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Superconducting tensor detector for mid-frequency gravitational waves: SOGRO

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in collaboration with

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Target science and a prototype design for a superconducting tensor detector for mid-frequency gravitational waves

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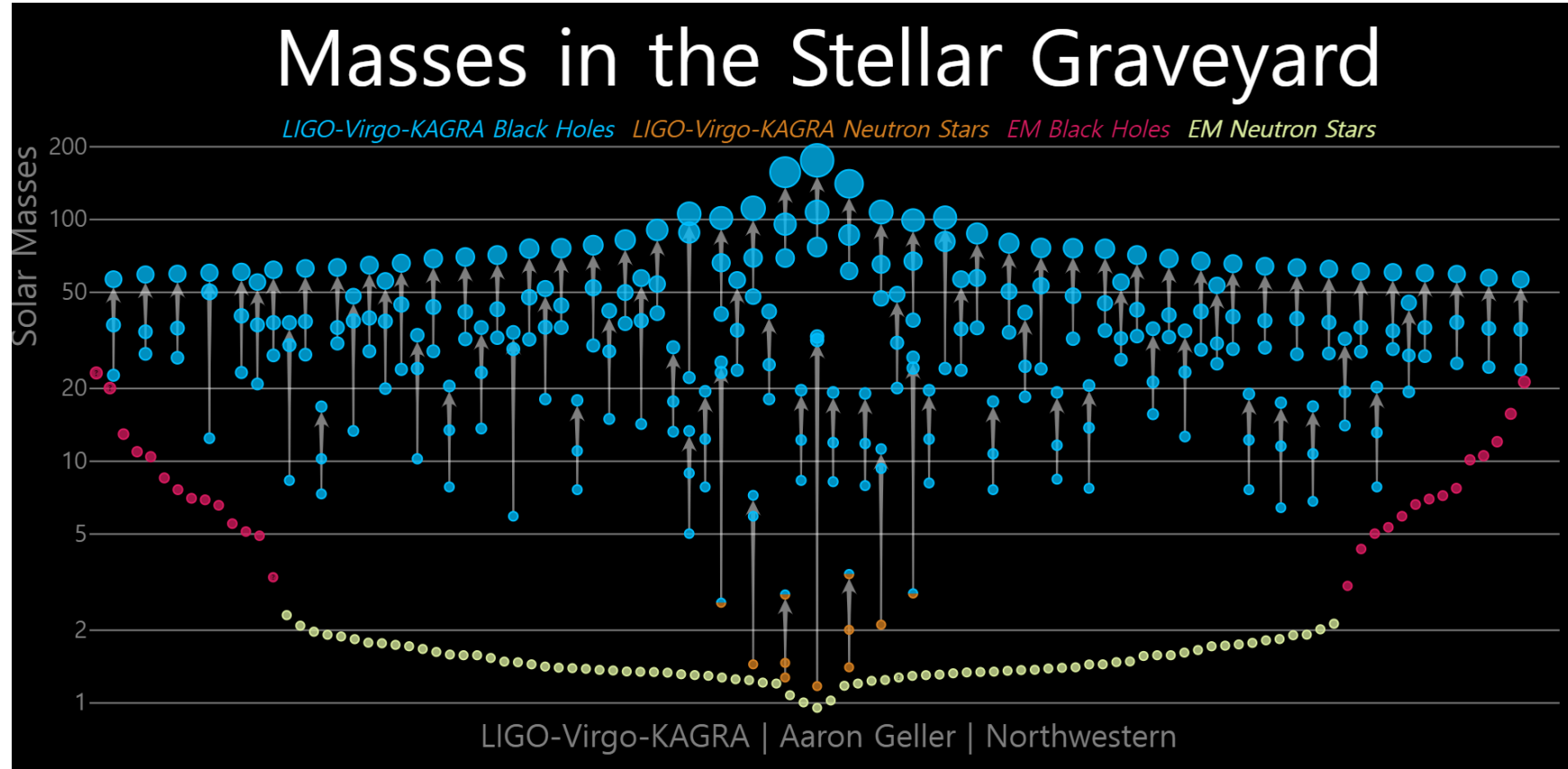
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Outline

- I. Introduction
- II. Basic Principle and Designs
- III. Science with SOGRO
- IV. Summary and Outlook

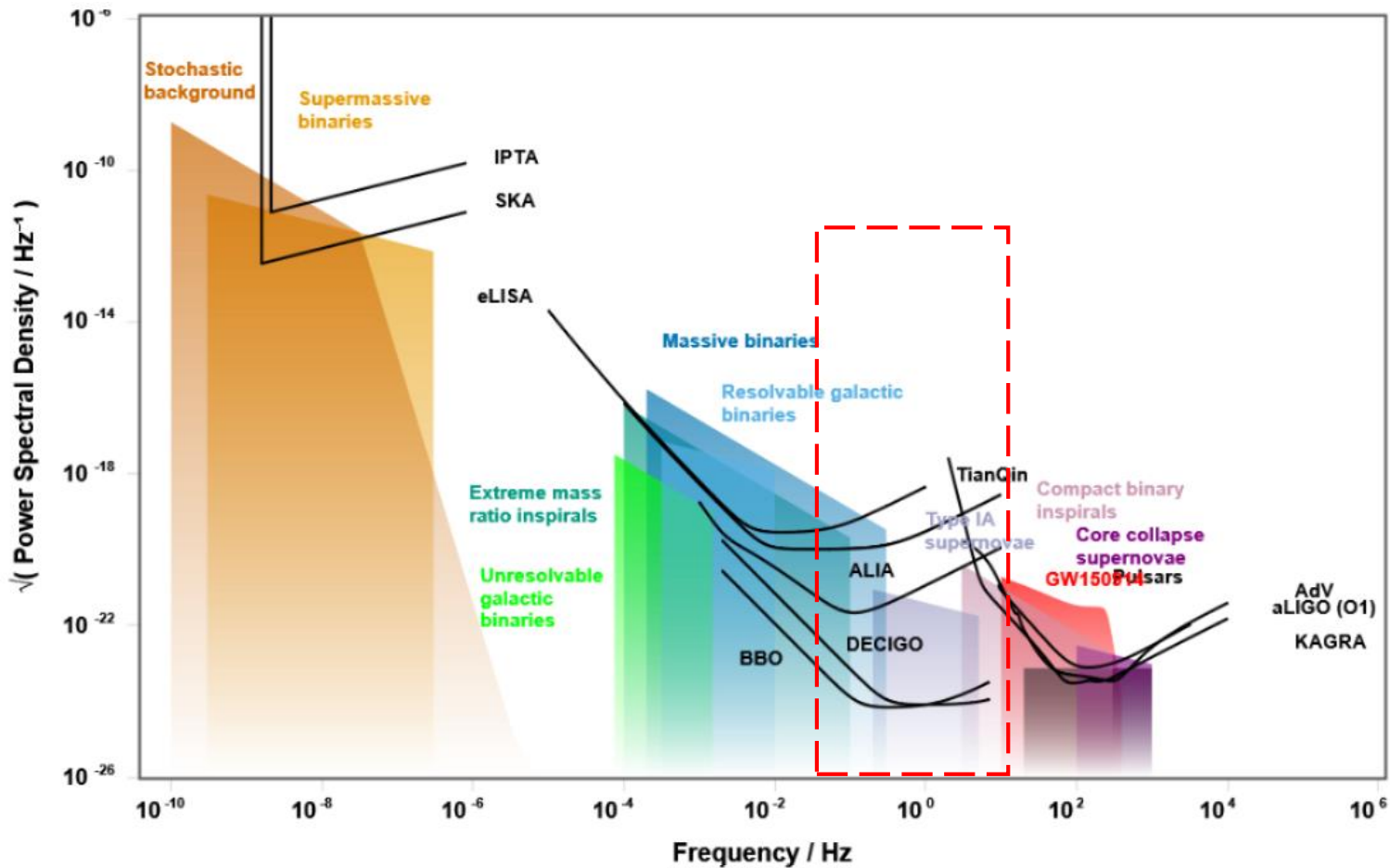
I. Introduction

✓ **GWs Observed:** O1 (2015.09.12~2016.01.19), O2 (2016.11.30~2017.08.25) & O3 (2019.04.01~2020.03.27)



✓ ~90 events in total from compact binary objects, e.g., BH-BH, NS-NS & BH-NS.

