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Institute for Quantum Optics and Quantum Information – Vienna

# Falling through masses in superposition: Quantum reference frames for indefinite metrics

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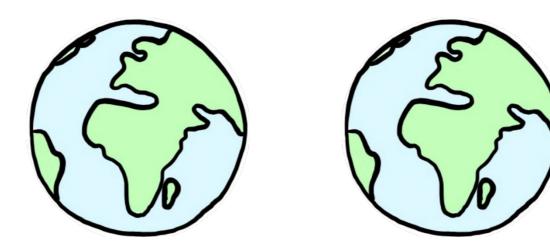
Humboldt Kolleg conference in Kitzbühel, 27 June 2022

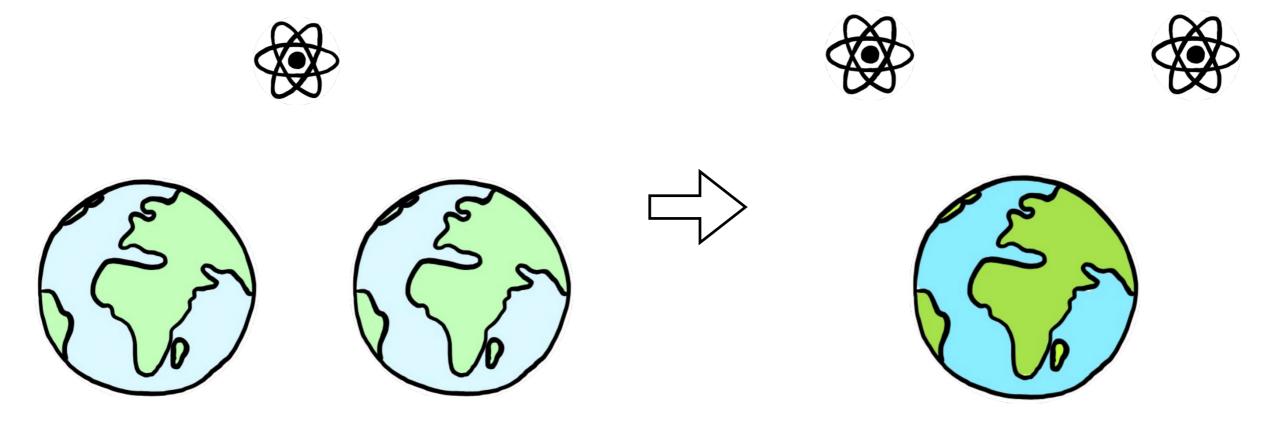




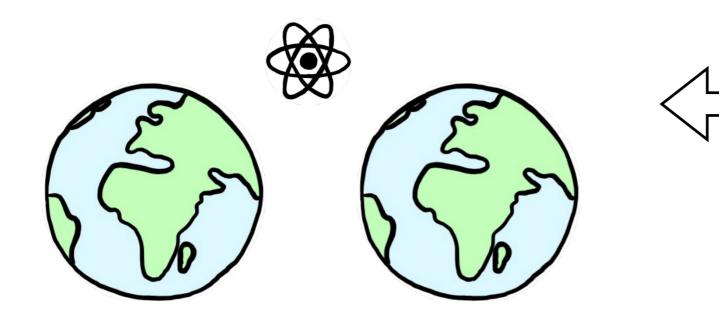


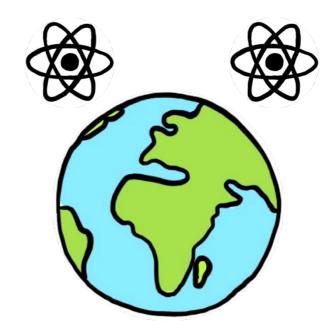






"Sitting on the Earth"





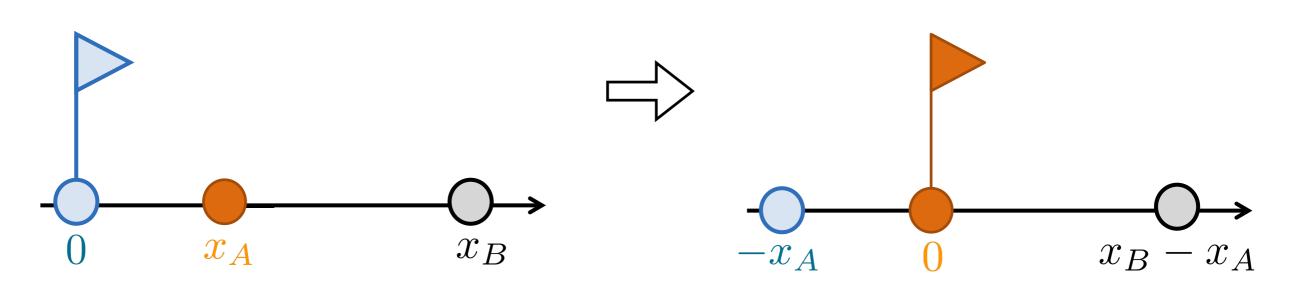
"Sitting on the Earth"

# Outline

- 1. Quantum Reference Frames Formalism Generalised Principle of Covariance
- 2. Applications Motion of a test particle Time dilation
- 3. Generalisations
- 4. Summary & Outlook

