

UNIVERSITÀ DEGLI STUDI DI MILANO $\frac{1}{49} \quad V_{II} \quad \frac{1}{50} \quad \frac{1}{50} \quad V_{II} \quad \frac{1}{50} \quad$ Exact mixed NNLO OCE-EW corrections The tothe Neutral Current Dreil-Yah process U 197 U 65 98 U 55 99 U 55 90 HALESSANCION CHANNEL OF THE OFFICE OF University of Milano, INFN Milano $g_{2} = 10$ LoopFest 2022, May 12th 2022 g = 230 g = $\begin{array}{c} g \\ W \\ \psi \\ 241 \end{array} \\ \begin{array}{c} 242 \\ 242 \end{array} \\ \begin{array}{c} 242 \\ 242 \end{array} \\ \begin{array}{c} 242 \\ 243 \end{array} \\ \begin{array}{c} 243 \\ 243 \end{array} \\ \\ \begin{array}{c} 243 \\ 243 \end{array} \\ \\ \begin{array}{c} 243 \\ 243 \end{array} \\ \end{array} \\ \begin{array}{c} 243 \\ 243 \end{array} \\ \\ \begin{array}{c} 243 \\ 243 \end{array} \\ \\ \end{array} \\ \begin{array}{c} 243$ in collaboration with: T.Armadillo, R.Bonciani, F.Buccioni, L.Buonocore, S.Devoto, M.Grazzini, S.Kallweit, N.Rana, F.Tramontano,

Drell-Yan results: arXiv:2106.11953, arXiv:2201.01754, 2205.03345 on-shell Z results arXiv:2007.06518, arXiv:211.1.12694

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Lepton-pair Drell-Yan production at hadron colliders



The factorisation theorems guarantee the validity of the above picture up to power correction effects

The interplay of QCD and EW interactions appears both in the partonic cross section and in the proton PDFs







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Channel	Not constraining PDFs	Constraining PDFs
Muons	0.23125 ± 0.00054	0.23125 ± 0.00032
Electrons	0.23054 ± 0.00064	0.23056 ± 0.00045
Combined	0.23102 ± 0.00057	0.23101 ± 0.00030

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at. unc. 40fb ⁻¹	stat. unc. 3ab ⁻¹	A.deviation of the SM prediction can point for the SM prediction can point be set of the
1.4%	0.2%	s the More diction under control at the O(0.5
3.2%	0.6%	in the TeV region of the $m_{\ell\ell}$ distribution ?
	l	0 0.070

 $m_{\ell\ell} \sim 1 \,\mathrm{TeV}$

 $\mathcal{O}(1\%) \quad m_{\ell\ell} \sim 1 \,\mathrm{TeV}$





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High precision determination of the SM parameters at the LHC

The template theoretical uncertainties propagate as systematic errors on the determination of $(m_W, m_Z, \sin^2 \theta_{eff}, \dots)$

Given the very high precision goal $\delta m_W/m_W \sim 1 \cdot 10^{-4}$, $\delta \sin^2 \theta_{eff} / \sin^2 \theta_{eff} \sim 1 \cdot 10^{-3}$ control on the shape of the distributions at the sub-percent level is needed, at a hadron collider...

The SM parameters are extracted from the data via template fitting. Templates = theoretical histograms of the kinematical distr.





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Neutral current Drell-Yan in fixed order



The availability of two completely independent calculations of such a complex set of corrections will be crucial for technical validation

Drell-Yan (1970) Baur, Brein, Hollik, Schappacher, Wackeroth (2001) $\Rightarrow \alpha_s^2 \, \sigma^{(2,0)} + \alpha \, \alpha_s \, \sigma^{(1,1)} + \alpha^2 \, \sigma^{(0,2)} +$ still missing Sudakov high-energy approximations R.Bonciani, L.Buonocore, M.Grazzini, S.Kallweit, N.Rana, F.Tramontano, AV, arXiv:2106.11953

T.Armadillo, R.Bonciani, S.Devoto, N.Rana, AV, arXiv:2201.01754 F.Buccioni, F.Caola, H.Chawdhry, F.Devoto, M.Heller, A.von Manteuffel, K.Melnikov, R.Röntsch, C.Signorile-Signorile, arXiv:2203.11237



Neutral current Drell-Yan in fixed order



resummation of logarithmically enhanced contributions

Monte Carlo: different matching algorithms at NLO-QCD +QCD-PS, NNLO-QCD +QCD-PS, NLO-EW +QED-PS MC@NLO, POWHEG, MINLO, MINNLOPS, Geneva, HORACE, POWHEG QCD+EW

Integrators: different resummation formalisms for qt-resummation up to N3LL-QCD ResBos, DYTurbo, Radlsh, SCETlib

most of the experimental analyses based on the "plug-and-play" convolution of NLO QCD and QED-FSR results the uncertainties of this combination are not available and observable dependent → requires a formal and a phenomenological discussions and the development of combined QCD and QED resummation

Drell-Yan (1970) Baur, Brein, Hollik, Schappacher, Wackeroth (2001) $\rightarrow \alpha_s^2 \sigma^{(2,0)} + \alpha \alpha_s \sigma^{(1,1)} + \alpha^2 \sigma^{(0,2)} + \checkmark$ still missing Sudakov high-energy approximations R.Bonciani, L.Buonocore, M.Grazzini, S.Kallweit, N.Rana, F.Tramontano, AV, arXiv:2106.11953

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Progress towards Drell-Yan simulations at NNLO QCD-EW

Strong boost of the activities in the theory community in the last 2 years!