- ✓ It opened up a new window to the universe: GW astronomy.
- ✓ Already gave lots of implications to gravitational physics and fundamental physics, e.g., test of GR in strong field ($\dot{P}_{orb} \sim - (10^{-14} \sim 10^{-12}) \rightarrow (0.1 \sim 1)$), origin of heavy elements including Ag, Hubble tension, ...
- ✓ **Gravitational Wave Spectrum:**

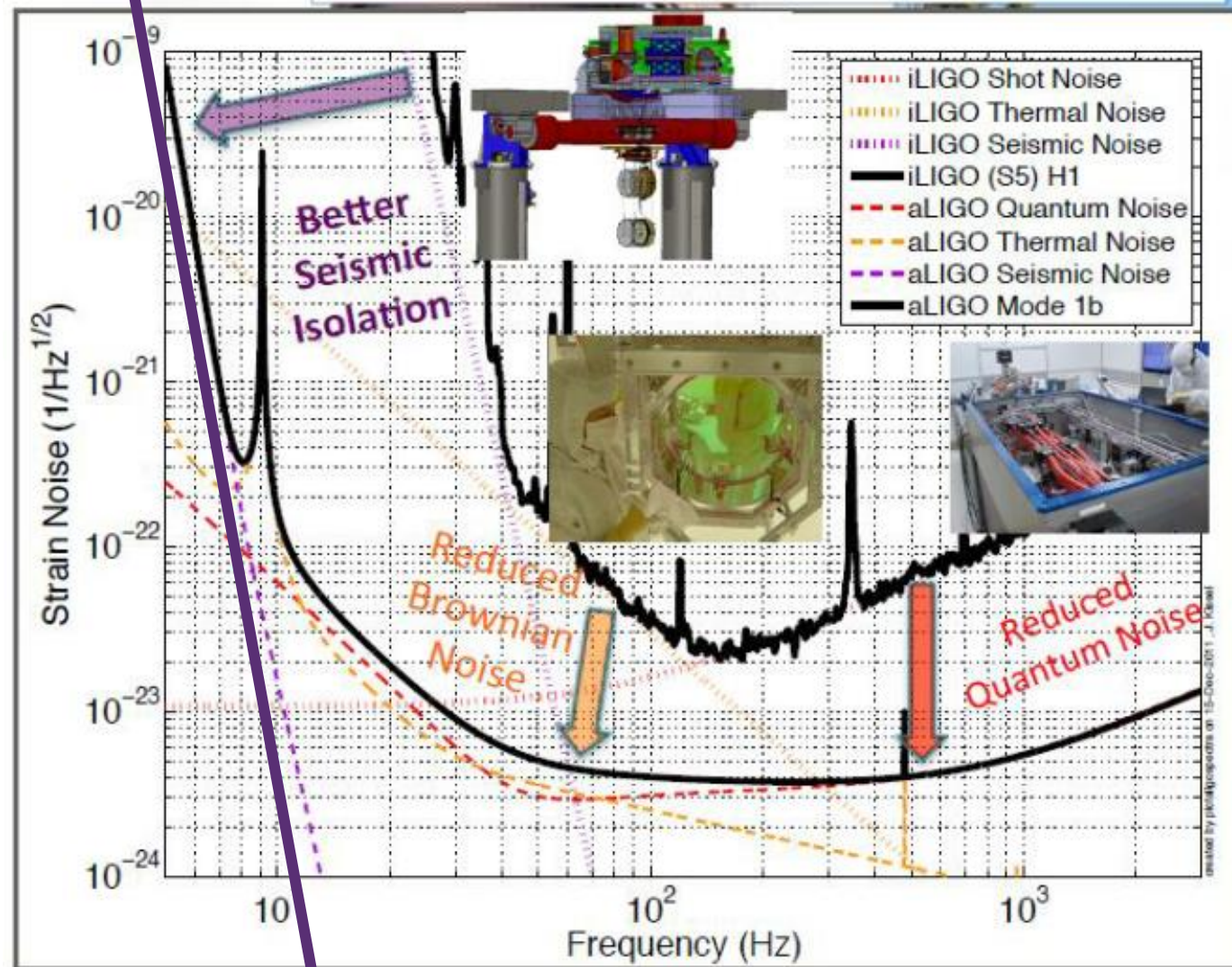


- Interferometer-type detectors:
 - aLIGO, aVirgo, KAGRA, eLISA, INDIGO
- Plans to improve sensitivity:
 - A+ (~ 22), Einstein Telescope (~ 23), Cosmic Explorer (~ 27), AAGO, TAIJI, TianQin, etc.
- **Terrestrial ones cover 10~1000 Hz only!**
- Multi-wavelength GW astronomy
- Mid-Frequencies (0.1~10 Hz):
 - Space: DECIGO ('01), BBO, ALIA, AMIGO
 - Ground: TOBA ('10), MIGA, ZAIGA

+ "SOGRO" ('13~)

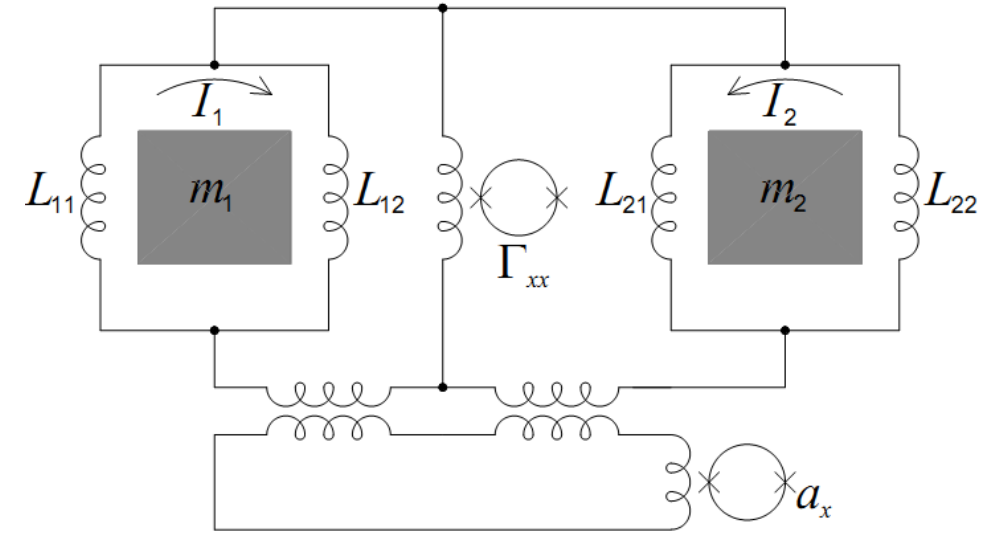
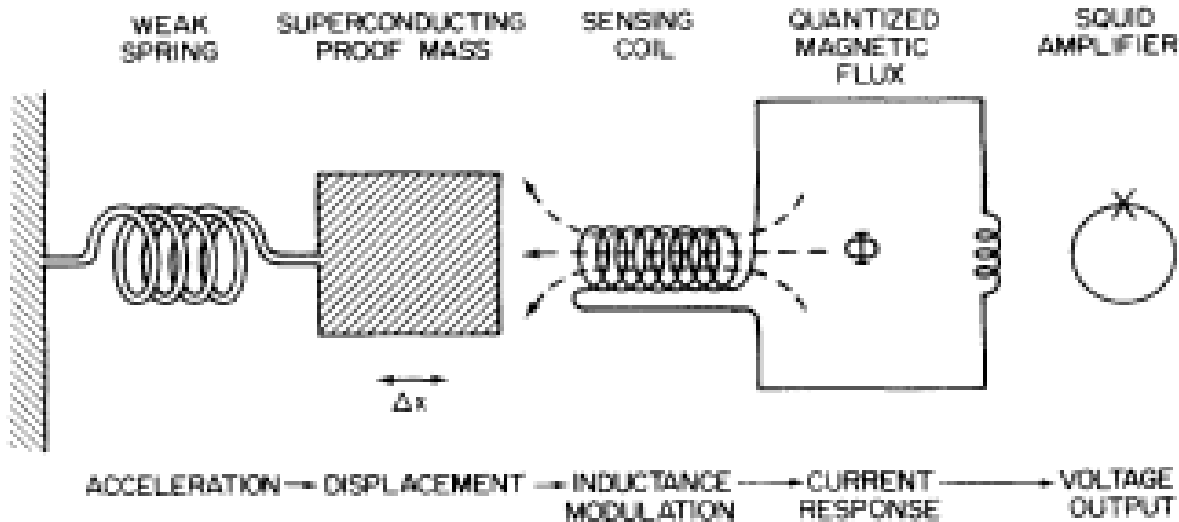
- ✓ Obstacles to observe GWs below ~ 10 Hz on the ground:

**Big barrier
due to
(Seismic
+ Newtonian)
noises!**



II. Basic Principle and Designs

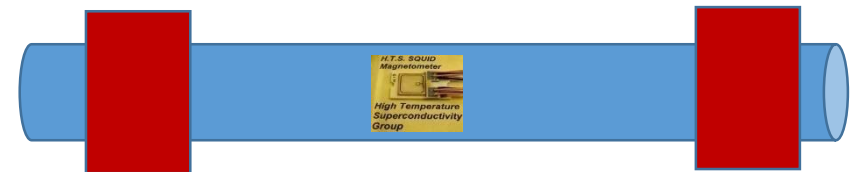
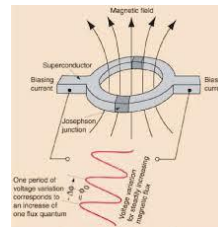
✓ Basic principle: Chan & Paik ('87)



→ Only relative motions matter!!

Test mass motion

- Induced current at sensing coil
- Measure flux at SQUID

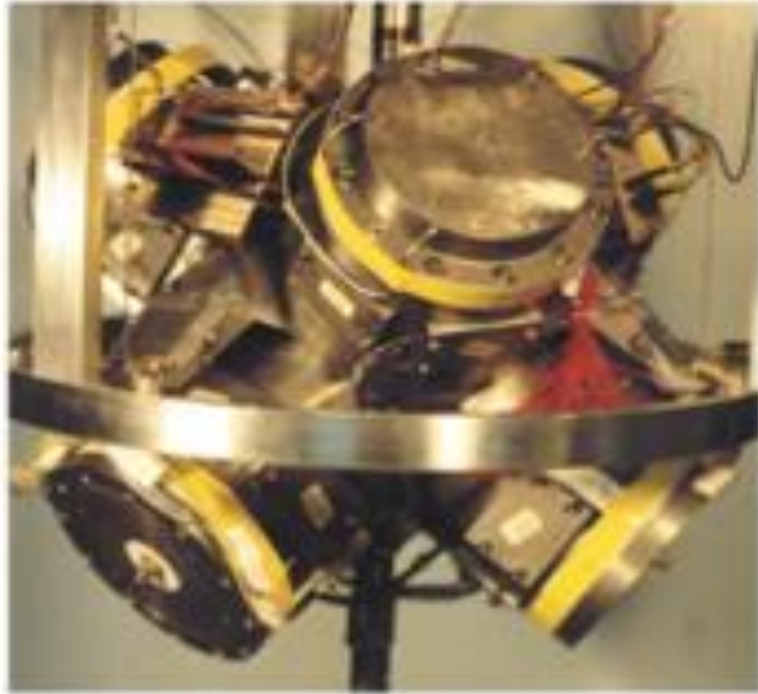


- Sensing coils & SQUIDs are mounted on the rigid stick.
- Two masses are freely moving.

