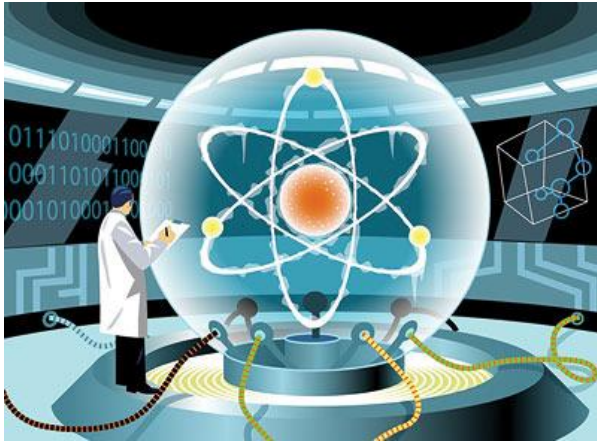
Computation in Sciences

- What was science like before computers were available?
- Computation has made a huge impact in ALL scientific disciplines
 - Computational Physics, Computational Chemistry, Systems Biology
 - Numerical simulation and CAD in vast areas of science and engineering
 - Expanding to machine learning and AI, impacting in all areas of society
- Development of new computational methods vs advanced hardware
 - Progress in HW is critical in the early days to get ideas flowing
 - Methods development accelerates the impact faster than new HW

New science is enabled by computational technology!!

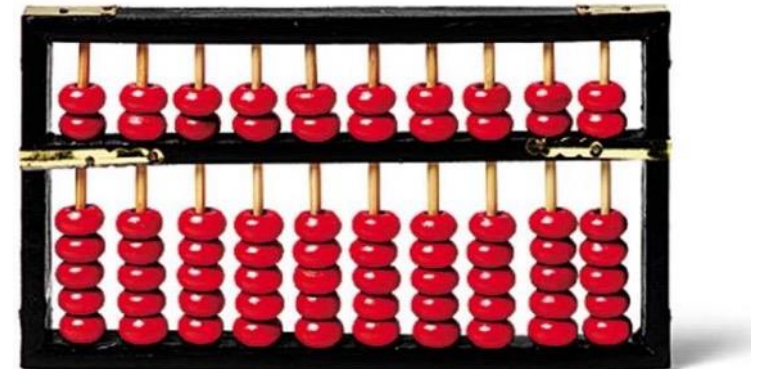
What is a Quantum Computer?

“A quantum computer differs more from a classical computer.....

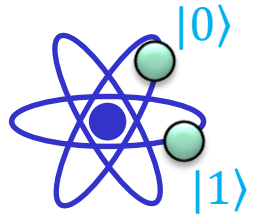


...than a classical computer differs from an **ABACUS**”

William Phillips
1997 Nobel Laureate

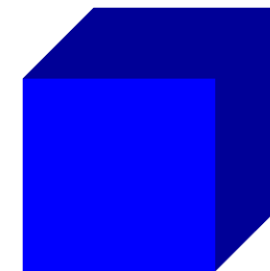
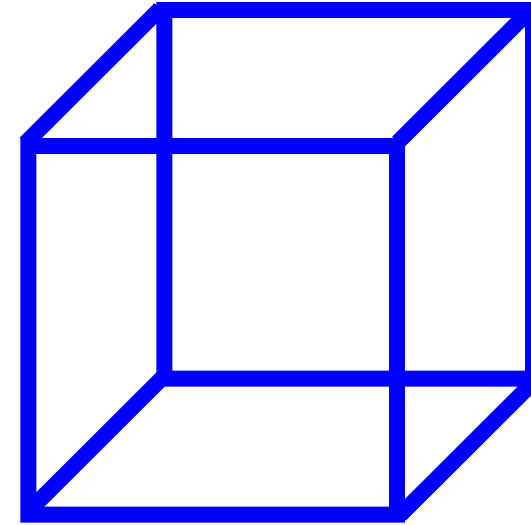


