

CP violating inflation

Venus Keus

DIAS

Institiúid Ard-Léinn | Dublin Institute for
Bhaile Átha Cliath | Advanced Studies



The Dark Side of the Universe DSU2022



Based on Phys. Rev. D 104 (2021) and work in progress
In collaboration with Kimmo Tuominen



TRANS & NON-BINARY PHYSICISTS

The Trans and Non-Binary Physicists Discord server is an online community for transgender and non-binary physicists -- from enthusiasts to professors! -- to socialise, network and support one another. All are welcome, and so far we have over 200 members from across the world!

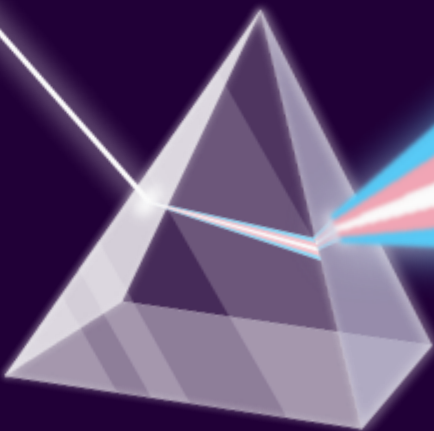
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transphysicists@gmail.com



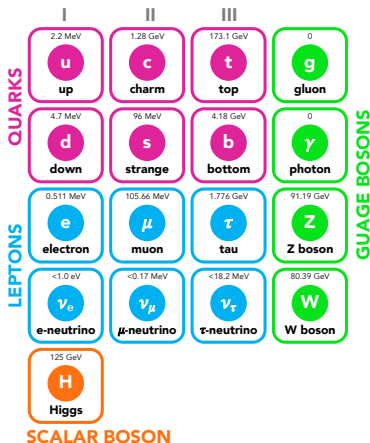
twitter.com/transphysicists



The Standard Model

Its current formulation was finalised in the 70's and predicted:

- the W & Z bosons
discovered in 1983
- the top quark
discovered in 1995
- the tau neutrino
discovered in 2000
- the Brout-Englert-Higgs mechanism
a scalar boson discovered in 2012



VK

experiment

JKK: Ask not what your ~~country~~ can do for you - ask what you can do for your ~~country~~.

experiment

Scalar extensions of the SM

SM + scalar singlets [link](#)

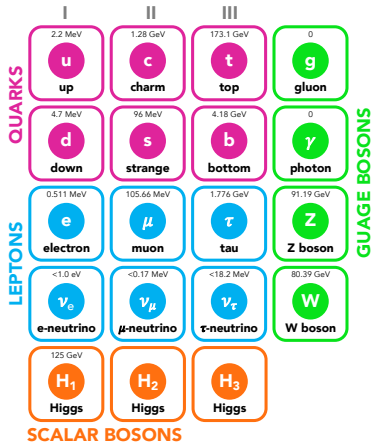
- Dark Matter **severely constrained**
- CP-violation **not possible**
- Inflation **DM incompatible**

2HDM: SM + a doublet [link](#)

- Dark Matter **constrained & CPV incompatible**
- CP-violation **severely constrained & DM incompatible**
- Inflation **DM incompatible**

3HDM: SM + 2 doublets [link](#)

- Dark Matter **many exotic possibilities**
- CP-violation **unbounded dark CP-violation**
- Inflation **easily achieved + exotic possibilities**
- Bonus: fermion mass hierarchy explanation