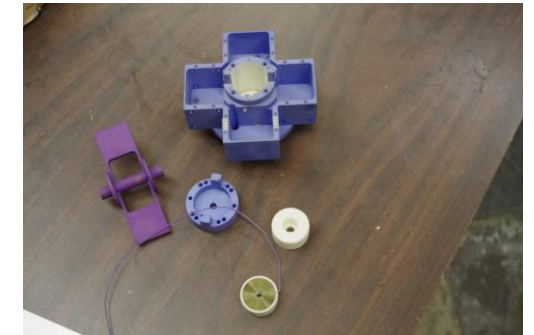
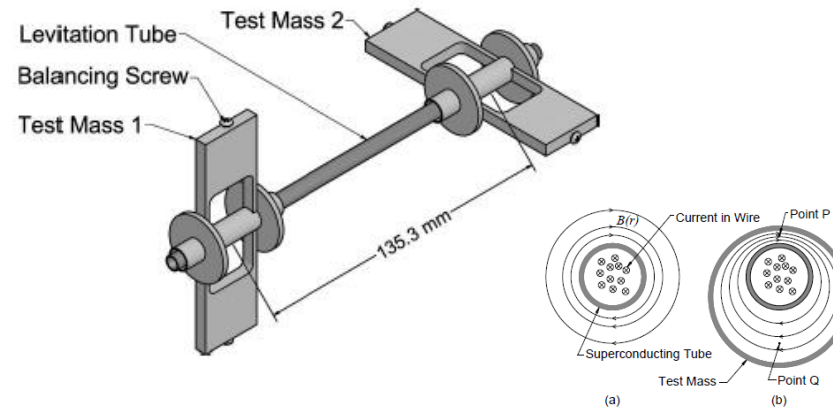
✓ A Bit of History for SOGRO:

- Wagoner, Will & Paik: 1979
- Superconducting Gravity Gradiometer (SGG):

Ho Jung Paik



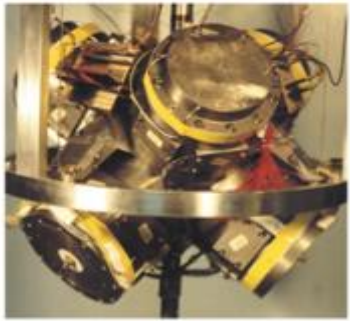
Moody, Paik, & Caravan (2002)



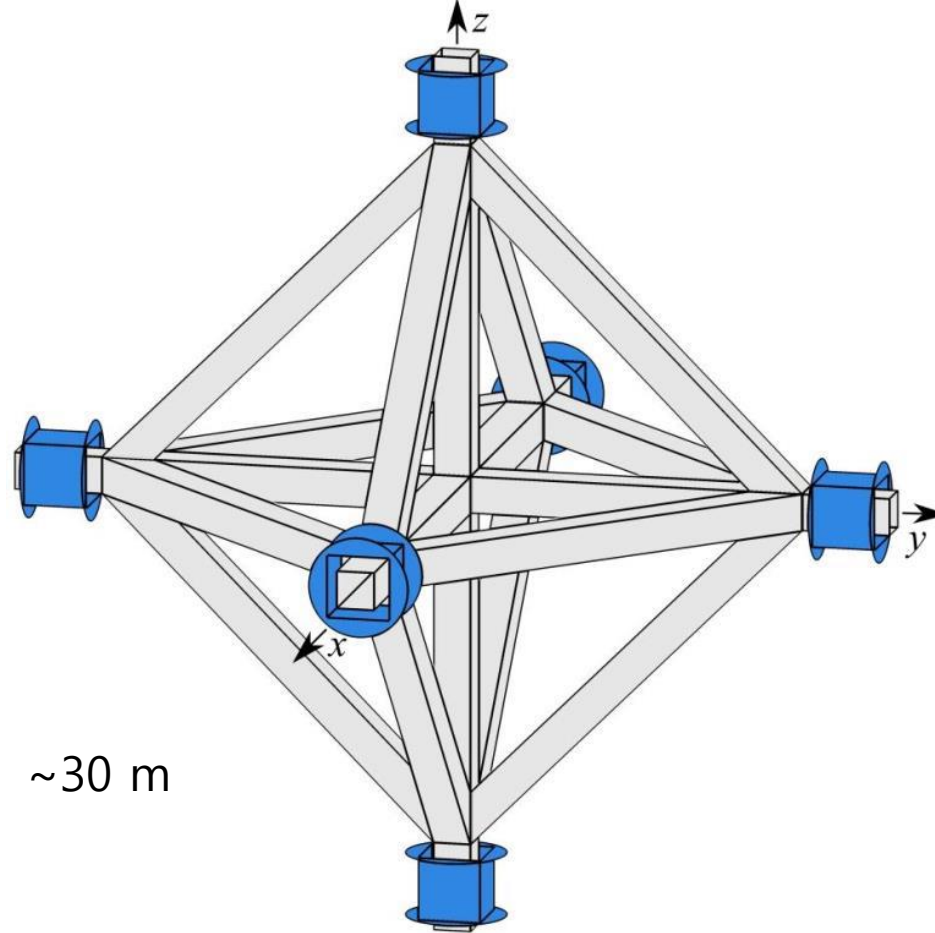
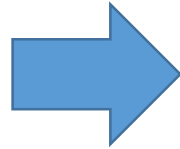
(Picture credit: H-M. Lee)

- ✓ Measure the relative motion of test masses
- ✓ Magnetic levitation, SQUID sensor
- ✓ Test mass: ~ 1 kg, Size: ~ 30 cm
- ✓ Sensitivity: $\sim 2 \times 10^{-11} s^{-2} Hz^{-1/2}$
- ✓ Developed for over 30 years at U. of Maryland

✓ Make it large!



~0.3 m



~30 m

- Combining 6 test masses, a tensor GW detector is formed;

$$h_{ii}(t) = \frac{2}{L} [x_{+ii}(t) - x_{-ii}(t)]$$

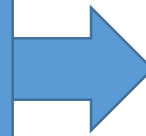
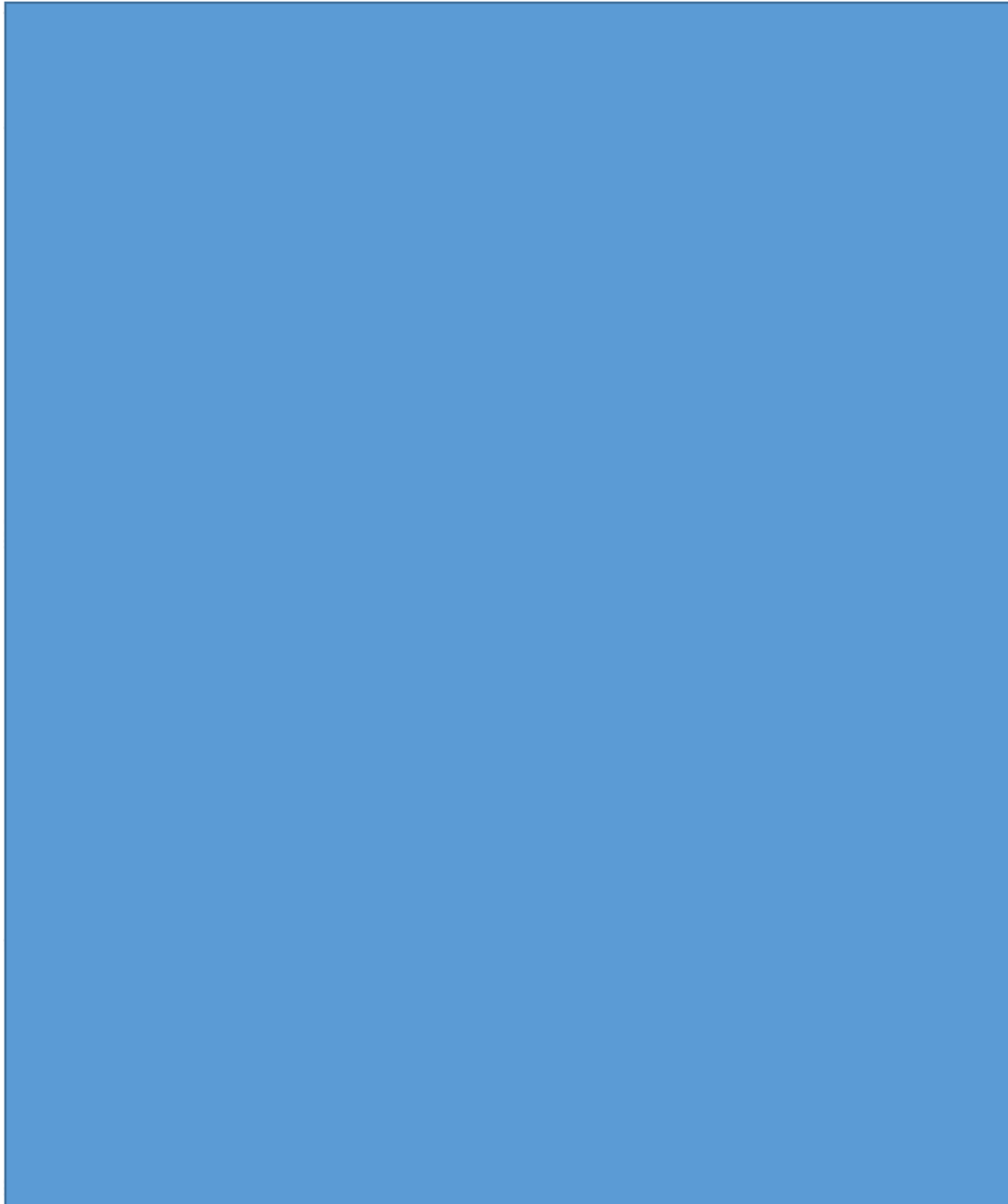
$$h_{ij}(t) = \frac{1}{L} \left\{ [x_{+ij}(t) - x_{-ij}(t)] - [x_{-ji}(t) - x_{+ji}(t)] \right\}, i \neq j$$