Critical Quantum Feature I: Superposition

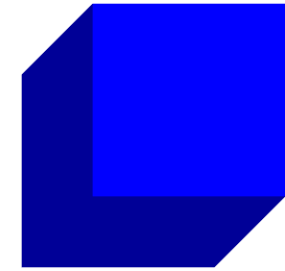


A classical bit: 0 or 1

qubit: $|\psi\rangle = a|0\rangle + b|1\rangle$

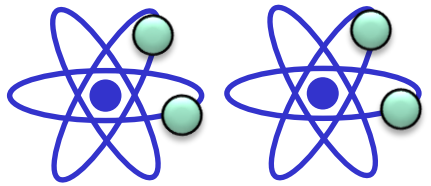


$|0\rangle$



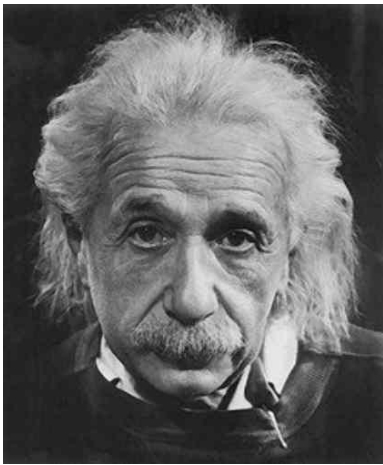
$|1\rangle$

Critical Quantum Feature II: Entanglement

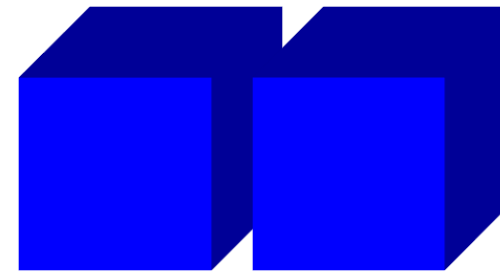
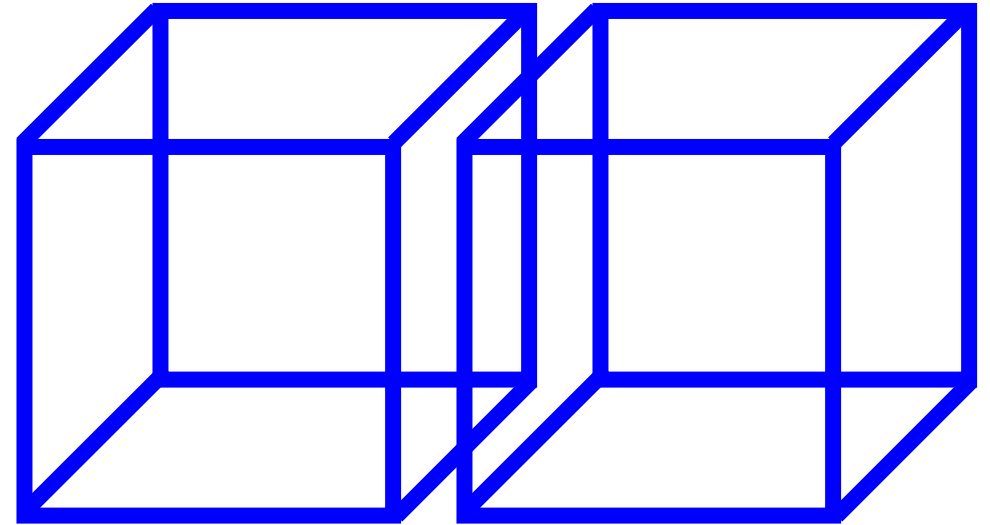


qubits: $|\psi\rangle = a|00\rangle + b|11\rangle$

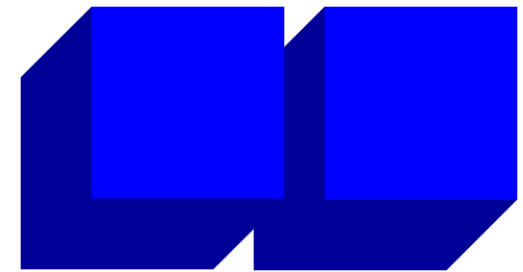
“spooky action-at-a-distance”
(A. Einstein)



entanglement: “wiring *without wires*”



$|0\rangle|0\rangle$

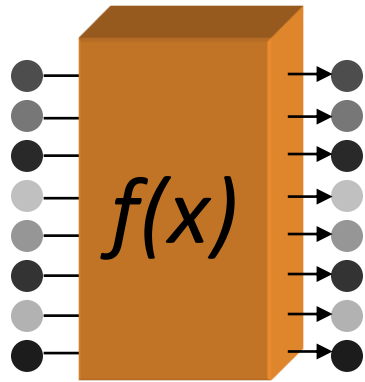


$|1\rangle|1\rangle$

GOOD NEWS...

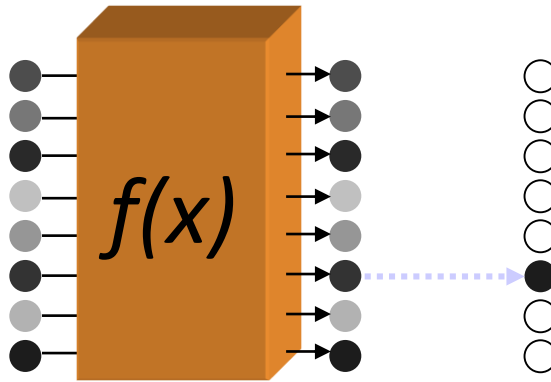
parallel processing
on 2^N inputs

e.g., $N=3$ qubits



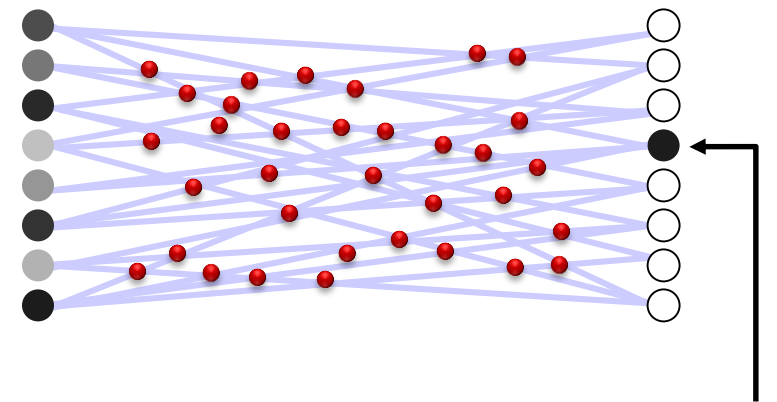
...BAD NEWS...

measurement gives
random result



...GOOD NEWS!

quantum interference



$$a_0|000\rangle + a_1|001\rangle + a_2|010\rangle + a_3|011\rangle \\ a_4|100\rangle + a_5|101\rangle + a_6|110\rangle + a_7|111\rangle$$

*$N=300$ qubits have more configurations
than there are particles in the universe!*



David Deutsch
(early 1990s)

depends on
all inputs

Application: Factoring Numbers

A quantum computer can factor numbers
exponentially faster than classical computers

$$39 = 3 \times 13 \text{ (...easy)}$$

$$38647884621009387621432325631 = ? \times ?$$



Key
generation

$$n = P * Q$$
$$d * e = 1 \bmod \Phi(n)$$

Encryption

$$c = m^e \bmod n$$

Public Key(n,e)

Decryption

$$m = c^d \bmod n$$

private key (d)

Physics of Trapped Ion Quantum Computing

Search for The “Perfect Qubit”?

- What is a good criteria for defining a “Perfect Qubit”?

$$|\psi\rangle = e^{i\gamma} \left(\cos \frac{\theta}{2} |0\rangle + e^{i(\omega t + \varphi)} \sin \frac{\theta}{2} |1\rangle \right)$$

$$T_1 = \infty$$

Zero Decay Errors

For hyperfine ground state of H,
the spontaneous transition rate
is estimated to be
 2.9×10^{-15} per second, or
1 per 11 million years

$$T_2 = \infty$$

Zero Dephasing Errors

For hyperfine ground state of Cs
Cs ν_{HF} = 9 192 631 770 Hz (EXACT!!)

