

# Correlated signals of first-order phase transition in dark sector

Po-Yan Tseng (*NTHU*)

Danny Marfatia (*U. of Hawaii*)

References:

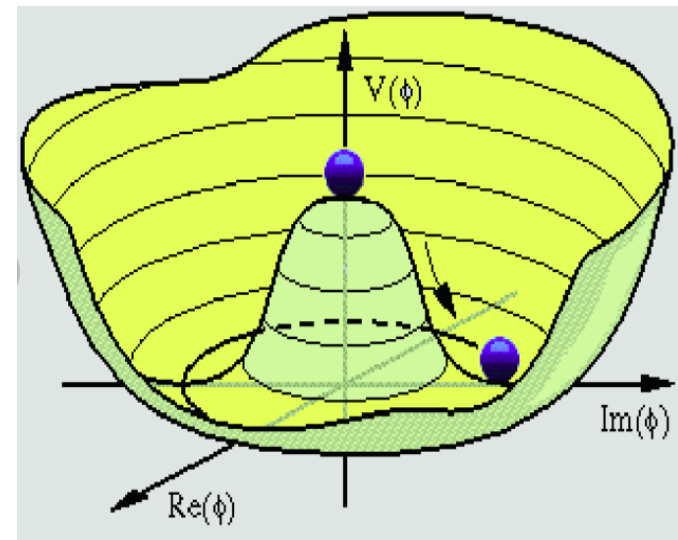
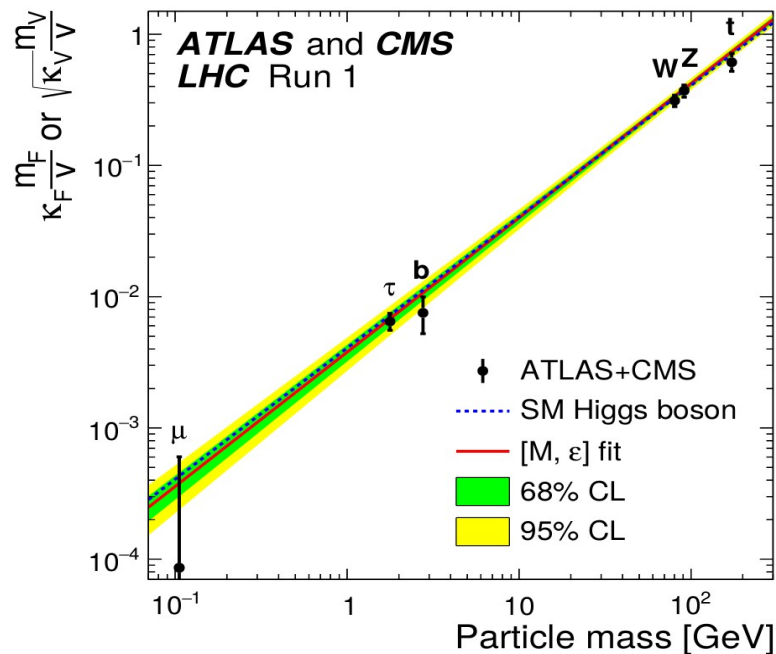
JHEP11(2021)068, arXiv:2107.00859, 2112.14588

**2022 CAU Beyond the Standard Model  
Workshop Feb. 7-10, 2022**



# Introduction

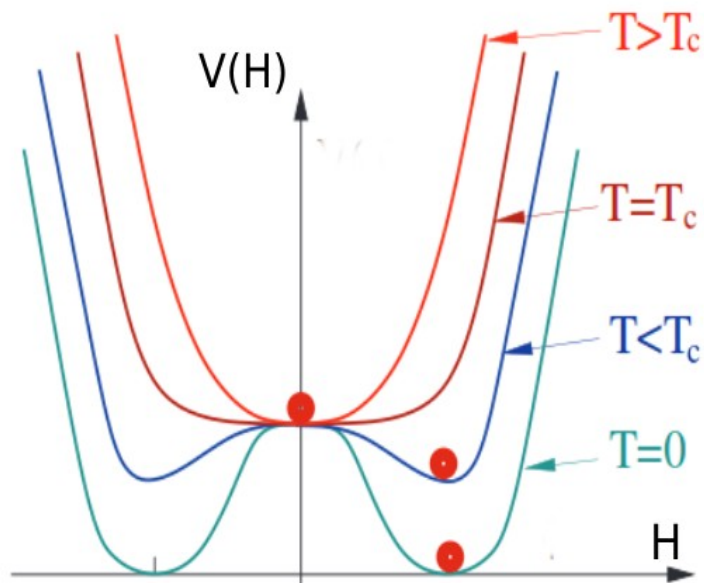
- 125 GeV Higgs gives the mass to the SM particles through **spontaneous symmetry breaking**.



Dezso Horvath: Higgs and BSM studies at the LHC

# Introduction

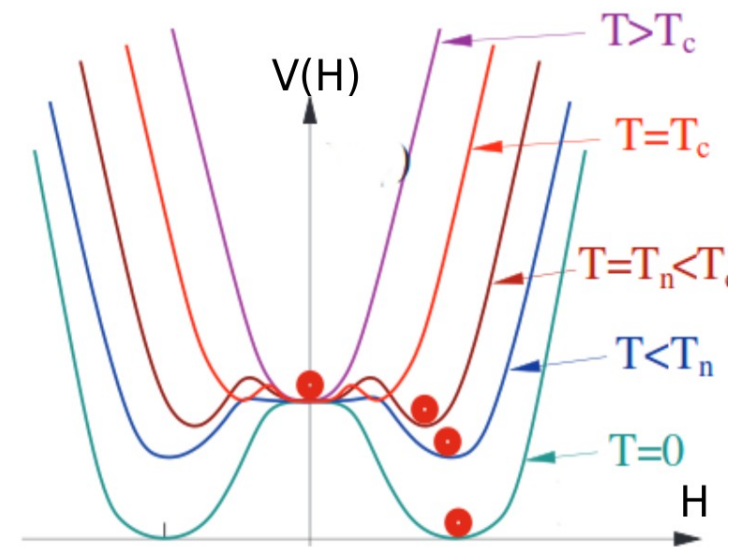
- Universe been through an **electroweak (QCD) phase transition** at  $T \sim 100 \text{ GeV}$  ( $100 \text{ MeV}$ )



Cross over

IN2P3

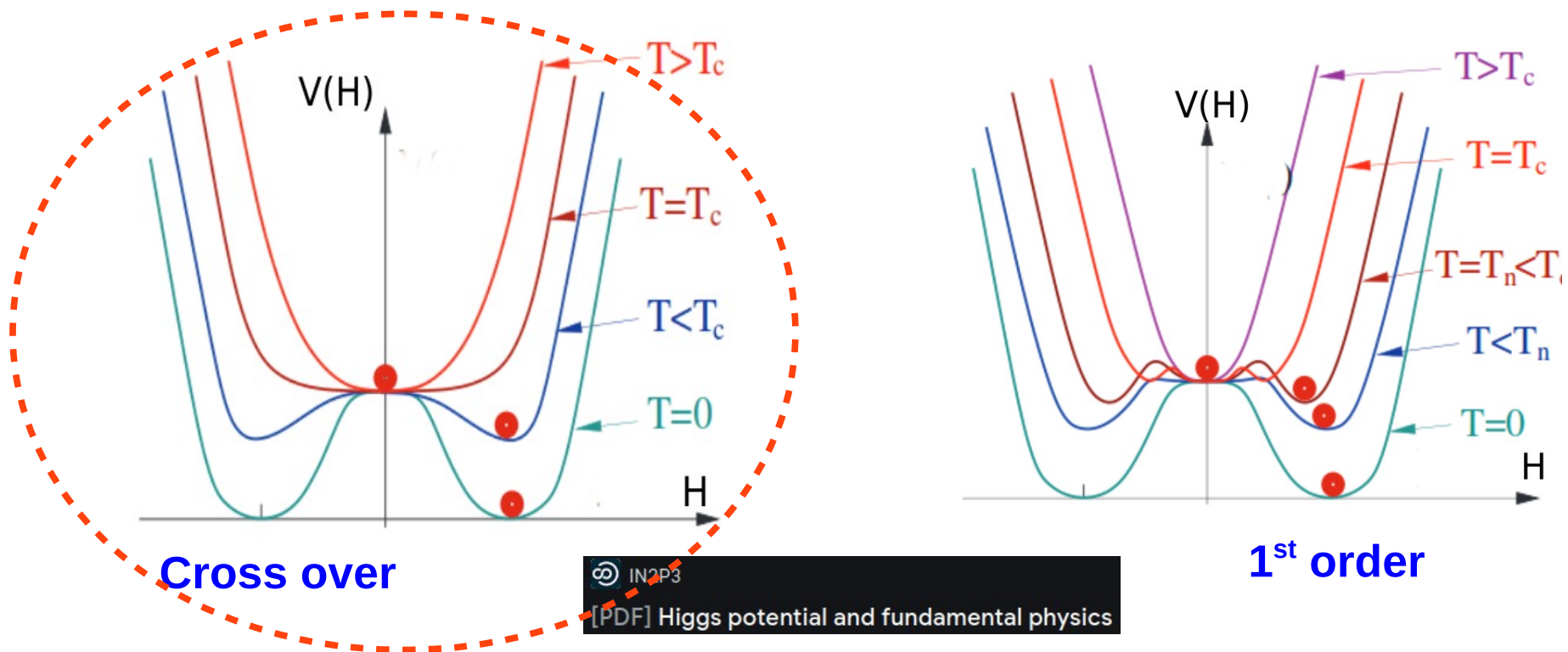
[PDF] Higgs potential and fundamental physics



1<sup>st</sup> order

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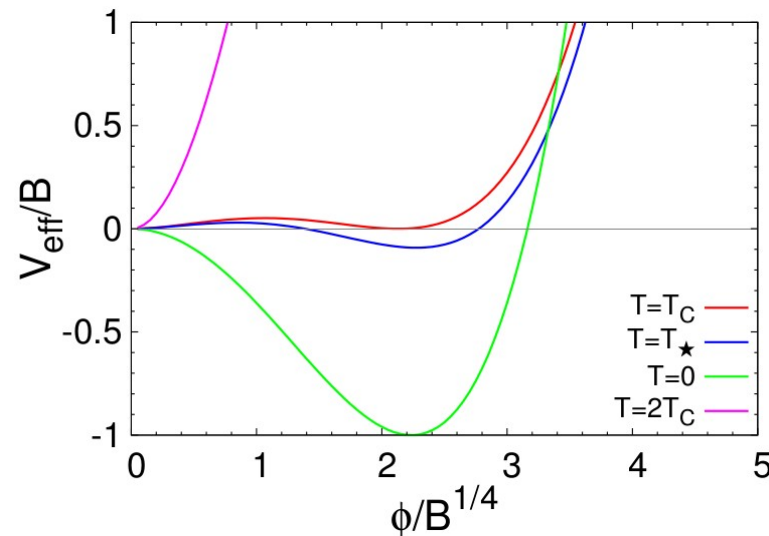
# Introduction

- The origin of DM mass may come from the **spontaneous symmetry breaking** inducing by another scalar.

$$\mathcal{L} \supset \bar{\chi} i \not{\partial} \chi - g_{\chi} \phi \bar{\chi} \chi - V_{\text{eff}}(\phi, T)$$

$$m_{\chi} \simeq g_{\chi} \langle \phi \rangle$$

- We consider **1<sup>st</sup> order phase transition (FOPT)**.

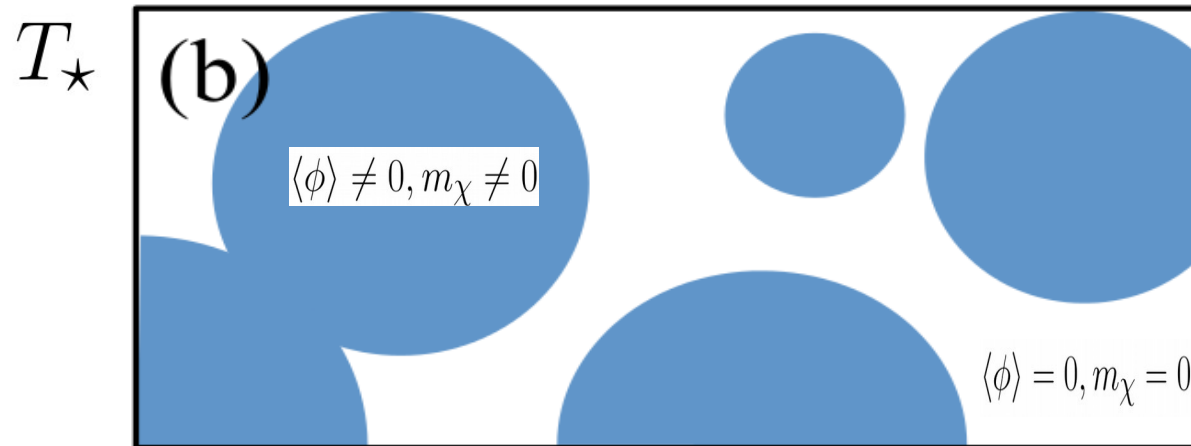


D.Marfatia, P.Y.Tseng

# Introduction

- More rich phenomenologies, if we consider **1<sup>st</sup> order phase transition (FOPT)**.

J.P.Hong, S.Jung, K.P.Xie: 2008.04430

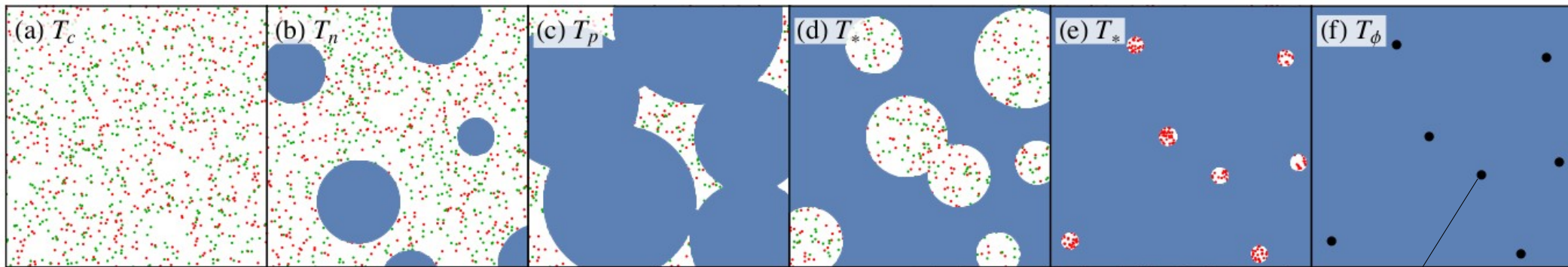


- DM particles **inside** the bubble becomes the DM relic density (bubble filtering DM: prof. C.S. Shin).
- DM particles **outside** the bubble could form macroscopic DM (Fermi Ball or primordial black hole)

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K.Kawana, K.P.Xie: 2106.00111