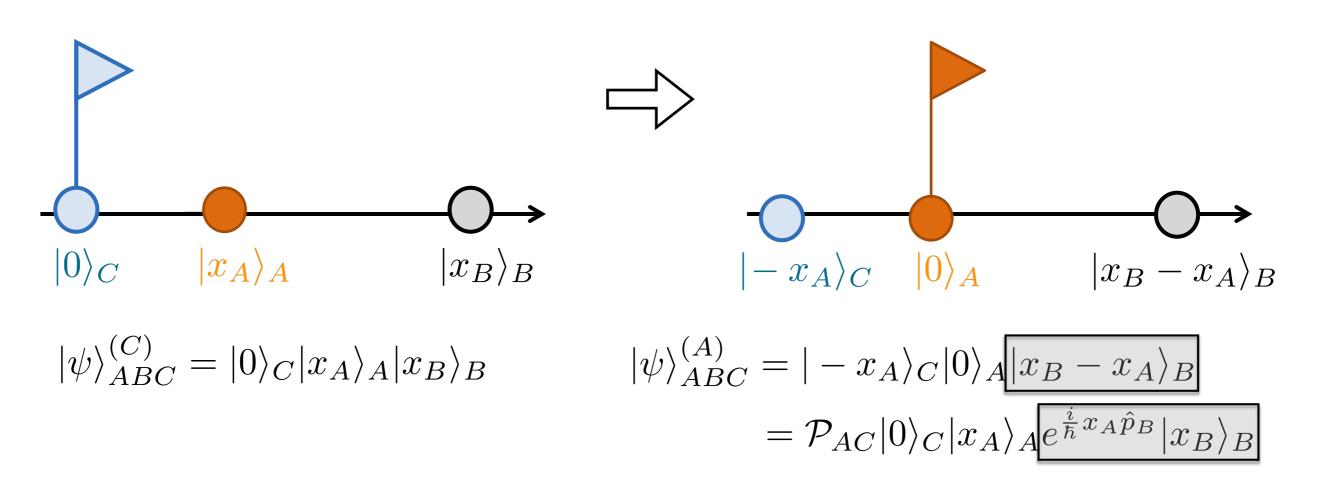
### **Classical Reference Frames**

### Formalism

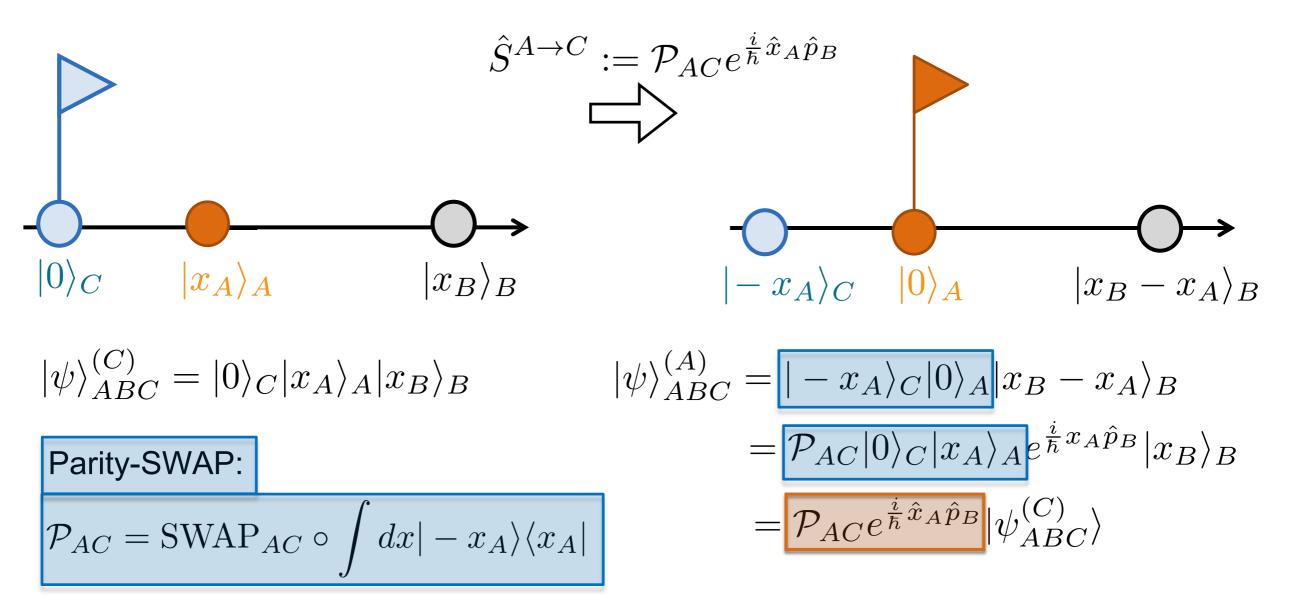


Relational physics (Rovelli): States are defined relative to other physical systems.