- $T_2 \approx 1$ sec baseline (Olmschenk et al., PRA 76, 052314, 2007)
- $T_2 \approx 5500$ sec (P. Wang et al., Nature Comm. 12, 233, 2021)

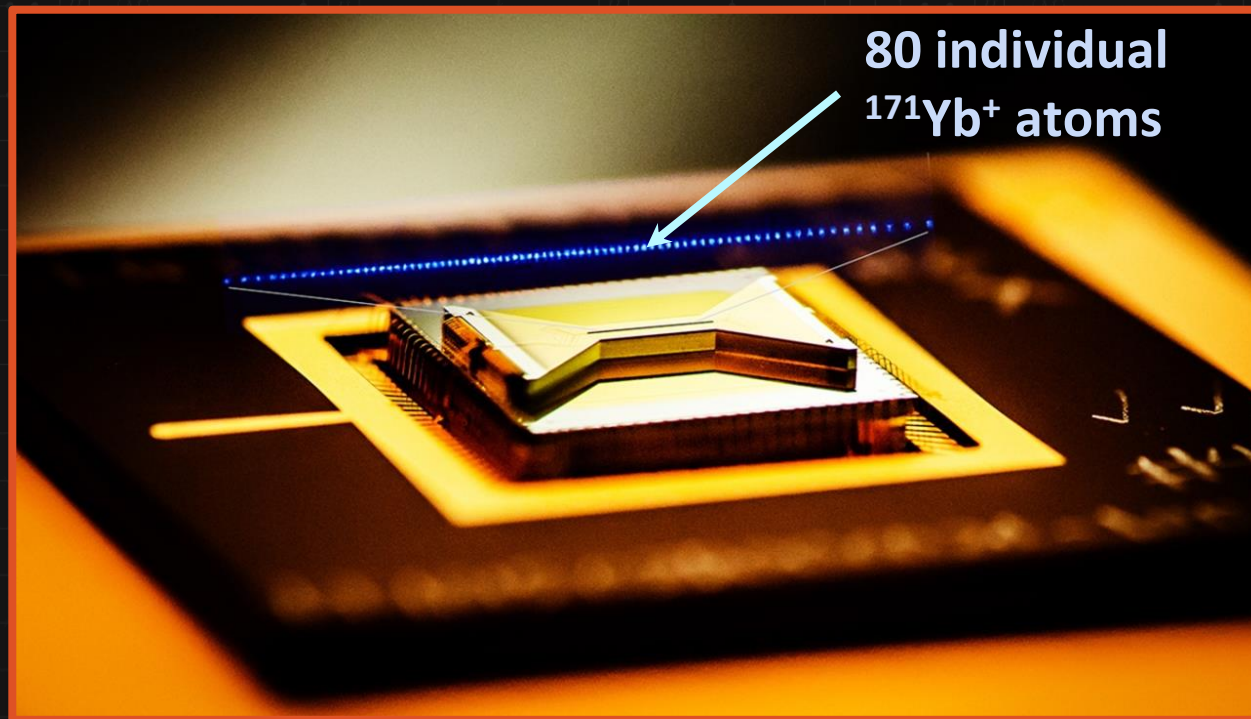
Hyperfine Ground State of an Atom is an ideal choice

Trapped Ion Hyperfine Qubit: $^{171}\text{Yb}^+$

- Qubit initialization by **optical pumping**:
 - Very high fidelity (**error $\sim 10^{-6}$**) limited by off-resonant scattering
- Qubit Measurement by **resonance fluorescence**:
 - High fidelity (**$\sim 10^{-3}$ - 10^{-4}**) limited by off-resonant scattering, dark counts
- Single-qubit gates by **off-resonant Raman transitions**:
 - Very high fidelity (**$\sim 10^{-4}$ - 10^{-5}**) limited by spontaneous emission, laser noise
- Two-qubit gates by **state-dependent force from Raman transitions**:
 - High fidelity (**$\sim 10^{-3}$ - 10^{-5}**) limited by spontaneous emission, laser noise



IONQ Qubit Technology



Sandia
National
Laboratories

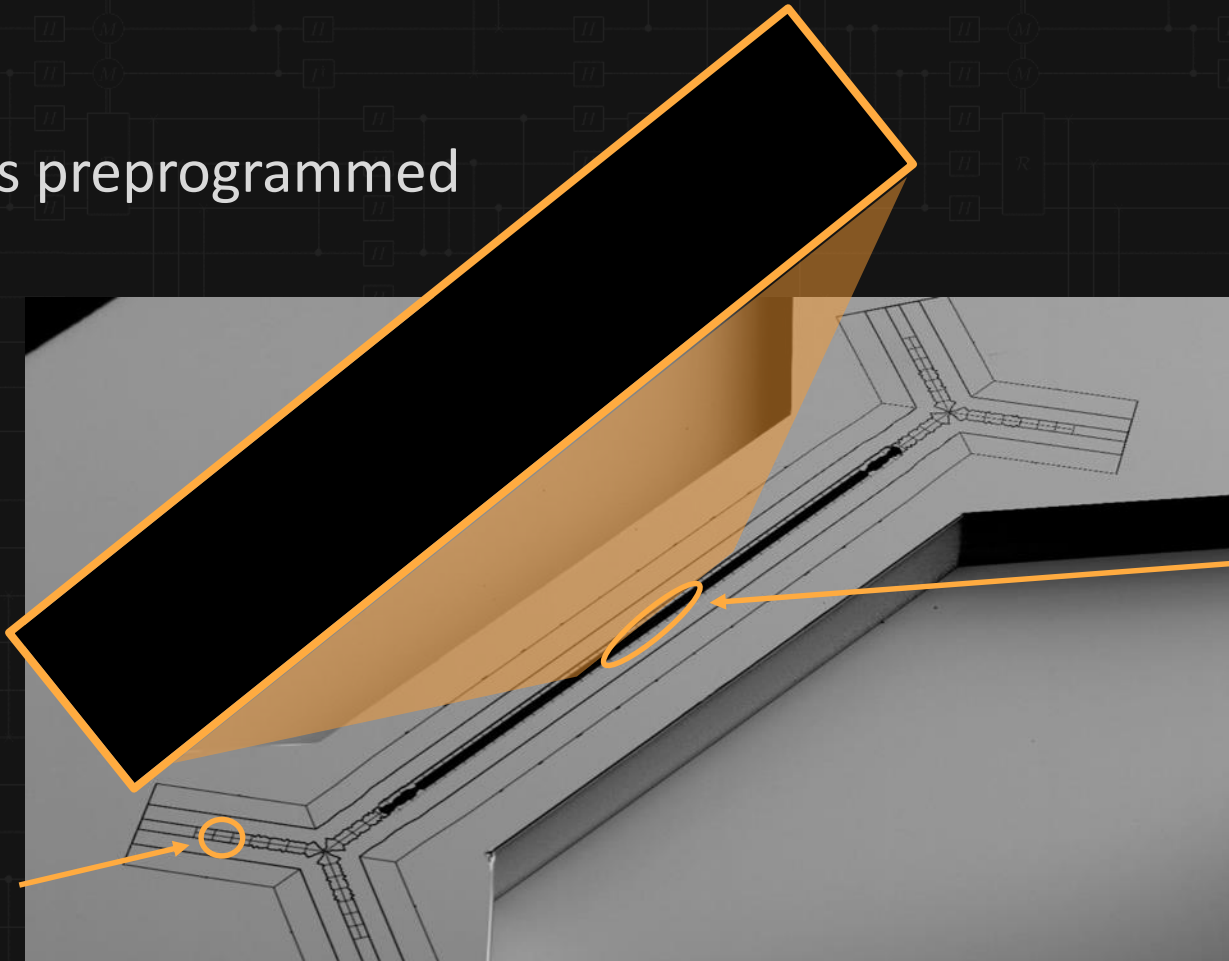
Based on Individual Atoms, with Fully Flexible Control