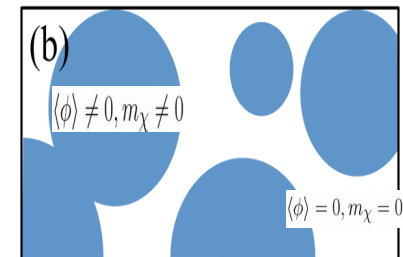
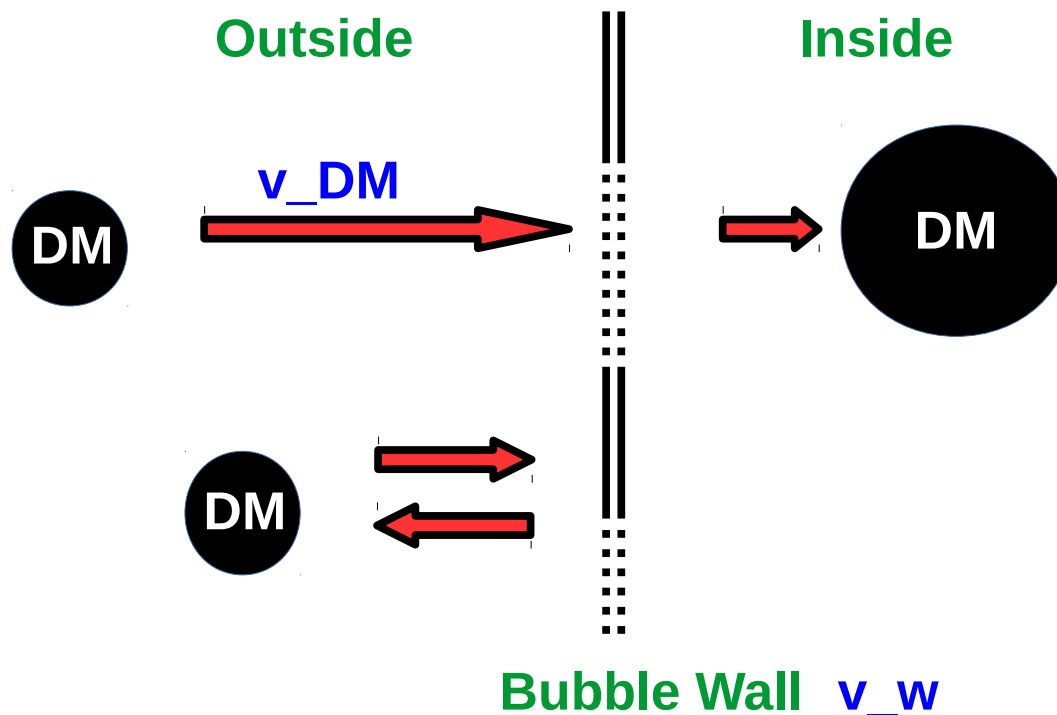


**FB, PBH**

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# Bubble filtering

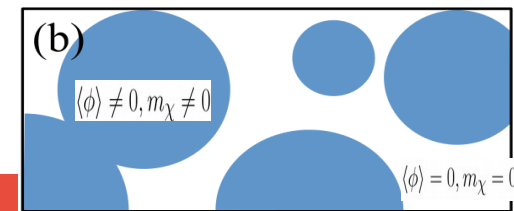
- During FOPT, massless (massive) DM particles locate outside (inside) the bubble, and **momentum conservation** must be satisfied at the bubble wall.





# Bubble filtering

- Suppose DM particle mass is very heavy:  $m_\chi \simeq g_\phi v_\phi \gg T_c$
- DM particles, remaining in **outside** the bubble (trapped in the *false vacuum*), will be aggregate by the expanding bubbles and form a macroscopic **Fermi-Ball(FB)**.
- For this to occur, there must be non-zero **asymmetry**  $\eta_\chi \equiv (n_\chi - n_{\bar{\chi}})/s$  in the false vacuum so that the an excess remain after pair annihilation.
- The  $\chi$  must carry a conserved global **U(1)\_Q** charge so that **FB** attains stability



# Number density of FB

- FBs start to form at  $T_*$  in the false vacuum, it shrinks and separates into smaller volumes.
- Critical volume  $V_* = 4\pi R_*^3/3$ , there is no other bubble forming inside during its shrinking  $\Gamma(T_*)V_*\Delta t \sim 1$ , corresponds to one FB.

- The number density of FB  $n_{\text{FB}}|_{T_*}$  is determined by

$$n_{\text{FB}}|_{T_*} V_* = F(t_*) :$$

$$n_{\text{FB}}|_{T_*} = \left(\frac{3}{4\pi}\right)^{1/4} \left(\frac{\Gamma(T_*)}{v_w}\right)^{3/4} F(t_*)$$

- The net Q-charge for a FB:  $Q_{\text{FB}} = \eta_\chi \left(\frac{s}{n_{\text{FB}}}\right)_{T_*}$

# FB mass profile

- The mass and radius of FB are obtained by minimizing the FB energy with respect to the radius  $dE_{\text{FB}}/dR = 0$  :

$$E_{\text{FB}} = \frac{3\pi}{4} \left(\frac{3}{2\pi}\right)^{2/3} \frac{Q_{\text{FB}}^{4/3}}{R} \left[ 1 + \frac{4\pi}{9} \left(\frac{2\pi}{3}\right)^{1/3} \frac{R^2 T^2}{Q_{\text{FB}}^{2/3}} \right] - \frac{3g_\chi^2}{8\pi} \frac{Q_{\text{FB}}^2 L_\phi^2}{R^3} + \frac{4\pi}{3} V_0(T) R^3$$

-----  
*Fermi gas kinetic energy*

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.....  
*Yukawa potential*

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*Temperature-dependent potential*

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$$R_{\text{FB}} = \left[ \frac{3}{16} \left(\frac{3}{2\pi}\right)^{2/3} \frac{Q_{\text{FB}}^{4/3}}{V_0} \right]^{1/4} \left[ 1 - \frac{\pi}{6\sqrt{3}} \frac{T^2}{V_0^{1/2}} \right]^{1/2},$$
$$M_{\text{FB}} = Q_{\text{FB}} (12\pi^2 V_0)^{1/4} \left( 1 + \frac{\pi}{4\sqrt{3}} \frac{T^2}{V_0^{1/2}} \right),$$

- FB relic abundance:  $\Omega_{\text{FB}} h^2 = \frac{M_{\text{FB}} n_{\text{FB}}|_{T_0}}{3M_{\text{Pl}}^2 (H_0/h)^2}$

# FB collapse to PBH

- The mass and radius of FB are obtained by minimizing the FB energy with respect to the radius  $dE_{\text{FB}}/dR = 0$  :

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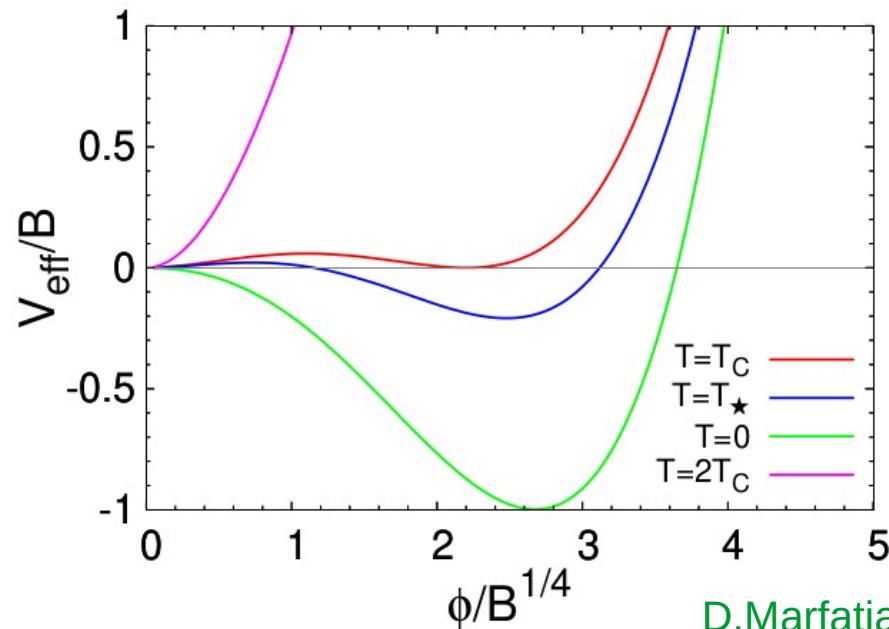
$$L_\phi(T) \equiv \left( \frac{d^2 V_{\text{eff}}}{d\phi^2} \Big|_{\phi=0} \right)^{-1/2} = (2D(T^2 - T_0^2))^{-1/2}$$

- If the FB temperature further cool down, attractive Yukawa potential dominate when  $L_\phi \simeq R_{\text{FB}}/Q_{\text{FB}}^{1/3}$  . FB starts collapsing to PBH.

# Quartic effective potential

- We consider the finite-temperature quartic effective potential induce the FOPT:

$$V_{\text{eff}}(\phi, T) = D(T^2 - T_0^2)\phi^2 - (AT + C)\phi^3 + \frac{\lambda}{4}\phi^4$$



D.Marfatia, P.Y. Tseng: 2107.00859





# Signals from FB



# Fermi ball

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D.Marfatia, P.Y. Tseng: 2107.00859

**Table 1.** Benchmark points with  $A = 0.1$ .  $N_{\text{events}}$  is the number of microlensing events expected in 70 hours of observation of M31 by Subaru-HSC.

	BP-1	BP-2	BP-3	BP-4	BP-5	BP-6	BP-7	BP-8
$\lambda$	0.134	0.158	0.193	0.078	0.062	0.072	0.053	0.060
$B^{1/4}/\text{keV}$	2.42	43.5	34.9	64.2	63.6	73.2	284	1390
$C/\text{keV}$	0.059	6.234	4.988	3.080	0.315	0.586	0.342	7.713
$D$	5.807	0.451	0.720	0.445	0.257	0.293	0.584	0.706
$\eta_\chi$	$7.34 \times 10^{-6}$	$1.37 \times 10^{-7}$	$3.51 \times 10^{-6}$	$4.55 \times 10^{-8}$	$6.98 \times 10^{-9}$	$3.64 \times 10^{-9}$	$8.54 \times 10^{-9}$	$2.40 \times 10^{-8}$
$T_{\text{SM}\star}/\text{keV}$	1.41	100.0	64.5	128.1	164.8	169.5	427.8	1601
$T_\star/\text{keV}$	0.57	34.2	21.6	52.3	84.8	86.9	201.0	879.0
$T_f/\text{keV}$	0.63	41.4	25.9	64.4	92.9	92.5	233.2	1005
$S_3(T_\star)/T_\star$	189	188	187	186	187	184	177	171
$M_{\text{FB}}/M_\odot$	$3.37 \times 10^{-6}$	$1.11 \times 10^{-6}$	$9.66 \times 10^{-6}$	$1.01 \times 10^{-7}$	$1.08 \times 10^{-8}$	$1.08 \times 10^{-9}$	$9.66 \times 10^{-11}$	$1.09 \times 10^{-11}$
$R_{\text{FB}}/R_\odot$	0.529	$7.77 \times 10^{-3}$	$2.15 \times 10^{-2}$	$2.09 \times 10^{-3}$	$1.00 \times 10^{-3}$	$3.86 \times 10^{-4}$	$2.83 \times 10^{-5}$	$1.64 \times 10^{-6}$
$Q_{\text{FB}}$	$4.70 \times 10^{56}$	$8.62 \times 10^{54}$	$9.38 \times 10^{55}$	$5.34 \times 10^{53}$	$5.74 \times 10^{52}$	$5.00 \times 10^{51}$	$1.15 \times 10^{50}$	$2.65 \times 10^{48}$
$\alpha$	$1.63 \times 10^{-2}$	$1.56 \times 10^{-2}$	$1.70 \times 10^{-2}$	$2.83 \times 10^{-2}$	$2.00 \times 10^{-2}$	$1.24 \times 10^{-2}$	$1.79 \times 10^{-2}$	$2.62 \times 10^{-2}$
$\beta/H_\star$	$3.43 \times 10^4$	$1.57 \times 10^3$	$3.01 \times 10^3$	$2.04 \times 10^3$	$1.86 \times 10^3$	$2.80 \times 10^3$	$4.44 \times 10^3$	$5.59 \times 10^3$
$v_\phi/T_\star$	3.554	4.175	3.958	4.889	3.987	3.501	4.724	4.469
$v_w$	0.890	0.940	0.937	0.946	0.886	0.854	0.923	0.916
$\Omega_{\text{FB}}h^2$	$1.79 \times 10^{-2}$	$5.81 \times 10^{-3}$	0.12	$2.94 \times 10^{-3}$	$4.56 \times 10^{-4}$	$2.70 \times 10^{-4}$	$2.39 \times 10^{-3}$	$3.38 \times 10^{-2}$
$N_{\text{events}}$	19.5	20.4	29.3	38.9	17.5	19.3	46.1	29.1
$\Delta N_{\text{eff}}$	0.391	0.226	0.248	0.394	0.497	0.425	0.261	0.408

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Input parameters from effective potential

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FB mass,  
radius and  
Q-charge

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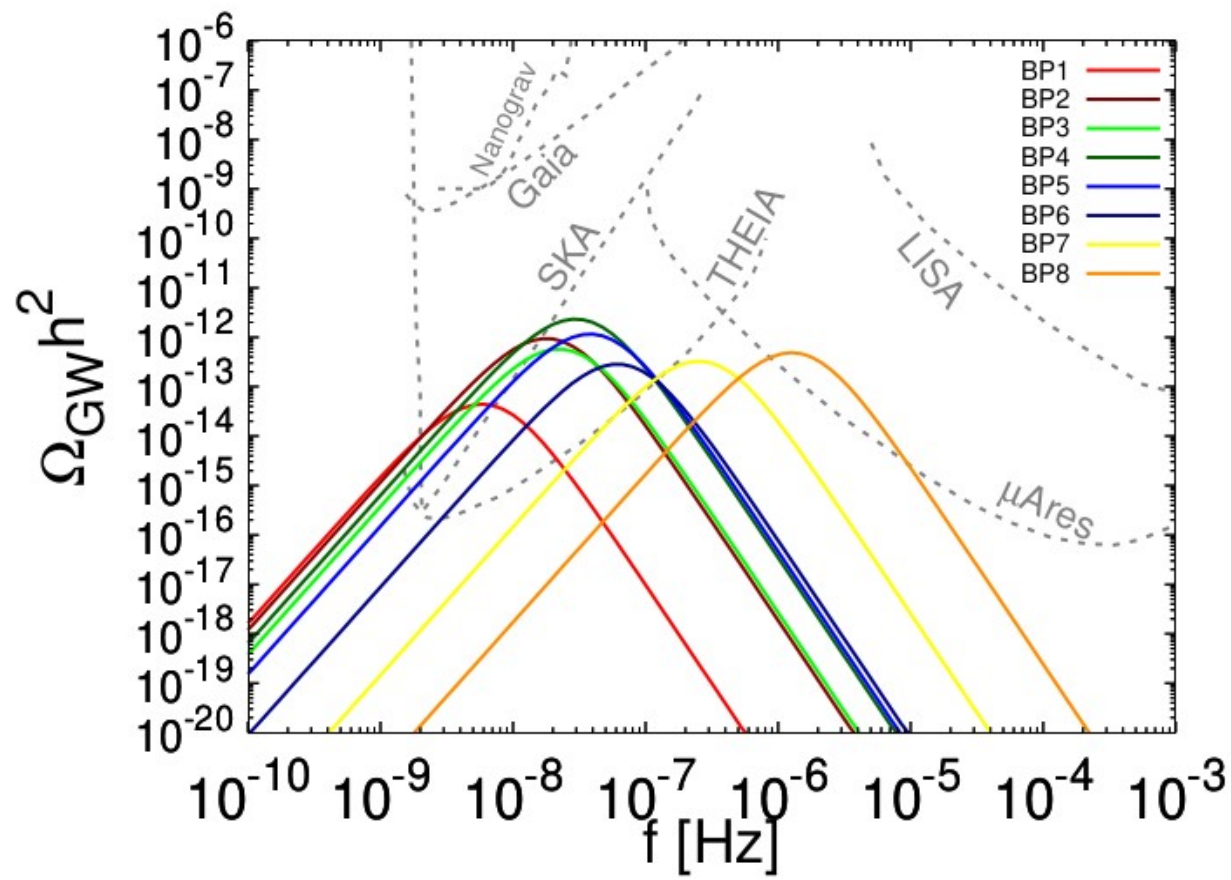
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$Q_{\text{FB}}$	$4.70 \times 10^{56}$	$8.62 \times 10^{54}$	$9.38 \times 10^{55}$	$5.34 \times 10^{53}$	$5.74 \times 10^{52}$	$5.00 \times 10^{51}$	$1.15 \times 10^{50}$	$2.65 \times 10^{48}$
$\alpha$	$1.63 \times 10^{-2}$	$1.56 \times 10^{-2}$	$1.70 \times 10^{-2}$	$2.83 \times 10^{-2}$	$2.00 \times 10^{-2}$	$1.24 \times 10^{-2}$	$1.79 \times 10^{-2}$	$2.62 \times 10^{-2}$
$\beta/H_\star$	$3.43 \times 10^4$	$1.57 \times 10^3$	$3.01 \times 10^3$	$2.04 \times 10^3$	$1.86 \times 10^3$	$2.80 \times 10^3$	$4.44 \times 10^3$	$5.59 \times 10^3$
$v_\phi/T_\star$	3.554	4.175	3.958	4.889	3.987	3.501	4.724	4.469
$v_w$	0.890	0.940	0.937	0.946	0.886	0.854	0.923	0.916
$\Omega_{\text{FB}}h^2$	$1.79 \times 10^{-2}$	$5.81 \times 10^{-3}$	0.12	$2.94 \times 10^{-3}$	$4.56 \times 10^{-4}$	$2.70 \times 10^{-4}$	$2.39 \times 10^{-3}$	$3.38 \times 10^{-2}$
$N_{\text{events}}$	19.5	20.4	29.3	38.9	17.5	19.3	46.1	29.1
$\Delta N_{\text{eff}}$	0.391	0.226	0.248	0.394	0.497	0.425	0.261	0.408