→ mathematical and theoretical developments and computation of universal building blocks

- 2-loop virtual Master Integrals with internal masses

U. Aglietti, R. Bonciani, arXiv:0304028, arXiv:0401193, R. Bonciani, S. Di Vita, P. Mastrolia, U. Schubert, arXiv:1604.08581, M.Heller, A.von Manteuffel, R.Schabinger arXiv:1907.00491, S.Hasan, U.Schubert, arXiv:2004.14908, M.Long, R, Zhang, W.Ma, Y, Jiang, L.Han, Z.Li, S. Wang, arXiv:2111.14130, X.Liu, Y.Ma, arXiv:2201.11669

- Altarelli-Parisi splitting functions including QCD-QED effects

D. de Florian, G. Sborlini, G. Rodrigo, arXiv:1512.00612

- renormalization

G.Degrassi, AV, hep-ph/0307122, S.Dittmaier, T.Schmidt, J.Schwarz, arXiv:2009.02229, S.Dittmaier, arXiv:2101.05154

\rightarrow on-shell Z and W production as a first step towards full Drell-Yan - pole approximation of the NNLO QCD-EW corrections

S.Dittmaier, A.Huss, C.Schwinn, arXiv:1403.3216, 1511.08016

- analytical total cross section including NNLO QCD-QED and NNLO QED corrections D. de Florian, M.Der, I.Fabre, arXiv:1805.12214

- ptZ distribution including QCD-QED analytical transverse momentum resummation L. Cieri, G. Ferrera, G. Sborlini, arXiv:1805.11948

- fully differential on-shell Z production including exact NNLO QCD-QED corrections M.Delto, M.Jaquier, K.Melnikov, R.Roentsch, arXiv:1909.08428

- total Z production cross section in fully analytical form including exact NNLO QCD-EW corrections R. Bonciani, F. Buccioni, R.Mondini, AV, arXiv:1611.00645, R. Bonciani, F. Buccioni, N.Rana, I.Triscari, AV, arXiv:1911.06200, R. Bonciani, F. Buccioni, N.Rana, AV, arXiv:2007.06518, arXiv:2111.12694

- fully differential on-shell Z and W production including exact NNLO QCD-EW corrections

F. Buccioni, F. Caola, M.Delto, M.Jaquier, K.Melnikov, R.Roentsch, arXiv:2005.10221, A. Behring, F. Buccioni, F. Caola, M.Delto, M.Jaquier, K.Melnikov, R.Roentsch, arXiv:2009.10386, 2103.02671,

\rightarrow complete Drell-Yan

- neutrino-pair production including NNLO QCD-QED corrections

L. Cieri, D. de Florian, M.Der, J.Mazzitelli, arXiv:2005.01315

- 2-loop amplitudes

M.Heller, A.von Manteuffel, R.Schabinger, arXiv:2012.05918

L.Buonocore, M.Grazzini, S.Kallweit, C.Savoini, F.Tramontano, arXiv:2102.12539

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- NNLO QCD-EW corrections to charged-current DY including leptonic decay (2-loop contributions in pole approximation).

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Different Kinds of contributions at $\mathcal{O}(\alpha \alpha_s)$ and corresponding problems μ



The double-real and real-virtual corrections already known from studies of the large transverse momentum lepton pair final state A.Denner, S.Dittmaier, T.Kasprzik, A.Muck, arXiv:1103.0914, A.Denner, S.Dittmaier, M.Hecht, C.Pasold, arXiv:1510.08742 J.Lindert et al., arXiv:1705.0**46**64 Now we can consider the inclusive spectrum, also in the $q_T \rightarrow 0$ limit U U

double-real contributions

amplitudes are easily generated with OpenLoops IR, subtraction care apply the numerical convergence when aiming at 0.1% precision

real-virtual contributions

amplitudes are easily gener##ed with OpenLo#ps ordRecola I-loop UV renormalisation and IR subtraction care about the numerical convergence when aiming at 0.1% precision

Ψυμγ double-virtual contributions generation of the amplitudes γ_5 treatment 2-loop UV renormalization subtraction of the IR divergences solution and evaluation of the Master Integrals g numerical evaluation of the squared matrix element





$$d\sigma = \sum_{m,n=0}^{\infty} d\sigma^{(m,n)} \qquad d\sigma^{(1,1)} = \mathscr{H}^{(1,1)} \otimes d\sigma_{LO} + \left[d\sigma_{R}^{(1,1)} - d\sigma_{CT}^{(1,1)} \right]_{q_T/Q > r_{cut}}$$

IR structure associated to the QCD-QED part derived from NNLO-QCD results via abelianisation (de Florian, Rodrigo, Sborlini, 2016, de Florian, Der, Fabre, 2018)

the q_T -subtraction formalism has been extended to the case of massive final-state emitters (heavy quarks in QCD, leptons in EW)

(Catani, Torre, Grazzini, 2014, Buonocore, Grazzini, Tramontano 2019.)

General structure of the inclusive cross section and the q_T -subtraction formalism in Matrix





General structure of the inclusive cross section and the q_T -subtraction formalism

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$$\int d\sigma_R^{(1,1)} \sim \sum_{i=1}^4 c_i \ln^i r_{cut} + c_0 + \mathcal{O}(r_{cut}^m) \quad \rightarrow \quad \int \left(d\sigma_R^{(1,1)} - d\sigma_{CT}^{(1,1)} \right) \sim c_0 + \mathcal{O}(r_{cut}^m)$$

The counterterm removes the IR sensitivity to the cutoff variable \rightarrow we need small values of the cutoff and explicit numerical tests to quantify the bias induced by the cutoff choice we can fit the r_{cut} dependence and extrapolate in the $r_{cut} \rightarrow 0$ limit (cfr. Buonocore, Kallweit, Rottoli, Wiesemann, arXiv:2111.13661, Camarda, Cieri, Ferrera, arXiv:2111.14509)