IONQ Autoloading Register

N=23 qubits preprogrammed

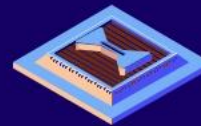
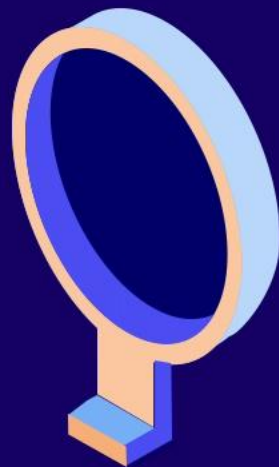
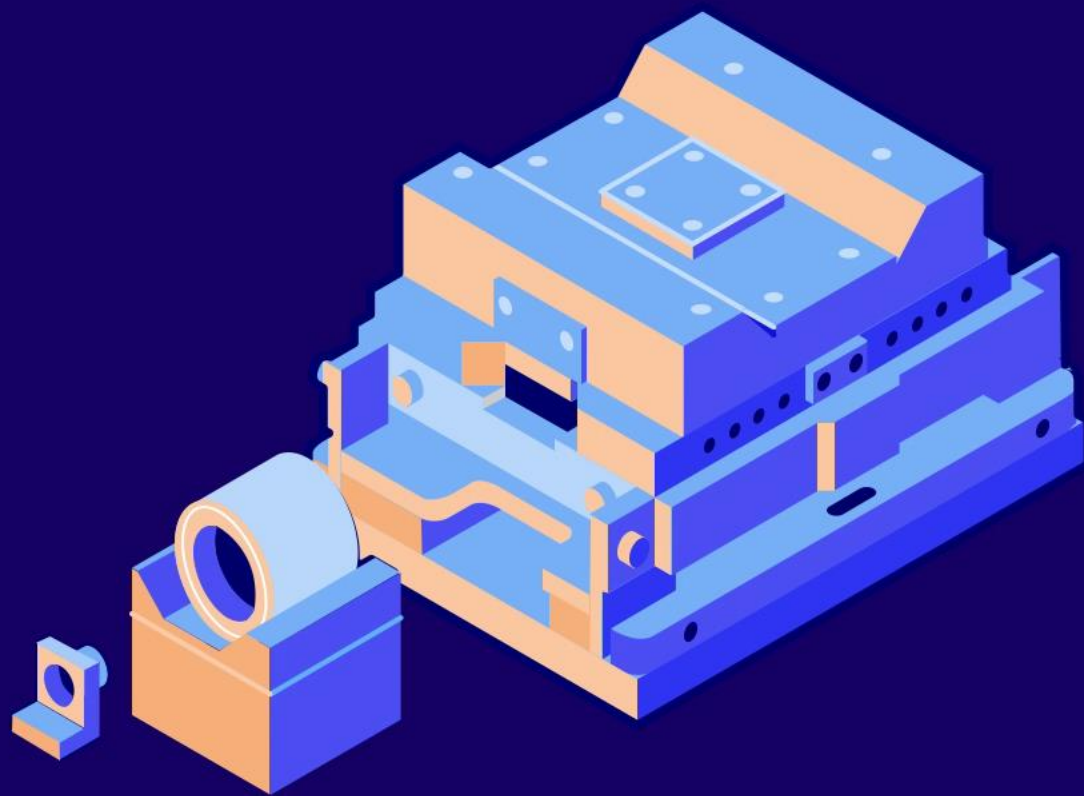
Loading
zone



Quantum
Computing
zone



Quantum Computer Module



Plenty of Room for New Physics

- Errors are dominated by systematic and control errors
 - Innovation in coherent control and error mitigation techniques
 - Robust hardware designs can reduce or eliminate most of these errors
- Error cancellation at the circuit level
- Multi-qubit entangling gates
- Nifty crosstalk cancellation techniques
- Gate performance maintained at dozens of qubits

All In Software!!

