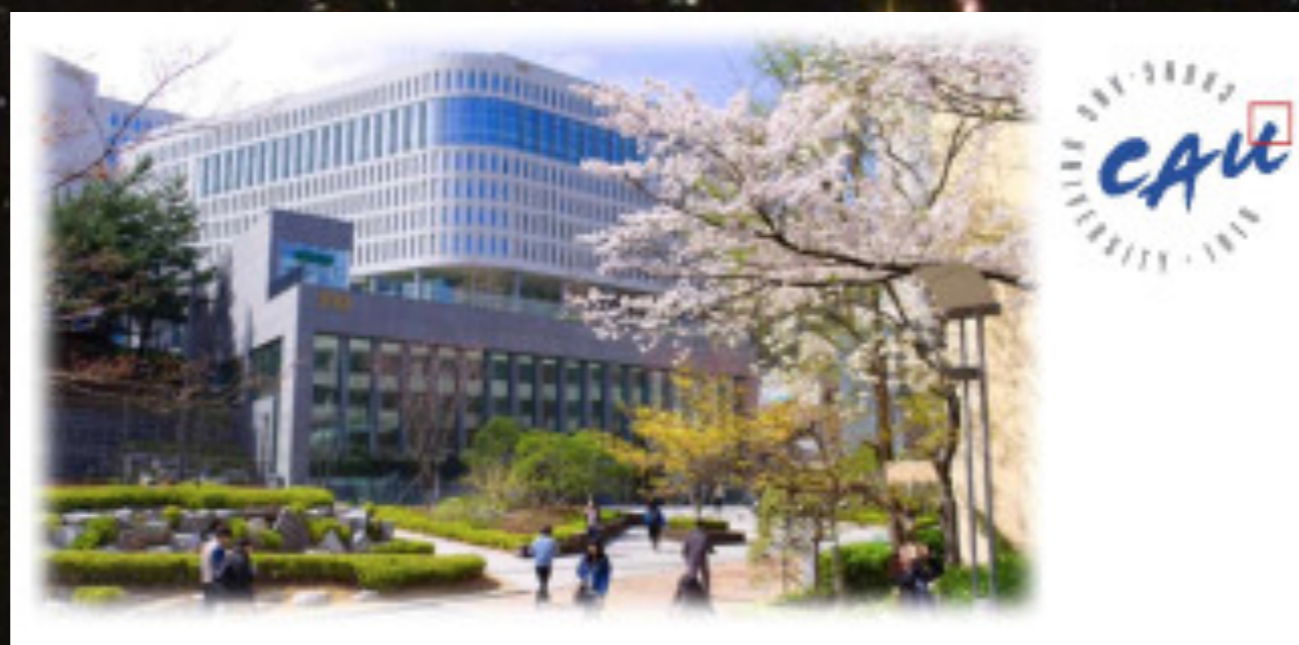
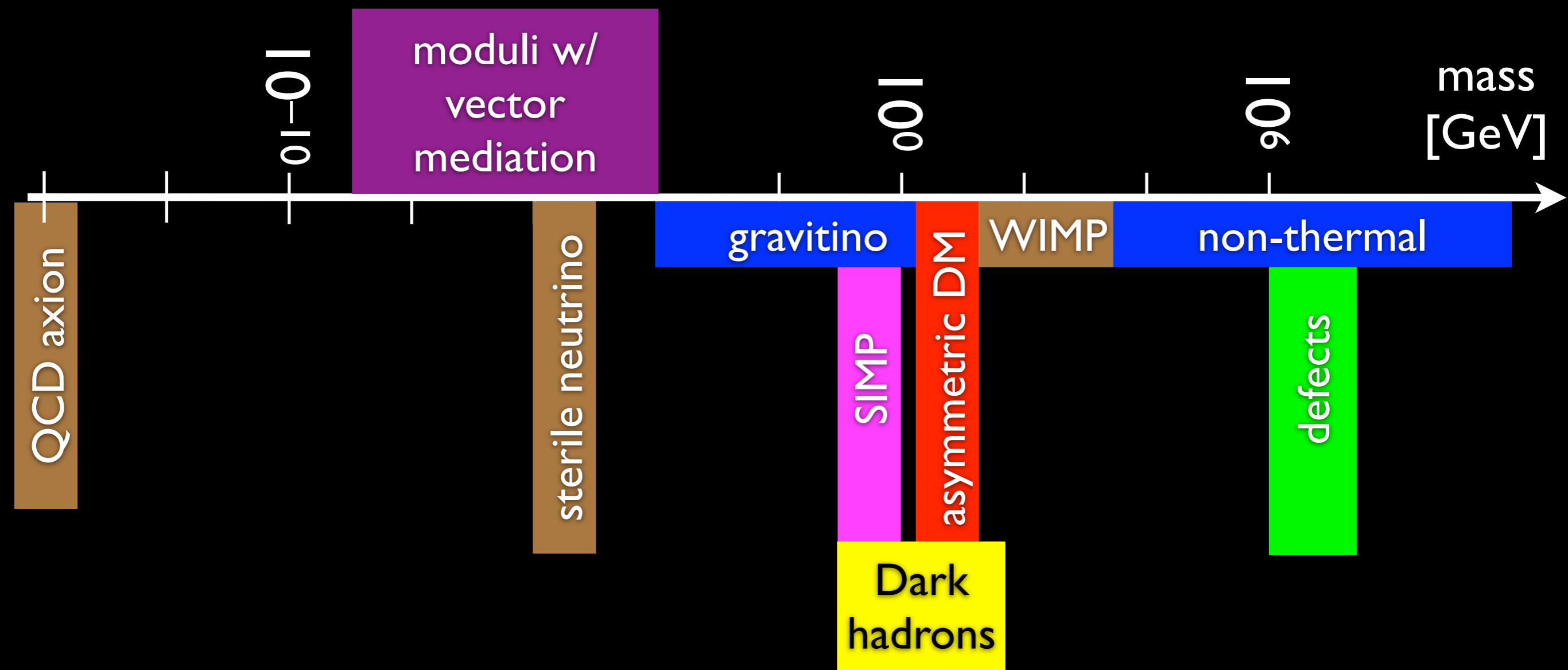
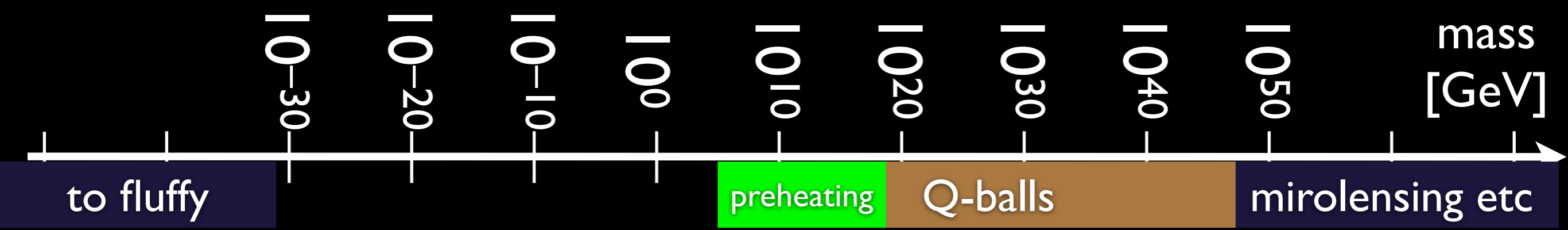


# Fun with Composite Dark Matter



Hitoshi Murayama (Berkeley, Kavli IPMU)  
2022 CAU BSM Workshop  
Feb 8, 2022



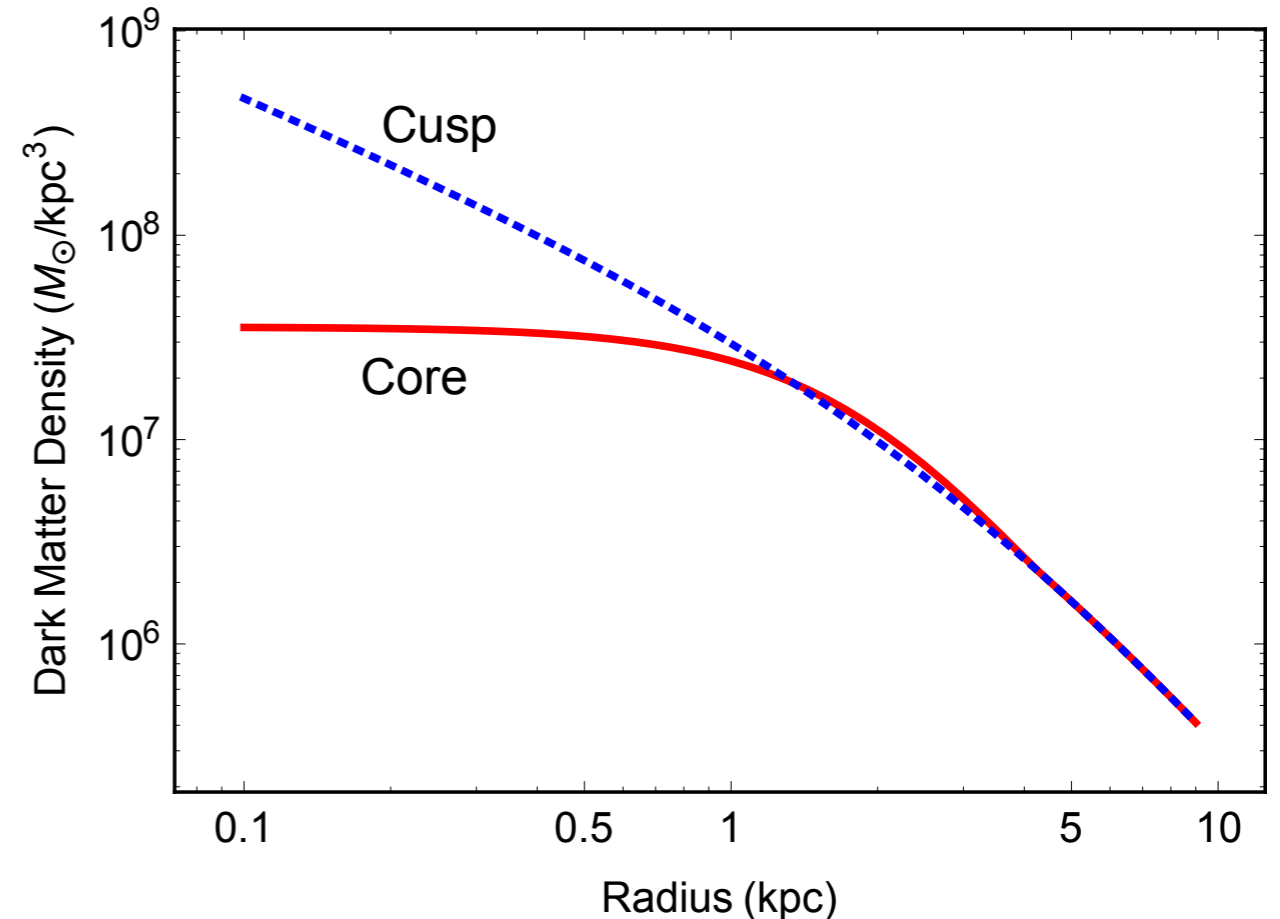
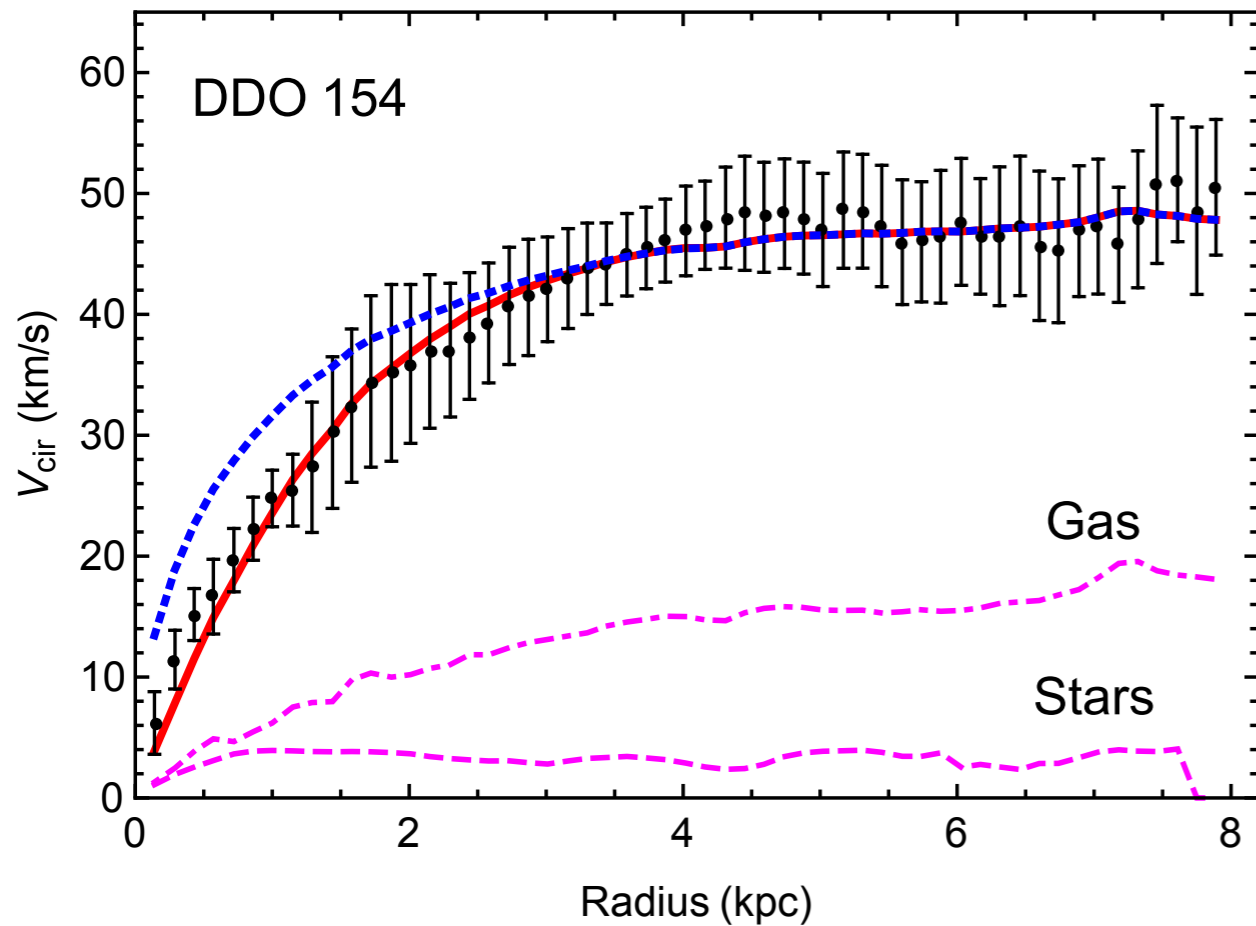
*Can't do justice to many many ideas in the literature!*

# Why Composite?

- **QCD is beautiful.** Nature may use it again
- **Self-interacting dark matter**
  - large cross section and light dark matter:  
Dark QCD is perfect
  - velocity dependence may need resonance:  
Dark QCD can provide it
- **asymmetric dark matter**
  - need to shed symmetric component:  
Easy for Dark QCD
- Also hierarchy problem, baryon asymmetry



# DDO 154 dwarf galaxy



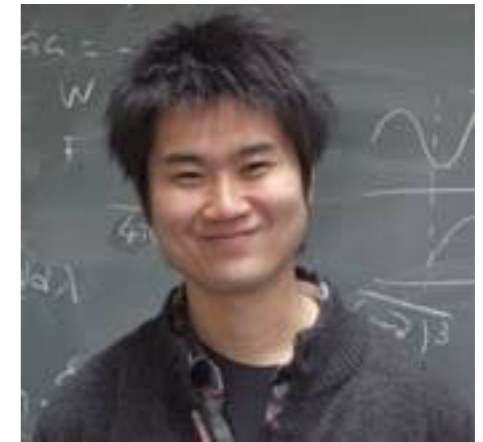
can be explained if dark matter scatters against itself  
Need Self-Interacting Dark Matter  $\sigma/m \sim 1 \text{ b} / \text{GeV}$   
(Spergel, Steinhardt astro-ph/9909386)  
if true, only astrophysical information beyond gravity



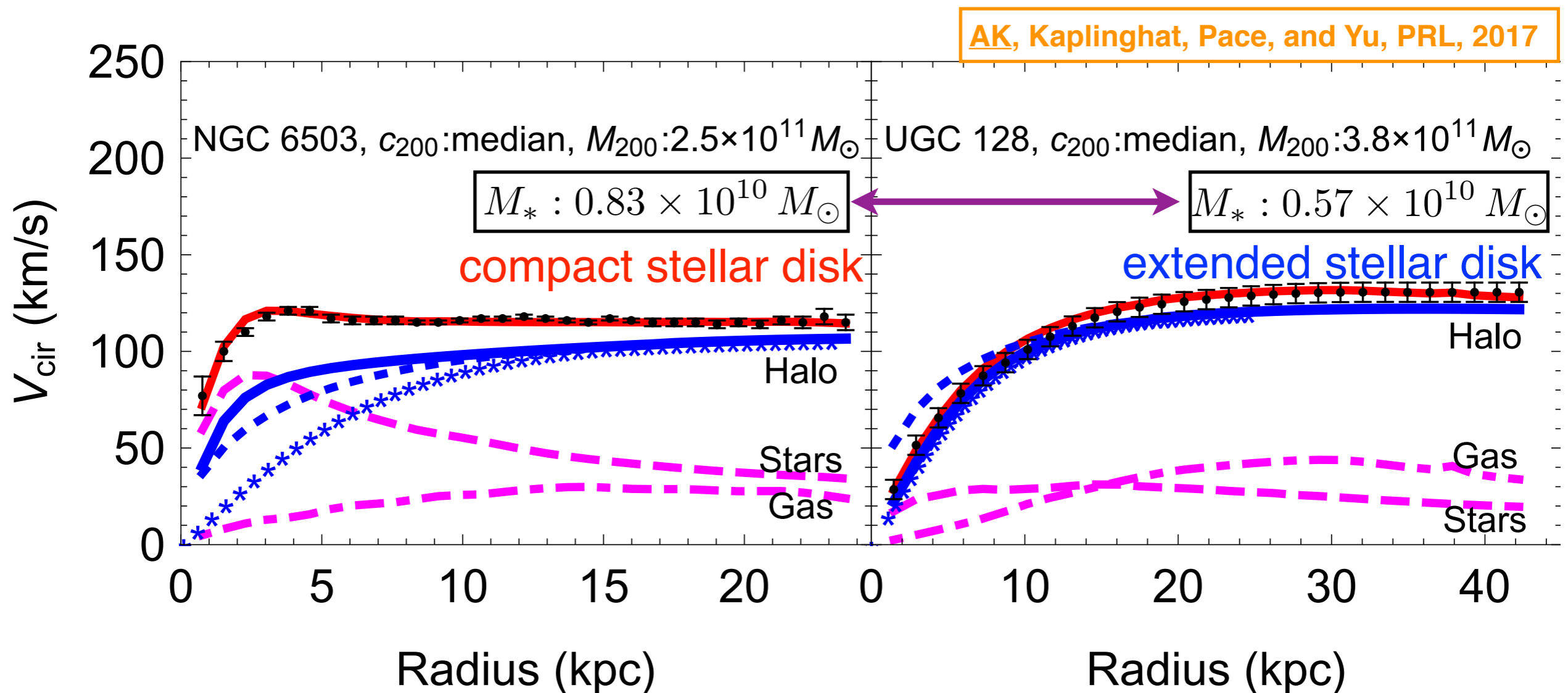
# Diversity in stellar distribution

Similar outer circular velocity and stellar mass, but different stellar distribution

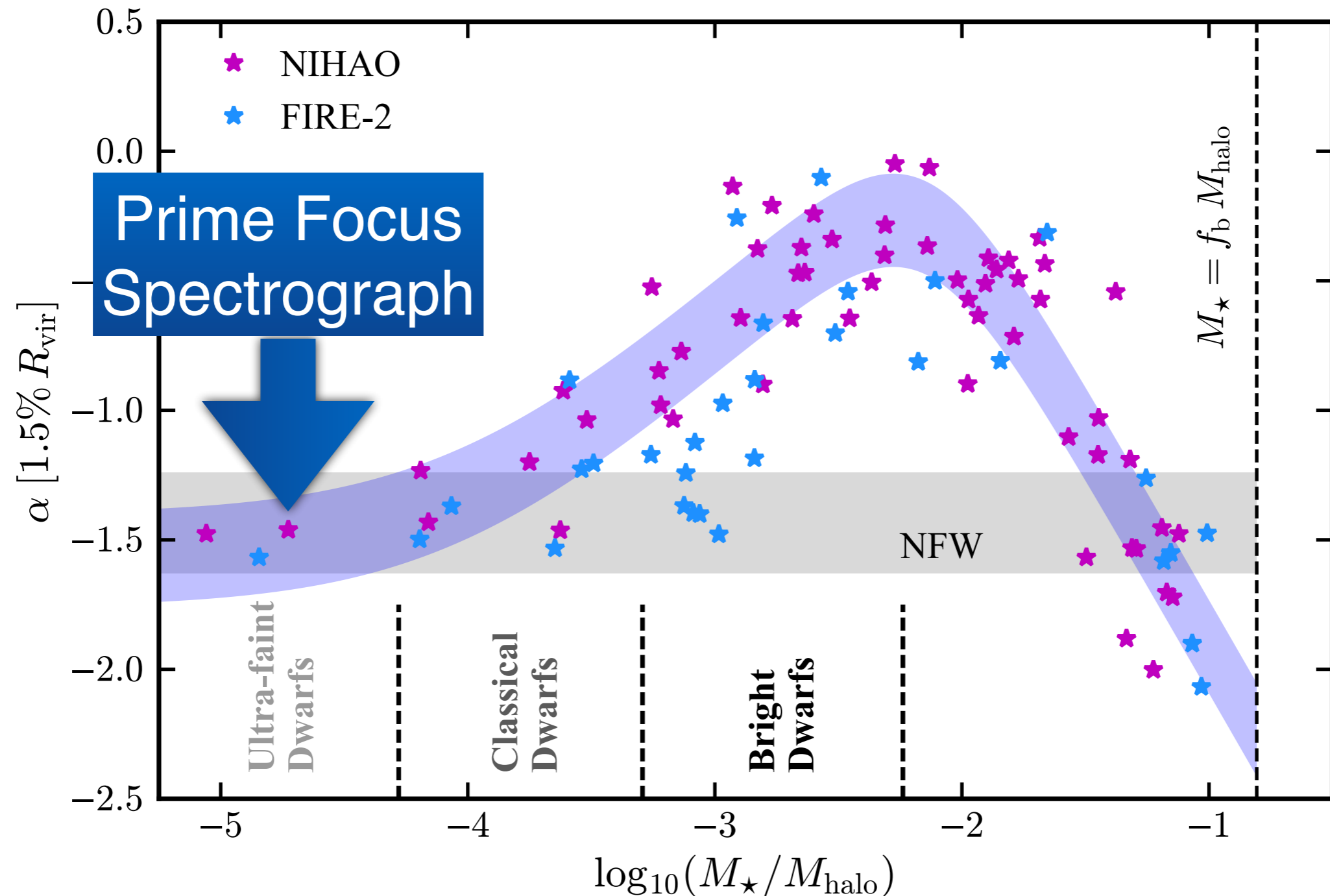
- compact  $\rightarrow$  redistribute SIDM significantly
- extended  $\rightarrow$  unchange SIDM distribution