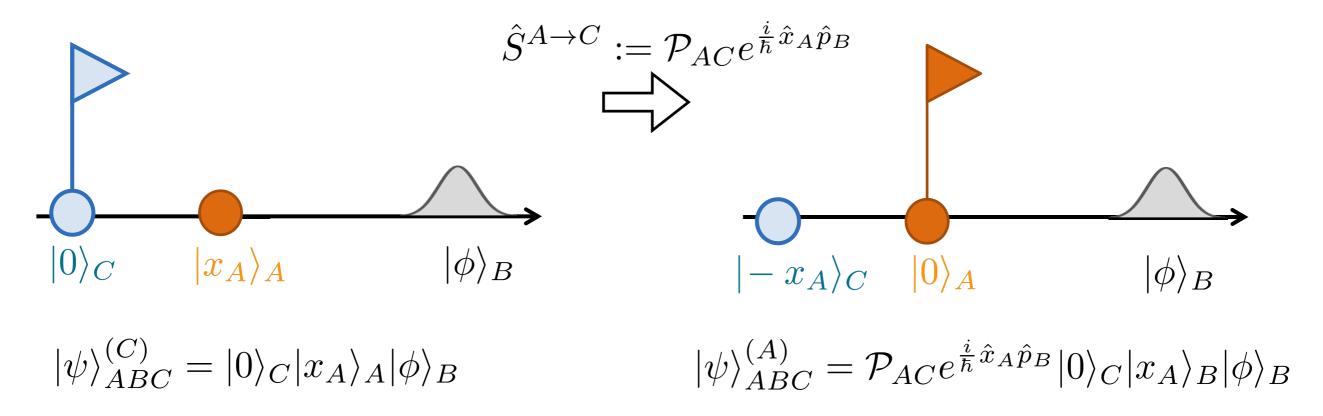
### Formalism



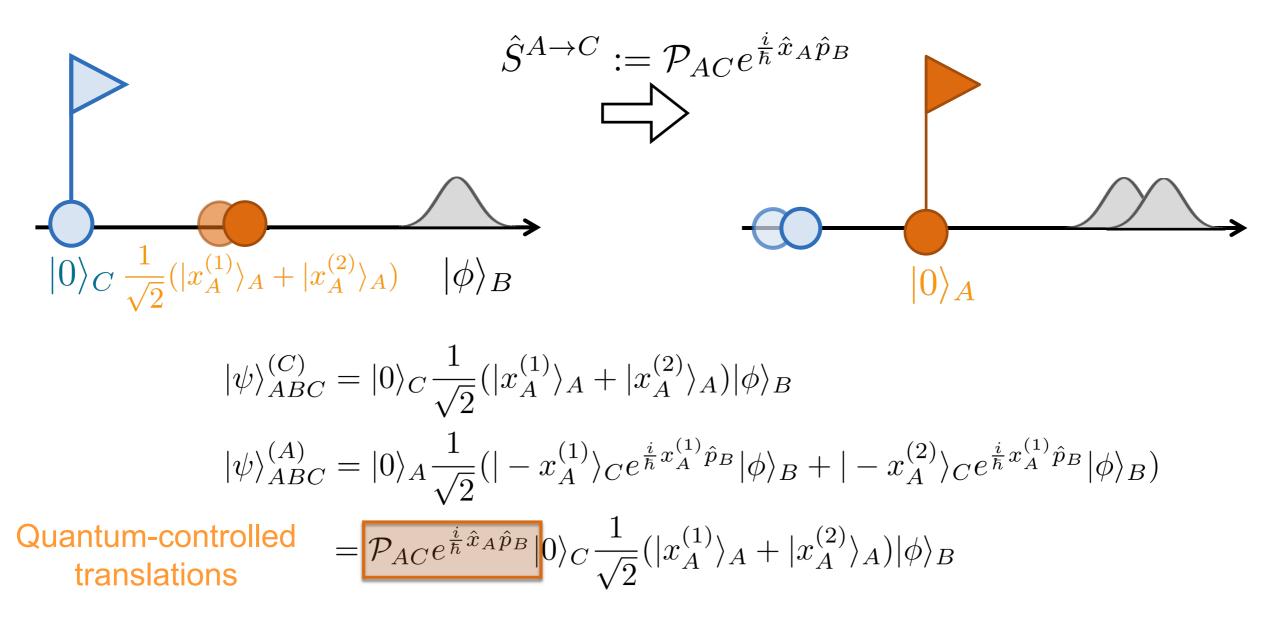
### Formalism



### Formalism

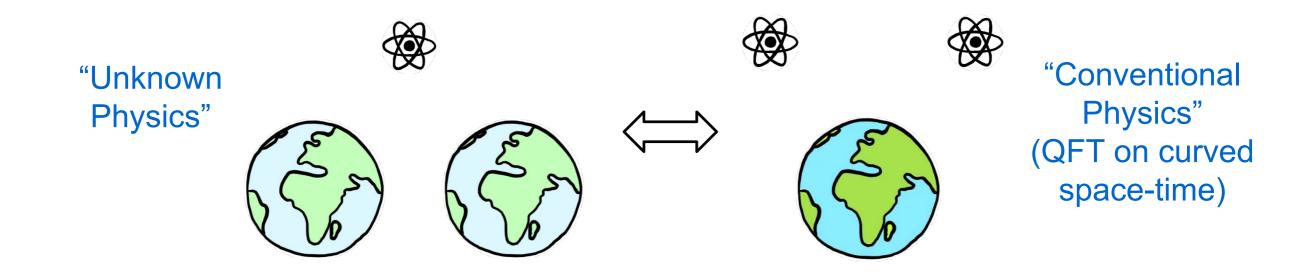


### Formalism



# How does an object fall in a superposition of gravitational fields?

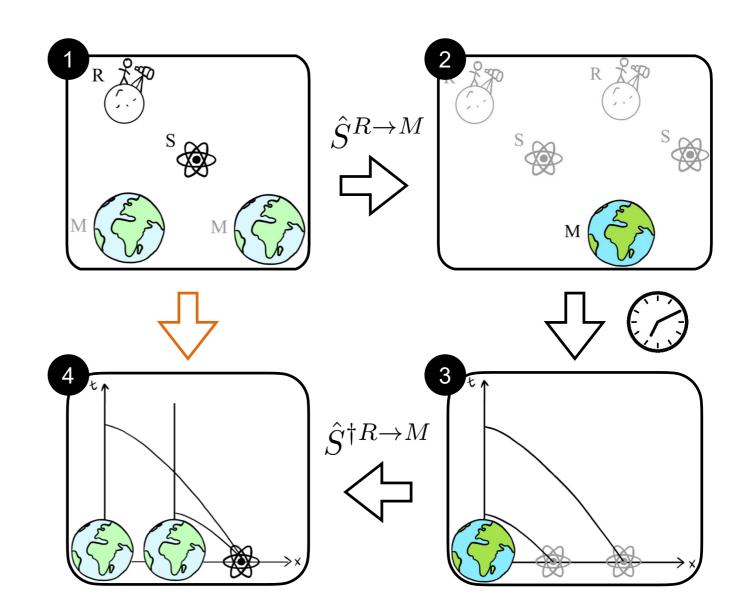
**Generalised Principle of Covariance** 



Covariance of dynamical laws under quantum coordinate transformations: *Physical laws retain their form under quantum coordinate transformations*.

### Applications

### Motion of a Test Particle



### Moving to the QRF of the Earth

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# Motion of a Test Particle **1** Reference Frame of R $|\psi\rangle_{RMS}^{(R)} = |0\rangle_R \frac{1}{\sqrt{2}} \left( (x_M^{(1)})_R + (x_M^{(2)})_M \right) |x_S\rangle_S \int_{\mathbb{R}}^{\mathbb{R}} \int_{\mathbb{R}}^{\mathbb{R}} \int_{\mathbb{R}}^{\mathbb{R}} \hat{S}_{R \to M} \int_{\mathbb{R}}^{\mathbb{R}} \hat{S}_{R}$

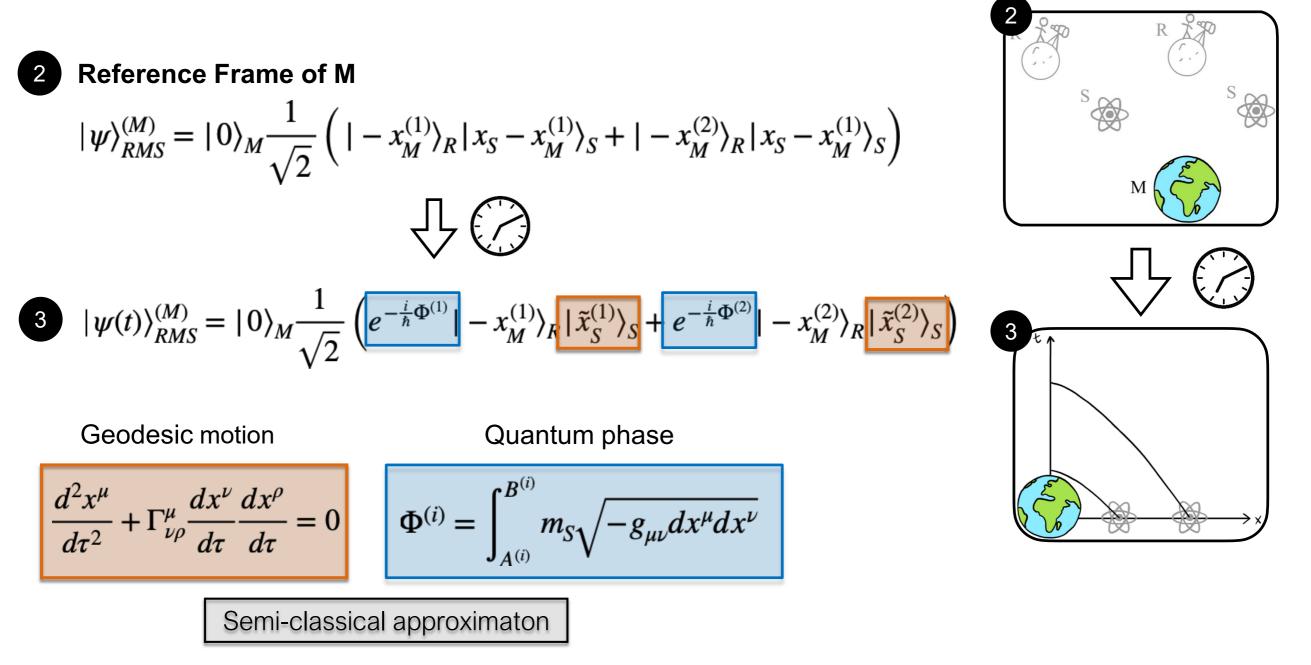


**Reference Frame of M** 

$$|\psi\rangle_{RMS}^{(M)} = |0\rangle_{M} \frac{1}{\sqrt{2}} \left( |-x_{M}^{(1)}\rangle_{R} |x_{S} - x_{M}^{(1)}\rangle_{S} + |-x_{M}^{(2)}\rangle_{R} |x_{S} - x_{M}^{(1)}\rangle_{S} \right)$$