Upcoming experimental probes

- Collider experiments

- 2021: LHC-RUN-III
- 2026: HL-LHC
- 2028: CEPC

- DM experiments

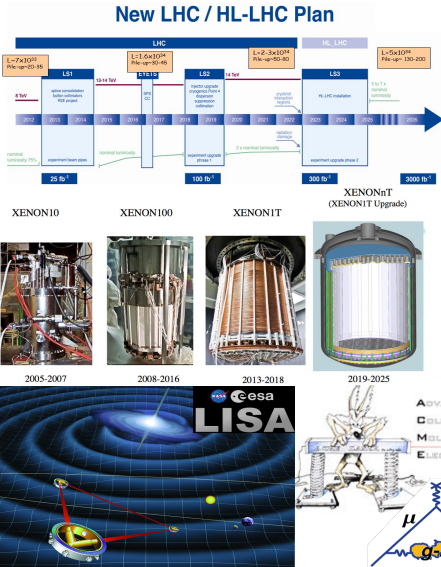
- 2020: XENONnT
- 2022: CTA

- GW experiments

- 2027: DECIGO
- 2034: LISA mission

- Precision experiments

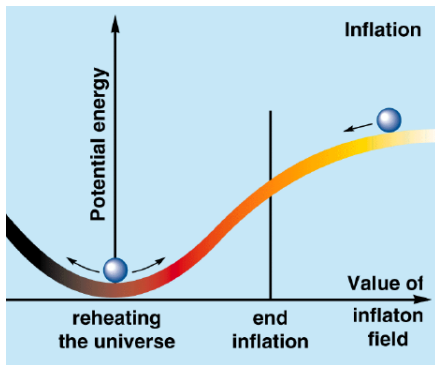
- 2020: $(g - 2)_\mu$
- 2020: Advanced ACME



Simplest and best in agreement with observation

Slow roll inflation:

driven by a scalar field (inflaton) slowly rolling down its smooth potential



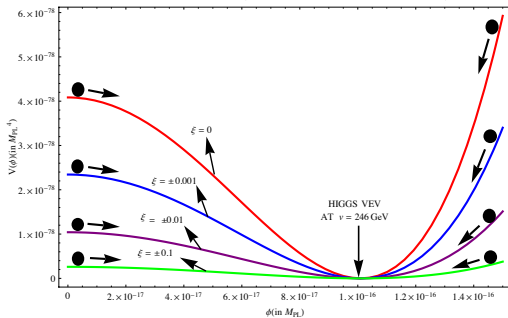
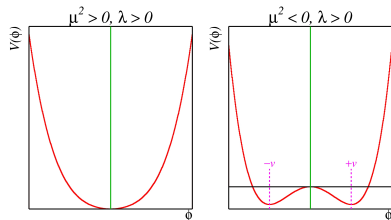
The Higgs inflation model

The SM Higgs potential:

$$V(\phi) = -\mu_h^2 \phi^\dagger \phi + \lambda_h (\phi^\dagger \phi)^2$$

Introducing a non-minimal coupling to gravity ξ :

$$\mathcal{L}_J = \frac{\sqrt{-g_J}}{2} \left[(\xi \phi^2 + M_{pl}^2) R + (\partial_\mu \phi)^2 - V(\phi) \right]$$



S. Choudhury, T. Chakraborty, S. Pal, [Nucl. Phys. B 880, 155-174 (2014)]

3HDMs: 3-Higgs doublet models

two scalar doublets + the SM Higgs doublet

ϕ_1, ϕ_2

ϕ_3

$$\phi_1 = \begin{pmatrix} h_1^+ \\ \frac{h_1 + i\eta_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} h_2^+ \\ \frac{h_2 + i\eta_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{h_3 + iG^0}{\sqrt{2}} \end{pmatrix}$$

Z_2 -symmetric 3HDM with dark CPV

Lagrangian invariant under a Z_2 symmetry $(-, -, +)$:

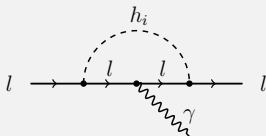
$$\phi_1 \rightarrow -\phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \text{SM fields} \rightarrow \text{SM fields}, \quad \phi_3 \rightarrow \phi_3$$

and respected by the vacuum $(0, 0, v)$:

$$\phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ h_1 + i\eta_1 \end{pmatrix}, \quad \phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ h_2 + i\eta_2 \end{pmatrix}, \quad \phi_3 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_h + h_3 \end{pmatrix}$$

Only ϕ_3 can couple to fermions: $\phi_u = \phi_d = \phi_e = \phi_3$

$$\begin{aligned} -\mathcal{L}_{Yukawa} = & Y_u \bar{Q}'_L i\sigma_2 \phi_u^* u'_R \\ & + Y_d \bar{Q}'_L \phi_d d'_R \\ & + Y_e \bar{L}'_L \phi_e e'_R + \text{h.c.} \end{aligned}$$



No contributions to electric dipole moments (EDMs)

