

Effective field theories for multi-field inflation

Jinn-Ouk Gong

Ewha Womans University
Seoul 03760, Korea

Dark Side of the Universe 2022
University of New South Wales, Australia
8th December, 2022

Outline

- 1 Introduction
- 2 EFT for multi-field inflation: Adiabatic study
 - How to construct top-down EFT
 - Validity of EFT
 - Correlation of correlation functions
- 3 Benchmark scenario for non-adiabaticity: Hybrid inflation
 - Multi-field dynamics in hybrid inflation
 - Regimes of different EFTs
 - Construction of EFT
 - Effects of quantum corrections
- 4 Conclusions

- 1 Introduction
- 2 EFT for multi-field inflation: Adiabatic study
 - How to construct top-down EFT
 - Validity of EFT
 - Correlation of correlation functions
- 3 Benchmark scenario for non-adiabaticity: Hybrid inflation
 - Multi-field dynamics in hybrid inflation
 - Regimes of different EFTs
 - Construction of EFT
 - Effects of quantum corrections
- 4 Conclusions

Why inflation?

Inflation can provide otherwise finely tuned initial conditions

Hot big bang

- Horizon problem
- Flatness problem
- Monopole problem
- Initial perturbations

Inflation

- Single causal patch
- Locally flat
- Diluted away
- Quantum fluctuations

Predictions of inflation are consistent with recent observations

Why multi-field inflation?

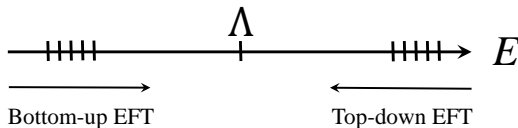
- No inflaton candidate in the standard model (cf. Higgs?)
- Typically BSM contains a number of scalar fields
- Rich phenomenologies, detectable signatures

We have both theoretical and observational motivations

Why effective field theory for inflation?

- $E_{\text{inflation}} (\sim 10^{15} \text{ GeV?}) \gg E_{\text{LHC}} = 14 \text{ TeV}$
- Hundreds of inflation models in the market
- Universality of EFT is very powerful

cf. S. Mukohyama's talk on Tue

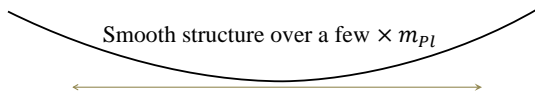


Universal features of heavy physics?

Why bothering EFT description?

Observations prefer smooth inflation with large enough regime

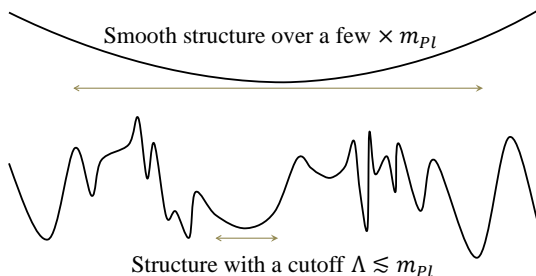
$$\mathcal{L}_{\text{eff}}[\phi] = \underbrace{\mathcal{L}_0[\phi]}_{\text{smooth}}$$



Why bothering EFT description?

Observations prefer smooth inflation with large enough regime

$$\mathcal{L}_{\text{eff}}[\phi] = \underbrace{\mathcal{L}_0[\phi]}_{\text{smooth}} + \underbrace{\sum_n c_n \frac{\mathcal{O}_n[\phi]}{\Lambda^{n-4}}}_{\text{EFT allows these}}$$



EFT introduces sub-cutoff structure: **tension with observations**

What kind of EFT?

Single field inflation
in Einstein gravity

What kind of EFT?

Single (multi) field inflation
No gravity effect
Symmetry principles
(Senatore et al.)

effective

Single field inflation
in Einstein gravity

What kind of EFT?

Single (multi) field inflation
 No gravity effect
 Symmetry principles
 (Senatore et al.)

Single field inflation
 in higher order gravity
 (Weinberg)

effective

effective

Single field inflation
 in Einstein gravity

What kind of EFT?

Single (multi) field inflation
 No gravity effect
 Symmetry principles
 (Senatore et al.)