➔ “Diagonal” channel, “In-line component”, or
XX mode

➔ “Off-diagonal” channel, “Cross component”,
or XY mode

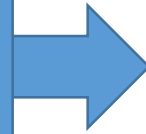
✓ Responses:

- **SOGRO:**
Superconducting
Omni-directional
Gravitational
Radiation
Observatory



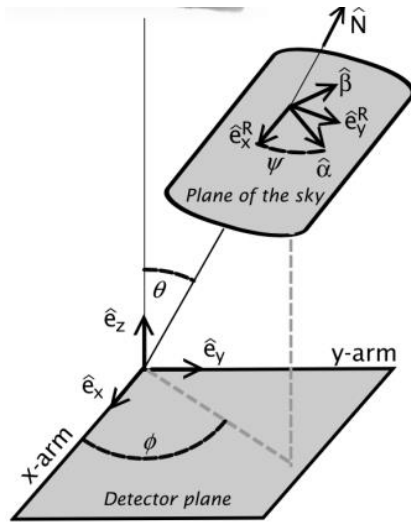
**SOGRO is
omni-directional!**

**6 channels in total:
Multi-channel (tensor)
detector!**



**able to distinguish
breeding and
longitudinal signals!**

✓ Sky localization (Simple estimation with Gaussian noise):



$$h_+ = h_{11} \sin^2 \phi - h_{12} \sin(2\phi) + h_{22} \cos^2 \phi,$$

$$h_x = (h_{23} \cos \phi - h_{13} \sin \phi) \sin \theta$$

$$+ \left(\frac{1}{2} (h_{11} - h_{22}) \sin(2\phi) - h_{12} \cos(2\phi) \right) \cos \theta,$$

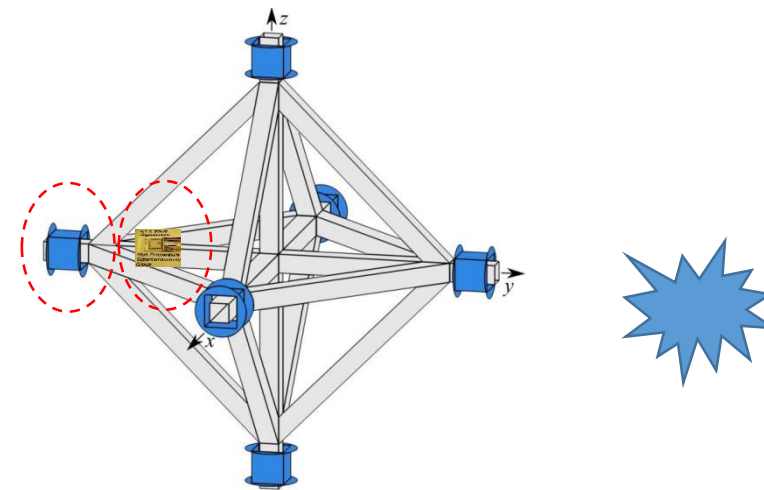
$$0 = (h_{11} + h_{22}) \cos \theta - (h_{13} \cos \phi + h_{23} \sin \phi) \sin \theta,$$

$$0 = (h_{11}^2 - h_{22}^2 + h_{13}^2 - h_{23}^2) \sin(2\phi)$$

$$- 2[h_{12}(h_{11} + h_{22}) + h_{13}h_{23}] \cos(2\phi).$$

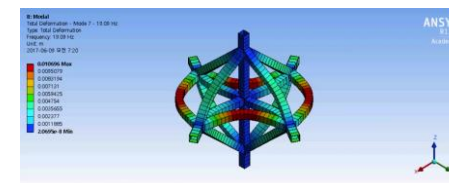
✓ Main noise sources:

- Antenna noise: Test mass
- Amplifier noise: SQUID



$$S_h(f) = \frac{32}{ML^2\omega^4} \left\{ \frac{k_B T \omega_D}{Q_D} + \frac{|\omega^2 - \omega_D^2|}{2\omega_p} \left(1 + \frac{1}{\beta^2} \right)^{1/2} k_B T_N \right\}, \quad k_B T_N = n\hbar\omega_p$$

- Platform thermal noise



$$S_{\xi, \omega_0}(f) = \frac{16}{m_{\text{eff}} L^2 \omega_0^2 Q_{\text{pl}} \omega} \frac{4k_B T_{\text{pl}}}{(1 - \omega^2/\omega_0^2)^2 + 1/Q_{\text{pl}}^2}. \quad S_{\xi}(f) = \sum_i S_{\xi, \omega_{0i}}(f)$$

- Newtonian noise

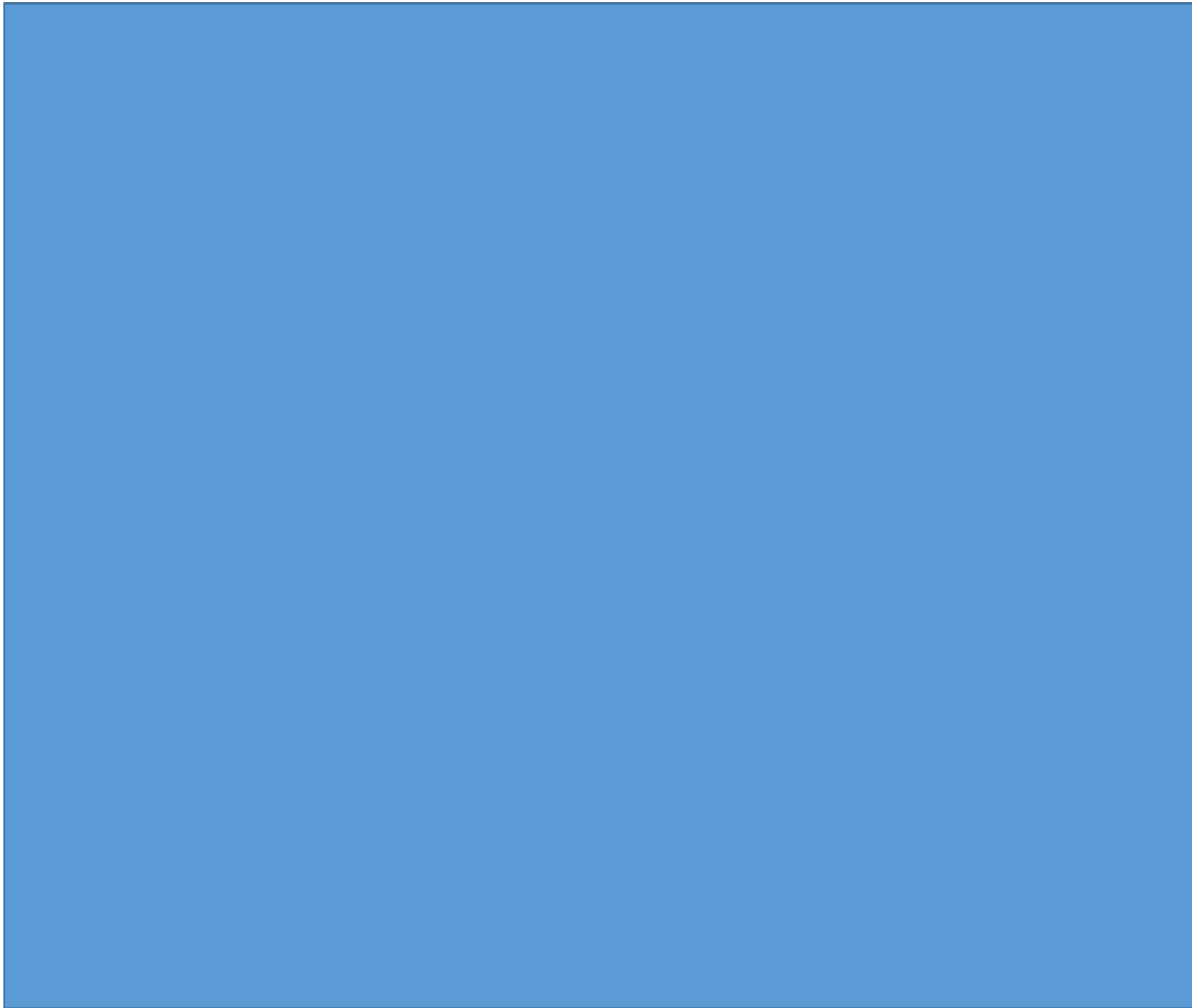
✓ **Platform strain noise:** Pre-stressed modal analyses using ANSYS