# **Time Evolution**

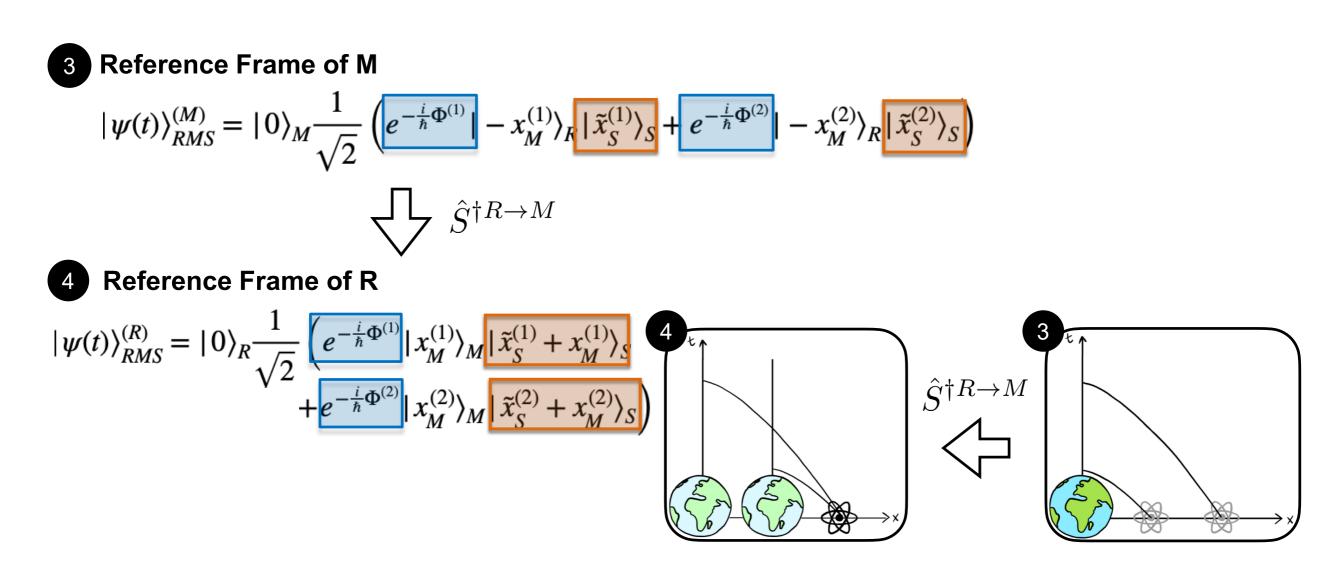
### Motion of a Test Particle



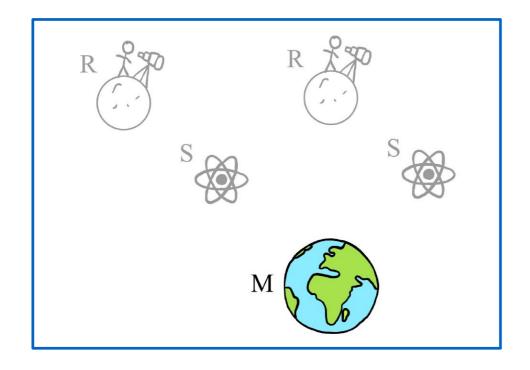
L. Stodolsky, Matter and Light Wave Interferometry in Gravitational Fields, Gen. Rel. Grav. 11, 391-405 (1979).

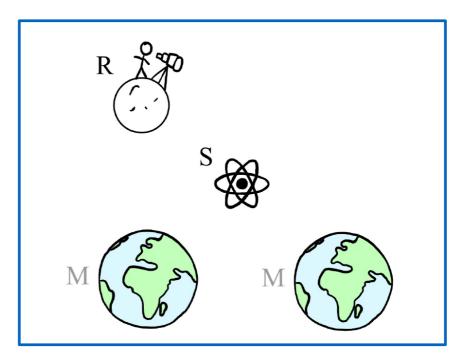
### Moving back to the lab QRF

### Motion of a Test Particle



Hamiltonian of one mass





Reference frame of M

Reference frame of R

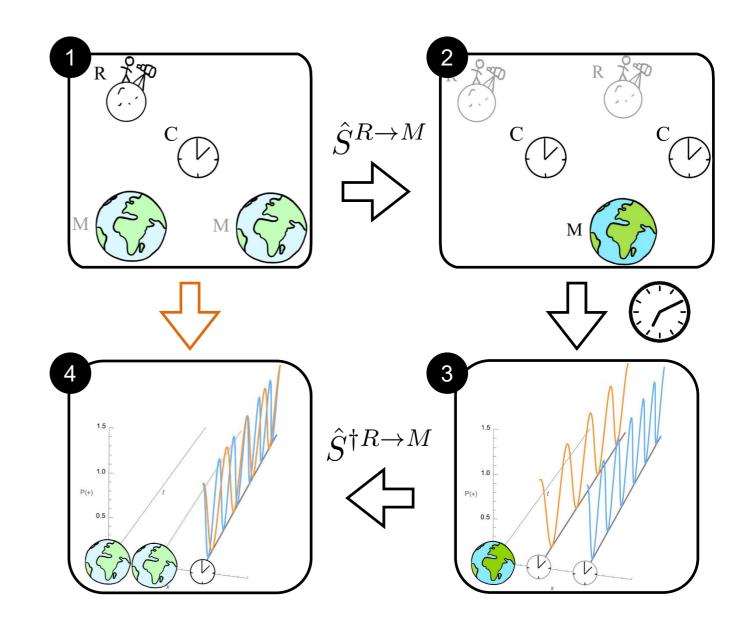
In the weak-field approximation:

$$\hat{H}_{SR}^{(M)} = \frac{\hat{\pi}_{S}^{2}}{2m_{S}} + m_{S}\hat{V}(\hat{q}_{S})$$