GW  
parameters

# Gravitational Wave

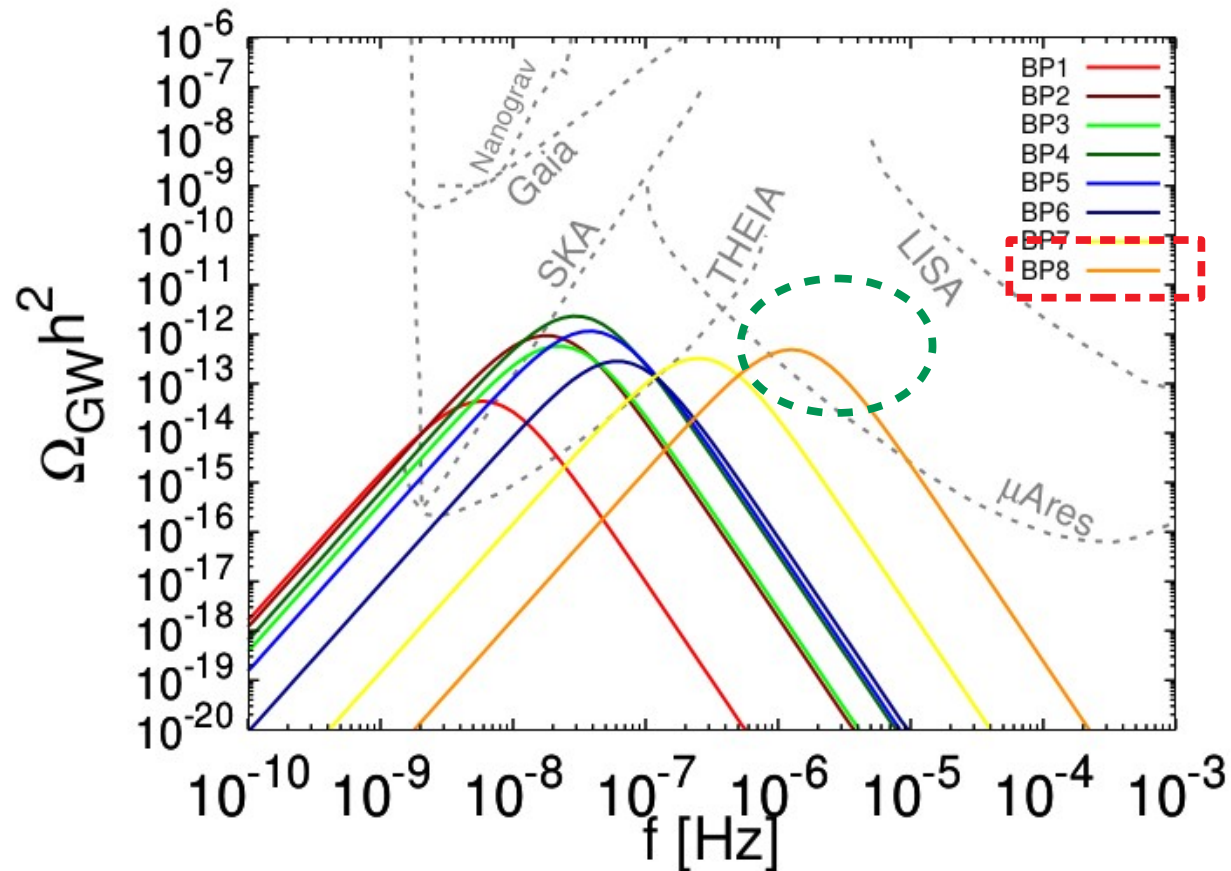
- GW spectra from the benchmark points:



D.Marfatia, P.Y. Tseng: 2107.00859

# Gravitational Wave

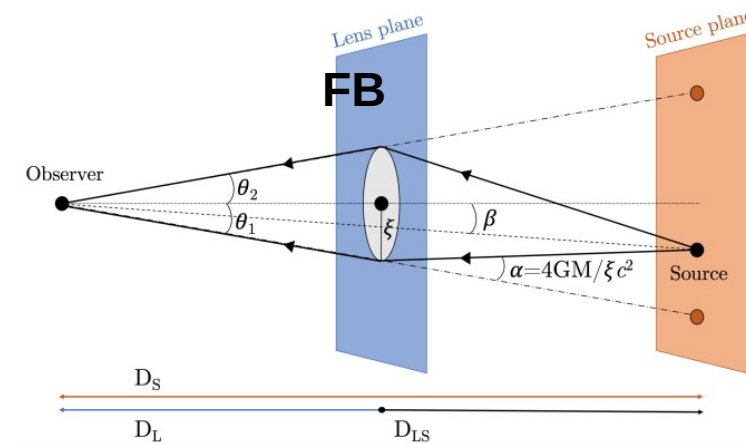
- GW spectra from the benchmark points:



D.Marfatia, P.Y. Tseng: 2107.00859

# Microlensing

- These FB mass and radius ranges can induce microlensing effects.



$$\theta_E \equiv \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_L D_S}}$$

$$\mu_{\text{tot}} = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

$\xrightarrow{u=1} 1.34$

D.Croon, D. McKeen, N. Raj: 2002.08962

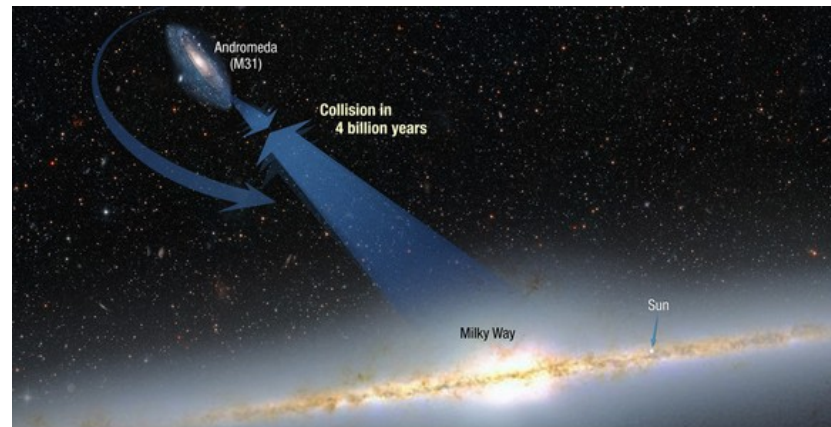
- The separating angle of two images of the background star are too small to be resolved, but we can observe the **sudden luminosity enhancement** of the star.



# Microlensing

- ◆ Astrophysical Sky surveys are ideal for observing microlensing. Ex. Subaru-HSC (observing M31).

FB halos surround MW and M31. FBs and stars have relative velocity of 250 km/s.

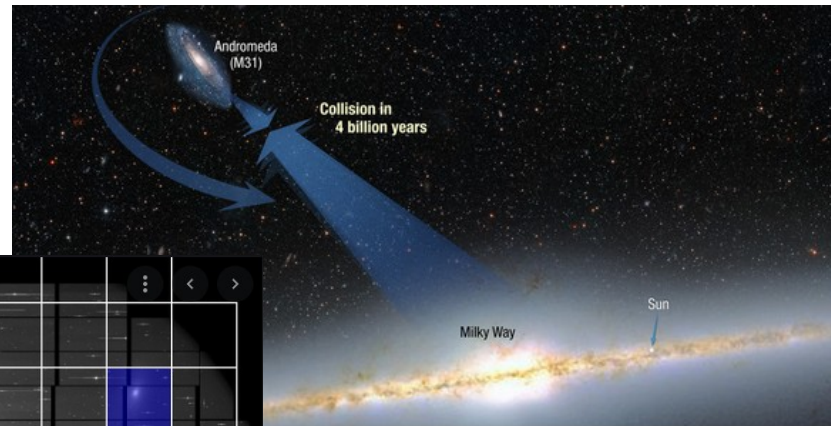


Milky Way Destined for Head-On Collision | NASA

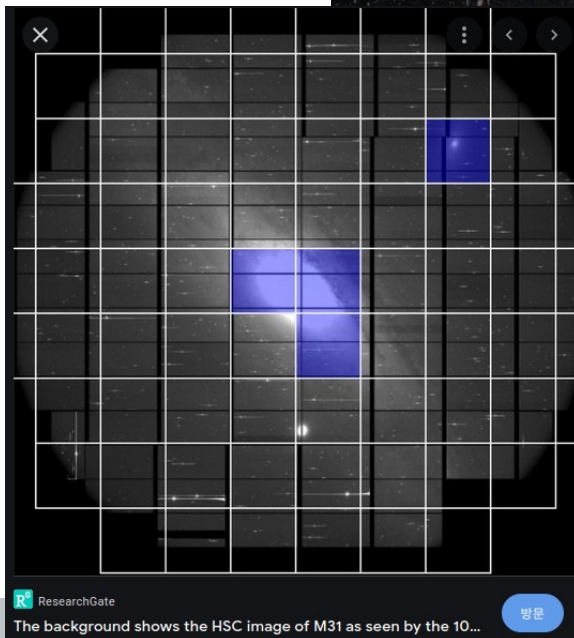
# Microlensing

- ◆ Astrophysical Sky surveys are ideal for observing microlensing. Ex. Subaru-HSC (observing M31 for 7 hrs).

FB halos surround MW and M31. FBs and stars have relative velocity of 250 km/s.



Milky Way Destined for Head-On Collision | NASA



M31 image from Subaru-HSC

# Microlensing

- If the lenses have a universal mass  $M_{\text{FB}}$ , with Maxwell-Boltzmann velocity distribution, then event rate per source star is

$$\frac{d^2\Gamma}{dxdt_E} = D_S \frac{f_{\text{DM}}}{M_{\text{FB}}} \left[ \rho_{\text{MW}}^{\text{DM}}(r_{\text{MW}}) \frac{v_E^4}{v_{\text{MW}}^2} e^{-v_E^2/v_{\text{MW}}^2} + \rho_{\text{M31}}^{\text{DM}}(r_{\text{M31}}) \frac{v_E^4}{v_{\text{M31}}^2} e^{-v_E^2/v_{\text{M31}}^2} \right]$$

$$v_E(x) = 2u_{1.34}(x)R_E(x)/t_E$$

- The  $t_E$  is the time duration for each event.

$$x \equiv D_L/D_S$$

# Microlensing

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$$\frac{d^2\Gamma}{dxdt_E} = D_S \frac{f_{\text{DM}}}{M_{\text{FB}}} \left[ \rho_{\text{MW}}^{\text{DM}}(r_{\text{MW}}) \frac{v_E^4}{v_{\text{MW}}^2} e^{-v_E^2/v_{\text{MW}}^2} + \rho_{\text{M31}}^{\text{DM}}(r_{\text{M31}}) \frac{v_E^4}{v_{\text{M31}}^2} e^{-v_E^2/v_{\text{M31}}^2} \right]$$

- Total event rate, we need to sum over the stars in M31

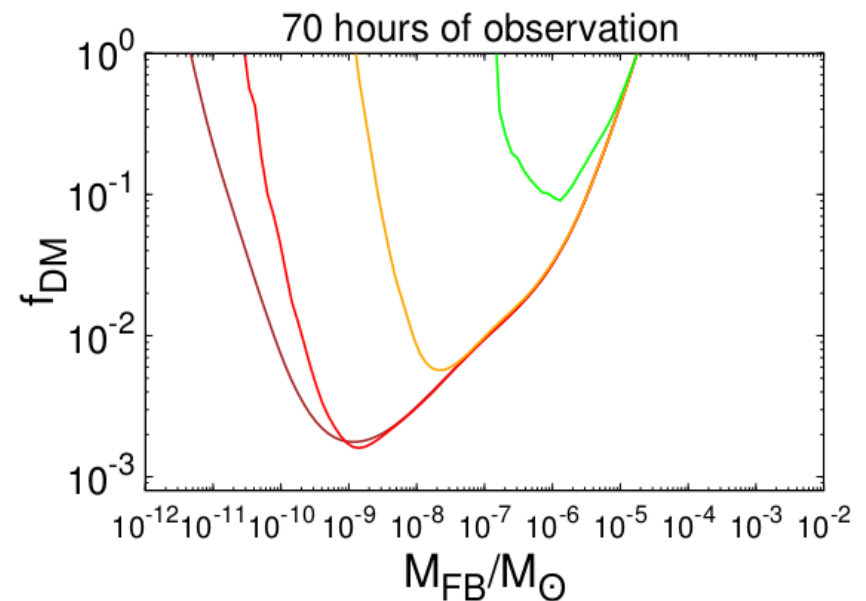
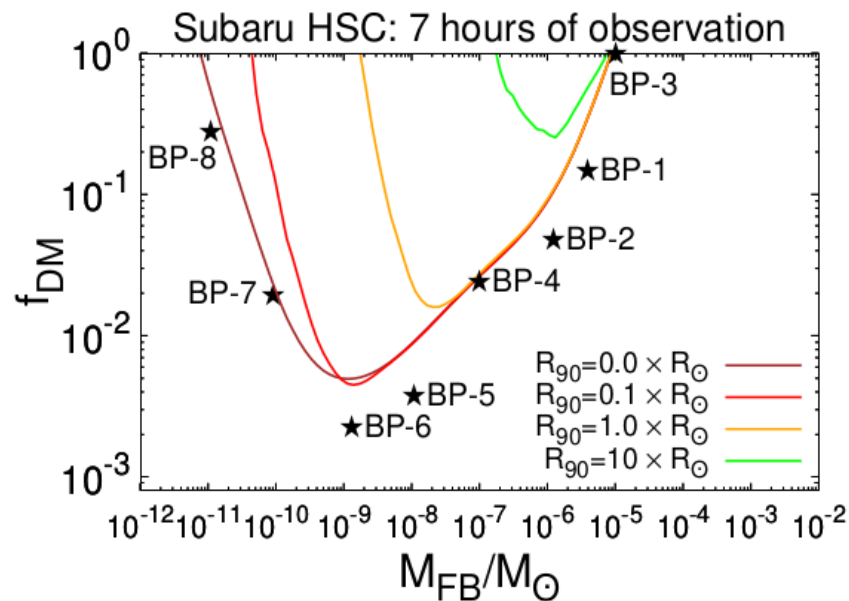
$$N_{\text{events}} = N_S T_{\text{obs}} \int dt_E \int dR_S \int_0^1 dx \frac{d^2\Gamma}{dxdt_E} \frac{dn}{dR_S}$$