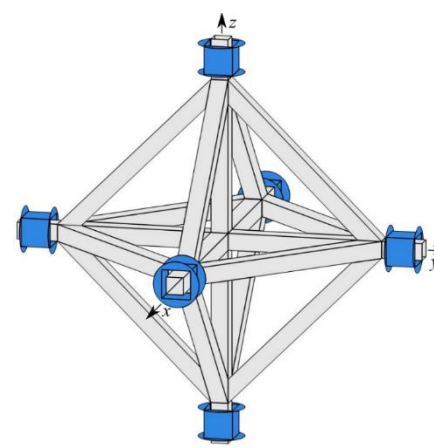
aSOGRO

pSOGRO

✓ Design parameters:



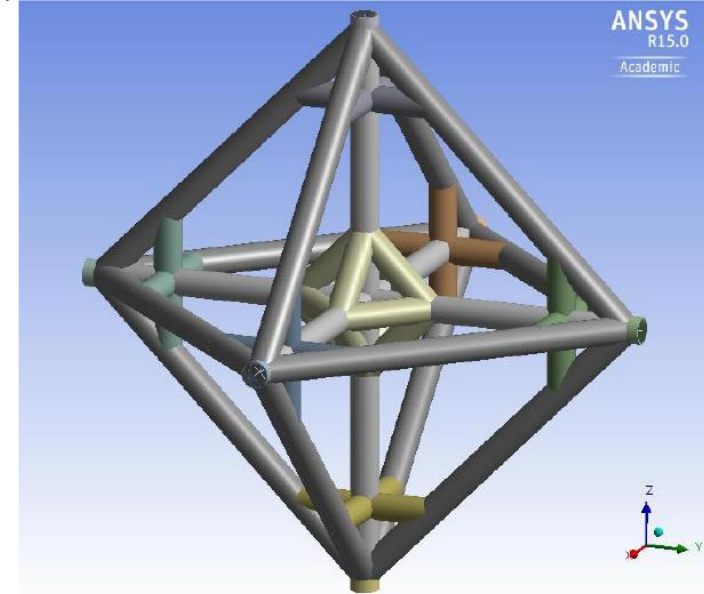
Bae+'22 Paik+ '16 & Paik+'20



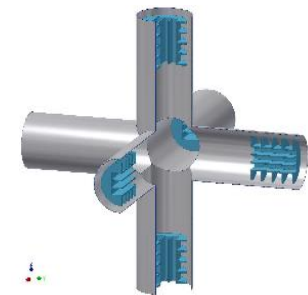
SOGRO/aSOGRO

(30 m, 50 m, 100 m)

- (100~250) tons
- ≤ 4 K
- Underground:
~200 m



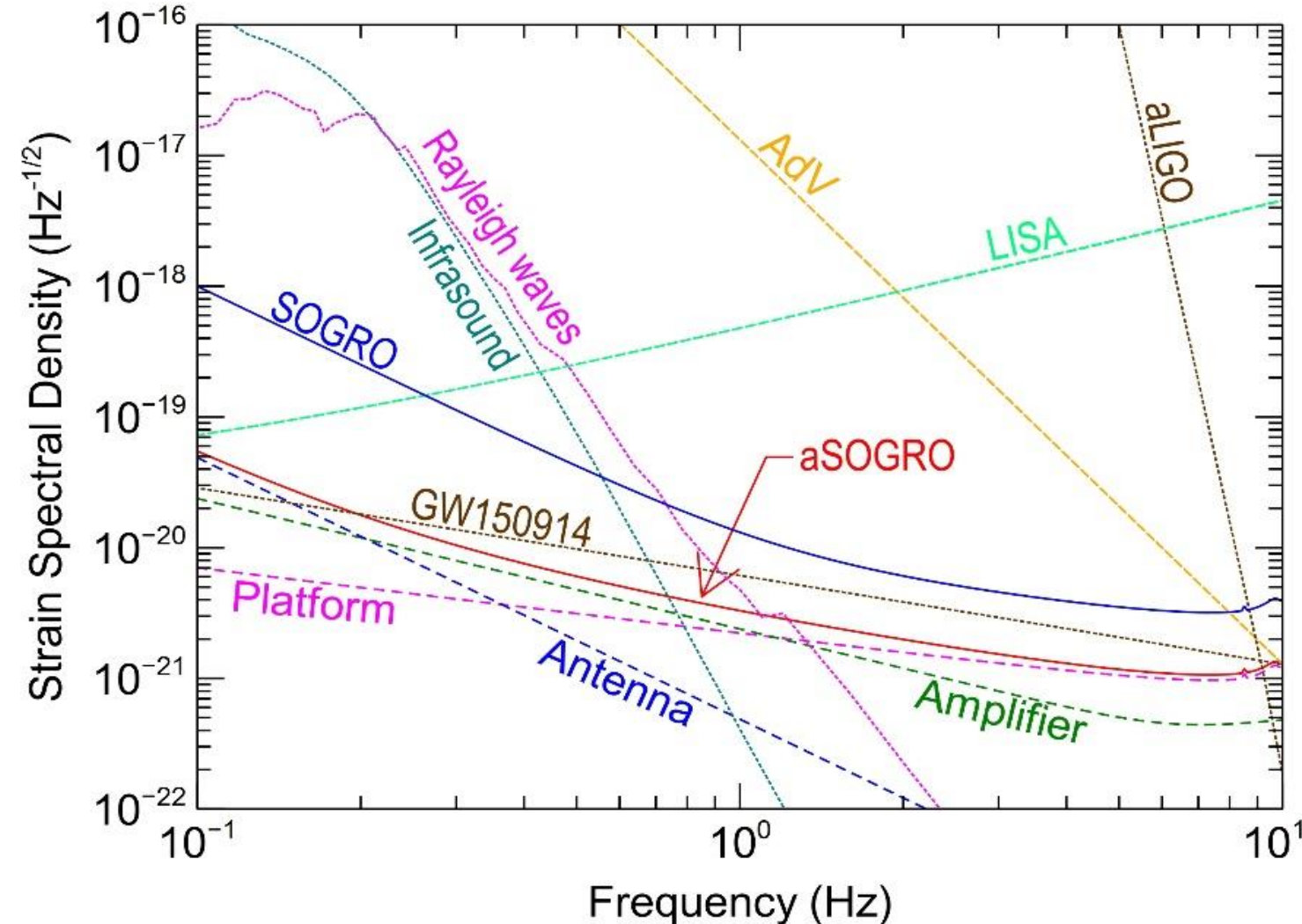
pSOGRO



2 m, 1 ton

✓ Sensitivity of SOGROs:

$$S_{h,\Sigma}(f) = \frac{16}{3ML^2\omega^4} \left[\frac{k_B T \omega_D}{Q_D} + \frac{|\omega^2 - \omega_D^2|}{\omega_p} \left(1 + \frac{1}{\beta^2} \right)^{1/2} k_B T_N \right], \quad k_B T_N = n\hbar\omega_p, \quad \Sigma \text{ over 5 channels}$$



$$\delta\phi_{\text{Rf}}(\vec{q}, z, \omega) = -2\pi \frac{\gamma G \rho_0}{k} \xi(\omega) e^{-zk} e^{i\vec{k}\cdot\vec{q}}$$

(Harms & Paik '15)

- Understanding its characteristic features is essential for designing the whole experiments.
- Find out the optimal design(s) for the platform which satisfies (all) desired requirements.

✓ Cooling of SOGRO System:

@ SNU workshop (2017/8/1)