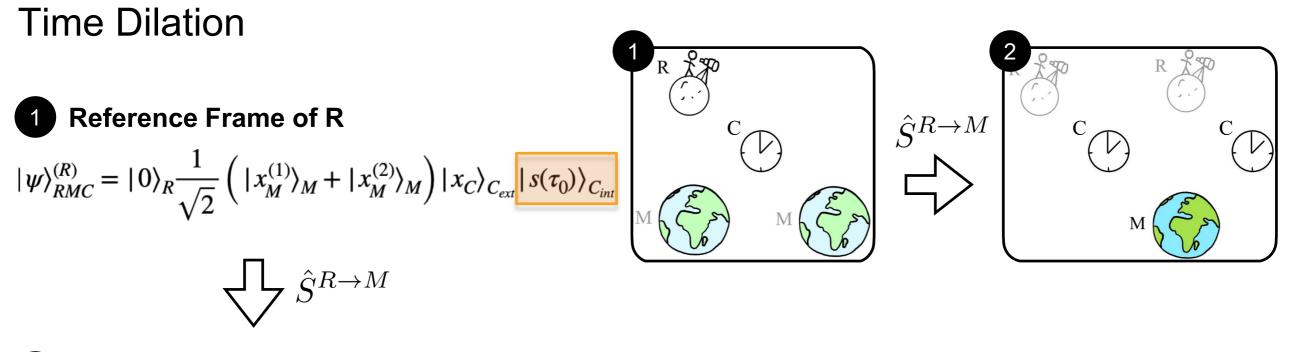
$$\hat{H}_{SM}^{(R)} = \hat{S}^{\dagger} \hat{H}_{SR}^{(M)} \hat{S} = \frac{\hat{p}_S^2}{2m_S} + m_S \hat{V}(\hat{x}_S - \hat{x}_M)$$

## Applications

**Time Dilation** 



### Moving to the QRF of the Earth





#### **Reference Frame of M**

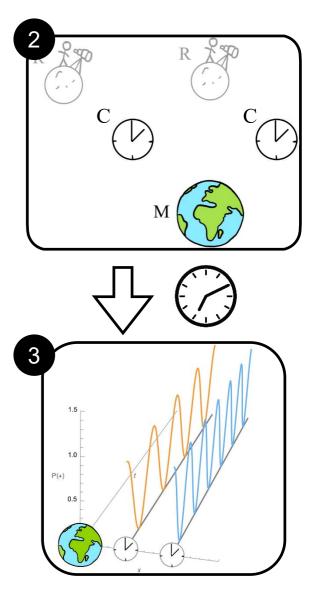
$$|\psi\rangle_{RMS}^{(M)} = |0\rangle_{M} \frac{1}{\sqrt{2}} \left( |-x_{M}^{(1)}\rangle_{R} |x_{C} - x_{M}^{(1)}\rangle_{C_{ext}} + |-x_{M}^{(2)}\rangle_{R} |x_{C} - x_{M}^{(1)}\rangle_{C_{ext}} \right) |s(\tau_{0})\rangle_{C_{int}}$$

clock's internal d.o.f.  $|s(\tau_0)\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$ 

### **Time Evolution**

**Time Dilation** 

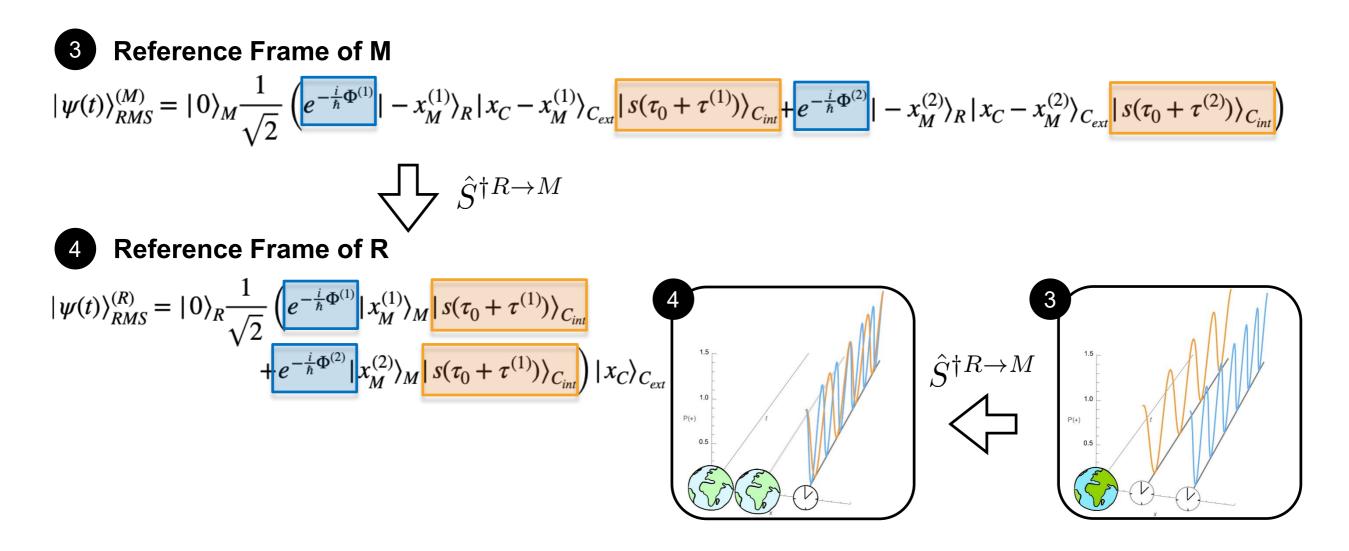
**Reference Frame of M** 2  $|\psi\rangle_{RMS}^{(M)} = |0\rangle_{M} \frac{1}{\sqrt{2}} \left( |-x_{M}^{(1)}\rangle_{R} |x_{C} - x_{M}^{(1)}\rangle_{C_{ext}} + |-x_{M}^{(2)}\rangle_{R} |x_{C} - x_{M}^{(1)}\rangle_{C_{ext}} \right) |s(\tau_{0})\rangle_{C_{int}}$  $3 |\psi(t)\rangle_{RMS}^{(M)} = |0\rangle_{M} \frac{1}{\sqrt{2}} \left( e^{-\frac{i}{\hbar} \Phi^{(1)}} - x_{M}^{(1)} \rangle_{R} |x_{C} - x_{M}^{(1)} \rangle_{C_{ext}} |s(\tau_{0} + \tau^{(1)})\rangle_{C_{int}} + e^{-\frac{i}{\hbar} \Phi^{(2)}} - x_{M}^{(2)} \rangle_{R} |x_{C} - x_{M}^{(2)} \rangle_{C_{ext}} |s(\tau_{0} + \tau^{(2)})\rangle_{C_{int}} \right)$ time evolution of the clock proper time  $\tau^{(i)}(t) = t \left( 1 + \frac{V(x_C - x_M^{(i)})}{c^2} \right) | s(\tau_0 + \tau^{(i)}) \rangle_{C_{int}} = e^{-\frac{i}{\hbar}\hat{\Omega}\tau^{(i)}} | s(\tau_0) \rangle_{C_{int}}$  $\hat{\Omega} = E_0 |0\rangle \langle 0| + E_1 |1\rangle \langle 1|$ 