Z_2 -symmetric 3HDM with dark CPV

The scalar potential: $V = V_0 + V_{Z_2}$ with

$$V_0 = -\mu_i^2(\phi_i^\dagger\phi_i) + \lambda_{ii}(\phi_i^\dagger\phi_i)^2 + \lambda_{ij}(\phi_i^\dagger\phi_i)(\phi_j^\dagger\phi_j) + \lambda'_{ij}(\phi_i^\dagger\phi_j)(\phi_j^\dagger\phi_i) \quad (i = 1, 2, 3)$$

which is CP-conserving (real parameters),

$$V_{Z_2} = -\mu_{12}^2(\phi_1^\dagger\phi_2) + \lambda_1(\phi_1^\dagger\phi_2)^2 + \lambda_2(\phi_2^\dagger\phi_3)^2 + \lambda_3(\phi_3^\dagger\phi_1)^2 + h.c.$$

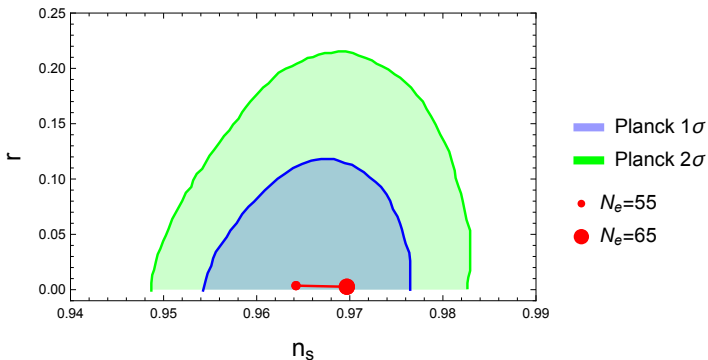
which is CP-violating (complex parameters).

The action of the model:

$$S_J = \int d^4x \sqrt{-g} \left[-\frac{1}{2} M_{pl}^2 R - D_\mu \phi_i^\dagger D^\mu \phi_i - V - \left(\xi_i |\phi_i|^2 + \underbrace{\xi_4(\phi_1^\dagger\phi_2)}_{Z_2\text{-symmetric}} + h.c. \right) R \right]$$

The sources of CP-violation are $\lambda_1 = |\lambda_1| e^{i\theta_1}$ and $\xi_4 = |\xi_4| e^{i\theta_4}$.

1σ and 2σ regions from Planck observation



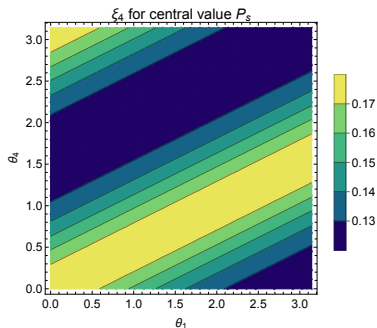
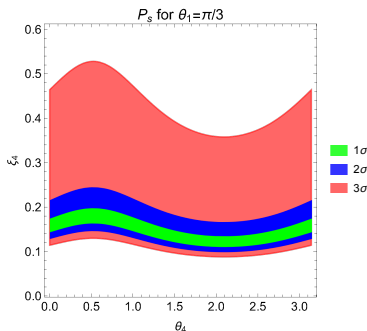
the

Tensor to scalar ratio $r = 16\epsilon$ and the **spectral index** $n_s = 1 - 6\epsilon + 2\eta$

calculated from the slow-roll parameters $\epsilon = \frac{1}{2} M_{pl}^2 \left(\frac{1}{\tilde{V}} \frac{d\tilde{V}}{d\tilde{A}} \right)^2$ and $\eta = M_{pl}^2 \frac{1}{\tilde{V}} \frac{d^2\tilde{V}}{d\tilde{A}^2}$

WMAP7 constraints on the scalar power spectrum P_s

$$P_s = \frac{1}{12 \pi^2 M_{pl}^6} \frac{(\tilde{v})^3}{(\tilde{v}')^2} = (2.430 \pm 0.091) \times 10^{-9}$$



In Higgs inflation: $|\xi| \simeq 4.785 \times 10^4 \sqrt{\lambda_h} \Rightarrow |\xi| \sim 10^3$

In our model: $|\xi_4| \simeq 4.785 \times 10^4 \sqrt{\lambda_i} \sqrt{X(\theta_1, \theta_4)} \Rightarrow |\xi_4| \sim 1/6$