Quantum Computer for Users



Useful Near-Term Quantum Algorithms

- **Quantum Machine Learning (QML):** Quantum advantages proven for
Learning complex patterns w/ quantum feature maps (arXiv:2010.02174)
Exponential gain in predicting certain worst-case error (arXiv:2101.02464)
Quantum correlations used in generative modeling (arXiv:2101.08354)
- **Quantum Chemistry and Materials Studies**
Variational quantum eigensolvers (VQE) for energy estimation
Quantum simulation of dynamics of excitation
Study of quantum many-body phenomena
- **Optimization Problems:** Quantum Approximate Optimization Algorithm

QML Example: Nearest Centroid Classifier

Data Set



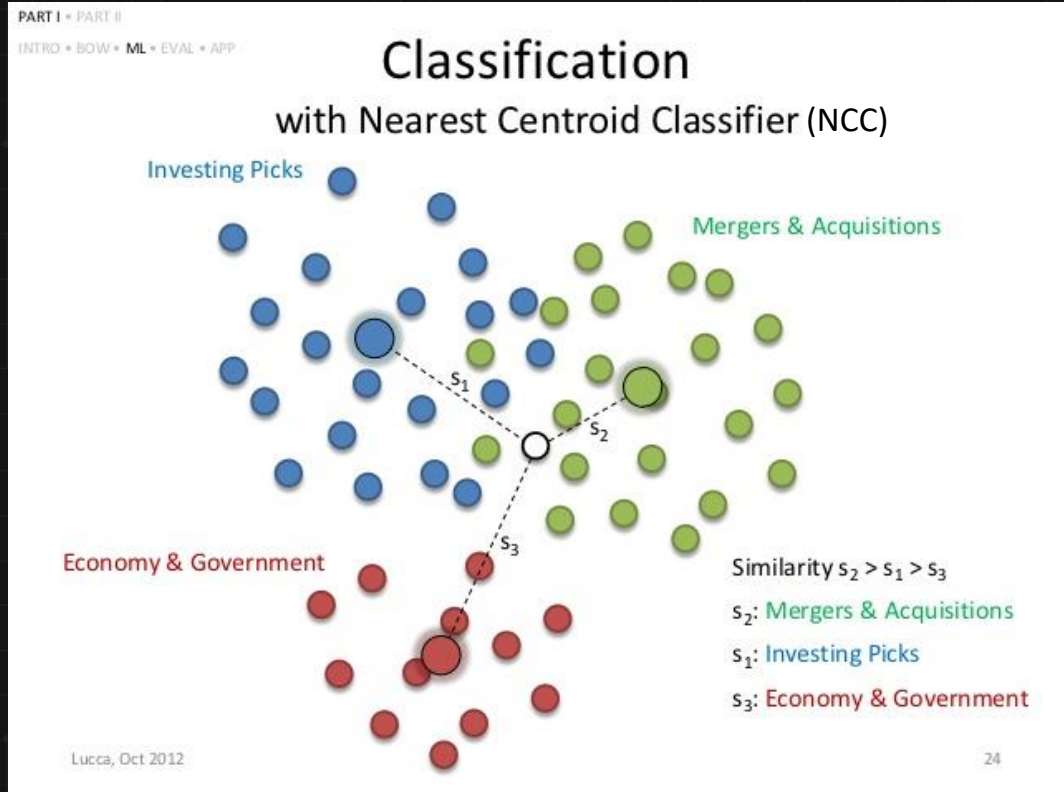
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3
4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5
6	6	6	6	6	6	6	6	6	6	6	6	6	6	6	6
7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7
8	8	8	8	8	8	8	8	8	8	8	8	8	8	8	8
9	9	9	9	9	9	9	9	9	9	9	9	9	9	9	9