Single field inflation
 in higher order gravity
 (Weinberg)

effective

effective

Single field inflation
 in Einstein gravity
 Strong adiabaticity

What kind of EFT?

Single (multi) field inflation
 No gravity effect
 Symmetry principles
 (Senatore et al.)

Single field inflation
 in higher order gravity
 (Weinberg)

Single field inflation
 in Einstein gravity
 Strong adiabaticity

Multi-field inflation
 in Einstein gravity
 Weaker or broken adiabaticity

effective

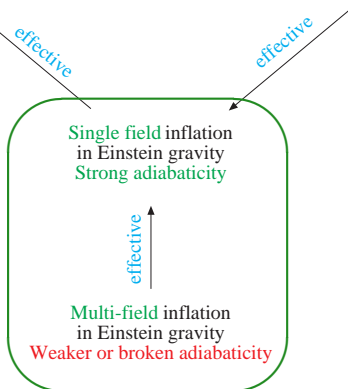
effective

effective

What kind of EFT?

Single (multi) field inflation
 No gravity effect
 Symmetry principles
 (Senatore et al.)

Single field inflation
 in higher order gravity
 (Weinberg)



Our focus

- 1 Introduction
- 2 EFT for multi-field inflation: Adiabatic study
 - How to construct top-down EFT
 - Validity of EFT
 - Correlation of correlation functions
- 3 Benchmark scenario for non-adiabaticity: Hybrid inflation
 - Multi-field dynamics in hybrid inflation
 - Regimes of different EFTs
 - Construction of EFT
 - Effects of quantum corrections
- 4 Conclusions

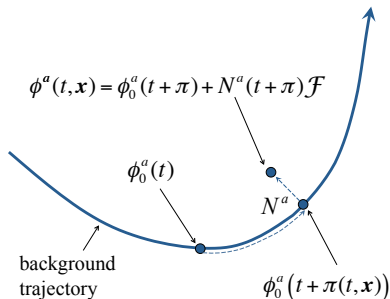
Adiabatic EFT recipe

☺ Recipe for top-down EFT ☺

- ① Write the action in terms of \mathcal{R} (along traj) and \mathcal{F} (off traj)
- ② Integrate out \mathcal{F} : $e^{S_{\text{eff}}[\mathcal{R}]} = \int [D\mathcal{F}] e^{S[\mathcal{R}, \mathcal{F}]}$
- ③ Effective single field action $S_{\text{eff}}[\mathcal{R}]$

More about recipe 1

- Write the action in terms of \mathcal{R} (along traj) and \mathcal{F} (off traj)



- \mathcal{R} : Curvature (or adiabatic) pert, related to π by $\mathcal{R} = -H\pi$
- \mathcal{F} : "Orthogonal" to the trajectory and hence to \mathcal{R}

More about recipe 2

② Integrate out \mathcal{F} : $e^{\text{Seff}[\mathcal{R}]} = \int [D\mathcal{F}] e^{S[\mathcal{R}, \mathcal{F}]}$

Equivalent to plugging the (linear) solution of \mathcal{F} back to the action

$$\underbrace{(-\square + M_{\text{eff}}^2)}_{\text{From quadratic terms purely in } \mathcal{F}} \mathcal{F} = \underbrace{-2\dot{\theta} \frac{\dot{\phi}_0}{H} \dot{\mathcal{R}}}_{\text{From the interaction with } \mathcal{R}}$$

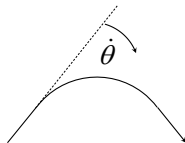
From quadratic terms purely in \mathcal{F}

From the interaction with \mathcal{R} : $S_2 \supset \int d^4x (-2\dot{\theta} \frac{\dot{\phi}_0}{H} \dot{\mathcal{R}} \mathcal{F})$

$\dot{\theta}$: angular velocity of trajectory

$\dot{\theta} = 0$: Straight, single field

$\dot{\theta} \neq 0$: Any deviations appear

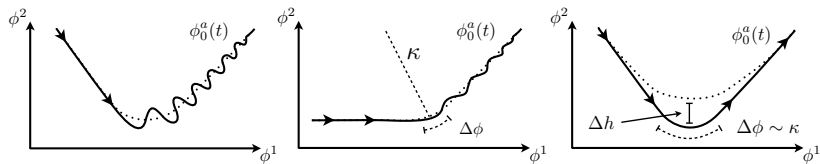


Q: Is replacing the solution of \mathcal{F} always **valid**?