General structure of the inclusive cross section and the q_T -subtraction formalism

$$d\sigma = \sum_{m,n=0}^{\infty} d\sigma^{(m,n)} \qquad d\sigma^{(1,1)} = \mathcal{H}^{(1,1)} \otimes d\sigma_{LO} + \left[d\sigma_{R}^{(1,1)} - d\sigma_{CT}^{(1,1)} \right]_{q_T/Q > r_{cut}}$$

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$$\mathcal{H}^{(1,1)} = H^{(1,1)} C_1 C_2 \qquad 2\operatorname{Re}\langle \mathcal{M}^{(0,0)} | \mathcal{M}^{(1,1)} \rangle = \sum_{k=-4}^0 \varepsilon^k f_i(s,t,m) \qquad |\mathcal{M}_{fin}\rangle \equiv (1-I) | \mathcal{M} \rangle \qquad H \propto \langle \mathcal{M}_0 | \mathcal{M}_{fin}\rangle = 0$$

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The IR poles are removed from the full 2-loop amplitude by means of a subtraction procedure (matching the real radiation one) 10 Pittsburgh, May 12th 2022



The double virtual amplitude: reduction to Master Integrals

$$2\operatorname{Re}\left(\mathscr{M}^{(1,1)}(\mathscr{M}^{(0,0)})^{\dagger}\right) = \sum_{i=1}^{N_{MI}} c_i(s,t,m;\varepsilon) \,\mathcal{T}_i(s,t,m;\varepsilon)$$



The double virtual amplitude: reduction to Master Integrals

$$2\operatorname{Re}\left(\mathscr{M}^{(1,1)}(\mathscr{M}^{(0,0)})^{\dagger}\right) = \sum_{i=1}^{N_{MI}} c_i(s,t,m;\varepsilon) \ \mathscr{T}_i(s,t,m;\varepsilon)$$

The coefficients c_i are rational functions of the invariants, masses and of ε The size of the total expression can rapidly "explode"

 \rightarrow careful work to identify the patterns of recurring subexpressions keeping the total size in the O(1-10 MB) range

The complexity of the MIs depends on the number of energy scales MIs relevant for the QCD-QED corrections, with massive final state Bonciani, Ferroglia, Gehrmann, Maitre, Studerus., arXiv:0806.2301, 0906.3671

MIs with I or 2 internal mass relevant for the EW form factor Aglietti, Bonciani, hep-ph/0304028, hep-ph/0401193

31 MIs with I mass and 36 MIs with 2 masses including boxes, relevant for the QCD-weak corrections to the full Drell-Yan

Bonciani, Di Vita, Mastrolia, Schubert., arXiv: 1604.08581

In the 2-mass case, 5 box integrals in Chen-Goncharov representation \rightarrow problematic numerical evaluation \rightarrow need an alternative strategy

cfr. also Heller, von Manteuffel, Schabinger, arXiv:1907.00491 for a representation of the MIs in terms of GPLs arXiv:2012.05918 for a description of the 2-loop virtual amplitude Alessandro Vicini - University of Milano



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Evaluation of the Master Integrals by series expansions T.Armadillo, R.Bonciani, S.Devoto, N.Rana, AV, 2205.03345

The Master Integrals satisfy a system of differential equations. The MIs are replaced by formal series with unknown coefficients \rightarrow eqs for the unknown coefficients of the series. The package DiffExp by M.Hidding, arXiv:2006.05510 implements this idea, for real valued masses, with real kinematical vars. But we need complex-valued masses of W and Z bosons (unstable particles) \rightarrow we wrote a new package (SeaSyde)



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We implemented the series expansion approach, for arbitrary complex-valued masses, working in the complex plane of each kinematical variable, one variable at a time

Complete knowledge about the singular structure of the MI can be read directly from the differential equation matrix

The solution can be computed with an arbitrary number of significant digits, but not in closed form \rightarrow semi-analytical



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Numerical evaluation of the hard coefficient function

The interference term $2\text{Re}\langle \mathscr{M}^{(1,1),fin} | \mathscr{M}^{(0,0)} \rangle$ contributes to the hard function $H^{(1,1)}$ After the subtraction of all the universal IR divergences, it is a finite correction It has been published in arXiv:2201.01754 and is available as a Mathematica notebook

Several checks of the MIs performed with Fiesta and PySecDec covering the whole $2 \rightarrow 2$ phase space in (s,t), in O(12 h) on one 32-cores machine

 \rightarrow a numerical grid for $2\text{Re}\langle \mathscr{M}^{(1,1),fin} | \mathscr{M}^{(0,0)} \rangle$ has been prepared



- A numerical grid has been prepared for all the 36 MIs, with GiNaC and SeaSyde (T.Armadillo, R.Bonciani, S.Devoto, N.Rana, AV, 2205.03345),

values at arbitrary phase space points with excellent accuracy via interpolation, with negligible evaluation time



$G_{\mu} ext{-scheme}$	$\sigma ~[{ m pb}]$	$\sigma^{(i,j)} \; [ext{pb}]$	$\mid \sigma^{(i,j)}/\sigma_{ m LO}$	
LO	$763.40(2)^{+12.7\%}_{-13.6\%}$	_	_	
NLO QCD	$802.26(6)^{+2.7}_{-4.2\%}$	38.86(6)	5.1%	
NNLO QCD	$802.5(7)^{+0.4}_{-0.8\%}$	0.2(7)	0.0%	p -3
NLO EW	$730.76(2)^{+12.7}_{-13.6\%}$	-32.65(3)	-4.3%	
NNLO QCD+EW	$769.8(7)^{+0.5}_{-0.6\%}$	—	_	
NNLO QCD+EW+MIX _{fact}	$768.2(7)^{+0.3}_{-0.7\%}$	-2.0(1)	-0.2%	
NNLO QCD+EW+MIX	$772.4(8)^{+0.3}_{-0.7\%}$	2.6(2)	0.3%	