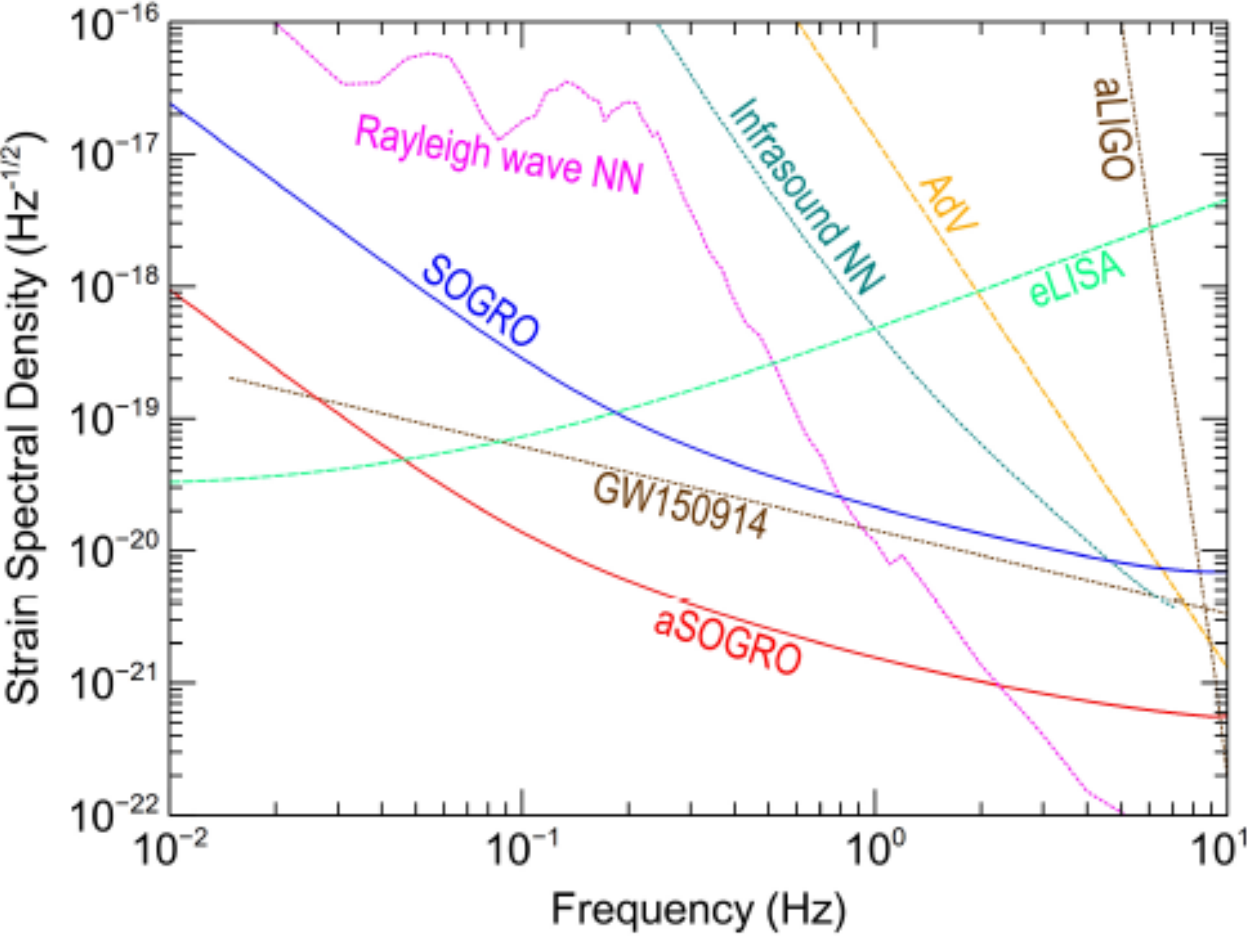
✓ **Concept for Cooling SOGRO System – 2nd Stage : 0.1 K**



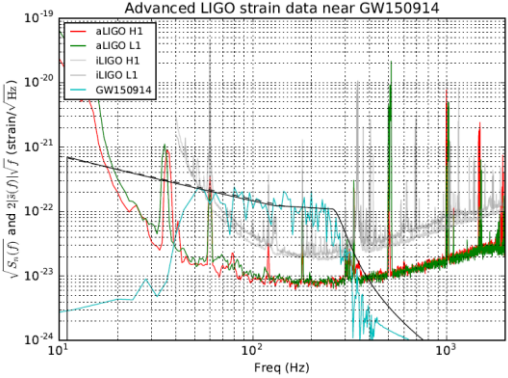
III. Science with SOGRO

1) Inspiralling BBH: "Stellar-mass binaries"

- Accurate measurements of inspiral phase
- Early notification to LIGO/Virgo/KAGRA



~ 10 days

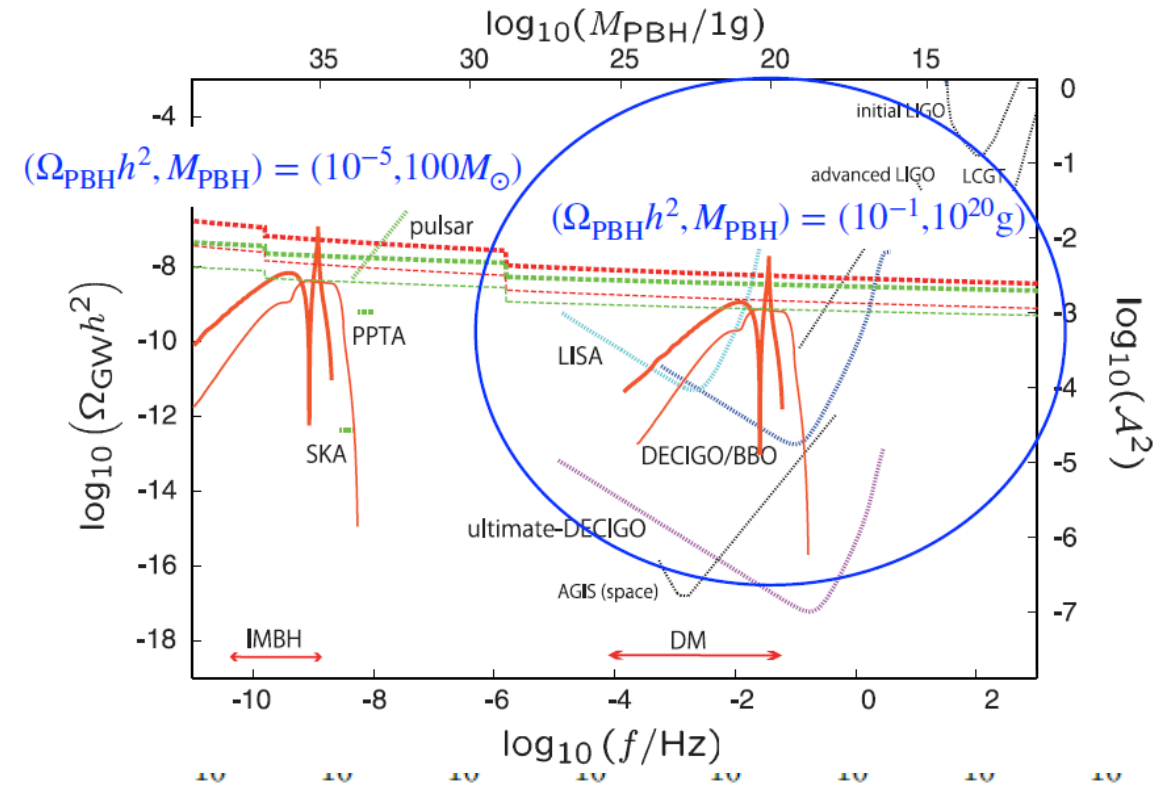


Observed for ~.2s

2) IMBH binary inspirals and mergers:



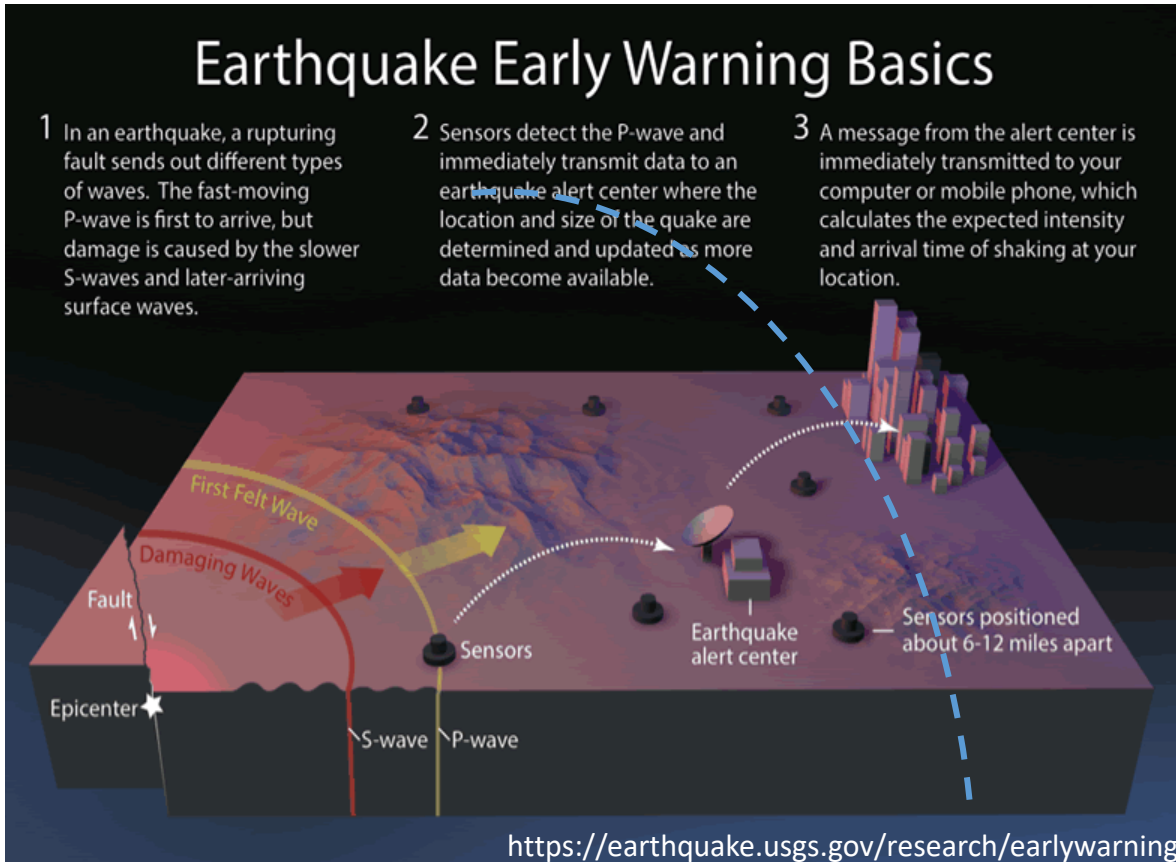
3) Stochastic Gravitational Wave Background



- Sasaki, Zhang & Pi ('18): "Scaloron"
- Espinosa, Racco & Riotto ('18): "SM Higgs instability"