More about recipe 2, cont: Validity of EFT

Truncation in \square/M_{eff}^2 : Non-local \rightarrow higher derivative theory

$$\mathcal{F} = \frac{-2\dot{\theta}(\dot{\phi}_0/H)}{-\square + M_{\text{eff}}^2} \dot{\mathcal{R}} = \frac{-2\dot{\theta}(\dot{\phi}_0/H)}{M_{\text{eff}}^2} \left[1 + \frac{\square}{M_{\text{eff}}^2} + \dots \right] \dot{\mathcal{R}}$$



Valid for “adiabatic trajectory”: M_{eff}^2 is most important, or

$$\left| \frac{\ddot{\theta}}{\dot{\theta}} \right| \ll M_{\text{eff}} \rightarrow \frac{\dot{\theta}^2}{M_{\text{eff}}^2} \gg 1 \text{ is OK (strong turn)}$$

More about recipe 3

- ③ Effective single field action $S_{\text{eff}}[\mathcal{R}]$

$$S_{\text{eff}}[\mathcal{R}] = \int d^4x a^3 \epsilon m_{\text{pl}}^2 \left[\left(1 + \frac{4\dot{\theta}^2}{M_{\text{eff}}^2} \right) \dot{\mathcal{R}}^2 + \dots \right]$$

Effects of heavy physics in “**speed of sound**”

$$c_s^{-2} \equiv 1 + \frac{4\dot{\theta}^2}{M_{\text{eff}}^2} \quad (\gg 1, \text{ possibly})$$

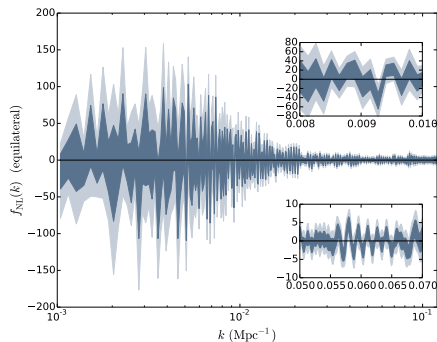
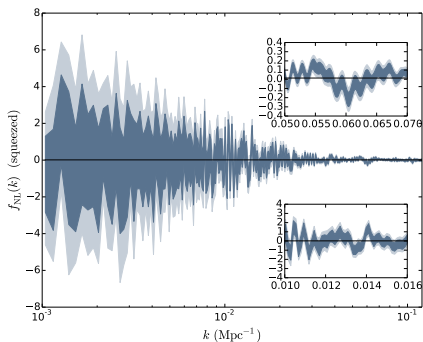
Manifest correlation between 2- & 3-point functions

Since the (deviation from scale-inv) $P_{\mathcal{R}}$ is specified by c_s , we can find c_s in terms of $P_{\mathcal{R}}$ and 3-pt fct is **completely fixed** by 2-pt fct

$$f_{\text{NL}}(k_1, k_2, k_3) = c_0^\Delta(\mathbf{k}) \log P_{\mathcal{R}} + c_1^\Delta(\mathbf{k}) \frac{d \log P_{\mathcal{R}}}{d \log k} + c_2^\Delta(\mathbf{k}) \frac{d^2 \log P_{\mathcal{R}}}{d \log k^2}$$

We only need precise measurement on $\mathcal{P}_{\mathcal{R}}(k)$

Reconstructed 3-pt function directly from CMB data



Marginal 2σ hints in the 3-pt fct at $k \sim 0.014$ Mpc $^{-1}$ and 0.06 Mpc $^{-1}$

- 1 Introduction
- 2 EFT for multi-field inflation: Adiabatic study
 - How to construct top-down EFT
 - Validity of EFT
 - Correlation of correlation functions
- 3 Benchmark scenario for non-adiabaticity: Hybrid inflation**
 - Multi-field dynamics in hybrid inflation
 - Regimes of different EFTs
 - Construction of EFT
 - Effects of quantum corrections
- 4 Conclusions

Why hybrid inflation?