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Phenomenology of Neutral Current Drell-Yan including exact NNLO QCD-EW corrections

R.Bonciani, L.Buonocore, S.Devoto, M.Grazzini, S.Kallweit, N.Rana, F.Tramontano, AV, arXiv:2106.11953 and work in preparation

SETUP (LHC @ $\sqrt{s} = 13$ TeV) CMS 2103.02708 • NNPDF31 nnlo as 0118 luxqed • $p_{T,\mu} > 53 \text{ GeV}$, $|y_{\mu}| < 2.4$, $m_{\mu^+\mu^-} > 150 \text{ GeV}$ **SETUP** (LHC @ $\sqrt{s} = 13 \text{ TeV}$) • massive muons (no photon lepton recombination) • WNPDF31 nnlo as 0118 luxqed • Gu scheme, complex mass scheme • $p_{\text{dy,mamic Scale}} \sum_{k=1}^{5.3} GeV_{\mu_F} = |\mu_{R^{\mu}}| \le m_{\mu^+\mu^-}^{2.4}, \quad m_{\mu^+\mu^-} > 150 \text{ GeV}$ • massive muons (no photon lepton recombination) • G_{μ} scheme, complex mass scheme Negative mixed $NRLO_{\mu_{R}}QCD-EW$ effects (-3% or more) at large invariant masses, absent in any additive combination \rightarrow impact on the searches for new physics

Good accuracy

of the factorised of QCD x EW Ansatz

Scale uncertainty at most the O(1%) between 1 and 2 TeV



The lepton transverse momentum distribution: QCD-EW corrections

R.Bonciani, L.Buonocore, M.Grazzini, S.Kallweit, N.Rana, F.Tramontano, AV, arXiv:2106.11953



In the jacobian peak region the xsec is very much affected by the fixed-order nature of the results

In the large transverse momentum tail the dominant topology is Z+jet (qg-induced) which receives negative and large EW corrections

The exact calculation deviates from the factorised approximation because the EW correction $d\sigma^{(0,1)}$ applies correctly to the $p_T^Z = 0$ bin but misses the large Sudakov logs which develop at $p_T^Z \gg 0$



500

Important impact on the Z+jet and W+jet generators

Estimate of the residual uncertainties: total cross section The impact of the NNLO QCD-EW corrections is twofold:

Ongoing phenomenological studies for full NC DY

A representative example from the results for the on-shell Z production total cross section R.Bonciani, F.Buccioni, N.Rana, AV, arXiv:2007.06518, arXiv:2111.12694

 \rightarrow dependence on the EW input-scheme choice

comparison of (G_{μ}, M_{W}, M_{Z}) and $(\alpha(0), M_{W}, M_{Z})$ (very conservative choice that maximises the spread of the results)

Gμ	α(0)	δ(G _μ -α(0)) (%)
55787	53884	3.53
55501	55015	0.88
55469	55340	0.23
	Gµ 55787 55501 55469	Gµα(0)557875388455501550155546955340

the LO + NLO-EW result would suffer of only 0.55% spread; the NLO-QCD and NNLO-QCD corrections are only LO-EW and reintroduce a dependence (\rightarrow 0.88%) which is reduced by the NNLO QCD-EW (\rightarrow 0.23%)

more accurate predictions (additional higher orders) reduced uncertainties (scale, inputs, matching)



Conclusions

The evaluation of the NNLO QCD-EW corrections is not yet a "pressing-just-one-button" game but

the main obstacles to compute the 2-loop virtual corrections have been understood and solved for NC DY

- amplitude manipulation
- IR structure

Two independent calculations are now available

The systematic automation of the progresses in the 2-loop virtual section is ongoing and will allow the study of NNLO QCD-EW corrections to other scattering processes be the starting point for the evaluation of NNLO-EW corrections

The phenomenological impact of mixed NNLO QCD-EW corrections is not negligible in the precision physics program at the LHC

A precise SM prediction is the mandatory starting point for any SMEFT study or search in a UV-complete model

• evaluation of Master Integrals with 2 internal complex-valued masses (SeaSyde)



Back-up



Combined QCD-EW simulation tools: impact of QED-FSR on MW



the impact on MW of the mixed QCD QED-FSR corrections strongly depends on the underlying QCD shape/model

given that the bulk of the corrections is included in the analyses

- what is the associated uncertainty ?
- what happens if we change the underlying QCD model ?

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can we constrain the formulation, for the $\alpha \alpha_{\rm c}$ contribution ?

The Neutral Current Drell-Yan cross section in the SM: perturbative expansion

$$\begin{split} \sigma(h_1 h_2 \to \ell \bar{\ell} + X) &= \sigma^{(0,0)} + \\ & \alpha_s \, \sigma^{(1,0)} + \alpha \, \sigma^{(0,1)} + \\ & \alpha_s^2 \, \sigma^{(2,0)} + \alpha \, \alpha_s \, \sigma^{(1,1)} + \alpha^2 \, \sigma^{(0,2)} + \\ & \alpha_s^3 \, \sigma^{(3,0)} + \dots \end{split}$$

$$\sigma(h_1 h_2 \to l\bar{l} + X) = \sum_{i,j=q\bar{q},g,\gamma} \int dx_1 \, dx_2 \, f_i^{h_1}(x_1,\mu_F) f_j^{h_2}(x_2,\mu_F) \, \hat{\sigma}(ij \to l\bar{l} + X)$$