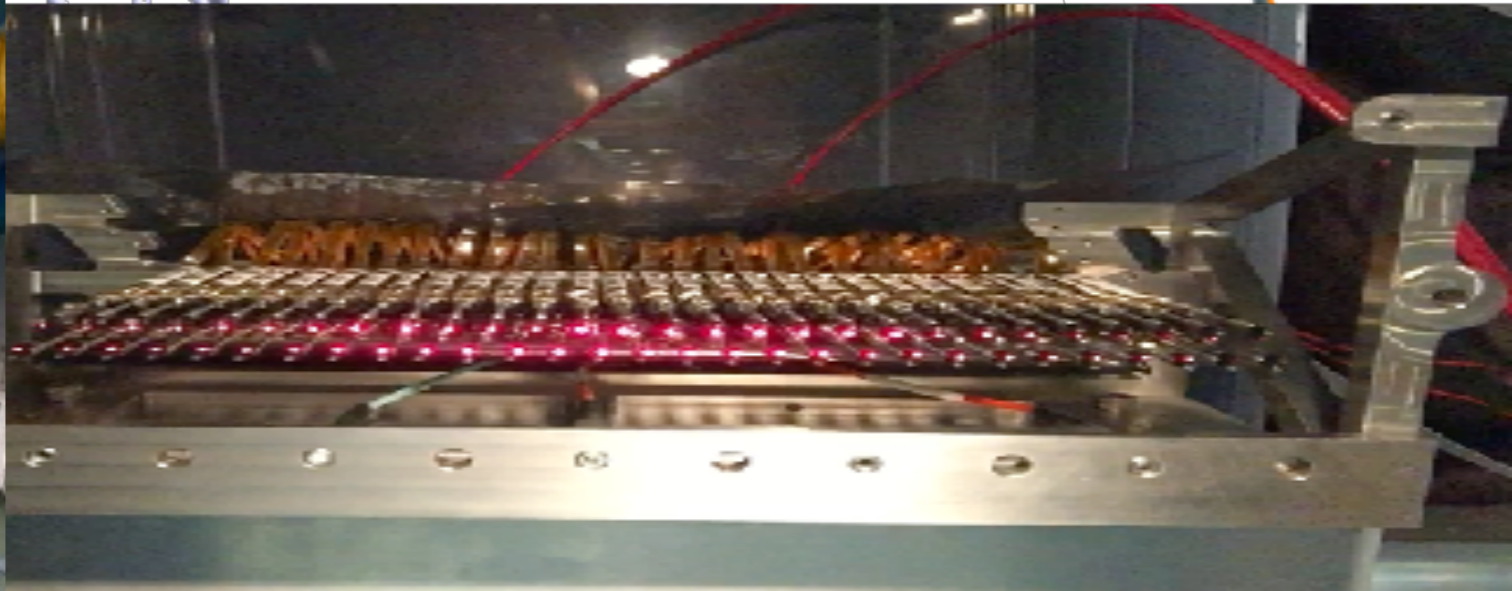
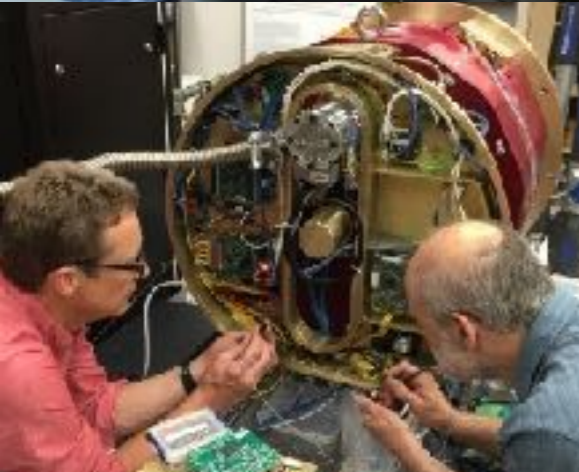
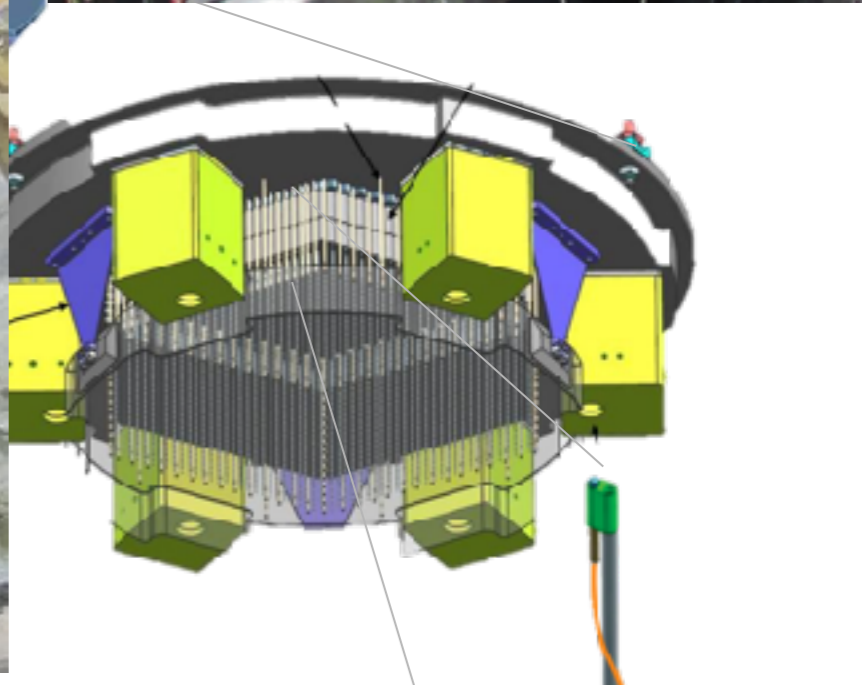
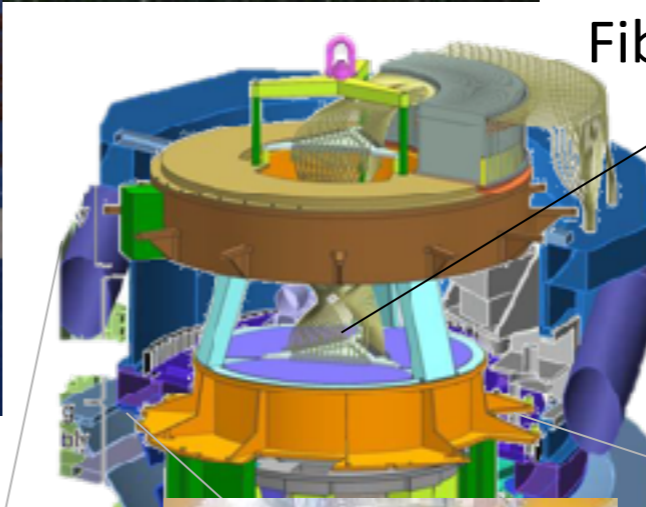
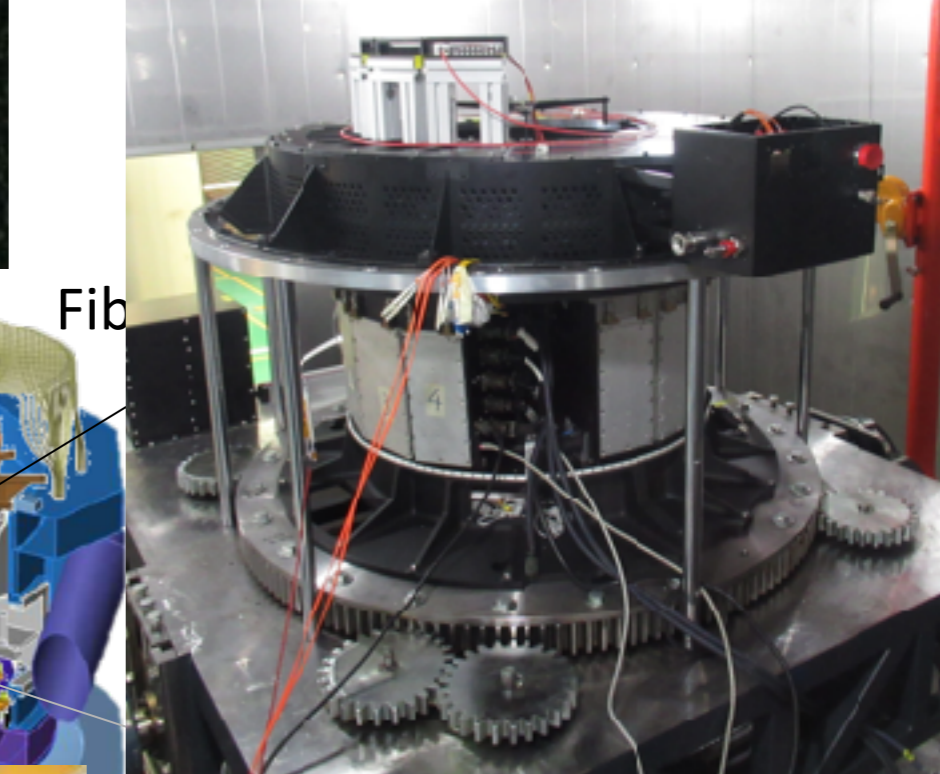
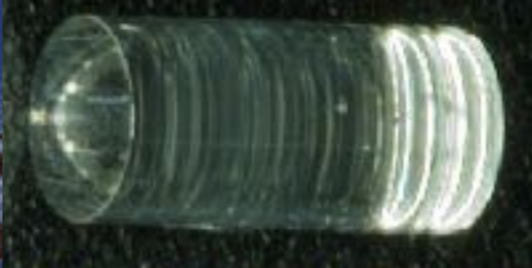
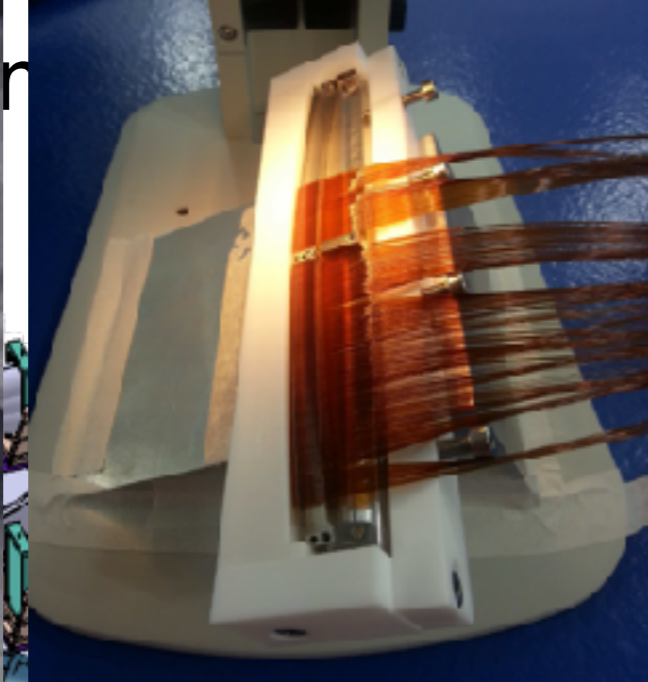
**Ayuki Kamada**



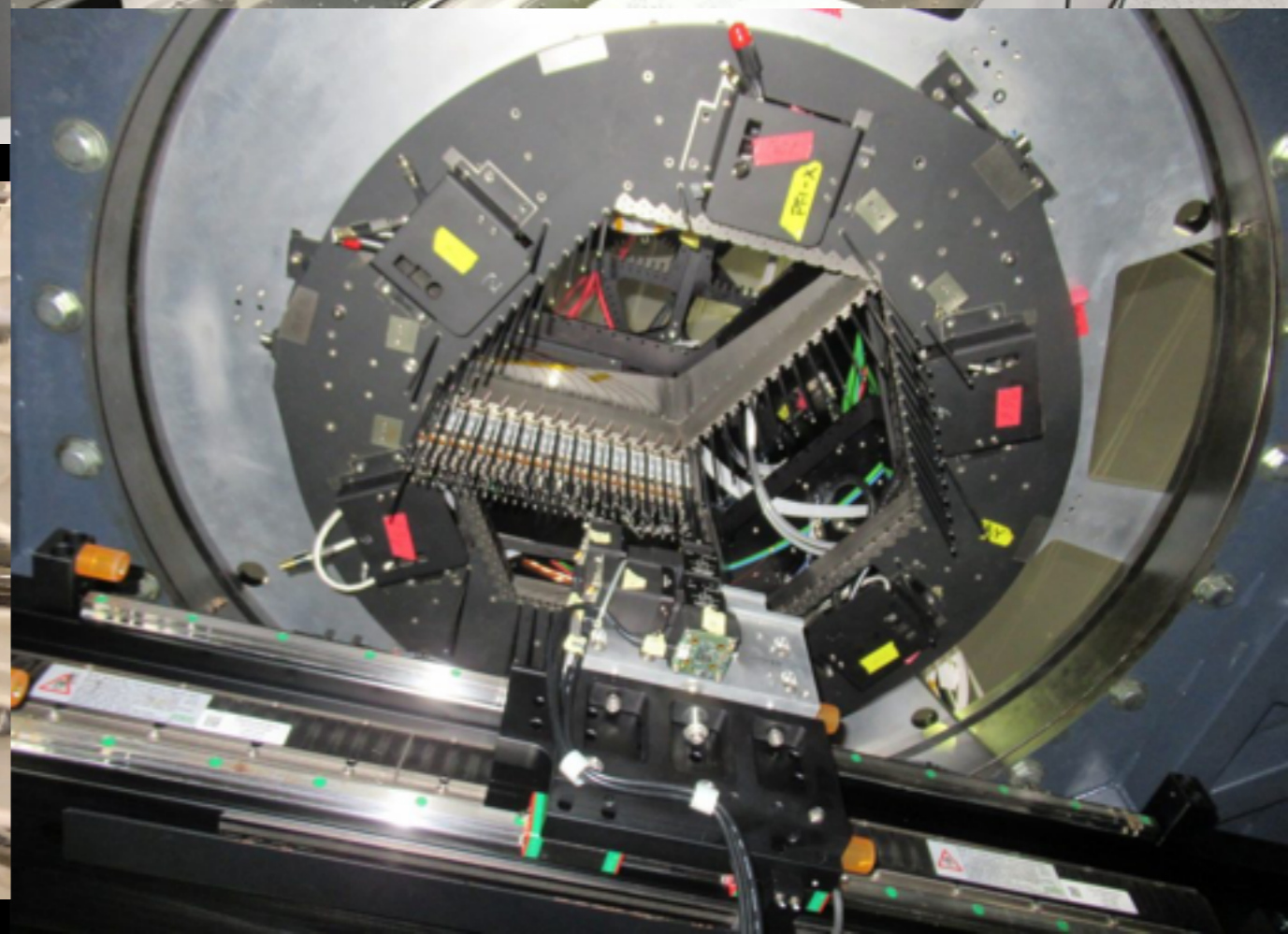
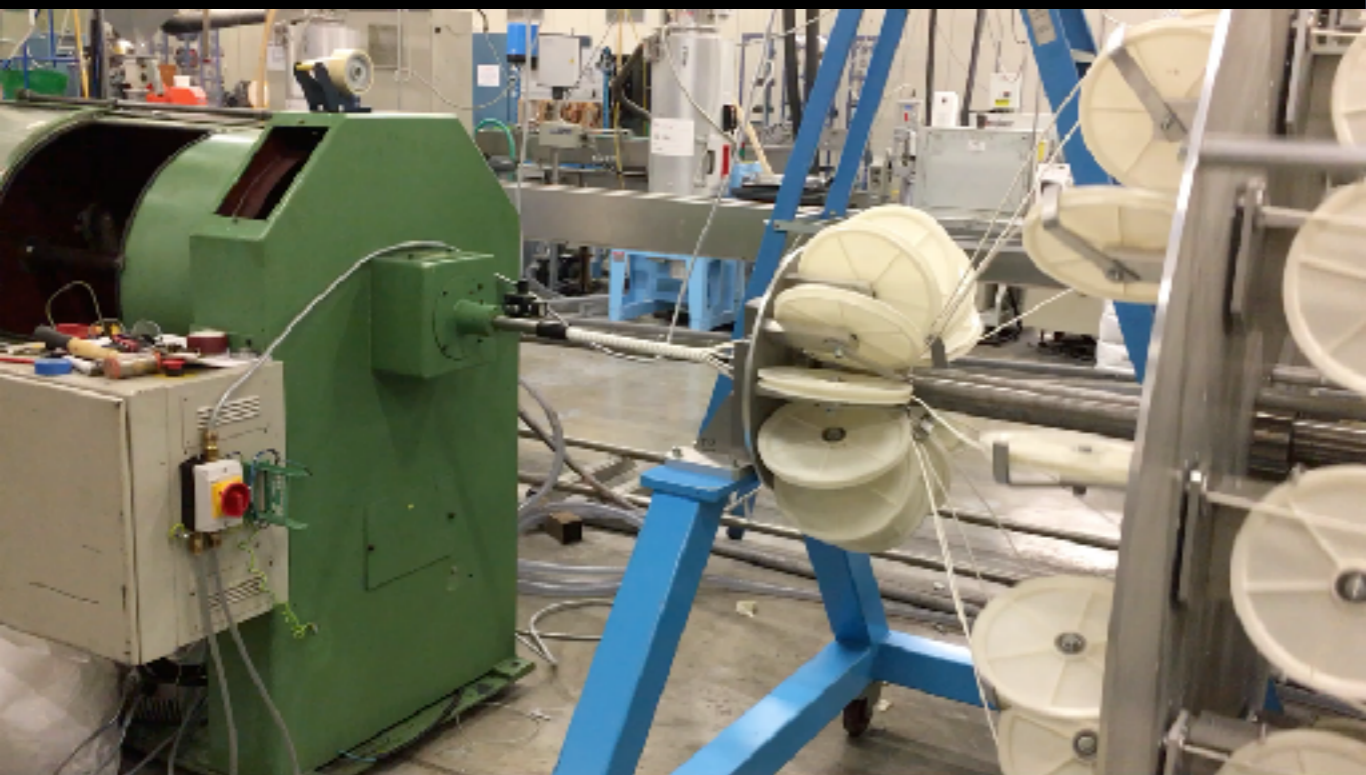
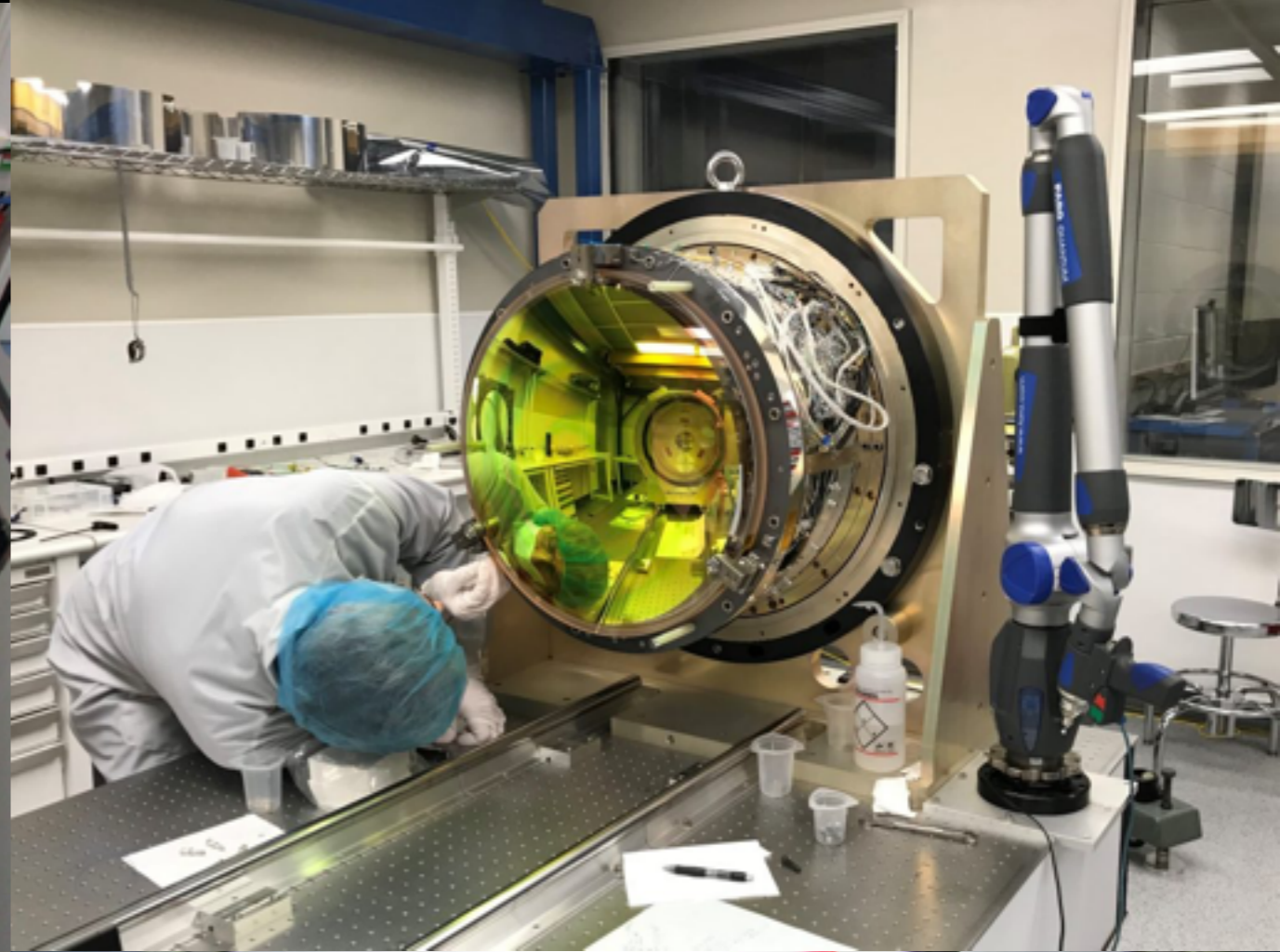
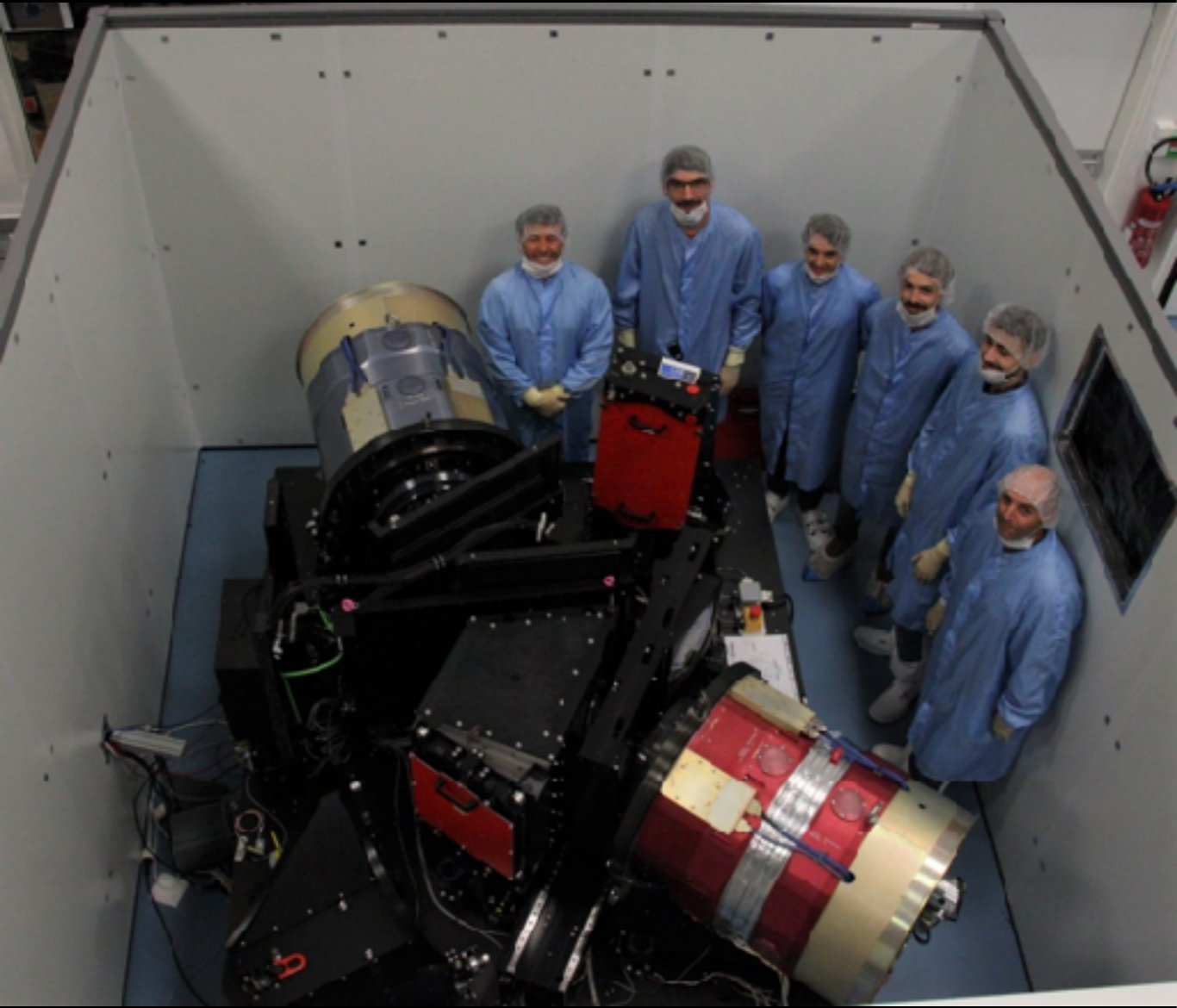
# Baryonic Feedback?









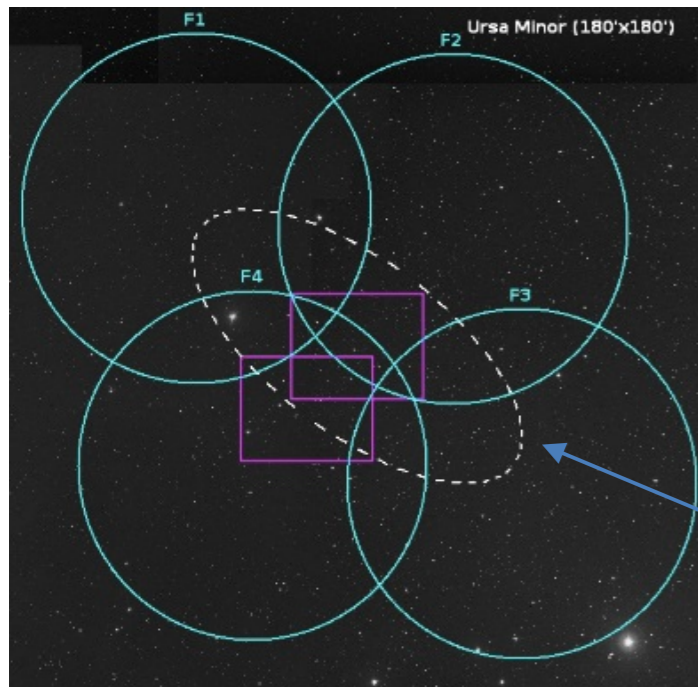




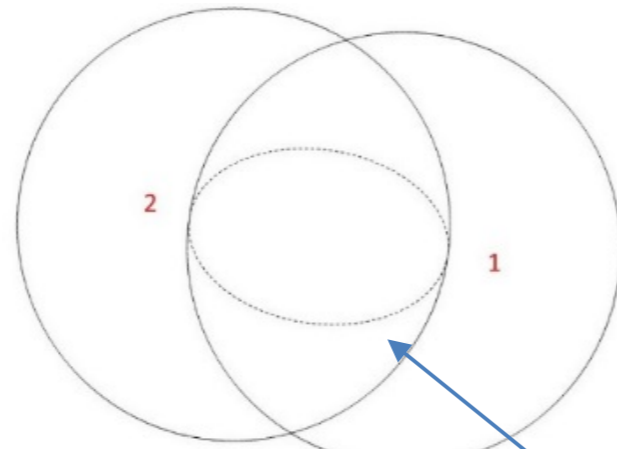
# PFS pointings for MW satellites

~ HSC imaging data are available for all samples ~

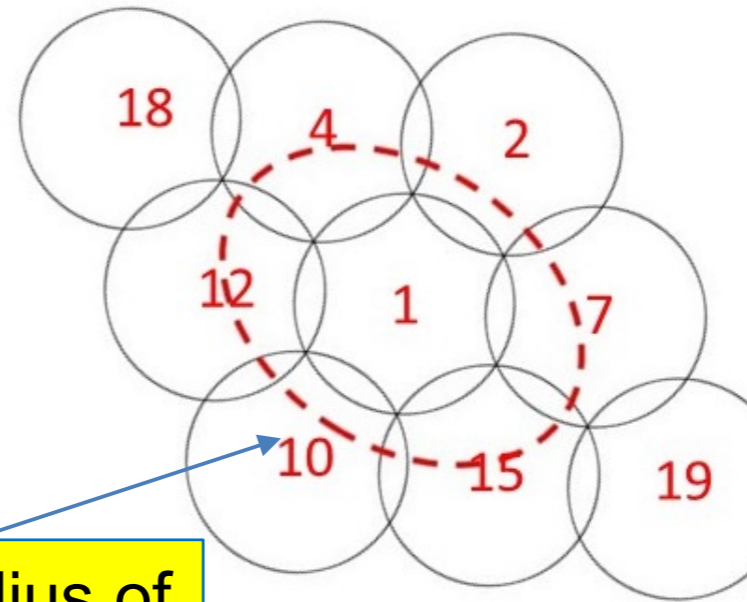
Ursa Minor



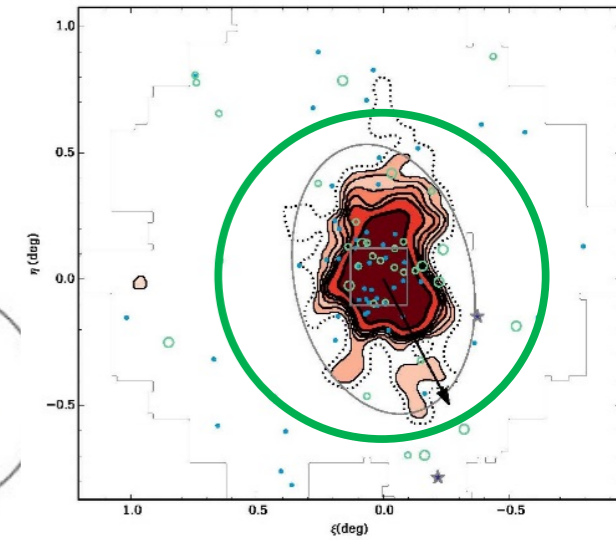
Draco



Sextans

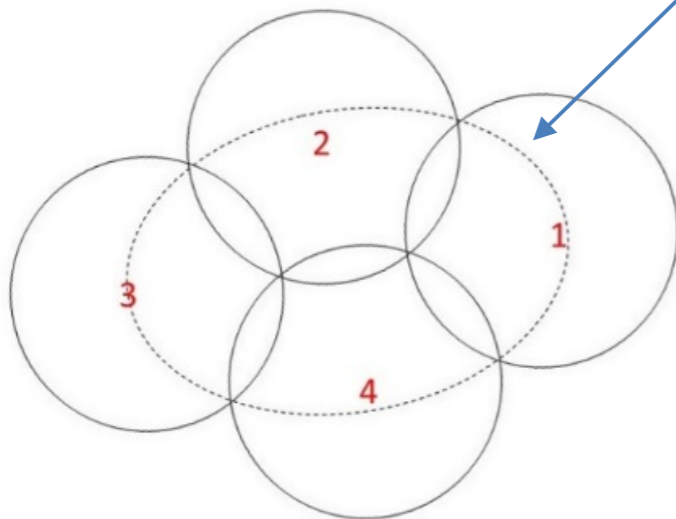


Bootes I

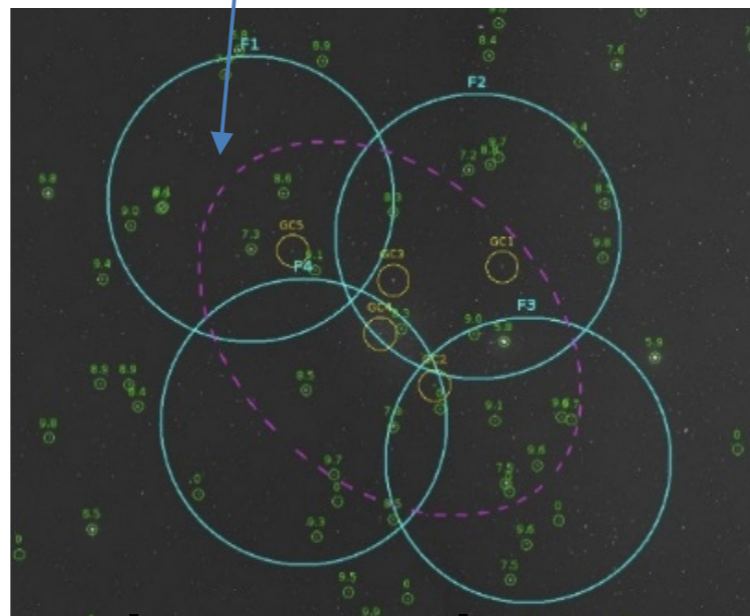


tidal radius of stellar comp.