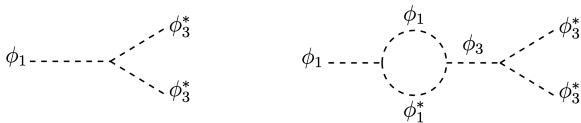
Reheating and scalar asymmetries

At the exit from inflation: doublets acquire an initial expectation value

$$\begin{cases} \phi_1 \rightarrow \phi_1 - a_1 e^{i\alpha} \\ \phi_1^\dagger \rightarrow \phi_1^* - a_1 e^{-i\alpha} \end{cases} \quad \begin{cases} \phi_2 \rightarrow \phi_2 - a_2 \\ \phi_2^\dagger \rightarrow \phi_2^* - a_2 \end{cases} \quad \begin{cases} \phi_3 \rightarrow \phi_3 - a_3 \\ \phi_3^\dagger \rightarrow \phi_3^* - a_3 \end{cases}$$

where the phase $\alpha = \alpha(\theta_1, \theta_4)$.

Instant reheating: the inflaton quickly decays to ϕ_3



Interference between tree & loop diagrams \Rightarrow unequal ϕ_3 & ϕ_3^* numbers

$$A_{CP}^1 = \Gamma_{(\phi_1 \rightarrow \phi_3^* \phi_3^*)}^{\text{tree+loop}} - \Gamma_{(\phi_1^* \rightarrow \phi_3 \phi_3)}^{\text{tree+loop}} \propto \sin(2\alpha + \theta_3)$$

Such asymmetries are then transferred to the fermion sector through the couplings of Higgs/W/Z with fermions.

A one-slide summary

Three scalar doublets:

$$\phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ h_1 + ih_{11} \end{pmatrix}, \quad \phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ h_2 + ih_{22} \end{pmatrix}, \quad \phi_3 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_h + h_3 \end{pmatrix}$$

Inflaton SM-Higgs

The potential:

$$V_0 = -\mu_i^2(\phi_i^\dagger \phi_i) + \lambda_{ii}(\phi_i^\dagger \phi_i)^2 + \lambda_{ij}(\phi_i^\dagger \phi_i)(\phi_j^\dagger \phi_j) + \lambda'_{ij}(\phi_i^\dagger \phi_j)(\phi_j^\dagger \phi_i)$$

$$V_{Z_2} = -\mu_{12}^2(\phi_1^\dagger \phi_2) + \lambda_1(\phi_1^\dagger \phi_2)^2 + \lambda_2(\phi_2^\dagger \phi_3)^2 + \lambda_3(\phi_3^\dagger \phi_1)^2 + h.c.$$



The sources of CP-violation are $\lambda_1 = |\lambda_1| e^{i\theta_1}$ and $\xi_4 = |\xi_4| e^{i\theta_4}$



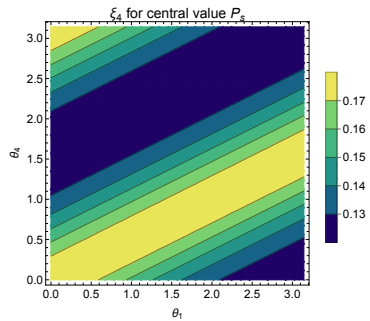
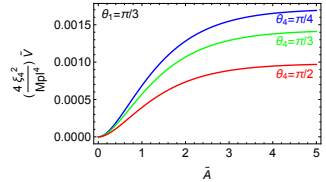
The action:

$$S_J = \int d^4x \sqrt{-g} \left[-\frac{1}{2} M_{pl}^2 R - D_\mu \phi_i^\dagger D^\mu \phi_i - V - \left(\xi_i |\phi_i|^2 + \underbrace{\xi_4(\phi_1^\dagger \phi_2)}_{Z_2\text{-symmetric}} + h.c. \right) R \right]$$

CP-violation inflation → ? Baryogenesis

The inflationary potential:

$$\tilde{V} = \left(\frac{M_{pl}^2}{2|\xi_4|} \right)^2 (1 - e^{-\bar{A}})^2 \underbrace{\chi(\theta_1, \theta_4)}_{\text{new}}$$



Summary

SM + scalar singlets

- Dark Matter **severely constrained**
- CP-violation **not possible**
- Inflation **DM incompatible**

2HDM: SM + a doublet

- Dark Matter **constrained & CPV incompatible**
- CP-violation **severely constrained & DM incompatible**
- Inflation **DM incompatible**