 $\sigma^{(1,1)}$ requires the evaluation of the xsecs of the following processes, including photon-induced $q\bar{q} \rightarrow l\bar{l}, \ \gamma\gamma \rightarrow l\bar{l}$ including virtual corrections of $\mathcal{O}(\alpha_s), \mathcal{O}(\alpha), \mathcal{O}(\alpha \alpha_s)$

0 additional partons

$$q\bar{q} \rightarrow l\bar{l}g, \ qg \rightarrow l\bar{l}q$$

$$q\bar{q} \rightarrow l\bar{l}\gamma, \ q\gamma \rightarrow l\bar{l}q$$

$$\begin{split} q\bar{q} &\rightarrow l\bar{l}g\gamma, qg \rightarrow l\bar{l}q\gamma, q\gamma \rightarrow l\bar{l}qg, g\gamma \rightarrow l\bar{l}q\bar{q} \\ q\bar{q} \rightarrow l\bar{l}q\bar{q}, q\bar{q} \rightarrow l\bar{l}q'\bar{q}', qq' \rightarrow l\bar{l}qq', q\bar{q}' \rightarrow l\bar{l}q\bar{q}', qq \rightarrow l\bar{l}qq \quad \text{at tree leve} \\ \end{split}$$

I additional parton

2 additional partons

including virtual corrections of $\mathcal{O}(\alpha)$

including virtual corrections of $\mathcal{O}(\alpha_s)$

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Computational framework

The complete calculation has been included in the Munich/Matrix framework

- fully automatic generation and bookkeeping of all the double-real and real-virtual contributions based on an interface with OpenLoops and Recola/Collier
- the 2-loop virtual corrections are separately computed and provided in fast-evaluation format

In this specific framework, main compatibility requirement to include the double-virtual corrections: the q_T -subtraction formalism to handle the IR singularities (Catani, Grazzini, 2007)

Upon inclusion of the appropriate scheme-dependent subtraction term, the double virtual corrections can be used with any other simulation code



General structure of the inclusive cross section and the q_T -subtraction formalism

$$d\sigma = \sum_{m,n=0}^{\infty} d\sigma^{(m,n)} \qquad d\sigma^{(1,1)} = \mathcal{H}^{(1,1)} \otimes d\sigma_{LO} + \left[d\sigma_{R}^{(1,1)} - d\sigma_{CT}^{(1,1)} \right]_{q_T/Q > r_{cut}}$$

IR structure associated to the QCD-QED part derived from NNLO-QCD results via abelianisation

(de Florian, Rodrigo, Sborlini, 2016, de Florian, Der, Fabre, 2018)

(Catani, Torre, Grazzini, 2014, Buonocore, Grazzini, Tramontano 2019.)

the q_T -subtraction formalism has been extended to the case of final-state emitters (heavy quarks in QCD, leptons in EW)



General structure of the inclusive cross section and the q_T -subtraction formalism

$$d\sigma = \sum_{m,n=0}^{\infty} d\sigma^{(m,n)} \qquad d\sigma^{(1,1)} = \mathcal{H}^{(1,1)} \otimes d\sigma_{LO} + \left[d\sigma_{R}^{(1,1)} - d\sigma_{CT}^{(1,1)} \right]_{q_T/Q > r_{cut}}$$

 q_T IR structure associated to the QCD-QED part derived from NNLO-QCD results via abelianisation (de Florian, Rodrigo, Sborlini, 2016, de Florian, Der, Fabre, 2018)



q_T

$$\stackrel{\gamma}{0}$$
 regions

$$r_{cut} = q_T^{cut} / Q$$





 q_T

 $q_T/$

If c

The q_T -subtraction and the residual cut-off dependency

$$d\sigma = \sum_{m,n=0}^{\infty} d\sigma^{(m,n)} \qquad d\sigma^{(1,1)} = \mathcal{H}^{(1,1)} \otimes d\sigma_{LO} + \left[\frac{d\sigma_{R}^{(1,1)} - d\sigma_{CT}^{(1,1)}}{q_T/Q} \right]_{q_T/Q > r_{cut}}$$

When $q_T/Q > r_{cut}$ the double-real and the real-virtual contributions, subtracted with CS dipoles, are finite

 $d\sigma_{CT}^{(1,1)}$ is obtained by expanding to fixed order the q_T resummation formula



The q_T -subtraction and the residual cut-off dependency

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Logarithmic sensitivity on r_{cut} in the double unresolved lim

The counterterm removes the IR sensitivity to the cutoff v

 \rightarrow we need small values of the cutoff

 \rightarrow explicit numerical tests to quantify the bias induced by the cutoff choice

we can fit the r_{cut} dependence and extrapolate in the $r_{cut} \rightarrow 0$ limit

it
$$\int d\sigma_R^{(1,1)} \sim \sum_{i=1}^4 c_i \ln^i r_{cut} + c_0 + \mathcal{O}(r_{cut}^m)$$
wariable
$$\int \left(d\sigma_R^{(1,1)} - d\sigma_{CT}^{(1,1)} \right) \sim c_0 + \mathcal{O}(r_{cut}^m)$$

(cfr. Buonocore, Kallweit, Rottoli, Wiesemann, arXiv:2111.13661 Camarda, Cieri, Ferrera, arXiv:2111.14509)