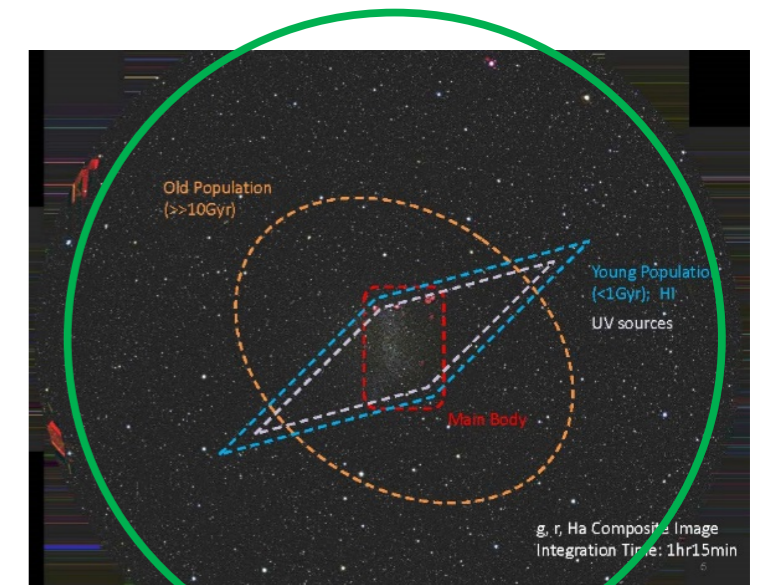
Sculptor



Fornax



NGC6822



also cosmology, galaxy evolution

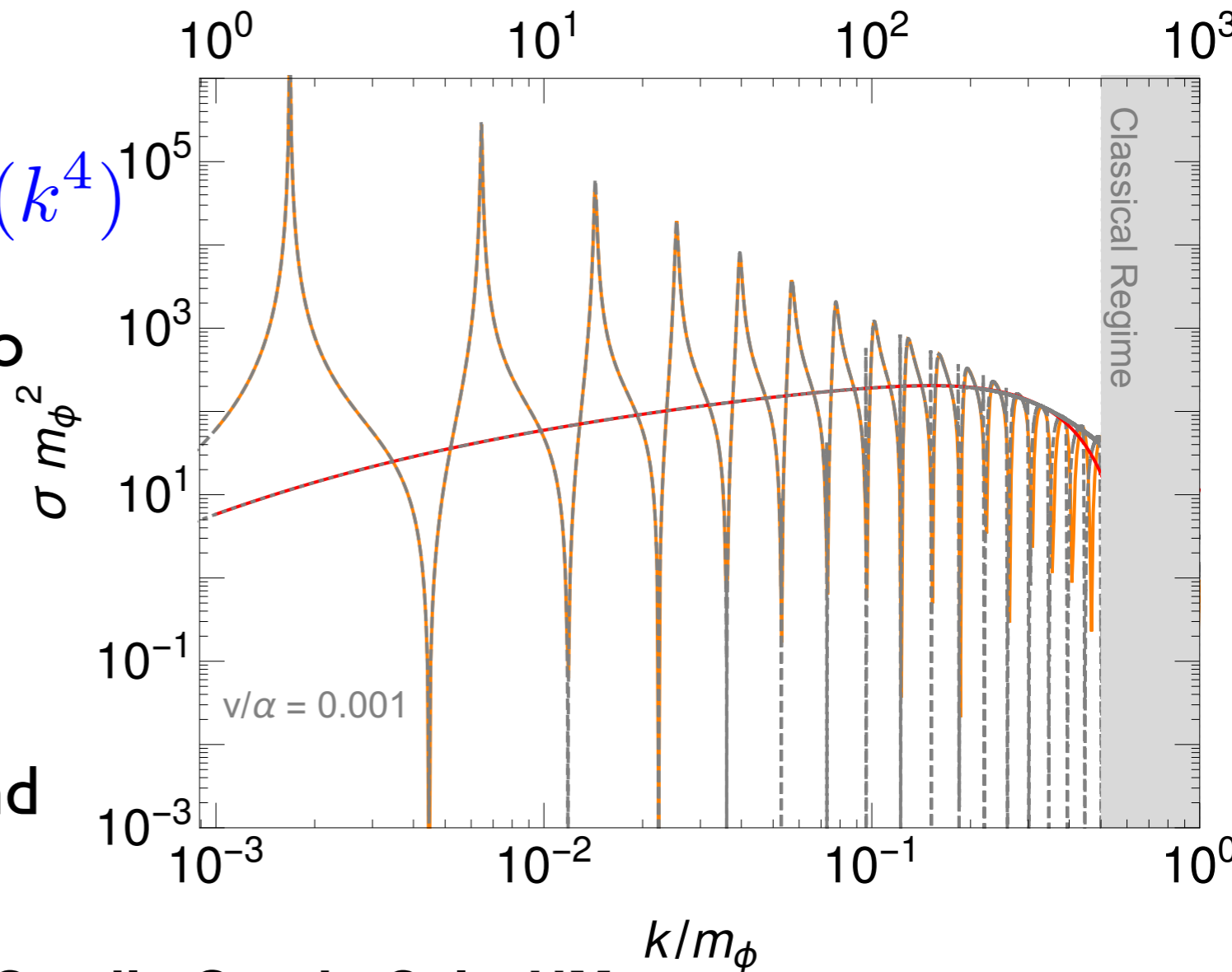
# Unified description of SIDM

- Hans Bethe: effective range theory

$$k \cot \delta = -\frac{1}{a} + \frac{1}{2} r_e k^2 + O(k^4)$$

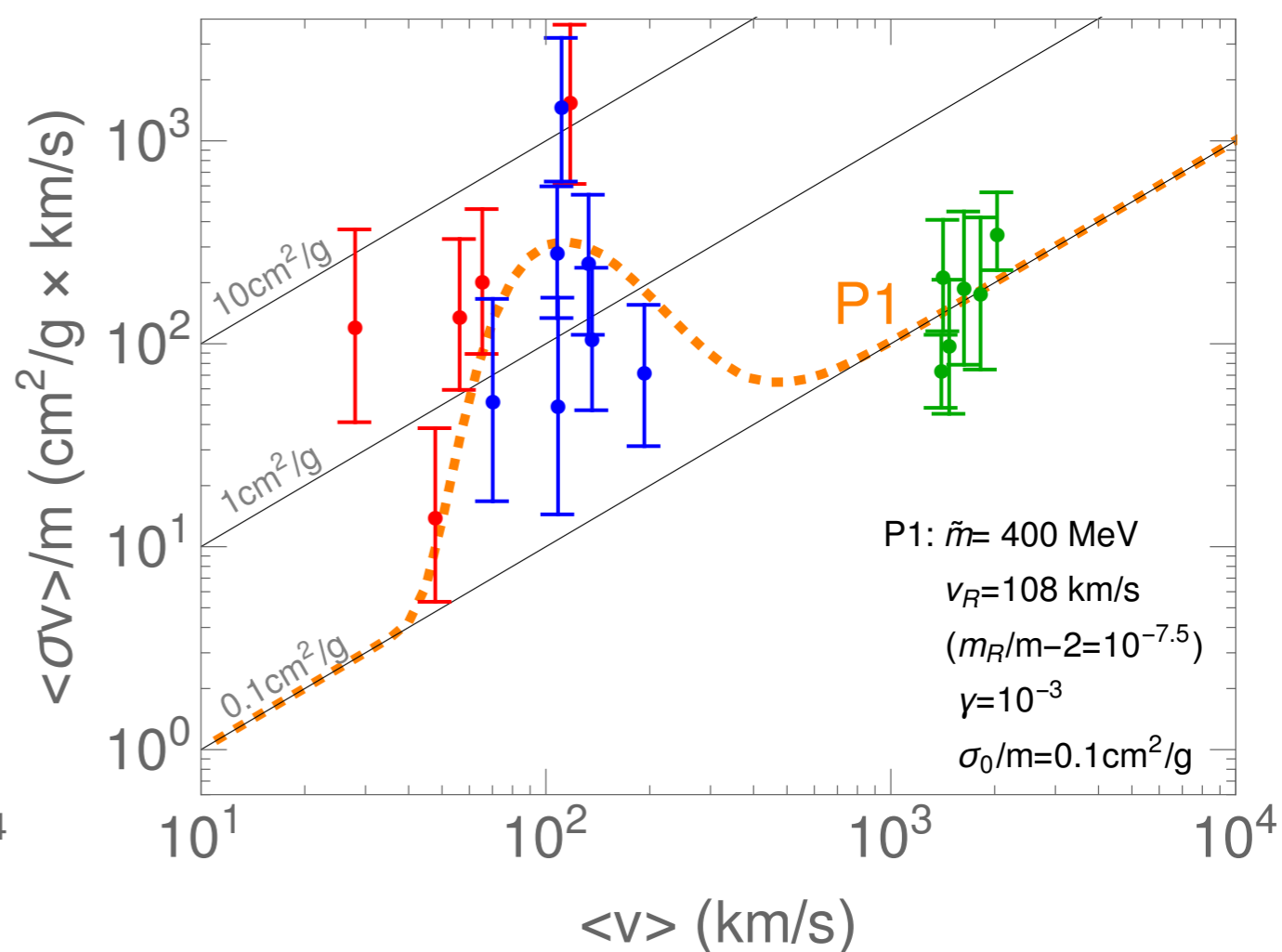
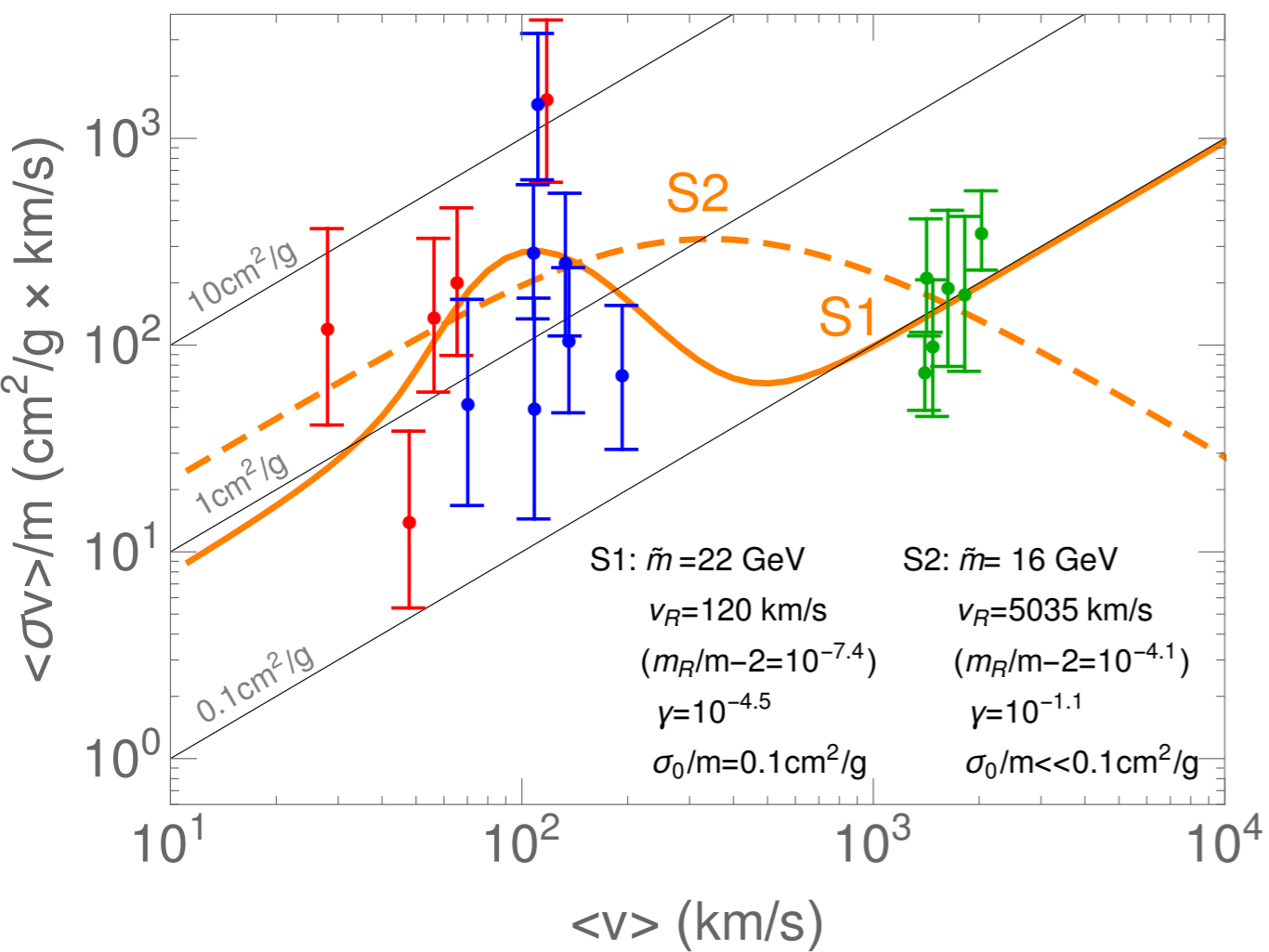
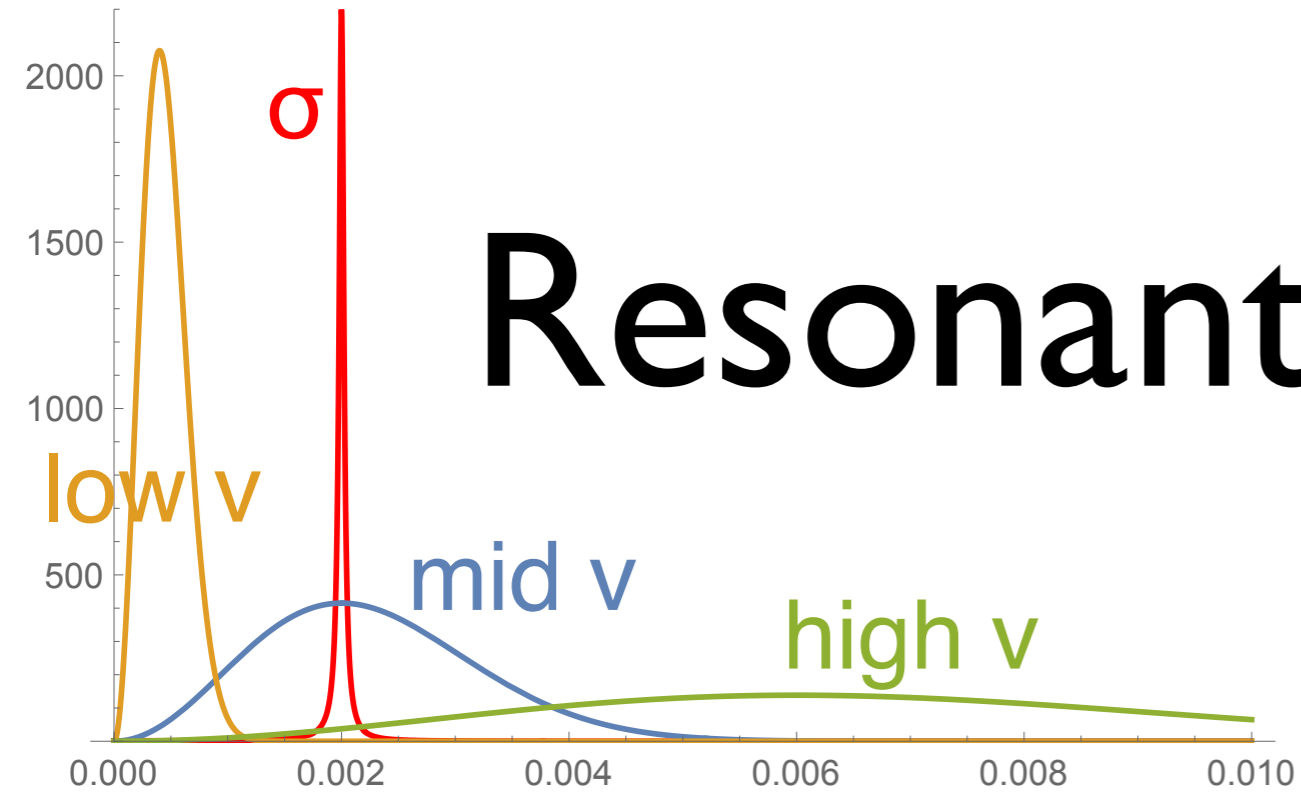
- only two parameters to describe scattering at low velocities
- fully unitary and non-perturbative
- ideal for simulations and phenomenology!

$$V = -\alpha \frac{e^{-m_\phi r}}{r}$$



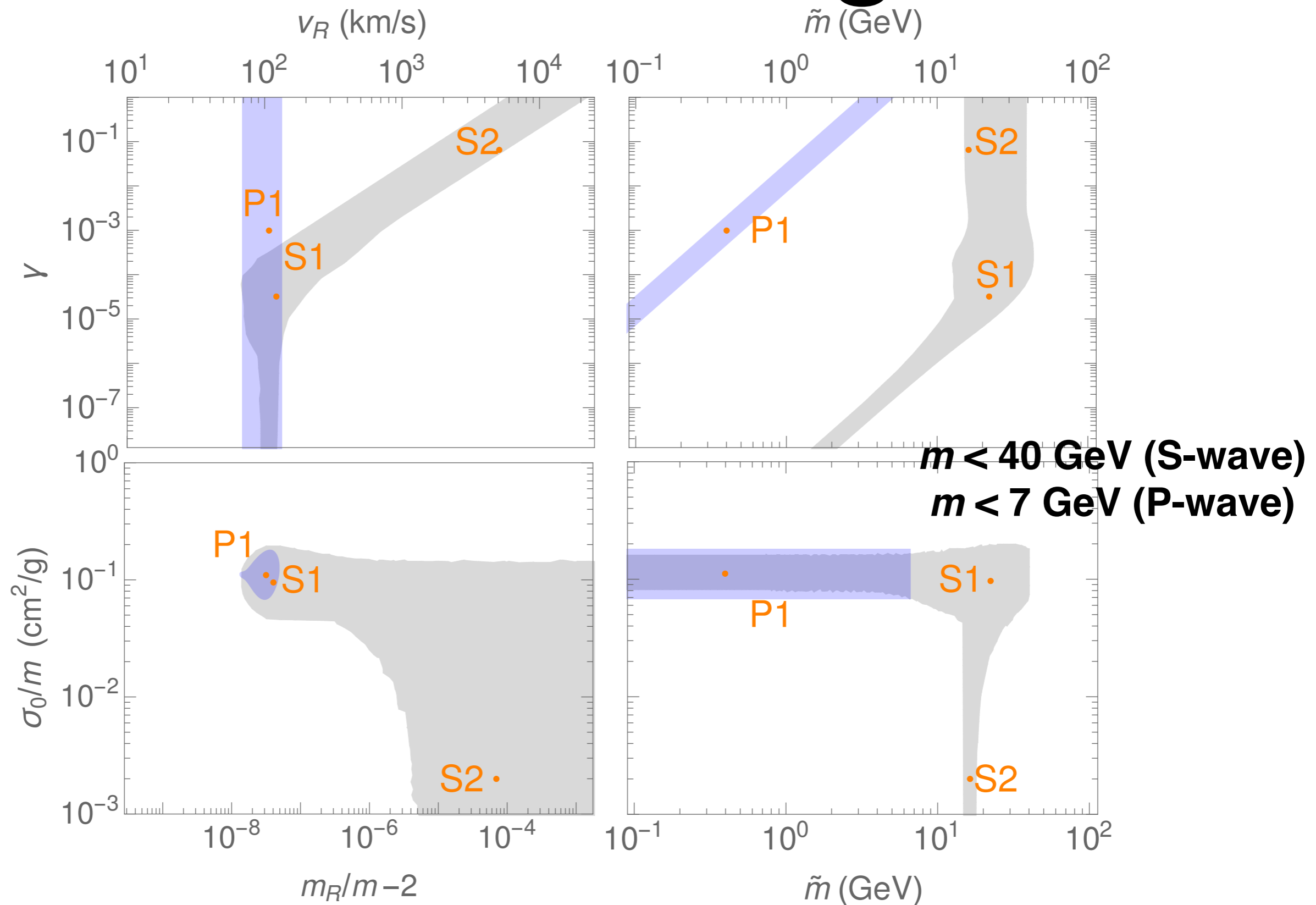


# Resonant scattering



**Xiaoyong Chu, Camilo Garcia-Cely, HM,**  
**Phys.Rev.Lett. 122 (2019) no.7, 071103**

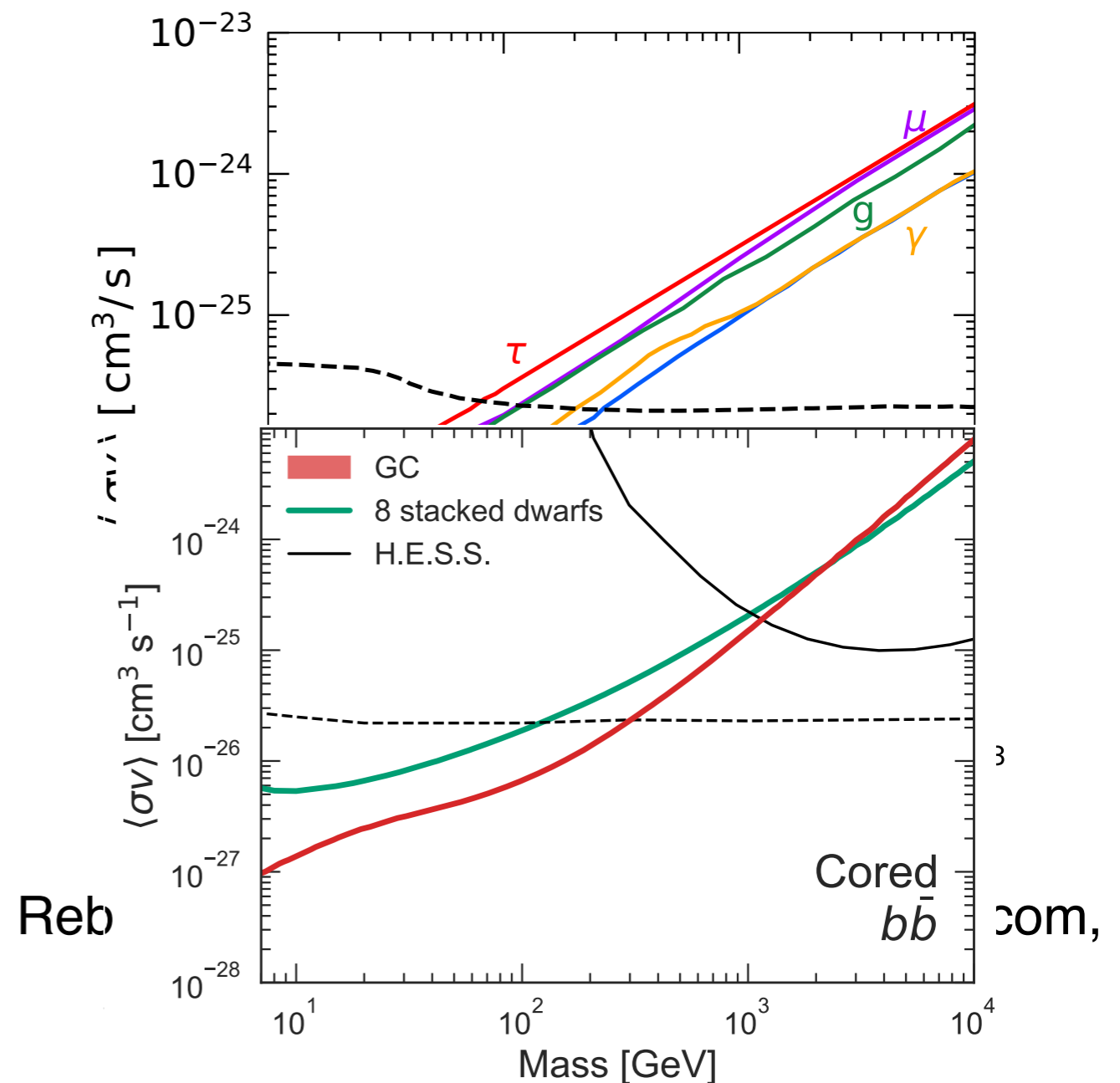
# needs to be light



Xiaoyong Chu, Camilo Garcia-Cely, HM,  
Phys.Rev.Lett. 122 (2019) no.7, 071103

# Standard Freeze-out doesn't work

- If self-interaction is in the S-wave, the unitarity limit says  $\sigma_0 < 4\pi\hbar^2/(mv)^2$
- For  $\sigma/m \sim \text{cm}^2/\text{g}$  for  $v \sim 10^{-3}$ , we need  $m < 14 \text{ GeV}$
- CMB limit on dark matter annihilation  $m > 20 \text{ GeV}$
- GC  $\gamma$  ray:  $m > 300 \text{ GeV}?$
- options
  - SIMP:  $3 \rightarrow 2$
  - asymmetric
  - freeze-in
  - down scattering



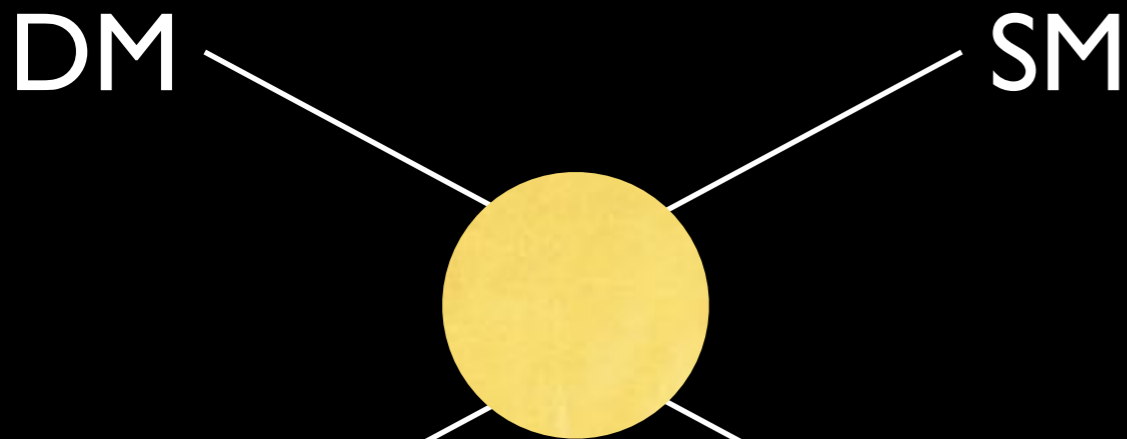
Abazajian, Horiuchi, Kaplinghat, Keeley,  
Macias, Ng, arXiv:2003.10416