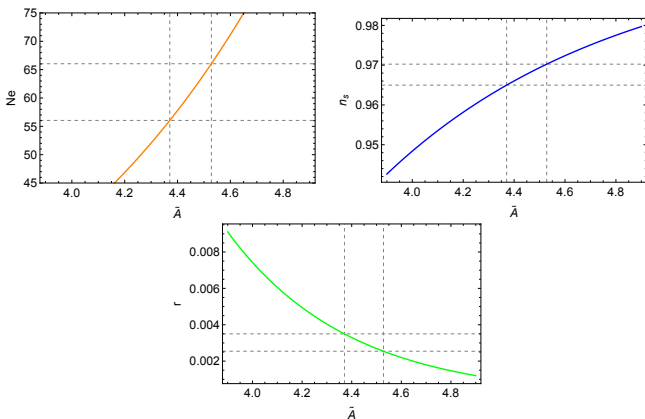
3HDM: SM + 2 doublets

- Dark Matter **CP-violating DM**
- CP-violation **unbounded dark CP-violation**
- Inflation **CP-violating inflation**
- Bonus: fermion mass hierarchy explanation

BACKUP SLIDES

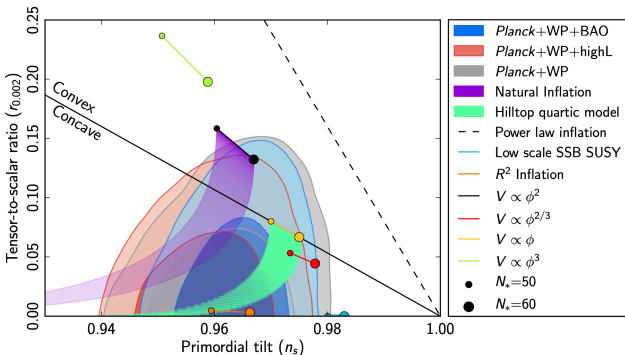
The slow roll parameters

number of e-folds N_e , the spectral index n_s , tensor to scalar ratio r



as a function of \tilde{N} with the $55 < N_e < 65$ grid-lines

Planck constraints on different inflationary models

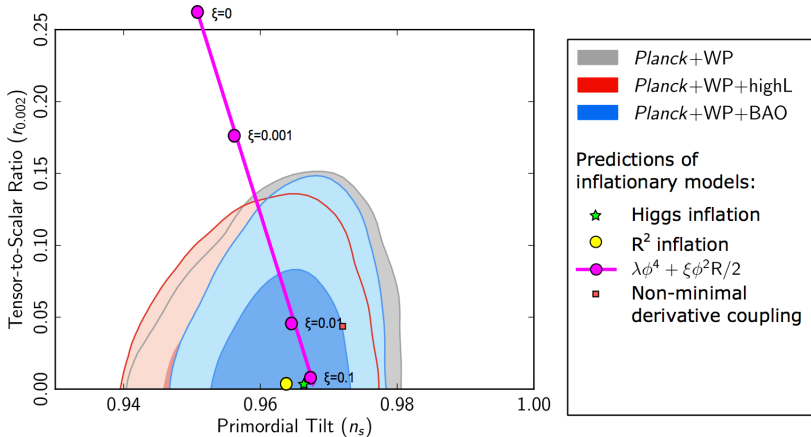


Tensor to scalar ratio $r = 16\epsilon$ and the **spectral index** $n_s = 1 - 6\epsilon + 2\eta$

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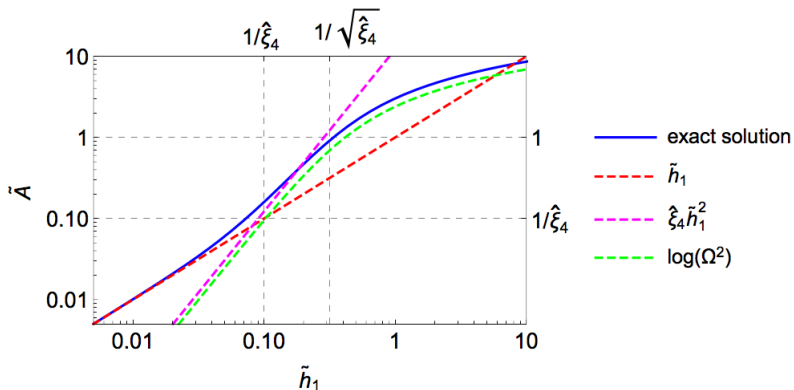
P. A. R. Ade *et al.* [Planck], [Astron. Astrophys. 571, A22 (2014)]