Subtraction of the IR divergences from the 2-loop amplitude

$$\begin{split} |\mathcal{M}^{(1,0),fin}\rangle &= |\mathcal{M}^{(1,0)}\rangle - \mathcal{I}^{(1,0)}|\mathcal{M}^{(0)}\rangle \,, \\ |\mathcal{M}^{(0,1),fin}\rangle &= |\mathcal{M}^{(0,1)}\rangle - \mathcal{I}^{(0,1)}|\mathcal{M}^{(0)}\rangle \,. \\ |\mathcal{M}^{(1,1),fin}\rangle &= |\mathcal{M}^{(1,1)}\rangle - \mathcal{I}^{(1,1)}|\mathcal{M}^{(0)}\rangle - \tilde{\mathcal{I}}^{(0,1)}|\mathcal{M}^{(0)}\rangle \,. \end{split}$$

$$\begin{split} \mathcal{I}^{(1,0)} &= \left(\frac{\alpha_s}{4\pi}\right) \left(\frac{s}{\mu^2}\right)^{-\epsilon} C_F \left(-\frac{2}{\epsilon^2} - \frac{1}{\epsilon}(3+2i\pi) + \zeta_2\right), \\ \mathcal{I}^{(0,1)} &= \left(\frac{\alpha}{4\pi}\right) \left(\frac{s}{\mu^2}\right)^{-\epsilon} \left[Q_u^2 \left(-\frac{2}{\epsilon^2} - \frac{1}{\epsilon}(3+2i\pi) + \zeta_2\right) + \frac{4}{\epsilon} \Gamma_l^{(0,1)}\right], \qquad \Gamma_l^{(0,1)} = Q_u Q_l \log\left(\frac{2p_1.p_3}{2p_2.p_3}\right) + \frac{Q_l^2}{2} \left(-1 - \frac{1+x_l^2}{1-x_l^2} \log(x_l^2)\right) \\ \mathcal{I}^{(1,1)} &= \left(\frac{\alpha_s}{4\pi}\right) \left(\frac{\alpha}{4\pi}\right) \left(\frac{s}{\mu^2}\right)^{-2\epsilon} C_F Q_u^2 \left(\frac{4}{\epsilon^4} + \frac{1}{\epsilon^3}(12+8i\pi) + \frac{1}{\epsilon^2}(9-28\zeta_2+12i\pi) \right) \\ &+ \frac{1}{\epsilon} \left(-\frac{3}{2} + 6\zeta_2 - 24\zeta_3 - 4i\pi\zeta_2\right) \right). \end{split}$$

 $2\text{Re}\langle \mathscr{M}^{(0,0)} | \mathscr{M}^{(1,1),fin} \rangle$ is free of any singularity

the analytical check of the cancellation of the IR poles in the QCD-weak sector is one very demanding test of the calculation

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we identify QCD-QED (poles up to $1/\epsilon^4$) and QCD-weak (poles up to $1/\epsilon^2$ with cumbersome coefficients) diagrams

standard NLO-QCD subtraction

NLO-EW subtraction, with massive leptons

 $^{(1)}|\mathcal{M}^{(1,0),fin}\rangle - \tilde{\mathcal{I}}^{(1,0)}|\mathcal{M}^{(0,1),fin}\rangle.$







The double virtual amplitude: generation of the amplitude

$$\mathscr{M}^{(0,0)}(q\bar{q} \to l\bar{l}) =$$



 $\mathscr{M}^{(1,1)}(q\bar{q} \to l\bar{l}) =$

to the second se

O(1000) self-energies + O(300) vertex corrections +O(130) box corrections + $Iloop \times Iloop$ (before discarding all those vanishing for colour conservation, e.g. no fermonic triangles)

DANARAKIKAKIKAKIKAKIKA $\frac{1}{2} \int_{2}^{2} \int_{2}^$

The double virtual amplitude: generation of the amplitude



Two independent calculations based on QGraf and FeynArts in the EW Background Field Gauge

The BFG choice guarantees the validity of EW Ward identities for the initial state vertex \rightarrow additional technical checks - UV finiteness when combining 2-loop vertex and quark WF in the full EW SM \rightarrow that combination has only IR poles - UV renormalisation is confined to the gauge-boson propagators sector, where IR divergences are absent

The I-loop check of the gauge-parameter independence identifies those subsets of diagrams yielding the cancellation.

The 2-loop calculation is organised splitting the total amplitude in the combination of different subsets, according to their EW charges (# of Ws, Zs, γ s)

O(1000) self-energies + O(300) vertex corrections +O(130) box corrections + $Iloop \times Iloop$ (before discarding all those vanishing for colour conservation, e.g. no fermonic triangles)

The double virtual amplitude: UV renormalization

G.Degrassi, AV, hep-ph/0307122, S.Dittmaier, T.Schmidt, J.Schwarz, arXiv:2009.02229 S.Dittmaier, arXiv:2101.05154

Complex mass scheme

$$\begin{split} \mu_{W0}^2 &= \mu_W^2 + \delta \mu_W^2, \quad \mu_{Z0}^2 = \mu_Z^2 + \delta \mu_Z^2, \quad e_0 = e + \delta e \\ \frac{\delta s^2}{s^2} &= \frac{c^2}{s^2} \left(\frac{\delta \mu_Z^2}{\mu_Z^2} - \frac{\delta \mu_W^2}{\mu_W^2} \right) & \text{the mass counterterms are defined} \\ &\text{at the complex pole of the propagator} \\ &\text{the weak mixing angle is complex valued} \quad c^2 \equiv \mu_W^2 / \mu_Z^2 \end{split}$$

BFG EW Ward identity

The bare couplings of Z and photon to fermions $\frac{g_0}{2} =$ c_0 in the (G_{μ}, μ_W, μ_Z) input scheme are given by $g_0 s_0$

Gauge boson renormalised propagators

$$\Sigma_{R,T}^{AA}(q^2) = \Sigma_T^{AA}(q^2) + 2 q^2 \delta g_A$$

$$\Sigma_{R,T}^{ZZ}(q^2) = \Sigma_T^{ZZ}(q^2) - \delta \mu_Z^2 + 2 (q^2 - \mu_Z^2) \delta g_Z$$