# Dark Pions



# Miracles



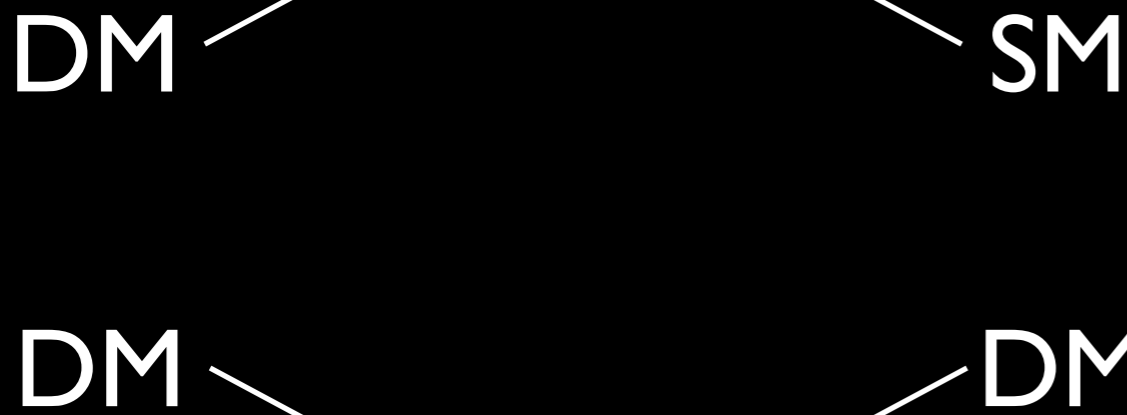
$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \approx \frac{\alpha^2}{m^2}$$

$$\alpha \approx 10^{-2}$$

$$m \approx 300 \text{ GeV}$$

WIMP miracle!

$$\frac{n_{\text{DM}}}{s} = 4.4 \times 10^{-10} \frac{\text{GeV}}{m_{\text{DM}}}$$

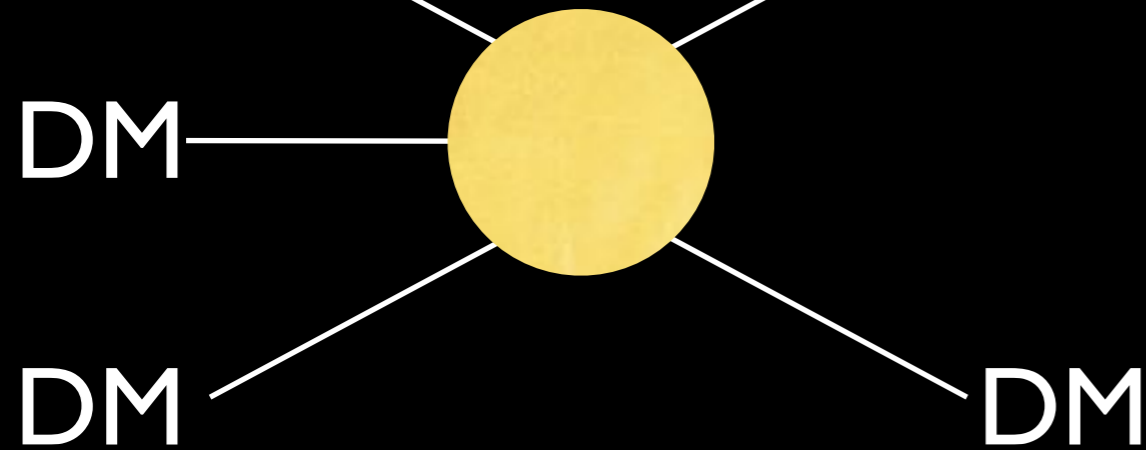


$$\langle \sigma_{3 \rightarrow 2\nu^2} \rangle \approx \frac{\alpha^3}{m^5}$$

$$\alpha \approx 4\pi$$

Hochberg, Kuflik,  
Volansky, Wacker

$$m \approx 300 \text{ MeV} \text{ arXiv:1402.5143}$$

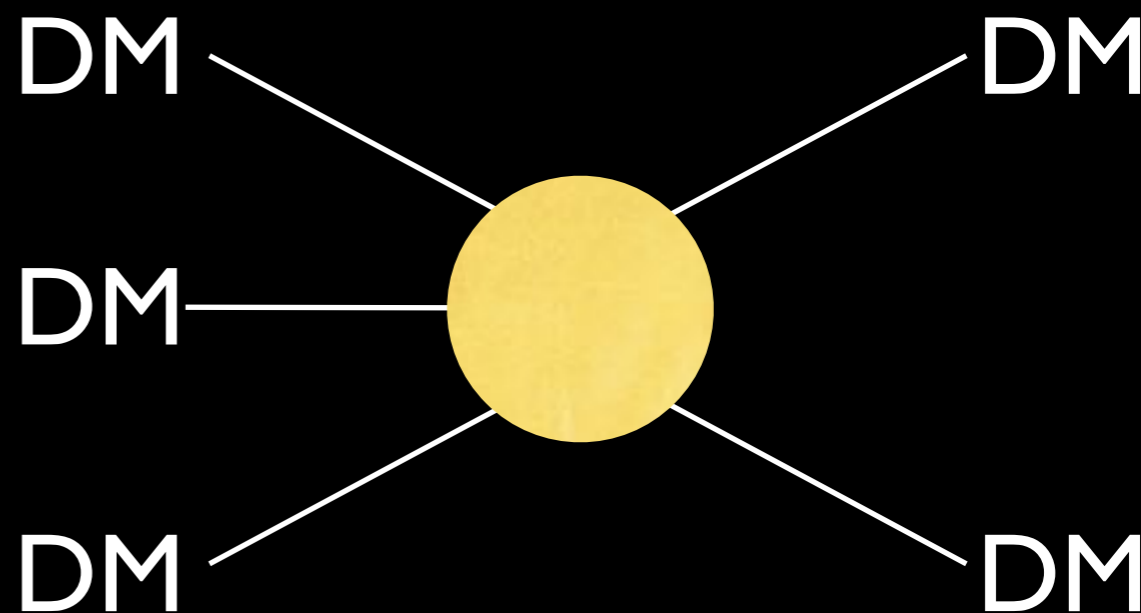


SIMP miracle!



# SIMPlEst Miracle

- SU(2) with 4 doublets
- Not only the mass scale is similar to QCD
- **dynamics itself can be QCD! Miracle<sup>3</sup>**
- DM = pions
- e.g. SU(4)/Sp(4) = S<sup>5</sup>



$$\mathcal{L}_{\text{chiral}} = \frac{1}{16f_{\pi}^2} \text{Tr} \partial^{\mu} U^{\dagger} \partial_{\mu} U$$

Hochberg, Kuflik, HM, Volansky, Wacker  
 Phys.Rev.Lett. 115 (2015) 021301

$$\mathcal{L}_{\text{WZW}} = \frac{8N_c}{15\pi^2 f_{\pi}^5} \epsilon_{abcde} \epsilon^{\mu\nu\rho\sigma} \pi^a \partial_{\mu} \pi^b \partial_{\nu} \pi^c \partial_{\rho} \pi^d \partial_{\sigma} \pi^e + O(\pi^7)$$

$$\pi_5(G/H) \neq 0$$

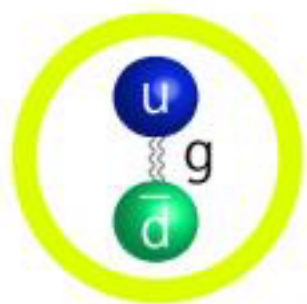
# LAGRANGIANS

## QCD

$$\mathcal{L}_{\text{quark}} = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \bar{q}_i i \not{D} q_i - \frac{1}{2} m_Q J^{ij} q_i q_j + h.c.$$

## Chiral Lagrangian

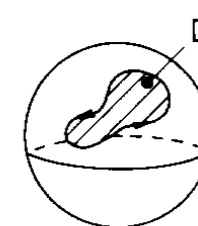
$$\mathcal{L}_{\text{Sigma}} = \frac{f_\pi^2}{16} \text{Tr} \partial_\mu \Sigma \partial^\mu \Sigma^\dagger - \frac{1}{2} m_Q \mu^3 \text{Tr} J \Sigma + h.c. - \frac{i N_c}{240 \pi^2} \int \text{Tr} (\Sigma^\dagger d\Sigma)^5$$



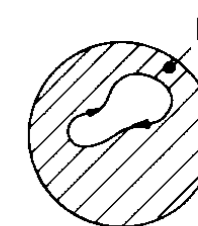
## Pions



(a)



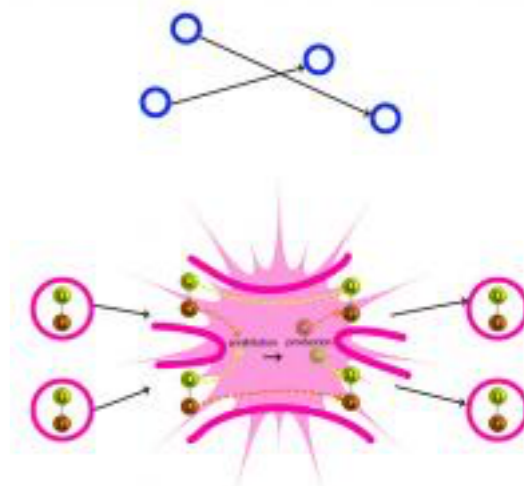
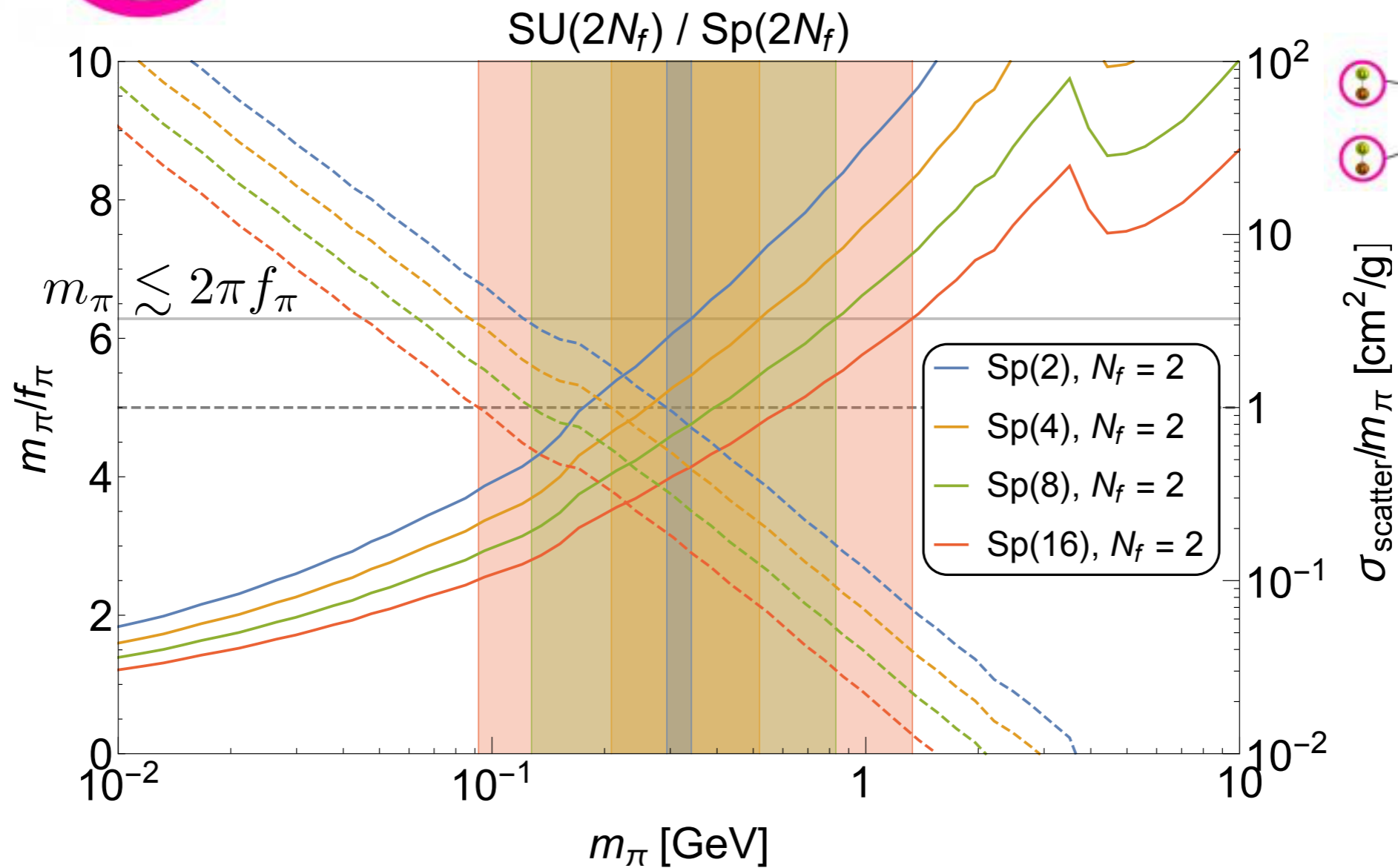
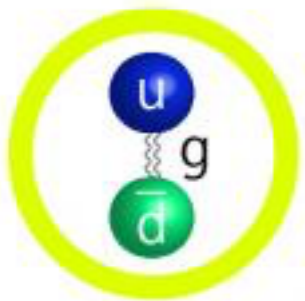
(b)



(c)

$$\mathcal{L}_{\text{pion}} = \frac{1}{4} \text{Tr} \partial_\mu \pi \partial^\mu \pi - \frac{m_\pi^2}{4} \text{Tr} \pi^2 + \frac{m_\pi^2}{12 f_\pi^2} \text{Tr} \pi^4 - \frac{1}{6 f_\pi^2} \text{Tr} (\pi^2 \partial^\mu \pi \partial_\mu \pi - \pi \partial^\mu \pi \pi \partial_\mu \pi) + \frac{2 N_c}{15 \pi^2 f_\pi^5} \epsilon^{\mu\nu\rho\sigma} \text{Tr} [\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi] + \mathcal{O}(\pi^6)$$

# The Results



Solid curves: solution to Boltzmann eq.

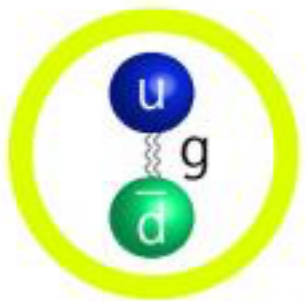
Dashed curves: along that solution

$$\frac{m_\pi}{f_\pi} \propto m_\pi^{3/10}$$

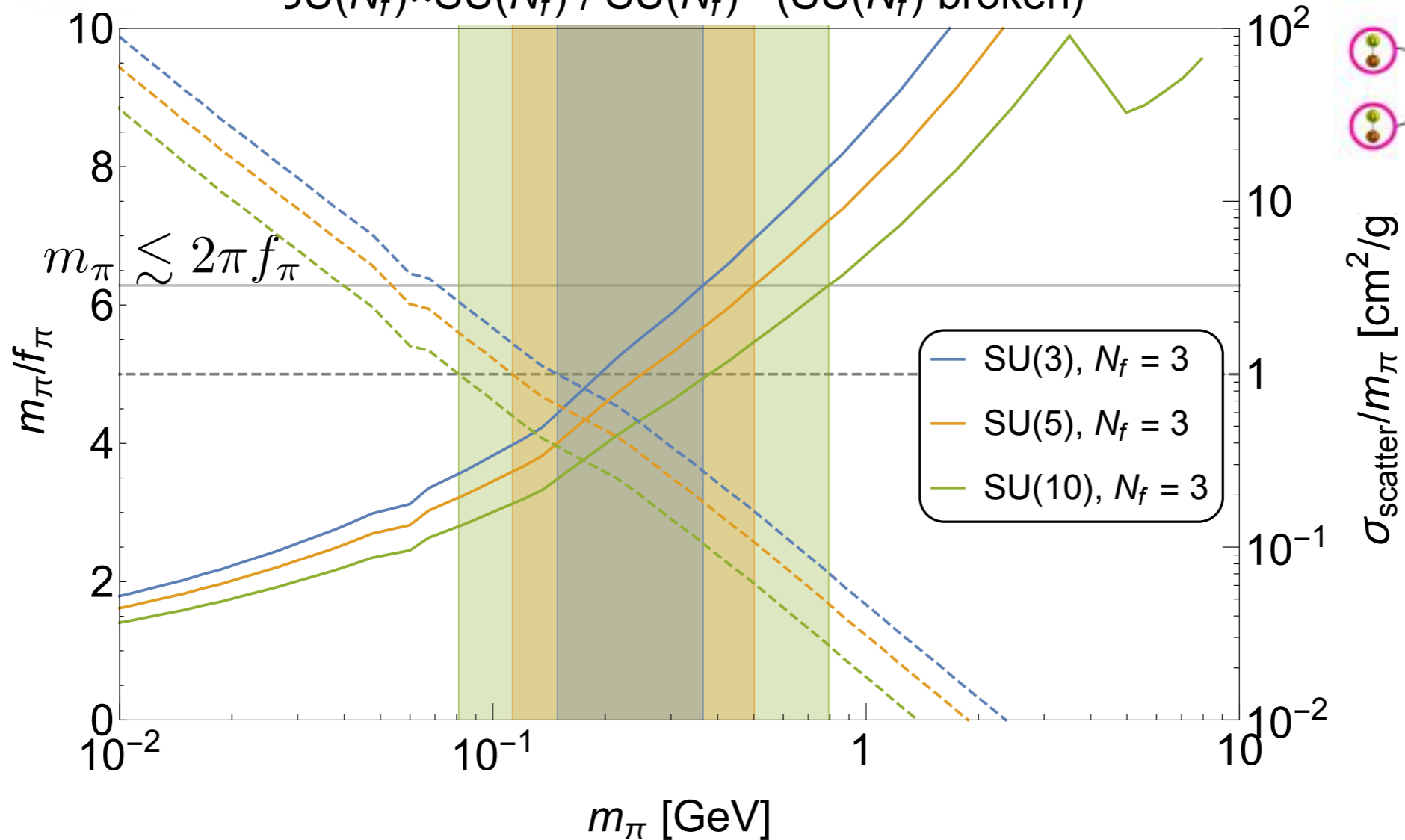
$$\frac{\sigma_{\text{scatter}}}{m_\pi} \propto m_\pi^{-9/5}$$



# The Results



$3U(N_f) \times SU(N_f) / SU(N_f)$  ( $SU(N_f)$  broken)



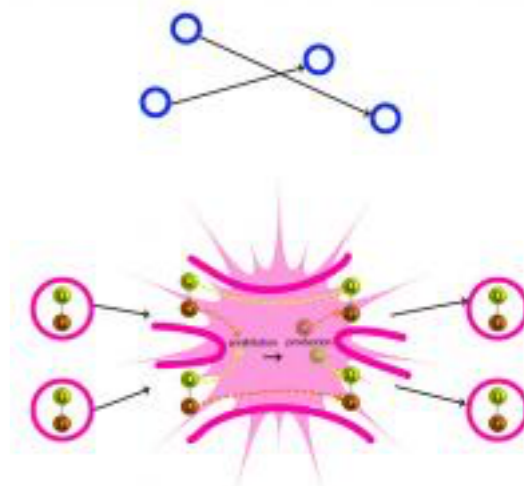
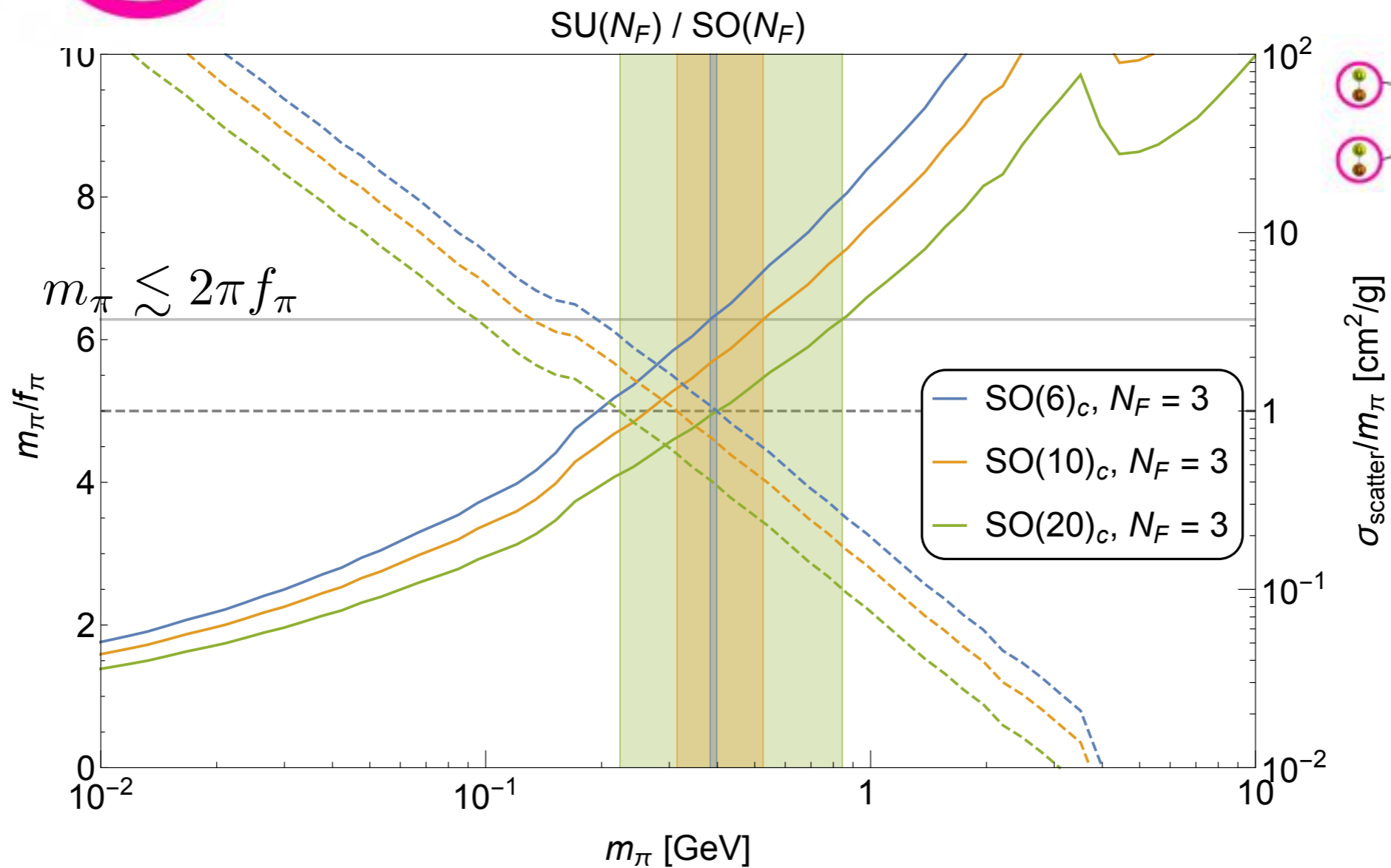
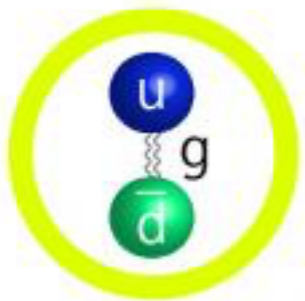
Solid curves: solution to Boltzmann eq.

Dashed curves: along that solution

$$\frac{m_\pi}{f_\pi} \propto m_\pi^{3/10}$$

$$\frac{\sigma_{\text{scatter}}}{m_\pi} \propto m_\pi^{-9/5}$$

# The Results



Solid curves: solution to Boltzmann eq.