✓ **Build multi detectors!!**

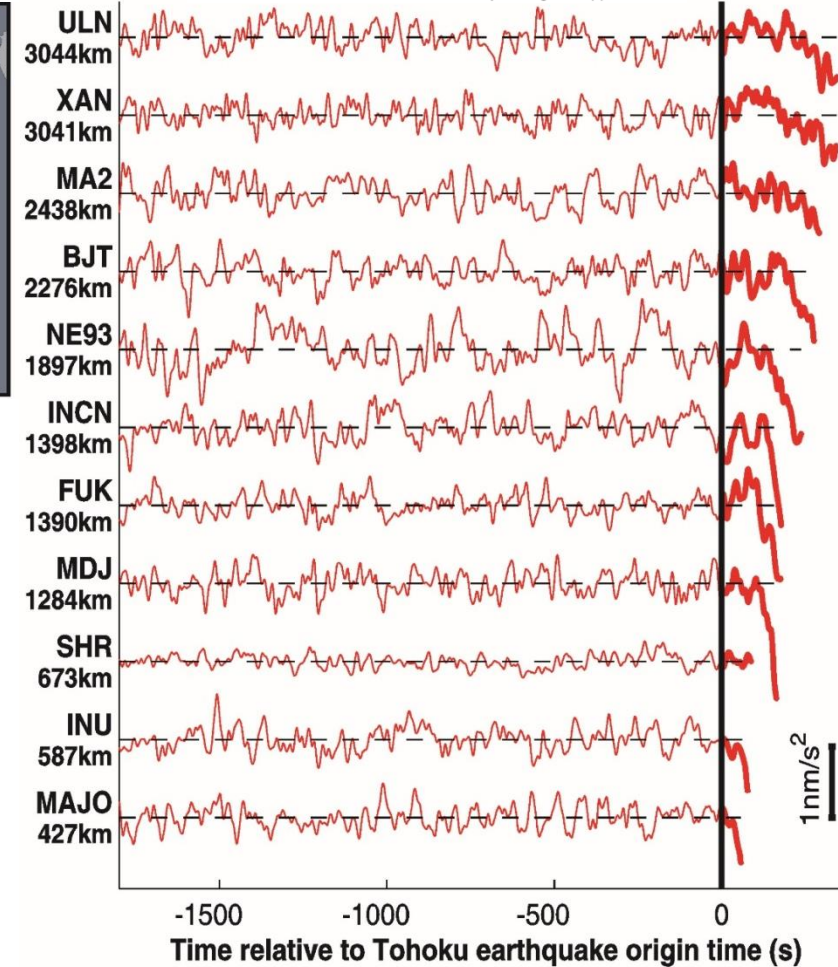
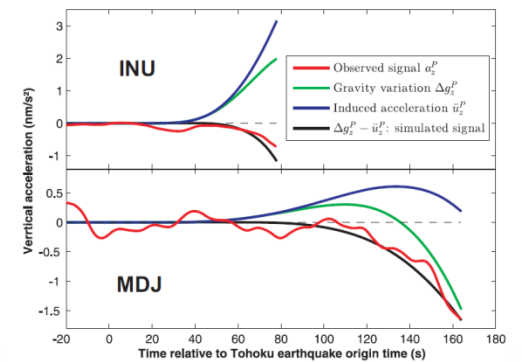
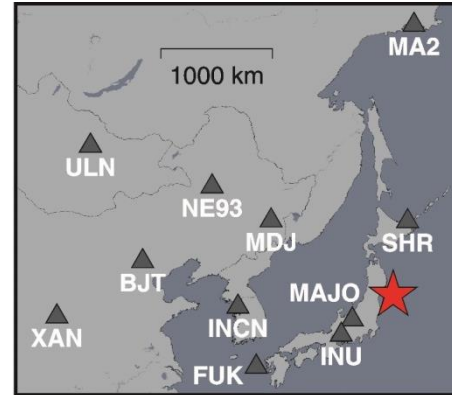
4) Earthquake Early Warning:



✓ Saves ~10 s for Kyungjoo-Busan (~76 km)

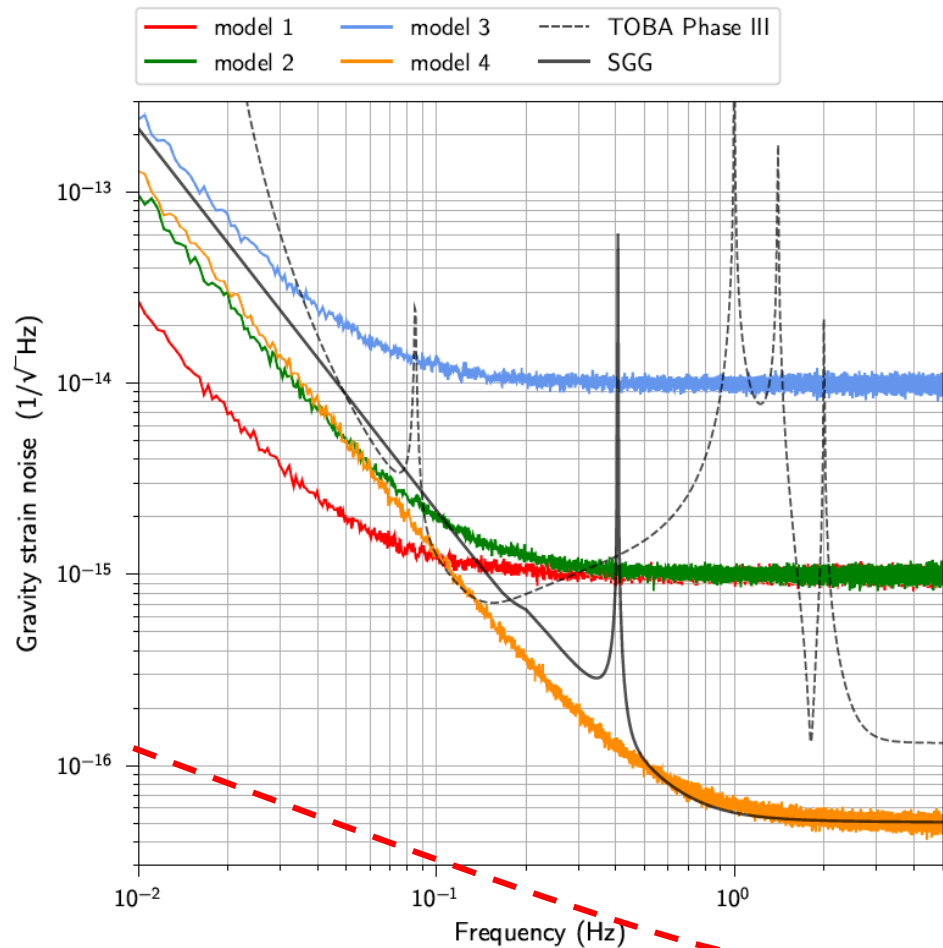
(Credit for slides: Ampuero '18)