Fit your model:
Find centroids of
each class of training data

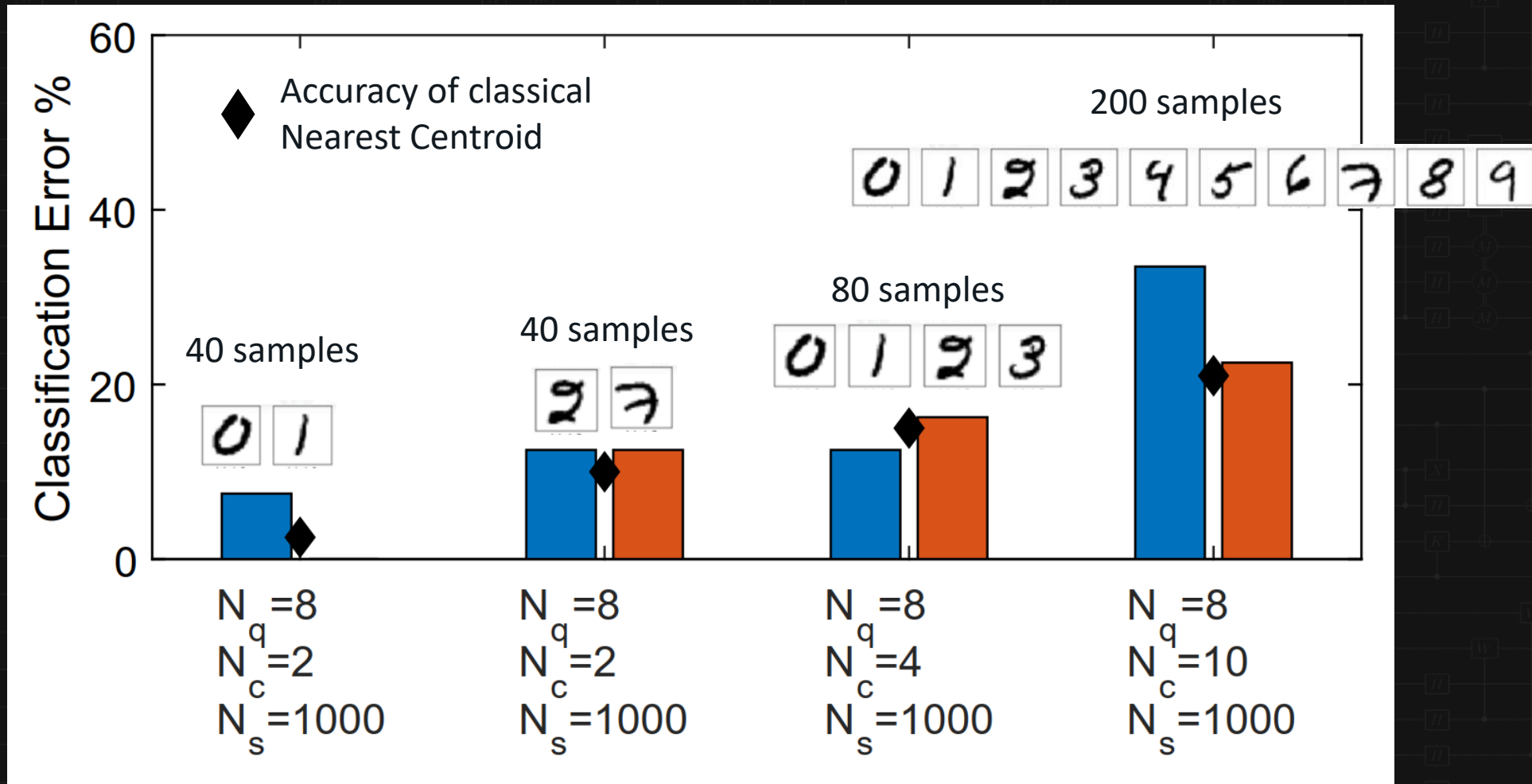


Predict labels of new data:
Compute distance to centroids
QUANTUMLY to assign labels
of the nearest centroid

Classification Model

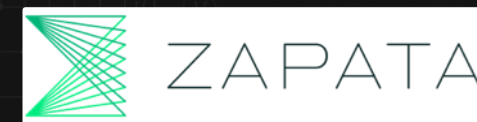
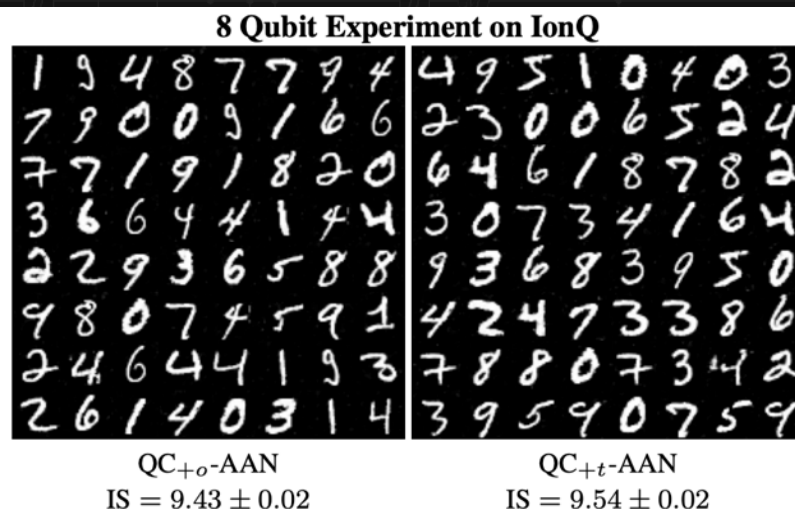
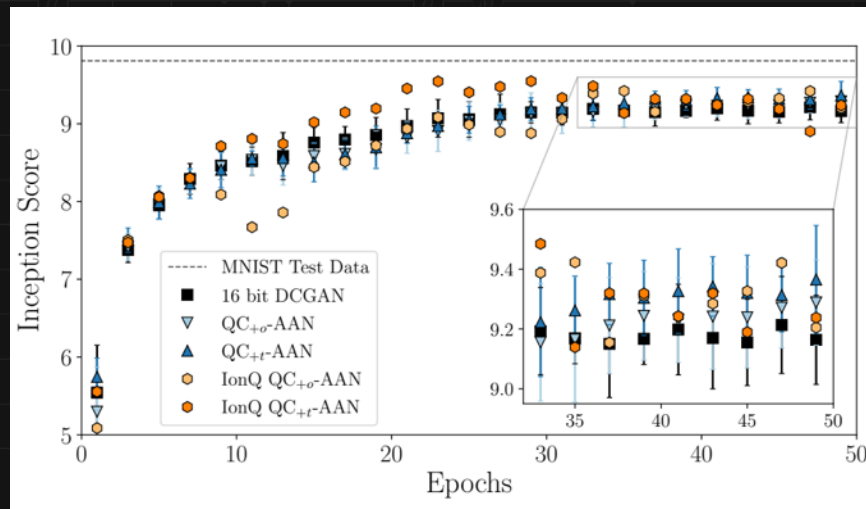


QML NCC: MNIST Database on 8 Qubits



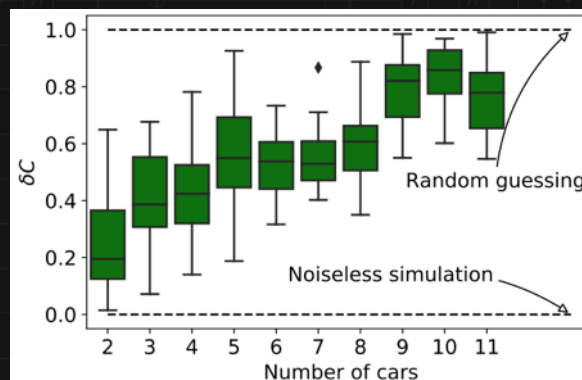
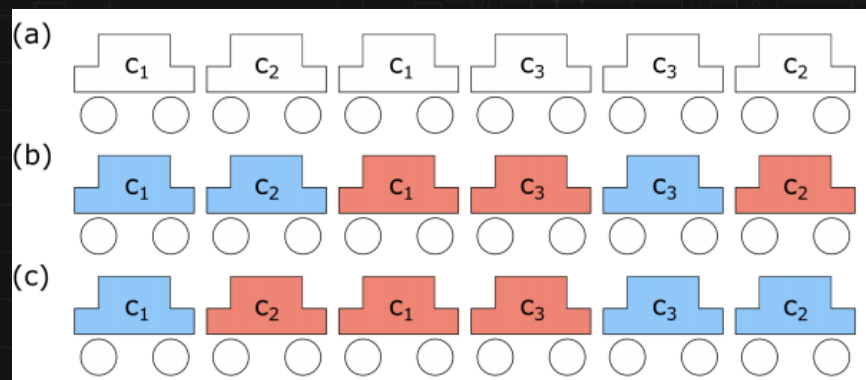
Other Examples