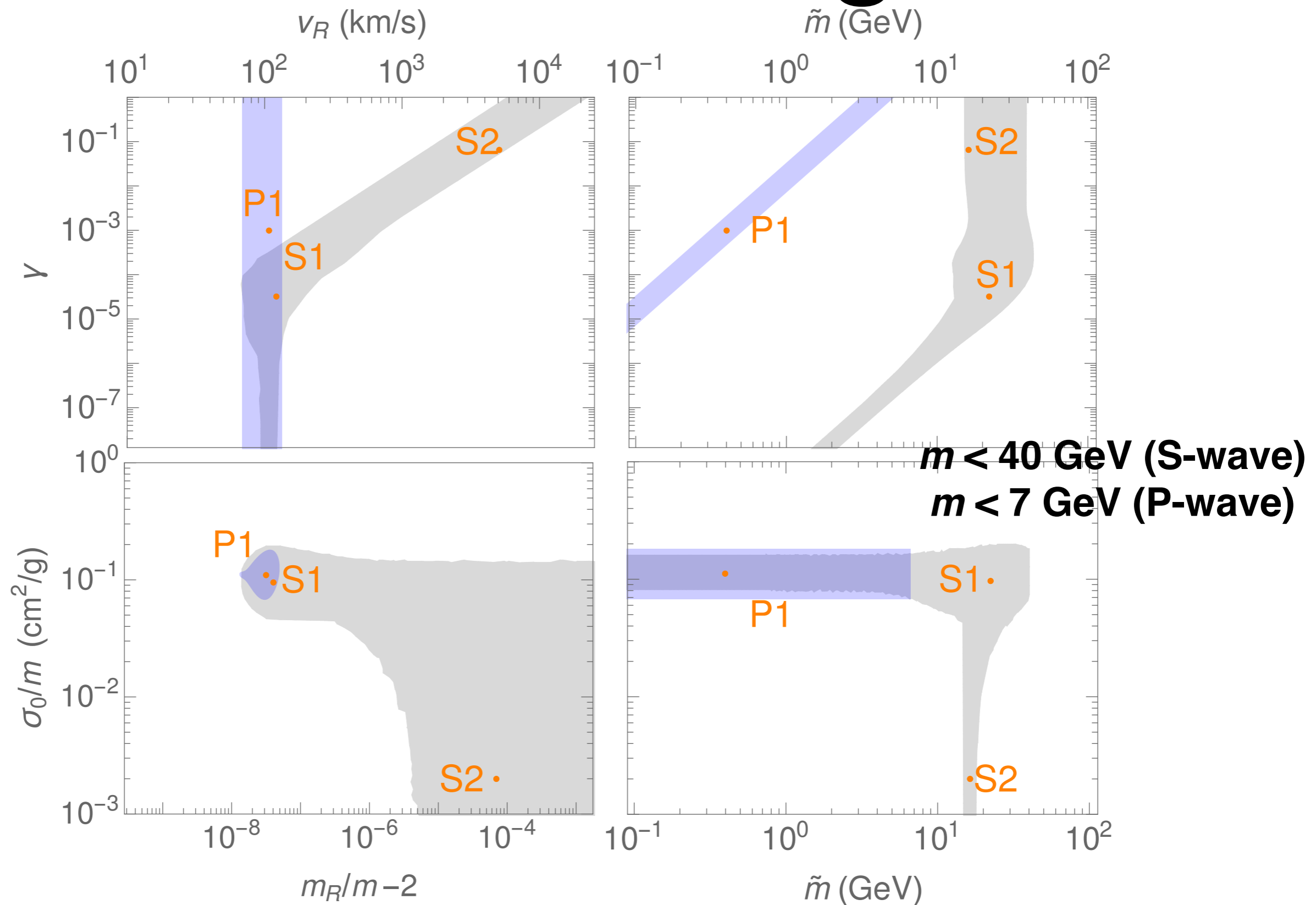
Dashed curves: along that solution

$$\frac{m_\pi}{f_\pi} \propto m_\pi^{3/10}$$

$$\frac{\sigma_{\text{scatter}}}{m_\pi} \propto m_\pi^{-9/5}$$



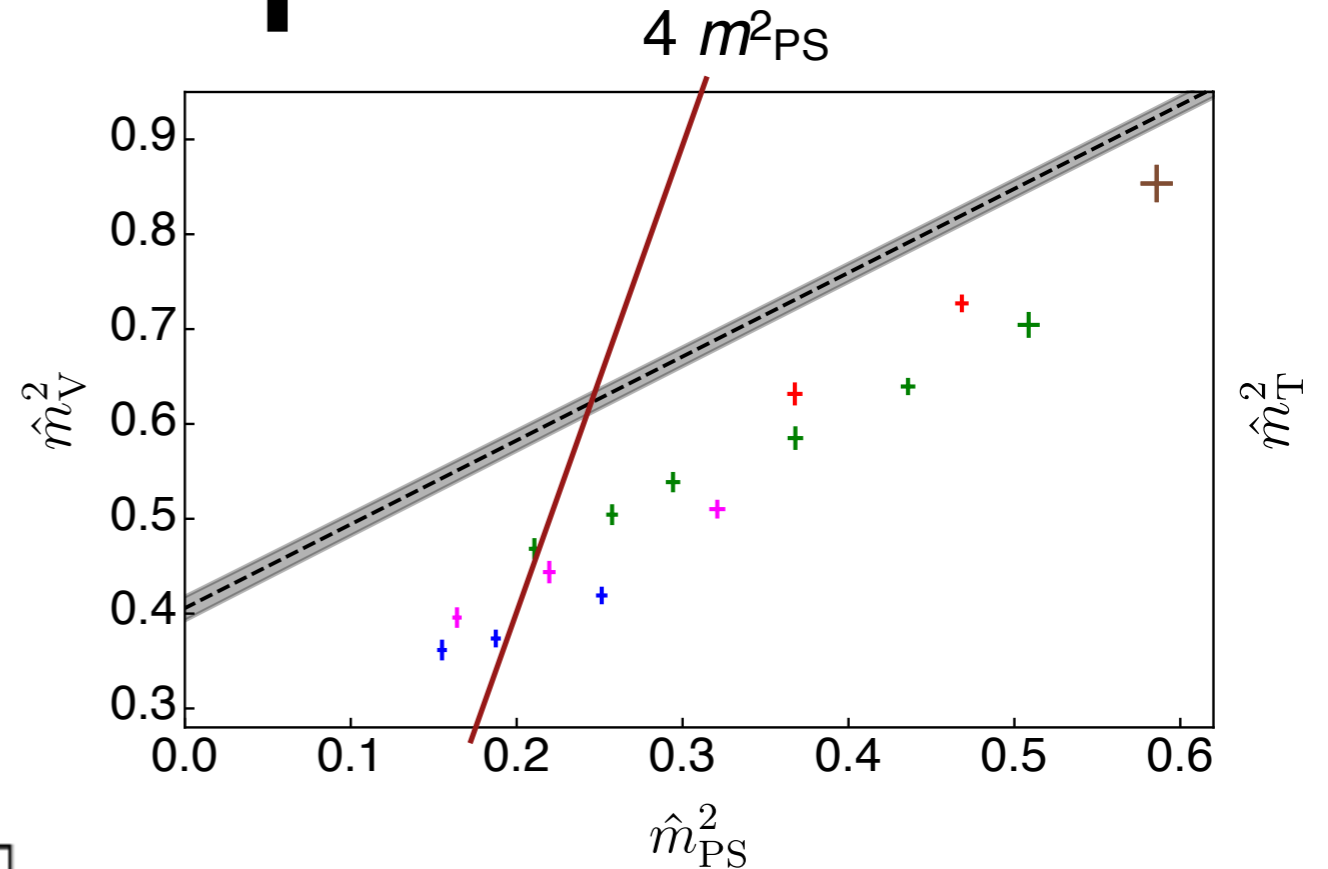
# needs to be light



Xiaoyong Chu, Camilo Garcia-Cely, HM,  
Phys.Rev.Lett. 122 (2019) no.7, 071103

# Resonance is plausible

- e.g.,  $K^+K^- \rightarrow \phi \rightarrow K^+K^-$ 
  - requires  $m_\phi = 2m_K$
  - $m_\phi \approx \Lambda + m_d + m_s$
  - $2m_K \approx 2((m_d + m_s) \Lambda)^{1/2}$
  - guaranteed to cross when  $m_s < \Lambda/4$
- also for  $\psi(3S)$ ,  $Y(4S)$
- but limited parameters

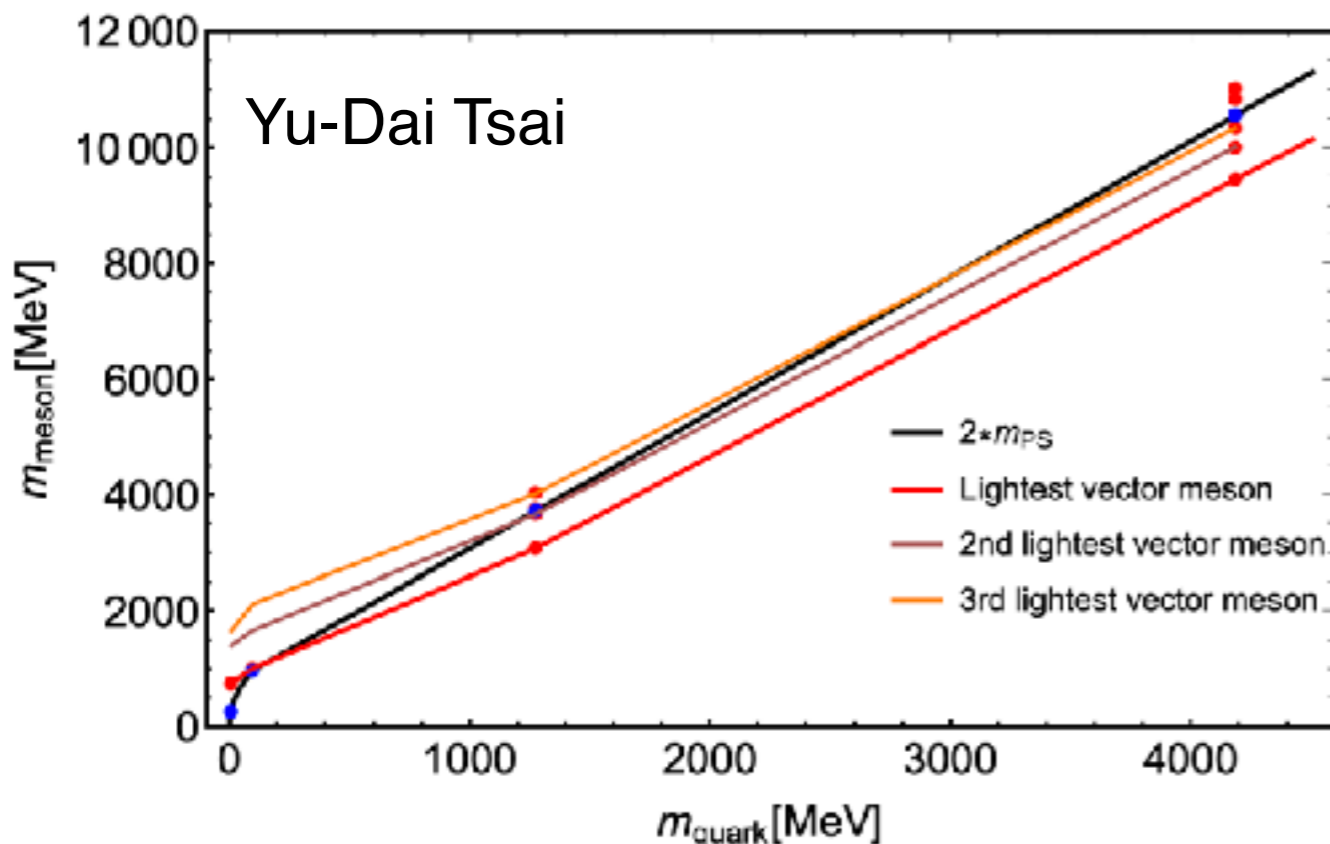


lattice calculation of  $Sp(4)$  with  $N_f=4$   
arXiv:1911.00437

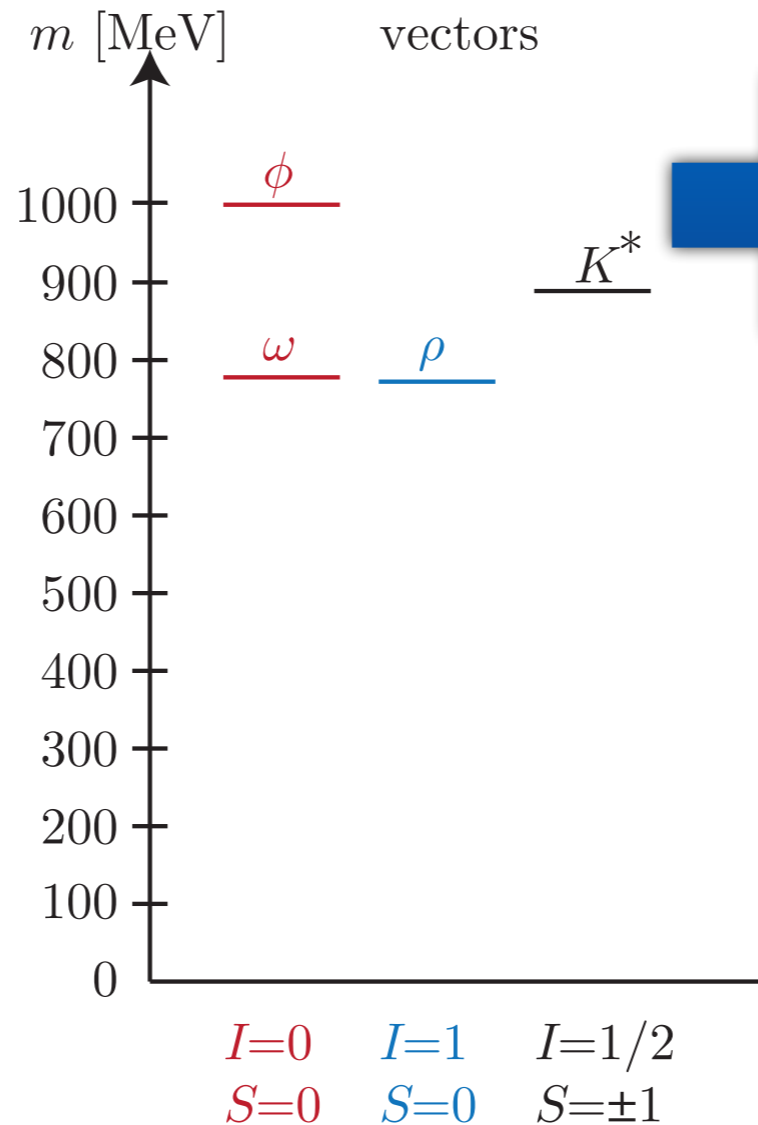
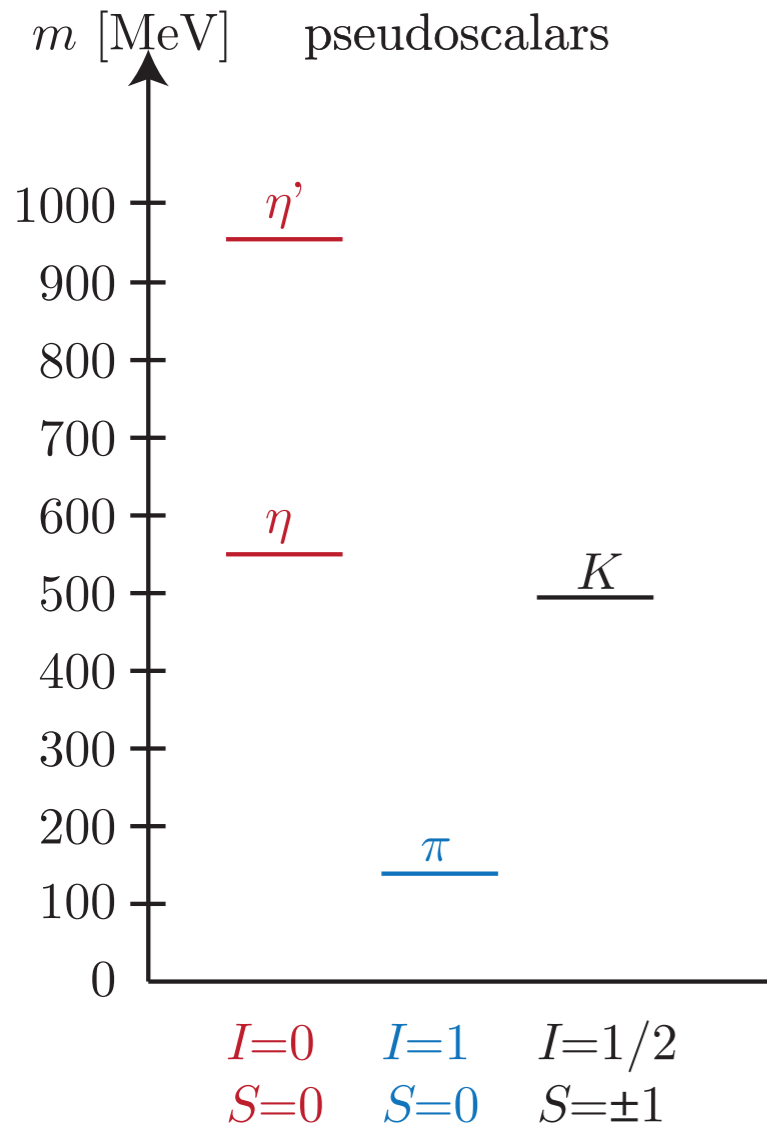
$$\frac{m(^8\text{Be}) - m(\alpha)}{m(^8\text{Be})} = 0.000012,$$

$$\frac{m(^{12}\text{C}) - m(^8\text{Be}) - m(\alpha)}{m(^{12}\text{C})} = 0.000026,$$

$$\frac{m(D^{+*}) - m(D^0) - m(\pi^+)}{m(D^{+*})} = 0.00051.$$



# revenge of sigmas



**tetra quarks  $(qq)(\bar{q}\bar{q})$**   
**meson molecule  $K^+K^-$**

## Gell-Mann–Okubo relation

$$K: 4 \times 0.496^2 = 0.984 \text{ GeV}^2$$

$$\pi_0, \eta: 0.140^2 + 3 \times 0.550^2 = 0.927 \text{ GeV}^2$$

$$K_0^*: 4 \times 0.680^2 = 1.85 \text{ GeV}^2$$

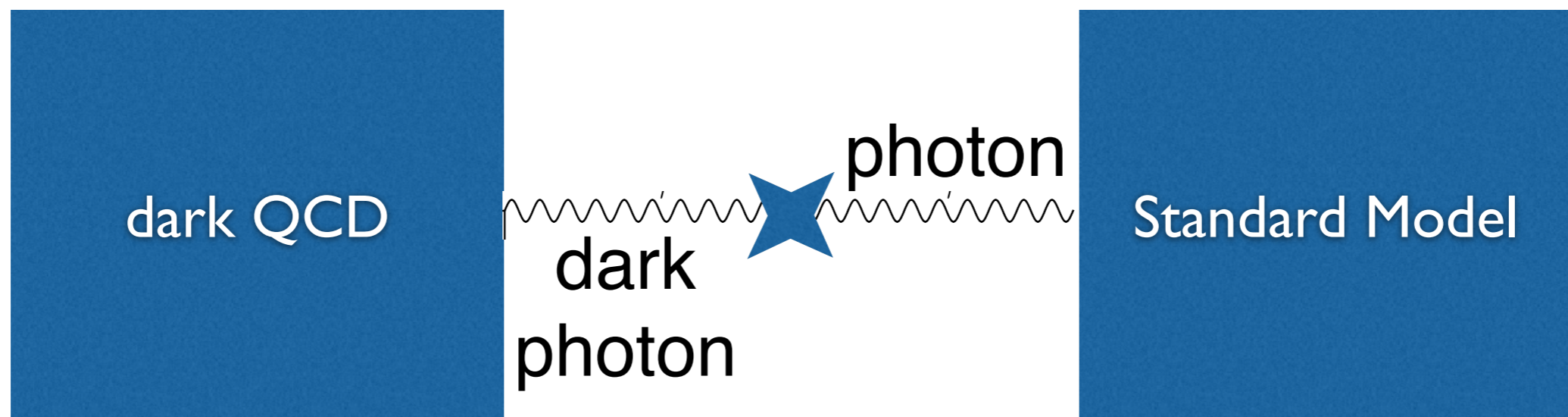
$$f_0: 0.980^2 + 3 \times 0.500^2 = 1.71 \text{ GeV}^2$$

$$K^*: 4 \times 0.890^2 = 3.168 \text{ GeV}^2$$

$$\rho, \omega\phi: 0.780^2 + (0.780^2 + 2 \times 1.00^2) = 3.217 \text{ GeV}^2$$



# vector portal



$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$

also axion portal: Hochberg, Kuflik, McGehee, HM, Schutz, arXiv:1806.10139  
 Higgs portal: Choi, Hochberg, Kuflik, Lee, Mambrini, HM, Pierre, arXiv:1707.01434

# Kinetically mixed U(1)

- e.g., the SIMPlEst model  
SU(2) gauge group with  
 $N_f=2$  (4 doublets)
- SU(4)=SO(6)
- gauge U(1)=SO(2)  
 $\subset$  SO(2)  $\times$  SO(3)  
 $\subset$  SO(5)=Sp(4)
- maintains degeneracy of quarks
- near degeneracy of pions for co-annihilation
- SO(6)/SO(5) linear sigma model

$$SU(4)/Sp(4) = S^5$$

$$(q^+, q^+, q^-, q^-)$$

$$(\pi^{++}, \pi^{--}, \pi_x^0, \pi_y^0, \pi_z^0) + \sigma$$

$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$

# revenge of WIMP

- annihilation

$$\pi^{++}\pi^{--} \rightarrow \gamma_D \rightarrow \gamma \rightarrow f\bar{f}$$

- after freeze out, charged pions **down scatter** to neutral ones

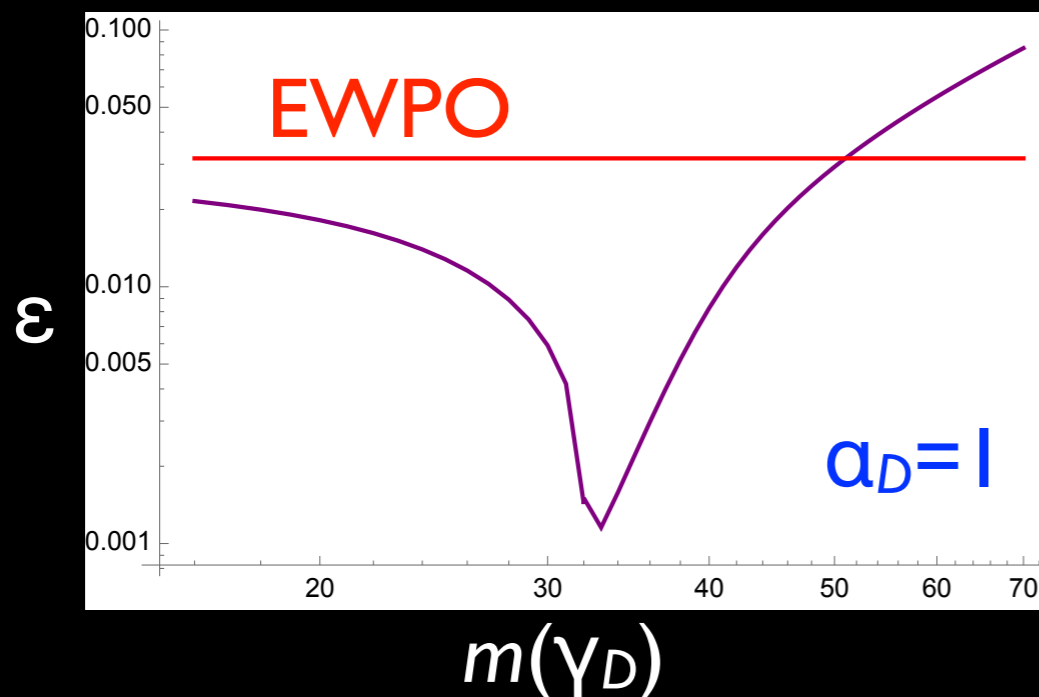
$$\pi^{++}\pi^{--} \rightarrow \pi_i^0\pi_i^0$$

- no direct/indirect limits

$$SU(4)/Sp(4) = S^5$$

$$(q^+, q^+, q^-, q^-)$$

$$(\pi^{++}, \pi^{--}, \pi_x^0, \pi_y^0, \pi_z^0) + \sigma$$



$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$



# or freeze-in

- if freeze-in, kinetic mixing can be very small
- both direct and indirect detection can be suppressed
- $SO(N_c)$  gauge theory with  $N_f=2$
- $SU(N_f)/SO(N_f) = SU(2)/SO(2) = SO(3)/SO(2)$   
linear sigma model

$$SU(2)/SO(2) = S^2$$

$$(q^+, q^-)$$

$$(\pi^{++}, \pi^{--}) + \sigma$$

$$\frac{\epsilon_\gamma}{2c_W} B_{\mu\nu} F_D^{\mu\nu}$$

# Dark Nucleons

Nell Hall (Berkeley), Thomas Konstandin (DESY),  
HM, Robert McGehee (Michigan)

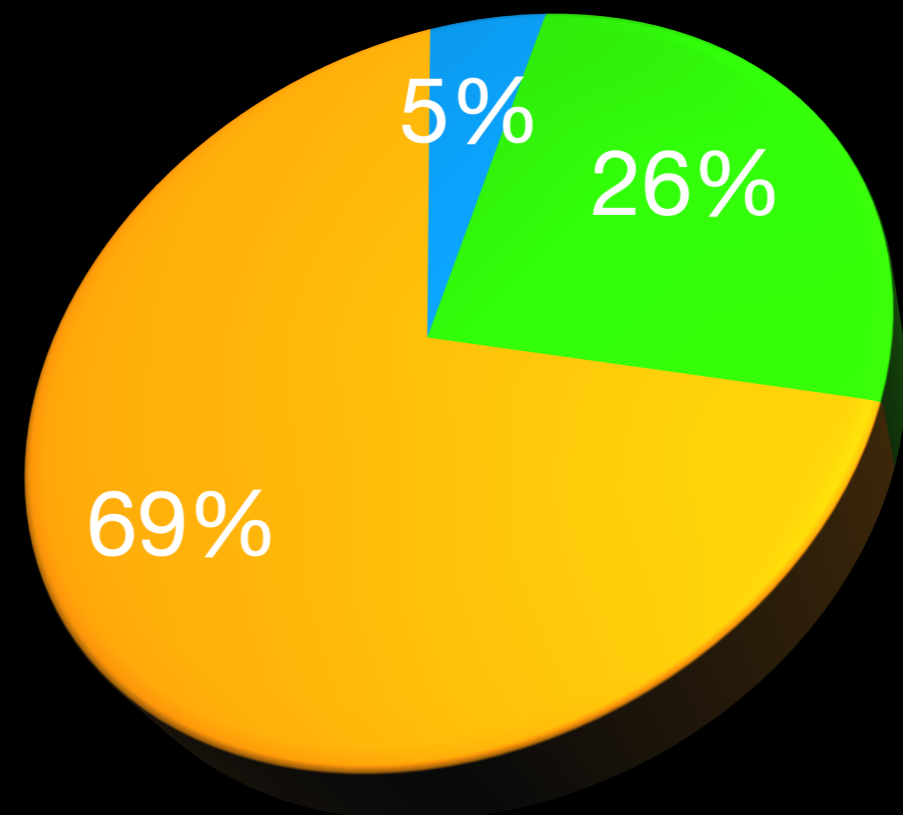
arXiv:1911.12342

+Bethany Suter (Berkeley) arXiv:2107.03398

# asymmetric dark matter

- may explain the coincidence between baryon and dark matter densities today
- need to efficiently get rid of symmetric component  
→ strongly coupled?
- proton mass is dynamical. also “dark proton?”
- If the same asymmetries,  $m_{ADM} \sim 6\text{GeV}$ , “light” dark matter
- need anomalies and non-anomalous gauge
  - simplest structure: copy of SM
- need equilibration mechanism between two asymmetries  
→ neutrino portal