After the UV renormalisation, the singular structure is entirely due to IR soft and/or collinear singularities

cancellation of the UV divergences combining vertex and fermion WF corrections

$$= \sqrt{4\sqrt{2}G_{\mu}\mu_{Z}^{2}} \left[1 - \frac{1}{2}\Delta r + \frac{1}{2}\left(2\frac{\delta e}{e} + \frac{s^{2} - c^{2}}{c^{2}}\frac{\delta s^{2}}{s^{2}}\right)\right] \equiv \sqrt{4\sqrt{2}G_{\mu}\mu_{Z}^{2}} \left(1 + \frac{1}{2}\left(-\Delta r + 2\frac{\delta e}{e}\right)\right] \equiv e_{ren}^{G_{\mu}} \left(1 + \delta g_{A}^{G_{\mu}}\right)$$

$$\Sigma_{R,T}^{AZ}(q^2) = \Sigma_T^{AZ}(q^2) - q^2 \frac{\delta s^2}{sc}$$
$$\Sigma_{R,T}^{ZA}(q^2) = \Sigma_T^{ZA}(q^2) - q^2 \frac{\delta s^2}{sc},$$

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The double virtual amplitude: γ_5 treatment The absence of a consistent definition of γ_5 in $n = 4 - 2\varepsilon$ dimensions yields a practical problem

The trace of Dirac matrices and γ_5 is a polynomial in ε The UV or IR divergences of Feynman integrals appear as poles $1/\varepsilon$

$$\mathrm{T}r(\gamma_{\alpha}\dots\gamma_{\mu}\gamma_{5}) \times \int d^{n}k \frac{1}{[k^{2}-m_{0}^{2}][(k+q_{1})^{2}-m_{1}^{2}][(k+q_{2})^{2}-m_{2}^{2}]} \sim (a_{0}+a_{1}\varepsilon+\dots) \times \left(\frac{c_{-2}}{\varepsilon^{2}}+\frac{c_{-1}}{\varepsilon}+c_{0}+\dots\right)$$

If a_1 is evaluated in a non-consistent way,

then poles might not cancel and the finite part of the xsec might have a spurious contribution



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- 't Hooft-Veltman treat γ_5 (anti)commuting in (4) n 4 dimensions preserving the cyclicity of the traces (one counterterm is needed)
- Kreimer treats γ_5 anticommuting in *n* dimensions, abandoning the cyclicity of the traces (\rightarrow need of a starting point)
- we adopted the naive anticommuting prescription (Kreim
 - we computed the 2-loop amplitude and, independently,
 - the cancellation of all the lowest order poles is checked
 - absence of fermionic triangles because of colour conservation

- Heller, von Manteuffel, Schabinger verified that the IR-subtracted squared matrix element are identical in the two approaches

her); we use
$$\gamma_5 = \frac{i}{4!} \epsilon_{\mu\nu\rho\sigma} \gamma^{\mu} \gamma^{\nu} \gamma^{\rho} \gamma^{\sigma}$$
 to compute traces with one
r, the IR subtraction term; both depend on the prescription cho
d (and non trivial)



The double virtual amplitude: solution and evaluation of the Master Integrals

The system of first-order linear differential equations satisfied by the 36 QCD-weak Master Integrals chosen by Bonciani et al. can be written in dlog form

$$d\mathbf{I} = \epsilon \, d\mathbb{A} \, \mathbf{I} \,, \qquad d\mathbb{A} = \sum_{i=1}^{n} \mathbb{M}_i \, d\log \eta_i$$

The letters η_i provide the complete information about the singular structure of the amplitude

Boundary Conditions The BCs have been evaluated outside the physical phase space and are expressed in exact form

Master Integrals 1-31

When the letters have a rational (linear) expression, it is possible to integrate the system in terms of GPLs

The appearance, for kinematical reasons, of four square roots among the letters is handled with a change of variables that makes all the new letters linear, leading to a GPL solution in the new variables

Master Integrals 32-36

The appearance of another distinct square root among the letters, makes it impossibile to linearise the weights \rightarrow the equations are formally solved with a Chen-Goncharov iterated representation

- the poles of these MIs contain Chen-Goncharov functions, but the latter cancel in the physical amplitude

 \cdot in the finite part, the Chen-Goncharov functions remain \rightarrow problems to evaluate the amplitude in the physical region



Total cross section in the fiducial region $G_{\mu} = 1.1663787 \times 10^{-5} \,\text{GeV}^{-2}, \ M_W = 80.358 \,\,\text{GeV}, \ \Gamma_W = 2.084 \,\,\text{GeV}, \ M_Z = 91.1535 \,\,\text{GeV}, \ \Gamma_Z = 2.4943 \,\,\text{GeV}$ $M_H = 125.09 \text{ GeV}, m_t = 173.07 \text{ GeV}$ NNPDF31_nnlo_as_0118_luxqed $p_T^{\mu^{\pm}} > 25 \,\text{GeV}, \quad |\eta^{\mu^{\pm}}| < 2.5, \quad m_{\mu^{+}\mu^{-}} > 50 \,\text{GeV}, \quad \mu_R = \mu_F = M_Z$

$\sigma \; [ext{pb}]$	$\sigma_{ m LO}$	$\sigma^{(1,0)}$	$\sigma^{(0,1)}$	$\sigma^{(2,0)}$	$\sigma^{(1,1)}$
q ar q	809.56(1)	191.85(1)	-33.76(1)	49.9(7)	-4.8(3)
qg		-158.08(2)		-74.8(5)	8.6(1)
$q(g)\gamma$			-0.839(2)		0.084(3)
q(ar q)q'				6.3(1)	0.19(0)
gg				18.1(2)	
$\gamma\gamma$	1.42(0)		-0.0117(4)		
tot	810.98(1)	33.77(2)	-34.61(1)	-0.5(9)	4.0(3)
$\sigma^{(m,n)}/\sigma_{\rm LC}$)	+4.2%	-4.3 %	$\sim 0\%$	+0.5 %

Accidental cancellation of NLO-QCD and NLO-EW, small contribution from NNLO-QCD \rightarrow the NNLO QCD-EW is comparable (or larger) in size than the combination of the previous orders

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Towards the NNLO-EW calculation ?