- Generating high-resolution handwritten digits



M. S. Rudolph et al.,
arXiv:2012.03924 (2020)

- Binary Paint Shop problem with QAOA

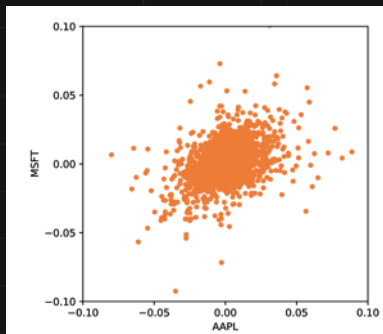


M. Streif et al.,
arXiv:2011.03403 (2020)

Joint Probability Distribution: Copula

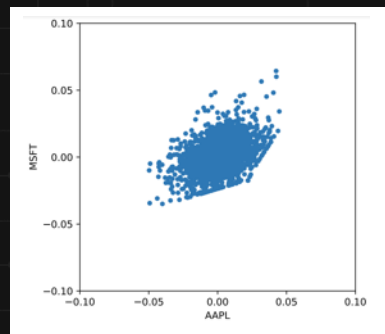
- Ion trap quantum computers are used to explore **Multi-variate machine learning techniques** using copulas
- **More efficient training** and Accurate models that capture outliers

Target Distribution



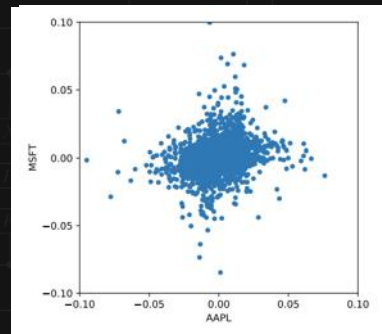
From training data

Classical GAN



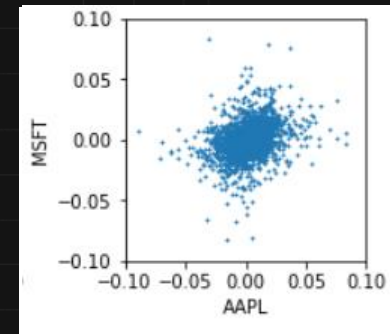
After 20,000 Iterations

Quantum GAN



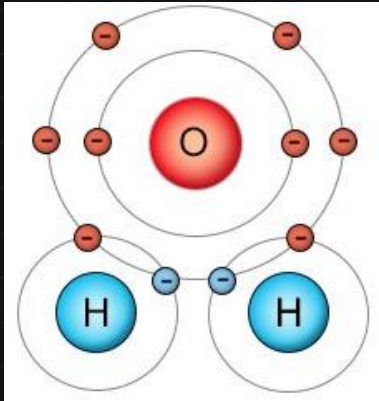
After 1,000 Iterations

Quantum CBM

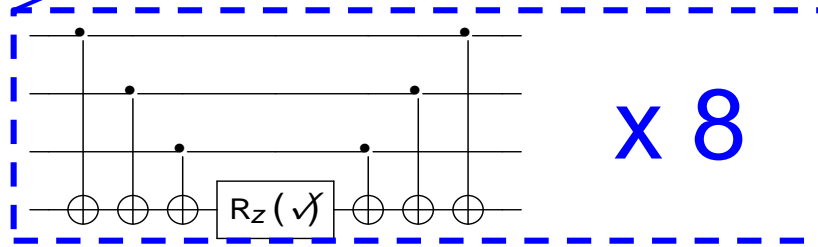


After 26 Iterations

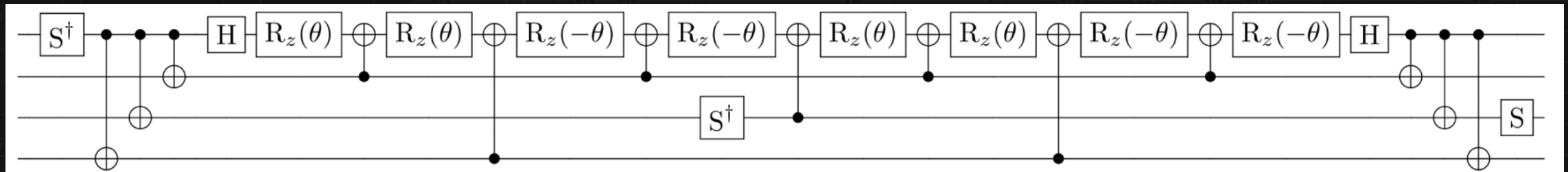
Quantum Chemistry Example: VQE



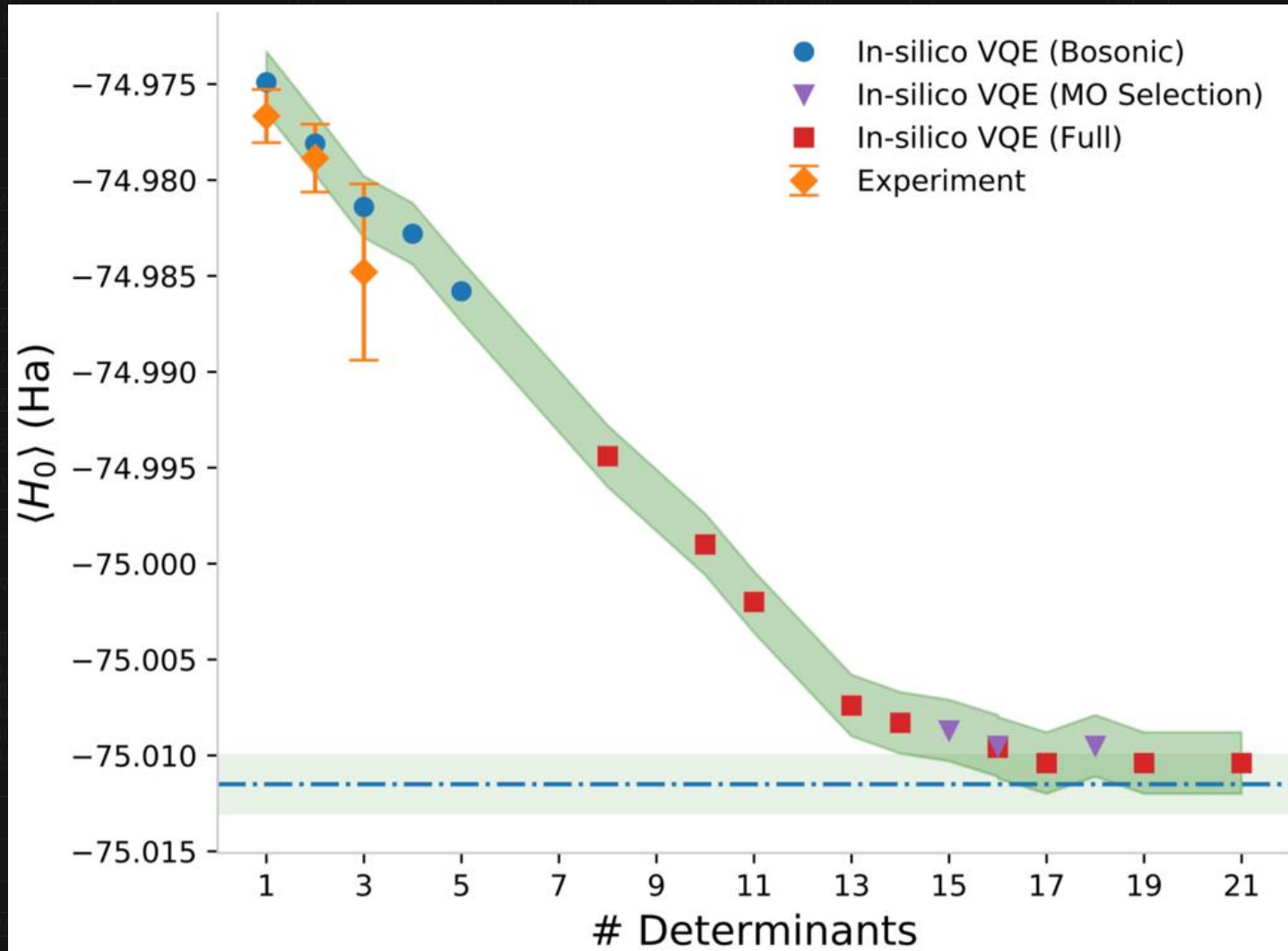
$$\hat{H} = \sum_{p,q} h_{pq} c_p^\dagger c_q + \sum_{p,q,r,s} h_{pqrs} c_p^\dagger c_q^\dagger c_r c_s$$



Order of Approx.	Naïve		Optimized		Binding Energy (Hartrees)
	qubits	gates	qubits	gates	
Baseline					-74.9624
+1 term	4	40	2	2	-74.9749
+2 terms	4	80	2	2	-74.9781
+3 terms	8	112	4	6	-74.9804
+4 terms	8	144	4	8	-74.9828
+5 terms	10	232	5	10	-74.9858
+8 terms	10	264	10	60	-74.9944
+10 terms	10	348	10	84	-74.9990
+11 terms	10	532	10	92	-75.0020
+13 terms	10	596	10	116	-75.0074
+15 terms	10	648	10	136	-75.0087
+19 terms	12	730	11	157	-75.0104
+21 terms	12	800	11	178	-75.0104
EXACT:					-75.0116



Quantum Chemistry Example: VQE



Order of Approx.	Naïve		Optimized		Binding Energy (Hartrees)
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+19 terms	12	730	11	157	-75.0104
+21 terms	12	800	11	178	-75.0104
EXACT:					-75.0116

Summary and Conclusion

- Quantum computers provide **fundamentally new way of computation**
 - Started out in Physics, transitioning into technology, **FAST**
 - New types of algorithms enable new types of applications
- Availability of **fully-connected programmable quantum computers**