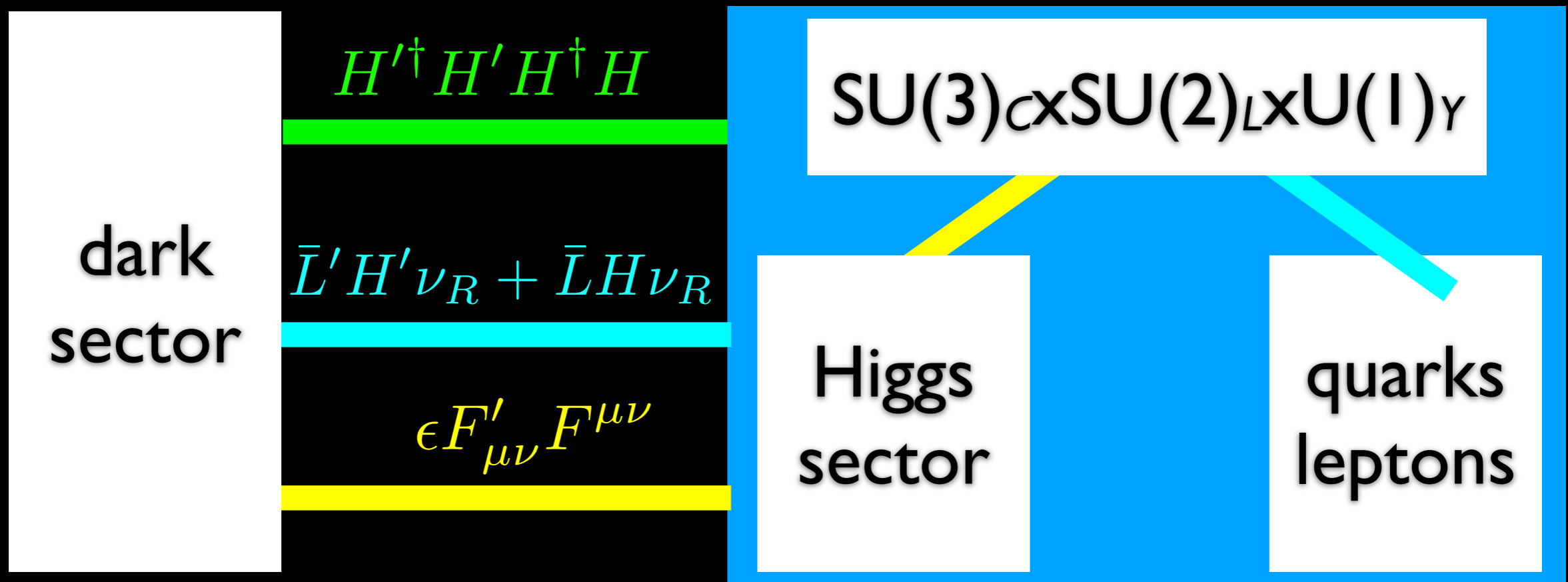
- baryon
- Dark Matter
- Dark Energy

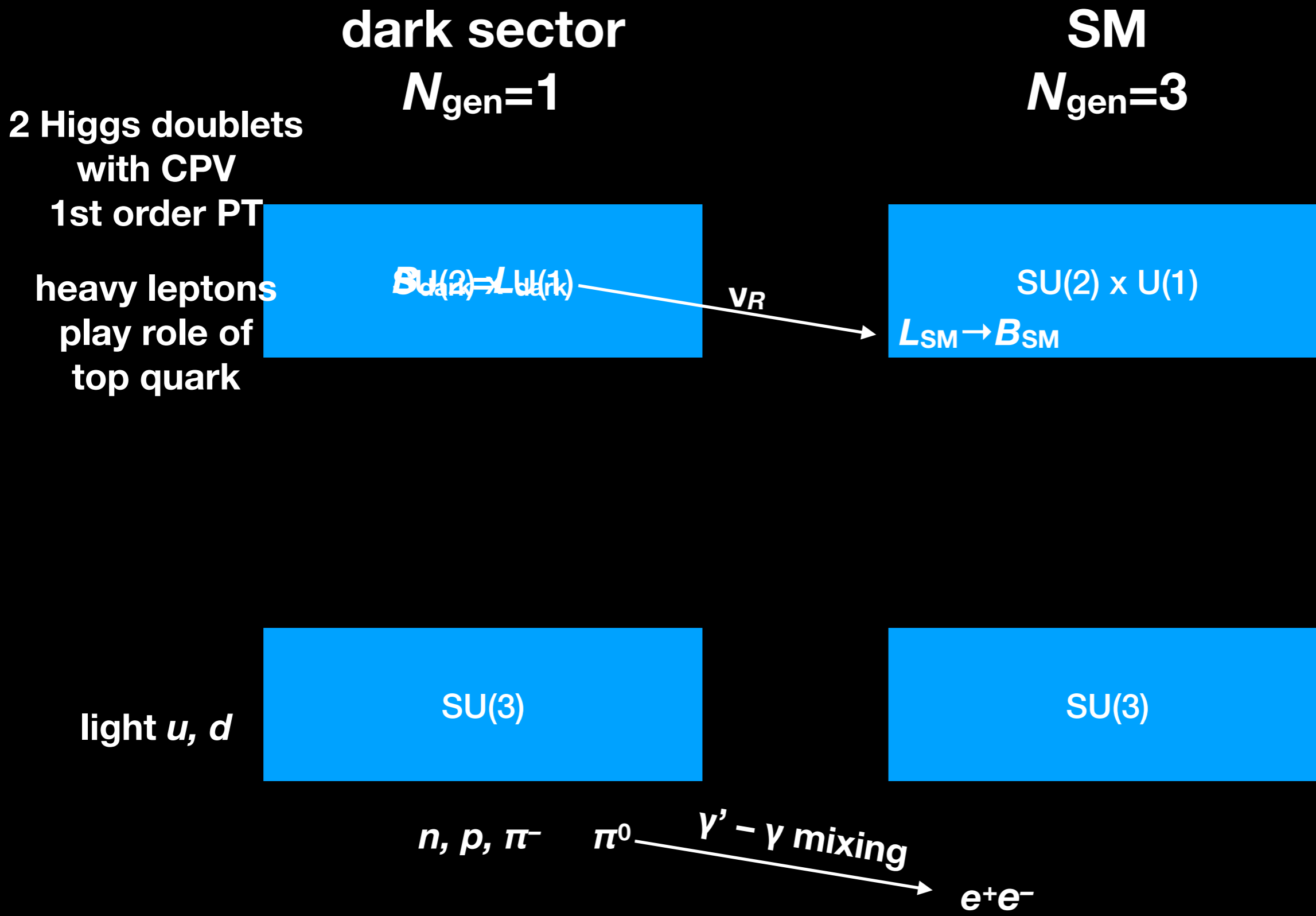


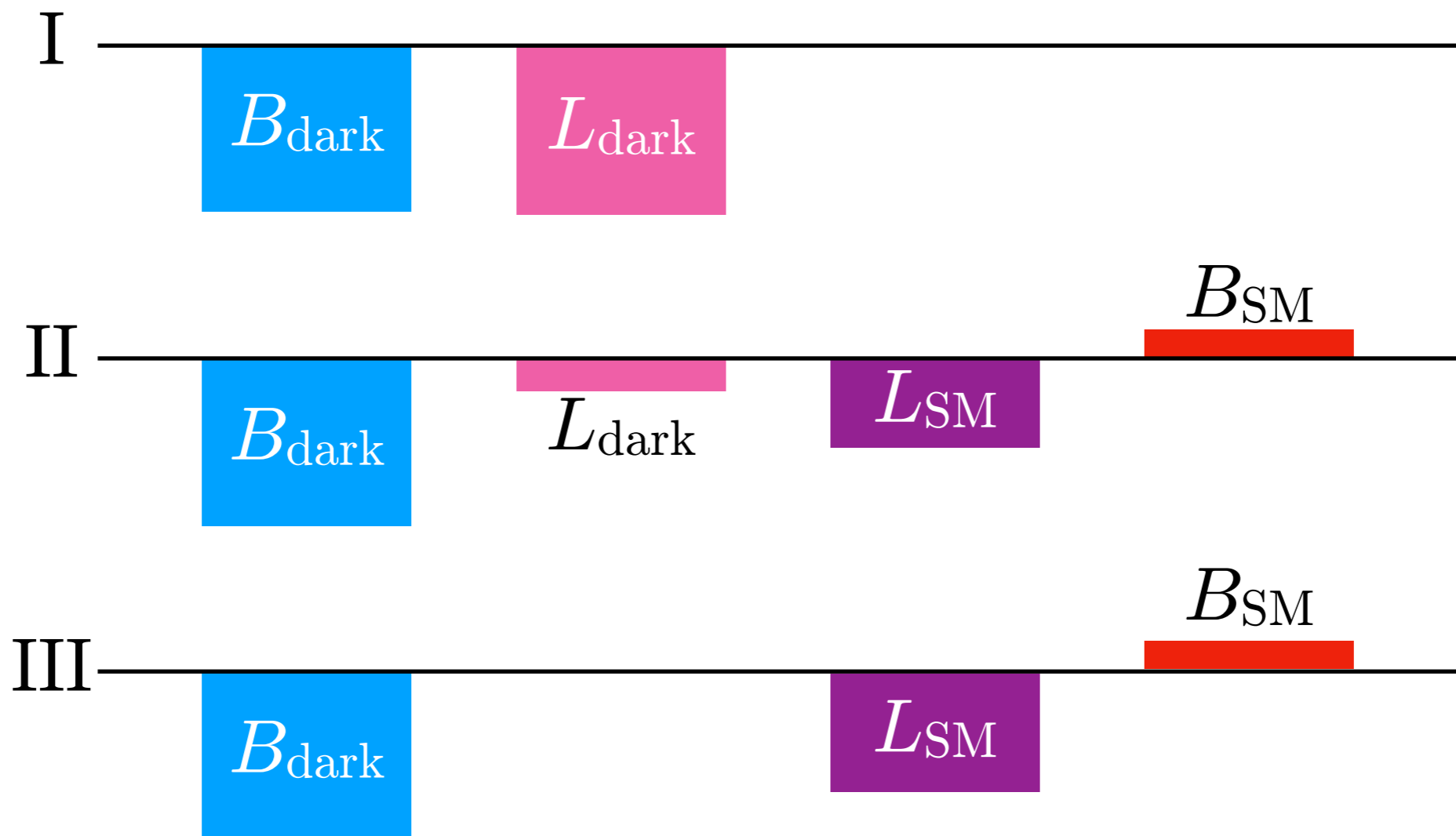


# portals

three possible portals in renormalizable theories







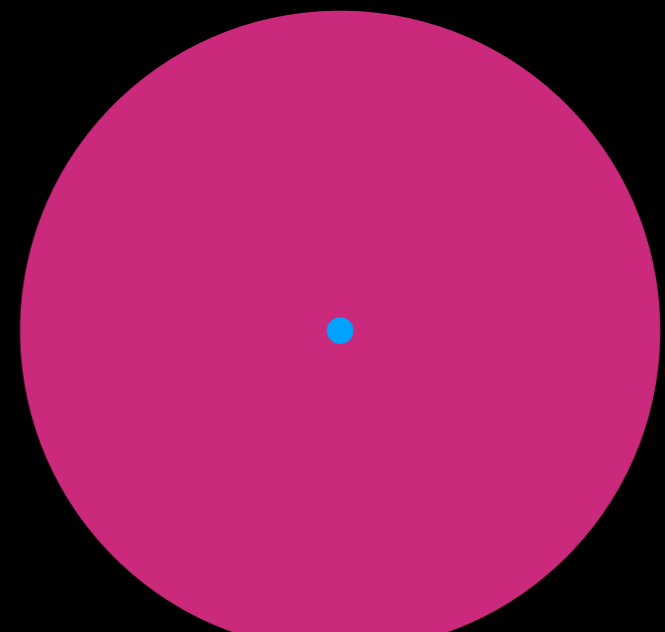
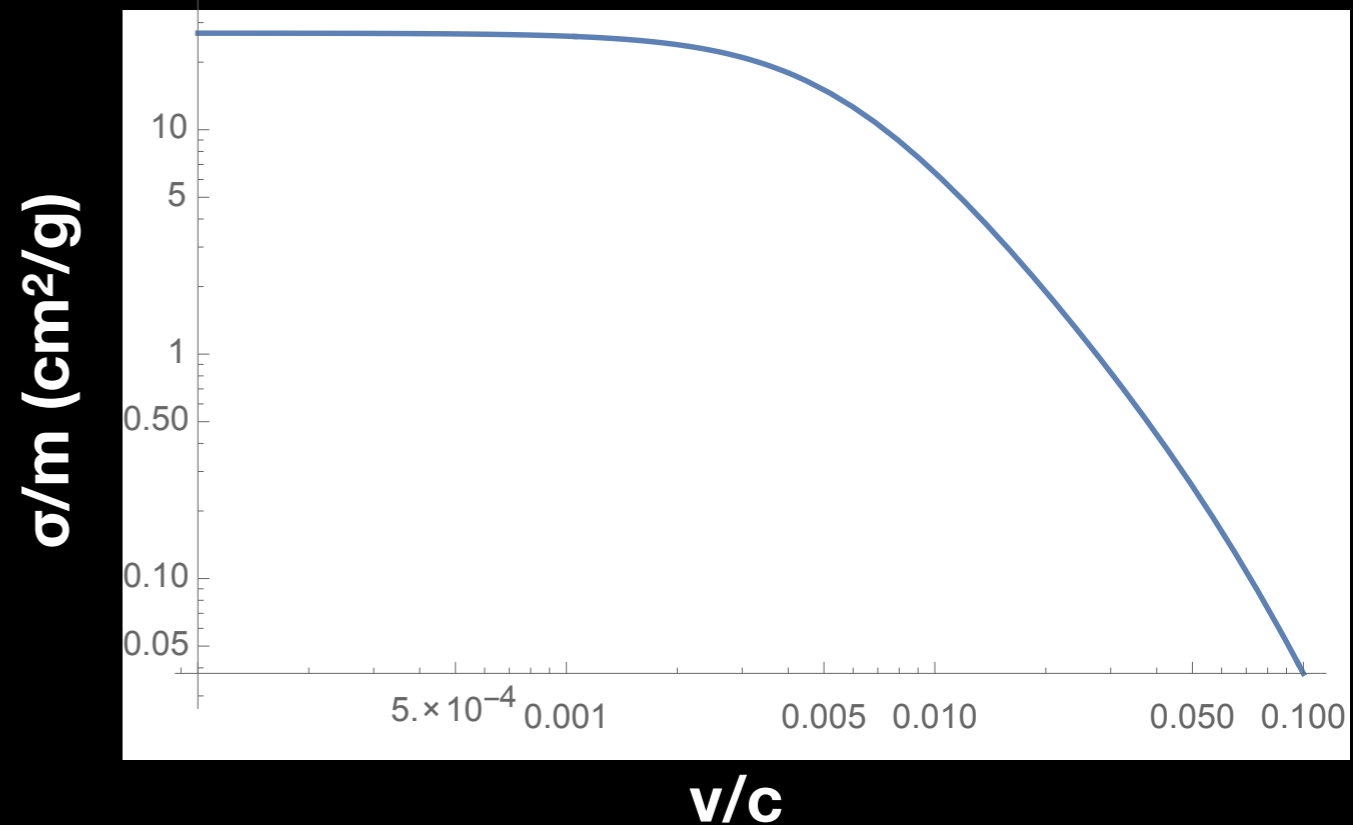
**If  $M_N > T_{\text{sphaleron}}$**   $B_{\text{SM}} = \frac{36}{133} B_{\text{dark}},$   $L_{\text{SM}} = -\frac{97}{133} B_{\text{dark}}$   $m_{n'} = 1.63 \text{ GeV}$

**If  $M_N < T_{\text{sphaleron}}$**   $B_{\text{SM}} = \frac{12}{37} B_{\text{dark}},$   $L_{\text{SM}} = -\frac{25}{37} B_{\text{dark}}$   $m_{n'} = 1.36 \text{ GeV}$



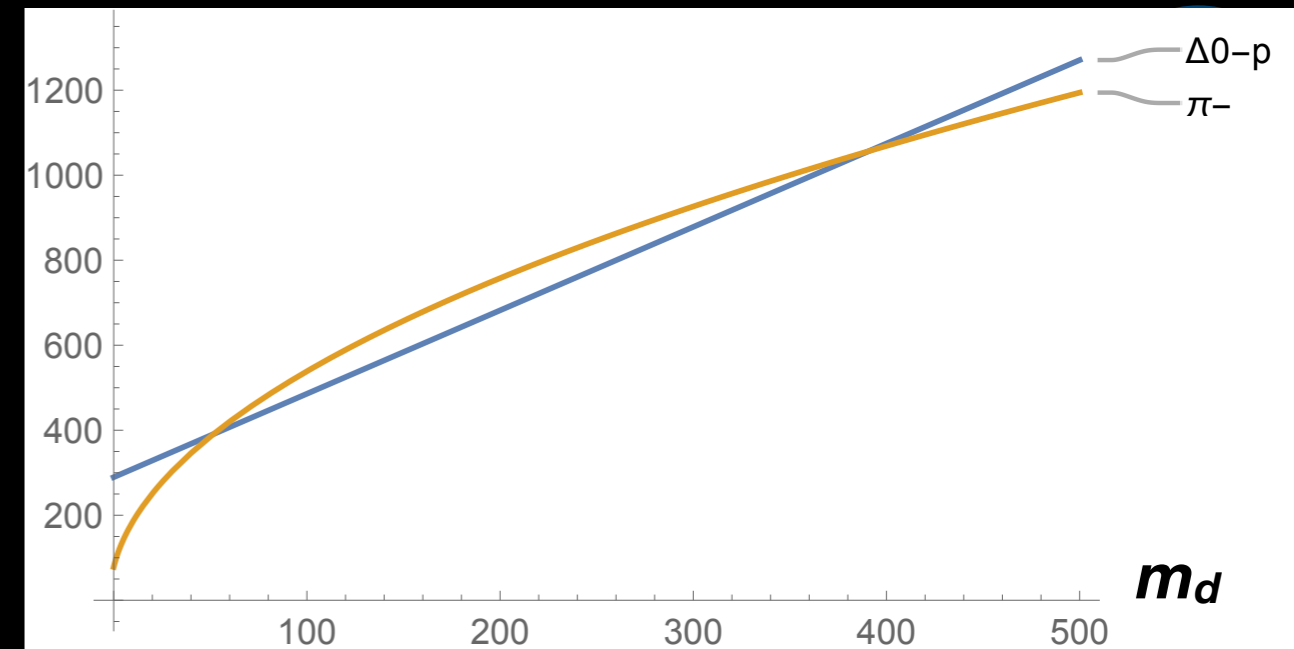
# *n-n* scattering

- *n-n* scattering has an anomalously large cross section  $a=18.9\text{fm}$
- also steep velocity dependence
- depending on the details of the QCD-like dynamics, it could provide SIDM

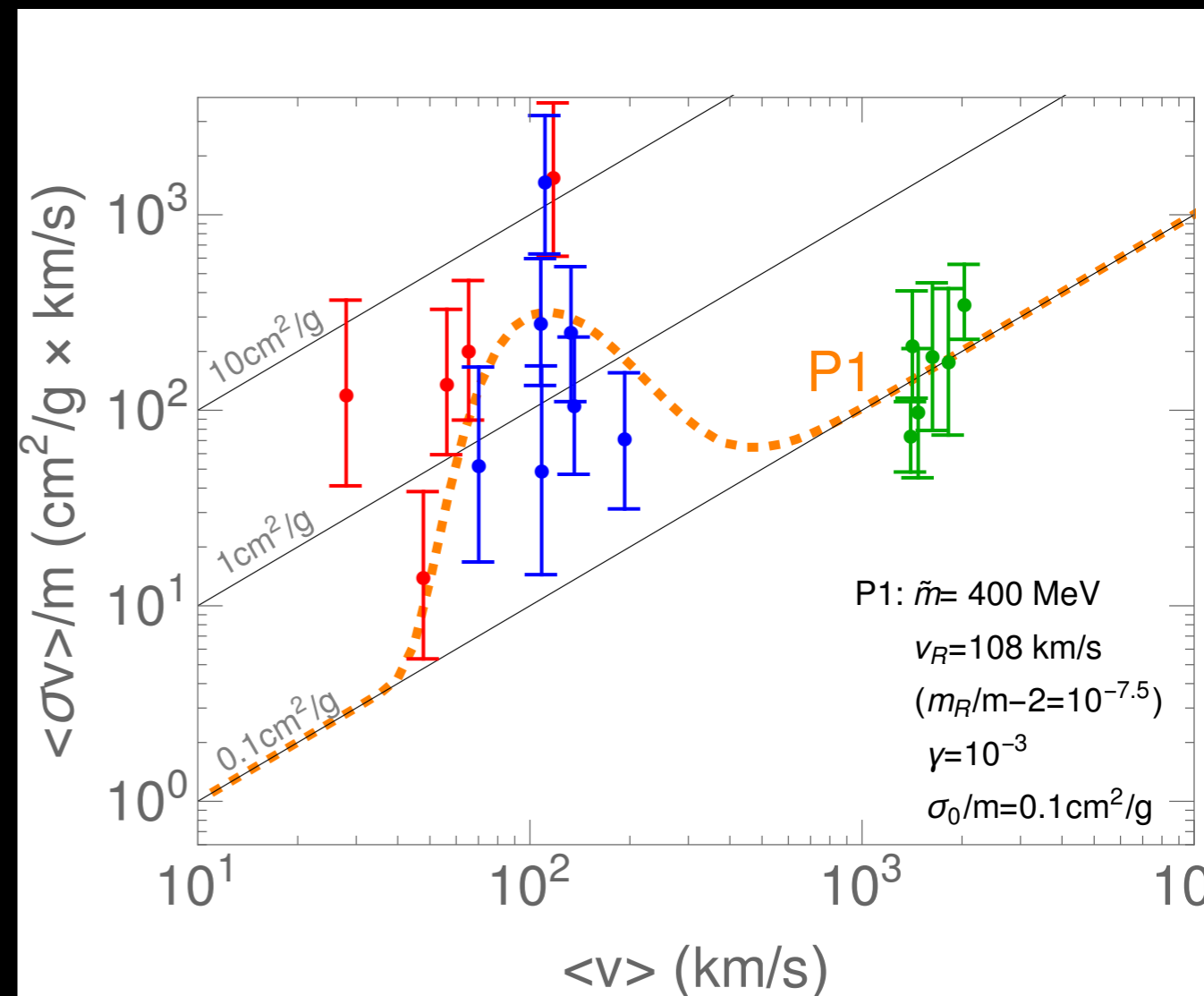


# baryon spectrum

- $m_u$  and  $m_d$  free parameters
- If  $m_d \ll m_u \ll \Lambda_{\text{QCD}}$ ,  $n'$  dominates
- If  $m_u \ll m_d \ll \Lambda_{\text{QCD}}$ ,  $p'$  dominates, together with  $\pi^-$  for charge neutrality
  - possibly a resonant interaction  $\pi^- p' \rightarrow \Delta^0 \rightarrow \pi^- p'$
  - may solve core/cusp problem



Robert McGehee, HM, Yu-Dai Tsai, in prep



Xiaoyong Chu, Camilo Carcia-Cely, HM, Phys.Rev.Lett. 122 (2019) no.7, 071103

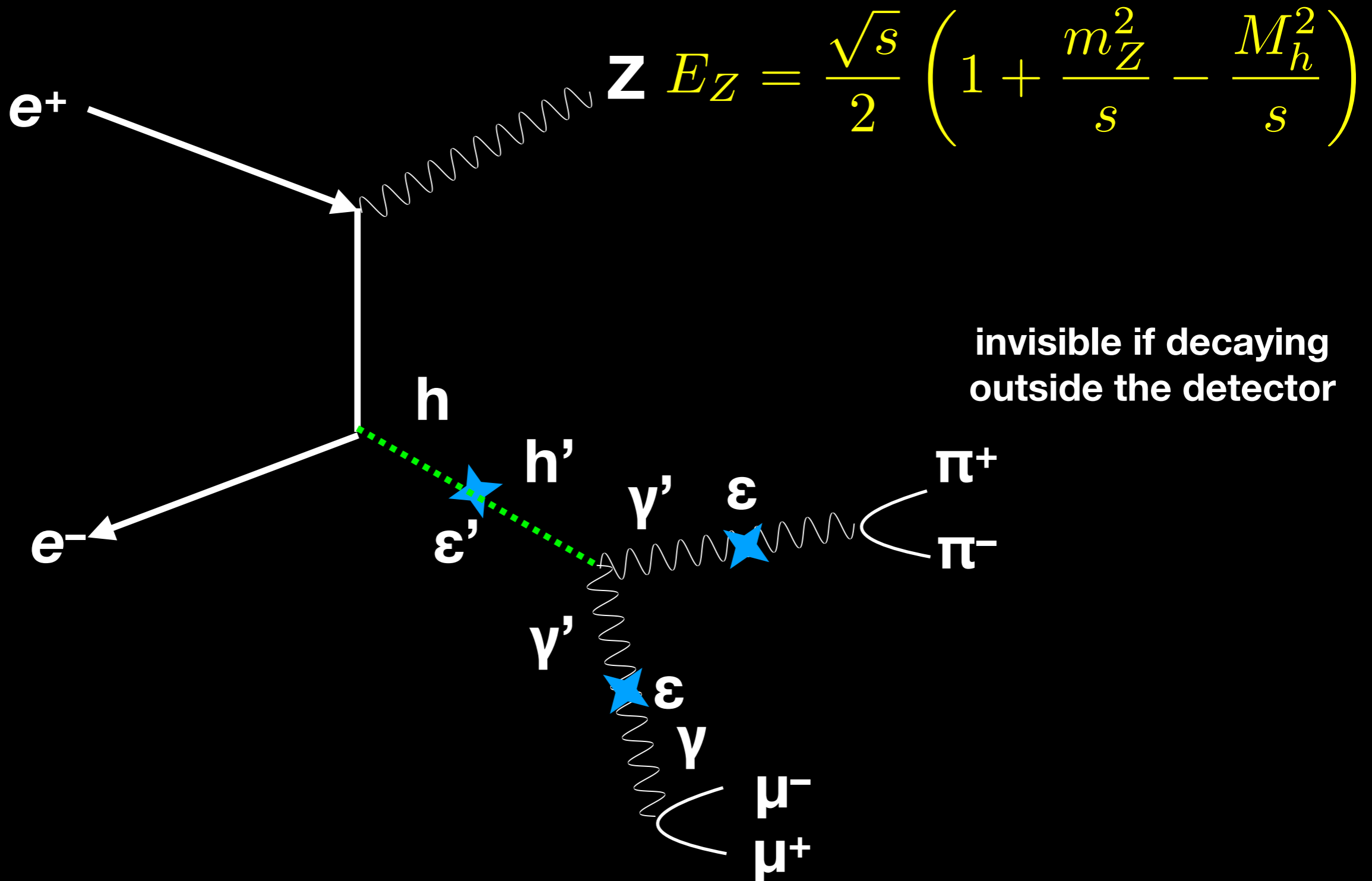
# neutrino portal

$$\mathcal{L} = y' \bar{L}' H \nu_R + y_i \bar{L}_i H \nu_R$$

$$\epsilon_i = \frac{y_i}{\sqrt{(y')^2 + (y_i)^2}} \quad M_\nu = \sqrt{(y')^2 + (y_i)^2} v$$