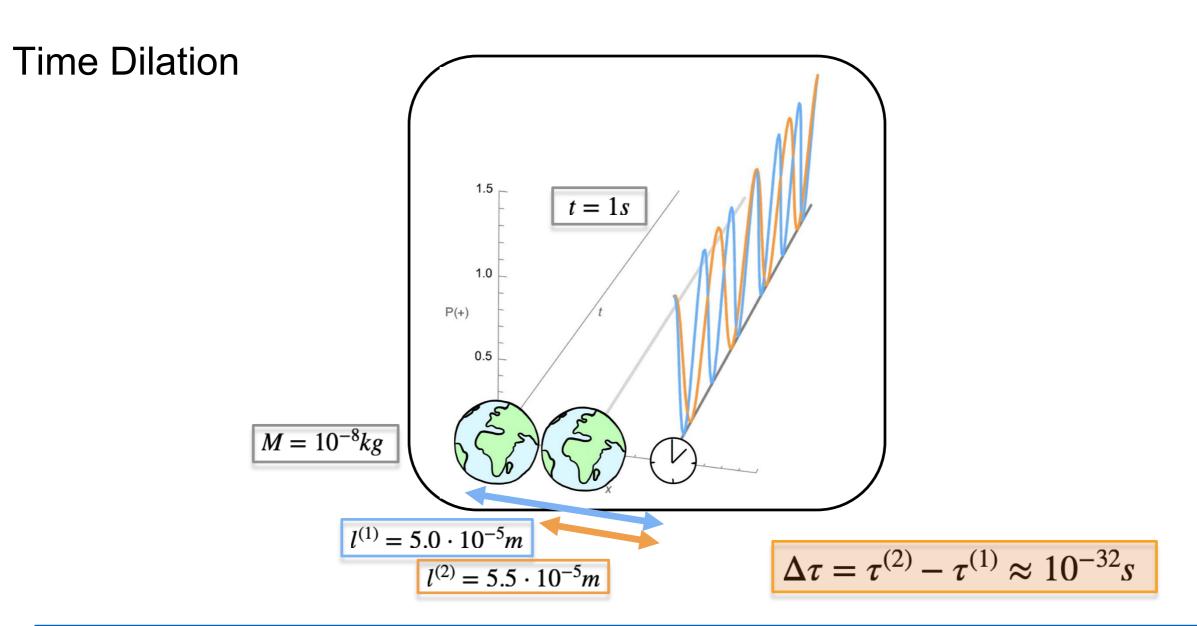
M. Zych, F. Costa, I. Pikovski, Č. Brukner, Nature Communication 2:505 (2011).

### Moving back to the lab QRF

### **Time Translation**

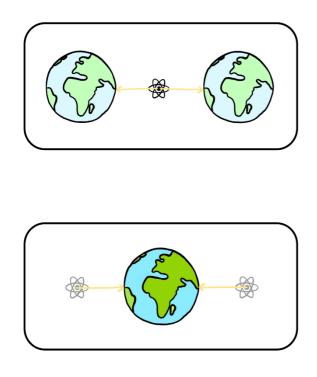


### **Applications**

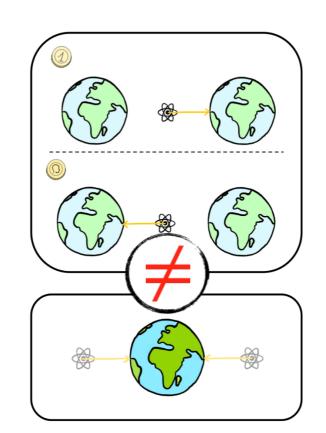


- Very tiny effect but still many orders of magnitude closer than the Planck time (10<sup>-44</sup> s)
- "Genuine superposition of space-times"

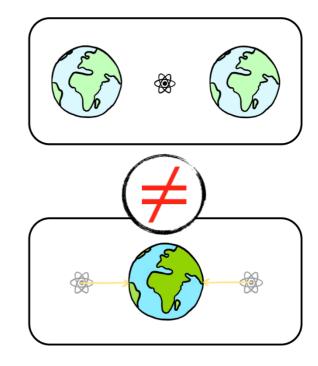
### Comparison with other approaches



Generalised Covariance

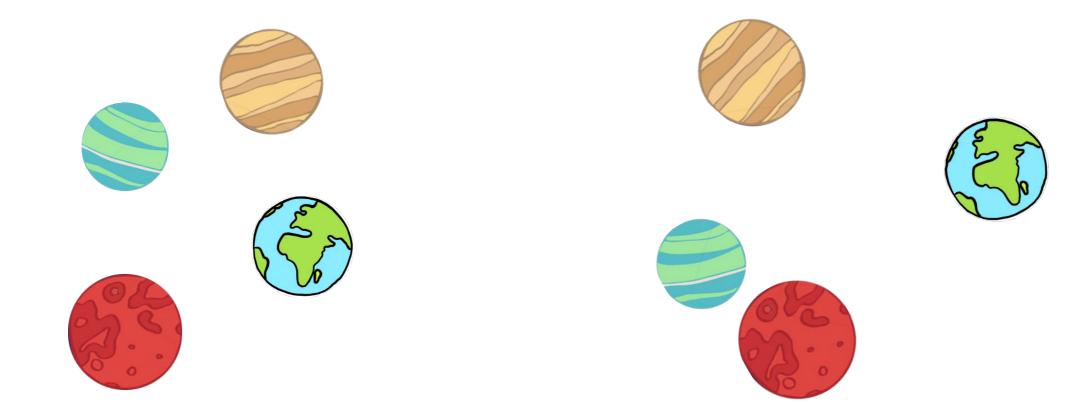


Collapse Models

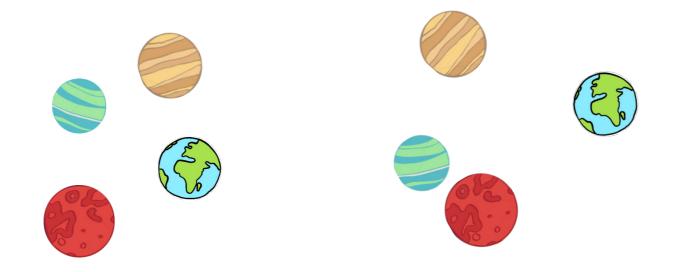


Semi-Classical Gravity

... to N masses in superposition



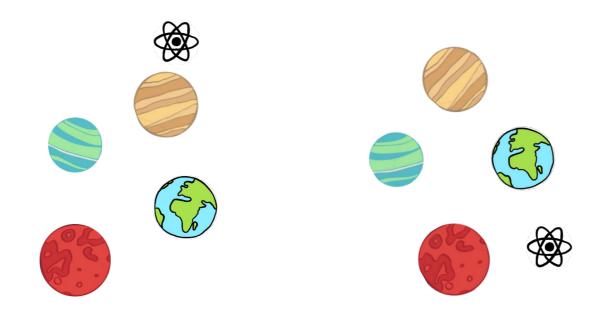
Can we always find a reference frame in which the metric becomes definite? No



Restrict to superpositions of relative-coordinate-distance preserving transformations:

- global translations
- global rotations

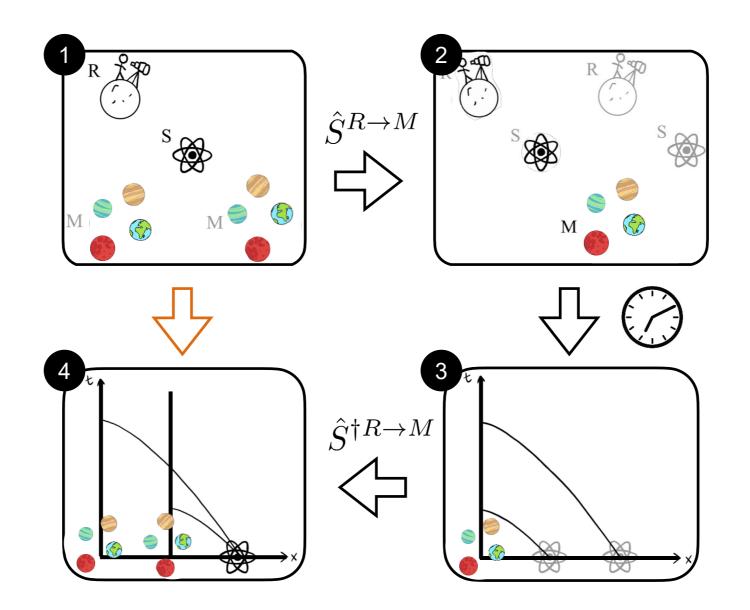
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Restrict to superpositions of relative-coordinate-distance preserving transformations:

- global translations
- global rotations

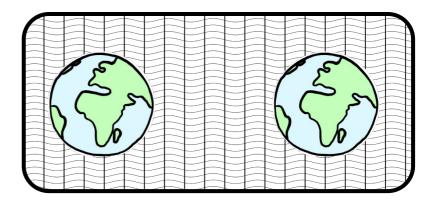
Does not limit us to trivial (i.e. diffeomorphism related) situations as the presence of probe particles **breaks the symmetry**.

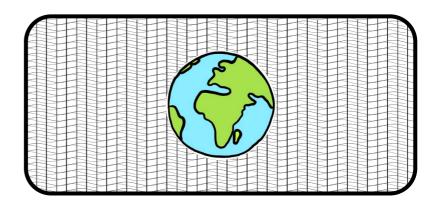


A.-C. de la Hamette, V. Kabel, E. Castro-Ruiz, and Č. Brukner, arXiv: 2112.11473 (2021).

# Outlook

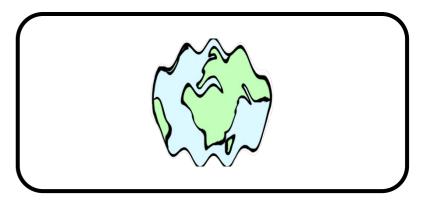
• Extend and apply frameworks to **quantum fields**.

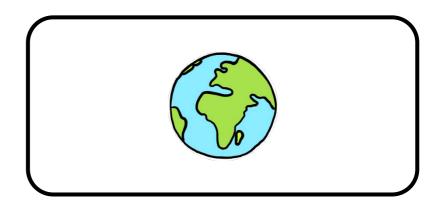




# Outlook

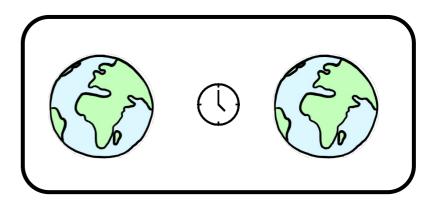
- Extend and apply frameworks to quantum fields.
- Go beyond semi-classical approximation for the massive objects and the gravitational fields

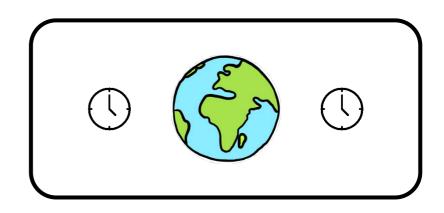




# Outlook

- Extend and apply frameworks to quantum fields.
- Go beyond semi-classical approximation for the massive objects and the gravitational fields
- Design experimental proposals for testing the generalised symmetry principle.



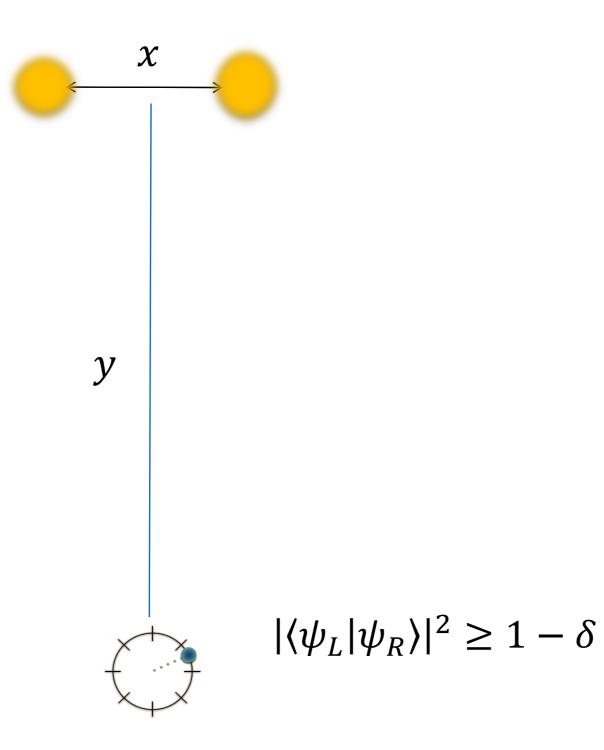


# Summary

- 1. Predictions based on **extended symmetry principle** while staying **agnostic** about the nature of gravitational field sourced by a mass in superposition.
  - Particle moves in superposition of geodesics, entangled with masses.
  - Clock ticks in superposition of proper times, entangled with masses.
- 2. Independent argument for the **quantum nature of the gravitational field** sourced by masses in superposition.