$$N_S = 8.7 \times 10^7$$

$$T_{\text{obs}} = 7 \text{ hrs}$$

# Microlensing

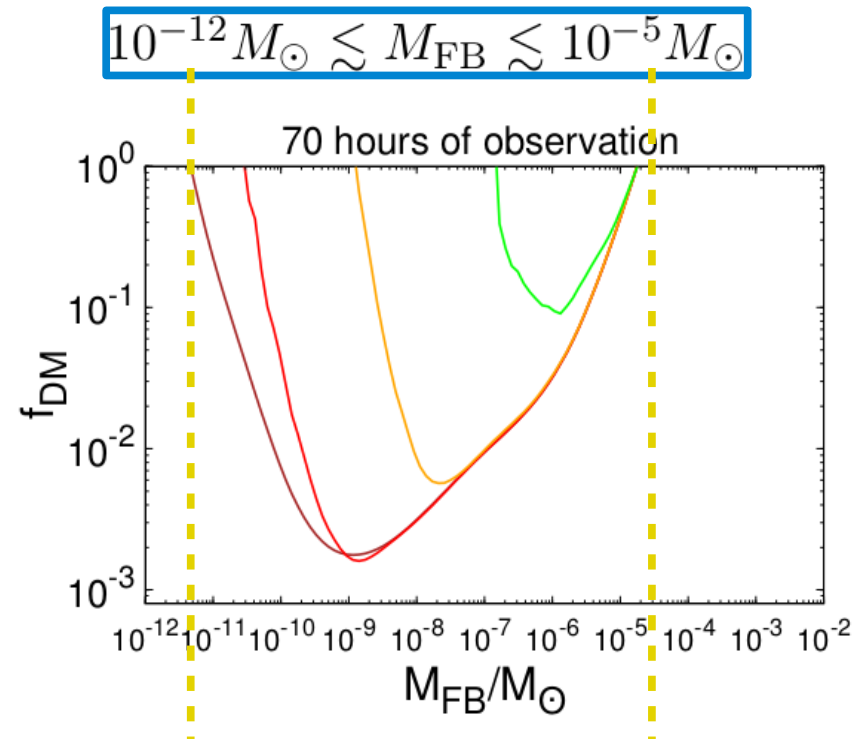
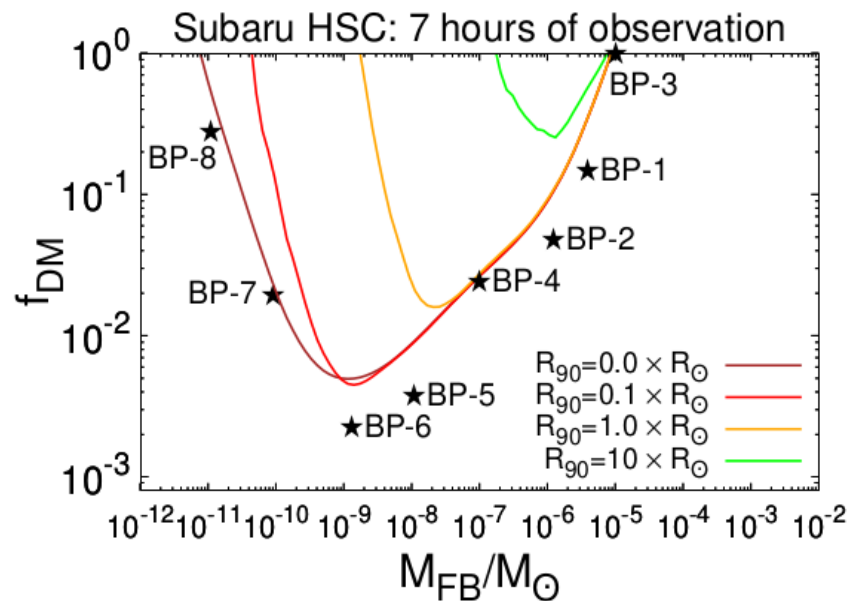
- The 95% CL on the fractional FB relic abundance  $f_{\text{DM}}$  requiring  $N_{\text{event}} \leq 4.74$  corresponds to one observed event at Subaru-HSC:



Here we included the finite size effect for microlensing.

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Here we included the finite size effect for microlensing.

# Relativistic degree of freedom

- The temperature of FOPT is lower than the BBN, and robust 95% CL upper limit is  $\Delta N_{\text{eff}} \lesssim 0.5$  . [2009.09745](#), [1103.1261](#)

**Table 1.** Benchmark points with  $A = 0.1$ .  $N_{\text{events}}$  is the number of microlensing events expected in 70 hours of observation of M31 by Subaru-HSC.

	BP-1	BP-2	BP-3	BP-4	BP-5	BP-6	BP-7	BP-8
$\lambda$	0.134	0.158	0.193	0.078	0.062	0.072	0.053	0.060
$B^{1/4}/\text{keV}$	2.42	43.5	34.9	64.2	63.6	73.2	284	1390
$C/\text{keV}$	0.059	6.234	4.988	3.080	0.315	0.586	0.342	7.713
$D$	5.807	0.451	0.720	0.445	0.257	0.293	0.584	0.706
$\eta_\chi$	$7.34 \times 10^{-6}$	$1.37 \times 10^{-7}$	$3.51 \times 10^{-6}$	$4.55 \times 10^{-8}$	$6.98 \times 10^{-9}$	$3.64 \times 10^{-9}$	$8.54 \times 10^{-9}$	$2.40 \times 10^{-8}$
$T_{\text{SM}\star}/\text{keV}$	1.41	100.0	64.5	128.1	164.8	169.5	427.8	1601
$T_\star/\text{keV}$	0.57	34.2	21.6	52.3	84.8	86.9	201.0	879.0
$T_f/\text{keV}$	0.63	41.4	25.9	64.4	92.9	92.5	233.2	1005
$S_3(T_\star)/T_\star$	189	188	187	186	187	184	177	171
$M_{\text{FB}}/M_\odot$	$3.37 \times 10^{-6}$	$1.11 \times 10^{-6}$	$9.66 \times 10^{-6}$	$1.01 \times 10^{-7}$	$1.08 \times 10^{-8}$	$1.08 \times 10^{-9}$	$9.66 \times 10^{-11}$	$1.09 \times 10^{-11}$
$R_{\text{FB}}/R_\odot$	0.529	$7.77 \times 10^{-3}$	$2.15 \times 10^{-2}$	$2.09 \times 10^{-3}$	$1.00 \times 10^{-3}$	$3.86 \times 10^{-4}$	$2.83 \times 10^{-5}$	$1.64 \times 10^{-6}$
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$\alpha$	$1.63 \times 10^{-2}$	$1.56 \times 10^{-2}$	$1.70 \times 10^{-2}$	$2.83 \times 10^{-2}$	$2.00 \times 10^{-2}$	$1.24 \times 10^{-2}$	$1.79 \times 10^{-2}$	$2.62 \times 10^{-2}$
$\beta/H_\star$	$3.43 \times 10^4$	$1.57 \times 10^3$	$3.01 \times 10^3$	$2.04 \times 10^3$	$1.86 \times 10^3$	$2.80 \times 10^3$	$4.44 \times 10^3$	$5.59 \times 10^3$
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Temperature  
of FOPT

# Relativistic degree of freedom

- The temperature of FOPT is lower than the BBN, and robust 95% CL upper limit is  $\Delta N_{\text{eff}} \lesssim 0.5$  . [2009.09754:1103.1261](#)

- We consider decoupled dark and SM sectors with temperature ratio  $r_T = \frac{T_i^{(D)}}{T^{(SM)}} \cdot$

- The extra effective neutrino number [Y.Nakai,M.Suzuki,F.Takahashi, M.Yamada: 2009.09754](#)

$$\Delta N_{\text{eff}} \simeq 0.49 \times \left( \frac{R}{0.13} \right)^{4/3} \left( \frac{g_{*0}^{(D)}}{g_{*0}} \right) \left( \frac{g_{*s0}}{g_{*s0}^{(D)}} \right)^{4/3}$$

$$g_{\star}^{(D)} = 2 * 2 * (7/8) + 1 = 4.5$$

- $R$  is the entropy ratio after the phase transition.



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$Q_{\text{FB}}$	$4.70 \times 10^{56}$	$8.62 \times 10^{54}$	$9.38 \times 10^{55}$	$5.34 \times 10^{53}$	$5.74 \times 10^{52}$	$5.00 \times 10^{51}$	$1.15 \times 10^{50}$	$2.65 \times 10^{48}$
$\alpha$	$1.63 \times 10^{-2}$	$1.56 \times 10^{-2}$	$1.70 \times 10^{-2}$	$2.83 \times 10^{-2}$	$2.00 \times 10^{-2}$	$1.24 \times 10^{-2}$	$1.79 \times 10^{-2}$	$2.62 \times 10^{-2}$
$\beta/H_\star$	$3.43 \times 10^4$	$1.57 \times 10^3$	$3.01 \times 10^3$	$2.04 \times 10^3$	$1.86 \times 10^3$	$2.80 \times 10^3$	$4.44 \times 10^3$	$5.59 \times 10^3$
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# Signals from PBH



# PBH: benchmark points

- Benchmark points for PBHs from FOPT.

D.Marfatia, P.Y. Tseng:2112.14588

	BP-1	BP-2	BP-3	BP-4	BP-5	BP-6
$\lambda$	0.097	0.177	0.084	0.198	0.198	0.077
$B^{1/4}/\text{MeV}$	37.89	16.55	3.412	1.843	0.286	2.411
$C/\text{MeV}$	0.551	1.329	0.054	0.260	0.047	0.022
$D$	1.257	0.138	0.413	0.750	0.794	0.286
$g_\chi$	0.031	0.020	0.187	0.240	0.118	0.164
$\eta_\chi$	$4.97 \times 10^{-9}$	$4.67 \times 10^{-11}$	$3.81 \times 10^{-13}$	$9.40 \times 10^{-16}$	$1.47 \times 10^{-18}$	$9.26 \times 10^{-17}$
$T_{\text{SM}\star}/\text{MeV}$	29.81	53.46	7.821	2.939	0.440	4.979
$T_\star/\text{MeV}$	18.72	36.89	3.156	1.126	0.157	2.908
$T_f/\text{MeV}$	19.73	37.13	3.338	1.343	0.214	3.071
$T_\phi/\text{MeV}$	17.72	21.64	2.737	0.800	0.077	2.361
$S_3(T_\star)/T_\star$	156	161	165	170	180	170
$M_{\text{PBH}}/M_\odot$	$3.18 \times 10^{-16}$	$1.08 \times 10^{-16}$	$1.07 \times 10^{-17}$	$1.07 \times 10^{-18}$	$3.91 \times 10^{-19}$	$3.99 \times 10^{-20}$
$Q_{\text{FB}}$	$5.02 \times 10^{42}$	$1.77 \times 10^{42}$	$1.14 \times 10^{42}$	$2.06 \times 10^{41}$	$4.48 \times 10^{41}$	$5.00 \times 10^{39}$
$\beta'$	$3.83 \times 10^{-17}$	$2.02 \times 10^{-19}$	$8.01 \times 10^{-23}$	$3.43 \times 10^{-26}$	$5.45 \times 10^{-30}$	$1.01 \times 10^{-27}$
$\alpha$	$1.26 \times 10^{-2}$	$1.72 \times 10^{-3}$	$2.78 \times 10^{-3}$	$9.23 \times 10^{-3}$	$1.81 \times 10^{-2}$	$1.14 \times 10^{-2}$
$\beta/H_\star$	$1.42 \times 10^4$	$2.55 \times 10^3$	$4.22 \times 10^3$	$2.86 \times 10^3$	$1.90 \times 10^3$	$2.74 \times 10^3$
$v_w$	0.840	0.694	0.845	0.935	0.968	0.843
$\Omega_{\text{PBH}}h^2$	0.108	$9.74 \times 10^{-4}$	$1.15 \times 10^{-6}$	$1.57 \times 10^{-9}$	$4.17 \times 10^{-13}$	$2.52 \times 10^{-10}$
$\Delta N_{\text{eff}}$	0.413	0.406	0.087	0.114	0.165	0.379

# PBH: benchmark points

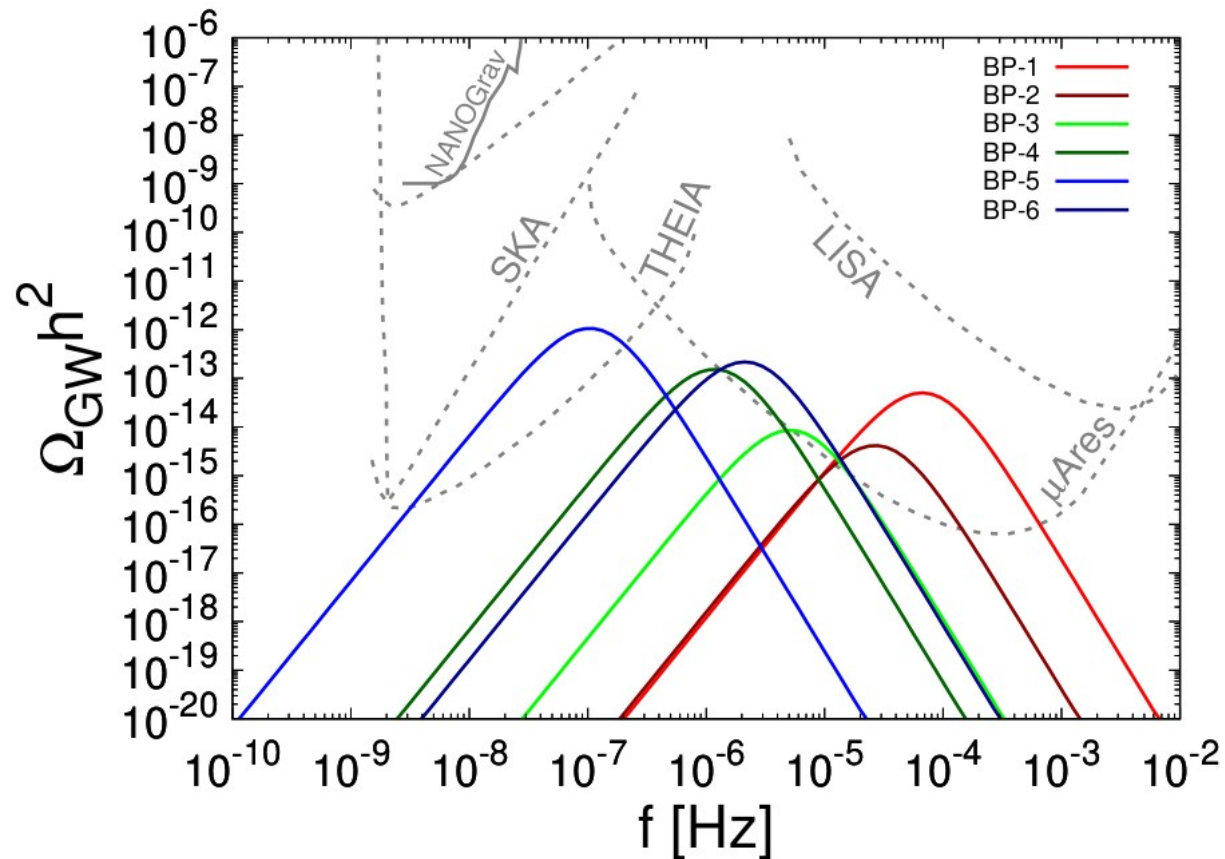
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D.Marfatia, P.Y. Tseng:2112.14588