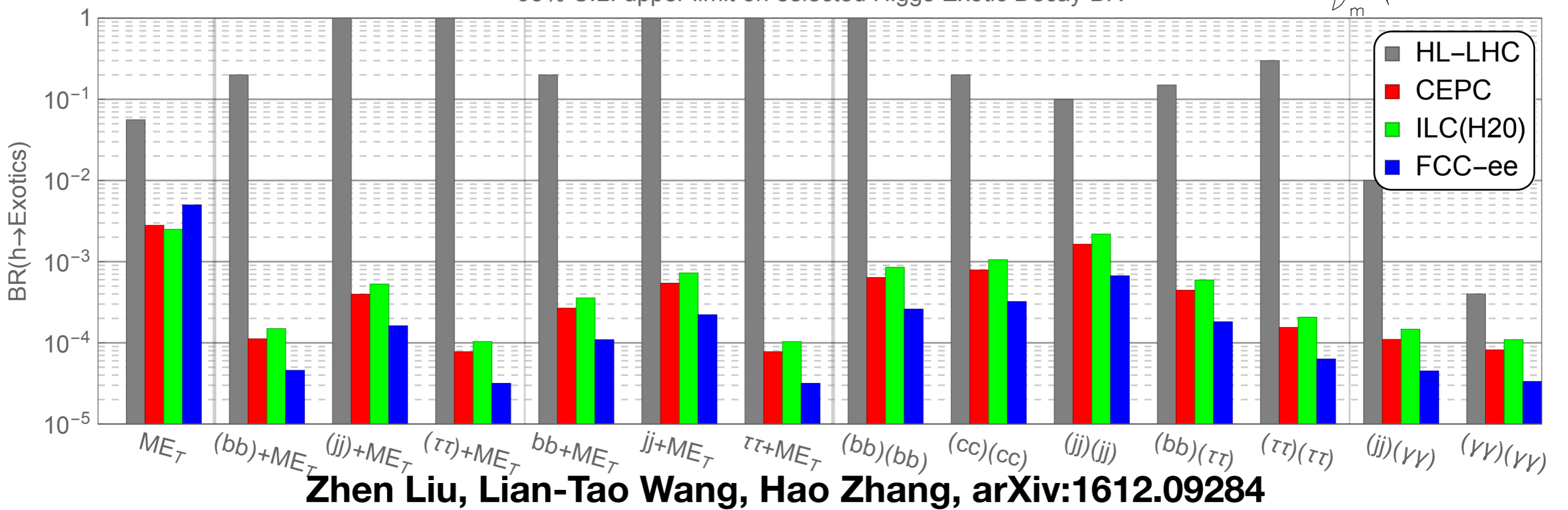
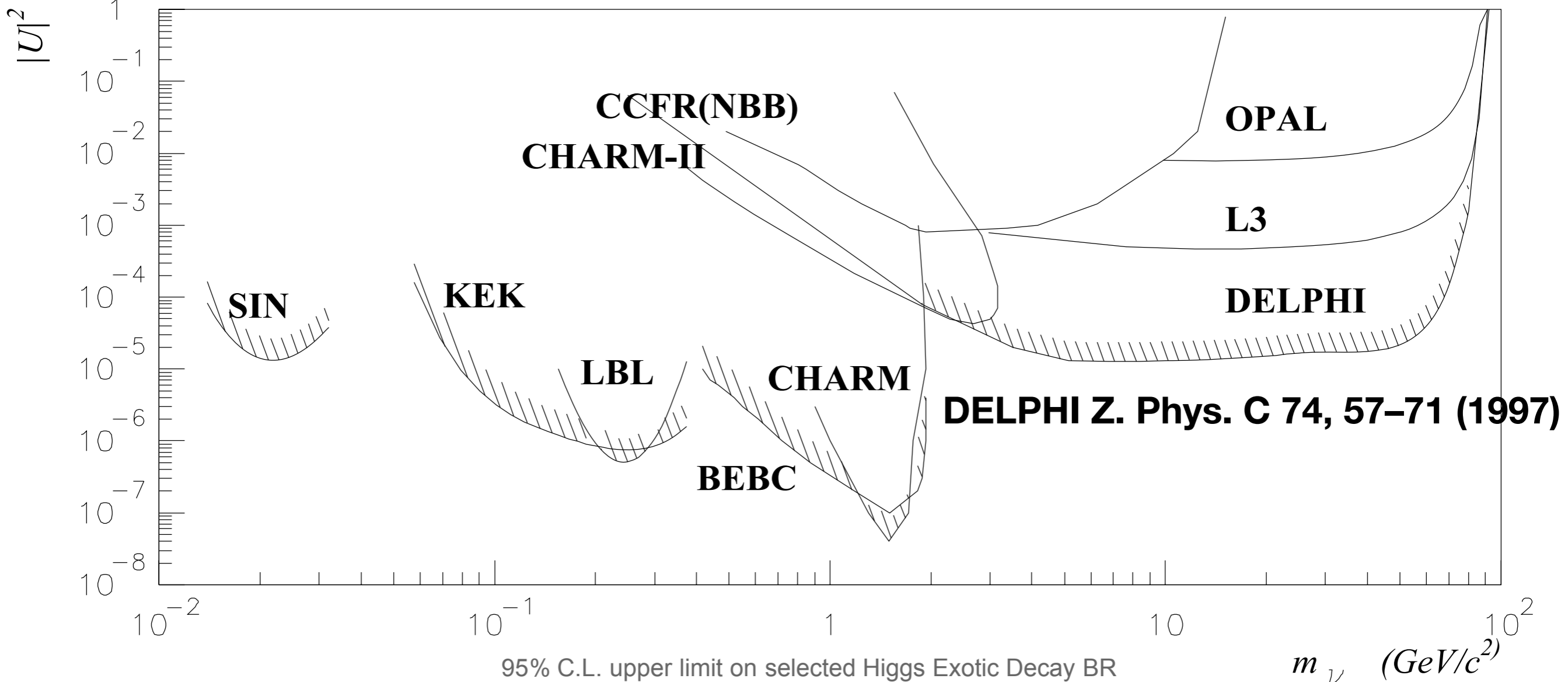
- charged current universality:  $\epsilon_i^2 < 10^{-3}$
- $\mu \rightarrow e \gamma$  constraint:  $\epsilon_e \epsilon_\mu < 4 \times 10^{-5} (G_F M_\nu)$
- $\tau \rightarrow \mu \gamma$  constraint:  $\epsilon_e \epsilon_\mu < 0.03 (G_F M_\nu)$
- If  $M_\nu < 70 \text{ GeV}$ ,  $\epsilon_i^2 < 10^{-5}$  (DELPHI:  $Z \rightarrow \nu \nu_R$ ,  $\nu_R \rightarrow l f f$ )
- equilibration of asymmetries requires only  $\epsilon_i > 10^{-16}$  or so
- (orders of magnitude estimates so far)

# Higgs portal





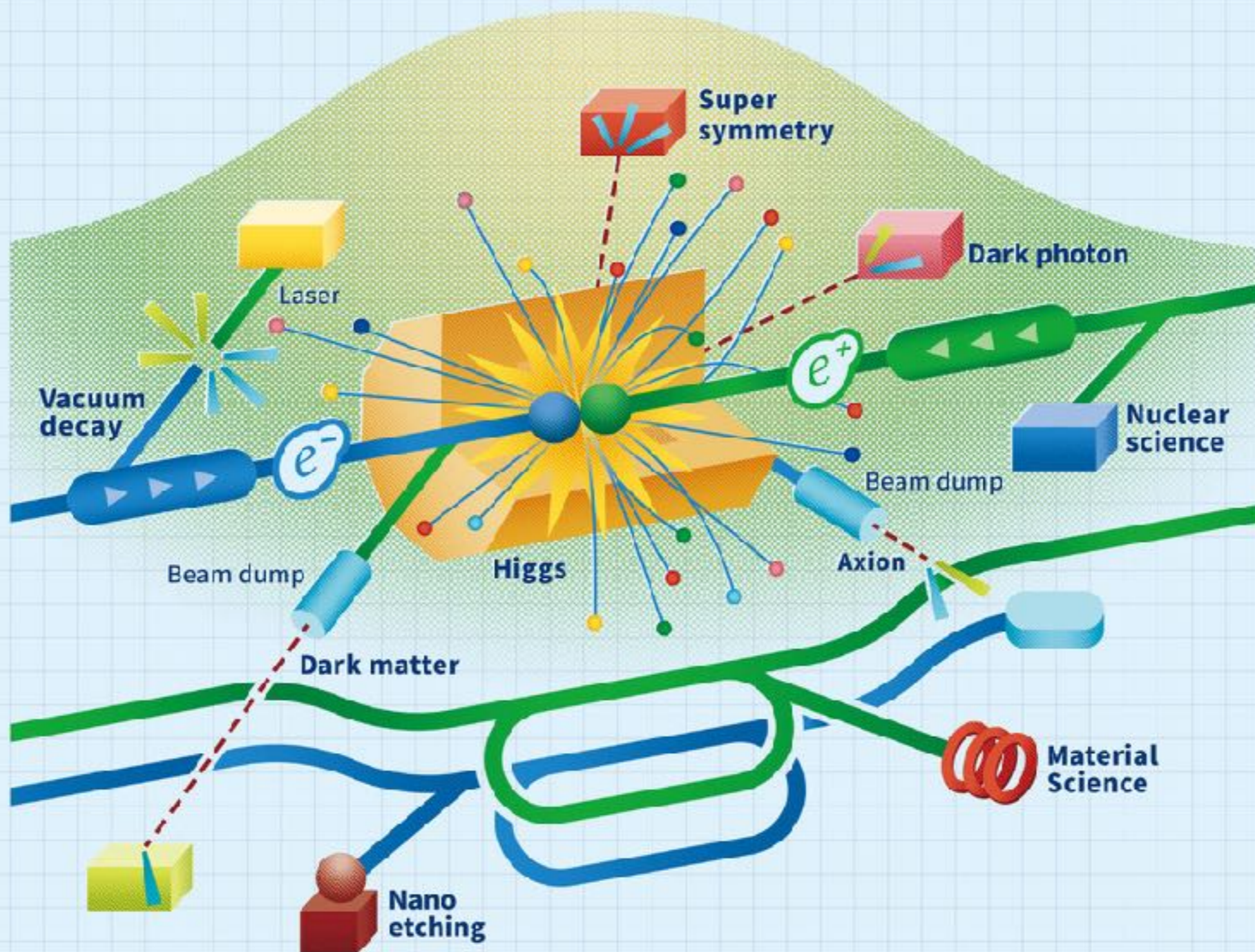






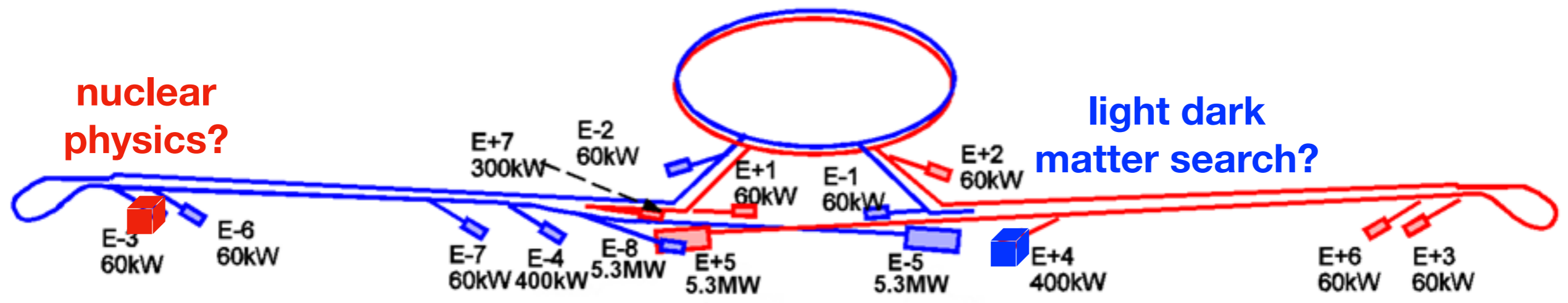
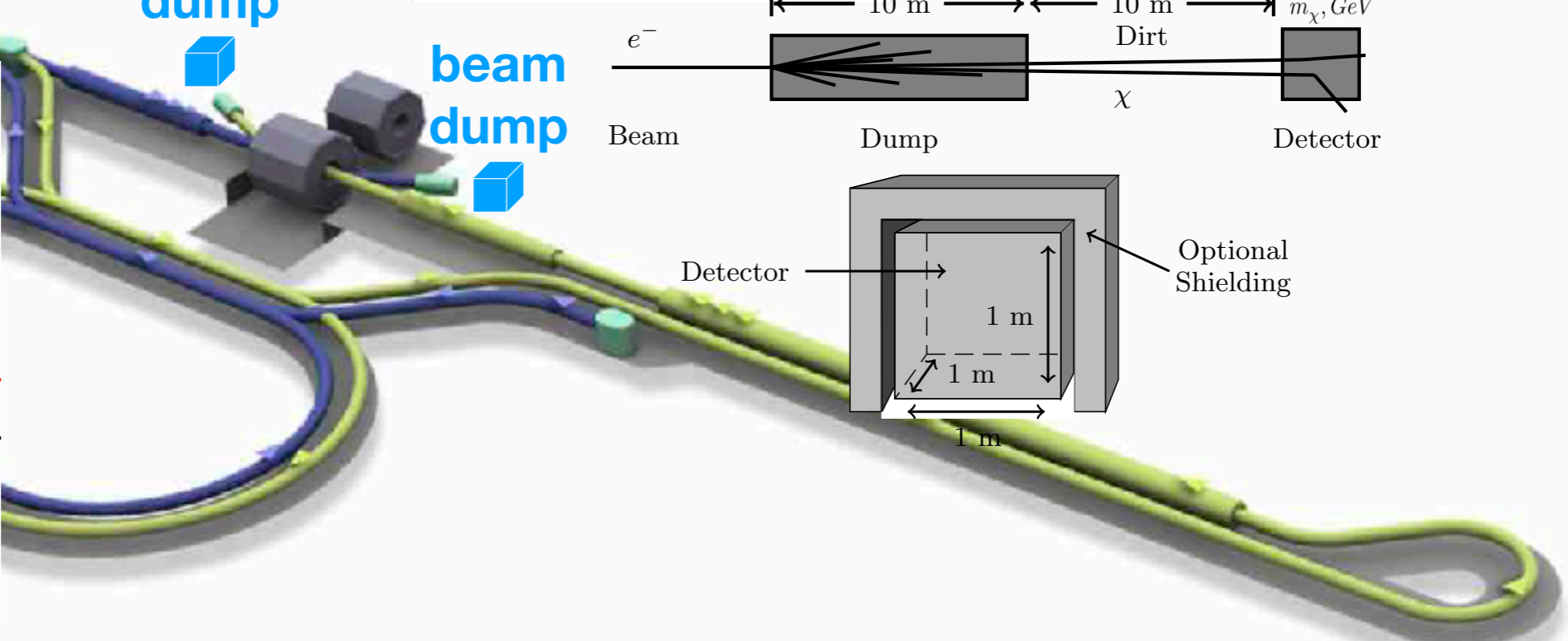
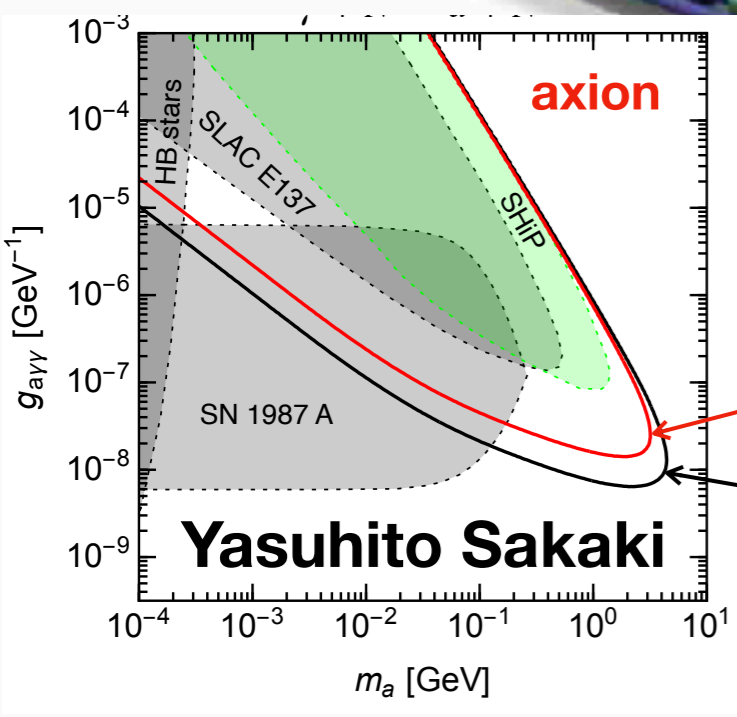
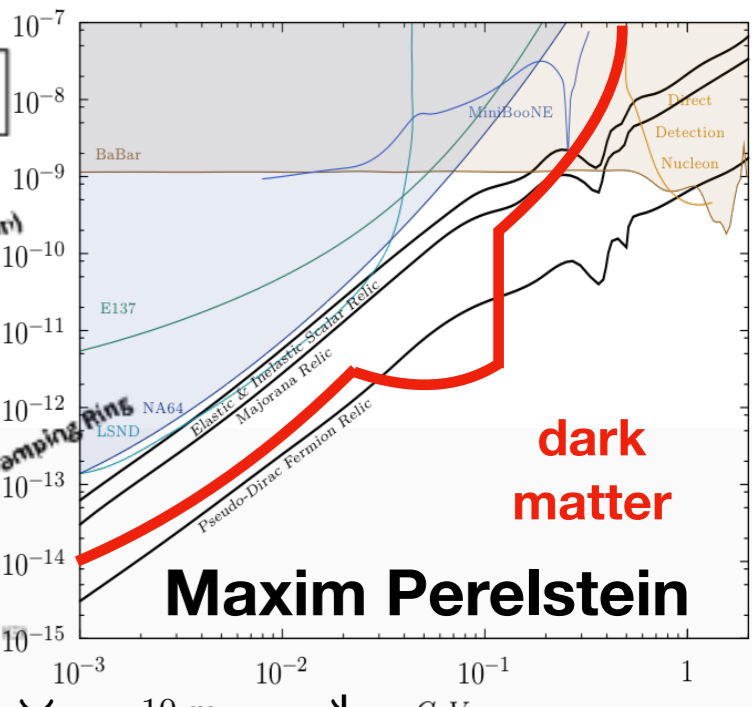
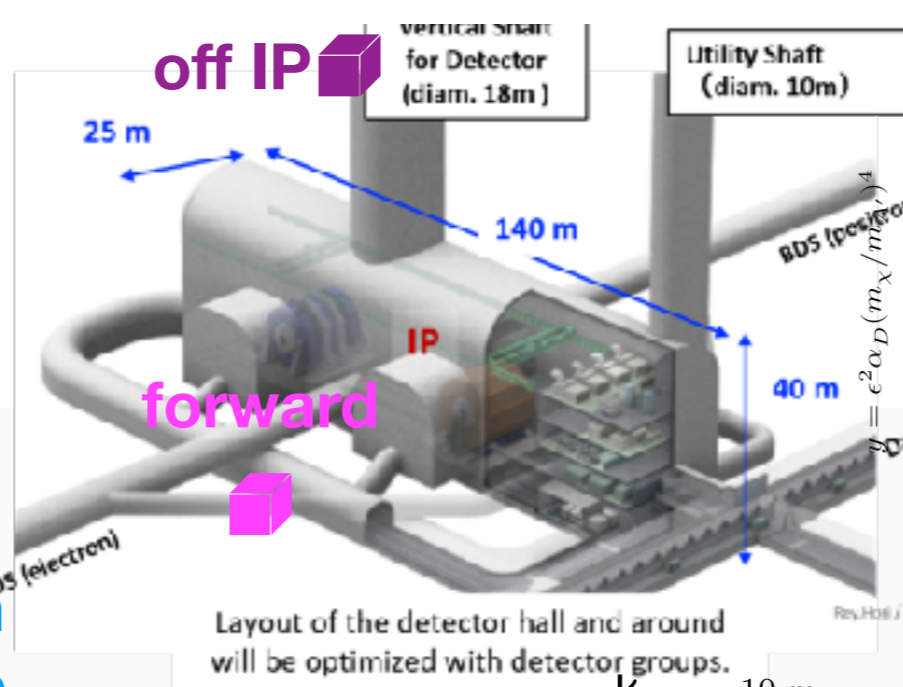
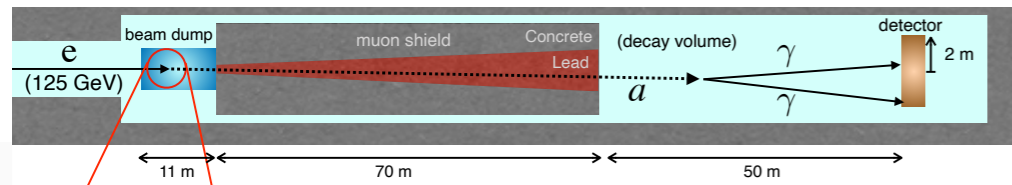
# ILCX 2021

## ILC Workshop on Potential Experiments



26-29 October 2021, Tsukuba, Japan



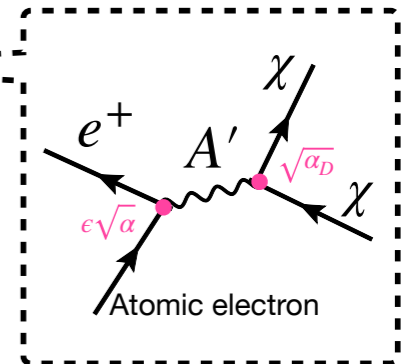
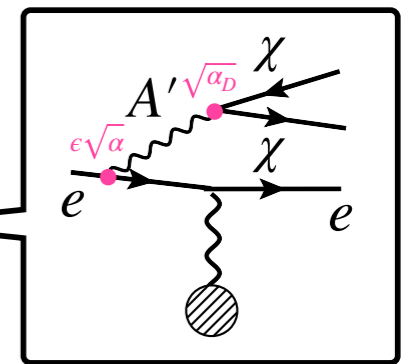
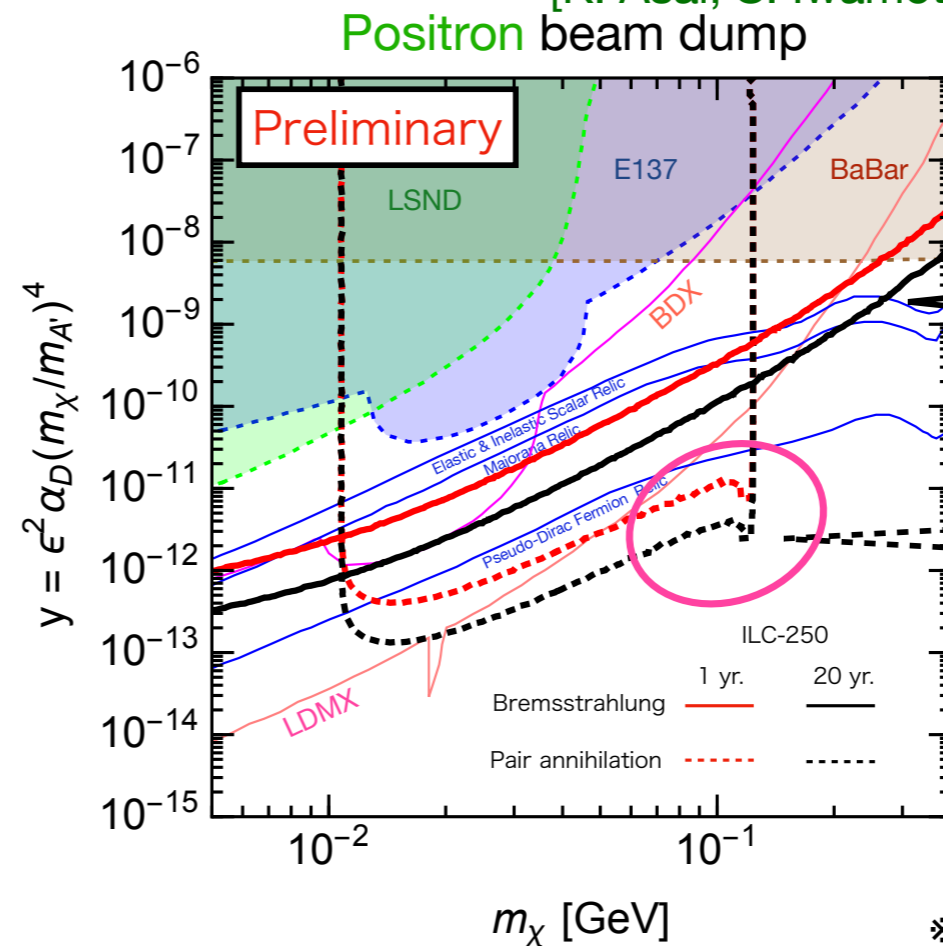
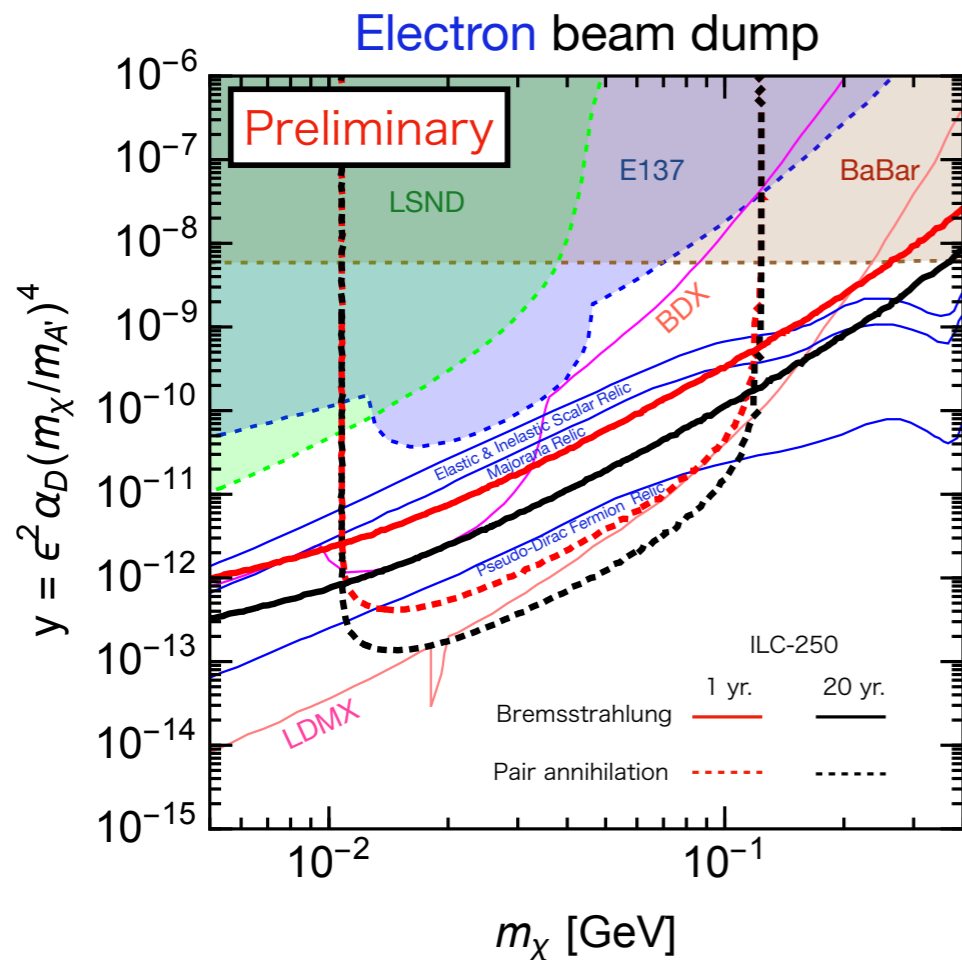




# Results of invisible decay search

## Sensitivity comparison of positron and electron beam dump experiment

[K. Asai, S. Iwamoto, M. Perelstein, Y. Sakaki, DU.]