 - Provides a testing ground for novel quantum algorithms
 - Continued performance scaling is key to enabling new approaches to challenging problems
- Progress in **QML, quantum chemistry and QAOA** algorithms
 - Optimization for hardware provide performance improvements
- Opportunities to explore and enable **new approaches computational sciences**

Team and Collaboration

- **Duke Team**
 Peter Maunz
 Taehyun Kim
 So-Young Baek
 Kai Hudek
 Caleb Knoernschild
 Kyle McKay
 Andre van Rynbach
 Emily Mount
 Daniel Gaultney
 Muhammed Ahsan
 Rachel Noek
 Stephen Crain
 Geert Vrijsen
 Volkan Inlek
 Ye Wang
 Junki Kim
 Yuhi Aikyo
 Clinton Cahall
 Chao Fang
 Robert "Tripp" Spivey
 George Schwartz
 Ke Sun
 Jacob Whitlow
 Ely Novakoski
- **Ken Brown Group (Duke)**
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 True Merrill
 Yu Tomita
 Michael Newman
 Jyothi Saraladevi
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 Mark Kuzyk
 Leo
 Natalie Brown
 Dripto Debroy
 Gloria Jia
 James Leung
 Muyuan Li
 Bichen Zhang
 Shilin Huang
 Omid Khosravani
 Evan Reed
 Eric
 Brad Bondurant
 Swanadeep Majumder
 Phoebe Chen
 Samuel Phiri
 Leon
- **University of Maryland**
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 Jonathan Mizrahi
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 Norbert Linke
 Ken Wright
 Shantanu Debnath
 Kale Johnson
 David Wong-Campos
 David Hucul
 Volkan Inlek
 Aaron Lee
 Kristi Beck
 Marko Cetina
 Michael Goldman
 Kevin Landsman
 Andrew
 Laird Egan
 Daiwei Zhu
- **Harris Corporation**
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 Randy Morse
 Lee Burberry
 Chris Corey
- **AOSense**
 Martin Boyd
 Scott Sullivan
 Jamil Abo-Shaeer
- **Sandia National Labs**
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 Christian Arrington
 Drew Hollowell
- **ColdQuanta, Inc.**
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 Alex Kato
 Evan Selim
- **NIST**
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 Sae Woo Nam
 Varun Verma
 Kyle McKay
 Dustin Hite
- **JPL**
 Matthew Shaw
 Francesco Marsili
 Emma Wollman