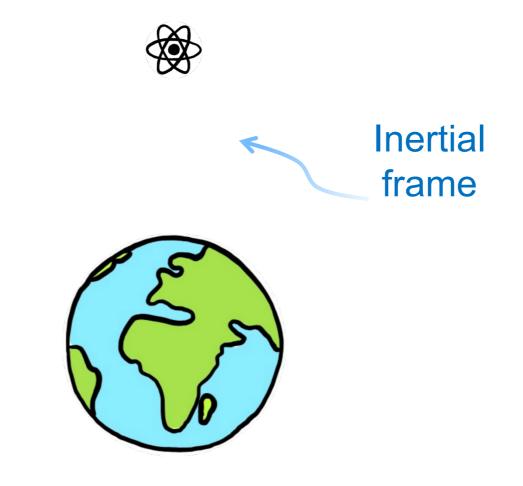
arXiv: 2112.11473





### Einstein's equivalence principle

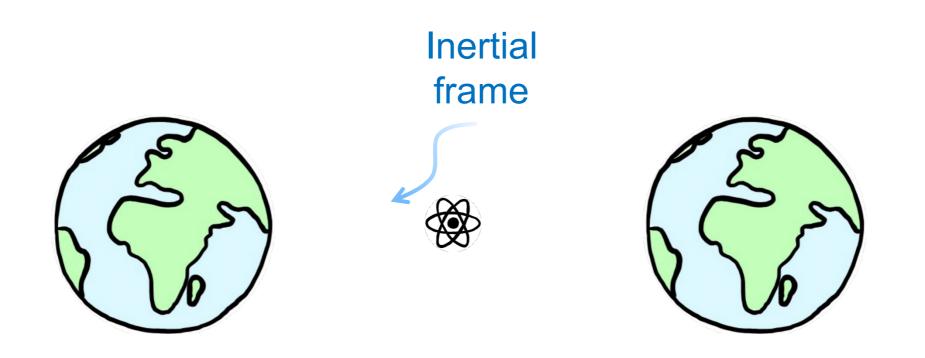
In any and every local Lorentz frame, anywhere and anytime in the universe, all the (nongravitational) laws of physics must take on their familiar special-relativistic form<sup>\*</sup>.



\* C. W. Misner, K. Thorne, and J. Wheeler, Gravitation. San Francisco: W. H. Freeman, 1973

# Quantum Einstein's equivalence principle

In any and every **quantum** locally inertial frame, anywhere and anytime in the universe, all the (nongravitational) laws of physics must take on their familiar special-relativistic form\*.

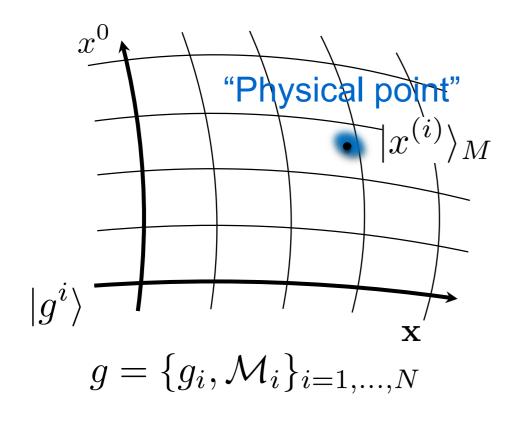


\* Compare with L. Hardy's "Quantum Equivalence Principle", arXiv:1903.01289

### Regime considered

"Superposition of semiclassical states of the gravitational field":

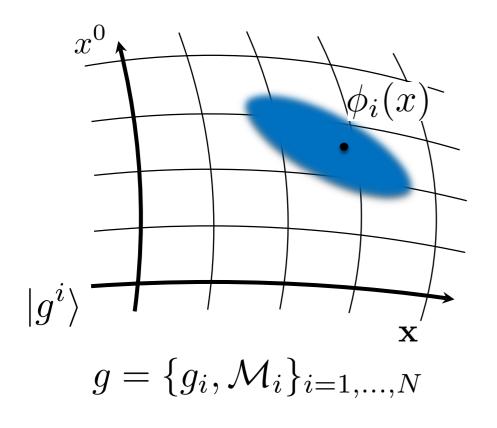
- 1. Macroscopically distinguishable gravitational fields are assigned orthogonal quantum state
- 2. Each well-defined gravitational field is described by GR
- 3. The quantum superposition principle holds for such gravitational fields



Operated-valued gravitational field:

$$\hat{g}_{\mu\nu}(\hat{x}_M)|g^i\rangle|x^{(i)}\rangle_M = g^i_{\mu\nu}(x^{(i)})|g^i\rangle|x^{(i)}\rangle_M$$
$$\frac{1}{4}\langle g^i|g^j\rangle\langle x^{(i)}|x'^{(j)}\rangle_M = \frac{\delta^{(4)}(x-x')}{\sqrt{-g_i(x)}}\delta_{ij}$$

### The quantum state of the gravitational field



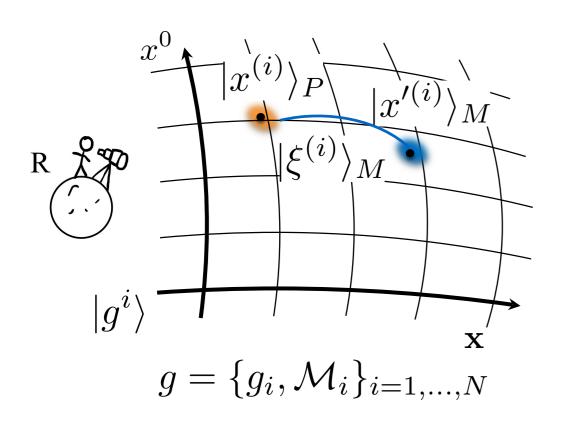
A general state of particle M and of the gravitational field, restricted to the classical manifold  $\mathcal{M}_i$ :

$$|g_i \triangleright \phi_i\rangle = \int d^4x \sqrt{-g_i(x)} \phi_i(x) |g^i\rangle |x^{(i)}\rangle_M$$

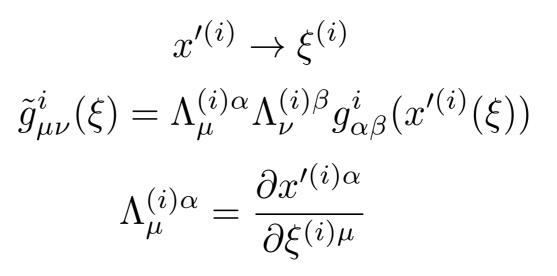
*Evaluation* of the metric field in the state:

$$\hat{g}_{\mu\nu}(\hat{x}_M) = |g_i \triangleright \phi_i\rangle = \int d^4x \sqrt{-g_i(x)} \phi_i(x) g^i_{\mu\nu}(x^{(i)}) |g^i\rangle |x^{(i)}\rangle_M$$

# QRF of a probe particle



Change coordinate to be centered at probe particle P:



Coord. change Parity-SWAP

### "Jumping" to the frame of the probe particle

$$\hat{S}|0\rangle_{R}|x^{(i)}\rangle_{P}|g^{i}\rangle|x^{\prime(i)}\rangle_{M} = -x^{(i)}\rangle_{R}|0\rangle_{P}|\tilde{g}^{i}\rangle|\xi^{(i)}(x)\rangle_{M}$$
$$\hat{S}\hat{g}_{\mu\nu}(\hat{x}_{M})|0\rangle_{R}|x^{(i)}\rangle_{P}|g^{i}\rangle|x^{\prime(i)}\rangle_{M} = \Lambda^{(i)\alpha}_{\mu}\Lambda^{(i)\beta}_{\nu}\tilde{g}^{i}_{\alpha\beta}(\xi)|-x^{(i)}\rangle_{R}|0\rangle_{P}|\tilde{g}^{i}\rangle|\xi^{(i)}\rangle_{M}$$