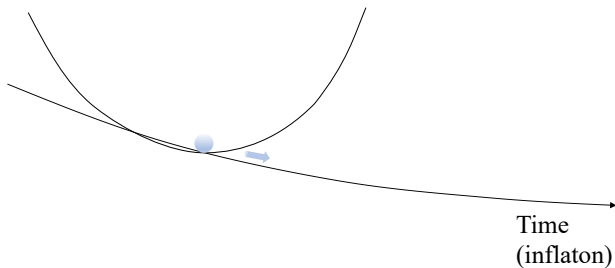
- (Relatively) realized easily, e.g. in SUSY / SUGRA
- Connections to particle physics
- Rich structure and phenomenology

How hybrid inflation proceeds



Inflation is occurring...

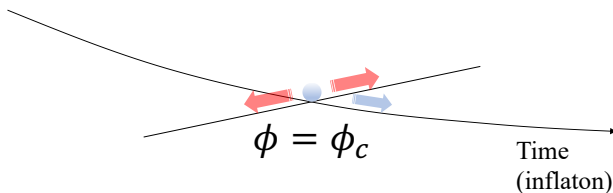
How hybrid inflation proceeds



Inflation is still occurring...

How hybrid inflation proceeds

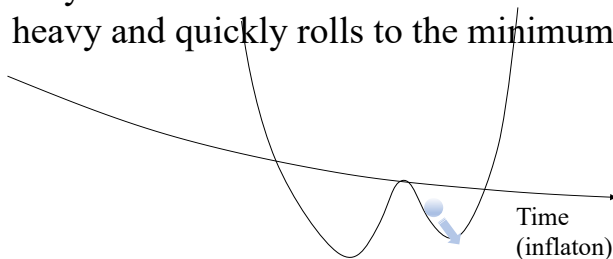
The direction orthogonal to the inflaton becomes massless



“Waterfall” phase transition

How hybrid inflation proceeds

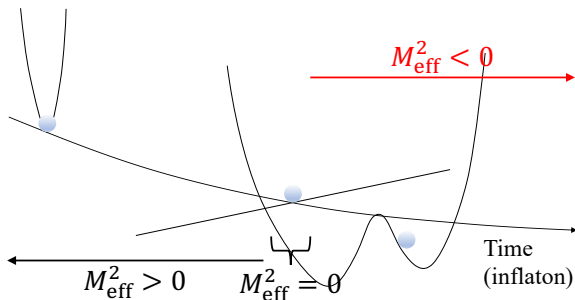
Very soon the waterfall field becomes heavy and quickly rolls to the minimum



- 2-field dynamics is essential, and cannot be integrated out
- At the heart of our picture lies the classical approximation
- **Q: Does the classical approximation remain *valid*?**

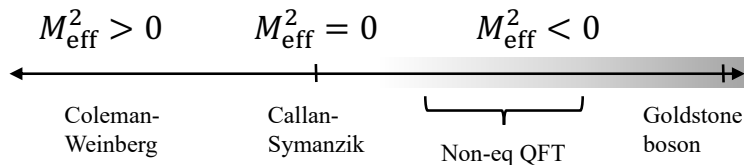
Regimes of different waterfall masses

Let M_{eff}^2 the effective mass squared of the waterfall field χ



- $\phi > \phi_c$: $M_{\text{eff}}^2 > 0$ so is trapped at $\chi = 0$
- $\phi = \phi_c$: $M_{\text{eff}}^2 = 0$ and waterfall transition occurs
- $\phi < \phi_c$: $M_{\text{eff}}^2 < 0$ and is tachyonic

Regimes of different EFTs



- $M_{\text{eff}}^2 > 0$: χ is integrated out, we find CW-type (Burgess, Cline, Holman 2003)
- $M_{\text{eff}}^2 = 0$: log diverges, resummed using CS eq (e.g. Peskin & Schroeder)
- $M_{\text{eff}}^2 < 0$: Just shift the background χ_0 when V_{eff} is minimized?