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$C/\text{MeV}$	0.551	1.329	0.054	0.260	0.047	0.022
$D$	1.257	0.138	0.413	0.750	0.794	0.286
$g_\chi$	0.031	0.020	0.187	0.240	0.118	0.164
$\eta_\chi$	$4.97 \times 10^{-9}$	$4.67 \times 10^{-11}$	$3.81 \times 10^{-13}$	$9.40 \times 10^{-16}$	$1.47 \times 10^{-18}$	$9.26 \times 10^{-17}$
$T_{\text{SM}\star}/\text{MeV}$	29.81	53.46	7.821	2.939	0.440	4.979
$T_\star/\text{MeV}$	18.72	36.89	3.156	1.126	0.157	2.908
$T_f/\text{MeV}$	19.73	37.13	3.338	1.343	0.214	3.071
$T_\phi/\text{MeV}$	17.72	21.64	2.737	0.800	0.077	2.361
$S_3(T_\star)/T_\star$	156	161	165	170	180	170
$M_{\text{PBH}}/M_\odot$	$3.18 \times 10^{-16}$	$1.08 \times 10^{-16}$	$1.07 \times 10^{-17}$	$1.07 \times 10^{-18}$	$3.91 \times 10^{-19}$	$3.99 \times 10^{-20}$
$Q_{\text{FB}}$	$5.02 \times 10^{42}$	$1.77 \times 10^{42}$	$1.14 \times 10^{42}$	$2.06 \times 10^{41}$	$4.48 \times 10^{41}$	$5.00 \times 10^{39}$
$\beta'$	$3.83 \times 10^{-17}$	$2.02 \times 10^{-19}$	$8.01 \times 10^{-23}$	$3.43 \times 10^{-26}$	$5.45 \times 10^{-30}$	$1.01 \times 10^{-27}$
$\alpha$	$1.26 \times 10^{-2}$	$1.72 \times 10^{-3}$	$2.78 \times 10^{-3}$	$9.23 \times 10^{-3}$	$1.81 \times 10^{-2}$	$1.14 \times 10^{-2}$
$\beta/H_\star$	$1.42 \times 10^4$	$2.55 \times 10^3$	$4.22 \times 10^3$	$2.86 \times 10^3$	$1.90 \times 10^3$	$2.74 \times 10^3$
$v_w$	0.840	0.694	0.845	0.935	0.968	0.843
$\Omega_{\text{PBH}}h^2$	0.108	$9.74 \times 10^{-4}$	$1.15 \times 10^{-6}$	$1.57 \times 10^{-9}$	$4.17 \times 10^{-13}$	$2.52 \times 10^{-10}$
$\Delta N_{\text{eff}}$	0.413	0.406	0.087	0.114	0.165	0.379

# Gravitational Wave

- GW spectra from the benchmark points:



D.Marfatia, P.Y. Tseng: 2112.14588

# PBH evaporation

- The evaporation of a PBH produces all particles with mass below the PBH temperature:

$$T_{\text{PBH}} \simeq 5.3 \text{ MeV} \times \left( \frac{10^{-18} M_{\odot}}{M_{\text{PBH}}} \right)$$

- For  $M_{\text{PBH}}/M_{\odot} \lesssim 10^{-20}$ , PBHs evaporated before today.
- The Hawking emission rate of primary particles:

$$\frac{dN_i}{dE dt} = \frac{n_i^{\text{d.o.f}} \Gamma_i(E, M_{\text{PBH}})}{2\pi(e^{E/T_{\text{PBH}}} \pm 1)}$$

# PBH evaporation

- The extragalactic gamma-ray background due to PBH evaporation

$$\frac{d^2\Phi}{dEdt} = \int_{t_{\text{CMB}}}^{\min(t_{\text{eva}}, t_0)} c[1 + z(t)] \frac{f_{\text{PBH}} \rho_{\text{DM}}}{M_{\text{PBH}}} \left. \frac{d^2 N_\gamma}{d\tilde{E} dt} \right|_{\tilde{E}=[1+z(t)]E} dt$$

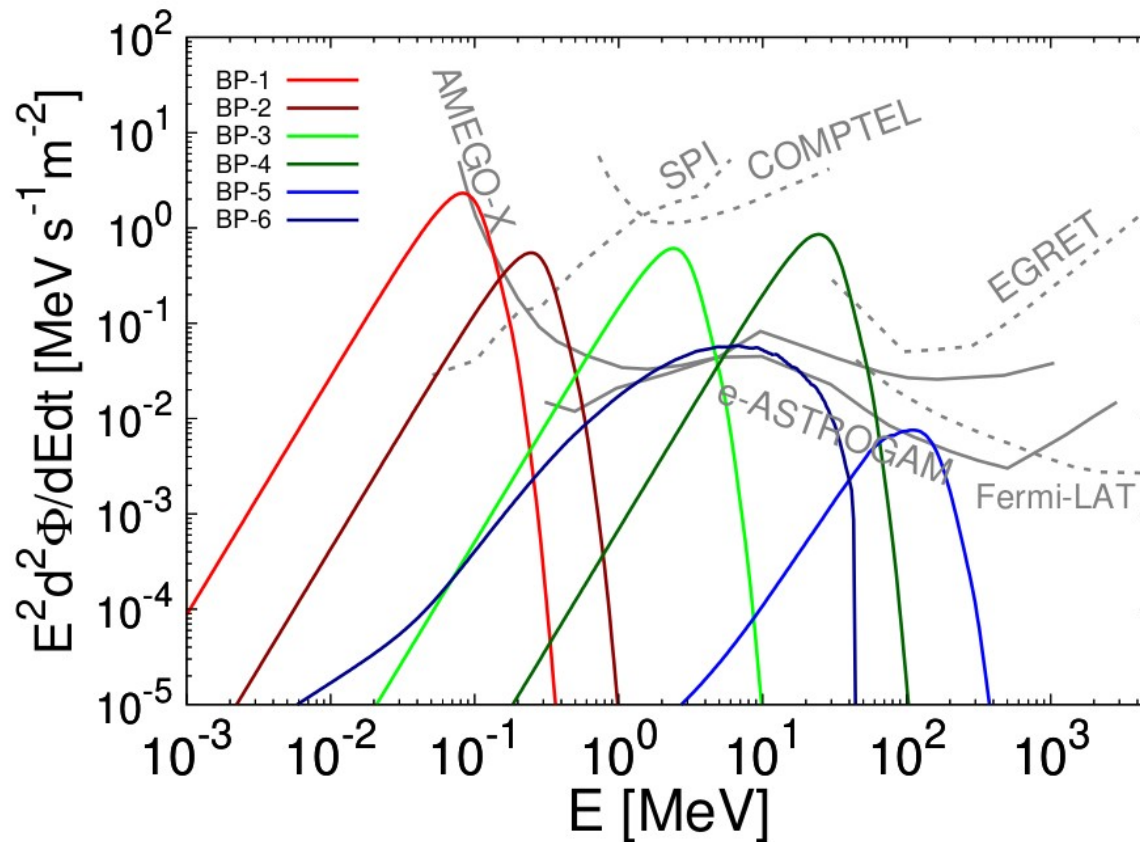
with average DM density  $\rho_{\text{DM}} = 1.27 \text{ GeV m}^{-3}$ .

- The evolution of the Universe is approximated as matter dominated until the current epoch

$$1 + z(t) = \left( \frac{t_0}{t} \right)^{2/3}$$

# PBH evaporation

- The extragalactic gamma-ray background due to PBH evaporation for the benchmark points







# Summary



# Summary

- ◆ We discuss two scenarios of fermion DM particles undergo FOPT by a **quartic effective potential**.
- ◆ FOPT endows DM mass and induces stochastic background **GW signals**.
- ◆ Fermion DM particles aggregate to form Fermi Ball via FOPT.
- ◆ FB of mass  $10^{-12}M_{\odot} \lesssim M_{\text{FB}} \lesssim 10^{-5}M_{\odot}$ , correlated observations of **GW** ( $10^{-9} \text{ Hz} - 10^{-5} \text{ Hz}$ ) from FOPT (*at SKA/THEIA*) and **microlensing** (*at Subaru-HSC*), can be made.

# Summary

- Via the attractive Yukawa potential, FB collapse to PBH.
- In the quartic effective potential framework with vacuum energy difference  $0.1 \lesssim B^{1/4}/\text{MeV} \lesssim 10^4$ , it produces PBHs of mass  $10^{-20} M_{\odot} \lesssim M_{\text{PBH}} \lesssim 10^{-15} M_{\odot}$ .
- The correlated observations of **GW** ( $10^{-7}$  Hz –  $10^{-4}$  Hz) from FOPT (at *THEIA*, *muAres*) and **extragalactic MeV gamma-ray** (at *AMEGO-X*, *e-ASTROGAM*), can be made.



**Thank you for your attention!**



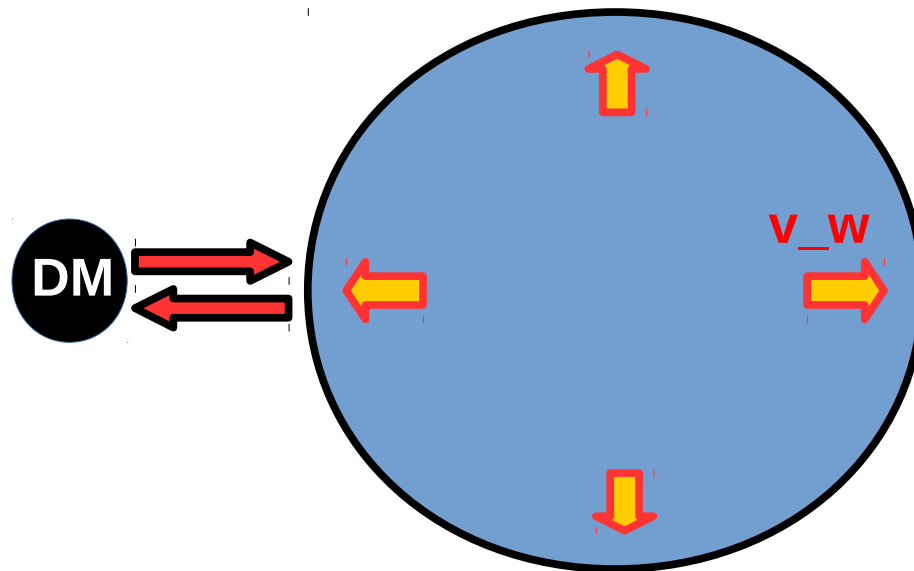


**Back up**



# Part-1: Bubble wall velocity

- ◆ Particles reflected by the bubble wall exert pressure on it, and slow down the bubble wall velocity.



# Part-1: Bubble filtering

- If a thermal DM flux is incident on the wall, the number density of DM that enter the bubble is:

$$n_{\chi}^{\text{in}} = n_{\bar{\chi}}^{\text{in}} \simeq \frac{g_{\text{DM}} T_{\star}^3}{\gamma_w v_w} \left( \frac{\gamma_w (1 - v_w) m_{\chi} / T_{\star} + 1}{4\pi^2 \gamma_w^3 (1 - v_w)^2} \right) e^{-\frac{\gamma_w (1 - v_w) m_{\chi}}{T_{\star}}}$$

D.Chway, T.H.Jung, C.S.Shin: 1912.04238

- DMs are filtered by the non-relativistic and relativistic bubble wall velocity:

$$n_{\chi}^{\text{in}} = \begin{cases} \sim e^{-m_{\chi}/T_{\star}} & \text{for } v_w \rightarrow 0 \\ \sim e^{-m_{\chi}/(2\gamma_w T_{\star})} & \text{for } m_{\chi}/(\gamma_w T_{\star}) \rightarrow 0 \end{cases}$$

# Part-1: Bubble filtering

- If  $T_\star < T_{\text{dec}}$ , the DM inside the bubble is decoupled from the thermal bath and become DM relic abundance.
- DM relic abundance today can be calculated by dividing  $n_\chi^{\text{in}} + n_{\bar{\chi}}^{\text{in}}$  by entropy  $s = (2\pi^2/45)g_\star S T^3$ :

$$\Omega_{\text{DM}} h^2 \simeq 6.29 \times 10^8 \frac{m_\chi (n_\chi^{\text{in}} + n_{\bar{\chi}}^{\text{in}})}{\text{GeV}} \frac{1}{g_\star S T_\star^3}$$

$$\Omega_{\text{DM}} h^2 \simeq \begin{cases} 1.27 \times 10^8 \left(\frac{m_\chi}{\text{GeV}}\right) \left(\frac{g_{\text{DM}}}{g_\star S}\right) \left(\frac{m_\chi}{2\gamma_w T_\star} + 1\right) e^{-\frac{m_\chi}{2\gamma_w T_\star}}, & \text{for } v_w \rightarrow 1 \\ 3.19 \times 10^7 \left(\frac{m_\chi}{\text{GeV}}\right) \left(\frac{g_{\text{DM}}}{g_\star S}\right) \left(\frac{1}{v_w}\right) \left(\frac{m_\chi}{T_\star} + 1\right) e^{-\frac{m_\chi}{T_\star}}, & \text{for } v_w \rightarrow 0. \end{cases}$$



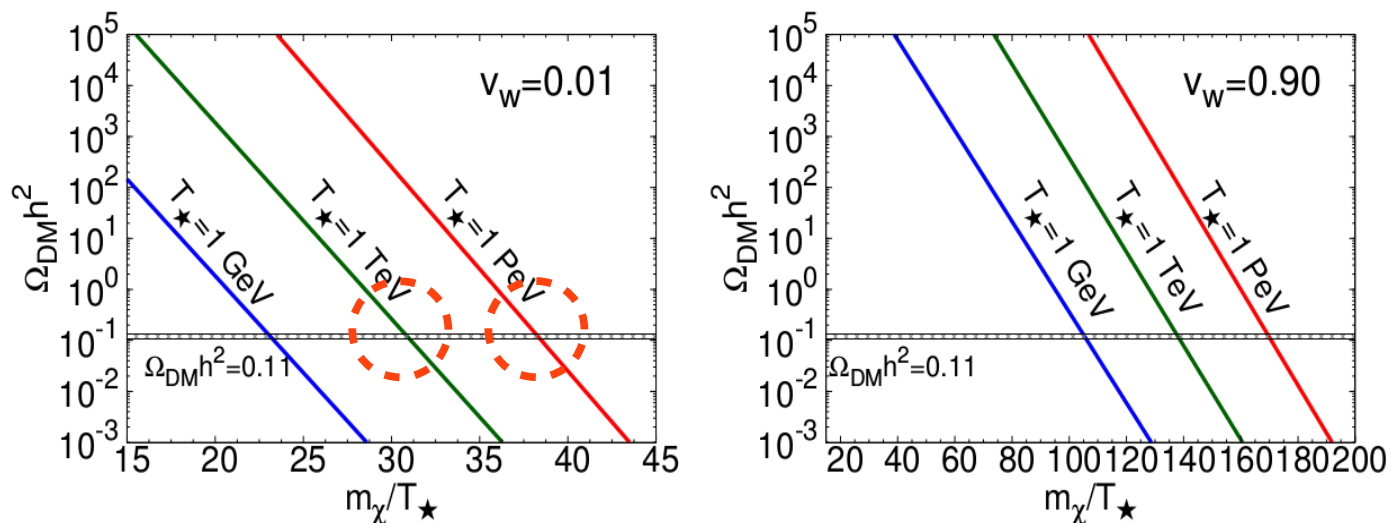
# Part-1: Bubble filtering

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- DM relic abundance today can be calculated by dividing  $n_\chi^{\text{in}} + n_{\bar{\chi}}^{\text{in}}$  by entropy  $s = (2\pi^2/45)g_\star S T^3$ :
- For example:  $m_\chi \simeq 1 \text{ TeV}, v_w \rightarrow 1$  requires

$$\frac{m_\chi}{2\gamma_w T_\star} \simeq 27$$

# Part-1: Bubble filtering

- If  $T_\star < T_{\text{dec}}$ , the DM inside the bubble is decoupled from the thermal bath and become DM relic abundance.
- DM relic abundance today can be calculated by dividing  $n_\chi^{\text{in}} + n_{\bar{\chi}}^{\text{in}}$  by entropy  $s = (2\pi^2/45)g_\star S T^3$  :



# Part-1: Bubble filtering

- ◆ Sudden DM freeze-out induced by a FOPT can easily accommodate DM mass above a PeV, which is beyond the current DM direct detection and LHC searches.
- ◆ We focus on the Gravitational Wave (GW) signals of Sudden DM freeze-out with a FOPT.