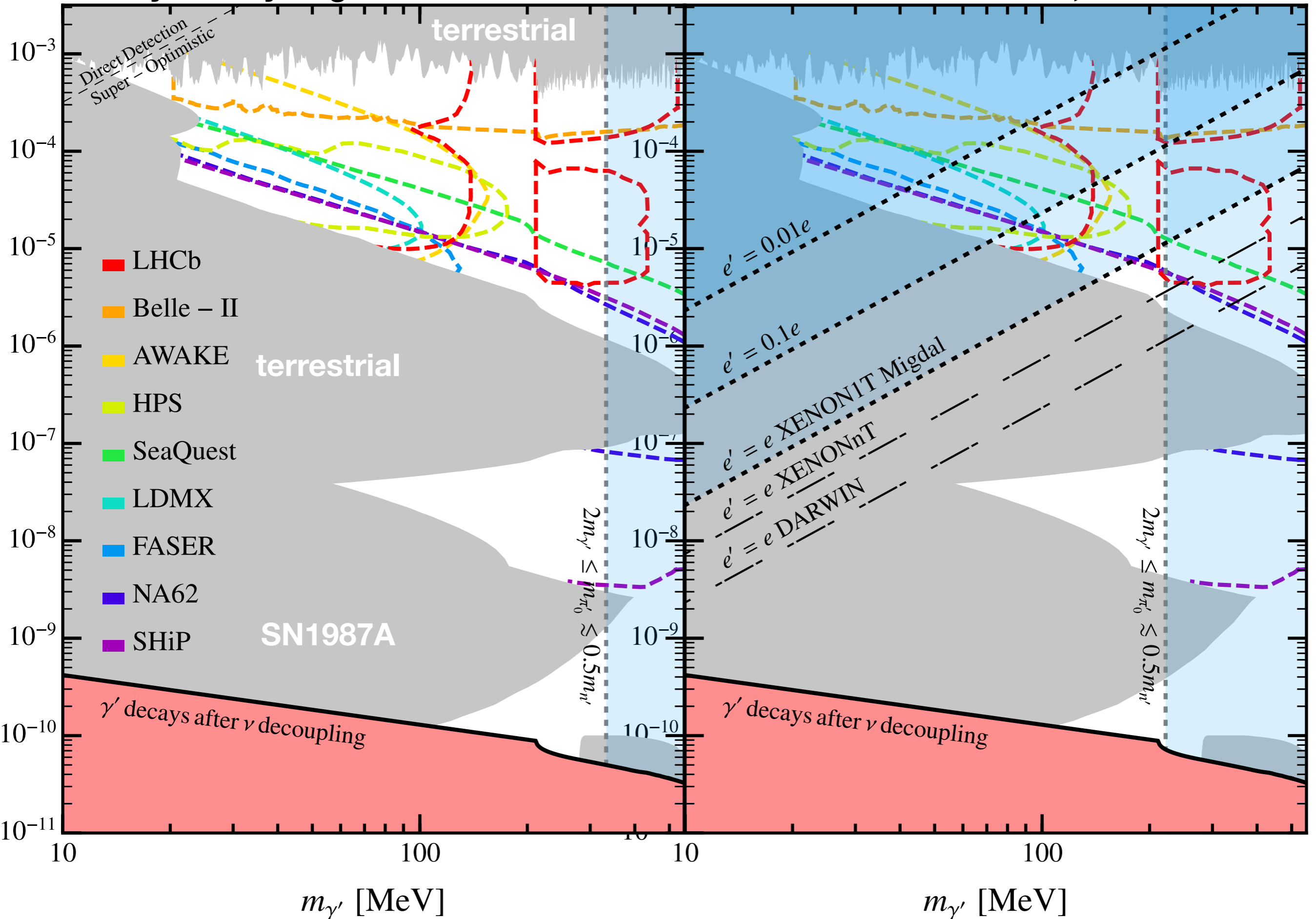
\*  $\alpha_D \equiv g_D^2/4\pi = 0.5$ ,  $m_{A'} = 3m_\chi$

A benchmark Model: 
$$-\frac{1}{4}F_{\mu\nu}^{A'}F_{\mu\nu}^{A'} - \frac{\epsilon}{2}F_{\mu\nu}F_{\mu\nu}^{A'} + \frac{m_{A'}^2}{2}A'_\mu A'^\mu + \bar{\chi}(iD_\mu\gamma^\mu - m_\chi)\chi, \quad D_\mu = \partial_\mu + ig_D A'_\mu$$

# Dark Neutron Dark Matter

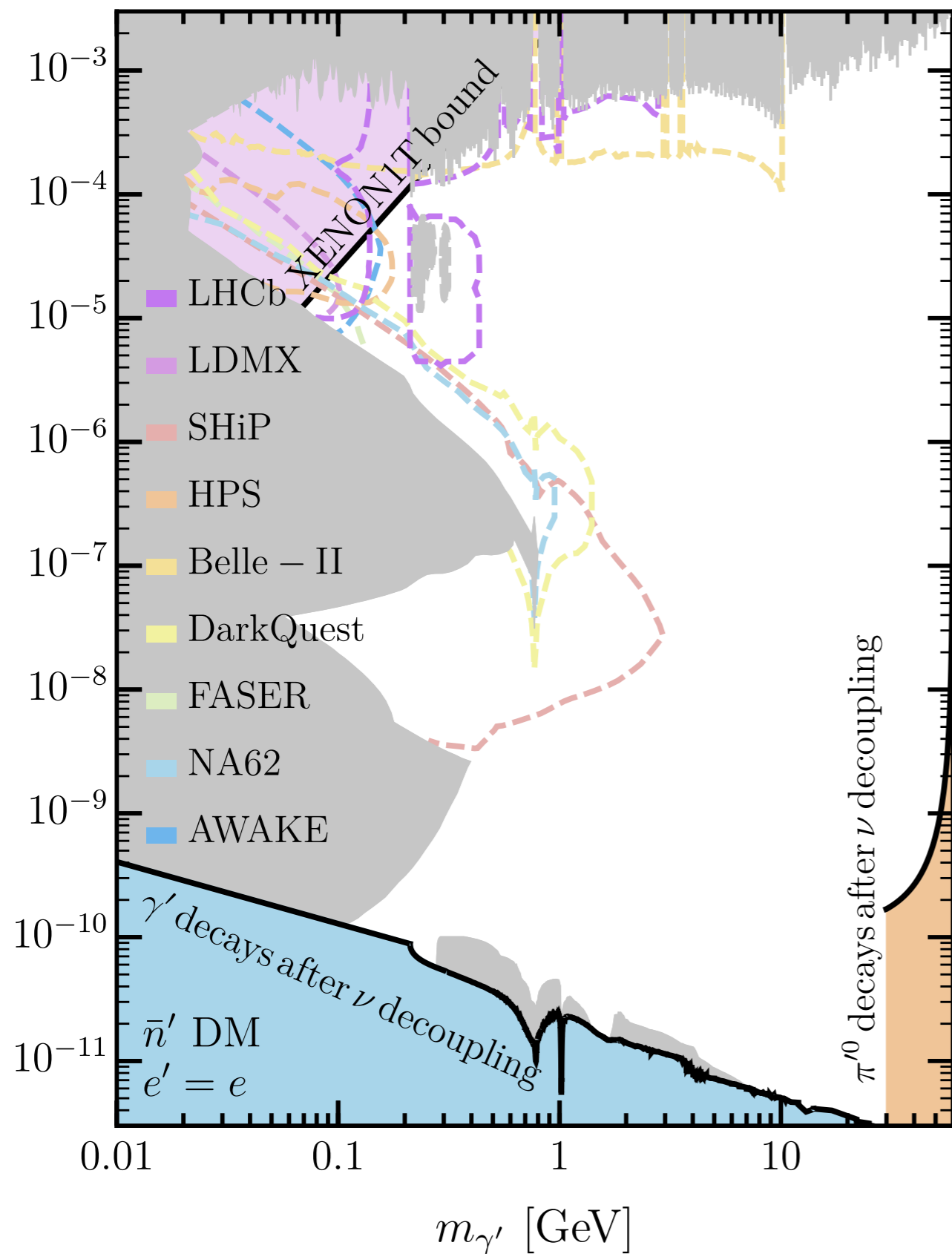
# Dark Proton & Pion Dark Matter

If the asymmetry originates in the dark side transferred to the SM side,  $m_{\text{DM}} \sim 1.5 \text{ GeV}$

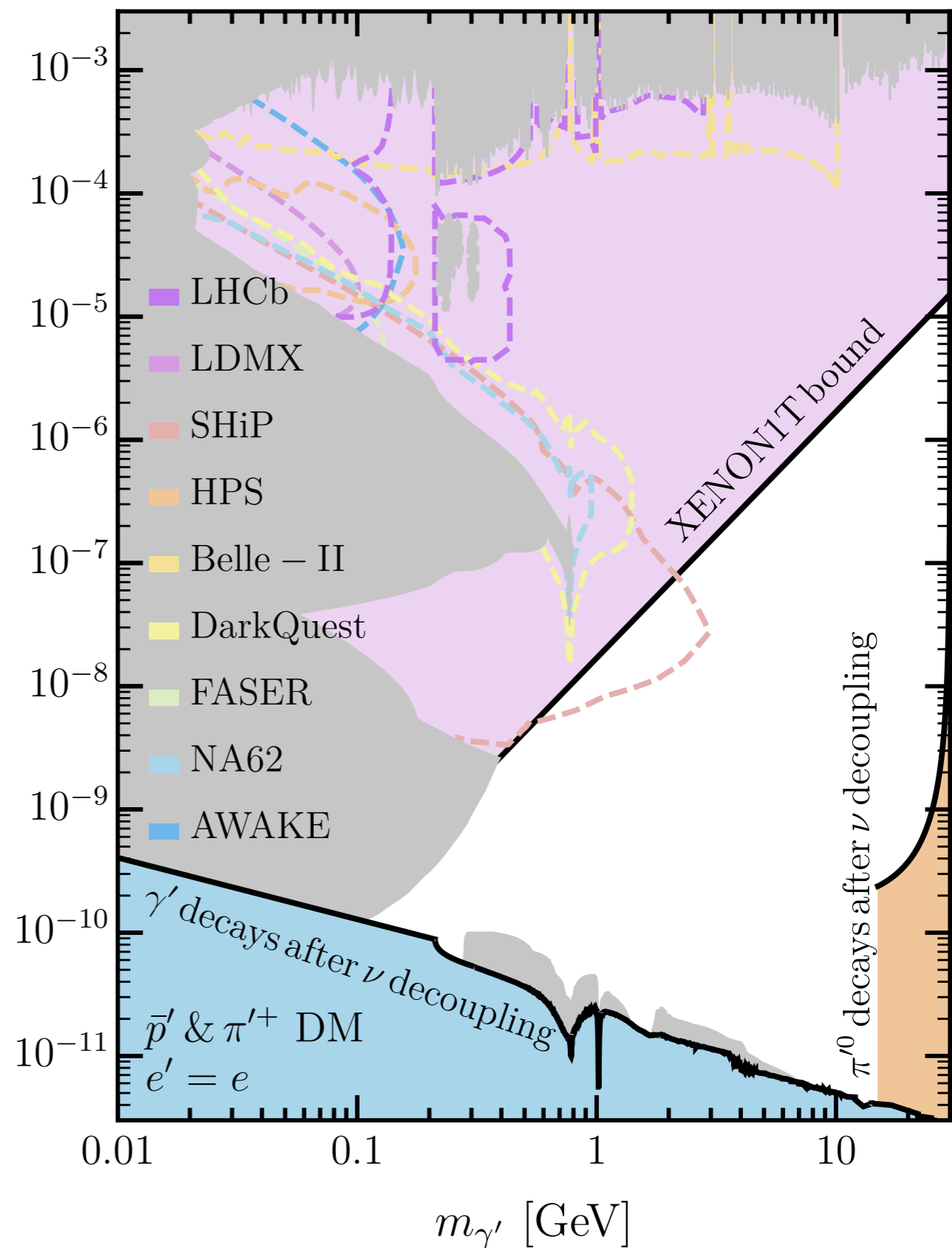


**If the asymmetry originates in the SM side transferred to the dark side**  
 **$m_{\text{DM}} \sim 60 \text{ GeV!}$  Not light even though asymmetric**

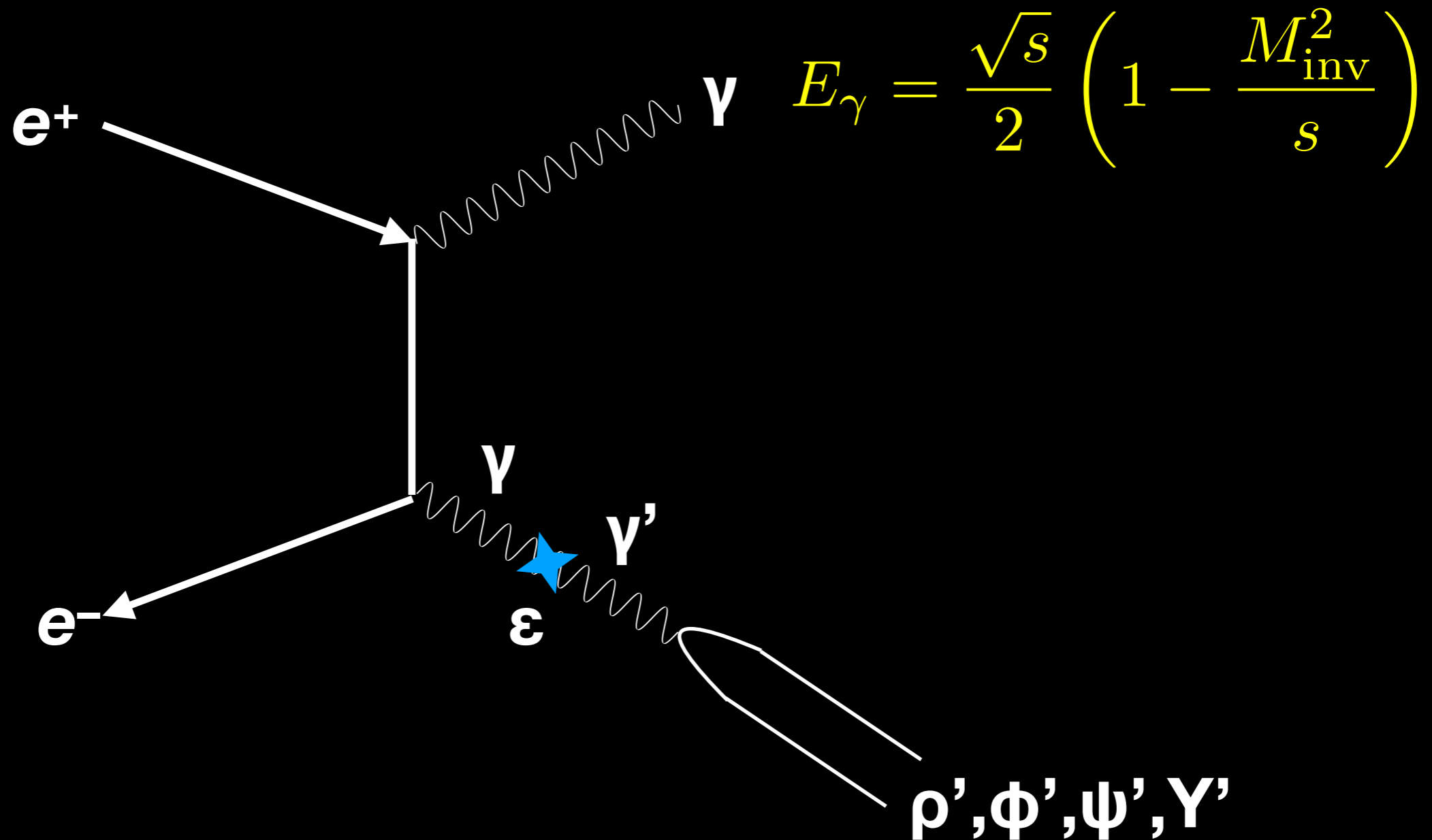
**dark neutron**



**dark proton**

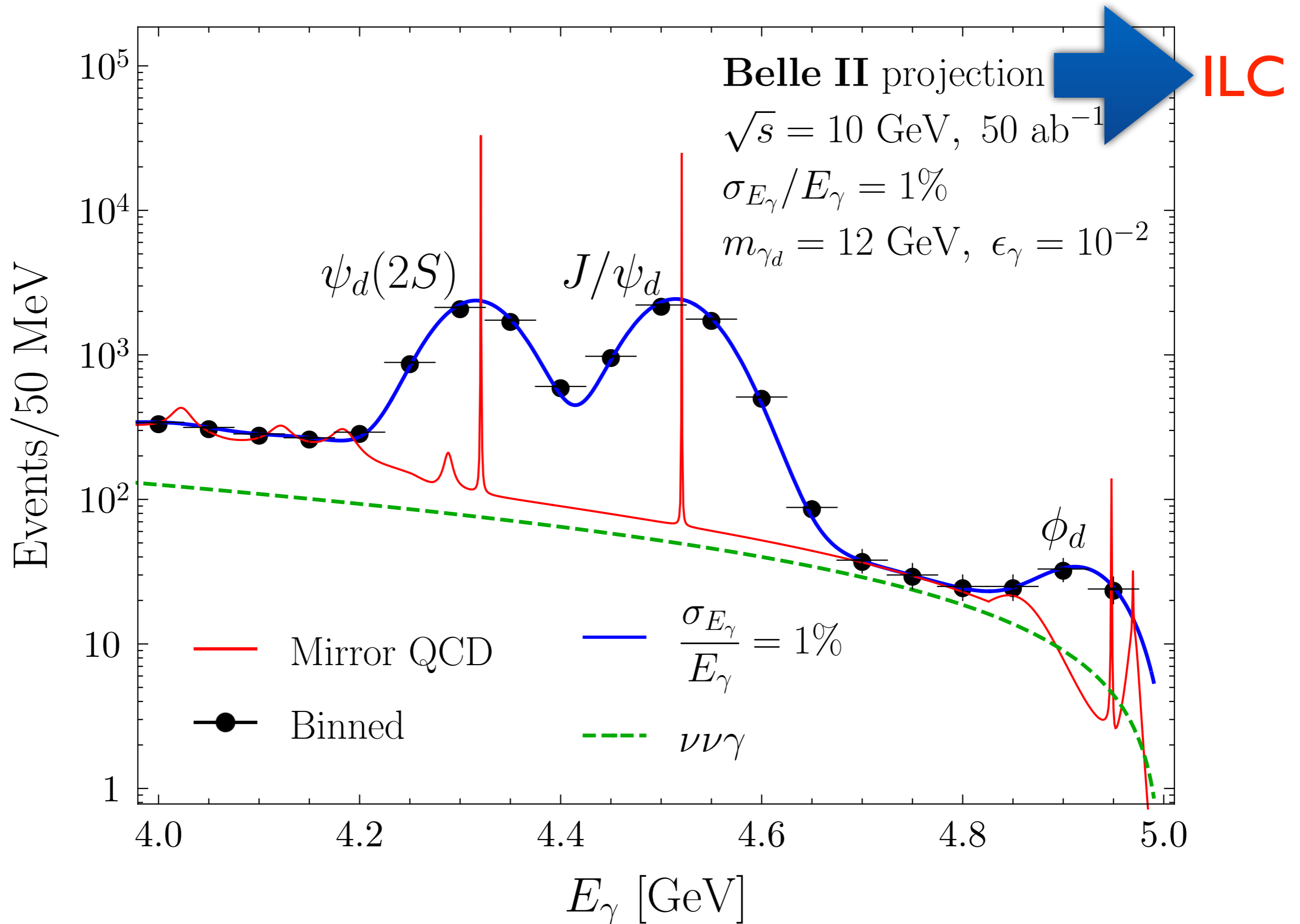


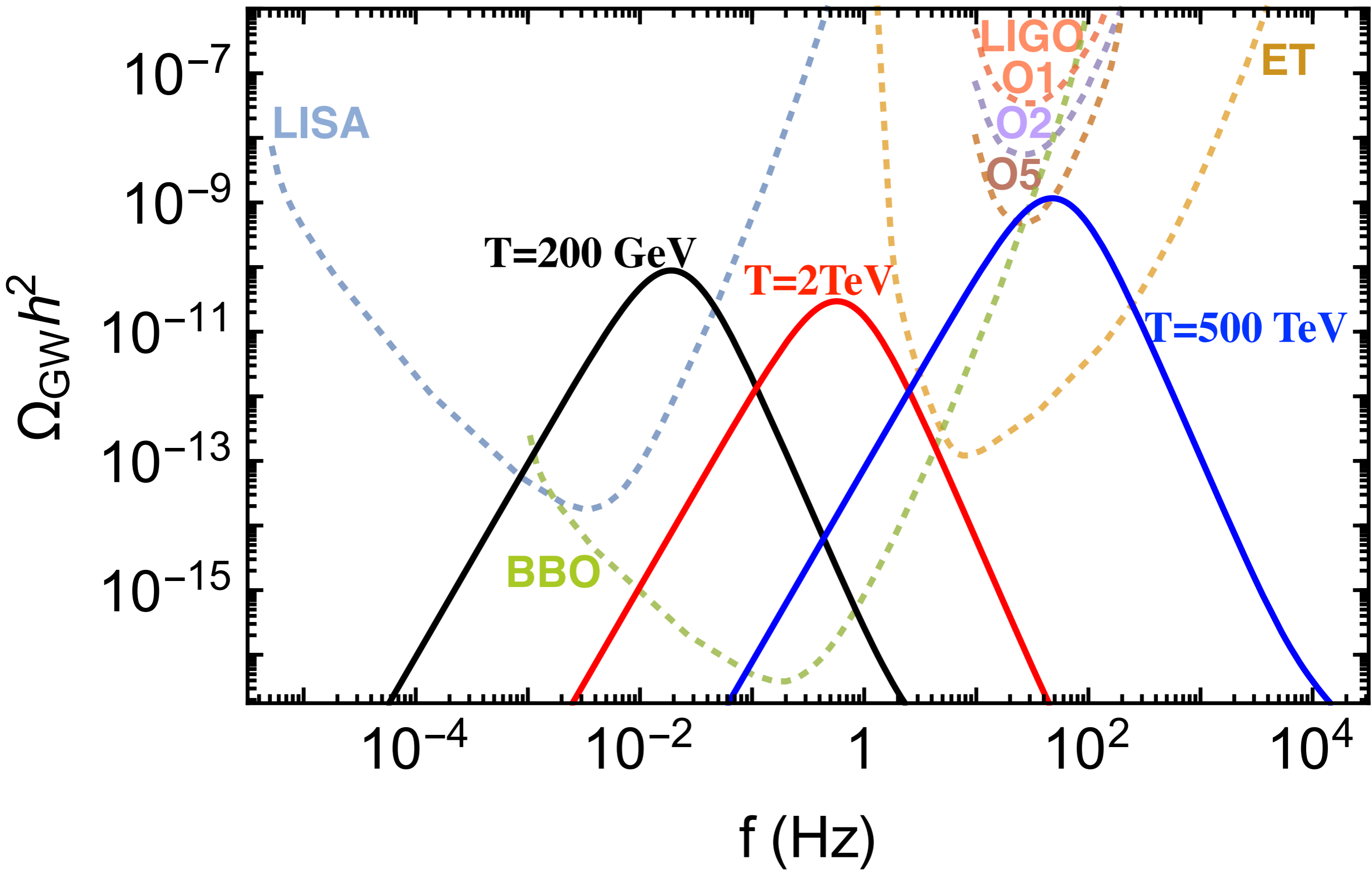
# Dark Spectroscopy



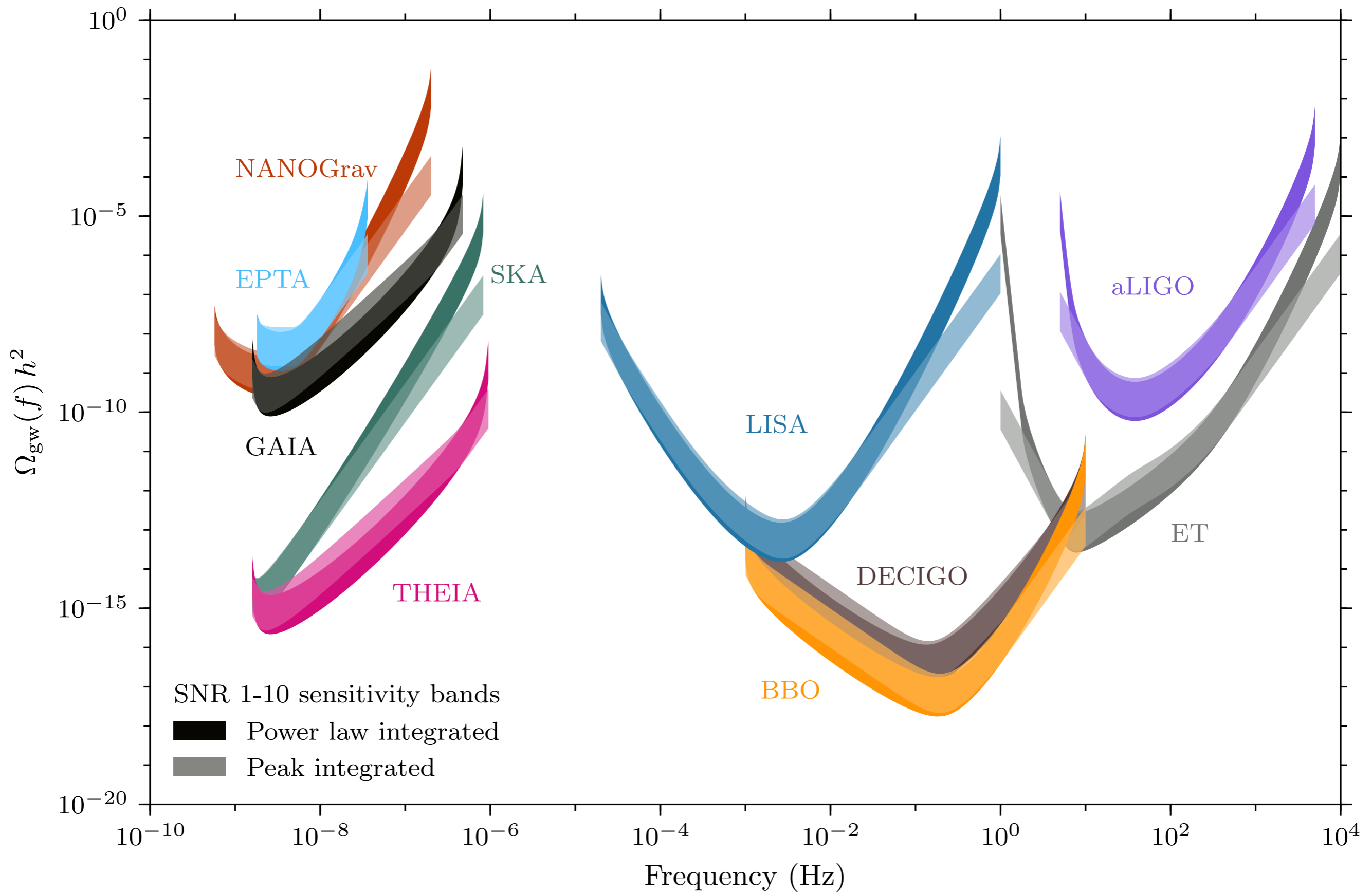


# Dark Spectroscopy





+Géraldine Servant

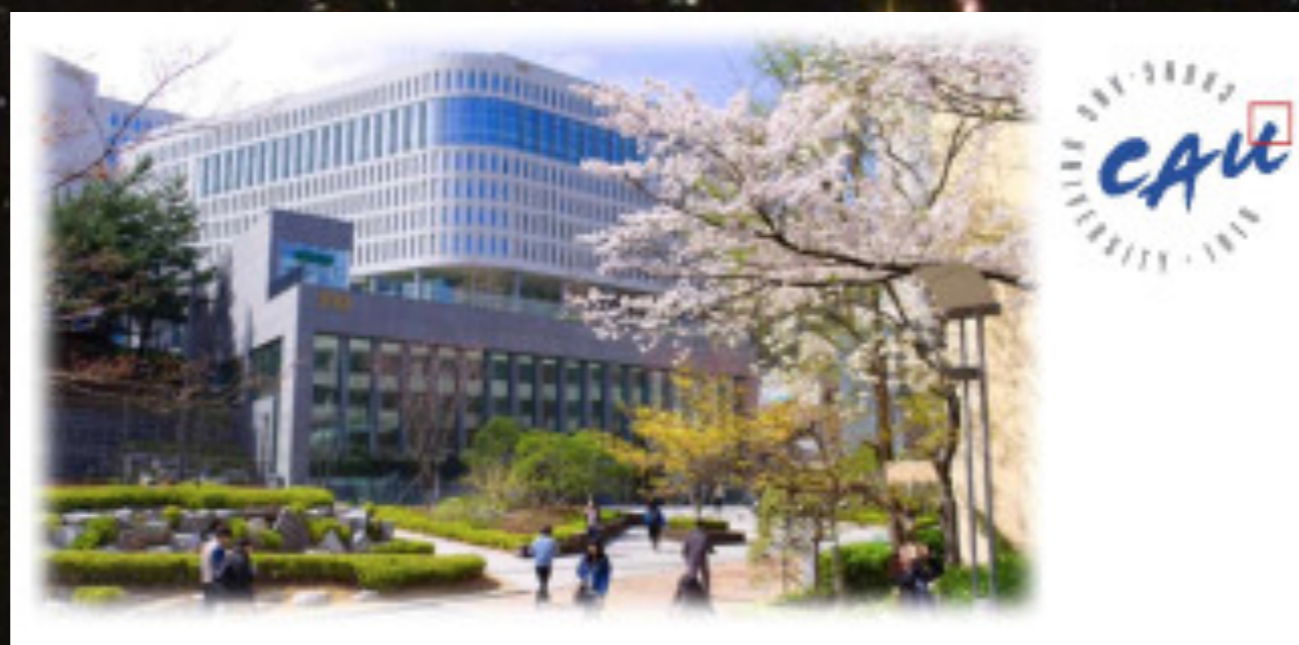


# New Methods for Dark Matter Discovery

- QCD is beautiful. Nature may use it again.
- dark matter, baryon asymmetry, hierarchy problem
- direct detection, beam dump, Mu2e, ILC
- **Dark spectroscopy!**
- **resonant self-interaction** in dwarf galaxies
- **rare Z and Higgs decays**
- gravitational wave



# Fun with Composite Dark Matter



Hitoshi Murayama (Berkeley, Kavli IPMU)  
2022 CAU BSM Workshop  
Feb 8, 2022