How to compute the effective potential

We take standard steps for one-loop corrected effective potential

$$\textcircled{1} \quad \text{2-field potential } V(\phi, \chi) = \underbrace{V_{\text{inf}}(\phi)}_{= \frac{1}{2} m^2 \phi^2} + \frac{\lambda}{4} \left(\frac{M^2}{\lambda} - \chi^2 \right)^2 + \frac{1}{2} g^2 \phi^2 \chi^2$$

(so that $M_{\text{eff}}^2 \equiv g^2 \phi^2 - M^2$)

$\textcircled{2}$ Expand $\chi = \chi_0 + \delta\chi$ with $\langle \chi \rangle = \chi_0$, and integrate over $\delta\chi$

$\textcircled{3}$ Regularize divergences

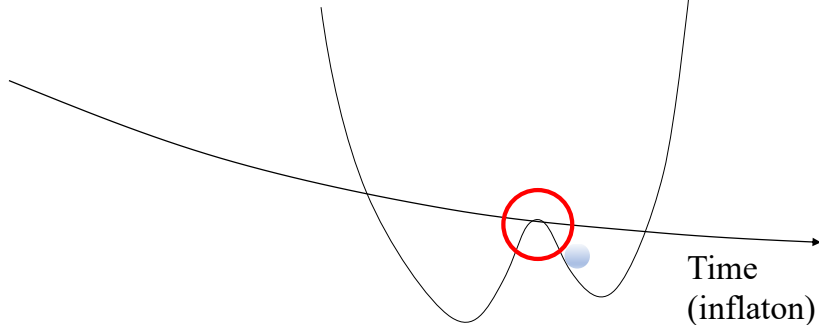
One-loop corrected effective potential

$$\begin{aligned}
 V_{\text{eff}}(\chi) = & -\frac{1}{2} |M_{\text{eff}}^2(\phi)| \chi_0^2 + \frac{\lambda}{4} \chi_0^4 \\
 & + \frac{1}{4(4\pi)^2} \left[-|M_{\text{eff}}^2(\phi)| + 3\lambda\chi_0^2 \right]^2 \left\{ \underbrace{\log \left[\frac{-|M_{\text{eff}}^2(\phi)| + 3\lambda\chi_0^2}{\Lambda^2} \right]}_{= i\pi + \log \left[\frac{|M_{\text{eff}}^2(\phi)| - 3\lambda\chi_0^2}{\Lambda^2} \right]} - \frac{3}{2} \right\}
 \end{aligned}$$

- V_{eff} is valid as long as the $|\chi_0| \lesssim |M_{\text{eff}}| / \sqrt{3\lambda}$
(N.B. Min at $\chi_0 = \pm |M_{\text{eff}}| / \sqrt{\lambda}$)
- As waterfall begins ($\chi_0 \sim 0$), log is imaginary but remains small
- $\Im V_{\text{eff}}$ is related to vacuum decay rate (Weinberg and Wu, 1987)

Validity of our EFT

Our EFT is valid near the top



Consistency check

- 1 Is backreaction to gravity under control? YES
- 2 Does the BG field grow exponentially? YES (those up to $k < m$)
- 3 Is the slow-roll maintained at the beginning?

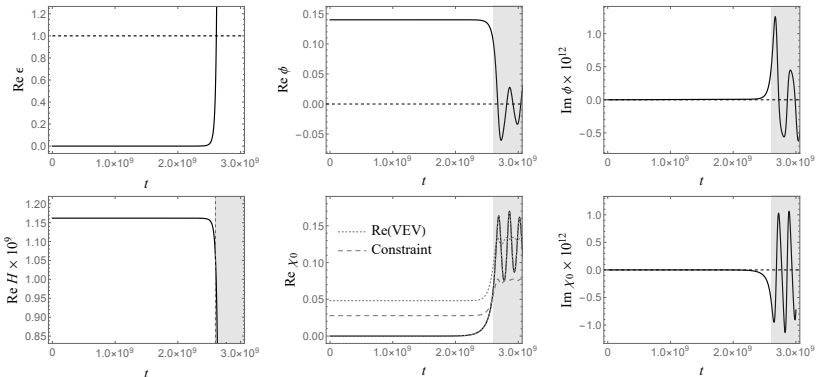
$$\frac{m}{g} \gtrsim \frac{M}{4\sqrt{\pi}}$$