# Part-1: Gravitational wave production

- A FOPT generates GWs from three processes: I). **Bubble collisions**, II). **Sound wave** in the plasma, III) **Magnetohydrodynamic (MHD) turbulence**.
- The relevant parameters are required to calculate the GW signals:

$$\left\{ \begin{array}{l} T_{\star}, \\ \alpha \equiv \frac{\left(1 - T \frac{\partial}{\partial T}\right) \Delta V_{\text{eff}}|_{T_{\star}}}{\rho(T_{\star})}, \quad \rho \equiv \pi^2 g_{\star} T^4 / 30 \\ \frac{\beta}{H_{\star}} \simeq T_{\star} \frac{d(S_3/T)}{dT} \Big|_{T_{\star}} \\ v_w \end{array} \right.$$

# Part-1: Gravitational wave production

- ◆ A FOPT generates GWs from three processes: I). **Bubble collisions**, II). **Sound wave** in the plasma, III) **Magnetohydrodynamic (MHD) turbulence**.

- ◆ The Euclidean action:

$$S_3(T) = 4\pi \int_0^\infty r^2 dr \left[ \frac{1}{2} \left( \frac{d\phi}{dr} \right)^2 + V_{\text{eff}}(\phi, T) \right]$$

- ◆ Bubble nucleation rate per unit volume:

$$\Gamma(T) = T^4 \left( \frac{S_3}{2\pi T} \right)^{3/2} e^{-\frac{S_3}{T}}$$

# Part-1: Gravitational wave production

- A FOPT generates GWs from three processes: I). **Bubble collisions**, II). **Sound wave** in the plasma, III) **Magnetohydrodynamic (MHD) turbulence**.
- The fraction of space in the false vacuum:

$$F(t) = \exp \left[ -\frac{4\pi}{3} v_w^3 \int_{t_c}^t dt' (t - t')^3 \Gamma(t') \right]$$

- The percolation temperature  $T_\star$  of FOPT is determined by :

$$F(t_\star) = 1/e \simeq 0.37$$

# Part-1: Gravitational wave production

- A FOPT generates GWs from: I). **Bubble collisions**

$$h^2 \Omega_{\text{env}}(f) = 1.67 \times 10^{-5} \left( \frac{H_*}{\beta} \right)^2 \left( \frac{\kappa \alpha}{1 + \alpha} \right)^2 \left( \frac{100}{g_*} \right)^{\frac{1}{3}} \left( \frac{0.11 v_w^3}{0.42 + v_w^2} \right) S_{\text{env}}(f)$$

C.Caprini et. al: 1512.06239

$$S_{\text{env}}(f) = \frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}}$$

- The peak frequency is determined by the time scale of FOPT  $1/\beta$ :

$$\frac{f_*}{\beta} = \left( \frac{0.62}{1.8 - 0.1 v_w + v_w^2} \right)$$

# Part-1: Gravitational wave production

- A FOPT generates GWs from: I). **Bubble collisions**

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C.Caprini et. al: 1512.06239

$$S_{\text{env}}(f) = \frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}}$$

- The peak frequency is determined by the time scale of FOPT. Then red-shift to present epoch

$$f_{\text{env}} = 16.5 \times 10^{-3} \text{ mHz} \left( \frac{f_*}{\beta} \right) \left( \frac{\beta}{H_*} \right) \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{\frac{1}{6}}$$



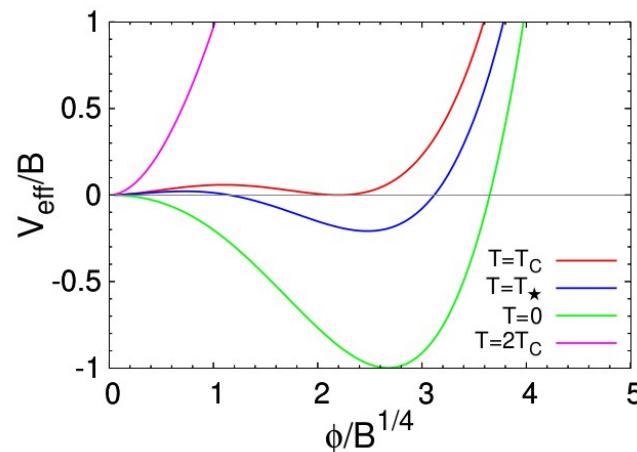
# Part-1: Scalar quartic Model

- ◆ The finite-temperature quartic effective scalar potential is:

$$V_{\text{eff}}(\eta, T) = \frac{\mu^2 + DT^2}{2}\eta^2 - \xi T\eta^3 + \frac{\lambda}{4}\eta^4$$

F.C.Adams: [hep-ph/9302321](https://arxiv.org/abs/hep-ph/9302321)

- ◆ Including one-loop Coleman-Weinberg and finite-temperature contributions, potentials of this form are commonly found in *inert singlet*, *inert doublet*, *MSSM*, and *Majoron models*.



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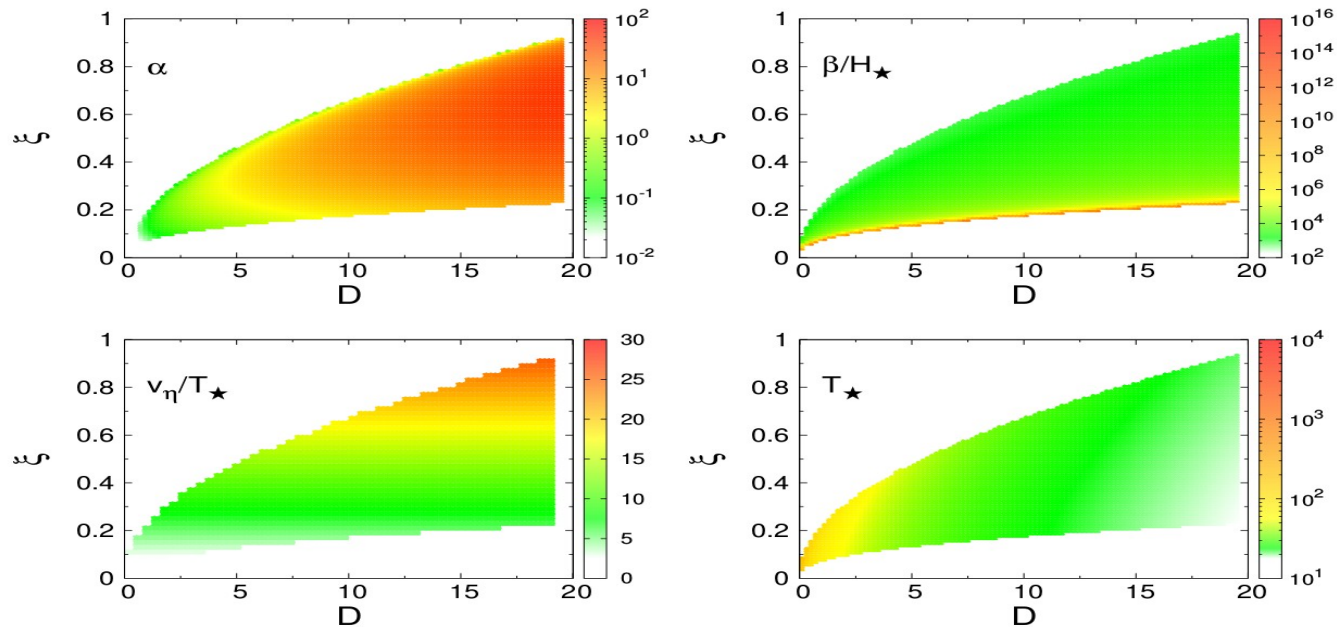


Figure 2. The parameters  $\alpha$ ,  $\beta/H_\star$ ,  $v_\eta/T_\star$ , and  $T_\star$  for the Scalar Quartic Model with  $\lambda = 0.1$ .

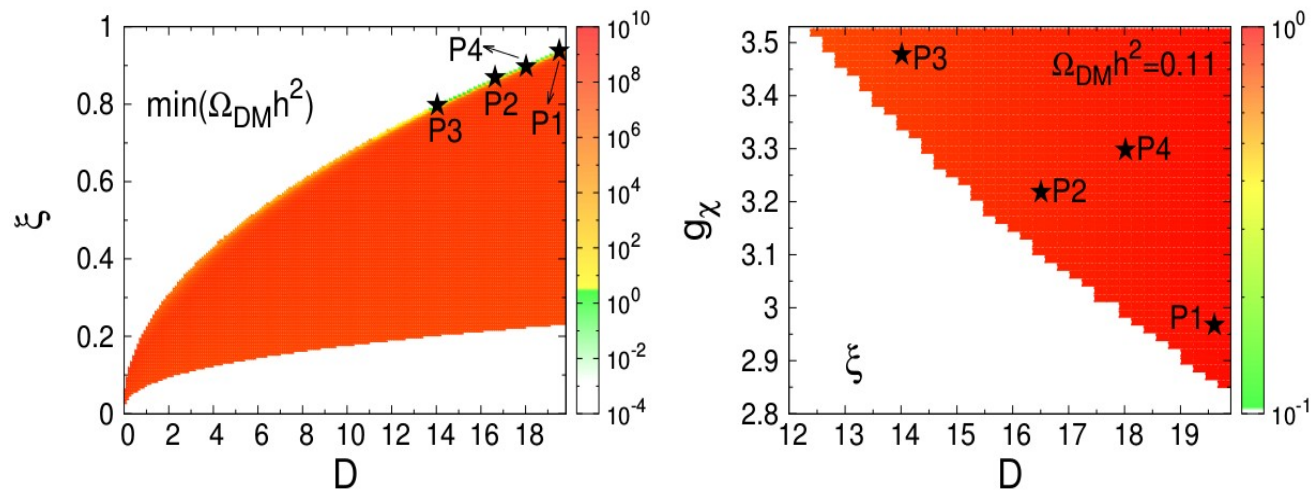
D.Marfatia, P.Y. Tseng: 2006.07313

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- ◆ Correct DM relic:



D.Marfatia, P.Y. Tseng: 2006.07313

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- ◆ Benchmark points:

Table 1. Benchmark points (with  $\lambda = 0.1$ ) for the Scalar Quartic Model that give  $\Omega_{\text{DM}}h^2 = 0.11$ .

	<b>P1</b>	<b>P2</b>	<b>P3</b>	<b>P4</b>
$\xi$	0.943	0.863	0.796	0.901
$D$	19.7	16.5	14.0	18.0
$g_\chi$	2.97	3.22	3.48	3.31
$\alpha$	0.089	0.082	0.076	0.121
$\beta/H_\star$	1116	1062	1015	1085
$v_\eta/T_\star$	25.71	23.41	21.49	24.51
$v_w$	0.768	0.763	0.760	0.791
$T_\star/\text{GeV}$	21.5	23.8	26.1	22.7
$m_\chi/\text{GeV}$	1642	1799	1953	1838

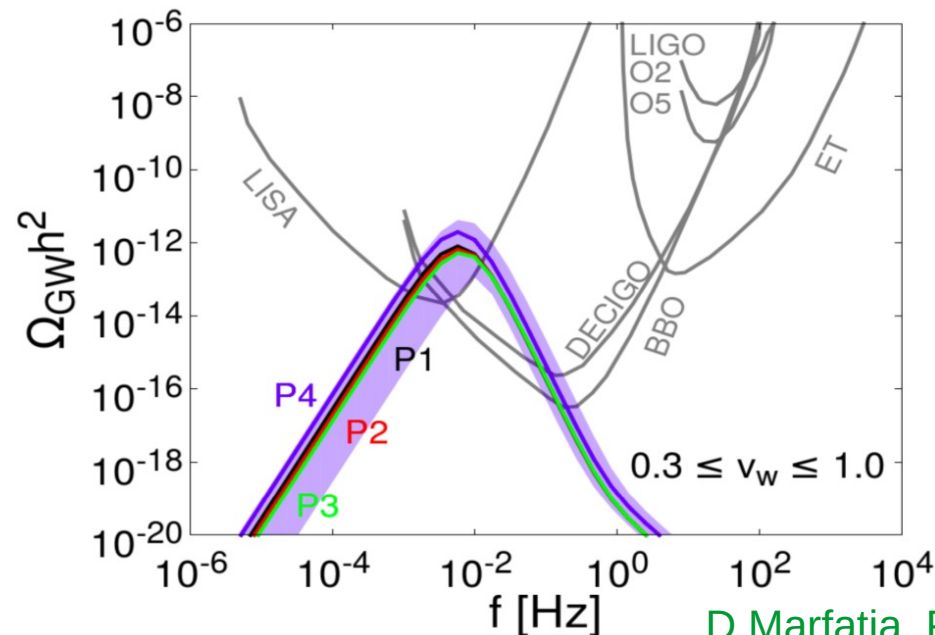
D.Marfatia, P.Y. Tseng: 2006.07313

# Part-1: Scalar quartic Model

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- ◆ GW signals:



D.Marfatia, P.Y. Tseng: 2006.07313

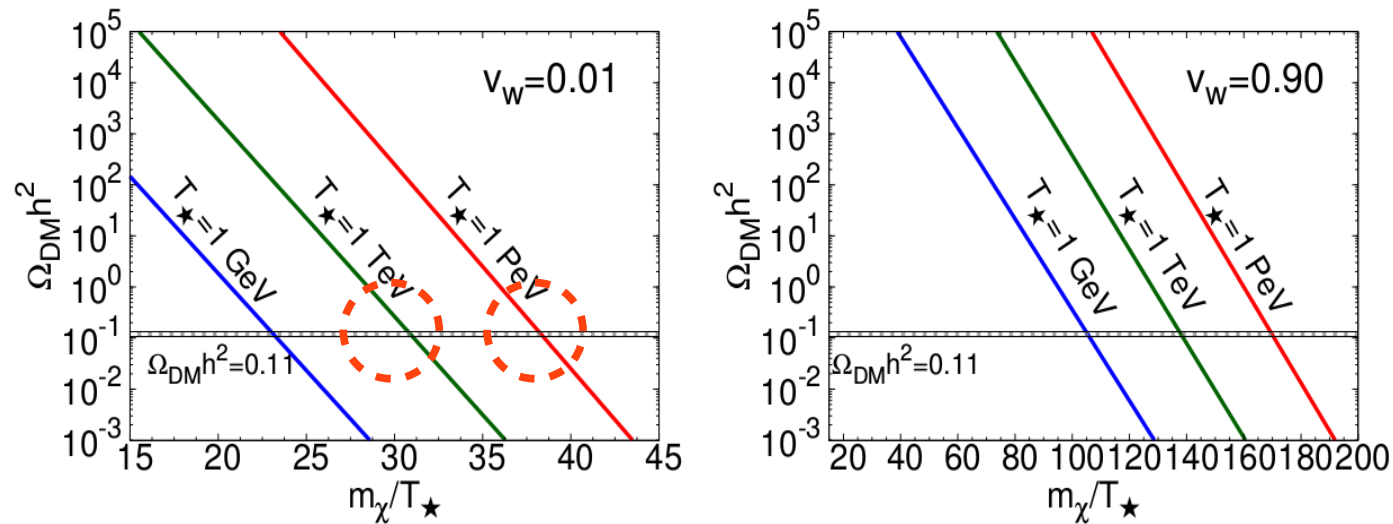
# Part-1: Summary

- ◆ We studied the **sudden freeze-out DM** as an alternative to the continuous **thermal freeze-out**.
- ◆ A necessary ingredient is a FOPT generates DM mass.
- ◆ The **DM relic abundance** may be determined by **bubble filtering**.
- ◆ Because FOPT triggers sudden DM freeze-out, **GW** offers a signature.