Other inflationary models



F. Bezrukov, [Class. Quant. Grav. 30, 214001 (2013)]

Reheating



Roadmap

Scalar extensions with or without a Z_2 symmetry:

- SM + scalar singlet(s)

- $\phi_{SM}, S \Rightarrow DM, CPV$

- $\phi_{SM}, S_1, S_2 \Rightarrow DM, CPV$

- 2HDM: SM + scalar doublet

- $\phi_1, \phi_2 \Rightarrow DM, CPV$

- $\phi_1, \phi_2 \Rightarrow DM, CPV$

- 3HDM: SM + 2 scalar doublets

- $\phi_1, \phi_2, \phi_3 \Rightarrow DM, CPV$

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Roadmap

- SM + scalar singlets
 - Dark Matter **severely constrained**
 - CP-violation **not possible**
 - Strong first order EWPT **constrained & DM incompatible**
- 2HDM: SM + a doublet
 - Dark Matter **constrained & CPV incompatible**
 - CP-violation **severely constrained & DM incompatible**
 - Strong first order EWPT **severely constrained**
- 3HDM: SM + 2 doublets
 - Dark Matter **many exotic possibilities**
 - CP-violation **unbounded dark CP-violation**
 - Strong first order EWPT **easily achieved**
 - Inflaton **easily achieved + exotic possibilities**

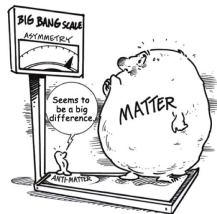
Baryon asymmetry in the universe

Sakharov's conditions for a successful baryogenesis mechanism:

- B-violation
- C & CP-violation
- Departure from thermal equilibrium

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$V_{ub} \neq V_{ub}^*; V_{td} \neq V_{td}^* \Rightarrow \text{CPV}$$



Observation $\frac{N(B)}{N(\gamma)} \approx 10^{-9} \gg 10^{-20}$ provided by the SM
 \Rightarrow **New sources of CPV needed.**

Dark Matter

We know it exists because of:

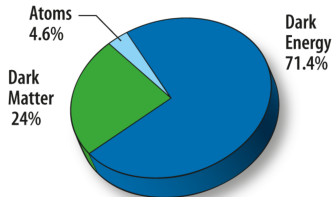
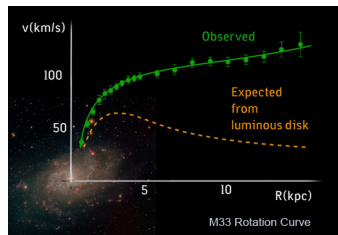
- galactic rotation curves
- the CMB pattern
- ...

None of the SM particles
are suitable DM candidates.

⇒ Beyond the SM

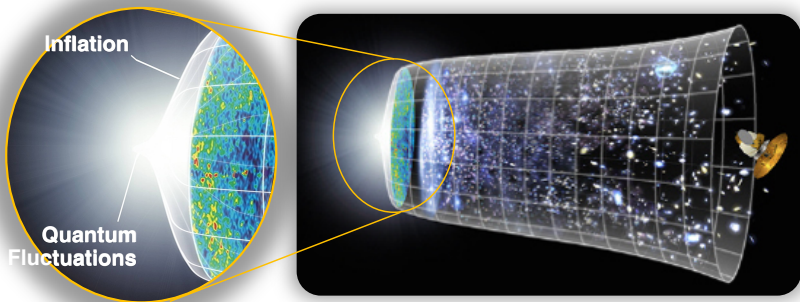
Weakly Interacting Massive Particles
(WIMPs)