Otherwise, $\delta\chi$ dominates and **classical approx breaks down**

Example 1: SR inflation after waterfall transition

SR inflation proceeds after waterfall transition (Clesse 2011, Kodama et al 2011)

$$\lambda = 5 \times 10^{-14}, \quad g = 2 \times 10^{-7}, \quad M = 3 \times 10^{-8} m_{\text{Pl}}, \quad m = 8 \times 10^{-12} m_{\text{Pl}}$$

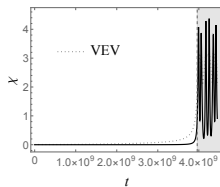
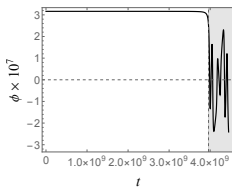
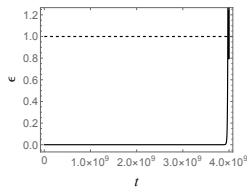


No significant effects at all

Example 2: Immediate end after waterfall transition

Standard result we expect from long time ago (Linde 1994)

$$\lambda = 10^{-1}, \quad g = 10^{-1/2}, \quad M = 10^{-7} m_{\text{pl}}, \quad m = 10^{-16} m_{\text{pl}}$$

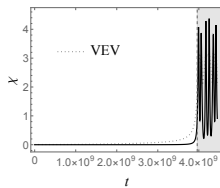
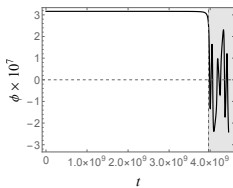
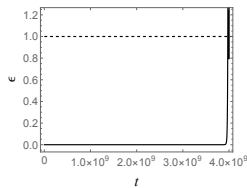


Without quantum effects, inflation ends immediately after $\phi = \phi_c$

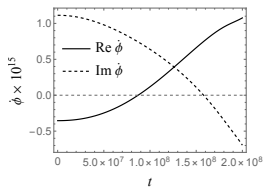
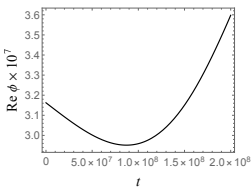
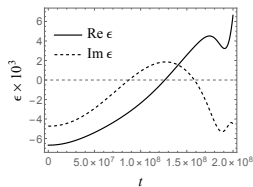
Example 2: Immediate end after waterfall transition

Standard result we expect from long time ago (Linde 1994)

$$\lambda = 10^{-1}, \quad g = 10^{-1/2}, \quad M = 10^{-7} m_{\text{Pl}}, \quad m = 10^{-16} m_{\text{Pl}}$$



Without quantum effects, inflation ends immediately after $\phi = \phi_c$

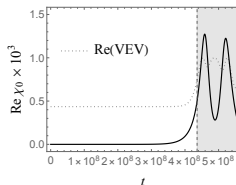
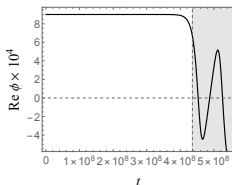
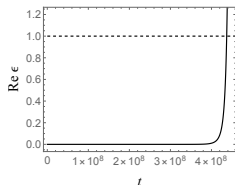


Quantum effects dominate from the beginning

Example 3: Constraint enforced

We impose $\phi < M/g$ and $m/g > M/(4\sqrt{\pi})$:

$$\lambda = 10^{-8}, \quad g = 10^{-4}, \quad M = 10^{-7} m_{\text{Pl}}, \quad m = 10^{-11} m_{\text{Pl}}$$



Classical approximation is valid

- 1 Introduction
- 2 EFT for multi-field inflation: Adiabatic study
 - How to construct top-down EFT
 - Validity of EFT
 - Correlation of correlation functions
- 3 Benchmark scenario for non-adiabaticity: Hybrid inflation
 - Multi-field dynamics in hybrid inflation
 - Regimes of different EFTs
 - Construction of EFT
 - Effects of quantum corrections
- 4 Conclusions

Conclusions

- EFT is a powerful tool, for (multi-field) inflation too
- Adiabatic EFT for multi-field inflation
 - Bottom-up and top-down approaches
 - Universal features described in the speed of sound
 - Correlation of correlation functions
- Broken adiabaticity: EFT for hybrid inflation
 - Different regimes of hybrid inflation allows different EFTs
 - Breakdown of EFT when quantum effects dominate
 - Classical considerations are never enough