# Part-1: Introduction

- The  $m_\chi/T_\star$  needed to produce the DM relic abundance depends on the velocity of bubble wall  $v_w$ .

$$T_\star = m_\chi/30 \text{ for } m_\chi = 1 \text{ TeV}, v_w = 0.01$$



# Part-1: Bubble wall velocity

- In the **ultrarelativistic** limit, the pressure on bubble wall can be obtained from the **light degree of freedom** inside and outside the bubble:

$$P = \frac{d_n g_\star \pi^2}{90} (1 + v_w)^3 \gamma_w^2 T_\star^4$$

D.Chway et.al : 1912.04238  
J.R.Espinosa et.al: 1004.4187  
D.Bodeker et.al : 0903.4099

$$d_n \equiv \frac{1}{g_\star} \left[ \sum_{0.2M_i > \gamma_w T_\star} \left( g_i^b + \frac{7}{8} g_i^f \right) \right]$$

- The  $v_w$  can be obtained by solving the eq.  $P = \Delta V_{\text{eff}}$  :

$$\alpha = \frac{d_n}{3} (1 + v_w)^3 \gamma_w^2$$

$$\alpha \equiv \frac{\left(1 - T \frac{\partial}{\partial T}\right) \Delta V_{\text{eff}}|_{T_\star}}{\rho(T_\star)}, \quad \rho \equiv \pi^2 g_\star T^4 / 30$$



# Part-1: Bubble wall velocity

- For bubble wall velocity  $v_w$  faster than the sound speed in plasma, but **not ultrarelativistic**, we use the approximation:

P.J.Steinhardt, Phys. Rev. D. 25, 2074 (1982)

$$v_w = \frac{\frac{1}{\sqrt{3}} + \sqrt{\alpha^2 + \frac{2}{3}\alpha}}{1 + \alpha}$$

## Part-2: anti-correlation

- ◆ The percolation condition using saddle point approximation:

$$F(t) = \exp \left[ -\frac{4\pi}{3} v_w^3 \int_{t_c}^t dt' (t-t')^3 \Gamma(t') \right]$$

$$F(t_\star) = 1/e \simeq 0.37$$

$$8\pi v_w^3 \Gamma(T_\star) \beta^{-4} \simeq 1$$

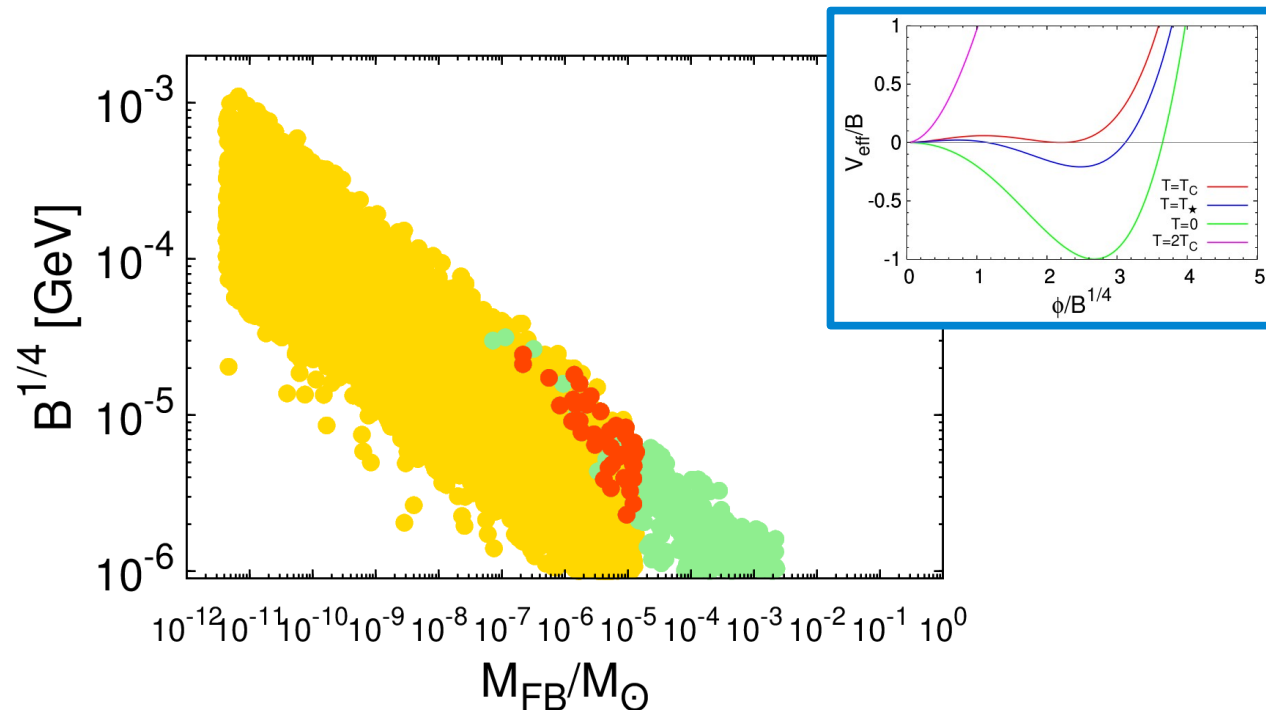
- ◆ Since  $\beta/H_\star$  is almost constant, thus  $\beta \propto H_\star \propto T_\star^2$  and from above condition, we have

$$T_\star^{-4} e^{-S_3(T_\star)/T_\star} \simeq B^{-1} e^{-S_3(T_\star)/T_\star} \simeq \text{constant}, \quad \text{i.e.,} \quad e^{-S_3(T_\star)/T_\star} \propto B$$

- ◆ Bubble nucleation rate per unit volume grow with vacuum energy density.
- ◆ For fixed  $\Omega_{\text{FB}} h^2$ , we obtain  $M_{\text{FB}} \propto 1/n_{\text{FB}}|_{T_0} \propto e^{3/4 \cdot (S_3(T_\star)/T_\star)} \propto B^{-3/4}$

# Part-2: Anti-correlation

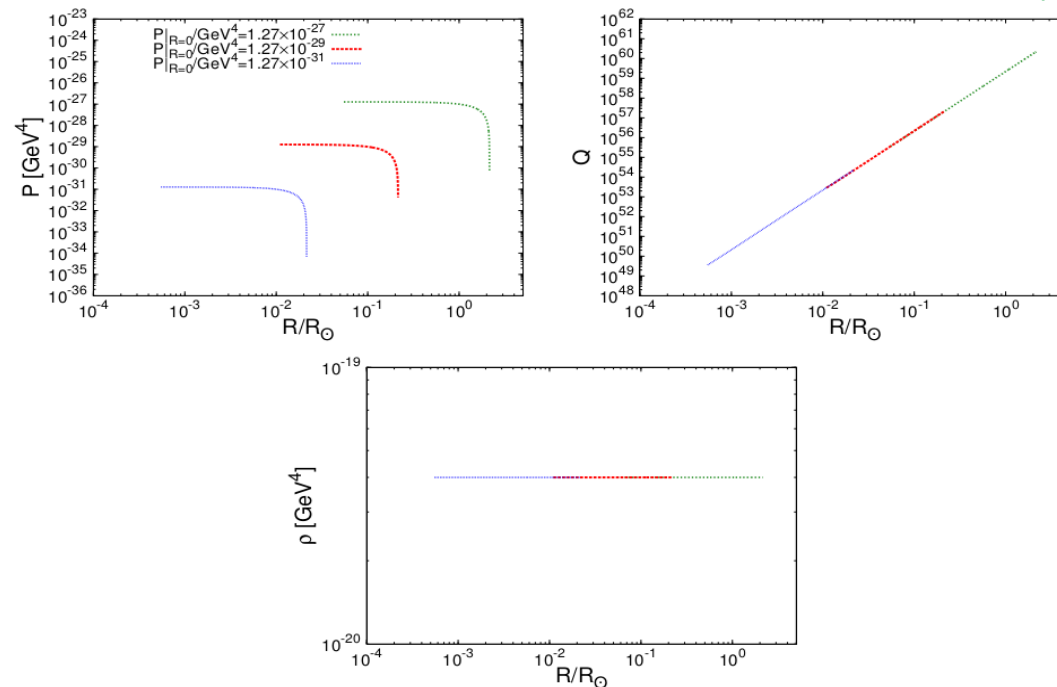
- We consider the finite-temperature quartic effective potential.
- Anti-correlation between the FB mass and energy scale of FOPT.



# Part-2: Number density of FB

- Solving the Tolman-Oppenheimer-Volkoff(TOV) equation to find the density profile of FB

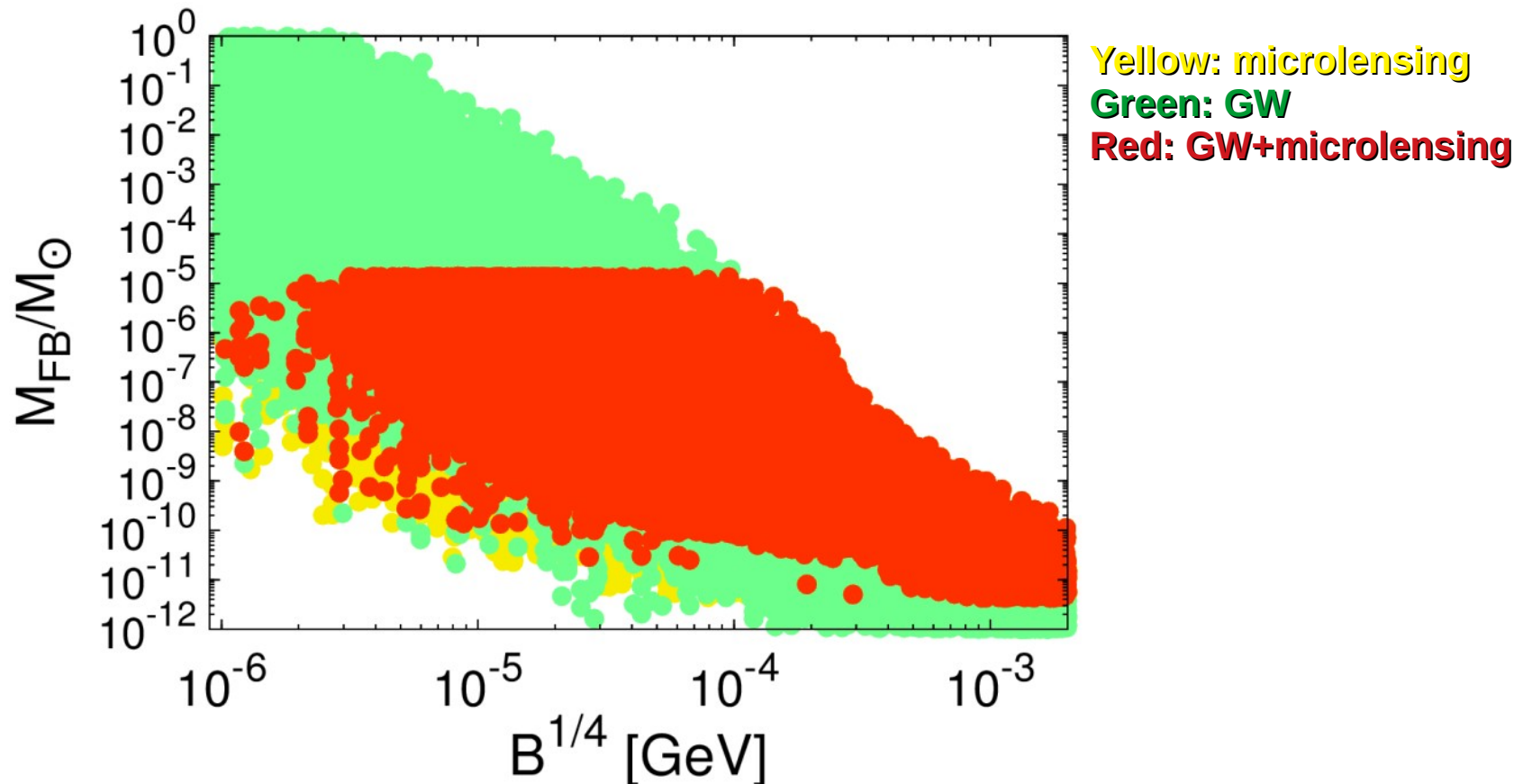
D.Marfatia, P.Y. Tseng: 2107.00859



**Figure 2.** The pressure  $P$  (upper-left),  $Q$ -charge within radius  $R$  (upper-right), and energy density profile (bottom) of a FB with  $B^{1/4} = 10$  keV for three boundary conditions,  $P|_{R=0} = 1.27 \times 10^{-27} \text{ GeV}^4$ ,  $P|_{R=0} = 1.27 \times 10^{-29} \text{ GeV}^4$ , and  $P|_{R=0} = 1.27 \times 10^{-31} \text{ GeV}^4$ . Correspondingly,  $(M_{\text{FB}}/M_\odot, R_{\text{FB}}/R_\odot) = (6.5079 \times 10^{-2}, 2.149)$ ,  $(6.4911 \times 10^{-5}, 0.2149)$ , and  $(6.5079 \times 10^{-8}, 2.149 \times 10^{-2})$ .

# Part-2: Correlated signals

- From BBN, the robust 95% CL upper limit is  $\Delta N_{\text{eff}} \lesssim 0.5$ .



# Part-2: Microlensing

- If the lenses have a universal mass  $M_{\text{FB}}$ , with Maxwell-Boltzmann velocity distribution, then event rate per source star is

$$\frac{d^2\Gamma}{dxdt_E} = D_S \frac{f_{\text{DM}}}{M_{\text{FB}}} \left[ \rho_{\text{MW}}^{\text{DM}}(r_{\text{MW}}) \frac{v_E^4}{v_{\text{MW}}^2} e^{-v_E^2/v_{\text{MW}}^2} + \rho_{\text{M31}}^{\text{DM}}(r_{\text{M31}}) \frac{v_E^4}{v_{\text{M31}}^2} e^{-v_E^2/v_{\text{M31}}^2} \right]$$

$$v_E(x) = 2u_{1.34}(x)R_E(x)/t_E$$

- The  $t_E$  is the time duration for each event.

$$x \equiv D_L/D_S$$

$u_{1.34}=1$  for point-like lens and background star.