The NNLO-EW corrections could modify in a non-trivial way the large-mass/momentum tails of the distributions Large logarithmic corrections (EW Sudakov logs) appear in the virtual corrections At two-loop level, we have up to the fourth power of $\log(s/m_V^2)$, the different corrections are comparable in size and with alternate signs

 \rightarrow how can we estimate the constant term ?



corrections to $e^+e^- \rightarrow q\bar{q}$ due to EW Sudakov logs



Towards the NNLO-EW calculation ?

The NNLO-EW corrections could modify in a non-trivial way the large-mass/momentum tails of the distributions Large logarithmic corrections (EW Sudakov logs) appear in the virtual corrections At two-loop level, we have up to the fourth power of $\log(s/m_V^2)$, the different corrections are comparable in size and with alternate signs

 \rightarrow how can we estimate the constant term ?



- The NNLO-EW corrections will require an extra step compared to the mixed QCD-EW case - for the number of additional Master Integrals (\rightarrow automation)
 - for the complexity of the amplitudes (size problems? large cancellations?)

- for the conceptual problems (γ_5 ?, complex-mass scheme at two-loop?) but the discussion has started

corrections to $e^+e^- \rightarrow q\bar{q}$ due to EW Sudakov logs



Differential distributions: exact vs approximated predictions

The exact $O(\alpha \alpha_s)$ corrections allow to test the validity of different recipes based on NLO-QCD and NLO-EW results

$$\frac{d\sigma_{fact}}{dX} = \frac{d\sigma^{(0,0)}}{dX} \left[1 + \frac{d\sigma^{(1,0)}}{dX} \left(\frac{d\sigma^{(0,0)}}{dX} \right)^{-1} \right] \times \left[1 + \frac{d\sigma^{(0,1)}}{dX} \left(\frac{d\sigma^{(0,0)}}{dX} \right)^{-1} \right]$$

$$\simeq \frac{d\sigma^{(0,0)}}{dX} + \frac{d\sigma^{(1,0)}}{dX} + \frac{d\sigma^{(0,1)}}{dX} + \frac{d\sigma^{(0,1)}}{dX} \frac{d\sigma^{(1,0)}}{dX} \left(\frac{d\sigma^{(0,0)}}{dX}\right)^{-1}$$

- Factorisation is expected to work when

the 2-loop virtual corrections are evaluated in pole approximation • on-shell Z boson form factor

factorised Ansatz

pole approximation

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• the last term is absent in a purely additive formulation

both QCD and EW corrections factorise w.r.t. the gauge boson production

• the giant K-factors (qg and q γ processes) should not be applied to photon-induced channels

in the hard coefficient, the 2-loop virtual is approximated by $H_{PA}^{(1,1)} = \frac{2\text{Re}(\mathcal{M}^{(1,1)}\mathcal{M}^{(0,0)*})_{PA}}{|\mathcal{M}^{(0,0)}|^2}$

• the resonant contributions of the γZ box diagrams cancel 33

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Dependence on r_{cut} of the NNLO QCD-EW corrections to NC DY

courtesy of S.Kallweit

Symmetric-cut scenario $p_{T.\ell^{\pm}} > 25 \,\text{GeV} \quad y_{\ell^{\pm}} < 2.5 \quad m_{\ell\ell} > 50 \,\text{GeV}$



• large power corrections in r_{cut} for mixed corrections explained by overall small size of corrections, and in parts also by cancellation between partonic channels

• by far less dramatic dependence at level of cross sections better than permille precision at inclusive level

Splitting into partonic channels



The q_T -subtraction and the residual cut-off dependency in different acceptance setups

courtesy of S.Kallweit

(cfr. Buonocore, Kallweit, Rottoli, Wiesemann, 2111.13661)

Symmetric cuts

• $p_{\mathrm{T},\ell^{\pm}} > 25\,\mathrm{GeV}$



Asymmetric cuts on ℓ_1 and ℓ_2 $p_{{ m T},\ell_1}>25\,{ m GeV}~p_{{ m T},\ell_2}>20\,{ m GeV}$





large power corrections in $r_{\rm cut}$

large power corrections in $r_{\rm cut}$

Asymmetric cuts on ℓ^+ and ℓ^-



no significant dependence on $r_{\rm cut}$

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Differential sensitivity to r_{cut}

Binwise $r_{\rm cut}$ dependence of the mixed NNLO QCD–EW corrections for NC Drell–Yan

Differential distribution in p_{T,μ^+} : peak (left panels) and tail (right panels) regions



 \blacktriangleright large $r_{\rm cut}$ dependence in particular around the peak of the distribution, and typically precision of $\leq 3\%$ on the relative mixed QCD-EW corrections (artificially large where corrections are basically zero)



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Binwise $r_{\rm cut}$ dependence of the mixed NNLO QCD–EW corrections for NC Drell–Yan



Differential distribution in $m_{\mu^+\mu^-}$: peak (left panels) and tail (right panels) regions

 \blacktriangleright quite large $r_{\rm cut}$ dependence throughout, and lower numerical precision of $\leq 10\%$ on the relative mixed QCD-EW corrections (but still permille-level precision at the level of cross sections)