$\underbrace{DM DM \rightarrow SM SM,}_{\text{pair annihilation}} \quad \underbrace{DM \not\rightarrow SM, \dots}_{\text{stable}}$



back

Inflation: an exponential expansion in the early universe



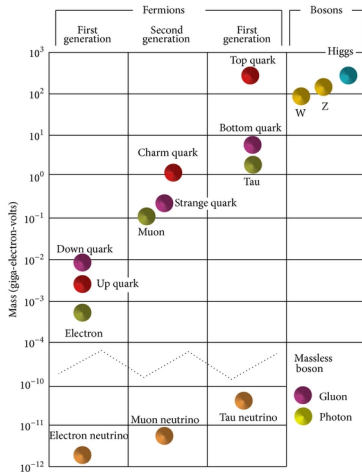
Explains: generation of primordial density fluctuations seeding structure formation, the flatness, homogeneity and isotropy of the universe

back

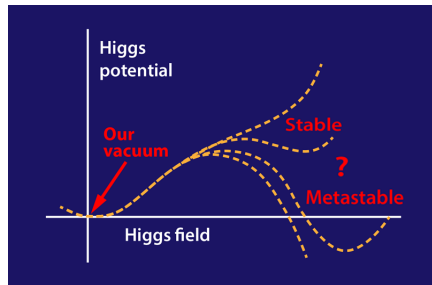
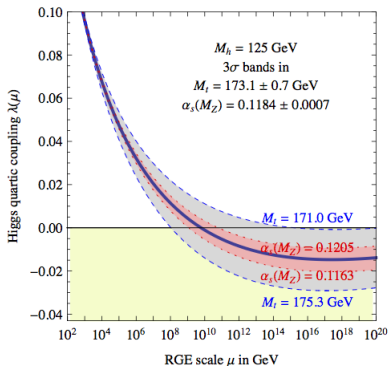
Fermion mass hierarchy in the SM

No explanation for

- $m_t/m_e \approx 10^6$
- $m_t/m_\nu \approx 10^{11}$



The SM electroweak vacuum is not stable



$$V = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$

\Rightarrow Scalar extensions can stabilise the EW vacuum.

back

D. Buttazzo, G. Degrandi, P. P. Giardino, G. F. Giudice, F. Sala, A. Salvio, A. Strumia [JHEP 1312, 089 (2013)]

Scalar singlet extension of SM

the SM Higgs doublet + a scalar singlet

 ϕ
 S

$$\phi = \begin{pmatrix} G^+ \\ \frac{h+iG^0}{\sqrt{2}} \end{pmatrix}$$

$$S = \begin{pmatrix} s \\ \sqrt{2} \end{pmatrix}$$

$S S \rightarrow \text{SM SM}$,
pair annihilation

$S \not\rightarrow \text{SM SM}$
stable

back

SM + scalar singlet

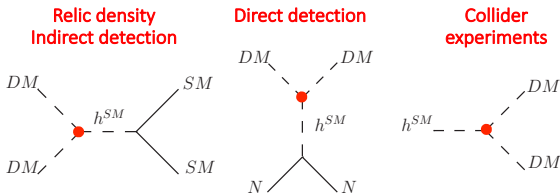
DM ✓, CPV ×

DM protected by a Z_2 symmetry (+, -) from decaying to SM particles.

SM fields \rightarrow SM fields, $\phi \rightarrow \phi$, $S \rightarrow -S$

The Lagrangian and the vacuum are Z_2 symmetric: $\langle \phi \rangle = v$, $\langle S \rangle = 0$

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{2}(\partial S)^2 - m_s^2 S^2 - \lambda_s S^4 - \lambda_{hs} \phi^2 S^2$$



Tension: all relevant interactions are governed by the same coupling!

2-Higgs doublet models (2HDMs)

the SM Higgs doublet + a scalar doublet

 ϕ_1 ϕ_2

$$\phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG^0}{\sqrt{2}} \end{pmatrix} \quad \phi_2 = \begin{pmatrix} H^+ \\ \frac{H+iA}{\sqrt{2}} \end{pmatrix}$$

Z_2 -symmetric 2HDM

DM ✓, CPV ×

DM is protected by a Z_2 symmetry (+, -) from decaying to SM particles:

$$\text{SM fields} \rightarrow \text{SM fields}, \quad \phi_1 \rightarrow \phi_1, \quad \phi_2 \rightarrow -\phi_2$$

Z_2 symmetry: only ϕ_1 couples to fermions $\phi_u = \phi_d = \phi_e = \phi_1$

$$-\mathcal{L}_{Yukawa} = Y_u \bar{Q}'_L i\sigma_2 \phi_u^* u'_R + Y_d \bar{Q}'_L \phi_d d'_R + Y_e \bar{L}'_L \phi_e e'_R + \text{h.c.}$$