2011 Tohoku earthquake



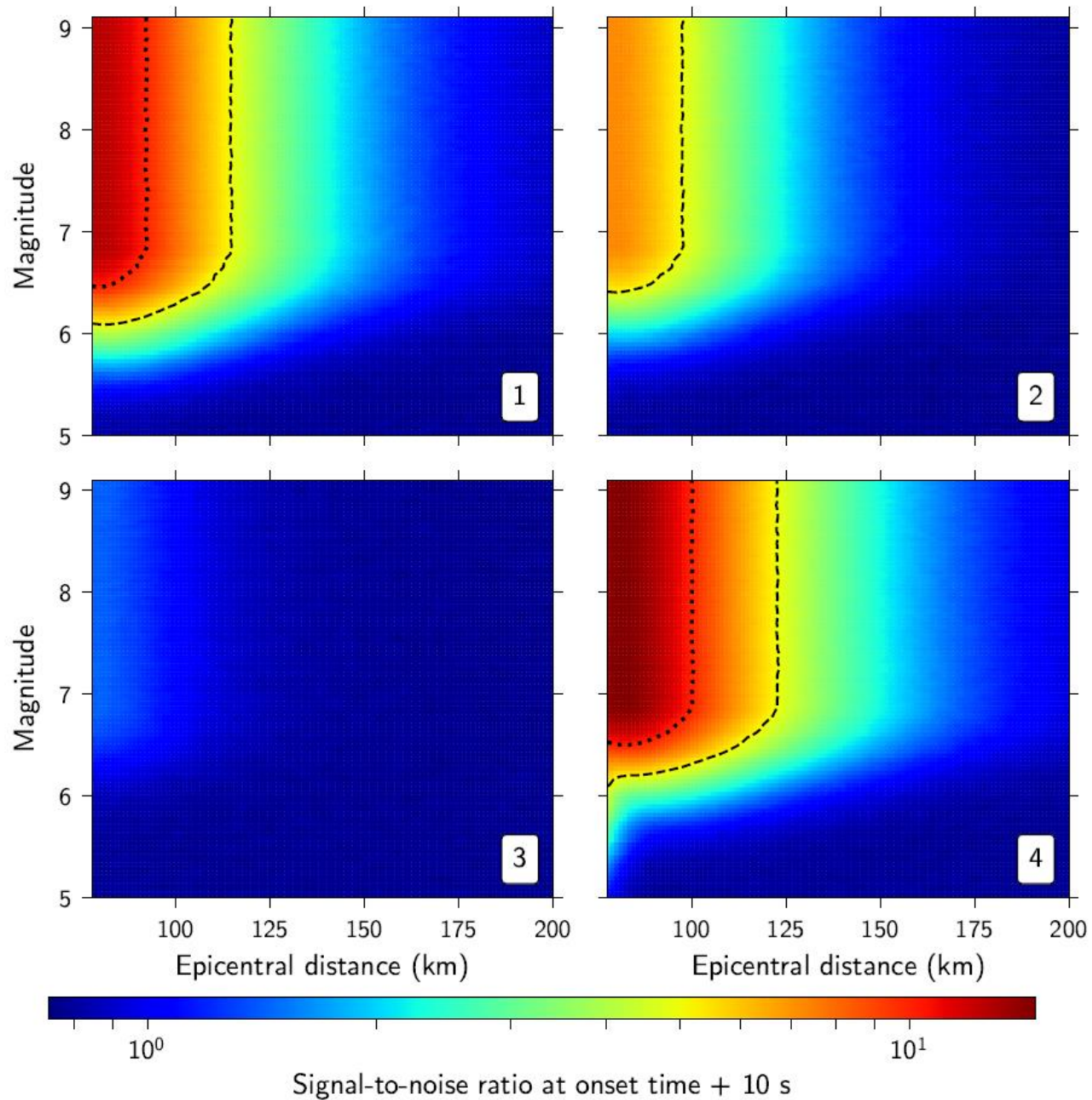
Vallée et al., Science, 2017²¹

SNR of matched filter detection



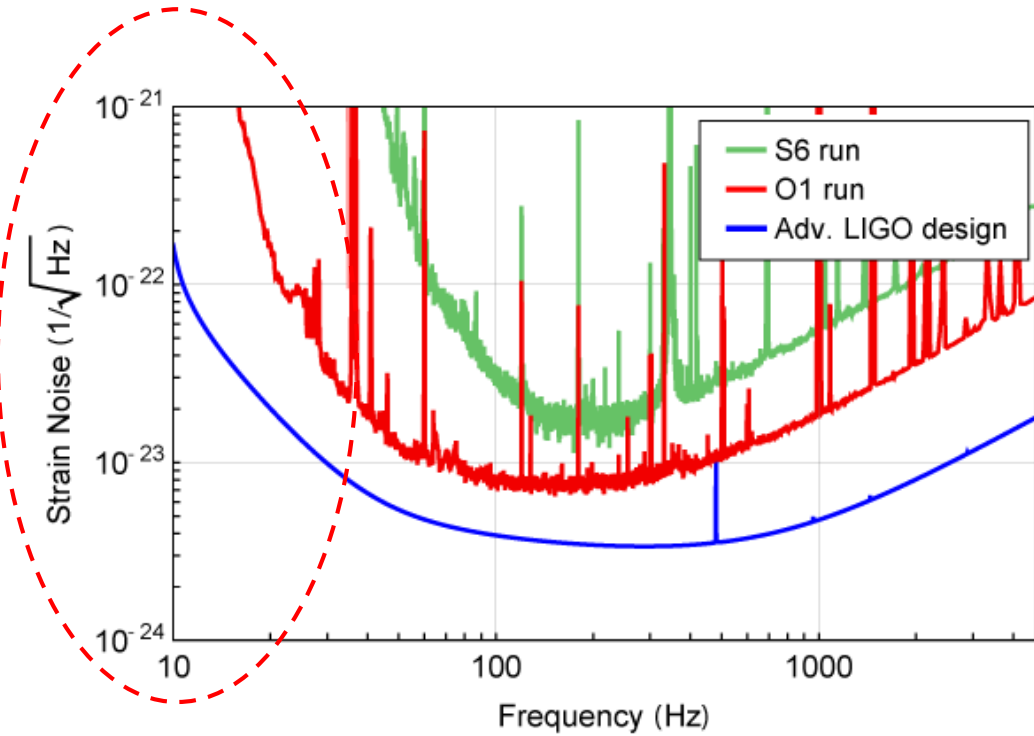
pSOGRO

(Credit for slide: Ampuero '18)

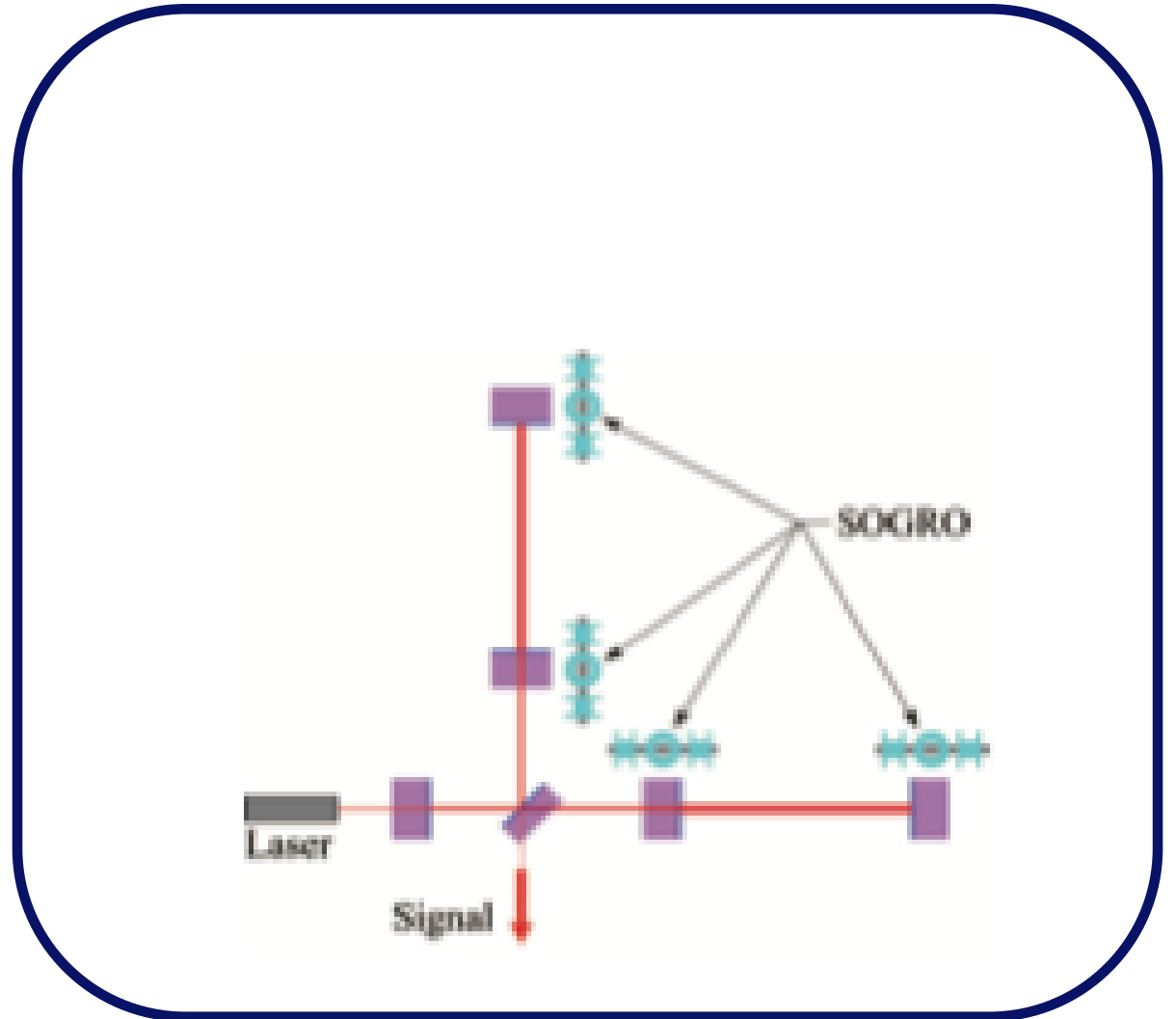


Signal-to-noise ratio at onset time + 10 s

5) Improve aLIGO sensitivity at low freqs:



<https://www.advancedligo.mit.edu/>



(Credit for figure: H. Paik)

IV. Summary and Outlook

- Brief introduction to SOGRO and its target sciences in $(0.1\sim 10)Hz$
- There still remain many technical and theoretical challenges, in particular, Newtonian noise reduction and civil engineering.

✓ **Budget estimated for the pSOGRO:**



Status in Asian Regions for GW Experiments

	Statements in 2019
Japan	<ul style="list-style-type: none">• KAGRA• R&Ds for B-DECIGO (2020s), DECIGO, TOBA
India	<ul style="list-style-type: none">• LIGO-India
China	<ul style="list-style-type: none">• Collaboration with KAGRA• Space projects (TianQin and Taiji)• ZAIGA (Terrestrial), AIGSO (Space)
Korea	<ul style="list-style-type: none">• Collaboration with KAGRA and <i>LIGO</i>^(*3)• Contribution to KAGRA+ ^(*1)• R&Ds for a 0.1-10Hz detector (SOGRO)
Taiwan	<ul style="list-style-type: none">• Collaboration with KAGRA• Contribution to KAGRA+ ^(*2)• Joining LISA consortium
Australia	<ul style="list-style-type: none">• OzGrav

(Based on K. Somiya's slide)

(*1) Squeezing experiment

(*2) High power laser, squeezing

(*3) Added by GK

✓ SOGRO in Space



- We strongly believe that the SOGRO experiment will bring lots of fruitful sciences and new chances in the future.
 - I was told that a Korean experimentalist visited UMD group and learned the SGG from A to Z.....
- **We hope that our pilot study will be a milestone of detector developments for GW astronomy in Korea.**

1/10⁽⁻²¹⁾ OF THANKS!