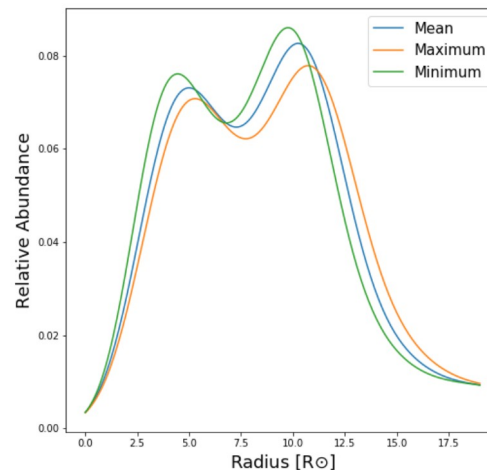
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- The radius distribution of stars in M31:

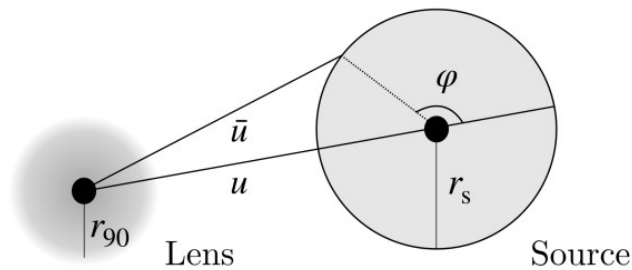


N.Smyth et.al: 1910.01285

# Part-2: Microlensing: Finit-size

- Finite-size effect:

D.Croon, D.McKeen, N.Raj, and Z.Wang: 2007.12697



$$\bar{u}(\varphi) = \sqrt{u^2 + r_s^2 + 2ur_s \cos \varphi}$$

- Solve the lens equation for along the edge of the source:

$$\bar{u}(\varphi) = t(\varphi) - \frac{m(t(\varphi))}{t(\varphi)}$$

- The magnification is the area of each image:

$$\mu_i = \eta \frac{1}{\pi r_s^2} \int_0^\pi t_{\varphi,i}^2(\psi) d\psi$$

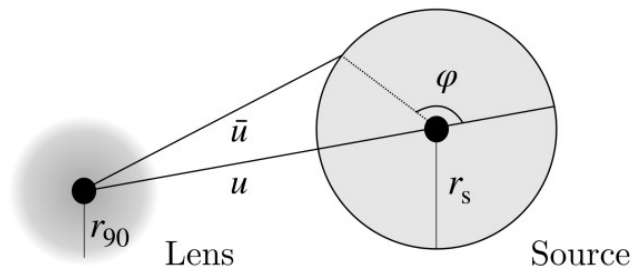
$$\psi = \tan^{-1} \frac{r_s \sin \varphi}{u + r_s \cos \varphi}, \quad 0 \leq \psi \leq \pi$$



# Part-2: Microlensing: Finit-size

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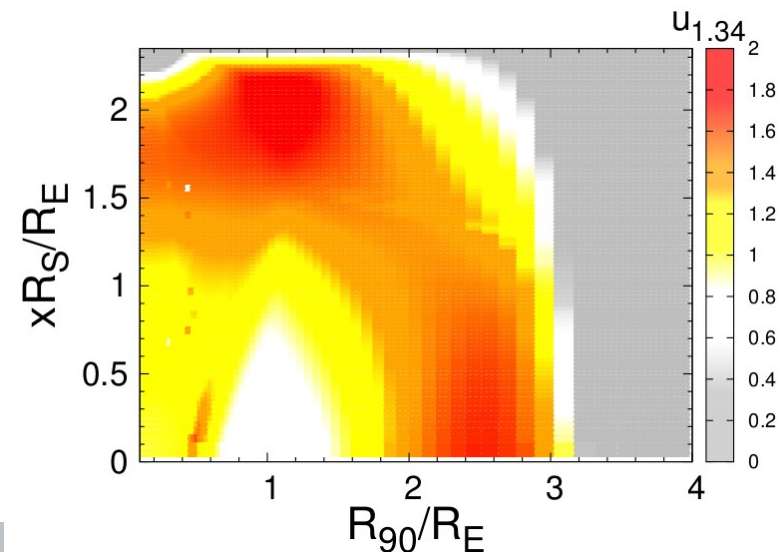
D.Croon, D.McKeen, N.Raj, and Z.Wang: 2007.12697



$$\bar{u}(\varphi) = \sqrt{u^2 + r_s^2 + 2ur_s \cos \varphi}$$

- The effective size for 1.34 times magnification:

$$\mu_{\text{tot}}(u \leq u_{1.34}) \geq 1.34$$



D.Marfatia, P.Y. Tseng: 2107.00859

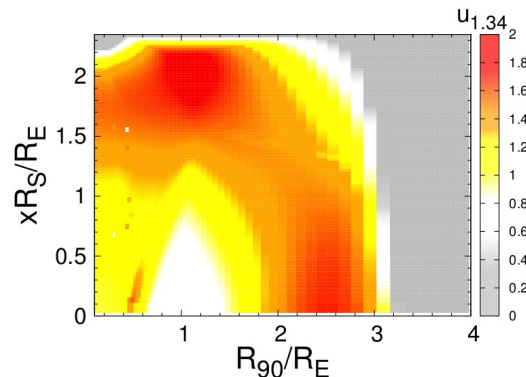
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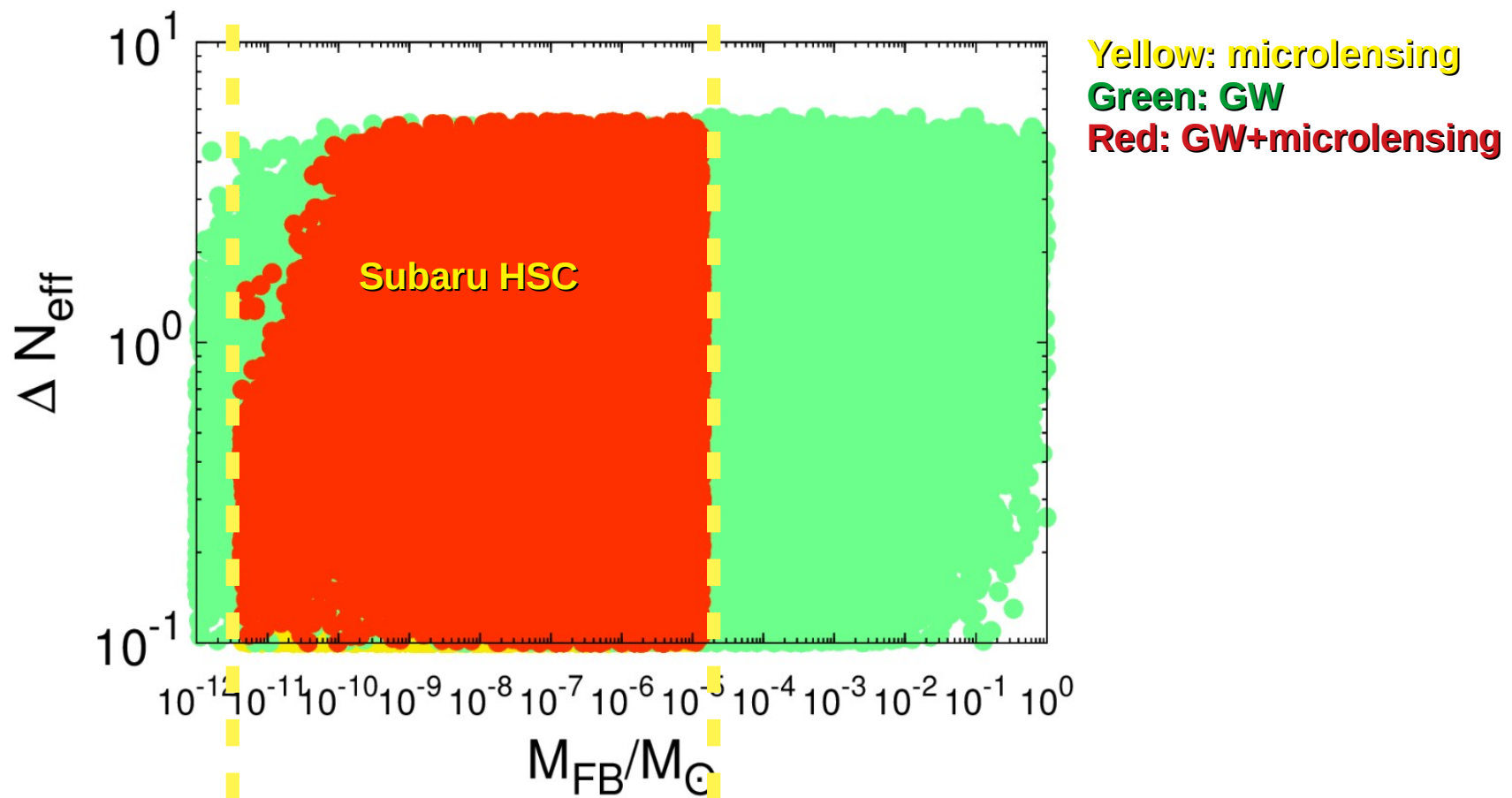
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D.Marfatia, P.Y. Tseng: 2107.00859

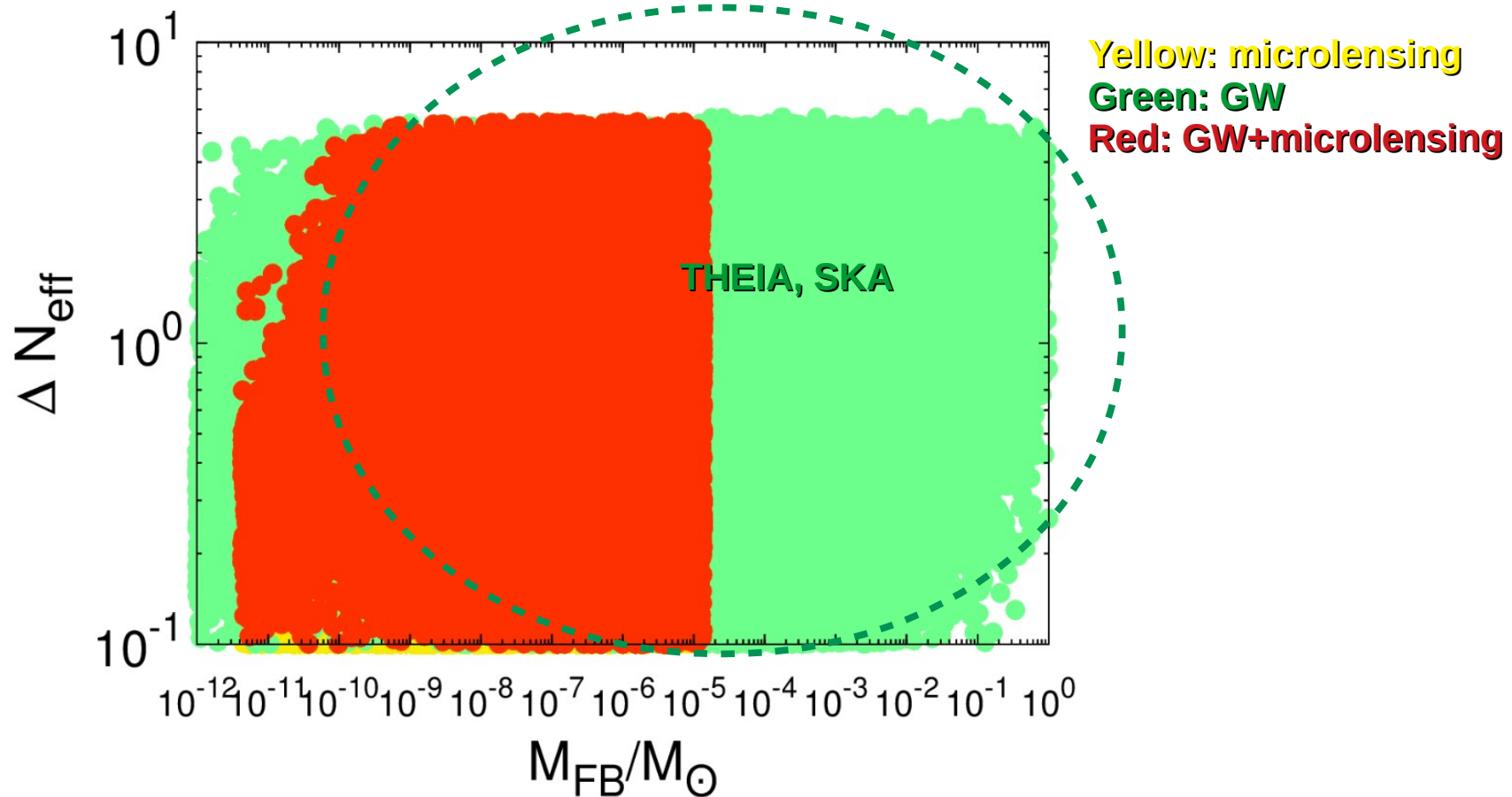
# Part-2: Correlated signals

- Correlated signals of GW and microlensing:



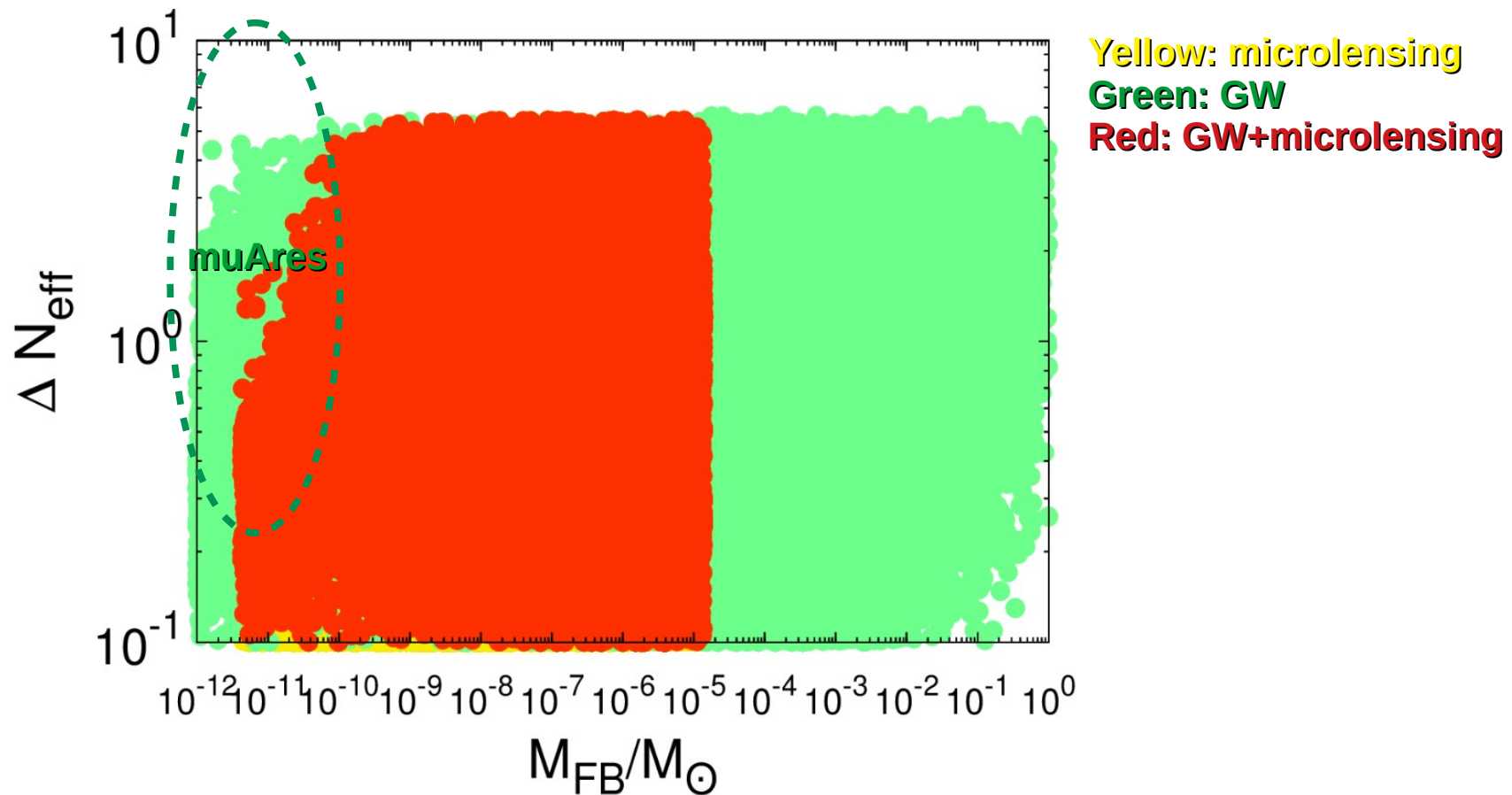
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