Z_2 symmetry respected by the vacuum: $\phi_1 = \begin{pmatrix} G^+ \\ \frac{v+h+iG^0}{\sqrt{2}} \end{pmatrix}$, $\phi_2 = \begin{pmatrix} H^+ \\ \frac{H+iA}{\sqrt{2}} \end{pmatrix}$

DM candidate: the lightest neutral particle from the dark doublet

$$HH \rightarrow h \rightarrow \text{SM}, \quad HA \rightarrow Z \rightarrow \text{SM}, \quad HH^\pm \rightarrow W^\pm \rightarrow \text{SM}$$

Tension: all scalar interactions are governed by the same coupling!
Gauge couplings are fixed!

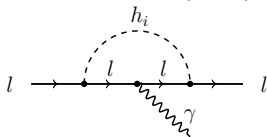
CP-violating 2HDM

DM ×, CPV ✓

Break the Z_2 symmetry and let the two doublets mix

$$\phi_1 = \left(\begin{array}{c} \phi_1^+ \\ \frac{v_1 + h_1^0 + ia_1^0}{\sqrt{2}} \end{array} \right), \quad \phi_2 = \left(\begin{array}{c} \phi_2^+ \\ \frac{v_2 + h_2^0 + ia_2^0}{\sqrt{2}} \end{array} \right)$$

No Dark Matter candidate!

Mixing doublets means h_i (mixtures of $h_{1,2}^0, a_{1,2}^0$) are CP-mixed states

contributing to electric dipole moments (EDMs).

CP-violation is very constrained!

back

3-Higgs doublet models (3HDMs)

two scalar doublets + the SM Higgs doublet

ϕ_1, ϕ_2

ϕ_3

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{h + iG^0}{\sqrt{2}} \end{pmatrix}$$

Z_2 -symmetric 3HDM with dark CPV

DM ✓, CPV ✓

DM is protected by a Z_2 symmetry $(-, -, +)$:

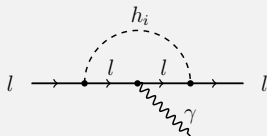
$$\phi_1 \rightarrow -\phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \text{SM fields} \rightarrow \text{SM fields}, \quad \phi_3 \rightarrow \phi_3$$

 Z_2 symmetry respected by the vacuum $(0, 0, v)$:

$$\phi_1 = \left(\begin{array}{c} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{array} \right), \quad \phi_2 = \left(\begin{array}{c} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{array} \right), \quad \phi_3 = \left(\begin{array}{c} G^+ \\ \frac{v+h+iG^0}{\sqrt{2}} \end{array} \right)$$

Only ϕ_3 can couple to fermions $\phi_u = \phi_d = \phi_e = \phi_3$ and $h_i = h$

$$\begin{aligned} -\mathcal{L}_{Yukawa} = & Y_u \bar{Q}'_L i\sigma_2 \phi_u^* u'_R \\ & + Y_d \bar{Q}'_L \phi_d d'_R \\ & + Y_e \bar{L}'_L \phi_e e'_R + \text{h.c.} \end{aligned}$$

**No contributions to electric dipole moments (EDMs)**

back

Z_2 -symmetric 3HDM with dark CPV

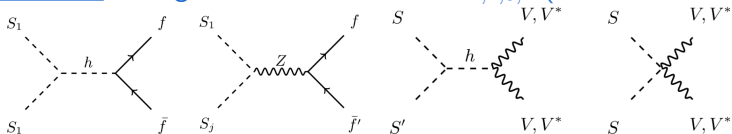
DM ✓, CPV ✓

DM is protected by a Z_2 symmetry $(-, -, +)$:

$$\phi_1 \rightarrow -\phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \text{SM fields} \rightarrow \text{SM fields}, \quad \phi_3 \rightarrow \phi_3$$

 Z_2 symmetry respected by the vacuum $(0, 0, v)$:

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{v+h+iG^0}{\sqrt{2}} \end{pmatrix}$$

DM candidate: the lightest CP-mixed state $S_{1,2,3,4}$ (mixtures of $H_{1,2}, A_{1,2}$)

Tension released: the extended dark sector allows for annihilations, co-annihilations and CP-violation!

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